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**Working Paper**

## Experiments and Simulations on Day-to-Day Route Choice-Behaviour

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# BONN ECON DISCUSSION PAPERS

Discussion Paper 35/2002

## Experiments and Simulations on Day-to-Day Route Choice-Behaviour

by

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# Experiments and Simulations on Day-to-Day Route Choice-Behaviour

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**Abstract:** The paper reports laboratory experiments on a *day-to-day route choice game* with two routes. Subjects had to choose between a main road *M* and a side road *S*. The capacity was greater for the main road. 18 subjects participated in each session. In equilibrium the number of subjects is 12 on *M* and 6 on *S*.

Two treatments with 6 sessions each were run at the Laboratory of Experimental Economics at Bonn University using RatImage. Feedback was given in treatment I only about own travel time and in treatment II on travel time for *M* and *S*. Money payoffs increase with decreasing time. The main results are as follows.

1. Mean numbers on *M* and *S* are very near to the equilibrium.
2. Fluctuations persist until the end of the sessions in both treatments.
3. Fluctuations are smaller under treatment II. The effect is small but significant.
4. The total number of changes is significantly greater in treatment I.
5. Subjects' road changes and payoffs are negatively correlated in all sessions.
6. A *direct* response mode reacts with more changes for bad payoffs whereas a *contrary* response mode shows opposite reactions. Both response modes can be observed.
7. The simulation of an extended payoff sum learning model closely fits the main results of the statistical evaluation of the data.

**Key Words:** travel behaviour research, information in intelligent transportation systems, day-to-day route choice, laboratory experiments, payoff sum model

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# 1 Introduction

Understanding individual travel behaviour is essential for the design of Advanced Traveller Information Systems (ATIS), which provide real-time travel information, like link travel times (ADLER AND BLUE 1998, BARFIELD AND DINGUS 1998). However, the response of road users to information is still an open question (E.G., BEN-AKIVA 1991, BONSALE 1992, MAHMASSANI AND LIU 1999). It is not clear whether more information is beneficial (BEN-AKIVA ET AL. 1991). Drivers confronted with too much information may become oversaturated in the sense that information processing becomes too difficult and users develop simple heuristics to solve the problem (GIGERENZER ET AL. 1999).

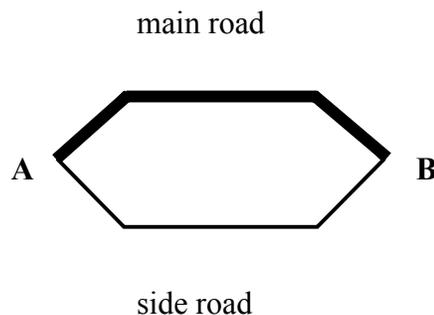
Drivers may also overreact to information and thereby cause additional fluctuations. Thus, the behaviour of the drivers has to be incorporated in the forecast (e.g. WAHLE ET AL. 2000, BEN-AKIVA ET AL. 1991, BONSALE 1992). ATIS can reduce fluctuations only if behavioural effects are correctly taken into account.

The Literature reports a number of experiments on route choice behaviour (e.g. BONSALE 1992, MAHMASSANI AND LIU 1999). Here we focus on the route choice in a generic two route scenario, which already has been investigated in the literature (e.g. IIDA ET AL. 1992). However our aim is to present experiments with a large number of periods and with sufficiently many independent observations for meaningful applications of non-parametric significance tests.

If one wants to investigate results of day to day route choice which can be transferred to more realistic environments, it is necessary to explore individual behaviour in an interactive experimental set-up. Does behaviour converge to equilibrium? Does more feedback reduce fluctuations? What is the structure of individual responses to recent experiences? Our experimental study tries to throw light on these questions.

## 2 Experimental Set-Up

Subjects are told that in each of 200 periods they have to make a choice between a main road  $M$  and a side road  $S$  for travelling from A to B.



**Figure 1:** Participants had to choose between a side road [S] and a main road [M]

They were told that  $M$  is faster if  $M$  and  $S$  are chosen by the same number of people. The number of subjects in each session was 18, mostly law and economic students from the University of

Bonn. The time  $t_M$  and  $t_S$  depends on the numbers  $n_M$  and  $n_S$  of participants choosing  $M$  and  $S$ , respectively:

$$t_M = 6 + 2n_M$$

$$t_S = 12 + 3n_S.$$

The period payoff was  $40 - t$  with  $t = t_M$  if  $M$  was chosen and  $t = t_S$  if  $S$  was chosen.

The total payoff of a subject was the sum of all 200 period payoffs converted to money payoffs in DM with a fixed exchange rate of .015 DM for each experimental money unit (Taler). Additionally, every participant received a lump sum payment of 200 Taler and a show- up fee of 10 DM. One session took roughly one and a half hours.

All pure equilibria of the game are characterized by

$$n_M = 12 \text{ and } n_S = 6,$$

resulting in a period payoff of 10 Taler per player. This sums up to 180 Taler per period, differing from the pareto-optimum with 181 Taler. The pareto-optimum can be reached by

$$n_M = 11 \text{ and } n_S = 7.$$

Two treatments have been investigated. In treatment I the subjects received:

- travel time of the last chosen route
- last chosen route
- payoff of the last period in Taler

- cumulated payoff in Taler
- number of the actual period

In treatment II additional feedback was provided about the travel time on the non-chosen-route in the last period. Six sessions were run with treatment I and six with treatment II. No further information was given to the subjects.

### **3 Equilibrium Predictions and Observed Behaviour**

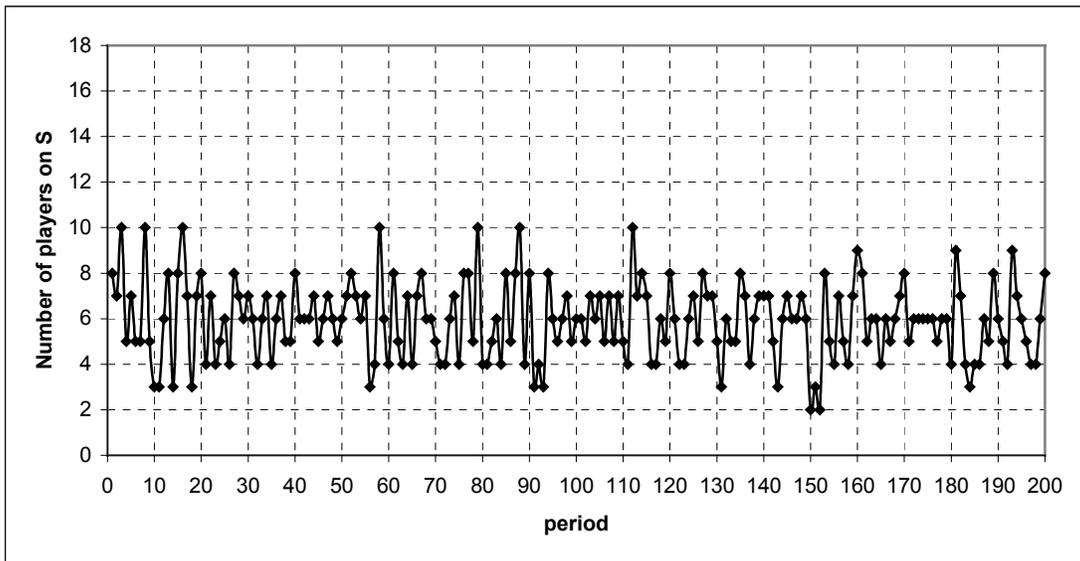
#### **3.1. Number of players on the side road $S$**

Figure 2 shows the number of participants on the side road  $S$  as a function of time for a typical session of treatment I.

It can be seen that there is no convergence to the theoretical equilibrium. There are substantial fluctuations until the end of the session. The same is true for all sessions of both treatments. The overall average of numbers of participants on  $S$  is very near to the equilibrium prediction. In each session the median number of players on the side road  $S$  is 6. The mean number of players on the side road  $S$  is 5.98 in treatment I and 6.06 in treatment II. The standard deviation of the session average from 6 is never greater than .17 and it is only .07 on the average. The fluctuations can be measured by the standard deviation of the number of participants choosing  $S$  per period. This

standard deviation is between 1.53 and 1.94. In view of these numbers one can speak of substantial fluctuations in each of the 12 sessions.

The fluctuations are a little larger under treatment I than under treatment II. The effect is significant. The null-hypothesis is rejected by a Wilcoxon-Mann-Whitney-Test on the significance level of 5 % (one sided).



**Figure 2:** Number of participants on S [a typical session of treatment I].

The game underlying the experiment has many pure strategy equilibrium points. In all of them the number of participants on the side road is 6, but the set of players who choose  $S$  can be any set of 6 players. The multiplicity of pure strategy equilibria poses a coordination problem which may be one of the reasons for non-convergence and the persistence of fluctuations. Feedback on

both travel times vs. feedback on only own travel time has a beneficial effect by the reduction of fluctuations, but this effect is relatively small.

### 3.2. Road changes

Figure 3 shows an example of the number of road changes as a function of time for a typical session of treatment I.

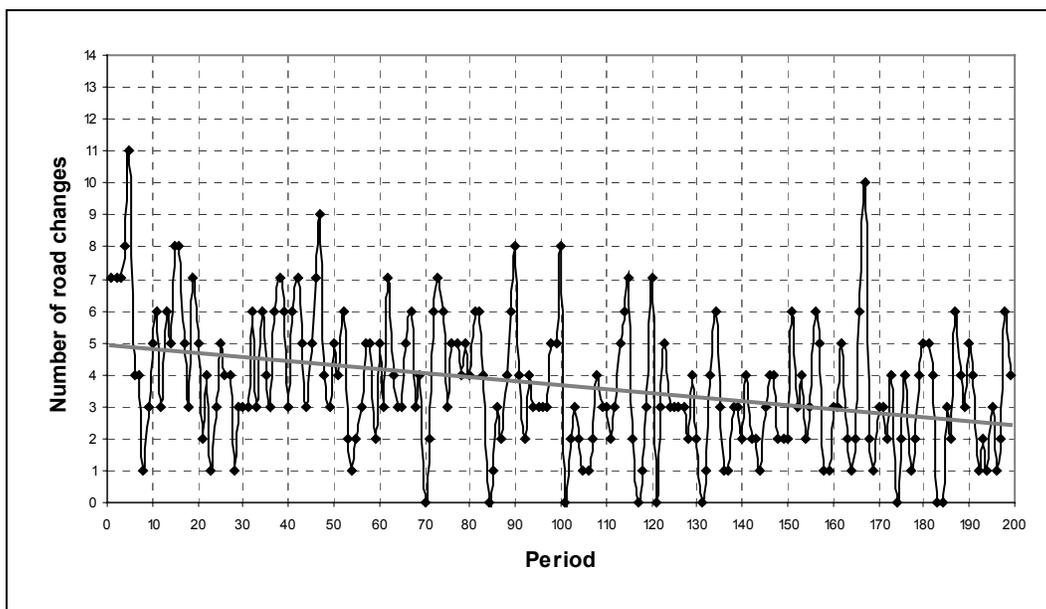
		number of players on S	
		mean	std. dev.
Treatment I	session I 01	6,02	1,814
	session I 02	5,91	1,691
	session I 03	6,01	1,849
	session I 04	5,85	1,748
	session I 05	6,1	1,81
	session I 06	6,03	1,793
	treatment I	5,98	1,784
Treatment II	session II 01	5,98	1,64
	session II 02	6,05	1,584
	session II 03	5,99	1,53
	session II 04	6,1	1,935
	session II 05	6,06	1,631
	session II 06	6,17	1,692
	treatment II	6,06	1,669

**Table 1:** Mean and standard deviation of the number of players on S.

There was a negative trend in each session of treatment II. By comparison in treatment I there were two sessions with a positive, two with a negative and two with an indifferent trend.

The fluctuations are connected to the total number of road changes within one session.

The Spearman-rank-correlation between the total number of road changes and the standard deviation of the number of participants per period on S is .795. This is significant on the level of 1 % (one sided). The median number of road changes is significantly higher in treatment I. The null-hypothesis is rejected by the Wilcoxon-Mann-Whitney-Test on a level of 5 % (one sided). The mean number of road changes under treatment I is also higher than under treatment II. A Wilcoxon-Mann-Whitney-Test rejects the null-hypothesis only on a very weak significance level of 8.98 % (one sided).



**Figure 3:** Number of road changes [a typical session of treatment I].

Under treatment I subjects who mainly choose only one of the roads feel the need to travel on the other road from time to time in order to get information on both roads. Under treatment II there is

no necessity for such information gathering. This seems to be the reason for the greater number of changes and maybe also for the stronger fluctuations under treatment I.

		number of road changes	
		mean	std. dev.
<b>Treatment I</b>	<b>session I 01</b>	5,08	2,298
	<b>session I 02</b>	3,87	1,865
	<b>session I 03</b>	5,16	1,934
	<b>session I 04</b>	5,19	1,931
	<b>session I 05</b>	5,28	2,391
	<b>session I 06</b>	4,35	2,083
	<b>treatment I</b>	4,82	2,084
<b>Treatment II</b>	<b>session II 01</b>	3,99	2,001
	<b>session II 02</b>	3,68	2,039
	<b>session II 03</b>	3,67	2,091
	<b>session II 04</b>	5,19	2,32
	<b>session II 05</b>	4,67	2,48
	<b>session II 06</b>	4,44	2,044
	<b>treatment II</b>	4,27	2,163

**Table 2:** Mean and standard deviation of the number of road changes

### 3.3. Payoffs

The mean payoffs per period in treatment I were significantly lower than in treatment II. The standard deviation of this random variable was higher in treatment I than in treatment II. In both cases a Wilcoxon-Mann-Whitney-Test rejects the null-hypothesis on a significance level of 5 %

(one sided). Nevertheless the efficiency with regard to the pareto optimum was in treatment I .91 and in treatment II .92. The payoffs are shown in Table 3 and 4.

Payoff 200 Periods [Treatment I]							
	I 01	I 02	I 03	I 04	I 05	I 06	I
mean	9,10	9,18	9,06	9,10	9,13	9,12	9,11
std. dev.	4,26	3,94	4,34	4,08	4,27	4,26	4,19
median	10	10	10	10	10	10	
mode	10	10	10	10	10	10	
min	-5	-2	-8	-8	-8	-11	
max	25	22	22	22	22	25	

**Table 3:** Mean payoffs in Treatment I.

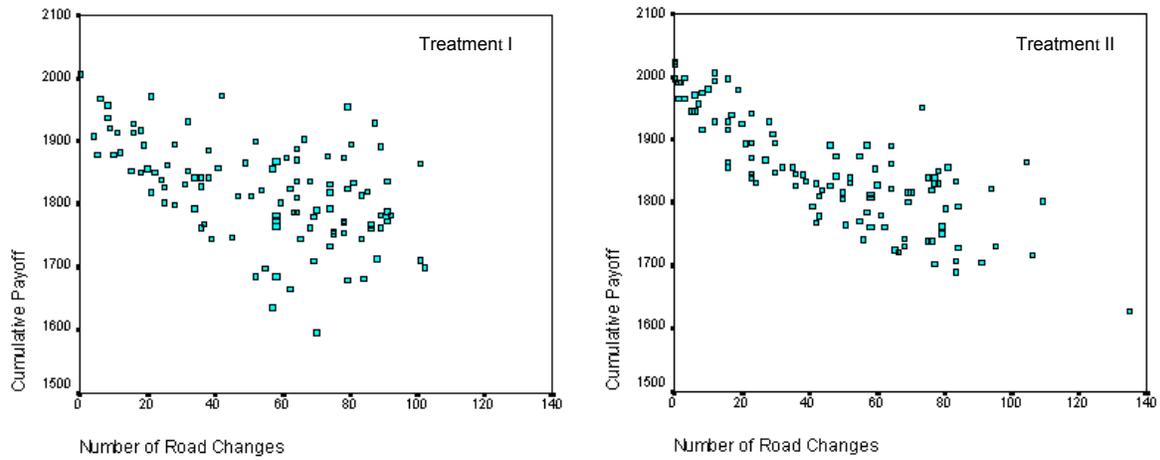
Payoff 200 Periods [Treatment II]							
	II 01	II 02	II 03	II 04	II 05	II 06	II
mean	9,25	9,32	9,35	8,99	9,28	9,26	9,24
std. dev.	3,80	3,77	3,60	4,58	3,85	4,03	3,94
median	10	10	10	10	10	10	
mode	10	10	10	10	10	10	
min	-2	-5	-2	-17	-2	-5	
max	22	22	22	28	22	25	

**Table 4:** Mean payoffs in Treatment II.

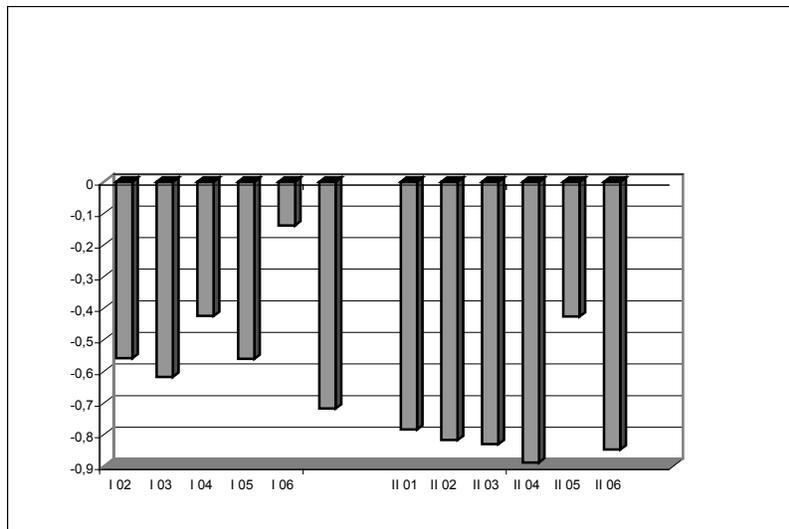
One might see that the information about the travel time on both routes effects only a small difference concerning the payoffs.

### 3.4. Payoffs and road changes

In all sessions the number of road changes of a subject is negatively correlated with the subject's payoff. Figure 4 shows that the negative correlation between the payoff in treatment II is stronger than in treatment I.



**Figure 4:** Scatter diagram cumulative payoff/number of road changes for treatment I and II.



**Figure 5:** Spearman rank correlation between cumulative payoffs and the number of road changes for each session of treatment I and II.

In both treatments the Spearman rank correlations between cumulative payoffs and the number of road changes are strictly negative. The Spearman-correlation-coefficients in treatment II are

lower than in treatment I. A Wilcoxon-Mann-Whitney-Test rejects the null-hypothesis on a significance level of 5 % (one sided). It is observed that some players in treatment I get an above average payoff even though they have a high change rate. The reason why this effect is not so often observed in treatment II might be, that the additional information about the travel time of the non chosen route was given. So it is not necessary for players to change in order to collect information. This might explain, that 3 players always stayed on the main road in treatment II, nevertheless it is surprising that one player did the same in treatment I.

Even if subjects change roads in order to get higher payoffs, they do not succeed in doing this on the average. This suggests that it is difficult to use the information provided by the feedback to one's advantage.

#### **4 Response mode**

A participant who had a bad payoff on the road chosen may change his road in order to travel where it is less crowded. We call this the *direct* response mode. A road change is the more probable the worse the payoff was.

The *direct* response mode is the prevailing one but there is also a *contrarian* response mode. Under the contrarian response mode a road change is more likely the better the payoff was. The

contrarian participant expects that a high payoff will attract many others and that therefore the road chosen will be crowded in the next period.

The equilibrium payoff is 10. Payoffs perceived as bad tend to be below 10 and payoffs perceived as good tend to be above 10. Accordingly we classified the response of a subject as direct if the road is changed after a payoff smaller than 10 or not changed after a payoff greater than 10. An opposite response is classified as contrarian. Table 2 shows the numbers of times in which a subject changes roads ( $c_-$  for a payoff below 10 and  $c_+$  for a payoff above 10), or stays at the same road ( $s_-$  for a payoff below 10 and  $s_+$  for a payoff above 10).

	<b>change</b>	<b>stay</b>
<b>payoff &lt; 10</b>	$c_-$	$s_-$
<b>payoff &gt; 10</b>	$c_+$	$s_+$

**Table 5:** 2x2 table for the computation of Yule coefficients.

For each subject such a 2x2 table has been determined and a Yule coefficient  $Q$  has been computed as follows.

$$Q = \frac{c_- \cdot s_+ - c_+ \cdot s_-}{c_- \cdot s_+ + c_+ \cdot s_-}$$

The Yule coefficient has a range from  $-1$  to  $+1$ . In our case a high Yule coefficient reflects a tendency towards direct responses and a low one a tendency towards contrarian responses.

In each of four sessions, one of them in Treatment I and three in treatment II, there was one player for whom no Yule coefficient could be determined since these four subjects never change roads. These subjects are not considered in the evaluation of Yule coefficients.

The mean and the standard deviation of the Yule coefficients are shown in Table 6.

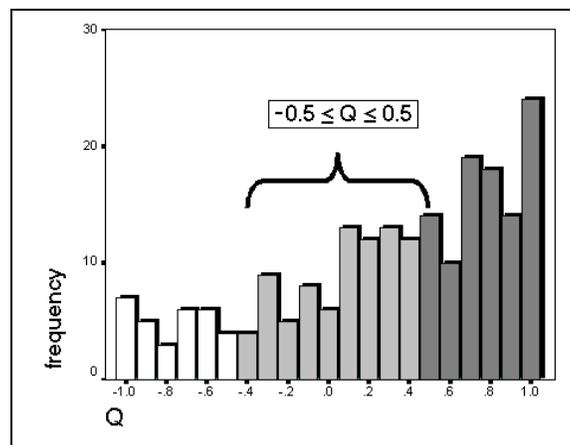
		Yule coefficients Q	
		mean	std. dev.
Experiment I	session I 01	0,214	0,654
	session I 02	0,373	0,592
	session I 03	0,277	0,525
	session I 04	0,191	0,603
	session I 05	0,313	0,584
	session I 06	0,332	0,542
	treatment I	0,283	0,585
Experiment II	session II 01	0,365	0,591
	session II 02	0,374	0,536
	session II 03	0,308	0,552
	session II 04	0,271	0,584
	session II 05	0,246	0,738
	session II 06	0,122	0,557
	treatment II	0,281	0,597

**Table 6:** Mean and standard deviation of the Yule coefficients in both treatments.

Evidence for the importance of both response modes can be found in the distributions of Yule coefficients within a session. If the two response modes were not present in behaviour one would expect distributions of Yule coefficients concentrated around 0. However the number of subjects with extreme Yule coefficients below  $-0.5$  or above  $+0.5$  tends to be greater than the number of subjects with Yule coefficients in the middle range between  $-0.5$  and  $+0.5$ . A Wilcoxon one sample

test supports this alternative hypothesis by rejecting the null-hypothesis that none of both numbers tends to be greater than the other, on the significance level of 1 % (two sided).

If one classifies subjects with Yule coefficients above +.5 as direct responders and subjects with Yule coefficients below -.5 as contrarian responders, then one receives 44 % direct responders, 14% contrarian responders and 42% unclassified subjects. The distribution of the Yule coefficients is shown in figure 6.



**Figure 6:** Distribution of the experimental Yule coefficients:

## 5 Simulations

In order to get more insight into this theoretical significance of our result, we have run simulations based on a version of a well known reinforcement learning model, the payoff-sum

model. This model already described by Harley (1981) and later by Arthur (1991) has been used extensively by Ereth and Roth (1995) in the experimental economics literature.

<p><b>Initialisation:</b> For each player <math>i</math> let <math>[x_{i,1}^1, \dots, x_{i,n}^1]</math> the initial propensity, where <math>n</math> is the number of strategies, which are used in the simulations.</p> <p><b>1. period:</b> Each player <math>i</math> chooses strategy <math>j</math> with probability <math>\frac{x_{i,j}^1}{\sum_j x_{i,j}^1}</math>.</p> <p><b>t+1. period:</b> For each player <math>i</math>, let <math>a_i^t</math> the payoff of player <math>i</math> in period <math>t</math>,  <math>j</math> the number of the chosen strategy in period <math>t</math>.</p> <p>IF <math>a_i^t \geq 0</math>:</p> $x_{i,j}^{t+1} := x_{i,j}^t + a_i^t$ $x_{i,k}^{t+1} := x_{i,k}^t, k \neq j$ <p>ELSE</p> $x_{i,j}^{t+1} := x_{i,j}^t$ $x_{i,k}^{t+1} := x_{i,k}^t - a_i^t, k \neq j$ <p>Each player <math>i</math> chooses strategy <math>j</math> with probability <math>\frac{x_{i,j}^{t+1}}{\sum_j x_{i,j}^{t+1}}</math>.</p>
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**Table 7:** The Payoff-Sum Model

Table 7 explains the version underlying our simulations. We are looking at player  $i$  who has to choose among  $n$  strategies  $1, \dots, n$  over a number of periods  $t, t=1..T$ . The probabilities with which each strategy  $i$  is chosen is proportional to its “propensity”  $x_{i,j}^t$ . In period 1 these propensities are

exogenously determined parameters. Whenever the strategy  $j$  is used in period  $t$ , the resulting payoff  $a_j^t$  is added to the propensity if this payoff is positive. If all payoffs are positive, then the propensity is the sum of all previous payoffs for this strategy plus its initial propensity. Therefore one can think of a propensity as a payoff sum.

In our experiments negative payoffs are not impossible. This creates a difficulty for the model, since one has to exclude the case that a propensity becomes negative. In the literature this is sometime solved by adding up the exponential of the payoffs instead of the payoffs themselves. Here we take another approach to this problem. If a negative payoff is obtained for the use of the strategy  $x_i$ , the absolute value of this payoff is added to all other propensities and the propensity of the strategy  $i$  remains unchanged. We think that this is the simplest generalisation of the original payoff sum model which was conceived for positive payoffs only.

In our simulations 18 players interact for 200 periods just like in our experiments. Each player has four strategies:

1. *main road*:

This strategy simply consists in taking the decision for the main road.

2. *side road*:

This strategy consists in taking the side road.

3. *direct*:

This strategy corresponds to the direct response mode. The payoff of a player is compared to his median payoff among his payoffs for all periods up to now. If the present payoff is

lower than this median payoff, then the road is changed. If the payoff is greater than this median payoff, the player stays on the same road as before. It may also happen that the current payoff is equal to the median payoff. In this case, the road is changed if the number of previous payoffs above the median is greater than the number of previous payoffs below the median. In the opposite case, the road is not changed. In the rare cases where both numbers are equal, the road is changed with probability  $\frac{1}{2}$ .

#### 4. *contrarian*:

A player who takes this strategy stays on the last chosen road if his current payoff is smaller than the median payoff among the payoffs for all previous periods and he changes the road in the opposite case. If the current payoff is equal to this median payoff, then he changes the road if the number of previous payoff below the median payoff is greater than the number above the median payoff. If the numbers of previous payoff below and above the median payoff are equal, the road is changed with probability  $\frac{1}{2}$ .

In the first period only strategy one and two were available to the simulated subjects since strategy three and four cannot be applied because there is not yet a median of previous payoffs.

The strategies *direct* and *contrarian* describe the response modes discussed in section 4, but with a small difference. There changing and staying was conditioned on how the last payoff differed from the equilibrium payoff 10. In the experiments the median payoff is very often at 10. However, in the simulations we did not want to build in prejudices based on theoretical values.

Our simulated players base their behaviour on initial propensities and observations only. Of course, it is assumed that as in the experiments the players get feedback about their own payoffs immediately after their choices. In the experimental treatment II additional feedback about the payoff on the route not chosen was given. The payoff sum model makes use of a player's own payoff only and therefore ignores the additional feedback of treatment II.

The differences between treatment I and treatment II cannot be explained by the payoff sum model since it does not process the additional feedback information given in treatment II. For the purposes of comparing our simulation data with the experimental data we ignore the differences between treatment I and II which are not big anyhow.

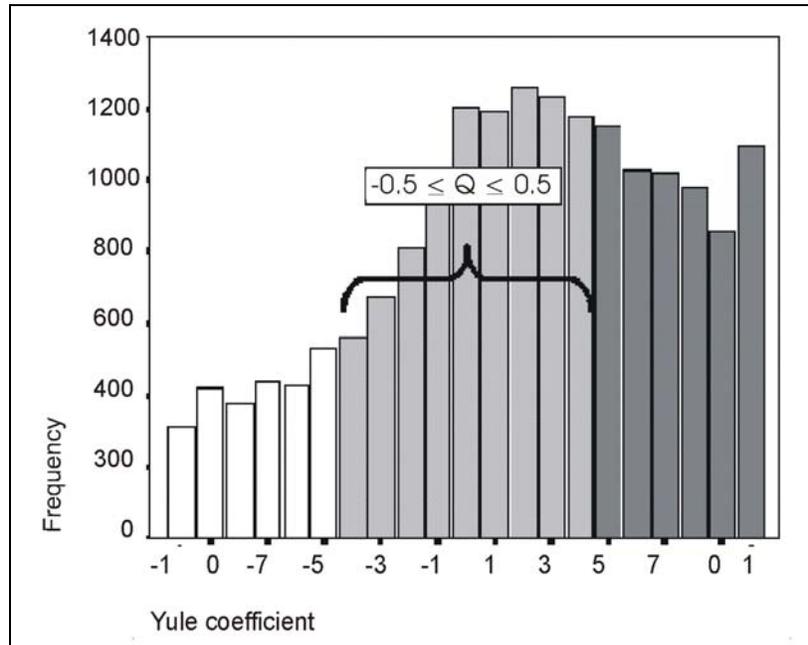
The difficulty arises that the initial propensities must be estimated from the data. We did this by varying the initial propensities for the strategies *main road* and *side road* over all integer values from 1 to 10 and the initial propensities for the strategies *direct* and *contrarian* over all integer values from 0 to 10. We compared the simulation results with the six variables listed in table 8. We aimed at simulation results which were between the minimum and maximum experimental results over all twelve sessions of treatment I and II. For each of the 12100 parameter combinations we have run 1000 simulations. There was only one parameter combination which satisfied the requirement of yielding means for the six variables between the minimal and maximal experimentally observed values. This was the parameter combination (4,3,3,2). The numbers refer to *main road*, *side road*, *direct* and *contrarian* in this order. The parameter

combination is a reasonable vector of initial propensities. The players know that the capacity of the main road is greater than that of the side road and the first two parameters reflect this knowledge. It is reasonable to suppose that at least in the beginning the simple strategies *main road* and *side road* have a greater propensity sum than *direct* and *contrarian*.

	min Ex I & II	Simulations	max Ex I & II
<b>mean(#(players[S]))</b>	5,85	5,88	6,17
<b>std_dev(#(players[S]))</b>	1,53	1,65	1,94
<b>mean(#(road_ch))</b>	3,67	5,17	5,28
<b>mean(#(last_road_ch))</b>	154,78	183,73	190,39
<b>mean(yule)</b>	0,12	0,14	0,37
<b>std_dev(yule)</b>	0,52	0,60	0,74

**Table 8:** Experiments and simulations with 18 players.

It is surprising that a very simple reinforcement model reproduces the experimental data as well as shown by table 8. Even the mean Yule coefficient is in the experimentally observed range. In spite of the fact that at the beginning of the simulation the behaviour of all simulated players is exactly the same. It is not assumed that there are different types of players. The distribution of the Yule coefficients of the simulated subjects is shown in figure 8. This distribution does not look exactly like the one of the experimentally observed Yule coefficient shown by figure 6. There are more values in the central range between -.5 and +.5. However, like in figure 6, many more observations are in the upper quartile than in the lowest one. This indicates that the direct response mode is much more frequent than the contrarian one, in the experiments as well as in the simulations.



**Figure 7:** Distribution of the simulated Yule coefficients.

The distribution of the Yule coefficients shown by figure 7 suggests that during the play the behaviour of many simulated players more and more concentrates on one strategy. This is the result of different learning histories.

It is not clear that in the actual experiments tendencies toward direct and contrarian behaviour are mere results of the learning history during the play of the game. Probably some of the experimental subjects bring such tendencies already to the laboratory. This may be due to prior learning outside the laboratory or to inherited behavioural inclinations. We do not want to pass judgement on this but an initial heterogeneity might explain the somewhat smaller concentration

of the experimental data in the middle range. One could of course try to get an even closer agreement with the experimental data by using a simulation model with subject heterogeneity. However this would involve the estimation of many more parameters.

## **6 Conclusion**

The study has shown that the mean numbers on both roads tend to be very near to the equilibrium. Nevertheless, fluctuations persist until the end of the sessions in both treatments. This is of particular interest in view of the fact that the experiments run over 200 periods which is unusually long and should be enough to show a tendency of convergence to equilibrium, if there is one.

Feedback on both road times significantly reduces fluctuations in treatment II compared to treatment I. However the effect is small. There is a significant rank correlation between the total number of road changes and the size of fluctuations. In treatment I road changes may serve the purpose of information gathering. This motivation has no basis in treatment II. However road changes may also be attempts to improve payoffs. The finding of a negative correlation between a subject's payoff and number of road changes suggests that on the average such attempts are not successful.

Two response modes can be found in the data, a *direct* one in which road changes follow bad payoffs and a *contrarian* one in which road changes follow good payoffs. One can understand these response modes as due to different views of the causal structure of the situation. If one expects that the road which is crowded today is likely to be crowded tomorrow one will be in the direct response mode but if one thinks that many people will change to the other road because it was crowded today one has reason to be in the contrarian response mode. We have presented statistical evidence for the importance of the two response modes.

We have also run simulations based on a simple payoff sum reinforcement model. Simulated mean values of six variables have been compared with the experimentally observed minimal and maximal of these variables. The simulated means were always in this range. Only four parameters of the simulation model, the initial propensities, were estimated from the data. In view of the simplicity of the model it is surprising that one obtains a quite close fit to the experimental data. The response modes *direct* and *contrarian* also appear in the simulations as the result of an endogenous learning behaviour by which initially homogeneous subjects become differentiated over time.

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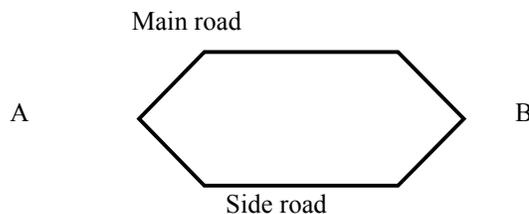
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## Appendix

### Leaflet to the traffic experiment

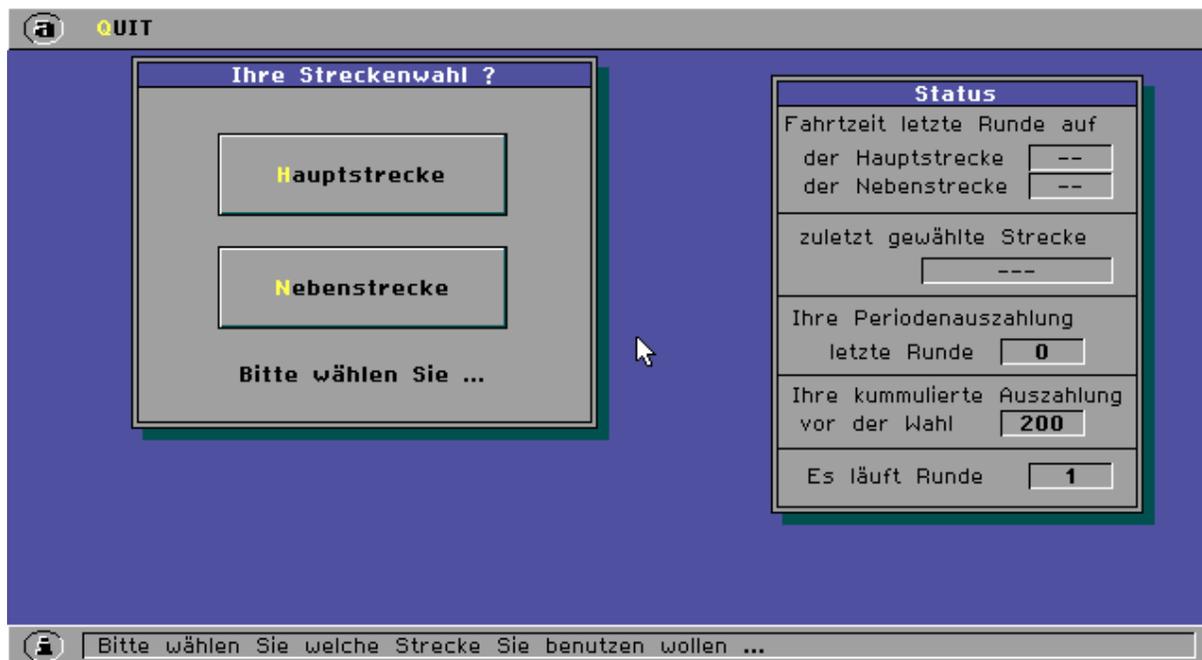
- Altogether 18 persons are participating in this experiment. The game situation is the same for every participant.
- The experiment consists of **200 periods**.
- In each period you are travelling from a **starting point A** to an **arrival point B**. You can either choose a **main road** or a **side road** to get from A to B (see drawing).



- For the travel time from A to B the following holds: On both routes the travel time increases with increasing traffic and decreases with decreasing traffic. If traffic is the same on the main and on the side road, the travel time is shorter on the main road than on the side road.
- You can make a new route choice in every period.
- **Your payoffs per period:**  
After each period you will receive a period payoff P which depends on the travel time T. Hereby holds:  $P = 40 - T$ . E.g. the shorter the travel time needed, the higher the payoff.
- **Your information per period:**  
The travel time on the route that you chose in the preceding period  
The travel time on the route that you did not choose in the preceding period (*only in Experiment II*)  
Your route chosen in the preceding period.  
Your period payoffs in the preceding period in **Talers**.  
Your cumulated payoffs before the route choice in **Talers**.  
Number of the current period.
- Each participant receives a seed capital of **200 Talers**. The exchange rate is **1,5 Pf** per Taler.

Independent of your success in the game you will receive a **10 DM** lump-sum payment for participation.

## Screenshot



## Translation

German	English
Ihre Streckenwahl?	Your route choice?
Hauptstrecke	main road
Nebenstrecke	side road
Bitte wählen Sie...	Please choose...
Fahrtzeit letzte Runde auf der Hauptstrecke	travel time in the preceding period on the main road
der Nebenstrecke	the side road
zuletzt gewählte Strecke	route chosen in the preceding period
Ihre Periodenauszahlung letzte Runde	Your period payoffs in the preceding period
Ihre kumulierte Auszahlung vor der Wahl	Your accumulated payoffs before the route choice
Es läuft Runde	This is period