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An Alternative Framework with Optimising Agents and Sticky Prices

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Monetary Policy for an Open Economy:  
An Alternative Framework with Optimising Agents and Sticky Prices

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ABSTRACT

The ‘new open-economy macroeconomics’ seeks to provide an improved basis for monetary and exchange-rate policy through the construction of open-economy models that feature rational expectations, optimising agents, and slowly adjusting prices of goods. This paper promotes an alternative approach for constructing such models by treating imports not as finished consumer goods but rather as raw-material inputs to the home economy’s productive process. This treatment leads to a clean and simple theoretical structure that has some empirical attractions as well. A particular small-economy model is calibrated and its properties exhibited, primarily by means of impulse response functions. The preferred variant is shown to feature a pattern of correlations between exchange-rate changes and inflation that is more realistic than provided by a more standard specification. Important recent events are interpreted in light of the alternative models.

Keywords: new open economy macroeconomics, monetary policy rules, exchange rates and inflation.

JEL classification number(s): E52, E58, F41.
SUMMARY

A major area of research activity in recent years is one that has been called ‘the new open-economy macroeconomics’. What is meant by this term is research into monetary policy questions using dynamic open-economy macro models that feature rational expectations, optimising agents, and slowly-adjusting prices of goods.

There has been a large and impressive volume of work in this area. Nevertheless, there are actually rather few examples of models in this category that are both truly dynamic (that is, models in which endogenous values remain away from their steady-state values for protracted periods) and realistically quantitative (that is, models that incorporate parameter values that are estimated from time series data or are calibrated in a careful and explicit manner). One objective of the present paper, accordingly, is to provide an accessible description of one such model—originally developed in McCallum and Nelson (1999a)—and to explore the properties of some significant variants. A second purpose, moreover, is to outline and promote a strategy regarding the treatment of imported goods that is analytically simpler than the one typically adopted, is superior empirically in several respects, and, at the same time, has important policy-relevant implications.

In particular, in the model described in this paper, imports are treated not as finished consumer goods, as is typical in the literature, but instead as raw-material inputs to the home economy’s productive process. This alternative treatment leads to a cleaner and simpler theoretical structure, relative to more standard treatments, and is empirically attractive, as discussed below.

Like other ‘new open economy macroeconomics’ (NOEM) models, our model features consumption behaviour that is based on household optimisation, as well as arbitrage conditions that dictate the relationship between exchange-rate adjusted returns on domestic and foreign securities. But our treatment of imports as inputs in production leads to different and more realistic inflation dynamics from those found in standard NOEM models. In the standard set-up, only a subset of the consumer price index is sticky. Costs of adjusting the prices of domestically produced goods lead to staggered behaviour of those prices, and to gradual adjustment of those prices to policy and other shocks. But unless a second form of nominal rigidity is imposed, these models imply that a large component of the consumer price index, namely the domestic-currency prices of imports, responds immediately and strongly to shocks. As we show, the result is that, in
aggregate, consumer price inflation is highly flexible in the standard models and, moreover, has a tight relationship with the change in the nominal exchange rate. Both of these features are highly unrealistic empirically, as we document.

In our alternative model, the total consumer price index, not just a subset, responds gradually to shocks. Movements in import prices influence overall inflation only via their impact on potential output. One result of this is more gradual and realistic predictions for the exchange rate/inflation relationship and for inflation dynamics than those of standard models. Our alternative model can be seen as compatible with a long-standing literature which holds that relative price changes, such as exchange rate changes, should not be associated with movements in the aggregate price level unless the relative price changes themselves alter aggregate supply (potential output). We demonstrate these features of our model by comparing its implications for inflation dynamics with those of the Gali and Monacelli (1999) NOEM model.

We use our model to analyze the experience of some small economies affected by the East Asian crisis of 1997–1998. Countries such as Australia, Canada, and New Zealand experienced double-digit depreciations of their nominal exchange rate during this episode. The relatively successful outcomes in Australia over this period suggest that the depreciation was associated with only a modest rise in inflation, and that it was unnecessary to increase interest rates sharply to bring inflation on target. Unlike the standard models, our alternative can account for why an ‘exchange rate shock’ can be associated with only modest increases in inflation and interest rates.

A more general point about our model for policy is that its implications regarding the control of inflation in an open economy differ sharply from those of standard NOEM models. In those models, the introduction of open-economy elements radically changes the overall price-setting behaviour in the economy. Because imports are final goods in these models, the resulting Phillips curve states that total consumer price inflation depends not only on the output gap but also on the real exchange rate or the terms of trade. In evaluating the implications of a domestic or foreign shock for inflation, it is insufficient for the monetary authority to consider only the shock’s effect on the output gap. Controlling inflation in an open economy thus involves considering channels that arise from the openness of the economy.
By contrast, in our framework, it is useful to think of the implications for inflation of any shock in terms of its effect on the output gap alone. In this sense, our model implies less of a contrast between controlling inflation in an open economy and controlling inflation in a closed economy. The effect of open-economy elements in our model is to increase the variety of shocks in the model that affect the output gap, not to create a separate channel besides the output gap through which monetary policy affects inflation. In general, our model provides little support for inflation-targeting central banks to be driven to large increases in interest rates in the face of even significant exchange rate depreciations, unless the depreciations are associated with large increases in output above potential.
1. Introduction

A major area of research activity in recent years is one that has been called ‘the new open-economy macroeconomics’.¹ What is meant by this term is research based on dynamic open-economy macro models that feature rational expectations, optimising agents, and slowly-adjusting prices of goods.² Pioneering publications in the area were provided by Obstfeld and Rogoff (1995, 1996), while other notable contributions include Gali and Monacelli (1999), Betts and Devereux (2000, 2001), Chari, Kehoe, and McGrattan (2000), Ghironi (2000), Svensson (2000), Batini, Harrison, and Millard (2001), Benigno and Benigno (2001), Corsetti and Pesenti (2001), Kollmann (2001a, 2001b), and Smets and Wouters (2001).³

Despite the impressive volume of work, however, there are actually rather few examples of models in this category that are both truly dynamic and realistically quantitative, i.e., ones that incorporate parameter values estimated from time series data or calibrated in a careful and explicit manner.⁴ One objective of the present paper, accordingly, is to provide an accessible description of one such model—originally developed in McCallum and Nelson (1999a)—and to explore the properties of some significant variants. A second purpose, moreover, is to outline and promote a strategy regarding the treatment of imported goods that is analytically simpler than the one typically adopted, is superior empirically in several respects, and, at the same time, has important policy-relevant implications.

In particular, in the model discussed below, imports are treated not as finished consumer goods, as is typical in the literature, but instead as raw-material inputs to the home economy’s productive process. This alternative treatment leads to a cleaner and simpler

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¹ Much of this literature can be found on the ‘New Open Economy Macroeconomics Homepage’ created by Brian Doyle (http://www.geocities.com/brian_m_doyle/open.html), and the web page on ‘Monetary Policy Rules in Open Economies’, created and maintained by Gianluca Benigno, Pierpaolo Benigno, and Fabio Ghironi (http://www.geocities.com/monetaryrules/mpoe.htm). An informative survey is Lane (2001).

² In other words, these models feature ‘sticky prices’ of goods and services, rendered plausible by the assumption of monopolistic competition in the sale of individual commodities. Asset prices, on the other hand, are assumed to adjust promptly.

³ One important precursor is Taylor (1988, 1993a), which includes a large (although incomplete) dose of individual optimisation. Another is Svensson and van Wijnbergen (1989). Also, the international real-business-cycle literature (e.g. Backus, Kehoe, and Kydland, 1992) differs mainly in its assumption of full price flexibility.

⁴ Such examples do include the papers mentioned in paragraph 1, with the exception of the Obstfeld-Rogoff contributions, which are primarily theoretical, and the one by Corsetti and Pesenti.
theoretical structure, relative to more standard treatments, and is empirically attractive in ways that will be discussed below.

The outline of the paper is as follows. We begin in Section 2 by laying out the basic structure of our model of a small open economy in a fashion that is intended to emphasise its simplicity. A presentation of the properties of various versions of the model appears in Section 3 and an application to exchange rate and inflation dynamics in Section 4. Section 5 considers policy-relevant implications of our approach, and Section 6 concludes.

2 Basic model

In this section we describe the basic version of our model. Since the optimising, general equilibrium analysis has already been worked out in McCallum and Nelson (1999a), here we take an informal expository approach. The model’s equations can be derived from an infinite-horizon framework in which households choose optimal paths for their consumption and asset holdings, and in which each household produces a good over which it has some market power. It is well known that the household’s optimisation leads in such a model to a first-order condition for consumption that can be expressed or approximated in the form

$$c_t = E_{t} c_{t+1} + b_0 + b_1 (R_t - E_{t} \Delta p_{t+1}) + v_t.$$  \hfill (1)

In equation (1), $b_1 < 0$, $c_t$ is the log of a Dixit-Stiglitz consumption-bundle aggregate of the many distinct goods that a typical household consumes in period $t$. $R_t$ is the nominal interest rate on home-country one-period securities (private or government), $E_{t} \Delta p_{t+1}$ is the inflation rate expected for next quarter (so $R_t - E_{t} \Delta p_{t+1}$ is the short-term real interest rate), and $v_t$ is a stochastic shock term that pertains to household preferences regarding present vs. future consumption. If this shock is serially correlated, then it gives some inertial behaviour to the path of consumption over and above that imparted into consumption by the other variables on the right-hand-side of (1). In closed-economy analysis, relation (1) is often combined with a log-linearised, per-household, overall resource constraint to yield an ‘expectational IS function’, to use the term of Kerr and King (1996). This step

5 An appendix that includes technical derivations is available from the authors.

6 Thus $c_t = \ln C_t$ where $C_t = \int C(z)^{(\theta-1)/\theta}dz/\theta$, where $\theta > 1$, $z$ indexes distinct goods, and the integral is over $(0, 1)$, while the corresponding price index is $P_t = \int P(z)^{(\theta-1)/\theta}dz/\theta$. 
presumes that investment and capital are treated as exogenous. The most common
version of that assumption is that the capital stock is fixed; since that assumption is rather
standard in the new open-economy macro (NOEM) literature, we shall adopt it here.\(^7\)

For our open-economy application, one is tempted to write the resource constraint as

\[
y_t = \omega_1 c_t + \omega_2 g_t + \omega_3 x_t - \omega_4 im_t, \quad (2')
\]

where \(y_t, g_t, x_t,\) and \(im_t\) are logarithms of output, government consumption, exports, and
imports while \(\omega_1, \omega_2, \omega_3,\) and \(\omega_4\) are steady state ratios of consumption, government
purchases, exports, and imports to output.\(^8\) But if imports are exclusively material inputs
to the production of home-country goods, and \(Y = \ln^{-1} y\) is interpreted as units of output,
then the relevant identity is

\[
y_t = \omega_1 c_t + \omega_2 g_t + \omega_3 x_t. \quad (2)
\]

This is, of course, the same as \((2')\) with \(\omega_4 = 0\). Either of these versions can be thought of
as the resource constraint for our model.

We require that import demand be modelled in an optimising fashion. Toward that end,
we assume that production of all consumer goods is effected by households that are
constrained by a production function of the constant elasticity of substitution (CES) form,
with labour and material imports being the two variable inputs. Then the cost-minimising
demand for imports equals

\[
im_t = y_t - \sigma q_t + \text{const.}, \quad (3)
\]

\(^7\) Exceptions include Chari, Kehoe, and McGrattan (2000) and Kollmann (2001a, 2001b).
Woodford (2000) shows that the combined behaviour of investment and consumption in a closed-economy, dynamic
general equilibrium model is well approximated by the consumption equation \((1)\) alone, provided the
interest-rate elasticity in \((1)\) is calibrated to take into account the interest sensitivity of investment.
Nevertheless, as McKibbin and Vines (2000) stress, an explicit separate treatment of consumption and
investment is crucial for analysing certain issues.

\(^8\) As resource constraints such as these are log-linear approximations of the linear relationships between the
corresponding unlogged variables, they can also be regarded as describing the percentage deviations of
these unlogged variables from their steady-state values. So \((\text{e.g.}) y_t\) can be thought of as the percentage
deviation of detrended output \((Y_t)\) from its steady-state level. Under the log interpretation, constant terms
should be included.
where \( \sigma \) is the elasticity of substitution between materials and labour in production, and where ‘const.’ denotes some constant.\(^9\) Also, \( q_t \) is the price of imports in terms of consumption goods. In other words, \( Q_t = \ln^{-1} q_t \) is the real exchange rate. Let \( P_t \) and \( S_t \) be the home country money price of goods and foreign exchange, with \( P_t^* \) the foreign money price of imports. Then if \( p_t, s_t, \) and \( p_t^* \) are logs of these variables, we have

\[
q_t = s_t - p_t + p_t^*. \tag{4}
\]

Symmetrically, we assume that export demand is given as

\[
x_t = y_t^* + \sigma^* q_t + \text{const.}, \tag{5}
\]

where \( y_t^* \) denotes production abroad and \( \sigma^* \) is the elasticity of substitution in production abroad.

Let us now consider output determination in a flexible-price version of the model. Taking a log-linear approximation to the home-country production function, we have

\[
y_t = (1-\alpha)a_t + (1-\alpha)n_t + \alpha im_t + \text{const.},
\]

where \( n_t \) and \( a_t \) are logs of labour input and a labour-augmenting technology shock term, respectively. We suppose for simplicity that households supply labour inelastically, with each supplying one unit per period. Thus, under price flexibility, we would have \( n_t = 0 \) and the flexible-price, natural rate (or ‘capacity’) value of \( y_t \) will be

\[
\bar{y}_t = (1-\alpha)a_t + \alpha [\bar{y}_t - \sigma q_t] + \text{const.},
\]

or

\[
\bar{y}_t = a_t - [\sigma\alpha/(1-\alpha)] q_t + \text{const.} \tag{6}
\]

But while \( \bar{y}_t \) would be the economy’s output in period \( t \) if prices could adjust promptly in response to any shock, we assume that prices adjust only sluggishly. An appreciation of the real exchange rate causes a change in the cost-minimising mix of factor inputs,

\(^9\) Thus the expressions ‘const.’ in different equations appearing below will typically refer to different constant magnitudes.
leading to a larger quantity of imports employed in production, and also to an increase in potential output. And if the economy’s demand quantity as determined by the rest of the system \( y_t \) differs from \( \bar{y}_t \), then the former quantity prevails—and workers depart from their (inelastic) supply schedules so as to provide whatever quantity is needed to produce the demanded output, with \( im_t \) given by (3).

In such a setting, the precise way in which prices adjust has a direct impact on demand, in a manner to be detailed shortly, and consequently on production. There are various models of gradual price adjustment utilised in the recent literature that are intended to represent optimising behaviour.\(^{10}\) In our analysis below we shall explore two candidates; for present purposes we need to list one representative.\(^{11}\) Principally because it is the most popular specification of price setting in current work with general equilibrium models (e.g. Roberts, 1995; Rotemberg and Woodford, 1997), we use the Calvo (1983) model, here expressed in the form

\[
\Delta p_t = \beta E_t \Delta p_{t+1} + \lambda (y_t - \bar{y}_t),
\]

(7)

where \( \beta \in (0,1) \) is a discount factor, and \( \lambda > 0 \). A standard feature of most current open-economy models is a relation implying uncovered interest parity (UIP). Despite its prominent empirical weaknesses, accordingly, we adopt one here:

\[
R_t - R_t^* = E_t \Delta s_{t+1} + \xi_t.
\]

(8)

We include a time-varying ‘risk premium’ term \( \xi_t \), however, that may have a sizeable variance and could be autocorrelated.

It remains to describe how monetary policy is conducted. In the spirit of most recent research in monetary economics, we presume that the monetary authority conducts policy in a manner suggested by the Taylor (1993b) rule, i.e., by adjusting a one-period nominal interest rate in response to prevailing (or forecasted future) values of inflation and the output gap, \( \tilde{y}_t = y_t - \bar{y}_t \):

\[
R_t = \mu_0 + \Delta p_t + \mu_1 (\Delta p_t - \pi^*) + \mu_2 \tilde{y}_t + e_{Rt},
\]

(9)

\(^{10}\) See McCallum and Nelson (1999b).

\(^{11}\) In our previous open-economy work, we used a third variant—the ‘P-bar’ model—which is briefly discussed in McCallum and Nelson (1999b).
where $\pi^*$ is the monetary authority’s inflation target. Our quantitative results in Section 3 and 4 will be based on an estimated variant of this rule.

Thus we have a simple log-linear system in which the nine structural relations (1)–(9) determine values for the endogenous variables $y_t$, $\bar{y}_t$, $\Delta p_t$, $R_t$, $q_t$, $s_t$, $c_t$, $x_t$, and $im_t$.

Government spending $g_t$ and the foreign variables $p_t^*$, $y_t^*$, $R_t^*$ are taken as exogenous—as are the shock processes for $v_t$, $u_t$, $e_{Rt}$, and $\xi_t$. We suggest that this is probably the simplest and cleanest model extant that includes the essential NOEM features.

Of course, it would be possible to append a money demand function such as

$$m_t - p_t = \gamma_0 + \gamma_1 y_t + \gamma_2 R_t + \eta_t,$$

and one of this general form—perhaps with $c_t$ replacing $y_t$—would be consistent with optimising behaviour.\(^{12}\) But, as many writers have noted, that equation would serve only to determine the values of $m_t$ that are needed to implement the $R_t$ policy rule.

With the structure given above, it is possible to calculate the (log of the) balance on goods and services account as

$$net_t = x_t - (im_t + q_t),$$

where it is assumed that the steady state trade balance is zero ($\omega_3 = \omega_4$). Also, we can calculate the log of the GDP deflator as

$$p_t^{DEF} = [p_t - \omega_3(s_t + p_t^*)]/(1 - \omega_3).$$

These represent extra features, however, that need not be included with the basic model (1)–(9).

Most open-economy macro models treat imports as finished consumer goods.\(^{13}\) Here, by contrast, we treat all imports as material inputs to the production process for domestically

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\(^{12}\) See McCallum and Nelson (1999b).

\(^{13}\) An alternative, used by Obstfeld and Rogoff (1995), is to specify that imports are not physically different form goods produced in the economy under study. More common is to assume that the consumption good in each country (or more precisely its Dixit-Stiglitz aggregate) is distinct.
produced goods.\textsuperscript{14} An advantage of this modelling strategy is that the relevant price index for produced goods is the same as the consumer price index (CPI), which implies that the same gradual price adjustment behaviour is relevant for all domestic consumption. In addition, it avoids the unattractive assumption, implied by the tradable vs. non-tradable goods dichotomisation, that export and import goods are perfectly substitutable in production. Furthermore, the evidence suggests that (under conservative assumptions) productive inputs actually comprise a larger fraction of U.S. imports than do consumer goods (including services).\textsuperscript{15} Thus, the emphasis in our model on imports’ role as raw materials appears reasonable.

3 Model properties

In this section we present impulse response analysis for our model. The calibration of the model (hereafter referred to as the MN model) is given in Table 1, and closely follows our (1999a) paper.\textsuperscript{16} For the policy rule, instead of (9), we use the following:

\begin{equation}
4^*R_t = 0.23E_{t-1} 4^*(\Delta y_t + \Delta p_t - \pi^*) + 0.81 4^*R_{t-1} + e_{Rt} \tag{9'}
\end{equation}

We found that this specification better described US monetary policy behaviour over 1979–1997, using quarterly data, than did a Taylor-type rule.\textsuperscript{17} Note that expectations based on period \( t-1 \) information are used in place of current variables on the right hand side of (9’), in order to reflect operationality—i.e., data actually available to the central bank.

Table 2 reports the standard deviations of four key variables in the model: the annualised nominal interest rate and inflation rate (\( 4^*R_t \) and \( 4^*\Delta p_t \)), the quarterly change in the nominal exchange rate (\( \Delta s_t \)), and the level of output (\( y_t \)). Also reported are the corresponding statistics from US data for 1973–1998 (with the output variable measured

\textsuperscript{14} Weale \textit{et al} (1989) is an early example of work that incorporated imported intermediate goods into a forward-looking structural model.

\textsuperscript{15} For a very brief summary of the results, see McCallum (2001), which includes a model presentation similar to that in this section.

\textsuperscript{16} The main exception is that we have used the basic consumption equation (1), and calibrated it according to our (1999b) estimates. In McCallum and Nelson (1999a) we instead used Fuhrer’s (2000) more general consumption equation that allowed for habit formation in preferences.

\textsuperscript{17} Rules like (9’), which essentially target nominal GDP growth, may also have some advantages over Taylor-type rules if there is considerable error in measuring potential output, and therefore the output gap term in the Taylor rule. On this, see McCallum (1999), Orphanides (1999), and our (1999a, 1999b) papers.
by detrended log GDP). The data and model standard deviations are reasonably close, with the exception of that for $\Delta s_t$, which is excessive in the model. However, for a realistic setting of the shock variances, the variability of $\Delta s_t$ tends to be lower in our model than it is in standard NOEM setups (such as the Galí-Monacelli model, studied in Section 4).

To provide information concerning the model’s dynamic properties, we now present impulse response functions for various shocks—beginning with a surprise 100 basis point increase in interest rates (a temporary, unit impulse to the $e_Rt$ shock term in policy rule (9’)). Figure 1 plots the responses of $y_t, \Delta p_t, R_t, q_t, s_t$, and net exports ($net_t$) to the policy shock. In the top-left panel it is seen that a one percentage point upward shock to the interest rate drives output down by about 0.3%, with the largest response coming in the period of the shock and then dying out quite slowly. Inflation drops in the period of the shock and returns to its initial value at much the same rate as output—a characteristic of the Calvo model of price setting. Both the real and the nominal exchange rate appreciate promptly in response to the monetary tightening. As time passes, the real exchange rate returns to its original value but there is a permanent nominal appreciation. Finally, the fall in income and the decrease in the real price of imports outweigh the price effect on import and export quantities, leading to an expansion in net exports. This is the direction of change that we would expect from a monetary policy tightening, but the magnitude and timing seem questionable. That observation leads us to note that our (1999a) value for $\sigma^*$, the price elasticity of export demand, is only 0.333. Since that is also the price elasticity of import demand, the Marshall-Lerner condition is not satisfied. Accordingly, we now assume that $\sigma^* = 1.0$, which leads to satisfaction of the Marshall-Lerner condition. Impulse response functions for a policy shock with this altered value are shown in Figure 2. There the net export balance does undergo a fall, while the responses of other variables are altered very little. For the rest of this section, this revised value for $\sigma^*$ is utilised.

Figures 3 and 4 report impulse response functions for shocks to the UIP relation and to income/production abroad. In the former, we see that an ‘exchange rate shock’—a depreciation—has little overall effect on the net trade balance because of the stimulus to output and hence import demand from higher exports. In the latter, an increase in demand from abroad—which is highly persistent—generates a small but long-lasting increase in output and a prolonged real exchange rate appreciation.
Table 1: Calibration

<table>
<thead>
<tr>
<th>Preference parameters</th>
<th>Shock processes</th>
</tr>
</thead>
<tbody>
<tr>
<td>$b_1 = -0.2$</td>
<td>$\rho_a$ (AR(1) of technology shock) = 0.95</td>
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<tr>
<td>$\beta = 0.99$</td>
<td>$\rho_v$ (AR(1) of IS shock) = 0.30</td>
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<tr>
<td></td>
<td>$\rho_{y^*}$ (AR(1) of foreign output) = 1.0</td>
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<tr>
<td></td>
<td>$\rho_{\kappa}$ (AR(1) of UIP shock) = 0.50</td>
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<table>
<thead>
<tr>
<th>Production parameters</th>
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<tbody>
<tr>
<td>$\theta = 6$</td>
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<td>$\sigma = 0.333$</td>
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<table>
<thead>
<tr>
<th>Other parameters</th>
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<tr>
<td>$\omega_1 = 0.89$, $\omega_2 = 0$, $\omega_3 = \omega_4 = 0.11$</td>
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<tr>
<td>$\sigma^* = 0.333$</td>
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<td>$\lambda = 0.086$</td>
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<td>$\rho_{\kappa}$ (AR(1) of UIP shock) = 0.50</td>
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<table>
<thead>
<tr>
<th>Innovation variances</th>
</tr>
</thead>
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<tr>
<td>$\sigma_{ea}^2 = (0.007)^2$</td>
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<tr>
<td>$\sigma_{e{y^*}}^2 = (0.02)^2$</td>
</tr>
<tr>
<td>$\sigma_{e\kappa}^2 = (0.01)^2$</td>
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<tr>
<td>$\sigma_{e\kappa}^2 = (0.04)^2$</td>
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Table 2: Model statistics

<table>
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<tr>
<th>Standard deviations of:</th>
<th>4*RT</th>
<th>4*ΔPt</th>
<th>ΔSt</th>
<th>yt</th>
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</thead>
<tbody>
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<td>MN model</td>
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<td>3.00</td>
<td>10.04</td>
<td>2.30</td>
</tr>
<tr>
<td>US data 1973 Q1–1998 Q4</td>
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<td>3.43</td>
<td>3.12</td>
<td>2.65</td>
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</tbody>
</table>

Note: Model statistics are averages across 100 model simulations. The simulations use a policy shock standard deviation of 0.8% (annualised). In the data, $R_t$ is the federal funds rate, $p_t$ and $s_t$ are measured as in Section 4 below, and $y_t$ is measured by linearly detrended log real GDP.

A major weakness apparent in Figures 1–4 is that there is not much persistence in inflation in response to any of these shocks. Accordingly, since the data for the US and other countries exhibit strongly persistent inflation, we would like to modify our model in a manner that will overcome this failure. The most straightforward way of doing so is to adopt a different model of gradual price adjustment, one that tends to impart inertia. We do so in Section 4, where we present some results based on a price-setting specification that is close to that of Fuhrer and Moore (1995).
4 Application: Dynamics of nominal variables

In this section we present an application of our model that illustrates some advantages—both in terms of its simplicity and empirical performance—of our open-economy approach over alternative, more standard NOEM models. The empirical regularity that we concentrate upon is the dynamics of two key nominal variables—inflation and the nominal exchange rate. The different treatment of imports in our model leads to a better match with the empirical evidence.

The ‘standard’ NOEM model that we use as a benchmark with which to compare the MN model is that of Galí and Monacelli (GM) (1999) which, like our model, is ‘small open economy’ in nature. A log-linearised version of the GM model is:

\[ y_t = (1 - \alpha_m) c_t + \alpha_m c_t^* + \alpha_m \chi (2 - \alpha_m) ft_t \]

(13)

\[ tt_t = -(R_t - E_t \Delta p_{t+1}^H) + E_t T_{t+1} + \kappa_t \]

(14)

\[ c_t = E_t c_{t+1} + b_1 (R_t - E_t \Delta p_{t+1}) + v_t \]

(15)

\[ \Delta p_H^t = \beta E_t \Delta p_{t+1}^H + \lambda c_t \]

(16)

\[ mc_t = [(1/\sigma) + \phi (1 - \alpha_m)] c_t + \alpha [1 + \phi \chi (2 - \alpha)] ft_t - (1 + \phi) \alpha t_t - (1/\sigma (1 - \rho_s)) v_t \]

(17)

\[ q_t = (1 - \alpha_m) ft_t \]

(18)

\[ \Delta p_t = \Delta p_H^t + \alpha_m (tt_t - tt_{t-1}) \]

(19)

\[ \Delta s_t = \Delta q_t + \Delta p_t \]

(20)

Here \( c_t^*, y_t^*, tt_t, \) and \( mc_t \) are the log-deviations of rest-of-world consumption, rest-of-world output, the terms of trade, and real marginal cost from their steady-state values, and \( \Delta p_H^t \) is the log-change in the nominal price of domestically produced goods. Foreign prices and interest rates are assumed constant.

The version of the MN model that we use for comparisons consists of six structural equations: the consumption condition (1), the Calvo pricing equation (7), the definition of
potential output (6), UIP condition (8), identity (20), and the following analogue to equation (13),

\[ y_t = \omega_1 c_t + (1 - \omega_1) \eta q_t + (1 - \omega_1) \beta y_{t-1}^*, \]

(21)

which can be obtained by substituting the export demand function (5) into our resource constraint (2). Both the GM and the MN model would be completed by a monetary policy rule and specification of the four shock processes.

The GM model has a strong claim to be viewed as a canonical NOEM model, owing to its elegance and tractability. The model can be expressed as a compact log-linear system and is also sufficiently dynamic to allow some comparisons with data.\(^{18}\) Even so, inspection of the model’s equations indicate that it is noticeably more complicated than the MN model. Because imports enter as final goods in the GM model, the model’s assumptions about price stickiness refer to the price of domestically produced goods, rather than the overall consumer price index. Therefore, the Calvo price setting equation links domestic-goods inflation \(\Delta p_t^H\) to real marginal cost (equation (16)), and equation (19) is required to obtain an expression for aggregate CPI inflation \(\Delta p_t\).\(^{19}\) By contrast, in our model (as in standard closed-economy models), Calvo price setting can be written directly as an equation linking aggregate CPI inflation to the output gap (equation (7)), with no further equations or substitutions needed. The different setup in the GM model also changes the form in which it is convenient to express certain key equations; hence in the GM model, the UIP condition (equation (14)) is written as a difference equation for the terms of trade rather than for the nominal exchange rate. Overall, the GM model has two more endogenous variables than the MN model (i.e., the GM model requires keeping track of three variables—\(\Delta p_t^H, mc_t\), and \(tt_t\)—that do not appear explicitly in the MN model, while the MN model has to keep track of potential output, which does not appear explicitly in the GM model).

We now present some quantitative comparisons between the GM and MN models. We have made some necessary adjustments to the GM model, as given by Galí and Monacelli (1999), for comparability with our own setup. Thus we have included IS and UIP shocks

\(^{18}\) Indeed, we have selected this particular model for comparison purposes in part because it follows a clear and convenient log-linear structure that is easy to reproduce from the Galí-Monacelli paper.

\(^{19}\) Equation (16) can be derived from optimal behaviour by monopolistically competitive producers in an environment of staggered contracts for prices of domestically produced goods. As for equation (7), we assume \(\lambda = 0.086\), the same value used by GM.
in the GM model (both specified to follow the same time-series processes as in the MN model). We have also made the technology shock \( a_t \) follow the same process as it does in the MN model; set \( b_1 = -0.2 \), so that the interest sensitivity of consumption in the two models are identical; and made the share of imports in GDP (\( \alpha_m \)) the same value (0.11) that it is in the MN model. For simplicity we have made the \( c_t^* \) process in the GM model identical to the \( y_t^* \) process in our model. The parameter \( \chi \) is chosen so that the coefficient on the terms of trade in equation (13) is the same as that on the real exchange rate in equation (21); aggregate demand thus has approximately the same real exchange-rate elasticity in each model.

In comparing the predictions of the GM and MN models, we focus upon the transmission of exchange rate changes to inflation—i.e., the extent to which each model supports the position that nominal exchange rate depreciations lead to increases in the home economy’s CPI inflation rate. In this regard, it is useful to consider the effects of risk premium (UIP) shocks specifically—since these shocks affect variables other than the nominal exchange rate (\( s_t \)) only via their effect on \( s_t \). But, as the exchange rate may act as a conduit through which other shocks (such as policy shocks) are transmitted to inflation, the discussion below would apply also to exchange rate changes produced by those shocks.

In our model, a change in \( s_t \) produced by a risk premium shock will affect inflation solely through its effect on the output gap \( y_t - \bar{y}_t \). A depreciation (i.e., a rise in \( s_t \)—and, in the absence of complete price flexibility, in \( q_t \) as well) tends to raise \( y_t - \bar{y}_t \) for two reasons: higher \( y_t \) due to higher export demand from the depreciation; and the negative effect of real depreciations on potential output \( \bar{y}_t \). Of these effects, the export demand effect on \( y_t \) is common to both our model and the standard model; therefore, it cannot account for different properties of the two models, so we focus instead on the channel from depreciations to \( \bar{y}_t \). For a given technology shock, a depreciation raises the cost of producing domestic goods in the MN specification and therefore reduces potential output (equation (6)), which will raise the inflation rate for the period during which the excess of output over potential persists.

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20 We keep GM’s choice of \( \phi = 1.0 \) for their model, which makes households’ desired labour supply elastic.

21 From a strict point of view, we consider it incoherent to refer to ‘effects of exchange-rate changes on inflation’ because exchange rates are endogenous variables, whose relationships with other variables are different for different shocks. But averages of these relationships are implied by any complete calibration. And we believe that the type of consideration at hand appears so often in professional and journalistic writings that it needs to be explicitly addressed and analysed.
In the GM model, by contrast, import prices directly enter the CPI (equation (19)), and therefore the exchange rate depreciation produced by a UIP shock affects inflation ‘directly’, not just via the output gap.

The different transmission of exchange-rate changes to inflation in the two models reflects the differing ways in which each treats a long-standing tension in macroeconomics, namely the role of relative prices (such as the exchange rate) in aggregate price level analysis. That relative price changes need not imply aggregate price level changes, in the absence of monetary accommodation, was stressed by early quantity theorists, including Wicksell (1906, p. 156). As Milton Friedman (1974) famously observed, with regard to other relative price changes,

‘The special conditions that drove up the price of oil and food required purchasers to spend more on them, leaving them less to spend on other items. Did that not force other prices to go down or to rise less rapidly than otherwise? Why should the average level of all prices be affected significantly by changes in the price of some things relative to others?’

Batten and Ott (1983) applied this argument specifically to exchange rate changes, and argued that the proposition that ‘a depreciating currency generates domestic inflation’ was a ‘myth’; neither the price level nor the inflation rate, they argued, would be raised in the long run by a depreciation unless the depreciation was accompanied by monetary expansion.

Ball and Mankiw (1995) pose the problem in terms of the equation of exchange identity, \( MV = PY \): for a given volume of aggregate nominal spending \( MV \) a rise in the price of a subset of the consumer price index (such as imports in the GM model) can raise the aggregate CPI \( P \) only if it alters the mix of total spending towards higher prices and lower aggregate output \( Y \).

It is enlightening to consider how the alternative models obtain the property that depreciations can produce inflation, instead of the purely relative price changes sketched by Friedman. In the GM model, the reason is that, under an interest rate policy rule, the depreciation leads to a rise in \( M_t \). Under an interest rate rule, nominal money rises passively\(^{22}\) to sustain the level of nominal spending consistent with the higher \( P_t \). Households do not then have ‘less to spend on other items’. This setup has the

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\(^{22}\) Via a money demand equation like (10).
implication that money and monetary growth are closely associated with exchange rate change at the business cycle frequency, which seems unattractive empirically for most industrial countries (see e.g. Rogoff, 1999).

In our model, exchange rate depreciations, by raising production costs, can be inflationary. But a crucial distinction from the GM and other standard models is that the inflationary impact of depreciations is limited by the extent to which they affect aggregate supply. Their impact is not linked to the weight given to imports in the CPI. In terms of the equation of exchange, depreciations raise $P_t$ in the MN model because they reduce $Y_t$ for a given $P_tY_t$; while in the GM model, depreciations raise $P_t$ because an endogenous increase in $M_t$ permits $P_tY_t$ to rise. In spirit, though not in detail, our approach can be considered to be similar to that of Ball and Mankiw’s (1995) ‘Relative Price Changes as Aggregate Supply Shocks’.

The different ways in which the alternative models treat the link between nominal exchange rates and inflation lead to different implications for the dynamic relationship between the two variables. We argue that empirically the relationship between nominal exchange rate change and inflation is typically very loose at the business cycle frequency, and that our model—but not the GM model—has no difficulty in reproducing this basic fact. Let us therefore examine the empirical evidence, using *International Financial Statistics (IFS)* data on nominal exchange rate and consumer price indices for several industrial countries. The correlations between $\Delta p_t$, the log-difference of consumer prices, and current ($\Delta s_t$) and lagged ($\Delta s_{t-k}$) changes in the log nominal exchange rate, are reported in Table 3. For

23 Apart from the higher export demand due to the depreciation noted earlier.
24 The exchange rate series used is the *IFS* index of the nominal market exchange rate (quarterly average). The exception is the United States, where we use a main-trading-partners index of the nominal exchange rate downloaded from the Federal Reserve Bank of St Louis’ FRED database. (A quarterly series was obtained by averaging the monthly observations of this series, which begins in January 1973). Our use of market exchange rates (the *IFS* label for bilateral rates against the $US$) is dictated by its availability for all countries since 1973. Results for the nominal effective exchange rate are reported in the Appendix. The *IFS* quarterly average of consumer prices is used as the price index for each country except the United Kingdom, where RPIX (seasonally adjusted) is used. For Germany, we found that the quarterly CPI inflation series exhibited seasonality, so we obtained a seasonally adjusted series using OLS regression on seasonal dummies. For Australia, the CPI series was adjusted in 1984 Q1 for a break. In computing the annual results in Table 4 below, we used annual averages of the quarterly series used in Table 3.
25 These correlations are of more interest than those between inflation and future $\Delta s$, since the issue we focus upon is what alternative models say about how shocks are transmitted from the exchange rate to current and future inflation. But consideration of the $(\Delta p_t, \Delta s_{t+k})$ correlations would not overturn our findings.
most countries, the sample period for calculating the correlations begins in 1973 with the demise of Bretton Woods. For Australia and New Zealand, which did not adopt floating exchange rates against the US or other countries until the mid-1980s, results are also reported for their more recent floating-rate sample period; and for France, Germany, and Italy, results are reported for the subsample commencing with the onset of the European Monetary System in 1979.

The overall impression we receive from Table 3 is the weakness of the bivariate correlations, regardless of lag length. A strong association between inflation and nominal exchange rate depreciation would lead to a high positive correlation, but for most countries, this correlation is rather close to zero. Even for those countries for which there is a statistically significant positive correlation—France, Germany, Italy, and New Zealand—the size of the correlation itself tends to be low, always below 0.3 for the full sample. The only prominent exception to the weakness of the correlations is the 0.46 correlation between inflation and the previous quarter’s exchange-rate change for Germany for 1979–1998.

A possible objection is that gradual pass-through of exchange-rate changes to inflation might imply that the empirical relationship between inflation and exchange rate depreciations is tighter if lower frequency data are considered. But if we look at annual data for the same countries (Table 4), the weakness of the correlations persists for the majority of the countries. For France, Germany, Italy, and New Zealand, it is true that the correlations are higher than they were on quarterly data. In the French and Italian cases, however, there appears to be a significant correlation between base money growth and nominal exchange rate change. This could mean that the results for those countries in Table 4 are still consistent with the arguments of Friedman (1974) and Batten and Ott (1983) given above; their contention that exchange rate depreciation does not lead to inflation refers to the case where the depreciation is not accompanied or produced by monetary expansion.

The exchange rate is only one channel through which shocks are transmitted to the inflation rate, so the low bivariate correlations reported in Tables 3 and 4 may simply reflect the fact that these other channels (such as the output gap) are not being held constant. But we will show that, although it includes an output gap as well as an

26 The correlation for 1979–1998 between Δs_t and the log-difference of currency in circulation is 0.46 for France and 0.41 for Italy.
Table 3: Nominal exchange rate change / inflation correlations, quarterly data

<table>
<thead>
<tr>
<th>Country</th>
<th>Sample Period</th>
<th>k = 0</th>
<th>k = 1</th>
<th>k = 2</th>
<th>k = 3</th>
<th>k = 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Australia</td>
<td>1973Q1–1998Q4</td>
<td>0.064</td>
<td>0.010</td>
<td>0.019</td>
<td>−0.085</td>
<td>−0.021</td>
</tr>
<tr>
<td>Australia</td>
<td>1984Q1–1998Q4</td>
<td>0.023</td>
<td>0.021</td>
<td>−0.031</td>
<td>0.060</td>
<td>−0.026</td>
</tr>
<tr>
<td>Canada</td>
<td>1973Q1–1998Q4</td>
<td>−0.031</td>
<td>0.010</td>
<td>−0.074</td>
<td>−0.028</td>
<td>0.004</td>
</tr>
<tr>
<td>France</td>
<td>1973Q1–1998Q4</td>
<td>0.225&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.226&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.145</td>
<td>0.157</td>
<td>0.064</td>
</tr>
<tr>
<td>France</td>
<td>1979Q2–1998Q4</td>
<td>0.325&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.323&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.254&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.325&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.230&lt;sup&gt;a&lt;/sup&gt;</td>
</tr>
<tr>
<td>Germany</td>
<td>1973Q1–1998Q4</td>
<td>0.166</td>
<td>0.258&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.115</td>
<td>0.013</td>
<td>0.001</td>
</tr>
<tr>
<td>Germany</td>
<td>1979Q2–1998Q4</td>
<td>0.260&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.460&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.284&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.126</td>
<td>0.125</td>
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<tr>
<td>Italy</td>
<td>1973Q1–1998Q4</td>
<td>0.285&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.228&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.235&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.244&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.116</td>
</tr>
<tr>
<td>Italy</td>
<td>1979Q2–1998Q4</td>
<td>0.245&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.222&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.229</td>
<td>0.207</td>
<td>0.174</td>
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<tr>
<td>Japan</td>
<td>1973Q1–1998Q4</td>
<td>0.050</td>
<td>0.147</td>
<td>0.106</td>
<td>0.063</td>
<td>−0.010</td>
</tr>
<tr>
<td>New Zealand</td>
<td>1973Q1–1998Q4</td>
<td>0.141</td>
<td>0.217&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.147</td>
<td>0.216&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.030</td>
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<tr>
<td>New Zealand</td>
<td>1985Q1–1998Q4</td>
<td>−0.100</td>
<td>0.076</td>
<td>−0.200</td>
<td>0.037</td>
<td>−0.237</td>
</tr>
<tr>
<td>United Kingdom</td>
<td>1973Q1–1998Q4</td>
<td>0.043</td>
<td>0.064</td>
<td>0.065</td>
<td>0.026</td>
<td>−0.035</td>
</tr>
<tr>
<td>United States</td>
<td>1973Q2–1998Q4</td>
<td>−0.103</td>
<td>−0.078</td>
<td>0.063</td>
<td>0.064</td>
<td>0.055</td>
</tr>
</tbody>
</table>

<sup>a</sup>. Significant at 0.05 level.
Table 4: Nominal exchange rate change / inflation correlations, annual data

<table>
<thead>
<tr>
<th>Country</th>
<th>Sample Period</th>
<th>$k = 0$</th>
<th>$k = 1$</th>
<th>$k = 2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Australia</td>
<td>1973–1998</td>
<td>−0.052</td>
<td>−0.128</td>
<td>−0.110</td>
</tr>
<tr>
<td>Australia</td>
<td>1984–1998</td>
<td>−0.057</td>
<td>0.175</td>
<td>0.331</td>
</tr>
<tr>
<td>Canada</td>
<td>1973–1998</td>
<td>−0.082</td>
<td>−0.029</td>
<td>0.033</td>
</tr>
<tr>
<td>France</td>
<td>1973–1998</td>
<td>0.336</td>
<td>0.142</td>
<td>0.091</td>
</tr>
<tr>
<td>France</td>
<td>1979–1998</td>
<td>0.467*</td>
<td>0.316</td>
<td>0.281</td>
</tr>
<tr>
<td>Germany</td>
<td>1973–1998</td>
<td>0.223</td>
<td>0.062</td>
<td>−0.340</td>
</tr>
<tr>
<td>Germany</td>
<td>1979–1998</td>
<td>0.491*</td>
<td>0.289</td>
<td>−0.185</td>
</tr>
<tr>
<td>Italy</td>
<td>1973–1998</td>
<td>0.398*</td>
<td>0.280</td>
<td>0.168</td>
</tr>
<tr>
<td>Italy</td>
<td>1979–1998</td>
<td>0.393</td>
<td>0.286</td>
<td>0.269</td>
</tr>
<tr>
<td>Japan</td>
<td>1973–1998</td>
<td>0.167</td>
<td>0.103</td>
<td>0.007</td>
</tr>
<tr>
<td>New Zealand</td>
<td>1973–1998</td>
<td>0.180</td>
<td>0.298</td>
<td>0.199</td>
</tr>
<tr>
<td>New Zealand</td>
<td>1985–1998</td>
<td>−0.083</td>
<td>0.463*</td>
<td>0.549*</td>
</tr>
<tr>
<td>United Kingdom</td>
<td>1973–1998</td>
<td>0.113</td>
<td>−0.026</td>
<td>−0.154</td>
</tr>
<tr>
<td>United States</td>
<td>1973–1998</td>
<td>−0.140</td>
<td>0.131</td>
<td>0.217</td>
</tr>
</tbody>
</table>

*a. Significant at 0.05 level.*

To investigate this, we now look at the same correlation in the GM model and in our open-economy model. We use a common monetary policy rule for both models, namely rule (9’) of Section 3.\textsuperscript{27} The policy shock standard deviation is set to 0.8% (annualised), which is the approximate estimated residual standard deviation for that estimated equation.

\textsuperscript{27} We have verified that our results in this section are robust to alternative plausible rules, such as those estimated for the US by Clarida, Galí, and Gertler (2000).
We therefore solved and simulated two alternative open-economy specifications, running each under two alternative price-setting specifications. The two price setting specifications used were Calvo and a version of Fuhrer-Moore (FM) (1995). The reason for our use of FM as well as Calvo pricing is that the latter has been criticised as implying far too little inertia in inflation dynamics (see Mankiw, 2001, for a recent discussion). For the MN model, using FM-type price setting instead of Calvo means replacing $\beta E\Delta p_{t+1}$ in equation (7) with the mixed backward/forward term $\beta [0.5\Delta p_{t-1} + 0.5E\Delta p_{t+1}]$, with symmetric weights on lagged and expected future inflation. For the GM model, it involves a corresponding replacement of the $\beta E\Delta p^H_{t+1}$ term in (16), leading to

$$\Delta p_t^H = \beta [0.5\Delta p_{t-1}^H + 0.5E\Delta p_{t+1}^H] + \lambda mc_t$$

(22)

instead of equation (16).

We then calculated the correlations implied by the models between quarterly inflation ($\Delta p_t$) and nominal exchange rate change, $\Delta s_{t-k}$. For each model, the results reported in Table 5 are averages of statistics across 100 simulations of 200 observations of artificial data.

Examination of Table 5 indicates that the correlations are sensitive to the choice of price-setting specification, and even more so to the choice of open-economy specification. Specifically, the contemporaneous correlation between $\Delta p_t$ and $\Delta s_t$ is strong in the GM model—0.83 when the Calvo price setting is used, 0.70 under FM price setting. The empirical evidence presented in Tables 3 and 4 provided no support for such a tight relationship (at any lag). Our alternative specification, on the other hand, implies a looser—and more realistic—relationship between inflation and exchange rate change. The correlations between the two series (at any lag of $\Delta s_t$) tend to be positive but weak; similarly, in the data in Table 3, the maximum correlation between $\Delta p_t$ and $\Delta s_{t-k}$ is no higher than 0.33 in 13 out of 14 cases.

Because our model constrains the extent to which inflation is driven by the exchange rate, it is also more successful at generating inflation persistence. This is evident in Figures 5 and 6, which plot the vector autocorrelation function for $[\Delta s_t \Delta p_t]^T$ for the GM and MN models. Figure 5 uses Calvo price setting; Figure 6, FM price setting.
In the GM model, $\Delta s_t$ fluctuations so dominate $\Delta p_t$ behaviour that inertia in domestic goods inflation generally fails to produce inflation persistence. Indeed, the autocorrelations of $\Delta p_t$ are close to zero in that model, regardless of price setting specification. By contrast, in the MN model, assumptions about gradual price adjustment on the part of domestic price-setters translate directly into assumptions about gradual adjustment of the aggregate consumer price index. As a result, $\Delta p_t$ exhibits a high degree of persistence, close to that in the data, and does so for both price-setting specifications.

Figures 7 and 8 depict the responses of inflation to a monetary policy shock (an unanticipated 100 basis point increase in $R_t$) in the GM and MN models.\(^{28}\) Calvo price setting (Figure 7) tends to produce a strong spike in inflation in the period of the shock. This is not consistent with much empirical evidence from VARs. Of the two open-economy specifications, the GM model produces a much larger—and therefore less plausible—reaction of inflation, because the policy tightening produces a large appreciation that in turn substantially reduces inflation in the model. In Figure 8, FM pricing does produce a gradual response of inflation in the MN model, but not in the GM model. Again, this lack of smoothness reflects the dominance of $\Delta s_t$ movements for $\Delta p_t$ behaviour in the GM model.\(^{29}\)

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\(^{28}\) We focus on the effects of a policy shock because this shock, unlike the risk premium (UIP) shock, is white noise, so impulse response functions more clearly reflect differences in the models’ dynamic structure (rather than shock dynamics).

\(^{29}\) Inflation dynamics also look smoother in the MN than in the GM model if we examine impulse response functions for a UIP shock.
5. Relevance for policy

The dynamic relationship between exchange rates and inflation implied by the structure of the MN model helps shed light on the experience of some small OECD economies during the East Asian currency crisis of 1997–1998. Australia, Canada, and New Zealand experienced double-digit depreciations of their trade-weighted exchange rates during this period. For a time, the monetary authorities of Canada and New Zealand tightened monetary policy in the belief (which, with hindsight, looks mistaken) that such a move was required to meet their inflation target. In Australia, on the other hand, monetary policy was not tightened. Of the three countries, the monetary policy response in Australia appears to have been the most appropriate, in that it was consistent with continued strong economic growth and maintenance of inflation on target.\(^{30}\)

In Figure 9, we depict a simple experiment intended as a stylised version of the effect of a shock such as the Asian crisis. We plot the responses of \(s_t\), \(4^* \Delta p_t\), \(y_t\) and \(4^* R_t\) to a 5% shock to the UIP condition (8) in our model. The UIP shock produces a 10% depreciation of \(s_t\) that wears off over time. Annualised inflation \(4^* \Delta p_t\) rises by a comparatively modest amount, less than 1 percentage point. The depreciation leads to an export boom and hence a rise in output \(y_t\). The interest rate \(R_t\), which continues to be determined by the policy rule (9''), actually declines by around 10 basis points (annualised) in the wake of the shock. The reason is that the temporary rise in the level of output produces anticipations of lower future \(\Delta y_t\), thus reducing expected nominal income growth, to which monetary policy responds. While the result that \(R_t\) declines is special to rule (9''), and would not hold if we had used rules (such as (9)) that respond to current values of inflation or the output gap level, our finding that the exchange rate depreciates by a large amount but inflation rises only moderately is robust to alternative policy rules.

By contrast, the same shock in the GM model leads to a rise in annualised inflation of over 5 percentage points. The responses for the GM model are not reported in Figure 9 because the inflation response in the GM model dwarfs that in the MN model, distorting the scale of the graph.\(^{31}\) Thus, of the two models, only the MN model can provide an

\(^{30}\) For discussions of this episode, see Bean (2000, pp. 77–78) McKibbin and Vines (2000), Mishkin and Schmidt-Hebbel (2001), and Svensson (2001).

\(^{31}\) The interest rate responses, on the other hand, are not too different in the GM and MN models, provided policy rule (9'') is used. They are very different if the Taylor rule (9), which responds to current inflation, is used. As an example, consider rule (9) specialised to \(\mu_1 = 0.5, \mu_2 = 0\) (the pure inflation targeting case). A 5% UIP shock then leads to a rise in annualised inflation of 5% in the GM model and a nominal interest
explanation for why an episode such as the Asian crisis can be associated with a sharp depreciation but little rise in either inflation or nominal interest rates. More generally, it appears that our model performs better than the more standard GM model in terms of matching the dynamic behaviour of nominal variables.

A more general point about our model for policy is that its implications regarding the control of inflation in an open economy differ sharply from those of standard NOEM models. In those models, the introduction of open-economy elements radically changes aggregate price-setting behaviour. As imports are final goods in these models, the implied Phillips curve has total consumer price inflation dependent not only on the output gap but also on the real exchange rate or terms of trade. In evaluating the implications of a domestic or foreign shock for inflation, it is insufficient for the monetary authority to consider only the shock’s effect on the output gap. Controlling inflation in an open economy thus involves considering channels that arise from the openness of the economy.

By contrast, in our framework, it is useful to think of the implications for inflation of any shock in terms of its effect on the output gap alone. In this sense, our model implies less of a contrast between inflation control in an open economy and inflation control in a closed economy. The effect of open-economy elements in our model is to increase the variety of shocks in the model that affect the output gap, not to create a separate channel besides the output gap through which monetary policy affects inflation. In general, our model provides little support for inflation-targeting central banks to be driven to large increases in interest rates in the face of even significant exchange rate depreciations, unless the depreciations are associated with large increases in output above potential.

6 Conclusion

In this paper we have discussed variants of an optimising open-economy model that we first used in McCallum and Nelson (1999a). Compared to more standard models in the new open economy macroeconomics (NOEM) literature, the model treats imports in a way that offers advantages both in terms of simplicity and empirical performance. The model’s dynamic properties as judged by impulse response functions seem quite sensible. Most notably, the model appears to be considerably more realistic regarding inflation dynamics than standard alternatives. This is a crucial property given that NOEM models have been designed primarily for monetary policy analysis.

rate increase of 750 basis points (annualised), compared to rises of only 0.5% and 80 basis points, respectively, in the MN model.
Appendix: Results with effective exchange rate

Table 3 in Section 4 gave correlations between quarterly changes in the CPI and in the nominal bilateral US dollar exchange rate for several countries. Table A1 below repeats the exercise using the log-change in the nominal effective exchange rate to measure $\Delta_s_t$.

As in Section 4, the only countries for which there appears to be much of a bivariate relationship between $\Delta p_t$ and $\Delta s_{t-k}$ are France, Germany, Italy, and New Zealand. The strongest correlation, 0.47, is between inflation and prior exchange rate change in New Zealand over the floating rate period. The magnitude of this correlation is largely due to the period 1985–1986, when an upsurge in inflation was preceded by a violent depreciation of New Zealand’s nominal effective exchange rate. Part of this correlation may, however, be spurious, because measured inflation in New Zealand in 1985–1986 was boosted by an unwinding of price controls and a shift to indirect taxation. Therefore, the table also reports as a memo item the correlation between $\Delta p_t$ and $\Delta s_{t-k}$ in New Zealand for 1987Q1–2000Q4, which excludes the mid-1980s but includes the large depreciation of recent years. The correlation between $\Delta p_t$ and $\Delta s_{t-k}$ is then insignificant.
Table A1: Nominal exchange rate change / inflation correlations, quarterly data, effective exchange rate indices

<table>
<thead>
<tr>
<th>Country</th>
<th>Sample Period</th>
<th>( k = 0 )</th>
<th>( k = 1 )</th>
<th>( k = 2 )</th>
<th>( k = 3 )</th>
<th>( k = 4 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Australia</td>
<td>1973Q1–1998Q4</td>
<td>0.166</td>
<td>0.051</td>
<td>0.003</td>
<td>−0.020</td>
<td>0.015</td>
</tr>
<tr>
<td>Australia</td>
<td>1984Q1–1998Q4</td>
<td>0.193</td>
<td>0.182</td>
<td>0.111</td>
<td>0.176</td>
<td>0.101</td>
</tr>
<tr>
<td>Canada</td>
<td>1973Q1–1998Q4</td>
<td>−0.087</td>
<td>0.016</td>
<td>−0.027</td>
<td>−0.045</td>
<td>0.020</td>
</tr>
<tr>
<td>France</td>
<td>1973Q1–1998Q4</td>
<td>0.204(^a)</td>
<td>0.209(^a)</td>
<td>0.219(^a)</td>
<td>0.217(^a)</td>
<td>0.121</td>
</tr>
<tr>
<td>France</td>
<td>1979Q2–1998Q4</td>
<td>0.324(^a)</td>
<td>0.280(^a)</td>
<td>0.315(^a)</td>
<td>0.342(^a)</td>
<td>0.202</td>
</tr>
<tr>
<td>Germany</td>
<td>1973Q1–1998Q4</td>
<td>0.008</td>
<td>0.006</td>
<td>−0.087</td>
<td>−0.055</td>
<td>0.010</td>
</tr>
<tr>
<td>Germany</td>
<td>1979Q2–1998Q4</td>
<td>0.126</td>
<td>0.226(^a)</td>
<td>0.030</td>
<td>0.031</td>
<td>0.160</td>
</tr>
<tr>
<td>Italy</td>
<td>1973Q1–1998Q4</td>
<td>0.369(^a)</td>
<td>0.234(^a)</td>
<td>0.215(^a)</td>
<td>0.249(^a)</td>
<td>0.240(^a)</td>
</tr>
<tr>
<td>Italy</td>
<td>1979Q2–1998Q4</td>
<td>0.185</td>
<td>0.169</td>
<td>0.156</td>
<td>0.125</td>
<td>0.160</td>
</tr>
<tr>
<td>Japan</td>
<td>1973Q1–1998Q4</td>
<td>0.039</td>
<td>0.145</td>
<td>0.166</td>
<td>0.097</td>
<td>0.022</td>
</tr>
<tr>
<td>New Zealand</td>
<td>1973Q1–1998Q4</td>
<td>0.101</td>
<td>0.220(^a)</td>
<td>0.149</td>
<td>0.418(^a)</td>
<td>0.057</td>
</tr>
<tr>
<td>New Zealand</td>
<td>1985Q1–1998Q4</td>
<td>−0.006</td>
<td>0.204</td>
<td>0.154</td>
<td>0.470(^a)</td>
<td>0.027</td>
</tr>
<tr>
<td>United Kingdom</td>
<td>1973Q1–1998Q4</td>
<td>0.068</td>
<td>0.091</td>
<td>0.159</td>
<td>0.168</td>
<td>0.083</td>
</tr>
</tbody>
</table>

**Memo item:**
New Zealand 1987Q1–2000Q4 −0.081 −0.183 −0.071 0.149 0.049

*Note:* Inflation series is the same as that used in the text. Source for effective nominal exchange rate is *IFS* except: Australia, where \( s \) is inverse of log quarterly average of Trade Weighted Index (source: Reserve Bank of Australia web page, www.rba.gov.au); and UK, where \( s \) from 1975 is inverse of log quarterly average Bank of England effective exchange rate series (spliced into *IFS* series prior to 1975).

*\(^a\)* Significant at 0.05 level.
References


Figure 1: Responses to Unit Shock to Policy Rule
Figure 2: Responses to Unit Shock to Policy Rule, sigma star = 1.0
Figure 3: Responses to Unit Shock to UIP Condn., sigma star = 1.0
Figure 4: Responses to Unit Shock to ystar. sigma star = 1.0
Figure 5: Vector Autocorrelations: Calvo price setting
Figure 6: Vector Autocorrelations: FM price setting
Figure 9: Responses to 5% Shock to UIP Condition