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AFRIAT'S THEOREM FOR GENERAL BUDGET SETS

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Abstract

Afriat (1967) showed the equivalence of the strong axiom of revealed preference and the existence of a solution to a set of linear inequalities. From this solution he constructed a utility function rationalizing the choices of a competitive consumer. We extend Afriat's theorem to a class of nonlinear budget sets. We thereby obtain testable implications of rational behavior for a wide class of economic environments, and a constructive method to derive individual preferences from observed choices. In an application to market games, we identify a set of observable restrictions characterizing Nash equilibrium outcomes.

JEL Code: D11, D43, C72.

Keywords: GARP, rational choice, revealed preferences, market games, SARP, WARP.

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INTRODUCTION

Samuelson (1938) proposed the theory of revealed preference as a new, entirely behavioral foundation for the analysis of the competitive consumer. He opened a new field of investigation by asking which conditions the consumer's observed behavior should satisfy to be rationalized, i.e. interpreted as the outcome of the maximization of a preference relation. He also provided a first, partial answer in terms of the Weak Axiom of Revealed Preference, WARP. The theory was further developed by Houthakker (1950), who identified the Strong Axiom of Revealed Preference, SARP, as a necessary and sufficient condition for rationalization.

Richter (1966) observed that Samuelson's and Houthakker's ideas were relevant for any problem of choice, much beyond the case of a consumer choosing consumption bundles at given, fixed prices. He developed an abstract version of the theory, allowing for 'budget sets' which are just non empty subsets of a given universal set of possible choices. In his Theorem 1 he proved that (a suitably generalized version of) the SARP is necessary and sufficient for the existence of a rationalizing preference, even in this extremely general setting. The proof is non constructive, using Zorn's Lemma.

Almost at the same time, Afriat (1967) developed revealed preference theory in a completely different direction. In the original context of the competitive consumer, he emphasized the operational aspects of the theory. He took as data a finite number of observations, each one consisting of the chosen bundle of goods and the prevailing prices, and proved that, if these data satisfy the SARP, a rationalizing utility can explicitly be constructed by elementary linear programming techniques.

Afriat's method has subsequently been expanded and refined, notably by Diewert (1973), Varian (1982) and most recently Fostel, Scarf and Todd (2004). All these contributions deal with the case of linear, competitive budgets, and remain firmly in Afriat's constructive, finite observations setting.

Another important theoretical development, which can also be ascribed to the line of research initiated by Afriat, is the approximation theory of Mas Colell (1978). He asks whether increasing in a regular way the number of observations one can fully identify the underlying preference of the consumer. Again for the case of linear competitive budgets, Mas Colell identifies conditions for a positive answer.

Samuelson's original ideas have thus been pursued in two quite different directions: Richter's very general, non constructive existence results, and, for the special case of competitive linear budgets, Afriat's

constructive approach, supplemented by Mas Colell's analysis of uniqueness and approximation.

Our contribution in this paper is to identify a class of choice problems which is much more general than the competitive consumer's and still retains sufficient structure to allow us to recover the exact analog of Afriat's and Mas Colell's results. We develop each of these extensions in the next two sections of the paper.

Our choice space is the positive orthant of some euclidean space, and we allow as admissible budgets all subsets of the choice space that can be obtained as the comprehensive closure of a compact set. Every budget in this class admits a description by means of an increasing continuous function (Lemma 1), and this allows us to obtain the analog of the Afriat's inequalities (Proposition 1).

Our class of budgets includes those considered by Matzkin (1991) and Chavas and Cox (1993), the only two papers, to the best of our knowledge, providing constructive rationalizations for the case of possibly non linear budgets. In both papers, the authors impose convexity assumptions, and in Proposition 2 (and the discussion thereof) we illustrate how our approach improves on their results.

Propositions 3 and 4 in the second section, on identification and approximation, are the analog in our setting of Mas Colell's results.

Besides its theoretical interest, the extension of Afriat's theory to our class of budgets may be relevant for applications. As an illustration, in the last section of the paper we use it to derive a set of testable implications of Nash behavior for a broad class of market games (Proposition 5).

1. EXISTENCE OF A RATIONALIZATION

Consider an individual choosing consumption bundles in R_+^L . A consumption experiment is a finite collection $(x_k, B_k)_{k=1, \dots, n}$, where $x_k \in B_k$ and $B_k \subset R_+^L$. The interpretation is that x_k is the observed choice of the individual when she has access to the set of consumption bundles B_k . We consider sets of alternatives of the form $B_k = \{x \in R_+^L \mid g_k(x) \leq 0\}$ with $g_k : X \rightarrow R$ an increasing, continuous function and $g_k(x_k) = 0$, for all $k = 1, \dots, n$.

Let $B' \subset R^L$ be closed, compactly generated¹, comprehensive² and such that $0 \in \text{Int}(B')$. We will show that our admissible sets of alternatives include all the sets obtained as $B = B' \cap R_+^L$, where B' has the previous

¹ $\exists K \subset R^L$, compact, such that $x \in B'$ implies $\exists y \in K \cap B'$, $x \leq y$.

² $\forall y \in R^L$, if $\exists x \in B'$, $y \leq x$, then $y \in B'$.

properties. The upper boundary of B is $b(B) = \{x \in B \mid y \gg x \Rightarrow y \notin B\}$. For any $x \in R_+^L$, let $\gamma_B(x) = \inf\{\lambda > 0 \mid x \in \lambda B\}$. When B is a convex set, the function γ_B is known in convex analysis as the gauge of B (see e.g. Rockafellar (1972)). The following Lemma can be proved by standard arguments.

Lemma 1. *Let $B = B' \cap R_+^L$, with $B' \subset R_+^L$ closed, compactly generated, comprehensive and such that $0 \in \text{Int}(B')$.*

- (1) $\gamma_B : R_+^L \rightarrow R$ is homogeneous of degree one: for any $k > 0$, and $x \in R_+^L$, $\gamma_B(kx) = k\gamma_B(x)$
- (2) $\gamma_B : R_+^L \rightarrow R$ is a continuous function
- (3) $\gamma_B : R_+^L \rightarrow R$ is increasing: for any $x, y \in R_+^L$, $y \gg x$ implies $\gamma_B(y) > \gamma_B(x)$
- (4) $B = \{x \in R_+^L \mid \gamma_B(x) \leq 1\}$, and
- (5) $b(B) = \{x \in R_+^L \mid \gamma_B(x) = 1\}$

Letting $g(x) = \gamma_B(x) - 1$, $B = \{x \in R_+^L \mid g(x) \leq 0\}$.

1.1. Afriat's inequalities. Fix a consumption experiment $(x_k, B_k)_{k=1, \dots, n}$. We say that the function $v : X \rightarrow R$ rationalizes the experiment if, for all k , $g_k(x) \leq 0$ implies $v(x) \leq v(x_k)$. We say that x_k is revealed preferred to x_j , $x_k R x_j$, if $g_k(x_j) \leq g_k(x_k) = 0$. Let H be the transitive closure of the relation R . The standard competitive case corresponds to $g_k(x_j) = p_k(x_j - x_k)$, where p_k is the price vector. The following Axiom is a variation of the SARP introduced by Varian (1982), in the linear case, to deal with the possibility of indifference.

Definition (GARP): the experiment $(x_k, B_k)_{k=1, \dots, n}$ satisfies GARP if, for any k, j , $x_k H x_j$ implies $g_j(x_k) \geq 0$.

It is convenient to express GARP as a condition on the elements of a square matrix. To each consumption experiment $(x_k, B_k)_{k=1, \dots, n}$, we associate an $(n \times n)$ matrix A with elements $a_{kj} = g_k(x_j)$.

Definition (Cyclical Consistency): a square matrix A of dimension n is cyclically consistent if for every chain $\{k, j, l, \dots, m\} \subset \{1, \dots, n\}$, $a_{kj} \leq 0, a_{jl} \leq 0, \dots, a_{mk} \leq 0$ implies that all terms are zero.

An experiment satisfies GARP if and only if the associated matrix A is cyclically consistent. Suppose A is cyclically consistent, and let $x_k H x_m$. This means that there are indices $\{j, l, \dots, h\}$ such that $a_{kj} \leq 0, a_{jl} \leq 0, \dots, a_{hm} \leq 0$. If $g_m(x_k) < 0$, $\{k, j, l, \dots, h, m\}$ would be a chain satisfying the premise in the definition of cyclical consistency. But then $a_{mk} = g_m(x_k) = 0$ would lead to a contradiction. Thus we must have $g_m(x_k) \geq 0$, i.e. GARP holds. In the other direction, let the experiment satisfy GARP, construct the associated matrix A and take a chain $\{k, j, l, \dots, h, m\}$ satisfying the premise of the definition of cyclical

consistency. For any two adjacent elements in the chain, say (j, l) , by going through the chain we have $x_l H x_j$. Applying GARP, it must be that $g_j(x_l) = a_{jl} \geq 0$, so that $a_{jl} = 0$. This is true for any couple of adjacent elements in the chain, i.e. Cyclical Consistency holds.

Lemma 2. *If a square matrix A of dimension n is cyclically consistent, there exist numbers $(v_k, \lambda_k)_{k=1, \dots, n}$, $\lambda_k > 0$, such that, for all $k, j = 1, \dots, n$,*

$$v_j \leq v_k + \lambda_k a_{kj}$$

Proof: See Fostel, Scarf and Todd (2004), sections 2 and 3. \square

We are now able to state our generalization of Afriat's Theorem.

Proposition 1. *Let $B_k = \{x \in R_+^L \mid g_k(x) \leq 0\}$ with $g_k : R_+^L \rightarrow R$ an increasing, continuous function and $g_k(x_k) = 0$, for $k = 1, \dots, n$. The following conditions are equivalent:*

- (1) *there exists a locally non satiated, continuous utility function v rationalizing the experiment $(x_k, B_k)_{k=1, \dots, n}$*
- (2) *the experiment $(x_k, B_k)_{k=1, \dots, n}$ satisfies GARP*
- (3) *there exist numbers $(v_k, \lambda_k)_{k=1, \dots, n}$, $\lambda_k > 0$, such that, for all $k, j = 1, \dots, n$,*

$$v_j \leq v_k + \lambda_k g_k(x_j)$$

Proof:

(1) \rightarrow (2): Let $x_k H x_j$: there exist indices (g, \dots, m) such that $x_k R x_g R \dots R x_m R x_j$. We want to show that $g_j(x_k) \geq 0$. Using the definition of R , $g_k(x_g) \leq 0, \dots, g_m(x_j) \leq 0$. If v rationalizes the experiment, we must have $v(x_k) \geq v(x_g) \geq \dots v(x_m) \geq v(x_j)$, implying $v(x_k) \geq v(x_j)$. If $g_j(x_k) < 0$, by the local non satiation of v and the continuity of g_j we could find $x \in X$ such that $g_j(x) < 0$ and $v(x) > v(x_k) \geq v(x_j)$, contradicting the fact that v rationalizes the experiment.

(2) \rightarrow (3): construct the matrix A associated with the experiment. By (2), A is cyclically consistent. Then use Lemma 2.

(3) \rightarrow (1): Let $v(x) = \min_k \{v_k + \lambda_k g_k(x)\}$. The function v is increasing and continuous on R_+^L . To show that it rationalizes the data, notice first that, for all j , $v(x_j) = \min_k \{v_k + \lambda_k g_k(x_j)\} = v_j$, using the Afriat's inequalities in (3) and the fact that $g_j(x_j) = 0$. Then, if we consider x such that $g_j(x) \leq 0$ we have $v(x) \leq v_j + \lambda_j g_j(x) \leq v_j = v(x_j)$. \square

In the competitive setting originally considered by Afriat, the inequalities in (3) take the form:

$$v_j \leq v_k + \lambda_k p_k(x_j - x_k)$$

This corresponds to choosing $a_{kj} = p_k(x_j - x_k)$ in Lemma 2, as explicitly done in Fostel et al. (2004). As it is clear from the discussion preceding Lemma 2, if the experiment satisfies GARP, the existence of the numbers $(v_k, \lambda_k)_{k=1, \dots, n}$ follows for *any* matrix A having the property that $a_{kj} \leq 0$ if x_k is revealed preferred to x_j . Our contribution is to notice that, in the general setting that we consider, one can choose $a_{kj} = g_k(x_j)$, and still obtain, in the last step of the proof, an explicit utility function defined on the entire consumption set.

1.2. Testing concavity. Consider now consumption experiments in which $B_k = \{x \in R_+^L \mid f_k(x) \leq 0\}$ with $f_k(x_k) = 0$ where $f_k : R_+^L \rightarrow R$ is not only increasing and continuous, but also quasi - convex and differentiable at x_k , for all $k = 1, \dots, n$. In this case, the gradient $\nabla f_k(x_k)$ identifies the unique supporting hyperplane of B_k at x_k .

For each (x_k, B_k) , let $C_k = \{x \in R_+^L \mid \nabla f_k(x_k)(x - x_k) \leq 0\}$. If we let $g_k(x) = \nabla f_k(x_k)(x - x_k)$, we can apply our definitions of R , H and GARP to the 'linearized' experiment $(x_k, C_k)_{k=1, \dots, n}$.

Proposition 2. *Let $B_k = \{x \in R_+^L \mid f_k(x) \leq 0\}$ with $f_k(x_k) = 0$ where $f_k : R_+^L \rightarrow R$ is increasing, continuous, quasi - convex and differentiable at x_k , for $k = 1, \dots, n$. The following conditions are equivalent:*

- 1') *there exists a locally non satiated, continuous and concave utility function v rationalizing the experiment $(x_k, B_k)_{k=1, \dots, n}$*
- 2') *the 'linearized' experiment $(x_k, C_k)_{k=1, \dots, n}$ associated with $(x_k, B_k)_{k=1, \dots, n}$ satisfies GARP*
- 3') *there exist positive numbers $(v_k, \lambda_k)_{k=1, \dots, n}$, $\lambda_k > 0$, such that, for all $k, j = 1, \dots, n$,*

$$v_j \leq v_k + \lambda_k \nabla f_k(x_k)(x_j - x_k)$$

Proof:

(1') \rightarrow (2'): Define R and H in terms of the linearized experiment $(x_k, C_k)_{k=1, \dots, n}$. Let $x_k H x_j$: there exists indices (g, \dots, m) such that $x_k R x_g R \dots R x_m R x_j$. From the definition of R , $\nabla f_k(x_k)(x_g - x_k) \leq 0, \dots, \nabla f_m(x_m)(x_j - x_m) \leq 0$.

If $v : R_+^L \rightarrow R$ is a locally non satiated, continuous, concave utility function rationalizing the (non linearized) experiment $(x_k, B_k)_{k=1, \dots, n}$,

each observation x_k is a maximizer of v on the convex set $B_k = \{x \in R_+^L \mid f_k(x) \leq 0\}$ and we have:

$$v(x) \leq v(x_k) + \alpha_k \nabla f_k(x_k)(x - x_k)$$

with $\alpha_k > 0$ (using local non satiation). If $x_k H x_j$ we then have $v(x_k) \geq v(x_j)$, and thus $v(x_k) \geq v(x_j)$. We need to show that $\nabla f_j(x_j)(x_k - x_j) \geq 0$. If this was not the case, by local non satiation we could find x such that $\nabla f_j(x_j)(x - x_j) < 0$ and $v(x) > v(x_j)$, contradicting the fact that v is a concave function rationalizing the experiment.

(2') \rightarrow (3'): construct the matrix A associated with the linearized experiment $(x_k, C_k)_{k=1, \dots, n}$. By (2'), A is cyclically consistent. Then use Lemma 2.

(3') \rightarrow (1'): Let $v(x) = \min_k \{v_k + \lambda_k \nabla f_k(x_k)(x - x_k)\}$. The function v is increasing and continuous on R_+^L . It is also concave, as the minimum of finitely many linear functions. To show that it rationalizes the data, notice first that, for all j , $v(x_j) = v_j$, using the Afriat's inequalities in (3'). Then, if we consider x such that $f_j(x) \leq 0$ we have $v(x) \leq v_j + \lambda_j \nabla f_j(x_j)(x - x_j) \leq v_j = v(x_j)$, where the first inequality follows from the definition of v , the second from the quasi - convexity of f_j , $f_j(x) \leq 0$ and the fact that, in the experiment, $f_j(x_j) = 0$. \square

If the experiment satisfies the premise of Proposition 2, we may consider two sets of testable conditions: those in 2'), and the 'non-linearized' ones, 2). If the experiment satisfies 2) but not 2') a rationalization is possible, but preferences cannot be represented by a concave utility function.

1.3. Comparison with previous results. Matzkin (1991) explicitly deals with nonlinear choice sets. She proves that the existence of a strictly concave rationalization is equivalent to the strong axiom of revealed preference when every choice (x, B) is either co-convex (i.e., B as in Lemma 1 and $B^c \cap R_+^L$ convex) or supportable (i.e., B as in Lemma 1, convex and supported by a unique hyperplane at x). Our main result, Proposition 1, does not require any additional assumption besides those in Lemma 1. On the other hand, the utility function that we construct from Afriat's inequalities need not be concave.

The first two statements of Proposition 2 above are similar to Matzkin's Theorem 2. Our approach, which exploits the representation of budget sets by means of the g functions, allows us to derive an exact analog of Afriat's inequalities, leading to a much easier construction of the concave utility function rationalizing the data.

To complete the comparison, in the co-convex case our construction immediately yields a concave rationalization of the data. If B is co-convex, the function $\gamma_B : R_+^L \rightarrow R$ is concave. Then, if we let $g(x) = \gamma_B(x) - 1$ for all $x \in R_+^L$, the rationalization obtained in (3) of Proposition 1 is concave as a minimum of concave functions. This is essentially Matzkin's Theorem 1.

Independently of Matzkin (1991), Chavas and Cox (1993) allow the consumer to face finitely many nonlinear budget constraints. They impose restrictions in order to convert the consumer's underlying optimization problem into a saddle-point problem. They do not formulate any axiom of revealed preference but express necessary and sufficient conditions for rationalization as explicit generalized Afriat's inequalities. Our Proposition 1 is more general: the budget sets considered above can clearly accommodate multiple constraints, but our result does not require any convexity assumption, like Chavas and Cox (1993)'s assumption 2. At the same time our proof is much more direct.

2. UNIQUENESS AND APPROXIMATION

In the theory of revealed preferences, besides the question of the existence of a rationalization, it is interesting to investigate the issue of uniqueness: can we fully identify the preferences of an individual by observing his behavior? The question has to be made precise. We cannot hope to identify preferences over a non finite choice set from observation of finitely many choices. Also, if we allow the individual to be indifferent among elements of a given set of alternatives, we must be able to observe *all* of his preferred choices at that set of alternative, not just one. The spirit of the exercise is thus quite different from the 'finite observation' methodology we followed until now. Nevertheless the question has been investigated for the case of the classical competitive consumer, facing linear budgets (see Mas Colell (1977), (1978)), and, not surprisingly, in our much larger class of possible budgets, things are simpler. In this section, we take the strictly positive orthant $X = R_{++}^L$ as our consumption set.

The main idea is that if we restrict attention to monotonic preferences, we can always simulate a choice between any pair of alternatives $y, z \in X$ by proposing to the individual the budget

$$B_{y,z} = \{x \in X \mid x \leq y\} \cup \{x \in X \mid x \leq z\}$$

To state the observation more precisely, let \mathbb{B} be the set of *all* budgets obtained as the intersection $B' \cap X$ with $B' \subset R^L$ closed, compactly generated, comprehensive and such that $0 \in \text{Int}(B')$. Let $h : \mathbb{B} \rightarrow X$ be the individual choice correspondence, with $h(B) \subset B$, $h(B) \neq \emptyset$ for all $B \in \mathbb{B}$.

For a given individual choice correspondence h , we say that x is revealed preferred to y , and we write $xR(h)y$, iff there exists $B \in \mathbb{B}$ such that $x, y \in B$ and $x \in h(B)$. We may also define the relation $P(h)$ as $xP(h)y$ iff there exists $B \in \mathbb{B}$ such that $x, y \in B$, $x \in h(B)$, $y \notin h(B)$. The weak axiom of revealed preference can then be stated as follows

Definition (WARP): the individual choice correspondence satisfies WARP if $[xR(h)y] \implies [\neg yP(h)x]$.

We also introduce an additional condition which is natural, given our restriction to monotonic preferences

Definition (Monotonic choice): the individual choice correspondence is monotonic if, for all $B \in \mathbb{B}$, $[x \in h(B), y \succ x] \implies [y \notin B]$.

A preference relation \succsim is a reflexive, complete, transitive binary relation on X . \succsim is monotonic if $x \succ y$ implies $x \succ z$, i.e. $x \succ y$ and $\neg y \succ z$. \succsim is upper semicontinuous if $\forall x \in X$ the set $\succsim(x) = \{y \in X \mid y \succsim x\}$ is closed in X . We say that a preference relation \succsim generates the individual choice correspondence h on \mathbb{B} if, for all $B \in \mathbb{B}$, $h(B) = \{x \in B \mid [y \in B] \implies x \succsim y\}$. This is stronger than simply requiring that \succsim rationalizes h , which corresponds to the inclusion \subset .

The following Proposition should be compared with Theorem 2' of Mas-Colell (1977). In our setting, given the large class of admissible budget sets, both the statement and the proof are simpler. Our result is actually closer to Arrow (1959), which requires that the class of admissible budgets contains all finite sets of up to three alternatives.

Proposition 3. *If the individual choice correspondence h is monotonic and satisfies WARP, $R(h)$ is the unique preference which generates it.*

Proof:

$R(h)$ is complete because for any $y, z \in X$, $B_{y,z} \in \mathbb{B}$.

To show that $R(h)$ is transitive, let $xR(h)y$, $yR(h)z$, i.e., there exists $B \in \mathbb{B}$ such that $x, y \in B$ and $x \in h(B)$, and $B' \in \mathbb{B}$ such that $y, z \in B'$ and $y \in h(B')$. Take now $B_{x,y,z} \in \mathbb{B}$, defined in the obvious way. We have to show that $x \in h(B_{x,y,z})$. Because h is monotonic, at least one of the three elements x, y, z must belong to $h(B_{x,y,z})$. If it is x , we are done. If on the other hand $y \in h(B_{x,y,z})$, then by WARP we should also have $x \in h(B_{x,y,z})$, and similarly if $z \in h(B_{x,y,z})$.

$R(h)$ generates h on \mathbb{B} . We have to show that for all $B \in \mathbb{B}$, $h(B) = \{x \in B \mid [y \in B] \implies xR(h)y\}$. Let x be an element of the set on the right hand side. If $x \notin h(B)$, then there exists $y \in B$, $x \neq y$, $y \in h(B)$, i.e. $yP(h)x$, contradicting WARP. In the other direction, take $x \in h(B)$. If $y \in B$, then by definition of $R(h)$ $xR(h)y$, i.e. x belongs to the right hand side.

To show uniqueness, assume there exists \succsim generating h , i.e. for any $B \in \mathbb{B}$ $h(B) = \{x \in B \mid [y \in B] \implies x \succsim y\}$. Clearly, for any couple of bundles (z, z') , if $zR(h)z'$ then $z \succsim z'$. In the other direction, if $z \succ z'$, by monotonicity it must be that $z \in \{x \in B_{z,z'} \mid [y \in B_{z,z'}] \implies x \succ y\} = h(B_{z,z'})$, implying $zR(h)z'$. \square

The uniqueness result in this proposition depends on the fact that we know the full choice correspondence: in the very last step of the proof we used the inclusion $\{x \in B_{z,z'} \mid [y \in B_{z,z'}] \implies x \succ y\} \subset h(B_{z,z'})$. It would not be enough to require that the observed choice $h(B_{z,z'})$ be an element of the set of preferred bundles. Indeed, an individual indifferent between z and z' could always choose z' when confronted with $B_{z,z'}$ and there would be no hope to fully identify her preferences.

Even under this stronger requirement, it is interesting to investigate to what extent one can reconcile this approach with the one of the previous section, in which only finitely many budgets are included in each experiment. This is the question of approximation, first raised, for the case of the competitive consumer, by Mas-Colell (1978).

Following his approach, we consider a sequence of finite experiments which becomes richer and richer at every step, and which 'tends' to the whole of \mathbb{B} . Let $\mathcal{K}(X)$ be the set of all non empty compact subsets of X . Endowed with the Hausdorff metric, $\mathcal{K}(X)$ is a separable metric space (See e.g. Aliprantis and Border (2000) chapter 3 for definitions and results, especially 3.76 and 3.77, p. 115). $\mathbb{B} \subset \mathcal{K}(X)$ inherits these properties. Let C_n be a collection of n elements of \mathbb{B} , and consider an increasing sequence of collection of sets $C_1 \subset C_2 \subset \dots \subset C_{n-1} \subset C_n \dots$ such that their union is dense in \mathbb{B} : $\overline{\cup_n C_n} = \mathbb{B}$. For each collection C_n , let \mathcal{R}_n be the set of upper semicontinuous, monotonic preferences which generate h on C_n . We obtain a decreasing sequence $\dots, \mathcal{R}_n \supset \mathcal{R}_{n+1}, \dots$

Proposition 4. *If the individual choice correspondence $h : \mathbb{B} \rightarrow X$ has closed values, is monotonic and upper hemi-continuous, and satisfies WARP, then $\cap_n \mathcal{R}_n = \{R(h)\}$.*

Proof:

We first show that $R(h) \in \cap_n \mathcal{R}_n$.

As shown in the proof of Proposition 3, $R(h)$ generates h on \mathbb{B} . $R(h)$ is monotonic. Let $z \gg y$. We have to show that $zR(h)y$ and $\neg yR(h)z$. Take $B_z = \{x \in X \mid x \leq z\}$. Clearly, $y, z \in B_z$. If $z \notin h(B_z)$, $\exists x \leq z$ $x \in h(B_z)$, contradicting the monotonicity of h ; thus $z \in h(B_z)$ and $zR(h)y$. If we also had $yR(h)z$, we would have that for all B with $(z, y) \in B$, if $z \in h(B)$ then $y \in h(B)$. Again, for $B = B_z$ this would contradict the monotonicity of h .

$R(h)$ is upper semicontinuous. We have to show that, $\forall x \in X$, the set $R(h)(x) = \{y \in X \mid yR(h)x\}$ is closed. Take a sequence $(y_n)_{n \geq 1}$ converging to y , such that $\forall n \ y_n R(h)x$. That is, $\forall n \ \exists B_n \in \mathbb{B}$ such that $y_n, x \in B_n$ and $y_n \in h(B_n)$. If we consider $B_{y_n, x}$, by monotonicity of h and WARP $y_n \in h(B_{y_n, x})$, $\forall n$. The sequence of sets $(B_{y_n, x})_{n \geq 1}$ converges in the Hausdorff metric to $B_{y, x}$, and, by u.h.c. of h , $y \in h(B_{y, x})$.

It remains to show that there is no other element in $\bigcap_n \mathcal{R}_n$.

Suppose there exists $\succ \in \bigcap_n \mathcal{R}_n$, $\succ \neq R(h)$. Then we can find $x, y \in X$ such that $x \succ y$ and $x \in R(h)(y)^c$. By u.s.c. of $R(h)$, $R(h)(y)^c$ is an open set. By monotonicity of \succ , we can take $x, y \in X$ such that $x \succ y$ and $x \in R(h)(y)^c$.

Using again the u.s.c. and monotonicity of both \succ and $R(h)$ we can actually claim more. There exists $\eta > 0$ such that, if we define

$$x_\alpha = x + (1 - \alpha)\eta \mathbf{1}$$

$$y_\beta = y + (1 - \beta)\eta \mathbf{1}$$

then, for all $\alpha \in [0, 1]$ and all $\beta \in [0, 1]$,

$$y_\beta \not\prec (x_\alpha)$$

$$x_\alpha \notin R(h)(y_\beta).$$

Fix now $\alpha = \beta = \frac{1}{2}$. To simplify notation, let us denote the ‘corner’ budget $B_{x_{\frac{1}{2}}, y_{\frac{1}{2}}}$ simply by \hat{B} . For any $\epsilon > 0$, consider the open set around \hat{B} defined by

$$\mathcal{O}^\epsilon = \{F \in \mathbb{B} \mid \mathcal{H}(F, \hat{B}) < \epsilon\}$$

where \mathcal{H} is the Hausdorff distance. We claim that, for any $\epsilon < \frac{\eta}{3}$, if $F \in \mathcal{O}^\epsilon$, then $x \in F$ and $y \in F$. Indeed, if e.g. x did not belong to F , then, by comprehensiveness of F , none of the points $y \geq x$ would be in F . But the closest point z to $x_{\frac{1}{2}}$ for which it is not the case that $z \geq x$ is at distance at least $\frac{\eta}{2}$ from $x_{\frac{1}{2}}$. Clearly, $\epsilon < \frac{\eta}{3} < \frac{\eta}{2}$ and the argument above contradicts the fact that $F \in \mathcal{O}^\epsilon$.

Observe now that, again for $\epsilon < \frac{\eta}{3}$, by a similar argument, if $F \in \mathcal{O}^\epsilon$, then $F \subset B_{x_0, y_0}$. Then, by monotonicity of $R(h)$, if $b \in F$ then either $x_0 R(h)b$ or $y_0 R(h)b$. If $x_0 R(h)b$, then it cannot be that $b R(h)y$, because this would imply $x_0 R(h)y$, which is false by construction. Remember that $y \in F$, so that, if we define $V = [R(h)(y) \cap B_{y_0}]$, we must have $h(F) \subset V$.

Using now the fact that $\bigcup_n C_n$ is dense in \mathbb{B} , there exist n and $B \in C_n$ such that $B \in \mathcal{O}^\epsilon$. Then, by our argument above we can find $b \in h(B) \subset V$. From the fact that $x \in B$, and that \succ generates

h on C_n , this implies $b \succcurlyeq x$. Finally, from $b \in V$, $y_0 \geq b$, and by monotonicity and u.s.c. of \succcurlyeq , $y_0 \succcurlyeq b$. We therefore obtain $y_0 \succcurlyeq x$, a contradiction. \square

3. APPLICATION: MARKET GAMES

Given a standard exchange economy, a market mechanism consists of a set of strategies (bids, offers, etc.) for every agent and an outcome function that maps strategy profiles into allocations of commodities. Fixing the strategies of the others, each player generates a set of consumption bundles as she varies her strategy. The individual problem can thus be expressed as the maximization of the player's preferences over a 'budget set'. Typically, the strategy chosen by a player has some influence on the 'terms of trade', and we should not expect the frontier of the budget set to be linear. Strategic market interactions are thus a natural setting for the application of our generalization of Afriat's theory. We show that, for a broad class of market mechanisms axiomatized by Dubey and Sahi (2003), individual 'budget sets' are exactly of the form covered by our Lemma 1. As an immediate corollary of Proposition 1 we obtain a set of testable restrictions which are necessary and sufficient to interpret the observed choices as Nash equilibrium outcomes.

Consider an economy composed by a finite group of individuals $i \in \{1, \dots, I\}$. Commodities are $l \in \{1, \dots, L\}$. The initial endowment of commodities of individual i is $e^i \in R_{++}^L$, and we denote her final consumption by $x^i \in R_+^L$. Traders bring goods to the market, and the market generates a vector of prices and an allocation of goods. Each good may be brought to one or more markets, and an action for an individual is a vector $a^i \in R_+^S$. For example if there are two commodities and each can be brought to two markets, $S = 4$. We can obtain the total amount of the L commodities needed to carry out action a^i by means of a 'summing-up' matrix M of dimension $L \times S$: $Ma^i \in R_+^L$. The market mechanism specifies a price vector $p \in P = R_{++}^L$ and an allocation $(x^i \in R_+^L)_{i \in I}$ as a result of the individual actions. We do not require the mechanism to be defined if the total quantity of any good brought to any market is zero. Let $\mathbb{A} = \{a \in R_+^{SI} \mid \sum_i a^i \gg 0\}$. A market mechanism is then a collection of functions $p : \mathbb{A} \rightarrow P$, $r^i : \mathbb{A} \rightarrow R_+^L$ such that

$$\textit{Exact Feasibility:} \text{ For all } a \in \mathbb{A}, \sum_i r^i(a) = \sum_i Ma^i$$

$$\textit{Budget Balance:} \text{ For all } a \in \mathbb{A}, \text{ and all } i \in I, p(a)r^i(a) = p(a)Ma^i$$

Dubey and Sahi show that if a mechanism satisfies natural properties of Aggregation, Invariance and Price Mediation, one can equivalently represent it by means of price and allocation functions, $p : R_{++}^S \rightarrow P$ and $z : R_+^S \times P \rightarrow R_+^L$. Prices only depend on the aggregate quantity $\bar{a} = \sum_i a^i$, and $r^i(a) = z(a^i, p(\bar{a}))$.

The mechanism, as defined by the two functions (p, z) , is anonymous: the action set is the same for all individuals, R_+^S . When applying a mechanism to a particular economy, we may impose individual feasibility: the total quantity of a commodity delivered by an individual cannot exceed her initial endowment. The action set of individual i is then $A^i = \{a^i \in R_+^S \mid Ma^i \leq e^i\}$. From now on, let us then define a mechanism for our economy as $\Gamma = \{(A^i)_{i \in I}, (p, z)\}$. The subset of individually feasible actions over which the maps (p, z) are defined is $A = \{a \in \times_i A^i \mid \sum_i a^i \gg 0\}$. At a profile of choices $a \in A$, the final bundle obtained by individual i is $x^i(a^i, a^{-i}) = e^i - Ma^i + z(a^i, p(a^i + \sum_{j \neq i} a^j))$. For given choices of the other individuals with $\sum_{j \neq i} a^j \gg 0$, the set of attainable consumption bundles of individual i is:

$$B^i(a^{-i}) = \{x^i \in R_+^L \mid \exists a^i \in A^i \text{ s.t. } x^i \leq x^i(a^i, a^{-i})\}$$

By feasibility, the set $B^i(a^{-i})$ is bounded. By budget balance, the fact that prices are strictly positive, and that $e^i \gg 0$, it contains 0 in its interior. If the function $x^i(\cdot, a^{-i}) : A^i \rightarrow R_+^L$ is continuous, the set is closed. As in Lemma 1 one could define continuous increasing functions $g^i(\cdot; a^{-i}) : R_+^L \rightarrow R$ such that

$$B^i(a^{-i}) = \{x^i \in R_+^L \mid g^i(x^i; a^{-i}) \leq 0\}$$

A market mechanism $\Gamma = \{I, (A^i)_{i \in I}, (p, z)\}$, and a collection of utility functions, $v^i : R_+^L \rightarrow R$, $i \in I$ define a market game $\{I, (v^i)_{i \in I}, \Gamma\}$ in which the strategy set of individual i is A^i , and her utility³ at the profile $a \in \times_i A^i$ is $v^i[x^i(a^i, a^{-i})]$. An active profile of strategies is $a \in \times_i A^i$ with $\sum_{j \neq i} a^j \gg 0$ for all $i \in I$. An active Nash equilibrium of $\{I, (v^i)_{i \in I}, \Gamma\}$ is an active profile such that, for all $i \in I$, and for all $b \in A^i$,

$$v^i[x^i(b, a^{-i})] \leq v^i[x^i(a^i, a^{-i})]$$

Equivalently, it is an active profile of strategies $a \in \times_i A^i$ such that, for all $i \in I$, and for all $x^i \in B^i(a^{-i})$, $v^i[x^i] \leq v^i[x^i(a)]$.

³To define utilities for the market game, we need to extend the market mechanism to the whole of $\times_i A^i$. This has been done in the literature for different subclasses of mechanisms, at the cost of introducing discontinuities (see e.g. Shapley (1976)). In our setting, we can always avoid the discontinuity by retaining only the observations corresponding to active profiles, as done here.

3.1. Rationalization. An experiment is a collection of observations of strategies chosen by a fixed set of individuals. We allow the observations to come from different market mechanisms. An experiment is thus a collection $(a_k, \Gamma_k)_{k=1, \dots, n}$ where all the market mechanisms have the same set of individuals I and, for each k , $a_k \in A_k$ is an active profile.

We say that the collection of utility functions $(v^i : R_+^L \rightarrow R)_{i \in I}$ rationalizes the experiment $(a_k, \Gamma_k)_{k=1, \dots, n}$ if, for all k , a_k is a Nash equilibrium of the market game $\{I, (v^i)_{i \in I}, \Gamma_k\}$.

Given an experiment $(a_k, \Gamma_k)_{k=1, \dots, n}$, we can construct data on the trades of individuals and on their budget sets:

$$\begin{aligned} x_k^i &= e_k^i - M_k a_k^i + z_k(a_k^i, p_k(\bar{a}_k)) \\ B_k^i &= \{x^i \in R_+^L \mid \exists a^i \in A_k^i \text{ s.t. } x^i \leq e_k^i - M_k a_k^i + z_k(a^i, p_k(a^i + \sum_{j \neq i} a_k^j))\} \\ &= \{x^i \in R^L \mid g_k^i(x^i) \leq 0\}. \end{aligned}$$

The expression of B_k^i in terms of the function g_k^i introduces an element of arbitrariness, but the set B_k^i is fully determined by observable entities.

With this notation, a_k is a Nash equilibrium of the market game $\{I, (v^i)_{i \in I}, \Gamma_k\}$ if and only if for each individual $i \in I$, $x \in B_k^i$ implies $v^i[x] \leq v_i[x_k^i]$.

For a given experiment $(a_k, \Gamma_k)_{k=1, \dots, n}$, we say that x_k^i is revealed preferred by i to x_j^i , $x_k^i R^i x_j^i$, if $g_k^i(x_j^i) \leq g_k^i(x_k^i) = 0$. Let H^i be the transitive closure of the relation R^i .

The experiment $(a_k, \Gamma_k)_{k=1, \dots, n}$ satisfies GARP if, for all $i \in I$, and any k, j , $x_k^i H^i x_j^i$ implies $g_j^i(x_k^i) \geq 0$.

Proposition 5. *The following conditions are equivalent:*

- (1) *there exists a collection of locally non satiated, continuous utility functions $(v^i)_{i \in I}$ rationalizing the experiment $(a_k, \Gamma_k)_{k=1, \dots, n}$*
- (2) *the experiment $(a_k, \Gamma_k)_{k=1, \dots, n}$ satisfies GARP*
- (3) *there exist numbers $((v_k^i, \lambda_k^i)_{k=1, \dots, n})_{i \in I}$, $\lambda_k^i > 0$, such that, for all $i \in I$ and all $k, j = 1, \dots, n$,*

$$v_j^i \leq v_k^i + \lambda_k^i g_k^i(x_j^i)$$

This characterization obviously relies on the availability of individual consumption data (as opposed to aggregate ones). On the other hand, we just require the observation of the *effective* choices of the players as the rules of the game and/or the initial endowments vary. Our result thus differs significantly from those obtained by Sprumont

(2000) for abstract interactive decision problems, which require the observation of a full joint choice function (i.e., the players' behavior for every conceivable subset of possible strategic choices).

3.2. Testing market power. If the price generated by the market mechanism is not sensitive to changes in the strategy of a individual i , Budget Balance implies that the individual is only able to move his net trades, $z(a^i, p(\bar{a})) - Ma^i = x(a^i, a^{-i}) - e^i$ in the linear space orthogonal to $p(\bar{a})$. A price taking consumer will choose consumption to maximize his utility on the budget

$$C^i(a^{-i}) = \{x^i \in R_+^L \mid p(\bar{a})(x^i - e^i) \leq 0\}$$

In an experiment $(a_k, \Gamma_k)_{k=1, \dots, n}$, we can construct competitive budget sets:

$$\begin{aligned} C_k^i &= \{x^i \in R_+^L \mid p_k(\bar{a}_k)(x^i - e_k^i) \leq 0\} \\ &= \{x^i \in R_+^L \mid f_k^i(x^i) \leq 0\}. \end{aligned}$$

with $f_k^i(x) = p_k(\bar{a}_k)(x - e_k^i)$, and define GARP in terms of these budgets. If an individual satisfies GARP in terms of the non linear budgets, i.e. 2) of Proposition 4, but fails GARP in terms of the competitive budgets $(C^i)_{k=1, \dots, n}$, we may take this as evidence of a rational individual who perceives his market power.

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