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Determinacy in New Keynesian models: a role for money after all?

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Determinacy in New Keynesian models: a role for money after all?

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Abstract

The New-Keynesian Taylor-Rule model of inflation determination with no role for money is incomplete. As Cochrane (2007a) argues, it has no credible mechanism for ruling out bubbles and as a result fails to provide a reason for private agents to pick a unique stable path. We propose a way forward. Our proposal is in effect that the New-Keynesian model should be formulated with a money demand and money supply function. It should also embody a terminal condition for money supply behaviour. If an unstable path occurred the central bank would switch to a money supply Rule explicitly designed to stop it via the terminal condition. This would be therefore a ‘threat/trigger strategy’ complementing the Taylor Rule — only to be invoked if

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inflation misbehaved. Thus we answer the criticisms levelled at the Taylor Rule that it has no credible mechanism for ruling out bubbles. However it does imply that money cannot be avoided in the new Keynesian set-up, contrary to Woodford (2008).

JEL classifications: E31, E52, E58

Keywords: New-Keynesian; Taylor Rule; Determinacy
1 Introduction

The New-Keynesian Taylor-Rule (NK, henceforth) approach to monetary economics provides the current standard model of inflation determination. By linking interest rate decisions directly to inflation and economic activity, Taylor Rules offered a convenient tool for studying monetary policy while abstracting from a detailed analysis of the demand and supply of money.\footnote{Woodford (2008) describes a class of New-Keynesian models and draws attention to the fact that interest rates transmit directly to intertemporal spending decisions and that monetary policy need not be framed in terms of monetary aggregates. For an account of the origins of the Taylor Rule in early work by Henderson and McKibbin (1993), see Minford (2008).} This change in the standard analytics is an understandable reflection of how most central banks now make monetary policy: by setting a short-term nominal interest rate, with little if any explicit role for money (see Friedman, 2003).\footnote{There are exceptions of course. For example, the European Central Bank (ECB) continues to assign a prominent role to money in its monetary policy strategy. In what the ECB calls its “two-pillar strategy,” one pillar is “economic analysis,” which “assesses the short-to-medium-term determinants of price developments.” In addition, a second pillar, “monetary analysis,” assesses the medium- to long-term outlook for inflation, exploiting the long-run link between money and prices.} Furthermore, econometric evidence supporting the stabilization properties of this rule (see Taylor, 1999) and its usefulness for understanding historical monetary policy (see Clarida, Gali, and Gertler, 2000) explains its popularity.\footnote{These developments have greatly influenced monetary policy research and teaching. This allowed the development of simpler models (see the survey in Clarida, Gali, and Gertler, 1999) and the replacement of the “LM curve” with a Taylor Rule in textbook treatments of the Hicksian IS-LM apparatus (see Taylor (2000) and Romer (2000)).}

While the NK approach has been remarkably successful, there are reasons to be uneasy about the lack of modelling of money markets. For example, Cochrane (2007a) argues that the way standard “New Keynesian” models work to discipline inflation is in fact incredible: In effect, the Fed threatens to raise inflation and interest rates without limit should inflation deviate from the stable path. That is, the Fed threatens hyperinflation or deflation, unless
inflation jumps to one particular value on each date. This is true: if inflation takes off along a bubble path in this model what is there to stop it? The New Keynesian answer seems to be: just the horrifying thought that this might happen! Essentially, the government threatens to ‘blow up the (monetary) world’ to use Cochrane’s phrase should any but one equilibrium occur. Because people believe this threat, inflation goes to this unique path. But would people really avoid deviant paths fearing this nuclear option? And would they believe that the Fed would stick with such a rule under such circumstances?

One problem is that these threats are not credible. The reason is that, once inflation or deflation happens, carrying through on the threat is a disastrous policy. As a result self-destructive threats are less likely to be carried out \textit{ex-post}, and thus less likely to be believed \textit{ex-ante}. A second problem with these threats is that even if they were credible and did actually happen, there seems to be nothing to stop people following the implied paths. While undesirable from a social viewpoint, they do not appear to be \textit{impossible}. Thus no transversality conditions on real variables appear to be violated for reasonable versions of NK models. What this shows is that the Taylor Rule is an incomplete description of monetary policy, at least within a NK model; it cannot account for determinate inflation before 1980, and after 1980 it lacks a clear mechanism for ruling out unstable paths (see Cochrane, 2007b). One has to assume that the authorities have some additional tool in their locker to rule out unstable paths.

Our proposal is in effect that the NK model should be formulated with a money demand and money supply function. It should also embody a terminal condition for money supply behaviour. If an unstable path occurred the central bank would switch to a money supply rule explicitly designed to stop it via say a terminal condition. This would be therefore a
threat or trigger strategy complementing the Taylor Rule — only to be invoked if inflation misbehaved. Of course if the strategy is credible it would never be observed and you would just get the Taylor Rule. Thus we achieve a determinate solution without appealing to the notion that the unstable paths are ruled out by an extreme threat to wreck the monetary economy⁴; and also answer the criticisms levelled at the Taylor Rule that it has no credible mechanism for ruling out bubbles — we do this via our threat strategy. However it does imply that money cannot be avoided in the NK set-up, contrary for example to Woodford (2008). There has to be a money supply rule operating in emergency at least. Thus in summary we reinterpret the nature of monetary policy under Taylor Rules used in NK models. Monetary policy is in effect not fully revealed by simply writing down a Taylor Rule; ‘behind it’ lies various implied commitments — viz to the provision of money according to a long-term (terminal) condition that limits undesirable behaviour of inflation with an override of the money supply rule implicit in the Taylor Rule.

The article is organized as follows. In Section 2 we construct the basic cashless model, and uncover the general properties of this model. We also study determinacy in the standard NK model. We verify that the issues are the same, and the Fed does in fact determine inflation by threatening hyperinflation, not by stabilizing past inflation. Section 3 explains how we deal with explosive solution paths in traditional macro models of the 1970s. We also answer the criticisms levelled at the Taylor Rule that it has no credible mechanism for ruling out bubbles — we do this via a terminal condition for money supply behaviour. Section 4

⁴Cochrane (2007b) argues this can be a non-Ricardian fiscal policy. This is a possible route but here we maintain the usual NK assumptions: that the Taylor Principle applies and that fiscal policy is Ricardian. Our objective is to show that the NK model can work in its own terms, by adding a ‘background condition’ relating to money supply policy.
provides concluding remarks.

2 Determinacy in New-Keynesian model

2.1 Determinacy in a frictionless New-Keynesian Model

The basic points do not require the Phillips - IS curve features of NK models, and thus they do not need any frictions. This might come as a surprise to those of us who have been brought up to think that in the Keynesian framework the Phillips curve pins down the inflation rate given output supply, which is demand determined. But in the NK literature it is routine to discuss inflation determination without mentioning the Phillips curve (see Woodford 2008 for example). Following Cochrane (2007a) we start with a very simple model consisting only of a Fisher equation and a Taylor Rule describing monetary policy:

\[
\begin{align*}
    i_t &= r + E_t \pi_{t+1} \\
    i_t &= r + \pi^* + \phi (\pi_t - \pi^*)
\end{align*}
\]

where \( i_t \) = nominal interest rate, \( \pi_t \) = inflation and \( r \) = constant real rate. The coefficient \( \phi > 0 \) measures how sensitive the central bank’s interest rate target is to inflation. We can
solve this model by substituting out the nominal interest rate, leaving only inflation,

\[ E_t \pi_{t+1} = \phi (\pi_t - \pi^*) + \pi^*, \]

or

\[ E_t \pi_{t+i+1} = \phi (E_t \pi_{t+i} - \pi^*) + \pi^*, \quad \text{(for } i \geq 0) \]

(1.3)

where we have a first order expectational difference equation in \( \pi_t \). The general solution for this first order difference equation can be expressed as

\[ E_t \pi_{t+i+1} = \pi^* + (E_t \pi_{t+1} - \pi^*) (\phi)^i, \quad \text{(for } i \geq 0) \]

(1.4)

Equation (1.4) has many solutions, and this observation forms the classic doctrine that inflation is indeterminate with an interest rate target. However, if \( \phi > 1 \) (Taylor Principle), all of these solutions except one eventually explode. This example makes it crystal-clear that inflation determination comes from a threat to increase future inflation if current inflation gets too high. If inflation takes off along a bubble path what is there to stop it in this model? The NK answer is: just the dreadful thought that this might happen. This is because in this model the monetary authority is absolutely committed to raising interest rates more than one for one with inflation, for all values of inflation. For only one value of inflation today will we fail to see inflation that either explodes or, more generally, eventually leaves a local region. Ruling out non-local equilibria, NK modellers conclude that inflation today jumps to the unique value that leads to a locally-bounded equilibrium path.
2.2 Determinacy in the three-equation model

Now let us consider a standard NK IS-LM model (for example, see Clarida et al., (1999) and Woodford (2003)). For determinacy questions, we can work with a stripped-down model without constants or shocks.

\[ y_t = E_t y_{t+1} - \sigma r_t, \quad \sigma > 0 \]  \hspace{2cm} (2.1)

\[ i_t = r_t + E_t \pi_{t+1}, \]  \hspace{2cm} (2.2)

\[ \pi_t = \beta E_t \pi_{t+1} + \gamma y_t, \quad \beta, \gamma > 0 \]  \hspace{2cm} (2.3)

where \( y_t \) = output, \( r_t \) = real interest rate, \( i_t \) = nominal interest rate, \( \pi_t \) = inflation.

This representation can represent deviations from a specific equilibrium of a model with shocks (see Cochrane (2007b). The first two equations derive from consumer first order conditions for consumption today vs. consumption tomorrow. The first equation is a log-linear approximation to an Euler equation for the timing of aggregate expenditure, sometimes called an “intertemporal IS relation.” This is the one that indicates how monetary policy affects aggregate expenditure: the expected short-term real rate of return determines the incentive for intertemporal substitution between expenditure in periods \( t \) and \( t + 1 \). The last equation is the NK Phillips curve. It is derived from the first order conditions of

---

\(^5\)See Woodford (2003, chaps. 3–5) for discussion of the microeconomic foundations underlying equations (2.1) and (2.2). Woodford (2008) refers to models of this kind “neo-Wicksellian,” to draw attention to the fundamental role in such models of a transmission mechanism in which interest rates affect intertemporal spending decisions, so that monetary policy need not be specified in terms of an implied path for the money supply, but the terminology “NewKeynesian” for such models has become commonplace, following Clarida et al. (1999), among others.
intertemporally-optimizing firms that set prices subject to costs. The remaining equation required to close the system is a specification of monetary policy. We might, for example, specify policy by a rule of the kind proposed by Taylor (1993) for the central bank’s operating target for the short-term nominal interest rate,

\[ i_t = \phi \pi_t, \quad \phi > 0. \] (2.4)

2.3 Can Such a Model Explain the Rate of Inflation?

A first question about this model is whether such a model which has thus far made no reference to the economy’s supply of money has any implication for the rate of inflation. Woodford (2008) argues that while a model like this does not determine the inflation rate independently of monetary policy, it does determine the inflation rate without any reference to money growth and without any need to specify additional relations beyond those listed above. He goes on to argue that there is nothing “conceptually incoherent” about a model of inflation determination that involves no role whatsoever for measures of the money supply. Using (2.4) to substitute for \( i_t \) in (2.2), the model (2.1)–(2.3) can be written in the form,

\[
\begin{bmatrix}
E_t y_{t+1} \\
E_t \pi_{t+1}
\end{bmatrix} = \frac{1}{\beta} \begin{bmatrix}
\beta + \sigma \gamma & -\sigma (1 - \beta \phi) \\
-\gamma & 1
\end{bmatrix} \begin{bmatrix}
y_t \\
\pi_t
\end{bmatrix}.
\]

The eigenvalues of matrix \( A \) that is, \( \lambda_1 \) and \( \lambda_2 \), are computed by setting \( \det (A - \lambda I) = 0 \).

\(^6\)This equation represents a log-linear approximation to the dynamics of aggregate inflation in a model of staggered price-setting of the kind first proposed by Calvo (1983).
This gives a second-order polynomial in $\lambda$:

$$\frac{1}{\beta} \left[ \lambda^2 - (1 + \beta + \sigma\gamma) \lambda + \beta (1 + \sigma\gamma\phi) \right] = 0$$

where $\lambda_1 + \lambda_2 = (1 + \beta + \sigma\gamma)$ and $\lambda_1\lambda_2 = \beta (1 + \sigma\gamma\phi)$.

**Proposition 1** If the number of eigenvalues of $A$ outside the unit circle is equal to the number of non-predetermined variables (or forward-looking variables), then there exists a unique stable solution. Blanchard and Kahn (1980)

**Proposition 2** Let $\lambda_1, \lambda_2$ lie in the complex plane, then: the $\lambda_i$’s ($i = 1, 2$) are both outside the unit circle if and only if the following conditions are satisfied:

$$|\lambda_1 + \lambda_2| < |1 + \lambda_1\lambda_2|$$

$$|\lambda_1\lambda_2| > 1.$$

For the usual parameter values in NK models ($\beta \approx 1, \sigma > 0, \gamma > 0$ and $\phi > 1$) the system guarantees both eigenvalues are greater than one. Thus the general solution for $E_t\pi_{t+1}$ can be expressed as

$$E_t\pi_{t+i+1} = \pi^* + A_1 (\lambda_1)^i + A_2 (\lambda_2)^i, \quad (\text{for } i \geq 0). \quad (2.5)$$

How does the Fed plan to stabilise inflation in this model? In this model, $E_t y_{t+i}$ and $E_t\pi_{t+i}$ explode in any equilibrium other than $y = 0$, $\pi = 0$. According to these New Keynesians, $\phi > 1$ (the Taylor Principle), would stabilize inflation. But how does it rule out the unstable path? Here NK authors become vague, saying that such paths would be ‘inconceivable’ and hence ‘ruled out by private agents’. Thus for example King (2000, p.
58–59, cited in Cochrane, 2007a) writes: “By specifying \( \phi > 1 \) then, the monetary authority would be saying, ‘if inflation deviates from the neutral level, then the nominal interest rate will be increased relative to the level which it would be at under a neutral monetary policy.’ If this statement is believed, then it may be enough to convince the private sector that the inflation and output will actually take on its neutral level.”

Ruling out such non-local equilibria, the NK tradition concludes that output and inflation are again determinate. According to Cochrane (2007a), in effect if current inflation misbehaves the Fed threatens to implement such paths (hyperinflation or hyperdeflation). Thus the threat is to ‘blow up the world’ — and this threat is supposed to be so terrifying that private agents expect the stable path instead. No economic consideration rules out the explosive solutions. With \( \phi > 1 \), the explosive solutions are legitimate solutions of the model, just as the multiple solutions are legitimate with \( \phi < 1 \).

This interpretation of the ruling-out of unstable paths raises many questions. Consider what is being said. 1) if inflation rises (falls), it will be forced into a hyperinflation (hyperdeflation) by the Fed. 2) if inflation remains on target, then the Fed will maintain it at that target. So we need to establish how this enables private agents to choose the stable path. Clearly they will prefer the stable path; but how can they be sure it will happen, given

\[ |\lambda_1 + \lambda_2| > |1 + \lambda_1 \lambda_2|. \]

For the usual parameter values in NK models and \( \phi < 1 \) this condition is met. That is, there are infinity of stable paths — the ‘non-uniqueness’ problem (Taylor, 1977).
that all the paths are feasible. The first question is: is the threat in statement 1) credible? People know that hyperinflation (hyperdeflation) is costly for the central bank/government too. If we think of inflation as a tax chosen by the government on optimising grounds then plainly the government will be thrown away from its optimum, obtaining excessive (inadequate) revenue etc. Thus if the central bank carries out this threat, the government’s and society’s interests would be badly damaged too. So people would conclude that the central bank would simply not follow up on its threat in society’s best interests. That is, they would expect the central bank to accommodate rising inflation \((\phi < 1)\). So clearly the implicit threat in NK models (the ‘Taylor Principle’) is simply not credible in equilibrium.

The second question is: assume the threat is credible; then if it were to be carried out is there anything to stop the unstable path continuing to infinity? One possible way that the path could be stopped is by violating real variable transversality conditions. In the New Keynesian model this is not the case, as noted by Cochrane. In models with a demand for real balances, McCallum (2008) notes that again transversality conditions on real money demand cannot rule out hyperinflations for reasonable preferences; Obstfeld and Rogoff (1983) reached the same conclusion when money enters the utility function, suggesting that the government could rule out hyperinflation by backing the currency at some fractional value. This is a policy suggestion, which acts in a similar way to our suggestion below, as we will explain.

Thus we find that a) the rule implies an incredible threat; and that b) even were it to be credible, it would imply that unstable paths would continue to infinity were they to occur. Under a) the Taylor Rule defaults to an accommodative rule under which there is indeterminacy of stable paths. Under b) unstable paths would carry on for ever were
they to occur. Hence there is nothing to make them infeasible. Thus effectively we have two possible NK models; either one with indeterminacy of stable paths or one with indeterminacy of unstable paths. Notice we are not attacking the NK model as such but we are arguing that it fails to provide a reason for private agents to pick a unique stable path.\footnote{We may note that McCallum (2008) agrees about the existence of this problem and proposes to rule them out by a ‘learnability condition’ — which he has also proposed in other contexts as a way of validating his minimum state variable solution methods for RE models. We note this; but while learnability may indeed, we concede, be desirable, we can envisage situations where agents already know the models that exist. In such situations learnability does not arise. Thus a criterion is needed for models to work when they are known. Otherwise we are reduced to saying that such-and-such a model will not work unless it is unknown because then it will work because it will be learnt — a strange proposition. We therefore believe a criterion more fundamental than learnability is needed.}

3 Traditional Macro Model and Inflation Determinacy

How do we deal with explosive solution paths in traditional macro models of the 1970s? Our objective here is twofold. We show that the solution of this model is similar to the NK model discussed above. Moreover, we shall show how explosive paths are ruled out in these models. We illustrate this with the aid of the Minford and Peel (2002) version of Cagan’s (1956) hyperinflation model, described by the equation system (3.1)–(3.2).

\[
\begin{align*}
m_t &= p_t - \alpha (E_t p_{t+1} - p_t), \quad \alpha > 0 \\
m_t &= \overline{m},
\end{align*}
\] (3.1) (3.2)

where \( m_t \) and \( p_t \) are the natural logarithms of money supply and the price level, respectively; and \( \overline{m} \) is a monetary target, and \( E \) is the rational expectations operator. The first equation is a money demand function, specifying that the demand for money responds
negatively to expected price level changes. The second equation is a money supply function where the government has a monetary target, $\bar{m}$. The above model is an example of RE models involving a future variable, and the main problem in solving the model comes from the presence of $E_t p_{t+1}$ in the first equation.

Substituting (3.2) in (3.1) for $m_t$ yields;

$$E_t p_{t+1} = \left(1 + \frac{\alpha}{\alpha}\right) p_t - \frac{\bar{m}}{\alpha}$$

or

$$E_t p_{t+i+1} = \left(1 + \frac{\alpha}{\alpha}\right) E_t p_{t+i} - \frac{\bar{m}}{\alpha} \quad \text{(for } i \geq 0) .$$

The solution of this first-order non-homogenous difference equation is:

$$E_t p_{t+i+1} = p^* + A (\lambda)^i, \quad \text{(for } i \geq 0)$$

$$E_t p_{t+i+1} = \bar{m} + (E_t p_{t+1} - \bar{m}) \left(1 + \frac{\alpha}{\alpha}\right)^i, \quad \text{(for } i \geq 0) .$$

where $\bar{m}$ is the equilibrium of $p_t$ (the ‘particular solution’), $\frac{1+\alpha}{\alpha}$ is the unstable root and $E_t p_{t+1} - \bar{m}$ is the constant (determined by the initial value $E_t p_{t+1}$) in the ‘general’ solution. Notice that the general solution for $E_t p_{t+1}$ has the same form as (1.4) above. Equation (3.5) gives an infinite number of solution paths for $E_t p_{t+i+1} (i \geq 0)$. For we are free to choose any value of $E_t p_{t+1}$ we like; the model does not restrict our choice. Another way of looking at (3.5) is to say that we can choose any future value for $E_t p_{t+i+1}$ we wish and work back from that to a solution for $E_t p_{t+1}$. Any view of this future will then compel a present which is consistent with it; any set of expectations is therefore self-justifying i.e. anything can happen
provided it is expected, but what is expected is arbitrary. Worse still, as (3.5) illustrates, these paths for events can be unstable; in fact, our model here implies that all paths for prices except that for which $E_t p_{t+1} = \bar{m}$, explode monotonically. Thus the model would assert that only by accident would an equilibrium price level be established, otherwise prices would be propelled into either ever-deepening hyperdeflation or ever-accelerating hyperinflation, even though money supply is held rigid!

To prevent these unstable paths, we appeal to an optimising government, choosing the inflation tax. Having chosen its optimum target — which here for simplicity we set at zero — we assume it sets a money supply target designed to achieve it, provided unstable paths do not occur. It then needs, in order to achieve this optimum, to prevent these unstable paths from occurring. It turns out that a commitment on its part to put an end to any inflation (deflation) bubble paths at some point, by decreasing (increasing) the money supply sufficiently to force prices off this path, will do the trick. For if people expect that inflation will stop at some period $t + N$ (at which the bank will ‘step in’), then desired real money balances in $t + N$ will now be higher and inflation would fall at $t + N$. If inflation falls in $t + N$ then people would postpone consumption at $t + N - 1$ and inflation would fall at $t + N - 1$ too. And so on. By backward induction the whole process gets invalidated. We can show this formally by imposing the terminal condition

$$E_t p_{t+i+1} - E_t p_{t+i} = 0 \text{ for } i \geq N.$$
Substituting the terminal condition in (3.4) yields

\[
E_t p_{t+N+1} = \left( \frac{1 + \alpha}{\alpha} \right) E_t p_{t+N} - \frac{m}{\alpha}
\]

\[
E_t p_{t+N+1} = m.
\]

This implies from (3.5)

\[
E_t p_{t+1} = m
\]

Finally, from (3.3) we have

\[
p_t = m
\]

An analogous argument can be constructed for the frictionless NK model discussed above. If inflation takes off along an explosive path what is there to stop it? Suppose the central bank commits to put an end to this path at some point by reducing money growth and if the commitment is credible, then the whole process gets invalidated. To see this let us impose the terminal condition, \(E_t \pi_{t+i+1} = E_t \pi_{t+i}\), (for \(i \geq N\)), on our frictionless NK model. Substituting the terminal condition in (1.3) yields \(E_t \pi_{t+N+1} = \pi^*\). Thus, we have \(\pi_t = E_t \pi_{t+1} = \pi^*\). We have ruled out unstable paths by appealing to a terminal condition on inflation implemented via the money supply (or money growth) rule. Is this terminal condition credible? As we have argued, the government has an incentive to prevent an unstable path because it is the stable path that maximises its objectives. There is a lot at stake here for it and people understand this. Therefore a commitment to stop these bubble paths is credible. This implies that money cannot be avoided in NK models, contrary to the
‘cashless world’ invoked by Woodford et al.⁹

It can be seen that this government commitment acts to disrupt unstable paths in just the same way that Obstfeld and Rogoff (1983)’s suggestion for government fractional backing of the currency prevents hyperinflation paths (while a transversality condition on real balances not tending to infinity because they would be swapped for consumption goods rules out hyperdeflation). Our suggestion can be thus thought of as a practical way of implementing the same idea.

Finally, we should note that the terminal condition acts like a special sort of monetary rule in which a variable (money) is used to implement a target for another variable (prices) by taking whatever value is necessary. Examples of such rules are fixed exchange rates in which reserves (thus money) are varied as much as necessary to hit an exchange rate target; or fixed interest rate rules in which money is varied as much as necessary to hit an interest rate target. Formally, two variables swap exogenous for endogenous status within an N-equation model; thus under fixed exchange rates, reserves become endogenous while the exchange rate is exogenised, whereas under floating exchange rates, reserves are exogenised and the exchange rate becomes endogenous. Under the terminal condition, money swaps its exogenous status (with prices endogenous) for endogenous status (with prices exogenous).

⁹We offer a similar argument incidentally as a possible interpretation of the European Central Bank’s second pillar. The second pillar could be regarded as a commitment device designed to anchor inflation expectations in the face of explosive paths for credit and broad money. Thus the ECB uses the Taylor Rule as a practical short term device but always stands ready to override this Rule should the behaviour of the banking sector threaten to produce unsatisfactory longterm inflation behaviour. Neumann (2006), in a review of monetary targeting by the Bundesbank, stresses the desire to influence public expectations of inflation as a central motivation for the strategy and a key element in its success.
4 Conclusion

The New Keynesian model of inflation determination has no effective mechanism for ruling out explosive bubbles. It fails to provide a reason for private agents to pick a unique stable path. We propose a way forward. Our proposal is in effect that the NK model should be formulated with a money demand and money supply function, as above in the ‘traditional’ model; as there too, it should embody a terminal condition on inflation. This is implemented by an override on the money supply rule explicitly designed to stop bubble paths at some point should they occur. To replicate the Taylor Rule we simply specify the money supply rule to imply the Taylor Rule being followed; thus the Taylor Rule has the interpretation of an operational money supply rule — as intended by Taylor in his original paper. It is apparent from our reformulation that nothing changes in the NK model; the model is solved with two unstable roots and these are ruled out via the terminal condition on inflation. Thus in summary we reinterpret the nature of monetary policy under Taylor Rules used in NK models. Monetary policy is in effect not fully revealed by simply writing down a Taylor Rule; ‘behind it’ lies various implied commitments — viz to the provision of money according to a long-term (terminal) condition that limits undesirable behaviour of inflation with an override of the money supply rule implicit in the Taylor Rule.
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