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## Liquidity shortages and monetary policy

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# LIQUIDITY SHORTAGES AND MONETARY POLICY

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# LIQUIDITY SHORTAGES AND MONETARY POLICY

## Abstract

The paper models the interaction between risk taking in the financial sector and central bank policy for the case of pure illiquidity risk. It is shown that, when bad states are highly unlikely, public provision of liquidity may improve the allocation, even though it encourages more risk taking (less liquid investment) by private banks. In general, however, there is an incentive of financial intermediaries to free ride on liquidity in good states, resulting in excessively low liquidity in bad states. In the prevailing mixed-strategy equilibrium, depositors are worse off than if banks would coordinate on more liquid investment. In that case, liquidity injection will make the free riding problem even worse. The results show that even in the case of pure illiquidity risk, there is a serious commitment problem for central banks. We show that unconditional free lending against good collateral, as suggested by the Bagehot Rule, fails to address the moral hazard problem: Even though we consider a model with pure illiquidity risk, it turns out that such a policy will encourage banks to behave naughtily, providing insufficient level of liquidity.

JEL Code: E5, G21, G28.

Keywords: monetary policy, liquidity risk, financial stability.

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*"When the music stops, in terms of liquidity, things will be complicated. But as long as the music is playing, you've got to get up and dance. We're still dancing,"* Chuck Prince, Citigroup chief executive, Financial Times July 10<sup>th</sup> 2007

*"Moral hazard fundamentalists misunderstand the insurance analogy"*

Lawrence Summers, Financial Times, Sept. 24th 2007

*"Just as imprudent banks have been saved from their mistakes by indulgent central bankers, so CDO-makers could be rewarded for the mess that they helped to create. ... The creators of CDOs and conduits may end the year with new Porsches. Vroom-vroom."*

Croesus's cousins, Economist, Sept. 22nd 2007

# 1. Introduction

## 1.1 The Issues

For quite some time, at least a few market participants had the feeling that financial markets have been susceptible to excessive risk taking, encouraged by extremely low risk spreads. There was the notion of abundant liquidity, stimulated by a "savings glut"; by an "investment drought" or by central banks running too-loose monetary policies. In that context, some brave economists warned against the rising risk of a liquidity squeeze which might force central banks to ease policy again (compare, for example, *A fluid concept*, *The Economist* (February 2007)). Frequently it was argued that it was exactly the anticipation of such a central bank reaction which encouraged further excessive risk taking: The belief in "abundant" provision of aggregate liquidity might have resulted in overinvestment in activities creating systemic risk.

Since August 2007, liquidity indeed has dried out worldwide. There has been an unprecedented freeze on the money markets, triggering desperate calls within the financial sector to lower interest rates.<sup>1</sup> Initially, central banks have been split over how to respond to the credit squeeze. Some central banks immediately pumped billions of extra money into the financial system; some even lowered interest rates. Others warned of the hazards of providing central bank insurance to those institutions that have engaged in reckless lending. **Mervyn King**, Bank of England governor, argued (FT, Sept. 12 2007): *"The provision of large liquidity facilities penalises those financial institutions that sat out the dance, encourages herd behaviour and increases the intensity of future crises."*

The current problems in financial markets provoked a heated debate on causes and potential solutions. At Jackson Hole, **James Hamilton** (2007) called for regulatory and supervisory reforms, pointing out that significant negative externalities have been created. This paper tries to shed some light on a crucial type of externality involved: the incentive of financial intermediaries to free ride on liquidity. The paper, the main part having been written before the outbreak of the crisis, concentrates on a

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<sup>1</sup> The eruption in credit market turmoil has taken some by surprise— see **Alan Greenspan's** remark *"I ask you if anybody in early June could contemplate what we are now confronted with?"* WSJ September 7, 2007. Others have been puzzled that it took so long to trigger fire sales – see the references in **Illing** 2007.

particular, but – from our point of view – key issue: It focuses on the interaction between risk taking in the financial sector and central bank policy. For that purpose, we analyse an economy with pure illiquidity risk. Intuition suggests that injection of public liquidity should always be welfare improving in that highly unrealistic case. A surprising result of the paper is that even for pure illiquidity risk, intuition turns out not to be correct in general.

We prove that insuring against aggregate risks will result in a higher share of less liquid projects funded. So liquidity provision as public insurance does indeed encourage higher risk taking. But one has to be careful about the impact on welfare: this effect will not necessarily result in “excessive” risk. For some parameter values, liquidity provision turns out to be welfare improving (as suggested in the traditional literature on lender of last resort, see **Goodhart/ Illing** 2002). In the presence of aggregate risk, banks may prefer to take no precaution against the risk of being run in bad states, when these states are highly unlikely. If so, public provision of liquidity to prevent inefficient bank runs improves upon the allocation, even though it encourages more risk taking (less liquid investment) by private banks. So liquidity provision by central banks provides an insurance against aggregate risk in an incomplete market economy, encouraging investment in projects which give a higher return, but at the same time exhibit higher risk of illiquidity.

But, unfortunately, this result does not hold in general. As we will show, the incentive of financial intermediaries to free ride on liquidity in good states may result in excessively low liquidity in bad states. In the prevailing mixed-strategy equilibrium, depositors are worse off than if banks would coordinate on more liquid investment. When the mixed-strategy equilibrium prevails, public liquidity injection would increase the incentive to free ride, making the free riding problem even worse. If that case prevails, the central bank should commit to abstain from intervening in order to discourage free riding. The results derived show that liquidity injection is a delicate issue possibly creating severe moral hazard problems.

The present paper builds on the set up of **Diamond/ Rajan** (2006) and extends it to capture the feedback from liquidity provision to risk taking incentives of financial intermediaries. As in **Diamond/ Rajan**, deposit contracts solve a hold up problem for impatient lenders investing in illiquid projects: these contracts give banks as financial intermediaries a credible commitment mechanism not to extract rents from their specific skills. But at the same time deposit contracts make non-strategic default very costly. Consequently, negative aggregate shocks may trigger bank runs with serious costs for the whole economy, thus destroying the commitment mechanism. **Diamond /Rajan** (2006) show that monetary policy can alleviate this problem in an economy with nominal deposits: Via open market operations, the central bank can mimic state contingent real debt contracts by adjusting the nominal price level to the size of the aggregate shock.

The paper extends the set up of **Diamond/Rajan** in several ways. In their model, the type of risky projects is exogenously given. Banks can either invest in risky, possibly illiquid projects or invest

instead in a safe liquid asset with inferior return. In the equilibrium they characterise, banks invest all resources either in illiquid or liquid assets. They do not analyse the feedback mechanism from monetary policy towards the risk taking of financial intermediaries when central bank policy works as an insurance mechanism against aggregate risk.

In contrast, the present paper determines endogenously the aggregate level of illiquidity out of private investments. As in Diamond/ Rajan, illiquidity is captured by the notion that some fraction of projects turns out to be realised late. In contrast to their approach, however, we allow banks to choose the proportion of funds invested in less liquid projects continuously. These projects have a higher expected return, but at the same time also a higher probability of late realisation. Because of that feature, some banks will have an incentive to free ride on liquidity. Banks investing a larger share in illiquid projects with higher, yet delayed returns will always be more profitable as long as they stay solvent. Yet there is an economic role for liquidity to satisfy the need for early withdrawals by investors in our model. The problem is that “naughty” free riding banks can always attract funds away from those prudent banks which had invested in more liquid, but less profitable assets (to use the poetic phrase by Mervyn King: those financial institutions that sat out the dance).

In times of a liquidity crisis, the “naughty” banks will run into trouble. They would have to leave the market, to make sure that ex ante expected returns for depositors are the same for all banks. If, however, the central bank provides liquidity to the market in bad states, this helps “naughty” banks to survive, allowing them to indeed pay out high returns later. The at first sight surprising, but at second thought quite intuitive reason is that “naughty” banks are always in a better position to attract funds even in a crisis – as long as policy helps them to stay solvent (Note that in this paper we abstract from insolvency except if triggered by illiquidity). The problem is that relying on such interventions ex ante will give all banks strong incentives to behave “naughty”, so liquidity is bound to dry out in the sense that there will be insufficient supply of real goods in the intermediate period. Of course, a commitment not to intervene in these cases is not really credible, as sadly has been demonstrated in the UK in September 2007, when Northern Rock (a mortgage bank in the UK which promised high deposit rates as a way to finance attractive investment in real estate) smashed the credibility of the Bank of England just the day after Mervyn King reconfirmed his brave statements in a letter to the chancellor.

Our results cast serious doubts on perceived wisdom as captured by the Bagehot Rule. According Walter Bagehot, in a pure liquidity crisis, central banks should lend freely against good collateral at a penalty rate. Our model shows that such a policy fails to address the moral hazard problem: Even though we consider a model with pure illiquidity risk, it turns out that unconditional lending will encourage banks to behave naughty, providing insufficient level of liquidity. Surprisingly, naughty banks will always be able to offer more good collateral than prudent banks as long as there is no solvency risk except triggered by illiquidity. Contrary to what has been suggested in the Bagehot rule, central banks should instead commit to target liquidity provision only to prudent banks.

## 1.2 Related Literature

Liquidity provision has been mainly analysed in the context of models with real assets - see **Diamond/ Dybvig** (1983), **Bhattacharya/ Gale** (1987), **Diamond/ Rajan** (2001, 2005), **Fecht/ Tyrell** (2005) and for a survey the reader of **Goodhart/ Illing** (2002). Only a few recent papers explicitly include nominal assets and so are able to address monetary policy (**Allen/ Gale** (1998), **Diamond/ Rajan** (2006), **Skeie** (2006) and **Sauer** (2007)). **Skeie** (2006) shows that nominal demand deposits, repayable in money, can prevent self-fulfilling bank runs of the **Diamond/ Dybvig** type, when interbank lending is efficient.

Here, we are concerned with bank runs triggered by real shocks as in **Diamond/ Rajan** (2006). Demand deposits provide a credible commitment mechanism. A related, but quite different mechanism has been analysed by **Holmström/ Tirole** (1998). They model credit lines as a way to mitigate moral hazard problems on the side of firms. In their model, **Holmström/ Tirole** also characterise a role for public provision of liquidity, but again they do not consider feedback mechanisms creating endogenous aggregate risk.

Apart from **Diamond/ Rajan** (2006), the paper most closely related is **Sauer** (2007). Building on the cash-in-the-market pricing model of **Allen /Gale** (2005), Sauer analyses liquidity provision by financial markets and characterises a trade-off between avoiding real losses by injecting liquidity and the resulting risks to price stability in an economy with agents subject to a cash-in-advance constraint. The present paper uses the more traditional framework with banks as financial intermediaries. This framework can capture the impact of financial regulation of leveraged institutions in a straightforward way.

## 1.3 Sketch of the Paper

Section 2 presents the basic settings of the model. Let us here sketch the structure informally. There are three types of agents, and all agents are assumed to be risk neutral.

- (1) **Entrepreneurs**. They have no funds, just ideas for productive projects. Each project needs one unit of funding in the initial period 0 and will either give a return early (at date 1) or late (at date 2). There are two types of entrepreneurs: Entrepreneurs of type 1 with projects maturing for sure early at date 1, yielding a return  $R_1 > 1$  and entrepreneurs of type 2 with projects yielding a higher return  $R_2 > R_1 > 1$ . The latter

projects, however, may be delayed: With probability  $1 - p$ , they turn out to be illiquid and can only be realised at date 2. For projects being completed successfully, the specific skills of the entrepreneur are needed. Human capital being not alienable entrepreneurs can only commit to pay a fraction  $\gamma R_i > 1$  to lenders. They earn a rent  $(1 - \gamma) R_i$  for their specific skills. Entrepreneurs are indifferent between consuming early or late.

(2) **Investors.** They have funds, but no productive projects on their own. They can either store their funds (with a meagre return 1) or invest in the projects of entrepreneurs. Investors are impatient and want to consume early (in period 1). Resources being scarce, there are less funds available than projects of either type. In the absence of commitment problems, investors would put all their funds in early projects  $R_1$  and capture the full return; Entrepreneurs would receive nothing. But financial intermediaries are needed to overcome commitment problems. In addition to the entrepreneur's commitment problem, specific collection skills are needed to transfer the return to the lender. As shown in Diamond/Rajan (2001, 2005), by issuing deposit contracts designed with a collective action problem (the risk of a bank run), bankers can credibly commit to use their collection skills to pass on to depositors the full amount received from entrepreneurs. So limited commitment motivates a role for banks as intermediaries.

(3) **Banks.** Due to their fragile structure, bankers are committed to pay out deposits as long as banks are not bankrupt. Holding capital (equity) can reduce the fragility of banks, but it allows bankers to capture a rent (assumed to be half of the surplus net of paying out depositors) and so lowers the amount of pledgeable funds. Like entrepreneurs, bankers are indifferent between consuming early or late.

Banks offer deposit contracts. There is assumed to be perfect competition among bankers, so investors deposit their funds at those banks offering the highest expected return at the given market interest rate. Most of the time (see footnote 3), we assume that investors are able to monitor all bank's investment. So if, in a mixed strategy equilibrium, banks differ with respect to their investment strategy, the expected return from deposits must be the same across all banks.

Except for introducing two types of entrepreneurs, the structure of the model is essentially the same as the set up of Diamond/Rajan (2006). By assuming that depositors (investors) value



consumption only at  $t = 1$ , all relevant elements are captured in the most tractable way: at date 1, there is intertemporal liquidity trade with inelastic liquidity demand. Banks competing for funds at date 0 are forced to offer conditions which maximise expected consumption of investors at the given expected interest rates. Whereas Diamond/Rajan (2006) just present numerical examples for illustrating relevant cases, we fully characterise the type of equilibria as a function of parameter values. Furthermore, we derive endogenously the extent of financial fragility as a function of the parameter values.

As a reference point, section 3 analyses the case of pure idiosyncratic risk. It is shown that banks will choose their share of investment in safe projects such that all banks will be always solvent, given that there is liquid trading on the inter bank market. Section 4 introduces aggregate shocks. The outcome strongly depends on the probability of a bad aggregate shock occurring. If this probability is low, banks care only for the good state (proposition 1 a)) and accept the risk of failure with costly liquidation in the bad state. In contrast, banks play safe if the probability of a bad shock is very high (proposition 1b)). For an intermediate range, however (proposition 2), financial intermediaries have an incentive to free ride on excess liquidity available in the good state. This leads to low liquidity in bad states. In the prevailing mixed-strategy equilibrium, depositors are worse off than if banks would coordinate on more liquid investment.

Section 5 analyses central bank intervention. With nominal bank contracts, monetary policy can help to prevent costly runs by injecting additional money before  $t=1$ . The real value of deposits will be reduced such that banks on the aggregate level are solvent despite the negative aggregate shock. It turns out that if the probability of a bad aggregate shock is low enough, central bank intervention is welfare improving, even though banks relying on liquidity injection will invest more in illiquid late projects. If, however, the probability of a bad aggregate shock is high, central bank intervention will make the free riding problem even worse. In any case, the central bank needs to be able to commit to restrict liquidity provision only to prudent banks. Otherwise, free riding crowds out all prudent banks in equilibrium. Such a commitment, however, is not dynamically consistent. So liquidity injection is a delicate issue, possibly creating severe moral hazard problems. Section 6 concludes.

## 2 The Model - Basic Settings

### 2.1 Agents, Technologies and Preferences

There is a continuum of risk-neutral *investors* with unit endowment at  $t=0$  who want to consume at  $t=1$ . They have access only to a storage technology with return 1, i.e. their wealth may be simply stored without perishing for future periods. As an alternative, they can lend their funds to finance profitable long term investments of entrepreneurs. Due to commitment problems, lending has to be done via financial intermediation.

There are two types of *entrepreneurs* who have ideas for projects: When funded, type  $i=1,2$  entrepreneurs can produce:

Type 1: Safe projects, yielding  $R_1 > 1$  for sure early at date 1.

Type 2: Risky projects, yielding  $R_2 > R_1 > 1$  either early at date 1 with probability  $p$  (and  $pR_2 < R_1$ ), or late at date 2 with probability  $1-p$

Borrowing and lending is done via competitive and risk-neutral *banks* of measure  $N$ , who have no endowment at  $t=0$ . Banks use the investor's funds (obtained via deposits or equity) to finance and monitor entrepreneurs' projects. They have a special collection technology such that they can capture a constant share  $0 < \gamma < 1$  of the project's return. The fragile banking structure allows them to commit to pass those funds which have been invested as deposits back to investors (see below). For funds obtained via equity, banks are able to capture a rent (assumed to be  $1/2$  of the captured return net of deposit claims).

Entrepreneurs and banks are indifferent between consumption at  $t=1$  or  $t=2$ . Because only banks have the special skills in collecting deposits from investors and returns from entrepreneurs, entrepreneurs cannot contract with investors directly; instead, they can only get projects funded via bank loans.

Resources are scarce in the sense that there are more projects than aggregate endowment of investors. This excludes the possibility that entrepreneurs might bargain with banks on the level of  $\gamma$ .

## 2.2 Timing

There are 4 periods:

(1)  $t = 0$

The banks offer deposit contract to investors, promising fixed payment  $d_0$  in the future for each unit of deposit. The investors deposit their endowments if  $d_0 \geq 1$ . The banks then decide the share  $\alpha$  of total funds to be invested in safe projects. Funded entrepreneurs receive loans and start their projects.  $d_0$  and  $\alpha$  are observable to all the agents, but  $p$  may be unknown at that date.

The *fixed payment deposit contract* has the following features:

- a) Investors can claim a fixed payment  $d_0$  for each unit of deposit at any date after  $t = 0$ ;
- b) Banks have to meet investors' demand with all resources available. If liquidity at hand is not sufficient, delayed projects have to be liquidated at a cost: Premature liquidation yields only  $c$  ( $0 < c < 1 < \gamma R_1$ ) for each unit.

These contracts are adopted in the banking industry as a commitment mechanism. Since collecting returns from entrepreneurs requires specific skills, the bankers would have an incentive to renegotiate with lenders at  $t = 1$  in order to exploit rents. So a standard contract would break down. As shown in **Diamond /Rajan** (2001), the debt contract can solve the problem of renegotiation: Whenever the investors anticipate a bank might not pay the promised amount, they will run and the bank's rent is completely destroyed by the costly liquidation. Therefore the banks will commit to the contract.

(2)  $t = \frac{1}{2}$

At that intermediate date,  $p$  is revealed and so the investors can calculate the payment from the banks. If a banks resources are not sufficient to meet the deposit contract, i.e. the investors' expected average payment at  $t = 1$  is  $d_1 < d_0$  for each unit of deposit, all investors will run the bank already at  $t = \frac{1}{2}$  in the attempt to be the first in the line, and so still being

paid  $d_0$ . When a bank is run at  $t = \frac{1}{2}$ , it is forced to liquidate all projects immediately (even those which would be realized early) trying to satisfy the urgent demand of depositors – so in the case of a run, the bank will not be able to recover more than  $c$  from each project.

To concentrate on runs triggered by real shocks, we exclude self fulfilling panics: As soon as  $d_1 \geq d_0$  investors are assumed never to run and to believe that the others don't run either.

(3)  $t = 1$

If the investors didn't run in the previous period, they withdraw and consume. The banks collect a share  $\gamma$  from the early projects. But as long as entrepreneurs are willing to deposit their rents at  $t = 1$  at banks, banks can pay out more resources to investors. Since early entrepreneurs retain the share  $1 - \gamma$  of the returns and they are indifferent between consumption at  $t = 1$  or  $t = 2$ , the banks can borrow from them against the return of late projects at the market interest rate  $r \geq 1$ .  $r$  clears market by matching aggregate liquidity demand with aggregate liquidity supply. We assume that there is a perfectly liquid inter bank market at  $t = 1$ , so even if early entrepreneurs trade with other banks, the initial bank will be able to borrow the liquidity needed to refinance delayed projects as long as it is not bankrupt.

(4)  $t = 2$

Banks collect return from late projects and repay the liquidity providers at  $t = 1$ . Both early and late entrepreneurs consume.

In the following sections we analyse the outcomes of the game in various scenarios.

### 3 Pure Idiosyncratic Shocks

As a baseline, consider the case in which  $p$  is deterministic and known to all the agents at  $t = 0$ . Equilibrium is characterised by the share  $\alpha$  of funds banks choose to invest in safe projects and the interest rate  $r$  for deposits invested at  $t = 1$ . The outcome is captured in the following lemma:

**LEMMA 1** *When  $p$  is deterministic, there exists a symmetric non-idle pure strategy equilibrium in which*

$$1) \text{ All the banks set } \alpha_i(p, r) = \alpha^*(p, r) = \frac{\gamma \frac{1-p}{r} - (1-\gamma)p}{\gamma \frac{1-p}{r} + (1-\gamma) \left( \frac{R_1}{R_2} - p \right)}, \quad \forall i \in [0, N];$$

2) *Interest rate  $r$  is determined by*

$$r \int_0^N (1-\gamma) [\alpha_i R_1 + (1-\alpha_i) p R_2] di = \int_0^N \gamma (1-\alpha_i) (1-p) R_2 di \text{ and } r \leq \frac{R_2}{R_1}.$$

*What's more, there exists no equilibrium in mixed strategies.*

**PROOF:** See Appendix.

By LEMMA 1 multiple equilibria exist for all  $1 \leq r \leq \frac{R_2}{R_1}$ . To make the analysis interesting, we introduce the following equilibrium selection criterion:

**DEFINITION** *An optimal symmetric pure strategy equilibrium profile  $\alpha^*(p, r^*)$  is given by*

$$(1) \ r^* = \arg \max_r \kappa_i = \alpha_i(p, r) R_1 + (1-\alpha_i(p, r)) p R_2;$$

$$(2) \ \forall \alpha'_i(p, r^*) \neq \alpha^*(p, r^*) \text{ with } \alpha_{-i}(p, r^*) = \alpha^*(p, r^*),$$

$$\kappa_i(\alpha^*(p, r^*)) \geq \kappa_i(\alpha'_i(p, r^*), \alpha_{-i}(p, r^*)) \text{ in which } -i \in [0, N] \setminus \{i\}.$$

The optimal symmetric equilibrium is the dominant equilibrium from the investor's point of view. Resources of investors being scarce, the market solution would maximise the payoff of investors in the absence of commitment problems (that is, in the case of  $\gamma = 1$ ). Since the optimal symmetric equilibrium comes closest to achieving that market outcome, from now on we will focus our analysis on this specific equilibrium.

**LEMMA 2** *When  $p$  is deterministic, there exists a unique optimal symmetric equilibrium of pure strategy in which*

$$1) \text{ All the banks set } \alpha^*(p, r^*) = \frac{\gamma - p}{\gamma - p + (1 - \gamma) \frac{R_1}{R_2}}, \forall i \in [0, N];$$

$$2) \text{ Interest rate } r^* = 1.$$

From now on, denote  $\alpha^*(p, r^*)$  by  $\alpha(p)$  for simplicity.

**PROOF:** See Appendix.

Then if the risks are purely idiosyncratic, the equilibrium outcome is given by:

**COROLLARY** *When there are idiosyncratic risks such that for one bank  $i$  the probability  $p_i$  follows i.i.d. with pdf  $f(p_i)$  with a non-empty support  $\Omega \subseteq [0, \gamma]$ , then there exists a unique optimal symmetric equilibrium of pure strategy in which*

$$1) \text{ All the banks set } \alpha(E[p_i]) = \frac{\gamma - E[p_i]}{\gamma - E[p_i] + (1 - \gamma) \frac{R_1}{R_2}}, \forall i \in [0, N];$$

$$2) \text{ Interest rate } r^* = 1.$$

This is pretty intuitive: As long as there are just idiosyncratic shocks, banks are always solvent via trade on the liquid inter bank market.

In the absence of aggregate risk, the optimal equilibrium can thus be characterised in a straightforward way. When there is only idiosyncratic risk, a share  $p$  of risky projects will always be realized early in the aggregate economy. The representative bank chooses the share  $\alpha^*$  of funds invested in safe projects such that in period 1, it is able to pay out depositors and equity to all investors. Otherwise, the bank would be bankrupt and forced to liquidate late projects at high costs (liquidation gives an inferior return of  $c < 1$ ).

So in the absence of aggregate risk, each bank invests in such a way that it is able to fulfill all claims of depositors at  $t=1$ . At that date, early entrepreneurs pay back  $\gamma R_j$  ( $j \in \{1,2\}$ ) to their bank. Being indifferent between consumption at  $t=1$  and  $t=2$ , early entrepreneurs will also deposit all their own rents – the share of retained earnings  $(1-\gamma) R_j$  – at safe banks. With a perfect liquid inter-bank market, unlucky banks with a high share of delayed projects are able to borrow loans from those banks which turn out to have a low share of delayed projects. So a representative bank is able to pay out at  $t=1$  total resources available  $\alpha R_1 + (1-\alpha) p R_2$  to depositors, when the market interest rate between  $t=1$  and  $t=2$  is  $r^* = 1$ . As shown in LEMMA 2,  $r^* = 1$  supports the equilibrium giving depositors the highest expected return.

Depositors having a claim of  $\gamma \cdot E[R(\alpha, r)] = \gamma [\alpha(\bar{p}, r) R_1 + (1-\alpha(\bar{p}, r)) R_2]$  per unit deposited, the total amount to be paid out via deposits at  $r^* = 1$  is  $\gamma [\alpha R_1 + (1-\alpha) R_2]$ . The representative bank will choose  $\alpha^*$  such that at  $t=1$ , there are just enough resources available to pay out all depositors, taking into account that early entrepreneurs are reinvesting their rents at banks as deposits at  $t=1$ . The condition  $\alpha R_1 + (1-\alpha) \bar{p} R_2 = \gamma [\alpha R_1 + (1-\alpha) R_2]$  gives as solution for  $\alpha^*$  as a function of  $\bar{p}$  (see FIGURE 1):

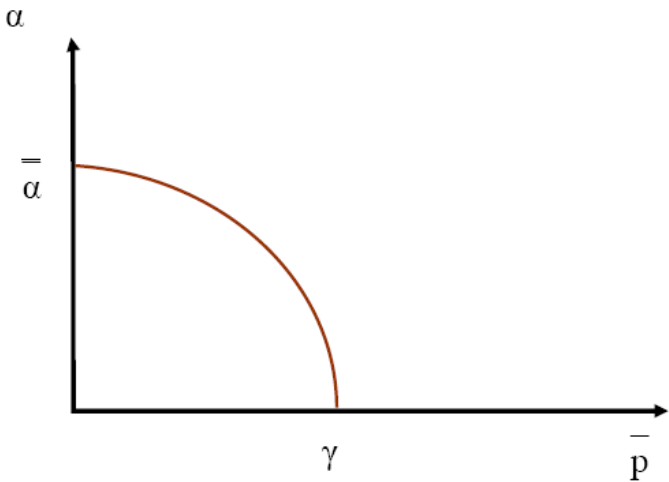


FIGURE 1:  $\alpha^*$  (the optimal share of funds invested in safe projects) as a function of  $\bar{p}$  (the aggregate share of type 2 projects realized early)

$$\alpha^*(\bar{p}) = \frac{\gamma - \bar{p}}{\gamma - \bar{p} + (1 - \gamma)(R_1 / R_2)}$$

$$\text{with } \frac{\partial \alpha^*}{\partial \bar{p}} = \frac{-(1 - \gamma)(R_1 / R_2)}{[\gamma - \bar{p} + (1 - \gamma)(R_1 / R_2)]^2} < 0; \quad \frac{\partial \alpha^*}{\partial R_2 / R_1} > 0.$$

$$\alpha^* \in [0, \bar{\alpha}] \text{ with } \alpha^*(\bar{p} = 0) = \bar{\alpha} = \frac{\gamma}{\gamma + (1 - \gamma)(R_1 / R_2)} > \gamma;$$

$$\alpha^*(\bar{p} = \gamma) = 0; \quad \alpha^*(\gamma = 1) = 1$$

The higher  $\bar{p}$  (the larger the share of early projects with a high payoff  $R_2$ ), the lower the share of funds invested in projects of type  $R_1$ . If  $\bar{p} > \gamma$ , the representative bank would be solvent at  $t = 1$  even when all funds were invested in risky type 2 projects. But even if  $\bar{p} = 0$ , there will be some investment in projects with a high payoff  $R_2$  as long as  $\gamma < 1$ . The reason is that all early entrepreneurs, deferring consumption until  $t = 2$ , provide liquidity at  $t = 1$ . They are willing to deposit their rents at solvent banks. Thus, banks are able to pay out investors all funds available at  $t = 1$  as long as they stay solvent. This way, with low interest rates, investors can also gain from the higher payoff of late projects, so  $\alpha^*(\bar{p} = 0) > \gamma$ . With  $R_2 / R_1$  increasing, the share  $\alpha$  invested in safe projects will rise, allowing investors to profit from higher returns of less liquid projects already at  $t = 1$ . Again, this is due to the fact that early entrepreneurs provide liquidity. Note, however, that there would be no funding of risky projects at all in the absence of a commitment problem (that is, if  $\gamma = 1$ ).

## 4 The Case of Aggregate Risk

The interesting case is the case of aggregate risk. Assume that  $p$  is now unknown to all the agents at  $t = 0$  and realizes at  $t = \frac{1}{2}$  as an aggregate risk. We assume that

(1)  $p$  can take just two possible values  $p_L$  or  $p_H$  with  $0 < p_L < p_H < \gamma$ ;

(2)  $p_H$  realizes with probability  $\pi$  and  $p_L$  with probability  $1 - \pi$ .

In the presence of aggregate risk, a bank has several options available: The bank may just take care for provisions in the good state, choosing  $\alpha^* = \alpha(p_H)$  and may take no precaution



against the risk of a bank run in the bad state  $p_L$ . If so, the bank is run when  $p_L$  realizes and is forced to liquidate all projects. Obviously, this does not make sense if the probability of the bad state is high enough. Instead, the bank may increase the share of safe assets to  $\alpha^* = \alpha(p_L)$  trying to prevent insolvency. If all banks would follow that strategy, there would be excess supply of liquidity in the good state  $p_H$ . This may give banks an incentive to free ride on the provision of liquidity by other banks, and a pure strategy equilibrium may not exist.<sup>2</sup> So a careful analysis of all cases is required. We will now show that there are 3 types of equilibria, depending on the probability  $\pi$  – the probability that a high share of early projects is realized.

A) PROPOSITION 1 a): If  $\pi$  is high enough (for  $\pi \in [\bar{\pi}_2, 1]$ ), all banks will choose  $\alpha^*(p_H)$ . With that strategy, banks will be run at  $p_L$ , so depositors get only the return  $c$  if the share of early projects with high yields turns out to be unpleasantly low. All agents in the economy being risk neutral, it is more profitable for banks to take that risk into account in order to gain from the high returns in aggregate state  $p_H$ , as long as that event is not very likely.

B) PROPOSITION 1 b): If  $\pi$  is low enough (for  $\pi \in [0, \bar{\pi}_1]$ ), all banks will choose  $\alpha^*(p_L)$ . In that case, banks will never be bankrupt, so they will be able to payout all depositors at  $t = 1$  even if the share of delayed projects is high. But if the share of delayed projects is low (in the state  $p_H$ ), there will be excess liquidity floating around at  $t = 1$ .

C) PROPOSITION 2: For some parameter constellations (for the intermediate range  $\pi \in [\bar{\pi}_1, \bar{\pi}_2]$ ), banks will be tempted to free ride<sup>3</sup> on the excess liquidity in state  $p_H$ . These banks invest all their funds in the risky projects ( $\alpha = 0$ ), trying to profit from the high returns available in case a large share of profitable projects happens to be realized early. The high expected returns in this case compensate depositors ex ante for the risk of getting just  $c$  in the other aggregate state of the world.

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<sup>2</sup> Banks may also hold some equity in order to cushion shocks. We will discuss this in section 6 but ignore equity in this section.

<sup>3</sup> **Bhattacharya/ Gale** (1987) have already shown that there is free riding on liquidity provision when investors cannot monitor the amount of projects invested by the intermediaries. Footnote 4 confirms their argument in our context. But we derive a stronger result. We show that for an intermediate range of parameter values, even with perfect monitoring of banks, some banks have an incentive to free ride on liquidity in good states, giving rise to a mixed strategy equilibrium, resulting in excessively low liquidity in bad states. In the prevailing mixed-strategy equilibrium, depositors are worse off than if banks would coordinate on more liquid investment.

**PROPOSITION 1** Given  $p_H$  and  $p_L$ , and suppose that  $\alpha$ 's are observable<sup>4</sup> to all investors: a) There is a unique optimal symmetric equilibrium of pure strategy such that all the banks set  $\alpha^* = \alpha(p_H)$  as soon as the probability of  $p_H$  satisfies

$$\pi > \bar{\pi}_2 = \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c}, \text{ in which } E[R_s] = \alpha(p_s)R_1 + (1 - \alpha(p_s))R_2, s \in \{H, L\}; \text{ b)}$$

When  $0 \leq \pi < \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c} = \bar{\pi}_1$ , there exists a unique optimal symmetric equilibrium

of pure strategy such that all the banks set  $\alpha^* = \alpha(p_L)$ .

**PROOF:** See Appendix.

The intuition behind PROPOSITION 1 is the following: When it is very unlikely that the low state realizes, i.e.  $\pi$  is very high, then the cost of a bank run is too small relative to the high return in the high state. So the best strategy for the banks is to exploit the maximum return from the high state and neglect the cost in the low state. On the contrary, when it is very likely that the low state realizes, then the cost of bank run is too high relative to the high return in the high state. Therefore the best strategy for the banks is to stick to the safest strategy and avoid the high cost in the low state. The interesting outcome takes place for intermediate  $\pi$  such that the cost of bank run is also intermediate and return from liquidity free-riding is sufficiently high in the high state:

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<sup>4</sup> This condition is crucial for  $\pi \in [0, \bar{\pi}_2]$ . If  $\alpha$ 's were not observable to investors in this range,  $\alpha(p_L)$  would fail to be a symmetric equilibrium of pure strategy. The reason is straight-forward: Suppose that all the banks coordinate and set  $\alpha^* = \alpha(p_L)$ , then there is always incentive for one single bank  $i$  to deviate and set  $\alpha_i = \alpha(p_H)$  because it earns positive profit at  $p_H$

$$\gamma [\alpha(p_H)R_1 + (1 - \alpha(p_H))R_2] - \gamma [\alpha(p_L)R_1 + (1 - \alpha(p_L))R_2] > 0,$$

and at  $p_L$  it is run with zero profit because of limited liability. In the end its expected profit is positive, which is larger than its peers who get zero profit because of perfect competition. Anticipating this, the banks would never coordinate to set  $\alpha^* = \alpha(p_L)$ .

**PROPOSITION 2** When  $\frac{\gamma \cdot E[R_L] - c}{\gamma R_2 - c} < \pi < \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c}$ , there exists no symmetric equilibrium of pure strategies. What's more, given  $p_H R_2 < R_1$  and  $c$  not too high ( $c < 1$ ) there exists a unique equilibrium of mixed strategies<sup>5</sup> such that for a representative bank:

1) With probability  $\theta$  the bank chooses to be risky – it sets  $\alpha_r^* = 0$ , and with probability  $1 - \theta$  to be safe – it sets  $\alpha_s^* > 0$ ;

2) Interest rates at states  $p_H$  and  $p_L$  are  $r_H > r_L > 1$ ;

3) At  $t = 0$  a risky bank offers a deposit contract with  $d_0^r = \gamma \left[ p_H R_2 + \frac{(1 - p_H) R_2}{r_H} \right]$  and a safe bank with  $d_0^s = \gamma \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_H R_2 + \frac{(1 - \alpha_s^*)(1 - p_H) R_2}{r_H} \right]$ ;

4) Equal return condition:  $\kappa_r = \pi d_0^r + (1 - \pi) c = d_0^s = \kappa_s$ ;

5) Market clearing conditions:

5a) At  $p_H$ :  $\theta D_r + (1 - \theta) D_s = \theta S_r + (1 - \theta) S_s$ , in which

$$\begin{cases} D_r = d_0^r - \gamma p_H R_2, \\ D_s = d_0^s - \gamma \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_H R_2 \right], \\ S_r = (1 - \gamma) p_H R_2, \\ S_s = (1 - \gamma) \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_H R_2 \right]; \end{cases}$$

5b) At  $p_L$ :  $r_L (1 - \gamma) \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_L R_2 \right] = \gamma (1 - \alpha_s^*) (1 - p_L) R_2$ , i.e.  $\alpha_s^* = \alpha^*(p_L, r_L)$ .

**PROOF:** See Appendix.

<sup>5</sup> As shown in Allen/Gale (2004), mixed-strategy equilibria with banks choosing different portfolios may be a generic feature of equilibria with financial intermediation.

Though complicated, the intuition behind is still not difficult to see (To help the reader see the insight a numerical example is provided in Appendix 2). Suppose that we increase  $\pi$  from 0 where all the banks set  $\alpha_i = \alpha(p_L)$ . When  $\pi$  just gets higher than  $\bar{\pi}_1$  free-riding on liquidity provision becomes profitable because

- (1) The cost of bank run is no longer too high;
- (2) At  $p_H$  the early entrepreneurs have excess liquidity supply. Therefore, an arbitrary bank  $i$  can free-ride and set its  $\alpha'_i = 0$ . By doing so it can trade liquidity at  $t = 1$  from early entrepreneurs with high return from its late projects and promise  $d'_0 = \gamma R_2 > \gamma \cdot E[R_L] = d_0$  to the investors. The higher return in state  $p_H$  compensates the fact that it is surely run at  $p_L$  due to liquidity shortage.

But if every bank would behave as a free-rider, there would not be sufficient liquidity supply. So free-riders and prudent banks must co-exist, i.e. the equilibrium is of mixed strategies.

The free-riding behaviour results in two consequences: (1) As more banks become free-riders, the interest rate  $r_H$  is bid higher; (2) The prudent banks set lower  $\alpha_s^* < \alpha(p_L)$  in order to cut down the opportunity cost of investing in safe projects. And in the end,  $r_H$  and  $\alpha_s^*$  are adjusted such that depositors are indifferent between the two types of banks.

On the aggregate level the probability of being a free-rider is determined by market clearing conditions for both states.

The resulting inefficiency is captured by the following corollary:

**COROLLARY** *For the equilibrium of mixed strategies defined by PROPOSITION 2, the banks are worse off than the case if they coordinate and choose  $\alpha_i = \alpha(p_L)$ .*

**PROOF:** The banks return is equal to  $d_0^s = \kappa(\alpha^*(p_L, r_L)) < \kappa(\alpha(p_L))$  by LEMMA 2, given the fact that  $r_L > 1$ .

*Q.E.D.*

FIGURE 2 illustrates the expected payoff for investors as characterized in PROPOSITION 1 and 2. When  $\pi$  (the probability that a large share of type 2 projects will be realised early) is very high, banks prefer to exploit the higher profitability of these projects rather than to self insure against the risk of a bank run. As long as the probability of a bank run is small enough (less than  $1 - \pi_2$ ), the risky strategy gives investors a higher expected return (PROPOSITION 1a).

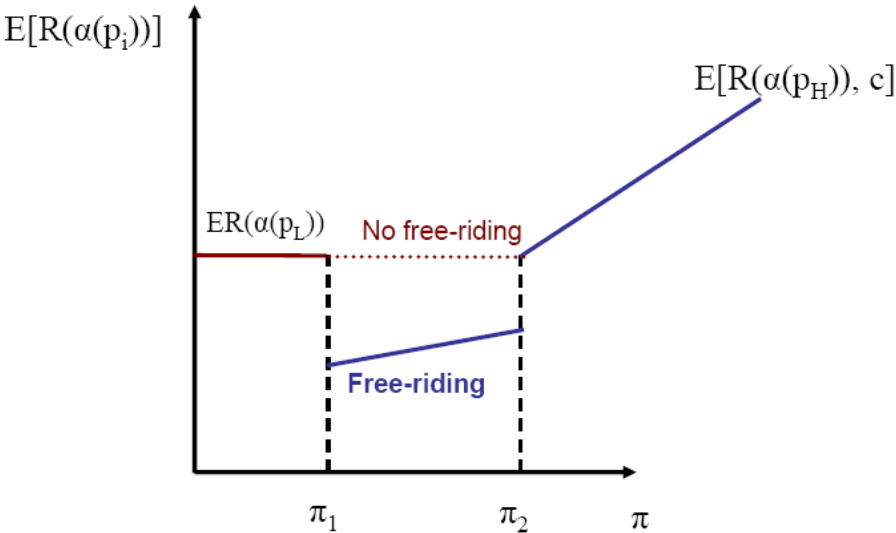


FIGURE 2: Expected payoff for investors as a function of  $\pi$  (the probability that the share of early type 2 projects is high)

In contrast, when it is very likely that the bad state (with a low share of early type 2 projects) occurs, banks prefer to play safe by investing sufficiently in type 1 projects so as to make sure to be never run (PROPOSITION 1b). Whenever  $\pi < \pi_2$ , such a strategy would give investors the highest expected payoff, even though the safe strategy results in excess liquidity if the good state turns out to be realized. But as shown in PROPOSITION 2, for  $\pi$  high enough there is an incentive of naughty banks to free ride on the excess supply of liquidity available in the good state. In the range  $\pi_1 < \pi < \pi_2$ , a mixed strategy equilibrium prevails with inferior return to investors. Free riding down the expected payoff for investors below the level feasible in the absence of free riding in this range.

## 5 Central Bank Intervention

Let us now consider the role of monetary policy. Suppose that central bank is now the fourth player in the game. We make some slight changes to the original game in the following way:

- (1) At  $t = 0$  the banks provide *nominal* deposit contract to investors, promising a fixed nominal payment  $d_0$  in the future. The central bank announces a minimum level  $\underline{\alpha}$  of investment on safe projects required to be eligible for liquidity support in times of a crisis;
- (2) At  $t=1/2$  the banks decide whether to borrow liquidity from central bank. If yes, the central bank commits to provide liquidity for banks provided they fulfil the requirement  $\underline{\alpha}$  ;
- (3) At  $t = 1$  the central bank supports those banks having fulfilled the requirement defined in (2) by injecting money at the low borrowing rate  $r^{CB} = 1$  if asked for.

For simplicity we assume that one unit of money is of equal value to one unit real good in payment. And the price level is determined by *cash-in-the-market* principle (Allen / Gale, 2005), i.e. the ratio of amount of liquidity (the sum of money and real goods) in the market to amount of real goods.

Central bank intervention may help to prevent inefficient liquidation in the case of aggregate shocks for high values of  $\pi$  (the probability of a high share of early projects  $p_H$  being high enough). This intervention reduces the critical threshold  $\bar{\pi}_2$  to the left (to  $\bar{\pi}_2'$ ) and so expands the range of parameter values for which it is optimal to choose the risky strategy  $\alpha^* = \alpha(p_H)$ . To avoid incentives for free riding, however, central bank intervention has to be made contingent on banks having investing a minimum level  $\underline{\alpha}$  in safe projects at stage 0.

By injecting liquidity in case of a crisis, the central bank can prevent inefficient liquidation of early projects via bank runs, raising expected returns of those banks choosing a risky strategy  $\alpha^* = \alpha(p_H)$  when  $p_L$  is realized. So let us consider the case of aggregate shocks when  $\pi$  is high and the central bank sets  $\underline{\alpha} = \alpha(p_H)$ . In this case banks will set  $\alpha^* = \alpha(p_H)$  and borrow liquidity from central bank only at  $p_L$ . Given this the investors will no longer run at  $p_L$  because they can only get  $c$  real goods plus  $d_0 - c$  money for each unit of deposit.

Instead if they wait till  $t = 1$ , they will get  $\kappa[R_H | p_L] = \alpha(p_H)R_1 + (1 - \alpha(p_H))p_L R_2 > c$  real goods plus  $d_0 - \kappa[R_H | p_L] = (1 - \alpha(p_H))(p_H - p_L)R_2$  money, and they are better off by waiting.

Now the lower bound for  $\alpha^* = \alpha(p_H)$  being the dominant strategy is shifted towards:

$$\bar{\pi}_2' = \frac{\gamma \cdot E[R_L] - \kappa[R_H | p_L]}{\gamma \cdot E[R_H] - \kappa[R_H | p_L]} < \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c} = \bar{\pi}_2$$

So free-riding is partially deterred and the investors are better off with higher return,

$$\pi\gamma \cdot E[R_H] + (1 - \pi)\kappa[R_H | p_L] > \pi\gamma \cdot E[R_H] + (1 - \pi)c.$$

For high enough  $\pi$  ( $\pi > \bar{\pi}_2'$ ), injection of money before  $t = 1$  can help to improve the allocation. Since it prevents costly runs, obviously, banks relying on central intervention will invest more in illiquid late projects. So the range of parameter values for which it is optimal to choose the risky strategy  $\alpha^* = \alpha(p_H)$  is expanded. Nevertheless, liquidity provision improves the allocation in an incomplete market economy, provided central bank intervention is made contingent on banks having investing a minimum level  $\underline{\alpha}$  in safe projects at stage 0. The central bank's goal is consistent with the banks' strategies since  $\underline{\alpha} = \alpha(p_H)$ .

Suppose now that  $\pi$  is low enough ( $0 \leq \pi \leq \bar{\pi}_1$ , with  $\bar{\pi}_1$  being the same as that in PROPOSITION 1). The equilibrium is very similar to PROPOSITION 1b. The central bank can simply announce  $\underline{\alpha} = \alpha(p_L)$ . The banks would coordinate to meet this requirement, since the cost of free-riding is too high (anyone who sets a lower  $\alpha$  would not be bailed out by the central bank and is run at  $p_L$ ).

When  $\pi$  is intermediate ( $\bar{\pi}_1 < \pi < \bar{\pi}_2'$ ) the equilibrium is again of mixed strategies, as in PROPOSITION 2. The difference is that the prudent banks now have an outside option to obtain cheap liquidity from the central bank when the market rate is bid up. Given that the central bank announces  $\underline{\alpha} = \alpha(p_L)$  and a prudent bank  $i$  sets  $\alpha_i = \underline{\alpha}$ , when at  $p_H$  the market rate is bid up by naughty banks, the prudent bank is able to obtain liquidity from the central bank instead of buying expensive liquidity from early entrepreneurs. In contrast, the naughty banks have to obtain liquidity at the higher market rate  $r^M \gg 1$  from early entrepreneurs. Naughty banks will be run at  $p_L$ . In the end, the expected nominal returns from both types of banks have to be equal in equilibrium.

The targeted injection is designed so as not to save the naughty bank: Due to the competitive banking service, the prudent banks will be forced to transfer **all** injected liquidity to their investors. So in the bad state, the naughty banks cannot obtain liquidity via the inter-bank market. Consequently, the prudent banks can meet their nominal deposit contract with cheap liquidity provided by the central banks, whereas the naughty banks would be punished struggling in vain to get liquidity from the market at a higher rate. Such a policy might work, provided the central bank has perfect knowledge about the type of banks. But if there is the slightest doubt whether a bank is really prudent or not, such a scheme runs the risk to fail.

Surely the central bank's intervention improves allocation when  $\pi$  is high, which seems to make the intervention justified. However, the welfare improvement for intermediate  $\pi$  is limited, or at least ambiguous, in comparison to the *laisser-faire* equilibrium as stated in PROPOSITION 2. Remember that what makes free-riding attractive there is the abundant liquidity supply at  $p_H$ . Here the prudent banks simply ask the central bank for liquidity, and all their early entrepreneurs have to go to the market seeking for buyers. This makes the market more abundant in liquidity at  $p_H$ , which makes free-riding more attractive. It lures more banks to be naughty. In the end, in comparison to the *laisser-faire* mixed strategy equilibrium, the share of naughty banks may increase – implying that there is less investment in safe project, hence less aggregate real return in  $t=1$  and more paper money – making the investors' welfare inferior.

On the other hand, the prudent banks set  $\alpha^P = \underline{\alpha} = \alpha(p_L)$  as required by the central bank. This is higher than the  $\alpha_s^*$  in the *laisser-faire* equilibrium. So the real early return from an individual prudent bank is higher. However, as just argued, the share of prudent banks is reduced. Thus, the aggregate level of real return to investors is ambiguous, likely to be lower.

FIGURE 3 illustrates the effects of targeted central bank liquidity provision on investors expected payoff. In the expanded range  $\pi > \bar{\pi}_2'$  for which the risky strategy is dominant, liquidity injection prevents bank runs with inefficient liquidation of early projects and thus raises expected returns to investors. In contrast, in the intermediate range with mixed strategy equilibria  $\bar{\pi}_1 < \pi < \bar{\pi}_2'$ , the payoff of *laisser-faire* equilibrium is likely to be lower as compared to the outcome in the absence of liquidity provision by the central bank.



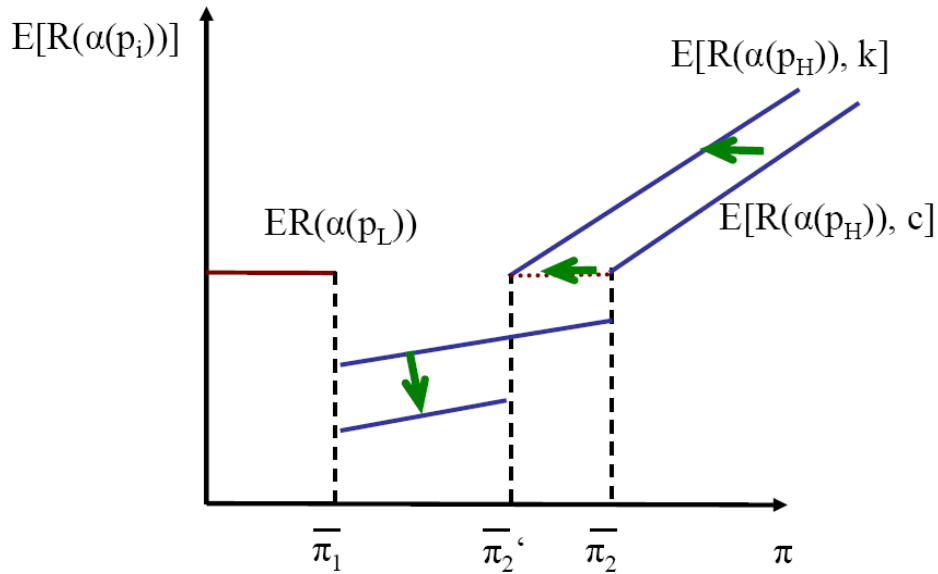


FIGURE 3: Expected payoff for investors under targeted central bank liquidity provision

In reality, however, things are likely to be even much worse because of a serious time inconsistency problem. It makes free riding even more attractive in the case of central bank intervention: Since banks face a pure illiquidity problem (all projects are known to be realized at some stage), illiquid banks can always credibly promise to pay back later. Therefore, ex post it is always welfare improving for the central bank to support the naughty banks, avoiding costly bank runs. Obviously, anticipating this behaviour ex ante increases incentives for free riding: Naughty banks, having invested all their funds in the risky projects ( $\alpha = 0$ ), can always afford to pay early investors a higher rate of return as long as central bank intervention helps to prevent bankruptcy. The problem is that naughty (free riding) banks have a higher average return than prudent banks, provided that they will be bailed out by central bank intervention. Because the naughty banks are absolutely better off than prudent banks when central bank money is provided, the incentive to free ride will be aggravated.

In formal terms, the time inconsistency problem turns liquidity provision (as defined at the beginning of this section) into liquidity flooding: The central bank just floods the market with liquidity via open market operation to keep the market rate at  $r^M = 1$ . This seems to be a fair description of the strategy central banks usually follow in times of crises. It may, however, have disastrous effects. The central bank is flooding the market for the following reasons: (1) A central bank has limited instruments for implementation. Rather than provide liquidity to specific targeted types of banks, open market operation is the central bank's most effective

(and simplest) device. It acts in its good faith that the city of Sodom should be spared from the destruction if a few righteous are found within (Genesis, 18:26); (2) When crisis hits, the naughty banks are those crying first. If the central bank gives in to their pressures too early, most of the liquidity injected is likely to be directed towards the naughty banks instead of the prudent ones. In the end, the market (which is only needed for the naughty banks at this time) is flooded by liquidity as a result.

In the end, liquidity flooding will crowd out all the prudent banks in equilibrium, as we prove now in PROPOSITION 3 for a special case.

**PROPOSITION 3** *Assume that  $\pi p_H R_2 + (1 - \pi) p_L R_2 \geq 1$  and that for  $\bar{\pi}_1 < \pi < 1$ ,  $d_0^j = \gamma R_1 < \pi p_H R_2 + (1 - \pi) p_L R_2$ . If the central bank is willing to provide liquidity to the entire market in times of crisis, all banks have an incentive to play naughty, choosing  $\alpha_j = 0$ .*

**PROOF:** Suppose that a representative bank chooses to be prudent with  $\alpha_i = \underline{\alpha}$ , and promises a nominal deposit contract  $d_0^i = \gamma [\underline{\alpha} R_1 + (1 - \underline{\alpha}) R_2]$  in order to maximize its investors return. Then when the bad state with high liquidity needs is realized, the central bank has to inject enough liquidity into the market to keep interest rate at  $r=1$  in order to ensure bank  $i$ 's survival. However, given  $r=1$ , a naughty bank  $j$  can always profit from setting  $\alpha_j = 0$ , promising the nominal return  $d_0^j = \gamma R_2 > d_0^i$  to its investors. Thus, surely the banks prefer to play naughty. For other parameter values, there may not exist any equilibrium at all with liquidity injection, suggesting that liquidity provision makes the world more vulnerable, driving banks to corner solutions (see Appendix).

Proposition 3 shows that providing market liquidity can be quite dangerous. Abraham argued in Genesis, God should save the entire city because a few good men are living in it. The problem with this advice is that such a rescue simply makes the naughty men (banks) better off without suffering the punishment (the bank runs) they deserve. So in order not to encourage even more free riding, the central bank should commit to abstain from bailing out naughty banks. It should stick firmly to its commitment as credible “lender to quality” instead of playing “lender of last resort”. Obviously, such a commitment is not really credible during a crisis: Once the bad state has been realized, liquidity injecting can prevent investors from running the banks, so ex post it will always be welfare improving. The efficient solution (targeting only prudent banks) is dynamically inconsistent.

These results show that liquidity injection is a delicate issue possibly creating severe moral hazard problems. It casts serious doubt on the desirability of central bank intervention. This argument seems to be very robust. It would be straightforward to introduce vulture funds in the model trying to buyout some of the bankrupt naughty banks in the bad state, financed by liquidity provision of early entrepreneurs. These vulture funds could at least partly mitigate the social costs involved with bank runs. We plan to do this in a future extension. Obviously, public liquidity provision will prevent the market price of failed banks from falling sufficiently to be profitable for vulture funds.

The current setup models pure illiquidity risk. With asymmetric information about insolvency risk, intuition suggests that the moral hazard problem is likely to become even worse. It is left for future research to find out whether this notion is true.

As is often the case with economic models, some policy conclusions are not clear cut: Assume the central bank would be really able to strictly commit to targeted liquidity provision. If that is the case, liquidity injection could definitely be welfare improving for some range of parameter values (for very high  $\pi$ ); for lower values, however, it turns out to have ambiguous effects. Which case is more relevant? The sets with different ranges of local equilibria are the result of the discrete probability space.

A natural extension would be to extend the set up to a continuous probability distribution for  $p$ . Our intuition is that the generic outcome for the continuous case is captured by the mixed-strategy equilibrium for the following reason: the set-up is characterised by serious non-convexities which are likely to result in mixed-strategy equilibria even for continuous state space. We plan to analyse this in future research. In any (or rather in the realistic) case, if commitment is not feasible, liquidity provision is haunted by moral hazard issues with disastrous impact.

Furthermore, liquidity injection may also impede the role of money as a medium to facilitate ordinary transactions. This question is left for future work (see Sauer 2007 for a first analysis of the trade-off between financial stability and price stability).

## 6 Conclusion

The paper analyses the interaction between risk taking in the financial sector and central bank policy in an economy with pure illiquidity risk. We extend the model of Diamond/ Rajan (2006) to capture the feedback from liquidity provision to risk taking incentives of banks. We show that liquidity provision encourages higher risk taking: insuring against aggregate risks results in a higher share of less liquid projects funded.

It turns out that the impact on welfare is ambiguous: Assume first the central bank is able to strictly commit to targeted liquidity provision. For some parameter values, liquidity provision turns out to be welfare improving, allowing banks to take more socially valuable risks. But we show that liquidity provision has ambiguous effects for other parameter values. More seriously: Central banks need to be able to commit to abstain from providing liquidity via open market operations in order to discourage free riding. Such a commitment, however, is not credible. In the absence of commitment, provision of public liquidity may have disastrous effects. It increases the incentive of financial intermediaries to free ride on liquidity in good states, resulting in excessively low liquidity in bad states. There is a serious dynamic consistency problem.

The surprising result is that – contrary to prevailing intuition - the moral hazard problem is inherent even in an economy with pure illiquidity risk. Of course in reality, unlike in models, there is no clear cut distinction between illiquidity and insolvency risk. It should be fairly straightforward to make the model more realistic and introduce asymmetric information about solvency of the financial intermediaries. A promising route might be to follow **Brunnermeier and Pederson** (2007). With private information about solvency risk the moral hazard problem is likely to become more serious. A detailed analysis is left for future research.

In the model presented, the optimal policy response depends to some extent on specific parameter values (the probability of the bad state occurring). This is an artifact of the discrete probability space. Our conjecture is that the generic outcome in continuous state space is the mixed-strategy equilibrium with commitment to no intervention as optimal solution. Again, we leave this to future research.

How should the dynamic consistency problem be solved? Do we really suggest not to intervene during an acute crisis? Following the "Austrian hangover theory" some argue that creating a recession might be necessary to purge the excesses of previous booms, leaving the

economy in a healthier state. The “winds of creative destruction” would cause healthy pain. We don’t think this is a sensible solution to the problem. Bad investments in the past should not require the unemployment of good workers in the present. Rather, we think the incentive problem needs to be addressed in other ways – by stronger regulation or alternative instruments. Just as in standard dynamic consistency problems, the right approach is to tackle the externalities directly. Currently, central banks are caught in a trap reminding of a Greek tragedy. It was a humiliating experience to see the credibility of the Bank of England being smashed by a Northern rock engaged in reckless lending.

The key challenge, of course, is the question what instruments should be used in order to address the underlying externalities. The current set-up provides some foundation to analyse this question: it is flexible enough to incorporate equity and the role of capital requirements. We plan to do this in future research.

Some may argue that a banking model cannot address realities of a modern economy with highly securitised markets. In our view, this is a misunderstanding: Following Diamond Rajan, we analysed the impact of liquidity injection in a sound model based on an explicit optimal contract for the underlying commitment problem which turns out to be a fragile banking system. As impressively demonstrated by Northern Rock, a run on markets with the risk of fire sales can be at least as devastating as a run on traditional banks, whenever there are leveraged institutions borrowing short and lending long. We have, however, serious doubts that the securitisation arrangements in the US subprime markets have been based on an optimal principal agent contract addressing the inherent incentive problems in an adequate way. We are still waiting for an optimal contract model of securitisation and are happy to analyse the impact of liquidity provision again in such a model whenever it will be available.

Our results cast serious doubts on perceived wisdom as captured by the Bagehot Rule. According Walter Bagehot, in a pure liquidity crisis, central banks should lend freely against good collateral at a penalty rate. Our model shows that such a policy fails to address the moral hazard problem: Even though we consider a model with pure illiquidity risk, it turns out that unconditional lending will encourage banks to behave naughty, providing insufficient level of liquidity. Surprisingly, naughty banks will always be able to offer more good collateral than prudent banks as long as there is no solvency risk except triggered by illiquidity. Contrary to what has been suggested in the Bagehot rule, central banks should instead commit to target liquidity provision only to prudent banks.

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# Appendix

## 1 Proofs

**PROOF OF LEMMA 1:** The proof is done by the following steps:

**Claim 1:** Any non-idle equilibrium must be symmetric.

Since the banks are competitive, therefore in equilibrium no bank is able to make strictly positive profit. Without restriction there exists a kind of equilibria in which some banks stay idle with zero profit by taking inferior strategies and getting no deposit at all. To make the results interesting, we exclude such equilibria throughout the paper.

As a direct conclusion, a representative bank  $i$  being active must achieve the same expected return  $\kappa_i = \gamma[\alpha_i R_1 + (1 - \alpha_i) p R_2] + \frac{\gamma(1 - \alpha_i)(1 - p) R_2}{r}$ . Given equilibrium outcome  $r$ , all the banks should take the same  $\alpha_i$  (here we don't require  $\alpha_i$  be pure strategy).

**Claim 2:** Any non-idle symmetric equilibrium of pure strategy takes the form stated in **LEMMA 1**.

Consider a representative bank  $i$  with  $\alpha_i$ . Its problem is to maximize its expected return, i.e.

$$\begin{aligned} \max_{\alpha_i} \quad & \kappa_i = \gamma[\alpha_i R_1 + (1 - \alpha_i) p R_2] + \frac{\gamma(1 - \alpha_i)(1 - p) R_2}{r} \\ \text{s.t.} \quad & r \int_0^N (1 - \gamma)[\alpha_i R_1 + (1 - \alpha_i) p R_2] di = \int_0^N \gamma(1 - \alpha_i)(1 - p) R_2 di. \end{aligned}$$

The constraint above is just market clearing condition.

By symmetry  $r(\alpha_i) = \frac{\gamma(1 - \alpha_i)(1 - p) R_2}{(1 - \gamma)[\alpha_i R_1 + (1 - \alpha_i) p R_2]}$ , then  $\kappa_i = \alpha_i R_1 + (1 - \alpha_i) p R_2$ . Since

$R_1 > p R_2$ ,  $\alpha_i$  takes the maximum possible value which is given by  $r(\alpha_i)$ , solve to get

$$\alpha_i(p, r) = \frac{\gamma \frac{1 - p}{r} - (1 - \gamma) p}{\gamma \frac{1 - p}{r} + (1 - \gamma) \left( \frac{R_1}{R_2} - p \right)}.$$

Suppose that bank  $i$  deviates by setting  $\alpha'_i(p, r) \neq \alpha^*(p, r)$ . Then

$$1) \text{ If } \alpha'_i(p, r) < \alpha^*(p, r), \kappa_i(\alpha'_i(p, r), \alpha_{-i}(p, r)) = \alpha'_i R_1 + (1 - \alpha'_i) p R_2 < \kappa_i(\alpha^*(p, r));$$

$$2) \text{ If } \alpha'_i(p, r) > \alpha^*(p, r), \text{ given } r \leq \frac{R_2}{R_1}$$

$$\begin{aligned} \kappa_i(\alpha'_i(p, r), \alpha_{-i}(p, r)) &= \gamma \left[ \alpha'_i R_1 + (1 - \alpha'_i) p R_2 + \frac{(1 - \alpha'_i)(1 - p) R_2}{r} \right] \\ &< \gamma \left[ \alpha^*(p, r) R_1 + (1 - \alpha^*(p, r)) p R_2 + \frac{(1 - \alpha^*(p, r))(1 - p) R_2}{r} \right] \\ &= \kappa_i(\alpha^*(p, r)). \end{aligned}$$

Therefore no unilateral deviation is profitable.

**Claim 3:** *There exists no equilibrium of mixed strategies.*

Suppose that there exists an equilibrium of mixed strategies in which a representative bank  $i$  takes a mixed strategy  $\sigma_i$  with  $\#\text{supp}\sigma_i \geq 2$ . Take two arbitrary elements  $\alpha_i^1, \alpha_i^2 \in \text{supp}\sigma_i$  and  $\alpha_i^1 \neq \alpha_i^2$ , given  $\sigma_{-i}$  and equilibrium outcome  $r$  the following equation must hold

$$\kappa_i(\alpha_i^1, \sigma_{-i}) = \kappa_i(\alpha_i^2, \sigma_{-i})$$

meaning that  $\alpha_i^1 = \alpha_i^2$ . A contradiction.

*Q.E.D.*

## **PROOF OF LEMMA 2:**

Since  $\frac{\partial \kappa_i}{\partial r} = \frac{\partial \kappa_i}{\partial \alpha_i(p, r)} \frac{\partial \alpha_i(p, r)}{\partial r} < 0$  and  $r \geq 1$ , so  $r^* = 1$  maximizes  $\kappa_i$ .

Suppose now bank  $i$  sets  $\alpha'_i(p, r^*) \neq \alpha_i(p, r^*)$ , then the liquidity it can borrow from early entrepreneurs is given by



$$\min \left[ (1-\gamma) \left[ \alpha'_i(p, r^*) R_1 + (1-\alpha'_i(p, r^*)) p R_2 \right], \frac{\gamma (1-\alpha'_i(p, r^*)) (1-p) R_2}{r^*} \right]$$

because of the resource constraint. Then

1) For  $\alpha'_i(p, r^*) > \alpha_i(p, r^*)$ ,

$$\begin{aligned} \kappa_i(\alpha'_i(p, r^*), \alpha_{-i}(p, r^*)) &= \gamma \left[ \alpha'_i(p, r^*) R_1 + (1-\alpha'_i(p, r^*)) R_2 \right] \\ &< \gamma \left[ \alpha_i(p, r^*) R_1 + (1-\alpha_i(p, r^*)) R_2 \right] = \kappa_i(\alpha^*(p, r^*)); \end{aligned}$$

2) For  $\alpha'_i(p, r^*) < \alpha_i(p, r^*)$ ,

$$\begin{aligned} \kappa_i(\alpha'_i(p, r^*), \alpha_{-i}(p, r^*)) &= \alpha'_i(p, r^*) R_1 + (1-\alpha'_i(p, r^*)) p R_2 \\ &< \alpha_i(p, r^*) R_1 + (1-\alpha_i(p, r^*)) p R_2 = \kappa_i(\alpha^*(p, r^*)). \end{aligned}$$

So  $\nexists \alpha'_i(p, r^*) \neq \alpha_i(p, r^*)$  such that  $\kappa_i(\alpha^*(p, r^*)) < \kappa_i(\alpha'_i(p, r^*), \alpha_{-i}(p, r^*))$ .

*Q.E.D.*

**PROOF OF PROPOSITION 1:** By LEMMA 2  $\alpha(p_H)$  and  $\alpha(p_L)$  maximize the banks' expected return at  $p_H$  and  $p_L$  respectively. The banks' expected return at  $p_H$  is higher than that at  $p_L$  because

$$\kappa(\alpha(p_H), p_H) = \gamma \left[ \alpha(p_H) R_1 + (1-\alpha(p_H)) R_2 \right] = \gamma \cdot E[R_H] > \kappa(\alpha(p_L), p_L) = \gamma \cdot E[R_L].$$

However banks with  $\alpha(p_H)$  are run at  $p_L$  and only get return of  $c$ , because

$$\kappa(\alpha(p_H), p_L) = \alpha(p_H) R_1 + (1-\alpha(p_H)) p_L R_2 < \alpha(p_H) R_1 + (1-\alpha(p_H)) p_H R_2 = \kappa(\alpha(p_H), p_H).$$

So the banks prefer  $\alpha(p_H)$  to  $\alpha(p_L)$  only if  $\gamma \cdot E[R_H] \pi + (1-\pi)c > \gamma \cdot E[R_L]$ , solve to get

$$\pi > \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c} = \bar{\pi}_1.$$

When  $\pi = 0$  the problem degenerates to deterministic case, so  $\alpha^* = \alpha(p_L)$  is still the unique optimal symmetric pure strategy equilibrium.

When  $0 < \pi < \bar{\pi}_1$  any strategic profile  $\alpha^*$  in which all banks set  $\alpha^* \neq \alpha(p_L)$  cannot be an optimal symmetric pure strategy equilibrium:

- 1) For  $\alpha^* \in (\alpha(p_H), \alpha(p_L))$ , the maximum return one bank can obtain at  $p_L$  is  $\alpha^* R_1 + (1 - \alpha^*) p_L R_2 < \alpha(p_L) R_1 + (1 - \alpha(p_L)) p_L R_2 = \kappa(\alpha(p_L))$ , and the maximum return one bank can obtain at  $p_H$  is  $\gamma[\alpha^* R_1 + (1 - \alpha^*) R_2] > \gamma[\alpha(p_L) R_1 + (1 - \alpha(p_L)) R_2] = \kappa(\alpha(p_L))$ . Given this fact, the banks are run at  $p_L$  and only get an actual return of  $\gamma[\alpha^* R_1 + (1 - \alpha^*) R_2] \pi + (1 - \pi) c$ , but one can deviate by setting  $\alpha_i = \alpha(p_H)$  making a higher expected return  $\gamma[\alpha(p_H) R_1 + (1 - \alpha(p_H)) R_2] \pi + (1 - \pi) c$ ;
- 2) For  $\alpha^* \in [0, \alpha(p_H))$  in which the banks are run at  $p_L$  (because  $\alpha^* R_1 + (1 - \alpha^*) p_H R_2 > \alpha^* R_1 + (1 - \alpha^*) p_L R_2$ ),  $\alpha^*$  is dominated by the optimal symmetric pure strategy equilibrium  $\alpha^* = \alpha(p_H)$  for deterministic  $p_H$ ;
- 3) For  $\alpha^* = \alpha(p_H)$ , by PROPOSITION 1  $\alpha^*$  is dominated by  $\alpha^* = \alpha(p_L)$ ;
- 4) For  $\alpha^* \in (\alpha(p_L), 1]$  in which the banks survive at both states,  $\alpha^*$  is dominated by  $\alpha^* = \alpha(p_L)$  because  $\gamma[\alpha^* R_1 + (1 - \alpha^*) R_2] < \gamma[\alpha(p_L) R_1 + (1 - \alpha(p_L)) R_2]$ .

Now suppose that  $\pi = \delta > 0$  and the banks still stick to  $\alpha^* = \alpha(p_L)$ . Then when  $p_H$  realizes with probability  $\pi$ , all early entrepreneurs have excess liquidity supply

$$\underbrace{(1 - \gamma)[\alpha(p_L) R_1 + (1 - \alpha(p_L)) p_H R_2]}_{\text{entrepreneurs' rent from early projects}} - \underbrace{\gamma(1 - \alpha(p_L))(1 - p_H) R_2}_{\text{early entrepreneurs' deposit in } t=1} > (1 - \gamma)[\alpha(p_L) R_1 + (1 - \alpha(p_L)) p_L R_2] - \gamma(1 - \alpha(p_L))(1 - p_L) R_2 = 0.$$

Knowing this, one bank  $i$  can exploit this opportunity by setting  $\alpha_i < \alpha(p_L)$  because all its liquidity shortage can be fulfilled by early entrepreneurs' deposit given  $r^* = 1$ . In this case  $\alpha_i = 0$  maximizes its return at  $p_H$ , i.e.  $\kappa_i(0, \alpha_i(p_L)) = \gamma R_2 > \gamma \cdot E[R_L] = \kappa_i(\alpha_i(p_L))$ .

However any deviation  $\alpha_i < \alpha(p_L)$  makes bank  $i$  run at  $p_L$ . Since  $\alpha_i$  is observable by its depositors, its expected return for its investors is now

$$\gamma R_2 \pi + c(1 - \pi).$$

Such deviation is profitable only if its expected return is higher than its peers, i.e.

$$\gamma R_2 \pi + c(1 - \pi) > \gamma \cdot E[R_L] \Leftrightarrow \pi > \frac{\gamma \cdot E[R_L] - c}{\gamma R_2 - c}.$$

Otherwise all the banks would stick to  $\alpha^* = \alpha(p_L)$ .

*Q.E.D.*

**PROOF OF PROPOSITION 2:** The proposition is proved by construction.

**Claim 1:** When  $\frac{\gamma \cdot E[R_L] - c}{\gamma R_2 - c} < \pi < \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c}$ , there exists no optimal symmetric pure strategy equilibrium.

PROPOSITION 1 already shows that for  $\frac{\gamma \cdot E[R_L] - c}{\gamma R_2 - c} < \pi < \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c}$  there exists no optimal symmetric pure strategy equilibrium because profitable unilateral deviation is always possible.

**Claim 2:** If an equilibrium of mixed strategies exist, the equilibrium can only have a two-point support  $\{\alpha_r^*, \alpha_s^*\}$  such that one bank survives at both states by choosing  $\alpha_s^*$  and survives at only one state by choosing  $\alpha_r^*$ .

Suppose that  $\alpha_1$  and  $\alpha_2$  ( $\alpha_1 \neq \alpha_2$ ) are two arbitrary elements in the support of the mixed strategies equilibrium,  $r_H$  and  $r_L$  are the corresponding equilibrium interest rates at  $p_H$  and  $p_L$  respectively. One bank shall be indifferent between choosing  $\alpha_1$  and  $\alpha_2$ .

Suppose that one bank survives at both states by choosing either  $\alpha_1$  and  $\alpha_2$ . So its expected return should be the same for both strategies,

$$\gamma \left[ \alpha_1 R_1 + (1 - \alpha_1) p_H R_2 + \frac{(1 - \alpha_1)(1 - p_H) R_2}{r_H} \right] = \gamma \left[ \alpha_2 R_1 + (1 - \alpha_2) p_H R_2 + \frac{(1 - \alpha_2)(1 - p_H) R_2}{r_H} \right],$$

i.e.  $\alpha_1 = \alpha_2$ , a contradiction. Therefore there is at most one strategy by which one bank survives at both states.

Suppose that by choosing either  $\alpha_1$  and  $\alpha_2$  one bank survives at one state but is run in the other, so its expected return should be the same for both strategies:

$$\begin{aligned} & \gamma \left[ \alpha_1 R_1 + (1 - \alpha_1) p_H R_2 + \frac{(1 - \alpha_1)(1 - p_H) R_2}{r_H} \right] \pi + (1 - \pi) c \\ = & \gamma \left[ \alpha_2 R_1 + (1 - \alpha_2) p_H R_2 + \frac{(1 - \alpha_2)(1 - p_H) R_2}{r_H} \right] \pi + (1 - \pi) c, \end{aligned}$$

i.e.  $\alpha_1 = \alpha_2$ , a contradiction.

Suppose that by choosing  $\alpha_1$  one bank survives at  $p_H$  and is run at  $p_L$ , and by choosing  $\alpha_2$  one bank survives at  $p_L$  and is run at  $p_H$ . This implies that

$$\gamma \left[ \alpha_1 R_1 + (1 - \alpha_1) p_H R_2 + \frac{(1 - \alpha_1)(1 - p_H) R_2}{r_H} \right] > \gamma \left[ \alpha_1 R_1 + (1 - \alpha_1) p_L R_2 + \frac{(1 - \alpha_1)(1 - p_L) R_2}{r_L} \right],$$

i.e.  $p_H R_2 + \frac{(1 - p_H) R_2}{r_H} > p_L R_2 + \frac{(1 - p_L) R_2}{r_L}$ , as well as

$$\gamma \left[ \alpha_2 R_1 + (1 - \alpha_2) p_H R_2 + \frac{(1 - \alpha_2)(1 - p_H) R_2}{r_H} \right] < \gamma \left[ \alpha_2 R_1 + (1 - \alpha_2) p_L R_2 + \frac{(1 - \alpha_2)(1 - p_L) R_2}{r_L} \right],$$

i.e.  $p_H R_2 + \frac{(1-p_H)R_2}{r_H} < p_L R_2 + \frac{(1-p_L)R_2}{r_L}$ , a contradiction.

Therefore there is at most one strategy by which one bank survives at one state and is run at the other.

Therefore the equilibrium profile of mixed strategies is supported by  $\{\alpha_r^*, \alpha_s^*\}$  such that one bank survives at both states by choosing  $\alpha_s^*$  and survives at only one state by choosing  $\alpha_r^*$ .

**Claim 3:** *In such equilibrium, interest rates at states  $p_H$  and  $p_L$  are  $r_H > r_L > 1$ .*

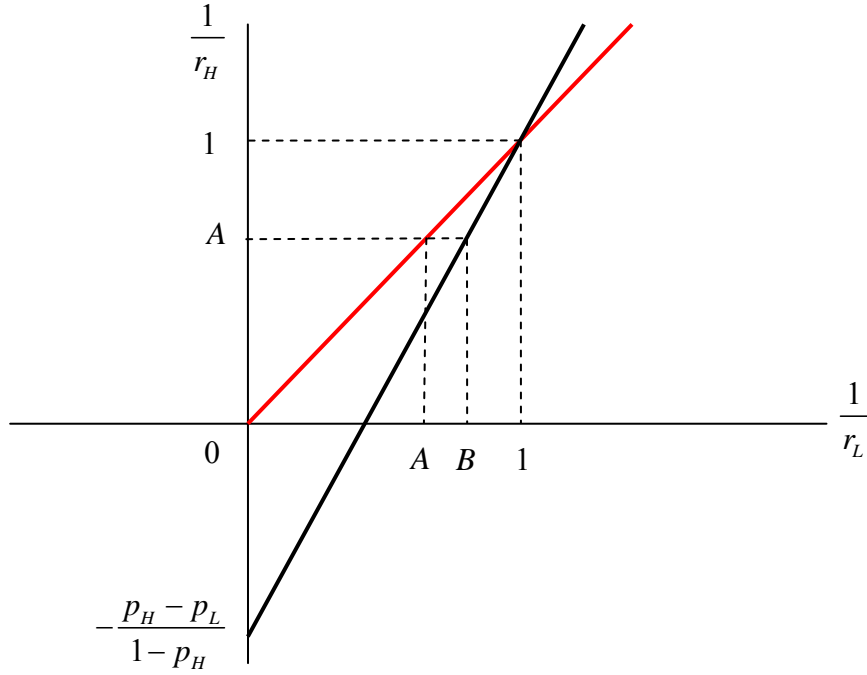
By choosing  $\alpha_s^*$  one bank should have equal return at both states:  $d_0^s = d_0^s(p_H) = d_0^s(p_L)$ , i.e.

$$\gamma \left[ \alpha_s^* R_1 + (1-\alpha_s^*) p_H R_2 + \frac{(1-\alpha_s^*)(1-p_H)R_2}{r_H} \right] = \gamma \left[ \alpha_s^* R_1 + (1-\alpha_s^*) p_L R_2 + \frac{(1-\alpha_s^*)(1-p_L)R_2}{r_L} \right].$$

With some simple algebra this is equivalent to

$$\frac{1}{r_H} = \frac{1-p_L}{1-p_H} \frac{1}{r_L} - \frac{p_H-p_L}{1-p_H}.$$

Plot  $\frac{1}{r_H}$  as a function of  $\frac{1}{r_L}$ :



The slope  $\frac{1-p_L}{1-p_H} > 1$  and intercept  $-\frac{p_H-p_L}{1-p_H} < 0$ , and the line goes through  $(1,1)$ . But

$r_H = r_L = 1$  cannot be equilibrium outcome here, because  $\alpha(p_L)$  is dominant strategy in this case and subject to deviation. So whenever  $r_H > 1$  (suppose  $\frac{1}{r_H} = A$  in the graph), there must

be  $r_H > r_L > 1$  (because  $\frac{1}{r_H} < \frac{1}{r_L} = B < 1$ ).

**Claim 4:** In such equilibrium, risky banks set  $\alpha_r^* = 0$  and safe banks  $\alpha_s^* > 0$ . Risky banks

promise  $d_0^r = \gamma \left[ p_H R_2 + \frac{(1-p_H)R_2}{r_H} \right]$  and are run at  $p_L$ ; safe banks survive at both states by

promising  $d_0^s = \gamma \left[ \alpha_s^* R_1 + (1-\alpha_s^*) p_k R_2 + \frac{(1-\alpha_s^*)(1-p_k)R_2}{r_k} \right]$  in which  $k \in \{H, L\}$ . Moreover,

$$\pi d_0^r + (1-\pi)c = d_0^s.$$

Since  $\frac{(1-\alpha_s^*)(1-p_H)R_2}{r_H} < \frac{(1-\alpha_s^*)(1-p_L)R_2}{r_L}$ , i.e. the safe banks get less liquidity from their

early entrepreneurs at  $p_H$ , and also these early entrepreneurs have higher liquidity supply at

$p_H$  (because  $(1-\gamma)[\alpha_s^* R_1 + (1-\alpha_s^*) p_H R_2] > (1-\gamma)[\alpha_s^* R_1 + (1-\alpha_s^*) p_L R_2]$ ), therefore there must be excess liquidity supply from these early entrepreneurs at  $p_H$ . This excess liquidity supply must be absorbed at  $r_H$  by the risky banks. As a result, the risky banks survive at  $p_H$  by free-riding excess liquidity supply and are run at  $p_L$ .

At  $r_H$  by setting  $\alpha_r^*$  the risky banks get a return of

$$d_0^r = \gamma \left[ \alpha_r^* R_1 + (1-\alpha_r^*) p_H R_2 + \frac{(1-\alpha_r^*)(1-p_H) R_2}{r_H} \right].$$

Since the banks are risk-neutral, the risky banks maximize the expression above by setting either  $\alpha_r^* = 0$  or  $\alpha_r^* = 1$  depending on all the other parameters.  $\alpha_r^* = 1$  is excluded because if so the banks become autarkic and survive at both states. Therefore for  $p_H R_2$  not too small and  $r_H$  not too big the risky banks maximize their return at  $r_H$  with  $\alpha_r^* = 0$ . This determines  $d_0^r$  in the claim.

Moreover the expected return should be equal for both types of banks,  $\pi d_0^r + (1-\pi)c = d_0^s$ , to deter the deviation between types.

**Claim 5:** *In such equilibrium, the strategy for the safe banks is given by  $\alpha_s^* = \alpha^*(p_L, r_L)$ , i.e.*

$$r_L (1-\gamma) [\alpha_s^* R_1 + (1-\alpha_s^*) p_L R_2] = \gamma (1-\alpha_s^*) (1-p_L) R_2.$$

Since the risky banks are run and safe banks survive at  $p_L$ , given  $r_L$  the safe banks maximize their return by setting  $\alpha_s^* = \alpha^*(p_L, r_L)$  by exhausting all liquidities provided by early entrepreneurs. By the proof of LEMMA 1 any unilateral deviation can only make lower return.

**Claim 6:** *There exists proper solution of  $\alpha_s^*$  for such equilibrium profile of mixed strategies.*

$$\text{By } d_0^r \pi + (1-\pi)c = d_0^s,$$

$$\gamma \left[ p_H R_2 + \frac{(1-p_H)R_2}{r_H} \right] \pi + (1-\pi)c = \gamma \left[ \alpha_s^* R_1 + (1-\alpha_s^*) p_H R_2 + \frac{(1-\alpha_s^*)(1-p_H)R_2}{r_H} \right] \dots (A).$$

By  $d_0^s = d_0^s(p_H) = d_0^s(p_L)$ ,

$$\gamma \left[ \alpha_s^* R_1 + (1-\alpha_s^*) p_H R_2 + \frac{(1-\alpha_s^*)(1-p_H)R_2}{r_H} \right] = \alpha_s^* R_1 + (1-\alpha_s^*) p_L R_2 \dots (B).$$

From (A) and (B), solve to get

$$\frac{\gamma(1-p_H)R_2}{r_H} = \frac{\alpha_s^* R_1 + (1-\alpha_s^*) p_L R_2 - (1-\pi)c - \pi\gamma p_H R_2}{\pi} \dots (C).$$

Apply (C) into (B), by some simple algebra we get a quadratic equation of  $\alpha_s^*$

$$(R_1 - p_L R_2) \alpha_s^{*2} - [\pi(\gamma R_1 - c) - (p_L R_2 - c) + (1-\pi)(R_1 - p_L R_2)] \alpha_s^* - (p_L R_2 - c)(1-\pi) = 0 \dots (D).$$

Define LHS of equation (D) as a function of  $\alpha_s^*$ :

$f(\alpha_s) = \omega \alpha_s^{*2} + \phi \alpha_s^* + \varphi$ , in which

$$\begin{cases} \omega = R_1 - p_L R_2 > 0, \\ \phi = -[\pi(\gamma R_1 - c) - (p_L R_2 - c) + (1-\pi)(R_1 - p_L R_2)], \\ \varphi = -(p_L R_2 - c)(1-\pi) < 0. \end{cases}$$

Since  $\phi^2 - 4\omega\varphi > 0$ , the quadratic equation has two real roots, denoted by  $\alpha_{s,2}^* < \alpha_{s,1}^*$ .

And by  $\frac{\varphi}{\omega} < 0$  and  $f(0) = \varphi < 0$ , we know  $\alpha_{s,2}^* \alpha_{s,1}^* < 0$ , i.e.  $\alpha_{s,2}^* < 0 < \alpha_{s,1}^*$ .

Moreover we find that

$$\begin{aligned} f(1) &= \omega + \phi + \varphi \\ &= R_1 - p_L R_2 - [\pi(\gamma R_1 - c) - (p_L R_2 - c) + (1-\pi)(R_1 - p_L R_2)] - (p_L R_2 - c)(1-\pi) \\ &= \pi(1-\gamma)R_1 \\ &> 0, \end{aligned}$$



we know that  $\alpha_{s,2}^* < 0 < \alpha_{s,1}^* < 1$ .

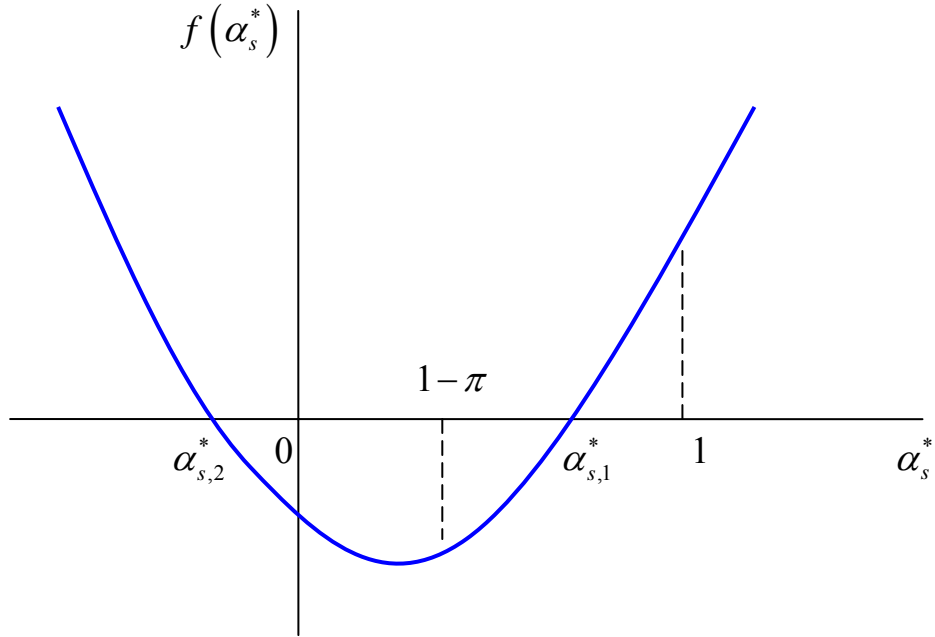
And again we can find that

$$\begin{aligned}
f(1-\pi) &= (R_1 - p_L R_2)(1-\pi)^2 - [\pi(\gamma R_1 - c) - (p_L R_2 - c) + (1-\pi)(R_1 - p_L R_2)](1-\pi) \\
&\quad - (p_L R_2 - c)(1-\pi) \\
&= [-\pi(\gamma R_1 - c) + (p_L R_2 - c)](1-\pi) - (p_L R_2 - c)(1-\pi) \\
&= -\pi(\gamma R_1 - c)(1-\pi) \\
&< 0,
\end{aligned}$$

we know that  $\alpha_{s,2}^* < 0 < 1-\pi < \alpha_{s,1}^* < 1$ .

This implies that in current settings, there always exists a plausible solution:  $\alpha_{s,1}^* \in (1-\pi, 1)$ .

All the arguments above can be captured by the following graph:



By equation (A)

$$\gamma \left[ p_H R_2 + \frac{(1-p_H)R_2}{r_H} \right] \pi + (1-\pi)c = \gamma \left[ \alpha_s^* R_1 + (1-\alpha_s) p_H R_2 + \frac{(1-\alpha_s^*)(1-p_H)R_2}{r_H} \right],$$

we already know that when  $\pi = \bar{\pi}_2$ ,  $\alpha_s^* = \alpha(p_L)$  and  $r_H = 1$ . When  $\pi = \bar{\pi}_2 + \delta$ ,  $\alpha_s \in (1 - \pi, 1)$ , then  $r_H$  has to be larger than 1 to make the equation still hold. From claim 3, this implies that  $r_H > r_L > 1$ .

**Claim 7:** *Given features described in previous claims, there exists no profitable unilateral deviation.*

Suppose that one bank  $i$  deviates by choosing  $\alpha_i \neq \alpha_s^*$  and  $\alpha_i \neq 0$ . Then by doing so there are three possible consequences:

- 1) The bank survives at both states. But by claim 5 its return at  $p_L$  must be lower than  $d_0^s$ . If it survives at both states, it cannot promise  $d_0^i \geq d_0^s$ . Given this, no investor would deposit at all;
- 2) It survives at  $p_H$  but is run at  $p_L$ . Since  $\alpha_i > 0$  by claim 4 its return at  $p_H$  must be lower than  $d_0^r$ ;
- 3) It survives at  $p_L$  but is run at  $p_H$ . By 1) its return is  $d_0^i < d_0^s$  at  $p_L$  and  $c$  at  $p_H$ . Its expected return is  $d_0^i \pi + (1 - \pi)c < d_0^s$ .

Therefore strategic profile  $\sigma_i$  cannot be a profitable unilateral deviation such that  $\sigma_i$  contains  $\alpha_i \neq \alpha_s^*$  and  $\alpha_i \neq 0$  with probability  $p \in (0, 1]$ .

And part 5) of the proposition is simply market clearing condition balancing aggregate liquidity supply and demand.

*Q.E.D.*

### **ADDENDUM TO PROPOSITION 3**

For those parameter values such that  $\pi p_H R_2 + (1 - \pi) p_L R_2 < 1$  there exists no equilibrium with liquidity injection. The reason is the following:

- (1) Any symmetric strategic profile cannot be equilibrium, because
  - a) If there is no trade under such strategic profile, i.e.  $\alpha$  is so small that the real return is less than 1, one bank can deviate by setting  $\alpha = 1$  and trading with investors;

b) If there is trade under such strategic profile, i.e.  $\alpha > 0$  for all the banks, then one bank can deviate by setting  $\alpha = 0$  and getting higher nominal return than the other banks.

(2) Any asymmetric strategic profile, or profile of mixed strategies, cannot be equilibrium, because

a) If there is no trade under such strategic profile, then the argument of 1 a) applies here;

b) If there is trade under such strategic profile, then one bank can deviate by choosing a pure strategy,  $\alpha = 0$ , and get better off – there is no reason to mix with the other dominated strategies.

## 2 A Numerical Example for the Equilibrium of Mixed Strategies

Suppose that  $p_H = 0.4$ ,  $p_L = 0.3$ ,  $\gamma = 0.6$ ,  $R_1 = 2$ ,  $R_2 = 4$ ,  $c = 0.8$ . Then

$$\alpha(p_H) = \frac{\gamma - p_H}{\gamma - p_H + (1 - \gamma)R_1 / R_2} = \frac{0.6 - 0.4}{0.6 - 0.4 + (1 - 0.6)0.5} = \frac{1}{2},$$

$$\alpha(p_L) = \frac{\gamma - p_L}{\gamma - p_L + (1 - \gamma)R_1 / R_2} = \frac{0.6 - 0.3}{0.6 - 0.3 + (1 - 0.6)0.5} = 0.6,$$

$$E[R_H] = \alpha(p_H)R_1 + (1 - \alpha(p_H))R_2 = \frac{1}{2} \times 2 + \frac{1}{2} \times 4 = 3,$$

$$E[R_L] = \alpha(p_L)R_1 + (1 - \alpha(p_L))R_2 = 0.6 \times 2 + 0.4 \times 4 = 2.8,$$

$$\bar{\pi}_2 = \frac{\gamma \cdot E[R_L] - c}{\gamma \cdot E[R_H] - c} = \frac{0.6 \times 2.8 - 0.8}{0.6 \times 3 - 0.8} = 0.88,$$

$$\bar{\pi}_1 = \frac{\gamma \cdot E[R_L] - c}{\gamma R_2 - c} = \frac{0.6 \times 2.8 - 0.8}{0.6 \times 4 - 0.8} = 0.55.$$

Take  $\pi = 0.7 \in (\bar{\pi}_1, \bar{\pi}_2)$  and by  $d_0^r \pi + (1 - \pi)c = d_0^s$

$$\gamma \left[ p_H R_2 + \frac{(1 - p_H)R_2}{r_H} \right] \pi + (1 - \pi)c = \gamma \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_H R_2 + \frac{(1 - \alpha_s^*)(1 - p_H)R_2}{r_H} \right],$$

$$0.6 \left[ 0.4 \times 4 + \frac{0.6 \times 4}{r_H} \right] \times 0.7 + 0.3 \times 0.8 = 0.6 \left[ \alpha_s^* \times 2 + (1 - \alpha_s^*) \times 0.4 \times 4 + \frac{(1 - \alpha_s^*) \times 0.6 \times 4}{r_H} \right] \dots (a).$$

By  $d_0^s = d_0^s(p_H) = d_0^s(p_L)$ ,

$$\gamma \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_H R_2 + \frac{(1 - \alpha_s^*)(1 - p_H) R_2}{r_H} \right] = \alpha_s^* R_1 + (1 - \alpha_s^*) p_L R_2,$$

$$0.6 \left[ \alpha_s^* \times 2 + (1 - \alpha_s^*) \times 0.4 \times 4 + \frac{(1 - \alpha_s^*) \times 0.6 \times 4}{r_H} \right] = \alpha_s^* \times 2 + (1 - \alpha_s^*) \times 0.3 \times 4 \dots (b).$$

Solve equations (a) and (b) to get  $\alpha_s^* = 0.47 < \alpha(p_H) < \alpha(p_L)$ ,  $r_H = 1.519$ .

And  $d_0^s = \alpha_s^* R_1 + (1 - \alpha_s^*) p_L R_2 = 1.576$ ,  $d_0^r = \frac{d_0^s - (1 - \pi)c}{\pi} = 1.908$ .

Market clearing at  $p_L$ :

$$r_L (1 - \gamma) \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_L R_2 \right] = \gamma (1 - \alpha_s^*) (1 - p_L) R_2,$$

$$r_L \times 0.4 \left[ 0.47 \times 2 + 0.53 \times 0.3 \times 4 \right] = 0.6 \times 0.53 \times 0.7 \times 4,$$

solve to get  $r_L = 1.414$ .

Market clearing at  $p_H$ :

$$D_r = d_0^r - \gamma p_H R_2 = 1.908 - 0.6 \times 0.4 \times 4 = 0.948,$$

$$D_s = d_0^s - \gamma \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_H R_2 \right] = 1.576 - 0.6 \left[ 0.47 \times 2 + 0.53 \times 0.4 \times 4 \right] = 0.503,$$

$$S_r = (1 - \gamma) p_H R_2 = 0.64,$$

$$S_s = (1 - \gamma) \left[ \alpha_s^* R_1 + (1 - \alpha_s^*) p_H R_2 \right] = (1 - 0.6) \left[ 0.47 \times 2 + 0.53 \times 0.4 \times 4 \right] = 0.715,$$

as well as

$$\theta D_r + (1 - \theta) D_s = \theta S_r + (1 - \theta) S_s,$$

solve to get  $\theta = 0.402$ .

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