EPRU Working Paper Series

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Total Factor Productivity Revisited: A Dual Approach to Development Accounting

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> > 2004-07

ISSN 0908-7745

The activities of EPRU are financed by a grant from The National Research Foundation

TOTAL FACTOR PRODUCTIVITY REVISITED: A DUAL APPROACH TO DEVELOPMENT ACCOUNTING*

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April 2004

This paper tackles a number of issues that are central to cross-country comparisons of productivity. We develop a "dual" method to compare levels of total factor productivity (TFP) across nations that relies on factor price data rather than the data on stocks of factors required by standard "primal" estimates. Consistent with the development accounting literature based on primal estimates, we find that TFP accounts for the bulk of differences in income per worker across countries. However, we also find that there are significant differences between TFP series calculated using the two different approaches. We trace the reason for this divergence to inconsistencies between the data on user costs of capital and physical stocks of capital. In addition, we establish that the standard Cobb-Douglas methodology of assuming a constant capital share of one-third for all countries is a very good approximation to a more general formulation under which countries have different aggregate production functions which do not require a constant elasticity of substitution between factors.

JEL: O47, O57

Keywords: TFP, Development Accounting, Dual Approach, Cobb-Douglas Hypothesis.

^{*}We would like to thank Francesco Caselli, Oded Galor, Peter Howitt, Peter Birch Sørensen, Anders Sørensen, Jon Temple, David Weil, Fabrizio Zilibotti and an anonymous referee for comments and suggestions. We are also grateful to seminar participants at Brown University, the University of Copenhagen, the Centre for Economic and Business Research in Copenhagen, and at the 2001 E.E.A. conference in Lausanne. The standard disclaimer applies. This paper was written while Carl-Johan Dalgaard was visiting Brown University's Economics Department, the hospitality of which is gratefully acknowledged. The activities of EPRU (Economic Policy Research Unit) are supported by a grant from The Danish National Research Foundation. The views expressed are those of the authors and do not necessarily represent those of the International Monetary Fund. Contact: saiyar@imf.org or carl-johan.dalgaard@econ.ku.dk.

I. Introduction

A recent consensus has arisen that differences in total factor productivity (TFP) explain most of the variation in per capita income that is observed across countries (Islam, 1995; Klenow and Rodriguez-Clare, 1998; Hall and Jones, 1999; Easterly and Levine, 2000; Aiyar and Feyrer, 2000). If this is indeed the case, or if the role of TFP is even a fraction as important as the consensus suggests, a closer look at how TFP is measured merits considerable attention.

Several contributions have stressed the problems associated with measuring, in particular, the stock of physical capital. Pritchett (2000) argues that the standard procedure of calculating the stock of capital, the perpetual inventory method, is likely to severely mismeasure the actual stock of capital – and thus its growth contribution. Hsieh (1999, 2002) voices similar concerns in his work on the seemingly miraculous growth experience of a set of East Asian countries. Hsieh notes that if capital accumulation has been as important to East Asian growth as the influential studies by Young (1992, 1994) suggest, one should have observed a secular decline in the real return to capital investment in these countries. He documents that this did not occur, and proceed to calculate "dual" TFP estimates. This approach relies on factor prices rather than physical stocks of inputs, thereby extending a literature that dates back to Griliches and Jorgenson (1967). The result is a marked upward correction of TFP growth in almost all of the East Asian countries examined by Young.

Hseih's approach allows the calculation only of *growth rates* of TFP – not levels - for a single country. Our central contribution is to extend this growth accounting methodology to the field of development accounting, by showing how a dual approach can be used to calculate the level of TFP at a single point in time for a cross section of countries. We apply the dual approach to calculate TFP levels for 22 OECD countries.

Empirically our key result is a confirmation of the consensus view of the development accounting literature: the bulk of cross-country differences in income can be attributed to differences in TFP, not factors of production. In fact, our dual TFP estimates exhibit even greater variance across countries than their primal counterparts.

Although both primal and dual methodologies confirm the importance of TFP, we find that the TFP series calculated by the primal and dual methods are far from identical (the correlation between them is 0.46), and are significantly different in their ranking of countries. We examine different possible sources for the divergence between the two series, and find that it can be accounted for by inconsistencies between our data on the user-costs of capital and our data on

capital stocks. We discuss, using particular country examples, how these inconsistencies lead to systematic movements in the relative magnitude of primal and dual estimates. The inconsistencies we find are noteworthy in that they arise from empirical sources that are commonly and extensively used by researchers in a wide number of economic fields. Moreover they arise for a sample of the richest countries in the world, which may be expected to have the most reliable data. One of the most useful roles of dual TFP estimates should therefore be to alert a researcher about inconsistencies in the data for countries in which divergence between primal and dual estimates is large.

In order to carry out our development accounting exercise, we need make very minimal assumptions about the production function. In particular, we do not have to assume a Cobb-Douglas formulation, or even a constant elasticity of substitution between factors of production. This allows us to employ different factor shares for different countries. We use National Accounts data to obtain factor shares for different countries, rather than assuming a capital share of one-third for all countries as is standard in the literature. This enables us to test whether the Cobb-Douglas production function is a good approximation of the real world; if it were not then we would expect our TFP series (calculated on the basis of a generalized production function) to diverge considerably from the series obtained by assuming Cobb-Douglas for all countries in the world. In fact our results strongly validate the use of Cobb-Douglas production functions; the correlation between the two series is 0.99 both for primal estimates and dual estimates.

The next section of this paper outlines the theory underlying our dual approach to levels-accounting. The third section describes the data and sources we use for our empirical work. The fourth section discusses our empirical results. The fifth section examines the reasons for the divergence between the two series. The sixth section discusses the issue of using National Accounts to estimate different factor shares for different countries, and shows how we are able to vindicate the common practise of assuming a Cobb-Douglas production function with a capital share of one-third for all nations. The subsequent section concludes.

II. Theory

The Solow growth accounting technique (Solow 1957) requires only the assumptions of constant returns to scale (CRS) in the production function and perfect competition. Denoting output by Y, the production function for a country may be written as

$$Y = AF(K, H), \tag{1.1}$$

Where A represents TFP, K is the stock of physical capital in that country, and F is a function that is homogenous of degree one in its two arguments. H is the country's stock of human capital, defined by H=hL where h is the average level of education and L is the country's labour force. Solow showed that the production function above yields the following growth accounting identity:

$$\hat{A} = \hat{y} - \alpha_{\kappa} \hat{k} - \alpha_{H} \hat{h}, \tag{1.2}$$

where y = Y/L, k = K/L, and h = H/L, α_K and α_H refer to the share of physical capital and human capital respectively in national output, and hats above variables denote growth rates.

With constant returns to scale and perfect competition there are no aggregate profits in the economy, so we have the national accounts identity $Y = rK + w_H H$, where r and w_H are the returns to physical and human capital respectively. Griliches and Jorgenson (1967) showed that this identity in conjunction with equation (1.2) implies

$$\alpha_K \hat{r} + \alpha_H \hat{w} = \hat{A} = \hat{y} - \alpha_K \hat{k} - \alpha_H \hat{h}, \tag{1.3}$$

Equation (1.3) shows us how to obtain both dual (left hand side) and primal (right hand side) estimates of TFP growth, using only the assumptions of CRS and perfect competition. This is the identity popularized by Hsieh (1999, 2002) in his work on East Asia.

Equation (1.3) is a differential equation whose discrete version may be used to calculate rates of growth of TFP over time. However, following Hall and Jones (1996), we consider a cross-sectional interpretation of the equation. Imagine that all the countries in the world are ranked along a continuum with i denoting the country index. Then we can reinterpret the hats above variables as denoting the proportional difference in a particular variable between two countries that are adjacent to one another along the continuum. For example, $\hat{r} = \frac{d \log r_i}{di}$. The factor shares are functions of the country index i, not constants.

In order to employ the above derivation, we need to rank countries such that similar ones are close to each other, because the cross-sectional formulation assumes that factor inputs, factor prices and factor shares are differentiable functions of the country index. Our ranking system uses an index that combines countries' capital shares, capital-labour ratios and human capital-labour ratios (for the primal estimates), and an index that combines countries' capital shares, returns to

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¹ Strictly speaking $\alpha_K = AF_K/Y$ and $\alpha_H = AF_H/Y$. But the assumption of perfect competition ensures that factors are paid their marginal products, so that α_K and α_H may be treated as factor shares that sum to unity.

human capital and returns to physical capital (for the dual estimates).² Once the countries have been sorted by this index, the TFP level for country i is recovered as

$$\log A_{i} = \int_{0}^{i} \hat{A}_{j} dj + \log A_{0}, \tag{1.4}$$

or, in discrete terms

$$\log A_i = \sum_{j=2}^i \Delta \log A_j + \log A_1 \tag{1.5}$$

Finally, discretizing equation (1.3) allows us to obtain

$$\overline{\alpha}_{K_i} \Delta \log r_i + \overline{\alpha}_{H_i} \Delta \log w_i = \Delta \log A_i
= \Delta \log y_i - \overline{\alpha}_{K_i} \Delta \log k_i - \overline{\alpha}_{H_i} \Delta \log h_i,$$
(1.6)

where $\bar{\alpha}_{H_i} = 0.5(\alpha_{Hi} + \alpha_{Hi+1})$ and $\bar{\alpha}_{K_i} = 0.5(\alpha_{Ki} + \alpha_{Ki+1})$. To summarize our procedure, we use the data we have on factor prices, factor shares and factor stocks to calculate primal and dual estimates of $\Delta \log A_i$ using equation (1.6). Equation (1.5) is then used to convert the two series of $\Delta \log A_i$ into levels of $\log A_i$. Because of the normalization implicit in equation (1.5) our TFP estimates are only valid up to a constant term.³

III. Data

In order to make equation (1.6) operational, data on the real stocks of capital, GDP per worker, income shares and factor prices are required. We were able to obtain such data on 22 OECD countries for 1980 and 21 for 1990.⁴ As the cross-sectional methodology outlined above requires that the countries under consideration are sufficiently "similar", we pool the data in order to get a denser clustering of countries. Hence, we treat our selection of countries as a set of 43 distinct observations, thereby effectively assuming that, say; the USA in 1980 is a different country from the USA in 1990.

² For the primal rankings we use an index z which equals $z_{\log k} + z_{\alpha_K} + z_{\log h}$ z, where

 $z_x = (x - mean(x)) / std(x)$ z. For the dual rankings we use $z_{\log w} + z_{\alpha_K} + z_{\log r}$.

³ In fact when we calculate TFP for a sample of n countries, we are only able to obtain the series for n-2 of them. We lose one observation in the calculation of labours share, and another when we perform the discrete version of integrating over the continuum of countries.

⁴ This discrepancy is due to lack of necessary labour data on Switzerland for 1990.

Stocks of physical capital and output per worker are taken directly from the Penn World Tables 5.6 (PWT).⁵ In order to compute the aggregate stock of human capital, we need data on human capital per worker, h, and total employment. Human capital is estimated in a way that has become fairly standard. We use Mincerian coefficients estimated by Psacharopoulos (1994) to weight the average years of primary (pyr), secondary (syr) and higher (hyr) education in a country. Assuming that the log of human capital per person is piecewise linear, we get that⁶

$$\log h = .134 * pyr + .101 * syr + .068 * hyr. \tag{1.7}$$

Data on total employment are obtained from the Yearbook of Labour Statistics 1998 (for L in 1990), and the OECD compendium 1996 (for L in 1980). Note, for future reference, that these numbers include both paid employees and the self employed.

Both the primal and the dual method require data on factor shares. To compute the share of human capital in total income, we use data on GDP as well as on the compensation of employees from the National Accounts Statistics (United Nations, (1993)). A problem with estimating the share of human capital as the total compensation of employees divided by GDP is that total compensation excludes the self employed. Hence, following Gollin (2002), we adjust for the wage income of the self employed, by assuming that the wage share in the unincorporated sector is equal to its share in the corporate sector. The correction requires a few simple steps. First, we obtain both total employment and the number of self employed workers (classified as "Employers and own account workers") from the Yearbook of Labour Statistics (ILO (1981), (1992)) allowing us to compute the ratio of self employed workers to paid employees. Second, we estimate the (adjusted) share of human capital as

$$\alpha_{H} = \frac{\text{(compensation of employees)}(1 + \frac{\text{self employed workers}}{\text{paid employees}})}{\text{GDP}}$$
(1.8)

Assuming CRS, the capital share is then given by $\alpha_K = 1 - \alpha_H$. In order to achieve as accurate an estimate for the annual wage itself, we divide the total compensation of employees by an estimate of the total number of paid employees. Specifically,

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⁵ The PWT make available data on five categories of capital are available. We use all of them to calculate the aggregate stock of physical capital.

⁶ The basic idea that this is the appropriate way to introduce human capital into an aggregate production function is due to Bils and Klenow (2000). Here we duplicate Hall and Jones (1999) in using Mincerian coefficients estimated by Psacharopoulos, i.e. we use the average Psacharopoulos reports for sub-Saharan Africa to weight primary education, the average for the world as a whole to weight secondary education, and the OECD average to weight higher education. An alternative approach would be to allow for variation in the return to education, using micro estimates for individual countries with respect to primary, secondary and tertiary years of schooling. Unfortunately, such data are not available for the countries in our sample, which is why we resort to the standard approach.

$$w = \frac{\text{compensation of employees}}{\text{(Total employment) } (1 - \frac{\text{self employed workers}}{\text{total employment}})}$$
(1.9)

These wages are then converted into 1980 international dollars for comparability. Note that the wage rate calculated above is the compensation per unit of (raw) labour, which we may denote as w_L , whereas what we need for the exercise we have outlined is w_H , the compensation per unit of human capital. From the production function in equation (1.1) and our assumption of perfect competition, it follows that:

$$W_H = AF_H \tag{1.10}$$

and

$$w_L = AF_H h \tag{1.11}$$

Therefore $w_H = w_L / h$, and $\log w_H = \log w_L - \log h$. Finally, we need an estimate of the real user cost of physical capital, r. Following Hall and Jorgenson (1967), we apply the following formula:

$$r = \frac{P_I}{P_{\nu}}(i - \pi_I + \delta), \tag{1.12}$$

where p_I is the price of a new unit of capital, p_y is the product price, i is the relevant nominal interest rate, π_I is the (expected) increase in the investment price, and δ is the (geometric) rate of depreciation. The right hand side of equation (1.12) simply quantifies the marginal costs of capital, assuming competitive markets along with the absence of convex costs of installation and investment irreversibility's. To see this, note that since profit maximizing behaviour implies $F_K = r$, equation (1.12) can be rewritten so as to yield $F_K \frac{P_y}{P_I} = (i - \pi_y + \delta - (\pi_I - \pi_y))$, where π_y is the rate of inflation. Thus, the equation states that, in units of output, the marginal product of capital $(F_K \frac{P_y}{P_I})$, net of depreciation plus capital gains $(\delta - (\pi_I - \pi_y))$ equals the real rate of interest $(i - \pi_y)$. To apply this formula, we use data from the PWT for p_I (the aggregate investment price index) and

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⁷ In the case of a one-good economy, where $p_y = p_I$ (thus $\pi_I = \pi_y$), equation (1.12) simply states that the marginal product of capital equals the real rate of return plus depreciation.

 p_y (the GDP deflator). In measuring i we use lending rates taken from IMF International Financial Statistics Yearbook, 1995. π_I is derived as the lagged percentage increase in the aggregate investment price index. The depreciation rates on the five categories of capital that are available in the PWT are taken from Hulten and Wyckoff (1981). The depreciation rate ultimately used in our user cost expression is then computed as a weighted average of these five depreciation rates; the weights being the relative size of the individual categories of capital in the total stock of capital. The resulting series for α_H , w and r are reported in the Appendix.

IV. Results: Primal vs. Dual

Following Klenow and Rodriguez-Clare (1997) (KRC) it is possible to decompose the variation in per capita output levels in our sample into that explained by variation in factors of production (or factor returns) and that explained by variation in TFP, calculate both by the primal and the dual method. Formally,

$$\frac{\operatorname{var}(\log y)}{\operatorname{var}(\log y)} = 1 = \frac{\operatorname{cov}(\log A, \log y)}{\operatorname{var}(\log y)} + \frac{\operatorname{cov}(\log Z, \log y)}{\operatorname{var}(\log y)}$$
(1.13)

where $Z \equiv F(K/L,h)$. The important question is whether there are significant differences in the share of the variation accounted for by our two different methodologies. The answer is provided by Table 1 below:

Table 1: Variance Decompositions

	$\frac{\text{COV}(\text{logy}, \text{logA})}{\text{VAR}(\text{log y})}$	$\frac{\text{COV}(\log y, \log Z)}{\text{VAR}(\log y)}$	$\frac{\text{VAR}(\log A)}{\text{VAR}(\log y)}$
Primal	0.32	0.68	0.44
Dual	0.35	0.65	0.76

Column 1 and 2 reveal that the share of the variation in output attributable to TFP is of the same order of magnitude whether dual or primal estimates are used. However, as the third column makes clear; dual TFP estimates varies much more across the countries in the sample, than their primal counterparts. This is also visually clear from Figure 1, which shows a cross plot of the primal and dual estimates. The size of this TFP variation is all the more striking considering we are examining

Needless to say, we would prefer to estimate separate user costs for each category of capital in the PWT. Unfortunately the individual investment prices are not available.

a group of relatively homogenous OECD countries. The primal and dual decompositions yield similar results only because the implicit covariance between calculated total factor productivity levels and logZ are different in magnitude. In general, the variance of log y is given by the sum of the variances of logA and logZ plus twice the covariance between the two -- the Klenow and Rodriguez-Clare decomposition distributes the covariance evenly between logA and logZ. Accordingly, both primal and dual TFP estimates are negatively correlated with the factor index logZ; but dual estimates more so.⁹

Nevertheless the key conclusion from this exercise is that the dual TFP calculations resoundingly support previous studies (based on primal calculations) which show that TFP differences, not differences in physical stocks of capital, are paramount in accounting for cross-country productivity differences.

At a more detailed level, Table 2 shows the ranking of all the countries in our sample using both primal and dual approaches.¹⁰ It is immediately apparent that there are significant differences in the ranking of countries using the two different sets of TFP estimates. In fact the correlation between the TFP series is only 0.46. USA (1990) moves up from rank 16 in the primal series to rank 13 in the dual series, and USA (1980) moves up 13 places from 25 to 12. Hong Kong in 1990 moves from being the second-most productive country to position 24.

It is interesting to note that by both primal and dual methodologies, there are a number of countries which move down in the productivity rankings in 1990 compared to their position in 1980. However, the number of such "switches" is greater in the dual rankings (12 switches) than in the primal rankings (6 switches).

Figure 2 shows a histogram of all the observations, in which TFP levels are measured relative to the TFP level for the USA in 1980. For each country the first two bars represent TFP in 1980 and the second two represent TFP in 1990. The black bars represent dual estimates, while the grey ones represent the primal series. The most visually arresting theme of the histogram is the shortness of the black bars relative to the grey ones; this is largely due to the fact that the USA in 1980 moves up 13 places in the rankings in the dual series. Only for 8 observations out of 40 do we

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⁹ A similar negative covariance between levels (and growth rates) of factor stocks, and levels (and growth rates) of TFP levels is present in the Klenow and Rodriguez-Clare study. A possible explanation is that standard calculations omit capital utilization (Dalgaard, 2003).

¹⁰ For this exercise we are using National Accounts data to estimate factor shares, as described in the previous section. Recall also that we are treating a country in 1980 and a country in 1990 as different points along the continuum; so that we have a "cross-section" of 43 countries (we lack data for Switzerland in 1990). We have to drop two observations in both the primal and dual estimation procedures, but there is an overlap of one country. Thus for purposes of comparison the final sample size is 40.

have that productivity relative to the USA in 1980 is higher according to the dual method compared to the primal method.¹¹

Among the observations for which the differences between primal and dual estimates are most stark are Hong Kong, Britain, Denmark and Finland in both years, West Germany (1990), Austria (1990), Belgium (1990), Spain (1990) and the Netherlands (1990). This can be seen by the discrepancy between the heights of the black and grey bars for these observations. In each of these cases the black bar is shorter than the grey one; measured productivity is greater by the primal measure than by the dual. Belgium, Canada, Denmark and Spain are interesting because they are the only countries in which the relative heights of the black and grey bars switch from 1980 to 1990; for each of these countries dual TFP was higher than primal TFP in 1980, while the opposite held in 1990. Japan is the only country in the sample for which dual TFP was higher than primal TFP in both years.

But why do the two TFP series diverge so much? In the subsequent section we attempt to pinpoint the sources of the divergence. But before we turn to this investigation it is worth pointing out that the divergence is not caused by any measurement issues regarding the stock of human capital. The reason is that the calculation of w_H made us of data on human capital stocks. Thus the dual estimates for TFP are not based only on factor returns, but also on average educational levels. Since both dual and primal TFP estimates make use of the same measure of human capital, measurement error in human capital is not causing the observed divergence.

V. Accounting for the Divergence in TFP Estimates

The poor correlation between dual and primal TFP estimates may arise for two reasons. The first possibility is that the theory on which the equality of dual and primal estimates is founded is wrong. This option is decidedly unattractive. All we need for the identity of primal and dual estimates is a production function with constant returns to scale in rival inputs and perfect competition. If these assumptions are not a good approximation to reality then we must abandon not just the comparison between dual and primal but also growth and levels-accounting exercises altogether, since the standard primal estimates presented in the literature typically employ at least these assumptions and usually additional ones.

¹¹ These observations are: Australia (1990), Belgium (1980), Canada (1980), Denmark (1980), Spain (1980), Japan (1980), Japan (1990) and New Zealand (1990).

 $[\]log w_H = \log w - \log h$

The second possibility is that the data on factor input and the data on factor prices are inconsistent with one another. In order to investigate to what extent this is the case, one can compare the factor price data used for the dual estimates with the wage and rental rates implied by our data on factor-stocks and our theoretical assumptions. It is straightforward to obtain series for rental rates and wage rates that are consistent with our data on factor shares, output per worker and stocks of capital. Specifically, the imputed wage rate for raw labour in country i, w_{Li} , is obtained by multiplying the share of human capital by output per worker

$$\tilde{w}_{Li} = \alpha_{Hi} \frac{Y_i}{L_i}. \tag{1.14}$$

Similarly, the imputed rental rate in country i, r_i , is given by

$$\tilde{r}_{Li} = \alpha_{Ki} \frac{Y_i}{K_i}. \tag{1.15}$$

Calculating the imputed wage and rental rates implied by our primal estimates allows us to pinpoint the source of divergence between primal and dual estimates (alternatively, we could have calculated the factor-stocks consistent with our dual estimates).

Figure 3 measures the wage rates obtained from National Accounts data (which we use for our dual estimates) on the horizontal axis; the vertical axis measures the wage rates imputed from our data on factor-stocks (equation (1.7.)). Both series are normalized by the US wage-rate in 1980. It is visually obvious that the two series are nearly identical; the correlation between them is 0.95. It follows that the wage data from the National accounts are consistent with perfect competition and our estimates of the labour force; the source of discrepancy between primal and dual estimates does not lie here.

By a process of elimination, therefore, it seems that the discrepancy must arise because our data on the user-cost of capital is inconsistent with our data on capital stocks from the Penn World Tables. This hypothesis is confirmed when we calculate the rental rates implied by our data on capital stocks using equation (1.8). Figure 4 plots the imputed rental-rates against the actual user-costs of capital, and Table 3 lists them. It is clear that the two series bear no discernable relation to one another. The correlation coefficient is actually negative, at -0.14. In general the imputed rates tend to be higher than the actual user-costs. This is spectacularly evidenced by Hong Kong, whose imputed rate is 44% in 1980 and 52% in 1990.

So which data are more reliable: our series on the user-costs of capital or our series on the capital stocks (which imply the rental-rates on the vertical axis in Figure 4)? This question may

not admit of a general answer. Countries and international institutions may differ in their ability to measure one or the other series correctly. An investigator must draw upon detailed knowledge of the specific country under examination when deciding whether to trust dual or primal estimates of productivity. However, it is worth commenting on some specific characteristics of our data on usercosts that contrast with our imputed series, and showing how these characteristics affect the comparison between primal and dual TFP for certain countries in our sample.

Figure 5 shows the proportionate changes in rental-rates over the decade for all the countries in our sample, for both the actual series and the imputed series. This reveals a systematic difference between the two. While the imputed rental rates have tended to remain stable over the decade or increase slightly, the actual user-costs in almost all countries seem to have fallen considerably. The Appendix contains our complete series for the user-cost of capital and documents this decline in user-costs. This pattern sheds some light on the divergence between primal and dual TFP estimates.

We had noted before that measured productivity declined over the 1980s for 12 countries by the dual measure, compared to 6 countries by the primal measure. This is directly attributable to the fall in user-costs over the decade for these countries.

Figure 2 documented primal and dual TFP estimates for all the countries in our sample. The differences between the grey bars and black bars in this figure can be explained in terms of the divergence between user-costs and imputed rental-rates. For example in Britain and Finland the dual estimate is below the primal estimate in both years; Table 3 shows that this is because user-costs are well below the level implied by capital stocks in both years. The imputed rental-rate in Britain in both 1980 and 1990 was 30%. The corresponding actual user-costs were 6% and 15% respectively. The imputed rental-rates in Finland in 1980 and 1990 were 17% and 15%; the corresponding user-costs were only 6% and 3%. We had earlier commented that Japan, alone in the sample, showed higher dual TFP than primal TFP for both years. Table 3 documents that for Japan the user-costs in both years are fairly similar to the imputed rental-rates. But because the latter are in general so much higher than the former, Japan's ranking among countries is much higher in the user-costs series, and this explains why its ranking is higher in the dual estimates. The most glaring discrepancy between user-costs and imputed rates is the case of Hong Kong. While its actual user-costs in 1980 and 1990 are 10% and 9% respectively, the imputed rental-rates implied by its capital stocks are entirely unreasonable, at 44% and 52% respectively. Unsurprisingly, its primal TFP estimates tower above its dual estimates.

What is one to make of the differences documented here? Obviously the two series are inconsistent with each other. One approach would be to argue that this shows that capital is not being paid its marginal product, and in particular, capital is being paid less than its marginal product (because in general the imputed rates are higher than the user-costs). While this is a tenable interpretation of our results, it should be noted that such an argument would constitute an indictment not just of our dual estimates of productivity but also most primal estimates that are standard in the literature. For if such imperfections are significant then α_K no longer equals KF_K/Y and standard growth and levels-accounting exercises lose all meaning.

The other interpretation of our results is that either capital stocks or user-costs or both are being badly measured; certainly they are not consistent if minimal theoretical requirements are satisfied. Are there then any grounds for suspecting that one series is measured more poorly than the other? This question, as we have stated before, seems answerable only in the context of detailed knowledge of particular countries. For example, we would be inclined to argue that in the case of Hong Kong capital stocks have been mismeasured, simply on the grounds that an implied rental rate in excess of 40% is thoroughly implausible.

Whatever the particular circumstances of particular nations, it seems that the dual methodology that we have presented here provides a useful way for researches to double-check the plausibility of their standard primal estimates of productivity. A large divergence between the estimates should alert the researcher to potential data-problems, especially with regard to the measurement of capital-stocks or user-costs.

VI. Income Shares and the Cobb-Douglas Hypothesis

As we mentioned in the introduction, all the results presented thus far have relied on estimating factor shares from national accounts data. We were able to do this because our minimal assumptions about the production function allowed us to use both country- and time-varying factor shares. We turn now to the issue of how well the standard Cobb-Douglas formulation holds up when compared to our more general method for estimating TFP. This question is of obvious interest and importance to empirical researchers. If the strong assumption of an identical Cobb-Douglas technology with a capital share of one-third for every country in the world leads to TFP estimates that are indistinguishable from ours, then that is welcome news both from the perspective of validating recent research in the growth literature and the perspective of making future research less

cumbersome.¹³ If the Cobb-Douglas formulation is indeed valid then there is a very simple formula that may be used to obtain dual estimates of TFP. Suppose the production function takes the form

$$Y = AK^{\alpha_K}H^{\alpha_H} \tag{1.16}$$

where $\alpha_K = 1 - \alpha_H = 1/3$. Then, noting that by the assumption of perfect competition, $K = \alpha_K Y/r$ and $H = \alpha_H Y/w_H$, it follows that

$$A = Y / \left[\left(\frac{\alpha_K Y}{r} \right)^{\alpha_K} \cdot \left(\frac{\alpha_H Y}{w_H} \right)^{\alpha_K} \right] = \left(\frac{r}{\alpha_K} \right)^{\alpha_K} \cdot \left(\frac{w_H}{\alpha_H} \right)^{\alpha_K}. \tag{1.17}$$

Taking logs then gives us

$$\log A = \alpha_K \log r + \alpha_H \log w_H - \alpha_K \log \alpha_K - \alpha_H \log \alpha_H \tag{1.18}$$

where the last two terms are constants that are equal for all countries. Equation (1.19) allows us to obtain dual estimates for the Cobb-Douglas approach; neither ranking of countries along a continuum nor any process of integration to get from growth rates to levels is necessary under such a formulation.¹⁴ Figures 6 and 7 depict scatter plots of Cobb-Douglas estimates against our generalized estimates: it immediately obvious that the data points cluster remarkably tightly about a 45 degree line from the origin. The correlation between the two series is very close to unity for the dual approach as well for the primal approach. In both cases the correlation is 0.99.¹⁵ The great similarity of the Cobb-Douglas estimates to our generalized estimates leads us to conclude that, for

Hall and Jones (1996) also use factor shares that vary across countries, but they obtain their factor shares by means of a calibration exercise rather than from the national accounts. In particular, they work with the identities $\alpha_{Ki} = r_i K_i / Y_i$ and $\alpha_{Hi} = 1 - \alpha_{Ki}$. Armed with data on capital stocks and national output, they calibrate the return on capital such that $\alpha_K = 1/3$ for the USA. They then assume that the return to capital in all nations is equal to that of the USA, and this allows them to calibrate different factor shares for all nations. But they find that using this calibrated approach leads to TFP estimates that are extremely similar to TFP from a simple Cobb-Douglas methodology. The close correlation between the two series leads them to be satisfied with a Cobb-Douglas framework in subsequent work (Hall and Jones, 1999). Although the calibrated approach described above does allow one to employ different factor shares for each country, it is clearly a more restrictive approach than our methodology of using national accounts data. In particular its assumption of equal rates of return to capital in all countries of the world appears to be contradicted by our data on factor prices (see Appendix 1).

Primal estimates of TFP under the Cobb-Douglas assumption are based on the familiar equation $\log A = \log Y - \alpha_K \log K - \alpha_H \log L - \alpha_H \log h$

¹⁵ When we compare the primal and dual estimates of TFP under the Cobb-Douglas formulation, we find that the correlation to be 0.53, which is comparable to, albeit slightly higher than, the correlation we found between primal and dual series using our more general approach 0.46. This result mirrors the fact that the divergence between dual and primal TFP estimates is due to data inconsistencies.

the purposes of measuring TFP, assuming a fixed capital share of one-third is a convenient and accurate shortcut.

VII. Concluding Remarks

In this paper we have developed a dual approach to TFP levels-accounting which combines methodologies due to Griliches and Jorgenson (1967) and Hall and Jones (1996). Comparing the results from this approach to the standard primal approach reveals significant differences between the two sets of TFP estimates for a group of 22 OECD countries. Our analysis reveals that the divergence between primal and dual TFP estimates is caused by data inconsistencies between the user-costs of capital and physical stocks of the same. This suggests that, even in rich countries with rigorously researched statistics there may be discrepancies in the data which a researcher should be aware of. We have argued that there is no general rule that would serve to identify which TFP estimates are preferable; what is needed is detailed knowledge of the particular country under consideration. Such knowledge may enable a researcher to determine whether data on user-costs or data on capital stocks are more reliable on a case-by-case basis. The usefulness of having two different methods of constructing productivity estimates is that their comparison can serve as a warning signal: a substantial divergence between the two should serve to alert the researcher that the data on physical stocks and factor prices are inconsistent with each other or with the assumptions of growth-accounting.

Whether one *a priori* has more faith in primal or dual estimates, one important conclusion is robust: the importance of TFP in accounting for cross-country income differences. Our dual estimates strongly support the view that TFP is more important than factor stocks in explaining the variation in income across countries. The variance in TFP levels is even greater under the dual methodology than using the traditional primal approach to development accounting.

Finally, we also found evidence to suggest that the Cobb-Douglas formulation with a constant capital share of one-third is a very good approximation to a world in which countries are allowed to have different production functions satisfying more general conditions. This is good news for growth researchers both in terms of increasing our confidence in previous work using the Cobb-Douglas formulation and in terms of allowing an accurate simplification of reality in future productivity studies.

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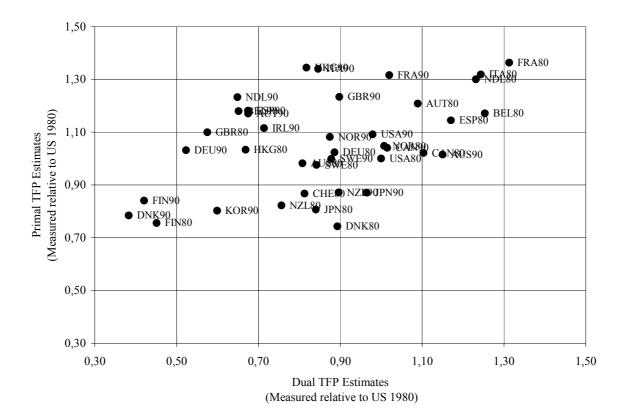
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Figure 1



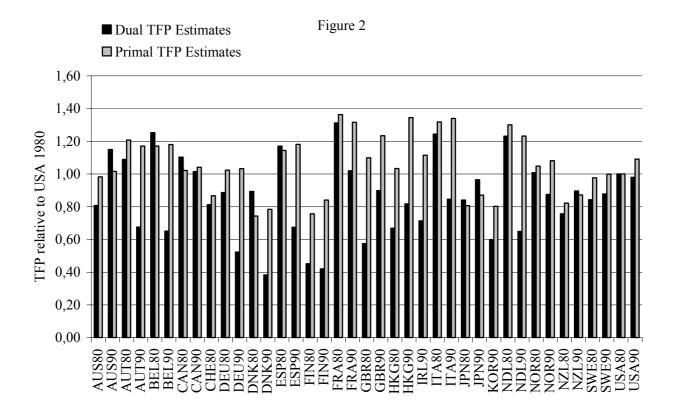


Figure 3

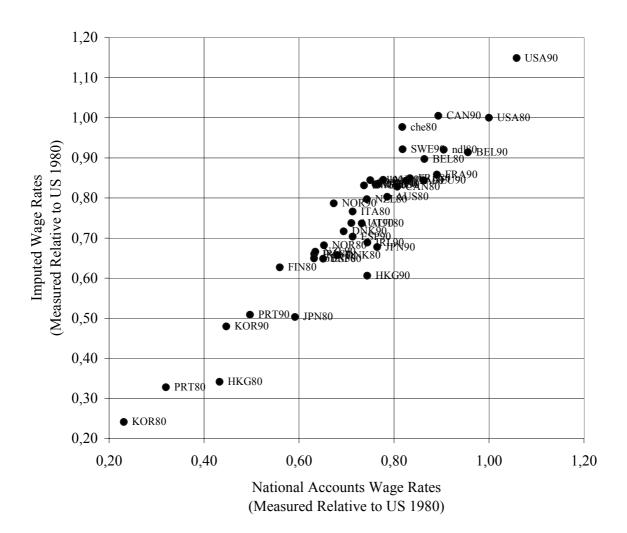
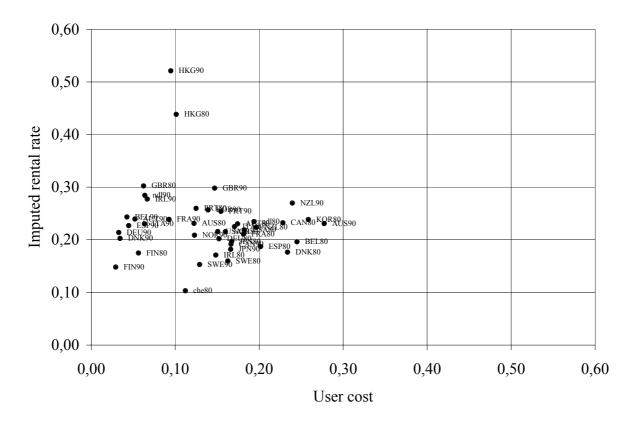


Figure 4



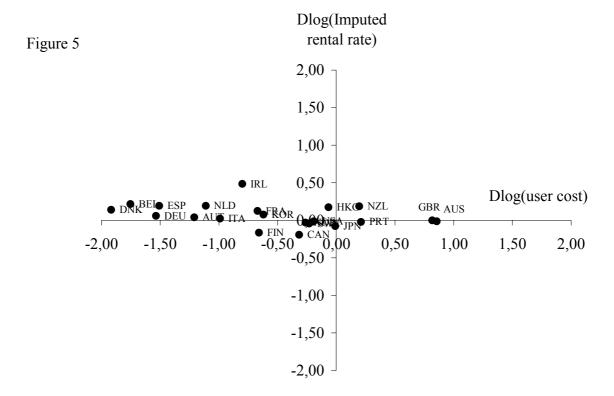
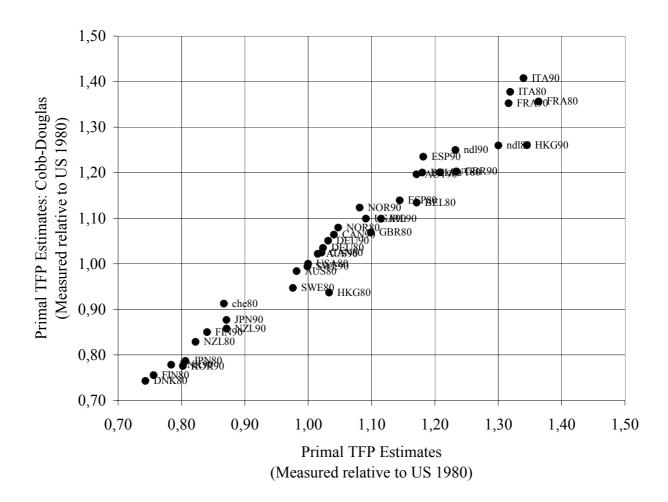


Figure 6



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Figure 7

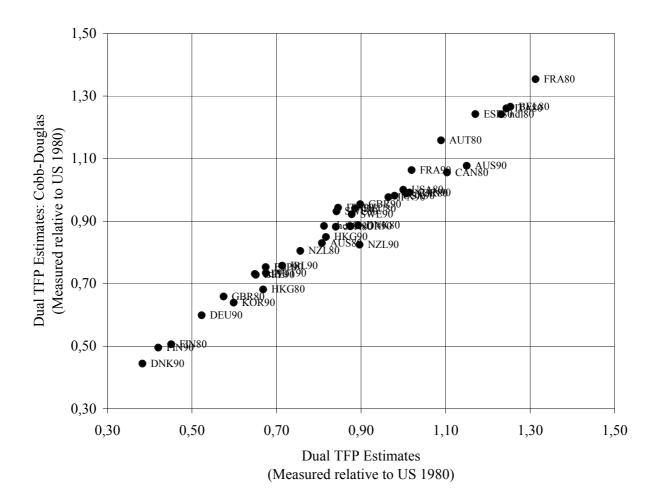


Table 2Dual vs. Primal TFP estimates

Year	Primal Approach	Rank	Year	Dual Approach
1980	FRA	1	1980	FRA
1990	HKG	2	1980	BEL
1990	ITA	3	1980	ITA
1980	ITA	4	1980	NLD
1990	FRA	5	1980	ESP
1980	NLD	6	1990	AUS
1990	GBR	7	1980	CAN
1990	NLD	8	1980	AUT
1980	AUT	9	1990	FRA
1990	ESP	10	1990	CAN
1990	BEL	11	1980	NOR
1980	BEL	12	1980	USA
1990	AUT	13	1990	USA
1980	ESP	14	1990	JPN
1990	IRL	15	1990	GBR
1990	USA	16	1990	NZL
1990	NOR	17	1980	DNK
1980	NOR	18	1980	DEU
1980		19	1980	SWE
	CAN	20		
1980	HKG		1990	NOR
1990	DEU	21	1990	ITA
1980	DEU	22	1980	SWE
1980	CAN	23	1980	JPN
1990	AUS	24	1990	HKG
1980	USA	25	1980	CHE
1990	SWE	26	1980	AUS
1980	AUS	27	1980	NZL
1980	SWE	28	1990	IRL
1990	NZL	29	1990	AUT
1990	JPN	30	1990	ESP
1980	CHE	31	1980	HKG
1990	FIN	32	1990	BEL
1980	NZL	33	1990	NLD
1980	JPN	34	1990	KOR
1990	KOR	35	1980	GBR
1990	DNK	36	1990	DEU
1980	FIN	37	1980	FIN
1980	DNK	38	1990	FIN
1980	KOR	39	1990	DNK

Note: IRL80, KOR80, PRT80 and 90 are excluded for this comparison

User cost and Imputed rental rates

Table 3

Table 3	rates		
V	1	Imputed	
Year	wbcode	rental rates	User cost
1980	AUS	0,23	0,12
1990	AUS	0,23	0,28
1980	AUT	0,23	0,17
1990	AUT	0,24	0,05
1980	BEL	0,20	0,25
1990	BEL	0,24	0,04
1980	CAN	0,23	0,23
1990	CAN	0,19	0,17
1980	CHE	0,10	0,11
1980	DEU	0,20	0,15
1990	DEU	0,21	0,03
1980	DNK	0,18	0,23
1990	DNK	0,20	0,03
1980	ESP	0,19	0,20
1990	ESP	0,23	0,04
1980	FIN	0,17	0,06
1990	FIN	0,15	0,03
1980	FRA	0,21	0,18
1990	FRA	0,24	0,09
1980	GBR	0,30	0,06
1990	GBR	0,30	0,15
1980	HKG	0,44	0,10
1990	HKG	0,52	0,09
1980	IRL	0,17	0,15
1990	IRL	0,28	0,07
1980	ITA	0,22	0,17
1990	ITA	0,23	0,06
1980	JPN	0,20	0,17
1990	JPN	0,18	0,17
1980	KOR	0,24	0,26
1990	KOR	0,26	0,14
1980	NLD	0,23	0,19
1990	NLD	0,28	0,06
1980	NOR	0,22	0,16
1990	NOR	0,21	0,12
1980	NZL	0,22	0,20
1990	NZL	0,27	0,24
1980	PRT	0,26	0,12

st.dev.		0,07	0,07	
Average		0,23	0,14	
1990	USA	0,22	0,15	
1980	USA	0,22	0,18	
1990	SWE	0,15	0,13	
1980	SWE	0,16	0,16	
1990	PRT	0,25	0,15	

APPENDIX

Year	wbcode	Human Capital Shar	e Annual Wage (a)	lnh	Usercost
1980	AUS	0,62	142,2	1,20	0,122
1990	AUS	0,59	140,7	1,21	0,277
1980	AUT	0,66	132,5	0,81	0,174
1990	AUT	0,58	128,6	0,86	0,052
1980	BEL	0,68	156,4	1,01	0,245
1990	BEL	0,61	173,0	1,07	0,042
1980	CAN	0,61	146,1	1,18	0,228
1990	CAN	0,61	161,7	1,22	0,166
1980	CHE	0,70	148,0	1,10	0,112
1980	DEU	0,64	137,8	1,09	0,152
1990	DEU	0,59	156,2	1,13	0,033
1980	DNK	0,64	123,2	1,29	0,234
1990	DNK	0,60	125,6	1,38	0,034
1980	ESP	0,64	117,8	0,66	0,202
1990	ESP	0,56	129,0	0,75	0,045
1980	FIN	0,61	101,3	1,22	0,056
1990	FIN	0,64	139,0	1,24	0,029
1980	FRA	0,67	150,9	0,73	0,181
1990	FRA	0,59	161,2	0,82	0,093
1980	GBR	0,64	114,3	1,00	0,062
1990	GBR	0,66	138,6	1,06	0,147
1980	HKG	0,51	78,3	0,81	0,101
1990	HKG	0,56	134,6	0,99	0,095
1980	IRL	0,75	114,4	0,93	0,148
1990	IRL	0,60	134,6	0,98	0,067
1980	ITA	0,60	129,1	0,65	0,171
1990	ITA	0,58	149,4	0,73	0,063
1980	JPN	0,65	107,1	0,98	0,167
1990	JPN	0,63	138,4	1,08	0,166

	St.dev	0,05	29,8	0,24	0,067
	mean	0,62	130,8	1,01	0,138
1990	USA	0,66	191,6	1,35	0,151
1980	USA	0,66	181,0	1,36	0,182
1990	SWE	0,68	148,1	1,11	0,129
1980	SWE	0,70	133,4	1,11	0,163
1990	PRT	0,64	89,9	0,44	0,154
1980	PRT	0,61	57,9	0,40	0,125
1990	NZL	0,55	114,8	1,33	0,239
1980	NZL	0,68	134,5	1,43	0,197
1990	NOR	0,57	121,9	0,96	0,123
1980	NOR	0,57	118,1	0,89	0,160
1990	NLD	0,57	135,8	1,02	0,064
1980	NLD	0,66	163,8	0,97	0,194
1990	KOR	0,63	80,9	1,10	0,139
1980	KOR	0,63	41,8	0,82	0,259

Notes: (a) thousands 1980 int'nal US\$