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### **Working Paper**

Trajectories of life satisfaction: Positive feedback loops may explain why life satisfaction changes in multi-year waves, rather than oscillating around a set-point

SOEPpapers on Multidisciplinary Panel Data Research, No. 674

**Provided in Cooperation with:** German Institute for Economic Research (DIW Berlin)

*Suggested Citation:* Headey, Bruce; Muffels, Ruud J. A. (2014) : Trajectories of life satisfaction: Positive feedback loops may explain why life satisfaction changes in multi-year waves, rather than oscillating around a set-point, SOEPpapers on Multidisciplinary Panel Data Research, No. 674, Deutsches Institut für Wirtschaftsforschung (DIW), Berlin

This Version is available at: https://hdl.handle.net/10419/99952

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**574** 

Trajectories of Life Satisfaction: Positive Feedback Loops May Explain Why Life Satisfaction Changes in Multi-Year Waves, Rather Than Oscillating Around a Set-Point

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ISSN: 1864-6689 (online)

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# Trajectories of Life Satisfaction: Positive Feedback Loops May Explain Why Life Satisfaction Changes in Multi-Year Waves, Rather Than Oscillating Around a Set-Point

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#### Abstract

Long term panel data enable researchers to construct *Life Satisfaction (LS) trajectories for individuals over time*. In this paper we analyse the trajectories of respondents in the German Socio-Economic Panel who recorded their LS for 20 consecutive years in 1991-2010. Previous research has shown that at least a quarter of these respondents recorded substantial long term changes in LS (Headey, Muffels and Wagner, 2010, 2012). In this paper, bar charts of LS trajectories, and subsequent statistical analysis, show that respondents tend to spend multiple consecutive years either above and/or below their own 20-year mean level of LS. These results are contrary to set-point theory which views LS as stable, except for short term fluctuations due to major life events.

In the later part of the paper we attempt to explain multi-year/medium term changes in LS. We estimate structural equation models with two-way causation between LS and variables usually treated as causes of LS, including health, frequency of physical exercise, frequency of social activities/social participation, and satisfaction with work and leisure. The results are interpreted as showing positive feedback loops between these variables and LS, such that gains and losses of LS tend to be reinforced over time.

The models are based on a modified concept of 'Granger-causation' (Granger, 1969). The main intuition behind Granger-causation is that if x can be shown to be statistically significantly related to y in a model which includes multiple lags of y, then it can be inferred that x is one cause of y.

Keywords: life satisfaction trajectories; set-point theory; positive feedback loops; Grangercausation

### Twenty-Year Trajectories Of Life Satisfaction: Positive Feedback Loops May Explain Why Life Satisfaction Changes In Multi-Year Waves, Rather Than Oscillating Around A Set-Point

The availability of long-term panel data means that researchers can now construct individual trajectories of life satisfaction (LS) over time. The dataset which provides the longest time series is the German Socio-Economic Panel (SOEP). In this paper we begin by analysing the trajectories of SOEP respondents who recorded their LS for twenty consecutive years from 1991-2010. Visual inspection of individual-level data, summarised in bar charts, makes it clear that many people go through quite long periods of life in which their LS is either well above or well below their own long-term mean. Furthermore, at least a quarter of the sample, as reported in previous papers, appear to record long-term, more or less permanent changes in LS, so that in more recent survey years they are substantially more (or less) satisfied with life than they were in earlier years (Headey, Muffels and Wagner, 2010, 2012). The evidence leads us to suggest that the still widely accepted set-point theory of LS (Brickman and Campbell, 1971; Lykken and Tellegen, 1996; Sheldon and Lucas, 2014), which views individual LS as fluctuating around a long-term stable set-point, can no longer be sustained. Set-point theory is primarily a theory of stability. It is suggested that the major challenge for researchers now is to develop a theory which can also account for medium and long term change.

Most of the paper involves taking some preliminary steps towards a revised theory. We reexamine relationships between LS and variables usually treated as determinants or causes of LS: health, exercise, frequency of socialising with friends, relatives and neighbours, and satisfaction with work and leisure. In reviews of LS research it is quite common to point out that these variables could just as well be consequences of LS, or both causes and consequences (Diener, 1999; Diener, Suh, Lucas and Smith, 1999; Frey and Stutzer, 2002). However, in empirical work the possibility of two-way causation is usually ignored. In the case of the link between health and LS, this is plainly a mistake. It has been shown in prospective studies that happy people live longer, which could only happen if happiness promotes better health (Deeg and van Zonneveld, 1989; Headey, Hoehne and Wagner, 2013). Although a priori reasoning is not so compelling in relation to other possible two-way linkages, it is surely plausible to hypothesise that happiness could cause as well as be caused by, frequency of exercise, social participation and satisfaction with work and leisure.

The evidence in this paper suggests that, in the LS field, two-way causation is pervasive.

Two-way causation – or what might be termed *positive feedback loops* – link multi-year changes in LS and associated variables. For example, changes in health, occurring in year t are estimated to produce changes in LS in year t+1. Then, in a positive feedback loop, changes that have occurred in LS are positively associated with changes in health in year t+2.

Estimation of structural equation models with two-way causation presents considerable difficulties and remains a controversial procedure in the social sciences (Wooldridge, 2010; Kline, 2011). However, as we shall see, the models in this paper appear to have very satisfactory fits to the SOEP data on which they are based. It is hoped that they give some preliminary insights into variables and a *feedback process* that may contribute to medium and long term change in LS.

#### CHALLENGES TO SET-POINT THEORY: NEED FOR A THEORY OF CHANGE

Set-point theory was developed by psychologists over a period of about thirty-five years, appearing to integrate an increasing range of results and becoming more or less the scientific paradigm within which LS researchers worked (Kuhn, 1962). In its original incarnation it was termed adaptation theory; its central claim being that individuals adapt back to their previous 'baseline' level of LS within a year or two of experiencing a major life event (Brickman and Campbell, 1971; Brickman, Coates and Janoff-Bulman , 1978). The theory was buttressed by finding that most individuals soon revert to baseline after making major financial gains or losses (Easterlin, 1974, 2009; but see Stevenson and Wolfers, 2008). LS was found to be positively related to the personality trait of extroversion and negatively related to neuroticism (Costa and McCrae, 1980). Since these traits are partly genetic and hence fairly stable, they appeared to help account for the presumed stability of LS. Lykken and Tellegen (1996), who coined the term set-point theory, seemed to put the triumphal arch on the theory by comparing the stability of the happiness of monozygotic and dizygotic twins, and inferring that happiness is at least 50 per cent hereditary. Their much quoted conclusion was that, "Trying to be happier may be as futile as trying to be taller".

In the last fifteen years or so, set-point theory has come under increasing challenge. Easterlin (2003), whose work on gains and losses in the financial domain had lent support to adaptation (or set-point) theory, reviewed the effects of changes in non-economic domains, mainly health and family life, and concluded that in these domains adaptation to change is partial, but by no means complete. In particular, evidence about people who developed chronic health problems showed that their LS is permanently lowered (Mehnert, Kraus, Nadler and

Boyd, 1990), and research on individuals who got married indicated that some (although by no means all) recorded long term gains in LS (Lucas, Clark, Georgellis and Diener, 2003).

The limitations of set-point theory became clearer as longer and longer term panel data became available. Fujita and Diener (2005), analysing the first seventeen years of SOEP data, found that many respondents had recorded substantial changes in LS, although they stopped short of concluding that set-point theory was deficient. Headey (2008a) and Headey, Muffels and Wagner (2010, 2012), using data from Australian and British household panels as well as SOEP, found that a quarter to a third of survey respondents (but not a majority) recorded substantial gains or losses of LS over periods ranging from a decade to twenty-five years.

Despite the evidence of panel data, set-point theory continues to be quite widely endorsed (see the forthcoming review volume: Sheldon and Lucas, 2014). The most cited evidence in its support continues to be that the only fairly common major life event which usually lowers LS is repeated or long term unemployment (Clark, Diener, Georgellis and Lucas, 2008). Figure 1 gives a stylised account of what many regard as the 'normal' trajectory of an individual's LS over time; a trajectory in line with set-point theory. We will later compare this trajectory with the actual trajectories of SOEP respondents.

#### **INSERT FIGURE 1 HERE**

The figure shows the trajectory of a person with a set-point of 7 on a 0-10 LS scale for the period 1991-2010. The trajectory is a flat line, except for an upward fluctuation lasting one year in the 1990s, and a similar downward fluctuation in the 2000s. An obvious prediction of set-point theory, encapsulated in Figure 1 and testable with the SOEP data, is that individuals who deviate from their set-point in a particular year will revert back to set-point within one, or at most two years.

Evidence about the merely temporary effects of life events may appear convincing but should not be over-interpreted. It is a non-sequitur to claim that, because specific life events do not change LS, then LS does not change. Panel data plainly show that many individuals report medium and long term changes in their LS. If these changes are not due to discrete life events, then they must be due to differences or changes in other variables. Which other variables? Economists Oswald and Wu (2010) have shown that differences in objective social, economic and environmental conditions in the fifty American states help to explain average differences in LS among the fifty populations. Political scientists, also using aggregate data, have indicated that differences in welfare state support, and in the extent of direct citizen participation in governmental decision-making have significant effects on LS (Radcliffe, 2001; see also Frey and Stutzer, 2001). Psychologists working in the positive psychology tradition have reported experimental evidence showing the beneficial effects on LS of altruistic actions, religious practice and activities which play to one's character strengths (Diener and Seligman, 2004; Lyubomirsky, Sheldon and Schkade, 2005; Dunn, Aknin and Norton, 2008; Headey, Schupp, Tucci and Wagner, 2010). On related lines, it has been found that individuals who prioritise altruistic and family goals are on average happier than those who prioritise financial and material goals (Nickerson, Schwarz, Diener and Kahneman, 2003; Headey, 2008b).

In previous papers, replicating results with German, Australian and British panel data, we found that LS is significantly affected by differences and changes in life goals and religious practice, and by behavioural choices relating to regular participation in social networks and social activities, frequency of physical exercise, and achieving a preferred balance between work and leisure (Headey, Muffels and Wagner, 2010, 2012). The links between the behavioural choices and LS held in within-person (fixed effects) panel regression models, confirming that changes in choices covary over time with changes in LS.

A limitation of most previous attempts to explain changes in LS (including our own) is that, while they may succeed in accounting for short term change, they do not offer a convincing explanation of how and why LS may remain substantially above (or below) its previous level in the medium or long term, rather than reverting to its previous level, as set-point theory would predict.

As already mentioned, we attempt to account for medium term change with two-way causation models (structural equation models), which include positive feedback loops between LS and variables usually treated as causes of LS. It must of course be conceded that disentangling two-way causation issues remains problematic, even with long term panel data. Previous researchers, using panel data, have claimed to find two-way causation between LS and domains satisfactions (mainly marriage and job satisfaction), and between LS and quality of social networks, health, housing and volunteering (Headey, Veenhoven and Wearing,

1991; Meier and Stutzer, 2004; Mathison et al, 2007; Nagazato, Schimmack and Oishi, 2011). These studies have been roundly criticised by researchers who claim that structural equation models involving two-way causation can be unstable in the sense that small, reasonably plausible changes in model specification can lead to quite different conclusions about direction of causation (Scherpenzeel and Saris, 1996; see also Wooldridge, 2010).

In this paper we suggest that more stable and better fitting models of LS can be estimated by conceptualising relationships in terms of *Granger-causation* (Granger, 1969; Granger and Newbold, 1974; Pearl, 2009). The intuitions behind Nobel Laureate, Clive Granger's concept of causation, are that (1) causes must precede effects and (2) if earlier values of an x variable (a presumed cause) can be shown to be statistically significantly related to later values of a y variable (a presumed effect) in equations which include multiple lagged versions of y, then it may be inferred that x is one cause of y. Granger's view was that, by including multiple lags of y, the researcher would usually take care of most of the variance due to omitted variables ('unobserved heterogeneity'), and so would avoid biased estimates and the autocorrelated error terms that indicate bias (Granger, 1969; Pearl, 2009; Woo1dridge, 2010; Beck and Katz, 2011; Wilkins, 2014).

We suggest extending Granger's approach to two-way causation and panel data, and being willing to infer that x and y may cause each other in models of the kind depicted in Figure 2. This model shows possible relationships between health (the x variable) and LS (the y variable). It is based on five waves of panel data, in line with the models to be estimated in this paper.

#### **INSERT FIG 2 HERE**

The causal paths of main interest in Figure 2 – usually referred to in the causal modelling literature as *cross-lagged paths* - are those with BU? and TD? above them. In referring to bottom-up (BU) and top-down (TD) paths, we are using terminology coined by Diener (Diener, 1984; Diener et al, 1999). He labels models in which LS is viewed as being caused by a weighted combination of *x* variables as BU models, and models in which evaluations of specific aspects of life are viewed as consequences (or spin-offs) of overall LS as TD models.

The curved arrows marked SP? in Figure 2 are a further attempt (in addition to Granger lags) to allow for the possibility that covariance between health and LS could be wholly or partly spurious. These curved arrows link the error terms (residuals) of each pair of x and y equations, and should be routinely included in structural equation panel models (Kessler and Greenberg, 1981; Finkel, 1996; Wooldridge, 2010).

'Extra' Granger lags are shown by dotted paths running along the top and bottom of Figure 2. As well as helping to avoid biased/spurious estimates of the coefficients of main interest, these extra lags can be given a substantive interpretation in LS research. If 'extra' lags of LS are significant in LS equations, it means that individual happiness at time t depends not just on happiness at t-1, but is also affected in a cumulative way by happiness in earlier periods. Evidence about the effects of lagged x variables on x at time t can be given a similar substantive interpretation.

In summary, four main outcomes are possible when we estimate Granger-style models of the kind depicted in Figure 2. One possibility is that the covariance between a particular x variable and LS will be found to be wholly spurious. Secondly, it is possible that only BU paths from x to LS will prove to be statistically significant. Alternatively, only TD paths from LS to x may be significant. If both BU and TD paths prove to be significant, then the inference will be that changes in x and changes in LS cause and reinforce each other in a positive feedback loop. For example, better or worse health in one time period may affect LS in the next time period, which in turn affects health in the period after that.

Estimation of two-way causation raises issues relating to model identification and assessment of model fit. These more detailed methodological issues are taken up in the next section.

#### **METHODS**

#### The German Socio-Economic Panel Survey (SOEP)

SOEP began in 1984 in West Germany with a sample of 12541 respondents (Wagner et al., 2007). Interviews have been conducted annually ever since. Everyone in the household aged 16 and over is interviewed. The cross-sectional representativeness of the panel is maintained by interviewing 'split-offs' and their new families. So when a young person leaves home ('splits off') to marry and set up a new family, the entire new family becomes part of the panel. The sample was extended to East Germany in 1990, shortly after the Berlin Wall came down, and since then has also been boosted by the addition of new immigrant samples, a

special sample of the rich, and recruitment of new respondents partly to increase numbers in 'policy groups'. There are now over 60,000 respondents on file, including some grandchildren as well as children of the original respondents. The main topics covered in the annual questionnaire are family, income and labor force dynamics. Questions on LS, domain satisfactions (job satisfaction, satisfaction with income etc), health, social participation and exercise have been included every year.

The sub-sample used in this paper comprises prime age respondents (25-64) who gave life satisfaction readings every year from 1991-2010 (N=1873). The reason for the age restriction is that set-point theory is usually said to apply most clearly to prime age adults (Diener et al, 1999). It is accepted that younger people are still maturing, and their LS may be quite volatile. In the case of older people, declining health may be a source of lowered LS (Gerstorf et al, 2008).

#### Measures

#### Life Satisfaction (LS)

LS is measured in SOEP on a 0-10 scale (mean=7.001 s.d.=1.830), the end-points of which are labelled 'totally dissatisfied' and 'totally satisfied'. Single item measures of LS are plainly not as reliable or valid as multi-item measures, but are internationally widely used in household panel surveys and have been reviewed as acceptably reliable and valid (Diener et al, 1999).

#### Variables potentially implicated in two-way causation with LS

#### Health

An internationally widely used, self-assessed health measure has been included in SOEP since the early 1990s. Respondents rate their own health on a 1-5 scale ('bad' to 'very good'). Despite its simplicity, this scale has been assessed as reasonably valid in that it correlates satisfactorily with physician ratings (Schwarze, Andersen and Silke, 2000). Its correlation with LS is 0.381.

#### Exercise

SOEP respondents are asked annually about how frequently they engage in active sport or exercise. The response scale runs from 0 ('not at all') to 5 ('every day'). The correlation of

this item with LS is 0.149. Frequency of exercise is usually found to be associated with LS, and also with reduction of depression and increased longevity (Gremeaux et al, 2012). Subjective measures, like the one in SOEP, are only moderately reliable; they correlate only moderately with objective measures of the kind provided by an accelerator or pedometer (Mackay, Oliver and Schofield, 2011). Women, particularly, are prone to overstate the amount they exercise.

#### Frequency of socialising with friends, relatives or neighbours (social participation)

The social participation index used here combines two correlated items about frequency of 'meeting with friends, relatives or neighbours' and 'helping out friends, relatives or neighbours'.<sup>12</sup> The response scale has just three points: 'every week', 'every month' and 'seldom or never'.<sup>3</sup> The correlation of this index with LS is 0.133.

#### Satisfaction with work and leisure

Job satisfaction and satisfaction with leisure are both measured by single questions asked on the same 0-10 ('totally dissatisfied' to 'totally satisfied') scale as LS. The correlation of LS with job satisfaction is 0.444 and with leisure satisfaction it is 0.348.

#### Exogenous variables included as 'controls' and also to assist with model identification

Additional exogenous variables are included in the panel models, both as standard 'controls' and also to assist with model identification. Standard 'controls' are: gender (female=1 male=0), age, age-squared, partner status (partnered=1 not partnered=0), years of education, household net income, unemployed (unemployed=1 other=0), disability status (disability=1 other=0).<sup>4</sup> It is also desirable to control for personality traits known to be correlated with LS (Lucas, 2008). The traits measured in SOEP are the so-called Big Five, which many psychologists regard as adequately describing normal or non-psychotic personality: neuroticism, extroversion, openness to experience, agreeableness and conscientiousness (Costa and McCrae, 1991). Since the traits are partly genetic (Lucas, 2008), it clearly makes sense to treat them as exogenous and causally antecedent to LS and the *x* variables in our models.

<sup>&</sup>lt;sup>1</sup> If all 27 years of available data had been used (1984-2010), the sample size would have been reduced to under 1000.

 $<sup>^{2}</sup>$  The correlations have varied from year to year but are usually around 0.3.

<sup>&</sup>lt;sup>3</sup> 'Seldom' or 'never' have been included as separate categories in more recent waves of SOEP.

<sup>&</sup>lt;sup>4</sup> Disability status was not included in models in which the Self-rated health scale was the *x* variable.

In any panel survey, what are called 'panel conditioning effects' are a possible source of bias. That is, panel members might tend to change their answers over time – and answer differently from the way non-panel members would answer - as a consequence just of being panel members. There is evidence in the SOEP data that panel members, in their first few years of responding, tend to report higher LS scores than when they have been in the panel for a good many years (Frijters, Haisken-DeNew and Shields, 2004). This could be due to 'social desirability bias'; a desire to look good and appear to be a happy person, which is stronger in the first few years of responding than in later years. Or it could be due to a 'learning effect'; learning to use the middle points of the 0-10, rather than the extremes and particularly the top end.

To compensate for these possible sources of bias, we include in all equations a variable which measures the number of years in which each panel member has already responded to survey questions.

#### Data analysis: structural equation modelling of two-way causation

Structural equation modelling, rather than OLS regression analysis, is required whenever the aim is to estimate a set of equations, rather than a single equation, and especially when twoway causal links are involved.<sup>5</sup> The structural equations in this article are estimated using maximum likelihood analysis.<sup>6</sup> Maximum likelihood coefficients and their associated standard errors can be given the same interpretation as regression coefficients. However, assessing the 'goodness of fit' of structural models is more complicated than for regression models. It is necessary to assess the overall fit between estimates for several equations and the input data for the model (a correlation or variance-covariance matrix).<sup>7</sup> Several measures of fit are conventionally used. The root mean squared error of approximation (RMSEA) and the standardized root mean residual (SRMR) are directly based on comparing differences (residuals) between the actual input matrix with the matrix implied by model estimates. It has

<sup>&</sup>lt;sup>5</sup> OLS regression analysis is essentially a single equation technique. Regression estimates derived from multiequation systems are likely to be biased, due to correlations between explanatory variables and error terms in some or all equations. A key assumption of OLS regression is that such correlations are zero.

<sup>&</sup>lt;sup>6</sup> ML estimates are usually consistent and asymptotically normal under the (not very restrictive) assumption of *conditional normality* (StataCorp, 2013). Only paths or covariances linking conditioning (i.e. control) variables may not be consistent and asymptotically normal (even then, the main problem lies just with estimates of standard errors). These paths are not usually of substantive interest. Substantive interest lies in paths (1) linking exogenous with endogenous variables and (2) between endogenous variables.

<sup>&</sup>lt;sup>7</sup> From a mathematical standpoint, a model can be viewed as a set of constraints - or a set of restricted paths limiting the possibilities of simply reproducing the input data. Attempts by a researcher to improve his/her model involve modifying these constraints to improve model fit...subject to the theory/hypotheses underlying the model.

become conventional to regard an RMSEA under 0.05 and an SRMR under 0.08 as satisfactory (Bentler, 1990; Browne and Cudeck, 1993).

More complicated assessments are provided by the Comparative Fit Index (CFI) and the Tucker-Lewis index (TLI). The CFI is based on a likelihood ratio (LR) chi-square test and takes account of the contribution of each estimate in the model to overall goodness of fit. The TLI is also derived from an LR chi-square test, and is particularly useful because it rewards parsimony and penalises models including explanatory variables which account for little variance, even if statistically significant. CFI and TLI fits above 0.90 used to be regarded as satisfactory, but some recent reviews recommend 0.95 (Bentler, 1990; Browne and Cudeck, 1993).

In addition to these composite measures of model fit, it is important to check for possible autocorrelation among residuals. As previously explained, autocorrelated errors are usually a symptom of omitted variables bias.

We used the new STATA 13 module for structural equation modelling to generate the results reported here (StataCorp, 2013). This package offers a range of estimators, including maximum likelihood, and includes the tests of goodness of fit described above. Statistically significant autocorrelated errors are routinely reported.

Models involving two-way causation can be unstable in the sense that they would never reach equilibrium and would 'blow up' if sufficient iterations were run (Finkel, 1995; StataCorp, 2013).<sup>8</sup> In view of this, Bentler and Freeman (1983) developed a test of model stability, which is used here.

Strictly speaking, maximum likelihood estimation of structural equations requires an assumption the endogenous variables are measured on an interval or ratio scale. In fact, all the endogenous variables in our equations (LS and the *x* variables) are measured on fairly long ordinal scales. However, it has become routine in research on LS to treat the data as interval-level. Andrews and Withey (1976) were the first researchers to show that, substantively, results using interval-level statistics were much the same as those using ordinal statistics. Most researchers since have followed their lead. An important practical reason for

<sup>&</sup>lt;sup>8</sup> Model 'stability' is here used as a technical term. Previously we used the term in a different sense to refer to Scherpenzeel and Saris's (1996) claim that two-way causation models of LS are unstable because apparently small differences in model specification can lead to substantially different estimates.

making interval scale assumptions in structural equation modelling is that, although equations can be estimated for models with ordinal or binary endogenous variables, few measures of

model fit are available, so it is often unclear whether one model is statistically preferable to another.<sup>9</sup>

### Model identification

Issues of model identification always arise in estimating models with possible two-way causal links. The basic question is whether there are there sufficient independent pieces of information (variances and covariances) in the input matrix to enable all free parameters in one's model to be estimated. If there are *not* enough independent pieces of information, the model is said to 'under-identified' and no mathematically correct solution is possible. In models with only one-way causation, identification is usually not a problem. But special steps are always needed to achieve identification of two-way causation models. There are three main approaches, all of which are implemented in this paper:-

(1) Exogenous variables may serve as instrumental variables. In our models the fourteen exogenous variables described earlier – socio-economic variables, personality traits and years in the panel - are linked to wave 1 versions of x and LS, but not to later waves. So they act as instruments to identify the equations for later waves. The rationale for omitting links to later waves is that, while one expects all these exogenous variables to influence x and LS at wave 1, there is no reason to expect them to influence measures taken at later waves, net of their effects on wave 1 variables (Kessler and Greenberg, 1981). Equivalently, we may say that there is no reason to expect the exogenous variables to be associated with *changes* over time in x and LS.

(2) In previous research lagged versions of x and LS were commonly used as instruments to identify equations (Headey, Veenhoven and Wearing, 1991; Scherpenzeel and Saris, 1996; Meier and Stutzer, 2004; Mathison et al, 2007; Nagazato, Schimmack and Oishi, 2011). However, in the models presented in this paper, the inclusion of multiple Granger-style lags increases rather than reduces the number of free parameters that need to be estimated. Our models are nevertheless still identified, due to inclusion of the fourteen exogenous variables. Further, in later computer runs we modified our models by removing some Granger-style lags – specifically longer term lagged effects of x on LS, and LS on x. Consequently, in our final models, this second approach to model identification came back into play.

(3) Equality constraints may be imposed. That is, sets of coefficients may be fixed (programmed) to be equal to each other, so reducing the number of free parameters that need to be estimated (Kessler and Greenberg, 1981; Finkel, 1995). No equality constraints were

<sup>&</sup>lt;sup>9</sup> Another limitation is that covariances between the error terms of equations cannot be estimated, so it becomes difficult to assess whether relationships are spurious.

imposed in the initial models estimated for this paper. However, both a priori reasoning and initial computer runs indicated that, empirically, some causal links appeared to be almost exactly the same in consecutive waves of data. So equality constraints were added in later runs, and in some cases improved model fit (see the Results section).

Because we make use of all three approaches to achieving identification in panel data models with two-way causation, our models are 'over-identified'; that is, they actually contain many more bits of information than are required to estimate parameters. This may seem like overkill, but it is ideal for maximum likelihood estimation; the maximum likelihood estimator is designed to find the best solution among the range of solutions available.

A final point relating to identification: the STATA 13 structural equation module includes built-in checks for identification; models that are not identified are either rejected outright, or else the iterative model-fitting procedure fails to converge.<sup>10</sup>

#### Time lags

Another important issue to consider in causal modelling is the *time lag* between changes in an explanatory variable and changes in the outcome variable. A 'common sense' view, which underlies Granger-causation and most other accounts of causation, is that causes must precede effects. In Figure 2 (above) it is implicitly assumed that changes in x (frequency of exercise) affect changes in LS after some discrete time lag, and that changes in LS, if they affect x at all, also take effect after a time lag. However, in considering our data, it is plausible to believe that the effects of x variables on LS might well be (a) continuous and/or (b) simultaneous or almost simultaneous. To continue our example, consider possible two-way effects between health and LS. It is reasonable to suppose that the two-way effects (if statistically significant) are continuous and perhaps almost simultaneous.

It can be shown mathematically that, if effects are continuous, cross-lagged models of the kind shown in Figure 2 yield unbiased and consistent estimates of the relevant coefficients (Coleman, 1968; Tuma and Hannan, 1984; Finkel, 1995). The point is that, if effects are continuous, the time points at which panel survey measurements are taken are arbitrary, and the task of the researcher is to recover the coefficients of change, using calculus (i.e. the branch of mathematics which deals with continuous change):

 $<sup>1.1 \</sup>qquad \qquad dy_t/dt = c_o + c_1 x_t + c_2 y_t$ 

<sup>&</sup>lt;sup>10</sup> When convergence fails, exactly the same Chi-square LR is produced repeatedly, model iteration after iteration.

$$1.2 dx_t / d_t = c_3 + c_4 y_t + c_5 x_t$$

These two differential equations state that instantaneous rates of change (the *c* coefficients) in x and y are dependent on each other over time (Coleman, 1968; Tuma and Hannan, 1984; Finkel, 1995). Additional mathematics shows that these equations are equivalent to the standard structural equations (2.1 and 2.2 below) for two-way cross-lagged causation between x and y, except that in the structural equations random error terms are added to take account of omitted variables.

2.1 
$$y_t = a_1 + b_1 x_{t-1} + b_2 y_{t-1} + e_1$$

2.2 
$$x_t = a_2 + b_3 y_{t-1} + b_4 x_{t-1} + e_2$$

These structural equations can be estimated to provide unbiased and consistent estimates of the continuous effect of x on y and y on x (Finkel, 1995).

Further modelling issues arise because the changes we are considering may be not just continuous, but also simultaneous. In Granger-causation it is assumed that causes precede effects, so strictly speaking, Granger's approach cannot be extended to simultaneous causation (Pearl, 2009). However, the word 'simultaneous' should not be taken absolutely literally in this context. The causal influences in question could be almost simultaneous, or more practically, could take effect at an interval considerably shorter than the length of time between panel surveys (Finkel, 1995). It might be thought that the way to deal with this possibility would be just to add simultaneous causal links to the model in Figure 2. Unfortunately, models with both simultaneous and cross-lagged links cannot usually, in practice, be estimated. This is due to problems both of under-identification and multicollinearity (Kessler and Greenberg, 1981; Finkel, 1995).<sup>11</sup> A practical, fall-back procedure that can be followed if, as we found here, a model of this type cannot be estimated is to estimate a model with *only* simultaneous links, and then compare results with those from a model with *only* cross-lagged links, or by extension, Granger-links (Greenberg and Kessler, 1982). If the signs of coefficients of interest in both models are the same, and the coefficients are also statistically significant, then the researcher can feel reassured that results are

<sup>&</sup>lt;sup>11</sup> Kessler and Greenberg (1981, chap. 3) describe how a multi-wave panel model of this kind may in principle be identified by using *equality constraints* (i.e. by constraining sets of parameters to be equal to each other). In practice, this approach to identification only succeeds if relationships among variables are quite far from equilibrium (i.e. relationships differ substantially from wave to wave of the panel data). In panel surveys of life satisfaction, it is reasonably clear that relationships between LS and causal variables of interest are much the same from wave to wave. Estimation of models with both simultaneous and cross-lagged links is also likely to run into problems because of multicollinearity; the effects on LS of x at time t and x at t-1 are likely to be too highly correlated for estimates to be reliable.

consistent with each other, although if the 'true' causal (time) lag is misspecified in both models, coefficients are likely to be under-estimates. This procedure was followed in the present paper and, as reported in detail below, the two-way estimates of main interest were always consistent. More to the point, the Granger-style models were in all cases a much better fit to the data than models with only cross-lagged links or only simultaneous links.

The periods covered by our five-wave panel models are consecutive and overlapping: 1991-95, 1992-1996...up to 2006-10. The reason for using all available five-year periods, instead of just four non-overlapping periods (1991-95, 1996-2000, 2001-05 and 2006-10) is to obtain more reliable results due to larger sample numbers.<sup>12</sup> An assumption which has to be met for this decision to be sensible is that relationships among variables do not change much within the overall time period. Inspection of bivariate correlations within and across waves suggests that this assumption is plausible.

#### RESULTS

#### Individual trajectories of change in LS

An improved theory of LS needs to be able to account for individual trajectories of change. Below are six bar charts which show the LS trajectories of the first and last three SOEP respondents in the datafile, among those who recorded their LS every year from 1991 to 2010. The first three joined the panel in 1984 in its first year; the last three joined in the early 1990s. Clearly, six cases do not constitute a representative sample, but their LS trajectories are instructive, especially in view of the more or less flat-line trajectory predicted by set-point theory.

#### **INSERT FIGURE 3 HERE**

Visual inspection suggests that Cases A, B and D have roller-coaster lives. They do not appear to have any set-point around which their LS fluctuates. Case A was a 33 year old married woman in 1991, with eighteen years of education and a household income close to the national median. She rated about average on the personality traits of both neuroticism and extroversion. Her LS rating was 8 on the 0-10 scale in 1991. It then fell every year until 1994,

<sup>&</sup>lt;sup>12</sup> So the observations are person-years, rather than just persons.

rose greatly in 1995, then kept falling again until 1998, was at 4 or 5 for most of the time between 1998 and 2006, and then at 6 or 7 in 2007-10.

By contrast, Cases C, E, and F had quite stable levels of LS in this period. Take Case F, a man age 30 in 1991 with 11.5 years of education and a below median income, who rated above average on neuroticism and about average on extroversion. His LS rating was 6 on the 0-10 scale in ten of these twenty years, and 7 in most other years. He dropped to a rating of 5 on just three occasions. Clearly, it would be reasonable to say that this man has an LS set-point between 6 and 7.

Inspection of many more trajectories suggests that about half the population just do not have a set-point. For the other half, the concept more or less applies.

An interesting feature of the trajectories is that, instead of recording short term fluctuations around a set-point, many respondents appear to spend several consecutive years above... or several years below their own long term (20-year) mean level of LS. This is suggested by pairs of within-person (fixed effects) regression analyses in which LS in year t is the independent variable and the dependent variables are, successively (i) LS in year t+1 and t-1 (ii) t+2 and t-2 (iii) t+3 and t-3 and (iv) t+4 and t-4. Recall that, in a fixed effects analysis, coefficients are calculated by relating deviations from each individual's own grand mean on the *y* variable to deviations from his/her grand means on explanatory variable(s).

#### **INSERT TABLE 1 HERE**

The coefficients in Table 1 suggest that if an individual is above his/her own long term (1991-2010) mean of LS in a particular year, then h/she is more rather than less likely to be above it in each (but, given the size of the coefficients, not all) of the four years beforehand and the four years afterwards.<sup>13</sup> These apparently innocuous regression results may have non-trivial implications for LS theory. They show that LS tends to change in medium term spurts or waves rather than fluctuating short term around a stable set-point.

<sup>&</sup>lt;sup>13</sup> Another way of making the same point: among individuals who were above their own 1991-2010 grand mean of LS in any particular year, just over 25% remained above it for all of the next four years. By chance only 6.25% would have done so.

# Structural equation models with 2-way causation: positive feedback loops between LS and x variables

In the rest of the paper we attempt preliminary explanations of why these medium term waves occur. We indicate that there appears to be two-way causation between LS and a range of *x* variables, so that positive feedback loops sometimes tend to perpetuate periods of above average LS, and sometimes perpetuate below average periods. Our initial modelling results led us to conjecture that the *x* variables might also tend to change in multi-year waves, rather than short term oscillations. It turned out that they do. Fixed-effects equations like those in Table 1 showed that health tends to changes in twelve-year waves (controlling for age and age-squared), while frequency of exercise, social participation and the other *x* variables have wavelengths similar to LS.

In analysing the five-wave panel data (see Figure 2 above), we first estimated relationships between LS and each particular *x* variable, deploying a Granger-style model with multiple lags. We then modified this model, removing statistically insignificant links and imposing equality constraints where appropriate. We then compared our final Granger-style model - both substantive causal estimates and measures of model fit - with results from one-way causal models, and also from cross-lagged and simultaneous causation models of the kind deployed in previous studies which have investigated two-way causation.

#### Health and LS

Our first step was to estimate a 'full' Granger-style model; that is, a model in which all lags of both self-assessed health and of LS were included in equations. It was immediately clear that all lags of the health measure were statistically significant in health equations, and that all lags of LS were significant in LS equations. This already suggested that the Granger approach was going to greatly improve model fit, compared with previous approaches. It was also clear, however, that the model could be pruned. While health lagged by one year had a statistically significant effect on LS, and LS lagged by one year had a significant effect on health, little additional variance was accounted for by 'extra' (2<sup>nd</sup>, 3<sup>rd</sup>) cross-lags. No extra cross-lags of LS were significant, and although some two-year cross-lags of health were significant at the 0.05 level, their effects were substantively trivial.<sup>14</sup> So we dropped extra cross-lags from our final model.

We also experimented with imposing equality constraints on the cross-lagged BU and TD links of main interest, marked =a and =b in Figure 2.<sup>15</sup> The rationale for imposing these constraints was that inspection of correlation matrices indicated that relationships between health and LS were similar within each wave of data, and also between consecutive waves. So it seemed reasonable to hypothesize that 'true' relationships were, in fact, constant or almost constant over time. In the event, a model with equality constraints was neither clearly a better, nor clearly a worse fit than a model without these constraints. It depended on which measures of fit one chose to place faith in. The LR Chi-square test and the CFI diagnosed a somewhat worse fit with the equality constraints in place, but the RMSEA and the TLI, which reward model parsimony, diagnosed an improved fit. On grounds of parsimony, we elected to treat the Figure 2 model with equality constraints as our preferred model.

A crucial point is that all reasonable variations of a Granger-style model, including the 'full' model with all available lags, indicated two-way causation between health and LS. All had similarly close fits to the data.

Table 2 gives both metric and standardized maximum likelihood estimates for the BU, TD and SP relationships marked in Figure 2. The standardized results are particularly useful because they enable us to compare effect sizes. (Self-assessed health and LS are measured on ordinal scales of different but arbitrary lengths). Table 2 also provides a fairly comprehensive set of measures of model fit.

#### **INSERT TABLE 2 HERE**

Positive feedback loops are found between self-assessed health and LS. The size of the standardized BU path from Health to LS (0.093 p<0.001) is greater the TD path from LS to Health (0.056 p<0.001). The relative size of the two-way links is approximately the same for

<sup>&</sup>lt;sup>14</sup> With a large sample size, it is obvious that many statistically significant but substantively trivial effects are likely to be found.

<sup>&</sup>lt;sup>15</sup> In the final run of this model the equality constraints on the BU and TD estimates for the equations for Exercise<sub>t+1</sub> and  $LS_{t+1}$  were dropped. The reason is that these are not 'Granger' equations in that no 'extra' (2<sup>nd</sup>, 3<sup>rd</sup>) lags are available. Consequently, as Granger would predict, the estimates of the BU and TD links from these equations are considerably higher than from the equations with multiple lags, and are probably biased (Granger and Newbold, 1974).

men and women, and for older and younger people.<sup>16</sup> The SP link, reflecting the effects of omitted variables, is 0.213 (p<0.001); much larger than either the BU or TD links.

This Granger-style health model has a satisfactory fit to the data with a CFI of 0.984 and a TLI of 0.977; both well above the conventional 'close fit' level of 0.95. The RMEA is 0.027 (below the standard cut-off of 0.05) and the SRMR is also 0.027 (below the 0.08 cut-off). No statistically significant autocorrelated errors are found. Model stability is satisfactory; all eigenvalues are within the unit circle (Bentler and Freeman, 1983).

It is crucial to compare the fit of the Granger-style model to all reasonable alternatives. All the other models we consider are 'nested' versions of the larger Granger-style model, so model fit can be directly compared (Bentler, 1990). A model with only one-way causation from health to LS, which includes 'extra' Granger lags and equality constraints, is a much worse fit to the data: CFI=0.829, TLI=0.757, RMSEA=0.104 and SRMR=0.066. A one-way TD model with causation running only from LS to health is even worse: CFI=0.817, TLI=0.740, RMSEA=0.105 and SRMR=0.067. Equally to the point, the Granger model is a closer fit to the data than either a cross-lagged model without 'extra' Granger lags, or a simultaneous causation model without extra lags. Both these alternative models (which include equality constraints equivalent to those in the Granger model) give the following fit readings: CFI=0.954, TLI=0.934, RMSEA=0.055 and SRMR=0.037.

Despite fitting the data less well, it is important to record that substantive estimates for BU and TD links in both the cross-lagged and simultaneous causation models are consistent with, although somewhat larger than estimates for our preferred model. The cross-lagged model gives a standardized BU estimate of 0.087 (p<0.001) and a TD estimate of 0.083 (p<0.001). The simultaneous causation model yields standardized BU and TD estimates of 0.125 (p<0.001) and 0.114 (p<0.001) respectively. The reason for these somewhat higher estimates is presumably that one consequence of omitting extra 'Granger' lags of outcome variables is to give an upward bias to estimates of the BU and TD links of main interest (Granger and Newbold, 1974).

Additional sensitivity tests were performed to check whether the equality constraints in the model are justified. The results were slightly ambiguous. It transpired that, if all constraints were removed, estimates of the BU and TD links were within 0.01 (standardized) of the

<sup>&</sup>lt;sup>16</sup> Results for sub-sets of the population are not printed here; available from the authors.

estimates in Table 2. Lagrange multiplier tests indicated that model fit would be just slightly improved (but only at the 0.05 significance level) by removing just one pair of equality constraints. On grounds of theory and parsimony, we elected not to make this change and to retain the model shown in Figure 2.

In summary, finding significant two-way links between health and LS is compatible with the interpretation that feedback loops are operating, so that having better or worse health results in more or less LS, which in turn results in better or worse health, and so on.

#### Exercise and LS

A full multiple-lag Granger model for links between frequency of exercise and LS indicated that both first and second lags of BU and TD relationships were statistically significant. However, the effect sizes of the second lags were small, suggesting just lingering effects. Again, as with the health model, inspection of the input correlation matrix made it clear that relationships within and between waves of data were quite similar over time. So we again opted for a model in which, as in Figure 2, the cross-lagged causal links of main interest were constrained to be equal. As before, all Granger lags of outcome variables were included.

#### **INSERT TABLE 3 HERE**

Two-way causal links are found between exercise and LS. Increased frequency of exercise increases LS. Then, in a positive feedback loop, enhanced LS leads to more frequent exercise. A comparison of the standardized coefficients indicates that the strength of the BU link from exercise to LS (0.036 p < 0.001) is greater than the TD link from LS to exercise (0.014 p < 0.001). The two-way links are again approximately the same for men and women, and for older and younger people. SP links, reflecting the effects of omitted variables, are also statistically significant (0.027 p < 0.001).

The Granger-style model has a satisfactory fit to the data with a CFI of 0.987 and a TLI of 0.982. The RMEA of 0.026 is below the standard cut-off of 0.05, and the SRMR of 0.022 is also satisfactory. No significant autocorrelated errors are reported. Model stability is again fine; all eigenvalues being within the unit circle (Bentler and Freeman, 1983).

The two-way Granger model is a closer fit to the input data than a one-way causation model (exercise->LS) and than either a cross-lagged or a simultaneous causation model. A one-way model (with 'extra' Granger lags and equality constraints) has these fit readings: CFI=0.960, TLI=0.943, RMSEA=0.047 and SRMR=0.025). Cross-lagged and simultaneous causation models both give the following fit readings: CFI=0.956, TLI=0.937, RMSEA=0.051 and SRMR=0.030. The simultaneous model has negative correlated terms, which are almost certainly a sign of poor model specification, since it is hard to envisage any omitted variable which could somehow correlate positively with exercise and negatively with LS, or vice-versa (Finkel, 1995).

Although they fit the data less well, estimates for BU and TD links in both the cross-lagged and simultaneous causation models are consistent with, although somewhat larger than estimates for our preferred model. The cross-lagged model gives a standardized BU estimate of 0.047 (p<0.001) and a TD estimate of 0.056 (p<0.001). The simultaneous causation model yields standardized BU and TD estimates of 0.064 (p<0.001) and 0.075 (p<0.001) respectively.

Lagrange multiplier tests of the equality constraints in the Granger-style model indicated that all the equality constraints were justified; that is, model fit would not be improved by removing any of them.

#### Frequency of socialising/social participation and LS

A full Granger model for links between LS and the social participation index indicated that both first and second cross- lags of BU and TD relationships were statistically significant. However, the effect sizes of the second lags were very small, so they were omitted.

#### **INSERT TABLE 4 HERE**

A modest degree of two-way causation is found between social participation and LS. The standardized BU link is 0.030 (p<0.001), while the TD link is 0.020 (p<001).<sup>17</sup> The SP link is also significant at 0.020 (p<0.001). The two-way links can again be interpreted as indicating

<sup>&</sup>lt;sup>17</sup> Again, no statistically significant differences were found between men and women, or older and younger people.

positive feedback loops. Active social participation enhances LS, and enhanced LS reinforces social participation. Results are much the same for men and women, and for older and younger people.

The measures of fit again do not give an unambiguous message as between the full Grangerstyle model and the reduced (Figure 2) model; measures which reward parsimony indicate that the reduced model is marginally preferable, whereas measures which give less weight to parsimony suggest that the full model is a slightly better fit. BU and TD estimates for both models are approximately the same, except that in the full model the BU and TD variance accounted for is partitioned between first and second lags of the explanatory variables, rather than being entirely attributed to first lags.

Alternative models - one-way causation, cross-lagged and simultaneous models – fit the data less well. The cross-lagged and simultaneous models both have CFIs of 0.950 and TLIs of 0.928, together with RMSEAs and SRMRs which are somewhat higher than for the Granger-style models. SP links in the simultaneous model are again negative, probably indicating model misspecification.

# A multivariate two-way causal model: links between exercise, social participation, health and LS

So far we have only assessed two-way causation between LS and *x* variables, taking one *x* at a time. However, it is a plausible hypothesis that health, exercise and social participation exert combined and perhaps more or less simultaneous effects on LS. If so, they should be entered at the same step in a causal model. It seemed possible that, in a multivariate model, one or more of these variables, would be shown not to have significant reciprocal effects with LS. Table 5 gives results for our preferred model with imposed equality constraints.

#### **INSERT TABLE 5 HERE**

It appears that health, exercise and active social participation all have statistically significant reciprocal effects with LS. They can combine to change happiness, and changes in happiness then affect subsequent health and subsequent frequency of exercise and social participation.

It is often the case that large structural equation models are a poor fit to the data. It is pleasing that this relatively large model is a satisfactory fit: CFI=0.986, TLI=0.980, RMSEA=0.024 and SRMR=0.027.<sup>18</sup>

#### Exercise and health reinforce each other

As well as forming feedback loops with LS, exercise and self-assessed health reinforce each other. In a model with a Figure 2 structure, the standardised effect of exercise on health is 0.039 (p<0.001) and the effect of health on exercise is 0.022 (p<0.001). These reciprocal effects presumably also contribute to keeping some individuals above their long term average LS for consecutive years, and keeping others below their long term level.

#### Job satisfaction, satisfaction with leisure and LS

In a final model we assess the effects of job satisfaction and satisfaction with leisure on LS. An assumption here is that job satisfaction and satisfaction with leisure should enter into a model of LS at a later causal step than the three *x* variables in our previous multivariate model. This assumption is in line with most research on LS in which domain satisfactions are treated as consequences of conditions like health, and also of variables measuring behavioural choices like social participation and exercise. Again, the estimates given in Table 6 are from our preferred model with constrained equalities.

#### **INSERT TABLE 6 HERE**

Job satisfaction has a significant BU effect on LS; the standardized effect being 0.082 (p<0.001). However, the TD and SP estimates are considerably higher at 0.128 (p<0.001) and 0.281 (p<0.001) respectively. Satisfaction with leisure also makes a significant contribution to LS (BU=0.042 p<0.001), and LS has a reciprocal effect on satisfaction with leisure (TD=0.059 p<0.001). The results suggest that, although there are feedback loops between these domain satisfactions and LS, the main direction of causation is top-down rather than bottom-up.

<sup>&</sup>lt;sup>18</sup> As was the case for some of the models with only one x variable, just one pair of imposed equality constraints in this multivariate model was diagnosed as not strictly justified; the LR test result would be improved if they were dropped. Again, however, the measures of fit which reward parsimony – the TLI and RMSEA - provide countervailing evidence in favour of retaining the constraints.

#### Additional sensitivity tests

Our two-way causal models are 'hybrid' models (Bollen, 2010) in the sense that they include both fixed and random effects, and account for between-person differences, as well as withinperson trajectories over time. Ideally, we would have preferred to check results, using a strictly within-person (fixed effects) estimator. However, when we attempted to do so we ran into problems of model instability of precisely the kind found in previous research. Our hope is that inclusion of 'extra' Granger lags and cross-sectional correlated error terms (SP? in Figure 2) has taken care of bias due to omitted variables, whether those variables exert fixed or time-varying effects. Also the models include the Big Five personality traits; personality traits being the most obvious fixed characteristics that ought to be included in any model of LS.<sup>19</sup> Finally, detailed checks indicated no statistically significant autocorrelated errors for the equations included in our models.

We also ran some models in which time-varying exogenous variables (partner status, unemployed etc) were linked to later waves of *x* and LS, not just to t1 measures. Some of the links proved to be statistically significant, but effect sizes were small and measures of model fit which reward parsimony did not indicate improvements. BU and TD estimates were scarcely affected.

#### DISCUSSION

#### Granger-style models fit the data well, and two-way causation is pervasive

Modified Granger-style models provide a coherent, consistent account of relationships between LS and *x* variables of interest. It appears that in this area of research *two-way causation is pervasive*. Granger-style models have a satisfactory fit to the data, and indeed are a much closer fit than alternative one-way causation, cross-lagged and simultaneous causation models of the kind deployed in previous research. However, we have found that estimates from cross-lagged and simultaneous causation models are broadly consistent with estimates from Granger-style models, at least in the sense that they also indicate two-way causation.

The assumption of one-way causation leads to biased over-estimates of the effects of x variables on LS

<sup>&</sup>lt;sup>19</sup> The 'extra' Granger lags also probably have the effect of taking care of covariance due to omitted variables (Finkel, 1995).

One implication of our findings is that researchers who have assumed one-way causation have produced seriously biased over-estimates of the effects of *x* variables on LS. Our estimates of BU effects in this paper are smaller than found in most previous research. Plainly, this is due to estimating two-way causation, and explicitly allowing for spuriousness, rather than assuming one-way causation. To illustrate this point, consider what happens to the relationship between the self-rated health scale and LS, when one moves from estimating a one-way relationship to two-way causation. The Pearson correlation between the two variables in the SOEP data is 0.381, and it is usual to see standardized multivariate regression estimates not much below this level (Andrews and Withey, 1976; Campbell, Converse and Rodgers, 1976; Argyle, 2001). In our first two-way causation model (Table 2), the estimated BU link is 0.093 (p<0.001) and in our final multivariate model (Table 5) it is 0.091 (p<0.001). Similarly, the Pearson correlation between social participation and LS is 0.133. Our standardized BU estimate in a multivariate model (Table 5) is 0.022 (p<0.001).

Checks for a range of x variables (including some not in this paper) indicate that these two examples are quite typical of what happens to relationships between x and LS when two-way causation and spuriousness are taken into account. It appears that the usual consequence of assuming one-way causation is over-estimation of relationships by factors of four to ten.<sup>20</sup>

# Two-way causation models may partly explain medium term changes in LS...why many people experience multi-year gains and/or losses of LS

The main current challenge for LS researchers is to develop a theory of change. Set-point theory is purely a theory of stability and does not account for evidence from panel surveys which shows that the LS trajectories of many respondents are subject to medium or long term change, and certainly do not fluctuate around a stable set-point.

The suggestion in this paper is that *positive feedback loops* between LS and associated variables may help to account for medium term change. If our models are valid, they provide a preliminary explanation of why an individual might enjoy an extended period of time with a level of LS above his/her own long term average, and then perhaps spend several consecutive years below this long term average.

<sup>&</sup>lt;sup>20</sup> This statement takes no account of measurement error. Typically, measurement error leads to underestimation ('attenuation') of relationships. However, this applies equally to estimates of one-way and two-way causal relationships.

The feedback loops in the models should not be over-interpreted. They might appear to imply that the same people keep getting happier and happier, while others get steadily more miserable. However, since they are not fixed effects (within-person) models, they do not imply that. Rather they indicate how changes (positive or negative changes) may be maintained for an extended period of time. Psychological adaptation mechanisms doubtless come into play and partly counteract the effects of both positive and negative changes. So, for example, one would expect that a change in exercise levels, or a change in health, would have a greater effect on LS in the short term than in the longer term. People partially adapt to almost all changes, but adaptation is often far from complete (Wilson and Gilbert, 2008).

From this perspective one key issue for future research is to explain why some individuals record more or less permanent changes, and 'lock in' at a level of LS substantially different from what they experienced earlier in life. This paper has focussed on medium term change. So far as we know, there is virtually no empirical research accounting for long term change.

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# Figure 2: Two-way causal links between self-rated health and LS: A 5-wave panel model with Granger-causation\* and imposed equality constraints



 Key:
 BU? = bottom-up effects?
 TD? = top-down effects?
 SP? = spurious effects?

 BU effects between consectutive waves were constrained equal to each other (=a), as were TD effects (=b)
 \* 'Extra' Granger-lags are shown by dotted arrows.



1991 1993 1995 1997 1999 2001 2003 2005 2007 2009 1992 1994 1996 1998 2000 2002 2004 2006 2008 2010 0

1991 1993 1995 1997 1999 2001 2003 2005 2007 2009 1992 1994 1996 1998 2000 2002 2004 2006 2008 2010

N

0

## Figure 3: Individual Trajectories of Life Satisfaction: Bar Charts

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1991 1993 1995 1997 1999 2001 2003 2005 2007 2009 1992 1994 1996 1998 2000 2002 2004 2006 2008 2010

0

 $\label{eq:table1} \begin{array}{c} \text{Table 1} \\ \text{Within-Person (Fixed Effects) Regressions Of } LS_{t+1}, LS_{t-1} \text{ etc on } LS_t \text{: Metric} \\ \text{ coefficients with standard errors in parentheses (N=36550)}^{ab} \end{array}$ 

Dependent variable	Independent variable LS <sub>t</sub>
LS <sub>t+1</sub>	0.248*** (0.005)
LS <sub>t-1</sub>	0.256*** (0.005)
LS <sub>t+2</sub>	0.143*** (0.005)
LS <sub>t-2</sub>	0.153 (0.005)
LS <sub>t+3</sub>	0.088*** (0.005)
LS <sub>t-3</sub>	0.096*** (0.006)
LS <sub>t+4</sub>	0.045*** (0.005)
LS <sub>t-4</sub>	0.050*** (0.006)

a. N = person-years.

b. Controls: age, age-squared.

	Metric ML estimates	Standardized ML estimates	Measures of model fü <sup>b</sup>	
Health <sub>t</sub>	0.190***	0.093***	LR Chi-square	3773.20***
>LS <sub>t+1</sub>	(0.005)	(0.003)	(df=136)	
(BU link)				
LSt	0.027***	0.056***	RMSEA	0.027
->Health <sub>t+1</sub>	(0.001)	(0.002)		
(TD link)				
Correlated	0.157***	0.213***	SRMR	0.027
error (SP link)	(0.004)	(0.005)		
			CFI	0.984
			TLI	0.977

Two-Way Causal Links Between Self-Assessed Health and LS (N=35698)<sup>a</sup>

a. N=person years

b. Model stability=0.000; all eigenvalues inside unit circle (Bentler and Freeman, 1983).

	Metric ML estimates	Standardized ML estimates	Measures of model fit <sup>b</sup>	
Exercise <sub>t</sub> >LS <sub>t+1</sub>	0.052*** (0.005)	0.036*** (0.002)	LR Chi- square (df=136)	3329.04***
(BU link)				
LSt	0.010***	0.014***	RMSEA	0.026
->Exercise <sub>t+1</sub>	(0.001)	(0.002)		
(TD link)				
Correlated error	0.024***	0.027***	SRMR	0.022
(SP link)	(0.005)	(0.005)		
			CFI	0.987
			TLI	0.982

# Two-Way Causal Links Between Exercise and LS (N=35244)<sup>a</sup>

a. N=person-years.

b. Model stability=0.000; all eigenvalues inside unit circle (Bentler and Freeman, 1983).

	Metric ML estimates	Standardized ML estimates	Measures of model fit <sup>b</sup>	
Social participation <sub>t</sub> >LS <sub>t+1</sub> (BU link)	0.130*** (0.010)	0.030*** (0.002)	LR Chi-square (df=136)	4252.57***
LS <sub>t</sub> ->Social participation <sub>t+1</sub> (TD link)	0.005*** (0.000)	0.020*** (0.002)	RMSEA	0.029
Correlated error (SP link)	0.007*** (0.002)	0.020*** (0.005)	SRMR	0.024
			TLI	0.980

# Two-Way Causal Links Between Social Participation and LS (N=35722)<sup>a</sup>

a. N=person years
b. Model stability=0.000; all eigenvalues inside unit circle (Bentler and Freeman, 1983).
\*\*\* significant at the 0.001 level

## Table 5:

	Metric ML	Standardized	Measures of model fit <sup>b</sup>	
	estimates	ML estimates		
Health			LR Chi-square (df=348)	7483.02***
$Health_t \rightarrow LS_{t+1}$	0.184***	0.091***	RMSEA	0.024
	(0.005)	(0.003)		
LSt	0.027***	0.055***	SRMR	0.027
->Health <sub>t+1</sub>	(0.001)	(0.002)		
Correlated error	0.157***	0.213***	CFI	0.986
(SP link)	(0.004)	(0.005)		
$Exercise_t$			TLI	0.980
Exerciset	0.026***	0.018***		
$\rightarrow LS_{t+1}$	(0.003)	(0.002)		
LSt	0.010***	0.015***		
->Exercise <sub>t+1</sub>	(0.001)	(0.002)		
Correlated error	0.022***	0.025***		
(SP link)	(0.005)	(0.005)		
Social participation				
Social	0.097***	0.022***		
>LS <sub>t+1</sub>	(0.010)	(0.002)		
LS <sub>t</sub> ->Social participation <sub>t+1</sub>	0.005***	0.020***		
	(0.000)	(0.002)		
Correlated error	0.007***	0.020***		
	(0.002)	(0.005)		

Two-Way Causal Links: LS Related to Health, Exercise and Social Participation (N=35067)<sup>a</sup>

a. N=person years. b. Model stability=0.000; all eigenvalues inside unit circle (Bentler and Freeman, 1983). \*\*\* significant at the 0.001 level

# Two-Way Causal Links: LS related to Job Satisfaction and Satisfaction with Leisure $(N=11911)^a$

	Metric ML estimates <sup>a</sup>	Standardized ML estimates <sup>a</sup>	Measures of model fit <sup>b</sup>	
Job satisfaction				
Job satis.t	0.070***	0.082***	LR Chi-square	1640.23***
->LS <sub>t+1</sub>	(0.004)	(0.005)	(di=232)	
(BU link)				
LS t ->	0.155***	0.128***	RMSEA	0.023
Job satis.t+1	(0.006)	(0.005)		
(TD link)				
Correlated	0.531***	0.281***	SRMR	0.024
error (SP link)	(0.018)	(0.008)		
Satisfaction with leisure			CFI	0.985
Leisure satis. t.	0.033***	0.042***	TLI	0.978
->LS <sub>t+1</sub>	(0.003)	(0.004)		
(BU link)				
LS->Leisure	0.076***	0.059***		
(TD link)	(0.006)	(0.004)		
Correlated	0.313***	0.171***		
error (SP link)	(0.017)	(0.009)		

a. N = person-years b. Model stability=0.000; all eigenvalues inside unit circle (Bentler and Freeman, 1983).