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## The sales effect of word of mouth: a model for creative goods and estimates for novels

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WISSENSCHAFTSZENTRUM BERLIN  
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SOCIAL SCIENCE RESEARCH  
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**The Sales Effect of Word of Mouth:  
A Model for Creative Goods  
and Estimates for Novels**

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## ABSTRACT

### **The Sales Effect of Word of Mouth: A Model for Creative Goods and Estimates for Novels**

by Jonathan Beck\*

Weekly sales of creative goods – like music records, movies or books – usually peak shortly after release and then decline quickly. In many cases, however, they follow a hump-shaped pattern where sales increase for some time. A popular explanation for this phenomenon is word of mouth among a population of heterogeneous buyers, but previous studies typically assume buyer homogeneity or neglect word of mouth altogether. In this paper, I study a model of new-product diffusion with heterogeneous buyers that allows for a quantification of the sales effect of word of mouth. The model includes Christmas sales as a special case. All parameters have an intuitive interpretation. Simulation results suggest that the parameters are estimable for data that are not too volatile and that cover a sufficiently large part of a title's life cycle. I estimate the model for four exemplary novels using scanner data on weekly sales.

*Keywords:* *new-product diffusion; word of mouth; creative industries*

*JEL Classification:* *C22, L82, M3*

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## ZUSAMMENFASSUNG

### **Die Verkaufswirkung von Mundpropaganda: ein Modell für kreative Produkte und Schätzwerte für Romane**

Meistens erreichen die wöchentlichen Verkäufe von kreativen Produkten wie Musikalben, Kinofilmen oder Büchern kurz nach Veröffentlichung ihren Höhepunkt und nehmen dann schnell ab. In einigen Fällen jedoch zeigen sie einen buckelartigen Verlauf mit zunächst ansteigenden Verkäufen. Eine populäre Erklärung für dieses Phänomen beruht auf der Existenz von Mundpropaganda unter heterogenen Käufern, doch bisherige Studien gehen typischerweise von der Annahme homogener Käufer aus oder vernachlässigen Mundpropaganda gänzlich. Dieses Papier betrachtet ein Modell der Verbreitung neuer Produkte unter heterogenen Käufern, welches eine Quantifizierung der Verkaufswirkung von Mundpropaganda ermöglicht. Das Modell beinhaltet Weihnachtsverkäufe als Spezialfall. Alle Modellparameter haben eine intuitive Bedeutung. Ergebnisse einer Simulation zeigen, dass die Parameter empirisch geschätzt werden können, wenn die Daten einen hinreichend großen Teil des Verkaufszyklus eines Titels abdecken und nicht zu volatil sind. Das Modell wird auf Scannerdaten für vier exemplarische Romane angewendet.

# 1 Word of mouth and hump-shaped sales

Weekly sales of creative goods – like music records, movies or books – usually peak shortly after release and then decline quickly. In many cases, however, they follow a hump-shaped pattern where sales increase for some time. For example, figure 1 plots weekly sales for two novels released on the German book market in 2003.<sup>1</sup> The horizontal axis in each panel of figure 1 denotes calendar weeks, starting from the release week of the respective title. Sales of title 1 increase for about seven weeks after release. Sales of title 2, instead, seem to decrease quite steadily from its second week onwards – apart from a somewhat outlying sixth-week sales peak.

An additional characteristic of creative industries is that Christmas purchases often represent an important share of a sales. Figure 1 therefore distinguishes non-December weeks from December weeks. The Christmas effect is relatively strong for title 2 and modest for title 1. Similar patterns of hump-shaped sales and seasonal spikes can be observed for music records and theatrical movie releases (Moe and Fader, 2001; Moul, 2006). A popular explanation for hump-shaped sales is product-specific word of mouth among heterogeneous buyers: an impressive novel can lead some readers to be enthusiastic promoters *vis-à-vis* potential buyers, such that sales increase for some time after the title’s release. The (non-)occurrence of word of mouth can thus determine success or failure of a particular title:

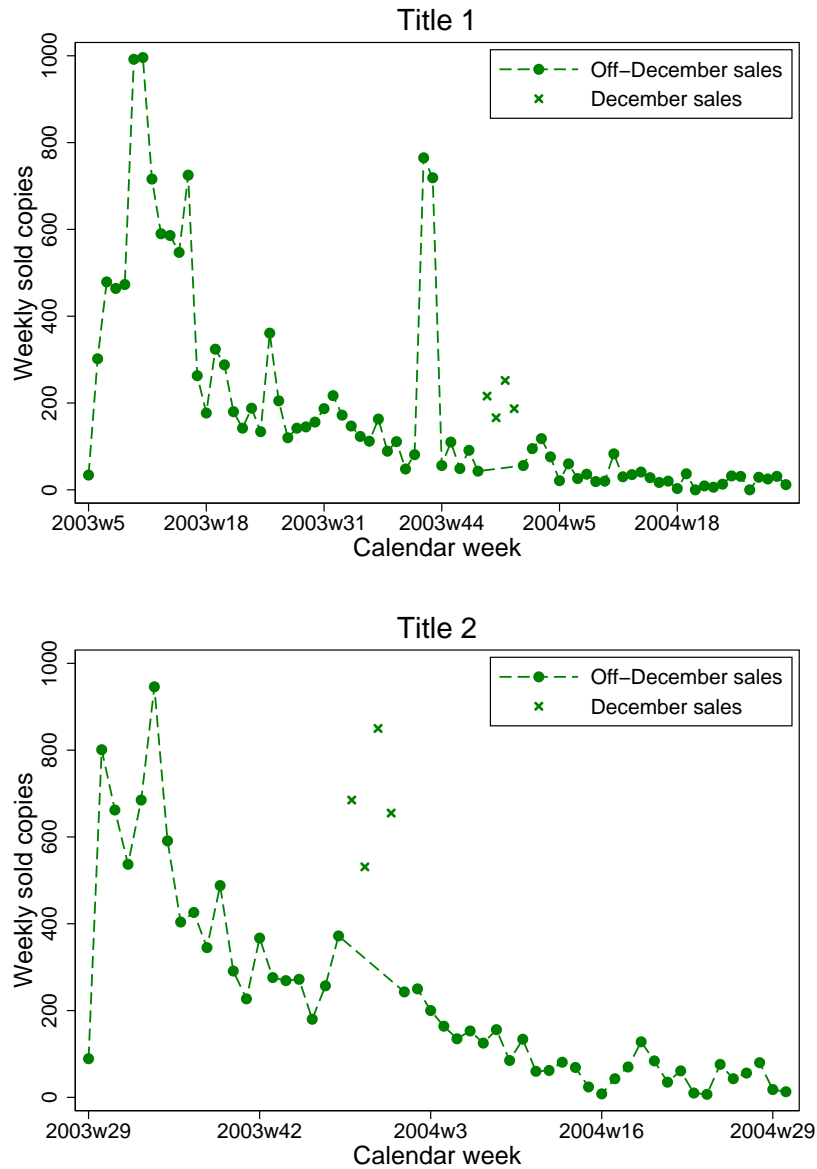
“Although *nobody knows* its fate when a new creative good appears, social contacts transmit consumers’ appraisals at a very low perceived cost to them, giving ‘word of mouth’ its importance for a creative good’s ultimate success. [...] The distribution of consumers between ‘buffs’ and ‘casuals’ strongly influences the organization of an art realm.” (Caves, 2000, p. 173)

In this paper, I propose and estimate a model of new-product diffusion that features two distinct types of buyers: independent buyers and buyers influenced by word of mouth. In this respect, the model thus closely follows Caves’ description of creative industries. As a result of this form of buyer heterogeneity, the model has the realistic property that the lack of word of mouth leads to unambiguously lower sales. In contrast, most previous studies of the sales performance of creative goods either assume buyer homogeneity or focus on other

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<sup>1</sup> Weekly sales of original hardcover editions, based on scanner data from a large sample of German retailers. Titles are anonymized; see section 4 for a more detailed description of the data.

Figure 1: Weekly unit sales for example book titles



aspects than word of mouth. Various studies look at the effect of academy nominations and awards, movie ratings, critic reviews or star participation on movie box office sales (see Moul, 2005; Elberse *et al.*, in press, for reviews). Regarding the effects of word of mouth in particular, De Vany and Walls (1996) present a model of information cascades with the property that box office failures and successes are equally likely and largely determined by opening week performance. The empirical section of their paper, however, focusses on characterizing overall movie demand rather than estimating title-specific word of mouth parameters. Moul (2006), in contrast, studies title-specific word of mouth effects in weekly box office figures. Whereas his data and research questions are comparable to the book market application studied here, his empirical strategy is based on a standard discrete choice model, which implies a reduced-

form interpretation. In some respects, the approach proposed in this paper can be regarded as more structural.

The empirical literature on the music or book industry is not as extensive. Moe and Fader (2001) model the intertemporal pattern of music record sales as a mixture of sales to different buyer segments and analyze weekly sales data for 20 popular albums. However, their model does not allow buyers to engage in word of mouth. Van den Bulte and Joshi (in press) use the same data to compare estimation results for a class of diffusion models, some of which featuring population heterogeneity. I discuss these models in some more detail in section 2.1. A number of recent studies look at online book sales (Chevalier and Goolsbee, 2003, for example), but with focus on internet-related questions rather than book market particularities.

More relevant to this paper is the study by Chevalier and Mayzlin (in press) on a particular case of word of mouth about books: consumer reviews on *Amazon.com*. As expected, they find that positive consumer reviews tend to increase sales. Sorensen and Rasmussen (2004) use scanner data on weekly book sales – similar to the data employed in this paper – to study the sales effects of *New York Times* book reviews. They find that both positive and negative reviews tend to increase sales. Hence, both studies corroborate the view that word of mouth is important for book sales and that it comes in various forms.

This paper is complementary to these studies in the sense that it provides estimates for the overall effect of word of mouth on a title's sales rather than two special cases. In addition, these studies follow a reduced-form estimation approach, whereas my estimates base on an explicit model of new-product diffusion and thus have a structural interpretation. I also include Christmas sales as a special case of word of mouth. Like most models of new-product diffusion, it is highly nonlinear in its parameters. In section 3 of the paper, I therefore assess its estimation properties by a set of Monte Carlo simulations. Results suggest that the parameters are estimable if the data cover a sufficiently large part of a title's life cycle and are not too volatile. In particular, book sales data often exhibit solitaire outliers such as those for title 1 in weeks 42 and 43 of 2003, which may be the effect of, for example, a television broadcast that featured the title or its author. The events that underlie such outliers may not always be identifiable, however, which can lead to high unexplained volatility in the data. I therefore discuss some of the consequences of data volatility and an approach to account for residual autocorrelation. Finally, in section 4 I present and discuss estimates for four exem-



plary novels, including those presented in figure 1. Estimates appear informative, intuitively reasonable and in line with ‘stereotype’ attributes commonly ascribed to creative goods.

I conclude that the structural empirical approach proposed in this paper provides a useful tool for applied research in various creative industry domains. For example, publishers can compare title-specific estimates to evaluate marketing strategies. Applied to a single title, it provides an estimate of consumer segmentation: information which can be valuable, for example, for marketing decisions concerning a title’s paperback release. Since the extent of word of mouth is typically hard to predict before a title’s release, a more policy-oriented analysis across titles and market segments may help characterize *ex ante* demand uncertainty (in the spirit of De Vany and Walls, 1996, 2004).

## 2 New-product diffusion with heterogeneous buyers

The idea that new-product diffusion is driven by word of mouth among heterogeneous buyers is not new. For example, a popular theory holds that the product life-cycle is determined by different adoption times of different consumer groups influencing each other, e.g. by innovators who adopt because of ‘intrinsic’ motivations and by imitators who adopt because the innovators do so (Rogers, 1995). Yet, most quantitative studies of new-product diffusion follow Bass (1969) and assume a homogeneous population of buyers, whose purchases are driven by ‘intrinsic’ and ‘social’ motivations at the same time.<sup>2</sup>

In principle, one could apply the Bass (1969) model to book sales data in order to generate a reduced-form estimate for the word of mouth effect; that approach, however, would miss an important feature of word of mouth in creative industries. Within a homogeneous population, word of mouth can only affect the speed of diffusion, that is, the time until every potential buyer has purchased the product. Word of mouth in Bass-type models cannot generate product failures or successes, because it has no effect on the total number of buyers. Moreover, scholars have argued that ignoring buyer heterogeneity can lead to biased estimates in applied research (Van den Bulte and Lilien, 1997; Bemmaor and Lee, 2002).

In what follows, I propose a parsimonious model of new-product diffusion with two buyer segments and argue that it represents a good tradeoff between face validity on the one hand

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<sup>2</sup> The Bass (1969) model was independently studied also in sociology, economics, as well as the statistics literature; for a review see Mahajan *et al.* (2000) and Van den Bulte and Joshi (in press).

and empirical tractability on the other hand – especially for the analysis of aggregate sales data of new creative goods.<sup>3</sup> The model coincides formally with a special case of a class of new-product diffusion models independently developed by Van den Bulte and Joshi (in press). A relevant difference is my explicit treatment of Christmas sales. I also propose a more intuitive interpretation of model parameters. For convenience, I present the model mostly in terms of my application: novels.

**Model.** Consider a new title that has just been released. Some buyers – buffs, fans of the author – are independently aware and intrinsically motivated to buy this title. In addition, they may act as promoters *vis-à-vis* other buyers, and are therefore labeled ‘influentials’.<sup>4</sup> A second type of buyer – the ‘imitator’ – only buys after being informed by word of mouth from at least one influential. Such word of mouth can take various forms, for example personal recommendations or book reviews. In fact, this need not involve a lot of talking: merely observing an influential person reading a certain book may induce imitator interest.

Denote with  $M$  the total number of potential buyers of the title under consideration.  $M$  does not include multiple or repeat purchases, total sales may therefore exceed  $M$ ; below, I introduce the particular case of Christmas present purchases by previous buyers. Let  $\theta$  denote the share of influentials in  $M$ . Sales to both influentials and imitators are distributed over time, but differently. Denote by  $F_i(t)$  the c.d.f. of sales to group  $i$  ( $i=1,2$ ) – that is, cumulative sales to group  $i$  divided by its population – and by  $f_i(t)$  the corresponding density.

Not all influentials buy the title straightaway in its release week, for example for budgetary reasons or lack of immediate leisure time. A standard assumption, instead, is that in every period the title is bought by a fraction  $p$  of those independent buyers who have not bought earlier. Excluding potential word of mouth effects, such behavior generates the steady decay pattern common to box office figures. In continuous terms,  $p$  is thus a hazard rate:  $p = \frac{f_1(t)}{1-F_1(t)}$ . Since  $F_1(0)=0$ , the cumulative number of sales to influentials at time  $t$ ,  $n_1(t)$ , can be solved for as

$$n_1(t) = \theta M F_1(t) = \theta M (1 - e^{-pt}). \quad (1)$$

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<sup>3</sup> Applications with more detailed micro- or consumer-level data are outside the scope of this paper; for such data, discrete choice models are more appropriate. Yet, decision makers other than retailers typically have access only to some kind of aggregated sales data (if any).

<sup>4</sup> The literature of new-product diffusion often focuses on technical innovations such as color television or the washing machine and therefore labels this consumer segment ‘innovators’. Here, I follow Keller and Berry (2003) and Van den Bulte and Joshi (in press) in using a more generally applicable term.

The number of imitator purchases depends on whether there is positive word of mouth by influential buyers. In particular, every influential recommends the product to  $\tilde{q}$  imitators each period following her purchase ( $\tilde{q} \geq 0$ ). If the title is not found worth recommending ( $\tilde{q}=0$ ), sales are determined by equation 1 and thus limited to a share  $\theta$  of their potential  $M$ . Notice that the model does not allow for negative (sales-destructive) word of mouth; I get back to this point in the next section.

If  $\tilde{q} > 0$ , the contacted imitators go ahead and buy the recommended title, unless they have not already done so due to an earlier recommendation.<sup>5</sup> Imitators do not recommend the product to other people (but they may offer it as a Christmas present, see below). Since the probability that an imitator exposed to word of mouth at time  $t$  has not been contacted and therefore has not bought earlier is  $1-F_2(t)$ , we can solve for the rate of imitator purchases:

$$f_2(t) = \tilde{q}n_1(t) * (1 - F_2(t)) \frac{1}{(1 - \theta)M}$$

or  $\frac{f_2(t)}{1 - F_2(t)} = qF_1(t),$  (2)

where  $F_1(t) = \frac{n_1(t)}{\theta M}$  and  $q = \tilde{q} \frac{\theta}{1 - \theta}.$

Using equation 1 and the fact that  $F_2(0)=0$ , this differential equation solves for

$$F_2(t) = 1 - e^{\frac{q}{p}(1 - e^{-pt} - pt)}. \tag{3}$$

Hence,  $n_2(t) = (1 - \theta)MF_2(t)$ , and we get for  $N(t)$ , the number of cumulative sales at time  $t$ :

$$N(t) = n_1(t) + n_2(t) = M(\theta(1 - e^{-pt}) + (1 - \theta)(1 - e^{\frac{q}{p}(1 - e^{-pt} - pt)}))$$

$$= M(1 - \theta e^{-pt} - (1 - \theta)e^{\frac{q}{p}(1 - e^{-pt} - pt)}). \tag{4}$$

**Interpretation.** It is possible that a particular title does not stimulate word of mouth ( $q=0$ ), or that the group of imitators has zero mass ( $\theta=1$ ). In either case, the model reduces to a negative exponential growth model and total sales  $N(t)$  are equal to  $n_1(t)$  as defined by equation 1.<sup>6</sup> Other boundary values for  $\theta$  and  $p$  are theoretically impossible or highly improbable for real

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<sup>5</sup> An formal assumption is that, at each point in time, each influential contacts a different set of imitators. In a continuous-time model, the probability that an imitator is contacted by more than one influential at once should be negligible.

<sup>6</sup> Notice that although the Bass model also reduces to equation 1 if its word of mouth parameter equals zero, the two models are not nested.

data. A title with  $p=0$  or  $\theta=0$  would never exhibit positive sales, and a title with  $p=1$  would sell to influentials only in week 1.

Obviously, the proposed 2-segment structure is a modest form of buyer heterogeneity: after all, everybody's different. Yet, the diffusion parameters also have an interpretation as sub-population averages that allows for some unsystematic within-segment heterogeneity. For example, an implicit assumption is that influential buyers immediately evaluate a title and decide whether to recommend it. That assumption is not overly restrictive, because readers often evaluate a book already from its first couple of pages. Nonetheless, anecdotal evidence suggests that some individuals are inclined to irrationally pile purchased books on their bedside table for years before reading and eventually recommending them. In this case,  $q$  can be regarded as an average recommendation rate: some influentials recommend more, some less, and the weekly average is  $q$ .

**Identification.** Equation 4 illustrates that the only “variable” in this and likewise models of new-product diffusion is time ( $t$ ). Correspondingly, the parameters of the model are identified by the shape of the sales curve: if there is positive word of mouth ( $q>0$ ), sales follow a hump-shaped pattern over time and the particular shape of this curve, combined with the assumptions of the model, allows to recover the respective parameter values. Yet, equation 4 also illustrates that  $M$  and  $\theta$  are not identified if  $q=0$  and that  $q$  is not identified if  $\theta=1$ ; that is, if sales are not hump-shaped but only follow the decay pattern of equation 1. The latter case – positive word of mouth without recipients – is arguably unrealistic. But the former case lies at the heart of marketing problems in creative industries: you never know how much a title would have sold had it had some word of mouth! Therefore, if estimated parameters include  $\hat{\theta}\approx 1$  and/or  $\hat{q}\approx 0$ , the other estimates are not reliable and a more restricted model may be applied to the respective data. Estimates for  $p$  or  $\theta$  that are unreasonably close to zero might suggest misspecification (systematic unobserved effects), or simply that sample size is too small or error variance too large. In section 3, I assess the importance of the latter two effects with a Monte Carlo simulation.

## 2.1 Possible extensions

The proposed model represents one out of several possibilities to formalize new-product diffusion within a heterogeneous (2-segment) population. At least for an application to creative goods markets, it seems reasonable to assume that (i) only influential buyers engage in word of mouth, which (ii) is directed only towards imitator buyers. Note that these assumptions only refer to sales-effective communication; they do not exclude general communication about a certain title that has no direct sales effect. Most readers like to talk about a book they have read, and they use forums like *Oprah's Book Club* to coordinate reading and follow-up communication. Although this holds for influential buyers ('buffs') as well – and may affect the timing of their purchase (parameter  $p$ ) – it does not affect the purchase decision. Imitators ('casuals'), instead, buy after and as a consequence of communication. In their case, word of mouth is sales-effective, and it is this particular word of mouth I focus on.

*Negative word of mouth.* One restriction in the above model is that it only considers positive word of mouth from influentials to imitators, although anecdotal evidence from the movie industry suggests that negative (sales-destructive) word of mouth can exist as well. In the 2-segment framework, negative word of mouth implies not only that  $q=0$ , but in addition that certain communication among influentials dissuades some of them from their initially planned purchase. As equation 1 illustrates, this would reintroduce another kind of identification problem: with negative word of mouth among influentials, their number ( $\theta M$ ) would be subject to change over time. Based on aggregate sales data alone, however, it is impossible to distinguish this effect from the decay parameter  $p$ . As an example, consider title 2 in figure 1, whose sales decline quickly after release. Based only on the figure, it is impossible to say whether the quick decline is due to negative word of mouth (decreasing  $\theta M$  over time) or a large decay parameter  $p$ . In order to identify an effect of negative word of mouth, one would either need more detailed data on post-purchase communication, such as *Amazon.com* consumer reviews, or be willing to impose restrictions on  $p$  in equation 1. Moul (2006) basically follows the latter approach, yet on the basis of a static discrete choice model.<sup>7</sup>

*Word of mouth among imitators.* In the above model, imitators care exclusively for recommendations from influentials. In general, however, word of mouth among imitators may also

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<sup>7</sup> Referring to Einav (in press), Moul (2006) notes that their discrete choice model yields estimates of a reduced-form character in the presence of intertemporal sales dynamics. This is due to the fact that, in order to capture these dynamics, one has to introduce the 'age' of a title (weeks since release) into the buyers' utility function, which amounts to assuming that buyer utility of consuming a particular title varies from one week to another, eventually in a non-linear fashion.

play a role. Van den Bulte and Joshi (in press) analyze a more general class of models which allows for positive word of mouth within both segments. These more general cases have the property that period sales can exhibit a 'dip' or are convex for early sales periods, when decreasing sales to influentials are not yet over-compensated by increasing sales due to word of mouth. The data studied in this paper do not seem to exhibit such patterns. For similar data from the U.S. market, Sorensen (in press) finds that sales for most titles peak in the early sales weeks (before the fifth week), which is inconsistent with the 'dip' property of the more general models analyzed by Van den Bulte and Joshi. Whereas Sorensen (in press) concludes that his econometric assumption of a monotone sales pattern over time is not critical for his purposes, the approach followed here is to explicitly consider word of mouth as the factor underlying a potential non-monotone pattern in early weeks.

Although attractive from a theoretical viewpoint, the more general models by Van den Bulte and Joshi (in press) come at the cost of at least one additional parameter. From an empirical viewpoint this is a drawback, as estimation difficulties usually increase exponentially with the number of parameters to be estimated. Moreover, the respective cumulative sales function – the analog to equation 4 – becomes rather complex and estimation based on standard methods appears to be troublesome. Reported estimates based on the most general model and sales data for 19 music CDs often seem to converge to theoretical limit values (0 or 1) or are of meager statistical significance.

Whereas unsatisfactory statistical significance may be an inevitable consequence of large data variance, degenerate estimates suggest that simpler models may suffice to analyze new-product diffusion in creative industries. Put differently, the nature of the data may often not allow the identification of complex diffusion models, in which case researchers have to make structural assumptions. For the purposes of this paper, the 4-parameter model presented above – which already provides for sufficient estimation issues (cf. section 3) – appears as a reasonable approximation to word of mouth communication about novels. Nevertheless, a detailed empirical comparison between alternative models, beyond that provided by Van den Bulte and Joshi (in press), is a promising subject of further research.

## 2.2 Incorporation of Christmas sales and estimation

So far I have neglected Christmas sales, which can represent an important share of overall sales. I propose the following Christmas effect. Within a certain time period – here I let that be the month of December – every previous purchaser of the title buys  $c$  extra copies in order to give them away as presents.<sup>8</sup> Christmas presents can be interpreted as a special case of word of mouth: instead of expressing a recommendation to read in a conversation, the recommender goes one step forward and assumes her counterpart’s purchase decision (Gabriel, 1997). Whereas such recommendation-by-donation directly leads to increased sales of a title, it does not necessarily lead to increased reading. The donor may be mistaken in the donee’s overall interest to read the presented title or in her interest to read it at that moment.<sup>9</sup> I therefore assume that copies purchased as Christmas presents do not lead to instantaneous additional word of mouth and corresponding sales. This is also consistent with the model’s assumption discussed earlier, namely that there are no second-order word of mouth effects through communication among imitators. Observed December sales then consist of two unobserved components: (i) the usual sales depending on the diffusion parameters and (ii) additional Christmas sales. A potential extension would be to allow Christmas presents to affect word of mouth in sales weeks *after* Christmas, when the donees have had a chance to unwrap their present and actually read the book. In that case, sales would pick up again after Christmas, relative to November, for example. At least for my example titles, however, this does not seem to be the case.

Furthermore, there is no reason to expect a particular distribution of the additional Christmas sales across the December sales weeks. For example, sales of title 1 in figure 1 seem to exceed their general trend in all four December weeks and by a similarly modest amount. Based on this observation, one may decide to model Christmas sales such that December sales enjoy a linear markup on top of the ‘usual’ sales predicted by the model parameters for that period. December sales of title 2, instead, vary strongly across the four weeks. Therefore, I do not impose a particular pattern but rather assume that Christmas sales are randomly distributed across the four December weeks. Sources for such randomness could be title-specific differences in store availability or aptness to be last-minute presents.

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<sup>8</sup> Alternatively, one may assume a longer Christmas season, or that only influentials or imitators purchase extra copies as Christmas presents. Estimation and interpretation of parameter  $c$  would be modified in a straightforward manner (see below).

<sup>9</sup> The potential ‘deadweight loss’ involved with misguided Christmas presents is subject to an academic debate initiated by Waldfogel (1993).

The standard approach to estimating the parameters of a new-product diffusion model is based on period sales, that is, first differences of the cumulative sales function (Srinivasan and Mason, 1986; Putsis and Srinivasan, 2000):

$$S(t) = N(t; \phi) - N(t-1; \phi) + \sum_{i=1}^4 \lambda_i D_{ti} + \varepsilon_t, \quad (5)$$

where  $S(t)$  denote sales of a given title during the period  $(t-1, t)$ ,  $N(\cdot)$  is defined by equation 4,  $\phi$  is the set of model parameters  $(M, \theta, p$  and  $q)$ , and  $t=1, \dots, T$ . The stochastic error  $\varepsilon$  may be autocorrelated; I discuss this case in more detail in the next section. The  $D_{ti}$  are dummy variables that account for the random distribution of Christmas sales across December weeks. More precisely,  $D_{t1}$  is equal to one if period  $t$  is the first week of December, and  $D_{t2}$ ,  $D_{t3}$  and  $D_{t4}$  are defined analogously. Constrained to be non-negative, these dummies' coefficients ( $\lambda_i$ ) capture all December sales that exceed those predicted by the otherwise best-fitting set of parameter values.<sup>10</sup>

Parameter  $c$  is implicit in the estimated  $\lambda$ -coefficients. Its exact estimate depends on whether one wants to impose a certain minimum delay between first purchase and Christmas gift decision. In other words, one may want to assume that only buyers who bought a title for own reading before week  $t^C$  qualify as potential Christmas donors. The additional Christmas sales are then  $c$  times  $N(t^C; \phi)$ , and an estimate for  $c$  is

$$\hat{c} = \frac{\sum \hat{\lambda}_i}{N(t^C, \hat{\phi})}. \quad (6)$$

In my application below,  $t^C$  is the last week of November; I thus assume that December for-read purchases are too short-termed in order to lead to additional for-present purchases.

### 2.3 Estimation in the presence of autocorrelation

It is possible that a shock in one week's sales figure has repercussions in following weeks. An example would be a news event or a television broadcast featuring the title or its author, which leads to increased sales not only in the week of the event but also in the following week, because some viewers are slower in executing their shopping list. Errors would then follow

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<sup>10</sup> Parameter identification would be complicated if December observations coincided with the early, increasing part of a title's sales curve. In practice, the vast majority of popular books is released in spring or early fall, with a safe distance to Christmas. Presumably, the fact that the book season starts with the book fair in October is an effort to animate word of mouth early enough such that it can boost Christmas sales.



an AR(1) process; the twin outliers in weeks 7/8 and 42/43 for title 1 seem to indicate a case in point. Such residual autocorrelation is conceptionally different from – and may arise on top of – the serial correlation of model sales inherent to the model diffusion process as captured by  $t$  in the estimation equation.

Franses (2002) proposes an auxiliary Gauss-Newton regression as a test for autocorrelation, where the estimated residuals obtained under the assumption of AR(0) errors (no autocorrelation) are regressed on their lagged values and on the evaluated first derivatives of the fitted model (with respect to each model parameter). For a test of AR(0) against the alternative that errors follow an AR(1) process, the auxiliary regression becomes

$$\hat{\varepsilon}_t = \mu_0 + \mu_1 \hat{\varepsilon}_{t-1} + \alpha_1 \frac{\partial \hat{G}(t; \phi)}{\partial \phi_1} + \alpha_2 \frac{\partial \hat{G}(t; \phi)}{\partial \phi_2} + \alpha_3 \frac{\partial \hat{G}(t; \phi)}{\partial \phi_3} + \alpha_4 \frac{\partial \hat{G}(t; \phi)}{\partial \phi_4},$$

where  $G(\cdot)$  denotes the nonlinear regression model and  $\phi$  the set of – in this case four – model parameters. The standard  $F$  test statistic for joint insignificance of the regressors then is a test statistic for autocorrelation. If joint insignificance of the  $\mu$ - and  $\alpha$ -estimates is rejected, the same holds for the hypothesis of no autocorrelation.

If the null hypothesis of AR(0) errors is rejected, one may include an AR(1) error term in estimation equation 5, which leads to the following empirical model:

$$S(t) = \rho S(t-1) + G(t; \phi) - \rho G(t-1; \phi) + \sum_{i=1}^4 \lambda_i D_{ti} + \varepsilon_t, \quad (7)$$

where  $G(t; \phi) = N(t) - N(t-1)$  as defined by equation 4,  $\phi$  denotes the set of model parameters ( $M, \theta, p$  and  $q$ ),  $\rho$  is the coefficient of autocorrelation and the  $\lambda_i$  capture Christmas present purchases as before.

The parameters in equations 5 and 7 can be estimated by nonlinear least squares (NLS). A grid search procedure, evaluating the sum of squared residuals for a number of combinations of parameter values, is used in order to find proper initial values for iterative estimation. Through log-transformations, I impose non-negativity for all parameters, and  $\theta, p \leq 1$ . Unfortunately, neither asymptotic nor small-sample properties of such NLS estimators are known (Boswijk and Franses, 2005); but their bias and consistency may be studied by means of a

Monte Carlo simulation. See Van den Bulte and Lilien (1997) and Bemmaor and Lee (2002) for simulation studies of the Bass (1969) model.<sup>11</sup>

### 3 Simulation

For an assessment of the properties of the proposed estimation strategy, I use equation 4 to generate artificial data for four different sets of parameters and  $T=60$ . Only the parameters  $\theta$  and  $q$  vary across sets. In all four sets,  $p=.05$ ,  $M=1000$  and  $c=0$ . Since the Christmas effect is additive, its exclusion should not affect the validity of the simulations. I chose parameter sets  $(\theta, q)$  such that they represent different stereotypes of titles: the ‘shockseller’ (set A), the ‘sleeper’ (set C), and two intermediate types (B,D). Parameter sets A, B, and C are also similar to estimates based on real data as reported in section 4. Figure 2 summarizes parameter values and presents the resulting sales patterns for each set. The peak sales date of the respective series is indicated by  $t^*$ ;  $t_{75}$  indicates the point in time where the series reaches 75% of total sales.

Following Van den Bulte and Lilien (1997), I perturb the artificial data with a multiplicative, log-normally distributed AR(0) error term  $u_t$  that has an expected value of 1 and a variance of  $\exp(\sigma^2)-1$ .<sup>12</sup> I assess three different error variances, where  $\sigma$  equals .06, .42 or .78, corresponding to the lowest, the intermediate and the highest variance used by Van den Bulte and Lilien (1997). For example,  $\sigma=.06$  implies that with a probability of about 95%, the difference between artificial and perturbed data is not larger than  $\pm 10\%$ . For  $\sigma=.78$ , instead, this difference is likely to lie within -80% and +200%. Comparing simulation results for different error variances provides an idea about how sensitive estimates are to solitaire shocks of different intensity.

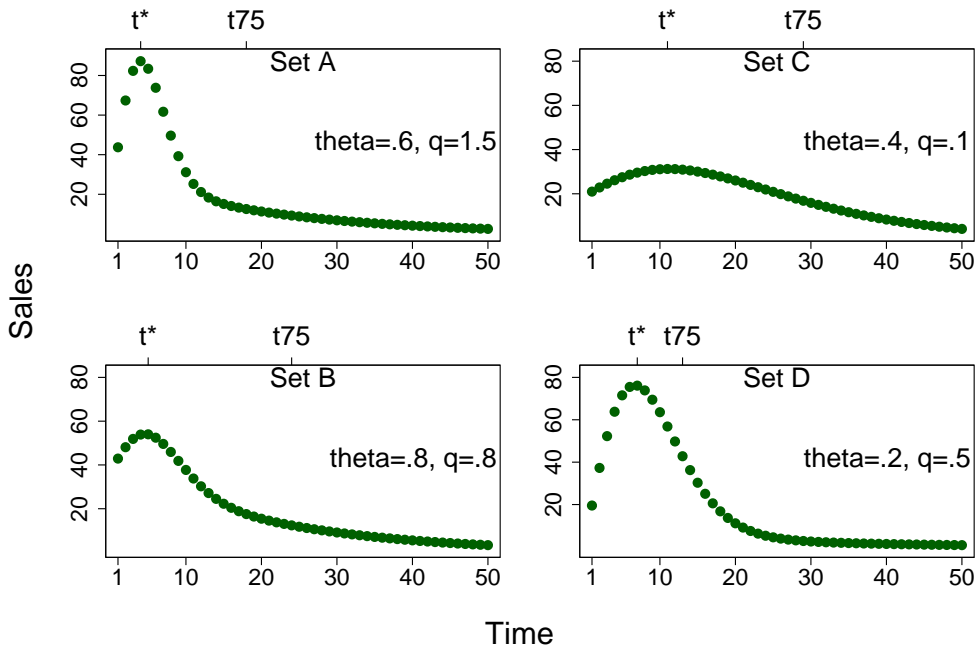
I estimate equation 5 with the perturbed data for  $S(t)$ , using the first 24, 40 or 56 observations. Estimates from diffusion models are usually quite sensitive to sample size; in particular, smaller samples that do not include  $t^*$  make estimation of  $M$  unfeasible (Debecker and Modis, 1994; Van den Bulte and Lilien, 1997). For each combination of parameters (4 variants), error

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<sup>11</sup> Boswijk and Franses (2005) propose an alternative estimation method for the Bass model based on weighted least squares and argue that it has better properties than the NLS approach, which has been implemented widely in similar applications. However, their approach is not applicable to the proposed diffusion model in a straightforward manner.

<sup>12</sup> If  $v_t$  is normally distributed with mean  $-\frac{\sigma^2}{2}$  and variance  $\sigma^2$ , then  $u_t = \exp(v_t)$  is log-normally distributed with mean 1 and variance  $\exp(\sigma^2)-1$ .

Figure 2: Simulated sales patterns



variance (3 variants) and sample size (3 variants), the perturbation and estimation procedure is repeated 1000 times. Altogether, this yields 36,000 sets of estimation results.

As error variance increases, a number of simulations result in degenerate estimates at or very close to boundary values zero ( $p$  and  $\theta$ ) or one ( $\theta$ ). In these cases, probably large absolute errors occurred in the early observations of the respective sample. Imagine large shocks in the first ten sales weeks of a type-B title as depicted in figure 2. Any estimation procedure may then have difficulties in identifying a hump-shaped sales curve and may converge to a set of parameter values that imply negatively sloped sales, like  $\theta=1$  or  $p=1$ . Effectively, such degenerate estimates indicate that the data are such that the procedure cannot distinguish this model from a simpler, 2- or 3-parameter model.

Therefore, the degree to which the occurrence of such degenerate results varies across simulation sets is a first indication of the estimator's sensitivity to differences in sample size and data variance. For a comparison across simulation sets, I define the estimation results of any repetition as degenerate if they fulfill at least one of the following conditions: (i)  $\hat{p}$  is smaller than .01 and not significantly different from zero (95% confidence), (ii)  $\hat{\theta}$  is smaller than .025 or larger than .975 and not significantly different from zero or one, respectively, (iii)  $\hat{M}$  is more than

Table 1: Number of degenerate results across simulation set\*

Sample size: T=24				
	Set A	Set B	Set C	Set D
$\sigma = .06$	0	91	2	0
$\sigma = .42$	246	164	522	624
$\sigma = .78$	536	498	760	720
Sample size: T=40				
	Set A	Set B	Set C	Set D
$\sigma = .06$	0	1	0	0
$\sigma = .42$	69	58	129	453
$\sigma = .78$	327	298	436	615
Sample size: T=56				
	Set A	Set B	Set C	Set D
$\sigma = .06$	0	0	0	0
$\sigma = .42$	22	39	56	410
$\sigma = .78$	207	192	320	568

\*Out of 1000 repetitions for every simulated set of parameters, sample size and variance.

tenfold observed cumulative sales.<sup>13</sup> Correspondingly, table 1 lists the number of degenerate results for each of the 36 simulation sets. As expected, the occurrence of degenerate estimates mainly seems to be driven by data variance ( $\sigma$ ): with low variance ( $\sigma = .06$ ), estimation seems to be unproblematic, except for two parameter sets with the small sample. With increasing data variance, all parameter sets are prone to yield degenerate results, but the effect is weaker for large samples.

A positive side to the occurrence of degenerate  $p$ - or  $\theta$ -estimates is that they are easily identified in practice: they are coupled with slow convergence and unreasonably large estimates for  $q$  (in the thousands) and/or  $M$  (in the millions). Given such results, the analyst may attempt to reduce data volatility before re-estimation, for example by identifying the causes for specific solitaire outliers.

Non-degenerate simulation results, on the other hand, seem fairly accurate. Table 2 gives means and medians of the simulated parameter estimates based on a relatively small sample (T=24) and low error variance ( $\sigma=.06$ ). Especially for sets A, B and D, estimates seem to be close to their true values, both in terms of the average and the mean. Estimation seems to be more difficult for set C, but this is not surprising: there, the first 24 observations cover a much

<sup>13</sup> This particular cutoff value for  $\hat{M}$  is not pivotal, since most degenerate sets of estimates come with  $M$ -estimates in the 6-digit range or higher and  $q$ -estimates in the 4-digit range or higher.

Table 2: Means and medians of simulated estimates for T=24 and  $\sigma=.06^*$

Parameter	$M$	$\theta$	$p$	$q$
Set A:				
<i>True value</i>	1000	.6	.05	1.5
Mean estimate	1003.3	.602	.050	1.521
Median estimate	999.7	.601	.050	1.509
Set B:				
<i>True value</i>	1000	.8	.05	.8
Mean estimate	1001.0	.800	.050	.806
Median estimate	999.9	.799	.050	.800
Set C:				
<i>True value</i>	1000	.4	.05	.1
Mean estimate	1173.9	.432	.058	.154
Median estimate	1113.7	.390	.051	.097
Set D:				
<i>True value</i>	1000	.2	.05	.5
Mean estimate	1021.8	.201	.055	.559
Median estimate	1003.0	.208	.050	.496

\*Based on 1000 repetitions for every set of parameters. Statistics exclude degenerate results.

smaller share of overall sales than for the other sets. One conclusion from this finding is that estimation of the model requires data on the major share of a title's first-release life cycle.

Table 3 summarizes estimation results based on the intermediate case of a sample size of 40 and  $\sigma=.42$ . In combination with two figures in the appendix, which give the results for the largest sample size in graphical form, this should give an idea about the overall results of the simulation. Table 3 suggests that, with decreasing values of  $q$ , parameter sets are increasingly inclined to the estimation difficulties that arise from increases in data variance. For every parameter set, increased error variance seems to induce a non-negligible bias on one or the other parameter estimate (mostly  $q$ ). Yet, this finding is in line with previous simulation studies, and hence not specific to the model studied here. Van den Bulte and Lilien (1997), as well as Bemmaor and Lee (2002), obtain similar results for the less complex 3-parameter Bass diffusion model.

Figures 4 and 5 in the appendix shed more light on estimation bias with increasing error variance. For every parameter in the four sets, they show a kernel density of the distribution of estimates with a sample size of 56, separately for the two larger error variances. The distribution of simulated estimates not only becomes more dispersed as error variance increases, but also seems to exhibit slight negative shifts. Most notably, the distribution of  $\theta$ -estimates appears to be bimodal for parameter set C, which has an intermediate value for  $\theta$  but the low-

Table 3: Means and medians of simulated estimates for T=40 and  $\sigma=.42^*$

Parameter	$M$	$\theta$	$p$	$q$
Set A:				
<i>True value</i>	1000	.6	.05	1.5
Mean estimate	1041.4	.631	.050	2.066
Median estimate	1012.2	.617	.047	1.769
Set B:				
<i>True value</i>	1000	.8	.05	.8
Mean estimate	1037.7	.738	.060	1.155
Median estimate	1020.4	.759	.047	.868
Set C:				
<i>True value</i>	1000	.4	.05	.1
Mean estimate	1087.1	.393	.073	12.470
Median estimate	1064.1	.456	.044	.100
Set D:				
<i>True value</i>	1000	.2	.05	.5
Mean estimate	1008.1	.233	.062	.630
Median estimate	996.0	.242	.051	.492
*Based on 1000 repetitions for every set of parameters. Statistics exclude degenerate results.				

est simulated value for  $q$  (equal to .1). As the respective distributions for  $q=.5$  (set D) and the other sets appear unproblematic, I conclude that estimates tend to become unstable for very low values of  $q$ .

In summary, the simulation exercise shows that the model is estimable if the data include a sufficiently large number of not too volatile observations. When using volatile data, analysts should be prepared to obtain degenerate estimates and should otherwise allow for slight bias when interpreting non-degenerate estimates; in particular, when the observed sales curve is relatively flat, indicating that word of mouth travels slow (low  $q$ ). Nevertheless, there is certainly room for methodological improvement. For example, the simulated error is a multiplicative one, which introduces heteroskedasticity depending on the absolute level of sales, whereas estimation assumes additive errors of constant variance. Yet, level-dependent heteroskedasticity is probably a realistic assumption, which may be exploited to improve estimates in the fashion recently demonstrated for the Bass model by Boswijk and Franses (2005). Progress along these lines, however, is outside the scope of this paper.

## 4 Application

The four example titles presented in the introduction come from a sample of novels that were released in Germany in 2003 as hardcover editions.<sup>14</sup> I obtained the data from *media control GfK International*, a marketing research firm that collects scanner data from over 750 points of sale (bookshops, department stores) as well as all main internet retailers in Germany. Not sampled are direct sales from publishers to consumers, book club sales and mail order sales. Supermarket sales are also not sampled, but they represent a small portion of book sales. Altogether, the sampled retail channels account for about 66% of total book sales in Germany. Yet, for the particular segment studied here (novels in hardcover), sales coverage of sampled channels is likely to be much higher. First, publisher direct sales are not very important for popular publications such as novels; direct sales usually concern professional publications. Second, book clubs can be regarded as a secondary market that only becomes important for a title after its diffusion in the primary market (which is studied here).

Furthermore, no particular estimation bias arises from this type of sampling. By law, book prices are the same across all retail channels.<sup>15</sup> In theory, independent buyers may be more inclined to order directly from publishers because they do not need retailer advice; in practice, however, title availability is high and ordering processes are quicker (typically overnight) at stationary bookshops and online retailers. Direct orders from publishers are thus unattractive for non-professional buyers. Based on a specific population weight for every point of sale, the scanner data were aggregated to represent nationwide sales. The sample period ends in summer 2004, providing up to 81 weekly observations per title. As demanded by the data proprietor, I received anonymized data where all title-, author- and publisher-specific information except for sales (by week) and price (constant) had been removed.<sup>16</sup>

In contrast to theatrical movies, new books do not have a particular weekday for release. A title may be shipped on a Friday, leaving only one or two sales days in its first calendar week. The analyst may then wrongfully interpret increasing sales in the title's second calendar week

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<sup>14</sup> Many titles in this random sample have low overall sales and zero sales in a lot of the observed weeks; but a significant number of titles exhibits hump-shaped sales. For the purposes of this paper, I therefore selected four example titles on the basis of the available number of sales observations and data volatility.

<sup>15</sup> In many European countries including Germany, book prices are by law subject to resale price maintenance; that is, retailers must not offer discounts from the publisher's list price. See Beck (2006) for more details.

<sup>16</sup> According to the raw data, single copies of title 1 and 3 were sold two and three weeks before sales of this title took off, respectively (with 33 and 129 copies sold in that week, respectively). I treated these early sales as erroneously booked advance orders and hence assumed that 34/130 copies were sold in the respective title's release week.

Table 4: Final estimation results for example titles\*

	Title 1	Title 2	Title 3	Title 4
$M$	17285.027 (3823.504)	13251.633 (692.085)	20388.379 (1351.369)	34350.723 (871.083)
$\theta$	.696 (.094)	.979 .	.550 (.099)	.870 (.028)
$p$	.022 (.015)	.064 (.005)	.055 (.014)	.054 (.003)
$q$	1.273 (.788)	2096.171 .	.287 (.104)	.635 (.114)
$\lambda_1$	137.481 (129.880)	461.750 (80.566)	1196.847 (126.896)	88.205 (97.366)
$\lambda_2$	0 .	321.662 (80.549)	2289.711 (126.160)	284.724 (97.323)
$\lambda_3$	132.403 (129.893)	653.708 (80.526)	3965.155 (125.590)	600.899 (97.282)
$\lambda_4$	38.084 (130.816)	470.941 (80.495)	1517.897 (125.224)	479.749 (97.241)
$\rho$	.356 (.113)	0	0	0
Observations (weeks)	76	53	43	80
$R^2$	.838	.957	.991	.981
Root MSE	128.3	78.9	117.9	96.5
Iterations	27	45	17	17
Total sales:				
observed	14842	13879	27809	34253
predicted	17593	15160	29358	35804
Price (EUR)	19.90	10.00	24.00	19.90

\*NLS estimates. Standard errors in parentheses (computed using the delta method, based on asymptotic standard errors for the log-transformed NLS parameters).

as a result of word of mouth, while in fact first- and second-week figures are not comparable due to a different number of sales days. Low sales figures in the first week, as compared to later weeks, for titles 1, 2 and 3 may indicate that this is an issue for the example titles studied here. Since I do not have information on title-specific release dates, my estimations therefore only use observations from the second week onwards, hence  $t=2, \dots, T$ .

*Direct estimates.* As expected, after an initial estimation round based on equation 5 and following the procedure outlined in section 2.3, the null hypothesis of AR(0) errors is rejected against the AR(1) alternative for title 1. For the other titles, it cannot be rejected. Therefore, I present results based on equation 5 for these titles. For title 1, I re-estimate the model with the AR(1) assumption (equation 7) and for  $t=3, \dots, T$ . Table 4 presents the corresponding results.

Except for title 2, all parameters appear reasonable and precisely estimated. With a  $\theta$ -estimate very close to one, a very large  $q$ -estimate and missing standard errors, the estimates for ti-



title 2 appear to be of the degenerate kind encountered in the simulation. Not surprisingly, the present model seems to be too complex for this title, whose weekly sales decrease quite steadily from week 2 onwards. In response, the estimation procedure converges to a set of parameters which implies this steady decrease.

Figure 3 plots sales and corresponding predicted values for all four titles. Due to the incorporation of autocorrelated errors, the predicted sales pattern for title 1 is not as smooth as for the other two titles. The respective  $\rho$ -estimate (in table 4) is quite significant and suggests that error autocorrelation is modestly positive. The fit measures  $R^2$  and root mean squared error (MSE), however, indicate that the data are in general more variant for title 1 as compared to the other titles, thus not only as a result of autocorrelation.<sup>17</sup> Regarding the estimates' economic significance, titles 3 and 4 both have an estimated period purchase probability ( $\hat{p}$ ) for influential buyers of around 5.5%. This implies that it takes around 13 weeks until half of the influential buyers have purchased the title. It takes 31 weeks with a hazard rate of 2.2%, as estimated for title 1. Accordingly, by its 76th sales week, title 1 has reached a lower share of predicted total sales (sum of  $\hat{M}$  and  $\hat{\lambda}_i$ ) than titles 3 and 4 in 43 and 80 sales weeks, respectively.

The estimated word of mouth parameters seem to suggest some stereotype attributes for the observed titles. Title 1, for example, resembles the shockseller pattern of simulation set A: influentials make up for a comfortable majority of buyers ( $\hat{\theta} \approx .7$ ); combined with a large word of mouth coefficient  $q$ , sales quickly and strongly peak, but then resume to a relatively slow decay pattern from week 20. Title 3, in contrast, with a relatively low  $q$ -estimate tends to have sleeper qualities, leading to sales that decrease much more slowly over time. Sales of title 4 sales exhibit an early but moderate peak. Correspondingly, its  $\theta$ -estimate suggests that a relatively small share of its buyers were driven by word of mouth (13%, excluding repeat Christmas purchases).

**Indirect estimates.** In order to account for Christmas present purchases as a special case of word of mouth, I use the  $\lambda$ -estimates and information on pre-December predicted cumulative sales  $N(t^C, \hat{\theta})$  – where  $t^C$  denotes the last November sales week – to obtain an estimate for  $c$  (cf. equation 6). Also, recall the word of mouth coefficient  $\tilde{q}$  from section 2, which has a more intuitive interpretation than  $q$  and is obtained from estimates  $\hat{q}$  and  $\hat{\theta}$  (cf. equation 2). Table 5 summarizes both  $c$ - and  $\tilde{q}$ -estimates, as implied by estimation results.

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<sup>17</sup> I include the  $R^2$  measure only to compare fit across titles. High  $R^2$  values are common in non-linear models and not per se suggestive of a good specification (Trajtenberg and Yitzhaki, 1989).

Figure 3: Observed sales and values predicted from the model

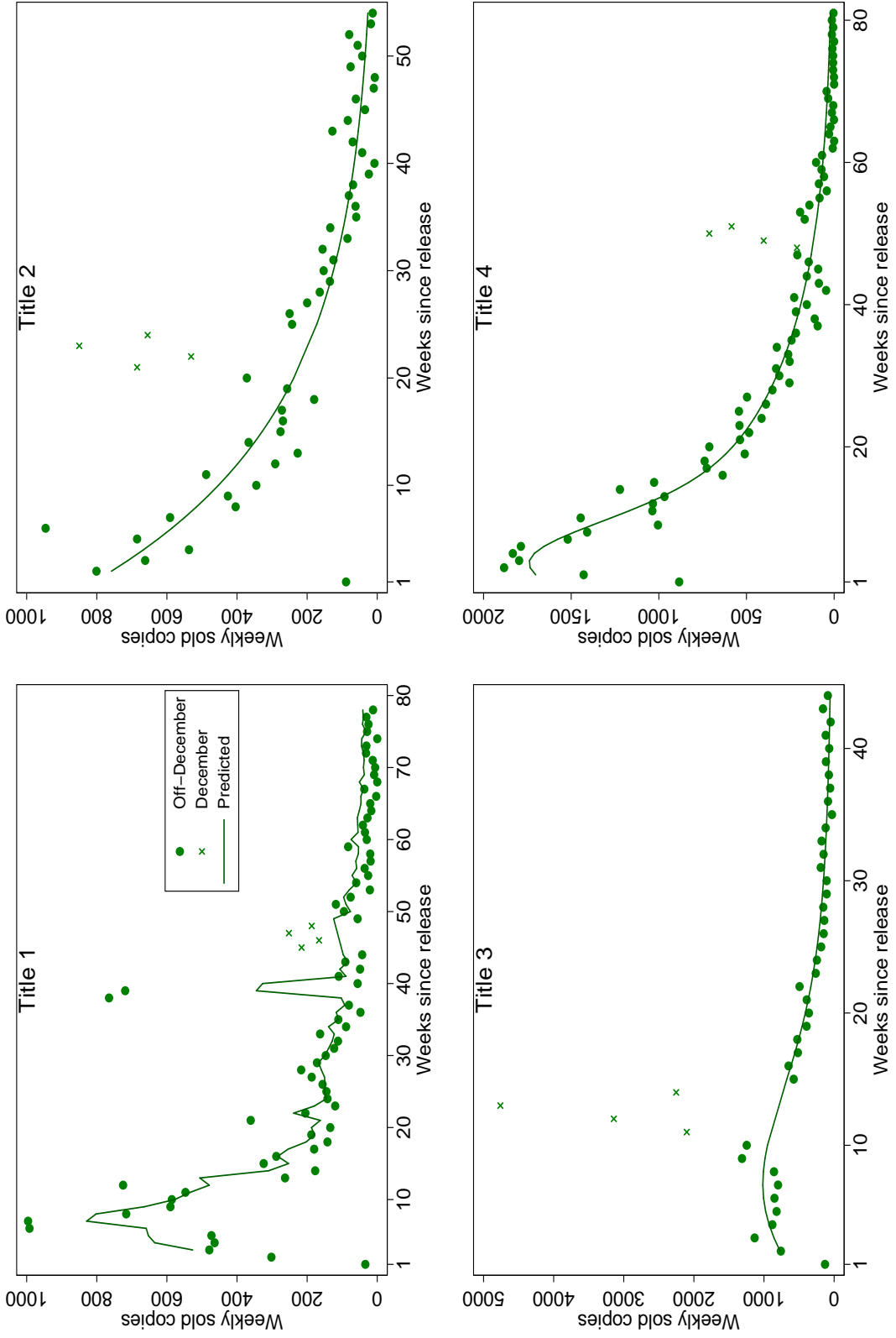


Table 5: Implied estimates

	Title 1	Title 3	Title 4
$\tilde{q}$	.556	.234	.095
$c$	.024	1.02	.047
$N(t^C, \hat{\theta})$	13012	8796	31107
$\sum \hat{\lambda}_i$	308	8969.6	1453.6

For title 1, the estimates  $\hat{q}$  and  $\hat{\theta}$  imply a  $\tilde{q}$  of about .6, indicating that almost six out of ten influential buyers are estimated to have recommended title 1 to imitators each period. A  $\hat{c}$  of about .02 suggests that on average only 2% of all pre-December buyers of title 1 are estimated to have purchased an additional copy as Christmas present in December. Interestingly, the other two titles have lower estimates for  $\tilde{q}$ , but higher  $\hat{c}$ . Title 3 is estimated to have generated about one Christmas present purchase per pre-December buyer on average. This seemingly negative correlation between  $\tilde{q}$ - and  $c$ -estimates, although hardly generalizable from a sample of three, is suggestive of a typology of book recommendations. Some titles are prone to instantaneous recommendation through classic word of mouth (as measured by a high  $\tilde{q}$ ), while classic word of mouth for other titles is withheld (low  $\tilde{q}$ ) in favor of a stronger form of recommendation: a surprise Christmas present (high  $c$ ).

## 5 Conclusion

Conventional wisdom holds that word of mouth between heterogeneous buyers is a crucial success factor for new creative goods. In this paper, I study a model of new-product diffusion that captures some of the particularities of word of mouth on new creative goods and especially the book market. Important features of this model are a heterogeneous population of buyers – whose word of mouth can have an effect on total sales of a title – and the explicit treatment of Christmas present purchases. Like most diffusion models, it is highly nonlinear in its parameters, which can complicate estimation in certain circumstances. A simulation exercise shows that parameters can be estimated fairly accurately with sufficiently many, not too volatile observations. Estimation results for four example titles appear informative and intuitively reasonable and thus illustrate the model’s applicability. Further development of empirical methodology is warranted, however, in order to reduce estimation bias, for example by incorporating level-dependent heteroskedasticity.

Both academic and professional researchers can fruitfully apply the approach I present in this paper. For example, an *ex-post* estimate of consumer segmentation for a particular hardcover edition of a title can be informative for publishers regarding the marketing strategy for future paperback or book club releases. In an analysis of sales of a single title, information on events behind outliers can be added to the model in the same fashion as the Christmas dummies in order to estimate additional sales effects of these events. Publishers can compare estimates across titles in order to test and evaluate marketing strategies.

Researchers concerned with public policy may also benefit. Demand uncertainty is often claimed to be an essential characteristic of creative industries: the *nobody knows* property (Caves, 2000). Regarding the book industry, demand uncertainty serves as a building block to justify the use of vertical restraints such as resale price maintenance (in Europe) or excessive returns policies (in the U.S.). The micro-economic foundations of demand uncertainty in creative industries are, however, in general unclear. This paper highlights a clear form of demand uncertainty: uncertainty about the occurrence and intensity of positive word of mouth. Applied to a larger number of titles, its empirical approach to word of mouth could shed light on the global nature of demand uncertainty in the book trade.

# Appendix

Figure 4: Distribution of simulated estimates ( $M, p$ )

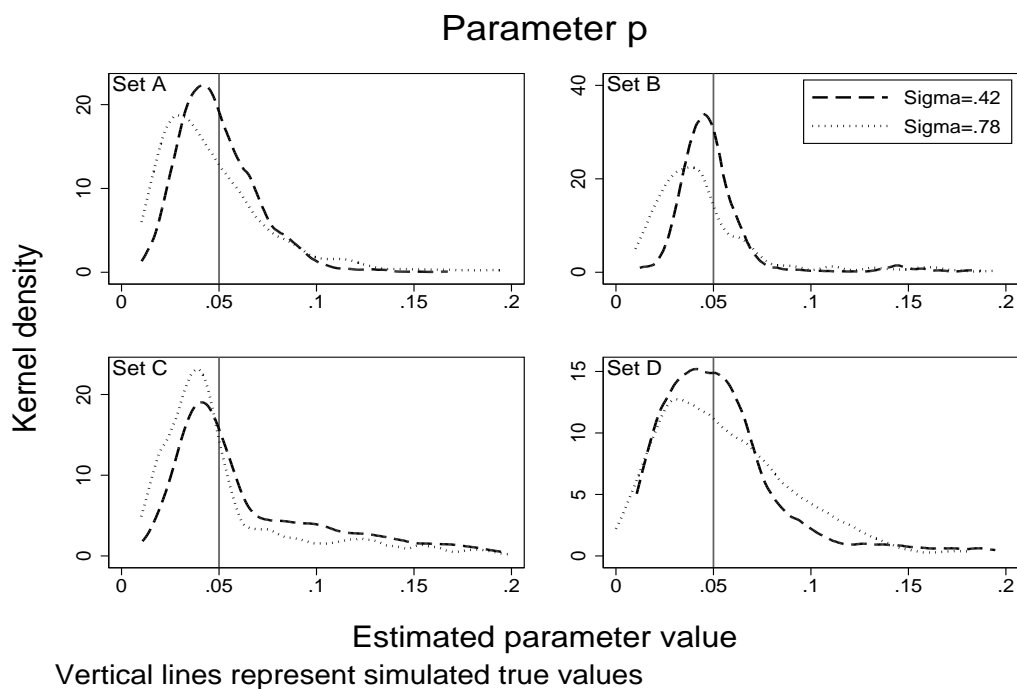
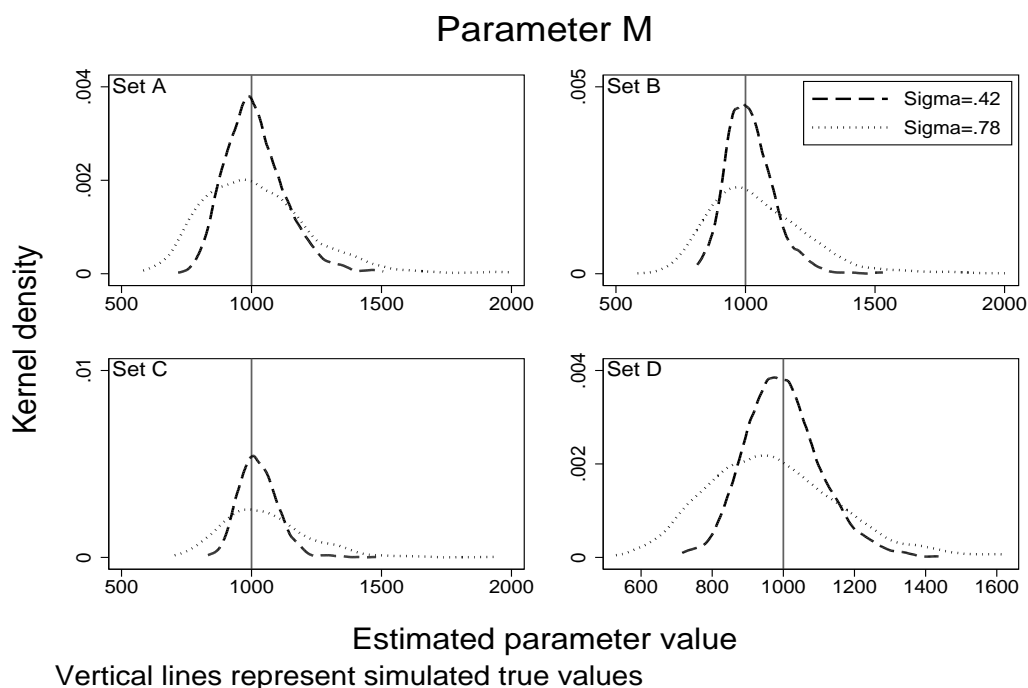
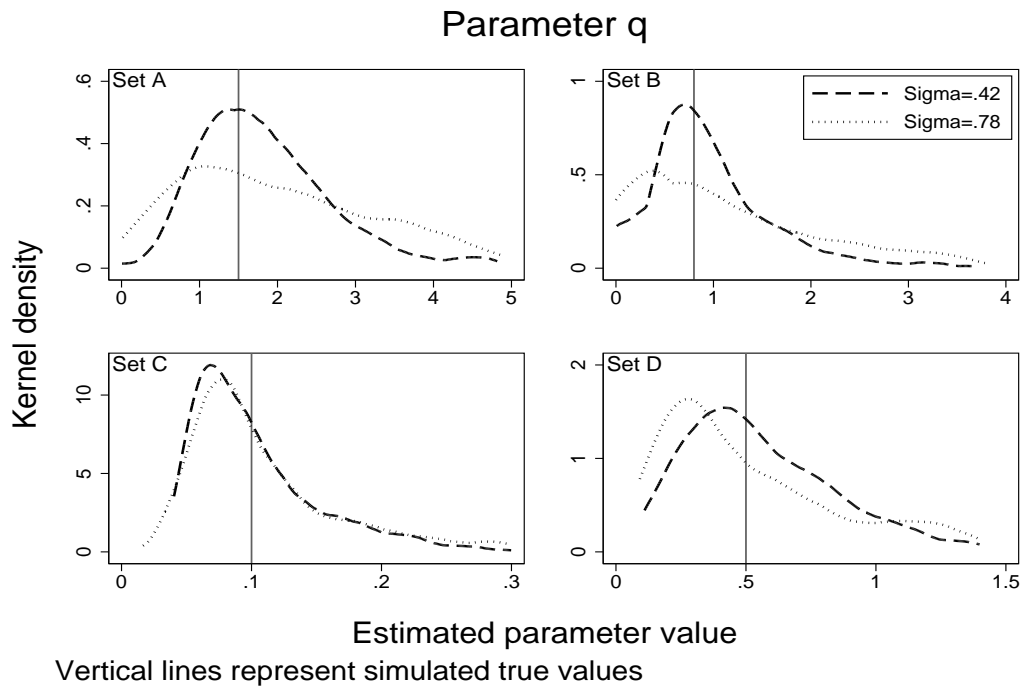
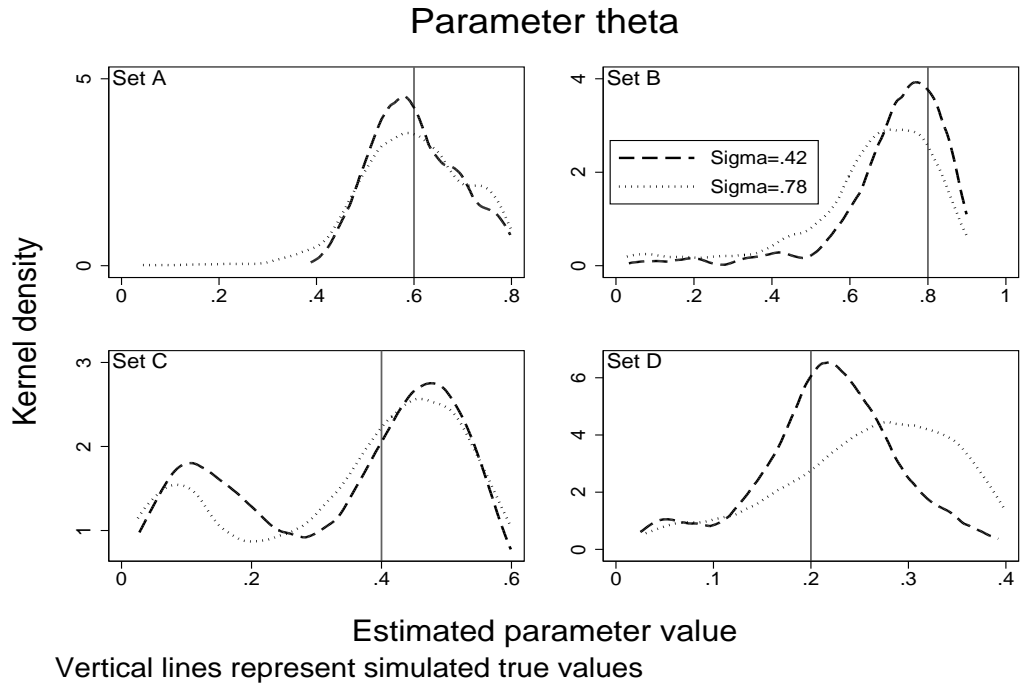


Figure 5: Distribution of simulated estimates ( $\theta, q$ )



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