Herz, Holger; Schunk, Daniel; Zehnder, Christian

Working Paper
How do judgmental overconfidence and overoptimism shape innovative activity?

CESifo Working Paper: Behavioural Economics, No. 4084

Provided in Cooperation with:
Ifo Institute – Leibniz Institute for Economic Research at the University of Munich

Suggested Citation: Herz, Holger; Schunk, Daniel; Zehnder, Christian (2013) : How do judgmental overconfidence and overoptimism shape innovative activity?, CESifo Working Paper: Behavioural Economics, No. 4084, Center for Economic Studies and Ifo Institute (CESifo), Munich

This Version is available at:
http://hdl.handle.net/10419/69592

Terms of use:
Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.
How Do Judgmental Overconfidence and Overoptimism Shape Innovative Activity?

Holger Herz
Daniel Schunk
Christian Zehnder

CESifo Working Papers

CESifo Working Paper No. 4084
Category 13: Behavioural Economics
January 2013

An electronic version of the paper may be downloaded
• from the SSRN website: www.SSRN.com
• from the RePEc website: www.RePEc.org
• from the CESifo website: www.CESifo-group.org/wp
How Do Judgmental Overconfidence and Overoptimism Shape Innovative Activity?

Abstract

Recent field evidence suggests a positive link between overconfidence and innovative activities. In this paper we argue that the connection between overconfidence and innovation is more complex than the previous literature suggests. In particular, we show theoretically and experimentally that different forms of overconfidence may have opposing effects on innovative activity. While overoptimism leads to an innovation enhancing effect, judgmental overconfidence inhibits innovation. Our results indicate that future research is well advised to take into account that the relationship between innovation and overconfidence may crucially depend on what type of overconfidence is most prevalent in a particular context.

JEL-Code: C920, D830, D230.

Keywords: innovation, entrepreneurship, overconfidence, experiment.
1 Introduction

Recent field evidence indicates that there is a positive link between overconfidence of managerial decision makers and innovative activities. For example, Galasso and Simcoe (2011) and Hirshleifer et al. (2012) show that CEOs who are overoptimistic regarding the future performance of their company, are more likely to pursue innovation, obtain more patents and patent citations, and are more likely to take their firms in a new technological direction. In this paper we argue that the connection between overconfidence and innovation is more complex than the previous literature suggests. Existing work focuses almost exclusively on overoptimism, the tendency of individuals to overestimate their abilities or chances of success. However, while there is indeed ample evidence indicating that people often exhibit this bias (see, e.g., Svenson 1981; Dunning et al. 1989; Alicke et al. 1995), many studies show that other forms of overconfidence are also prevalent. In particular, it is a well established fact that many people have a tendency to overestimate the precision of their information. This phenomenon is commonly referred to as judgmental overconfidence (see, e.g., Lichtenstein et al. 1982; Russo and Schoemaker 1992). In this paper we show theoretically and experimentally that the effect of judgmental overconfidence on innovative activity goes in the opposite direction of the effect of overoptimism, i.e., judgmental overconfidence inhibits innovation. Our results indicate that future research is well advised to take into account that the relationship between innovation and overconfidence may crucially depend on what type of overconfidence is most prevalent in a particular context.

To cleanly isolate the effects of judgmental overconfidence and overoptimism on innovative activities, we rely on the methods of experimental economics. We implement a modified version of a management task developed by Ederer and Manso (forthcoming) in our laboratory. This task confronts our participants with one of the core features of the innovative process: the trade-off between exploration and exploitation (see, e.g., March 1991, for an extensive discussion). Specifically, our subjects take on the role of a manager of an ice cream stand, whose aim is to find the product mix that maximizes the profit of the ice cream stand. The participants are provided with a default business strategy which delivers a known level of profit. Fine-tuning this strategy (exploitation) allows to increase profits to a certain extent. However, in order to increase profits substantially, the participants need to be willing to change the product mix radically (exploration). In addition to completing the innovation task, our subjects also participate in a number of experimental tests that allow us to elicit measures for judgmental overconfidence and overoptimism, as well as to gather proxies for intelligence and ambiguity aversion.

To substantiate the intuitive hypothesis that judgmental overconfidence and overopti-
mism have opposing effects on innovative activity, we formally analyze a stylized version of our laboratory environment. In particular, we consider a setup in which an agent has the choice between exploitation of the best business strategy currently available to him and the exploration of a novel business strategy in each of a finite number of periods. We show that overoptimism (formalized as an upwardly biased belief about the average profitability of exploration) leads to excessive exploration, while judgmental overconfidence (formalized as an underestimation of the variance in exploratory profits) implies that there is too little exploration.

The experimental data confirm the theoretical prediction that judgmental overconfidence has a significantly negative effect on innovative activity. Participants who exhibit higher degrees of judgmental overconfidence engage in shorter exploratory phases, are less likely to systematically keep track of their exploratory outcomes, and explore a smaller number of new flavors. Moreover, the data also support the hypothesis that judgmental overconfidence results in suboptimal business strategies which lead to both lower overall profits as well as lower maximum per-period profits. Taken together, these results corroborate the fact that judgmental overconfidence has a decisive impact on innovative activity at the individual level.

With regard to overoptimism our theoretical analysis predicts an exploration enhancing effect, which ultimately leads to the implementation of a superior business strategy. However, while the implementation of a superior business strategy boosts maximum per-period profits, the additional costs necessary to obtain such a strategy exceed the additional benefits so that the effect on total profits is hypothesized to be negative. Our experimental data provides some support for a positive impact of overoptimism on exploration and a negative impact on profits, but these effects are weak and remain mostly insignificant. Note, however, that the prediction that overoptimism leads to the implementation of superior business strategies is well aligned with the field evidence mentioned above. Galasso and Simcoe (2011) and Hirshleifer et al. (2012) both find a robust positive association between CEO overconfidence, R&D expenditures and citation-weighted patent counts, confirming that overconfidence leads to more and ultimately better innovations.\footnote{Since they do not observe the opportunity costs of R&D, the net effect on firm profits cannot be properly addressed with their data.}

One potential concern with our approach to study individual innovative activity is that the results may not be generalizable to settings outside the laboratory. Previous studies have not tested whether the experimental exploration-exploitation trade-off implied by the experimental management game is related to real-life innovative activity. To close this gap we test the external validity of our behavioral measure using a sample of middle-managers
of a financial services company. The managers not only participated in our laboratory experiment, but we also surveyed their superiors in their company to collect external data on their individual innovative activity and performance at the workplace. We find a strong and significant correlation between performance in the experimental task and external measures of creativity, performance, gestalt motivation and taking charge behavior. These findings suggest that our laboratory setting is well suited to study the determinants and antecedents of innovative behavior at the individual level.

Our paper extends existing research in several ways. First, our study contributes to a small, but growing literature on the individual determinants of innovative activity. While the literature on the role of innovation at the industry and firm level has made immense progress in recent years (for recent reviews of this literature see, e.g., Hulten, 2010; Arora and Gambardella, 2010; Hall and Lerner, 2010; Fagerberg et al., 2010), our understanding of the individual determinants of innovative activity is still quite limited. However, there is an emerging literature suggesting that behavioral biases such as overconfidence may have an important impact on people’s entrepreneurial and innovative behavior. The general view taken in this research is that individuals are overoptimistic with regard to the returns of potential innovations, for example by overestimating success probabilities of implementing an innovation, which in turn leads to excessive innovation, entrepreneurial activity and market entrance (see, for example, Camerer and Lovallo, 1999; Bernardo and Welch, 2001; Lowe and Ziedonis, 2006; Galasso and Simcoe, 2011; Hirshleifer et al., 2012). Our work not only confirms the relevance of this channel, but also clarifies that it is of great importance to distinguish between overoptimism and judgmental overconfidence. This point is crucial, because these two forms of overconfidence have not always been clearly distinguished in earlier work, although they represent two very different types of biases (see, e.g., Moore and Healy, 2008; Hilton et al., 2011; Heger and Papageorge, 2012 for a discussion).

Second, our study is related to previous work investigating the link between overconfidence and various forms of performance. For example, Benos (1998), Daniel et al. (1998), and Odean (1998) theoretically link judgmental overconfidence to poor trading performance in financial markets and Biais et al. (2005) provide experimental evidence in support of this relationship. Larkin and Leider (2012) provide experimental evidence that overoptimistic agents sort into convex incentive contracts, which may have undesirable consequences for the firm if such sorting is not taken into account. Spinnewijn (2010) analyzes the consequences of different forms of overconfidence in job search on optimal unemployment insurance, and

---

2There is an extensive literature on individual determinants in the entrepreneurship literature. However, this work focuses mainly on characteristics such as wealth, age, education, risk and other socio-demographic characteristics (see, e.g., Kihlstrom and Laffont, 1979; Evans and Leighton, 1989; Blanchflower and Oswald, 1998; Hurst and Lusardi, 2004).
Bolton et al. (forthcoming) show that judgmental overconfidence can be a beneficial attribute of a leader because it can facilitate coordination. We add a new angle to this literature by differentiating the effects of overoptimism and judgmental overconfidence on individuals’ innovative activity.

Finally, our paper also makes a methodological contribution. Existing work on individual determinants of initiative, creativity and innovation at the workplace mostly relies on questionnaire methods (see Bateman and Crant, 1993; Morrison and Phelps, 1999; Parker, 1998), and interviewing techniques (see Frese et al., 1996). While the correlational evidence obtained in these studies yields useful insights, there is also a natural concern that relying on truthful self-reporting of employees may be problematic, because employees may strategically misrepresent the truth. An additional difficulty is that eliciting personality characteristics using questionnaires or interviewing methods does not provide the researcher with a behavioral measure of innovative activity, so that studying policies or the impact of institutions on innovative activity is difficult. Our approach relies on an incentivized laboratory task that we validate using external data, and therefore provides an attractive and incentive compatible alternative which may help to overcome such problems in future research.

The paper proceeds as follows: In Section 2 we present the experimental setup that we used to measure innovative activity and both forms of overconfidence at the individual level. In section 3, we formally derive the hypothesized effects of judgmental overconfidence and overoptimism on innovative activities, based on a stylized model of our experimental setup. Section 4 presents the results and relates our experimental measures to external measures of innovative activity at the workplace. Section 6 concludes.

2 Experiment

We set up a laboratory environment that enables us to assess empirically whether overoptimism and judgmental overconfidence have opposing effects on innovative activity at the individual level. Laboratory experiments have the advantage that participants’ behavior can be observed in a well-defined and tightly controlled environment. In our case we confront each of our participants with an identical innovation task. The task is based on a paradigm developed by Ederer and Manso (forthcoming) and captures the trade-off between exploration and exploitation, which is one of the core elements of innovative decisions. Moreover, our participants go through a series experimental tests that provide us with standardized proxies for overoptimism, judgmental overconfidence, cognitive abilities and ambiguity aversion. These measures allow us to isolate the separate effects of different forms of overconfidence on individual innovation in a very clean and simple way.
2.1 The Ice Cream Stand Task

Our management task consists in operating a virtual ice cream stand for 20 periods. In every period, participants can change six different variables. Three variables are categorical: The location of the stand (business district, stadium, or school), the flavor of the ice cream, and the ice cream color intensity (light or bright). Participants are free to choose a flavor without explicitly predefined options. We include this category to add a dimension in which subjects have to generate own ideas about what to choose. The other three variables, sugar content, flavor intensity and price, can be chosen continuously.

The profit function is designed such that every location has a unique, profit-maximizing bliss point. For deviations from the location specific optimal choice in color intensity, sugar content, flavor intensity, and price, we use a linear penalty function to reduce the payoff. The impact of flavor on profits is independent of the location. Subjects do not know the profit functions. However, as part of the instructions they receive a letter from a fictional previous manager of the stand. The previous manager describes the business strategy he used while selling ice cream in the business district. He mentions that he sold ice cream with orange flavor, he lists flavor intensity, sugar content, and the price that he applied, and he also reveals that he had chosen a light ice cream color. The manager further reveals that he has tried several combinations of variables in the business district, and he emphasizes that he has never changed the flavor of the ice cream nor the location. Finally, he also mentions the per period profit he realized using this business strategy. In addition to the details about his own business strategy, the previous manager also provides general information about the business, explaining that the effect of flavor on per period profits is independent of the location and that different locations may require very different strategies.

The participants thus face the choice between fine-tuning the business strategy of the previous manager (exploitation) or discovering a completely different, more profitable strategy (exploration). The payoffs of the game are defined such that the potential additional profits from fine-tuning the previous manager’s strategy in the business district are small. The only sizeable increase in profit in the business district can be achieved by changing the

---

3Our task is a modified and extended version of the innovation experiment developed by Ederer and Manso (forthcoming). We are grateful to the authors for providing us with their original experimental code.

4In total, 65 different flavors are predefined and coded. If a participant chooses a non-predefined flavor, he or she is asked to pick another flavor.

5In Appendix C we show location specific bliss points and maximally achievable profits at each location in table C.1 and the penalty factors associated with a deviation of one unit in table C.2. The factors for the different flavors are based on real sales numbers in Germany in 2008 provided by “E.I.S. Eis Infoservice der deutschen Markeneishersteller” (see table C.3). To prevent an immediate clustering on obvious choices, we exclude the four most prominent flavors (chocolate, vanilla, strawberry and chocolate chip). The instructions explicitly inform participants that offering these four flavors is never profitable, because they are already offered by successful competitors in all locations.
flavor. On the other hand, changing the location to the school, the most profitable location, requires large changes in at least two other variables to obtain a per period profit which reaches the level of the default business strategy.

During the experiment subjects receive multiple feedback which helps them to learn about the profitability of different strategies. First, they are informed about the profit they obtain at the end of every period. Second, they are also given a customer reaction that contains information about the optimality of their choices. In particular, they receive a binary feedback with regard to one randomly chosen continuous choice variable. To facilitate learning and to allow for systematic exploration, subjects also receive a table in which they can take notes about their choices, profits, and feedback in each period. The subjects are compensated according to a so-called “exploration contract” which has been shown to be effective in motivating innovative behavior. Hence, they were not paid for their performance in periods 1-10, but received the acquired profits in periods 11-20.

The ice cream task allows us to observe the extent to which subjects engage in exploratory activities. We focus on four measures of innovative activity in the ice cream stand task: First, a measure for a subject’s exploratory behavior is the length of the exploratory phase. Ederer and Manso (forthcoming) define the exploratory phase as the number of periods in which a participant is actively exploring novel business strategies, and not simply fine tuning a particular business strategy. Second, the average subject specific standard deviation of the business strategy choices in the three continuous variables, price, flavor intensity and sugar content, is indicative of the exploratory behavior of a subject. Achieving high profits at locations other than the business district requires radically altering choices in these three categories. Average subject specific standard deviations are a direct measure of the extent to which a participant engaged in exploration within these variables. Third, we

---

6For example, if the computer randomly selects the sugar content as the feedback variable and the subject has chosen a sugar content that is above the optimal level for the chosen location, the feedback takes the form: “Many of your customers tell you that the ice cream is too sweet”. The subjects only receives feedback of this sort for the continuous variables.

7A subject enters an exploratory phase if he for the first time chooses a location that differs from the location chosen by the previous manager, changes the color or the flavor of the ice cream, or makes a substantial change in one of the three continuous variables. The exploratory phase ends if a participant stops making such substantial changes in the product mix. To test the robustness of our results, we defined different thresholds that determine whether a change in one of the continuous variables counts as substantial. The threshold that we use is set to a change of at least .25 units in at least one of the variables. Changing this threshold does not qualitatively change our results. Our measure of the exploratory phase differs from that in Ederer and Manso (forthcoming). They require a change in location for the exploratory phase to start and returning to the default location ends the exploratory phase. Again, changing this measure and using the exact definition from Ederer and Manso (forthcoming) does not qualitatively change any of our results.
analyze exploration behavior in the flavor dimension in which subjects were not provided with predefined options. The degree of exploration in this category measures the extent to which a subject generates ideas about potentially profitable business strategies. Fourth, we also analyze subjects’ willingness to invest into exploration by measuring how extensively they take notes.\(^8\)

In every experimental session, subjects first completed the ice cream task and then participated in additional experiments to measure individual preferences, abilities and behavioral biases. We collected proxies for judgmental overconfidence, overoptimism, intelligence and ambiguity aversion. The experimental elicitation of these measures is described in the following subsection.

\subsection*{2.2 Additional Experimental Measurements}

To measure judgmental overconfidence, we adopt the confidence interval elicitation procedure of [Biais et al.]\(^{2005}\), which is originally based on [Lichtenstein et al.]\(^{1982}\). In this task participants are asked to provide an upper and a lower limit such that they are 90 percent confident that the correct answer falls between the two. This is repeated for 10 different questions (see Appendix D). Correct answers are not incentivized, which is the standard procedure for this task. Judgmentally overconfident participants typically provide too narrow ranges, so that actual values fall outside the range more than 10 percent of the time. We therefore use the number of questions for which the true answers fall outside the stated range as a proxy for judgmental overconfidence in our analysis.\(^9\)

We operationalize overoptimism as people’s expectations about their own absolute performance in the Raven Progressive Matrices test ([Raven et al.]\(^{2003}\)). The Raven Progressive Matrices test is a so-called “culture-free” IQ test because it does not depend heavily on verbal skills or other knowledge explicitly taught during formal education. The test consists of 12 items, each of which presents a pattern of abstract figures. The test taker must choose the missing part out of 8 predefined solutions to complete the pattern. Our participants first have to correctly solve two training patterns before each subject is given a total of 12 minutes to complete twelve different patterns without any feedback. After having completed the task subjects are asked to guess the number of patterns that they have solved correctly.

\(^8\) In the students sessions in 2010, we collected the tables in which the subjects could take down notes on their business strategies. While taking notes is not of particular importance for a subject who fine-tunes a business strategy, it is essential for a subject who chooses to explore and who radically alters the business strategy. Therefore, the extent to which a subject took notes during the experiment is indicative of his/her overall inclination to explore.

\(^9\) Evidence for the stability of individual differences in judgmental overconfidence has been provided by [Klayman et al.]\(^{1999}\), [Parker and Fischhoff]\(^{2005}\) and [Jonsson and Allwood]\(^{2003}\).
We use the difference between the guessed number of correctly solved patterns and the actual number of correctly solved patterns as a proxy for an individual’s overoptimism. The performance in IQ test itself serves as a control variable for an individual’s cognitive abilities. In line with the usual methodology in this task, individuals are neither paid for their performance in the task, nor for the accuracy of their expectations.

Finally, subjects participate in a separate lottery experiment in which we elicit each subjects’ ambiguity aversion. Instructions for the elicitation procedure can be found in appendix E.

### 2.3 Procedures and Subject Pool

We recruited 119 subjects from a subject pool that includes students of the University of Zurich and the Swiss Federal Institute of Technology (ETH). In addition to our student participants we also invited 35 middle managers of a financial industries company with approximately 550 employees to participate in our experiment. All experimental sessions (including the ones with the managers) were conducted in the laboratory of the University of Zurich. The experiments were computerized with the software z-tree (Fischbacher, 2007). Student data was collected in 4 sessions in October 2009 and June 2010. The managers participated in three sessions in November and December 2009. A session lasted, on average, 90 minutes. During the experiment, experimental currency units called Taler were used to keep track of monetary earnings. The exchange rate was set at 75 Taler = CHF 1. Subjects on average earned CHF 37 (approx. USD 37) during the experiment.

### 3 Theoretical Analysis and Hypotheses

In this section we theoretically analyze a stylized version of the exploration-exploitation trade-off which is central in our experimental setup. This allows us to formally derive a set of testable hypotheses which will help to organize our data analysis.

---

Student subjects were drawn from a database of volunteers using ORSEE (Greiner, 2004). The number of participants differed across sessions. However, all experiments were purely individual decision experiments, so session size should not influence the results. In the first student session in October 2009, the exchange rate was set to 100 Taler = CHF 1. Moreover, subjects in this session received a show-up fee of CHF 10. In all other sessions the show-up fee was set to 0 and the exchange rate was set to 75 Taler= CHF 1. We don’t find any significant differences in behavior in the first session, and therefore pool the data in the analysis.

---
3.1 Assumptions

We consider an agent $i$ who faces a finite time horizon of $T$ periods and discount the future at a rate of $\delta$. In every period the agent needs to implement a business strategy. We represent the per-period utility of a particular business strategy by $\omega$. When deciding which strategy to implement in a particular period, the agent always has the possibility to either exploit an existing business strategy or to explore and to implement an innovative and novel business strategy. If an agent decides to exploit in period $t$, he implements the best business strategy currently available to him ($\omega^m_t$). If an agent decides to explore in period $t$, he implements a novel business strategy $\omega_t$ which is drawn from an agent specific distribution $F(\omega, \mu_i, \sigma_i)$, where $\mu_i$ is the mean and $\sigma_i$ is the standard deviation of agent $i$’s strategy distribution. We assume that $F$ is differentiable and has support on the whole real line. Differences in $\mu_i$ and $\sigma_i$ can be interpreted as differences in an agents’ ability and precision in generating ideas for new business strategies. It is assumed that draws from $F$ are iid.\footnote{By assuming that the distribution $F$ remains constant over time, we abstract from learning effects. This greatly simplifies the analysis and as long as the updating process itself is not affected by overconfidence, the consideration of learning would not alter our results.}

3.2 Optimal Behavior

We start by showing how an agent $i$ who in period $t$ faces the choice between implementing the best business strategy currently available to him ($\omega^m_t$) and drawing a novel business strategy $\omega_t$ from the distribution $F(\omega, \mu_i, \sigma_i)$ optimally behaves.\footnote{The best business strategy available to the agent in period 1 ($\omega^m_1$) can either be thought of as a default business strategy or there may not be a best business strategy at all (which is identical to assuming that $\omega^m_1 = -\infty$).}

**Proposition 1 (Stopping Rule)** An agent $i$ facing a distribution of business strategies $F(\omega, \mu_i, \sigma_i)$ will explore a novel business strategy $\omega_t$ in period $t$ if the best available business strategy $\omega^m_t$ is strictly inferior to his period-dependent threshold strategy $\overline{x}_t$. Otherwise, agent $i$ will exploit and implement $\omega^m_t$. The period-dependent threshold strategy $\overline{x}_t$ is always weakly superior to $\mu_i$ and weakly decreasing over time, i.e., if the agent stops exploring and starts exploiting in period $t$, he will also exploit in all later periods $t' > t$.

**Proof**: See Appendix A.

The behavior described in Proposition 1 is intuitive. As long as the best available business strategy is strictly inferior to the mean of the agent’s strategy distribution $\mu_i$, exploration is always optimal, because the expected utility of a newly drawn business strategy surpasses the utility of the best business strategy already available. Once the utility of the best available...
business strategy surpasses $\mu_i$, exploration becomes subject to a trade-off. On the one hand, the agent faces an immediate cost, because the expected utility of the newly drawn business strategy is lower than the utility of the best strategy already available to him. On the other hand, however, the agent has the chance of drawing a business strategy which is superior to the best strategy available to him so far, and if this happens, he not only benefits in the current period, but also in all future periods. Obviously, the agent’s incentive to engage in exploration is decreasing in the value of the best available business strategy. In each period $t$ there is a threshold value. If the value of the best available business strategy surpasses the threshold, the agent switches to exploitation. Otherwise, he continues exploring and searches for a better business strategy. In addition, it is important to notice that the benefits of exploration (given a certain best strategy which is already available) decrease over time. The reason is that a shorter time horizon lowers the benefit of having a new best idea.\footnote{A difference between the theory and our experiment is the fact that in the experiment, subjects were not paid for the first 10 periods. However, this does not eliminate the exploration-exploitation trade-off in these periods. It has to be noted that the fixed per period payment that results from exploitation in our theory is a simplifying assumption. In the experiment, subjects can (marginally) improve their profit by exploiting the best currently available strategy and fine-tuning the strategy based on customer feedback. Therefore, exploration in early periods still comes at the cost of forgoing the benefits of implementing a better adjusted business strategy in later periods.}

\section{3.3 Effects of Overoptimism and Judgmental Overconfidence}

Previous work indicates that many people exhibit two distinct forms of overconfidence. On the one hand, people tend to be overoptimistic regarding their abilities (see, e.g., Svenson 1981; Dunning et al., 1989; Alicke et al., 1995). On the other hand, people often overestimate their precision, i.e., they are judgmentally overconfident (see, e.g., Lichtenstein et al., 1982; Russo and Schoemaker, 1992). Our formalization allows us to capture both behavioral biases in a natural way. We assume that the agent has imprecise information about $\mu_i$ and $\sigma_i$, i.e., he forms subjective beliefs $\hat{\mu}_i$ and $\hat{\sigma}_i$ which may deviate from the true mean and standard deviation of the agent’s distribution.

An agent is overoptimistic if $\hat{\mu}_i > \mu_i$. In this case he is overconfident regarding his ability in generating ideas, i.e., he overestimates the average quality of his ideas.\footnote{Dubra (2004) analyzes a related form of overoptimism in a different search context.} To isolate the effect of overoptimism, we model overoptimism as a translation of the whole probability density function to the right, such that all moments of the distribution other than the mean are unaffected by overoptimism.

We say that an agent is judgmentally overconfident if $\hat{\sigma}_i < \sigma_i$. Judgmental overconfidence implies that the agent overestimates his precision in generating ideas, i.e., he underestimates the variance of the distribution from which he draws ideas. We assume that judgmental
overconfidence leads to a simple mean preserving reduction of variance as it is defined in Diamond and Stiglitz (1974). That is, we assume that density is shifted from the tails towards the mean of the distribution. As a consequence, an agent behaves according to his perceived idea distribution function $F(\omega, \hat{\mu}_i, \hat{\sigma}_i)$, while ideas are actually drawn from the true idea distribution function $F(\omega, \mu_i, \sigma_i)$.

We are interested in how overoptimism and judgmental overconfidence affect the trade-off between exploration and exploitation. To analyze these effects we need to investigate how the agent’s distorted beliefs about the distribution of his ideas affect the period-dependent thresholds $\overline{\sigma}_t$. Misperceptions in $\mu_i$ and $\sigma_i$ that raise $\overline{\sigma}_t$ lead to an inefficiently long exploration phase, whereas misperceptions that lower $\overline{\sigma}_t$ cause an inefficiently short exploration phase.

**Proposition 2 (Effect of Judgmental Overconfidence)** The period-dependent stopping thresholds $\overline{\sigma}_t$ for an agent who is judgmentally overconfident regarding the variance of the quality of his ideas ($\hat{\sigma}_i < \sigma_i$) are too low ($\frac{\partial \omega_t}{\partial \sigma_i} > 0$). This implies that a judgmentally overconfident agent will, on average, explore fewer novel strategies than would be optimal given the true distribution of his business strategies.

**Proof:** See Appendix A.

**Proposition 3 (Effect of Overoptimism)** The period-dependent stopping thresholds $\overline{\sigma}_t$ for an agent who is overoptimistic regarding the average quality of his ideas ($\hat{\mu}_i > \mu_i$) is too high ($\frac{\partial \omega_t}{\partial \mu_i} > 0$). This implies that an overoptimistic agent will, on average, explore more novel strategies than would be optimal given the true distribution of his business strategies.

**Proof:** See Appendix A.

We have established that, in our model, the two different forms of overconfidence, overoptimism and judgmental overconfidence, have opposing impacts on an agent’s decision to explore or to exploit. Overoptimism, an overestimation of average ability in idea generation, unambiguously leads to excessive exploration. On the other hand, judgmental overconfidence, an underestimation of the variance of the idea generation process, unambiguously leads to too little exploration.

The inefficiencies caused by overoptimism and judgmental overconfidence are also reflected in the realized profits of the agent’s innovative activities:

**Corollary 1** The excessive exploration caused by overoptimism harms overall profits of the agent. However, the per period profit of the ultimately realized idea is increasing in overoptimism. The insufficient exploration caused by judgmental overconfidence, on the other hand, decreases both overall profits and the per period profit of the ultimately realized idea.
The corollary is intuitive. Proposition 1 identifies a unique profit maximizing business strategy: the agent should explore novel business strategies until he reaches a period in which the per-period utility of the best business strategy already available to him surpasses a period-dependent threshold utility. From this period on the agent should exploit this business strategy and implement it in all remaining periods. Propositions 2 and 3 show that both overoptimism and judgmental overconfidence induce the agent to deviate from this profit maximizing strategy. Hence, both these biases decrease overall profits of the agent. However, the fact that overoptimism increases the period-dependent stopping thresholds $\omega_t$ also implies that the agent explores more business strategies than in the absence of the bias. Accordingly, an overoptimistic agent will, on average, end up implementing better business strategies than an unbiased, but otherwise identical agent.

3.4 Hypotheses

The formal analysis of the stylized model of our experiment yields the following hypotheses that we can test using our experimental data:

**Hypothesis 1 (Judgmental Overconfidence)** *In our experiment, a higher degree of judgmental overconfidence is hypothesized to lead to less exploratory activity. In particular, subjects with high judgmental overconfidence are expected to have shorter exploratory phases, a lower variance in product mix choices and to explore less ice cream flavors. In addition, a higher level of judgmental overconfidence is also expected to decrease a subject’s propensity to take systematic notes about the results of his or her exploratory activities. Finally, we expect that the inefficiently low exploration leads to smaller total and maximum per period profits.*

Intuitively, judgmentally overconfident subjects believe that they have pinned down the potential profits in the task relatively precisely. Controlling for other subject characteristics, this overconfidence reduces the believed profitability of exploration, which we expect to observe in our experimental data.

**Hypothesis 2 (Overoptimism)** *In our experiment, a higher degree of overoptimism is hypothesized to lead to more exploratory activity. In particular, subjects with high overoptimism are expected to have longer exploratory phases, a higher variance in product mix choices, and to explore more ice cream flavors. A higher level of overoptimism is also expected to manifest itself in an increase of a subject’s propensity to take notes. Finally, we expect that the inefficiently high exploration leads to smaller total, but higher maximum per period profits.*
Intuitively, overoptimistic subjects overestimate the expected profitability of novel ideas. This biases them towards excessive exploration. Excessive exploration is expected to increase the profitability of the best available idea at the end of the experiment. However, the additional gross revenues are outweighed by the costs caused by excessive exploration, which reduces expected total profits.

We will test these hypotheses against the data in the next section.

4 Results: Effects of Overoptimism and Judgmental Overconfidence

In this section we show to what extent our measures of judgmental overconfidence and overoptimism predict innovative behavior in the experimental management task that we have implemented. Proposition \(2\) predicts that judgmental overconfidence decreases exploratory activity and Corollary \(1\) implies that the reduction in innovation harms per period profits. Our data yield the following result:

Result 1 (Judgmental Overconfidence)  Judgmental overconfidence significantly reduces explorative and innovative activity and negatively affects the average earnings as well as the maximum per period profit in the ice cream task.

Support for Result \(1\) comes from Figure \(1\) and Table \(1\). In Figure \(1\) we split our sample of participants at the median level of judgmental overconfidence and present our four measures of innovative activity for people with high and low levels of judgmental overconfidence. The figure reveals that subjects exhibiting a higher level of judgmental overconfidence have shorter exploratory phases (two sample t-test: \(p = 0.015\)), are less likely to take comprehensive notes of explored business strategies (\(p = 0.001\)), and have a smaller average individual standard deviation in their choices of the three continuous strategic variables in the ice cream task (\(p = 0.023\)). Although judgmentally overconfident subjects also try out a smaller number of flavors, this difference is not statistically significant (\(p = 0.123\)).

Table \(1\) confirms the results illustrated in Figure \(1\) using regression analysis. Column (1) shows the marginal effects of a Poisson estimation, in which we regress the length of the exploratory phase on judgmental overconfidence, overoptimism, and control variables for IQ, ambiguity aversion, and being part of the student subject pool. We use a Poisson model because the length of the exploratory phase is a variable counting the number of periods in which a subject keeps exploring the product mix before turning towards fine tuning. We find a highly significant negative impact of judgmental overconfidence on the length of the
exploratory phase. Per unit increase in the subject’s degree of judgmental overconfidence, a subject stops exploring 0.47 periods earlier.\footnote{As already pointed out in section \ref{sec:methods}, this result is robust with respect to changes in the definition of the exploratory phase. Requiring a change in flavor or in location as a starting point of the exploratory phase, or changing the threshold at which changes in the continuous variables no longer count as exploratory does not qualitatively change the result.}

Figure 1: Median Splits

The sample is split in two halves at median judgmental overconfidence. The top left figure shows a median split for the length of the exploratory phase. The top right figure shows a median split for the number of explored flavors. The bottom left figure shows a median split for the frequency of completed notes. The bottom right picture shows a median split for the average standard deviation in the continuous variable choices of the product mix.

In column (2) we use a Poisson regression to examine the effect of judgmental overconfidence on the number of different ice cream flavors that a subject explored over the course of the experiment. We find that overconfidence in judgment leads to a highly significant reduction in the number of explored flavors. Per unit increase in the subject’s degree of judgmental overconfidence, the number of explored flavors on average decreases by 0.17.

Column (3) reports the marginal effects of a probit regression on a dummy that indicates whether or not a subject took comprehensive notes of explored business strategies and the
associated profits. Taking notes is an indicator of the effort that subjects invested in exploring. We hypothesized that a judgmentally overconfident subject is less willing to explore, and therefore should be less willing to invest effort in exploratory activities, like taking notes. This is also what we find in the data. Indeed, it becomes 7.6% less likely that a subject took comprehensive notes during the experiment per unit increase in the subject’s degree of judgmental overconfidence.

Table 1: Regression Analysis of Measures for Innovative Activity on Covariates

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
<th>(6)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Expl. Num. of Notes</td>
<td>Avg. Std. Deviation</td>
<td>Total Profit (Points)</td>
<td>Max. Profit (Points)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>IQ</td>
<td>0.232</td>
<td>0.027</td>
<td>0.023</td>
<td>-1.356</td>
<td>-2.751</td>
<td></td>
</tr>
<tr>
<td>Overopt.</td>
<td>0.115 **</td>
<td>0.004</td>
<td>0.025</td>
<td>-28.32</td>
<td>-2.560</td>
<td></td>
</tr>
<tr>
<td>Judg. OC.</td>
<td>-0.469 ***</td>
<td>-0.076 **</td>
<td>-0.028</td>
<td>-79.28*</td>
<td>-9.307*</td>
<td></td>
</tr>
<tr>
<td>Student</td>
<td>-0.012</td>
<td>-0.236</td>
<td>-0.186*</td>
<td>38.50</td>
<td>7.863</td>
<td></td>
</tr>
<tr>
<td>Amb. Av.</td>
<td>-0.033</td>
<td>0.267*</td>
<td>0.042</td>
<td>-0.024</td>
<td>-35.72</td>
<td>-1.543</td>
</tr>
<tr>
<td>Constant</td>
<td>1.203 ***</td>
<td>2262.62 ***</td>
<td>265.086 ***</td>
<td>1.203 ***</td>
<td>2262.62 ***</td>
<td>265.086 ***</td>
</tr>
</tbody>
</table>

Columns (1) and (2) report marginal effects of Poisson regressions on count data. Column (3) shows marginal effects of a probit regression. Columns (4)-(6) show coefficients of robust regressions. Student is a dummy variable for the student subsample. Significance levels: * p < 0.1, ** p < 0.05, *** p < 0.01. Subjects that made inconsistent choices in the ambiguity aversion task are excluded. Inclusion of these subjects does not qualitatively change the result. Data on notes is only available for student subjects participating in experiments in 2010, which reduces the sample size to 98.

In column (4) we investigate the impact of judgmental overconfidence on the average individual standard deviation in the choice of the continuous strategic variables (price, flavor intensity and sugar content) in the experiment. Using a robust regression we find that judgmental overconfidence has a negative impact on the average standard deviation, indicating that overconfidence reduces the degree of exploration within these variables.\[16\] In contrast

\[16\]In columns (4), (5) and (6) of table 1 we use robust regressions because our data contains a number of outliers.
to the result based on the median split in Figure 1, this result is, however, not significant ($p = 0.25$). This regression also reveals that our student sample is slightly less explorative in this domain than our manager sample.

Finally, Columns (5) and (6) examine how judgmental overconfidence affects per period profits of participants in the ice cream stand task. Our theory predicts that insufficient exploration should ultimately lead to a reduction in achieved as well as maximum per period profits. We present the results of robust regressions of achieved earnings and maximum per period profits on our explanatory variables. The regression estimates indeed reveal a negative relationship between judgmental overconfidence and performance in the task. The coefficients of judgmental overconfidence are large and significant at the 10 percent level. Per unit increase in the subject’s degree of judgmental overconfidence, total profits in the ice cream task decrease by 79 points ($p = 0.055$) and the maximum per period profit decreases by 9.3 ($p = 0.053$) points.

Taken together, the evidence presented in Figure 1 and Table 1 reveals a clear and consistent picture of the effects of judgmental overconfidence on individual innovation. The evidence shows that the tendency to overestimate the precision of one’s information is detrimental to innovative activity, reduces explorative efforts and leads to lower profits. This provides strong support for our theoretical predictions on judgmental overconfidence stated in Proposition 2 and Corollary 1.

Regarding the effect of overoptimism on exploratory activities and profits Proposition 3 and Corollary 1 suggest that overoptimism increases innovative activity, decreases total earnings due to over-exploration, but increases the maximum per period profit that a subject achieves during the experiment. Our data yield the following result:

**Result 2 (Overoptimism)** Overoptimism increases the number of explored flavors, the length of the exploratory phase, the average standard deviation of product mix choices and the tendency to take comprehensive notes in the ice cream task. However, this positive relationship is only statistically significant for the number of explored flavors. Moreover, overoptimism neither significantly affects total profits nor the maximum per period profit in our experiment.

An inspection of the estimations presented in Table 1 reveals that our measure of overoptimism is positively related to all four exploration measures, but affects only one of them significantly. Column (2) shows that per unit increase in a subject’s degree of overoptimism, the number of explored flavors increases by .18 units. Besides this effect overoptimism does not significantly affect our measures of exploratory activity. Hence, we cannot reject the hypothesis that overoptimism has no effect on exploratory behavior in our setup. In addition,
there is also no evidence for an effect of overoptimism on profits. The regressions for total earning and maximum per period profits in Columns (5) and (6) do not yield significant results for the overoptimism variable.

In light of the existing field data the lack of a strong impact of overoptimism on innovative activity in our data is somewhat surprising. In particular, Galasso and Simcoe (2011) find a robust correlation between CEO overconfidence and innovative activities of the company. Even more so, they find that overconfident CEO’s obtain more patents and citations per dollar of R&D. This implies that they are more likely to generate particularly good innovations, but it does not imply that they are more profitable since the measure ignores potential opportunity costs. This is precisely what our model suggests.

The existing field evidence as well as aspects of our data suggest that the failure to find significant correlations between overoptimism and innovative activity in our experiment may be a consequence of our overoptimism measure. Interestingly, the regressions in Table I reveal that our IQ measure itself is also not predictive with respect to the innovative activities of our subjects. It is therefore likely that the culture-free intelligence measure that we used is not strongly related to a subject’s creativity and innovativeness. It is therefore possible that overoptimism in the domain of culture-free intelligence does not generalize to overoptimism in the domain of creativity and innovative activity. If this is the case, it is not surprising that our proxy for overoptimism, the difference between guessed correct patterns in the Raven’s IQ task and the true number of correct patterns in the Raven’s IQ task, does not correlate with observed behavior in the ice cream task. The current state of research does not provide much insights regarding more appropriate measures of overoptimism in the context we are interested in. We hope that future research will show how and to what extent different forms of overoptimism correlate across different domains of choices, so that it becomes easier to find a useful measure for the domain one is interested in.

5 External Validity of the Experimental Task

A potential pitfall of a laboratory measure of exploratory activity and innovation is that it is unclear to what extent the measure captures the same type of innovativeness that real-world companies care about. We identify the extent to which our laboratory measure correlates with real-life innovation behavior by comparing the laboratory decisions of our manager participants with external data on their individual innovativeness and performance on the job. To obtain measures of the on-the-job innovativeness in the company, we sent an online survey to the direct supervisor of each manager participant as well as to a person in the HR
department who was familiar with the manager’s dossier.  

Every manager was rated in five different categories: Taking charge behavior, action orientation, gestalt motivation, creativity, and performance. “Taking Charge” is measured via an established questionnaire from the management literature (Morrison and Phelps, 1999). Taking Charge is defined as “Constructive efforts by employees to effect functional change with respect to how work is executed”. It is measured with a 10-item questionnaire on a 5-point Likert scale and has previously been associated with innovative behavior in the company (see Unsworth, 2001). While taking charge has originally been developed as a pro-active personality and initiative measure, there is convergence to the view that initiative and pro-activity are necessary determinants of innovative activity (see Unsworth and Parker, 2003). We have adapted the items measuring “Action Orientation” and “Gestalt Motivation” from the ”Bochumer Inventar zur berufsbezogenen Persoenlichkeitsbeschreibung” (Hossiep and Paschen, 2003). This is the most widely used psychological assessment of job related personality characteristics in Germany. There are 9 items for action orientation” and 12 items for gestalt motivation. Both are elicited on a 7-point Likert scale. Persons with high levels of action orientation start implementing ideas as soon as a decision has been made. They are very goal oriented and do not get distracted by obstacles or difficulties when carrying out a project. Gestalt motivation is defined as having a self-starting, pro-active work approach and the motivation to change processes and situations according to one’s own agenda. It describes the attitude to actively create and change the environment and organizational processes the employee is involved in, and therefore captures the incremental innovations to organizational processes that every employee can achieve. “Creativity” and “Performance” were each assessed with a 4 item questionnaire on a 7-point Likert scale. Both of these questionnaires were developed by us. All questions can be found in Appendix D.

We received 31 completed surveys from direct supervisors and 26 surveys from the HR department. The correlations between the supervisor ratings and the HR-ratings are generally high (\( \rho \in [0.46, 0.66] \)) and significant, with the exception of the action orientation ratings (see table B.3 in Appendix B). Since more data is available for supervisor ratings

---

17To ensure anonymity, we did not contact the supervisors directly, but through a third agency, which subsequently matched the survey data to the experimental data. This procedure guaranteed that neither we nor the financial industry company can link performance in the experimental task or the rating in the survey to the identity of a manager.

18All items used in the survey are reproduced in Appendix D.

19Originally, this is a self-report questionnaire. We rephrased the items such that the ratings relate to a third person.

20We did not obtain two completed surveys for all of the 35 participating managers, because there was turnover at the company and for some managers no direct supervisor or HR person was available.
and since supervisors are, in general, closer to the managers during everyday business, we focus on supervisor ratings in our analysis below.\footnote{In appendix B, we also provide the analysis for pooled ratings. The patterns do not change qualitatively.}

When investigating the relation between these external measures and our laboratory measure of innovative activity, we find the following result:

**Result 3 (External Validity)** Profit measures in the Ice Cream Task are strongly correlated with performance, creativity and gestalt motivation measures in the company. The profit measures are also strongly correlated with taking charge behavior.

| Table 2: Pairwise Correlations of experimental and external survey measures |
|---|---|---|---|---|
| | (1) Creativity | (2) Gestalt motivation | (3) Action orientation | (4) Taking Charge | (5) Performance |
| Profit Period | 0.33* | 0.44** | 0.23 | 0.44** | 0.49*** |
| 11-20 (Points) | (0.07) | (0.013) | (0.22) | (0.014) | (0.005) |
| Max. Period | 0.34* | 0.46*** | 0.28 | 0.46*** | 0.52*** |
| Profit (Points) | (0.06) | (0.009) | (0.13) | (0.009) | (0.003) |
| Observations | 31 | 31 | 31 | 31 | 31 |

The table reports pairwise correlation coefficients. p-values are reported in parentheses below the correlation coefficient. Significance levels: * p < 0.1, ** p < 0.05, *** p < 0.01.

Support for Result 3 comes from Table 2. The table shows pair-wise correlation coefficients between average and maximum profit measures and the employee ratings in the external surveys. First of all, it is noteworthy that every single correlation coefficient is positive, indicating that performance in the experimental task is directionally consistent with all our external measures. Manager creativity is significantly correlated with both profit measures in the ice cream task, subject earnings over the last ten periods in the experiment as well as the maximum per period profit achieved by a subject throughout the experiment. The same picture arises when looking at gestalt motivation. Both profit measures are highly positively correlated with the reported gestalt motivation (the correlation coefficient is always above 0.4) and the correlations are always significant at least at the 5 percent level. The relationship between action orientation and our experimental task is less clear. The correlation coefficients are lower (between 0.2 and 0.3), and not statistically significantly different.
When looking at the correlation with taking charge behavior, the performance in the experimental task is again highly predictive. Correlation coefficients range between 0.4 and 0.47, and statistical significance is always at least at the five percent level. The experimental profit measures also correlate positively with the overall performance rating in the company. Overall, the performance measures in the experimental task are highly correlated with the external evaluations of creativity, gestalt motivation, taking charge behavior and performance. This is evidence that behavior in management games like our ice cream task is an admissible proxy for innovative activity in companies.

6 Conclusion

In this paper we argue that the connection between overconfidence and innovative activity is more nuanced than the existing literature suggests. In particular, we show that different forms of overconfidence may have opposing effects on innovative activity. While overoptimism leads to the innovation enhancing effect which has been identified in previous field work, judgmental overconfidence inhibits innovation. Our results indicate that future research is well advised to take into account that the relationship between innovation and overconfidence may crucially depend on what type of overconfidence is most prevalent in a particular context.

Our paper makes a number of contributions. To the best of our knowledge we are the first pointing out that different forms of overconfidence can have opposing effects on innovative activity. This is an important insight since overoptimism and judgmental overconfidence have not always been clearly distinguished in previous research.

Moreover, our approach to experimentally study the individual determinants of innovative behavior is, again to the best of our knowledge, novel. Our experiments provide a behavioral measure that is a useful complement to the questionnaire and interview methods currently used for this kind of research. The external evidence provided in this paper suggests that experiments provide valid measurements of individual innovative activity.

\[22\] Remember that action orientation was also the only category in which the correlation between the HR and supervisor ratings was low. Probably our external measure of action orientation is very imprecise. In addition, by definition the concept of action orientation is more focused on the implementation of a given idea rather than the development of new ideas. Since the ice cream stand task is more closely related to the process of idea generation, it is plausible that action orientation is not an individual characteristic that is of particular importance in the experimental task.

\[23\] We also regressed the score in every category separately on every single profit measure (regression results are available upon request), and cluster standard errors on supervisors (20 different supervisors are responsible for the 31 ratings). Significance of the regression coefficients is approximately in the same range as the pair-wise correlations reported here, which do not use clustered standard errors.
Finally, we believe that the distinction between overoptimism and judgmental overconfidence provides interesting avenues for future research on the importance of overconfidence as a driver of innovation. From a theoretical perspective, distinguishing between overoptimism and judgmental overconfidence seems to be of importance in the screening process for innovators. Depending on the nature of the search costs, it might be beneficial to employ over-optimistic employees, whereas judgmental overconfidence will be harmful to the employer. Future research may shed further light on these questions.

Acknowledgements

We are grateful to Stefan Bechtold, Florian Ederer, Ernst Fehr, Michael Kosfeld, Gustavo Manso, Dana Sisak, Eric Zwick and seminar participants at Boston University, Harvard University, the University of Zurich and ETH Zurich as well as participants of the ESA International Meetings 2010 at the University of Copenhagen and the Meeting of the European Economics Association 2012 in Malaga for helpful suggestions and comments.
References


Appendix A: Proofs

In this section, we formally derive propositions 1-3 from section 3.

Proof of Proposition 1 (Optimal Stopping Rule)

We first show that if an agent’s optimal choice is to explore in period $t$, then the agent’s optimal choice in period $t-1$ is also to explore. This implies that an optimally behaving agent who chooses to exploit in any period $t < T$, will never switch to explore in any later period $t' > t$.

The proof is by contradiction. Define $V_t(\omega^m)$ as the present value of having a best idea $\omega^m$ in period $t$ if the agent chooses optimally between exploitation and exploration in every period $t' \geq t$. Assume that an agent who has access to a best idea $\omega^m$ prefers to explore in period $t$. This implies:

$$\mu + \delta [P(\omega > \omega^m)E[V_{t+1}(\omega)|\omega > \omega^m] + (1 - P(\omega > \omega^m))V_{t+1}(\omega^m)] \geq \omega^m + \delta V_{t+1}(\omega^m),$$

$$\delta P(\omega > \omega^m) [E[V_{t+1}(\omega)|\omega > \omega^m] - V_{t+1}(\omega^m)] \geq \omega^m - \mu. \quad (1)$$

The best idea available to the agent in period $t-1$ must satisfy $\omega^m_{t-1} \leq \omega^m$. If $\omega^m_{t-1} = \omega^m$, the agent exploits if:

$$\mu + \delta [P(\omega > \omega^m)E[V_{t}(\omega)|\omega > \omega^m] + (1 - P(\omega > \omega^m))V_{t}(\omega^m)] < \omega^m + \delta V_{t}(\omega^m),$$

$$\delta P(\omega > \omega^m) [E[V_{t}(\omega)|\omega > \omega^m] - V_{t}(\omega^m)] < \omega^m - \mu. \quad (2)$$

Switching from exploitation in period $t-1$ to exploration in period $t$, requires that conditions [1] and [2] are satisfied at the same time. This implies:

$$E[V_{t+1}(\omega)|\omega > \omega^m] - V_{t+1}(\omega^m) > E[V_{t}(\omega)|\omega > \omega^m] - V_{t}(\omega^m), \quad (3)$$

or

$$\frac{\partial [E[V_{t}(\omega)|\omega > \omega^m] - V_{t}(\omega^m)]}{\partial t} > 0. \quad (4)$$

Note that having an idea $\omega' > \omega$ available in period $t$ guarantees a per period profit which is at least as large as the per period profit generated by having the idea $\omega$. The reason is that the (expected) per period profit of exploration is always $\mu$ independent of the best idea available in the period, while the per period profit of exploitation is $\omega^m_t$ and therefore
increases in the utility of the best idea available in the period. This implies that \( \frac{\partial V_t(\omega_m)}{\partial \omega_t} \geq 0 \). Thus, since this also holds for all later periods \( t' > t \), the positive effect of a better idea on the present value is larger the longer the remaining time horizon. This implies \( \frac{\partial V_t(\omega_m)}{\partial \omega_t} \leq 0 \). As a consequence, the difference between \( E[V_t(\omega)|\omega > \omega_m] - V_t(\omega_m) \) must be weakly decreasing in the period \( t: \frac{\partial [E[V_t(\omega)|\omega > \omega_m] - V_t(\omega_m)]}{\partial t} \leq 0 \). This contradicts equation (3).

The fact that it is never optimal for an agent to switch back to exploring once she has started to exploit implies that there exists a period-dependent stopping threshold. Let’s denote \( \omega_t \) as the agent’s stopping threshold in period \( t \). If the best idea available in period \( t \) exceeds the threshold, the agent exploits, otherwise he explores. Since an agent will never switch from exploitation back to exploration, the stopping threshold must be weakly decreasing over time: \( \frac{\partial \omega_t}{\partial t} \leq 0 \).

Assume that the best idea available to the agent in period \( t \) is \( \omega_t^m \). If it turns out that exploitation is optimal in period \( t \) (and all following periods \( t' > t \)), the agent’s present value is:

\[
V_t(\omega_t^m) = T - t \sum_{\tau=0}^{T-t} \delta^\tau \omega_t^m, \\
V_t(\omega_t^m) = \frac{1 - \delta^{T-t+1}}{1 - \delta} \omega_t^m. \tag{5}
\]

If the agent decides to explore in period \( t \) instead, the present value depends not only on the explore-exploit decision in period \( t \), but also on the explore-exploit decision in all subsequent periods. To determine the stopping threshold in period \( t \), however, it suffices to analyze the value of the exploration strategy under the assumption that the best idea available to the agent in period \( t \) already exceeds the stopping threshold in period \( t + 1 \): \( \omega_t^m > \omega_{t+1} \). If it is optimal to explore in period \( t \) if \( \omega_t^m > \omega_{t+1} \), this will necessarily also be the case for smaller values of \( \omega_t^m \), since the value of exploitation is than strictly smaller. The agent’s present value if he explores in period \( t \) is therefore given by

\[
V_t(\omega_t^m) = \mu + F(\omega_t^m) \sum_{\tau=1}^{T-t} \delta^\tau \omega_t^m + [1 - F(\omega_t^m)] \sum_{\tau=1}^{T-t} \delta^\tau E[\omega|\omega \geq \omega_t^m], \\
V_t(\omega_t^m) = \mu + F(\omega_t^m) \frac{\delta - \delta^{T-t+1}}{1 - \delta} \omega_t^m + \frac{\delta - \delta^{T-t+1}}{1 - \delta} \int_{\omega_m}^{\infty} f(\omega) \omega d\omega. \tag{6}
\]

The stopping threshold \( \overline{\omega}_t \) is therefore defined as the \( \omega_t^m \) which equalizes the right-hand sides of equations (5) and (6). Implicitly, the stopping threshold \( \overline{\omega}_t \) is defined by the following
condition:

\[ [1 - \delta^{T-t+1} - (\delta - \delta^{T-t+1})F(\omega_t)]\overline{\omega}_t - (\delta - \delta^{T-t+1}) \int_{\omega_t}^{\infty} f(\omega) \omega d\omega = (1 - \delta) \mu. \quad (7) \]

The derivative of the left-hand side of equation (7) with respect to \( \omega_t \) is strictly positive:

\[ 1 - \delta^{T-t+1} - (\delta - \delta^{T-t+1})F(\omega_t) > 0 \]

This implies that the stopping threshold \( \omega_t \) is unique.

**Proof of Proposition 2: The Effect of Judgmental Overconfidence**

We investigate how the agent’s distorted belief about the variance in the distribution of business strategies (\( \hat{\sigma}_i < \sigma_i \)) affects the thresholds \( \omega_t \). For this purpose we consider two distributional functions: \( F_1(\omega) = F(\omega, \mu, \sigma_1) \) and \( F_2(\omega) = F(\omega, \mu, \sigma_2) \). We follow [Diamond and Stiglitz (1974)] and assume that \( F_2(\omega) \) results from a mean preserving spread of \( F_1(\omega) \) so that the two distribution functions cross exactly once (at \( \hat{\omega} \)):

\[ F_2(\omega) - F_1(\omega) \leq (\geq) 0 \text{ when } \omega \geq (\leq) \hat{\omega}. \quad (8) \]

We show that the stopping threshold \( \overline{\omega}_t \) of an agent who believes that the idea distribution function is given by \( F_1(\omega) \) is strictly smaller than the threshold of an agent who believes that the idea distribution function is given by \( F_2(\omega) \) (see equation (7) for the definition of \( \overline{\omega}_t \)):

\[ [1 - \delta^{T-t+1} - (\delta - \delta^{T-t+1})F_1(\omega)]\overline{\omega} - (\delta - \delta^{T-t+1}) \int_{\omega}^{\infty} f_1(\omega) \omega d\omega \geq [1 - \delta^{T-t+1} - (\delta - \delta^{T-t+1})F_2(\omega)]\overline{\omega} - (\delta - \delta^{T-t+1}) \int_{\omega}^{\infty} f_2(\omega) \omega d\omega. \]

This can be rewritten as

\[ F_2(\overline{\omega})\overline{\omega} + \int_{\overline{\omega}}^{\infty} f_2(\omega) \omega d\omega \geq F_1(\overline{\omega})\overline{\omega} + \int_{\overline{\omega}}^{\infty} f_1(\omega) \omega d\omega, \]

\[ \int_{\overline{\omega}}^{\infty} f_2(\omega) \omega d\omega - \int_{\overline{\omega}}^{\infty} f_1(\omega) \omega d\omega \geq F_1(\overline{\omega})\overline{\omega} - F_2(\overline{\omega})\overline{\omega}, \]

\[ \int_{\overline{\omega}}^{\infty} [f_2(\omega) - f_1(\omega)] \omega d\omega \geq (F_1(\overline{\omega}) - F_2(\overline{\omega}))\overline{\omega}. \]
Note that

\[ F_1(\omega) - F_2(\omega) = \int_{-\infty}^{\omega} [f_1(\omega) - f_2(\omega)] d\omega = \int_{\omega}^{\infty} [f_2(\omega) - f_1(\omega)] d\omega. \]  

(9)

Therefore, we can further rewrite as follows:

\[ \int_{\omega}^{\infty} [f_2(\omega) - f_1(\omega)] \omega d\omega \geq \int_{\omega}^{\infty} [f_2(\omega) - f_1(\omega)] \omega d\omega, \]

\[ \int_{\omega}^{\infty} [f_2(\omega) - f_1(\omega)] (\omega - \omega) d\omega \geq 0. \]  

(10)

Equation (10) is satisfied as a direct consequence of condition (8). This can be seen as follows: If \( \bar{\omega} \geq \hat{\omega} \), condition (10) follows immediately by stochastic dominance of \( F_2 \) over \( F_1 \) in the relevant domain. If \( \bar{\omega} < \hat{\omega} \), condition (10) follows from the fact that (10) holds with equality for \( \bar{\omega} \to -\infty \) and (10) is strictly positive for some \( \bar{\omega} \geq \hat{\omega} \). By condition (8), equation (10) must then also hold for all \( \bar{\omega} > -\infty \).

This implies that a decrease in the variance unambiguously leads to a decrease in the threshold. Hence, judgmental overconfidence reduces exploration incentives and reduces the likelihood of participation in innovative activities.

**Proof of Proposition 3: The Effect of Overoptimism**

We investigate how the agent’s distorted belief about the mean of the distribution of business strategies (\( \hat{\mu}_i > \mu_i \)) affects the thresholds \( \bar{\omega}_t \). For this purpose we compare two otherwise identical distributions with different means: \( F_1(\omega) = F(\omega, \mu_1, \sigma) \) and \( F_2(\omega) = F(\omega, \mu_2, \sigma) \), where \( \mu_1 > \mu_2 \). \( F_2(\omega) \) results from a translation of the density function of \( F_1(\omega) \) to the right. This keeps all moments of the distribution other than the mean constant. The translation to the right implies first-order stochastic dominance, i.e., \( F_1(\omega) \leq F_2(\omega) \) for all \( \omega \).

We show that the stopping threshold \( \bar{\omega}_t \) of an agent who believes that the idea distribution function is given by \( F_1(\omega) \) is strictly larger than the threshold of an agent who believes that the idea distribution function is given by \( F_2(\omega) \) (see equation (7) for the definition of \( \bar{\omega}_t \)):

\[
[1 - \delta^{T-t+1} - (\delta - \delta^{T-t+1}) F_1(\bar{\omega})] \bar{\omega} - (\delta - \delta^{T-t+1}) \int_{\bar{\omega}}^{\infty} f_1(\omega) \omega d\omega - (1 - \delta) \mu_1 \leq \\
[1 - \delta^{T-t+1} - (\delta - \delta^{T-t+1}) F_2(\bar{\omega})] \bar{\omega} - (\delta - \delta^{T-t+1}) \int_{\bar{\omega}}^{\infty} f_2(\omega) \omega d\omega - (1 - \delta) \mu_2.
\]
This can be rewritten as

\[
[F_1(\omega) - F_2(\omega)]\omega + \int_{\omega}^{\infty} [f_1(\omega) - f_2(\omega)] \omega d\omega + \frac{1 - \delta}{\delta - \delta^{T-t+1}} (\mu_1 - \mu_2) \geq 0
\]

Using again equation (9) we can further rewrite:

\[
\int_{\omega}^{\infty} [f_1(\omega) - f_2(\omega)] (\omega - \bar{\omega}) d\omega + \frac{1 - \delta}{\delta - \delta^{T-t+1}} (\mu_1 - \mu_2) \geq 0
\]

This inequality follows immediately from first order stochastic dominance. It follows that an increase in \(\mu_i\) leads to an increase in \(\bar{\omega}\). Overoptimism therefore unambiguously leads to an increase in exploratory behavior and to increased participation in innovative activities.
Appendix B: Additional Tables

Table B.1: Summary Statistics of Supervisor Ratings

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean</th>
<th>Std. Dev.</th>
<th>Min.</th>
<th>Max.</th>
<th>Obs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Creativity</td>
<td>0.651</td>
<td>0.229</td>
<td>0</td>
<td>1</td>
<td>32</td>
</tr>
<tr>
<td>Gestalt Motivation</td>
<td>0.749</td>
<td>0.16</td>
<td>0.375</td>
<td>1</td>
<td>32</td>
</tr>
<tr>
<td>Action Orientation</td>
<td>0.664</td>
<td>0.173</td>
<td>0.241</td>
<td>0.944</td>
<td>32</td>
</tr>
<tr>
<td>Taking Charge</td>
<td>0.709</td>
<td>0.153</td>
<td>0.325</td>
<td>1</td>
<td>32</td>
</tr>
<tr>
<td>Performance</td>
<td>0.694</td>
<td>0.207</td>
<td>0.292</td>
<td>1</td>
<td>32</td>
</tr>
</tbody>
</table>

Summary statistics of a transformed measure that reflects the realized percentage of achievable points in the reported measure.

Table B.2: External Data Questionnaires

<table>
<thead>
<tr>
<th>Questionnaire</th>
<th>Source</th>
<th>Correlation $^1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Taking charge</td>
<td>Morrison and Phelps (1999)</td>
<td>0.66***</td>
</tr>
<tr>
<td>Action orientation</td>
<td>Hussiep and Paschen (2003)</td>
<td>0.32</td>
</tr>
<tr>
<td>Gestalt motivation</td>
<td>Hussiep and Paschen (2003)</td>
<td>0.62***</td>
</tr>
<tr>
<td>Creativity</td>
<td>own items</td>
<td>0.46**</td>
</tr>
<tr>
<td>Performance</td>
<td>own items</td>
<td>0.64***</td>
</tr>
</tbody>
</table>

$^1$ Correlation reports the pair-wise correlation coefficient between the supervisor and the HR rating. P-values are reported in parentheses. Significance levels: * $p<0.1$, ** $p<0.05$, *** $p<0.01$.

Table B.3: External Data Questionnaires

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Creativity</td>
<td>0.26</td>
<td>0.32*</td>
<td>0.08</td>
<td>0.27</td>
<td>0.41**</td>
</tr>
<tr>
<td>Profit Period</td>
<td>(0.12)</td>
<td>(0.07)</td>
<td>(0.68)</td>
<td>(0.012)</td>
<td>(0.02)</td>
</tr>
<tr>
<td>Max. Period</td>
<td>0.20</td>
<td>0.28</td>
<td>0.11</td>
<td>0.23</td>
<td>0.39**</td>
</tr>
<tr>
<td>Profit (Points)</td>
<td>(0.26)</td>
<td>(0.12)</td>
<td>(0.54)</td>
<td>(0.19)</td>
<td>(0.03)</td>
</tr>
<tr>
<td>Observations</td>
<td>26</td>
<td>26</td>
<td>26</td>
<td>26</td>
<td>26</td>
</tr>
</tbody>
</table>

Pairwise correlation coefficients between experimental measures and external survey measures (pooled ratings from supervisors and the HR department). P-values in parentheses. Significance levels: * $p<0.1$, ** $p<0.05$, *** $p<0.01$. 31
Appendix C: Parameters used in the Ice Cream Stand Task

Table C.1: Optimal product mix and maximal achievable profit by location

<table>
<thead>
<tr>
<th></th>
<th>Business District</th>
<th>School</th>
<th>Stadium</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sugar Content</td>
<td>1.5%</td>
<td>9.5%</td>
<td>5.5%</td>
</tr>
<tr>
<td>Flavor Intensity</td>
<td>7.5%</td>
<td>1.5%</td>
<td>5.5%</td>
</tr>
<tr>
<td>Color</td>
<td>light</td>
<td>bright</td>
<td>light</td>
</tr>
<tr>
<td>Price</td>
<td>7.5</td>
<td>2.5</td>
<td>7.5</td>
</tr>
<tr>
<td>Maximum Profit</td>
<td>100</td>
<td>200</td>
<td>60</td>
</tr>
</tbody>
</table>

Table C.2: Penalty factors for deviation from the optimal product mix

<table>
<thead>
<tr>
<th></th>
<th>Business District</th>
<th>School</th>
<th>Stadium</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sugar Content</td>
<td>5</td>
<td>6</td>
<td>0.5</td>
</tr>
<tr>
<td>Flavor Intensity</td>
<td>5</td>
<td>6</td>
<td>0.5</td>
</tr>
<tr>
<td>Color</td>
<td>20</td>
<td>60</td>
<td>0.5</td>
</tr>
<tr>
<td>Price</td>
<td>5</td>
<td>6</td>
<td>0.5</td>
</tr>
</tbody>
</table>

Table C.3: The effect of flavor on profit

<table>
<thead>
<tr>
<th>Flavor</th>
<th>Factor</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lemon</td>
<td>3.15</td>
</tr>
<tr>
<td>Joghurt</td>
<td>2.6</td>
</tr>
<tr>
<td>Nut</td>
<td>1.9</td>
</tr>
<tr>
<td>Banana</td>
<td>1.45</td>
</tr>
<tr>
<td>Walnut</td>
<td>1.4</td>
</tr>
<tr>
<td>Cherry</td>
<td>1.2</td>
</tr>
<tr>
<td>Orange</td>
<td>1.15</td>
</tr>
<tr>
<td>Woodruff</td>
<td>1.08</td>
</tr>
<tr>
<td>Raspberry</td>
<td>1.0</td>
</tr>
<tr>
<td>56 other flavors</td>
<td>0.9-1.0</td>
</tr>
</tbody>
</table>
Appendix D: Questionnaires

Judgmental Overconfidence Questionnaire

Miscalibration Questions (True Answers in parantheses)
1. Martin Luther King’s age at death (39).
2. Length (in kilometers) of the Nile River (6671).
3. Number of countries that are members of OPEC (12).
4. Number of books in the Old Testament (5).
5. Weight (in kgs) of an empty Boeing 747 (180890).
6. Year in which J.S. Bach was born (1685).
7. Gestation period (in days) of an Asian elephant (645).
8. Diameter (in kilometers) of the moon (3475).
9. Air distance (in kilometers) from London to Tokyo (9550).
10. Deepest known point (in meters) in the oceans (11034).

External Questionnaires Given to the Supervisors and the HR

Taking Charge Questionnaire (5-point Likert Scale)
This person often...
1. tries to adopt improved procedures for doing his or her job.
2. tries to change how his or her job is executed in order to be more effective.
3. tries to bring about improved procedures for the work unit or department.
4. tries to institute new work methods that are more effective for the company.
5. tries to change organizational rules or policies that are nonproductive or counterproductive.
6. makes constructive suggestions for improving how things operate within the organization.
7. tries to correct a faulty procedure or practice.
8. tries to eliminate redundant or unnecessary procedures.
9. tries to implement solutions to pressing organizational problems.
10. tries to introduce new structures, technologies, or approaches to improve efficiency.

Performance Questionnaire (7-point Likert Scale)
1. He/she has usually exceeded the required performance.
2. Compared to colleagues with similar job profile and tenure, he/she excels in task achievement.

24 This questionnaire is adopted from Biais et al. (2005).
25 This questionnaire is taken from Morrison and Phelps (1999).
3. Concerning his field of activity, he/she possesses extraordinary skills.
4. He/she possesses an extraordinary work and achievement motivation.

**Action Orientation Questionnaire** (7-point Likert Scale) \(^{26}\)
1. The employee’s time management does not enable him/her to complete his/her tasks on time.
2. The employee does not hesitate to implement decisions.
3. The thorough analysis of a task paralyses his/her actions.
4. Even if he/she is working on an urgent task, he/she tends to interrupt it to do something else in between.
5. If multitasking is necessary, he/she has difficulties organizing everything effectively.
6. If he/she has to complete an unpleasing task, he/she likes to procrastinate.
7. Whatever he/she puts on a day’s schedule is finished in the evening.
8. If he/she has to complete too many tasks at once, he/she has problems deciding which one to start with.
9. It is easy for him/her, to adhere to his/her priorities at work.

**Creativity Questionnaire** (7-point Likert Scale)
1. The employee has the ability to quickly find usable solutions for novel problems.
2. The employee has extraordinary ideas that help advancing the project.
3. The employee has the ability to create something completely new out of existing things.
4. The employee looks for solutions outside of ordinary patterns.

**Gestalt Motivation Questionnaire** (7-point Likert Scale) \(^{27}\)
1. If I delegate a task to him/her, he/she does anything to fully implement it.
2. If he/she has set a goal, he/she consequently strives for it.
3. If he/she undertakes something, he/she will only be satisfied if he/she accomplishes it.
4. If things go wrong, he/she increases his/her effort even more.
5. He/she is inclined to work hard and persistently.
6. He/she approaches problems in an active way.
7. If something goes wrong, he/she immediately looks for solutions.
8. If possibilities arise to shape something, he/she exploits them.
9. He/she immediately takes the initiative, if no one else does it.
10. He/she quickly avails him/herself of opportunities to achieve his/her goals.
11. He/she usually does more than required from him/her.
12. He/she is particularly good in implementing ideas.

\(^{26}\)This questionnaire is adopted from Hossiep and Paschen (2003)
\(^{27}\)This questionnaire is adopted from Hossiep and Paschen (2003).
Appendix E: Instructions

Instructions for the Ice Cream Task

You are now taking part in a scientific study. A research foundation has provided funds for this research. Please read the following instructions carefully. Everything that you need to know in order to participate in this experiment is explained below. Should you have any difficulties in understanding these instructions please notify us. We will answer your questions at your cubicle.

During the course of the experiment you can earn Taler. The amount that you earn during the experiment depends on your decisions. All the gains that you make during the course of the experiment will be exchanged into cash at the end of the experiment.

The exchange rate will be: 75 Taler = 1 CHF

At the end of the experiment, you will receive your earned amount in cash.

Please note that communication between participants is strictly prohibited during the experiment. In addition we would like to point out that you may only use the computer functions which are required for the experiment. In case you have any questions, dont hesitate to ask us. An instructor will answer your questions at your cubicle.

Detailed procedures for the first part of the experiment

In this part of the experiment, you will take on the role of an individual running an ice cream stand. There will be 20 periods in which you will have to make decisions on how to run the business in order to maximize profit. These decisions will involve the location of the stand, the flavour of the ice cream, the sugar content and flavour intensity, and the ice cream color and price. You can freely choose all these variables. Your goal is to chose them such that you achieve maximal profit. At the end of each period, you will learn what profits you made during that period. You will also hear some customer reactions that may help you with your choices in the following periods. The decisions you make in one period, will be the default choices for the next period.
Previous Manager Guidelines

Dear X,

I have enclosed the following guidelines that you may find helpful in running your ice cream stand. These guidelines are based on my previous experience running this stand. When running my business, I followed these basic guidelines:

- Location: Business District
- Sugar Content: 3%
- Flavour Intensity: 7%
- Ice Color: light
- Price: 8.2 Taler
- Flavour: Orange

With these choices, I was able to make an average profit of about 90 Taler per period. I have experimented with alternative choices of sugar and flavour intensity, as well as ice cream color and price. The above choices were the ones I found to be the best. I have not experimented with alternative choices of location though. They may require very different strategies. There is another ice cream stand in town which is famous for his chocolate-, vanilla-, straciatella- and strawberry icecream. It makes no sense to sell these flavours. Otherwise it is known that the demand for ice cream flavours is typical for the German speaking area. I also know that the flavour has no impact on the optimal price, color, flavour intensity or sugar content.

Regards,

Previous Manager

Payment

Your compensation will be based on the profits you make with your lemonade stand. You will get paid your own ice cream stand profits in the last 10 periods of the experiment. The profit achieved in periods 1-10 is not relevant for your own payment.

Example:
If your income in periods 11-20 was 3000 Taler, you will receive 40 CHF at the end of the study in cash.
Instructions for the Elicitation of Ambiguity Aversion

We measured subjects’ ambiguity aversion in an experiment that took place after the ice cream task. Subjects were given the following instructions:

You now have the possibility to participate in a series of lotteries. Potential earnings will be added to your overall income, potential losses will be subtracted from your overall income. At the end, one lottery will be randomly chosen. Your income will depend on your decisions in the chosen lottery and the outcome of the lottery.

In the following, there are two urns and each urn contains 20 balls, which are either red or blue. You have to decide from which urn you want to draw a ball.

If the ball is red, you receive 8 CHF. If the ball is blue, you receive 0 CHF.

- Urn 1 contains 20 balls which can randomly be either red or blue.
- Urn 2 contains red and blue balls in known quantities.

Please choose for each of the following lotteries whether you want to draw a ball from urn 1 or urn 2:

1. Lottery: Draw from urn 2 which contains 16 red and 4 blue balls, or draw from urn 1 which contains 20 balls that are either red or blue.

2. Lottery: Draw from urn 2 which contains 14 red and 6 blue balls, or draw from urn 1 which contains 20 balls that are either red or blue.

3. Lottery: Draw from urn 2 which contains 12 red and 8 blue balls, or draw from urn 1 which contains 20 balls that are either red or blue.

4. Lottery: Draw from urn 2 which contains 10 red and 10 blue balls, or draw from urn 1 which contains 20 balls that are either red or blue.

5. Lottery: Draw from urn 2 which contains 8 red and 12 blue balls, or draw from urn 1 which contains 20 balls that are either red or blue.

6. Lottery: Draw from urn 2 which contains 6 red and 14 blue balls, or draw from urn 1 which contains 20 balls that are either red or blue.

7. Lottery: Draw from urn 2 which contains 4 red and 16 blue balls, or draw from urn 1 which contains 20 balls that are either red or blue.