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A nonparametric analysis of regional unemployment dynamics in Britain

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# A Nonparametric Analysis of Regional Unemployment Dynamics in Britain

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Abstract. This paper estimates the probability distribution of relative county unemployment in Britain for the years 1981-1995. We find that the distribution is unimodal in all years, with a falling variance between 1989 and 1994. We use bootstrap methods to determine critical values for the two tails of the distribution, and analyse intra-distribution dynamics. An unemployment transition is defined as a move between a tail and the centre of the distribution (and *vice versa*). We calculate transition probabilities and find that the probability of leaving any given state is very low. We also find that high (low) unemployment regions have a higher probability of entering a state of lower (higher) unemployment than a state of higher (lower) unemployment.

Keywords: Regional unemployment, panel data, asymmetric effects in the persistence of transition dynamics, nonparametric analysis.

JEL Classification: E24, R12, C14.

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# 1 Introduction

In this paper we use nonparametric methods to describe the county-level dynamics of unemployment in Britain. We want to analyse first the distribution of relative unemployment to know whether it is multimodal. The high-unemployment areas of Scotland, Wales and northern England are often contrasted with the lower unemployment areas in the south; counties in those regions might form a group separate from the rest. Secondly, we would like to know whether the variance of unemployment across counties has changed during recent years. A falling variance could either imply that high-unemployment counties are recovering due to migration and capital movements, or that the geographical distribution of shocks has changed over time ( $\sigma$ -convergence, see Barro and Sala-i-Martin, 1995). Finally, we are interested in assessing the relative fortunes of different counties by identifying those enjoying persistent prosperity and those suffering persistent unemployment. We want to know, for example, whether it is more difficult to recover from a (relative) depression than it is to fall from (relative) prosperity. ( $\beta$ -convergence).

There exists a substantial literature studying regional unemployment persistence for different countries. Blanchard and Katz (1992) studied the US, Jimeno and Bentolila (1995) Spain, and Decressin and Fatás (1995) European regions. The results suggest that migration plays a key role in the US so that regional labour demand shocks have only a small transitory effect on regional unemployment. In Europe, however, it is through changes in labour force participation<sup>2</sup> that employment is affected in the short run, and through migration in the long run. There is no long-run effect on unemployment in either case. Spain is an exception, according to Jimeno and Bentolila; unemployment responds more to labour demand shocks, and its changes last longer.

In Bianchi and Zoega (1996), we use similar conventional methodology to look at regional unemployment data for Britain in order to measure the persistence of relative unemployment rates in the ten regions, and the response to changes in regional labour demand. We measure steady-state unemployment rates for each of the regions, and the speed of adjustment towards these steady-states following regional shocks. Regional unemployment appears either to be nonstationary or if there is any convergence over time, it is extremely slow. The point estimates imply that if unemployment in any one region is 5% higher than its steady-state value (that is 500 basis points higher), the unemployment rate will fall by only 65 basis points in the first year (0.65%) and that it would take more than 12 years for unemployment to return to steady state. If the rate started out 10% higher than the steady state value, it would take more than 17 years to return to the steady-state value. Thus, British regional labour markets appear to be much less integrated than labour markets in continental Europe and in the US. In the latter, migration eliminates unemployment differentials within 4-6 years.

 $<sup>^{1}</sup>$ Counties may possibly get trapped at very high levels of unemployment if some of the adjustment mechanisms – migration and capital movements – break down.

<sup>&</sup>lt;sup>2</sup>This includes early retirement and disability pension.

These results lend support to earlier studies of regional labour markets in Britain (see Blackaby and Manning, 1981; Hughes and McCormick, 1987, 1994; Evans and McCormick, 1994; Pissarides and McMaster, 1989; Pissarides and Wadsworth, 1990; Jackman and Savouri, 1992; and Pencavel, 1994). Pissarides and McMaster, using interregional migration data, find that migration responds very slowly to differences in regional unemployment. Their results imply that it can take more than twenty years for an unemployment differential in a depressed region to disappear. Evans and McCormick find an integrated labour market for non-manuals, where migration equalizes regional unemployment rates, but they find the market for manuals to be localized with persistent unemployment differentials across regions, and hardly any interregional migration in response to unemployment differences.

The objective of this paper is to look more closely at regional labour market dynamics in Britain using non-parametric methods. In doing so we attempt to provide an alternative methodology for analysing regional developments. We use kernel density estimation to estimate the probability distribution of relative unemployment rates across 64 counties for the years 1981-1995. This enables us to test for the existence of modes in the distribution and to observe changes in the variance of relative unemployment during this period. Also, we look at movements of counties within the distribution between years and calculate transition probabilities of leaving states of different relative unemployment.

The organization of this paper is as follows. Section 2 describes the statistical framework (our definitions of shocks and persistence, nonparametric density estimation, construction of bootstrap confidence intervals and classification analysis, the analysis of intra-distribution dynamics, etc). Section 3 has the empirical results. Section 4 concludes.

# 2 The Statistical Framework

#### 2.1 Intra-distribution Dynamics

We have longitudinal data on unemployment rates<sup>3</sup> for n = 64 counties from 1981 to 1995. We are interested in establishing empirical facts about shocks to their unemployment ratios as well as the persistence of these shocks. To this end we construct a formal statistical definition of shocks based on classification analysis and the concept of intra-distribution dynamics.

We denote by  $x_i$  the ratio of unemployment in county i to the aggregate British unemployment rate, and by f(x) its probability distribution at time t. In Figure 1 it is assumed that we know the probability distribution of the data and we fix a value of  $\alpha$  to define the area in each tail of the distribution. This allows us to identify two critical values,  $c_1$  and

<sup>&</sup>lt;sup>3</sup>These are annual averages. The rates are calculated by expressing the number of unemployed claimants as a percentage of the estimated total workforce (the sum of of unemployed claimants, employees in employment, self-employed, HM forces and participants on work-related training programmes). Source: *Employment Gazzette*, various issues.

 $c_2$ , on the real line such that

is

$$\int_{-\infty}^{c_1} f(x) dx = \int_{c_2}^{+\infty} f(x) dx = \alpha.$$

Then, we define county i to be in the state of:

We construct an indicator variable for county i at time t,  $I_i(t)$ , which takes the values 0,1 and 2 (respectively, the states of low, average and high unemployment), i.e.:

$$I_i(t) = \begin{cases} 0 & \text{if } x_i \in S_0, \\ 1 & \text{if } x_i \in S_1, \\ 2 & \text{if } x_i \in S_2. \end{cases}$$
 (1)

By doing the above classification analysis for each county (i = 1, ..., n) and every year (t = 1981, ..., 1995), we are able to focus on intra-distribution dynamics. We now have the following definition:

**Definition:** a county i is hit by a positive shock at time t if  $I_i(t+1) < I_i(t)$ ; it is affected by a negative shock if  $I_i(t+1) > I_i(t)$ .

# 2.2 Nonparametric Density Estimation and Classification Analysis

Given the data and a positive value  $\alpha \leq 1/3$ , inference on intra-distribution dynamics requires us to know the true probability f(x). As a matter of fact, the true probability is never known, but we can replace f(x) by a non-parametric estimate

$$\hat{f}_h(x) = (nh)^{-1} \sum_{i=1}^n K\left(\frac{x - x_i}{h}\right) = (nh)^{-1} \sum_{i=1}^n K(u), \tag{2}$$

where h > 0 is the bandwidth (governing the degree of smoothness of the estimate, with larger values of h producing a smoother density estimate) and  $K(u) = 1/\sqrt{2\pi} \cdot \exp(-1/2u^2)$  being the Gaussian kernel (see Silverman, 1986; Härdle, 1990).

In this way, we obtain  $estimates\ \hat{c}_1$  and  $\hat{c}_2$  of the critical values whereas our classification analysis depends on the "true" critical values  $c_1$  and  $c_2$ . We therefore construct confidence intervals for  $c_1$  and  $c_2$ , i.e.

$$\Pr(\underline{c}_1 \le c_1 \le \overline{c}_1) = \Pr(\underline{c}_2 \le c_2 \le \overline{c}_2) = c \tag{3}$$

where c is the coverage probability (for example c = 0.80).

The situation is summarised in Figure 2, which shows two regions of indeterminancy; if  $x_i$  is in the interval  $[\underline{c}_1, \overline{c}_1]$  or  $[\underline{c}_2, \overline{c}_2]$ , it is unknown whether county i should be allocated to state  $S_0$  or  $S_1$ . Counties with unemployment ratios smaller than  $\underline{c}_1$ , however, are allocated to the state of low unemployment with probability c, and counties with unemployment ratios bigger than  $\overline{c}_2$  are allocated to the state of high unemployment. In other words, with probability c, a county i with  $\overline{c}_1 < x_i < \underline{c}_2$  at time t but  $x_i > \overline{c}_2$  at time t+1, can be defined to have been affected by a negative shock at time t. However, for a county s in the same situation at time t (that is with  $\overline{c}_1 < x_s < \underline{c}_2$ ) and with  $x_s > \underline{c}_2$  but  $x_s < \overline{c}_2$  at time t+1, the switch from  $S_1$  to  $S_2$  could be generated by noise rather than by a genuine negative shock.

Given the above considerations, we define the five areas in the distribution according to

$$I_{i}(t) = \begin{cases} 0 & \text{if} \quad x_{i} \in S_{0} \\ 5 & \text{if} \quad x_{i} \in (\underline{c}_{1}, \overline{c}_{1}] \\ 1 & \text{if} \quad x_{i} \in S_{1} \\ 5 & \text{if} \quad x_{i} \in (\underline{c}_{2}, \overline{c}_{2}] \\ 2 & \text{if} \quad x_{i} \in S_{2}, \end{cases}$$

$$(4)$$

where 5 represents the code of the indicator in the regions of indeterminancy (regardless of whether we are in between  $S_0$  and  $S_1$ , or  $S_1$  and  $S_2$ ).

As the density of the data is estimated nonparametrically, we use the bootstrap approach to construct the confidence intervals. This means that given an optimal bandwidth h,<sup>5</sup> calculated using the plug-in method of Sheather and Jones (1991), we resample with replacement from the original data. Due to an effect of the Gaussian kernel, bootstrap samples drawn from  $f_h$  have a variance larger than the sample variance of the data, so the following transformation is required (see Efron and Tibshirani, 1993, page 231 and 234 for details)

$$x_i^* = \bar{y}^* + (1 + h^2 \hat{\sigma}^2)^{-1/2} (y_i^* - \bar{y}^* + he_i), \quad i = 1, \dots, n,$$
 (5)

where  $\mathbf{y}^* = (y_1^*, \dots, y_n^*)'$  are sampled with replacement from  $\mathbf{x} = (x_1, \dots, x_n)'$ ;  $\bar{y}^* = \text{mean}(\mathbf{y}^*)$ ,  $\hat{\sigma}^2$  is the sample variance of  $\mathbf{x}$ ; and  $e_i$  are standard normal variables generated by the computer.<sup>6</sup>

The construction of the confidence intervals and the implementation of the classification analysis can be summarised as follows:

<sup>&</sup>lt;sup>4</sup>A more complete treatment of the problem would require a joint, rather than pointwise, confidence interval for the quantiles across time.

<sup>&</sup>lt;sup>5</sup>By optimal we mean here the minimisation of the trade-off between the bias and the variance of the estimator in a AMISE (asymptotic mean integrated squared error) sense. See for example Marron, Jones and Sheather (1992), Sheather and Jones (1991), Bianchi (1995a).

<sup>&</sup>lt;sup>6</sup>It can be shown (see Efron and Tibshirani, 1993, page 234) that if  $\mathbf{y}^*$  is sampled with replacement from  $\mathbf{x}$ ,  $\mathbf{e} = (e_1, \dots, e_n)'$  has a standard normal distribution and h is fixed, then: i)  $\mathbf{r}^* \equiv \mathbf{y}^* + h\mathbf{e}$  is distributed according to  $\hat{f}_h$ ; ii)  $\mathbf{r}^*$  has the same mean as  $\mathbf{y}^*$  and variance  $\hat{\sigma}^2 + h^2$ ; iii)  $\mathbf{x}^* = (x_1^*, \dots, x_n^*)'$  defined as in equation (5) has the same mean as  $\mathbf{r}^*$  but variance approximately equal to  $\hat{\sigma}^2$ .

- 0. select bandwidth h from the sample data using a data-driven bandwidth selector (for example, Sheather and Jones, 1991);
- 1. draw B bootstrap samples  $\mathbf{y}^*$  of size n from  $\mathbf{x}$  by sampling with replacement;
- 2. define the rescaled bootstrap samples  $\mathbf{x}^*$  as in (5);
- 3. for each boostrap sample  $\mathbf{x}^*$ , estimate the density  $\hat{f}_h(\mathbf{x}^*)$  and, given  $\alpha$ , obtain the critical value pairs  $\{\hat{c}_1^*(b), \hat{c}_2^*(b)\}_{b=1}^B$ ;
- 4. derive the confidence limits  $\underline{c}_k$ ,  $\overline{c}_k$  by taking the  $\{(B-Bc)\}$ -th and the  $\{Bc\}$ -th largest of the B replicates  $\hat{c}_k^*$ , k=1,2;
- 5. construct the indicator  $\hat{I}_i(t)$  as in (4), for i = 1, ..., n and t = 2, ..., T (this gives an  $n \times (T-1)$  design matrix with elements 0, 1, 2 or 5);
- 6. at t = 1, fix  $\hat{c}_k = \text{median}\{\hat{c}_k^*(b)\}_{b=1}^B$ , for k = 1, 2, and classify the *i*-th county in  $S_0$  if  $x_i \leq \hat{c}_1$ ,  $S_2$  if  $x_i > \hat{c}_2$  or  $S_1$  otherwise;
- 7. for t = 2, ..., T, allocate counties falling in the indeterminancy regions to the same state they were at t 1; this gives an  $n \times T$  design matrix,  $\mathbf{D}$ , with elements 0, 1, or 2.

The design matrix **D** summarises most information on intra-distribution dynamics which is relevant for making inference about transition probabilities (these describe the probability of a county leaving one state of relative unemployment for another). For these, we analyse the *columns* of the matrix; at each point in time, from t = 2, ..., T, we count the proportion of counties that moved from  $S_l$  to  $S_m$ , for l, m = 1, 2, 3, between t - 1 and t. This will allow us to address the issue of  $\beta$ -convergence: this implies that counties with high (low) relative unemployment should have higher transition probabilities to states of lower (higher) relative unemployment than counties with higher (lower) unemployment rates.

To address the issue of  $\sigma$ -convergence, nonparametric density estimation can be used first to test for the number of modes in the true probability distribution f(x). It is of interest whether the counties can be grouped into high- and low-unemployment areas in that way. Thus it is possible that certain regions of the country have high mean unemployment while others have a much lower mean rate. A formal test for unimodality can easily be implemented by the bootstrap method, as discussed in Silverman (1981, 1983, 1986) and Efron and Tibshirani (1993). Having detected the number of modes, we then measure changes in the variance across the counties over time. If the variance is falling over time, we have a case of  $\sigma$ -convergence. This might either suggest the operation of adjustment mechanisms, such as inter-county labour migration, or changes in the geographical distribution of shocks.

Finally, we can also record the *dating* of the different shocks and, by looking at the kernel density estimates for these dates, check whether positive and negative shocks occurred at different times.

 $<sup>^7\</sup>mathrm{A}$  summary of the procedure is reported in the Appendix. See Bianchi (1997) for an application to per-capita GNP series.

#### 2.3 Generalization and Model Selection

Before turning to the empirical analysis of unemployment data, we briefly discuss the advantages of our statistical methodology. We also generalize the model to an arbitrary number of states and discuss the choice of our model's parameters.

The advantage of non-parametric methods in the context of our analysis is clearly flexibility, in so far that virtually any shape of the density can be accounted for by the method. Regardless of whether the empirical distribution is well approximated by a Gaussian distribution or has fat tails, skewness and/or kurtosis, non-parametric density estimation will automatically estimate the different shapes. Using parametric methods, on the other hand, one would have to try a variety of parametric families and choose the family which best fits the data in each year. Moreover, it is very unlikely that the way nonparametrics are implemented may influence the results; it is well known that the choice of the kernel function is not of great significance and that the choice of the bandwidth need not be subjective because data driven methods with optimal statistical properties are readily available — such as for example the plug-in method of Sheater and Jones (1991).

However, the choice of the number of unemployment states and the areas in the tails of the distribution deserves a more detailed explanation. The analysis presented in previous sections is based, in fact, on a threefold classification of unemployment (high, low, average) with  $\alpha = 0.30$ . This is only for expositional purposes, as the underlying model can be generalized to include a higher number of states with different probability areas in each state. The generalization requires us to carefully consider two extreme situations depicted in Figure 3. The first situation is that of a county moving from a state of low (high) to a state of average unemployment in a given time period — a movement from 'a' to 'b' in Figure 3 — to revert back to the low (high) unemployment state next period — movement from 'b' to 'c'. In both cases, we have very small movements in the neighbourhood of the cut point  $c_1$  ( $c_2$ ) which, intuition suggests, should not be recorded as genuine state transitions. Such spurious transitions will not be detected in our framework thanks to the construction of the indeterminancy regions obtained from bootstrap confidence intervals. However, when a county jumps, within the state of average unemployment from a level close to  $c_1$  to a level close to  $c_2$ , this may be a cause for concern. The movement from 'd' to 'e' in Figure 3, in fact, should be detected as a truly genuine transition in our analysis of intradistribution dynamics but it may not be detected in practice. In the context of a three-state model, the risk of failing to detect a large movement of this kind is higher the lower the value of  $\alpha$ . For this reason, the largest possible value of  $\alpha$  minimising the distance between the two cut points  $c_1$  and  $c_2$ ,  $\alpha = 1/3$ , should be selected to minimise this risk. A better alternative may be to allow for a higher number of unemployment states, such as for example five (lower, low, average, high, higher) instead of three.

To summarise, we can represent our general statistical model by the parameters' set

<sup>&</sup>lt;sup>8</sup>The method of Sheater and Jones is statistically optimal in the sense of minimising the mean square error of the estimator. Marron et al (1992) report the results of an extensive simulation study showing the excellent performance of the SJ bandwidth selector in small samples.

<sup>&</sup>lt;sup>9</sup>We thank Danny Quah for raising this point.

 $M = \{h, S, \alpha_1, \dots, \alpha_S, c\}$ , where h is the bandwidth for the non-parametric density estimate of (relative) unemployment rates; S is the number of unemployment states;  $\alpha_s$  is the probability area for the s-th state, with  $\sum_{s=1}^{S} \alpha_s = 1$ ; and c is the coverage probability for the confidence intervals. It is clear from the discussion above that there is a natural choice for most of our parameters, which is as follows:  $h = h_{\rm SJ}$ , where  $h_{\rm SJ}$  is the bandwidth selected by the method of Sheater and Jones (1991); and  $\alpha_1 = \alpha_2 = \alpha_3 = 1/3$  or  $\alpha_1 = \alpha_2 = \alpha_3 = \alpha_4 = \alpha_5 = 1/5$ . The choice of the coverage probability c for the construction of confidence intervals remains more subjective, as any number between 0.80 and 0.95 could be selected. Nevertheless, the closer the value of c is to unity, the wider the confidence interval for the cut points. A value of c equal to 0.95 or 0.90 may lead therefore to an overlap of the indeterminancy regions. In our application, we have selected a value of c = 0.80 to avoid this.

# 3 Empirical Results

Following the statistical methodology described in Section 2, we take a look at the levels of unemployment in 64 counties from 1981-1995. The data are shown in Figure 4 (top-panels); the county unemployment rates in the left-hand side panel, the aggregate unemployment rate in the right-hand side panel. Because we are interested in looking at the unemployment problem in different counties relative to the national aggregate, the counties unemployment rates are divided by the UK aggregate; this leads to the series plotted in the bottom-left panel of Figure 4.<sup>10</sup>

The bottom-right panel shows the boxplot representation of these series, which presents the distribution of the data in different years. A drop in the median of the distributions (represented by the horizontal line in the box) can be noticed after 1982 to a value closer to unity; also there is a significant reduction in the dispersion of the distributions (represented by the size of the box) over the last 4-5 years. For most years, the densities appear somewhat skewed towards large values, but with very few outliers.

For the unemployment ratios, the bandwidths selected by the method of Sheather and Jones (see Table in the Appendix) give the density estimates shown in Figure 5. The probability distribution is unimodal in all years. There is a clearly visible fall in the mean (relative) unemployment in the early 1980s, and also in the variance of the distribution in the early 1990s. The latter is presumably caused by the uncharacteristically deep recession in the South. The fall in the variance around 1990 and the increase in the first half of 1990's is a reflection of the regional distribution of shocks. Both the recovery in the late 1980's and the recession in the 1990's were concentrated in the South.

<sup>&</sup>lt;sup>10</sup>We could have used here absolute unemployment rates rather than relative unemployment rates and this would not change the results of our analysis. In fact, densities of absolute and relative unemployment rates are identical, apart from a scaling factor. In any given year the absolute unemployment rate can be derived from the relative rate by multiplying every observations by the average British unemployment rate. But this would just shift the mode of our density.

<sup>&</sup>lt;sup>11</sup>Formal multimodality tests using nonparametric kernel density estimation and the bootstrap reject multimodality in all years — see the results reported in the Appendix.

The densities, together with a fixed value for the area in the tails of the distribution,  $\alpha=1/S$  with S=3, give the intra-distribution dynamics in Table 1. Figure 6 plots the intra-distribution dynamics for 10 counties, <sup>12</sup> one from each of the 10 regions. The first panel shows the intra-distribution dynamics for Greater London. London starts out in the area of low unemployment but in 1983 enters the zone of indeterminancy between "low" and "normal" unemployment. In 1988 it enters the area of normal unemployment and finally in 1993 the area of high unemployment.

positive shocks

Figure 7 shows the density estimate of the *dates* of the shocks. It appears that positive shocks occurred more frequently in the period between 1985 and 1993 (and, within this period, more frequently in 1989), whereas most negative shocks (which particularly affected South-East counties) occurred in 1981 and 1991.

It is also interesting to examine whether it is more likely or less likely for a given county finding itself in the left-tail of the distribution to move to the centre than for a similar county in the high-unemployment right-tail of the distribution. The matrix in Table 3 has the transition probabilities between the three states, which is calculated as the average probability over the 14 years. The first row refers to  $S_0$ , the second row to  $S_1$ , and the third to  $S_2$ . The first number in row 1 shows the probability that a county in region  $S_0$  in year t-1 will remain in that same state in year t. The second number is the probability of moving from state  $S_0$  to  $S_1$  and the last number is the probability of moving to state  $S_2$ .

We see that changes in the relative county unemployment rates are very persistent. The probability that a county stays in the current state between any two years is 92.5% for  $S_0$ , 95.8% for  $S_1$  and 97.2% for state  $S_2$ . The probability of getting out of a bad state,  $S_2$ , is only 3.3% and about the same as the probability of getting out of the good one, 3.2%.

Table 4 has the analogous transition probabilities for the case of five states with S=5 and  $\alpha=0.2$ . Again we find that relative unemployment is very persistent. However, we also find that a county with a high (low) level of relative unemployment has a higher probability of moving to a state of lower (higher) unemployment. This implies  $\beta$ -convergence. For example, a county finding itself in the second highest unemployment state has a probability of 2.68% of moving to the highest state and a probability of 4.68% of moving to one of the three states with lower unemployment. Similarly, a county in the second lowest state of unemployment has a probability of 5.41% of moving to the state of lower unemployment and a probability of 7.11% of moving to a state of higher unemployment.

We conclude that the key results of our analysis of intra-distribution dynamics — the persistence of relative unemployment — is not sensitive to our choice of the number of states. However, using five states allows us to take a closer look at the dynamics. <sup>13</sup>

because

 $<sup>^{12}</sup>$ We would like to point out that the seven metropolitan districts are strictly speaking not counties in the sense that each has more than one local government.

 $<sup>^{13}</sup>$ We also derived the transition probabilities using coverage probabilities (c) of 0.85 and 0.90, with very similar results.

# 4 Conclusions

This paper has used nonparametric methods to analyse unemployment persistence. We used data on unemployment at the county level in Britain from 1981-1995 to test for the number of modes in the probability distribution across the counties. We found the distribution to be unimodal in every year. While in any given year there are counties with very high and very low unemployment rates, we do not detect significant subgroups in the data with either high or low rates.

By constructing confidence intervals for quantiles (critical values) in the density which leave 33% of observations in each tail of the distribution, we analysed the persistence of movements of counties between the three states of unemployment (low, average, high), corresponding to the middle and the two tails of the distribution. We found that the transition probabilities were the same for the two tails. We also found that positive shocks mainly occurred in the period 1985-1993, whereas negative shocks, which mostly affected counties in the South-East, occurred in 1981 and, particularly, in 1991.

The transition probabilities confirmed a high degree of persistence of changes in relative unemployment. Thus the probability that a county finding itself in a state of high unemployment will stay in that state in the following year is around 97%. This implies that the regional adjustment mechanisms of inter-county migration and capital movements are very weak. When using five states of unemployment instead of three, we again found unemployment persistence, but also a tendency for high unemployment regions to recover and low unemployment regions to experience rising unemployment. This presents evidence in favour of weak  $\beta$ -convergence.

# Figures and Tables

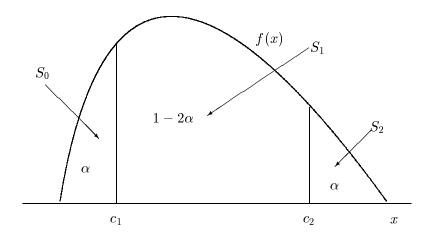


Figure 1: Classification analysis.

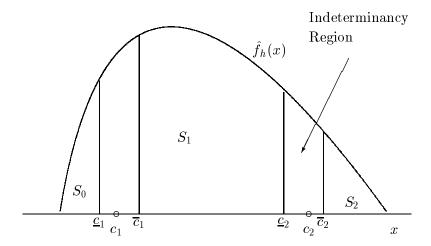


Figure 2: Classification analysis with indeterminancy regions.

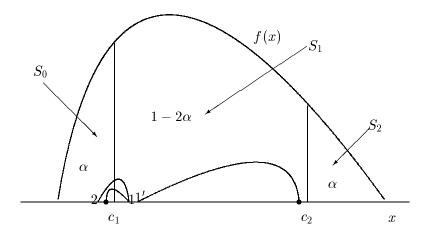


Figure 3: Example of two extreme cases in our classification analysis.

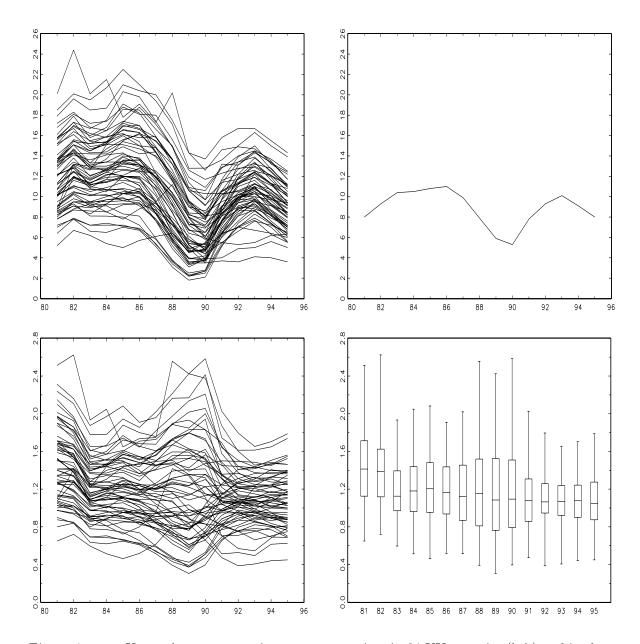


Figure 4: Top: Unemployment rates in percentage points in 64 UK counties (left) and in the UK (right), from 1981 to 1995. Bottom: unemployment ratios (left) with the corresponding boxplots (right).

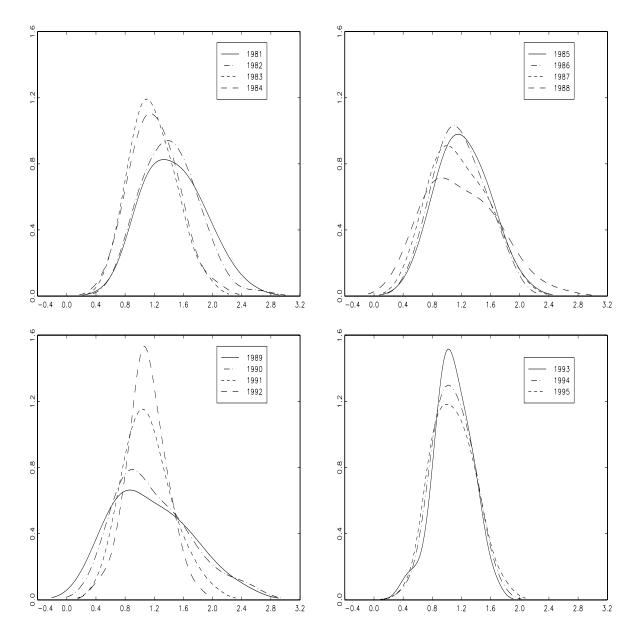


Figure 5: Kernel density estimates for the unemployment ratios of 64 counties in different years using the bandwidths reported in the Appendix.

County	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95
1	1	5	5	5	5	5	5	0	0	5	1	1	1	1	1
2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0	0	0	0	5	0	0	0
4	1	1	1	1	1	1	5	5	5	1	5	2	2	2	2
5 6	$\frac{1}{0}$	$\begin{array}{c} 1 \\ 0 \end{array}$	1 5	1 5	1 5	1 5	1 5	5 1	5 1	1 1	1 1	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{5}{2}$
7	0	5	0	5	5	0	5	0	0	0	5	1	1	5	5
8	0	0	0	0	0	0	0	0	0	0	0	1	5	5	0
9	0	1	1	1	1	1	1	1	1	1	5	2	2	2	2
10	1	1	1	1	1	1	1	5	5	5	1	5	5	5	5
11	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
13	0	5	5	5	0	0	0	0	0	0	5	5	5	0	0
$\frac{14}{15}$	$\frac{1}{0}$	$\frac{1}{0}$	1 0	$\frac{1}{0}$	$\frac{1}{0}$	$\frac{1}{0}$	$\frac{1}{0}$	$\frac{1}{0}$	$\frac{5}{0}$	$\frac{1}{0}$	$\frac{1}{0}$	$\frac{1}{0}$	1 5	1 5	1 5
16	1	5	5	5	1	5	5	1	1	1	1	1	1	1	1
17	2	5	5	5	5	$\overset{\circ}{2}$	$\overset{\circ}{2}$	5	5	5	2	2	2	2	2
18	1	1	1	1	1	1	1	1	1	1	1	5	5	5	5
19	1	5	5	5	5	5	5	5	0	5	1	5	5	1	1
20	0	0	5	5	5	0	0	0	0	0	0	5	1	5	5
21	0	0	0	0	5	5	5	5	5	5	1	1	1	1	1
22	0	5	5	0	0	5	0	0	0	0	5	5	0	0	0
23 24	2 1	$\frac{2}{1}$	2 1	2 1	2 1	2 1	2 1	5 1	5 5	2 5	2 1	2	2 1	2	2 1
25	2	2	$\stackrel{\scriptscriptstyle{1}}{2}$	2	2	5	1	1	1	1	1	1	5	5	5
26	1	5	1	1	1	1	1	1	1	1	1	1	1	1	1
27	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
28	1	5	1	5	5	5	5	5	5	5	1	5	5	5	5
29	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
30	1	1	1	1	1	1	5	0	0	0	5	5	5	5	5
$\frac{31}{32}$	$\frac{1}{2}$	1 2	1 2	1 2	1 2	1 2	$\frac{1}{2}$	1 2	5	5	5	5	5	2	$\frac{2}{2}$
32 33	1	1	1	1	1	1	1	1	1	5	1	1	1	1	1
34	2	2	2	2	2	2	2	2	5	2	2	2	5	5	2
35	0	0	0	0	5	5	5	5	5	5	0	0	0	0	0
36	2	5	5	5	5	5	5	5	5	5	5	5	5	5	1
37	$^2$	2	2	2	2	2	2	2	2	2	2	2	2	2	2
38	2	5	5	1	1	1	1	1	1	1	1	5	5	5	5
39 40	1 2	5	5	1 2	5	1 2	1 2	1 2	1 2	1 2	1 2	1 2	1 2	5	$\frac{5}{2}$
41	1	1	1	5	1	1	∠ 5	1	1	5	0	∠ 5	∠ 5	1	1
42	2	2	2	2	2	2	$\frac{3}{2}$	2	2	2	$\frac{\circ}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	5	2
43	1	1	1	1	1	1	5	0	0	0	5	5	5	5	5
44	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
45	2	2	2	2	2	2	2	5	5	1	1	1	1	1	1
46	2	2	2	2	2	2	2	2	2	5	2	5	5	5	5
47	2	2	2	2	2	2	2	2	2	5	2	5	5	5	5
48 49	$\frac{2}{2}$	$\frac{5}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$	$\frac{2}{2}$
50	1	1	1	1	1	1	1	1	1	5	0	0	0	0	0
51	1	5	5	5	5	1	1	1	1	5	1	1	1	1	1
52	$^2$	2	$^2$	2	2	5	2	2	2	5	5	1	1	1	1
53	0	0	0	0	0	0	5	5	1	5	0	0	0	0	0
54	2	2	2	2	2	2	2	2	2	2	5	1	1	5	1
55 5.0	1	5	1	1	1	1	5	5	5	5	1	1	1	1	5
56 57	$\frac{2}{0}$	5 0	$\begin{array}{c} 1 \\ 0 \end{array}$	$\frac{5}{0}$	$\frac{5}{0}$	$\frac{2}{0}$	$\frac{2}{5}$	2 1	$\frac{2}{1}$	$\frac{2}{0}$	$\frac{2}{0}$	$\frac{2}{0}$	$\frac{2}{0}$	$\frac{2}{0}$	$\frac{2}{0}$
58	1	1	1	2	5	5	о 5	$\frac{1}{2}$	$\frac{1}{2}$	5	1	1	5	5	5
59	1	1	1	1	1	1	1	1	5	5	1	1	5	5	5
60	0	1	1	5	5	5	1	5	5	1	0	0	0	0	0
61	0	0	0	0	0	0	0	5	5	0	0	0	0	0	0
62	2	2	2	2	2	2	2	2	2	2	2	2	2	2	5
63	2	5	5	5	5	5	2	2	2	2	5	1	1	1	1
64	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
							15								

Table 1: Results of our classification analysis by nonparametric density estimation with bandwidths h reported in the Appendix, S=3,  $\alpha=1/3$ , c=0.80 and B=1000. Note: 5 represents the outcome for the indeterminancy region. Horizontal lines in the table distinguish the 10 British regions.

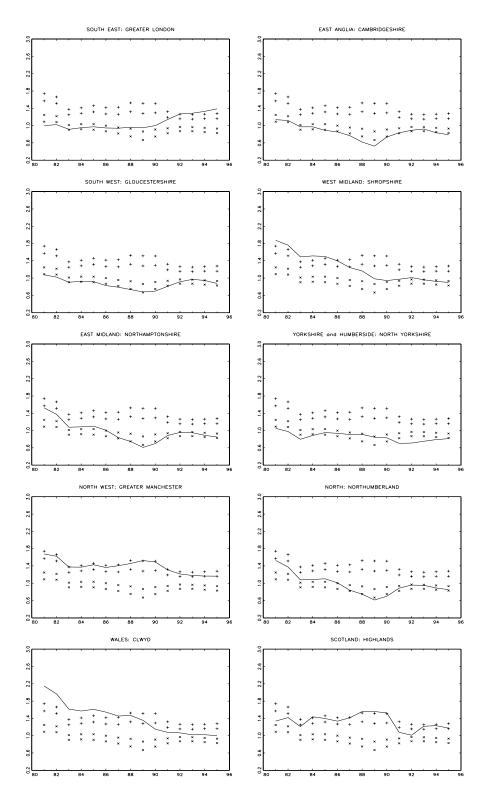


Figure 6: Plot of unemployment ratios for 10 counties. Note: the  $\times$  symbols mark the indeterminancy region for  $c_1$ ; the + symbols represent the indeterminancy region for  $c_2$ .

	Positive shocks			Negative shocks			
Index	County	Date	$Y^+$	Index	County	Date	$Y^-$
1	Bedfordshire (SE)	1987	3	1	Bedfordshire (SE)	1990	5
8	Hertfordshire (SE)	1994	1	4	East Sussex (SE)	1991	4
19	Dorset (SW)	1988	2	5	Essex (SE)	1991	4
25	Shropshire (WM)	1986	9	6	Gr. London (SE)	1987	4
30	Northamptonshire (EM)	1987	8	6	Gr. London (SE)	1991	4
36	Greater Manch (NW)	1994	1	7	Hampshire (SE)	1991	4
38	Cheshire (NW)	1983	12	8	Hertfordshire (SE)	1991	3
41	Cumbria (N)	1990	3	9	Isle of Wight (SE)	1981	10
43	Northumbershire (N)	1987	8	9	Isle of Wight (SE)	1991	4
45	Clwyd (Wales)	1989	6	19	Dorset (SW)	1990	5
50	Powys (Wales)	1990	5	20	Gloucerstershire (SW)	1992	3
52	West Glam (Wales)	1991	4	21	Somerset (SW)	1990	5
53	Borders (SC)	1990	5	31	Nottingham (EM)	1993	2
54	Central (SC)	1991	4	41	Cumbria (N)	1993	2
56	Fife (SC)	1982	3	53	Borders (SC)	1988	2
56	Fife (SC)	1985	10	57	Granpian (SC)	1987	2
57	Grampian (SC)	1989	6	58	Highlands (SC)	1983	7
60	Orkneys (SC)	1990	5	58	Highlands (SC)	1990	5
63	Tayside (SC)	1991	4	60	Orkneys (SC)	1981	9

Table 2: Summary results from the classification analysis concerning the dating and the persistence of shocks. Legend: SE = South East; SW = South West; WM = West Midlands; EM = East Midlands; N = North; NW = North West; SC = Scotland.

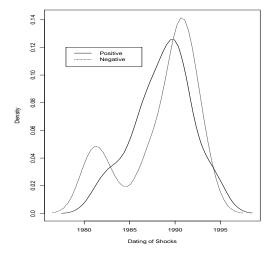


Figure 7: Density estimate of the dating of positive and negative shocks. Note: h = 6 for the density estimate of both positive and negative shocks.

	$S_0$	$S_1$	$S_2$
$S_0$	0.968	0.032	0.000
$S_1$	0.027	0.949	0.024
$S_2$	0.000	0.033	0.967

Table 3: Transition probabilities with  $\alpha = \{1/3, 1/3, 1/3\}$  and c = 0.80.

	${S}_0$	${S}_1$	${S}_2$	${S}_3$	$S_4$
$S_0$	0.9575	0.0425	0.0000	0.0000	0.0000
$S_1$	0.0268	0.9263	0.0277	0.0149	0.0042
$S_2$	0.0079	0.0633	0.8841	0.0447	0.0000
$S_3$	0.0000	0.0000	0.0711	0.8749	0.0541
$S_4$	0.0000	0.0000	0.0048	0.0391	0.9561

Table 4: Transition probabilities with  $\alpha = \{0.20, 0.20, 0.20, 0.20, 0.20\}$  and c = 0.80.

# **Appendix**

#### The 64 counties

Sou	th East	Sout	h West	30	Northamptonshire	Wa	les
1	Bedfordshire	16	Avon	31	Nottinghamshire	45	Clwyd
2	Berkshire	17	Cornwall	You	kshire and Humberside	46	Dyfed
3	Buckinghamshire	18	Devon	32	South York. Met.	47	Gwent
4	East Sussex	19	Dorset	33	West York. Met.	48	Gwynedd
5	Essex	20	Gloucestershire	34	Humberside	49	Mid Glamorgan
6	Greater London	21	Somerset	35	North Yorkshire	50	Powys
7	Hampshire	$^{22}$	Wiltshire	No	rth West	51	South Glamorgan
8	Hertfordshire	$\mathbf{Wes}$	t Midland	36	Greater Manchester	52	West Glamorgan
9	Isle of Wight	23	W.Midlands Met.	37	Merseyside Met.	Sco	tland
10	Kent	24	Hereford and Worcester	38	Cheshire	53	Borders
11	Oxfordshire	25	Shropshire	39	Lancashire	54	Central
12	West Sussex	$^{26}$	Staffordshire	No	rth	55	Dumfries and Galloway
				40	Cleveland	56	Fife
Eas	t Anglia	East	Midland	41	Cumbria	57	Grampian
13	Cambridgeshire	$^{27}$	Derbyshire	42	Durham	58	Highlands
14	Norfolk	28	Leicestershire	43	Northumberland	59	Lothians
15	Suffolk	$^{29}$	Lincolnshire	44	Tyne and Wear Met.	60	Orkneys
					-	61	Shetlands
						62	Strathclyde
						63	Tayside
						64	Western Isle

Table 5: List of counties. Note: Surrey (South East) and Warwickshire (West Midlands) not included due to missing observations for some years.

#### Bandwidth selection for density estimation

Using the method of Sheater and Jones (1991), we have calculated the bandwidths reported in the table below.

	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95
h	0.22	0.20	0.16	0.17	0.20	0.19	0.20	0.24	0.26	0.22	0.17	0.12	0.11	0.14	0.15

Table 6: Bandwidth selected by Sheather and Jones (1991) plug-in method.

#### **Bootstrap Multimodality Tests**

A formal unimodality test is constructed based on the concept of critical bandwidth introduced by Silverman (1981, 1983, 1986). A critical bandwidth  $\hat{h}_m$  is defined as the smallest possible h producing a density with at most m modes, which means that for all  $h < \hat{h}_m$  the estimated density  $\hat{f}_h$  has at least m+1 modes. This idea of critical smoothing is naturally related to hypothesis testing and, in particular, to multimodality tests. Indeed, if the true underlying density has two modes, a large value of  $\hat{h}_1$  is expected, because a

considerable amount of smoothing is required to obtain a unimodal density estimate from a bimodal density. This suggests that  $\hat{h}_m$  can be used as a statistic to test

$$H_0$$
:  $f(x)$  has  $m$  modes versus  $H_1$ :  $f(x)$  has more than  $m$  modes. (6)

Here, a 'large' value of  $\hat{h}_m$  indicates more than m modes, thus rejecting the null. How large is large in this context is assessed by the bootstrap, as discussed by Silverman and, among the others, by Izenman and Sommer (1988) and Efron and Tibshirani (1993).

The steps to test for multimodality can then be summarised as:

- 1. Draw B bootstrap samples  $\mathbf{x}^*$  of size n using (5);
- 2. for each boostrap sample  $\mathbf{x}^*$  compute the critical bandwidth consistent with m-modality,  $\hat{h}_m^*$ . Denote the values of  $\hat{h}_m^*$  by  $\hat{h}_m^*(1), \hat{h}_m^*(2), \dots, \hat{h}_m^*(B)$ ;
- 3. obtain an estimate of the achieved significance level (or p-value) of the test as  $\widehat{ASL}_m = \#\{\hat{h}_m^*(b) \geq \hat{h}_m\}/B$ ; <sup>14</sup>
- 4. fail to reject the null hypothesis of m modes in the density whenever  $\widehat{ASL}_m$  is larger than standard levels of significance.

By implementing the above test in each year, we have obtained the results shown in Table 7. In all years, we fail to reject unimodality.

Year	$\widehat{ASL}$ $(m=1)$	$\widehat{ASL}$ $(m=2)$
1981	0.50	0.53
1982	0.20	0.63
1983	0.77	0.57
1984	0.52	0.24
1985	0.79	0.85
1986	0.76	0.31
1987	0.49	0.27
1988	0.79	0.47
1989	0.76	0.74
1990	0.60	0.98
1991	0.98	0.84
1992	0.92	0.63
1993	0.59	0.79
1994	0.88	0.49
1995	0.36	0.36

Table 7: Bootstrap multimodality tests with B = 1000 replications.

<sup>&</sup>lt;sup>14</sup>It has been proven by Silverman that the event  $\hat{h}_m^* > \hat{h}_m$  is equivalent to the event that  $\hat{f}_{\hat{h}_m}^*$  has more than m modes. This result implies that it is not necessary to compute  $\hat{h}_m^*$  for each bootstrap sample; one needs only to check the proportion of cases when  $\hat{f}_{\hat{h}_m}^*$  has more than m modes.

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