Wilckens, Sebastian

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Should WTO Dispute Settlement Be Subsidized?

by Sebastian Wilckens
Should WTO Dispute Settlement Be Subsidized?

Sebastian Wilckens*

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Abstract

This paper develops a model of the WTO dispute settlement process (DSP) to study the recent proposal by legal scholars to subsidize litigation costs. The high cost of litigation, so the argument, is a major obstacle for developing countries to using the DSP to enforce developed countries’ compliance with WTO rules. The paper shows that this proposal may be misguided. In particular, a reduction of litigation costs may lead large countries to impose larger trade impediments where before they may have raised barriers only a little. Thus, a cost reduction may even weaken the smaller countries’ position in the DSP. Moreover, the model sheds light on the structure of the dark figure of un-accused offenses, suggesting that the observed record of disputes notified to the WTO is systematically biased.

Keywords: Developing Countries, Dispute Settlement, GATT/WTO, Tariff Retaliation, Trade Disputes

JEL Classification: F13

*Department of Economics, Christian-Albrechts-Universität zu Kiel, Wilhelm-Seelig-Platz 1, D-24098 Kiel, Germany, wilckens@economics.uni-kiel.de. I am particularly grateful to Horst Raff and Rolf J. Langhammer for their guidance and support. I would like to thank Mathis Klepper, Gunnar Wiedenfels and Simone Alfarano as well as participants at the Brown-Bag-Seminar of the University of Kiel and conference participants at the European Trade Study Group meeting in Vienna who improved this paper with thoughtful comments and helpful suggestions.
1 Introduction

An essential change in the course of the transformation of the General Agreement on Tariffs and Trade (GATT) to the World Trade Organization (WTO) in 1995 was the institutionalization of a Dispute Settlement System (DSS). From 1995 until the end of 2005 there were 335 disputes notified to the WTO, consisting of 368 individual countries’ complaints. The major share of these complaints (222) was filed by high income countries and against high income countries (235), while there have been only 22 complaints and 21 defences by low-income countries.\textsuperscript{1} This extremely asymmetric usage of the DSS has been traced back to an institutional bias of the DSS by scholars from the fields economics, law and politics. A prominent proposal to overcome this supposed bias of the DSS is a reduction of litigation costs.\textsuperscript{2}

Apart from the cost reduction proposal, the supposed bias of the DSP as such is analyzed in this paper. Some empirical studies have already examined whether or not the unbalancedness of the record of disputes with respect to income groups indicates a systematic bias of the DSS against poorer countries. In the pioneer paper by [Horn et al., 1999] the hypothesis that a dispute in a given bilateral product-market-pairing (PMP) occurs randomly is tested empirically. The PMP-approach explains the observed pattern of disputes quite accurately, since bigger and richer countries with more PMPs are supposed to be involved in more disputes than smaller and poorer countries with less PMPs. Another empirical paper by [Guzman and Simmons, 2005] analyzes the pattern of disputes in terms of the complainants’ and respondents’ GDP. The authors reject the “power hypothesis” which “...predicts that countries will file fewer complaints if they are poor and politically weak than if they are rich and politically powerful.”\textsuperscript{3}

Although these empirical findings basically reject the hypothesis of a biased system, there is reason to believe that an institutional bias exists, even if it does not show up in the data. It is a known result in trade theory that a larger country may improve its welfare

\textsuperscript{1} The figures on the notified disputes are taken from the author’s own dataset, which is based on the record of disputes on the WTO’s website. Income classifications of countries correspond to the Worldbank’s classification scheme.

\textsuperscript{2} The proposals include legal assistance, financial assistance and the introduction of procedurally simplified “Small Claims” proceedings for complaints of minor value. See for example [Busch and Reinhardt, 2003] and [Footer, 2001]

\textsuperscript{3} [Guzman and Simmons, 2005], page 559.
by offending a trade agreement with a smaller trading partner, even if the smaller country retaliates.\(^4\) Moreover, it is an empirically supported thesis that poor countries face higher costs associated with the preparation of a complaint than rich countries do.\(^5\) In the light of just these two arguments it should already become questionable that the observed record of disputes is generated by an unbiased random process. As a matter of fact, up to now there is no information on the dark figure of disputes, which are those cases where a country experienced a violation but did not report it to the WTO. [Guzman and Simmons, 2005] conclude: “In the absence of a clear sense of how many cases developing countries ‘ought to’ have initiated, we really do not know whether these filed cases represent equal access or not.”\(^6\) Therefore, empirical approaches that try to shed light on the question of a systemic bias seem to be a dead end.

Theory on trade agreements is dominated by the employment of an infinitely repeated prisoner’s dilemma game in order to explain a country’s incentive to comply with, or to offend against a trade agreement.\(^7\) The common ground of these models is the assumption that an offense by one of the trading partners leads to non-cooperative behavior of both trading partners in each of the following periods. As a consequence existing trade agreements are assumed and required to be self-enforcing, such that the afore mentioned trigger strategy successfully deters countries from defecting.\(^8\) Thus, in contrast to reality, violation and retaliation remain off-equilibrium-path strategies in these models.

All in all, existing empirical studies’ inference is likely to be based on a systematically biased set of observations, while existing theory does not provide any explanation for the occurrence of disputes if one leaves alone the idea that policymakers may be possessed by a “demon” who leads them to irrational behavior from time to time.\(^9\)

In order to be able to (i) explain the occurrence of trade disputes and (ii) analyze the

\(^4\)A classic reference is “Do Big Countries Win Tariff Wars?” by [Kennan and Riezman, 1988].

\(^5\)See [Bown, 2005], [Guzman and Simmons, 2005] and [Busch and Reinhardt, 2003] who argue that costs play an important role in the poorer countries’ decision whether or not to file a complaint. See [Footer, 2001] for a verbal analysis.

\(^6\)[Guzman and Simmons, 2005], page 591.

\(^7\)[Bagwell and Staiger, 1999] use a two country approach. [Maggi, 1999] uses a three country approach of the described fashion.

\(^8\)[Bagwell and Staiger, 2002], page 99, believe: “The fundamental deterrent to such behavior, and the deterrent that therefore rests at the foundation of all others, is the fear of initiating a breakdown in the entire cooperative arrangement and thereby causing a ‘trade war’.”.

\(^9\)See [Kovenock and Thursby, 1992].
effects of the proposed reduction of litigation costs this paper takes a different slant by providing an explicit model of the DSP. The regulations of the Dispute Settlement Understanding (DSU), which governs the rules of retaliation, are taken at face value and applied to a two country tariff setting game. In this setup violation does not necessarily have to be an off-equilibrium strategy. It rather depends upon a country’s relative size and the pertinent level of litigation costs whether or not a trade agreement is violated, and whether or not the offended country decides to file a costly complaint.

The remainder of this paper is organized as follows. Section 2 starts by presenting the underlying two country trading environment. After a brief setup of the model’s fundamental equations, the rules of the sequential tariff setting game are introduced. The setup is completed by modeling the WTO’s provisions of retaliation. Subsequently the game is solved via backward induction, and best response functions are derived. The equilibria of the game are presented as functions of country size and litigation costs. Moreover, the proposal of a reduction of litigation costs is examined in a comparative static analysis. In section 4 the robustness of the results is verified in the course of an extension of the basic model. Finally section 5 summarizes the results, establishes links to empirical studies in support of the results and points out implications for the dark figure of disputes.

2 The Model

The analysis is based on a trade model with two countries (Home and Foreign) and three goods ($x$, $y$, and $z$), which allows for different country or market sizes. The underlying utility functions are assumed to be quasilinear in both countries: $U[x, y, z] = z + u_x[x] + u_y[y]$. While $u_x[.]$ and $u_y[.]$ are assumed to exhibit decreasing marginal utility, $z$ is assumed to be a numeraire good with price $p_z$ fixed at unity. Trade in the numeraire good is assumed to be determined residually by the condition of balanced trade.

For the sake of simplicity of the economic arguments, a simple model, where both countries differ only in their demand for one of the two non-numeraire goods, is analyzed at first. In section 4 the analysis is extended to a more cumbersome model, where demand for both non-numeraire goods is affected in order to account for country size differences.
2.1 Setup of the Trading Environment

Home’s demand functions are obtained from the quasilinear utility function $U[x, y, z] = z + (a x - \frac{x^2}{2n})^\frac{1}{b} + (a y - \frac{y^2}{2})^\frac{1}{b}$, while Foreign’s underlying utility function is given by $U^*[x, y, z] = z + (a x - \frac{x^2}{2})^\frac{1}{b} + (a y - \frac{y^2}{2})^\frac{1}{b}$. Since all parameters are assumed to be positive, Home receives more (less) utility from the consumption of good $x$ than Foreign if $n$ is larger (smaller) than unity. An alternative way to think of the setup of this basic model is to assume two different types of consumers in each country. Consumers of type $x$ only derive utility from the consumption of good $x$ and the numeraire good, whereas consumers of type $y$ only derive utility from the consumption of good $y$ and the numeraire good. Assume then that Home has $n$ consumers of type $x$, while Foreign has one consumer of type $x$ and that there is one consumer of type $y$ in each country. Home’s demand functions for good $x$ and $y$ are given by:

$$D_x[p_x] := (a - bp_x)n$$ \hspace{1cm} (1)

$$D_y[p_y] := a - bp_y$$ \hspace{1cm} (2)

Foreign’s demand functions for good $x$ and $y$ are given by:

$$D^*_x[p_x] := a - bp_x$$ \hspace{1cm} (3)

$$D^*_y[p_y] := a - bp_y$$ \hspace{1cm} (4)

While both countries have a positive demand for both good $x$ and good $y$, good $x$ is produced only in Foreign, whereas good $y$ is produced only at Home\textsuperscript{10}:

$$S^*_x[p_x] := bp_x$$ \hspace{1cm} (5)

$$S_y[p_y] := bp_y$$ \hspace{1cm} (6)

Consequently, Home becomes a net importer of good $x$ and a net exporter of good $y$, while Foreign becomes a net importer of good $y$ and a net exporter of good $x$. Note that the two\textsuperscript{10}The underlying production functions are assumed to exhibit decreasing returns to scale. The production functions for $x$ and $y$ are given by $x[l] = \sqrt{2M}$ and $y[l] = \sqrt{2M}$ respectively, where $l$ denotes any input factor.
countries are symmetric except for the multiplicative parameter $n$, which represents the size of the home market demand for good $x$. For $n = 1$ the two countries would be completely symmetric, while for $n > 1$ ($n < 1$) it holds that Home’s import demand is larger, (smaller) than Foreign’s import demand.

By assumption, each country’s sole policy variable is a per unit import tariff on its import good. Home’s import tariff on good $x$ is denoted by $\tau$, while Foreign’s import tariff on good $y$ is denoted by $\tau^*$. After the introduction of tariffs the demand functions for each country’s import good are $D_x[p_x] := (a - b(p_x + \tau))n$ and $D_y^*[p_y] := a - b(p_y + \tau^*)$, respectively. Market clearing conditions are given by $D_x[p_x] + D_y[p_y] + D_x^*[p_x] = S_x[p_x]$ and $D_y[p_y] + D_y^*[p_y, \tau^*] = S_y[p_y]$, respectively.

Solving for $p_x$ and $p_y$ yields equilibrium world market prices as functions of the associated import tariffs. Substituting the equilibrium prices into each country’s demand and supply functions yields the equilibrium quantities as functions of the import tariffs.

**Welfare Considerations**

Consumer surplus in sector $x$ at Home is given by $cs_x[p_x] = \int_{p_x}^{\hat{p}_x} D_x[p_x] dp_x$. Substituting for $p_x$ with $\hat{p}_x[\tau] + \tau$ yields consumer surplus in equilibrium as a function of Home’s tariff:

$$\hat{cs}_x[\tau] = \frac{n(a - 2b\tau)^2}{2b(2 + n)^2}$$

Home’s tariff revenue is simply equilibrium demand multiplied by $\tau$ yielding $\hat{tr}_x[\tau] = \frac{nn(a - 2b\tau)^2}{2b(2 + n)^2}$. Thus, Home’s equilibrium welfare in sector $x$ can be expressed as a function of its import tariff $\tau$ and the market size parameter $n$:

$$\hat{w}_x[\tau, n] = \frac{n(a - 2b\tau)(a + 2b(1 + n)\tau)}{2b(2 + n)^2} \quad (7)$$

Home’s consumer surplus in sector $y$ is given by $cs_y[p_y] = \int_{p_y}^{\hat{p}_y} D_y[p_y] dp_y$. Substituting for $p_y$ with $\hat{p}_y[\tau^*]$ yields consumer surplus in equilibrium as a function of $\tau^*:

$$\hat{cs}_y[\tau^*] = \frac{(a + b\tau^*)^2}{18b}$$

Producer surplus of Home’s exporting industry is $ps_y[p_y] = \int_{p_y}^{\hat{p}_y} S_y[p_y] dp_y$. Substituting for $p_y$ with $\hat{p}_y[\tau^*]$ yields producer surplus in equilibrium as a function of $\tau^*$:

$$\hat{ps}_y[\tau^*] = \frac{(-2a + b\tau^*)^2}{18b}$$

Thus, Home’s equilibrium welfare in sector $y$ can be expressed as a function

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11. See Mathematical Appendix 6.1.
12. Note that all equilibrium values will be labeled with a hat in the following.
depending solely upon Foreign’s import tariff $\tau^*$:

$$\hat{w}_y[\tau^*] = \frac{1}{18} \left( \frac{5a^2}{b} - 2a\tau^* + 2b\tau^{*2} \right)$$

(8)

Home’s aggregated equilibrium welfare is simply the sum of welfare in both sectors and therefore dependent upon its own import tariff $\tau$, Foreign’s import tariff $\tau^*$ and the market size parameter $n$:

$$\hat{w}[\tau, \tau^*, n] = \frac{1}{18} \left( \frac{5a^2}{b} - 2a\tau^* + 2b\tau^{*2} \right) + \frac{n(a - 2b\tau)(a + 2b(1 + n)\tau)}{2b(2 + n)^2}$$

(9)

Foreign’s aggregated equilibrium welfare is obtained in an analogous manner. It is as well a function of Home’s import tariff $\tau$, Foreign’s import tariff $\tau^*$ and the market size parameter $n$:

$$\hat{w}^*[\tau, \tau^*, n] = \frac{a^2 + 2ab\tau^* - 8b^2\tau^{*2}}{18b} + \frac{a^2(2 + 2n + n^2) - 2abn^2\tau + 2b^2n^2\tau^2}{2b(2 + n)^2}$$

(10)

Both aggregated welfare functions are concave in each country’s own tariff and decreasing in the other country’s tariff. A unilaterally welfare-maximizing tariff will be referred to as an “optimal tariff”. The pair of optimal tariffs $\tau_o$ and $\tau^*_o$ is given by:

$$\tau_o[n] = \frac{an}{4b + 4bn}$$

(11)

$$\tau^*_o = \frac{a}{8b}$$

(12)

While Foreign’s optimal tariff is a constant, Home’s optimal tariff is an increasing function of its own market size $n$. This dependency stems from the increasing ability to influence the terms-of-trade in one’s favor with increasing market size. From the equations above it is obvious that Home’s optimal tariff will be lower, (higher) than Foreign’s optimal tariff if $n < 1$, $(n > 1)$.

Note that up to now all welfare components of sector $x$ only depend on changes of Home’s policy variable $\tau$, while all welfare components of sector $y$ react to changes of Foreign’s policy.

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13See Mathematical Appendix 6.2.

14Note that $\frac{\partial \hat{w}_x[n]}{\partial n} = \frac{a}{8b(1+n)^2}$ is always positive.
variable $\tau^*$. As a consequence each country is vulnerable in its export sector, while it can harm the other country by restricting access to its own import sector. Interaction between the tariff choices of both countries will now be established by means of a sequential game.

### 2.2 Trade Disputes as Sequential Games

Thinking of the two countries as any two WTO members that are involved in bilateral trade, it is reasonable to assume these countries have committed themselves to some kind of trade agreement. For simplicity, it is assumed that the two countries have committed themselves to an initial free trade agreement, which implies that both $\tau$ and $\tau^*$ have to be equal to zero in order to fulfill the agreement. Under such a type of agreement, countries could be tempted to violate the agreement by a unilateral increase of the import tariff in order to benefit from an increase in their own welfare.\(^{15}\)

Let Home be the first mover in this sequential game. Then Home will decide whether to violate the agreement to a certain extent, by raising its tariff above the allowed level, or to comply with the agreement. Foreign, being the second mover, observes the choice of the first mover. In case the first mover violates the agreement, the second mover can choose between doing nothing and filing a complaint at costs $c$ at the Dispute Settlement Body (DSB) in order to be entitled to retaliate against Home.\(^{16}\)

Although the typical dispute settlement process consists of multiple stages, starting with a request for consultations, via the ruling of panel and appellate body, up to the request for the suspension of concessions, in this model it is reduced to a single decision of the second mover (to complain or not to complain).\(^{17}\)

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\(^{15}\)A typical WTO example for such a situation would be any WTO member’s obligation to grant every trading partner an import tariff that is lower than or equal to its Most-Favored-Nation import tariff, while at the same time this particular member possibly would like to discriminate among its trading partners by setting different import tariffs.

\(^{16}\)Litigation costs can be thought of as to incorporate the direct monetary costs of hiring a law firm or a consulting company in the course of the preparation of the complaint as well as the loss of political goodwill of the trading partner. [Nordström, 2005] emphasizes the role of direct monetary litigation costs and provides empirical data on its composition.

\(^{17}\)This simplification of the legal process is achieved by assuming (i) the presence of perfect information, (ii) perfect monitoring and (iii) absence of legal failure. While perfect monitoring means that a violation of the trade agreement will always be detected by the harmed victim, the absence of legal failure means that the panel judges every violation to be a violation.
Linking First and Second Mover

The DSU states that “the level of the suspension of concessions or other obligations authorized by the DSB shall be equivalent to the level of the nullification or the impairment.”

While the exact method of calculating the level of nullification or impairment is left to the discretion of the ruling panel, legal practice is dominated by a counterfactual trade value approach. The trade value approach simply compares price times quantity of the traded good before and after the disputable trade measure. The difference between these two trade values is seen as the level of nullification or impairment suffered by the complainant. Or, in terms of the model at hand, the damage to the second mover.

The trade value of Home’s import good $tv_\tau$, is simply Home’s import demand times the equilibrium world market price: $tv_\tau := (D_x[p_\tau + \tau])\hat{p}_\tau$. Consequently, the change in the trade value due to an increase in Home’s import tariff is given by $\Delta tv_\tau := (D_x[p_\tau + \tau])\hat{p}_\tau - (D_x[p_\tau[0] + 0])\hat{p}_\tau[0]$. In this model the expression becomes:

$$\Delta tv_\tau = \frac{n\tau(-a(2 + 3n) + 2bn\tau)}{(2 + n)^2}$$  \hspace{1cm} (13)

The change in trade value of the foreign import good $\Delta tv_y[\tau^*]$ is obtained by similar means:

$$\Delta tv_y[\tau^*] := (D_y[p_\tau[\tau^*] + \tau^*])\hat{p}_\tau[\tau^*] - (D_y[p_\tau[0] + 0])\hat{p}_\tau[0]$. For the example at hand this expression becomes:

$$\Delta tv_y[\tau^*] = \frac{1}{9}\tau^*(-5a + 2b\tau^*) \hspace{1cm} (14)$$

The equivalence condition cited above requires that the retaliative distortion of the trade value has to be less than or equal to the distortion that was caused by the initial violation. This condition holds if $\Delta tv_y[\tau^*] \leq \Delta tv_\tau$. Solving this expression for $\tau^*$ yields Foreign’s maximum retaliative tariff as a function of Home’s violative tariff $\tau$ and the market size ratio.

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18DSU Article 22, para 4.
19See [Jordan, 2005], pages 119-124 for a discussion of the employed calculation methods. The dominating method used in this paper was employed for example in the following cases: WT/DS26 EC-Hormones, WT/DS27 EC-Bananas, WT/DS160 US-Copyright.
n. Let this equivalence restriction on Foreign’s retaliative tariff be denoted by $\tau^{\ast}_{eq}$:

$$
\tau^{\ast}_{eq}[\tau, n] = \frac{5a(2 + n) - \sqrt{25a^2(2 + n)^2 - 72abn(2 + 3n)\tau + 144b^2n^2\tau^2}}{4b(2 + n)}
$$

(15)

The Dispute Settlement System’s equivalence condition thus creates a strategic link between Home’s violative tariff on imports of good $x$ and the Foreign’s retaliative tariff on imports of good $y$.

3 Equilibrium Analysis

Due to the assumption of perfect information the subgame perfect equilibrium tariffs are found by backward induction, starting with Foreign as the second mover.

3.1 The Second Mover’s Equilibrium Strategy

For a given violation of the initial free trade agreement (i.e. $\tau > 0$) Foreign has to make two decisions. First, how much to retaliate within the permitted interval $0 \leq \tau^{\ast}_{r} \leq \tau^{\ast}_{eq}$. Second, whether or not to file a complaint at costs $c$ in order to be entitled to retaliate with a retaliative tariff $\tau^{\ast}_{r}$.

3.1.1 The Optimal Retaliative Tariff

Earlier calculations have shown that Foreign would maximize its welfare by setting its optimal tariff $\tau^{\ast}_{o} = \frac{a}{b}$ if it faced an unrestricted optimization problem.\(^{20}\) However, if the equivalence condition restricts Foreign’s retaliation to a level below $\tau^{\ast}_{o}$, Foreign will completely exploit the admissible retaliation tariff and set its retaliative tariff $\tau^{\ast}_{r}$ equal to $\tau^{\ast}_{eq}[\tau, n]$. In short, Foreign’s retaliative tariff $\tau^{\ast}_{r}$ is given by:

$$
\tau^{\ast}_{r}[\tau, n] = \min\{\tau^{\ast}_{o}, \tau^{\ast}_{eq}[\tau, n]\}
$$

(16)

\(^{20}\)Since Foreign’s welfare is a continuous function of its import tariff $\tau^{\ast}$, which is strictly increasing on the interval between zero and $\tau^{\ast}_{o}$, it follows that Foreign’s welfare-maximizing retaliative tariff $\tau^{\ast}_{r}$ has an upper bound at its optimal tariff $\tau^{\ast}_{o}$. 
3.1.2 To Retaliate or not to Retaliate

After the extent of Foreign’s retaliation has been determined, the question of whether or not Foreign will retaliate at all remains to be analyzed.

Necessary Condition for Retaliation

Since Foreign is an importer of good $y$, the analysis of Foreign’s retaliation decision and Foreign’s associated possible welfare gains can be restricted to sector $y$. Foreign will retaliate whenever the welfare gain in sector $y$ due to retaliation is higher than litigation costs (i.e. $\hat{w}_y^*[\tau^* | \tau, n] - \hat{w}_y^*[0] > c$ has to hold). Since the maximum achievable welfare gain in sector $y$ is realized when Foreign implements $\tau^*_o$ as its retaliative tariff, it follows that litigation costs are prohibitively high if $c \geq \hat{w}_y^*[\tau^*_o] - \hat{w}_y^*[0]$ holds. This condition states that litigation costs are prohibitive whenever welfare from complaining and retaliating is lower than welfare from doing nothing, even though the complainant is entitled to set its optimal tariff. The consequence of such prohibitively high litigation costs would be a breakdown of the strategic link between Home’s and Foreign’s actions. Therefore, the remainder of the analysis focuses on the case of non-prohibitive costs, such that $c < c_p$ holds, where $c_p$ stands for prohibitive costs. Note that the prohibitive level of litigation costs is independent of market size in the current model. Since the market size of Foreign is normalized to one, $c_p$ is a constant and it is possible to express litigation costs more conveniently as a fraction of prohibitive costs. Define $c := \gamma c_p$, then $\gamma = \frac{c}{c_p}$ displays present costs as a fraction of prohibitive costs. It follows that $\gamma < 1$ is a necessary condition for Foreign to retaliate.

Sufficient Condition for Retaliation

While Foreign’s litigation costs are exogenously determined, the admissible level of Foreign’s retaliative tariff $\tau^*_eq[\tau, n]$ depends positively upon the market size ratio $n$ and the level of Home’s initial violation $\tau$. In other words, the larger the offending country’s market relative to the offended country’s market and the more severe the offense, the higher will be the level

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21 Due to perfect information, Home anticipates that Foreign is not retaliating when costs are prohibitive. Therefore, Home would always play its optimal tariff while Foreign would never retaliate.

22 In the model at hand $c_p$ is given by $c_p = \frac{\alpha^2}{\tau^* n}$. 

10
of permitted retaliation according to the equivalence condition.\textsuperscript{23} As a consequence, there will be a vector of combinations of $\gamma$, $n$ and $\tau$ that leads Foreign to be indifferent between retaliating and not retaliating. Since the model has tariffs as strategic instruments, it is convenient to express the locus of Foreign’s indifference in terms of Home’s tariff $\tau$. Setting Foreign’s welfare gain from retaliation equal to litigation costs ($c = \hat{w}_g^*[\tau, n] - \hat{w}_g^*[0]$), one can solve for Home’s tariff, that leads Foreign to be indifferent between retaliating and not retaliating, as a function of $\gamma$ and $n$. This indifference-inducing tariff of Home is denoted as $\tau_i[\gamma, n]$ in the following.

$$
\tau_i[\gamma, n] = \frac{a(12 + 18n - \sqrt{18(4 + n(20 + 17n)) + 18(2 + n)^2\sqrt{1 - \gamma - (2 + n)^2\gamma})}}{24bn}
$$

The $n$-$\tau$-space in Figure 1 is intersected by two indifference curves. The upper curve represents the case of prohibitive costs (i.e. $\gamma_1 = 1$). The lower curve represents a case of $\gamma < 1$. Thus, the $n$-$\tau$-space can be separated into a northeastern set of locations where Foreign will retaliate (i.e. $\tau > \tau_i[\gamma, n]$) and a southwestern set of locations, where Foreign will not retaliate.\footnote{Formally the benefit from retaliating is increasing in the market size of the offender ($\frac{\partial \hat{w}_g^*[\tau, n]}{\partial n} > 0$) and increasing in the severity of the offense ($\frac{\partial \hat{w}_g^*[\tau, n]}{\partial \tau} > 0$), for any given non-prohibitive level of litigation costs if $\tau_{eq}^*[\tau, n] < \tau_g^*$ holds.}

Figure 1:
retaliate (i.e. \( \tau \leq \tau_i[\gamma, n] \)).

The figure reveals that Foreign’s retaliation threshold is lower, the lower the level of litigation costs. It also shows that \( n \) and \( \tau \) are “substitutes” from the perspective of Foreign, who is eventually interested in the level of admissible retaliation. In other words, a Home country with a small market, raising its import tariff steeply, could result in the same \( \Delta \tau \) (which translates into the admissible retaliation tariff) as a Home country with a large market which raises its import tariff only slightly.

3.1.3 Intermediate Results
For non-prohibitive costs, Foreign’s best response tariff \( \hat{\tau}^* \) is given by:

\[
\hat{\tau}^* = \begin{cases} 
0, & \text{iff } \tau \leq \tau_i[\gamma, n] \\
\tau^*_r[n, \tau], & \text{iff } \tau > \tau_i[\gamma, n]
\end{cases}
\]  

(17)

3.2 The First Mover’s Equilibrium Strategy
3.2.1 General Considerations
Home sets its tariff, anticipating the consequences of doing so in terms of whether or not there will be any retaliation and in terms of the extent of a possible retaliation. Note that Home’s welfare as a function of its import tariff \( \tau \) is no longer a continuous function, not even for the set of non-prohibitive tariffs. Home’s welfare will now have a step at the point where Foreign switches between retaliating and not retaliating due to an incremental increase in Home’s offense. Therefore, one has to distinguish between two cases, depending on whether Foreign retaliates or not. In the following, offenses triggering retaliation (i.e. \( \tau > \tau_i[\gamma, n] \)) will be referred to as major offenses, while smaller levels of violation which do not trigger retaliation (i.e. \( 0 < \tau \leq \tau_i[\gamma, n] \)) will be referred to as minor offenses.

Given Foreign retaliates with its retaliative tariff \( \tau^*_r[\tau, n] \), this will decrease Home’s welfare in its exporting sector \( y \). Therefore, Home will raise its own import tariff only as long as the marginal benefit accruing in sector \( x \) is larger than the marginal loss in sector \( y \) due to foreign retaliation. Home’s welfare, given Foreign retaliates, is found by substituting
Foreign’s retaliative tariff $\tau^*_r[\tau, n] = \min\{\tau^*_o, \tau^*_eq[\tau, n]\}$ into Home’s welfare function:

$$
\hat{w}[\tau, n] = \hat{w}_x[\tau, n] + \begin{cases} 
\hat{w}_y[\tau^*_o], & \text{iff } \tau^*_eq[\tau, n] > \tau^*_o \\
\hat{w}_y[\tau^*_eq[\tau, n]], & \text{iff } \tau^*_eq[\tau, n] \leq \tau^*_o
\end{cases}
$$

(18)

The first case can be ruled out to occur for $n < 1$. The welfare-maximizing tariff is denoted by $\tau_{ma}[n]$ in the following. $\tau_{ma}[n]$ can be shown to exhibit the following properties:

$$
\tau_{ma}[n] = \begin{cases} 
< 0, & \text{iff } n < 1 \\
= 0, & \text{iff } n = 1 \\
> 0, & \text{iff } n > 1
\end{cases}
$$

(19)

The basic message from this result is that it does not pay for a country to commit a major offense against a country with a larger import market. This result can be explained by the fact that the global deadweight loss, arising from the trade war, is split unevenly between the two countries, with the smaller country bearing the larger part of it.

### 3.2.2 Identifying Sets of Dominated Strategies

Consider Figure 2. The bold indifference curve represents $\tau_i[\gamma, n]$ for prohibitive costs (i.e. $\gamma_1$), while the thin indifference curve represents $\gamma < 1$. The dashed upward sloping curve depicts Home’s optimal tariff.

I. Clearly all combinations of $\tau$ and $n$ located above Home’s optimal tariff can be excluded from further analysis for the simple reason that the choice of all these locations is strictly dominated by choosing $\tau_o[n]$.

II. There is a second strictly dominated set of tariffs, which can be excluded from further analysis as well. Consider those cases where $\tau < \tau_o[n] \land \tau < \tau_i[\gamma, n]$. For all tariffs located in

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24The case of $\tau^*_eq[\tau, n] > \tau^*_o$ implies that the distortion in trade value due to Home’s initial offense has to be greater than the distortion in trade value that would result from foreign retaliation, even if Foreign plays its optimal tariff, which is $\tau^*_o$. Suppose for the moment that the market size ratio is smaller than unity. Then Home’s optimal tariff which is $\tau_o[n] = \frac{an}{1+n}$ would fall short of Foreign’s optimal tariff. But in order to cause a trade value distortion that translates into a foreign tariff of at least $\frac{an}{1+n}$, Home would have to raise its tariff above its optimal tariff, which is a strictly dominated strategy.

25The subscript $ma$ should remind the reader of the fact that this tariff is associated with a major offense.

26See Mathematical Appendix 6.3.
this set Home could raise its tariff, thereby getting closer to its optimal tariff, without any negative effects since Foreign would only retaliate if the retaliation threshold was exceeded. Hence this set of tariffs is strictly dominated by playing $\tau_i[\gamma, n]$.

III. Yet another set of tariffs is strictly dominated. Consider the set of tariffs where $\tau < \tau_o[n] \land \tau > \tau_i[\gamma_1, n]$ and recall that $\tau_i[\gamma_1, n]$ is the set of $n$-$\tau$-combinations that entitles Foreign to retaliate exactly with its optimal tariff $\tau^*_o = \frac{a}{b}$. Hence, any $n$-$\tau$-combinations located above $\tau_i[\gamma_1, n]$ trigger the same amount of retaliation since Foreign’s maximum retaliative capacity is already exhausted. While triggering the same punishment, these $n$-$\tau$-combinations increase Home’s welfare the more, the closer they are to its optimal tariff $\tau_o[n]$. Therefore, all these $n$-$\tau$-combinations are strictly dominated by playing $\tau_o[n]$.

3.2.3 Best Responses

Best Response for $n \leq 1$

Home would choose to play its optimal tariff $\tau_o[n]$ up to the market size of $n_{oi}[\gamma]$,27 which corresponds to the point labeled A. Home countries with markets larger than $n_{oi}[\gamma]$ but still

---

27The subscript “oi” should remind the reader of the fact that $n_{oi}$ denotes the critical market size where Home switches from playing $\tau_o[n]$ to playing $\tau_i[\gamma, n]$. The existence and the properties of this lower switching point $n_{oi}[\gamma]$ are examined in the Mathematical Appendix 6.4.
smaller than unity will choose to play $\tau_i[\gamma, n]$.

Note for the moment that the smallest countries (i.e. $n \leq n_{oi}[\gamma]$) can play their optimal tariff without harming their trading partners enough to trigger a complaint, while slightly larger countries (i.e. $n > n_{oi}[\gamma]$), still being smaller than their trading partners, have to discipline their offenses to a level below their optimal tariff in order not to exceed the retaliation threshold $\tau_i[\gamma, n]$, since committing major offenses has been shown to be a strictly dominated strategy for $n < 1$.

Best Response for $n > 1$

In those cases where Home’s market is larger than Foreign’s (i.e. $n > 1$), the best response function is obtained by a somewhat more complex analysis than for the cases of $n \leq 1$, because now the option of committing a major offense may be profitable for Home. After having identified three strictly dominated sets of tariffs for $n > 1$ in the preceding paragraphs, one has to analyze whether Home’s best response will be either to choose its tariff to equal

1. its optimal tariff $\tau_o[n]$,
2. the current retaliation threshold $\tau_i[\gamma, n]$ or
3. some tariff $\tau_{ma}[n]$ between $\tau_i[\gamma, n]$ and $\tau_i[\gamma_1, n]$.

Note that option 1 will trigger fixed retaliation of $\tau_o^* = \frac{a}{b}$, while option 2 will trigger no retaliation at all, and option 3 will trigger retaliation of $\tau_{eq}[\tau, n]$, which is elastic in the magnitude of the initial offense.

Welfare from option 1 will be denoted by $\hat{w}_o[n]$.\textsuperscript{28} It is obtained by substituting $\tau_o[n]$ for $\tau$ and $\tau_o^*$ for $\tau^*$ into Home’s welfare function:

$$\hat{w}_o[n] := \hat{w}_x[\tau_o[n], n] + \hat{w}_y[\tau_o^*]$$

Welfare from option 2 will be denoted by $\hat{w}_i[\gamma, n]$. It is obtained by substituting $\tau_i[\gamma, n]$ for

\textsuperscript{28}For $\hat{w}_o[n]$, it can be shown that $\frac{\partial \hat{w}_o[n]}{\partial n} > 0$ and $\frac{\partial^2 \hat{w}_o[n]}{\partial^2 n} < 0$. See Mathematical Appendix 6.5.
τ and 0 for τ∗ into Home’s welfare function:

\[
\hat{w}_i[\gamma, n] := \hat{w}_x[\tau_i[\gamma, n], n] + \hat{w}_y[0]
\] (21)

Welfare from option 3 will be denoted by \(\hat{w}_{ma}[n]\). It is obtained by substituting \(\tau_{ma}[n]\) for \(\tau\) and \(\tau_{eq}^*[\tau_{ma}[n], n]\) for \(\tau^*\) into Home’s welfare function:

\[
\hat{w}_{ma}[n] := \hat{w}_x[\tau_{ma}[n]] + \hat{w}_y[\tau_{eq}^*[\tau_{ma}[n], n]]
\] (22)

Home’s welfare under these three alternative strategies is depicted in Figure 3. The dashed curve represents \(\hat{w}_o[n]\), which is Home’s welfare when both Home and Foreign play their optimal tariffs. The dotted curve represents \(\hat{w}_{ma}[n]\), which is Home’s welfare from committing an offense given Foreign retaliates elastically. The three continuous curves represent \(\hat{w}_i[\gamma, n]\) for different cost-levels. The upper bold continuous curve is associated with prohibitive costs (i.e. \(\gamma_1\)). The lower bold continuous curve is associated with zero costs (i.e. \(\gamma_0 = 0\)), while the finer continuous curve in the middle represents intermediate costs of \(0 < \gamma < 1\).

Suppose for the moment that costs were fixed at some level where \(0 < \gamma < 1\). Then Home’s best response depends solely on its size. Home countries being only slightly larger than Foreign (\(n < n_{io}[\gamma]\)) would avoid any retaliation and violate the agreement only by \(\tau_i[\gamma, n]\). This can be seen from Figure 3 since for Home countries being smaller than \(n_{io}[\gamma]\) the fine continuous curve yields the highest welfare level. Home countries being sufficiently large (i.e. \(n > n_{io}[\gamma]\)) will play their optimal tariff and take Foreign’s retaliation into account.

The economic reason for this behavior can be explained by considering the right hand side of Figure 2 (i.e. \(n > 1\)) again. Note that the gap between \(\tau_i[\gamma, n]\) and \(\tau_o[n]\) widens with increasing market size. This means that the opportunity cost of playing the threshold tariff \(\tau_i[\gamma, n]\) is increasing in \(n\) since \(\tau_i[\gamma, n]\) is decreasing in \(n\) while \(\tau_o[n]\) is increasing in \(n\).

Consequently, there is a switching point in terms of \(n\) where Home’s opportunity costs of

29Earlier it was argued that it is a dominant strategy for Home to play its optimal tariff \(\tau_o[n]\) given that Foreign already plays its optimal tariff \(\tau^*\). Therefore, the case in which Home plays \(\tau_{ma}[n]\) given that Foreign plays \(\tau^*_o\) can be excluded from the analysis.

30Note that costs are a shift parameter of \(\hat{w}_i[\gamma, n]\), while \(\hat{w}_o[n]\) and \(\hat{w}_{ma}[n]\) are independent of costs.

31The subscript “io” should remind the reader of the fact that \(n_{io}\) denotes the critical country size where Home switches from playing \(\tau_i[\gamma, n]\) to playing \(\tau_o[n]\).
avoiding retaliation will equal Home’s costs from taking retaliation into account. At this point Home will switch from playing \( \tau_i[\gamma, n] \) to playing \( \tau_o[n] \).\(^{32}\)

Due to the assumption of non-negative and non-prohibitive costs, the location of this higher switching point will always lie between the fixed values of \( n_{io}[\gamma_0] = 1.38504 \) and \( n_{io}[\gamma_1] = 2.46187 \).\(^{33}\)

Figure 3 already suggests that playing \( \tau_{ma}[n] \) will be an inferior choice for most levels of litigation costs. Since the affected set of \( n-\gamma \)-combinations is very small and the implemented tariff level \( \tau_{ma}[n] \) as well as the associated welfare level \( \hat{w}_{ma}[n] \) are extremely close to \( \tau_i[\gamma, n] \) and \( \hat{w}_i[\gamma, n] \) in this particular region, further analysis of this option is omitted.\(^{34}\)

\(^{32}\)The existence and the properties of this higher switching point \( n_{io}[\gamma] \) are examined in the Mathematical Appendix 6.7.

\(^{33}\)The numerical value of \( n_{io}[\gamma_0] \) is obtained by setting \( \hat{w}_o[n] \) equal to \( \hat{w}_i[\gamma_0, n] \) and solving for \( n \). The numerical value of \( n_{io}[\gamma_1] \) is obtained by setting \( \hat{w}_o[n] \) equal to \( \hat{w}_i[\gamma_1, n] \) and solving for \( n \).

\(^{34}\)For the sake of completeness it has to be stated that the first mover will only play \( \tau_{ma}[n] \) if it holds both that \( \gamma \leq 0.03086 \) and \( 1 < n \leq 1.40231 \). See Mathematical Appendix 6.6.
3.2.4 Intermediate Results

Home’s best response $\hat{\tau}$ is given by:

$$\hat{\tau} = \begin{cases} 
\tau_o[n], & \text{if } n > n_{io}[\gamma] \\
\tau_i[\gamma, n], & \text{iff } n_{oi}[\gamma] < n \leq n_{io}[\gamma] \\
\tau_o[n], & \text{if } n \leq n_{oi}[\gamma]
\end{cases}$$

(23)

Stated verbally:

1. The biggest Home countries will play their optimal tariffs and take Foreign’s retaliation into account.
2. Home countries of intermediate market size will restrict their tariff to a level below their optimal tariff in order to avoid retaliation by bothering Foreign no more than the latter’s tolerance level.
3. The smallest Home countries will play their optimal tariff because they do not cause enough damage to trigger retaliation.

3.3 Equilibria

Both Home’s and Foreign’s best response functions are conditional on $n$ and the level of litigation costs. Therefore the pair of subgame perfect Nash equilibrium tariffs ($\hat{\tau}; \hat{\tau}^*$) is dependent upon the exogenously determined levels of $\gamma$ and $n$. Figure 4 shows that the $\gamma$-$n$-space is divided into three large and one negligible small area of different equilibria. The grey area in the northwest of Figure 4 represents a trade war between the two countries, where each country is playing its optimal tariff. This type of equilibrium occurs predominantly if Home is large enough to put up with Foreign’s retaliation. It is bordered below by $n_{io}[\gamma]$.

The white area in the center of Figure 4 represents the equilibria, in which one country bothers the other country just so much that retaliation is avoided. The economic intuition for the existence of this type of equilibrium is that either Home countries are too small to be willing to put up with retaliation, or Home’s opportunity costs of a minor offense are

\[\text{See preceding footnote.}\]

\[\text{The opportunity costs of a minor offense are Home’s forgone benefits from a tariff increase to } \tau_o[n].\]
relatively low, which is the case if litigation costs are relatively high. This type of equilibrium is bordered above by $n_{o}[\gamma]$ and below by $n_{o}[\gamma]$. Note that both afore-mentioned types of equilibria only exist for non-prohibitive costs. The striped area, which stretches at the bottom and along the right edge of Figure 4 represents the set of equilibria where Home plays its optimal tariff, while Foreign does not retaliate. This type of equilibrium occurs if either Home’s market is so small that Foreign is not harmed enough in order to be willing to pay litigation costs (the cases at the bottom) or costs are prohibitive (the cases at the right edge where $\gamma \geq 1$ holds).

### 3.4 Comparative Statics in Litigation Costs

After having computed the Nash equilibrium tariff pairs as functions of country size and litigation costs, it is possible to finally analyze the effects of a reduction of litigation costs by consulting Figure 4 again. It is useful to distinguish between a cost reduction that passes the threshold of prohibitive costs on the one hand and a cost reduction that occurs within the range of non-prohibitive costs on the other hand.
3.4.1 Prohibitive Initial Costs

Consider the case where initial litigation costs are prohibitive (i.e. \( \gamma \geq 1 \)). Then the initial equilibrium tariff pair is given by \((\tau_o[n]; 0)\), with the Home playing its optimal tariff and Foreign not retaliating at all. The effects of a reduction of litigation costs to a level just an increment below the prohibitive threshold of \( \gamma = 1 \) are dependent upon the pertinent level of \( n \).

The tariff of a large Home country with \( n > n_{io}[\gamma] \) is left unchanged, although Foreign implements retaliation of \( \tau_o^* \).

In the case of an intermediate size Home country with \( n_{oi}[\gamma] < n \leq n_{io}[\gamma] \) compliance is improved since the post shock tariff pair is \((\tau_i[\gamma, n]; 0)\).

In the case of a small Home country with \( n \leq n_{oi}[\gamma] \) both countries’ tariffs and welfare levels are left unchanged.

3.4.2 Non-prohibitive Initial Costs

Now consider the case where initial non-prohibitive litigation costs (i.e. \( \gamma < 1 \)) are further reduced.

For high values of \( n \), where the initial set of equilibrium tariffs is \((\tau_o[n]; \tau_o^*)\), a reduction of litigation costs will have no effect at all, and the equilibrium does not change.

Suppose the initial equilibrium set of tariffs was \((\tau_i[\gamma, n]; 0)\), which corresponds to any location inside the white area in the center of Figure 4. In this case the effects depend even further on \( n \). If \( n \leq n_{io}[\gamma_0] \), the reduction in litigation costs does not change the equilibrium strategies as such since the post shock equilibrium strategies are again \((\tau_i[\gamma, n]; 0)\).

Nevertheless, Home will set a lower tariff because the absolute level of \( \tau_i[\gamma, n] \) has been reduced in the course of the cost reduction. However, if \( n > n_{io}[\gamma_0] \), the cost reduction may change the equilibrium, such that Home commits a more severe offense by switching to its optimal tariff \( \tau_o[n] \) thereby triggering retaliation of Foreign, who switches to its own optimal tariff \( \tau_o^* \). The finding that a reduction of litigation costs may lead to more severe offenses, although the cost reduction succeeds in rendering retaliation more attractive, might seem

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37 Recall that \( n_{io}[\gamma_0] \) is equal to 1.38504 and therefore independent of any values of parameters and variables.

38 See preceding footnote.
paradoxical at first sight, but it becomes clear upon closer investigation.\textsuperscript{39} Note that this paradoxical effect only occurs for offenders with markets of larger size than the ones of their victims (i.e. $n_{io[\gamma_0]} = 1.38504 < n \leq 2.46187 = n_{io[\gamma_1]}$).

Suppose the initial equilibrium set of tariffs was $(\tau_o[n]; 0)$, which corresponds to the striped area at the bottom of Figure 4. In this case a reduction of costs improves the compliance of Home, who switches from playing $\tau_o[n]$ to playing $\tau_i[\gamma, n]$, while Foreign’s tariff remains at zero. Thus, the reduction of litigation costs may succeed in forcing countries into compliance by rendering retaliation more attractive. Note that this intuitive effect only occurs for offenders being smaller than their victims (i.e. $n \leq 1$).

3.5 Key Findings of the Basic Model

The model’s predictions suggest that the current DSS does not succeed in protecting small countries’ trade interests against large countries’ offenses. One may call this an institutional bias of the system.

Moreover, a reduction of litigation costs has been found to improve small countries’ compliance, while it entices even more large countries than before to commit major offenses. Consequently, large countries’ trade interests would be protected even better from small countries’ offenses, while small countries would suffer from more severe offenses than before. Hence, a subsidization of litigation costs is supposed to worsen the system’s institutional bias.

4 Extension

4.1 Rationale and Model Adaptations

In order to analyze if the results of the first model are robust to variations, this subsection models the asymmetry of the two countries in a different way, while the structure of the

\textsuperscript{39}The reduction of litigation costs initially affects Foreign’s decision by lowering the tolerated level of violation (i.e. lowering $\tau_i[\gamma, n]$). Consequently, Home’s opportunity costs of a minor offense increase since the gap between its optimal tariff $\tau_o[n]$ and the retaliation threshold widens. At some point the welfare gain, which is associated with this tariff gap, exceeds the welfare loss that would arise in the course of provoked retaliation. If litigation costs are reduced below that point, Home will switch from committing a minor offense to committing a major offense.
analysis remains unchanged. Throughout this section the emphasis is put on highlighting the crucial differences that result from the changed specifications.

Suppose the representative consumers’ quasilinear utility functions were identical in both countries.\footnote{Let utility for a representative consumer be given by: $U[x, y, z] = U^*[x, y, z] = z + (ax - \frac{x^2}{2})\frac{1}{b} + (ay - \frac{y^2}{2})\frac{1}{b}$. Again trade is balanced via the numeraire good $z$.} Suppose further that Foreign has one consumer while Home has $n$ identical consumers. Consequently demand at Home is $n$ times foreign demand in both sectors. Demand at Home is then given by:

$$D_x[p_x] := (a - bp_x)n$$

$$D_y[p_y] := (a - bp_y)n$$

Foreign’s demand is given by:

$$D^*_x[p_x] := a - bp_x$$

$$D^*_y[p_y] := a - bp_y$$

Again Foreign supplies only good $x$ while Home supplies only good $y$.

$$S^*_x[p_x] := bp_x$$

$$S^*_y[p_y] := bp_y$$

Equilibrium prices, quantities, welfare levels and optimal tariffs are obtained in an analogous manner to the calculations conducted in the first model. However, unlike before, Foreign’s welfare in sector $y$, which is denoted by $\hat{w}^*_y[\tau^*_o, n]$, has become a function of the country size ratio $n$. Consequently Foreign’s optimal tariff $\tau^*_o[n]$ has become a function of $n$ as well. It is given by: $\tau^*_o[n] = \frac{a}{b(3 + 4n + n^2)}$. Note that Foreign’s optimal tariff now clearly decreases in $n$, since Foreign’s ability to influence world market prices and hence its ability to generate terms of trade gains deteriorates with increasing $n$.

The rules of the tariff setting game and the modeling of the WTO’s Equivalence Condition remain unchanged.
4.2 The Second Mover’s Equilibrium Strategy

4.2.1 The Optimal Retaliative Tariff

Again Foreign’s welfare is a continuous function of its import tariff $\tau^*_o$, which is positive and strictly increasing on the interval between zero and $\tau^*_o[n]$ for $n < \infty$. Thus, Foreign’s retaliative tariff $\tau^*_r$ is given by $\tau^*_r[\tau, n] = \min\{\tau^*_o[n], \tau^*_e[\tau, n]\}$. 

4.2.2 To Retaliate or not to Retaliate

Necessary Condition for Retaliation

Litigation costs are prohibitive if $c \geq \hat{w}_y^*[\tau^*_o[n]] - \hat{w}_y^*[0]$ is satisfied. Substituting explicit values for $\hat{w}_y^*[\tau^*_o[n]]$ and $\hat{w}_y^*[0]$ yields prohibitive costs $c_p$ as a function of $n$:

$$c_p[n_p] = \frac{a^2}{2b(2+n_p)^2(3+4n_p+n_p^2)}$$

(30)

The subscript $p$ is appended to the country size parameter $n$ in order to be able to identify the cases where costs are prohibitive in terms of country size.\textsuperscript{41} Equation 30 reveals that an increase in litigation costs leads to a decrease of the threshold where costs have a prohibitive effect in terms of country size (i.e. $\frac{\partial c_p[n_p]}{\partial n_p} < 0$). Since $c_p[n_p]$ is a continuous and monotonically decreasing function, it holds that $n < n_p$ is a necessary condition for retaliation.\textsuperscript{42}

Sufficient Condition for Retaliation

Foreign will only retaliate if the welfare gain associated with the implementation of its retaliative tariff $\tau^*_r[\tau, n]$ exceeds litigation costs. Thus there will be a vector of combinations of $\tau$, $n$ and $n_p$ which leads Foreign to be indifferent between retaliating and not retaliating. The set of these indifference inducing combinations can be found in terms of Home’s tariff $\tau$. The resulting tariff $\tau_i[n_p, n]$ is again a function of costs (already expressed in terms of

\textsuperscript{41} If e.g. $n_p = 2$ Foreign would not complain against offenses committed by countries of size $n \geq 2$, no matter how severe the offenses may be.

\textsuperscript{42} For $c_p[n_p]$ the following properties can be shown to hold:

$$c_p[n_p] = \begin{cases} < c_p[n], & \text{if } n_p > n \\ = c_p[n], & \text{if } n_p = n \\ > c_p[n], & \text{if } n_p < n \end{cases}$$

23
the prohibitive country size ratio \( n_p \) and country size. Figure 5 illustrates that the thin

![Figure 5:](image)

hook-shaped \( \tau_i[n_p, n] \)-curve only runs up to the level of \( n \) where \( n = n_p \), since \( \tau_i[n_p, n] \) does not exist for prohibitive costs (i.e. \( n \geq n_p \)). This indifference curve separates the \( n-\tau \)-space into two different strategic sections. Combinations of \( \tau \) and \( n \) lying to the southwest (i.e. low \( \tau \) and low \( n \)) or to the east (i.e. \( n \geq n_p \)) of the curve will not trigger foreign retaliation, whereas combinations of \( \tau \) and \( n \) lying above the curve will trigger foreign retaliation.

The bold downward sloping curve labeled \( \tau[n] \) represents all combinations in the \( n-\tau \)-space where the permitted retaliative tariff \( \tau^{eq}_i[\tau, n] \) equals Foreign’s optimal tariff \( \tau^*_i[n] \). Economically this means that Foreign’s retaliation is inelastic in Home’s initial violation for combinations of \( n \) and \( \tau \) that lie above the \( \tau[n] \)-curve, since Foreign will never retaliate with a tariff that is higher than its optimal tariff.

\[^{43}\text{Analytically } \tau[n] \text{ is found by setting } \tau^{eq}_i[\tau, n] \text{ equal to } \tau^*_i[n] \text{ and solving for } \tau.\]

24
4.3 The First Mover’s Equilibrium Strategy

4.3.1 General Considerations

The perfectly informed Home country decides between committing a minor offense (i.e. \( \tau \leq \tau_i[n_p, n] \)), which does not trigger retaliation, and a major offense (i.e. \( \tau > \tau_i[n_p, n] \)), which does trigger retaliation.44

Similarly to the calculations in the first model it can be shown to hold as well in this model that it does not pay for a country to commit a major offense against a larger country.45

4.3.2 Identifying Sets of Dominated Strategies

Consider Figure 6 in order to identify sets of strictly dominated strategies.

\[ \text{Figure 6:} \]

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44Note that now \( \tau_i[n_p, n] \) does not exist for \( n > n_p \), since costs are prohibitive in these cases. Therefore it seems reasonable to count as well those violative tariffs as major offenses, where Home plays its optimal tariff because costs are prohibitive.

45Again Home’s welfare, given Foreign retaliates, is found by substituting Foreign’s retaliative tariff \( \tau^*_r[\tau, n] = \tau^*_r[\tau, n] - \min\{\tau^*_o[n], \tau^*_eq[\tau, n]\} \) into Home’s welfare function:

\[
\hat{w}[\tau, n] = \hat{w}_e[\tau, n] + \begin{cases} \hat{w}_y[\tau^*_o[n], n], & \text{if } \tau^*_o[\tau, n] > \tau^*_o[n] \\ \hat{w}_y[\tau^*_eq[\tau, n], n], & \text{if } \tau^*_eq[\tau, n] \leq \tau^*_o[n] \end{cases}
\]

It holds as well in this model that the first case (i.e. \( \tau^*_eq[\tau, n] > \tau^*_o[n] \)) can be ruled out to occur for \( n \leq 1 \).
I. Clearly all tariffs above the optimal tariff are strictly dominated by setting the optimal tariff.

II. Moreover, all tariffs below \( \tau_i[n_p, n] \) are dominated by setting a tariff of \( \min\{\tau_o[n], \tau_i[n_p, n]\} \).

III. Combinations of \( n \) and \( \tau \) that lie within the wedge shaped area to the right of point B are strictly dominated by setting the optimal tariff.

**Best Response for \( n \leq 1 \)**

Since it does not pay for a Home country of size smaller than unity to commit a major offense, Home’s choice will be a tariff \( \tau \leq \tau_i[n_p, n] \). As Figure 6 shows there is again the opportunity for Home to play its optimal tariff \( \tau_o[n] \) without triggering retaliation as long as Home is smaller than \( n_{oi}[n_p] \). Home countries of greater size, but still smaller than unity will play \( \tau_i[n_p, n] \) in order not to trigger retaliation.\(^{46}\) This lower switching point \( n_{oi}[n_p] \) can be shown to exhibit qualitatively the same properties of its counterpart in the simple model (i.e. \( \frac{\partial n_{oi}[n_p]}{\partial n_p} < 0 \)).\(^{47}\)

**Best Response for \( n > 1 \)**

If Home is larger than Foreign, the best response function again consists of three possible tariffs which have not yet been shown to be dominated by another tariff. Similar to the first model the three remaining sets of Home’s tariffs are

1. its optimal tariff \( \tau_o[n] \),
2. the current retaliation threshold \( \tau_i[n_p, n] \) and
3. \( \tau_{ma}[n] \) lying in between \( \tau_i[n_p, n] \) and \( \tau[n] \).

Assuming non prohibitive costs, the point \( n_{oi}[n_p] \) where Home switches from committing a minor offense to committing a major offense can be derived along the lines of the calculations in the previous model.\(^{48}\) The paradoxical result that a reduction of litigation costs may

\(^{46}\) Mathematically the fundamental difference between the simple model and the current variation of the model lies in the fact there may be either (i) no switching point at all (this applies for values where \( n_p < 0.897 \)) or (ii) a single switching point (this applies for values where \( n_p > 1 \)) or (iii) two switching points (this applies for values where \( 0.897 \leq n_p \leq 1 \)). In the case of two switching points Home would actually switch its strategy twice with increasing \( n \) from zero to unity (first from \( \tau_o[n] \) to \( \tau_i[n_p, n] \) and then back to \( \tau_o[n] \)).

\(^{47}\) This property can be shown to hold in an analogous manner to the proceedings of the Mathematical Appendix 6.4.

\(^{48}\) Again the switching points between the three sections of Home’s best response function are obtained by substituting Home’s three possible offensive tariffs and Foreign’s associated retaliative tariffs pairwise into Home’s
lead even smaller countries than before to committing a major offense holds as well in this model.\textsuperscript{49} Just like before \( n_{io}[n_p] \) is bounded above (at \( n = 1.6025 \)) and below (at \( n = 1.2128 \)) at absolute levels of country size, while it is cost-elastic only between these boundaries. Consequently, countries of size \( n \leq 1.2128 \) will never play \( \tau_o[n] \), countries of size \( n > 1.6025 \) will always play \( \tau_o[n] \), while countries of size \( 1.2128 < n \leq 1.6025 \) will play either \( \tau_o[n] \) or \( \tau_i[n_p, n] \) depending upon the pertinent level of litigation costs.\textsuperscript{50}

### 4.4 Equilibria

Figure 7 shows the occurrence of three different subgame perfect Nash equilibrium tariff pairs \((\hat{\tau}; \hat{\tau}^*)\) in the \( n_{p}-n\)-space.\textsuperscript{51} The diagonal line starting at the origin, has a slope of one. It divides the \( n_{p}-n\)-space into one upper triangular shaped set, where \( n > n_p \) holds and one lower triangular shaped set, where \( n < n_p \) holds. Clearly all \( n_{p}-n\)-combinations in the upper set exhibit prohibitive costs, such that the equilibrium in the upper triangular is given by \((\tau_o[n]; 0))\). This tariff pair constitutes as well an equilibrium in the striped area lying below the 45-degree line and below the \( n_{io}[n_p]\)-curve. Although costs are not prohibitive in this area, the offense and therefore the permitted level of retaliation is not large enough to let Foreign break even with litigation costs.

The white area represents all combinations of \( n_p \) and \( n \) leading to an equilibrium tariff pair of \((\tau_i[n_p, n]; 0)\). This area is bordered below by \( n_{io}[n_p] \), above by \( n_{io}[n_p] \) and to the left by the condition of non-prohibitive costs (i.e. the 45-degree line).

These welfare functions are set equal to each other in a pairwise fashion. Solving for \( n \) then yields either an absolute value of \( n \) at the switching point or the value of \( n \) at the switching point as a function of \( n_p \) respectively. Setting \( \hat{w}_o[n] \) equal to \( \hat{w}_{ma}[n] \) yields the absolute value of \( n \) for which Home is indifferent between playing \( \tau_o[n] \) and \( \tau_{ma}[n] \). Its value is \( n = 1.2128 \). The values of \( n \) where Home is indifferent between playing \( \tau_i[n_p, n] \) on the one hand and playing \( \tau_o[n] \) or \( \tau_{ma}[n] \) on the other hand clearly have to depend upon costs and country size. Therefore the switching point \( n_{io}[n_p] \) is again obtained by setting \( \hat{w}_i[n_p, n] \) equal to \( \hat{w}_o[n] \) and solving this expression for \( n \).

\textsuperscript{49}Formally, \( \frac{\partial \hat{w}_{io}[n_p]}{\partial n} < 0 \) can be shown to hold in this model.

\textsuperscript{50}Again playing \( \tau_{ma}[n] \) will be dominated by playing one of the other two tariffs except for the occurrence of a very narrow range of country size ratios and costs. Consequently further analysis of this option is omitted for the same reasons as in the previous model. For the sake of completeness it can be shown that the Home will only play \( \tau_{ma}[n] \) if it holds both that \( n_p \geq 3.7480 \) and \( 1 < n \leq 1.2128 \).

\textsuperscript{51}Recall that a high (low) level of \( n_p \) corresponds to a low (high) level of litigation costs.
The upper grey area represents a trade war equilibrium with both countries playing their optimal tariffs. It is bordered below by $n_{io}[n_p]$ and to the left by the condition of non-prohibitive costs.

4.5 Comparative Statics in Litigation Costs

Again one has to distinguish between a cost reduction that passes the threshold of prohibitive costs and a cost reduction that occurs within the set of non-prohibitive costs.

4.5.1 Prohibitive Initial Costs

Consider the case where litigation costs are reduced from an initially prohibitive level (i.e. $n \geq n_p$) to a level lying an increment below this threshold. Then, similar to the findings of the first model, the consequences of the cost reduction depend upon the country size ratio. For large values of $n$ the cost reduction triggers a trade war (i.e. $(\tau_o[n]; \tau_o^*[n])$). For intermediate values of $n$ the cost reduction improves compliance (i.e. $(\tau_i[n_p, n]; 0)$), and for low values of $n$ the post shock tariff pair coincides with the initial tariff pair (i.e. $(\tau_o[n]; 0)$).
4.5.2 Non-prohibitive Initial Costs

Now consider the case where initial non-prohibitive litigation costs (i.e. \( n < n_p \)) are further reduced.

For high values of \( n \), where the initial equilibrium is a trade war (i.e. \((\tau_o[n]; \tau^*_o[n])\)), the cost reduction has no effect and the initial equilibrium does not change.

For intermediate values of \( n \), where the initial equilibrium is \((\tau_i[n_p, n]; 0)\), the effects of a reduction of litigation costs depend even further on the country size ratio. If \( n \leq 1.2128 \), the cost reduction does not change the equilibrium strategy. If \( n > 1.2128 \), a cost reduction may change the equilibrium in a paradoxical way, just as in the basic model.

Finally, if the initial set of tariffs is \((\tau_o[n]; 0)\), which corresponds to the striped area to the right of the 45-degree line, a cost reduction improves the compliance of Home, who switches from playing \( \tau_o[n] \) to playing \( \tau_i[n_p, n] \), while Foreign’s tariff remains at zero.

4.6 Key Findings of the Extended Model

While the basic model includes market power only in Home’s offensive sector (i.e. its import sector), the extension includes market power in both Home’s offensive (import) and Home’s defensive (export) sector. Moreover, it is constructed such that the answer to the question whether a particular level of litigation costs is prohibitive or not, depends upon the country size ratio.

Despite these differences, the results of the basic model have been shown to be qualitatively robust to the conducted change in the model’s specifications.

In particular, a subsidization of litigation costs has been shown to worsen the system’s bias as well under the alternative assumptions of the model extension.

5 Conclusion

The outcomes of both models suggest that the DSS is unable to level out existing power imbalances between countries and therefore does not provide equality before the law. This finding is based on the fact that a country’s ability to enforce a trade agreement under the rules of the DSS depends crucially upon the country’s retaliative capacity, which in turn is
country specific. Moreover, litigation costs have been found to be a key determinant of a
violated country’s decision whether or not to file a complaint. Since several DSS experts argue
that litigation costs are supposed to be higher for developing countries than for developed
countries, the former may face not only a disadvantage in terms of retaliative capacity but
as well in terms of absolute litigation costs.⁵²

The results have been employed to analyze the effects of a reduction of litigation costs.
The findings suggest that a reduction of litigation costs succeeds in improving smaller coun-
tries’ compliance, while it entices larger countries to commit more severe offenses.⁵³ Thus,
a subsidization of litigation costs is supposed to make smaller countries even worse off than
before, while large countries would enjoy a better protection of their trade interests against
smaller countries.

Besides, a reduction of litigation costs is supposed to lead to more trade disputes surfacing
in the dispute settlement record and cause an increase in the implementation of retaliation
at the same time.

Another result of the model is related to the question whether or not the usage of the
dispute settlement system is biased. The theoretical model predicts that a country is more
likely to file a complaint if it (i) has a relatively high retaliative capacity, (ii) faces low litiga-
tion costs and (iii) suffers from an offense at a relatively high level. While these theoretical
findings may explain the dominance of rich countries in the dispute settlement record, they
mean at the same time that the observable sample of reported disputes is biased in favor of
countries with these particular characteristics. Therefore, the finding of [Horn et al., 1999],
which suggests that disputes occur randomly and reasonably proportional to the number
of a country’s product-market-pairings, may still be correct. However, in the light of the
model at hand, the number of a country’s product-market-pairings should no longer be seen
as the central reason for the occurrence of a dispute, but rather as a side effect, that may be
positively correlated with the real drivers of offenses and complaints which are a country’s

⁵²See [Bown, 2005] and [Nordström, 2005]. One reason for their finding is the fact that many developed countries
have already sunk their litigation costs by running a permanent mission at Geneva, while developing countries
face variable costs since they would have to hire law firms and consulting firms in order to prepare a complaint.
Another reason may be the developing countries’ fear of a loss of political goodwill, which could as well be seen
as a component of litigation costs.

⁵³This result parallels findings of the Economics of Crime literature. See for example [Becker, 1968], who shows
that a reduction in litigation costs may lead some offenders to switch to more severe offenses, while it may reduce
the offensive level of others.
retaliative capacity, litigation costs and the intensity of violation. Hence the theory suggests that the observable sample of disputes does not reflect the country-specific characteristics of the unobservable population of disputes. Therefore the unreported offenses (i.e. the dark figure of offenses) should contain a disproportionately large share of countries lacking retaliative capacity, facing high litigation costs and being offended against at lower intensity. This typically applies for developing countries.

Finally, the model seems to provide a theoretical foundation for some existing empirical studies. The model’s predictions agree with the empirical findings of [Bown, 2005], who concludes on page 16: “Our formal evidence indicates that, despite market access interests in a dispute, an exporting country is less likely to participate in WTO litigation if it has inadequate power for trade retaliation, if it is poor and does not have the capacity to absorb substantial legal costs, if it is particularly reliant on the respondent country for bilateral assistance, or is engaged with the respondent in a preferential trade agreement. These are characteristics typically associated with developing countries in the WTO membership.” The empirical study of [Guzman and Simmons, 2005] supports the results as well. [Guzman and Simmons, 2005], page 591 find that “…developing countries are using the DSU in a way that reflects their current incapacity to launch effective legal cases against potential trade law violators.”.
6 Mathematical Appendix

6.1 Equilibrium Prices

Equilibrium world market prices as functions of the associated import tariffs are given by:

\[ \hat{p}_x[\tau] = \frac{a + an - bn\tau}{2b + bn}, \quad \hat{p}_y[\tau^*] = \frac{2a}{3b} - \frac{\tau^*}{3} \]

6.2 Properties of the Aggregated Welfare Functions

To show that a country’s welfare is concave in its own tariff it has to hold that:

(i) \[ \frac{\partial \hat{w}[\tau, \tau^*, n]}{\partial \tau} > 0 \Leftrightarrow \frac{n(an - 4b(1 + n)\tau)}{(2 + n)^2} > 0 \]

This condition is satisfied if the numerator is positive (i.e. if \( an(1 + n) > 0 \) holds).

Solving this expression for \( \tau \) yields \( \tau < \frac{an}{4n + 1} \), which is again Home’s optimal tariff \( \tau_o \).

(ii) \[ \frac{\partial^2 \hat{w}[\tau, \tau^*, n]}{\partial^2 \tau} < 0 \Leftrightarrow -\frac{4bn(1 + n)}{(2 + n)^2} < 0 \]

This condition is always satisfied.

A country’s welfare is decreasing in the other country’s tariff if it holds that:

\[ \frac{\partial \hat{w}[\tau, \tau^*, n]}{\partial \tau^*} < 0 \Leftrightarrow \frac{2b\tau^* - a}{9} < 0 \]

This condition is satisfied if it holds that \( \tau^* < \frac{a}{2b} \), where \( \frac{a}{2b} \) is the prohibitive level of \( \tau^* \), meaning that the traded amount of good \( y \) would equal zero under such a high tariff.
6.3 Properties of $\tau_{ma}[n]$

Aggregated welfare at Home in case of a major offense is given by:

$$\hat{w}[^{\tau}, n] = \hat{w}_x[^{\tau}, n] + \hat{w}_y[min\{\tau_{eq}[^{\tau}, n], \tau^*_o\}]$$

For the cases where permitted retaliation has already reached $\tau^*_o$, the maximization of $\hat{w}[^{\tau}, n]$ yields again Home's optimal tariff $\tau_o[n]$ since $\tau^*_o$ is independent of $\tau$. Therefore the optimal tariff remains unchanged, while welfare at Home is reduced by a fixed amount.

For the case of flexible retaliation (i.e. $\tau_{eq}[^{\tau}, n] \leq \tau^*_o$) Home's welfare from a major offense is:

$$\hat{w}[^{\tau}, n] = \frac{a^2(140 + 176n + 35n^2)}{72b(2 + n)^2} - \frac{72b^2n(2 + n)^2 - 3a(2 + n)(12bn\tau + \sqrt{25a^2(2 + n)^2 - 72abn(2 + 3n)\tau + 144b^2n^2\tau^2})}{72b(2 + n)^2}$$

Taking the first derivative of $\hat{w}[^{\tau}, n]$ w.r.t. $\tau$ yields:

$$\frac{\partial \hat{w}[^{\tau}, n]}{\partial \tau} =$$

$$\frac{3an(a(2 + 3n) - 4bn\tau)}{2(2 + n)\sqrt{25a^2(2 + n)^2 - 72abn(2 + 3n)\tau + 144b^2n^2\tau^2}} - \frac{n(a + 4br)\sqrt{25a^2(2 + n)^2 - 72abn(2 + 3n)\tau + 144b^2n^2\tau^2}}{2(2 + n)\sqrt{25a^2(2 + n)^2 - 72abn(2 + 3n)\tau + 144b^2n^2\tau^2}}$$

Setting this expression equal to zero and solving for $\tau$ yields a polynomial of degree eight in $n$. After having applied a Taylor Series expansion of degree four around the value $n = 1$, the approximation of $\tau_{ma}[n]$ is given by $\tau_{ma}[n] = \frac{a}{8} \left( \frac{(n-1)}{15} - \frac{17(n-1)^2}{1125} + \frac{817(n-1)^3}{84375} - \frac{1679(n-1)^4}{421875} \right)$

The positive real roots of the polynomial are $n_1 = 1$ and $n_2 = 4.01578$. Obviously it holds that $\tau_{ma}[n] = 0 \forall n = 1$.

$\frac{\partial \tau_{ma}[n]}{\partial n}$ is positive at $n_1 = 1$ and negative at $n_2 = 4.01578$. This means that $\tau_{ma}[n]$ is crossing the zero line from below at $n_1 = 1$ and from above at $n_2 = 4.01578$. Hence $\tau_{ma}[n]$ must be positive between unity and $n_2$ and negative for values of $n$ which are either smaller than unity or larger than $n_2$. 


6.4 Properties of the lower switching point \( n_{oi}[\gamma] \)

\( n_{oi}[\gamma] \) is the country size ratio where the first mover switches from playing \( \tau_o[n] \) to playing \( \tau_i[\gamma, n] \). It is found by setting them equal to each other and solving for \( n \). The polynomial has only one positive real root. It takes on the value 1 for \( \gamma = 1 \) and the value 0 for \( \gamma = 0 \).

The local Taylor approximation of \( n_{oi}[\gamma] \) at a particular value of \( \gamma \), with \( 0 < \gamma < 1 \), is strictly increasing in \( \gamma \). In other words, locally \( 0 < n < 1, 0 < \gamma < 1 \) it holds that \( \frac{\partial n_{oi}[\gamma]}{\partial \gamma} > 0 \).

6.5 Properties of \( \hat{w}_o[n] \)

Substituting Home’s optimal tariff into its welfare function in sector \( x \), substituting Foreign’s optimal tariff in to Home’s welfare in sector \( y \) and adding them together yields:

\[
\hat{w}_o[n] := \hat{w}_x[\tau_o[n], n] + \hat{w}_y[\tau^*_o]
\]

In explicit terms the function reads:

\[
\hat{w}_o[n] = \frac{a^2(17 + 25n)}{64b(1 + n)}
\]

The first and second derivatives w.r.t. \( n \) are given by:

\[
\frac{\partial \hat{w}_o[n]}{\partial n} = \frac{a^2}{8b(1 + n)^2}, \quad \frac{\partial^2 \hat{w}_o[n]}{\partial^2 n} = -\frac{a^2}{4b(1 + n)^2}
\]

6.6 Identifying the Area where \( \hat{w}_{ma}[n] \) is preferred

The country size at the intersection of \( \hat{w}_{ma}[n] \) and \( \hat{w}_o[n] \) is found by subtracting \( \hat{w}_{ma}[n] \) from \( \hat{w}_o[n] \), setting this difference equal to zero and solving for \( n \). Since \( \hat{w}_{ma}[n] \), and consequently the difference between the two welfare functions, is a polynomial of degree eight, the regula falsi method is employed to find the real and positive root of this expression.

At the fixed point of \( n = 1.40231 \), \( \hat{w}_{ma}[n] \) and \( \hat{w}_o[n] \) intersect. Since \( \frac{\partial \hat{w}_o[n]}{\partial n} > \frac{\partial \hat{w}_{ma}[n]}{\partial n} \) holds locally at \( n = 1.40231 \), welfare from \( \hat{w}_{ma}[n] \) will be higher (lower) than welfare from \( \hat{w}_o[n] \) iff \( n < 1.40231 (n > 1.40231) \) holds. Therefore, a necessary and sufficient condition for the first mover to prefer playing \( \tau_{ma}[n] \) over \( \tau_o[n] \) is that \( 1 < n < 1.40231 \) holds.

Given this necessary and sufficient condition holds, it still depends on the actual level
of costs whether it is preferred to play $\tau_{ma}[n]$ or $\tau_{i}[\gamma, n]$ in this interval. The intersection of $\hat{w}_{ma}[n]$ and $\hat{w}_{i}[\gamma, n]$ at the point where $n = 1.40231$ can be solved for a cost level of $\gamma = 0.03086$. Speaking graphically, litigation costs have to be lower than 0.03086 to shift the $\hat{w}_{i}[\gamma, n]$-curve so much downward that its intercept with the $\hat{w}_{ma}[n]$-curve lies in the interval of $1 < n < 1.40231$. Therefore, a necessary condition for the first mover to prefer playing $\tau_{ma}[n]$ over $\tau_{i}[\gamma, n]$ is that $0 < \gamma < 0.03086$ holds.

6.7 Properties of the higher switching point $n_{io}[\gamma]$

$n_{io}[\gamma]$ is the country size ratio where the first mover switches from playing $\tau_{i}[\gamma, n]$ to playing $\tau_{o}[n]$. It is found by setting the two corresponding welfare functions equal to each other and solving for $n$. The resulting polynomial has eight roots, meaning that there are eight intersections of $\hat{w}_{o}[n]$ and $\hat{w}_{i}[\gamma, n]$. Four of them are complex, and four are real. The only root that is positive and real for $n > 1$ (two other real roots are globally negative. Another real root is positive, but globally smaller than unity.\footnote{This positive real root, being smaller than unity, coincides with the lower switching point $n_{oi}[\gamma]$. This is due to the fact that welfare from both playing $\tau_{o}[n]$ and playing $\tau_{i}[\gamma, n]$ always has to coincide in $n_{oi}[\gamma]$ because the associated tariffs themselves are identical, and both do not trigger any retaliation at $n_{oi}[\gamma]$.}) is therefore $n_{io}[\gamma]$. It takes on the value 2.46187 for $\gamma = 1$ and the value 1.38504 for $\gamma = 0$. The local Taylor approximation of $n_{io}[\gamma]$ at a particular value of $\gamma$, with $0 < \gamma < 1$, is strictly increasing in $\gamma$. In other words, locally ($1.38504 < n < 2.46187, 0 < \gamma < 1$) it holds that $\frac{\partial n_{io}[\gamma]}{\partial \gamma} > 0$. 

locally $0 < \gamma < 1$) it holds that $\frac{\partial n_{io}[\gamma]}{\partial \gamma} > 0$. 

35
References


