

Hommes, Cars; Sonnemans, Joep; Tuinstra, Jan; van de Velden, Henk

**Working Paper**

## Coordination of Expectations in Asset Pricing Experiments

Tinbergen Institute Discussion Paper, No. 03-010/1

**Provided in Cooperation with:**

Tinbergen Institute, Amsterdam and Rotterdam

Suggested Citation: Hommes, Cars; Sonnemans, Joep; Tuinstra, Jan; van de Velden, Henk (2003) : Coordination of Expectations in Asset Pricing Experiments, Tinbergen Institute Discussion Paper, No. 03-010/1, Tinbergen Institute, Amsterdam and Rotterdam

This Version is available at:

<http://hdl.handle.net/10419/85859>

**Standard-Nutzungsbedingungen:**

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

**Terms of use:**

*Documents in EconStor may be saved and copied for your personal and scholarly purposes.*

*You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.*

*If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.*



TI 2003-010/1

Tinbergen Institute Discussion Paper

# Coordination of Expectations in Asset Pricing Experiments

*Cars Hommes*

*Joep Sonnemans*

*Jan Tuinstra*

*Henk van de Velde*

*CeNDEF, Department of Economics, Faculty of Economics and Econometrics, University of Amsterdam.*

**Tinbergen Institute**

The Tinbergen Institute is the institute for economic research of the Erasmus Universiteit Rotterdam, Universiteit van Amsterdam, and Vrije Universiteit Amsterdam.

**Tinbergen Institute Amsterdam**

Roetersstraat 31

1018 WB Amsterdam

The Netherlands

Tel.: +31(0)20 551 3500

Fax: +31(0)20 551 3555

**Tinbergen Institute Rotterdam**

Burg. Oudlaan 50

3062 PA Rotterdam

The Netherlands

Tel.: +31(0)10 408 8900

Fax: +31(0)10 408 9031

Please send questions and/or remarks of non-scientific nature to [driessen@tinbergen.nl](mailto:driessen@tinbergen.nl).

Most TI discussion papers can be downloaded at <http://www.tinbergen.nl>.

# Coordination of Expectations in Asset Pricing Experiments

Cars Hommes      Joep Sonnemans      Jan Tuinstra  
Henk van de Velden

CeNDEF, Department of Economics, University of Amsterdam  
Roetersstraat 11, 1018 WB Amsterdam, The Netherlands

Januari 2003

**Acknowledgements:** We benefitted from comments by seminar participants at the Universities of Amsterdam, Dortmund, Groningen, Maastricht and participants of the Review of Financial Studies Conference on Experimental and Behavioral Finance, Mannheim December 12-13, 2002. We especially thank our discussant Thomas Langer for his helpful comments. Financial support under a NWO-Pionier grant is gratefully acknowledged

**Corresponding Author:** Joep Sonnemans, Department of Economics and CeNDEF, University of Amsterdam, Roetersstraat 11, 1018 WB, Amsterdam, The Netherlands. E-mail: [j.h.sonnemans@uva.nl](mailto:j.h.sonnemans@uva.nl), Phone: ++31-20-525-4249.

# Coordination of Expectations in Asset Pricing Experiments

**Abstract:** We investigate expectation formation in a controlled experimental environment. Subjects are asked to predict the price in a standard asset pricing model. They do not have knowledge of the underlying market equilibrium equations, but they know all past realized prices and their own predictions. Aggregate demand of the risky asset depends upon the forecasts of the participants. The realized price is then obtained from market equilibrium with feedback from individual expectations. Each market is populated by six subjects and a small fraction of fundamentalist traders. Realized prices differ significantly from fundamental values. In some groups the asset price converges slowly to the fundamental price, in other groups there are regular oscillations around the fundamental price. Participants coordinate on a common prediction strategy. The individual prediction strategies can be estimated and correspond, for a large majority of participants, to simple linear autoregressive forecasting rules.

**Keywords:** experimental economics, expectations, asset pricing, coordination

**JEL classification code:** C91, C92, D84, G12, G14

# 1 Introduction

Expectations play an important role in economics. Decisions of economic agents are based upon their expectations and beliefs about the future state of the market. Through these decisions expectations feed back into the actual realization of the economic variables. This *expectations feedback mechanism* seems to be particularly important for financial markets. For example, if many traders expect the price of a certain asset to rise in the future, their demand for this asset increases which, by the law of supply and demand, will lead to an increase of the market price. This *self-confirming* nature of expectations is typical for speculative asset markets and it illustrates that the “psychology of the market” may be very important. A theory of expectation formation is therefore a crucial part of modelling economic or financial markets.

It is hard to observe or obtain detailed information about individual expectations in real markets. One approach is to obtain data on expectations by survey data analysis, as done for example by Turnovsky (1970) on expectations about the Consumers’ Price Index and the unemployment rate during the post-Korean war period. Frankel and Froot (1987) use a survey on exchange rate expectations and Shiller (1990) analyzes surveys on expectations about stock market prices and real estate prices. However, since in survey data research one can not control the underlying economic fundamentals, or the information that the forecaster possesses, it is hard to measure expectation rules in different circumstances.

An alternative approach is to study expectation formation in an experimental setting. In this paper we report the findings of a laboratory experiment about expectation formation in a simple asset pricing model. In this experiment we ask the participants to give their expectation of next period’s price of an unspecified risky asset. Submitting predictions is the only task for the participants. They do not have knowledge of the underlying market equilibrium equation, but they know all past realized prices and, of course, their own predictions. Their earnings are inversely related to the prediction error they make. Given the price forecast of a participant, a computer program computes the associated aggregate demand for the risky asset and subsequently the market equilibrium price. The realized price thus becomes a function of the individual forecasts. Our experiment is designed in order to obtain explicit information about expectations of participants in such a controlled expectations feedback environment.

As mentioned above, the experimental approach has certain advantages over survey data research. A first advantage is that the experimenters have control over the underlying fundamentals. Uncertainty about economic fun-

damentals affects expectations of agents in real markets. In the experiment we can control the economic environment and the information subjects have about this environment. In our experiment economic fundamentals are constant over time. Participants have perfect information about the mean dividend and the interest rate, and could use this information to compute the, constant, fundamental price. A second advantage is that we get explicit information about individual expectations. Since in our setup there is no trade, our data is not disturbed by speculative trading behavior, or by changes in the underlying demand and/or supply functions of the participants. Prior to the experiment the only unknown to the experimenters is the way subjects form expectations. Hence, our experimental approach provides us with ‘clean’ data on expectations.

We study an experimental asset pricing model with 6 participants and a small fraction of programmed ‘robot’ traders. These robot traders (henceforth called *fundamentalist traders*) always predict the fundamental price and trade on the basis of that prediction. Their presence stabilizes the asset price dynamics and inhibits the occurrence of speculative bubbles.

Our main findings are the following. Realized experimental asset prices differ significantly from the (constant) fundamental price. We observe different types of behavior. In some groups the price of the asset converges (slowly) to the fundamental price and in other groups there are large oscillations around the fundamental price. For some groups these oscillations have a decreasing amplitude and prices seem to converge to the fundamental price slowly; in other groups the amplitude of the oscillations is more or less constant over the duration of the experiment and there is no apparent convergence.

We are particularly interested in the *individual prediction strategies* used by the participants. Analysis of the predictions reveals that the dispersion between prediction strategies is much smaller than the forecast errors participants make on average. This indicates that participants within a group tend to *coordinate on a common prediction strategy*. Although participants make forecasting errors, they are similar in the way that they make these errors. Estimation of the individual prediction strategies shows that participants tend to use simple linear prediction strategies, such as naive expectations, adaptive expectations or ‘autoregressive’ expectations. Again, participants within a group seem to coordinate on using the same type of simple prediction strategy.

Although economic experiments are well suited for a detailed investigation of expectation formation in a controlled dynamic environment only little experimental work on expectation formation has been done. Williams (1987) considers expectation formation in an experimental double auction market

which varies from period to period by small shifts in the market clearing price. Participants predict the mean contract price for 4 or 5 consecutive periods. The participant with the lowest forecast error earns \$1.00. In Smith, Suchanek and Williams (1987) expectations are studied in a similar fashion. The drawback of the observations on expectations formation from these experiments is that they are obtained in market experiments where participants also have to trade and where the primary goal is to investigate aggregate behavior of market prices. A number of other laboratory experiments focus on expectation formation exclusively. Schmalensee (1976) presents subjects with historical data on wheat prices and asks them to predict the mean wheat price for the next 5 periods. Two other noteworthy experiments on expectation formation are Dwyer, Williams, Battalio and Mason (1993) and Hey (1994). In these papers a time series is generated by a random walk or a simple linear first order autoregressive process, respectively and participants have to predict the next realization, sequentially. The drawback of the last two papers is that no economic context is given. Most importantly, the main problem with all these experiments is that the expectations feedback is ignored. In our experiment we have explicitly accounted for this expectations feedback, which we believe to be very important for many economic environments, and especially for financial markets. Finally, Gerber, Hens and Vogt (2002) recently studied a repeated experimental beauty contest in which participants each period place either a buy or a sell order. Prices are determined by total market orders and noise. Although this is a positive feedback system like in our experiment, however, they don't measure explicitly expectations and their experimental environment is more stylized. They also find a high level of coordination.

The paper is organized as follows. Section 2 describes the design of the experiment and Section 3 discusses the underlying asset pricing model. Section 4 presents an analysis of the realized asset prices, whereas Section 5 focuses on the individual prediction strategies. Concluding remarks are given in Section 6.

## 2 Experimental design

In financial markets traders are involved in two related activities: *prediction* and *trade*. Traders make a prediction concerning the future price of an asset, and given this prediction, they make a trading decision. We designed an experiment that is exclusively aimed at investigating the way subjects form predictions. We solicit predictions from the subjects about the price of a certain asset for the next period. Given these predictions the computer



derives the associated individual demand for the asset and subsequently the market clearing price (i.e. the price at which aggregate demand equals aggregate supply). Each subject therefore acts as an advisor or a professional forecaster and is paired with one trader, which may be thought of as a large pension fund. The subject has to make the most accurate prediction for this trader and then the trader (i.e. the computer) decides how much to trade. The earnings of the subjects in the experiment are inversely related to their prediction error.

The experiment is presented to the participants as follows. The participants are told that they are an advisor to a pension fund and that this pension fund can invest its money in a risk free asset (a bank account) with a risk free gross rate of return  $R = 1 + r$ , where  $r$  is the real interest rate, or it can decide to invest its money in shares of an infinitely lived risky asset. The risky asset pays uncertain dividends  $y_t$  in period  $t$ . Dividends  $y_t$  are *IID* distributed with mean  $\bar{y}$ . The mean dividend  $\bar{y}$  and interest rate  $r$  are common knowledge. The task of the advisor (i.e. the participant) is to predict the price of the risky asset. Participants know that the price of the asset is determined by market equilibrium between demand and supply of the asset. Although they do *not* know the exact underlying market equilibrium equation they are informed that the higher their forecast is, the larger will be the fraction of money invested in the risky asset and the larger will be the demand for stocks. They do not know the investment strategy of the pension fund they are advising and the investment strategies of the other pension funds. The participants are not explicitly informed about the fact that the price of the asset depends on their prediction or on the prediction of the other participants. They also do not know the number of pension funds or the identity of the other members of the group.

The information for the participants is given in computerized instructions. Comprehension of the instructions is checked by two control questions. At the beginning of the experiment the participants are given two sheets of paper with a summary of all necessary information, general information, information about the stock market, information about the investment strategies of the pension funds, forecasting task of the financial advisor and information about the earnings. The handout also contains information about the financial parameters (mean dividend and risk free rate of return) with which an accurate prediction of the fundamental price can be made. Finally they are given a table from which they can read, for a given forecast error, their earnings (see Appendix C). Appendix B contains an English translation of the information given to the participants.

In every period  $t$  in the experiment the task of the participants is to predict the price  $p_{t+1}$  of the risky asset in period  $t + 1$ , given the avail-

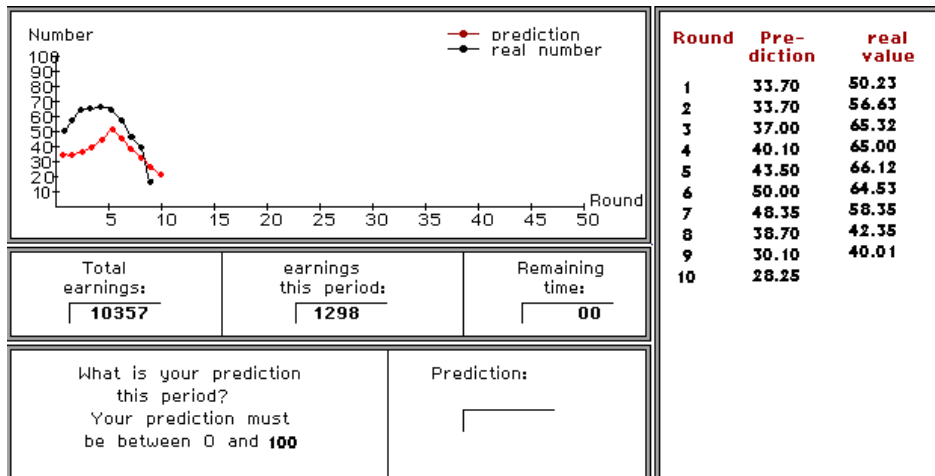


Figure 1: English translation of the computer screen as seen by the participants during the experiment. Predictions and prices have different colors.

able information. This information consist of past prices of the risky asset  $p_{t-1}, p_{t-2}, \dots, p_1$  and the participant his own past individual predictions  $p_{ht}^e, p_{h,t-1}^e, \dots, p_{h1}^e$ , where  $p_{h\tau}^e$  is the price participant  $h$  expects for period  $\tau$ . Subjects are told that their price forecast has to be between 0 and 100 for every period. In periods 1 and 2 no information about past prices is available. At the end of period  $t$ , when all predictions for period  $t + 1$  have been submitted, the participants are informed about the price in period  $t$  and earnings for that period are revealed. Figure 1 shows an English translation of the computer screen the participants are facing during the experiment. On the screen the subjects are informed about their earnings in the previous period, total earnings, a table of the last twenty prices and the corresponding predictions and a time series of the prices and the predictions.

The earnings of the participants consist of a “show-up” fee of 10 Dutch guilders (1 Dutch guilder is approximately 0.45 EURO) and of the earnings from the experiment which depended upon their forecasting errors. The number of points earned in period  $t$  by participant  $h$  is given by the (truncated) quadratic scoring rule

$$e_{ht} = \max \left\{ 1300 - \frac{1300}{49} (p_t - p_{ht}^e)^2, 0 \right\},$$

where 1300 points is equivalent to 1 Dutch guilder. Notice that earnings are zero in period  $t$  when  $|p_t - p_{ht}^e| \geq 7$ .<sup>1</sup>

<sup>1</sup>Paying participants according to quadratic forecast error is equivalent (up to a con-

An experimental asset market consists of 6 participants and a certain fraction of fundamentalist traders and it lasts for 51 periods. A total of 42 subjects (7 groups) participated in this experiment. Subjects (mostly undergraduates in economics, chemistry and psychology) were recruited by means of announcements on information boards in university buildings. The computerized experiment was conducted in the CREED laboratory. It lasted for approximately 1.5 hours and average earnings were 49.45 Dutch guilders (approximately 22.44 EURO).

### 3 The price generating mechanism

#### 3.1 The asset pricing model

The realized prices are generated by a standard asset pricing model with heterogeneous beliefs. For textbook treatments of this model see e.g. Cuthbertson (1996) or Campbell, Lo and MacKinlay (1997). Each trader can choose between investing his money in a risk free asset with a risk free gross rate of return  $R = 1 + r$  or investing his money in shares of an infinitely lived risky asset. The price of this risky asset in period  $t$  is  $p_t$ . For each share dividends  $y_t$  are paid out in period  $t$ . These dividends are assumed to be independently and identically distributed with mean  $\bar{y}$  and variance  $\sigma_y^2$ . The *fundamental value* (i.e. the discounted value of future dividends) of the risky asset is therefore equal to

$$p^f = \frac{\bar{y}}{r}.$$

The asset market is populated by 6 pension funds and a small fraction of fundamentalist traders, as discussed below. Each pension fund  $h$  is matched with a participant to the experiment and makes an investment decision at time  $t$  based upon this participant's prediction  $p_{h,t+1}^e$  of the asset price. The fundamentalist traders always predict the fundamental price  $p^f$  and make a trading decision based upon this prediction. Moreover, the fraction  $n_t$  of these fundamental traders in the market is endogenous and depends positively upon the absolute distance between the asset price and the fundamental value.<sup>2</sup> The greater this distance the more these fundamental traders will invest, and the other way around. These fundamentalist traders therefore

---

stant) with paying them according to risk-adjusted profit of the traders (for details see Hommes (2001)).

<sup>2</sup>This is similar to the model discussed in Brock and Hommes (1998) where the fraction  $n_{ht}$  of trader using prediction strategy  $h$  is also endogenous. In their paper this fraction depends positively upon past performance of the prediction strategy.

act as a ‘stabilizing force’ pushing prices in the direction of the fundamental price. Their presence therefore excludes the possibility of speculative bubbles in asset prices. DeGrauwe, DeWachter and Embrechts (1993) discuss a similar stabilizing force in an exchange rate model with fundamentalists and chartists. In the same spirit Kyle and Xiong (2001) introduce a long-term investor that holds a risky asset in an amount proportional to the spread between the asset price and its fundamental value.

The market clearing price is determined as follows. The amount of shares pension fund  $h$  wants to hold in period  $t$  depends positively upon the expected excess return  $p_{h,t+1}^e + \bar{y} - Rp_t$ . This means that an increase in the expected price of the asset for period  $t + 1$  leads to an increase in demand for the asset in period  $t$ . The market clearing price in period  $t$  is then given as (cf. Campbell, Lo and MacKinlay (1997), eq. 7.1.4 and Brock and Hommes (1998), eq. 2.7)

$$p_t = \frac{1}{1+r} [(1-n_t)\bar{p}_{t+1}^e + n_t p^f + \bar{y} + \varepsilon_t], \quad (1)$$

where  $\bar{p}_{t+1}^e = \frac{1}{6} \sum_{h=1}^6 p_{h,t+1}^e$  is the average predicted price for period  $t + 1$ . The current period’s asset price is therefore determined by (average) beliefs about next period’s asset price and an extra noise term  $\varepsilon_t$ , where the latter corresponds to (small) stochastic demand and supply shocks. Note that the realized price at time  $t$  is determined by the price predictions for time  $t + 1$ . Therefore, when traders have to make a prediction for the price in period  $t + 1$  they do not know the price in period  $t$  yet, and they can only use information on prices up till time  $t - 1$ .

In the experiment the risk free rate of return,  $r = 0.05$ , and the mean dividend,  $\bar{y} = 3$ , are fixed such that  $p^f = 60$ . Small demand and supply shocks  $\varepsilon_t$  are independently drawn from  $N(0, \frac{1}{4})$ . In order to be able to compare the different groups in the experiment, we used the same realizations of the demand and supply shocks for each group. Finally, the weight  $n_t$  of the fundamentalist traders is given by

$$n_t = 1 - \exp\left(-\frac{1}{200} |p_{t-1} - p^f|\right), \quad (2)$$

which indeed increases as the price moves away from the fundamental price. Notice that  $n_t = 0$  for  $p_{t-1} = p^f$ . Moreover, given  $p^f = 60$ , the weight of the fundamentalist traders is bounded above by  $\bar{n} = 1 - \exp(-\frac{3}{10}) \approx 0.26$ . The weight of the other traders is the same for each trader and equal to  $(1 - n_t)/6$ .

An important feature of the asset pricing model is its *self-confirming* nature: if all traders have a high (low) prediction the realized price will also

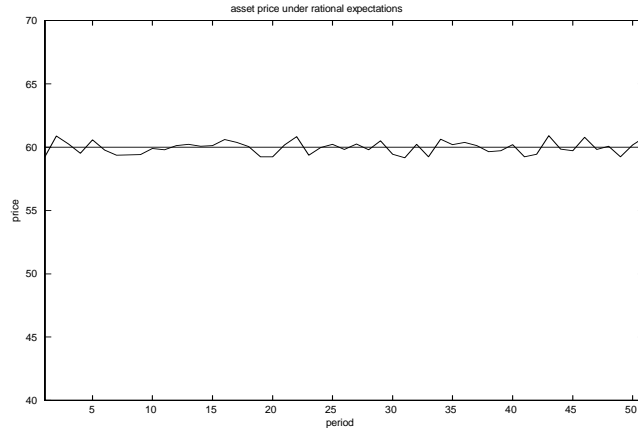


Figure 2: Asset price fluctuations when all participants have rational expectations and forecast  $p_{h,t+1}^e = p^f$ . The horizontal line at  $p^f = \bar{y}/r = 60$  denotes the fundamental value.

be high (low). This important feature is characteristic for a speculative asset market: if traders expect a high price, the demand for the risky asset will be high, and as a consequence the realized market price will be high, assuming that the supply is fixed.

### 3.2 Benchmark expectations rules

This subsection discusses some important benchmark expectations rules in the asset pricing model. In Sections 4 and 5 we will discuss which of these benchmarks gives a good description of the results from our asset pricing experiments. The development of the asset price depends upon the (subjective) expectations of the different trader types. Under rational expectations the subjective expectation  $E_{ht}$  of trader type  $h$  is equal to the objective mathematical conditional expectation  $E_t$ , for all  $h$ . Given that bubbles cannot occur in our framework this gives  $E_t p_{t+1} = p^f$ . Equation (1) then gives

$$p_t = p^f + \frac{1}{1+r} \varepsilon_t.$$

Therefore, under rational expectations  $p_t$  corresponds to independent drawings from the normal distribution with mean  $p^f = 60$  and variance  $(\sigma_\varepsilon/R)^2 = 5/21$ . Figure 2 shows the asset price under rational expectations for the realization of the demand and supply shocks that was used in the experiment.

The rational expectations hypothesis is quite demanding. It requires that participants know the underlying asset pricing model and use this to

compute the conditional expectation for the future price and that they do not make structural forecast errors. In particular, rational expectations requires knowledge about the beliefs of all other participants. It will only prevail when participants are able to coordinate on the rational expectations equilibrium.

Let us now consider asset price behavior when participants use simple forecasting rules instead of rational expectations. They do not have (exact) knowledge of the underlying model, but have their own beliefs about the development of asset prices and use this belief and the available time series observations to predict the price. The belief of a participant is sometimes called a *perceived law of motion*. Given those perceived laws of motion the price generating model is then referred to as the *implied actual law of motion*. The main objective of this paper is to get some insights into the nature of the perceived laws of motion people actually use. When participants have to predict a price for time  $t + 1$ , they know the interest rate  $r$  (which is constant over time), the mean dividend  $\bar{y}$ , the realized prices up to time  $t - 1$  and their own price predictions up to time  $t$ . A general form of a participant's forecasting rule or prediction strategy therefore is

$$E_{ht}(p_{t+1}) = p_{h,t+1}^e = f_h(p_{t-1}, p_{t-2}, \dots, p_1, p_{ht}^e, p_{h,t-1}^e, \dots, p_{h1}^e, \bar{y}, r), \quad (3)$$

where  $f_h$  can be any (possibly time-varying) function. There are no restrictions on the specification  $f_h$  and the possibilities are therefore unbounded. Given participants forecasting rules (3), the implied actual law of motion becomes

$$p_t = \frac{1}{R} \left[ \sum_{h=1}^6 (1 - n_t) f_h(p_{t-1}, \dots, p_1, p_{ht}^e, \dots, p_{h1}^e, \bar{y}, r) + n_t p^f + \bar{y} + \varepsilon_t \right].$$

The actual dynamics of prices is to a great extent characterized by the prediction strategies used by the traders. Depending on the prediction strategies used by the agents (which may, for example, be nonlinear or discontinuous) almost any type of price behavior can occur.

We will now briefly discuss the dynamics of our asset pricing model under a number of simple and well known expectation rules. Notice that, since participants know the values of  $\bar{y}$  and  $r$ , they have enough information to infer the fundamental value and predict it for any period, i.e. they can give  $p_{h,t+1}^e = p^f$  as a forecast, for all  $t$ .

The perhaps simplest expectations scheme corresponds to *static or naive expectations*, where

$$p_{h,t+1}^e = p_{t-1},$$

that is, the participant's prediction for the next price corresponds to the last observed asset price. Under the assumption that all traders have naive

expectations the price dynamics reduces to

$$p_t - p^f = \frac{1 - n_t}{1 + r} (p_{t-1} - p^f) + \frac{1}{1 + r} \varepsilon_t.$$

It can be easily seen that in this case prices will converge to the neighborhood of the fundamental price (see the left panel of Figure 3). Moreover, in the absence of any stochastic demand and supply shocks, prices converge monotonically to the fundamental price. This also holds true for another well known prediction strategy, *adaptive expectations*, which corresponds to

$$p_{h,t+1}^e = w p_{t-1} + (1 - w) p_{ht}^e = p_{ht}^e + w (p_{t-1} - p_{ht}^e),$$

where  $0 < w \leq 1$ . Hence, under adaptive expectations the prediction is adapted in the direction of the last observed price. The weight parameter  $w$  determines how fast predictions are updated. Notice that naive expectations corresponds to a special case of adaptive expectations, where  $w = 1$ .

We conclude this discussion on prediction strategies by looking at the class of linear autoregressive prediction strategies with 2 lags, that is

$$p_{h,t+1}^e = \alpha_h + \beta_{h1} p_{t-1} + \beta_{h2} p_{t-2}. \quad (4)$$

We will refer to (4) as the *AR(2)* prediction rule. Notice that the endogeneity of the fraction of fundamentalist traders  $n_t$  introduces a nonlinearity in the price generating mechanism (1), even if all prediction strategies are linear. Now let  $\beta_l = \frac{1}{6} \sum_{h=1}^6 \beta_{hl}$ , for  $l = 1, 2$ . Depending on the values of  $\beta_1$  and  $\beta_2$  one can have different types of dynamics. In particular, if  $\beta_1^2 + 4R\beta_2 < 0$  the price will oscillate around the steady state price. In the absence of stochastic demand and supply shocks, these oscillations will converge to the steady state if  $\beta_2 > -R$ , but they will converge to a limit cycle when  $\beta_2 < -R$ . On the other hand, if  $\beta_1^2 + 4R\beta_2 > 0$ , the prices move monotonically or jump up and down, one period below the steady state and the next period above the steady state. If  $|\beta_1| + |\beta_2| < R$ , these price movements converge to the steady state.

The *AR(2)* prediction strategy (4) can be rewritten as

$$p_{h,t+1}^e = \alpha + \beta p_{t-1} + \delta (p_{t-1} - p_{t-2}),$$

where  $\beta \equiv \beta_1 + \beta_2$  and  $\delta \equiv -\beta_2$ . Expressed in this way it provides a nice intuition. Participants believe that the price will be determined by the last observation (the first two terms on the right-hand side) but they also try to follow the *trend* in the prices (expressed in the third term): if  $\delta > 0$  they believe that an upward movement in prices will continue the next period,

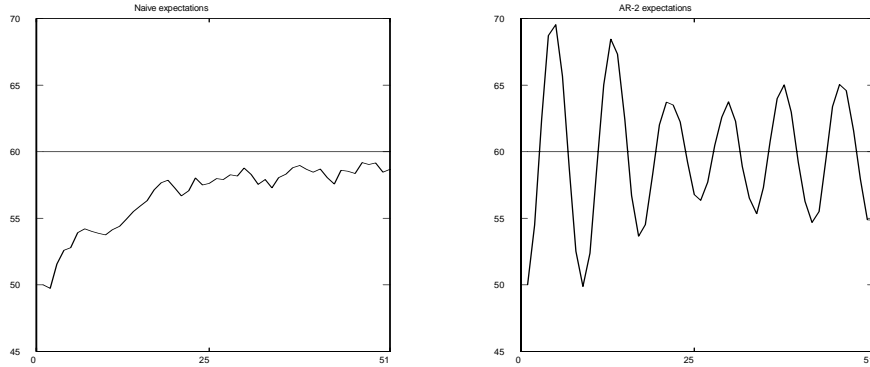


Figure 3: The realized price if all participants use naive expectations (left panel) or  $AR(2)$  expectations  $p_{h,t+1}^e = 30 + \frac{3}{2}p_{t-1} - p_{t-2}$  (right panel).

whereas if  $\delta < 0$  they believe an upward movement in the prices will be (partially) offset by a downward movement in prices in the next period. The former correspond to *trend chasers* or *positive feedback traders*, whereas the latter correspond to so-called *contrarians*.

The left panel of Figure 3 shows the evolution of the realized price if everybody in the experiments uses naive expectations, the right panel of Figure 3 shows what happens if everybody uses  $AR(2)$  expectations  $p_{h,t+1}^e = 30 + \frac{3}{2}p_{t-1} - p_{t-2}$ . For both cases we assumed that  $p_{h1} = p_{h2} = 50$ , for all  $h$ . Furthermore, we used the same realization of demand and supply shocks  $\varepsilon_t$  as in the experiment.

## 4 Aggregate behavior of asset prices

Figure 4 shows the realized asset prices in the experiment for the seven groups. The horizontal line in the graphs corresponds to the fundamental price of 60.

We can classify the different groups in three different categories:

- i) *monotonic convergence*: the price in groups 2 and 5 seems to converge monotonically to the fundamental price from below;
- ii) *converging oscillations*: the price in groups 4 and 7 oscillates around the fundamental price but the amplitude of the oscillations decreases over time indicating convergence to the fundamental price; and



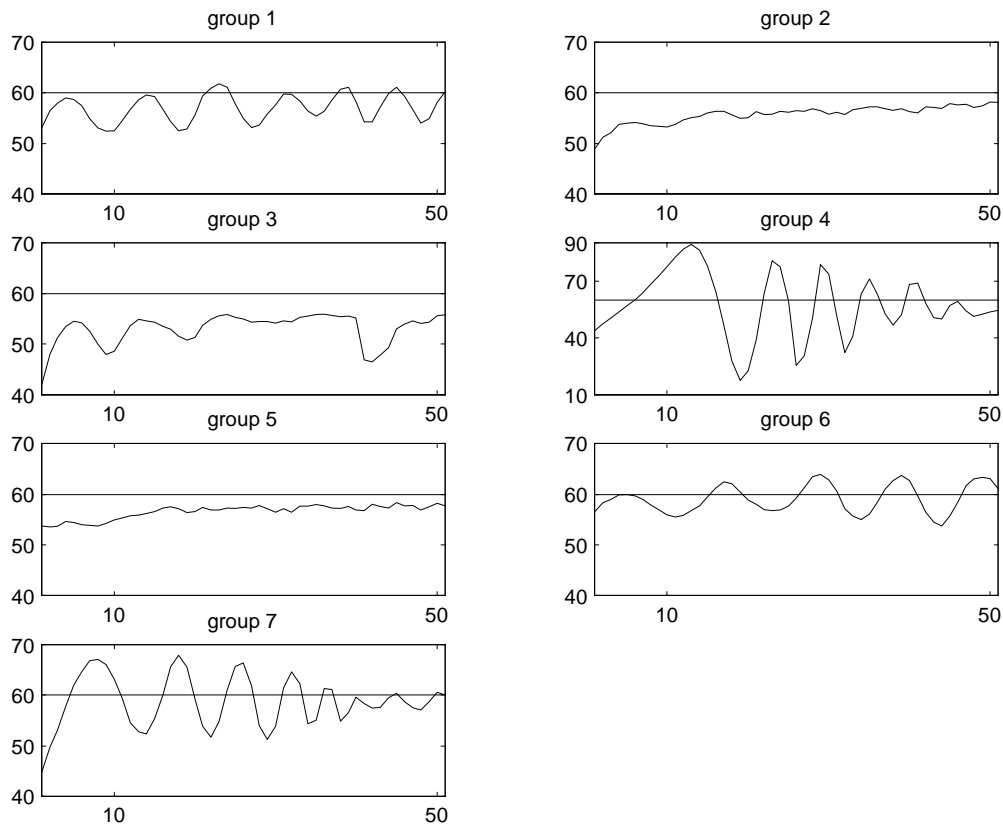


Figure 4: Realized prices for the different groups. The vertical lines at  $p = 60$  correspond to the fundamental price.

- iii) *persistent oscillations*: the price in groups 1 and 6 oscillates but the amplitude of this oscillations is more or less constant. In these groups there does not seem to be convergence to the fundamental price.

Group 3 is more difficult to classify, it starts out with oscillations, but from a certain period on there seems to be monotonic convergence to the fundamental price.<sup>3</sup>

Comparing Figure 4 with Figures 2 and 3 one observes that realized prices under the naive expectations benchmark resemble realized prices in groups 2

<sup>3</sup>The sudden fall of the asset price in group 3 from 55.10 in period 40 to 46.93 in period 41 is due to the fact that one of the participants predicts 5.25 for period 42. It is likely that this corresponds to a typing error (maybe his/her intention was to type 55.25), since this participants' 5 previous predictions all were between 55.00 and 55.40, giving him/her the very high average earnings of 1292 out of 1300 points in these periods.

and 5 of the experiment remarkably well. On the other hand, the oscillatory behavior of the realized price in groups 1, 4, 6 and 7 in the experiment is qualitatively similar to the asset price behavior when participants use  $AR(2)$  prediction strategies. Clearly, naive and  $AR(2)$  prediction strategies give a qualitatively much better description of aggregate asset price fluctuations in the experiment than does the benchmark case of rational expectations.

Mean and variance						
	1-25		26-51		1-51	
	sample average	sample variance	sample average	sample variance	sample average	sample variance
group 1	56.66	8.67	57.26	6.09	56.97	7.30
group 2	54.44	3.20	56.88	0.43	55.68	3.28
group 3	52.26	10.06	53.73	7.70	53.01	9.23
group 4	60.64	408.15	54.19	162.39	57.35	287.70
group 5	55.68	2.05	57.48	0.24	56.60	1.93
group 6	58.43	3.65	59.81	10.82	59.13	7.65
group 7	58.99	41.22	58.63	12.16	58.81	25.90
RE	59.95	0.23	59.97	0.24	59.96	0.23
Naive	54.98	5.78	58.38	0.24	56.71	5.84
$AR(2)$	59.88	35.03	59.76	12.59	59.77	23.12

Table 1: Mean and variance of realized asset prices

Table 1 shows the sample average and sample variance of realized prices for the whole interval of 51 periods and for two subintervals of 25 and 26 periods, for the 7 groups. The table also reports sample averages and sample variances of three important benchmarks discussed in Section 3 (they are denoted RE, Naive and  $AR(2)$ , respectively). Inspection of Table 1 confirms our earlier conclusion: naive expectations or  $AR(2)$  expectations gives a much better description of aggregate price behavior than does rational expectation. Comparing the rational expectations benchmark with the 7 experimental groups, we see for almost all (sub)intervals that the sample average is lower and the sample variance is higher in the experiment than under rational expectations. From this we conclude that in this experimental asset pricing model we have *i) undervaluation* of the asset; *ii) excess volatility* of the asset prices. Moreover, sample average and variance of the realized prices are more in line with those of naive and  $AR(2)$  expectations. In terms of sample mean and sample variance naive and  $AR(2)$  expectations yield much better results than rational expectations.

The undervaluation of the asset can be explained as follows. We have restricted prices to lie between 0 and 100. Since agents have no prior information about the price generating process, many initial guesses lie around 50. Most of the initial guesses will therefore be smaller than the fundamental price of 60. In fact, the first realized price  $p_1$  is 48.96 on average (averaged over groups), whereas the final realized price  $p_{51}$  is 58.18 on average.<sup>4</sup> So, the undervaluation actually (slowly) disappears as time goes by. Also the volatility of prices decreases over time. In particular for the groups where there is slow but steady convergence to the fundamental price, the variance in the second subinterval approaches the variance under rational expectations.

As a final remark on the realized asset prices we note that the influence of the fundamentalist traders on the asset pricing dynamics seems to be limited. In all groups but group 4 the maximum weight of the fundamentalist traders is below 0.087, implying that the weight of each of the participants fluctuates between 0.167 and 0.152. For most of these groups the weight of the fundamental traders takes its maximum value at the start of the experiment. Only in group 4 the fundamentalist traders seem to have a significant impact. In period 13 (at the first peak) their weight is 0.136 and in period 19 (at the first dale) their weight is 0.191, decreasing the weights of the other traders to 0.135. Hence, in this group at times the weight of the fundamentalist traders is similar in magnitude to the weights of the participants and the fundamentalist traders seem to have stabilized the dynamics in this group. In all other groups the impact of the fundamentalist traders is small.

## 5 Individual prediction strategies

We now turn to the individual prediction strategies of the participants in our asset pricing experiment. In Subsection 5.1 we show that participants tend to coordinate on a common prediction strategy. Subsection 5.2 discusses earnings per group. Subsection 5.3 investigates whether participants use the available information efficiently. Finally, in Subsection 5.4 we present results on characterising and estimating the individual prediction strategies.

### 5.1 Coordination

Figure 5 shows, per group, the predictions of all participants. A striking feature of Figure 5 is that different participants seem to *coordinate* on some

---

<sup>4</sup>Our conjecture is that if we would have picked the interest rate and the mean dividend such that the fundamental price would be below 50 the asset would be overvalued during the experiment.

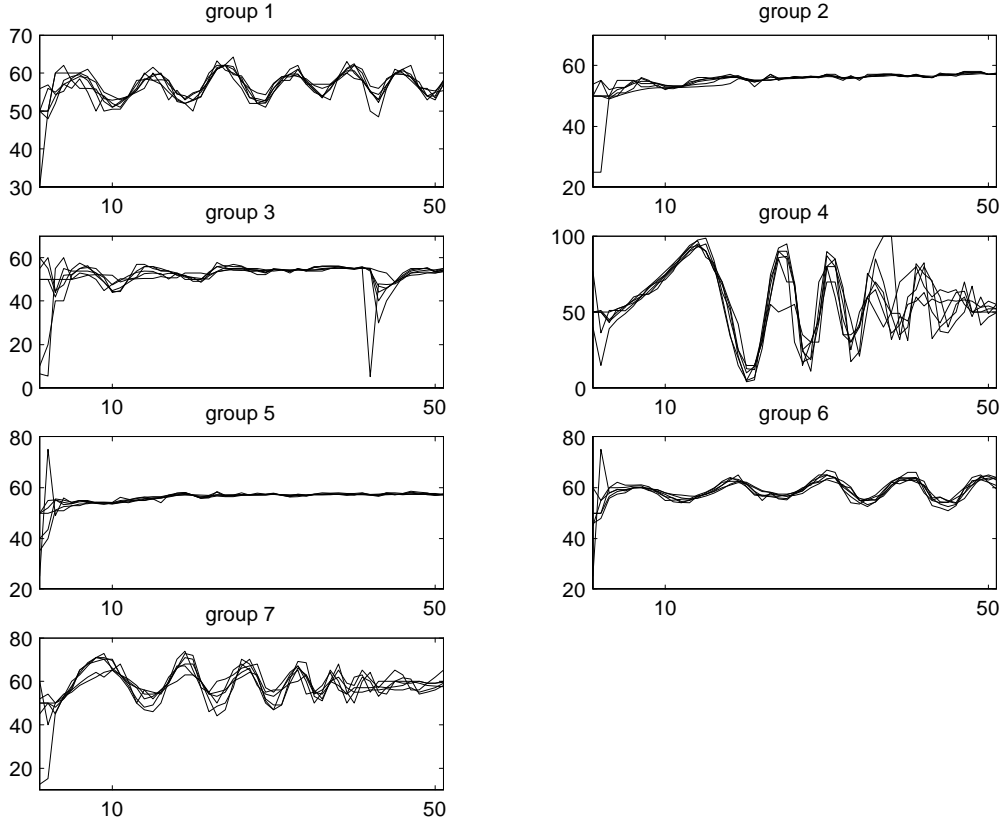


Figure 5: Individual predictions per group.

common prediction strategy. This coordination of expectations is obtained in all seven groups.

In order to quantify this coordination on a common prediction strategy we consider, for each group, the *average individual quadratic forecast error*

$$\frac{1}{6 \times 40} \sum_{h=1}^6 \sum_{t=11}^{40} (p_{ht}^e - p_t)^2,$$

which corresponds to the individual quadratic forecast error averaged over time and over participants within a group. Note that the first 10 observations are neglected in order to allow participants to learn how to predict prices accurately. Defining  $\bar{p}_t^e = \frac{1}{6} \sum_{h=1}^6 p_{ht}^e$  as the average prediction for period  $t$  in a group (averaged over individuals in that group) we find that the average individual quadratic forecast error can be broken up into two separate terms,

as follows

$$\frac{1}{6 \times 40} \sum_{h=1}^6 \sum_{t=11}^{50} (p_{ht}^e - p_t)^2 = \frac{1}{6 \times 40} \sum_{h=1}^6 \sum_{t=11}^{50} (p_{ht}^e - \bar{p}_t^e)^2 + \frac{1}{40} \sum_{t=11}^{50} (\bar{p}_t^e - p_t)^2. \quad (5)$$

The first term on the right-hand side of (5) measures the *dispersion between individual predictions*. It gives the distance between the individual prediction and the average prediction  $\bar{p}_t^e$  within the group, averaged over time and participants. Note that it equals 0 if and only if all participants, in one group, use exactly the same prediction strategy. Hence, this term measures deviation from coordination on a common prediction strategy. The second term on the right-hand side of (5) measures the average distance between the mean prediction  $\bar{p}_t^e$  and the realized price  $p_t$ . If individual expectations can be described as “rational expectations with error”, where the error has mean zero and is serially uncorrelated and uncorrelated with the errors of the other participants, then we should expect that individual forecast errors cancel each other out in the aggregate. This is consistent with Muth (1961) who gives the following formulation of the rational expectations hypothesis (p.316):

*“The hypothesis can be rephrased a little more precisely as follows: that expectations of firms (or, more generally, the subjective probability distribution of outcomes) tend to be distributed, for the same information set, about the prediction of the theory (or the “objective” probability distributions of outcomes).”*

In other words, individual expectations may be wrong, but in the aggregate expectations should be approximately correct. If this is the case then this second term should be relatively small.

Table 2 shows, for each of the seven groups, how the average quadratic forecast error is broken up in these two terms.<sup>5</sup>

From inspection of Table 2 it is clear that only a relatively small part (ranging from 20% in group 1 to 38% in group 3) of the average quadratic forecasting error (first column) can be explained by the dispersion in expectations (second column). This confirms our conjecture that there is coordination on a common prediction strategy. The observation that a relatively large part of the average quadratic forecast error is due to the difference between the average expectation and the realized price (third column) implies that

---

<sup>5</sup>For group 3, we have excluded the observation at time  $t = 42$ , where one of the participants appeared to make a typing error (see footnote 2), which has a big impact on these measures. If we include this observation we get 15.70, 11.10 and 4.60, respectively.

	avg. individual error	avg. dispersion error	avg. common error
group	$\frac{1}{240} \sum_{h,t} (p_{ht}^e - p_t)^2$	$\frac{1}{240} \sum_{h,t} (p_{ht}^e - \bar{p}_t^e)^2$	$\frac{1}{40} \sum_t (\bar{p}_t^e - p_t)^2$
1	6.38	1.28 (20%)	5.10 (80%)
2	0.77	0.19 (25%)	0.58 (75%)
3	7.58	2.86 (38%)	4.72 (62%)
4	325.77	93.21 (29%)	232.56 (71%)
5	0.55	0.11 (20%)	0.44 (80%)
6	5.15	1.24 (24%)	3.91 (76%)
7	24.76	8.52 (34%)	16.24 (66%)

Table 2: Different measures for the individual prediction strategies

“rational expectations with error” is not a good description of participants’ expectation formation. In fact, it suggests that participants’ mistakes are correlated. We therefore conclude that participants make significant forecasting errors, but they are alike in the way that they make these forecasting errors.

## 5.2 Earnings

Comparing Figure 5 with Figure 4 suggests that the participants are performing quite well. Table 3 shows the earnings from predicting per group. Note that participants in groups 4 and 7 earn a relatively small amount, whereas participants in groups 2 and 5 make substantial earnings, close to the maximum. The prices in groups 2 and 5 are not equal to the fundamental price (the only rational expectation price) but the earnings in these groups are almost as high as earnings of rational forecasters. In this sense the behavior of these subjects can be considered as ‘close’ to rational. To some extent the same can be said about the other groups with the exception of groups 4 and 7. These last groups show a relatively high price volatility.

Earnings in Dutch guilders								
group	1	2	3	4	5	6	7	average
earnings	43.73	49.36	41.58	15.91	49.03	44.77	31.74	39.45

Table 3: Earnings by group. When all participants predict the fundamental price average earnings per groups would be around 50.75.

### 5.3 Informational efficiency

The analysis of Table 2 suggests that participants make structural forecast errors. However, if participants are rational their forecast error should be uncorrelated with available information. To test whether participants are rational in this sense, we computed, for each participant, the first 10 lags of the autocorrelation function of the time series of forecast errors  $p_t - p_{ht}^e$ , where we only used the last 40 observations. The significant lags are presented in Table 4.

	group 1	group 2	group 3	group 4	group 5	group 6	group 7
1	1-3-4-7-8	1-2	–	1-3-4	1	1-4-5-6-9-10	1
2	1-3-4-8	–	–	1-3-4	2	1-4-5-6-9-10	1-2-3
3	1-3-4-5	1	1	1-3-6	–	1-4-5-6-10	1-2-3-8
4	1-3-4-7-8	1	1-2	1-3-4-6	–	1-4-5-10	1-3-4-8
5	1-3-4-7	1	1	1-3-4	2	1-4-5-6-9-10	1-2-3
6	1-3-4-5-7-8	2	1	1-3-8	1-8	1-4-5-6-9-10	1-3-4-8

Table 4: Autocorrelation structure in individual forecast errors

Notice that the autocorrelation function of the forecast errors is significant at the first lag for many participants. However, participants do *not* have  $p_t$  in their information set, when predicting  $p_{t+1}$ . Hence, they are not able to exploit the first order autocorrelation structure in the forecast errors to improve their predictions. Therefore one should ignore the significant first order lags and focus on higher order lags of the autocorrelation function. We thus find that for about one third of the participants there is no exploitable (linear) structure in the forecast errors at all. Ignoring the first lag, we note that the second lag is only significant for 8 out of the 42 participants. Stated differently, the most easily detected linear structure has been exploited efficiently by 34 participants. Notice that most structure in the forecast errors can be found in the groups where the realized price oscillates around the fundamental price. Furthermore, there is much similarity between the autocorrelation structure of participants within a group, again indicating that participants in the same group seem to coordinate on a common prediction strategy.

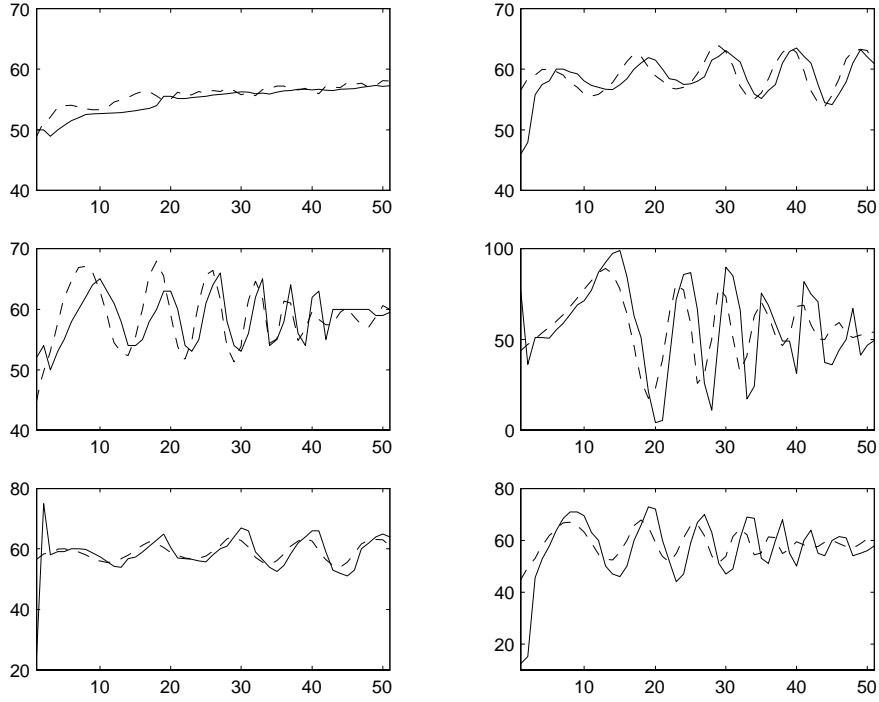


Figure 6: Predictions and realized prices. Solid lines correspond to individual predictions, dashed lines correspond to realized price. Upper left panel: participant 1 in group 2, upper right panel: participant 6 in group 6, middle left panel: participant 4 in group 7, middle right panel: participant 3 in group 4, lower left panel: participant 2 in group 6 and lower right panel: participant 3 in group 7.

#### 5.4 Characterising and estimating individual prediction strategies

We will now try to characterize the individual prediction strategies. Some participants try to extrapolate certain trends and by doing so overreact and predict too high or too low. Other participants are more cautious when submitting predictions. When prices are rising (declining) they usually predict a price lower (higher) than the actual price. Examples of the latter are participant 1 in group 2, participant 6 in group 6 and participant 4 in group 7 in Figure 6.(a)-(c). Figure 6.(d)-(f) shows three examples of trend extrapolators, participant 3 in group 4, participant 2 in group 6 and participant 3 in group 7. These prediction strategies exhibit an *overreaction* of predictions with respect to trends in prices.



The individual degree of overreaction can be quantified as follows. Table 5 shows, for each group, the average absolute (one-period) change in predictions of participant  $h$ ,

$$\Delta_h^e = \frac{1}{40} \sum_{t=11}^{50} |p_{ht}^e - p_{h,t-1}^e|.$$

The average change in the price,  $\Delta = \frac{1}{40} \sum_{t=11}^{50} |p_t - p_{t-1}|$ , and the average change in predictions per group  $\bar{\Delta}^e = \frac{1}{6} \sum_{h=1}^6 \Delta_h^e$  are also reported. We will say that individual  $h$  *overreacts* if  $\Delta_h^e > \Delta$  and we will say that individual  $h$  is *cautious* if  $\Delta_h^e \leq \Delta$ .

	group 1	group 2	group 3	group 4	group 5	group 6	group 7
$\Delta_1^e$	2.34	0.17	2.96	13.10	0.27	1.57	2.89
$\Delta_2^e$	1.60	0.65	2.39	11.37	0.49	2.27	3.63
$\Delta_3^e$	2.20	0.37	1.63	16.98	0.30	1.92	6.01
$\Delta_4^e$	1.65	0.45	0.62	16.26	0.30	1.72	2.99
$\Delta_5^e$	2.56	0.41	1.31	12.80	0.53	1.78	4.88
$\Delta_6^e$	2.24	0.57	1.44	13.78	0.46	1.31	4.07
$\bar{\Delta}^e$	2.10	0.44	1.73	14.05	0.39	1.76	4.08
$\Delta$	1.83	0.43	0.97	10.39	0.47	1.44	3.09

Table 5: Individual and average degrees of overreaction

The table measures the *degree of overreaction*. For a majority of participants in groups 1, 3, 4, 6 and 7 the individual degrees of overreaction are higher than the changes in the realized prices. Oscillatory behavior is thus caused by overreaction of a majority of agents. In groups 2 and 5 the changes in predictions are similar to the changes in prices. Convergence to the fundamental price occurs when a majority of traders is ‘cautious’.

The final step in our analysis of the individual prediction strategies is to try to estimate simple forecasting rules. The prediction strategies of all 42 participants can be described by the following general simple linear model

$$p_{h,t+1}^e = \alpha_h + \sum_{i=1}^4 \beta_{hi} p_{t-i} + \sum_{j=0}^3 \gamma_{hj} p_{ht-j}^e + \nu_t, \quad (6)$$

where  $\nu_t$  is an independently and identically distributed noise term. Notice that this general structure includes several interesting special cases: *i)*

naive expectations ( $\beta_{h1} = 1$ , all other coefficients equal to 0); *ii*) adaptive expectations ( $\beta_{h1} + \gamma_{h0} = 1$ , all other coefficients equal to 0) and *iii*)  $AR(L)$  processes (all coefficients equal to 0, except  $\alpha_h, \beta_{h1}, \dots, \beta_{hL}$ ). We estimated (6) for all 42 participants, using observations from  $t = 11$  to  $t = 51$ . The estimation results can be found in Tables 7 and 8 in Appendix A. These results are qualitatively summarized in Table 6.

	$AR(1)$ (Naive)	$AR(2)$	$AR(3)$	Adaptive	Other
group 1	0	5	0	0	$B(4, 2)$
group 2	4(3)	0	0	1	$B(1, 2)$
group 3	2	3	0	1	–
group 4	0	3	1	0	$B(3, 1), B(4, 3)$
group 5	3	1	0	1	$B(2, 1)$
group 6	0	5	0	0	$B(2, 2)$
group 7	0	4	1	0	$B(1, 2)$
total	9	21	2	3	7

Table 6: Estimation results for individual prediction strategies

Here  $B(k, l)$  refers to a prediction strategy where the first  $k$  lags of the price and the first  $l$  lags of the prediction are significant in the regression. We find 9 participants with  $AR(1)$  beliefs (of which 3 participants use naive expectations), 21 participants with  $AR(2)$  beliefs, 2 participants with  $AR(3)$  beliefs and 3 participants with adaptive beliefs.<sup>6</sup> The remaining 7 participants use more complicated prediction rules. Notice that the  $AR(1)$  and adaptive rules are all found in groups 2, 3 and 5, and the  $AR(2)$  and  $AR(3)$  rules are all found in groups 1, 3, 4, 6 and 7. This is consistent with the finding that in groups 2 and 5 the price seems to converge monotonically and that in groups 1, 4, 6 and 7 the price oscillates around some steady state. Group 3 takes a somewhat special position, starting out with oscillations and ending with monotonic convergence to the fundamental price. Prediction strategies within groups are more similar than strategies between groups which is consistent with the finding that participants within one group seem to coordinate on a common prediction strategy.

<sup>6</sup>We arrive at the naive and adaptive expectations strategies in the following way. For the  $AR(1)$  processes we tested the joint hypothesis  $\alpha_h = 0$  and  $\beta_{h1} = 1$  (naive expectations). For processes where only the coefficients on  $p_{t-1}$  and  $p_{ht}^e$  are significant we tested the joint hypothesis  $\alpha_h = 0$  and  $\beta_{h1} + \gamma_{h0} = 1$  (adaptive expectations).

The  $AR(2)$  prediction strategy can be rewritten as a trend following rule

$$p_{h,t+1}^e = \alpha_h + \beta_h p_{t-1} + \delta_h (p_{t-1} - p_{t-2}),$$

where  $\beta_h \equiv \beta_{h1} + \beta_{h2}$  and  $\delta_h \equiv -\beta_{h2}$ . For all of the 18  $AR(2)$  prediction strategies in the “oscillating” groups (1, 4, 6 and 7) we have  $\widehat{\beta}_{h1} > 0$  and  $\widehat{\beta}_{h2} < 0$ . The latter inequality is equivalent with  $\delta_h > 0$ , which implies that all these participants try to follow the trend: they expect that a recent upward (or downward) movement in prices will continue in the near future. These participants therefore correspond to so-called *positive feedback traders*. Another interesting feature is that for the estimated  $AR(2)$  strategies in the (oscillating) groups the variation in  $\widehat{\beta}_{h1} + \widehat{\beta}_{h2}$  seems to be lower than the variation in  $\widehat{\beta}_{h2}$ . This suggest that participants within a group have the same value of  $\beta_h = \beta_{h1} + \beta_{h2}$  but have different values of the trend coefficient  $\delta$ . We tested this hypothesis for the 5 relevant groups. Only for groups 1 and 4 we cannot reject the hypothesis that  $\beta_h = \beta_{h1} + \beta_{h2}$  is the same for all  $h$ .

In order to characterize the different estimated prediction strategies, we can determine, for each of them, what happens if all participants in a group use that estimated prediction strategy. Recall that in this experiment, even if all participants use linear prediction rules, the asset price dynamics will be a nonlinear dynamical system because the weight  $n_t$  of the fundamentalist traders changes over time. We find that 8 of the estimated  $AR(2)$  prediction strategies (3 in group 1, 1 in group 4, 3 in group 6 and 1 in group 7) are locally unstable and lead to persistent oscillations in the asset prices, if used by all participants in a group.<sup>7</sup> Two of the  $AR(1)$  rules (1 in group 2 and 1 in group 3) are stable but lead to a very different steady state price when used by all participants in a group.<sup>8</sup> Moreover, if these  $AR(1)$  rules are used by all participants in a group without fundamentalist traders and without an upper limit on predictions and asset prices, exploding bubbles emerge.

The estimated rules can also be used to get some insight in the following questions: what happens *i)* in the long run; *ii)* in the absence of fundamentalist traders. In order to investigate these issues we did the following numerical exercises. For each group the estimated individual prediction strategies were programmed and the experiment was ran with these programmed prediction strategies. First this experiment was ran for more than 50 periods to investigate long run behavior. For each group we find that realized asset price stabilize close to the fundamental value. Secondly, we investigated what

<sup>7</sup>Recall from Section 3 that an  $AR(2)$  rule is locally unstable and leads to oscillating behavior when  $\beta_1^2 + 4R\beta_2 < 0$  and  $\beta_2 < -R$ .

<sup>8</sup>Recall from Section 3 that an  $AR(1)$  rule is locally unstable when  $\beta_1 > R$ .

would happen in the absence of fundamentalist traders. Also here we found, for all groups, convergence to a steady state close to the fundamental price. Of course, analyses like these have to be considered with care, since we use the estimated prediction strategies in a context which is different from the context where they were used by the participants.

One final remark is in order. From the estimation results we should not draw the conclusion that these prediction strategies are typical for the different individuals, in the sense that these individuals will use the same rule in another context as well. Actually, participants coordinate on some kind of behavior and this behavior becomes self-fulfilling: the estimated relationships are consistent with that behavior.

## 6 Concluding Remarks

In this paper we investigated expectation formation in a simple experimental asset pricing model. Each market is populated by six participants and a certain fraction of fundamentalist traders. We observe slow and monotonic convergence to the fundamental price, as well as regular oscillations around the fundamental price. In most groups the asset is undervalued and exhibits excess volatility. Simple expectation schemes (or *popular models* (Shiller (1990)) such as naive expectations or autoregressive expectations give a much better description of aggregate market behavior than do rational expectations. From the analysis of the individual prediction strategies we find that participants within a group tend to coordinate on a common prediction strategy. Moreover, these popular models can be estimated rather accurately, and this reveals that participants indeed tend to use simple (linear) forecasting models.

In Hommes, Sonnemans, Tuinstra and van de Velden (2002) we studied expectation formation in a slightly different designed asset pricing experiment. There we also found that participants tend to coordinate on a common prediction strategy. This coordination of expectations therefore seems to be a robust result in these asset pricing experiments.

Let us finally try to develop an intuition for the emergence of expectational coordination. Participants in these experiments have an incentive to coordinate their prediction strategies, since the market clearing price is close to the average prediction. Participants who succeed in predicting the average prediction well, perform well in the experiment. This feature of the asset pricing experiment may be similar to real asset markets, and is consistent with the ideas of Keynes (1936, p.156) who, in a much quoted passage, compared behavior of traders in financial markets to so-called *beauty contests*:

*“[P]rofessional investment may be likened to those newspaper competitions in which the competitors have to pick out the six prettiest faces from a hundred photographs, the prize being awarded to the competitor whose choice most nearly corresponds to the average preferences of the competitors as a whole; so that each competitor has to pick, not those faces which he himself finds prettiest, but those which he thinks likeliest to catch the fancy of the other competitors, all of whom are looking at the problem from the same point of view. .... [W]e devote our intelligences to anticipating what average opinion expects the average opinion to be.”*

From our experiments we find that participants are rather successful in “anticipating what average opinion expects the average opinion to be”.

It is illuminating to compare our results with those of van de Velden (2001), who uses the experimental approach to investigate expectation formation in a ‘cobweb’ commodity market with a supply response lag. He shows that, for an unstable cobweb model, the heterogeneity of expectations leads to excess volatility of realized prices but there does not seem to be any coordination on a common prediction strategy. An important difference between the asset pricing model discussed here and the cobweb model is the way in which expectations play a role in the model. The asset pricing model has an *expectations confirming* structure, which means that if people expect the price of the asset to increase it will indeed increase. We have already argued that this gives participants an incentive to coordinate on similar prediction strategies. On the other hand, the cobweb model has an *expectations reversing* structure: if a high price is expected, firms will produce a lot and by the equality of demand and supply the realized market equilibrium price will then be low. This structure is detrimental to coordination because, when most participants submit a prediction which lies above (below) the fundamental price, then it pays off to give a prediction below (above) the fundamental price. Market institutions therefore seem to play an important role in the emergence of coordination of expectations. Our results suggest that in speculative asset markets coordination on a trend may lead to (temporary) deviations from fundamentals.

## References

- [1] Brock, W.A. and C.H. Hommes, 1998, “Heterogeneous Beliefs and Routes to Chaos in a Simple Asset Pricing Model,” *Journal of Economic Dynamics and Control*, **22**, 1235-1274.

- [2] Campbell, J.Y., A.W. Lo and A.C. MacKinlay, 1997, *The Econometrics of Financial Markets*. Princeton: Princeton University Press.
- [3] Cuthbertson, K., 1996, *Quantitative Financial Economics: Stocks, Bonds and Foreign Exchange*. Chichester: Wiley.
- [4] DeGrauwe, P., H. DeWachter and M. Embrechts, 1993, *Exchange Rate Theory. Chaotic Models of Foreign Exchange Markets*. Oxford: Blackwell.
- [5] Dwyer, G.P., A.W. Williams, R.C. Battalio and T.I. Mason, 1993, "Tests of Rational Expectations in a Stark Setting," *Economic Journal*, **103**, 586-601.
- [6] Frankel, J.A. and K.A. Froot, 1987, "Using Survey Data to Test Standard Propositions Regarding Exchange Rate Expectations," *American Economic Review*, **77**, 133-153.
- [7] A. Gerber, T. Hens and B. Vogt, 2002, "Rational Investor Sentiment," Working Paper No. 126, Institute for Empirical Research in Economics, University of Zurich.
- [8] Hommes, C.H., 2001, "Financial Markets as Nonlinear Adaptive Evolutionary Systems," *Quantitative Finance*, **1**, 149-167.
- [9] Hommes, C.H., J. Sonnemans, J. Tuinstra and H. van de Velden, 2002, "Expectations and Bubbles in an Asset Pricing Experiments," CeNDEF Working Paper WP 02-05, University of Amsterdam.
- [10] Keynes, J.M., 1936, *The General Theory of Interest, Employment and Money*. London: Macmillan.
- [11] Kyle, A.S. and W. Xiong, 2001, "Contagion as a Wealth Effect," *Journal of Finance*, **56**, 1401-1440.
- [12] Schmalensee, R., 1976, "An Experimental Study of Expectation Formation," *Econometrica*, **44**, 17-41.
- [13] Shiller, R.J., 1990, "Speculative Prices and Popular Models," *Journal of Economic Perspectives*, **4**, 55-65.
- [14] Smith, V.L., G.L. Suchanek and A.W. Williams, 1988, "Bubbles, Crashes and Endogenous Expectations in Experimental Spot Asset Markets," *Econometrica*, **56**, 1119-1151.

- [15] van de Velden, H., 2001, *An Experimental Approach to Expectation Formation in Dynamic Economic Systems*. Dissertation, University of Amsterdam.
- [16] Williams, A.W., 1987, "The Formation of Price Forecasts in Experimental Markets," *Journal; of Money, Credit and Banking*, **19**, 1-18.

## A Individual prediction strategies

This appendix contains the estimated individual prediction strategies for the 42 participants of this experiment. The estimated relationship has the following general structure

$$p_{h,t+1}^e = \alpha_h + \sum_{i=i}^4 \beta_{hi} p_{t-i} + \sum_{j=0}^3 \gamma_{hj} p_{ht-j}^e.$$

This was estimated on data from the experiment from  $t = 11$  to  $t = 51$ . The first 10 periods are neglected in order to allow for some coordination or learning. The following Tables 7 and 8 show the results. We have one table for each group and for each participant this table gives the estimated relationship. The constant term is always part of the regression although sometimes it is not significantly different from 0. These cases are indicated with a \*. We tried to fit the simplest model, so that there is no serial correlation in the residuals at the 5% significance level.

### Some remarks:

1. The estimates indicated by a \* are not significantly different from 0 at the 5% level.
2. Group 2: for participant 1 the null hypothesis of adaptive expectations,  $H_0 : (\alpha = 0 \text{ and } \beta_1 + \gamma_0 = 1)$ , cannot be rejected at the 5% significance level; for participants 2 and 6 the null hypothesis of naive expectations,  $H_0 : (\alpha = 0, \beta_1 = 1)$  cannot be rejected at the 5% significance level, for participant 3 this hypothesis is rejected. <sup>a)</sup>For the sample considered participant 5 exactly uses naive expectations.
3. Group 3: for participant 4 the null hypothesis of adaptive expectations,  $H_0 : (\alpha = 0, \beta_1 + \gamma_0 = 1)$  cannot be rejected. <sup>b)</sup>Participant 1 submitted an expectation of 5.25 in period 42, where we have a strong belief that he planned to submit 55.25. We therefore, replaced the 42'th observation on this participant by 55.25.
4. Group 5: for participant 1 the null hypothesis that this participant averages over the last two prices,  $H_0 : (\alpha = 0, \beta_1 = \beta_2 = \frac{1}{2})$  cannot be rejected; for participant 4 the null hypothesis of adaptive expectations cannot be rejected.
5. For all groups with  $AR(2)$  strategies we find that for the estimated  $AR(2)$  strategies the variation in  $\hat{\beta}_{h1} + \hat{\beta}_{h2}$  is much smaller than the



group 1	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_4$	$\gamma_0$	$\gamma_1$	$\gamma_2$	$\gamma_3$	$R^2$
part. 1	26.83	1.58	-1.05							0.83
part. 2	18.42	1.22	-0.55							0.79
part. 3	28.43	1.55	-1.05							0.81
part. 4	29.24	1.22	-0.72							0.84
part. 5	34.35	1.61	-1.23							0.77
part. 6	20.53	1.94	-2.24	1.88	-0.71	0.48	-0.60			0.95
group 2	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_4$	$\gamma_0$	$\gamma_1$	$\gamma_2$	$\gamma_3$	$R^2$
part. 1	-2.59*	0.27				0.78				0.98
part. 2	-1.08*	1.02								0.88
part. 3	-6.38	1.11								0.92
part. 4	3.76	0.91				0.32	0.21			0.97
part. 5 <sup>a)</sup>		1								1
part. 6	7.22*	0.87								0.77
group 3	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_4$	$\gamma_0$	$\gamma_1$	$\gamma_2$	$\gamma_3$	$R^2$
part. 1 <sup>b)</sup>	13.74	0.74								0.85
part. 2	-32.49	1.60								0.68
part. 3	0.25*	1.82	-0.83							0.94
part. 4	2.25*	0.24				0.71				0.81
part. 5	10.60	1.20	-0.41							0.88
part. 6	10.97	1.30	-0.51							0.85
group 4	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_4$	$\gamma_0$	$\gamma_1$	$\gamma_2$	$\gamma_3$	$R^2$
part. 1	10.26*	1.28	-1.96	0.84		0.63				0.79
part. 2	4.36*	2.14	-3.27	3.08	-1.31		0.90	-1.45	0.84	0.80
part. 3	13.87	1.85	-1.10							0.82
part. 4	15.76	1.65	-0.89							0.85
part. 5	1.87*	1.86	-1.49	0.54						0.70
part. 6	16.82	1.38	-0.70							0.57

Table 7: Estimated individual prediction strategies for groups 1 to 4

variation in  $\widehat{\beta}_{h2}$  alone. We know that the prediction strategy can be represented as

$$p_{h,t+1}^e = \alpha_h + \beta_h p_{t-1} + \delta_h (p_{t-1} - p_{t-2}),$$

where  $\beta_h \equiv \beta_{h1} + \beta_{h2}$  and  $\delta_h \equiv -\beta_{h2}$ . Our hypothesis now is that  $\beta_h$  (and possibly  $\alpha_h$ ) is the same for all participants in a group and  $\delta_h$  differs across participants in a group. We tested this hypothesis in all groups where the  $AR(2)$  prediction strategy emerges. We cannot reject the hypothesis at a 5% level for the  $AR(2)$  prediction strategies in groups 1 and 4. The results are given in Table 9.

For group 1 we have no significant differences in  $\beta_{h1} + \beta_{h2}$ , for group 4 we

group 5	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\gamma_0$	$\gamma_1$	$R^2$
part. 1	1.36*	0.49	0.48				0.80
part. 2	11.32	0.80					0.79
part. 3	7.18	0.87					0.88
part. 4	2.00*	0.63			0.33		0.93
part. 5	12.08	0.79					0.75
part. 6	2.97*	0.79	-0.41		0.57		0.83
group 6	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\gamma_0$	$\gamma_1$	$R^2$
part. 1	3.17*	1.36	-0.41				0.96
part. 2	-9.60	2.48	-0.80			-0.52	0.96
part. 3	12.83	1.85	-1.06				0.90
part. 4	32.53	2.05	-1.60				0.93
part. 5	6.70	1.94	-1.06				0.97
part. 6	21.43	1.32	-0.69				0.95
group 7	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\gamma_0$	$\gamma_1$	
part. 1	41.77	0.85	-0.55				0.45
part. 2	41.54	0.99	-0.68				0.66
part. 3	11.08*	2.11	-1.31				0.84
part. 4	61.71	0.67				-0.72	0.47
part. 5	28.52	1.77	-1.82	0.56			0.67
part. 6	30.08	1.47	-1.00				0.71

Table 8: Estimated individual prediction strategies for groups 5 to 7

have no significant differences in  $\alpha_h$  and in  $\beta_{h1} + \beta_{h2}$ . In all other groups the hypothesis is rejected.

	$\alpha$	$\beta$	$\delta_1$	$\delta_2$	$\delta_3$	$\delta_4$	$\delta_5$	$\delta_6$
group 1	–	0.52	1.06	0.62	1.04	0.71	1.17	–
group 4	15.48	0.74	–	–	1.11	0.90	–	0.36

Table 9: Test for homogeneous positive feedback expectations

## B Information for Participants

### General information.

You are a **financial advisor** to a pension fund that wants to optimally invest a large amount of money. The pension fund has two investment options: a risk free investment and a risky investment. The risk free investment is putting all money on a bank account paying a fixed interest rate. The alternative risky investment is an investment in the stock market. In each time period the pension fund has to decide which fraction of their money to put on the bank account and which fraction of the money to spend on buying stocks. In order to make an optimal investment decision the pension fund needs an accurate prediction of the price of stocks. As their financial advisor, you have to predict the stock market price (in guilder) during 52 subsequent time periods. Your earnings during the experiment depend upon your forecasting accuracy. The smaller your forecasting errors in each period, the higher your total earnings.

### Information about the stock market.

The stock market price is determined by equilibrium between demand and supply of stocks. The supply of stocks is fixed during the experiment. The demand for stocks is mainly determined by the aggregate demand of a number of large pension funds active in the stock market. Some of these pension funds are advised by a participant to the experiment, others use a fixed strategy. There is also some uncertain, small demand for stocks by private investors but the effect of private investors upon the stock market equilibrium price is small. The price of the stocks is determined by market equilibrium, that is, the stock market price in period  $t$  will be the price for which aggregate demand equals supply.

### Information about the investment strategies of the pension funds.

The precise investment strategy of the pension fund that you are advising and the investment strategies of the other pension funds are unknown. The bank account of the risk free investment pays a fixed interest rate of 5% per time period. The holder of the stocks receives an uncertain dividend payment

in each time period. These dividend payments are uncertain however and vary over time. Economic experts of the pension funds have computed that the average dividend payments are 3 guilder per time period. The return of the stock market per time period is uncertain and depends upon (unknown) dividend payments as well as upon price changes of the stock. As the financial advisor of a pension fund you are **not** asked to forecast dividends, but you are only asked to forecast the price of the stock in each time period. Based upon your stock market price forecast, your pension fund will make an optimal investment decision. The higher your price forecast the larger will be the fraction of money invested by your pension fund in the stock market, so the larger will be their demand for stocks.

#### **Forecasting task of the financial advisor.**

The only task of the financial advisors in this experiment is to forecast the stock market index in each time period as accurate as possible. The price of the stock will always be between 0 and 100 guilder. The stock price has to be predicted **two** time periods ahead. At the beginning of the experiment begins, you have to predict the stock price in the first **two** periods, that is, you have to give predictions for time periods 1 and 2. After all participants have given their predictions for the first two periods, the stock market price in the first period will be revealed and based upon your forecasting error your earnings for period 1 will be given. After that you have to give your prediction for the stock market index in the third period. After all participants have given their predictions for period 3, the stock market index in the second period will be revealed and, based upon your forecasting error your earnings for period 2 will be given. This process continues for 52 time periods.

To forecast the stock price  $p_t$  in period  $t$ , the available information thus consists of

- past prices up to period  $t - 2$ ,
- past predictions up to period  $t - 1$ ,
- past earnings up to period  $t - 2$

#### **Earnings.**

Earnings will depend upon forecasting accuracy only. The better you predict the stock market price in each period, the higher your aggregate earnings.

Earnings will be according to the following earnings table.

## C Payoff Table

Payoff table 1300 points equal 1 guilder									
error	points	error	points	error	points	error	points	error	points
0.1	1300	1.5	1240	3	1061	4.4	786	5.8	408
0.15	1299	1.55	1236	3.05	1053	4.45	775	5.85	392
0.2	1299	1.6	1232	3.1	1045	4.5	763	5.9	376
0.25	1298	1.65	1228	3.15	1037	4.55	751	5.95	361
0.3	1298	1.7	1223	3.2	1028	4.6	739	6	345
0.35	1297	1.75	1219	3.25	1020	4.65	726	6.05	329
0.4	1296	1.8	1214	3.3	1011	4.7	714	6.1	313
0.45	1295	1.85	1209	3.35	1002	4.75	701	6.15	297
0.5	1293	1.9	1204	3.4	993	4.8	689	6.2	280
0.55	1292	1.95	1199	3.45	984	4.85	676	6.25	264
0.6	1290	2	1194	3.5	975	4.9	663	6.3	247
0.65	1289	2.05	1189	3.55	966	4.95	650	6.35	230
0.7	1287	2.1	1183	3.6	956	5	637	6.4	213
0.75	1285	2.15	1177	3.65	947	5.05	623	6.45	196
0.8	1283	2.2	1172	3.7	937	5.1	610	6.5	179
0.85	1281	2.25	1166	3.75	927	5.15	596	6.55	162
0.9	1279	2.3	1160	3.8	917	5.2	583	6.6	144
0.95	1276	2.35	1153	3.85	907	5.25	569	6.65	127
1	1273	2.4	1147	3.9	896	5.3	555	6.7	109
1.05	1271	2.45	1141	3.95	886	5.35	541	6.75	91
1.1	1268	2.6	1121	4	876	5.4	526	6.8	73
1.15	1265	2.65	1114	4.05	865	5.45	512	6.85	55
1.2	1262	2.7	1107	4.1	854	5.5	497	6.9	37
1.25	1259	2.75	1099	4.15	843	5.55	483	6.95	19
1.3	1255	2.8	1092	4.2	832	5.6	468	error $\geq 7$	0
1.35	1252	2.85	1085	4.25	821	5.65	453		
1.4	1248	2.9	1077	4.3	809	5.7	438		
1.45	1244	2.95	1069	4.35	798	5.75	423		