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Industrial policy and firm heterogeneity

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MEMORANDUM

No 02/99

Industrial Policy and Firm Heterogeneity

By

Pedro P. Barros and Tore Nilssen

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Industrial Policy and Firm Heterogeneity

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March 15, 1999

Abstract

Our concern is with a firm-specific industrial policy. When R&D subsidies or taxes are differentiated among firms, the question arises which firms in an industry should receive such support. We analyze a situation where firms differ in their R&D technologies in two distinct ways: they differ both in the costs of performing R&D activities and in the output obtained from such activities. We find that the optimal firm-specific industrial policy is affected differently by the two sources of firm heterogeneity. Furthermore, a change in a firm's R&D productivity has an ambiguous effect on the optimal policy towards the firm.

JEL Numbers: O31, L52, F13

Keywords: firm heterogeneity, industrial policy, R&D

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1 Introduction

A country's trade policy has many facets, among them measures directed towards production, such as export subsidies, and others directed towards innovation, such as R&D subsidies or taxes. The former measures are increasingly difficult for governments to pursue, due to successful trade negotiations in GATT and elsewhere. This leads to a need for further analysis of trade-policy measures directed towards innovation. Our concern in the present paper is with one important aspect of R&D subsidies or taxes that distinguishes this policy instrument, in our view, from other trade-policy instruments: Whereas these other instruments tend to be industry-specific, aimed at industries in particular need of government support (or taxation, as the case may be), the support of R&D activities is, in its nature, firm-specific and even project-specific.

When R&D subsidies or taxes are differentiated among firms, the question arises which firms should receive such support. We attack this question on the industry level, asking which firms in an industry should receive the highest R&D subsidy, or pay the lowest R&D tax. In order to do this, we model an industry with several domestic firms that, by way of simplification, export all of their production to the world market. These firms, together with a number of foreign firms operating in the same industry, participate in a non-tournament R&D competition a la Spencer and Brander (1983): During an initial stage, each firm invests in process-innovation activities that bring down its production costs in the ensuing production stage, in which firms compete in quantities.\footnote{See Beath et al. (1995) for a survey of various models of R&D competition.}

Our focus is on a situation where domestic firms differ both in their costs of doing R&D and in their R&D productivities, i.e., the rates at which their R&D activities transform into reduced production costs. In order to model such a heterogeneity among domestic firms, it is, of course, essential that the model features more than one domestic firm. With several domestic firms and a government that is restricted to intervene at the R&D stage only, it is possible to distinguish three different motives for government intervention. First, there is the profit-shifting motive; when firms compete in quantities on the product market, this motive calls for an R&D subsidy (Spencer and Brander, 1983): Such a subsidy makes domestic firms produce more, entailing a contraction of foreign firms' R&D and production and therefore leaving more of the available profit to be earned by the domestic firms. Secondly, there is the need to correct for the incentives that each firm has to overinvest in R&D beyond what cost minimization prescribes in situations where lower marginal costs entail a higher market share.
(Brander and Spencer, 1983); this calls for a tax on R&D. Finally, with several domestic firms exporting their production, there is a need to intervene in order to keep the domestic firms from competing too heavily with each other on the world market; this, again, calls for an R&D tax (Dixit, 1984; Klette, 1994; Bagwell and Staiger, 1994).\footnote{Issues not raised in the present analysis, which would have a bearing on the question of a tax vs. subsidy on R&D, include: firms' strategic variables (Grossman, 1988); free entry (Horstmann and Markusen, 1986); spillovers (Leahy and Neary, 1999); uncertainty (Bagwell and Staiger, 1994); and resource constraints (Dixit and Grossman, 1986).}

Industrial policy in non-tournament models of international R&D competition is discussed in a few papers since Spencer and Brander (1983), such as Bagwell and Staiger (1994), Miyagiwa and Ohno (1997) and Leahy and Neary (1996, 1999). A firm-specific industrial policy does not seem to have been studied in the received literature, though. The studies closest to ours are those by Leahy and Montagna (1997) and Long and Soubeyran (1997a, 1997b) on firm-specific production subsidies (or taxes). However, as noted above, we believe that firm-specific policies more naturally occur at the R&D level than at the production level.\footnote{The literature on targeting, such as Dixit and Grossman (1986), Spencer (1988) and Neary (1994), is mainly concerned with which industry to support, rather than which firms in an industry. A crude kind of firm-specific support is, however, discussed by Dixit (1988) in a tournament model of R&D competition with asymmetric R&D efficiency. Here, the government controls how many domestic firms participate in an international patent race; in a sense, then, the government performs an industrial policy that discriminates on the firm level.}

A building block in our analysis is a model of non-tournament R&D competition among firms that differ in their R&D technologies, and this model is in itself a novelty.\footnote{The model is discussed further in Barros and Nilssen (1999).} The models of R&D competition that are closest to ours in the received literature are by Rosen (1991), Poyago-Theotoky (1996), and Yin and Zuscovitch (1998). However, in these models, firms have identical R&D technologies and differ only in their initial, or pre-R&D, production costs.

With our focus on firm-specific government policy, our analysis is closely related to studies of R&D cooperation, or research joint ventures, among heterogeneous firms (Veugelers and Kesteloot 1996, Kesteloot and Veugelers 1997, Long and Soubeyran 1997c, Röller et al. 1997): With a firm-specific policy and all domestic production being exported, the government's optimum level of R&D activity in each domestic firm coincides with what the firm itself would choose if all domestic firms were cooperating at the R&D stage.

Long and Soubeyran (1997c, 1997d) and Salant and Shafer (1998a, 1998b) nd that, even if the firms participating in a research joint venture are ex-ante identical, the optimum R&D efforts may be asymmetric, because increased differences in production costs lead to an increase in industry profit; in our analysis, we invoke so much convexity in R&D costs that this phenomenon does not occur. Salant and Shafer (1998b) are particularly interesting, since
they, too, note the formal resemblance between R&D cooperation and firm-specific R&D subsidies, as described above; however, they discuss only cases with identical firms and are concerned with the possible optimality of treating firms differently even if they are identical.

In Section 2 below, we present our model of the following three-stage situation. In the first stage, the government decides on firm-specific taxes on the R&D activities of the domestic firms in a particular industry. In the second stage, firms, both domestic and foreign, decide on how much R&D to perform when each firm's R&D affects its production costs but the cost per unit of R&D effort as well as the rate at which R&D effort is transformed into production-cost reductions differ among the firms. In the third stage, the firms compete on the world market by simultaneously deciding on produced quantities, and all domestic production is exported. In this Section, we also discuss the relevance of having firms differ in their R&D efficiency along two dimensions, both R&D costs and R&D productivity. In the subsequent sections, the gain in insights obtained from allowing both dimensions is made clear. In Section 3, we focus on the R&D game between the firms, which is stages two and three above. In particular, we discuss the comparative statics of firms' R&D activities and production quantities with respect to changes in R&D efficiency.

The main results of the analysis are in Sections 4 and 5. Central to the understanding of how firm heterogeneity affects industrial policy is, in our view, the distinction between a government's corrective and strategic motives for intervention. In order to make this distinction clear, we start our analysis of the government's optimum firm-specific industrial policy with restricting foreign firms to do no R&D, since this restriction eliminates the rent-shifting motive for intervention (in the absence of any production subsidy). We characterize the optimum firm-specific policy in this case, which is always a tax on R&D efforts when the only motives for intervention are the corrective ones, and then, somewhat counter-intuitive, that a firm with a relatively high R&D productivity does not necessarily pay a relatively high tax. The reason for the ambiguity is the interplay of two forces. On one hand is the direct effect: A higher R&D productivity makes a firm do more R&D, ceteris paribus, i.e. the firm's incentive to overinvest in R&D increases; this calls quite naturally for a higher tax the higher the R&D productivity is. On the other hand, there is a strategic effect: The more a firm's domestic rivals produce, the larger is the negative externality that the firm imposes upon them, and the higher is the tax necessary to impose on this firm. Since an increase in R&D productivity lowers a firm's costs and therefore lowers its rivals' production, this effect calls for a lower tax the higher the R&D productivity is.

In Section 5, we introduce R&D activities also among the foreign firms, so that the
optimum policy now also has a strategic element, with the consequence that the optimum policy towards a particular firm may be either a tax or a subsidy. The comparative-statics results, however, stand essentially unaltered from the previous analysis. In particular, the ambiguity in the relation between the R&D productivity and the optimum policy persists, for the same reason as outlined above. Section 6 provides some concluding comments.

2 The model

To set our analysis in the simplest framework possible, we consider a foreign market with demand given by a linear inverse demand function,

\[ P = a - bQ \]  

(1)

where \( P \) is price and \( Q \) is total quantity supplied in the market. On the supply side, there are \( n \) firms competing in quantities.\(^5\) A number \( m \) of firms are domestic and the other \( n - m \) firms are foreign (that is, firms located in other countries). Denote by \( M \) the set of domestic firms and by \( N \) the set of all firms in the market. Domestic firms are labelled from 1 through \( m \) and, thus, foreign firms from \((m + 1)\) through \( n \). Let \( q_i \) be the quantity produced by firm \( i \).

The production technology is characterized by constant returns to scale. The level of a firm's unit production cost depends on the R&D activity performed by the firm. In particular, the unit production cost of firm \( i \) is given by:

\[ c_i = c_i - \mu x_i \]  

(2)

where \( c_i \) is the initial level of unit production cost and \( \mu x_i \) is the reduction in cost obtained by firm \( i \), depending on its R&D investment, \( x_i \), and its R&D productivity, measured by \( \mu \). A higher \( \mu \) means a more efficient firm in doing R&D activities. As indicated by the subscripts on \( c_i \) and \( \mu \), we do not restrict firms to be equal.\(^6\)

Denote R&D costs by \((x_i; \sigma_i)\), where \( \sigma_i \) is a firm-specific parameter, i.e., R&D costs are not restricted to be equal across firms. A higher \( \sigma_i \) means a less efficient firm, with \( (0; \sigma_i) = 0; @ = @ > 0 \) and \( @ = @ \sigma_i > 0 \), that is, both total costs and marginal costs increase with \( \sigma_i \). We assume that \((x_i; \sigma_i)\) has the convexity properties with respect to \( x_i \).

---

\(^5\)The assumption of a homogeneous good leads naturally to Cournot competition. Under Bertrand competition, no asymmetry can survive with a homogeneous good.

\(^6\)Note the absence of technological spillovers in the proposed formulation. The results obtained below cannot, thus, be attributed to spillover effects.
required to ensure that second-order conditions of \( \text{firm} \) \( i \)'s maximisation problem and the Dixit (1986) stability condition are satis\-'ed.\(^7\)

Government intervention is assumed to occur at the R&D stage. No production subsidies exist. We allow for a tax on each domestic \( \text{firm} \) per unit of its R&D investment. Denote by \( \frac{\%}{\text{i}} \) 2 \( \mathbb{M} \); the tax rate. We put \( \frac{\%}{\text{i}} = 0 \) for each foreign \( \text{firm} \), assuming that foreign governments are passive. This is made for convenience as our interest lies in how asymmetries across domestic \( \text{firms} \) affect domestic industrial policy.

Firm \( i \) has a profit function given by

\[
\pi_i = \pi_i(q; x_i; \%_i) = (P - c_i)q_i - \sum_{j \in N_{nf}} \pi_{ji}q_j - \%_i x_i
\]

where \( q; x \) and \( \% \) are vectors of \( \text{firms} \)'s production quantities, research activities, and taxes, respectively.

One idiosyncratic feature of our model is the two-dimensional heterogeneity in R&D efficiency: Firms' R&D technologies may vary with respect to both R&D productivity and R&D costs. A simple reparametrization is useful to clarify the meaning of this double dimensionality. Let \( y_i = \mu x_i \) be the decision variable of each \( \text{firm} \), i.e., let \( \text{firms} \) decide on R&D output rather than R&D input. Then, \( \text{firm} \) \( i \)'s profit function can be written as:\(^8\)

\[
\pi_i = \nabla P(Q) \cdot e_i + y_i \cdot \sum_{j \in N_{nf}} \pi_{ji}q_j + \frac{y_i^A}{\mu} \cdot \pi_i
\]

where we made use of the definition of \( c_i \). Thus, we can interpret our model in a different way, stating that it reflects two different sources of heterogeneity in R&D costs: one multiplicative (given by \( 1=\mu_1 \)) and another one having any form. In particular, for some specifications, the effect of \( \mu \) will be indistinguishable from that of \( 1=\mu_1 \) (for example, \( \cdot (x_i; \mu_1) = \mu_2 x_i^2 = (\mu_1 \cdot \mu_2) y_i^2 \)). In this sense, our model comprises more standard R&D technology formulations as special cases. However, in a cost function, say, of the type

\[
\cdot = \mu_1 x_i + x_i^2 = \mu_1 y_i + \frac{1}{\mu_1} y_i^2;
\]

the two sources of heterogeneity have different implications. Having said this, let us stress that our preferred interpretation is in terms of heterogeneity in both R&D productivity and R&D costs, with R&D effort as the choice variable rather than R&D output.

Like Spencer and Brander (1983), we assume the market is abroad, so that all production of domestic \( \text{firms} \) is exported and none of the foreign \( \text{firms} \)'s production is imported. Thus, the

\(^7\)Details are provided in the appendix, available at http://ppbarros.fe.unl.pt/papers.html, or by request to the authors.

\(^8\)Omitting the tax component.
government, maximising national welfare, takes no notice of consumers' surplus and simply maximises the sum of domestic firms' profits, net of the R&D tax; i.e., the government maximises:

\[ W = \sum_{i=1}^{X} [\tilde{\pi} + \frac{3}{2}x_i] \]  

Our interest is with the following three-stage situation: In stage 1, the government decides on a vector \( (\gamma_1; \ldots; \gamma_m) \) of R&D taxes, one for each domestic firm. In stage 2, firms, domestic and foreign, choose their level of R&D activities, thus determining their costs in the subsequent production. In stage 3, finally, firms choose production quantities. We will be looking for the subgame-perfect equilibrium of this game.

3 R&D competition with firm heterogeneity

Before dealing with the international competition setting, it is useful to characterize and interpret the R&D stage competition. For this purpose, assume that only two (domestic) firms are present in the market \((m = n = 2)\). We consider the following two-stage game: First, firms decide on R&D investments; and, second, after R&D investments have been made and become common knowledge, firms decide on their production levels.

A starting question is whether initial low-cost firms perform more R&D, or not. The way to obtain an answer to this question is to assume that firm 1 has higher initial costs \( \tilde{\pi}_1 > \tilde{\pi}_2 \). Otherwise, firms are identical, i.e., \( \mu_1 = \mu_2 = \mu \) and \( \sigma_1 = \sigma_2 = \sigma \).

The solution to the second-stage problem is the following pair of quantities:

\[ q_i = \frac{\bar{a}}{3} + \mu(2x_i - x_j); \quad \bar{a} = a + 2\tilde{\pi}_1 + \tilde{\sigma}_1; \quad i, j = 1, 2; i \neq j \]  

First-stage equilibrium profits are

\[ \tilde{\pi}_i = q_i^2 - (x_i + \tilde{\pi}_i); \quad i = 1, 2 \]  

Thus, substituting by the relevant expressions, first-stage optimal R&D choices satisfy

\[ \frac{4\mu}{9} (\bar{a} + \mu(2x_i - x_j)) \frac{\partial}{\partial x_i} = 0; \quad i = 1, 2 \]  

Even if we cannot explicitly solve for \( x_i; i = 1, 2 \), without specification of a particular functional form for R&D costs, it is nonetheless possible to show the next result.\(^1\)

---

9 Note the implicit assumption of absence of a distortionary cost of public funds.
10 Details on how to prove this and many of the subsequent results in this article can be found in the appendix, available at http://pbarros.fe.unl.pt/papers.html, or by request to the authors.
Remark 1 When firms are equal, except with respect to initial costs, the initial low-cost firm does more R&D than the initial high-cost firm. Thus, the initial cost gap among firms is broadened by the activities at the R&D stage.

The simplest way to show our claim is to consider the case of identical firms \( c_1 = c_2 \), and then take an increase in \( \theta_i \) and a simultaneous decrease in \( \theta_j \) (both resulting from an increase in \( c_1 \)). As the induced changes in \( x_1 \) and \( x_2 \) keep the sign constant, a difference \( c_1 - c_2 \) can be seen as a series of infinitesimal changes starting from an initial identical position. It is easy to obtain \( dx_1 = \theta c_1 < 0 \) and \( dx_2 = \theta c_1 > 0 \), from which results \( d(x_1 - x_2) = \theta c_3 < 0 \).

The above remark shows that ex-ante asymmetries in production costs result in a higher incentive to invest in R&D by the lower cost firm. The result is not novel, but the intuition behind it will prove useful below. Suppose that no R&D effort is present. The low-cost firm produces more in equilibrium. Since R&D reduces the constant marginal cost of producing the final good, an equal marginal R&D outcome is applied to a greater mass of production by the low cost firm. Therefore, this firm has a higher marginal benefit from R&D, which leads to a higher equilibrium R&D investment and to an increase in production cost asymmetries.

To focus on the role played by R&D productivity heterogeneity, we assume next no initial asymmetry on the basic cost parameter: \( c_i = c \beta_i \). On the other hand, firms are allowed to differ in their abilities to put R&D effort to use. The assumption of a common \( c \) allows us to write equilibrium quantities produced by each firm as:

\[
q_i = \frac{\theta + 2\mu x_i + \mu x_j}{\beta_i} \quad i;j = 1;2; i \neq j
\]

where \( \theta := a - \mu c \). By differentiation in equations (10), we have

Remark 2 The following comparative statics results hold in the quantity sub-game:

\[
\frac{\partial q_i}{\partial x_i} > 0; \quad \frac{\partial q_i}{\partial \mu_i} > 0; \quad \frac{\partial q_i}{\partial x_j} < 0; \quad \frac{\partial q_i}{\partial \mu_j} < 0 \quad i;j = 1;2; i \neq j
\]

These results are intuitive ones, as they say that increases in R&D investment or in R&D productivity increase own production and reduce the other firm’s production (in equilibrium). Note that these effects should not be taken as changes in equilibrium values of the full game.

\[\text{Poyago-Theotoky (1996) obtains the same result, under a similar demand structure, a linear cost reduction function (set as a convex function of R&D effort) and quadratic R&D costs. We have a simpler R&D productivity function but a more general R&D cost function.}\]

\[\text{The implication of differences in the costs of performing a given level of R&D activity can be derived in the same way. We will refer to them along the way.}\]

\[\text{Remember that } n = m = 2. \text{ The following sections generalise this assumption.}\]
in the case of the R&D productivity parameter \( \mu \) (or \( \mu_j \)), as it is necessary to include the strategic effect through equilibrium choices of R&D efforts.

We are now ready to characterize the R&D competition stage. Equilibrium choices of R&D efforts solve the following set of first-order conditions:

\[
\frac{4}{3} \mu \left( \mu + 2 \mu x_i \mu x_j \right) \frac{\partial}{\partial \mu_i} = 0; \quad i; j = 1; 2; i \neq j
\]  

(12)

Once again, without specifying a functional form for \( \prime \), it is not possible to solve explicitly for \( x_i \); \( i = 1; 2 \). Nonetheless, the following comparative statics can be obtained.

Remark 3 The effects of changes in R&D parameters are:

\[
\frac{\partial x_i}{\partial \mu_i} > 0; \quad \frac{\partial x_i}{\partial \mu_j} < 0; \quad \frac{\partial x_i}{\partial \prime_i} < 0; \quad \frac{\partial x_i}{\partial \prime_j} > 0; \quad i; j = 1; 2; i \neq j
\]

From this remark, it is easy to obtain that \( x_1 \) \( x_2 \) is increasing in \( \mu_k \) and decreasing in \( \mu_k \). It is also straightforward to show that \( x_1 \) \( x_2 \) is increasing in \( \prime_2 \) and decreasing in \( \prime_1 \).

All these effects are, again, in line with what economic intuition predicts. Increases in productivity (or cost savings) stimulate own R&D investment and reduce investment by competitors (in equilibrium).\(^{14}\)

4 Industrial Policy Implications: The corrective tax

The discussion of firm-specific industrial policy in open economies must take into account two different concerns: first, the rivalry between domestic firms; and second, the competition with foreign firms. In order to highlight the role of rivalry among heterogeneous domestic firms, we first consider the case where no foreign firm conducts R&D activities. This assumption excludes from the model the strategic motive for intervention that arises when domestic firms' net R&D costs affect foreign firms' R&D decisions (Spencer and Brander, 1983).\(^{15}\) Later on, in Section 5, this assumption will be relaxed, so that both corrective and strategic motives are present.

Consider \( m \) domestic firms and \( n \) foreign firms, with \( x_i = 0; i \leq 2 \) \( n \leq M \), i.e. foreign firms do no R&D. In stage 3, firm \( i \)'s choice of production quantity \( q_i \) is given by the following first-order condition:

\[
\frac{\partial}{\partial q_i} = P_i q_i + \frac{\partial P_i}{\partial q_i} q_i = a_i q_i q_i q_i Q = 0
\]  

(13)

\(^{14}\)Further implications of our model of R&D competition are discussed in Barros and Nilssen (1999).

\(^{15}\)Note that there still is rent-shifting in the model: when foreign firms do no R&D, they cannot get lower costs. They therefore end up with lower market shares, and the domestic firms with higher market shares, than when foreign R&D is allowed.
Summing over all n first-order conditions and solving for the aggregate quantity, we obtain:

\[ Q = \frac{na_i P_{i2N}}{n+1} \]  

(14)

Inserting this in each rm's first-order condition, we obtain each rm's stage-3 production decision

\[ q = \frac{\Theta + n\mu x_i P_{j2M} \delta x_j}{P n + 1}; \quad i \not\in M \]

\[ q = \frac{\Theta i P_{j2M} \delta x_j}{n + 1}; \quad i \in M \]

where \( \Theta := a_i n\xi + P_{j2M} \delta x_j i \not\in M \); is assumed to be high enough so that all rms produce positive quantities in equilibrium. Differences in the basic marginal cost parameter, \( \xi \), translate into differences in \( \Theta \).

We can now proceed to second-stage equilibrium levels of R&D investment. The reduced-form profit is given by:

\[ \pi_i = q^2 \pi_i - i(x_i; \delta i) - \pi \]

(15)

Each rm's first-order condition with respect to the level of its R&D investment is:

\[ \Theta = 2q \Theta i i(x_i; \delta i) \]

(16)

This provides us with a set of conditions, from which we have:

**Remark 4** An increase in the R&D tax of rm i decreases its own R&D effort and increases that of rival j:

\[ \frac{dx_i}{\partial \pi} < 0; \quad \frac{dx_j}{\partial \pi} > 0 \]

This result can be easily seen as a particular case of the comparative statics above. A change in \( \pi \) is essentially similar to a change in the cost parameter \( \delta i \). Basic economic intuition holds in this setting. An increase in the tax of rm i induces a lower R&D effort of this rm and a higher effort of rivals.

Proceeding to the first stage, where the government chooses an R&D tax rate for each domestic rm, we recall the objective function for the government: \( W = \sum_{i \in M} (\pi_i + \pi x_i) \).

We obtain the optimal tax on domestic rm i in the following way. Suppose the government is able to choose R&D activities of each rm, \( x_i \), directly. The problem is:

\[ \max_{f x_i \in M} W = \sum_{i \in M} \pi_i (x_i; \delta i) \]

(17)
The optimal government choices solve:

$$
\frac{2}{3} \sum_{j=2}^{M} q \left( \frac{q}{q_i} \right)^{5} g_{ij} = 0; \quad i \leq M
$$

(18)

To have the government's preferred outcome implemented through a set of subsidies \( \theta q_{2M} \), the optimal subsidy structure is given by the difference between each domestic firm's first-order condition (16) and the government's first-order condition for this firm (18):

$$
\theta_i = 2 \sum_{j=2}^{M} g_{ij} \frac{q}{q_i}
$$

(19)

Since, in our model, \( g_{ij} = \mu = (n+1) \), we have:

**Proposition 1** Suppose that, in equilibrium, each domestic firm does at least some R&D. The optimal policy taxes all domestic firms. The equilibrium tax is:

$$
\theta_i = \frac{2\mu}{n+1} \sum_{j=2}^{M} g_{ij} q = \frac{2\mu}{n+1} (Q_m i q) > 0
$$

(20)

where \( Q_m \) is total production by domestic firms.

It is immediate to see that

**Corollary 1** If firms have equal R&D productivity \( \mu_f = \mu \), then those that produce more are taxed less.

To see the implications of this proposition, take the case of all firms being equal except for efficiency in the costs of doing R&D. More efficient firms will conduct more R&D, have lower costs and face a lower tax.

This proposition implies that for small productivity asymmetries across firms, more efficient firms are less penalized by the government because they are better positioned from the start (lower \( g_q \)) and/or more cost-effective in conducting R&D activities (lower \( g_{ij} \)). They are more quantity efficient in the sense that they produce more. They are, therefore, in a better position to extract rents in the foreign market. The government uses the tax to divert production to the more efficient firm.

Asymmetry of firms does not change the policy prescription of taxing firms to curtail the strategic incentive to over-invest in R&D from the point of view of the domestic government. However, it adds the insight that more quantity-efficient firms should be taxed at a lower rate.

A related question is whether all firms do R&D under the optimal tax structure (an assumption underlying the above characterization).
Proposition 2 If firms are not too quantity asymmetric, then all domestic firms perform R&D at strictly positive levels.

Proof: Substitute the equilibrium value of the subsidy in a domestic firm's first-order condition to get:
\[
2\mu_i/n + 1 \cdot \sum_{j \in M_{nf}} q_j \frac{\partial q_i}{\partial q_i} = 0 \tag{21}
\]
The term in parenthesis is positive for \( q_i = q_j \), yielding an equilibrium choice of \( x_i > 0; 8i \in M \).
By continuity, there exists \( \varepsilon > 0 \) such that \( \sum_{j \in M_{ nf}} q_j \frac{\partial q_i}{\partial q_i} > 0 \); \( 8i \), which ensures a positive investment in R&D.

From the proof of the above result, it is clear that the greater the number of foreign firms, the easier it is to fulfill the condition for positive R&D investment levels for domestic firms. Of course, if firms are sufficiently asymmetric, then some of them may not invest in R&D. For equal research productivity (\( \mu_i = \mu_j \)) the first firms to stop doing R&D are the less cost-efficient ones; and for the same R&D cost structure (\( \sigma_i = \sigma_j \)), the less productive ones in R&D will be the first ones to quit R&D activities.

A central question is, of course, how a domestic firm's R&D technology affects the R&D tax put upon it. The next proposition addresses the issue.

Proposition 3 If a firm gets more efficient in the sense of a decrease on R&D costs, then its R&D tax decreases; while if it gets more efficient in the alternative sense of an increase in R&D productivity, then the R&D tax may increase or decrease:
\[
\frac{\partial q_i}{\partial \sigma_i} > 0; \quad \frac{\partial q_i}{\partial \sigma_j} < 0; \quad \frac{\partial q_i}{\partial \mu_i} < 0; \quad \frac{\partial q_i}{\partial \mu_j} > 0 \tag{22}
\]
The surprising result in the proposition is the ambiguous effect of an increase in R&D productivity upon the firm-specific tax. The tax may increase or decrease, and this is so because two conflicting effects are present. First, there is a strategic effect: The corrective tax is higher the larger the quantity produced by rival firms. An increase in the R&D productivity of one firm leads to a reduction in domestic rivals' production. Thus, a lower tax on this firm is required. Second, there is a direct effect: A higher R&D productivity also means a stronger incentive, at the margin, for the firm to (over)invest in R&D. Thus, a heavier tax should be implemented. Taking together the two effects, an ambiguous qualitative implication results from the model.
5 Optimal taxes with foreign R&D

The assumption that foreign firms do not invest in R&D is unreasonable in many cases and it is unwarranted but for illustrative purposes. We now relax the assumption. On the other hand, we reduce the heterogeneity among firms to a minimum by dividing firms in three groups, two domestic and one foreign, with homogeneity within each group. Thus, there are three types of firms partitioned in two sets, \( M_1 \) and \( M_2 \), of domestic firms and a set \( M_3 \) of foreign firms, with \( M = M_1 \cup M_2 \) and \( M_3 = N \cap M \). Firms within each group are equal with respect to R&D costs and R&D productivity technology. Foreign firms also do R&D, and they are endowed with parameters \( (\mu_3; \delta_3) \). Domestic firms of type \( i \) are characterised by \( (\mu_i; \delta_i) \); \( i = 1, 2 \). All three types of firms have identical initial production costs, \( c \). Let \( m_i \) be the number of firms in set \( M_i \); \( i = 1, 2, 3 \).

In the first stage, the government chooses an R&D tax to apply to each domestic firm. The government’s objective function is the sum of profits and tax revenue. The existence of foreign firms doing R&D means that there is a strategic incentive for government intervention in order to affect the foreign firms’ R&D decisions (Spencer and Brander, 1983). The effect of this strategic effect is tempered, in our model, by the government’s desire to exploit the heterogeneity among the domestic firms.

The stage of production of the final good is essentially the same, rendering second-stage profits given by:

\[
\pi_i = q_i^2 \left( x_i - \delta_i \right)
\]  

where

\[
q = a_j \left[ c + (n_i - m_i + 1)\mu_i x_i - m_j \mu_j x_j - m_k \mu_k x_k \right]; \quad i;j;k = 1, 2, 3; i \neq j \neq k
\]

(24)

Profit maximisation yields the following set of first-order conditions:

\[
2q \frac{\partial q_i}{\partial \mu_i} = 0; \quad i = 1, 2, 3;
\]

(25)

From these conditions, we get the analog of Remark 3. Moreover, it is straightforward to show that cost reductions are positively related to own efficiency and negatively associated with rivals’ efficiency:

Remark 5 The effects of changes in R&D parameters are:

\[
\begin{align*}
\frac{\partial x_i}{\partial \mu_i} &> 0; \quad \frac{\partial x_i}{\partial \delta_i} < 0; \quad \frac{\partial x_i}{\partial c} > 0; \quad \frac{\partial x_i}{\partial \mu_j} < 0 \\
\frac{\partial x_i}{\partial \mu_j} &< 0; \quad \frac{\partial x_i}{\partial \delta_j} > 0; \quad \frac{\partial x_i}{\partial c} < 0; \quad \frac{\partial x_i}{\partial \mu_k} > 0
\end{align*}
\]
The optimal government choices, if it could determine each domestic firm's R&D activity directly, solve:

\[
2 \sum_{j=2}^{M} q \frac{\partial q}{\partial x_i} + 2 \sum_{j=2}^{M} q \frac{\partial q}{\partial x_g} = 0 \quad (26)
\]

To have this outcome implemented, the optimal tax must be:

\[
\frac{3}{2} \frac{\partial}{\partial x_i} = \sum_{k=2}^{M} q k \frac{\partial q}{\partial x_i} q k > 0 ; \quad i \neq j, \quad i, j \in \{1, 2, \ldots, M \} \quad (27)
\]

It remains to show that it is not optimal for the government to have only one domestic firm active in equilibrium (with taxes inducing exit of all others). This issue is similar, under our structure, to the problem of merger profitability. From this literature, it is well-known that, in the linear oligopoly with constant marginal costs and quantity-setting firms, a merger is not profitable unless it encompasses a very significant share of existing firms. Thus, assuming that firms are not too heterogeneous and that the number of foreign firms is high enough, the above tax does characterise the optimal tax structure.

Making the relevant substitutions we can write the optimal tax, for the two types of domestic firms, as

\[
\frac{3}{2} \frac{\partial}{\partial x_i} = \frac{1}{2} \left( \frac{m_1 q_1 + m_2 q_2}{2} \right) > 0 ; \quad (29)
\]

and it is designed to internalise the effect of one domestic firm doing R&D on the profits of the other domestic firms. Since more R&D means lower costs in the final production stage, the firm is a tougher competitor. The cross-effect among domestic firms is negative, which justifies why a government that maximises industry profits has an interest in taxing R&D activities.

The second term in the tax structure is:

\[
\frac{3}{2} \frac{\partial}{\partial x_i} = \frac{1}{2} \left( m_1 q_1 + m_2 q_2 \right) < 0 \quad (30)
\]

and it constitutes the strategic incentive of governments to subsidise domestic R&D efforts. Increasing R&D by a domestic firm induces lower R&D spending by the foreign firms, which benefits all domestic firms.

\[\text{---}^{16}\text{See Salant et al. (1983).} \]
This decomposition into corrective and strategic components shows that the optimal tax can be positive or negative, depending on the relative strength of these two opposite forces, a result in line with the analysis of Dixit (1984) and others on multi¬rm subsidies.

We look now at the possibly different ways domestic ¬rm are treated by the tailor-made industrial policy set by the government. The difference in tax rates among the two types of domestic ¬rms is:

\[
\frac{\frac{3\delta}{\alpha}}{\frac{3\delta}{\alpha}} = 2 \frac{\mu_2 \frac{\partial^2 q_2}{\partial x_1} i q_1 \frac{\partial^2 q_1}{\partial x_2} q_2 \frac{\partial^2 q_1}{\partial x_3}}{\frac{\partial^2 q_2}{\partial x_2} q_1 \frac{\partial^2 q_1}{\partial x_3} + \frac{\partial^2 q_2}{\partial x_2} q_2 \frac{\partial^2 q_1}{\partial x_3} + \frac{\partial^2 q_2}{\partial x_2} q_1 \frac{\partial^2 q_1}{\partial x_3} + \frac{\partial^2 q_2}{\partial x_2} q_2 \frac{\partial^2 q_1}{\partial x_3} + \frac{\partial^2 q_2}{\partial x_2} q_1 \frac{\partial^2 q_1}{\partial x_3} + \frac{\partial^2 q_2}{\partial x_2} q_2 \frac{\partial^2 q_1}{\partial x_3} (31)
\]

Again, it is useful to look separately at the corrective and strategic components of the optimal tax. Take first the difference due to the use of the tax structure for corrective purposes: In order to compare different ¬rs' tax rates, we define as the difference between two ¬rs' corrective tax components. Inserting the results of Section 4 in (31), we find:

\[
\delta := \frac{2Q}{n+1} (\mu_1 i \mu_2) + \frac{2}{n+1} (\mu_2 q_2 i \mu_1 q_1)
\]

For \(\mu_1 = \mu_2\); \(\delta > 0\) if \(q_2 < q_1\), which is the result of lower R&D costs or lower initial costs of ¬rm 2. If, on the other hand, the only difference across ¬rs is on R&D productivity, there is an ambiguity: By doing less R&D, the more R&D productive ¬rm may still have a lower marginal cost of production, and consequently a greater production volume. The lower R&D productivity runs in favour of a smaller tax, but a lower quantity is associated with a lower tax for other ¬rs (the externality imposed by other ¬rs is smaller). Therefore, the evolution of the relative tax is ambiguous. Heterogeneity in R&D costs and heterogeneity in R&D productivity may have different implications for the optimal corrective tax imposed by the government.

A decrease in R&D costs always implies a decrease in the respective corrective tax. The effect works through the optimal choice of R&D. As costs of doing R&D decrease, a ¬rm will increase its investment in R&D activities. This makes the ¬rm relatively more efficient, which in turn makes it more attractive for the government to decrease its tax and divert production to this more efficient ¬rm.

The same effect operates when a ¬rm becomes more R&D productive. If the ¬rm is more R&D productive, it will increase R&D efforts, giving rise to the effects previously described. The effect is, however, combined with the direct impact of R&D on the level of marginal costs of production. Even if R&D effort remains constant, an increase in R&D productivity entails a production cost reduction, which giving an incentive to the government to decrease the tax on this ¬rm, as it becomes a more efficient producer.
Consider now the strategic part of the tax. By construction, the linearity of the model in the quantity stage results in
\[
\frac{\partial g}{\partial \mu_1 x_1} = \frac{\partial g}{\partial \mu_2 x_2}; \quad g \geq M_3
\] (33)

Thus, we can write the strategic part of (31) as:
\[
\Delta = m_1 q_1 \frac{\partial g}{\partial \mu_1} + m_2 q_2 \frac{\partial g}{\partial \mu_2} (\mu_1 - \mu_2) \frac{\partial g}{\partial \mu_2 x_2} m_3
\] (34)

which is negative for \( \mu_1 > \mu_2 \).

Therefore, the firm with the higher R&D productivity receives a higher subsidy according to this effect. The reason is that a higher \( \mu \) also implies a relative efficiency of this firm in rent shifting. Consequently, the firm endowed with a higher \( \mu \) is used in a more intense way by the government for that purpose. On the other hand, differences in R&D costs alone are not sufficient to induce differential treatment of domestic firms. Again there is a difference: Heterogeneity in R&D costs does not give rise to differences in the strategic R&D tax, while heterogeneity in R&D productivity does.

Taking the two effects together, if a firm is more efficient in both productivity and costs than the other, it has a higher subsidy. However, there is an indeterminacy if we cannot order firms in terms of the two efficiency characteristics.

The definition of the policy instrument as a value per unit of R&D effort is not the only one possible. A different tax structure could be defined in relation to R&D output, defined as the achieved cost reduction. Under a tax/subsidy definition based on R&D output a firm producing a higher quantity faces a lower tax. Define a tax \( \tilde{\omega} \) as proportional to \( \mu x_i \), thus
\[
\tilde{\omega}_i = \mu x_i
\] (35)

In this case, the difference between the two groups of domestic firms in the corrective tax is:
\[
\tilde{\omega}_1 - \tilde{\omega}_2 = \frac{2}{n+1} (q_2 - q_1) \tag{36}
\]

With equal initial costs of production of the final good, quantities are directly related to R&D output, so that \( q_1 < q_2 \) if and only if \( \mu_1 x_1 < \mu_2 x_2 \). Thus, from expression (36):
\[
\tilde{\omega}_1 > \tilde{\omega}_2 \text{ if } \mu_1 x_1 < \mu_2 x_2 \tag{37}
\]

The strategic part of \( \tilde{\omega}_i \) is equal for both firms, as the focus on the output of R&D activities already corrects for the relative efficiency of domestic firms in rent shifting. Thus, in this
special specification of the tax, the ex-post more efficient firm receives the lower tax. It may, or may not, correspond to a higher level of R&D effort. The ranking of firms according to R&D effort ($x_i > x_j$) may not be identical to that based on R&D output ($\mu x_i \gg \mu x_j$). One firm can do less R&D than the other and still obtain a higher R&D output due to differences in R&D productivity, as long as no clear ranking, in terms of the two efficiency parameters, across domestic firms exists.

### 6 Final remarks

The optimal government intervention faces two conflicting forces. First, there is the strategic incentive to profit shifting of Spencer and Brander (1983), which prescribes a subsidy to R&D activities of domestic firms. Second, there is an incentive to correct the negative impact of one domestic firm's R&D on the other through imposition of a tax. The strategic subsidy is larger for the more R&D efficient firm, while the corrective tax is lower for such a firm. Therefore, efficient firms receive a more favorable tax treatment. This is so because (a) they are relatively more successful in shifting profits from foreign firms; and (b) they impose a smaller external effect upon other domestic firms.

There is, however, an indeterminacy if heterogeneous firms cannot be ranked in terms of efficiency characteristics. The indeterminacy is resolved if the tax is defined in terms of R&D output, rather than effort. In this case, the tax automatically compensates for differences in R&D productivity.

The present analysis shows that firm heterogeneity has a complex way of affecting the optimum industrial policy when firm-specific instruments are available. In particular, a firm with a high R&D productivity may or may not be taxed more. On the other hand, differences in R&D costs do not affect the strategic component of government intervention.

Because of the ambiguities we point out in our analysis, it is not clear, in general, how differences in R&D technology transform into differences in the government's rm-specific R&D policy. The formulae that we produce in the ensuing analysis may give the impression that there is a way out of this complexity. It is necessary to stress, however, that we do our analysis throughout with the assumption that the government has complete information. When firms are heterogeneous and the policy is rm-specific, the government has a formidable task to pick winners. The informational requirements needed to fine-tune such a policy seem to be quite strong, as no robust prediction emerges. Therefore, we think it still may be wise to adhere to the advice of Nelson (1982), Stoneman (1987), and others, that picking winners
is rarely successful. Our modest contribution is that, even if the information problem can be overcome, firm heterogeneity makes the link between firm characteristics and the optimal firm-specific R&D policy a complex one.

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