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## Inflation, Taxation and Capital Cost

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No. 19, 1979

## INFLATION, TAXATION AND CAPITAL COST

by

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Revised January, 1979

Abstract: In times of inflation, most existing systems of taxation introduce new distortions into the allocation of resources. In this paper, the effects of inflation via taxes on the firm's cost of capital are analyzed. The taxes considered are the corporate income tax and household taxes on dividends and capital gains. The first part of the paper presents the model of a firm aiming at maximizing the value of its shares in the portfolios of the stockholders. The nominal cost of capital of this firm, financed by equity and debt in a given proportion, is derived. The cost of equity and debt are then taken at their nominal values as the firm observes them on the capital market.

We then analyze the net real cost of capital, where market rates of return are adjusted for inflation. This makes it possible to determine the net effects of inflation on capital cost, recognizing several counteracting tendencies operating through the tax system. It turns out that for most reasonable assumptions, the real cost of capital will fall as a result of inflation when both profit tax and taxes on dividends and capital gains are taken into account.

In the last section finally, we present different ways of indexing the system of taxation to insulate it from inflationary distortions.

## Part I

### I:1 The problem<sup>1</sup>

The world inflation of the 1970's has called forth a growing litterature on the causes as well as the effects of the inflation surge. The litterature on the effects of inflation has been partly normative by dealing with indexing the economy to avoid distortions added by inflation - to already existing ones - through the tax system.

A large part of the recent litterature on the distorting effects of inflation deals with profit taxation and the cost of capital. Another part deals with inflation and taxation of income in the household sector.

In this paper we deal both with the profit taxation of the business sector and the income taxation of the household sector. The central concept of our analysis is the cost of capital and our intention is to make a detailed analysis of how taxation influences capital cost in times of inflation.

When there is inflation there are distortions produced by the tax system because not all real costs are deductible for taxation and because not all real income is included in taxable profits. Also costs of debt and equity become distorted.

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<sup>1</sup>We are grateful to Martin Feldstein, National Bureau of Economic Research and to Sven-Erik Johansson, Stockholm School of Economics, for valuable criticism and helpful suggestions.

It has been contended that the net outcome of these distortions is that inflation increases the required real before tax rate of return on investment - the gross cost of capital.<sup>1</sup> The results of our analysis points in the opposite direction. It seems that for most reasonable assumptions the real cost of capital will fall as a result of inflation when both profit tax and personal taxes on dividends and capital gains are taken into account.

When the effects of inflation on capital accumulation of private firms are analyzed in the literature the analysis is often limited to the system of profit taxation. Two counteracting tendencies operate through the corporate tax system in times of inflation. First, increased borrowing costs, due to inflation, are deductible. Second, because depreciation allowances are based on historical costs, inflation undermines their real significance. Therefore, part of capital consumption may become included in the tax base (or accelerated depreciations are diminished in real terms).<sup>2</sup>

Another interesting line of development of the analysis of inflationary effects through the tax system is represented by Feldstein and different coauthors.<sup>3</sup> These authors include also income taxation in the household sector and they use a general equilibrium framework,

<sup>1</sup> Tideman and Tucker in a recent Brookings volume claim that inflation increases capital cost for all kinds of investment. Their numerical analysis rests upon a model that is not fully presented in their paper. It seems, though, that the objective of their model firm is not to maximize stockholders' wealth, because depreciation allowances are not discounted by stockholders' required rate of return - the cost of equity - but by the average cost of equity and debt (less the rate of inflation). See Tideman and Tucker [1976], especially appendix A and also Nelson [1976].

<sup>2</sup> This is recognized by Sumner [1973] in his short remarks on the effects of inflation on capital cost. Contrary to Tideman and Tucker, Sumner therefore holds that the net result is inconclusive. At low inflation rates an increased rate of inflation would tend to increase capital cost, whereas capital cost would be decreased at high rates of inflation by further increases. See Sumner, op cit, p 30.

<sup>3</sup> See Feldstein [1977], Feldstein, Green and Shesinsky [1978] and Feldstein and Summers [1978].

(as compared to the above authors whose models are more partial) to study how inflation influences i.e. costs of equity and debt and the debt-to-equity ratio. But with the general equilibrium framework the corporate tax system is stylized and does not allow a detailed analysis of how capital cost is influenced by tax laws in times of inflation. For instance, accelerated depreciations are disregarded, which restricts the results. Another (implicit) assumption is that one dollar of retained earnings creates a capital gain of one dollar. This would not be the case - due to differential taxation of dividends and capital gains - on an optimal growth path.

When the distortionary effects of inflation on capital cost via the tax system are analysed, different norms can be used. The inflationary situation can be compared to resource allocation in a world without inflation and free of tax distortions.<sup>1</sup> The other way is to compare capital cost with the inflationary distortions introduced in times of inflation by the construction of the tax system to capital cost with those distortions present that are due to the tax system at zero rate of inflation.<sup>2</sup>

If the tax system represents a deliberate choice on the part of the government to intervene in the allocation of resources but the tax system was constructed without regard to inflation, this second norm should be used. The idea that depreciation rules for tax purposes should reflect a real economic loss of value has a very limited scope in Sweden as well as in several other countries. By way of accelerating depreciation allowances governments make effective tax rates lower than statutory tax rates, not primarily to compensate for historical cost depreciation in times of inflation<sup>3</sup>.

<sup>1</sup> This norm is used by Sandmo [1974] in his short comments on inflation.

<sup>2</sup> This norm is inherent in the numerical analysis of Tideman and Tucker [1976].

<sup>3</sup> See Bergström [1977] and Södersten [1978].

Therefore, when we discuss effects of inflation on capital cost our main norm of comparison is capital cost with those distortions present that are due to taxation of profits and household income at zero rate of inflation. We also discuss briefly the over all norm of capital cost with no tax distortions (and a zero rate of inflation).

Our paper contains a detailed (partial equilibrium) analysis of the counteracting effects of inflation on the cost of capital. Our model is in the Jorgenson<sup>1</sup> tradition of a firm aiming at maximizing the value of its shares in the portfolios of stockholders. The nominal cost of capital of this firm, financed by equity and bonds in a given proportion, is derived. The cost of equity and debt are then taken at their nominal values as the firm is assumed to observe them on the capital market.

We then analyse the net real cost of capital, where market rates of return are adjusted for inflation. This allows us to determine the net effects of inflation on capital cost. Different ways of indexing taxation to insulate the cost of capital from inflationary distortions are discussed.

The analysis is first performed for corporate taxation only. Thereafter the different cases are worked through for corporate taxation as well as personal taxes. In both cases we proceed by first presenting the model used in the analysis.

## I:2. The model

To analyse how inflation affects capital cost we will use the model presented in Bergström [1976] and Bergström-Södersten [1977] with some special assumptions added. First, we will assume that there is an expected rate of inflation of  $100 \cdot p$  % on the price of capital goods,  $P_k(s)$ . Therefor we have  $P_k(s) = P_k(v)e^{p(s-v)}$ . Second, we assume that the firm keeps a constant debt-to-equity ratio.

<sup>1</sup> Jorgenson himself early introduced inflation into his model, but because he used depreciations for tax purposes on replacement values and did not have explicit debt financing the essence of the problem with inflation was concealed. Se Jorgenson [1965] and [1968].

This last policy is introduced by assuming that the book value of outstanding debt,  $S(s)$ , related to the current value of the capital stock,  $P_k(s)K(s)$ , is a constant:

$$\frac{S(s)}{P_k(s)K(s)} = h.$$

We also assume that the firm finances its gross investments by debt in the same relation,  $h$ , so that gross borrowing is  $hP_k(s)I(s)$ , where  $I(s)$  is gross real investment.

Therefore, without any amortization the stock of debt at point in time,  $s$ , would amount to

$$\int_{-\infty}^s hP_k(v)I(v)dv.$$

It is assumed that the stock of capital,  $K(s)$ , depreciates at the exponential decay rate,  $\delta$ , and as capital gains per unit of capital through price inflation is  $p$ , the rate of amortization, to keep the debt-equity ratio constant, is  $(\delta-p)$ :

$$\begin{aligned} S(s) &= \int_{-\infty}^s P_k(s)e^{-p(s-v)}hI(v)e^{-(\delta-p)(s-v)}dv \\ &= P_k(s) \int_{-\infty}^s hI(v)e^{-\delta(s-v)}dv \\ &= hP_k(s)K(s). \end{aligned}$$

Therefore, by amortizing the debt at the rate of capital depreciation less the rate of inflation, when a constant fraction of gross investment is financed by loans, as assumed here, the debt-ratio is kept constant<sup>1</sup>.

<sup>1</sup> With  $S(s) = hP_k(s)K(s)$  and  $P_k(s)K(s)$  equal to debt plus equity the debt to equity ratio is simply  $h/(1-h)$ . We consider here only the book value of debt, not the market value.

Failure to adjust the rate of amortization to the rate of capital gains through inflation would obviously result in changes in the average debt to equity ratio. For the implication of this, see p 7, note 3.

Note also that the rate of amortization can be negative -  $(\delta-p) < 0$  - meaning that the firm borrows on its appreciated capital stock (in excess of the gross borrowing to finance gross investment).

It will be assumed that the firm can deduct a fraction  $\gamma$  of the book value of capital,  $D(s)$ , from profits for tax purposes and that profits so defined are taxed at the rate  $\tau$ . The book value of capital is made up of investments at historical costs.

The management is assumed to maximize the value of the firm in the portfolios of the stockholders and to observe a rate of return,  $k$ , demanded by stockholders for investment in common stocks.

With product price  $P(s)$ , wage rate  $w(s)$  labor input  $L(s)$ , and interest rate  $i(s)$ , the objective is to maximize the present value of all future cash flows<sup>1</sup>

$$J = \int_{s=t}^{\infty} e^{-k(s-t)} \left[ (1-\tau(s)) \{P(s)F[K(s), L(s)] - w(s)L(s) - i(s)hP_k(s)K(s)\} - (\delta-p)hP_k(s)K(s) - (1-h)P_k(s)I(s) + \gamma\tau(s)D(s) \right] \quad (I:1)$$

where  $F[K(s), L(s)]$  is a decreasing return to scale production function.

This maximization may not violate the two equations of motion:

$$\dot{K}(s) = I(s) - \delta K(s)$$

$$\dot{D}(s) = P_k(s)I(s) - \gamma D(s).$$

This is a control problem with control variables labor input,  $L(s)$  and gross investment,  $I(s)$  and the hamiltonian,  $H$ :

$$H = e^{-k(s-t)} \left[ (1-\tau(s)) \{P(s)F[K(s), L(s)] - w(s)L(s) - i(s)hP_k(s)K(s)\} - (\delta-p)hP_k(s)K(s) - (1-h)P_k(s)I(s) + \gamma\tau(s)D(s) + \lambda_1(s) \{I(s) - \delta K(s)\} + \lambda_2(s) \{P_k(s)I(s) - \gamma D(s)\} \right]. \quad (I:2)$$

We assume that this (properly defined) control problem has a solution which calls for decreasing returns to scale in production. We disregard, int.al., that there would be instantaneous adjustments to the optimal path with infinitely large investment or disinvestment.

<sup>1</sup> Parameters assumed constant are written without time indices in.

The necessary conditions used for (I:2) gives:<sup>1</sup>

$$\frac{\partial H}{\partial I} = e^{-k(s-t)} [-(1-h)P_k + \lambda_1 + \lambda_2 P_k] = 0 \quad (I:3)$$

and

$$\dot{\lambda}_1 + (1-\tau(t))(PF_k - hP_k) - (\delta-p)hP_k = \lambda_1(k+\delta) \quad (I:4a)$$

$$\dot{\lambda}_2 + \tau(t)\gamma = \lambda_2(k+\gamma). \quad (I:4b)$$

By solving the differential equations (I:4) we get for  $k$ ,  $\delta$  and  $\gamma$  constant (but  $\tau(t)$  still a function of time):

$$\lambda_1 = \int_{s=t}^{\infty} [(1-\tau(s))(PF_k - hP_k) - (\delta-p)hP_k] e^{-(k+\delta)(s-t)} ds \quad (I:5a)$$

$$\lambda_2 = \int_{s=t}^{\infty} \tau(s)\gamma e^{-(k+\gamma)(s-t)} ds \quad (I:5b)$$

Therefore  $\lambda_1$  is the capital value, internal to the firm, of getting another unit of capital, recognizing that a new unit of capital gives rise to future (after tax) marginal value productivities and debt services.  $\lambda_2$  is the capital value of all future tax savings from depreciation charges following upon an increase of the book value of capital by one unit.

Condition (3) above says then that the capital value of expected future cash flows, due to the investment of one unit of capital,  $\lambda_1 + \lambda_2 P_K$ , must equal the present loss of cash flow from the investment outlay,  $(1-h)P_K$ .

Noting that condition (3) must hold over time all along the optimal path of the firm, it follows that

$$\dot{\lambda}_1 = (1-h-\lambda_2)\dot{P}_K - P_K\dot{\lambda}_2 \quad (I:6)$$

<sup>1</sup> Time indices are skipped in most cases to save space. The optimal condition concerning labor input is not needed for our purposes.

at all points in time. Introducing the assumption that the firm expects future tax rates  $\tau$  (as well as rates of depreciation for tax purposes) to be constant makes  $\dot{\lambda}_2$  in (I:6) equal zero. By substituting (I:4) into (I:3) and using (I:6) with the assumption  $\dot{\lambda}_2=0$ , we may then solve for  $PF'_K/P_K$ , which is the gross rate of return before tax on real investment on the optimal path

$$\frac{PF'_K}{P_K} = \delta - p + ih + \frac{k}{1-\tau} \left[ 1 - h - \frac{\tau[\gamma - (\delta-p)]}{k+\gamma} \right]. \quad (I:7)$$

The formula (I:7) gives the minimum gross rate of return that the firm can afford to earn on new investment, leaving shareholders no worse off, i.e. the gross cost of capital<sup>1</sup>.

### I:3. Nominal capital cost

By subtracting from gross capital cost, given by (I:7), the rate of economic depreciation we get the net cost of capital, here called  $r$ . Following established tradition, we will define the economic depreciation of an investment as the change in nominal value<sup>2</sup>. This depreciation charge, which maintains intact the original nominal amount invested, is  $\delta-p$  times replacement cost, because capacity depreciates at the "exponential decay" rate  $\delta$  and because capital value appreciates at the rate  $p$ .

By this definition of economic depreciation, then, net capital cost,  $r$  is also the internal rate of return on the marginal investment project, i.e. a project with zero capital value at net cost of capital  $r$ . Subtracting  $(\delta-p)$  from (I:7) gives<sup>3</sup>

$$r = ih + \frac{k}{1-\tau} \left[ 1 - h - \frac{\tau[\gamma - (\delta-p)]}{k+\gamma} \right]. \quad (I:8)$$

<sup>1</sup> Letting  $PF'_K/P_K = c$ ,  $P_K c$  then stands for what has been called the user cost or rental price of capital. Cf. Jorgenson & Siebert [1968].

<sup>2</sup> Cf. Samuelson [1964].

<sup>3</sup> If the rate of debt amortization would be kept at  $\delta$  instead of  $\delta-p$  an extra term would be added to (I:8), namely

$$\frac{ph[\frac{k}{1-\tau} - i]}{k+\delta}$$

which means that the inflation induced fall in the average debt to equity ratio would, ceteris paribus, increase, leave unaffected

or reduce capital cost, depending on whether  $\frac{k}{1-\tau} \geq i$ . Cf p 4.

Now, by investing one dollar on the capital market by buying a bond, one can enjoy the consumption of  $i$  dollars without impairing the original nominal amount invested. Therefore, our interpretation of the net cost of capital  $r$  as the nominal rate of return of the marginal investment makes possible a direct comparison between  $r$  and the nominal rates of return on the capital market,  $i$  and  $k$ .<sup>1</sup>

Now, for the interpretation of (I:8), let us first assume that the rate of depreciation for tax purposes,  $\gamma$ , equals the rate of economic depreciation,  $\delta - p$ . Since  $h$  is the portion of the firm's investment financed by borrowing,  $(1-h)$  is the portion financed by equity capital making the net cost of capital a weighted average of the cost of debt and the (before tax) cost of equity. If instead  $\gamma > \delta - p$ , i.e. the firm is allowed to defer taxes through acceleration of depreciation charges relative to our norm of economic depreciation, the cost of equity is weighted by

$$1 - h = \frac{\tau[\gamma - (\delta - p)]}{k + \gamma} . \quad (I:9)$$

This weight, in turn, is the portion of the firm's investments financed by equity capital.

Thus  $\gamma > \delta - p$  implies that a third part of capital growth,  $\tau[\gamma - (\delta - p)]/(\gamma + k)$ , is financed by deferred taxes, adding the weights up to one. However, this last cost of finance is zero and consequently it does not show up in (I:8).

Now, to focus on the effects of inflation, the last term of (I:9) may be split up into

$$\frac{\tau[\gamma - (\delta - p)]}{k + \gamma} = \frac{\tau[\gamma - \delta]}{k + \gamma} + \frac{\tau p}{k + \gamma}$$

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<sup>1</sup> This implies that compensation for real loss of value of investments on the part of lenders and suppliers of equity capital is contained in the nominal rates  $i$  and  $k$ . These nominal market rates will be adjusted in times of inflation to contain an element of real depreciation. See section 4 below.

Therefore, in the formula for capital cost there is a negative term due to inflation, amounting to

$$-\frac{k}{(1-\tau)(k+\gamma)} \frac{\tau p}{(1-\tau)(k+\gamma)} = -\frac{\tau p(k+\gamma) - \tau p \gamma}{(1-\tau)(k+\gamma)}$$

Net capital cost can therefore be rewritten

$$r = ih + \frac{k}{1-\tau} \left[ 1 - h - \frac{\tau[\gamma-\delta]}{k+\gamma} \right] - \frac{\tau p}{1-\tau} + \frac{\tau \gamma p}{(1-\tau)(k+\gamma)} \quad (I:10)$$

The first two terms of (I:10) corresponds to capital cost without inflation<sup>1</sup>. The third term may be interpreted as a reduction (ceteris paribus) of capital cost due to the fact that the rate of depreciation for tax purposes is not reduced by the rate of inflation itself, to what we have called "economic depreciation", ( $\delta-p$ ). More precisely, the third term of (I:10) is a result of the fact that capital gains are not taxed (if only economic depreciations were allowed to be deducted for tax purposes, capital gains would be taxed). The fourth term, finally, represents the consequence for capital cost of the fact that depreciations are calculated on the basis of historical costs rather than replacement costs. Inflation reduces the real base on which depreciation charges are calculated.

To summarize our analysis of the nominal net cost of capital in times of inflation we state that two counteracting tendencies operate:

- 1) Capital gains are not taxed. This tends to reduce capital cost.
- 2) The real tax base for depreciations is reduced. This tends to increase capital cost.

The net outcome of (1) and (2) can not be determined, however, without assumptions as to how inflation affects market rates of return  $k$  and  $i$ . This is the subject of the next section.

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<sup>1</sup> Of course market rates,  $k$  and  $i$ , would be different in times of inflation compared to times of stable prices.

#### I:4. Real capital cost

For empirical purposes, e g estimating investment functions, equation (10) gives the appropriate measure of capital cost. However, for the analysis of inflationary distortions on resource allocation, nominal net cost of capital,  $r$ , must be transformed into a real cost of capital to be compared to the cost of capital at zero inflation. Real net cost of capital,  $r^*$ , will be defined as

$$r^* = r - p$$

Actually decomposing net cost of capital,  $r$  in (10), into a real part corresponding to capital cost without inflation and another part that is due to inflation, is the task of general equilibrium analysis, since the effects of inflation on market rates  $k$  and  $i$  need to be known.

These market rates will react to inflation in a complex way, reflecting both borrowers' and lenders' adjustments to inflation (and taxation). This paper deals with one side of this market, borrowers' reactions to inflation when nominal interest - but not equity cost - is deductible and when taxable profit is determined by deductions reflecting depreciations based upon historical investment costs.

On the supply side there are substitution effects between savings and consumption as well as between investment alternatives because inflation influences yield differentials - nominal before tax as well as real after tax - again because nominal interest is taxed and capital gains are taxed at relatively low marginal rates or not at all.

These are the problems analyzed in a series of papers by Feldstein et al.<sup>1</sup>

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<sup>1</sup> See Feldstein [1976], Feldstein, Green and Sheshinsky [1978] and Feldstein & Summers [1978].

For our purposes it will suffice to simply assume that the nominal rates of return will rise with the rate of inflation. This means that we study what happens to the cost of capital when there is inflation but when real rates of return to equity and debt stay constant, i.e.:

$$k = k^* + p, \quad i = i^* + p$$

where starred variables indicate cost of equity and debt, respectively, at zero inflation<sup>1</sup>.

Using our definition of the firm's real net cost of capital and the above assumptions regarding the effects of inflation on the nominal costs of equity and debt we get

$$r^* = i^*h + \frac{k^*}{1-\tau} \left[ 1-h - \frac{\tau[\gamma-\delta]}{k^*+\gamma} \right] + \frac{\tau p \gamma}{(1-\tau)(k^*+p+\gamma)} \left[ \frac{k^*+\delta}{k^*+\gamma} \right] - \frac{\tau}{1-\tau} p + \frac{\tau}{1-\tau} p(1-h) \quad (I:11)$$

The first two terms of  $r^*$  is net capital cost at zero inflation recognizing the possibility that the tax laws may provide for acceleration of depreciation charges ( $\gamma > \delta$ ). Relative to this norm of constant prices, the effects of inflation on the firm's real net capital cost is captured by the last three terms. For the first two, the interpretation closely follows that given in connection with (I:10): Inflation on the one hand brings about a real reduction in the base on which depreciation charges are taken, assuming that tax depreciation is calculated on historical cost. On the other hand, not taxing capital gains results in a reduction in real capital cost.

The last term of (11)  $\frac{\tau p(1-h)}{1-\tau}$ , reflects the assumption that (after tax) cost of equity rises with  $p$  and that this increase is not deductible for tax purposes. This effect partially offsets the reduction in capital cost from not taxing capital gains. For a complete offset, however, tax laws should also provide for a restriction in the deductibility of interest costs, allowing only deduction of real interest,  $i^*$ .

<sup>1</sup> It seems, in fact, that the adjustment of nominal interest rates due to inflation would be an approximate increase by the rate of inflation in the Fisherian tradition, although this is a net outcome of complex interactions due to taxation on both borrowers' and lenders' sides of the market. See Feldstein and Summers [1978].

Now, the untaxed capital gain and the taxed increased cost of equity - the fourth and fifth terms added - result in a net lowering of capital cost by  $\frac{\tau ph}{1-\tau}$ , which, in turn, can be interpreted as the effect of allowing the inflation increased interest on debt to be deductible. We see then, that the inflationary effects via the tax system can be described in two different ways.

The first one says that capital cost is lowered since capital gains are not taxed and raised because the inflation increased cost of equity is not a deductible cost to the firm. The other way, which states the net of these two effects, says there is a fall in real capital cost due to allowing the firm to deduct full interest on debt when determining taxable profits.

Reformulating (I:11) in line with the last interpretation yields

$$r^* = i^*h + \frac{k^*}{1-\tau} \left[ 1-h - \frac{\tau[\gamma-\delta]}{k^*+\gamma} \right] + \frac{\tau p \gamma}{(1-\tau)(k^*+p+\gamma)} \left( \frac{k^*+\delta}{k^*+\gamma} \right) - \frac{\tau ph}{1-\tau} \quad (I:12)$$

making it evident that the net effect of inflation on the firm's real cost of capital depends on two opposing forces: The current practice of basing depreciation charges on historical cost vs allowing the firm to deduct nominal cost of debt - including the part that constitutes compensation to lenders for inflation (p).

Real net cost of capital  $r^*$ , therefore, will rise, remain unaffected or fall, depending on

$$h < \frac{\gamma}{k^*+p+\gamma} \left[ \frac{k^*+\delta}{k^*+\gamma} \right].$$

For instance, letting  $k^* = 3\%$ ,  $p = 7\%$ ,  $\gamma = 20\%$  and  $\delta = 10\%$ , - not fully unreasonable figures for Swedish industry in the mid 70's - a firm normally financing  $> 37.6\%$  of its capital growth by debt (h), would find investment incentives improve as a result of inflation. The advantage from deducting that part of the nominal cost of debt, constituting an inflationary compensation, would outweigh the loss from historical cost depreciation.

Table 1 extends this example to include several alternatives regarding rates of capacity depreciation ( $\delta$ ) and depreciation for tax purposes ( $\gamma$ ) as well as the rate of inflation (p). The table indicates values of h above which inflation reduces real cost of capital. An indicated value of h in the table says that all firms with more of its total capital financed by debt will get a lower capital cost by inflation.

It may be noted that the critical values of  $h$  falls as the rate of inflation increases. Thus, at high rates of inflation even firms with low debt financing would find their real costs of capital fall as a result of inflation.

Table 1. Ratio of debt to total capital balancing counteracting effects on capital cost

p	$\delta = 0.05$		$\delta = 0.10$	
	$\gamma = 0.05$ (1)	$\gamma = 0.10$ (2)	$\gamma = 0.10$ (3)	$\gamma = 0.20$ (4)
0.02	0.50	0.41	0.67	0.45
0.05	0.38	0.34	0.56	0.40
0.07	0.33	0.31	0.50	0.38
0.10	0.28	0.26	0.43	0.34

Comparing the first and third columns of table 1 brings out another result regarding the effects of inflation on investment projects of different lengths. It takes a higher  $h$  to compensate for the loss due to historical cost depreciation the higher the rate of capacity depreciation ( $\delta$ )<sup>1</sup>. Therefore, in times of inflation, historical cost depreciation discriminates against short lived investments (with a high  $\delta$ )<sup>2</sup>.

We can summarize the effects of inflation on real capital cost via the corporate tax system as follows:

- (1) Inflation increases capital cost because depreciation charges are taken on historical cost. This effect is stronger, the shorter the investment period.
- (2) Inflation decreases capital cost because deduction of the nominal cost of debt is allowed. The higher the debt to equity ratio, the stronger is this capital cost decreasing effect of inflation.

<sup>1</sup> By comparing the first column ( $\delta=.05, \gamma=.05$ ) with the third ( $\delta=.10, \gamma=.10$ ) we compare investments of different life lengths when there is no deferral of corporate taxes due to accelerated depreciations.

<sup>2</sup> This is due to our assumption of amortization.

## Part II

### II:1 Shareholder taxation and capital cost

In part I of this paper we did not take into account that capital income in the corporate sector of the economy is taxed twice. On top of the corporate profit tax dividends are taxed in the household sector at stockholders' marginal rate of income tax. To the extent that retained earnings lead to capital gains on corporate stocks these are also taxed in the household sector, albeit at a relatively low rate.<sup>1</sup>

In this part of the paper we pose the very same questions as we did in the first part, but we take into account the so called "double taxation" of corporate source income.

Now, let  $k$  represent stockholders' rate of return on alternative financial investments. This rate of return is assumed to be taxed as personal income at the marginal income tax rate,  $T$ , of the "representative" stockholder. Therefore stockholders' required net rate of return is  $k(1-T)$ .<sup>2</sup>

A further assumption here about the cost of equity to the firm,  $k(1-T)$ , is that  $k$  is independent of  $T$ . This means that personal taxation of equity income cannot be shifted. If investors have no alternatives, international or national, to avoid a general personal income tax that is applicable to all sources of household income this is a reasonable assumption. In this way, from the management

<sup>1</sup> The analysis here draws upon Södersten [1977] and Bergström and Södersten [1976]. It is not implied by our assumptions that there is a one-to-one relation between retained earnings and capital gains. This relation depends on the differential taxation of dividends and capital gains. See Bergström and Södersten [1976].

<sup>2</sup> For many countries this assumption may obviously be questioned, bearing in mind e.g. that capital gains on alternative investments open to households often receive a preferential tax treatment.

(firm) point of view, an increased personal taxation lowers the cost of equity because the net rate of return to equity which shareholders apply when discounting expected cash flow in evaluating shares, is lowered.

Following Swedish (and U.S.) tax rules we let dividends from the corporate sector be taxed at the marginal income tax rate,  $T$ , and (accrued) capital gains,  $dV(t)/dt$ , at a lower rate,  $\alpha T$ , ( $\alpha < 1$ )<sup>1</sup>. The value of the firm's common stocks,  $V(t)$ , can now be formulated as the capital value of all future cash flow (expected with certainty):

$$V(t) = \int_{s=t}^{\infty} \{U(s)(1-T) - \alpha T \frac{dV(s)}{ds}\} e^{-k(1-T)(s-t)} ds \quad (\text{II:1})$$

where  $U(t)$  is the sum of dividends<sup>2</sup> and the second term under the integration sign is the assumed tax on accrued capital gains. (By this formulation we disregard new issues of common stocks, which requires  $U(t) \geq 0$ , contrary to the case above with profit taxes only.)

The capital value (II:1) can be reformulated to a simpler form<sup>3</sup>

$$V(t) = \int_{s=t}^{\infty} \frac{U(s)(1-T)}{1-\alpha T} e^{-\frac{k(1-T)}{1-\alpha T}(s-t)} ds \quad (\text{II:2})$$

Dividends  $U(t)$  are already defined by the bracketed term in formula (I:1), p.5 of this paper. By insertion of this expression for  $U(t)$  in (II:2), we get an expression for the value of the firm in stockholders' portfolios with regard to the profit tax, the personal income tax and the capital gains tax.

<sup>1</sup> The parameter  $\alpha$  takes care of the fact that the rate of capital gains tax is lower than the marginal rate of income tax and further that in practice capital gains are taxed only upon realization, meaning that the effective rate is lower than the statutory rate when the latter is transformed to a tax on accruals (which in turn presupposes known holding periods). See Bailey [1969].

<sup>2</sup> This formulation presupposes that all expectations are held with certainty and that shareholders are identical.

<sup>3</sup> Take the derivative of  $V(t)$  in (II:1) with respect to the lower limit of integration, giving

$$\frac{dV(t)}{dt} = - \{U(t) - \alpha T \frac{dV(t)}{dt}\} + k(1-T)V(t)$$

which can be rewritten as

$$\frac{dV(t)}{dt} = \frac{k(1-T)}{1-\alpha T} V(t) - U(t)(1-T)$$

From the solution of this differential equation we get (II:2).

Capital cost can now be derived in a manner similar to that of part I of this paper. The procedure will not be repeated here.

A complication should be mentioned, though. Even if investments are reversible there will now be a bound - an upper bound - on the volume of investment, due to our financial assumptions.

With a constant debt-to-equity ratio gross investments will be limited to the amount given by the volume that absorbs all retained earnings as the equity financed part. To invest more than this would call for new issues, a possibility we have excluded (here, but not in the case above of profit taxation only) in order to simplify the analysis.

Nevertheless, we treat the present problem as if there were no bound on the investment plan meaning that we study only free intervals where bounds are ineffective.<sup>1</sup>

We proceed, then, as if there were no bounds and after substitution for  $U(t)$  from (I:1) in (II:2) and using the same procedure as in part I of this paper we can compute the nominal net cost of capital (to be compared with I:8) as

$$r = ih + \frac{k(1-T)}{(1-\tau)(1-\alpha T)} \left[ 1 - h - \frac{\tau[\gamma - (\delta - p)]}{\frac{k(1-T)}{1-\alpha T} + \gamma} \right] \quad (\text{II:3})$$

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<sup>1</sup>

Appelbaum and Harris [1978] have studied control problems with both upper and lower bounds on the investment plan. In free intervals "myopic rules" of the unbounded problem are still operative. See also Arrow [1964] and [1968].

## II:2 Double taxation and real capital cost

The next step is to assume, again, that the nominal rate of interest,  $i$ , and stockholders' nominal required rate of return,  $k$ , increase with the rate of inflation such that  $i = i^* + p$  and  $k = k^* + p$ , where again  $i^*$  and  $k^*$  express real rates. Note here that our assumption that the net rate of return,  $k(1-T)$ , is used in discounting means that the inflation compensating part of the nominal rate of return on stockholders' alternative investments,  $k$ , is also taxed at the marginal rate of income tax,  $T$ .

Substituting  $k^*+p$  and  $i^*+p$  for  $i$  and  $k$  in (II:3) gives after some manipulations the basic result of our analysis:

$$\begin{aligned}
 r^* = i^*h^* + \frac{k^*(1-T)}{(1-\tau)(1-\alpha T)} & \left[ 1 - h - \frac{\tau(\gamma-\delta)}{\frac{k^*(1-T)}{1-\alpha T} + \gamma} \right] + \\
 \frac{\tau p \gamma}{(1-\tau) \left[ \frac{(k^*+p)(1-T)}{1-\alpha T} + \gamma \right]} & \left[ \frac{\frac{k^*(1-T)}{1-\alpha T} + \delta}{\frac{k^*(1-T)}{1-\alpha T} + \gamma} \right] - \frac{\tau p h}{1-\tau} \\
 - \frac{(T-\alpha T)p}{(1-\tau)(1-\alpha T)} & \left[ 1 - h - \frac{\tau \gamma}{\left[ \frac{(k^*+p)(1-T)}{1-\alpha T} + \gamma \right]} \frac{(\gamma-\delta)}{\left[ \frac{k^*(1-T)}{1-\alpha T} + \gamma \right]} \right]
 \end{aligned} \tag{II:4}$$

This is the real net cost of capital with regard to both profit taxation and personal income and capital gains taxes. We see that the personal taxes have substantially complicated the expression for real capital cost compared to that with regard to profit taxation only (compare (II:4) to (I:12)). The different terms of (II:4), however, still have an intuitively clear economic interpretation.

The first two terms represent the net cost of capital without inflation. This real net cost of capital at zero inflation is our norm of comparison for the further analysis. The third term represents the capital cost increasing effect, in times of inflation, due to historical cost depreciations (as compared to replacement cost depreciation, inherent in the inflation free cost of capital. Cf. the third term of (I:12)).

The fourth term shows that capital cost is reduced, because the full nominal interest on debt is deductible against corporate profits, whereby in fact the "real rate of amortization",  $p$ , is deductible for taxation.

The fifth awkward looking term has to do with stockholders' taxation. It represents, on the one hand, a reduction of capital cost due to the fact that stockholders are taxed at marginal income tax rate  $T$  also for that part of the nominal rate of return,  $k$ , on alternative financial investments that is a compensation for inflation,  $p$ . Stockholders' real rate of return net of tax is then  $k(1-T) - p = k^*(1-T) - pT$ , implying a reduced cost of equity to the firm. On the other hand, there is an increase of capital cost following from the fact that nominal capital gains on stockholdings are taxed at the rate  $\alpha T$ .

It may be noted that the term added by the introduction of personal taxes tends to lower real capital cost, provided capital gains receive a preferential tax treatment (i.e.  $\alpha T < T$ ). In other words, taxing stockholders' nominal rate of return on alternative financial investments at marginal tax rate  $T$ , outweighs the capital cost increasing effect of taxing nominal capital gains on corporate stock.<sup>2</sup>

Expression II:4 makes it evident that the net effect of inflation on real capital cost depends on four opposing forces. These include current practice of basing depreciation allowances on historical costs, of allowing the firm to deduct nominal costs of debt, of taxing shareholders' nominal rates of return on alternative financial investments and of taxing nominal capital gains on corporate stock.

After some rearranging of (II:4), it can be demonstrated that if

$$T \geq \tau + \alpha T(1-\tau) \quad (\text{II:5})$$

<sup>1</sup> See note 2 on page 18.

<sup>2</sup> This is not the whole story, however, since personal taxation also affects the third term of (II:4), reflecting the increase in capital cost due to historical cost depreciation.

i.e. stockholders' marginal income tax rate is greater than or equal to the total tax burden on retained profits, then net real capital cost  $r^*$  will fall as a result of inflation. Assuming the corporate tax rate ( $\tau$ ) to be 50 % and  $\alpha$ , i.e. that part of (accrued) capital gains that must be declared as taxable income, to be 15 %, this condition means that the firm would find real capital cost fall when shareholders' marginal tax rate  $T$  exceeds 54 %. Assuming, instead,  $\alpha = 0.4$ , capital cost will fall when  $T > 62.5$  %.<sup>1</sup>

If, on the other hand, (II:5) does not hold, capital cost will still fall provided

$$h > 1 - \frac{\tau[(1-Z)(1-\alpha T) + \tau ZQ(1-T)]}{\tau + \alpha T(1-\tau) - T} \quad (\text{II:6})$$

where

$$Z = \frac{\gamma}{\left[ \frac{(k^*+p)(1-T)}{1-\alpha T} + \gamma \right]}$$

and

$$Q = \frac{\gamma - \delta}{\frac{k^*(1-T)}{1-\alpha T} + \gamma}$$

To explore the meaning of this requirement for the firm's debt ratio we have calculated some numerical examples including several alternatives of  $T$ ,  $\alpha$ ,  $\gamma$  and  $p$ . Tables 2A and 2B, which assume the corporate income tax rate  $\tau$  to be 50 %, the rate of capacity depreciation  $\delta$  to be 10 % and stockholders' real required rate of return  $k^*$  to be 3 %, indicate values of  $h$  above which inflation will reduce real cost of capital. A certain value of  $h$  in the tables, says then that all firms with more of its total capital financed by debt will get a lower cost of capital as a result of inflation.

It may be noted that the critical values of  $h$  falls as the rate of inflation and the marginal rate of income tax rise. Also,  $h$  falls when the corporate income tax is lowered by way of accelerated depreciation ( $\gamma > \delta$ ) or the capital gains tax parameter  $\alpha$  is reduced.

<sup>1</sup> Cf. Bailey for empirical estimates of  $\alpha$  for the U.S.

The most important result emerging from Tables 2A and 2B, however, is that for reasonable values of the parameters real cost of capital falls as a result of inflation. This conclusion presumes - realistically - that most stockholders are located in income brackets with high marginal tax rates and/or that the corporate tax system provides for acceleration of depreciation allowances ( $\gamma > \delta$ ). Taking into account personal taxes on dividends and capital gains, therefore, reinforces the tendencies noticed in the first part of the paper, namely that under certain circumstances, inflation will lower real capital cost.

Tabell 2. Ratio of debt to total capital above which inflation will reduce real cost of capital

Table 2A:  $\alpha = 0.4$

p	T							
	0.3		0.4		0.5		0.6	
	$\gamma=0.1$	$\gamma=0.2$	$\gamma=0.1$	$\gamma=0.2$	$\gamma=0.1$	$\gamma=0.2$	$\gamma=0.1$	$\gamma=0.2$
0.02	0.52	0.22	0.39	0.01	0.05	0	0	0
0.07	0.25	0.09	0.03	0	0	0	0	0
0.10	0.14	0.03	0	0	0	0	0	0

Table 2B:  $\alpha = 0.15$

p	T							
	0.3		0.4		0.5		0.6	
	$\gamma=0.1$	$\gamma=0.2$	$\gamma=0.1$	$\gamma=0.2$	$\gamma=0.1$	$\gamma=0.2$	$\gamma=0.1$	$\gamma=0.2$
0.02	0.42	0.07	0.13	0	0	0	0	0
0.07	0.09	0	0	0	0	0	0	0
0.10	0	0	0	0	0	0	0	0

### II:3 Eliminating distortions with profit taxes and personal taxes on dividends and capital gains

The results presented in previous sections lead us to the question of indexing. How can the inflationary distortions via the tax system be eliminated?

The standard norm of comparison in the literature on inflation and taxation is capital cost at zero inflation and no distortions from the tax system. Recognizing, however, that governments in many countries, e.g. Sweden, consciously intervene in resource allocation promoting in particular industrial growth by various means of accelerating depreciation allowances<sup>1</sup>, another norm is of great interest: The norm of capital cost at zero inflation given the distorting system of taxation. We will first state ways of eliminating distortions relative to this last mentioned norm.

1. Change the system of corporate taxation so that the book value on which depreciation charges are taken may be adjusted for price changes. This makes the third term of (II:4) vanish.<sup>2</sup> Furthermore, let only the real interest rate  $i^*$  be deducted against corporate profits. This eliminates the fourth term of (II:4).

Change personal taxation so that stockholders are taxed only for the real rate of return on alternative financial investments. In this way nominal after tax cost of equity becomes

$k - T(k-p) = k(1-T) + pT$ . This in turn means that the real after tax cost of equity is  $k^*(1-T)$ .<sup>3</sup>

Finally, let stockholders be taxed only for real capital gains on corporate stock. Capital gains tax at time  $t$  would then equal

$$\alpha T \left[ \frac{dV(t)}{dt} - pV(t) \right].$$

With all these adjustments net capital cost becomes

$$r_1^* = i^* h + \frac{k^*(1-T)}{(1-\tau)(1-\alpha T)} \left[ 1 - h - \frac{\tau(\gamma-\delta)}{\frac{k^*(1-T)}{1-\alpha T} + \gamma} \right]$$

<sup>1</sup> See Bergström [1977] and Södersten [1978].

<sup>2</sup> This can be seen by substituting  $\gamma T P_K(s) D(s)$  for  $\gamma T D(s)$  in (I:1), p.5 and then performing the analysis as we have done it in the paper.

<sup>3</sup> Since  $k = k^* + p$ , then  $k(1-T) + pT - p = k^*(1-T)$ .

where capital cost is still a function of the tax system (in a way intended by the government) but independent of the rate of inflation.

2. As a special case of the above procedure, free depreciation can be allowed.<sup>1</sup> In our model, this would require  $\gamma$ , the rate of tax depreciation to be infinitely large<sup>2</sup>. Rewriting (II:4) under this condition gives

$$r_2^* = i^*h + \frac{k^*(1-T)}{(1-\tau)(1-\alpha T)} (1-h-\tau) - \frac{p}{1-\tau} \frac{\tau h}{\tau} - \frac{pT(1-h-\tau)}{(1-\tau)(1-\alpha T)} + \frac{p\alpha T(1-h-\tau)}{(1-\tau)(1-\alpha T)}$$

The first two terms again represent net cost of capital at zero rate of inflation. By applying then the last three rules of case 1) above capital cost becomes independent of inflation (but not of taxation). Thus, investment incentives would be preserved at zero inflation standards.

3. Finally, let us look at the over all norm of no inflationary and no tax distortions. By letting tax depreciations be taken on replacement cost at a rate coinciding with capacity depreciation, (i.e.  $\gamma=\delta$ ), the third term of (II:4) disappears and as well as the ratios within the brackets of the second and fifth terms.

As above allowing only real interest to be deductible takes away the fourth term. If, on top of this, the real cost of equity,  $k^*$ , is deducted for tax purposes the corporate tax system would be "corrected".

For personal taxation, capital gains on corporate shareholdings should be taxed at the same rate as other capital income ( $\alpha=1$ ). For the final corrections on the personal taxation side there are two ways to choose between, one real and the other nominal. Remaining distortions from personal taxation may be eliminated either by taxing real capital gains and real rates of return on alternative investments or by taxing nominal capital gains (at the same rate as other capital income) as well as nominal rates of return on alternative investments. This last alternative means that the two components of the last term of (II:4) cancel out, whereas the first alternative means that both these components are zero.

<sup>1</sup> This was the case in Sweden during the years 1938-51

<sup>2</sup> To make an investment "evaporate" immediately  $\gamma$  must go to infinity.

With all these adjustments capital cost would be

$$r_3^* = i \cdot h + k \cdot (1 - h).$$

This procedure would thus result in a distortion-free tax system, untouched by inflation. Capital cost would be invariant both with respect to taxes and inflation.

The latter results stated above make it clear that to have a neutral tax system, it is not necessary to have a real norm of taxation. Even a nominal norm will do as long as the norm is consequently stuck to. The principle of real taxation described above could be substituted by nominal taxation - both corporate and personal.

We have already described the choice between real and nominal personal taxation above. To see that there is a similar choice also for profit taxation let the firm deduct nominal rates  $k$  and  $i$  and tax the capital gains on real corporate capital in the firm. This last rule eliminates the fourth term of (II:4) and the net result is again  $r_3^*$  above.

#### II:4 Concluding remarks

It seems evident that the most rational and most simple way of indexing the tax system is the first way, described under alternative 1) above. This alternative of indexing results in just that cost of capital intended by the government by the construction of the tax system (in an inflation free world). Furthermore, it is an easy correction to undertake as the only information needed is the rate of inflation. This rate of inflation is used to adjust book values, nominal costs of debt, nominal rates of return on alternative investments, and the values of common stocks. In practice it would be conceivable to define broad price indices of capital goods to be used for approximate corrections of existing tax systems.

The other two alternatives would change the present tax laws also at zero rate of inflation. The third alternative - alternative 3 - would furthermore require knowledge of capacity depreciations to be applied to replacement cost as the basis for tax depreciations.

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