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Have Euro Area Government Bond Risk Premia Converged To Their Common State?

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Have euro area government bond risk premia converged to their common state ?*

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Abstract

We derive a model in which a standard international capital asset pricing model (ICAPM) is nested within an ICAPM with market imperfections. In the latter model an idiosyncratic stochastic factor affects the return of risky government bonds (over a risk-free rate) on top of the systematic component that is common to all countries (and that is interacted with a time-varying idiosyncratic "beta"). We introduce asymptotic convergence from the full ICAPM with imperfections to the standard model by multiplying the idiosyncratic factor by convergence operators. The model is then estimated using weekly government bond returns for Belgium, France, Italy, Germany, and the Netherlands over the period 1995-2006. We find that the idiosyncratic components have converged towards zero for all countries over the sample period. By the end of the sample period the government bond markets considered are almost fully efficient, with the exception of Italy.

JEL Classifications: E43, G12

Keywords: Government bonds, euro area, risk premia, state space methods

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1 Introduction.

This paper investigates the integration of the government bond markets in five euro area countries (Belgium, France, Italy, Germany, and the Netherlands) during the period 1995-2006. The existing literature suggests that the correlation of government bond returns between different (euro area) countries has increased in recent years: government bond returns seem to be driven less by country-specific or local idiosyncratic factors and more by common international factors.

Two related strands of the literature investigate the integration of international government bond markets.

The first strand of the literature focuses on the presence of a common international risk factor in international government bond yield differentials, i.e. the spreads between local yields to maturity versus the yields to maturity of some benchmark country (most often Germany). An early contribution that emphasizes the presence of local and global factors in government bond spreads of high yielders like Italy versus Germany is Favero et al. (1997). Codogno et al. (2003) relate US risk factors (corporate and banking risk) to country-specific default risk for a number of countries among which are Belgium, France, Italy, and the Netherlands. They conclude that the impact of international risk factors is higher in countries with a higher government debt. They also find that, for the year 2002, the liquidity component in the bond spreads is not very important. Bernoth et al. (2004) examine yield spreads of EU countries versus Germany and the United States. They conclude that international risk factors captured by US corporate risk affect spreads, but evidence on the interaction of global risk with local fundamentals or liquidity indicators is mixed. Their results do suggest that the introduction of the euro has decreased liquidity premia in euro area government bond spreads. Favero et al. (2007) argue that the changing risk attitude of international investors interacts with liquidity indicators. Dungey et al. (2000) do not use a proxy for international risk but explicitly filter the common factor out of the government bond spreads through the use of factor analysis. They find a common factor in the long-term bond yield differentials of Australia, Japan, Germany, Canada, and the UK versus the US. Geyer et al. (2004) filter out a common component in the bond spreads of Austria, Belgium, Italy, and Spain versus Germany. They find a significant impact of European risk proxies on the common factor and interpret the common factor as a risk premium that reflects the risk of a failure of EMU that could lead to the reintroduction of exchange rate risks.

The second strand of the literature investigates the presence of a common factor in excess bond

returns or bond risk premia (i.e. the realized one-period holding return of a long-term government bond in excess of the return of a one-period bond in the same country). Ilmanen (1995) finds that the excess bond returns of the US, Canada, Japan, Germany, France, and the UK are highly correlated over the period 1978-1993. Cappiello et al. (2003) find a high correlation between the returns of government bonds of different countries and argue that the introduction of the euro has lead to near perfect correlation among bond returns within EMU countries. Barr and Priestley (2004) look at the US, UK, Japan, Germany, and Canada and find that one quarter of excess government bond returns is related to local market risk while the remainder is due to world bond market risk. They find no time variation in the level of integration over the period 1986-1996.

In this paper we add to the second strand of the literature. We investigate whether the country-specific or idiosyncratic components in the excess returns or risk premia of the government bonds of the euro area countries under consideration have converged towards zero. In standard asset pricing models (see e.g. Harvey 1991) such components imply inefficiencies since only systematic common risk should be rewarded. As a result, if the idiosyncratic components have converged towards zero, the excess returns or risk premia have converged towards their common state and the efficiency of the government bond markets under investigation is said to have increased.

The contribution of this paper to the literature is both theoretical and methodological.

Theoretically, we use an international capital asset pricing model (ICAPM) as presented for instance by Harvey (1991) where a representative global investor invests in the bond markets of different countries. Acharya and Pedersen (2005) show that the pricing equations of a CAPM derived in a frictionless economy but expressed in net returns, i.e. returns minus some arbitrary idiosyncratic premium, are equivalent to those derived from a CAPM where frictions are explicitly incorporated. Thus we can allow for impediments and imperfections on the local bond markets simply by rewriting an ICAPM for net returns. The standard ICAPM is then obtained if the idiosyncratic premia equal zero. In the paper we assume that impediments and imperfections in the local bond markets (i.e. market-specific transaction costs and taxation) disappear gradually over time. In particular, the idiosyncratic premia in the returns of government bonds over a risk-free rate converge to zero asymptotically so that, in the limit, the standard asset pricing equations hold. Acharya and Pedersen's equivalence result thus allows us to nest a standard ICAPM into an ICAPM with market imperfections and to assume that the latter gradually converges to the former.

Methodologically, we use a linear state space approach to estimate the latent factor decomposition of the excess returns or risk premia that is implied by the theoretical model. In particular, we use weekly data over the period 1995-2006 to decompose the government bond risk premia of Belgium, France, Germany, Italy, and the Netherlands into a common component and an idiosyncratic component.¹

The country-specific time-varying impacts of the common factor on the bond spreads, the "betas" (i.e. the ratios of the conditional covariance of the common factor and the bond returns over the conditional variance of the common factor), are also estimated. Del Negro and Otrok (2006) provide a Bayesian method to estimate a dynamic factor model with time-varying loadings where the factor loadings are assumed to follow driftless random walks. The approach that we follow, while less general in nature, is better suited for a CAPM since it involves the direct parameterization of the conditional covariances and variances in the "betas". In other words, the time-varying loadings in our approach are not stochastic so that our model still fits into a standard linear state space framework.²

We then investigate whether the idiosyncratic components in the government bond risk premia have converged towards zero by multiplying the idiosyncratic components in the bond risk premia by convergence operators of the type suggested by Luginbuhl and Koopman (2004).

Our results suggest that our ICAPM with market imperfections converges to a standard ICAPM, i.e. the idiosyncratic components in the excess returns converge towards zero for all five countries implying that the efficiency of the euro area government bond markets under consideration has increased. By the end of the sample period the government bond markets considered are almost fully efficient, with the exception of Italy. The results imply a decrease in the relevance of market imperfections like illiquidity (in particular market-specific transaction costs) and taxation in the government bond markets of the euro area. We find that the reduction of the risk premia can be attributed to a decrease in local market imperfections rather than to a decrease in the country-specific exposure to international risk. We do not attribute the decrease in the idiosyncratic components solely to the introduction of the euro on 1/1/1999 because, first, the existing literature argues that convergence most likely is part of a wider global phenomenon (see

¹As such we avoid the use of proxies. The latter are often imperfectly capturing the common state. For instance, US risk proxies may be only a part of the common factor and, as Geyer et al. (2004) suggest, European factors also are part of the story.

²Our approach of dealing with conditional covariances in a state space framework is an extension of the state space models with time-varying conditional variances as studied by Harvey et al. (1992).

e.g. Schulz and Wolff 2008) and, second, our results suggest that, with the exception of Italy, the decrease of the idiosyncratic components starts some time after the introduction of the euro.

The outline of the paper is as follows. Section 2 presents the theoretical model. In section 3 we present the empirical specification and the estimation method. We also discuss data issues. Results from the estimations are reported in section 4, while the final section concludes.

2 The model.

There is a representative international investor who maximizes expected utility by choosing a consumption path over an infinite lifetime. This investor invests in the government bond markets of N different countries (i = 1, ..., N), in a risk-free asset b, and in an international portfolio w. The period t+1 returns of the bonds i ($\forall i$), the risk-free asset b, and the portfolio w are denoted by R_{it+1} ($\forall i$), R_{bt+1} , and R_{wt+1} . The variable α_{it+1} (>0) reflects the cost of impediments and imperfections encountered on the bond market of country i ($\forall i$). In particular, α_{it+1} captures market-specific transaction costs and tax components in bond returns. We assume that $\lim_{t\to+\infty}\alpha_{it+1}=0$, i.e. these costs converge to zero as time passes by. For the risk-free asset b and for the portfolio w we assume that these costs are zero, i.e. $\alpha_{wt+1}=\alpha_{bt+1}=0$.³ The period t+1 utility function for the international investor is denoted by $u(c_{t+1})$ where c_{t+1} is period t+1 real consumption of the investor. The subjective rate of time preference of the investor is captured by the discount factor ρ (with $0 < \rho < 1$). The stochastic discount factor which drives the returns R_{it+1} ($\forall i$) and R_{wt+1} is defined as $m_{t,t+1} \equiv \rho \frac{u'(c_{t+1})}{u'(c_t)}$.

These assumptions lead to the following first-order conditions,

$$E_t \left[m_{t,t+1} (R_{it+1} - \alpha_{it+1}) \right] = 1 \tag{1}$$

$$E_t [m_{t,t+1}] R_{bt+1} = 1 (2)$$

$$E_t \left[m_{t,t+1} R_{wt+1} \right] = 1 \tag{3}$$

where E_t is the expectations operator conditional on the period t information set and where eq.(1) holds $\forall i$. All first-order conditions reflect the fact that, in the optimum, the investor is

³We thus assume that there is no common factor in the liquidity premium. See Acharya and Pedersen (2005) and Favero et al (2007) for evidence on this for respectively the US stock market and euro area bond markets.

indifferent between consuming an amount of 1 at time t or investing this amount into i ($\forall i$), b, or w and consuming $(R_{it+1} - \alpha_{it+1})$, R_{bt+1} , or R_{wt+1} at time t+1. The expected, discounted marginal utility of both decisions is equal. Since $\lim_{t\to+\infty} \alpha_{it+1} = 0$, eq.(1) converges asymptotically to the standard Euler equation. We thus nest a standard CAPM into a CAPM with market imperfections and we assume that the latter gradually converges to the former. This is possible because of Acharya and Pedersen's (2005) equivalence result which shows that the pricing equations of our CAPM derived for a frictionless economy with returns minus some arbitrary idiosyncratic premium α_{it+1} , are equivalent to those derived for a CAPM where frictions are explicitly incorporated.

In appendix A we show that we can write,

$$E_t[R_{it+1}] - R_{bt+1} = E_t[\alpha_{it+1}] + \beta_{it+1}(E_t[R_{wt+1}] - R_{bt+1})$$
(4)

where $\beta_{it+1} = \frac{cov_t[R_{wt+1}, R_{it+1} - \alpha_{it+1}]}{V_t[R_{wt+1}]}$. This equation states that the expected excess return of bond i over the risk-free asset's return depends on the expected costs of market imperfections on market i, on the expected excess return of the international portfolio $(R_{wt+1} - R_{bt+1})$, and on β_{it+1} which reflects the conditional covariance of the country-specific net bond return and the return on the global portfolio.

We rewrite eq.(4) as,

$$\widetilde{R}_{it+1} = \alpha_{it+1} + \beta_{it+1} \widetilde{R}_{wt+1} + \varrho_{it+1} \tag{5}$$

where the " \sim " over a variable denotes excess returns, i.e. $\widetilde{R}_{it+1} = R_{it+1} - R_{bt+1}$ and $\widetilde{R}_{wt+1} = R_{wt+1} - R_{bt+1}$, where $\beta_{it+1} = \frac{cov_t \left[\widetilde{R}_{wt+1}, \widetilde{R}_{it+1} - \alpha_{it+1}\right]}{V_t \left[\widetilde{R}_{wt+1}\right]}$. The error term $\varrho_{it+1} = \left(\widetilde{R}_{it+1} - E_t \left[\widetilde{R}_{it+1}\right]\right) - \left(\alpha_{it+1} - E_t \left[\alpha_{it+1}\right]\right) - \beta_{it+1} \left(\widetilde{R}_{wt+1} - E_t \left[\widetilde{R}_{wt+1}\right]\right)$ where $E_t \left[\varrho_{it+1}\right] = 0$. It is straightforward to show that $cov_t \left(\widetilde{R}_{wt+1}, \varrho_{it+1}\right) = 0$, and $cov_t \left(\alpha_{it+1}, \varrho_{it+1}\right) = 0$. Hence ϱ_{it+1} can be interpreted as pure measurement error. Our estimations show that its variance is always small and insignificant so we will neglect it in what follows.⁴

The remainder of the paper deals with the identification and the estimation of α_{it+1} , \widetilde{R}_{wt+1} , and β_{it+1} , and with the question of whether the variable α_{it+1} has converged towards zero. If it has, the efficiency of the government bond market is said to have increased.

⁴The estimation results with measurement error are available from the authors upon request.

3 Empirical specification, data, and estimation method.

3.1 Empirical specification.

We estimate the following system (where i = 1, ..., N),

$$\widetilde{R}_{it+1} = \alpha_{it+1} + \beta_{it+1} \widetilde{R}_{wt+1} \tag{6}$$

$$\alpha_{it+1} = \kappa_{it+1}\mu_i + \pi_i\alpha_{it} + \kappa_{it+1}\varepsilon_{it+1} \tag{7}$$

$$\beta_{it+1} = \phi_{it+1}\beta_{it} + \chi_{it+1} \tag{8}$$

$$\widetilde{R}_{wt+1} = \mu_w + \pi_w \widetilde{R}_{wt} + \varepsilon_{wt+1} \tag{9}$$

The main variable of interest is α_{it+1} . In section 2 we assume that $\lim_{t\to+\infty}\alpha_{it+1}=0$. We therefore model the idiosyncratic component α_{it+1} as an AR(1) process, i.e. $\overline{\alpha}_{it+1}=\mu_i+\pi_i\overline{\alpha}_{it}+\varepsilon_{it+1}$ with $0<\pi_i<1$, multiplied by a deterministic convergence operator κ_{it+1} where $\lim_{t\to+\infty}\kappa_{it+1}=0$. Thus, $\alpha_{it+1}=\overline{\alpha}_{it+1}\kappa_{it+1}$. We can write $\overline{\alpha}_{it+1}=\mu_i/(1-\pi_iL)+\varepsilon_{it+1}/(1-\pi_iL)$ where L is the lag operator. Multiplication by κ_{it+1} then gives $\alpha_{it+1}=\kappa_{it+1}\mu_i/(1-\pi_iL)+\kappa_{it+1}\varepsilon_{it+1}/(1-\pi_iL)$. On multiplication of both sides of the latter expression by $(1-\pi_iL)$ we obtain eq.(7). For κ_{it} we use the following specification (see Luginbuhl and Koopman 2004),

$$\kappa_{it} = \exp\left[\xi_i(t - \tau_i)\right] / (1 + \exp\left[\xi_i(t - \tau_i)\right])$$
(10)

where $\xi_i < 0$ is the rate of convergence. Since $\xi_i < 0$ we have $\kappa_{it} = 0$ for $t \to +\infty$ and $\kappa_{it} = 1$ for $t \to -\infty$. In a sample of size T the fact that $\xi_i < 0$ implies that $\kappa_{it} \approx 0$ for $t >>> \tau_i$ and that $\kappa_{it} \approx 1$ for $t <<< \tau_i$. The parameter τ_i with $1 < \tau_i < T$ determines the mid-point of the change. Note that the model implies that $\alpha_{it+1} > 0$. We do not impose this condition in the estimations. Instead, we impose the weaker condition $\mu_i > 0$ (for i = 1, ..., N) which is easy to implement. Imposing $\alpha_{it+1} > 0$ would necessitate the use of nonlinear state space techniques which would seriously complicate the empirical analysis with only limited impact on the results since our results show that the restriction $\alpha_{it+1} > 0$ is only violated sporadically.

The error term ε_{it+1} is white noise and is assumed to follow a GARCH(1,1) process,

$$\varepsilon_{it+1} = h_{it+1}^{1/2} \nu_{it+1} \tag{11}$$

where $\nu_{it+1} \sim i.i.d(0,1)$ and where

$$h_{it+1} = V_t \left[\varepsilon_{it+1} \right] = \delta_i^a + \delta_i^b \varepsilon_{it}^2 + \delta_i^c h_{it} \tag{12}$$

with $\delta_i^a > 0$, $0 < \delta_i^b < 1$, $0 < \delta_i^c < 1$, and $0 < \delta_i^b + \delta_i^c < 1$. Note that the unconditional variance of ε_{it+1} is given by $\delta_i^a/(1 - \delta_i^b - \delta_i^c)$.

As can be seen in eq.(9) we assume that the common component \widetilde{R}_{wt+1} follows an AR(1) process with $0 < \pi_w < 1$ and where ε_{wt+1} is white noise and follows a GARCH(1,1) process,

$$\varepsilon_{wt+1} = h_{wt+1}^{1/2} \nu_{wt+1} \tag{13}$$

where $\nu_{wt+1} \sim i.i.d(0,1)$ and where

$$h_{wt+1} = V_t \left[\varepsilon_{wt+1} \right] = \delta_w^a + \delta_w^b \varepsilon_{wt}^2 + \delta_w^c h_{wt} \tag{14}$$

with $\delta_w^a > 0$, $0 < \delta_w^b < 1$, $0 < \delta_w^c < 1$, and $0 < \delta_w^b + \delta_w^c < 1$. Note that the unconditional variance of ε_{wt+1} is given by $\delta_w^a/(1-\delta_w^b-\delta_w^c)$.

Eq.(8) represents the law of motion for β_{it+1} . In Del Negro and Otrok's (2006) factor model β_{it+1} is assumed to follow a driftless random walk, i.e. $\phi_{it+1} = 1$ and χ_{it+1} is white noise. The approach that we follow in this paper is based on a direct parameterization of the conditional covariance and variance in β_{it+1} . Remember from section 2 that $\beta_{it+1} = \frac{g_{it+1}}{h_{wt+1}} = \frac{cov_t \left[\tilde{R}_{wt+1}, \left(\tilde{R}_{it+1} - \alpha_{it+1}\right)\right]}{V_t \left[\tilde{R}_{wt+1}\right]}$. This can be written as $\beta_{it+1} = \frac{g_{it+1}}{h_{wt+1}} = \frac{cov_t \left[\varepsilon_{wt+1}, \varepsilon'_{it+1}\right]}{V_t \left[\varepsilon_{wt+1}\right]}$ where $\varepsilon'_{it+1} = \varepsilon^R_{it+1} - \kappa_{it+1}\varepsilon_{it+1}$ with $\varepsilon^R_{it+1} = \tilde{R}_{it+1} - E_t \left[\tilde{R}_{it+1}\right]$ and $\kappa_{it+1}\varepsilon_{it+1} = \alpha_{it+1} - E_t \left[\alpha_{it+1}\right]$, and where h_{wt+1} is given by eq.(14). We parameterize the conditional covariance g_{it+1} as a function of the lagged cross-product of the errors ε_{wt+1} and ε'_{it+1} and of its own lag (i.e. the diagonal bivariate VEC(1,1) of Bollerslev et al. 1988),

$$g_{it+1} = \gamma_i^a + \gamma_i^b \varepsilon_{wt} \varepsilon_{it}' + \gamma_i^c g_{it} \tag{15}$$

with $\gamma_{i}^{a} > 0$, $0 < \gamma_{i}^{b} < 1$, $0 < \gamma_{i}^{c} < 1$, and $0 < \gamma_{i}^{b} + \gamma_{i}^{c} < 1$ for i = 1, ..., N. Note that from eq.(6) we can write $\varepsilon_{it+1}^{'} = \varepsilon_{it+1}^{R} - \kappa_{it+1}\varepsilon_{it+1} = \beta_{it+1}\varepsilon_{wt+1}$ so that eq.(15) can be rewritten as,

$$g_{it+1} = \gamma_i^a + \gamma_i^b \beta_{it} \varepsilon_{wt}^2 + \gamma_i^c g_{it} \tag{16}$$

Substituting eqs.(14) and (16) into $\beta_{it+1} = \frac{g_{it+1}}{h_{wt+1}}$ we obtain eq.(8) with $\phi_{it+1} = \frac{\gamma_i^b \varepsilon_{wt}^a + \gamma_i^c h_{wt}}{h_{wt+1}}$ and $\chi_{it+1} = \frac{\gamma_i^a}{h_{wt+1}}$ (where we have used $g_{it} = \beta_{it} h_{wt}$). Contrary to the specification for β_{it+1} considered by Del Negro and Otrok our specification for β_{it+1} can still be estimated in a linear state space framework with maximum likelihood. Our approach of dealing with conditional covariances in a state space framework is an extension of the state space models with time-varying conditional variances as studied by Harvey et al. (1992).

3.2 A look at the data.

We calculate weekly holding period returns on government bonds for 5 countries: Belgium, France, Germany, Italy, and the Netherlands. As in many other studies bond returns are computed from the J.P. Morgan government bond indices (see e.g. Barr and Priestley 2004). An advantage of these indices is that the returns can be calculated in local currency (Belgian franc, French franc, German mark, Italian lira, Dutch guilder before 1/1/1999; euro afterwards). According to Ilmanen (1995) this is equivalent to analyzing currency hedged returns, i.e. a bond's local currency return can be considered a bond's currency hedged return for any foreign investor, independent of his home country. Local currency returns are relevant since we are interested in interest rate risk, not in exchange rate risk.

Since data are available on a daily basis we calculate the daily returns as the growth rate in the government bond index. We annualize the returns by multiplying by 260 (=number of trading days per year). We calculate the excess government bond returns or government bond risk premia by subtracting from the returns the risk free interest rate for which we use the 1 week eurocurrency rate provided by Financial Times/Intercapital (in local currency, annualized), and which is also available on a daily basis. The excess returns are in real terms because the inflation components in the government bond returns are cancelled out by the inflation components in the risk free rates (see Harvey 1991). This is in accordance with our theoretical model which holds for real returns. We then average the (annualized) daily excess returns to (annualized) weekly excess returns (monday to friday). Aggregation from daily to weekly data avoids the occurrence of day-of-the-week effects and averages out other noise while considerably reducing the computational time of our state space estimations.

The resulting dataset covers the period 06-01-1995 to 29-12-2006 providing 626 weekly observations per country. All data are taken from Datastream.

In table 1 we report the unconditional means and standard deviations of the annualized government bond excess returns of the 5 countries under investigation. First, we note that, irrespective of the sample period considered, the average excess returns are highest for Italy and lowest for

⁵We use the total return index over all maturities. Alternative indices with maturity bands 1-10 or 7-10 years are not available for all 5 countries for the period that we want to focus on (that is the period including the years before the introduction of the euro). An alternative method that we have considerered is to calculate returns from the zero coupon bond yield curves. Reliable data are available from BIS, but are again not available for the period that we want to focus on.

Germany. For the full sample period the average annualized risk premium on government bonds of Italy is about 0.8 percentage points higher than the average annualized risk premium on German bonds. Second, for all countries, the average annualized excess return or risk premium in the first half of the sample (1995-2000) is considerably higher than in the second half of the sample (2001-2006). We test the significance of the mean excess return in each country and we find that it is significantly different from zero over the total period 1995-2006 and in the period 1995-2000 while the null hypothesis of a zero unconditional mean cannot unambiguously be rejected during the period 2001-2006.

In table 2 we report the unconditional correlations of the annualized government bond excess returns. First, the reported correlations clearly suggest that the excess returns are driven by a common component as our theoretical model predicts and as reported for instance by Ilmanen (1995). Second, we note that the correlation between the excess returns is considerably higher in the second half of the sample which indicates that the idiosyncratic components of the risk premia have become less relevant.

3.3 Estimation.

3.3.1 Method.

We obtain estimates for the unobserved states α_{it+1} and R_{wt+1} , for the conditional variance series h_{it+1} and h_{wt+1} , for the conditional covariance series g_{it+1} and thus for β_{it+1} , for the convergence operator series κ_{it+1} , and for the parameters in the model by putting the model described in section 3.1 in state space form. In particular, we estimate a Gaussian linear state space system including time-varying conditional variances (see Harvey et al. 1992 and Kim and Nelson 1999, chapter 6) and covariances. In Appendix B we report the state space representation of the model. Estimates of the state vector are obtained with the Kalman filter and smoother. Given the assumption of stationarity the initialization of the filter is non-diffuse.

The time-varying conditional variances and covariances complicate the otherwise standard state space framework. To deal with this we follow the approach by Harvey et al. (1992) and augment the state vector with the shocks ε_{it+1} and ε_{wt+1} . The Kalman filter then provides estimates of the conditional variance of the shocks, i.e. estimates for h_{it+1} and h_{wt+1} . This also allows us to calculate g_{it+1} and β_{it+1} . We refer to appendix B for more details on the approach followed.

To deal with potential computational difficulties that are caused by the relatively large dimension of the observation vector we follow the univariate approach to multivariate filtering and smoothing as presented by Koopman and Durbin (2000) and Durbin and Koopman (2001, chapter 6). A major advantage of this approach is that we can avoid taking the inverse of the variance matrix of the one-step-ahead prediction errors. We refer to Koopman and Durbin (2000) for the filtering and smoothing recursions and for the calculation of the likelihood.

3.3.2 Identification.

As is standard in factor models, first, to identify the factor loadings β_{it+1} we impose an unconditional variance of unity on ε_{wt+1} , i.e. $\sigma_w^2 = 1$. This amounts to setting $\delta_w^a = 1 - \delta_w^b - \delta_w^c$ (see Dungey et al. 2000). Second, implicitly factor loadings are also estimated on the states α_{it+1} since eq.(6) can be written as $\widetilde{R}_{it+1} = \kappa_{it+1} \overline{\alpha}_{it+1} + \beta_{it+1} \widetilde{R}_{wt+1}$. We impose $\kappa_{i1} = 1$ ($\forall i$). Third, the sign of the factor loadings β_{it+1} cannot be identified because of the sign invariance of the factor variance decompositions of the spreads. Therefore, we impose $\beta_{it+1} > 0$. Since $\beta_{it+1} = \frac{g_{it+1}}{h_{wt+1}}$ we need $g_{it+1} > 0$ and $h_{wt+1} > 0$. It is straightforward to show that under the processes and parameter restrictions discussed in section 3.1 these conditions hold. Fourth, our model contains constants (i.e. the data we use are not in deviations from the mean). Since we can only estimate N constants but the model contains N+1 constants (i.e. μ_w and μ_i for i=1,...,N where N=5) we need to impose an identifying restriction on the constants. One possibility is to impose $\sum_{i=1}^{N} \mu_i = 0$. We cannot impose this condition since we have implemented $\mu_i > 0$ (for i = 1, ..., N) to capture the non-negativity of α_{it+1} (see section 3.1). Instead we impose $\mu_w = 0$. We justify this by noting that in our data analysis in section 3.2 we find, for all countries, that the unconditional mean of the excess returns R_{it+1} is not significantly different from zero in the second part of the sample while it is highly significant in the first part of the sample. Since β_{it+1} is strictly positive a value $\mu_w > 0$ cannot lead to an unconditional mean of zero of the excess returns at any point in time. Therefore the restriction $\mu_w = 0$ is sensible.

4 Results.

In table 3 we present the parameter estimates obtained from the estimation of the system given by eqs.(6) to (15). We also report a test for first-order autocorrelation in the one-step-ahead prediction errors of the system, i.e. a Ljung-Box test, and a goodness of fit test, i.e. the Akaike Information Criterion (AIC). These tests are discussed in Durbin and Koopman (2001, pages 34 and 152 respectively). In figures 1-12 we present different time series obtained from the estimation reported in table 3.

From table 3 we note, first, that there are significant convergence effects since ξ is significantly lower than zero for all countries. Also, according to a comparison of the AIC statistic for our model with convergence effects and the statistic calculated for the same model but without convergence effects (i.e. when setting $\kappa_{it} = 1 \,\forall i, t$), we find that the model with convergence effects is clearly preferred. In figures 1-5 the smoothed estimates for the idiosyncratic components α_{it} are contrasted with the excess returns \widetilde{R}_{it} . As can be seen from the figures the idiosyncratic components have decreased for all countries. By the end of 2006 the magnitude of α_{it} is very close to zero for all countries with the exception of Italy. The estimated convergence operator series κ_{it} are reported in figure 7 and show the convergence of α_{it} towards zero for all countries. It also shows that at the end of the sample period convergence has not been as radical for Italy as it has been for the other countries.

Second, the persistence in the conditional variance series h_{it} of the idiosyncratic component errors is very high as reflected by the sum $\delta_i^b + \delta_i^c$ which is close to 1 for all countries, i.e. we find integrated GARCH estimates for h_{it} . From inspection of figures 8 and 9 we note that this is most likely due to the level shift in the variance of α_{it} in all countries (see e.g. Lamoureux and Lastrapes).⁶ The conditional variance h_{wt} for the common component \tilde{R}_{wt} is reported in figure 10. While it is rather persistent there is no integrated GARCH nor any indication of a structural break in this series. This is important for the estimated series for β_{it} which are approximated by dividing the estimated series for the conditional covariance g_{it} by the estimated series for h_{wt} . In figure 11 we report the conditional covariance series g_{it} for all countries. We find that g_{it} is constant for most of the sample period for all countries. In the first years of the sample there is some time-variation (i.e. a decline) in g_{it} for France and the Netherlands (as reflected also by an estimate for γ_i^b that is significantly different from zero for these countries). As can be seen in figure 12 the impact of this time variation in g_{it} on the country-specific impacts β_{it} is very small however so that the movement in β_{it} is largely determined by h_{wt} and is therefore very similar

⁶The finding of integrated GARCH may be due to the fact that κ_{it} seems to capture the decrease in the mean of α_{it} (second half of sample) more than the decrease in the variance (first half of sample). Since Enders (2004, p140-141) argues that the finding of integraded GARCH causes no inference problems we do not try to alleviate this.

across countries. In table 4 we report the estimation results of the system given by eqs.(6) to (15) but with a constant conditional covariance g_{it} , i.e. $\gamma_i^b = \gamma_i^c = 0$ for all i. From this table we note that our results are hardly affected by the imposed restrictions and that the AIC statistics reported in tables 3 and 4 are of equal magnitude (the time-varying g_{it} model is only slightly preferred). The magnitude of the estimated constant $g_{it} = \gamma_i^a$ is highest for Italy and lowest for Germany, indicating that the impact of international risk on average is (slightly) higher for Italy. This provides some support for Codogno et al. (2003) who find that international risk factors are more important for the yields of Italian government bonds.

Our results thus suggest that it is α_{it} , rather than β_{it} , that is responsible for the decrease in government bond excess returns in all countries. The reduction of the risk premia can be attributed to a decrease in illiquidity (in particular market-specific transaction costs) and taxation rather than to a decrease in the country-specific exposure to international risk. As far as liquidity is concerned this supports Bernoth et al. (2004) who argue that the introduction of the euro has decreased liquidity premia for euro area government bonds. Codogno et al. (2003) and Favero et al. (2007) find that, for the years 2002 and 2003, the liquidity component for government bonds is not very important.

It is tempting to attribute the decrease in the idiosyncratic components to the introduction of the euro on 1/1/1999. However, the convergence most likely is also part of a wider global phenomenon. Financial integration may also have accelerated because of more intense trade, improvements in information technology, and other technological and financial innovations (see e.g. Schulz and Wolff 2008). An indication for this in our results is that we estimate that the convergence te zero of α_{it} starts rather late (see figure 7), quite some time after the introduction of the euro on 1/1/1999. The exception here is Italy where the large decrease of the variance in α_{it} in the nineties clearly affects κ_{it} before the introduction of the euro.

5 Conclusions.

In this paper we derive a model in which a standard international capital asset pricing model (ICAPM) is nested within an ICAPM with market imperfections. In the latter model an idiosyncratic stochastic factor affects the risk premium or excess return of government bonds on top of the systematic component that is common to all countries (and that is interacted with a time-varying

idiosyncratic "beta"). We introduce asymptotic convergence from the full ICAPM with imperfections to the standard model by multiplying the idiosyncratic factor by convergence operators.

Methodologically, we use a linear state space approach to estimate the latent factor decomposition of the excess returns or risk premia that is implied by the theoretical model. In particular, we use weekly data over the period 1995-2006 to decompose the government bond excess returns of Belgium, France, Germany, Italy, and the Netherlands into a common component and an idiosyncratic component. The country-specific time-varying impacts of the common factor on the bond spreads, the "betas" (i.e. the ratios of the conditional covariance of the common factor and the risk premium over the conditional variance of the common factor), are also estimated. We investigate whether the idiosyncratic components in government bond excess returns have converged towards zero.

Our results suggest that the idiosyncratic components have converged towards zero for all five countries over the sample period: the variance and the mean of the idiosyncratic components are stronly reduced so that by the end of 2006 the idiosyncratic components are very close to zero in magnitude for all countries but Italy. Therefore, by the end of the sample period, the government bond markets of Belgium, France, Germany, and the Netherlands are almost fully efficient. Moreover, the reduction of the risk premia in all countries is attributed to a decrease in local market impediments and imperfections rather than to a decrease in the country-specific exposure to international risk.

References

Acharya, V., and L. Pedersen (2005): "Asset pricing with liquidity risk," *Journal of Financial Economics*, 77, 375–410.

BARR, D., AND R. PRIESTLEY (2004): "Expected returns, risk and the integration of international bond markets," *Journal of International Money and Finance*, 23, 71–97.

Bernoth, K., J. von Hagen, and L. Schuknecht (2004): "Sovereign risk premia in the European government bond market," *ECB Working Paper 369*.

Bollerslev, T., R. Engle, and J. Wooldridge (1988): "A capital asset pricing model with time-varying covariances," *Journal of Political Economy*, 96(1), 116–131.

- Cappiello, L., R. Engle, and K. Sheppard (2003): "Asymmetric dynamics in the correlations of global equity and bond returns," *ECB Working Paper 204*.
- COCHRANE, J. (2005): Asset Pricing. Princeton University Press.
- Codogno, L., C. Favero, and A. Missale (2003): "Yield spreads on EMU government bonds," *Economic Policy*, 18, 503–532.
- DEL NEGRO, M., AND C. OTROK (2006): "Dynamic factor models with time-varying parameters," mimeo.
- Dungey, M., V. Martin, and A. Pagan (2000): "A multivariate latent factor decomposition of international bond yield spreads," *Journal of Applied Econometrics*, 15, 697–715.
- Durbin, J., and S. Koopman (2001): Time series analysis by state space methods, Oxford Statistical Science Series. Oxford University Press.
- Enders, W. (2004): Applied Econometric Time Series. Wiley.
- FAVERO, C., F. GIAVAZZI, AND L. SPAVENTA (1997): "High yields: the spread on German interest rates," *The Economic Journal*, 107, 956–985.
- FAVERO, C., M. PAGANO, AND E. VON THADDEN (2007): "How does liquidity affect government bond yields?," CSEF Working Paper 181.
- GEYER, A., S. KOSSMEIER, AND S. PICHLER (2004): "Measuring systematic risk in EMU government yield spreads," *Review of Finance*, 8, 171–197.
- Hamilton, J. (1994): Time series analysis. Princeton University Press.
- HARVEY, A., E. RUIZ, AND E. SENTANA (1992): "Unobserved component time series models with ARCH disturbances," *Journal of Econometrics*, 52, 129–157.
- HARVEY, C. (1991): "The world price of covariance risk," Journal of Finance, XLVI(1), 111–157.
- ILMANEN, A. (1995): "Time-varying expected returns in international bond markets," Journal of Finance, L(2), 481–506.
- Kim, C., and C. Nelson (1999): State-space models with regime switching: classical and Gibbs-sampling approaches with applications. MIT Press.

KOOPMAN, S., AND J. DURBIN (2000): "Fast filtering and smoothing for multivariate state space models," *Journal of Time Series Analysis*, 21(3), 281–296.

LAMOUREUX, C., AND W. LASTRAPES (1990): "Persistence in variance, structural change, and the GARCH model," *Journal of Business and Economic Statistics*, 8, 225–234.

LUGINBUHL, R., AND S. KOOPMAN (2004): "Convergence in European GDP series: a multivariate common converging trend-cycle decomposition," *Journal of Applied Econometrics*, 19, 611–636.

Schulz, A., and G. Wolff (2008): "Sovereign bond market integration: the euro, trading platforms and globalization," *Deutsche Bundesbank Discussion Paper (Series 1) 12.*

Appendix A. Derivation of eq.(4).

Write eq.(1) as,

$$E_t[m_{t,t+1}] E_t[R_{it+1} - \alpha_{it+1}] + cov_t(m_{t,t+1}, R_{it+1} - \alpha_{it+1}) = 1$$
(A1)

From eq.(2) we have $E_t[m_{t,t+1}] = 1/R_{bt+1}$. By using this into eq.(A1) and re-arranging we obtain,

$$E_t[R_{it+1}] - R_{bt+1} = E_t[\alpha_{it+1}] - cov_t(m_{t,t+1}, R_{it+1} - \alpha_{it+1})R_{bt+1}$$
(A2)

Since $\alpha_{wt+1} = 0$ eq.(A2) written for R_{wt+1} is,

$$E_t[R_{wt+1}] - R_{bt+1} = -cov_t(m_{t,t+1}, R_{wt+1})R_{bt+1}$$
(A3)

(alternatively, use eq.(3) with $E_t[m_{t,t+1}] = 1/R_{bt+1}$ to obtain this).

Note that eq.(A2) can be rewritten as,

$$E_{t}[R_{it+1}] - R_{bt+1} = E_{t}[\alpha_{it+1}]$$

$$-cov_{t}(m_{t,t+1}, R_{it+1} - \alpha_{it+1}) R_{bt+1} \frac{cov_{t}(m_{t,t+1}, R_{wt+1})}{cov_{t}(m_{t,t+1}, R_{wt+1})}$$
(A4)

By using eq.(A3) into this we obtain,

$$E_{t}[R_{it+1}] - R_{bt+1} = E_{t}[\alpha_{it+1}] + \frac{cov_{t}(m_{t,t+1}, R_{it+1} - \alpha_{it+1})}{cov_{t}(m_{t,t+1}, R_{wt+1})} (E_{t}[R_{wt+1}] - R_{bt+1})$$
(A5)

We assume that the returns $R_{it+1} - \alpha_{it+1}$ are driven by the stochastic discount factor $m_{t,t+1}$ as in the following equation,

$$R_{it+1} - \alpha_{it+1} = \tau_{it+1} m_{t,t+1} + u_{it+1} \tag{A6}$$

where u_{it+1} is white noise and where $\tau_{it+1} = \frac{cov_t(m_{t,t+1}, R_{it+1} - \alpha_{it+1})}{V_t[m_{t,t+1}]}$. This assumption implies that we impose causality running from the stochastic discount factor (i.e. consumption) to asset returns. We refer to Cochrane (2005, pages 37-41) for an enlightening discussion on this assumption and on why it can be justified. By averaging the RHS and LHS of eq.(A6) over N international assets we can write,

$$R_{wt+1} = \tau_{wt+1} m_{t,t+1} \tag{A7}$$

where $R_{wt+1} = N^{-1} \sum_{i=1}^{N} R_{it+1}$ and $\tau_{wt+1} = N^{-1} \sum_{i=1}^{N} \tau_{it+1} = \frac{cov_t(m_{t,t+1}, R_{wt+1})}{V_t[m_{t,t+1}]}$ and where we use the assumption $\alpha_{wt+1} = N^{-1} \sum_{i=1}^{N} \alpha_{it+1} = 0$ and $N^{-1} \sum_{i=1}^{N} u_{it+1} = 0$ to obtain the result.

Then note that,

$$V_t[R_{wt+1}] = \tau_{wt+1} cov_t(m_{t,t+1}, R_{wt+1})$$
(A8)

and,

$$\begin{array}{lll} cov_{t}(R_{it+1}-\alpha_{it+1},R_{wt+1}) & = & \tau_{it+1}\tau_{wt+1}V_{t}\left[m_{t,t+1}\right] \\ & = & \frac{cov_{t}(m_{t,t+1},R_{it+1}-\alpha_{it+1})}{V_{t}\left[m_{t,t+1}\right]}\tau_{wt+1}V_{t}\left[m_{t,t+1}\right] \\ & = & cov_{t}(m_{t,t+1},R_{it+1}-\alpha_{it+1})\tau_{wt+1} \\ & = & \frac{cov_{t}(m_{t,t+1},R_{it+1}-\alpha_{it+1})}{cov_{t}(m_{t,t+1},R_{wt+1})}V_{t}\left[R_{wt+1}\right] \end{array}$$

where the last line uses eq.(A8). This gives,

$$\frac{cov_t(m_{t,t+1}, R_{it+1} - \alpha_{it+1})}{cov_t(m_{t,t+1}, R_{wt+1})} = \frac{cov_t(R_{it+1} - \alpha_{it+1}, R_{wt+1})}{V_t[R_{wt+1}]} = \beta_{it+1}$$
(A9)

By substituting eq.(A9) into eq.(A5) we obtain eq.(4) in the text.

Appendix B. State space representation of the model.

The state space system with state vector S_{t+1} is,

$$y_{t+1} = Z_{t+1} S_{t+1} \tag{B1}$$

$$S_{t+1} = T_{t+1}S_t + K_{t+1}\eta_{t+1} \tag{B2}$$

with

$$\eta_{t+1|t} \sim N(0, Q_{t+1})$$
(B3)

$$S_1 \sim N(A_1, P_1) \tag{B4}$$

Since N=5 we have $y_{t+1}=\begin{bmatrix}\widetilde{R}_{1t+1} & \widetilde{R}_{2t+1} & \widetilde{R}_{3t+1} & \widetilde{R}_{4t+1} & \widetilde{R}_{5t+1}\end{bmatrix}'$,

$$S_{t+1} = \begin{bmatrix} 1 & \alpha_{1t+1} & \alpha_{2t+1} & \alpha_{3t+1} & \alpha_{4t+1} & \alpha_{5t+1} & \widetilde{R}_{wt+1} & \varepsilon_{1t+1} & \varepsilon_{2t+1} & \varepsilon_{3t+1} & \varepsilon_{4t+1} & \varepsilon_{5t+1} \end{bmatrix}',$$

$$\eta_{t+1} = \begin{bmatrix} \varepsilon_{wt+1} & \varepsilon_{1t+1} & \varepsilon_{2t+1} & \varepsilon_{3t+1} & \varepsilon_{4t+1} & \varepsilon_{5t+1} \end{bmatrix}',$$

$$A_1 = \begin{bmatrix} 1 & \frac{\mu_1}{1-\pi_1} & \frac{\mu_2}{1-\pi_2} & \frac{\mu_3}{1-\pi_3} & \frac{\mu_4}{1-\pi_4} & \frac{\mu_5}{1-\pi_5} & \frac{\mu_w}{1-\pi_w} & 0 & 0 & 0 & 0 & 0 \end{bmatrix}'$$

where $\mu_w = 0$,

$$diag(P_1) = \begin{bmatrix} 0 & \frac{\sigma_{\alpha_1}^2}{1-\pi_1^2} & \frac{\sigma_{\alpha_2}^2}{1-\pi_2^2} & \frac{\sigma_{\alpha_3}^2}{1-\pi_2^2} & \frac{\sigma_{\alpha_4}^2}{1-\pi_2^2} & \frac{\sigma_{\alpha_5}^2}{1-\pi_5^2} & \frac{\sigma_w^2}{1-\pi_0^2} & \sigma_{\alpha_1}^2 & \sigma_{\alpha_2}^2 & \sigma_{\alpha_3}^2 & \sigma_{\alpha_4}^2 & \sigma_{\alpha_5}^2 & \sigma_w^2 \end{bmatrix}'$$

where
$$\sigma_{\alpha i}^2=\delta_i^a/(1-\delta_i^b-\delta_i^c)$$
 (for $i=1,...,5$) and $\sigma_w^2=\delta_w^a/(1-\delta_w^b-\delta_w^c)=1$,

$$diag(Q_{t+1}) = \begin{bmatrix} h_{wt+1} & h_{1t+1} & h_{2t+1} & h_{3t+1} & h_{4t+1} & h_{5t+1} \end{bmatrix}'$$

where $h_{it+1} = \delta^a_i + \delta^b_i \varepsilon^2_{it} + \delta^c_i h_{it}$ (for i = 1, ..., 5) and $h_{wt+1} = \delta^a_w + \delta^b_w \varepsilon^2_{wt} + \delta^c_w h_{wt}$ with $\delta^a_w = 1 - \delta^b_w - \delta^c_w$,

where $\beta_{it+1} = \frac{g_{it+1}}{h_{wt+1}}$ with $g_{it+1} = \gamma_i^a + \gamma_i^b \beta_{it} \varepsilon_{wt}^2 + \gamma_i^c g_{it}$ (for i=1,...,5),

where $\mu_w = 0$ and where $\kappa_{it+1} = \exp\left[\xi_i(t+1-\tau_i)\right]/(1+\exp\left[\xi_i(t+1-\tau_i)\right])$ (for i=1,...,5). Note that $\kappa_{i1} = 1$ (for i=1,...5).

Some technical notes:

- 1. To apply the method proposed by Harvey et al. (1992) the conditional distribution of the error η_{t+1} is assumed to be Gaussian. The unconditional distribution is of course not normal (see Hamilton 1994, p662).
- 2. Consistent estimation necessitates system matrices Z_{t+1} , T_{t+1} , K_{t+1} , and Q_{t+1} that are either constant, exogenous or predetermined (see Hamilton 1994, chapter 13) which is the case in our model.
- 3. The filter is initialized with the matrices A_1 and P_1 which, given the assumption of stationary states, contain the unconditional means and variances of the states.
- 4. The time-varying conditional variances h_{it+1} and h_{wt+1} complicate the linear Gaussian state space framework. To deal with this we follow the approach by Harvey et al. (1992) and we include the shocks ε_{it+1} and ε_{wt+1} in the state vector. We note then that h_{it+1} (for i=1,...,5) and h_{wt+1} and therefore Q_{t+1} are functions of the unobserved states ε_{it} and ε_{wt} . Harvey et al. (1992) replace h_{it+1} and h_{wt+1} in the system by $h_{it+1}^* = \delta_i^a + \delta_i^b \varepsilon_{it}^{*2} + \delta_i^c h_{it}^*$ and $h_{wt+1}^* = \delta_w^a + \delta_w^b \varepsilon_{wt}^{*2} + \delta_w^c h_{wt}^*$ where the unobserved ε_{it}^2 and ε_{wt}^2 are replaced by their conditional expectations $\varepsilon_{it}^{*2} = E_t \varepsilon_{it}^2$ and $\varepsilon_{wt}^{*2} = E_t \varepsilon_{it}^2$. Note that $E_t \varepsilon_{it}^2 = [E_t \varepsilon_{it}]^2 + [E_t (\varepsilon_{it} E_t \varepsilon_{it})^2]$ and $E_t \varepsilon_{wt}^2 = [E_t \varepsilon_{wt}]^2 + [E_t (\varepsilon_{wt} E_t \varepsilon_{wt})^2]$

where the quantities between square brackets are period t Kalman filter output (conditional means and variances of the states ε_{it} and ε_{wt}). Thus, given h_{it}^* and h_{wt}^* (which are initialized by the unconditional variances of ε_{it} and ε_{wt} , i.e. $\sigma_{\alpha i}^2$ and σ_w^2) and given the Kalman filter output from period t, namely $E_t(S_t)$ and $V_t(S_t)$, we can calculate h_{it+1}^* and h_{wt+1}^* and the system matrix Q_{t+1} which makes it possible to calculate $E_t(S_{t+1})$, $V_t(S_{t+1})$ and $E_{t+1}(S_{t+1})$, $V_{t+1}(S_{t+1})$, and so on...

5. The time-varying conditional covariances g_{it+1} and time-varying β_{it+1} further complicate the linear Gaussian state space framework. Note that g_{it+1} and β_{it+1} can be replaced by $g_{it+1}^* = \gamma_i^a + \gamma_i^b \beta_{it}^* \varepsilon_{wt}^{*2} + \gamma_i^c g_{it}^*$ and $\beta_{it+1}^* = \frac{g_{it+1}^*}{h_{wt+1}^*}$ where ε_{wt}^{*2} and h_{wt+1}^* are calculated as reported in 4. The variable h_{wt}^* is initialized by the unconditional variance of ε_{wt} , i.e. σ_w^2 , while g_{it}^* is initialized by the unconditional covariance $\frac{\gamma_i^a}{1-\gamma_i^b-\gamma_i^c}$.

Tables and Figures

Table 1. Unconditional means and standard deviations of excess government bond returns.

	Belgium	France	Germany	Italy	Netherlands	
	Full sample					
	06-01-1995 to 29-12-2006					
Mean	0.0352	0.0324	0.0298 0.0379 0		0.0333	
Standard deviation	0.2488	0.2559	0.2402	0.2402 0.2915 0		
Test	0.0004	0.0016	0.0020	0.0012	0.0008	
	First half of sample					
	06-01-1995 to 29-12-2000					
Mean	0.0454	0.0426	0.0384	0.0493	0.0443	
Standard deviation	0.2510	0.2636	0.2360	0.3170	0.2556	
Test	0.0015	0.0045	0.0043	0.0062	0.0024	
	Second half of sample					
	05-01-2001 to 29-12-2006					
Mean	0.0250	0.0222	0.0212	0.0265	0.0223	
Standard deviation	0.2465	0.2480	0.2444	0.2634	0.2373	
Test	0.0732	0.1141	0.1261	0.0764	0.0980	

Note: Test reports the p-value of the test that the sample mean equals zero

Table 2. Unconditional correlations of excess government bond returns.

	Belgium	France	Germany	Italy	Netherlands			
	Full sample							
	06-01-1995 to 29-12-2006							
Belgium	1	-	-	-	-			
France	0.9544	1	-	-	-			
Germany	0.9600	0.9334	1	-	-			
Italy	0.7903	0.8265	0.7627	1	-			
Netherlands	0.9630	0.9362	0.9792	0.7630	1			
	First half of sample							
		06-0	01-1995 to 29-12-2000					
Belgium	1	-	-	-	-			
France	0.9176	1	-	-	-			
Germany	0.9354	0.8809	1	-	-			
Italy	0.6373	0.7021	0.5844	1	-			
Netherlands	0.9375	0.8853	0.9700	0.5952	1			
	Second half of sample							
	05-01-2001 to 29-12-2006							
Belgium	1	-	-	-	-			
France	0.9946	1	-	-	-			
Germany	0.9847	0.9893	1	-	-			
Italy	0.9830	0.9886	0.9791	1	-			
Netherlands	0.9917	0.9943	0.9917	0.9821	1			

Table 3. Maximum likelihood estimation of the common factor model with GARCH errors and convergence effects (eqs. 6-15).

		Country	y-specific para	meters		Common parameter
	Belgium	France	Germany	Italy	Netherlands	
μ	0.0446	0.0433	0.0397	0.0460	0.0434	-
	(0.0112)	(0.0119)	(0.0116)	(0.0123)	(0.0121)	-
π	-0.1429	-0.1632	-0.1924	-0.1166	-0.2145	-0.0421
	(0.0503)	(0.0569)	(0.0655)	(0.0416)	(0.0615)	(0.0383)
ξ	-0.0204	-0.0166	-0.0204	-0.0080	-0.0178	-
	(0.0033)	(0.0032)	(0.0039)	(1.9E-6)	(0.0033)	-
au	552.23	562.89	571.50	625.99	570.25	-
	(16.550)	(22.546)	(16.119)	(0.0024)	(18.464)	-
δ^a	9.8E-5	1.6E-6	1.4E-5	6.0E-5	0.0001	0.0863 a
	(2.8E-5)	(1.0E-6)	(5.2E-6)	(2.8E-5)	(2.9E-5)	(0.0427)
δ^b	0.3724	0.1224	0.2069	0.1285	0.6522	0.0685
	(0.0556)	(0.0232)	(0.0258)	(0.0242)	(0.1222)	(0.0252)
δ^c	0.6223	0.8775	0.7924	0.8713	0.3386	0.8451
	(0.0559)	(0.0232)	(0.0259)	(0.0243)	(0.1211)	(0.0564)
γ^a	0.0116	0.2440	0.2360	0.2479	0.0515	-
	(0.0111)	(0.0116)	(0.0115)	(0.0120)	(0.0211)	-
γ^b	0.0109	0.3879	5.5E-6	0.0004	0.1286	-
	(0.0177)	(0.1781)	(2.0E-5)	(0.0009)	(0.0630)	-
γ^c	0.9510	5.9E-5	0.0059	0.0009	0.7813	-
	(0.0469)	(0.0002)	(0.0100)	(0.0022)	(0.0888)	-
Cou	ntry-specific L	jung-Box test	: no autocorre	lation in the	one-step-ahead	d prediction errors
pval	0.172	0.139	0.725	0.480	0.866	-
			Full model: go	odness of fi	t	
AIC^c	-13.9169					
AIC^n		-13.8562				

Note: Hessian based standard errors between brackets. a For the common state the estimate of δ^a is obtained from $\delta^a=1-\delta^b-\delta^c$. The Ljung-Box test uses lag length 1 (see Durbin and Koopman, 2001, p.34). AIC^c is Akaike Information Criterion for the model with convergence while AIC^n is the criterion if no convergence, i.e. $\kappa_{it}=1$ ($\forall i,t$). A model with a smaller AIC is preferred (see Durbin and Koopman, 2001, p.152).

Table 4. Maximum likelihood estimation of the common factor model with GARCH errors and convergence effects (eqs. 6-15) under the restriction of constant conditional covariances $g_{it} = \gamma_i^a$ (i.e. $\gamma_i^b = \gamma_i^c = 0$).

	Country-specific parameters					Common parameters
	Belgium	France	Germany	Italy	Netherlands	
μ	0.0456	0.0448	0.0394	0.0481	0.0450	-
	(0.0119)	(0.0128)	(0.0121)	(0.0139)	(0.0133)	-
π	-0.1451	-0.1753	-0.1521	-0.1232	-0.2315	-0.0410
	(0.0480)	(0.0578)	(0.0682)	(0.0417)	(0.0562)	(0.0374)
ξ	-0.0201	-0.0161	-0.0198	-0.0084	-0.0169	-
	(0.0032)	(0.0032)	(0.0039)	(0.0007)	(0.0033)	-
au	550.05	559.31	568.77	596.66	564.36	-
	(17.257)	(26.304)	(18.946)	(3.8328)	(22.235)	-
δ^a	0.0001	2.0E-6	1.4E-5	6.8E-5	9.2E-5	0.0915^{a}
	(3.0E-5)	(1.3E-6)	(5.4E-6)	(3.2E-5)	(2.4E-5)	(0.0469)
δ^b	0.3826	0.1302	0.2019	0.1308	0.5765	0.0679
	(0.0574)	(0.0248)	(0.0242)	(0.0253)	(0.1080)	(0.0275)
δ^c	0.6132	0.8697	0.7973	0.8690	0.4177	0.8406
	(0.0584)	(0.0248)	(0.0244)	(0.0254)	(0.1078)	(0.0621)
γ^a	0.2405	0.2470	0.2395	0.2513	0.2393	-
	(0.0109)	(0.0112)	(0.0109)	(0.0116)	(0.0109)	-
Cou	ntry-specific L	jung-Box test:	no autocorre	lation in the	one-step-ahead	d prediction errors
pval	0.180	0.214	0.593	0.418	0.803	-
			Full model: go	odness of fi	t	
AIC^c	-13.9137					
AIC^n	-13.8498					

Note: Hessian based standard errors between brackets. a For the common state the estimate of δ^a is obtained from $\delta^a=1-\delta^b-\delta^c$. The Ljung-Box test uses lag length 1 (see Durbin and Koopman, 2001, p.34). AIC^c is Akaike Information Criterion for the model with convergence while AIC^n is the criterion if no convergence, i.e. $\kappa_{it}=1$ ($\forall i,t$). A model with a smaller AIC is preferred (see Durbin and Koopman, 2001, p.152).

Figure 1: Risk premium and idiosyncratic state α_{it} for Belgium

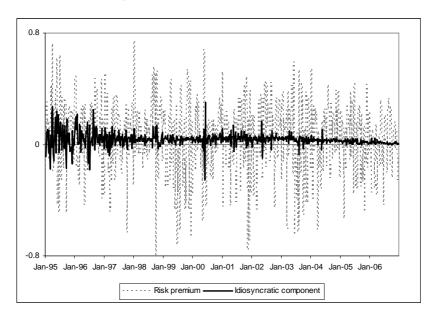


Figure 2: Risk premium and idiosyncratic state α_{it} for France

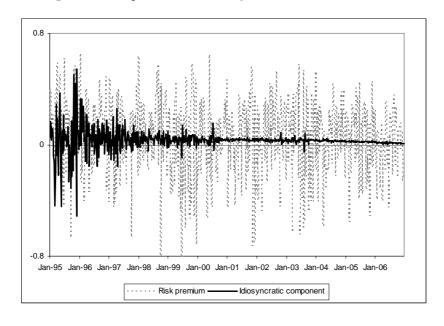


Figure 3: Risk premium and idiosyncratic state α_{it} for Germany

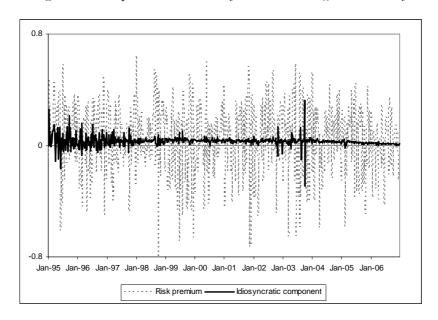


Figure 4: Risk premium and idiosyncratic state α_{it} for Italy

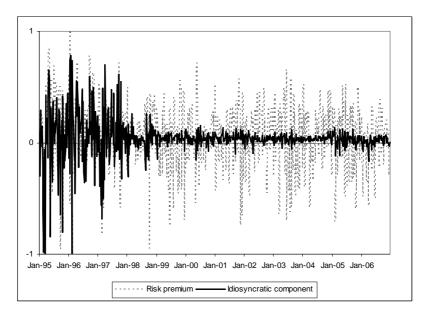


Figure 5: Risk premium and idiosyncratic state α_{it} for the Netherlands

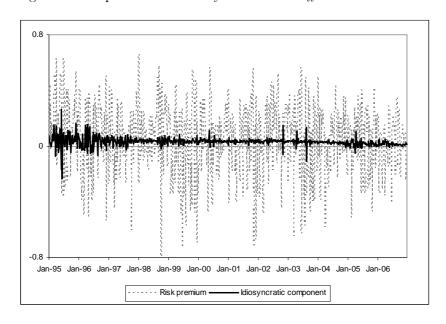


Figure 6: Common state \widetilde{R}_{wt}

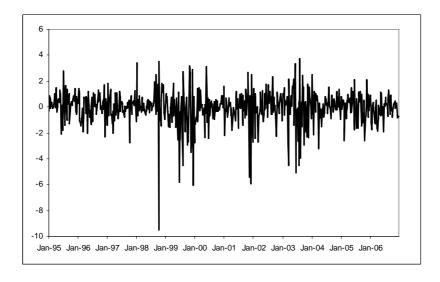


Figure 7: Convergence dynamics of the idiosyncratic states α_{it} (convergence operators κ_{it})

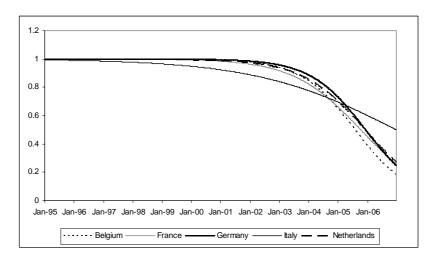


Figure 8: GARCH series h_{it} for Belgium, France, Germany, and the Netherlands

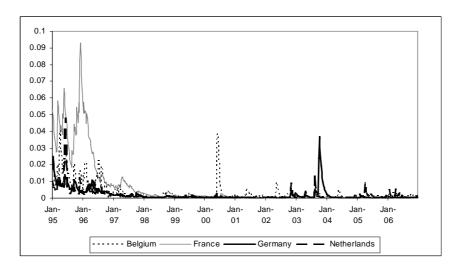


Figure 9: GARCH series h_{it} for Italy

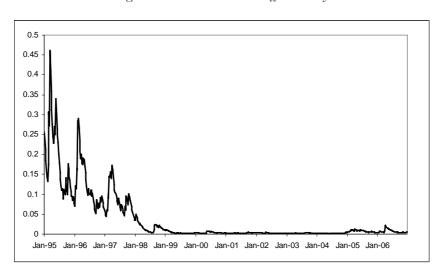


Figure 10: GARCH series h_{wt} for the common state

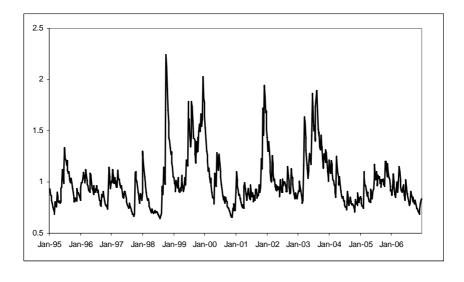


Figure 11: Conditional covariance series g_{it} for all countries

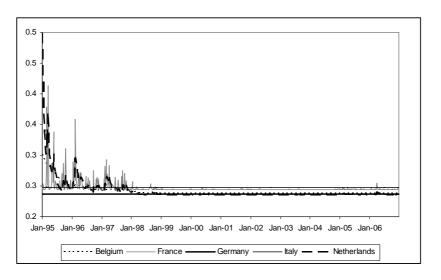


Figure 12: Time-varying β_{it} for all countries

