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Do real interest rates converge? Evidence from the European Union


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Do real interest rates converge? Evidence from the European Union

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Do real interest rates converge?

Evidence from the European Union

by

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Abstract

We test for real interest parity (RIP) in the EU25 area. Our contribution is two-fold: First, we account for the previously overlooked effects of structural breaks on real interest rate differentials. Second, we test for RIP against the EMU average. For the majority of our sample countries we obtain evidence of real interest rate convergence towards the latter. Convergence, however, is a gradual process subject to structural breaks, typically falling close to the launch of the euro. Our findings have important implications relating to the single monetary policy and the progress new EU members have achieved towards joining the euro.

Keywords: real interest rate parity; convergence, structural breaks; EU; EMU;

JEL classification: F21, F32, C15, C22

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1. INTRODUCTION

Uncovered Interest Parity (UIP) and Purchasing Power Parity (PPP), two cornerstone parity conditions in international macroeconomics, imply, when combined, that expected real returns are equalised across countries. This proposition, known as Real Interest Parity (RIP), has significant implications for international investors and policy-makers alike: If national real interest rates were bound to converge, the scope for international portfolio diversification would be significantly reduced; and national monetary policy as a tool of effective macro-management would be restricted to the degree it affects the international real interest rate (see Mark, 1985).1

Due to its important consequences, RIP has attracted considerable empirical attention. The existing literature has mainly focused on RIP against the USA evolving significantly over time. Early studies, such as Mishkin (1984a, 1984b), Cumby and Obstfeld (1984) and Mark (1985) tested, and generally rejected, RIP by imposing unity restrictions on the intercept and slope coefficients in regressions of domestic on foreign real interest rates. These, however, were criticised for overlooking possible unit roots in the regression’s variables. A number of authors subsequently tested for cointegration between the two rates, typically finding mean reversion for the residuals of the cointegrating regression.2 Nevertheless, this approach was also criticised for allowing the coefficient of the foreign real interest rate to deviate from its theory-consistent unity value. Hence, the literature moved towards RIP tests based on real interest rate differentials (RIRDs) where unity coefficients are by definition imposed.3

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1 As RIP underpins a number of mainstream monetary models of exchange determination (see e.g. Frenkel 1976, Frankel 1979, Mussa 1982) its validity is also important for our understanding of exchange rate movements and the authorities’ ability to manage them.
3 Alternative tests of RIP include MacDonald and Taylor (1989) and Fraser and Taylor (1990), who test and reject the RIP-consistent hypothesis according to which nominal interest rate differentials predict future inflation differentials. Marston (1995) finds that movements of RIRDs can be explained using
Early studies adopting this approach (see e.g. Meese and Rogoff, 1988 and Edison and Pauls, 1993) found unit roots in RIRDs, thus rejecting RIP. These studies, however, were based on the standard Augmented Dickey Fuller (1979, ADF) test, known to be subject to a number of drawbacks, including low power and biases in the presence of structural breaks and non-linearities. Wu and Chen (1998), Gagnon and Unferth (1995) and Ong et al. (1999) increase power through panel data tests, providing evidence in favour of RIP. More recently, a number of studies, including Obstfeld and Taylor (2002), Nakagawa (2002), Mancuso et al. (2003), Holmes and Maghrebi (2006) and Ferreira and Leon-Ledesma (2007), estimate non-linear models upholding RIRD mean-reversion, though not always around a zero value.

Overall, the recent literature has achieved significant progress towards overturning the early unit root RIRD findings. Yet, some important points remain unaddressed. Most prominently, the literature has overlooked the potential effects of structural breaks in RIRD series. Such breaks reduce further the already low power of ADF tests (see Perron, 1989) and may result in non-linear models being erroneously selected as the best description of an otherwise linear data generation process (see Koop and Potter, 2001). In recent years, a number of events that may have caused structural breaks in RIRD series have taken place. These include the introduction of market and monetary policy reforms in a number of countries and the launch of the European variables included in the current information set, leading to rejection of the RIP hypothesis. Kugler and Neusser (1993) adopt a stationary multivariate time-series framework using ex-post real interest rates, obtaining findings favourable towards RIP. A similar conclusion is reached by Cavaglia (1992) who applies Kalman filtering techniques to estimate the persistence of ex-ante real interest rate differentials. Obstfeld and Taylor (2002) increase power by using larger sample periods and a generalised least square version of the ADF test.

Non-linear adjustment to RIP is theoretically justified by market imperfections such as those in Dumas (1992). These include transaction and other sunk costs in international trading, legal obligations imposing on agents to hold assets for minimum time periods and trading rules postulating that differences between returns exceed certain thresholds before arbitrage trading is initiated. Such imperfections imply that small non-zero RIRD values are not arbitraged, while large deviations from zero trigger trading restoring RIP.

Fountas and Wu (2000) are an important exception. However, their analysis is undertaken within a cointegration framework and, as a result, is subject to the critique discussed above.
Economic and Monetary Union (EMU) in Europe in 1999. Lack of investigation of the effects of such events is surprising, particularly given that the appropriate econometric methods are now well-developed. The first contribution of this paper is to precisely fill this gap, i.e. to analyse international real interest rate convergence accounting for structural breaks in the RIRD series.

We focus on the European Union (EU), an area whose members (old and new) have all experienced one or more of the potential breaks mentioned above. Previous studies on Europe test RIP against Germany (see e.g. Holmes 2002 and 2005, Leon-Ledesma 2007). We instead test, for the first time to the best of our knowledge, RIP against the EMU average. This is the second contribution of this paper, as our analysis provides important insights relating to the workings of the single currency. The reason is the following: The European Central Bank (ECB) operates under an institutional mandate to set nominal interest rates for the EMU average. The ECB 2 per cent inflation objective also refers to the EMU average. In practise, therefore, the ECB is meant to conduct monetary policy in the interests of the Euroland as a whole by way of managing the EMU average real interest rate (see Aksoy et al, 2002).\footnote{Aksoy et al (2002) argue that this institutionally-mandated “euro-wide” conduct of the single monetary policy would be welfare maximizing. There is no hard evidence to suggest that this policy is not implemented in practise, although in a recent paper Heinemann and Hufner (2004) argue that it is possible that small EMU countries have an excessive, relative to their size, weight in the ECB decision making process.} Changes in the latter are exactly the channel through which the single monetary policy is meant to be transmitted to the eurozone’s individual economies. For transmission to be uniform, national RIRDs against the EMU average must be mean-reverting and display similar persistence patterns. If the opposite is true, shifts in the eurozone average-oriented ECB policy would result in intra-EMU asymmetric monetary shocks, posing member-states with differential, and potentially unwelcome, output gap and asset prices’ responses. All in all, the degree of convergence of national real interest rates towards the EMU average
conveys important information relating to the “one size fits all” monetary policy debate. Furthermore, by assuming both UIP and PPP, RIP is a comprehensive measure of economic integration among countries that are candidates to form a common currency area. As textbook monetary union theory suggests, the net cost of abolishing national currencies is a negative function of the degree of integration between the prospective union’s member states. Hence, the degree of real interest rate convergence between the new EU members and the EMU average provides useful insights relating to the progress the former have achieved towards adopting the euro.

Our econometric analysis is comprehensive as it covers all but one EU25 countries. Following the majority of existing studies, it is based on ex-post real interest rates calculated using identical definitions for nominal interest and inflation rates (see section 2 below). This eliminates biases due to invalid approximations of inflation expectations (see e.g. Ferreira and Leon-Ledesma, 2007) and/or non-identical definitions of real returns (see e.g. Dutton, 1993). Data availability defines our sample to cover 1996-2005 (monthly frequency), a decade characterised by full capital mobility within Europe, free, in relation to the new EU countries, from the original shock of transition of the early 1990s. We extend the standard ADF unit root tests first by correcting for residuals’ heteroscedasticity and normality applying the wild-bootstrap simulation technique used by Argyrou and Gregoriou (2007); then by accounting for the effects of structural breaks on RIRD series. These turn out to be captured by the minimum Lagrange Multiplier (LM) unit root test by Lee and Strazicich (2003), which allows for two endogenous structural breaks in the series’ level and/or trend and has superior econometric properties against alternative endogenous single-breaks tests, such as the one by Perron (1997).

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8 Due to data limitations, we had to exclude Luxembourg from our analysis.
Our findings turn out to be novel and interesting: First, we reject the null of unit root RIRD behaviour for 21 out of 24 sample countries. Allowing for two rather than one or no structural breaks is critical in this respect. Second, structural breaks fall close to important economic events, most prominently (but not exclusively) the euro’s launch in 1999. Third, we find evidence of rapid real interest rate convergence in the EMU area prior to 1999 followed by divergence between some “core” and “periphery” EMU countries (as well as the UK) thereafter. Fourth, we find that most (though not all) of the new EU members have achieved convergence to the EMU average by the end of 2005. Overall, our findings are generally favourable towards RIP in the EU area. Convergence, however, is found to be a gradual process subject to structural breaks. In addition, there exist some important country-specific exceptions for which convergence is rejected.

The remainder of the paper is structured as follows: Section 2 outlines our testing methodology. Section 3 describes the data. Section 4 discusses our empirical findings. Finally, section 5 summarises and offers concluding remarks.

2. DATA

Real interest rate differentials can be calculated using either ex-ante or ex-post real returns, as well as alternative definitions for nominal interest and inflation rates. Following the majority of existing studies we use ex-post real returns so as to bypass the empirically tricky subject of approximating empirically inflation expectations. Also, to minimize the influence of factors such as foreign-exchange risk, whose role is more prominent in interest rates of longer-maturity (see e.g. Ferreira and Leon-Ledesma, 2007), we define nominal interest rates as the three-month money market rate. Finally, to eliminate biases relating to different definitions of national price levels (see e.g.
Dutton, 1993), inflation rates are calculated for all countries using the harmonised consumer price index (HCPI).

HCPI data is available for the post-1996 period only. This defines our sample to cover 1996-2005 (a total of 120 monthly observations), a period when the vast majority of capital controls had been abolished in the EU area. Data for three-month money market rates and HCPI series is taken from the Eurostat Databank provided by Datastream. The monthly HCPI series exhibit strong seasonality patterns for which we account by seasonal adjustment. As we consider investments of three-month maturity, we transform the quoted annualised three-month nominal interest rates into a three-month continuously compounded nominal rate of return. Then, following Ferreira and Leon-Ledesma (2007), for every period \( t \) we calculate ex-post real interest rates \( r_t \) as the difference between the three-month continuously compounded nominal rate of return observed in period \( t-3 \) \( (i_{t-3, t}) \) minus the percentage change of the HCPI recorded between period \( t-3 \) and \( t \) \( (\pi_{t-3, t}) \). Our analysis, therefore, is based on real rates of return on investments lasting for three months, calculated by \( r_t = (i_{t-3, t}) - (\pi_{t-3, t}) \). These rates are then used to construct the RIRD series against the EMU average denoted by \( (r - r^*) \). The latter, \( r^* \), is calculated using the EMU three-month money market rate and HCPI series provided by Datastream. Hence, \( r^* \) is a weighted average of national real returns with the weights determined by the source of our data, Eurostat.

Table 1 presents the series’ summary statistics. Three features stand out. First, RIRDS in the pre-2004 EU countries (EU15), and in particular in the current EMU ones, are on average smaller and less volatile than those of the new EU members (i.e. the ten countries that joined the EU in 2004). Furthermore, real interest rates in the former

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9 For the old EU members our sample period is three months longer, extending to 1996.03
10 We adjust the series using the Census X11 multiplicative seasonal adjustment method, used by the US Bureau of Census to seasonally adjust publicly released data. The X11 routine is available in EViews.
group are on average more highly correlated with the EMU average. Second, there exist important differences among individual countries within the same group. For example, average RIRD in the core EMU countries are in absolute value lower than in the EMU periphery. Similar differences are also observed within the opt-out EU countries (Denmark, Sweden and the UK) and the new EU members. Finally, for the majority of our sample countries the estimated RIRD series and are not normally distributed, a strong indication for the existence of structural breaks.

3. EMPIRICAL METHODOLOGY

The benchmark test of RIP has been widely discussed in the literature (see e.g. Ferreira and Leon-Ledesma, 2007) so to preserve space we do not present its derivation here. We restrict ourselves in saying that this is based on the stochastic model given by equation (1) below:

\[(r - r^*)_t = \alpha + \rho (r - r^*)_{t-1} + \mu_t\]  

where \(\mu_t\) is a white noise error. Equation (1) can be reformulated as an autoregressive model of order \(k\) given by equation (2)

\[\Delta(r - r^*)_t = \alpha + \phi (r - r^*)_{t-1} + \sum_{i=1}^{k} \beta_i \Delta(r - r^*)_{t-i} + \mu_t\]  

where \(\phi = \sum_{i=1}^{k} \rho_i - 1\) and \(\sum_{i=1}^{k} \rho_i = \rho\). Equation (2) is an Augmented Dickey-Fuller (ADF) regression where \(\phi > 0\) (corresponding in equation (1) to \(\rho > 1\)) describes an explosive process; \(\phi = 0\) (\(\rho = 1\)) random walk behaviour; \(\phi < 0\) and \(\alpha \neq 0\) (\(\rho < 1\) and \(\alpha \neq 0\)), stationarity around a non-zero mean; and \(\phi < 0\) and \(\alpha = 0\) (\(\rho < 1\) and \(\alpha = 0\)) stationarity

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11Throughout this paper we define core EMU countries to be those EMU members empirical literature had identified as belonging to a European optimum currency area prior to the introduction of the euro (see e.g. Bayoumi and Eichengreen 1993). These include France, Germany, Austria and the Benelux countries.
around a zero mean. Out of these conditions only the last one is consistent with RIPR. Equations (1) and (2) can also include a trend term to test for trend- rather than level-stationarity. In the steady-state, trend stationarity is not consistent with RIP. However, within a finite sample, a significant trend term might imply (though not necessarily) deterministic convergence towards RIP (see section 4 below).

The standard ADF test is known to be subject to a number of drawbacks potentially leading to biased inference. These include deviations from the assumption of iid distribution for the residual term $u_t$ in equation (2), as well as structural breaks in the series tested for stationarity.\footnote{In addition, the standard ADF test does not capture non-linear mean reversion although, it should be kept in mind, rather than genuine the latter may be a reflection of either a small number of outliers (see van Dijk et al, 1999), or structural breaks in the series tested for stationarity (see Koop and Potter, 2001). We would have liked to investigate the existence of non-linearities in RIRD series over the three sub-samples identified by our analysis below, however we could not do so due to the resulting small number of observations in each of the three sub-samples.} Regarding the former, given the evidence presented in Table 1, it is reasonable to expect that the error terms of our preferred ADF specifications may be non-normal. We address this problem following Arghyrou and Gregoriou (2007), who correct the critical values of the standard ADF test for heteroscedasticity and non-normality using the wild bootstrap simulation technique described in the Appendix. As far as structural breaks are concerned, Perron’s (1989) initial approach to account for them was to allow for a single exogenously imposed structural break under both the null and alternative hypotheses. Subsequent literature has emphasized the need to determine the break endogenously from the data (see e.g. Zivot and Andrews, 1992; Perron, 1997).\footnote{As these tests have been extensively used in the literature, we do not discuss them here.} More recently, the endogenous two-break minimum LM unit-root test of Lee and Strazicich (LS, 2003) counterbalances the potential loss of power of tests that ignore more than one break. The test includes breaks under both the null and the alternative hypotheses, with rejections of the null
unambiguously implying stationarity.\textsuperscript{14} Focusing on RIRD series, a brief description of the test by LS has as follows: Consider the data generating process described by

\[(r-r^\ast)_t = \delta' Z_t + \eta_t , \quad \eta_t = \lambda \eta_{t-1} + \theta_t\]  \hspace{1cm} (3)

where \(Z_t\) is a vector of exogenous variables and \(\theta_t \sim iid N (0, \sigma_\theta^2)\). LS analyze two alternative models: First, Model A that allows for two shifts in the level of real interest rate differentials: \(Z_t = [1, t, D_{t1}, D_{t2}]\), where \(D_{jt} = 1\) for \(t \geq T_{bj} + 1 \) \((j=1,2)\) and 0 otherwise. \(T_b\) indicates the time period when a break occurs. Second, Model C that allows for two shifts in the series’ level and trend: \(Z_t = [1, t, D_{t1}, D_{t2}, DT_{t1}, DT_{t2}]\), where \(DT_{jt} = t - T_{bj}\) for \(t \geq T_{bj} + 1 \) \((j=1,2)\) and 0 otherwise. In Model A, the null and alternative hypotheses are given by equations (4) and (5), respectively:

\[
(r-r^\ast)_t = \mu_0 + d_1 B_{jt} + d_2 B_{jt} + (r-r^\ast)_{t-1} + \nu_{lt}\]  \hspace{1cm} (4)

\[
(r-r^\ast)_t = \mu_1 + \gamma t + d_1 D_{jt} + d_2 D_{jt} + \nu_{lt}\]  \hspace{1cm} (5)

where the error terms \((\nu_{lt}, \nu_{2t})\) are stationary processes; \(B_{jt} = 1\) for \(t = T_{bj} + 1 \) \((j=1,2)\) and 0 otherwise. For Model C, we add the previously defined \(D_{jt}\) terms to (4) and \(DT_{jt}\) terms to (5), respectively. An LM score principle is used to estimate the LS unit root test statistic based on the following regression model:

\[
\Delta(r-r^\ast)_t = \delta' \Delta Z_t + \phi \tilde{S}_{t-1} + \sum_{i=1}^{k} \gamma_i \Delta \tilde{S}_{t-i} + \omega_t\]  \hspace{1cm} (6)

where \(\tilde{S}_t = (r-r^\ast)_t - \tilde{\psi}_s - Z_t \tilde{\delta} ; t = 2, \ldots, T; \tilde{\delta}\) are coefficients in the regression of \(\Delta(r-r^\ast)_t\) on \(\Delta Z_i; \tilde{\psi}_s = (r-r^\ast)_1 - Z_1 \tilde{\delta}\), where \((r-r^\ast)_1\) and \(Z_1\) denote the first observations of \((r-r^\ast)_t\) and \(Z_t\), respectively; and \(\Delta \tilde{S}_{t-i}\) terms \((i=1, \ldots, k)\) are included

\textsuperscript{14} The null hypothesis in the endogenous two-break unit root test of Lumsdaine and Papell (1997) assumes no structural breaks, while the alternative does not necessarily imply broken trend stationarity. Thus, rejecting the null may be interpreted as rejection of a unit root with no structural break, and not necessarily as rejection of a unit root per se.
to account for serial correlation. We can consequently test the unit root null hypothesis by examining the t-statistic ($\tilde{r}$) associated with $\phi = 0$.

Following LS we determine the lag length of the $\Delta \tilde{S}_{t-i}$ terms using a general to specific approach. More specifically, at each combination of break points $\lambda = (\lambda_1, \lambda_2)'$ in the time interval $[0.1T, 0.9T]$ we start from a maximum of $k = 12$ (due to monthly frequency) terms and reduce the model according to whether the last term is significant at the 10% level. If not, the last term is dropped and the model is re-estimated with $k = 11$ terms. The process is repeated until a non-zero maximum augmented term is found; or $k$ is set to zero. The minimum LM unit root test determines the time location of the two endogenous breaks, $\lambda_j = T_{bj} / T$, $j = 1, 2$, using a grid search as follows:

$$\text{LM}_r = \inf_{\lambda} \tilde{r}(\lambda)$$

The break points are located where the test statistic is minimized. Compared to the structural breaks tests by Zivot and Andrews (1992) and Perron (1997) the minimum LM unit root test shares the endogenous identification of breaks. However, as LS (2003) demonstrate, it has comparable or higher power, allows for two rather one structural breaks, and is not subject to spurious rejections of the null when the series is unit root with breaks. Hence, the minimum LM test has the significant advantage that rejection of the null unambiguously implies convergence.\(^{18}\)

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\(^{15}\) As Strazicich et al (2004, p. 135) argue, this approach has been shown to perform well when compared to alternative data-dependent methods to select the number of the lagged augmented terms (see e.g. Ng and Perron, 1995).

\(^{16}\) Following LS (2003) we exclude the first and last quintile of the data from this interval so as to ensure that breaks are not located at the series' end-points.

\(^{17}\) LS (2003) also propose an alternative minimum LM unit root test, $\text{LM}_\rho$, determining the time location of the two breaks using a grid search given by $\text{LM}_\rho = \inf_{\lambda} \hat{P}(\lambda)$. As results between the two test’s variants turned out to be very similar, we only discuss those obtained from the $\text{LM}_r$ statistic.

\(^{18}\) A drawback of the minimum LM unit root test is that it does not allow for more than two structural breaks. However, tests of this kind, not subject to the critique of spurious rejection of the null, are not yet available to empirical researchers. Bai and Perron (2003) have developed a popular test capturing
4. EMPIRICAL FINDINGS

4.1. Stationarity analysis

We first test for real interest rate convergence towards the EMU average using the standard ADF test described by equation (2). The results are reported in Table 2, column (a). At the 5 per cent level or lower we reject the null of unit root only in 10 out of 24 countries. Allowing for a trend term does not increase evidence of stationarity (see Table 2, column (b)). However, the misspecification tests estimated for the residuals of our preferred ADF models revealed non-normality and time-varying heteroscedasticity for the majority of our sample countries. We correct for heteroscedasticity and non-normality using the wild-bootstrap correction applied by Argyrou and Gregoriou (2007). This yields the confidence intervals reported in Table 2, column (c). The lower limits of these intervals provide the corrected critical values for the ADF test. Our unit root findings remain robust to this wild bootstrap correction. Indeed, for a number of countries the latter overturns the previous findings of stationarity.

We now test for stationarity using Perron’s (1997) unit root test allowing for one endogenous structural break. The results appear in Table 2, columns (d) and (e), respectively reporting the test’s results allowing for a break in the series’ level; and level and trend. Compared to the ADF tests, evidence of stationarity does not increase, as at the 5 per cent level the null of unit root is rejected only in 8 and 4 cases respectively. Furthermore, as RIRDs have been calculated against the EMU average, the multiple structural series in linear models. However, their test accounts only for shifts in a series’ mean (rather than mean and trend) and does not test the null of unit root behaviour. As a result, it is not applicable in this context of our analysis. As far as the latter is concerned, our tests reported below show that two breaks are enough to reject the null of unit root in the overwhelming majority of the examined cases.

19 To preserve space, these are not reported here but are available upon request.
20 Following Argyrou and Gregoriou (2007) we report the confidence intervals rather then the p-values, to allow for a more powerful test in the presence of extreme outliers in the data.
21 We have repeated the same analysis for the ADF test with constant and trend. The results, not reported here but available upon request, remain unaffected.
lack of stationarity for almost all EMU countries, including France and Germany, reduces significantly the plausibility of the reported results.

Finally, we implement the LM minimum unit root test by LS (2003). Our findings are presented in columns (f) and (g) of Table 2, respectively testing for stationarity with two breaks in the series’ level; and level and trend. Compared to the previous results, these make impressive reading, as between them they reject the null of unit root in 21 out of 24 countries. In these cases, selection between the two alternative model specifications (indicated with bold letters) is made on the basis of the strongest rejection of the null.\footnote{As a robustness test, we repeated the selection exercise using the Akaike information criterion. The preferred specifications remain identical to those indicated in Table 2 with bold letters.} Using this criterion, for all but two EU15 countries we select stationarity with two breaks in the series’ level and trend. For Spain, we select stationarity with two breaks in the series’ level, whereas Italy is the only EU15 country where the null is maintained. For the new EU members, the model with two breaks in level is selected for Latvia, Lithuania, Malta, Slovakia and Slovenia; while the model with breaks in level and trend is selected for Cyprus, the Czech Republic and Estonia. Finally, for Hungary and Poland we maintain the null of unit root.

4.2. Structural breaks

The results of the LM-two break unit root test provide interesting insights relating to the timing of the identified structural breaks. More specifically, our preferred specifications suggest a break in 1999, the year of EMU’s inception, in six EMU countries (Belgium, Finland, France, Germany, Ireland, and the Netherlands). For Greece we obtain a break in 2000.09, three months after the announcement of this country’s accession to the EMU. Finally, Austria, Portugal and Spain have all experienced breaks in 2000, the year following the launch of the euro. A break in 2000 may also have taken place in Italy, the only EMU country for which the LM$_t$ test
maintains the null of unit root, whereas in Spain, another break had occurred in 1998, shortly after the announcement of Spain’s inclusion in the EMU. A second, though less pervasive, cluster of breaks is observed in 2003, affecting Austria, Finland, France, Germany and Ireland, while a break of similar timing (2004) is observed for Portugal.

Breaks of timing similar to those in the eurozone have also taken place in the three opt-out EU countries. On the other hand, breaks in the new EU countries are not so evidently clustered and can be linked to more than one event. In Cyprus, the Czech Republic, Estonia, Hungary, Slovakia and Slovenia, breaks are observed in 1999-2000. Although these fall close to the launch of the euro, they may also reflect country-specific events such as the start and/or conclusion of accession negotiations with the EU, and/or reforms in the implemented framework of monetary policy. Such factors may also be relevant in explaining the breaks recorded in Cyprus and Malta in 1998, as well as Estonia and Malta in 2001 and Latvia in 2002.

All in all, our findings strongly indicate that the euro’s introduction has caused structural breaks in all EMU countries. Structural breaks in the new EU countries are more widely dispersed and, in addition to euro’s launch, may also be linked to country-specific events. Finally, the South-East Asia financial crisis of 1997 appears to have been of limited significance, as our preferred specifications suggest breaks falling close to that event only for Greece, Denmark and the Czech Republic.

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23 Formal accession negotiations between the EU and the new EU countries were introduced in two phases. First in March 1998 for the so-called Luxemburg six (Cyprus, the Czech Republic, Estonia, Hungary and Poland) followed in February 2000 by the so-called Helsinki six (Bulgaria, Latvia, Lithuania, Malta, Romania and Slovakia). Negotiations with ten of these countries were completed successfully in December 2002. The new countries joined the EU on 1 May 2004. Romania and Bulgaria joined the EMU on 1 January 2007.

24 At the beginning of our sample period all new EU countries were implementing monetary strategies involving exchange rate targets against major international currencies. However, following a number of currency devaluations in the 1990s, all Central European countries switched to an explicit inflation-targeting regime or variants of it (the Czech Republic in January 1998; Hungary in June 2001; Poland in September 1996; Slovakia in January 1999 and Slovenia in January 2002). On the other hand, the Baltic and Mediterranean countries have maintained their fixed-exchange rate policies and have joined, along with Slovakia and Slovenia, the ERM-II (Estonia, Lithuania and Slovenia joined in June 2004; Cyprus, Latvia and Malta in May 2005; and Slovakia in November 2005). Out of these countries Slovenia joined the EMU country on 1 January 2007; with Cyprus and Malta set to follow on 1 January 2008.
4.3. Convergence analysis

We now discuss the implications of the LM$_t$ unit root tests regarding real interest rate convergence in the EU area. We depict our findings in Figure 1. This presents the $(r - r^*)_t$ series calculated for all sample countries against the fitted deterministic-trend values in each of the three-sub periods defined by the two breaks points identified by our preferred minimum LM-test specifications.\footnote{For those countries where the null of unit root is maintained, the three sub-samples are defined by the model accounting for breaks in both the level and the trend of the series.} The deterministic-trend values are given by the long-run solution for $(r - r^*)$, obtained from the estimation of the autoregressive model in equation (1) including a trend term.\footnote{The results do not change when linear trends are estimated directly using ordinary least squares.}

Starting from the EMU countries, an interesting distinction emerges between the core and the periphery ones. In the former, RIRDs start from negative values and converge towards zero during the run-up to the euro. Following the latter’s introduction, breaks of differential effects are observed resulting, in positive RIRD trend values in Germany and France, and negative RIRD trend values in Austria, Belgium and the Netherlands. Finally, during the last sub-sample, deterministic trends in all countries have shifted towards zero. Having said so, at the end of our sample period (2005) these trends were set, with the exception of Belgium, towards positive RIRDs values.

The experience of periphery EMU countries is significantly different, the only exception being Finland, whose real interest rate had converged to the EMU average by the end of 2005. For the remaining countries, (Greece, Ireland, Italy, Portugal and Spain) we initially observe substantial positive RIRD trend values. These were fast reduced during the run-up to the euro, so that by the end of the first-sub sample they were in negative territory. The only exception is Greece, where RIRD did not converge to zero but actually increased further prior to euro’s introduction. Following the latter, trend RIRD values in Ireland, Greece and Spain stabilized in negative levels, whereas in
Portugal and Italy they moved towards zero. Finally, at the end of our sample we observe trends towards zero in Finland, Ireland, Portugal and Italy (although in the case of the latter the LMₜ test has maintained the null of unit root). On the other hand, trend RIRD values are negative and declining in Greece and Spain.²⁷

Moving on to the three opt-out EU countries, long-term trends towards RIP, showing relatively little change over time, are observed in Denmark and Sweden, both of which had converged to the EMU average by the end of 2005. An entirely different picture is observed for the UK where \((r – r^*)\), trends were consistently positive, deviating from the RIP-consistent zero value throughout our sample.

Finally, and in relation to the new EU countries, leaving aside secondary idiosyncrasies, four groups of countries emerge. The first consists of the Mediterranean states of Cyprus and Malta where convergence is observed, with little structural change, throughout the period under consideration. The second includes the Czech Republic, Estonia and Slovakia where, generally speaking, RIRD trends were positive-increasing during the first sub-period, positive-declining during the second sub-period; and stabilized around zero during the third sub-period. The third consists of Lithuania and Slovenia, where RIRD trends were positive-declining during the first sub-period, increasing during the second, and converging towards zero during the third. The fourth includes Latvia, Hungary and Poland, for which convergence is rejected. More specifically, the LMₜ test rejects the unit root hypothesis for Latvia, but at the same time suggests a substantially negative trend differential at the end of our sample. On the other hand, for Hungary and Poland, the unit root hypothesis is maintained and, at the same time, substantially positive RIRD values are observed in recent years.

²⁷ For Greece this is not so evident in Figure 1, due to the scale of the relevant diagramme caused by some excessively positive RIRD values in the early years of our sample. The calculated RIRD series for Greece over the period following the second identified structural break (2009.09-2006.03) has been consistently negative with an average value equal to -0.27 per cent. On an annual basis, this is higher than one percentage point.
5. SUMMARY AND CONCLUSION

This paper has tested the real interest parity (RIP) hypothesis in the EU25 area making a two-fold contribution. First, we account for the effects of the previously overlooked structural breaks in real interest rate differential (RIRD) series. Second, RIP is tested for the first, to best of our knowledge, time against the EMU average. This provides important insights relevant to the workings of the single currency and the progress achieved by the new EU members towards joining it. Our analysis covers 1996-2005 (monthly data) and is based on ex-post RIRDs, calculated using identically defined nominal and price inflation rates. Using the minimum Langrange Multiplier two-break test developed by Lee and Strazicich (2003), we provide evidence generally in favour of real interest rate convergence towards the EMU average. This, however, is a gradual process, subject to structural breaks. Furthermore, convergence is rejected for a small, but not negligible, number of countries.

Our convergence findings imply that for the majority of our sample countries the steady-state costs of losing monetary independence should in principle be not too high, especially for small countries whose ability to influence the EMU average real interest rate would be minimal either within our outside the union. In the same spirit, and as RIP is a comprehensive measure of economic integration, the convergence progress achieved by the majority of the new EU countries indicates that these countries are now significantly closer to joining the single currency than ten years ago.

These conclusions, however, may not apply in the short- and medium-run. As convergence was found to be a quite heterogeneous and gradual, at best, process, the loss of monetary independence may well imply sub-optimal economic stabilization in individual countries (see e.g. Heinemann and Huefner 2004, Hayo and Hofmann, 2006). This may be more than a merely transitory problem, as its welfare implications are
unknown and potentially significant. Addressing this question is not possible without estimating an open-economy dynamic stochastic general equilibrium model capturing the inter-temporal effects of ultimately transitory yet persistent deviations from RIP, a task beyond the scope of the present paper. Having said so, and adopting a purely financial point of view, it is plausible to argue that the observed heterogeneity in the convergence process implies that risk-averse agents would have benefited from diversifying their portfolios across EU countries rather than pursuing country-specific investment strategies during the sample period covered by our analysis.

On the other hand, in countries such as Greece, Spain and Italy, rejection of convergence implies that the adoption of the euro has caused asymmetric, relative to the rest of the EMU members, monetary shocks. These may have resulted in less transitory, and consequently more serious, economic costs such as bubbles in assets’ prices (see e.g. Fernandez-Kranz and Hon 2006) and current account deterioration beyond the degree justified by higher than EMU average economic growth (see e.g. Argyrou 2006 and Argyrou and Chortareas 2008). The experience of these countries suggests that countries such as Latvia, Hungary, Poland and, perhaps most prominently, the UK, where convergence was also rejected, adopting the euro in the foreseeable future may be significantly more costly than in the rest of the current EMU outs.

Finally, a note relating to possible extensions of our work is due. Our findings provide a solid platform to pursue further research on the question of real interest rate convergence in Europe by means of investigating the specific factors underlying the structural shifts in the RIRD series identified here. For example, the fast convergence observed in periphery EMU countries during the run up to the euro may be due to a reduction in a risk premium embodied in nominal interest rates but also, as we consider ex-post real interest rates, faster than anticipated inflation reduction. In a similar
fashion, the negative trend-differential values observed following the launch of the euro may reflect complete elimination of any previously existing risk premia as well as higher than EMU average inflation rates, potentially reflecting productivity differentials against the EMU average or a degree of incompatibility between the single monetary policy and the macro-fundamentals of these countries. These questions could be examined within a model of RIRD determination decomposing the latter’s movements as the sum of factors such as those mentioned above. Constructing and estimating such a model would provide us with further insights on the structural changes that have taken place in our sample countries, the workings of the single monetary policy and the welfare effects caused by euro participation.

REFERENCES


APPENDIX

A potential source of bias in standard ADF analysis is violations of the assumptions of normality and heteroscedasticity under which the critical values of the ADF test have been derived. In a recent paper Arghyrou and Gregoriou (2007) address this problem using a wild bootstrap simulation technique. This entails estimation of a new series given by:

\[(r_t - r^*)_t = (r_t - r^*)_t u_t\]  \hspace{1cm} (1A)

where \(u_t\) is drawn from the two-point distribution

\[u_t \begin{cases} 
-(5^0.5-1)/2 \text{ with probability } p= \frac{1+(5^0.5)}{2(5^0.5)} \\
(5^0.5+1)/2 \text{ with probability } (1-p) 
\end{cases} \]  \hspace{1cm} (2A)

The \(u_t\) terms are mutually independent drawings from a distribution independent of the original data characterised by the properties \(E(u_t) = 0, \ E(u_t^2) = 1\) and \(E(u_t^3) = 1\). Hence, any non-normality/heteroscedasticity in \(r_t\) is preserved in the created series \((r_t - r^*)_t\). We generate 10,000 sets of \((r_t - r^*)_t\) series. Subsequently, for each bootstrap iteration, a series of DF tests is constructed under the null hypothesis \(\phi = 0\). Therefore the generated sequence of artificial data has a true \(\phi\) coefficient of zero. However, when we regress the artificial DF test for a given bootstrap sample \(0t\) estimated values of \(\phi\) that differ from zero will result. This procedure provides an empirical distribution for \(\phi\) and their associated standard errors based exclusively on the re-sampling of the original series \((r_t - r^*)_t\). Therefore appropriate critical values are obtained for the null hypothesis of unit root (\(\hat{\phi} = 0\)) in equation (2). The results of this bootstrap experiment are reported in column (c) of Table 2 and discussed in section 4.1.
Table 1: Descriptive statistics of real interest rate differentials against the EMU average ($r-r^*$)

<table>
<thead>
<tr>
<th></th>
<th>Mean</th>
<th>Std Deviation</th>
<th>Normality</th>
<th>Correlation coefficient between $r$ and $r_{EMU}$</th>
</tr>
</thead>
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<tr>
<td><strong>EMU countries</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Austria</td>
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<td>0.05*</td>
<td>0.73</td>
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<tr>
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<td>0.37</td>
<td>0.18</td>
<td>0.66</td>
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<tr>
<td>Finland</td>
<td>0.04</td>
<td>0.35</td>
<td>0.00**</td>
<td>0.53</td>
</tr>
<tr>
<td>France</td>
<td>0.01</td>
<td>0.18</td>
<td>0.87</td>
<td>0.90</td>
</tr>
<tr>
<td>Germany</td>
<td>0.05</td>
<td>0.25</td>
<td>0.06+</td>
<td>0.79</td>
</tr>
<tr>
<td>Greece</td>
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<td>1.19</td>
<td>0.00**</td>
<td>0.63</td>
</tr>
<tr>
<td>Ireland</td>
<td>-0.18</td>
<td>0.48</td>
<td>0.38</td>
<td>0.72</td>
</tr>
<tr>
<td>Italy</td>
<td>0.11</td>
<td>0.38</td>
<td>0.00**</td>
<td>0.83</td>
</tr>
<tr>
<td>Netherlands</td>
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<td>0.41</td>
<td>0.00**</td>
<td>0.31</td>
</tr>
<tr>
<td>Portugal</td>
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<td>0.10</td>
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</tr>
<tr>
<td>Spain</td>
<td>-0.15</td>
<td>0.34</td>
<td>0.06+</td>
<td>0.87</td>
</tr>
<tr>
<td>Average</td>
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<td>0.43</td>
<td>N/A</td>
<td>0.67</td>
</tr>
<tr>
<td><strong>Opt-out EU countries</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Denmark</td>
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<td>0.30</td>
<td>0.05*</td>
<td>0.66</td>
</tr>
<tr>
<td>Sweden</td>
<td>0.20</td>
<td>0.40</td>
<td>0.17</td>
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<tr>
<td>UK</td>
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<td>Estonia</td>
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<td>Hungary</td>
<td>0.94</td>
<td>0.75</td>
<td>0.49</td>
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<td>Latvia</td>
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<td>0.03*</td>
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<td>0.96</td>
<td>0.00**</td>
<td>0.50</td>
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<tr>
<td>Malta</td>
<td>-0.02</td>
<td>0.55</td>
<td>0.07+</td>
<td>0.34</td>
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<td>Poland</td>
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<td>1.04</td>
<td>0.23</td>
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<td>Slovakia</td>
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<td>1.75</td>
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<td>0.84</td>
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<td>0.36</td>
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<tr>
<td>Average</td>
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<td>0.96</td>
<td>N/A</td>
<td>0.44</td>
</tr>
</tbody>
</table>

Notes: +, *, ** respectively denote statistical significance at the 10, 5 and 1 per cent level. Normality is the p-value of the Normality Chi-square Bera-Jarque test for non-normality.
Table 2: Unit root tests: Augmented Dickey Fuller and Perron (1997)

<table>
<thead>
<tr>
<th></th>
<th>(a) ADF with constant only</th>
<th>(b) ADF with constant and trend</th>
<th>(c) Wild bootstrap analysis: Lower limits of confidence interval</th>
<th>(d) Perron (1997) single break test with shift in constant</th>
<th>(e) Perron (1997) single break test with shift in constant and trend</th>
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</thead>
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<td>95%</td>
<td>99%</td>
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<td><strong>EMU countries</strong></td>
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<td></td>
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</tr>
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<td><strong>Opt-out EU countries</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
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</tr>
<tr>
<td><strong>New EU countries</strong></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cyprus</td>
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<td>-4.48 [10]**</td>
<td>-2.96</td>
<td>-3.20</td>
<td>-3.54</td>
</tr>
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</table>

Notes: +, *, ** respectively denote statistical significance at the 10, 5 and 1 per cent level. The lower limits of the reported wild bootstrap critical values are the critical values of the ADF test corrected for heteroscedasticity/non-normality. The statistical significance of the Perron (1997) t-scores is determined using the test’s critical values corrected for small samples (100 observations).
Table 2 (continued): Unit root tests: Lee and Strazicich (2003)

<table>
<thead>
<tr>
<th></th>
<th>Breaks in constant</th>
<th>Breaks in constant and trend</th>
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<tr>
<td></td>
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<tr>
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</tr>
</tbody>
</table>

Notes: *, ** respectively denote statistical significance at the 10, 5 and 1 per cent level. Bold letters indicate the preferred specification of the minimum LM-unit root test, determined by the strongest rejection of the null. The selected models remain robust when selection is undertaken using the Akaike information criterion (results available upon request). Statistical inference is drawn by comparing the LM$_τ$ tests reported in columns (f) and (g) with the critical values reported taken in Table 2 in Lee and Strazicich (2003), for Models A and C (II) respectively.
Figure 1: Core EMU countries

Austria

Belgium

France

Germany

The Netherlands
Figure 1 (cont'd): Periphery EMU countries

Finland

Greece

Ireland

Italy

Portugal

Spain
Figure 1 (cont'd): Opt-out countries

Denmark

Sweden

United Kingdom
Figure 1 (cont'd): New EU countries - II

Lithuania

Poland

Slovakia

Slovenia