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# Working Paper Productivity as if Space Mattered: An Application to Factor Markets Across China

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# Productivity as if Space Mattered: An Application to Factor Markets Across China

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# Abstract

Although firms may face radically different production conditions, this dimension of firm heterogeneity is often overlooked. We model input demand across local factor markets, explicitly considering search costs which explain why firms care about both the price and availability of inputs. The model is estimated by combining firm and population census data. The results quantify the role of regional factor markets in firm productivity and location. Considering modern China as a large country with substantial regional variation, we find within industry interquartile labor costs vary by 30-80%, leading to 2-17% interquartile differences in TFP. These estimates imply that in general equilibrium, homogenization of labor markets would lead to a 1.63% increase in real income. Furthermore, favorably endowed regions attract more economic activity, providing new insights into within-country comparative advantage and specialization.

JEL-Code: D500, F100, J300, O100.

Keywords: general equilibrium, factor endowments, structural estimation, productivity.

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# **1** Introduction

A number of studies document large and persistent differences in productivity across both countries and firms (Syverson, 2011). However, these differences remain largely 'some sort of measure of our ignorance' (Abramovitz, 1956). This paper inquires to what extent the supply characteristics of regional input markets might help explain such systematic productivity dispersion across firms, differences which remain a 'black box' as pointed out by Melitz and Redding (2012). It would be surprising if disparate factor markets result in similar outcomes, when clearly the prices and quality of inputs available vary considerably. Modeling firm adaptation to different factor markets quantifies the importance of local factor market characteristics for firm productivity and location.

Differences between factor markets, especially for labor, are likely to be especially stark in developing economies undergoing urbanization (Lewis, 1954), or when government policies increase relocation costs beyond those normally present. Even the US labor market, which is considered relatively fluid, exhibits high migration costs as measured by the wage differential required to drive relocation (Kennan and Walker, 2011) and 'substantial departures from relative factor price equality' (Bernard, Redding, and Schott, 2013). Thus, free movement of factors does not mean frictionless movement, and recent work has indicated imperfect factor mobility has sizable economic effects (Topalova, 2010). Rather than considering the forces which cause workers to locate across space, this paper instead takes a different turn to inquire what existing differences in regional input markets imply for firm behavior.

Although there might be many complementary ways to address this question, we take an approach rooted in the general equilibrium trade literature to understand how local endowments impact firms which enter endogenously, as typified by Bernard, Redding, and Schott (2007). We extend their model to incorporate entry across regional markets with richer employment structures and regional input quality. Each region is endowed with a different distribution of skill types and wages across workers. Industries vary in their ability to effectively use and substitute between different types of labor (e.g. Bowles, 1970). Firms hire teams of workers by choosing the optimal combination of workers given local conditions. Our estimates indeed show that unlike in standard neoclassical models, firm hiring responds to both the wages and availability of a worker type. Since each firm's optimal labor force varies by industry technology and region, the comparative suitability of regions varies by industry. Since industries also differ in factor intensity, differences in the local costs of capital and materials also influence the comparative advantage of a region.<sup>1</sup> Firms thus locate in proportion to the cost advantages available.

In the model, finding new employees entails fixed costs and the ease of finding any type of

<sup>&</sup>lt;sup>1</sup>Here the comparison of firms *within* country isolates the role of factor markets from known international differences in production technology: e.g. Trefler (1993), Fadinger (2011) and Nishioka (2012).

worker increases with their regional supply. Therefore firm hiring depends on the joint distribution of worker types and wages. Since labor demand depends on technology and regional labor markets, this implies effective labor costs vary by region and industry. These labor costs help explain differences in productivity.<sup>2</sup> But are these differences economically important? To quantify real world supply conditions, we use the model to derive estimating equations which fix: 1) hiring by wage and worker type distributions, 2) substitution into non-labor inputs, 3) firm location in response to local factor markets, and 4) the role of heterogeneous factor markets on real income.

The estimation strategy combines manufacturing and population census data for China in the mid-2000s, a setting which exhibits substantial variation of a large number of labor market conditions. By revealing how firm demand for skills varies with local conditions, the model quantifies the unit costs for labor across China. The estimates imply within industry interquartile differences in effective labor costs of 30 to 80 percent. A second stage estimates production functions, explicitly accounting for regional cost differences. Since firms are capable of substituting into non-labor inputs, productivity differences are smaller than labor cost differences of 2 to 17 percent, and explain 4 to 43 percent of the variance of productivity.<sup>3</sup> Additionally considering local capital and materials frictions shows that regional capital and material quality explain similar ranges of productivity differences. In general equilibrium, the model implies that homogenizing worker distributions and wages across factor markets would increase real incomes by 1.63 percent. Furthermore, we show that economic activity locates where regional costs are lowest, as implied by the model.

We conclude this section by relating the paper to existing work. The paper then continues by laying out a model that incorporates a rich view of the labor hiring process. The model explains how firms internalize the local distribution of worker types and wages to maximize profits, resulting in an industry specific unit cost of labor by region. Section 3 places these firms in a general equilibrium, monopolistic competition framework, in particular addressing the determination of factor prices, welfare and firm location. Section 4 explains how the model can be estimated with a simple nested OLS approach, which allows for well developed techniques such as instrumental variable estimators to be used. Section 5 discusses details of the data, while Section 6 presents model estimates and uses them to explain the effect of different regional input markets on firm behavior. Section 7 concludes.

**Related work.** This paper models firms which depend on local factor markets in a fashion typified by the Heckscher-Ohlin-Vanek theory of international trade (e.g. Vanek, 1968). The

<sup>&</sup>lt;sup>2</sup>Effective labor costs are driven by the complementarity of regional endowments with industry technology, and the paper refers to these additional real production possibilities as 'productivity'.

<sup>&</sup>lt;sup>3</sup>These substantial differences underscore Kugler and Verhoogen (2011): since TFP is often the 'primary measure of [...] performance', accounting for local factor markets might substantially alter estimates of policy effects.

departures from H-O-V in the model relax assumptions about perfect labor substitutability and homogeneous factor markets, which quantifies the role of local labor markets and input costs. On the product market side, we consider many goods as indicated by Bernstein and Weinstein (2002) as appropriate when considering the locational role of factor endowments. We follow a multisector approach similar to Melitz (2003), but add free entry by firms across regions. A firm's optimal location depends on local costs which arise from the regional distribution of worker types and wages, but competition from firms which enter the same region prevent complete specialization. The model quantifies the intensity of firm entry and shows that within country, advantageous local factor markets are important for understanding specialization patterns.<sup>4</sup>

Recently, both Borjas (2009) and Ottaviano and Peri (2010) have emphasized the importance of more complete model frameworks to estimate substitution between worker types. In distinction to the labor literature, our interest is firm substitution across factor markets. Dovetailing with this are theories proposing that different industries perform optimally under different degrees of skill diversity. Grossman and Maggi (2000) build a theoretical model explaining how differences in skill dispersion across countries could determine comparative advantage and global trade patterns. Building on this work, Morrow (2010) models multiple industries and general skill distributions, and finds that skill diversity is explains productivity and export differences in developing countries.

The importance of local market characteristics, especially in developing countries, has recently been emphasized by Karadi and Koren (2012). These authors calibrate a spatial firm model to sector level data in developing countries to better account for the role of firm location in measured productivity. Moretti (2011) reviews work on local labor markets and agglomeration economies, explicitly modeling spatial equilibrium across labor markets. Distinct from this literature, we take the outcome of spatial labor markets as given and focus on the trade offs firms face and the consequences of regional markets on effective labor costs and firm location.<sup>5,6</sup>

Although we are unaware of other studies estimating model primitives as a function of local market characteristics, existing empirical work is consonant with the theoretical implications. Iranzo, Schivardi, and Tosetti (2008) find that higher skill dispersion is associated with higher TFP in Italy. Similarly, Parrotta, Pozzoli, and Pytlikova (2011) find that diversity in education leads to higher productivity in Denmark. Martins (2008) finds that firm wage dispersion affects firm

<sup>&</sup>lt;sup>4</sup>In spirit, this result is akin to Fitzgerald and Hallak (2004) who study the role of cross country productivity differences in specialization. In this paper, differences in unit labor costs predict specialization across regions.

<sup>&</sup>lt;sup>5</sup>Several papers have explored how different aspects of labor affect firm-level productivity. There is substantial work on the effect of worker skills on productivity (Abowd Kramarz and Margolis (1999, 2005), Fox and Smeets (2011)). Other labor characteristics that drive productivity include managerial talent and practices (Bloom and Reenen, 2007), social connections among workers (Bandiera, Barankay, and Rasul, 2009), organizational form (Garicano and Heaton, 2010) and incentive pay (Lazear, 2000).

<sup>&</sup>lt;sup>6</sup>Determinants of productivity include market structure (Syverson (2004)), product market rivalry and technology spillovers (Bloom, Schankerman, and Van Reenen (2007)) and vertical integration (Hortaçsu and Syverson (2007), Atalay, Hortacsu, and Syverson (2012)).

performance in Portugal. Bombardini, Gallipoli, and Pupato (2011) use literacy scores to show that countries with more dispersed skills specialize in industries characterized by lower skill complementarity. In contrast, this paper combines firm and population census data to explicitly model regional differences, leading to micro founded identification and estimates. The method used is novel, and results of this paper highlight the degree to which firm behavior are influenced through the availability of inputs at the micro level.<sup>7</sup>

Clearly this study also contributes to the empirical literature on Chinese productivity. Ma, Tang, and Zhang (2011) show that exporting is positively correlated with TFP and that firms self select into exporting which, ex post, further increases TFP. Brandt, Van Biesebroeck, and Zhang (2012) estimate Chinese firm TFP, showing that new entry accounts for two thirds of TFP growth and that TFP growth dominates input accumulation as a source of output growth. Hsieh and Klenow (2009) posit that India and China have lower productivity relative to the US due to resource misallocation and compute how manufacturing TFP in India and China would increase if resource allocation was similar to that of the US. This paper uncovers local factors that determine productivity. How this interacts with the above mechanisms is a potential area for further work.<sup>8</sup>

# **2** The Role of Local Factor Markets in Production

This section develops a model of local factor markets which impact firm's input choices and productivity. Firms combine homogeneous inputs (materials, capital) and differentiated inputs (types of labor). We model variation in regional capital and material quality and detailed labor markets in which firms search for workers. When hiring, firms respond to both the wages and quantities of locally available worker types. While homogeneous inputs are mobile within industries, we take the distribution of labor endowments as given. Special cases of the model would include perfect factor mobility (equal endowments in all regions) or high migration costs (equalization up to mobility costs). Industries have different technologies available for combining types of labor into teams. We proceed with a detailed specification of the labor hiring process, solving for firms' optimal responses to local labor market supply conditions. This quantifies the unit cost for labor by region in terms of observable local conditions and model parameters.

<sup>&</sup>lt;sup>7</sup>The importance of backward linkages for firm behavior are a recurring theme in both the development and economic geography literature, see Hirschman (1958) and recently Overman and Puga (2010).

<sup>&</sup>lt;sup>8</sup>Such regional differences might help explain the Chinese export facts of Manova and Zhang (2012) and the different impact of liberalization across trade regimes found by Bas and Strauss-Kahn (2012).

## 2.1 Production Technology

Firms within an industry *T* face a neoclassical production technology  $F^T(M, K, L)$  which combines materials *M*, capital *K* and labor *L* to produce output. An industry specific capital stock  $K^T$  is available, and in equilibrium is available at rental rate  $r_K^T$ . However, regional characteristics may augment or reduce the effective capital available to a firm, so that the effective rental rate of capital in industry *T* and region *R* is  $\tau_R^K r_K^{T,9}$ . Similarly, an industry specific stock of materials  $M^T$  is available at price  $r_M^T$ . Region characteristics again imply that the price of materials in industry *T*, region *R* are  $\tau_R^M r_K^T$ .

While *M* and *K* are composed of homogeneous units, effective labor *L* is produced by combining heterogeneous worker types. There are S skill types of workers which are distributed unequally across regions *R*. The distribution of worker types in region *R* is denoted  $a_R = (a_{R,1}, \ldots, a_{R,S})$ . The regional wages for each type are take as exogenous by workers and firms, and in equilibrium are denoted  $w_R = (w_{R,1}, \ldots, w_{R,S})$ . Workers do not contribute equally to output. This occurs for two reasons. First, each type provides an industry specific level of human capital  $\underline{m}_i^T$ . Second, when a worker meets a firm, this match has a random quality  $h \ge 1$  which follows a Pareto distribution,  $\Psi(h) \equiv 1 - h^{-k}$ .

In order to interview workers, a firm must pay a fixed search cost of f effective labor units, at which point they may hire from a distribution of worker types  $a_R$ . The firm hires on the basis of match quality, and consequently chooses a minimum threshold of match quality for each type they will retain,  $\underline{h} = (\underline{h}_1, \dots, \underline{h}_S)$ .<sup>10</sup> Upon keeping a preferred set of workers, the firm may repeat this process *N* times until achieving their desired workforce. At the end of hiring, the amount of human capital produced by each type *i* is given by

$$H_i \equiv N \cdot a_{R,i} \underline{m}_i^T \int_{\underline{h}_i}^{\infty} h d\Psi.$$
(2.1)

From a firm's perspective, the threshold of worker match quality  $\underline{h}$  is a means to choose an optimal level of H. However, as a firm lowers its quality threshold, it faces an increasing average cost of each type of human capital  $H_i$ . These increasing average costs induce the firm to maintain  $\underline{h}_i \ge 1$  and to increase N to search harder for suitable workers.

The amount of L produced by the firm depends on the composition of a team through a tech-

<sup>&</sup>lt;sup>9</sup>One view of this assumption is that it allows for a static realization of regional dynamic forces that influence factor efficiency that are beyond the scope of this paper, e.g. Cingano and Schivardi (2004). Another is that it captures differences in local factor market development (e.g. for credit as in Guiso, Pistaferri, and Schivardi, 2013).

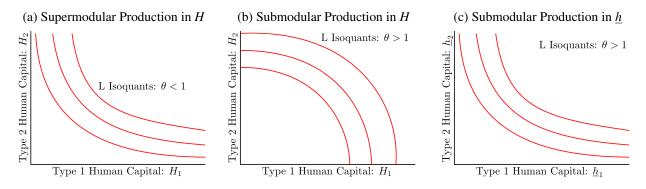
<sup>&</sup>lt;sup>10</sup>This assumption is familiar from labor search models (see Helpman, Itskhoki, and Redding (2010)). Unlike Helpman, et al., here differences in hiring patterns are determined by local market conditions.

nological parameter  $\theta^T$  in the following way:

$$L \equiv \left(H_1^{\theta^T} + H_2^{\theta^T} + \ldots + H_{\mathbb{S}}^{\theta^T}\right)^{1/\theta^T}.$$
(2.2)

Notice that in the case of  $\theta^T = 1$ , this specification collapses to a model where *L* is the total level of human capital  $\sum H_i$ . More generally, the Marginal Rate of Technical Substitution of type *i* for type *i'* is  $(H_i/H_{i'})^{\theta^T-1}$ .  $\theta^T < 1$  implies worker types are complementary, so that the firm's ideal workforce tends to represent a mix of all types (Figure 2.1a). In contrast, for  $\theta^T > 1$ , firms are more dependent on singular sources of human capital as *L* becomes convex in the input of each single type (Figure 2.1b).<sup>11</sup> Below, we show that despite the convexity inherent in Figure 2.1b, once firms choose the quality of their workers through hiring standards <u>*h*</u>, the labor isoquants resume their typical shapes as in Figure 2.1c. This avoids the possibility that some worker types are never hired, in line with real world data patterns.

Figure 2.1: Human Capital Isoquants



Although the technology  $\theta^T$  is the same for all firms in an industry, firms do not all face the same regional factor markets. Explicitly modeling these disparate markets emphasizes the role of regional heterogeneity in supplying human capital inputs to the firm in terms of both price and quality. This provides not only differences in productivity across regions by technology, but since industries differ in technology, local market conditions are more or less amenable to particular industries. We now detail the hiring process, introducing different markets and deriving firms' optimal hiring to best accommodate these differences.

## 2.2 Unit Labor Costs by Region and Technology

The total costs of hiring labor depend on the regional wage rates  $w_R$ , the availability of workers  $a_R$ , and the unit cost of labor in region R using technology T, labeled  $c_R^T$ . Since the total number

<sup>&</sup>lt;sup>11</sup>See Morrow (2010) for a more detailed interpretation of super- and sub-modularity and implications.

of each type *i* hired is  $Na_{R,i}(1 - \Psi(\underline{h}_i))$ , the total hiring bill is

Total Hiring Costs : 
$$N\left[\sum_{i} w_{R,i} a_{R,i} \left(1 - \Psi(\underline{h}_{i})\right) + f c_{R}^{T}\right].$$
 (2.3)

To produce a given vector  $(H_1, \ldots, H_S)$ , the firm faces a trade-off between the quantity and quality of workers hired. For instance, the firm might hire a large number of workers and "cherry pick" the best matches by choosing high values for <u>h</u>. Alternatively, the firm might save on interviewing costs f by choosing a low number of prospectives N and permissively low values for <u>h</u>. Local trade offs and the dependence on the regional labor supply characteristics  $a_R$  and  $w_R$  is made explicit by considering the technology and region specific cost function  $C^T(H|a_R, w_R)$ , defined by

$$C^{T} \equiv \min_{N,\underline{h}} N\left[\sum_{i} a_{R,i} w_{R,i} \left(1 - \Psi(\underline{h}_{i})\right) + f c_{R}^{T}\right] \text{ where } H_{i} = N a_{R,i} \underline{m}_{i}^{T} \int_{\underline{h}_{i}}^{\infty} h d\Psi \quad \forall i.$$
(2.4)

Letting  $\mu_i$  denote the Lagrange multiplier for each of the S cost minimization constraints, the first order conditions for  $\{\underline{h}_i\}$  imply  $\mu_i = w_{R,i}/\underline{m}_i^T \underline{h}_i$ , while the choice of N implies

$$C^{T}(H|a_{R},w_{R}) = \sum_{i} \mu_{i}H_{i} = N\sum w_{R,i}a_{R,i}\int_{\underline{h}_{i}}^{\infty} h/\underline{h}_{i}d\Psi.$$
(2.5)

Equation (2.5) shows that the multipliers  $\mu_i$  are the marginal cost contribution (per skill unit) to  $H_i$  of the last type *i* worker hired. The cost function  $C^T$  implies the unit labor cost of *L* in region *R* is

Unit Labor Cost Problem : 
$$c_R^T \equiv \min_H C^T (H|a_R, w_R)$$
 subject to  $L = 1.$  (2.6)

The unit labor cost function may be solved (Appendix D.4) as

Unit Labor Costs : 
$$c_R^T = \left[\sum_{i \text{ hired}} \left[a_{R,i}\left(\underline{m}_i^T\right)^k w_{R,i}^{1-k} / f\left(k-1\right)\right]^{\theta^T / \beta^T}\right]^{\left(\beta^T / \theta^T\right) / (1-k)},$$
 (2.7)

where

$$\boldsymbol{\beta}^T \equiv \boldsymbol{\theta}^T + k - k \boldsymbol{\theta}^T. \tag{2.8}$$

The trade off between being more selective (high  $\underline{h}$ ) and avoiding search costs ( $fc_R^T$ ) is clearly illustrated by combining Equations (2.3) and (2.5), which shows:

$$\sum_{i} a_{R,i} w_{R,i} \int_{\underline{h}_{i}}^{\infty} \left(h - \underline{h}_{i}\right) / \underline{h}_{i} d\Psi = f c_{R}^{T}.$$
(2.9)

The LHS of Equation (2.9) decreases in  $\underline{h}$ , so when a firm faces lower interviewing costs it can afford to be more selective by increasing  $\underline{h}$ . Conversely, in the presence of high interviewing costs, the firm optimally "lowers their standards"  $\underline{h}$  to increase the size of their workforce without interviewing additional workers. The number of times a firm goes to hire workers, N, can be solved as N = 1/fk. Thus, N is decreasing in both hiring costs and k. Increases in k imply lower match quality, so that repeatedly screening workers has lower returns.

## **2.3 Optimal Local Input Patterns**

The above reasoning shows the relationship between technology and the optimal choice of worker types. It is intuitive that if the right tail of the match quality distribution is sufficiently thick, there are a few excellent matches for each type of worker, so all types are hired.<sup>12</sup> Since match quality follows a Pareto distribution with shape parameter k, expected match quality is E[h] = k/(k-1). As  $k \to 1$  match quality increases, so for k sufficiently close to one, all worker types should be hired. To be precise, a sufficient condition for a firm to optimally hire every type of worker, stated as Proposition 1, is that  $\beta^T$  of (2.8) is positive. This clearly holds for  $\theta^T \leq 1$ , and for  $\theta^T > 1$ , the condition is equivalent to  $k < \theta^T / (\theta^T - 1)$ . This induces the isoquants depicted in Figure 2.1c, which illustrates a more standard trade off between different types of workers, so long as the coordinates are transformed to the space of hiring standards <u>h</u>.

## **Proposition 1.** If $\beta^T > 0$ then it is optimal for a firm to hire all types of workers.

Proof. See Appendix.

Thus, for  $\beta^T > 0$ , all worker types are hired. The optimal share of workers of type *i* hired by firm *j* under technology *T* in region *R*, labeled  $s_{R,ij}^T$ , is fixed by (2.6):<sup>13</sup>

$$s_{R,ij}^{T} = a_{R,i}^{\theta^{T}/\beta^{T}} w_{R,i}^{-k/\beta^{T}} \left(\underline{m}_{i}^{T}\right)^{k\theta^{T}/\beta^{T}} \left(\widehat{c}_{R}^{T}\right)^{(k-1)\theta^{T}/\beta^{T}} \left(f\left(k-1\right)\right)^{-\theta^{T}/\beta^{T}}.$$
(2.10)

where  $\tilde{c}_R^T$  denotes the unit labor cost function at wages  $\left\{w_{R,i}^{k/(k-1)\theta^T}\right\}$ .<sup>14</sup> Notice that in (2.6), unlike most production models, the factor prices  $w_R$  are not sufficient to determine the factor shares a firm will buy. The availability of workers  $a_R$  is crucial in determining shares hired because costly search makes firms sensitive to the local supply of each worker type.

<sup>&</sup>lt;sup>12</sup>This is important, not only for the analytical convenience of avoiding complete specialization in the hiring of worker types, but also because we find that each region-industry combination hires all types of workers in the data.

<sup>&</sup>lt;sup>13</sup>See Supplemental Appendix.

<sup>&</sup>lt;sup>14</sup>Formally  $\tilde{c}_R^T \equiv \min_H C^T \left( H | a_R, \left\{ w_{R,i}^{-k/\theta^T(1-k)} \right\} \right)$  subject to L = 1.

The role of regional capital and material quality,  $\tau_R^K$  and  $\tau_R^M$ , is similar and affords a simple pattern of relative factor use. Each production technology  $F^T$  assumes a Cobb-Douglas form:

$$F^{T}(M,K,L) = M^{\alpha_{M}^{T}} K^{\alpha_{K}^{T}} L^{\alpha_{L}^{T}} \quad \text{with} \quad \alpha_{M}^{T} + \alpha_{K}^{T} + \alpha_{L}^{T} = 1.$$
(2.11)

The ratio of expenditure on capital  $(K_R^T)$  or materials  $(M_R^T)$  to wages  $(W_R^T)$  under technology T in region R is easily seen to be

$$K_R^T/W_R^T = \left(\alpha_K^T/\alpha_L^T\right)/r_K^T\tau_R^K, \qquad M_R^T/W_R^T = \left(\alpha_M^T/\alpha_L^T\right)/r_M^T\tau_R^M.$$
(2.12)

### 2.4 Unit Costs: The Role of Substitution

Equation (2.7) summarizes the cost of one unit of labor *L* in terms of the Pareto shape parameter *k*, the technology  $\theta^T$  and regional characteristics  $a_R$  and  $w_R$ . It is then straightforward to derive total unit costs from (2.7) and (2.11) as

$$\text{Fotal Unit Costs}: \quad u_R^T = \left(\tau_R^M r_M^T / \alpha_M^T\right)^{\alpha_M^T} \left(\tau_R^K r_K^T / \alpha_K^T\right)^{\alpha_K^T} \left(c_R^T / \alpha_L^T\right)^{\alpha_L^T}, \quad (2.13)$$

where  $u_R^T$  represents the regional component of unit costs for industry *T* in region *R*. Within an industry, productivity then varies across regions as in the following example: assume Firm 1 in region *R* and Firm 2 in region *R'* have the same total expenditure on inputs, *E*. By definition, Firm 1's output,  $Y_1$ , is  $E/u_R^T$  while Firm 2's output  $Y_2$  is  $E/u_{R'}^T$ . Therefore relative output is

$$Y_{1}/Y_{2} = u_{R'}^{T}/u_{R}^{T} = \left(\tau_{R'}^{M}/\tau_{R}^{M}\right)^{\alpha_{M}^{T}} \left(\tau_{R'}^{K}/\tau_{R}^{K}\right)^{\alpha_{M}^{T}} \left(c_{R'}^{T}/c_{R}^{T}\right)^{\alpha_{L}^{T}}.$$

Industry differences in productivity therefore depend on 1) regional labor costs and quality and 2) the intensity of factors in production. Estimating both quantifies regional productivity differences. However, we first resolve factor prices and firm location in general equilibrium.

# **3** Firm Production under Monopolistic Competition

This section combines the insights into firm behavior just developed into a general equilibrium model of monopolistic competition. Firms, who are ex ante identical, choose among regions to locate. Key to a firm's location decision are the expected profits of entry. These profits depend on 1) the distribution of worker types and wages, 2) capital and material quality and 3) the competition present from other firms who enter the region. We characterize production and location choices conditional on local factor markets. Most strikingly, lower regional production costs attract more

firms for any given technology, which determines the intensity of economic activity.

Furthermore, we show an equilibrium wage vector exists which supports these choices by firms for any distribution of labor endowments (e.g. as would be implied by assuming nominal or real wage equalization across regions). Thus, endowment distributions as implied by both complete or incomplete labor mobility are consistent with this framework. Rather than use a macro level model which determines worker location *a priori*, we will use micro level population census data to observe the actual composition of labor markets.<sup>15</sup> Our goal is to understand how firms optimally respond to local factor markets as they are, not to predict where workers choose to locate.

### 3.1 Firms and Consumers

Each region *R* is endowed with a population  $\mathbb{P}_R$  composed of  $\mathbb{S}$  worker types. Firms may enter any region *R* by paying a sunk entry cost  $F_e$ . Firms then receive a random cost draw  $\eta_j \sim G$  and face a fixed production cost  $f_e$ .<sup>16</sup> Akin to Bernard, Redding, and Schott (2007), firms combine different types of inputs to produce. Each firm *j* produces a distinct variety, and in equilibrium a mass of firms  $\mathbb{M}_R^T$  enter. Entrants with cost draws less than a prohibitively high cost level  $\overline{\eta}_R^T$  produce.  $\mathbb{M}_R^T$  and  $\overline{\eta}_R^T$  together determine the set of varieties available to consumers.

Consumer preferences over varieties j and quantities  $\left\{Q_{R_j}^T\right\}$  take the Dixit-Stiglitz form

$$U_{R}^{T} \equiv U\left(\mathbb{M}_{R}^{T}, \overline{\eta}_{R}^{T}, Q_{R}^{T}\right) = \mathbb{M}_{R}^{T} \int_{0}^{\overline{\eta}_{R}^{T}} \left(Q_{Rj}^{T}\right)^{\rho} dG(j)$$

in each region and industry, with total utility  $U(\mathbb{M}, \overline{\eta}, Q) \equiv \Pi_T \Pi_R (U_R^T)^{\sigma_R^T}$ , where  $\sigma_R^T$  are relative weights put on final goods normalized so that  $\sum_{T,R} \sigma_R^T = 1$ . As shown in the Appendix, each  $\sigma_R^T$ has the usual interpretation as the share of income spent on goods from each region and technology pair (R, T).<sup>17</sup>

Firms are the sole sellers of their variety, and thus are monopolists who provide their variety at a price  $P_{R_j}^T$ . Consumers, in turn, face a vector of prices  $\{P_{R_j}^T\}$ , and a particular consumer with

<sup>&</sup>lt;sup>15</sup>There are many forces at work in determining the composition of local labor markets in China. In this respect, the literature is even unresolved as to what extent Chinese labor markets reflect an agriculturally transitioning 'dual economy' (Zhang, Yang, and Wang, 2011) or if models best suited to advanced industrial economies are more appropriate. Since China has undergone sweeping changes withing the last generation, we remain agnostic and rely on the data.

<sup>&</sup>lt;sup>16</sup>This follows Melitz (2003).  $G(\eta)$  is assumed to be absolutely continuous with  $\mathbb{E}\left[\eta^{\rho/(\rho-1)}\right]$  finite.

<sup>&</sup>lt;sup>17</sup>Note that since the demand for goods from each (R,T) pair enter preferences multiplicatively, complete specialization cannot occur which considerably simplifies the analysis.

income *I* has the following demand curve for each variety:

$$Q_{Rj}^{T} = I \cdot \left( P_{Rj}^{T} U_{R}^{T} / \sigma_{R}^{T} \right)^{\frac{1}{\rho-1}} / \sum_{t,r} \left( \sigma_{r}^{t} \right)^{\frac{1}{\rho-1}} \mathbb{M}_{r}^{t} \int_{0}^{\overline{\eta}_{r}^{t}} \left( \left( P_{r,z}^{t} \right)^{\rho} U_{r}^{t} \right)^{\frac{1}{\rho-1}} dG(z) \,.$$
(3.1)

Clearly, even if consumers have different incomes, aggregate demand for variety j corresponds to that of a representative consumer with income equal to aggregate income,  $I_{Agg}$ . Since labor is supplied inelastically,  $I_{Agg}$  is necessarily

$$I_{\text{Agg}} = \sum_{R} \sum_{i} \underbrace{w_{R,i} a_{R,i} \mathbb{P}_R}_{\text{Total Wages of Type i in R}} + \sum_{R} \sum_{T} \underbrace{\tau_R^M r_M^T M^T + \tau_R^K r_K^T K^T}_{\text{Non-labor Income}}.$$
 (3.2)

After paying an entry cost of  $F_e$  output units, firms know their cost draw, which paired with regional input markets determine their total unit cost  $u_R^T$ . Firms maximize profits

$$\pi_{Rj}^{T}\left(P_{Rj}^{T}\right) = \left(P_{Rj}^{T} - u_{R}^{T}\eta_{j}\right)Q_{Rj}^{T} - u_{R}^{T}f_{e}$$

by choosing an optimal price  $P_{Rj}^T = u_R^T \eta_j / \rho$ , resulting in a markup of  $1/\rho$  over costs. Firms who cannot make a positive profit do not produce to avoid paying the fixed cost of  $f_e$  output units. Since profits decrease in costs, there is a unique cutoff cost draw  $\overline{\eta}_R^T$  which implies zero profits, while firms with  $\eta_j < \overline{\eta}_R^T$  produce.<sup>18</sup> As there are no barriers to entry besides the entry cost  $F_e$ , firms enter in every region until expected profits are zero. This yields the

Spatial Zero Profit Condition : 
$$\mathrm{E}\left[\pi_{Rj}^{T}\right] = u_{R}^{T}F_{e}, \quad \forall R, T.$$

Finally, differences in regional factor markets influence consumer welfare. As shown in the appendix, in equilibrium welfare  $W(I_{Agg}, \{u_R^T\})$  of an economy with income  $I_{Agg}$  and Industry-Region unit costs  $\{u_R^T\}$  is given by

$$W = \rho^{\rho} (1-\rho)^{1-\rho} f_{e}^{\rho-1} \left(\overline{\eta}_{1}^{1}\right)^{-\rho} \left(\frac{\int_{0}^{\overline{\eta}_{1}^{1}} (\eta_{j})^{\rho/(\rho-1)} dG(j)}{\int_{0}^{\overline{\eta}_{1}^{1}} (\eta_{j})^{1/(\rho-1)} dG(j)}\right) \cdot I_{\text{Agg}} \cdot \Pi_{T} \Pi_{R} \left(\frac{\sigma_{R}^{T}}{u_{R}^{T}}\right)^{\sigma_{R}^{T}}.$$
 (3.3)

From Equation (3.4), if unit costs were to change to  $\{v_R^T\}$  while holding aggregate income constant, the percentage change in real income under from old to new unit costs is therefore

$$\left[W\left(I_{\text{Agg}},\left\{v_{R}^{T}\right\}\right)-W\left(I_{\text{Agg}},\left\{u_{R}^{T}\right\}\right)\right]/W\left(I_{\text{Agg}},\left\{u_{R}^{T}\right\}\right)=\Pi_{T}\Pi_{R}\left(u_{R}^{T}/v_{R}^{T}\right)^{\sigma_{R}^{I}}-1.$$
(3.4)

<sup>&</sup>lt;sup>18</sup>The Appendix shows the cutoff cost  $\overline{\eta}_R^T$  depends only on  $f_e$ ,  $F_e$ , and G, and so does not vary by region or industry.

Having determined behavior in the product market, we now examine input markets.

## 3.2 Regional Factor Market Clearing

The remaining equilibrium conditions are that input prices guarantee firm input demand exhausts materials, capital stocks, and each regional pool of workers. To fix expenditure, we assume each budget share  $\sigma_R^T$  is proportional to  $\mathbb{P}_R$ , so that  $\sigma_R^T = \sigma^T \mathbb{P}_R$  for some  $\sigma^T$ .<sup>19</sup> Since production is Cobb-Douglas, the share of total costs (equal to  $I_{Agg}$ ) which go to each factor is the factor output elasticity. Therefore full resource utilization of materials and capital requires the effective capital  $(K_R^T)$  and materials  $(M_R^T)$  used in each region to satisfy

$$M^{T} = \alpha_{M}^{T} \sigma^{T} I_{\text{Agg}} \mathbb{P} / r_{M}^{T}, \qquad K^{T} = \alpha_{K}^{T} \sigma^{T} I_{\text{Agg}} \mathbb{P} / r_{K}^{T}, \qquad (3.5)$$

$$M^T = \sum_R \tau_R^M M_R^T, \qquad \qquad K^T = \sum_R \tau_R^K K_R^T, \qquad (3.6)$$

where  $\mathbb{P} \equiv \sum_{R} \mathbb{P}_{R}$  is the total population. These four equations capture the allocation of technology specific resources across regions.

In contrast, effective labor of  $L_R^T$  is produced by each technology in each region. Since the wage bill  $L_R^T c_R^T$  must receive a share  $\alpha_L^T$  of total revenues,

Aggregate Labor Demand : 
$$L_R^T = \alpha_L^T \sigma^T I_{\text{Agg}} \mathbb{P}_R / c_R^T$$
. (3.7)

Embedded in each  $L_R^T$  is the set of workers hired by firms attendant to regional market conditions. The total demand for employees of each type in region *R* implied by Equation (2.10) must equal the supply of  $a_{R,i}\mathbb{P}_R$ . Wages are therefore determined by

$$a_{R,i}w_{R,i} = \sum_{T} \underbrace{\sigma^{T}}_{\text{Industry Share Per Capita Labor Share}} \cdot \underbrace{\alpha_{L}^{T}}_{\text{Labor Share}} \cdot \underbrace{H_{R,i}^{\theta^{T}} / \Sigma_{j} H_{R,j}^{\theta^{T}}}_{\text{Type Share}} \cdot I_{\text{Agg}} \quad \forall R, i.$$
(3.8)

Equation (3.8) shows that type *i*'s contribution to mean wages,  $a_{R,i}w_{R,i}$ , is the sum over income spent an industry, times labor's share, times the wages attributable to each type.<sup>20</sup>

Solving Equation (3.8) requires finding a wage for each worker type in each region that fully employs all workers. We do so in the Appendix, leading to

#### Proposition 2. An equilibrium wage vector exists which clears each regional labor market.

<sup>19</sup>This assumption implies that any two regions with identical skill distributions have the same wage schedule.

<sup>20</sup>The equilibrium type share is 
$$H_{R,i}^{\theta^T} / \Sigma_j H_{R,j}^{\theta^T} = \left( a_{R,i} \left( \underline{m}_i^T \right)^k w_{R,i}^{1-k} \right)^{\theta^T / \beta^T} / \Sigma_j \left( a_{R,j} \left( \underline{m}_j^T \right)^k w_{R,j}^{1-k} \right)^{\theta^T / \beta^T}$$
.

## 3.3 Regional Specialization of Firms

Differences in input costs will influence the relative concentration of firms across regions through entry. Since regions vary in population size  $\mathbb{P}$ , the relevant metric is the number of firms per capita,  $\mathbb{M}_R^T \cdot G(\overline{\eta}_R^T) / \mathbb{P}_R$ . The impact of different regional costs can be clearly seen by fixing an industry *T* and considering the ratio of firms per capita in region *R* versus *R'* as in Equation (3.9):

Firms per Capita, R to R': 
$$\frac{\mathbb{M}_{R}^{T} \cdot G(\overline{\eta}_{R}^{T}) / \mathbb{P}_{R}}{\mathbb{M}_{R'}^{T} \cdot G(\overline{\eta}_{R'}^{T}) / \mathbb{P}_{R'}} = \frac{u_{R'}^{T}}{u_{R}^{T}} = \left(\frac{\tau_{R'}^{K}}{\tau_{R}^{K}}\right)^{\alpha_{L}^{T}} \left(\frac{\tau_{R'}^{M}}{\tau_{R}^{M}}\right)^{\alpha_{M}^{T}} \left(\frac{c_{R'}^{T}}{c_{R}^{T}}\right)^{\alpha_{L}^{T}}$$
(3.9)

Equation (3.9) shows that areas with lower unit labor costs, capital costs or material costs have more firms per capita. Additionally, the larger the share of a factor in production, the more important are differences between regions. This relationship is summarized as

**Proposition 3.** Within an industry, regions with lower factor costs have more firms per capita.

The next section lays out a strategy to structurally estimate model parameters.

# 4 Estimation Strategy

This section lays out an estimator for the structural model parameters above. The estimator involves two stages, with a simple intervening computation. The first stage determines regional quality and firm labor demand, and unlike many approaches, is based on the firm-level shares of workers hired across regions. The second stage equation uses regional unit labor costs from the first stage to estimate the production function. Feasibility is illustrated by simulating a data set consistent with the model above and recovering model primitives accurately with the estimator.

### 4.1 First Stage Estimation

Equation (2.10) determines the share of each type of workers hired in each region *R* and industry *T*. Taking logs and allowing for errors  $\varepsilon_{ij}$  across firms *j* and types *i* implies

$$\ln s_{R,ij}^T = -\frac{k}{\beta^T} \ln w_{R,i} + \frac{\theta^T}{\beta^T} \ln a_{R,i} + \frac{\theta^T}{\beta^T} k \ln \underline{m}_i^T + \frac{\theta^T (k-1)}{\beta^T} \ln \frac{\widetilde{c}_R^T}{f (k-1)} + \varepsilon_{ij}, \qquad (4.1)$$

To estimate this equation we use a combination of type and region fixed effects.<sup>21</sup> To further explain how regional variation identifies the model we discuss equilibrium hiring predicted by

<sup>&</sup>lt;sup>21</sup>We suggest the convention of creating of type and region fixed effects, omitting the highest type fixed effect. The remaining type coefficients then correspond to the estimates of  $(\theta^T / \beta^T) k \ln \underline{m}_i^T / \underline{m}_{\mathbb{S}}^T$ .

Equation (4.1) in Appendix D.2. Implicit in this estimation strategy is the assumption that firms do not have monopsony power over their local factor market (e.g. Manning (2011)), and accordingly we will restrict our analysis to regions with a minimum of five employers.

In order to control for firm characteristics which might influence hiring patterns across worker types,  $\underline{m}_i^T$  is allowed to vary with firm observables labeled Controls<sub>j</sub>:

$$\underline{m}_{ij}^{T} \equiv \underline{m}_{i}^{T} \cdot \exp\left(\operatorname{Controls}_{j} \gamma_{i}^{T}\right), \qquad (4.2)$$

where  $\gamma_i^T$  is a type-industry specific estimate which influences the value of each worker type in an industry. The inclusion of Controls<sub>j</sub> makes type specific human capital vary by firm, and accordingly we denote unit labor costs as  $c_{Rj}^T$ . We will use such worker type specific controls capture the effects of economic geography (e.g. deeper urban labor markets and skill agglomeration) and firm organization (e.g. foreign ownership). Finally, the linear form of Equation (4.1) allows many well understood estimation techniques to be applied to the model, such as instrumental variable approaches.

Regional capital and material quality are determined by Equation (2.12). Quality can be estimated using each firm *j*'s input expenditure ratios, as at the region level, these ratios deviate from the industry average. In particular, allowing for errors  $\zeta_i^K$  and  $\zeta_i^M$ ,

$$\ln \frac{K_{R,j}^{T}}{W_{R,j}^{T}} = \ln \frac{1}{r_{K}^{T}} \frac{\alpha_{K}^{T}}{\alpha_{L}^{T}} - \ln \tau_{R}^{K} + \zeta_{j}^{K}, \qquad \ln \frac{M_{R,j}^{T}}{W_{R,j}^{T}} = \ln \frac{1}{r_{M}^{T}} \frac{\alpha_{M}^{T}}{\alpha_{L}^{T}} - \ln \tau_{R}^{M} + \zeta_{j}^{M}.$$
(4.3)

The first stage estimates are used to estimate the production function in a second stage.

# 4.2 Second Stage Estimation

From above we can estimate  $\theta^T$ , k,  $\underline{m}_i^T / \underline{m}_{\mathbb{S}}^T$ ,  $\gamma_i^T$  and therefore can estimate regional differences in unit labor cost functions,  $\Delta \ln c_R^T \equiv \mathbb{E}\left[\ln c_{Rj}^T | R, T, \text{Controls}_j\right] - \mathbb{E}\left[\ln c_{Rj}^T | T\right]$ . From above, revenues  $P_{Rj}^T Q_{Rj}^T$  for a firm *j* satisfy

$$\ln P_{Rj}^T Q_{Rj}^T = \alpha_M^T \ln M_j / \tau_R^M + \alpha_K^T \ln K_j / \tau_R^K + \alpha_L^T \ln L_j - \ln \rho \eta_j.$$
(4.4)

As firm expenditure on labor  $L \cdot c_{Rj}^T$  equals the share  $\alpha_L^T$  of revenues  $P_{Rj}^T Q_{Rj}^T$ , we have  $L_j c_{Rj}^T = \alpha_L^T P_{Rj}^T Q_{Rj}^T$  and taking differences with the population mean gives

$$\Delta \ln L_j = \Delta \ln P_{R_j}^T Q_{R_j}^T - \Delta \ln c_{R_j}^T.$$
(4.5)

Taking differences of Equation (4.4) with the population mean and using (4.5) yields

$$\Delta \ln P_{Rj}^T Q_{Rj}^T = \alpha_M^T \Delta \ln M_j / \tau_R^M + \alpha_K^T \Delta \ln K_j / \tau_R^K + \alpha_L^T \Delta \ln P_{Rj}^T Q_{Rj}^T - \alpha_L^T \Delta \ln c_{Rj}^T - \Delta \ln \eta_j.$$

Rearranging yields the estimating equation

$$\Delta \ln P_{Rj}^T Q_{Rj}^T = \frac{\alpha_M^T}{1 - \alpha_L^T} \Delta \ln \frac{M_j}{\tau_R^M} + \frac{\alpha_K^T}{1 - \alpha_L^T} \Delta \ln \frac{K_j}{\tau_R^K} - \frac{\alpha_L^T}{1 - \alpha_L^T} \Delta \ln c_{Rj}^T - \frac{1}{1 - \alpha_L^T} \Delta \ln \eta_j.$$
(4.6)

In the Appendix, we illustrate the estimator by simulating the production model above and apply these steps. In the simulation, the two stage estimator explains 97% of the variation in firm output, suggesting that the ease of implementation comes at only a small efficiency cost. Since the equations implied by the model are linear, well known methods to accommodate such features as heteroskedasticity can be easily introduced.<sup>22</sup>

The entire estimation procedure is now briefly recapped.

## 4.3 Estimation Procedure Summary

- 1. Using  $s_{R,ij}^T$ , the share of workers of type i hired in region *R* and industry *T* by firm *j*, estimate Equation (4.1) for each industry, using type and region fixed effects.
- 2. Using input expenditure ratios, estimate Equation (4.3) using industry fixed effects.
- 3. Recover  $\widehat{\theta^T}$ ,  $\widehat{k}$ ,  $\underline{\widehat{m_i^T}/\underline{m}_{\mathbb{S}}^T}$ ,  $\widehat{\gamma_i^T}$ ,  $\overline{\widehat{\tau_R^K}}$  and  $\widehat{\tau_R^M}$ . Bootstrap standard errors or use the delta method.
- 4. Calculate  $\widehat{\Delta \ln c_{Rj}^T}$  from Equation (2.7) using regional data and estimates from Step 2.
- 5. Estimate Equation (4.6) using  $\widehat{\Delta \ln c_{Rj}^T}$ ,  $\widehat{\tau_R^K}$  and  $\widehat{\tau_R^M}$ .

Having laid out both a model detailing the interaction of firm technologies with local market conditions and specifying an estimation strategy, we now apply the method to China. The next section discusses these data in detail while the sequel presents results.

# 5 Data

Firm data come from the 2004 Survey of Industrial Firms conducted by the Chinese National Bureau of Statistics, which includes all state owned enterprises and private enterprises with sales over 5 million RMB. The data include firm ownership, location, industry, employees by education

<sup>&</sup>lt;sup>22</sup>Estimates of the model using FGLS yield the same general patterns with small differences.

level, profit and cash flow statements. Firm capital stock is reported fixed capital, less reported depreciation while materials are measured by value. For summary statistics, see Appendix E.3. From the Survey, a sample was constructed of manufacturing firms who report positive net fixed assets, material inputs, output, value added and wages.<sup>23</sup> The final sample includes 141,464 firms in 284 prefectures and 19 industries at the two digit level.

Regional wage distributions are calculated from the 0.5% sample of the 2005 China Population Census. The census contains the education level by prefecture of residence, occupation, industry code, monthly income and weekly hours of work. We restrict the sample to employees age 15 to 65 who report positive wages and hours of work. The regional wage distribution is recovered from the average annual income of employees by education using census data. While firm data is from 2004 and census data is from 2005, firm skill mix is remarkably stable over time: Ilmakunnas and Ilmakunnas (2011) find the standard deviation of plant-level education years is very stable from 1995-2004 in Finland, and Parrotta, Pozzoli, and Pytlikova (2011) find that a firm-level education diversity index was roughly constant over a decade in Denmark.

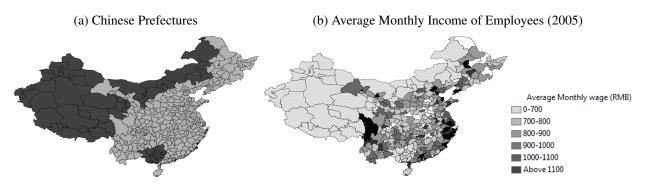
GIS data from the China Data Center at the University of Michigan locates firms at the county and prefecture level. Port locations are provided by GIS data and supplemented by data from the World Port Index. These data provide controls for urban status, distance to port, highway density and distance to cities.

Finally, household consumption shares for each industry are aggregated from the three digit level from the 2002 Input-Output Table of China, as constructed by the Department of National Economy Accounting, State Statistical Bureau.

Figure 5.1a illustrates the prefectures of China, which we define as regions from the perspective of the model above. Prefectures are similar in population size to a US commuting zone, as used by Autor, Dorn, and Hanson (2012) and computed by Tolbert and Sizer (1996). Prefectures illustrated by a darker shade in the Figure operate under substantially different government policies and objectives. These regions typically have large minority populations or historically distinct conditions, with the majority declared as autonomous regions, and have idiosyncratic regulations, development, and educational policies. We exclude the five Autonomous Provinces and one predominantly minority Province (Qinghai) which has a very low density of population and economic activity.<sup>24</sup> What remains are the lighter shaded regions of Figure 5.1a, preserving 284 prefectures displaying distinct labor market conditions.

 <sup>&</sup>lt;sup>23</sup>The results are robust to exclusion of firms with fewer than 8 employees which operate in a different legal regime.
 <sup>24</sup>See the Information Office of the State Council of the People's Republic of China document cited.

#### Figure 5.1: Chinese Prefectures



## 5.1 Worker Types

Workers are defined as people between ages 15 and 65 who work outside the agricultural sector and are not employers, self-employed, or in a family business. This characterization includes (illegal) migrants. The definition of distinct, imperfectly substitutable worker types is based primarily on formal schooling attained. Census data from 2005 shows that the average years of schooling for workers in China ranges from 8.5 to 11.8 years across provinces, with sparse postgraduate education. The most common level of formal education is at the Junior High School level or below. Reflecting substantial wage differences by gender within that group, we define Type 1 workers as Junior High School or Below: Female and Type 2 workers as Junior High School or Below: Male.<sup>25</sup> Completion of Senior High School defines Type 3 and completion of Junior College or higher education defines Type 4.

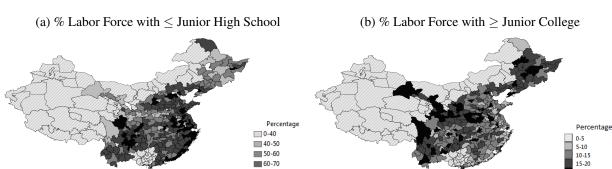
## 5.2 Regional Variation

Key to the analysis is regional variation in skill distribution and wages. Here we briefly discuss both, with further details in Appendix E. While this paper explains individual firms' responses to existing labor market conditions rather than providing a theory of worker location, it is clear that the recent history of China has exhibited massive internal migration (Chan, 2013).<sup>26</sup> Monthly incomes vary substantially across China as illustrated in Figure 5.1b. This is due to both the composition of skills (proxied by education) across regions and the rates paid to these skills. Figure 5.2 contrasts educational distributions of the labor force. Figure 5.2(a) shows those with a Junior High School education (the mandated level in China), while Figure 5.2(b) displays those with a Junior College

<sup>&</sup>lt;sup>25</sup>Differentiation of gender for low skill labor is especially important in developing countries as a variety of influences result in imperfect substitutability across gender. Bernhofen and Brown (2011) distinguish between skilled male labor, unskilled male labour and female labour and find that the factor prices across these types differ substantially.

<sup>&</sup>lt;sup>26</sup>In 2005, the median share of within prefecture migration is 77 percent, dominating across prefecture migration.

or higher level of attainment.



Above 70

#### Figure 5.2: Low and High Educational Attainment Across China (2005)

The differing composition of input markets across China in 2004-2005 stem from many factors, including the dynamic nature of China's rapidly growing economy, targeted economic policies and geographic agglomeration of industries across China.<sup>27</sup> Faber (2012) finds that expansion of China's National Trunk Highway System displaced economic activity from counties peripheral to the System. Similarly, Baum-Snow, Brandt, Henderson, Turner, and Zhang (2012) show that mass transit systems in China have increased the population density in city centers, while radial highways around cities have dispersed population and industrial activity. An overview of Chinese economic policies is provided by Defever and Riano (2012), who quantify their impact on firms.

Of particular interest for labor markets are substantial variation in wages and the attendant migration this induces. The quantitative extent to which labor market migration has been stymied by the *hukou* system of internal passports is not well studied, although its impact has likely lessened since 2000.<sup>28</sup> Since little is known about the impact of illegal immigration on firm behavior (see Brown, Hotchkiss, and Quispe-Agnoli (2013) for a notable exception), and as the ease of obtaining a legal hukou is not independent of education,<sup>29</sup> we control for the regional share of nonagricultural hukou held by each type of worker without any *a priori* expectation of sign. Given that rural to urban migration typifies the pattern of structural transformation underway, we control for rural and urban effects for each type of worker below. Given what little is known about the actual determinants of prefecture level migration in China, modeling firm decisions when faced with dynamically changing input markets is an interesting avenue for further work.

Having discussed the data, we now apply the estimation procedure developed above.

<sup>&</sup>lt;sup>27</sup>We consider regional price variation at a fixed point in time. Reallocation occurs (Suqin Ge and Dennis Tao Yang, 2013) and is important in explaining dynamics (e.g. Borjas (2003)), but dynamics are outside the scope of this paper.

<sup>&</sup>lt;sup>28</sup>The Hukou system and its reform in the late 1990s are well explained in Chan and Buckingham (2008). The persistence of such a stratified system has engendered deep set social attitudes which likely affect economic interactions between Hukou groups, see Afridi, Li, and Ren (2012).

<sup>&</sup>lt;sup>29</sup>High income and highly educated workers can more easily move among urban regions as local governments are likely to approve their migration applications (Chan, Liu, and Yang, 1999).

# **6** Estimation Results

This section reports estimation results, then turns to a discussion of the quantitative labor cost and productivity differences accounted for by local market conditions in China. The section continues by testing the firm location implications of the model, finding broad support that economic activity locates where estimated unit labor costs are lower. Finally, we compare estimation results of this unit cost based method with one approach common in the literature, which does no account for regional factor markets and models labor types as input stocks.

## 6.1 Estimates of Market Conditions and Production Technologies

The full first stage regression results for several manufacturing industries in China are presented in Tables A.3 and A.4 of Appendix C. A representative set of estimates for the General Machines industry are presented in Table 1. The first box in Table 1, labeled Primary Variables, are consistent with the model: increases in the local wages for a type decrease firm demand for that type, while increases in the availability of a type increase firm demand.<sup>30</sup> Though values for the coefficients  $(\theta^T / \beta^T) \ln \underline{m}_i / \underline{m}_4$  are not specified by the model, their estimated values do increase in type in Table 1, which is consonant with formal education increasing worker output.

Primary Variables	ln (% Hired)	Firm Controls	
$\ln(w_{R,i})$	-2.687***	$\underline{m}_1 * \text{Urban Dummy}$	-1.384***
$\ln\left(a_{R,i}\right)$	1.794***	$\underline{m}_2 * \text{Urban Dummy}$	-0.980***
$\underline{m}_1$ ( $\leq$ Junior HS: Female)	-10.170***	$\underline{m}_3 * \text{Urban Dummy}$	0.427***
$\underline{m}_2$ ( $\leq$ Junior HS: Male)	-6.171***	$\underline{m}_4 * \text{Urban Dummy}$	2.336***
$\underline{m}_3$ (Senior High School)	-3.180***	<u>m</u> 1*% Foreign Equity	-2.448***
		<u>m</u> 2*% Foreign Equity	-1.864***
		<u>m</u> <sub>3</sub> *% Foreign Equity	0.311***
Regional Controls		<u>m</u> 4*% Foreign Equity	3.847***
$\underline{m}_1 * \%$ Non-Ag Hukou	-5.957***	$\underline{m}_1 * \ln(\text{Firm Age})$	0.934***
<u>m</u> 2*% Non-Ag Hukou	-3.072***	$\underline{m}_2 * \ln(\text{Firm Age})$	0.403***
<u>m</u> <sub>3</sub> ∗% Non-Ag Hukou	-3.218***	$\underline{m}_3 * \ln(\text{Firm Age})$	0.143***
<u>m</u> <sub>4</sub> *% Non-Ag Hukou	-7.026***	$\underline{m}_4 * \ln(\text{Firm Age})$	0.351***
Observations: 62,908. $R^2$ :	0.139	Includes Regional Fixe	d Effects

Table 1: First Stage Results: General Machines

Standard errors in parentheses. Significance: \*\*\* p<.01, \*\* p<.05, \* p<.1.

The remaining two boxes include regional controls from the Census and firm level controls from the manufacturing survey. The regional controls are by prefecture, and include the percentage

<sup>&</sup>lt;sup>30</sup>This second result is in line with recent findings on firm and industry responses to changes in labor supply of Gonzalez and Ortega (2011) and Dustmann and Glitz (2012).

of each type with a non-agricultural Hukou. The firm level controls include the share of foreign equity, whether the firm is in an urban area, and the age of the firm. Most interestingly, firms in urban areas or with higher shares of foreign equity tend to have increasingly higher demand for higher skilled workers, as evidenced by the increasing pattern of coefficients across worker types.<sup>31</sup>

Inclusion of controls for average worker age, which control for accumulated skill or vintage human capital, do not appreciably alter the results. Other controls which did not appreciably alter the results include State Ownership<sup>32</sup> and the percentage of migrants in a region.

As the regional labor supply available to the manufacturing sector may not be perfectly inelastic, we instrument worker wages and availability ( $w_{R,i}$  and  $a_{R,i}$ ) by service sector wages, unemployment and total workforce shares. The results (see Appendix) do not drastically change the point estimates of structural model parameters, while the standard errors of estimates increase.

These first stage estimates are interesting in themselves, as the model then implies the unit cost function for labor by region. The dispersion of estimated unit labor costs in the General Purpose Machine industry are depicted in Figure 6.1.

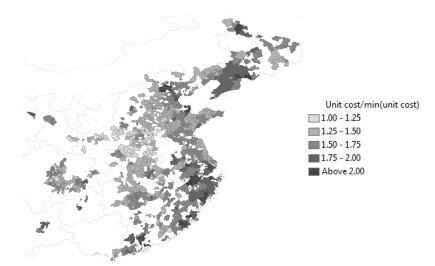


Figure 6.1: Geographic Dispersion of Unit Labor Costs: General Machines

Many other features of regional factor markets might influence the relative effectiveness of capital and materials to labor, such as the depth of input/output markets, infrastructure or agglomerative forces. To control for these features, we use Equation (4.3) to estimate regional capital and material quality using the distance from the center of each firm's county to the nearest large city

<sup>&</sup>lt;sup>31</sup>The latter of these two patterns is supported by estimates of the skill composition in Swedish firms by Carl Davidson, Fredrik Heyman, Steven Matusz, Fredrik Sjoholm, and Susan Zhu (2013).

<sup>&</sup>lt;sup>32</sup>The two industries with the highest share of state ownership, Printing and Transport, were censored over concerns regarding hiring incentives and geographic location. Both industries in any case are relatively capital intensive, so that labor market concerns are not of primary importance.

(per 100 km), arriving at

$$\widehat{\ln \tau_R^K} = .339 \cdot \text{Distance to City (per 100 km)} + \text{Industry Fixed Effect},$$
$$\widehat{\ln \tau_R^M} = .270 \cdot \text{Distance to City (per 100 km)} + \text{Industry Fixed Effect}.$$

The model primitives of the two stage estimation procedure across industries are summarized in Tables 2 and 3. Standard errors are calculated using a bootstrap procedure stratified on industry and region, presented in the Appendix. Table 2 displays the estimated model primitives, showing a range of significantly different technologies  $\theta^T$  and match quality distributions through *k*. Table 3 shows the second stage estimation results, where the regional unit labor costs are calculated using regional data and the first stage estimates.

Industry	k	θ	Industry	k	θ
Beverage	2.12 (.38)	1.24 (.08)	Non-ferrous Metal	2.89 (.38)	1.15 (.05)
Electrical	2.60 (.15)	1.22 (.02)	Non-metal Products	2.02 (.16)	1.25 (.04)
Food	1.59 (.36)	1.28 (.13)	Paper	6.25 (3.8)	0.73 (.11)
General Machines	2.50 (.14)	1.22 (.03)	Plastic	3.51 (.29)	1.08 (.03)
Iron & Steel	3.21 (.56)	1.00 (.06)	PC & AV	2.21 (.14)	1.41 (.04)
Leather & Fur	2.15 (.70)	0.76 (.14)	Specific Machines	1.63 (.18)	1.43 (.07)
Precision Tools	2.34 (.18)	1.43 (.05)	Textile	3.73 (.36)	0.95 (.03)
Metal Products	3.20 (.24)	1.10 (.03)	Wood	1.52 (.22)	1.62 (.17)

Table 2: Hiring Model Primitive Estimates

Bootstrapped Standard Errors reported in parentheses.

Industry	$\alpha_L$	$\alpha_{K}$	$\alpha_M$	Industry	$\alpha_L$	$\alpha_{K}$	$\alpha_M$
Beverage	.17 (.06)	.10 (.01)	.67 (.04)	Non-metal Products	.21 (.02)	.07 (.01)	.60 (.02)
Electrical	.27 (.01)	.13 (.01)	.46 (.01)	Paper	.12 (.39)	.14 (.03)	.57 (.30)
Food	.16 (.08)	.08 (.01)	.68 (.06)	PC & AV	.18 (.01)	.20 (.01)	.43 (.01)
General Machines	.18 (.02)	.12 (.01)	.60 (.02)	Plastic	.26 (.04)	.14 (.01)	.41 (.02)
Iron & Steel	.43 (.07)	.06 (.01)	.46 (.05)	Precision Tools	.22 (.01)	.15 (.01)	.42 (.01)
Leather & Fur	.03 (.11)	.14 (.02)	.64 (.07)	Specific Machines	.13 (.03)	.16 (.01)	.53 (.02)
Metal Products	.25 (.01)	.13 (.01)	.45 (.01)	Textile	.08 (.06)	.11 (.01)	.63 (.04)
Non-ferrous Metal	.43 (.03)	.08 (.01)	.41 (.02)	Wood	.27 (.12)	.09 (.02)	.52 (.08)

Table 3: Second Stage Estimates

Bootstrapped Standard Errors reported in parentheses.

While the capital coefficients may seem low, they are not out of line with other estimates which specifically account for material inputs (e.g. Javorcik (2004)). For the specific case of China, there

are few comparable studies.<sup>33</sup>

## 6.2 Implied Productivity Differences Across Firms

Table 4 quantifies the implied differences in unit labor costs. The  $c_R^T$  column displays the interquartile (75%/25%) unit labor cost ratios by industry where unit labor costs have been calculated according to the model, and range from about 30 to 80 percent cost differences within industry. The  $(c_R^T)^{\alpha_L^T}$  column takes into account substitution into non-labor inputs and range from 2 to 17 percent. For example, consider two firms in General Machines at the 25th and 75th unit labor cost percentile. If both firms have the same wage bill, the labor (*L*) available to the lower cost firm is 1.41 times greater than the higher cost firm. From Table 3 above, the estimated share of wages in production is  $\alpha_L^T = .18$ , so the lower cost firm will produce  $1.41^{.18} = 1.06$  times as much output as the higher cost firm, holding all else constant.

		o.T			
	$c_R^T$	$(c_R^T)^{\alpha_L^I}$		$c_R^T$	$(c_R^T)^{\alpha_L^i}$
Industry	75/25	75/25	Industry	75/25	75/25
Beverage	1.51	1.07	Non-metal Products	1.42	1.08
Electrical	1.38	1.09	Paper	1.66	1.06
Food	1.81	1.10	PC & AV	1.44	1.07
General Machines	1.41	1.06	Plastic	1.35	1.08
Iron & Steel	1.34	1.13	Precision Tools	1.80	1.14
Leather & Fur	1.92	1.02	Specific Machines	1.99	1.09
Metal Products	1.33	1.07	Textile	1.37	1.03
Non-ferrous Metal	1.45	1.17	Wood	1.47	1.11

Table 4: Intraindustry Unit Labor Cost Ratios

Table 4 indicates that the range of total unit costs faced by firms within the same industry are indeed substantial, even after explicitly taking into account the technology  $\theta^T$  and the ability to substitute across several types of local workers. However, the second stage estimates indicate these differences are attenuated by substitution into capital and materials. Thus, while differences in regional markets indicate an interquartile range of 30-80% in unit cost differences, substitution into other factors reduces this range to between 2-17%.

Table 5 displays similar calculations for capital and materials. The  $(\tau_R^K)^{\alpha_K^T}$  and  $(\tau_R^M)^{\alpha_M^T}$  columns display the interquartile ratio of capital and material quality, ranging from about 8 to 14 percent for

<sup>&</sup>lt;sup>33</sup>Though not directly comparable, macroeconomic level estimates include Chow (1993) and Ozyurt (2009) who find much higher capital coefficients. These studies do not account for materials. The most comparable study is Fleisher and Wang (2004) who find microeconomic estimates for  $\alpha_K$  in the range of .40 to .50 (they do not differentiate between capital and materials) and this compares favorably with the combined estimates of  $\alpha_K + \alpha_M$  in Table 3.

capital and 6 to 11 percent for materials. Clearly estimated differences in labor markets are substantially wider, in part due to the fact that we observe more information about workers than types of capital or materials. Finally, the  $u_R^T$  column contains the differences in productivity implied by regional cost differences as laid out in Section 2.4.

	$( au_R^K)^{lpha_K^T}$	$\left( au_{R}^{M} ight)^{lpha_{M}^{T}}$	$u_R^T$		$( au_R^K)^{lpha_K^T}$	$( au_R^M)^{lpha_M^T}$	$u_R^T$
Industry	75/25	75/25	75/25	Industry	75/25	75/25	75/25
Beverage	1.11	1.09	1.10	Non-metal Products	1.13	1.10	1.11
Electrical	1.14	1.11	1.11	Paper	1.12	1.09	1.10
Food	1.11	1.09	1.12	PC & AV	1.14	1.11	1.10
General Machines	1.12	1.09	1.09	Plastic	1.10	1.08	1.11
Iron & Steel	1.09	1.07	1.14	Precision Tools	1.12	1.09	1.12
Leather & Fur	1.08	1.06	1.07	Specific Machines	1.12	1.09	1.09
Metal Products	1.12	1.10	1.09	Textile	1.09	1.07	1.06
Non-ferrous Metal	1.11	1.08	1.16	Wood	1.12	1.09	1.11

Table 5: Intraindustry Capital, Material and Productivity Ratios

Table 6 examines the variance of productivity by industry under the unit cost method (Column 1) compare to estimating output by a Cobb-Douglas combination of capital, materials and the number of each worker type (Column 2). Column 3 of Table 6 shows the average percentage that unexplained productivity is reduced per firm under the unit labor cost method.<sup>34</sup> As shown by the Table, the variance of unexplained productivity is reduced by 4 to 45 percent once local factor markets are explicitly accounted for, showing that this approach does indeed provide more information about the determinants of firm productivity.

	Unit	Four	Avg %		Unit	Four	Avg %
Industry	Cost $\sigma^2$	Types $\sigma^2$	Reduced	Industry	Cost $\sigma^2$	Types $\sigma^2$	Reduced
Beverage	.40	.54	.21	Non-metal Products	.27	.43	.25
Electrical	.38	.67	.29	Paper	.45	.56	.15
Food	.43	.59	.16	PC & AV	.71	.94	.23
General Machines	.32	.46	.19	Plastic	.38	.65	.28
Iron & Steel	.22	.66	.45	Precision Tools	.46	.69	.24
Leather & Fur	.47	.46	.04	Specific Machines	.49	.61	.13
Metal Products	.37	.61	.28	Textile	.41	.45	.08
Non-ferrous Metal	.21	.64	.44	Wood	.26	.45	.28

Table 6: Percentage of Productivity Explained by Unit Cost Method

<sup>34</sup>Most models used in production estimation assume perfect labor substitutability. Such models imply that, conditional on wages, the local composition of the workforce is irrelevant for hiring. The approach of this paper incorporates local factor supply and an empirical comparison with other models is presented in Appendix C.2. We next quantify the net impact of these productivity differences across China by evaluating the change in real income consumers would experience if labor markets were homogeneous.

### 6.3 Welfare and Local Factor Market Costs

Letting  $\{u_R^T\}$  be the estimated unit costs for China,  $\mathbb{P}_R$  the population of manufacturing workers in region *R* and  $\chi^T$  the share of consumption for each industry *T* as given by the 2002 Input-Output Tables for China, Equation (3.4) can be computed for new unit costs  $\{v_R^T\}$ . In particular, we consider a hypothetical Chinese economy in which complete worker mobility has caused the distribution of workers and wages across regions to equalize. To arrive at  $\{v_R^T\}$ , we use our model parameter estimates while assuming that each region contains the nationally averaged frequency of each worker type who receives the nationally averaged wage for their type. This implies a more even distribution of worker types and wages that will reallocate expenditure across regions and industries in potentially advantageous ways. In particular, more firms will enter into areas where costs drop and will exit areas where costs rise. Direct calculation of Equation (3.4) yields a real income gain of 1.63 percent. This suggests that while factor market differences are large, if firms eventually relocate in response to these new conditions as in our model, the net welfare gains are in line with other estimates of the gains from trade for large countries.

Since firms locate freely, the model predicts that these substantial cost differences drive economic activity towards more advantageous locations, which we now examine.

## 6.4 Firm Location

Per capita volumes of economic activity across regions are determined by Equation (3.9), which states that relatively lower industry labor costs should attract relatively more firms to a region. Table 7 summarizes estimates of this relationship, controlling for regional distance to the nearest city (weighted by the share of log value added in a region).<sup>35</sup> A firm's distance from a city may explain many factors, and above we have seen firms closer to cities have relatively higher capital and material quality. Even controlling for geography, the impact of advantageous labor markets still often remains. Whenever the relationship between value added and labor costs is statistically significant, the relationship is negative, in line with the model.<sup>36</sup> While the point estimates vary, the median significant estimate is about -.7, indicating a 10% increase in unit labor costs is associated with an 7% decrease in value added per capita.

<sup>&</sup>lt;sup>35</sup>Rizov and Zhang (2013) find that aggregate productivity is higher in regions with high population density, and the theory of this paper implies productivity drives increased entry.

<sup>&</sup>lt;sup>36</sup>These results are robust if distance is unweighted, and to the inclusion of Economic Zone status.

		Std	100 km	Std		Std		
Industry	$\ln\left(c_{R}^{T}\right)$	Err	to City	Err	Const	Err	Obs	$R^2$
Beverage	-0.671***	(.241)	-0.0993	(.097)	18.74***	(2.936)	155	.035
Electrical	0.229	(.376)	-0.769***	(.120)	8.844*	(4.489)	166	.253
Food	-0.555**	(.219)	-0.439***	(.113)	15.82***	(2.070)	171	.108
General Machines	-0.408	(.351)	-0.776***	(.120)	16.39***	(4.247)	195	.206
Iron & Steel	-0.880	(.609)	-0.426***	(.132)	15.07***	(2.396)	160	.080
Leather & Fur	-1.052***	(.262)	-0.554***	(.159)	23.60***	(3.177)	89	.300
Metal Products	0.0490	(.383)	-0.769***	(.113)	10.58***	(4.014)	157	.260
Non-ferrous Metal	-2.096***	(.430)	-0.534***	(.119)	28.64***	(3.610)	139	.199
Non-metal Products	-0.423	(.281)	-0.495***	(.070)	16.39***	(3.270)	259	.155
Paper	-0.806***	(.200)	-0.354***	(.121)	19.12***	(2.099)	159	.155
PC & AV	-0.611**	(.279)	-1.037***	(.152)	19.66***	(3.506)	90	.318
Plastic	0.00746	(.334)	-0.671***	(.104)	10.66***	(3.773)	159	.209
Precision Tools	-0.271	(.274)	-0.677***	(.156)	13.51***	(3.109)	68	.170
Specific Machines	-0.238	(.177)	-0.452***	(.094)	14.01***	(2.190)	167	.121
Textile	-0.623**	(.292)	-0.777***	(.099)	17.26***	(2.584)	186	.260
Wood	-2.020***	(.313)	-0.567***	(.165)	43.74***	(5.214)	133	.215

Table 7: Determinants of Regional (Log) Value Added per Capita

Standard errors in parentheses. Significance: \*\*\* p<.01, \*\* p<.05, \* p<.1.

# 7 Conclusion

This paper examines the importance of local supply characteristics in determining firm input usage and productivity. To do so, a theory and empirical method are developed to identify firm input demand across industries and heterogeneous labor markets. The model derives labor demand as driven by the local distribution of wages and available skills. Firm behavior in general equilibrium is derived, and determines firm location as a function of regional costs. This results in an estimator which can be easily implemented in two steps. The first step exploits differences in firm hiring patterns across distinct regional factor markets to recover firm labor demand by type, and similarly, differences in regional factor quality. These estimates quantify local unit labor costs and combine otherwise disparate data sets on firms and labor markets into a unified framework. The second step introduces local factor market costs into production function estimation. Both steps characterize the impact of local market conditions on firm behavior through recovery of model primitives. This is of particular interest when explaining the relative productivity or location of firms, especially in settings where local characteristics are highly dissimilar.

Applying the model framework to China, which possesses a large number of distinct and varied factor markets shows this approach uncovers substantial determinants of firm heterogeneity. Estimates imply an interquartile difference in labor costs of 30 to 80 percent and productivity differences of 2 to 17 percent. Differences in capital and material quality explain similar interquartile differences. The results illustrate that local factor market conditions explain substantial differences in firm workforce composition, input use and productivity. This is underscored by the estimate that complete homogenization of labor markets would lead to a 1.63 percent increase in real income for Chinese consumers as firms adapt to local factor market conditions. In addition, the variance of unexplained productivity is reduced by 4 to 45 percent compared to a standard estimation approach which does not account for local factor markets. Modeling a firm's local environment yields substantial insights into production patterns that are quantitatively important.

The importance of local factor markets for understanding firm behavior suggests new dimensions for policy analysis. For instance, regions with labor markets which generate lower unit labor costs tend to attract higher levels of firm activity within an industry. As unit labor costs depend on rather the distribution of wages *and* worker types that represent substitution options, this yields a deeper view of how educational policy or flows of different worker types impact firms. For this reason, work evaluating wage determination could be enriched by taking this approach.<sup>37</sup> Taken as a whole, the results show that policy changes which influence the composition of regional labor markets will likely have sizable effects on firm productivity and location. Finally, the substantial differences *within industry* suggest that at the regional level, inherent comparative advantages exist which policymakers might leverage.<sup>38</sup>

Furthermore, as pointed out by Ottaviano and Peri (2013), little is known about the dynamic relationships between labor markets and firm behavior, and this paper provides both a general equilibrium theory and structural estimation strategy to evaluate these linkages.<sup>39</sup> Having seen that cost and productivity differences inherent in local factor markets are potentially large, our approach could be of use in evaluating trade offs between regional policies or ongoing trends across regions. Finally, nothing precludes the application of this paper's approach beyond China, and it is suitable for analyzing regions which exhibit a high degree of labor market heterogeneity. Further work could leverage or extend the approach of combining firm, census and geographic data to better understand the role of local factor markets on firm behavior.

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<sup>38</sup>For a discussion of broader policy implications of regional differences in production, see Luger and Evans (1988).

<sup>&</sup>lt;sup>37</sup>There is large literature following Hellerstein, Neumark, and Troske (1999). For instance, Van Biesebroeck (2011) find the usual relationship between wages and marginal productivity breaks down in less developed countries. Investigating this relationship using our approach could shed light on regional determinants of labor market clearing, for instance evaluating gender differentials as in Dong and Zhang (2009).

<sup>&</sup>lt;sup>39</sup>Early results suggest firm entry is responsive to labor market changes, especially in manufacturing (Olney, 2013).

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# Appendix

The organization of the Appendix is as follows: Section A contains proofs of results discussed in the main text. Section B evaluates the efficacy of the reduced form model estimator. Section C contains more detail regarding model estimates. Three supplemental appendices are provided for online publication: Section D contains additional details on the model solution and properties. Section E contains summary statistics. Section F contains supplemental empirical results.

# A Proofs

**Proposition.** If  $\beta^T > 0$  then it is optimal for a firm to hire all types of workers.

*Proof.* Let  $c_R^T$  denote a firm's unit labor cost when all worker types are hired, and  $\check{c}_R^T$  the unit labor cost if a subset of types  $\mathbb{T} \subset \{1, \ldots, \mathbb{S}\}$  is hired. For the result, we require that  $c_R^T \leq \check{c}_R^T$  for all  $\mathbb{T}$ . Considering a firm's cost minimization problem when  $\mathbb{T}$  are the only types available shows with Equation (2.7) that

$$\check{c}_{R}^{T} = \left[\sum_{i \in \mathbb{T}} \left[ a_{R,i} \left( \underline{m}_{i}^{T} \right)^{k} w_{R,i}^{1-k} / f\left(k-1\right) \right]^{\theta^{T}/\beta^{T}} \right]^{\left(\beta^{T}/\theta^{T}\right)/(1-k)}$$

Considering then that

$$c_{R}^{T}/\check{c}_{R}^{T} = \left[1 + \left(\sum_{i \notin \mathbb{T}} \left[a_{R,i}\left(\underline{m}_{i}^{T}\right)^{k} w_{R,i}^{1-k}\right]^{\theta^{T}/\beta^{T}} / \sum_{i \in \mathbb{T}} \left[a_{R,i}\left(\underline{m}_{i}^{T}\right)^{k} w_{R,i}^{1-k}\right]^{\theta^{T}/\beta^{T}}\right)\right]^{\left(\beta^{T}/\theta^{T}\right)/(1-k)},$$

clearly  $c_R^T \leq \check{c}_R^T$  so long as  $\beta^T / \theta^T (1-k) \leq 0$ , which holds for  $\beta^T > 0$  since k > 1.

#### Proposition. An equilibrium wage vector exists which clears each regional labor market.

*Proof.* What is required is to exhibit a wage vector  $\{w_{R,i}\}$  that ensures Equation (3.8) holds. To do so, first note that the resource clearing conditions determine wages, provided an exogenous vector of unit labor costs  $\{c_R^T\}$ . Since all prices are nominal, WLOG we normalize  $I_{Agg} = 1$  in the following

**Lemma.** There is a wage function that uniquely solves (3.8) given unit labor costs.

*Proof.* Formally, we need to exhibit  $\mathbb{W}$  such that

$$a_{R,i} = \mathbb{W}_{R,i}\left(\left\{c_{R'}^{T'}\right\}\right)^{-1} \sum_{t} \alpha_{L}^{t} \sigma^{t} \left(c_{R}^{t}\right)^{k/\beta^{t}-1} \left(\frac{\mathbb{W}_{R,i}\left(\left\{c_{R'}^{T'}\right\}\right)^{1-k} a_{R,i}\left(\underline{m}_{i}^{t}\right)^{k}}{f\left(k-1\right)}\right)^{\theta^{t}/\beta^{t}} \forall R, i.$$

Fix  $\{c_{R'}^{T'}\}$  and define  $h_{R,i}(x) \equiv \sum_{t} \alpha_L^t \sigma^t (c_R^t)^{k/\beta^t - 1} (x^{1-k}a_{R,i}(\underline{m}_i^t)^k / f(k-1))^{\theta^t/\beta^t}$ ,  $g_{R,i}(x) \equiv a_{R,i}x$ . For the result we require a unique *x* s.t.  $g_{R,i}(x) = h_{R,i}(x)$ .  $g_{R,i}$  is strictly increasing and ranges from 0 to  $\infty$ , while  $h_{R,i}(x)$  is strictly decreasing, and ranges from  $\infty$  to 0, so *x* exists and is unique.

Of course, unit labor costs are not exogenous as in the Lemma, but rather depend on endogenous wages  $\{w_{R,i}\}$ . However, the lemma does show that the following mapping:

$$\{w_{R,i}\} \underset{\text{Equation 2.7}}{\mapsto} \{c_R^T(\{w_{R,i}\})\} \underset{\text{Lemma}}{\mapsto} \mathbb{W}\left(\{c_R^T(\{w_{R,i}\})\}\right),$$

which starts at one wage vector  $\{w_{R,i}\}$  and ends at another wage vector  $\mathbb{W}$  is well defined. This follows if we can show the function  $\{c_R^T \circ \mathbb{W}(\{c_R^T\})\}$ , where  $c_R^T$  is the unit cost function of Equation (2.7), has a fixed point  $\{\hat{c}_R^T\}$  and so  $\mathbb{W}(\{\hat{c}_R^T\})$  is a solution to Equation (3.8).

We first show that any equilibrium wage vector must lie in a strictly positive, compact set  $\times_{R,i} [\underline{w}_{R,i}, \overline{w}_{R,i}]$ . From (3.8),  $H_{R,i}^{\theta^T} / \Sigma_j H_{R,j}^{\theta^T} \in [0,1]$  so  $w_{R,i} \leq \overline{w}_{R,i} \equiv \sum_t \alpha_L^t \sigma^t / a_{R,i}$ . Let

$$\underline{b}_{R} \equiv \min_{i} \sum_{t} \alpha_{L}^{t} \sigma^{t} \left( a_{R,i} \left( \underline{m}_{i}^{t} \right)^{k} \right)^{\theta^{t}/\beta^{t}} / \sum_{i} \left[ a_{R,i} \left( \underline{m}_{i}^{t} \right)^{k} \right]^{\theta^{t}/\beta^{t}} a_{R,i},$$

and we will show that a lower bound for equilibrium wages is  $\underline{w}_R \equiv \begin{bmatrix} \underline{b}_R, & \dots, & \underline{b}_R \end{bmatrix}$  for each *R*. Consider that for  $\mathbb{W}$  evaluated at  $\{c_R^T(\underline{w}_R)\}$ ,

$$\mathbb{W}_{R,i} = \sum_{t} \alpha_{L}^{t} \sigma^{t} \left( a_{R,i} \left( \underline{m}_{i}^{t} \right)^{k} \left( \mathbb{W}_{R,i} / \underline{w}_{R} \right)^{1-k} \right)^{\theta^{t} / \beta^{t}} / \sum_{i} \left[ a_{R,i} \left( \underline{m}_{i}^{t} \right)^{k} \right]^{\theta^{t} / \beta^{t}} a_{R,i}.$$
(A.1)

Evaluating Equation (A.1), if  $\mathbb{W}_{R,i} \leq \underline{w}_R$  then  $\mathbb{W}_{R,i} \geq \underline{w}_R$ , and otherwise,  $\mathbb{W}_{R,i} \geq \underline{w}_R$  so  $\{\underline{w}_R\}$  is a lower bound for  $\mathbb{W}\left(\left\{c_R^T(\underline{w}_R)\right\}\right)$ . Since necessarily  $\mathbb{W}\left(\left\{c_R^T(\hat{w}_R)\right\}\right) = \{\hat{w}_R\}$ ,  $\mathbb{W}$  is increasing in  $\{c_R^T\}$ , and  $c_R^T(w_R)$  is increasing in  $w_R$ , we have  $\{\hat{w}_R\} = \mathbb{W}\left(\left\{c_R^T(\hat{w}_R)\right\}\right) \geq \mathbb{W}\left(\left\{c_R^T(\underline{w}_R)\right\}\right) \geq \{\underline{w}_R\}$ . In conclusion, all equilibrium wages must lie in  $\times_{R,i} [\underline{w}_{R,i}, \overline{w}_{R,i}]$ . Now define a strictly positive, compact domain for  $\{c_R^T\}$ ,  $\times_R [\underline{c}_R^T, \overline{c}_R^T]$ , by

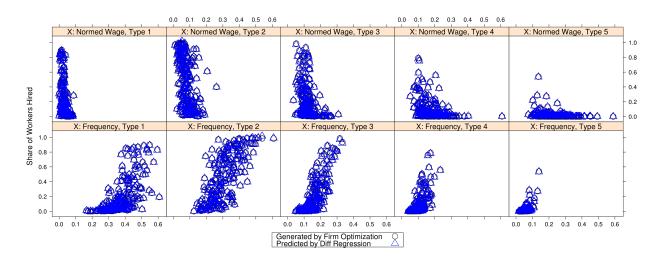
$$\underline{c}_{R}^{T} \equiv \inf_{\times_{i} \left[ \underline{w}_{R,i}, \overline{w}_{R,i} \right]} c_{R}^{T} \left( w_{R} \right) = c_{R}^{T} \left( \underline{w}_{R} \right), \qquad \overline{c}_{R}^{T} \equiv \sup_{\times_{i} \left[ \underline{w}_{R,i}, \overline{w}_{R,i} \right]} c_{R}^{T} \left( w_{R} \right) = c_{R}^{T} \left( \overline{w}_{R} \right).$$

Now consider the mapping  $\mathbb{C}(\{c_R^T\}) \equiv \{c_R^T \circ \mathbb{W}(\{c_R^T\})\}$  on  $\times_R[\underline{c}_R^T, \overline{c}_R^T]$ , which is continuous on this domain. By above,  $\mathbb{W}_{R,i}(\{c_R^T\}) \leq \overline{w}_{R,i}$  for each R, i so  $\mathbb{C}(\{c_R^T\}) \leq \{\overline{c}_R^T\}$ . Also by above,  $\mathbb{C}(\{c_R^T\}) \geq \{c_R^T \circ \mathbb{W}(\{c_R^T(\underline{w}_R)\})\} \geq \{c_R^T(\{\underline{w}_R\})\} = \{\underline{c}_R^T\}$ . Thus  $\mathbb{C}$  maps  $\times_R[\underline{c}_R^T, \overline{c}_R^T]$  into itself and by Brouwer's fixed point theorem, there exists a fixed point  $\{\widehat{c}_R^T\}$ , which implies  $\mathbb{W}(\{\widehat{c}_R^T\})$  is an equilibrium wage vector.

# **B** Model Simulation and Estimator Viability

A model simulation was constructed using parameters given in Table A.1. In the simulation, firms maximize profits conditional on local market conditions, and applying the estimator above produces Tables A.2a and A.2b. The Estimate column contains results while the model values are reported in the Predicted column. The estimates are very close to the predicted values. Figure A.1 further confirms this by plotting the simulated and predicted differences in the share of workers hired. For ease of comparison, Figure A.1 plots regional frequencies along the horizontal axis and (linearly) normalized wages for each worker type. As the Figure suggests, the  $R^2$  in both cases are high: .99 for the first stage and .97 for the second stage.

Figure A.1: Simulation Fit



Variable	Description	Value
$\theta^T$	Technological parameter.	2
k	Pareto shape parameter.	1.5
$\{\underline{m}_i\}$	Human capital shifters.	$\{4, 8, 12, 16, 20\}$
$\{w_{R,i}\}$	Regional wages by type.	~LogNormal $\mu = (12, 24, 36, 48, 60), \sigma = 1/3.$
$\{a_{R,i}\}$	Regional type frequencies.	~LogNormal $\mu = (.4, .3, .15, .1, .05), \sigma = 1/3,$
		scaled so that frequencies sum to one.
<i>K</i> , <i>M</i>	Firm capital and materials.	~LogNormal $\mu = 1, \sigma = 1$ .
L	Level of <i>L</i> employed by firm.	Profit maximizing given K, M and region.
$\alpha_M, \alpha_K, \alpha_L$	Production Parameters.	$\alpha_M = 1/6,  \alpha_K = 1/3,  \alpha_L = 1/2.$
Control	Misc variable for output.	$\sim$ LogNormal $\mu = 0, \sigma = 1.$
Coeff	Exponent on Control.	Control Coeff= $\pi$ .
$\{\boldsymbol{\omega}_j\}$	Firm idiosyncratic wage costs.	~LogNormal $\mu = 0, \sigma = .1$ .
Sample: 200	) regions with 20 firms per region	, with errors ~LogNormal( $\mu = 0, \sigma = 1/2$ ).

Table A.1: Simulation details

Table A.2: Simulation Results

(a)	Simulation	First Stage	Estimates:	Technology	and Human	Canital
(a)	Simulation	I not Stage	Loundues.	reennoiogy	and Human	Capital

Variable	Parameter	Estimate	Std Err	Predicted
$\{\ln a_{R,i}\}$	$\left(  heta^T / eta^T  ight)$	3.912	.0019	4
$\{\ln w_{R,i}\}$	$(-k/\beta^T)$	-2.922	.0021	-3
Dummy (Type = 1)	$(\theta^T / \beta^T) k (\ln \underline{m}_1 / \underline{m}_5)$	-9.376	.0057	-9.657
Dummy (Type = 2)	$(\theta^T/\beta^T) k(\ln \underline{m}_2/\underline{m}_5)$	-5.295	.0045	-5.498
Dummy (Type = 3)	$(\theta^T/\beta^T) k(\ln \underline{m}_3/\underline{m}_5)$	-2.950	.0031	-3.065
Dummy (Type = 4)	$\left(\theta^T/\beta^T\right)k\left(\ln \underline{m}_4/\underline{m}_5\right)$	-1.274	.0024	-1.339

(b) Simulation Second Stage Estimates: Production Parameters

Variable	Parameter	Estimate	Std Err	Predicted
ln <i>M</i>	$\alpha_M/(1-\alpha_L)$	.3298	.0079	.3333
ln K	$\alpha_{K}/(1-\alpha_{L})$	.6680	.0080	.6667
$\ln c_{RT}$	$-\alpha_L/(1-\alpha_L)$	9303	.0748	-1
Control	Control Coeff	3.148	.0079	3.141

#### Model Estimates: Baseline and Instrumental Variables C

Too do not service of the service of	Domono	Electrical		General	Iron &	Leather	Precision	Metal
mansuy	Develage	dinha	Dep	Dependent Variable: $\ln (\% type)$	oleci ble: ln (%t	& rui (ype)	Equipinent	FIOUUCIS
$\ln(w_{R,i})$	$-1.808^{a}$	$-2.977^{a}$	-0.870	$-2.687^{a}$	$-2.150^{a}$	$-0.708^{c}$	$-4.517^{a}$	$-3.174^{a}$
$\ln(a_{R,i})$	$1.673^{a}$	$1.878^{a}$	$1.489^{a}$	$1.794^{a}$	$1.018^{a}$	$0.636^{a}$	$3.358^{a}$	$1.439^{a}$
$m_1$ ( $\leq$ Junior HS: Fem)	-8.447 <sup>a</sup>	-9.491 <sup>a</sup>	-3.186	$-10.170^{a}$	$7.190^{a}$	-2.052	$-13.450^{a}$	$-5.800^{a}$
$m_2$ ( $\leq$ Junior HS: Male)	$-5.947^{c}$	-7.181 <sup>a</sup>	-1.504	-6.171 <sup>a</sup>	$12.370^{a}$	-1.089	$-11.160^{a}$	$-2.176^{c}$
m <sub>3</sub> (Senior High School)	-2.470	-4.475 <sup>a</sup>	1.123	$-3.180^{a}$	$14.210^{a}$	$-2.058^{c}$	$-4.100^{b}$	-0.758
$m_1 * \%$ Non-Ag Hukou	0.837	-7.619 <sup>a</sup>	$-2.341^{b}$	$-5.957^{a}$	$-2.373^{c}$	-4.544 <sup>a</sup>	$-7.142^{a}$	$-6.038^{a}$
$m_2*\%$ Non-Ag Hukou	0.306	-3.272 <sup>a</sup>	-1.880	$-3.072^{a}$	-1.355	-2.882 <sup>c</sup>	$-3.957^{c}$	$-1.805^{b}$
<i>m</i> <sub>3</sub> *% Non-Ag Hukou	-1.102	-0.593	-0.837	$-3.218^{a}$	$-2.394^{a}$	$-1.606^{b}$	0.315	$-1.104^{b}$
$m_4*\%$ Non-Ag Hukou	-3.913	-4.572 <sup>a</sup>	-0.426	$-7.026^{a}$	$10.130^{a}$	-8.496 <sup>a</sup>	1.793	$-2.491^{b}$
$\underline{m}_1 * \text{Urban Dummy}$	-0.271	$-1.379^{a}$	-1.462 <sup>a</sup>	-1.384 <sup>a</sup>	$-1.393^{a}$	-0.0822	-1.032 <sup>a</sup>	$-1.408^{a}$
$\underline{m}_2 * \text{Urban Dummy}$	-0.007	-0.991 <sup>a</sup>	-1.085 <sup>a</sup>	$-0.980^{a}$	-0.585 <sup>a</sup>	-0.128	$-1.176^{a}$	$-0.533^{a}$
$\underline{m}_3 * \text{Urban Dummy}$	$0.286^{c}$	$0.139^{b}$	0.175	$0.427^{a}$	$0.503^{a}$	$0.220^{c}$	-0.249	$0.247^{a}$
$\underline{m}_4 * \text{Urban Dummy}$	$2.212^{a}$	$1.513^{a}$	$1.743^{a}$	$2.336^{a}$	3.275 <sup>a</sup>	$0.683^{a}$	$1.053^{a}$	$2.147^{a}$
$m_1 * \%$ Foreign Equity	$0.531^{a}$	$1.030^{a}$	$0.841^{a}$	$0.934^{a}$	$0.751^{a}$	-0.107	$1.952^{a}$	$0.876^{a}$
$m_2*\%$ Foreign Equity	$0.422^{a}$	$0.678^{a}$	$0.661^{a}$	$0.403^{a}$	$0.354^{a}$	-0.0680	$1.840^{a}$	$0.335^{a}$
$m_3*\%$ Foreign Equity	0.106	$0.259^{a}$	$0.197^{b}$	$0.143^{a}$	0.083	$0.257^{a}$	$0.574^{a}$	$0.145^{a}$
$m_{4*}\%$ Foreign Equity	-0.005	$0.232^{a}$	0.015	$0.351^{a}$	-0.069	0.249	0.033	-0.150
$m_1 * \ln(\text{Firm Age})$	$-2.803^{a}$	-0.215	$-0.983^{a}$	$-2.448^{a}$	$-2.160^{a}$	0.113	$0.727^b$	-0.627 <sup>a</sup>
$m_2 * \ln(\text{Firm Age})$	$-2.290^{a}$	-0.547 <sup>a</sup>	-0.494 <sup>c</sup>	-1.864 <sup>a</sup>	-1.662 <sup>a</sup>	$-0.190^{b}$	0.319	-0.788 <sup>a</sup>
$m_3 * \ln(\text{Firm Age})$	$0.714^{a}$	-0.114	0.016	$0.311^{a}$	$0.862^{a}$	0.198	$-0.510^{b}$	$0.417^{a}$
$m_4 * \ln(\text{Firm Age})$	$2.840^{a}$	1.621 <sup>a</sup>	$2.301^{a}$	$3.847^{a}$	$5.656^{a}$	$3.133^{a}$	0.279	$3.488^{a}$
Regional Fixed Effects	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Observations	8,900	48,960	15,228	62,908	18,704	19,408	10,808	42,744
R-squared	0.124	0.117	0.098	0.139	0.168	0.208	0.246	0.124
Note: a, b and c denote 1,	5 and 10% 5	5 and 10% significance level respectively	level respe	ectively.				

Table A.3: First Stage Estimates I

	Non-ferrous	Other			PC & AV	Specific		
Industry	Metal	Non-metal	Paper	Plastic	Equipment	Machines	Textile	Wood
				Depender	<b>Dependent Variable: In</b>	ı (%type)		
$\ln(w_{R,i})$	$-3.096^{a}$	$-1.693^{a}$	-1.542 <sup>a</sup>	-3.324 <sup>a</sup>	$-3.371^{a}$	$-1.260^{a}$	$-2.230^{a}$	$-1.220^{b}$
$\ln(a_{R,i})$	$1.627^{a}$	$1.664^{a}$	$0.332^{b}$	$1.321^{a}$	$2.785^{a}$	$1.961^{a}$	$0.830^{a}$	$2.286^{a}$
$m_1$ ( $\leq$ Junior HS: Fem)		$-7.246^{a}$	$-3.469^{c}$	-7.881 <sup>a</sup>	$-13.770^{a}$	$-10.130^{a}$	1.588	$-10.890^{a}$
$m_2$ ( $\leq$ Junior HS: Male)		$-3.128^{a}$	-0.645	$-4.596^{a}$	$-11.970^{a}$	-4.811 <sup>a</sup>	$2.703^{b}$	-9.086 <sup>a</sup>
m <sub>3</sub> (Senior High School)		-0.808	0.076	-2.657 <sup>b</sup>	$-7.325^{a}$	-1.515	$3.468^{a}$	$-6.106^{b}$
$m_1 * \%$ Non-Ag Hukou		$-2.750^{a}$	$-6.210^{a}$	-6.682 <sup>a</sup>	$-7.176^{a}$	$-4.763^{a}$	-6.271 <sup>a</sup>	-0.301
<i>m</i> <sub>2</sub> <i>*%</i> Non-Ag Hukou		$-1.750^{a}$	-6.148 <sup>a</sup>	$-4.710^{a}$	$-5.210^{a}$	$-4.295^{a}$	-5.555 <sup>a</sup>	-0.308
<i>m</i> <sub>3</sub> *% Non-Ag Hukou		$-2.198^{a}$	-3.251 <sup>a</sup>	-2.685 <sup>a</sup>	0.597	$-1.463^{a}$	-3.264 <sup>a</sup>	-2.549 <sup>a</sup>
<i>m</i> <sub>4</sub> *% Non-Ag Hukou		$-3.926^{a}$	-7.690 <sup>a</sup>	$-7.074^{a}$	$-3.291^{a}$	-2.447	-4.025 <sup>a</sup>	$-13.060^{a}$
$\underline{m}_1 * \text{Urban Dummy}$		$-1.333^{a}$	-0.691 <sup>a</sup>	$-1.057^{a}$	-1.881 <sup>a</sup>	$-1.597^{a}$	$-0.650^{a}$	$-1.630^{a}$
$\underline{m}_2 * \text{Urban Dummy}$		$-0.834^{a}$	$-0.338^{b}$	$-0.590^{a}$	$-1.619^{a}$	-1.234 <sup>a</sup>	-0.421 <sup>a</sup>	$-0.720^{a}$
$\underline{m}_3 * \text{Urban Dummy}$		$0.250^{a}$	$0.350^{a}$	$0.272^{a}$	$-0.512^{a}$	$0.216^b$	$0.285^{a}$	0.129
$\underline{m}_4 * \text{Urban Dummy}$		$2.570^{a}$	$2.644^{a}$	$2.413^{a}$	$0.902^{a}$	$1.924^{a}$	$2.709^{a}$	$3.331^{a}$
<i>m</i> <sub>1</sub> <i>*%</i> Foreign Equity		$0.834^{a}$	$0.407^{a}$	$0.877^{a}$	$1.340^{a}$	$1.588^{a}$	$0.214^{a}$	$0.415^{a}$
<i>m</i> <sub>2</sub> <i>*%</i> Foreign Equity		$0.244^{a}$	$0.153^{c}$	$0.361^{a}$	$1.072^{a}$	$0.750^{a}$	$0.202^{a}$	0.176
<i>m</i> <sub>3</sub> <i>*%</i> Foreign Equity		0.028	0.039	0.048	$0.294^{a}$	$0.169^{a}$	$0.137^{a}$	-0.142
<i>m</i> <sub>4</sub> <i>*%</i> Foreign Equity		$-0.310^{a}$	-0.012	0.000	$-0.160^{b}$	0.097	$0.442^{a}$	0.197
$m_1 * \ln(\text{Firm Age})$		$-1.016^{a}$	$-1.899^{a}$	-0.857 <sup>a</sup>	0.310	-1.601 <sup>a</sup>	$-0.384^{a}$	-0.423
$m_2 * \ln (\text{Firm Age})$		$-0.768^{a}$	-0.819 <sup>a</sup>	$-0.773^{a}$	0.223	-1.675 <sup>a</sup>	-0.058	0.066
$m_3 * \ln (\text{Firm Age})$		0.105	$0.457^{a}$	$0.398^{a}$	-0.049	0.100	$0.445^{a}$	-0.468
$m_4 * \ln (\text{Firm Age})$	$4.413^{a}$	$3.429^{a}$	$4.850^{a}$	$3.776^{a}$	$0.321^{a}$	$1.629^{a}$	$4.391^{a}$	$3.850^{a}$
Regional Fixed Effects		Yes	Yes	Yes	Yes	Yes	Yes	Yes
Observations		61,388	22,792	36,940	26,796	31,264	73,168	14,516
R-squared		0.150	0.164	0.130	0.188	0.177	0.221	0.245
Note: a, b and c denote 1, 5 a		nd 10% significance level respectively	l respectiv	ely.				

# Table A.4: First Stage Estimates II

itai ucts		156	30a	8	33	11	38	61	05	6	33a	16 <sup>b</sup>	2	<i>p</i> 0	t2 <sup>a</sup>	bJa bJa	382	<b>5</b> 4 <i>a</i>	$10^{a}$	32 <sup>a</sup>	$q_{0}$	$2^a$	SS	257	16	
Metal Products		-4.545 <sup>t</sup>	1.38	-2.84	2.66	4.79	-5.19	-0.97	-0.95	2.02	-1.23	-0.64	0.11	1.91	1.34	0.35	0.0882	0.66	-2.21	-1.98	0.67	4.71	Y	14,257	0.14	
Precision Equipment	4	-3.198															$0.147^{c}$					<i>ж</i> .		7	Ŭ	
Leather & Fur	type)	'															$0.249^{b}$									
Iron & Steel	iable	$-2.903^{c}$	0.737	6.569	12.11	13.66	-3.391	-2.213	-2.582	9.228	-1.384 <sup>a</sup>	$-0.608^{b}$	$0.500^{b}$	$3.310^{a}$	$0.739^{a}$	$0.330^{a}$	0.0786	-0.00873	$-2.191^{a}$	-1.764 <sup>a</sup>	$0.851^{a}$	$5.806^{a}$	Yes	18,600	0.168	
General Machines	Dependent Var	-2.891	$1.693^{a}$	-9.858	-5.764	-2.967	$-6.158^{b}$	-3.259	-3.145	-6.701	$-1.399^{a}$	$-0.994^{a}$	$0.431^{a}$	$2.347^{a}$	$0.928^{a}$	$0.397^{a}$	$0.151^{a}$	$0.340^{a}$	-2.471 <sup>a</sup>	$-1.904^{a}$	0.324	$3.888^{a}$	Yes	62,563	0.139	ectively.
Food	De	-0.186	$1.507^{a}$	-1.710	-0.259	2.302	-2.187	-1.690	-0.704	0.774	$-1.439^{a}$	$-1.057^{a}$	0.176	$1.613^{a}$	$0.854^{a}$	$0.675^{a}$	$0.205^{b}$	-0.0120	-0.957a	-0.451	0.0237	$2.325^{a}$	Yes	15,087	0.097	level resp
Electrical Equip	•	$-3.238^{b}$	$1.787^{a}$	$-9.325^{b}$	$-6.928^{c}$	-4.301	-7.779 <sup>b</sup>	-3.373	-0.543	-4.320	-1.401 <sup>a</sup>	-1.012 <sup>a</sup>	0.139	$1.545^{a}$	$1.029^{a}$	$0.678^{a}$	$0.254^{a}$	$0.224^{b}$	-0.225	$-0.582^{b}$	-0.110	$1.658^{a}$	Yes	48,750	0.118	and 10% significance level respectively
Beverage		-1.721	$1.456^{a}$	-7.807	-5.249	-2.035	0.101	-0.453	-1.375	-3.923	-0.299	-0.0368	0.327	$2.204^{a}$	$0.526^{a}$	$0.417^{a}$	0.103	0.0120	$-2.860^{a}$	$-2.342^{a}$	$0.758^{a}$	$2.897^{a}$	Yes	8,783	0.124	
Industry		$\ln(w_{R,i})$	$\ln(a_{R,i})$	$m_1$ ( $\leq$ Junior HS: Fem)	$m_2$ ( $\leq$ Junior HS: Male)	m <sub>3</sub> (Senior High School)	$m_1*\%$ Non-Ag Hukou	$m_2*\%$ Non-Ag Hukou	$m_3*\%$ Non-Ag Hukou	$m_4*\%$ Non-Ag Hukou	$\underline{m}_1 * \text{Urban Dummy}$	$\underline{m}_2 * \text{Urban Dummy}$	$\underline{m}_3 * \text{Urban Dummy}$	$\underline{m}_4 * \text{Urban Dummy}$	$m_1 * \%$ Foreign Equity	<i>m</i> <sub>2</sub> *% Foreign Equity	m <sub>3</sub> *% Foreign Equity	<i>m</i> <sub>4</sub> <i>*%</i> Foreign Equity	$m_1 * \ln(\text{Firm Age})$	$m_2 * \ln(\text{Firm Age})$	$m_3 * \ln (\text{Firm Age})$	$m_4 * \ln (\text{Firm Age})$	Regional Fixed Effects	Observations	R-squared	Note: a, b and c denote 1, 5

Table A.5: First Stage IV Estimates I

	Non-ferrous	Other			PC & AV	Specific		
Industry	Metal	Non-metal	Paper	Plastic	Equipment	Machines	Textile	Wood
				Dependent	e: ln (	(%type)		
$\ln(w_{R,i})$	-2.137	-1.008	-3.339	-3.621	-2.965	-1.469	-1.984	-2.190
$\ln\left(a_{R,i} ight)$	$1.586^{a}$	0.0881	$2.669^{a}$	$1.335^{b}$	$2.869^b$	$2.074^{b}$	0.632	$2.004^{b}$
$m_1$ ( $\leq$ Junior HS: Fem)	-7.588	-2.266	$-13.16^{a}$	-7.977	-9.795	$-10.54^{a}$	2.482	-7.942
$m_2$ ( $\leq$ Junior HS: Male)	-3.320	0.475	$-11.35^{b}$	-4.611	-7.848	-5.203	3.580	-5.772
m <sub>3</sub> (Senior High School)	-1.036	0.839	-6.854 <sup>c</sup>	-2.649	-1.729	-1.735	4.063	-3.304
<i>m</i> <sub>1</sub> *% Non-Ag Hukou	$-2.898^{c}$	-7.227 <sup>c</sup>	-7.501	$-6.344^{b}$	$-9.315^{c}$	-4.400	$-7.153^{c}$	-0.925
<i>m</i> <sub>2</sub> *% Non-Ag Hukou	-1.808	-7.175	-5.441	-4.350	-5.861	-3.927	-6.481	-0.640
<i>m</i> <sub>3</sub> *% Non-Ag Hukou	-2.212	-3.458	0.609	-2.521	0.253	-1.432	-3.468	-2.300
<i>m</i> <sub>4</sub> *% Non-Ag Hukou	-4.097	-7.538	-2.892	-6.724	2.990	-2.423	-3.940	-9.706
$\underline{m}_1 * \text{Urban Dummy}$	$-1.351^{a}$	$-0.705^{a}$	$-1.903^{a}$	-1.063 <sup>a</sup>	$-1.064^{a}$	$-1.587^{a}$	-0.652 <sup>a</sup>	-1.622 <sup>a</sup>
$\underline{m}_2 * \text{Urban Dummy}$	-0.855 <sup>a</sup>	$-0.355^{c}$	-1.638 <sup>a</sup>	-0.595 <sup>b</sup>	$-1.177^{a}$	-1.227 <sup>a</sup>	$-0.424^{b}$	$-0.707^{b}$
$\underline{m}_3 * \text{Urban Dummy}$	$0.247^{c}$	0.344	-0.503	0.277	-0.224	0.220	$0.294^{b}$	0.206
$\underline{m}_4 * \text{Urban Dummy}$	$2.583^{a}$	$2.677^{a}$	$0.936^{a}$	$2.404^{a}$	$1.061^{b}$	$1.874^{a}$	$2.695^{a}$	$3.095^{a}$
$m_1*\%$ Foreign Equity	$0.829^{a}$	$0.405^{a}$	$1.340^{a}$	0.875 <sup>a</sup>	$1.945^{a}$	$1.588^{a}$	$0.207^{a}$	$0.412^{a}$
<i>m</i> <sub>2</sub> <i>*%</i> Foreign Equity	$0.243^{a}$	$0.155^{c}$	$1.074^{a}$	$0.357^{a}$	$1.840^{a}$	$0.749^{a}$	$0.198^{a}$	0.153
<i>m</i> <sub>3</sub> *% Foreign Equity	0.0265	0.0430	$0.296^{b}$	0.0468	$0.575^{a}$	$0.167^{b}$	$0.136^{b}$	-0.128
<i>m</i> <sub>4</sub> <i>*%</i> Foreign Equity	$-0.312^{b}$	-0.0326	-0.167	-0.0189	0.0393	0.108	$0.472^{a}$	0.371
$m_1 * \ln(\text{Firm Age})$	$-1.024^{a}$	$-1.910^{a}$	0.312	-0.854 <sup>a</sup>	0.715	$-1.590^{b}$	$-0.387^{b}$	-0.429
$m_2 * \ln(\text{Firm Age})$	$-0.803^{a}$	$-0.817^{b}$	0.216	$-0.790^{a}$	0.341	$-1.670^{a}$	-0.0606	0.0192
$m_3 * \ln(\text{Firm Age})$	0.106	0.467	-0.0426	0.400	-0.461	0.0970	$0.454^{a}$	-0.379
$m_4 * \ln(\text{Firm Age})$	$3.503^{a}$	$4.848^{a}$	0.326	$3.793^{a}$	0.220	$1.637^{a}$	$4.404^{a}$	$3.781^{a}$
Regional Fixed Effects	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Observations	60,946	22,667	26,761	36,816	10,808	31,078	72,828	14,126
R-squared	0.150	0.164	0.188	0.129	0.246	0.178	0.219	0.212
Note: a, b and c denote 1, 5 ar	5 and 10% sign	nd 10% significance level respectively.	l respective	ly.				

Table A.6: First Stage IV Estimates II

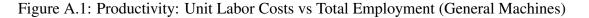
Industry	k	θ	Industry	k	θ	
Beverage	2.18 (.55)	1.16 (.11)	Non-ferrous Metal	2.35 (.20)	1.19 (.03)	0.03
Electrical	2.84 (.20)	1.18 (.03)	Non-metal Products	17.0 (5.2)	0.51 (.29)	0.29
Food	1.10 (.51)	1.39 (1.1)	Paper	2.24 (.16)	1.39 (.04)	0.04
General Machines	2.72 (.17)	1.18 (.03)	Plastic	3.69 (.33)	1.07 (.03)	0.03
Iron & Steel	6.01 (2.8)	0.91 (.07)	PC & AV	2.05 (.22)	1.48 (.09)	0.09
Leather & Fur	1.92 (.73)	0.73 (.18)	Specific Machines	1.70 (.19)	1.44 (.08)	0.08
Precision Tools	3.93 (.44)	1.02 (.03)	Textile	4.21 (.65)	0.88 (.04)	0.04
Metal Products	4.25 (.63)	1.07 (.05)	Wood	2.06 (.3)	1.33 (.09)	0.09

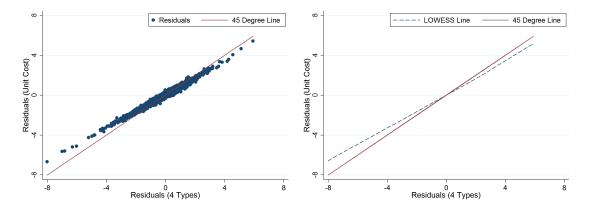
Table A.7: Hiring Model Primitive IV Estimates

Bootstrapped Standard Errors reported in parentheses.

## C.1 Residual Comparison: Unit Labor Costs vs Substitutable Labor

Of particular interest for work on productivity are the residuals remaining after the second estimation step, which are often interpreted as idiosyncratic firm productivity. Figure A.1 contrasts unexplained productivity (estimation residuals) when unit labor costs are used with estimates that measure labor by including the employment of each worker type. Examining the 45 degree line also plotted in the Figure, a general pattern emerges: above average firms under the employment measure are slightly less productive under the unit cost approach, while below average firms are more productive. This suggests that a more detailed analysis of the role of local factor markets may substantially alter interpretation of differences in firm productivity.





## C.2 Comparison with Conventional Labor Measures

The estimates above reflect a procedure using regional variation to recover the unit cost of labor. Often, such information is not incorporated into production estimation. Instead, the number of employees or total wage bill are used to capture the effective labor available to a firm. The mean of the second stage estimates using these labor measures are contrasted with unit cost method in Table A.8 (full results in Table A.16 of the Supplemental Appendix). The production coefficients using the total wage bill or total employment are very similar, reflecting the high correlation of these variables. However, both measures mask regional differences in factor markets. Once local substitution patterns are taken into account explicitly, substantial differences emerge.<sup>40</sup> Most notably, the capital share tends to be higher under the approach of this paper, while the labor share is substantially lower.

Table A.	8: Seco	ond Sta	ge Esti	mates vs	Home	ogeneou	ıs Labor	Estim	ates
	Unit	Labor	Cost	Tota	l Wage	Bill	Total	Employ	yment
	$\alpha_L$	$\alpha_K$	$\alpha_M$	$\alpha_L$	$\alpha_K$	$lpha_M$	$\alpha_L$	$\alpha_K$	$\alpha_M$
Average	0.21	0.12	0.53	0.28	0.09	0.56	0.28	0.09	0.58

Pushing this comparison further, Table A.15 predicts the propensity to export of firms by residual firm productivity. The first column shows the results under the unit cost method. The second and third columns show the results when labor is measured as perfectly substitutable (either by employment of each type or wages). Note that in all cases, regional and industry effects are controlled for. The Table illustrates that productivity estimates which account for regional factor markets are almost twice as important in predicting exports as the other measures. Section F.2 of the Appendix shows that similar results hold when examining sales growth and three year survival rate: productivity under the unit cost approach is more important in predicting firm performance, suggesting the other measures conflate the role of advantageous factor markets with productivity.

Table A.9:	Explaining	Propensity t	to Export with	Productivity

Exp	ort Dummy (2	2005)
0.0260***		
(0.00430)		
	0.0140***	
	(0.00248)	
		0.0177***
		(0.00262)
Yes	Yes	Yes
127,082	127,082	127,082
0.204	0.204	0.204
	0.0260*** (0.00430) Yes 127,082	(0.00430) 0.0140*** (0.00248) Yes Yes 127,082 127,082

<sup>&</sup>lt;sup>40</sup>The residuals remaining after the second estimation step, which are often interpreted as idiosyncratic firm productivity, are compared in Appendix C.1.

## **D** Supplemental Derivations

#### D.1 Derivation of Region-Techonology Budget Shares

The expressions which fix the cutoff cost draw  $\overline{\eta}_R^T$  and mass of entry  $\mathbb{M}_R^T$  can be neatly summarized by defining the mass of entrants who produce,  $\widetilde{\mathbb{M}}_R^T$ , and the (locally weighted) average cost draw in each region,  $\widetilde{\eta}_R^T$ :

$$\widetilde{\mathbb{M}}_{R}^{T} \equiv \mathbb{M}_{R}^{T} G\left(\overline{\eta}_{R}^{T}\right), \qquad \widetilde{\eta}_{R}^{T} \equiv \int_{0}^{\overline{\eta}_{R}^{T}} \left(\eta_{z}^{T} u_{R}^{T} \left(U_{R}^{T}\right)^{1/\rho}\right)^{\rho/(\rho-1)} dG(z) / G\left(\overline{\eta}_{R}^{T}\right)$$

Using the profit maximizing price  $P_{Rj}^T$  and combining Equations (2.13), (3.2) and (3.1) then yields the equilibrium quantity produced,

$$Q_{Rj}^{T} = \rho I_{\text{Agg}} \left( u_{R}^{T} \eta_{j} \left( U_{R}^{T} / \sigma_{R}^{T} \right)^{1/\rho} \right)^{\rho/(\rho-1)} / u_{R}^{T} \eta_{j} \sum_{t,r} \left( \sigma_{r}^{t} \right)^{1/(1-\rho)} \widetilde{\mathbb{M}}_{r}^{t} \widetilde{\eta}_{r}^{t}.$$
(D.1)

Aggregating revenues using Equation (D.1) shows that each consumer's budget share allocated to region R and industry T is

Consumer Budget Share for R, T: 
$$(\sigma_R^T)^{1/(1-\rho)} \widetilde{\mathbb{M}}_R^T \widetilde{\eta}_R^T / \sum_{t,r} (\sigma_r^t)^{1/(1-\rho)} \widetilde{\mathbb{M}}_r^t \widetilde{\eta}_r^t.$$
 (D.2)

Consequently, since free entry implies expected profits must equal expected fixed costs, the mass of entrants  $\mathbb{M}_R^T$  solves the implicit form<sup>41</sup>

$$(1-\rho)I_{\text{Agg}}\left(\left(\sigma_{R}^{T}\right)^{1/(1-\rho)}\widetilde{\mathbb{M}}_{R}^{T}\widetilde{\eta}_{R}^{T}/\sum_{t,r}\left(\sigma_{r}^{t}\right)^{1/(1-\rho)}\widetilde{\mathbb{M}}_{r}^{t}\widetilde{\eta}_{r}^{t}\right) = \mathbb{M}_{R}^{T}u_{R}^{T}\left(f_{e}G\left(\overline{\eta}_{R}^{T}\right) + F_{e}\right), \quad (D.3)$$

while the equilibrium cost cutoffs  $\overline{\eta}_R^T$  solve the zero profit condition<sup>42</sup>

$$(1-\rho)I_{\text{Agg}}\left(\sigma_{R}^{T}\right)^{1/(1-\rho)}\left(u_{R}^{T}\overline{\eta}_{R}^{T}\left(U_{R}^{T}\right)^{1/\rho}\right)^{\rho/(\rho-1)} = u_{R}^{T}f_{e}\sum_{t,r}\left(\sigma_{r}^{t}\right)^{1/(1-\rho)}\widetilde{\mathbb{M}}_{r}^{t}\widetilde{\eta}_{r}^{t}.$$
 (D.4)

 $\frac{1}{4^{1}\text{To see a solution exists, note that for fixed prices, } \{\widetilde{\eta}_{R}^{T}\}, \text{ and } \{\overline{\eta}_{R}^{T}\}, \text{ necessarily } \mathbb{M}_{R}^{T} \in A_{R}^{T} \equiv [0,(1-\rho)I_{\text{Agg}}/u_{R}^{T}F_{e}]. \text{ Existence follows from the Brouwer fixed point theorem on the domain } \times_{R,T}A_{R}^{T} \text{ for } H\left(\{\widetilde{\mathbb{M}}_{R}^{T}\}\right) \equiv (1-\rho)I_{\text{Agg}}\left((\sigma_{R}^{T})^{1/(1-\rho)}\widetilde{\mathbb{M}}_{R}^{T}\widetilde{\eta}_{R}^{T}/\sum_{t,r}(\sigma_{r}^{t})^{1/(1-\rho)}\widetilde{\mathbb{M}}_{r}^{T}\widetilde{\eta}_{r}^{t}\right)/u_{R}^{T}\left(f_{e}G\left(\overline{\eta}_{R}^{T}\right)+F_{e}\right).$ 

<sup>&</sup>lt;sup>42</sup>To see a solution exists, note that for fixed prices,  $\{\mathbb{M}_{R'}^{T'}\}\$  and  $\{U_R^T\}\$ , the LHS ranges from 0 to  $\infty$  as  $\overline{\eta}_R^T$  varies, while the RHS is bounded away from 0 and  $\infty$  when min  $\{\widetilde{\eta}_r^t G(\overline{\eta}_r^t)\} > 0$ .  $\widetilde{\eta}_R^T G(\overline{\eta}_R^T) > 0$  follows from inada type conditions on goods from each T and R.

Equations (D.3) and (D.4) fix  $\overline{\eta}_R^T$  since combining them shows

$$\int_0^{\overline{\eta}_R^T} \left( \eta_z^T / \overline{\eta}_R^T \right)^{\rho/(\rho-1)} dG(z) / G\left(\overline{\eta}_R^T\right) = 1 + F_e / f_e G\left(\overline{\eta}_R^T\right).$$

In particular,  $\overline{\eta}_R^T$  does not vary by region or technology. Thus, Equation (D.4) shows that

$$U_R^T u_R^T / \sigma_R^T = \left[ (1-\rho) I_{\text{Agg}} / f_e \sum_{t,r} \left( \sigma_r^t \right)^{1/(1-\rho)} \widetilde{\mathbb{M}}_r^t \widetilde{\eta}_r^t \right]^{1-\rho} / \left( \overline{\eta}_R^T \right)^{\rho}.$$
(D.5)

where the RHS does not vary by region or technology. Combining this equation with (3.1) shows  $Q_{Rj}^T = Q_{R'j}^{T'}$  for all (T,R) and (T',R'), so that  $\mathbb{M}_R^T u_R^T / \sigma_R^T = \mathbb{M}_{R'}^{T'} u_{R'}^{T'} / \sigma_{R'}^{T'}$ . At the same time, using Equation (D.5) reduces (D.2) to

Consumer Budget Share for R, T: 
$$\mathbb{M}_{R}^{T}u_{R}^{T}/\sum_{t,r}\mathbb{M}_{r}^{t}u_{r}^{t} = \sigma_{R}^{T}/\sum_{t,r}\sigma_{r}^{t} = \sigma_{R}^{T}$$

Since  $\sum_{t,r} \sigma_r^t = 1$ , each region and industry receive a share  $\sigma_R^T$  of consumer expenditure.

#### **D.2** Regional Variation in Input Use

Equation (4.1) specifies the relative shares of each type of worker hired. Since input markets are competitive, firms and workers take regional labor market characteristics as given. As characteristics such as wages worker availability and human capital vary, the share of each labor type hired differs across regions. These differences can be broken up into direct and indirect effects. Direct effects ignore substitution by holding the unit labor cost  $\tilde{c}_{RT}$  constant, while indirect effects measure how regional differences give rise to substitution. The direct effects are easy to read off of Equation (4.1), showing:

Direct Effects: 
$$d \ln s_{R,T,i}/d \ln w_{R,i}|_{\tilde{c}_{RT} \text{ constant}} = -k/\beta^T < 0,$$
 (D.6)

$$d\ln s_{R,T,i}/d\ln a_{R,i}|_{\widetilde{c}_{RT} \text{ constant}} = \theta^T/\beta^T > 0, \qquad (D.7)$$

$$d\ln s_{R,T,i}/d\ln \underline{m}_{i}^{T}\big|_{\widetilde{c}_{RT} \text{ constant}} = k\theta^{T}/\beta^{T} > 0.$$
 (D.8)

These direct effects have the obvious signs: higher wages  $(w_{R,i} \uparrow)$  discourage hiring a particular type while greater availability  $(a_{R,i} \uparrow)$  and higher human capital  $(m_{T,i} \uparrow)$  encourage hiring that type.

The indirect effects of substitution through  $\tilde{c}_{RT}$  are less obvious as seen by

$$d\ln \tilde{c}_{RT}^{k}/d\ln w_{R,i} = \left(k/\theta^{T}\right) \left[a_{R,i}\left(\underline{m}_{i}^{T}\right)^{k} w_{R,i}^{1-k-\beta^{T}/\theta^{T}}\right]^{\theta^{T}/\beta^{T}} \tilde{c}_{RT}^{k\left(\theta^{T}/\beta^{T}\right)} > 0, \tag{D.9}$$

$$d\ln \tilde{c}_{RT}^{k}/d\ln a_{R,i} = -\left[a_{R,i}\left(\underline{m}_{i}^{T}\right)^{k} w_{R,i}^{1-k-\beta^{T}}/\theta^{T}\right]^{\theta^{T}/\beta^{T}} \tilde{c}_{RT}^{k\left(\theta^{T}/\beta^{T}\right)} \qquad <0, \tag{D.10}$$

$$d\ln \tilde{c}_{RT}^{k}/d\ln \underline{m}_{i}^{T} = -k \left[ a_{R,i} \left( \underline{m}_{i}^{T} \right)^{k} w_{R,i}^{1-k-\beta^{T}/\theta^{T}} \right]^{\theta^{T}/\beta^{T}} \tilde{c}_{RT}^{k\left( \theta^{T}/\beta^{T} \right)} \qquad < 0.$$
(D.11)

Thus, the indirect effects counteract the direct effects through substitution. To see the total of the direct and indirect effects, define the Type-Region-Technology coefficients  $\chi_{i,R,T}$ :

$$\chi_{i,R,T} \equiv 1 - \left[a_{R,i}\left(\underline{m}_{i}^{T}\right)^{k} w_{R,i}^{1-k-\beta^{T}/\theta^{T}}\right]^{\theta^{T}/\beta^{T}} \widetilde{c}_{RT}^{k\left(\theta^{T}/\beta^{T}\right)}.$$

Investigation shows that each  $\chi_{i,R,T}$  is between zero and one. Combining Equations (D.6-D.8) and Equations (D.9-D.11) shows that the direct effect dominates since

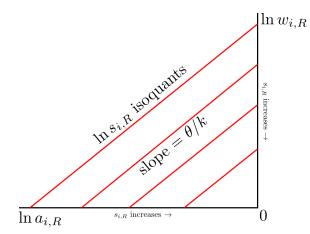
Total Effects: 
$$d \ln s_{R,T,i}/d \ln w_{R,i} = \left[-k/\beta^T\right] \chi_{i,R,T} < 0,$$
 (D.12)

$$d\ln s_{R,T,i}/d\ln a_{R,i} = \left[\theta^T/\beta^T\right]\chi_{i,R,T} > 0, \qquad (D.13)$$

$$d\ln s_{R,T,i}/d\ln \underline{m}_{i}^{T} = \left[k\theta^{T}/\beta^{T}\right]\chi_{i,R,T} > 0.$$
 (D.14)

Equations (D.12-D.14) summarize the relationship between regions and labor market characteristics. For small changes in labor market characteristics, the log share of a type hired in linear in log characteristics with a slope determined by model parameters and a regional shifter  $\chi_{i,R,T}$ . These (local) isoquants for the share of type *i* workers hired in region *R* are depicted in Figure A.1.

Figure A.1: Local isoquants for Share of Workers Hired



## **D.3** Regional Variation in Theory: Isoquants

Equations (D.12-D.14) also characterize local isoquants of hiring the same share of a type across regions. It is immediate that for small changes in market characteristics,  $(\Delta_w, \Delta_a, \Delta_m)$ , the share of a type hired is constant so long as

$$-\left(k/\theta^{T}\right)\Delta_{w}/w_{R,i}+\Delta_{a}/a_{R,i}+k\Delta_{m}/\underline{m}_{i}^{T}=0.$$

For instance, firms in regions *R* and *R'* will hire the same fraction of type *i* workers for small differences in characteristics  $(\Delta_w, \Delta_a)$  so long as

$$\Delta_w / \Delta_a = \left( \theta^T / k \right) w_{R,i} / a_{R,i}. \tag{D.15}$$

By itself, an increase in type *i* wages  $\Delta_w$  would cause firms to hire a lower share of type *i* workers as indicated by the direct effect. However, Equation (D.15) shows that firms would keep the same share of type *i* workers if the availability  $\Delta_a$  increases concurrently so that Equation (D.15) holds.

### **D.4** Derivation of Unit Labor Costs

Unit labor costs by definition solve

Unit Labor Costs: 
$$c_R^T \equiv \min_H C_T \left( H | a_R, w_R \right)$$
 subject to  $L = \left( H_1^{\theta^T} + H_2^{\theta^T} + \ldots + H_{\mathbb{S}}^{\theta^T} \right)^{1/\theta^T} = 1.$ 

Under the parameterization  $\Psi(h) = 1 - h^{-k}$ , Equations (2.1) become

$$H_i = a_{R,i}k/(k-1) \cdot \underline{m}_i^T \underline{h}_i^{1-k} \cdot N.$$
 (D.16)

From the FOCs above,  $w_{R,i}H_i/\underline{m}_i^T\underline{h}_iC_T(H|a_R,w_R) = H_i^{\theta^T}/\sum_j H_j^{\theta^T}$ , and  $L = 1 = \left(\sum_j H_j^{\theta^T}\right)^{1/\theta^T}$  so

$$\underline{h}_{i} = w_{R,i} H_{i}^{1-\theta^{T}} / \underline{m}_{i}^{T} C_{T} \left( H | a_{R}, w_{R} \right).$$
(D.17)

Substitution now yields

$$H_i = a_{R,i}k/(k-1) \cdot \underline{m}_i^T \left( w_{R,i}H_i^{1-\theta^T}/\underline{m}_i^T C_T \left( H|a_R, w_R \right) \right)^{1-k} \cdot N.$$
(D.18)

Further reduction and the definition of  $\beta^T$  shows that

$$H_{i}^{\beta^{T}} = H_{i}^{\theta^{T}+k-k\theta^{T}} = a_{R,i}k/(k-1) \cdot \left(\underline{m}_{i}^{T}\right)^{k} w_{R,i}^{1-k} C_{T} \left(H|a_{R},w_{R}\right)^{k-1} N.$$
(D.19)

Again using  $\left(\sum_{j} H_{j}^{\theta^{T}}\right)^{1/\theta^{T}} = 1$  then shows

$$1 = \sum_{i} \left[ a_{R,i}k/(k-1) \cdot \underline{m}_{i}^{Tk} w_{R,i}^{1-k} \left(c_{R}^{T}\right)^{k-1} N \right]^{\theta^{T}/\beta^{T}}.$$
 (D.20)

From the definition of the cost function we have (substituting in D.17)

$$c_{R}^{T} = N\left[\sum_{i} a_{R,i} w_{R,i} \underline{h}_{i}^{-k} + f c_{R}^{T}\right] = \sum_{i} w_{R,i} \left(\left(k-1\right)/k\right) H_{i}/\underline{m}_{i}^{T} \underline{h}_{i} + N f c_{R}^{T}.$$

Therefore from  $w_{R,i}H_i/\underline{m}_i^T\underline{h}_iC_T(H|a_R,w_R) = H_i^{\theta^T}$  it follows

$$1 = \sum_{i} (k-1) / k \cdot H_{i}^{\theta^{T}} + Nf = (k-1) / k + Nf,$$

and therefore N = 1/fk. Now from Equation (D.20),  $c_R^T$  is seen to be Equation (2.7).

### **D.5** Derivation of Employment Shares

Combining Equations (D.17), (D.19) and N = 1/fk shows

$$\underline{h}_{i} = a_{R,i}^{\left(1-\theta^{T}\right)/\beta^{T}} \left(\underline{m}_{i}^{T}\right)^{-\theta^{T}/\beta^{T}} w_{R,i}^{1/\beta^{T}} \left(c_{R}^{T}\right)^{-1/\beta^{T}} / \left(f\left(k-1\right)\right)^{\left(1-\theta^{T}\right)/\beta^{T}}.$$
(D.21)

Let  $A_{R,i}^T$  be the number of type *i* workers hired to make L = 1, exclusive of fixed search costs. By definition,  $A_{R,i}^T = N|_{L=1} \cdot a_{R,i} (1 - \Psi(\underline{h}_i)) = a_{R,i} \underline{h}_i^{-k} / fk$ . Using Equation (D.21),

$$A_{R,i}^{T} = k^{-1} (k-1) a_{R,i}^{\theta^{T}/\beta^{T}} (\underline{m}_{i}^{T})^{k\theta^{T}/\beta^{T}} w_{R,i}^{-k/\beta^{T}} (c_{R}^{T})^{k/\beta^{T}} ((k-1)f)^{-\theta^{T}/\beta^{T}}.$$

Labor is also consumed by the fixed search costs which consist of  $N|_{L=1} \cdot f = 1/k$  labor units. Therefore, if  $\widetilde{A}_{R,i}^T$  denotes the total number of type *i* workers hired to make L = 1, necessarily  $\widetilde{A}_{R,i}^T = A_{R,i}^T + \widetilde{A}_{R,i}^T/k$  so  $\widetilde{A}_{R,i}^T = k(k-1)^{-1}A_{R,i}^T$ , and the total number of type *i* workers hired in region *R* using technology *T* is  $L_R^T \widetilde{A}_{R,i}^T$ . The total number of employees in *R*, *T* is  $\sum_i L_R^T \widetilde{A}_{R,i}^T = L_R^T (c_R^T)^{k/\beta^T} (\widetilde{c}_R^T)^{(1-k)\theta^T/\beta^T}$ , where  $\widetilde{c}_R^T$  denotes the unit labor cost function at wages  $\left\{ w_{R,i}^{k/(k-1)\theta^T} \right\}^{43}$ .

<sup>43</sup>Formally  $\tilde{c}_R^T \equiv \min_H C_T \left( H | a_R, \left\{ w_{R,i}^{-k/\theta^T (1-k)} \right\} \right)$  subject to L = 1.

# **D.6 Derivation of Indirect Utility**

First, note that within an industry *T* and region *R*, the quantity a firm *j* produces relative to quantity  $\overline{Q}_R^T$  that the highest cost firm produces is  $Q_{Rj}^T/Q_{Rj}^T = (\overline{\eta}_R^T/\eta_j)^{1/(1-\rho)}$ . From the condition that the highest cost firm makes zero profits,  $\overline{Q}_R^T = \rho f_e/(1-\rho) \overline{\eta}_R^T$ , and consequently

$$Q_{Rj}^{T} = \rho f_{e} \left(\overline{\eta}_{R}^{T}\right)^{\rho/(1-\rho)} / (1-\rho) \left(\eta_{j}\right)^{1/(1-\rho)}.$$

Since the share of income spent on industry T and region R,  $\sigma_R^T I_{Agg}$ , must equal total costs,

$$\sigma_{R}^{T}I_{\text{Agg}} = u_{R}^{T}\mathbb{M}_{R}^{T}\left[\int_{0}^{\overline{\eta}_{R}^{T}}\rho f_{e}\left(\overline{\eta}_{R}^{T}\right)^{\rho/(1-\rho)}/(1-\rho)\left(\eta_{j}\right)^{1/(1-\rho)} + f_{e}dG(j) + F_{e}\right]$$

Free entry and constant markups also implies that entry costs  $u_R^T F_e$  must equal expected profits, so

$$u_{R}^{T}\left[\int_{0}^{\overline{\eta}_{R}^{T}}f_{e}\left(\overline{\eta}_{R}^{T}\right)^{\rho/(1-\rho)}/\left(\eta_{j}\right)^{1/(1-\rho)}-f_{e}dG(j)\right]=u_{R}^{T}F_{e}.$$

Combining these expressions shows

$$\mathbb{M}_{R}^{T} = \sigma_{R}^{T} I_{\text{Agg}} / u_{R}^{T} \left[ \int_{0}^{\overline{\eta}_{R}^{T}} f_{e} \left( \overline{\eta}_{R}^{T} \right)^{\rho/(1-\rho)} / (1-\rho) \left( \eta_{j} \right)^{1/(1-\rho)} dG(j) \right].$$

Finally, expanding the expression for welfare and using  $\sum_{T,R} \sigma_R^T = 1$ , we have

$$W = \Pi_{T} \Pi_{R} \left( \mathbb{M}_{R}^{T} \right)^{\sigma_{R}^{T}} \left( \int_{0}^{\overline{\eta}_{R}^{T}} \left( Q_{Rj}^{T} \right)^{\rho} dG(j) \right)^{\sigma_{R}^{T}}$$
  
=  $\rho^{\rho} (1-\rho)^{1-\rho} f_{e}^{\rho-1} \left( \overline{\eta}_{1}^{1} \right)^{-\rho} \left( \frac{\int_{0}^{\overline{\eta}_{1}^{1}} (\eta_{j})^{\rho/(\rho-1)} dG(j)}{\int_{0}^{\overline{\eta}_{1}^{1}} (\eta_{j})^{1/(\rho-1)} dG(j)} \right) \cdot I_{\text{Agg}} \cdot \Pi_{T} \Pi_{R} \left( \frac{\sigma_{R}^{T}}{u_{R}^{T}} \right)^{\sigma_{R}^{T}}.$ 

Note that since  $\overline{\eta}_R^T$  depends only of  $f_e, F_e$  and G, only the term  $I_{\text{Agg}} \cdot \Pi_T \Pi_R \left(\sigma_R^T / u_R^T\right)^{\sigma_R^T}$  can vary with regional endowments.

#### **D.7** Limited Factor Price Equalization

Since workers are imperfectly substitutable, they induce spillovers within firms, and consequently are not paid their marginal product.<sup>44</sup> Mirroring this, the equation for unit labor costs shows that regions with different skill distributions, say region *R* and *R'*, typically cannot have both  $c_R^T = c_{R'}^T$  and  $w_R = w_{R'}$ . However, factor price equalization for labor holds in a limited fashion. Summing across types in (3.8) implies

Average Wages : 
$$\sum_{i} a_{R,i} w_{R,i} = \sum_{T} \alpha_L^T \sigma^T I_{Agg},$$

so average wages are constant across regions. This is summarized as

#### **Proposition 4.** Average wages are equalized across regions.

Proposition 4 shows that while the model allows for heterogeneity of wages by worker type, general equilibrium forces still imply that factor price equalization holds *on average*. As is well known, this prediction will rarely hold in any real world setting, but can be understood in terms of factor augmenting technology differences (e.g. Trefler (1993)).

# **E** Supplemental Summary Statistics

## E.1 Educational Summary Statistics

UNICEF suggests that the typical Chinese primary school entrance age is 7 (Source: childinfo.org). Compulsory education lasts nine years (primary and secondary school) and ends around age sixteen. Figure A.1a illustrates the average years of schooling for the Chinese labor force, while Table A.10 displays the frequency of each worker type and their average monthly wages by Province.

<sup>&</sup>lt;sup>44</sup>Such spillovers are internalized by firms in the model. The extent to which spillovers might also occur across industries is beyond the scope of this study, however see Moretti (2004) for evidence in the US context.

# Figure A.1: Chinese Educational Attainment (2005)

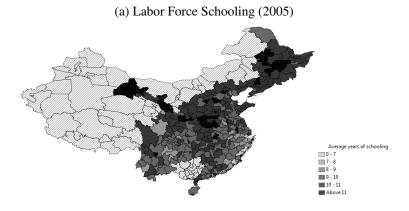


Table A.10: Educational and Wage Distribution by Province (2005)

Province	Fraction o	f Labor For	ce by Ec	lucation	Avg Monthly Wage by Education						
	≤Junior HS	$\leq$ Junior HS	Senior	College	$\leq$ Junior HS	$\leq$ Junior HS	Senior	College			
	(Female)	(Male)	HS	or Above	(Female)	(Male)	HS	or Above			
Anhui	0.296	0.485	0.155	0.063	581	862	866	1210			
Beijing	0.140	0.284	0.299	0.277	796	1059	1314	2866			
Chongqing	0.272	0.408	0.227	0.093	582	820	872	1379			
Fujian	0.348	0.453	0.146	0.052	695	942	1103	1855			
Gansu	0.216	0.399	0.271	0.114	507	738	869	1135			
Guangdong	0.327	0.362	0.231	0.080	748	967	1281	2719			
Guizhou	0.292	0.478	0.162	0.069	572	758	925	1189			
Hainan	0.328	0.334	0.259	0.080	532	694	894	1527			
Hebei	0.230	0.515	0.190	0.066	515	793	832	1233			
Heilongjiang	0.217	0.393	0.285	0.104	515	740	797	1096			
Henan	0.229	0.428	0.234	0.109	487	675	714	1079			
Hubei	0.271	0.384	0.264	0.081	541	757	809	1262			
Hunan	0.263	0.444	0.229	0.063	634	828	889	1267			
Jiangsu	0.314	0.400	0.210	0.076	758	994	1086	1773			
Jiangxi	0.291	0.456	0.196	0.056	525	783	794	1240			
Jilin	0.204	0.382	0.307	0.107	522	745	809	1163			
Liaoning	0.250	0.410	0.219	0.120	576	822	848	1366			
Shaanxi	0.203	0.406	0.277	0.114	497	731	805	1149			
Shandong	0.288	0.441	0.203	0.068	602	823	863	1398			
Shanghai	0.221	0.321	0.272	0.186	891	1155	1450	3085			
Shanxi	0.169	0.520	0.221	0.089	502	872	857	1113			
Sichuan	0.277	0.480	0.162	0.081	541	737	829	1477			
Tianjin	0.258	0.321	0.285	0.136	995	1019	1074	1617			
Yunnan	0.275	0.495	0.160	0.070	504	697	896	1542			
Zhejiang	0.357	0.469	0.129	0.045	817	1097	1299	2333			

# E.2 Provincial Summary Statistics

			Dopulation Consus								
		acturing		Population Cens							
	Firm	Avg	# of	# Region-	Monthly	Avg Yrs					
Province	Count	Workers	Regions	Industries	Wage	School					
Anhui	2,070	199.3	17	822	832	8.925					
Beijing	2,976	137.3	2	128	1665	11.542					
Chongqing	967	261.8	3	184	862	9.606					
Fujian	6,314	206.5	9	504	945	8.170					
Gansu	439	259.3	14	658	805	9.728					
Guangdong	19,108	278.1	21	1269	1137	9.607					
Guizhou	722	207.0	9	464	805	8.565					
Hainan	86	162.6	3	151	830	9.772					
Hebei	4,576	229.2	11	623	781	9.527					
Heilongjiang	837	258.3	13	622	774	10.197					
Henan	5,301	224.4	17	798	720	10.053					
Hubei	2,266	236.3	14	742	789	9.731					
Hunan	3,200	188.4	14	751	843	9.588					
Jiangsu	20,028	168.5	13	756	1013	9.431					
Jiangxi	1,363	237.3	11	556	766	9.208					
Jilin	677	268.7	9	477	796	10.340					
Liaoning	4,570	161.6	14	770	865	10.152					
Shaanxi	1,070	318.5	10	548	787	10.068					
Shandong	11,374	211.2	17	947	825	9.596					
Shanghai	8,521	145.6	2	119	1577	10.569					
Shanxi	1,056	375.5	11	619	847	9.895					
Sichuan	2,858	234.0	21	887	800	9.149					
Tianjin	2,236	186.1	2	128	1119	10.243					
Yunnan	659	233.5	16	695	794	8.675					
Zhejiang	23,965	143.3	11	629	1098	8.201					

Table A.11: Descriptive Statistics by Province (2005)

# E.3 Industrial Summary Statistics

Table A.12 presents the distribution of firms by industry and other descriptive statistics.

						Share of		
	# of	# of	Avg # of		White		State	Foreign
Industry	firms	Regions	workers	Female	Collar	Export	Equity	Equity
Beverage	2,225	155	219.20	0.281	0.114	0.150	0.107	0.121
Electrical	12,241	166	201.58	0.289	0.106	0.351	0.030	0.195
Food	3,807	171	193.98	0.321	0.091	0.266	0.060	0.202
General Machines	15,727	195	152.68	0.205	0.117	0.262	0.047	0.115
Iron & Steel	4,676	160	227.40	0.148	0.088	0.101	0.032	0.056
Leather & Fur	4,852	89	320.70	0.362	0.036	0.682	0.005	0.335
Precision Tools	2,702	68	214.89	0.296	0.180	0.457	0.063	0.299
Metal Products	10,686	157	146.93	0.233	0.086	0.332	0.028	0.161
Non-ferrous Metal	3,607	139	157.75	0.186	0.093	0.180	0.035	0.093
Non-metal Products	15,347	259	195.57	0.207	0.090	0.169	0.059	0.088
Paper	5,698	159	151.05	0.269	0.061	0.127	0.026	0.131
Plastic	9,235	159	140.47	0.298	0.065	0.327	0.019	0.235
PC & AV	6,699	90	402.04	0.342	0.120	0.571	0.038	0.459
Specific Machines	7,816	167	176.76	0.197	0.154	0.244	0.072	0.166
Textile	18,292	186	222.43	0.390	0.044	0.406	0.018	0.168
Wood	3,629	133	137.04	0.288	0.050	0.290	0.025	0.137

Table A.12: Manufacturing Survey Descriptive Statistics (2005)

# **F** Supplemental Empirical Results

## F.1 Verisimilitude of Census and Firm Wages

One of the main concerns about combining census data with manufacturing data is the representativeness of regional labor market conditions in determining actual wages within firms. It turns out they are remarkably good predictors of a firm's labor expenses. We construct a predictor of firm wages based on Census data and test it as follows: First, compute the average wages per prefecture. Second, make an estimate CensusWage by multiplying each firm's distribution of workers by the average wages of each type from the population census. Third, regress actual firm wages on CensusWage. The results are presented in Table A.13 of Appendix F.1. Not only is the  $R^2$  of this predictor very high for each industry, but the coefficient on CensusWage is close to one in all cases, showing that one-for-one the census based averages are excellent at explaining the variation in the wage bill across firms.

Industry	D	ependent Va	ariable: ln (Fi	rm Wage)		
	ln (Census Wage)	Std Dev	Constant	Std Dev	Obs	$R^2$
Beverage	1.052***	(0.0147)	-0.904***	(0.204)	2223	0.85
Electrical	1.018***	(0.0103)	-0.370***	(0.138)	12213	0.86
Food	1.032***	(0.0104)	-0.602***	(0.144)	3766	0.83
General Machines	1.020***	(0.0063)	-0.365***	(0.091)	15711	0.84
Iron & Steel	1.049***	(0.0082)	-0.777***	(0.116)	4663	0.87
Leather & Fur	0.982***	(0.0112)	0.116	(0.165)	4851	0.87
Precision Tools	1.018***	(0.0221)	-0.332	(0.308)	2689	0.83
Metal Products	1.012***	(0.0094)	-0.286**	(0.130)	10654	0.83
Non-ferrous Metal	1.054***	(0.0092)	-0.833***	(0.127)	3588	0.88
Non-metal Products	0.981***	(0.0085)	0.16	(0.122)	15329	0.80
Paper	1.012***	(0.0086)	-0.335***	(0.120)	5695	0.82
Plastic	1.015***	(0.0129)	-0.340**	(0.170)	9214	0.85
PC & AV	1.021***	(0.0172)	-0.354	(0.224)	6685	0.86
Specific Machines	1.036***	(0.0105)	-0.580***	(0.139)	7780	0.83
Textile	0.981***	(0.0060)	0.132	(0.084)	18281	0.86
Wood	0.965***	(0.0136)	0.309	(0.197)	3619	0.78

Table A.13: Census Wages as a Predictor of Reported Firm Wages

Standard errors in parentheses. Significance: \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

# F.2 Firm Performance Characteristics and Productivity

	Sales Growth Rate (2005-7)						
Productivity under Unit Cost method	-0.0924**						
	(0.0419)						
Productivity under $L = 4$ Types		-0.0648**					
		(0.0264)					
Productivity under L = Wage Bill			-0.0641**				
			(0.0285)				
Prefecture and Industry FE	Yes	Yes	Yes				
Observations	107,143	107,143	107,143				
R-squared	0.027	0.027	0.027				

Table A.14: Explaining Growth with Productivity

Standard errors in parentheses. Significance: \*\*\* p<.01, \*\* p<.05, \* p<.1.

	Survival Rate (2005-7)							
Productivity under Unit Cost method	0.0184***							
	(0.00248)							
Productivity under $L = 4$ Types		0.0109***						
		(0.00165)						
Productivity under L = Wage Bill			0.00968***					
			(0.00165)					
Prefecture and Industry FE	Yes	Yes	Yes					
Observations	127,082	127,082	127,082					
R-squared	0.023	0.022	0.022					

## Table A.15: Explaining Survival with Productivity

Standard errors in parentheses. Significance: \*\*\* p<.01, \*\* p<.05, \* p<.1.

# F.3 Production Estimates by Method

Table A.16 compares the production coefficients under three measures of labor: unit labor costs, total wages, and employment of each worker type. In the latter case, the coefficient for type *i* workers are labeled  $\alpha_I^i$ .

	Unit	Labor	Cost	Tota	al Wag	e Bill		Employment of Each Type						
Industry	$\alpha_L$	$\alpha_K$	$\alpha_M$	$\alpha_L$	$\alpha_K$	$\alpha_M$		$\alpha_L^1$	$\alpha_L^2$	$\alpha_L^3$	$\alpha_L^4$	$\alpha_K$	$\alpha_M$	
Beverage	.13	.10	.70	.23	.06	.71		.07	.01	.07	.06	.07	.75	
Electrical	.25	.14	.47	.34	.12	.47		.06	.02	.08	.12	.12	.53	
Food	.14	.09	.70	.16	.06	.73		.07	.03	.09	.08	.12	.52	
General Machines	.17	.12	.60	.25	.09	.61		.03	.01	.09	.03	.06	.76	
Iron & Steel	.40	.07	.48	.25	.07	.68		.04	.03	.06	.08	.10	.66	
Leather & Fur	.10	.13	.59	.27	.09	.55		.01	.07	.11	.05	.06	.71	
Precision Tools	.20	.16	.43	.44	.08	.38		.02	.13	.07	.05	.09	.57	
Metal Products	.24	.14	.46	.30	.12	.48		.09	.03	.05	.23	.11	.44	
Non-ferrous Metal	.40	.08	.43	.17	.10	.65		.03	.04	.06	.02	.06	.71	
Non-metal Products	.20	.07	.61	.20	.06	.67		.04	.04	.10	.07	.11	.55	
Paper	.18	.14	.53	.28	.11	.52	-	.09	.02	.10	.08	.14	.47	
Plastic	.27	.14	.41	.31	.13	.43		.04	.01	.08	.06	.09	.65	
PC & AV	.16	.21	.43	.48	.14	.35	-	.11	.07	.08	.24	.16	.41	
Specific Machines	.10	.16	.55	.31	.10	.48		.03	.01	.06	.13	.11	.53	
Textile	.12	.11	.61	.29	.07	.56		.03	.09	.08	.08	.06	.58	
Wood	.22	.10	.56	.23	.08	.62		.03	.07	.07	.08	.07	.63	

Table A.16: Second Stage Estimates vs Homogeneous Labor Estimates