Optimal Severance Pay in a Matching Model

Giulio Fella*

Queen Mary, University of London, Mile End Road, London E1 4NS, UK

Abstract

This paper uses an equilibrium matching framework to study jointly the optimal private provision of severance pay and the allocational and welfare consequences of government intervention in excess of private arrangements. Firms insure risk-averse workers by means of simple explicit employment contracts. Contracts can be renegotiated ex post by mutual consent. It is shown that the privately optimal severance payment is bounded below by the fall in lifetime wealth associated with job loss. Simulations show that, despite contract incompleteness, legislated dismissal costs largely in excess of such private optimum are effectively undone by renegotiation and have only a small allocational effect. Welfare falls. Yet, for deviations from laissez faire in line with those observed for most OECD countries, the welfare loss is small.

JEL classification: J23, J64, J65.

Keywords: Severance pay, contracts, renegotiation.

*E-mail: g.fella@qmul.ac.uk The idea for this paper was born out of conversation with Giuseppe Bertola to whom I am most grateful. I am also indebted to Fabrizio Zilibotti (the editor), an anonymous coeditor and two referees, Paola Manzini, Ioana Marinescu, Julien Prat, Christopher Tyson, and to seminar participants at the IIES and Pompeu Fabra. Steve Nickell kindly made available the data on institutions and worker flows for OECD countries. The IIES provided generous hospitality while working on this paper.
1 Introduction

Employment contracts often contain explicit severance payments provisions\(^1\). Furthermore, in many countries minimum levels of severance payments and other forms of employment protection are enshrined in legislation. The existence of such measures is difficult to understand in the light of standard labour market models in which homogeneous\(^2\) workers maximise expected labour income and wages are perfectly flexible.

From a general equilibrium perspective, risk-neutral behaviour requires perfect insurance or complete asset markets. Together with wage flexibility and unconstrained side-payments, perfect insurance implies that any spillover between a worker and her current employer is internalised and the market equilibrium is constrained efficient. As pointed out by Lazear (1990), employment protection measures have no useful role to play in such environment and there is no reason why a firm which takes aggregate quantities as given should offer them. In brief, it is hard for models based on risk-neutral labour market behaviour to provide a role for job security measures when wages can adjust freely. As argued in Pissarides (2001), this implies that “...much of the debate about employment protection has been conducted within a framework that is not suitable for a proper evaluation of its role in modern labour markets.”

This paper studies the optimal private provision of one form of employment protection, severance pay, in an environment in which it plays an economic role as risk-averse workers can only imperfectly insure against idiosyncratic labour income shocks. This optimal contracting problem is cast within Mortensen and Pissarides’s (1994) equilibrium matching model. Using an equilibrium framework, the paper can explore jointly the privately optimal size of severance pay and the allocational and welfare effects of a mandated discipline which deviates from it.

\(^{1}\)For the US, Bishow and Parsons (2004) document that, over the period 1980-2001, roughly 40 per cent of workers in establishments with more than 100 employees, and 20 per cent in establishments below such threshold, were covered by severance payment clauses. For the UK, the 1990 Workplace Industrial Relations Survey reveals that 51 per cent of union companies bargain over the size of non-statutory severance pay for non-manual workers and 42 per cent for manual workers (Millward et al. 1992). Even for Spain, a country usually associated with high level of state-mandated employment protection, Lorences et al. (1995) document that between 8 and 100 per cent of collective agreements in a given sector establish levels of severance pay in excess of legislated measures.

\(^{2}\)See Fella (2005) for a model with heterogeneous workers in which consensual termination restrictions increase firms’ investment in the general training of unskilled workers.
The two key features of this exercise are: (i) simple explicit contracts, and (ii) renegotiation by mutual consent.

Feature (i) rules out reputation-based complete implicit contracts and ensures that excessive mandated severance pay is non-neutral. This would not be the case with risk-neutral firms and complete contracting, as the latter would be a substitute for complete insurance markets. Excessive severance pay legislation would also be undone by a simple intertemporal contract mandating that workers rebated to firms the excess of the legislated termination pay over its privately optimal level. Since courts are unlikely to enforce contracts aimed at circumventing legislation, though, such an arrangement would be feasible only if supported by a self-enforcing implicit agreement. Yet the arrangement cannot be self-enforcing as a worker about to be fired would have no ex post incentive to honour such an ex ante pledge.\(^3\)

While feature (i) stacks the odds in favour of non-neutrality, feature (ii) imposes the natural, joint-rationality constraint that a firm-worker pair do not leave money on the table if they can avoid it. It allows the parties to potentially circumvent legislation, if there are mutual gains from doing so, but only by means of ex post, spot side payments. Since such ex post side payments are state-dependent, insurance is possibly imperfect and excessive mandated severance pay is a priori non-neutral.

The paper establishes a lower bound for the optimal severance payment size. This equals the fall in lifetime wealth associated with job loss. Hence, job security in the form of positive redundancy pay is part of an optimal contract whenever workers enjoy positive rents. Positive workers’ rents imply costly mobility and call for insurance against job loss.

By yielding a closed-form lower bound for the optimal severance pay the model provides a metric against which to assess the extent to which observed legislated measures are excessive. Such a metric is used to construct a series for the lower bound on optimal severance pay for a sample of OECD countries and compare it to the corresponding series for legislated payments. It turns out that for a large proportion of these countries mandated payments do not significantly exceed, and are often significantly lower than, their optimal lower bound. Even for those countries for which this is not the case, the observed

\(^3\)Privately negotiated severance payment are also unenforceable through reputation alone in the standard matching framework with anonymity in which a firm coincides with one job and, when a job becomes unprofitable, there are no third parties that can punish a firm that reneges on an implicit contract.
deviation from the private optimum is inconsistent with quantitatively important changes in the allocation of labour in the light of the model’s numerical results. Therefore, the model implies a direction of causation from factors which generate high workers’ rents and unemployment duration to high severance pay but rules out the reverse. The same causation also goes from low unemployment benefits to large severance payments, coeteris paribus.

Despite their a priori non-neutrality, legislated severance payments above private optima have small allocational effects. The reason is that a legislated severance payment in excess of the private optimum just determines the maximum transfer in case of separation. In equilibrium, the firm pays it only if the productivity shock is so low that the firm cannot credibly threat to continue the match at the contract wage. If the productivity realization is not so negative, yet below its reservation value, the parties agree to label the separation a quit and exchange a lower severance payment which equals the firm’s present value of profits at the contract wage and current productivity realization. This is Pareto optimal as it makes the worker strictly better off and leaves the firm indifferent between continuation and separation. As the legislated severance payment is renegotiated when the marginal job is destroyed it has only a minor, general equilibrium, impact on the reservation productivity and the job destruction rate. The wage component of the contract falls to rebalance the parties’ respective shares of the surplus from a new match.

While the allocation of labour is hardly affected, very large deviations from the private optimum may have considerable negative effects on workers’ welfare as, by overinsuring against job loss, they increase income fluctuation relative to laissez-faire. Yet, for only two countries in our dataset are observed deviations large enough to imply an upper bound on the welfare loss equal to a third of a percentage point fall.

The model is related to a number of papers in the literature. MacLeod and Malcolmson (1993) is the closest antecedent to the contracting framework studied in the paper. In a risk-neutral framework they show how incomplete contracts of the fixed price and severance payment variety can solve the hold up problem, as they are infrequently renegotiated. Severance payments reduce the probability of renegotiation of the fixed-price component of the contract. This paper applies MacLeod and Malcolmson’s insight about the infrequent renegotiation of simple, explicit, fixed-price contracts to the optimal pri-
vate provision of insurance. This contrasts with the implicit contract literature pioneered by Azariadis (1975) and Baily (1974). That literature was mainly concerned with establishing minimal restrictions on contracts or information that could generate a deviation from the first-best, full-insurance outcome and a trade-off between risk sharing and productive efficiency. By assuming that reputational considerations ruled out firm-initiated renegotiation of implicit agreements that literature resolved the trade-off in favour of risk sharing. Instead, by allowing for renegotiation by mutual consent our paper emphasises the constraint that ex post efficiency imposes on insurance provision by means of simple, explicit contracts.

Recently, Alvarez and Veracierto (2001), Bertola (2004) and Pissarides (2004) have explored the role of employment protection within a fully dynamic framework with risk-averse workers. Alvarez and Veracierto (2001) show that exogenously-imposed severance payments can have large positive effects on employment and welfare in a model with costly frictions and self-insurance. Bertola (2004) shows, within a competitive equilibrium environment, that collectively administered income transfers may improve welfare and efficiency by reducing the consumption fluctuation associated with job mobility. Both papers do not allow for optimal private contracts. We show that allowing for optimal private contracting implies there is no welfare-improving role for legislated employment protection. Yet, Pareto optimal renegotiation implies that the allocational effects and welfare costs of excessive government intervention are small.

Pissarides (2004) shows that optimal private contracts feature severance pay and, possibly, advance notice. Being partial equilibrium though, his model cannot address the allocational effects of excessive government intervention. On the other hand, contrary to this paper, Pissarides (2004) allows for dismissal delays (advance notice). He shows that, as long as state-provided unemployment insurance is low enough for it not to make it worthwhile for the parties to take advantage of such third-party income transfer, dismissal delays provide additional (imperfect) insurance against the uncertain length of unemployment spells at a lower cost to the firm than severance pay.

A related literature studies the optimal size and time path of unemployment benefits in search and matching models with risk-averse workers. For tractability, it studies environment in which severance pay has little or no role. Acemoglu and Shimer (1999)
show that positive unemployment benefits increase efficiency and welfare relative to *laissez faire* in a directed search model without job loss. The matching models with wage bargaining and hand-to-mouth consumers of Cahuc and Lehmann (2000), Fredriksson and Holmlund (2001) and Coles and Masters (2006) also imply that the optimal size of unemployment benefits is strictly positive.

Finally, Blanchard and Tirole (2005) study the optimal joint design of unemployment insurance and employment protection in a static, partial-equilibrium setup. Because the model is static, it blurs the distinction between severance pay and unemployment benefits and the analysis emphasises the optimal financing of benefits by means of layoff taxes.

Common to all these papers is the result that, in a dynamic context, moral hazard implies that efficient and/or optimal insurance by means of unemployment benefits is imperfect and job loss costly. This paper shows that severance pay complements unemployment insurance and derives a lower bound for the optimal severance payment as a function of unemployment duration and benefits. It shows that costly job loss calls for positive severance pay. The same insight underpinning Acemoglu and Shimer (1999) also implies that severance payments are not a perfect substitute for unemployment benefits either. We show that productive efficiency still requires the latter to be positive.

The paper is structured as follows. Section 2 introduces the economic environment. Section 3 derives the equilibrium of the renegotiation game and derives the agents’ Bellman equation. Section 4 characterises the optimal contract. Section 5 calibrates the model and derives empirical implications. Section 6 considers some extensions and Section 7 concludes. All proofs are in Appendix A.1.

## 2 Environment

### 2.1 Description

Time is continuous and the horizon infinite. The economy is composed by an endogenous number of risk-neutral establishments (or firms) and a unit mass of risk-averse workers with infinite lifetimes. Workers are endowed with an indivisible unit of labour and
maximise the present value of utility from consumption

\[ \mathbb{E} \int_t^\infty u(c_s) e^{-\phi(s-t)} ds \]  

where \( \mathbb{E} \) is the expectation operator conditional on the information set at time \( t \), \( \phi \) is the subjective discount rate, \( c_s \) is consumption at time \( s \) and \( u(\cdot) \) is the increasing and strictly concave felicity function.

There are no insurance markets, but agents can self-insure by investing in the only, riskless, asset available. Therefore, workers’ maximisation problem is subject to the dynamic budget identity

\[ da_t = (ra_t + z_t - c_t) dt, \]  

where \( r \) is the exogenous riskless rate, \( a_t \) the stock of wealth and \( z_t \) is the net-of-tax flow of non-capital income. Disposable non-capital income \( z_t \) equals the wage \( w_t \) for an employed worker and the unemployment benefit \( b \) for an unemployed one. Borrowing is subject to a solvency constraint which will be specified case-by-case.

In what follows it assumed \( r = \phi \). Hence, if markets were complete, workers would choose a flat consumption profile.

Firms maximize the expected present value of profits discounted at the market interest rate. Each establishment requires one worker in order to produce. Because of search frictions, it takes time for a firm with a vacant position to find a worker. Such frictions are captured by a constant returns to scale, strictly concave, matching technology \( M(U_t, V_t) \), where \( U_t \) is the number of unemployed workers and \( V_t \) the number of vacancies. With constant returns instantaneous matching rates depend only on market tightness \( \theta_t = V_t/U_t \). Contact rates are denoted \( q(\theta_t) = M(U_t, V_t)/V_t \), for vacant firms, and \( p(\theta_t) = M(U_t, V_t)/U_t \), for unemployed workers.

Keeping an open vacancy entails a flow cost \( m > 0 \). If a firm and worker meet and form a match, they negotiate an initial contract. At time \( t_0 \), when the contract is signed, the worker starts producing a unit flow of output. At any time \( t > t_0 \), the job may be hit by a shock with instantaneous probability \( \lambda \) and the parties decide, after observing the productivity realization, whether to continue or end the match and on which terms.
Following a shock the match-specific value of productivity takes a new value\(^4\) \(y\), with \(y\) distributed according to a time-invariant, continuous cumulative density function \(G(y)\) with support \(Y = [y_l, 1]\).

A worker who becomes unemployed receives a net-of-tax flow of unemployment benefits \(b\) independently from the reason for separation. We assume \(b < 1\) to ensure a non-degenerate equilibrium with positive employment exists. As in Acemoglu and Shimer (1999), benefits are assumed to be financed by a lump-sum tax \(\tau\). The unemployment benefit fund is balanced at all times.

The paper focuses on simple, realistic employment contracts featuring state-independent wages and termination pay. Namely, we assume that a long-term, initial contract \(\sigma = (w, F)\) only specifies a, post-tax, wage \(w\) in case production takes place and a layoff payment \(F\) from the firm to the worker in case of layoff\(^5\).

Crucially it is assumed that termination payments can be conditioned on who takes verifiable steps to end the relationship. A separation is deemed a dismissal if and only if the firm gives the worker written notice that it no longer wishes to continue the employment relationship. The end of the relationship is deemed a quit if the worker gives written notice that she no longer intends to continue in employment\(^6\). That is, neither party can claim the counterpart has unilaterally severed the relationship unless they can produce a written document, signed by the other party, proving their claim. This seems broadly consistent with existing practices in most countries. A separation is consensual if both parties sign a written document stating their agreement to terminate the relationship and exchange any termination payment specified in the document. Until one of these actions is taken the employment relationship is considered in existence.

At any time the parties can renegotiate the terms of the current contract \((w, F)\). This ensures that mutual gains which are not exhausted by the ex ante contract can be reaped ex post. If the initial contract is renegotiated, there are two possibilities. Either the contract wage is renegotiated and the match continues or the parties agree to renegotiate

\[^4\]The assumption that new jobs are created at the top of the productivity distribution is without loss of generality. What matters is that a new match has positive surplus.

\[^5\]This is broadly consistent with the form of observed labour contracts. Proposition 5 shows that even such a simple contract delivers full insurance in the benchmark economy.

\[^6\]Alternatively, not showing up for work without providing a medical certificate could be interpreted as a signal that the worker has quit.
the severance payment and separate.

We allow for the possibility that the government mandates a minimum layoff payment \( F_m \). Such a minimum standard imposes a constraint \( F \geq F_m \) on the contracted layoff payment \( F \), since a contract in breach of existing legislation would not be upheld in court. Although the mandated minimum constraints \emph{ex ante} contracting, it does not prevent a firm-worker pair from negotiating a lower \emph{spot} side payment upon separation if doing so is Pareto optimal. The parties can achieve this in two equivalent ways. They can label the separation a quit or a voluntary redundancy rather than a layoff, in which case transfers between them are unconstrained by legislation. Alternatively, they can label the separation a layoff with the worker rebating to the firm, on the spot, the difference between the legislated payment \( F \) and the ex post Pareto optimal one.

We restrict attention to stationary equilibria and drop time indices in what follows.

3 Contracts and renegotiation

In order to solve for the optimal contract, one has to work backwards from the moment a contract is already in place.

In what follows we denote by \( W_u(a) \) the lifetime expected utility of a worker entering unemployment as a function of her stock of assets \( a \). \( W_u \) is assumed continuous and increasing, as it is indeed the case in equilibrium.

3.1 Contract renegotiation

After the parties match and a contract is signed at time \( t_0 \), the parties play an infinite horizon renegotiation game along the lines of MacLeod and Malcolmson (1993). The game is illustrated in Figure 1.

The first offer of renegotiation is made at \( t_0 \) and subsequent offers follow at intervals of finite length \( \Delta \). Let \( \Omega_w, \Omega_F \subset \mathbb{R} \) denote respectively the set of possible wage and severance-pay offers and \( S = Y \times \Omega_w \times \Omega_F \times \mathbb{R} \) the state space. The two sets \( \Omega_w, \Omega_F \) are assumed to be continuous and bounded. There is a potentially an infinite number of bargaining rounds, each of them characterized by the following sequence of moves.
Figure 1: Renegotiation game

(n.1) Given the current state \( s = (y, w, F, a) \in S \), the worker chooses one of the following two types of action: 1) proposing to produce at a wage \( w_n \in \Omega_w \); 2) proposing to separate with a side payment \( F_n \in \Omega_F \).

(n.2) Given the state and the worker’s choice of action, the firm chooses among the following three actions: 1) laying the worker off; 2) accepting the worker’s proposal; 3) rejecting the worker’s proposal.

If it lays off the worker the game ends and the firm has to pay the contractual severance payment\(^7\). Its payoff is \(-F\) and the worker’s is \(W_u(a + F)\).

If \( F_n \) is proposed at n.1 and the firm accepts, the game ends and the firm and worker obtain respectively payoffs \(-F_n\) and \(W_u(a + F_n)\).

If \( w_n \) has been proposed at n.1 and the firm accepts, the wage component of the contract transits to \( w' = w_n \). If instead the firm rejects either a wage or a severance pay proposal, the contract is unchanged and \( w' = w \). Trade takes place in the current round at the prevailing contract wage \( w' \) for a time interval of length of time \( \Delta \), generating instantaneous income flows \((y - w')\Delta\) and \(w'\Delta\) for the firm and worker respectively. The worker chooses her optimal consumption level \( \hat{c}(y, w', F, a) \). At the end of \( \Delta \), the game moves to n.3.

(n.3) With probability \( \lambda \Delta \) a new realization \( \tilde{y} \) is drawn from \([y_l, 1]\) and the match pro-

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\(^7\)Since the initial contract satisfies any legislated lower bound by assumption, it is a sufficient statistics for the severance payment in case of unilateral layoff.
ductivity transits to $y' = \tilde{y}$. With probability $1 - \lambda \Delta$ the match productivity is unchanged; i.e. $y' = y$. The game moves to stage $n+1.1$ characterized by $(y', w', F, a')$, with $a' = a + (ra + w' - \tilde{c}) \Delta$.

This extensive form is meant to capture the following three aspects. First, the insight of MacLeod and Malcomson (1993) that if trade takes place over time, rather than at a fixed date, simple fixed-price contracts are not necessarily renegotiated. If trade under the terms of the current contract is profitable for both parties, refusing to revise the contract is a credible threat for the party who opposes renegotiation. This is captured by the fact that trade takes place at the current contract wage unless the match ends or the contract is renegotiated\(^8\). Second, the threat to refuse renegotiation is constrained by a party’s option to unilaterally end the match. The threat to end the match, when credible, limits a fixed-price contract ability to provide insurance against productivity fluctuations in case the match continues. Third, the parties can renegotiate existing arrangement when this is Pareto optimal.

The renegotiation game above is a stochastic bargaining game. Merlo and Wilson (1995) derive a sufficient condition for a stochastic, alternating offer bargaining game to have unique stationary equilibrium payoffs. Such condition is violated if agents are risk-averse. Removing the alternating offer assumption, by giving the worker all the bargaining power, is sufficient to guarantee uniqueness of payoffs\(^9\).

The equilibrium concept used is stationary subgame perfect equilibrium (SSP) in pure strategies. A strategy profile (a payoff profile) is pair of strategies (payoffs), one for each player. A subgame perfect equilibrium is a strategy profile such that no player can benefit from deviating from her strategy at any stage. A strategy profile is stationary if it depends only on the current state and offer. A strategy profile is SSP if it is stationary and subgame perfect. It follows that a SSP payoff profile is also stationary.

We now show that SSP payoffs can be characterized in terms of the solution to a

\(^8\) It would be straightforward to allow the parties to choose optimally whether to trade or not at the prevailing wage in case the match survives. If lockouts are illegal and the current contract wage exceeds the disutility of labour (zero in this case) trade always takes place if the match survives. Lockouts are indeed illegal in a number of countries. Furthermore, if legal lockouts destroyed insurance with positive probability by allowing the firm to renegotiate the contract, the parties could negotiate a Pareto improving clause ruling them out.

\(^9\) As it turns out, Proposition 5 shows that giving all bargaining power to the worker is without loss of generality in the absence of government intervention as payoffs are always determined by outside options.
recursive optimization problem. Let $\beta = 1 - r\Delta$ denote the discount factor over a time interval $\Delta$ and let $\mathbb{E}$ denote the expectation operator over the future realization of $y'$ conditional on its current value $y$; i.e. given a generic function $h(y')$ it is $\mathbb{E}h(y') = (1 - \lambda\Delta)h(y) + \lambda\Delta \int h(\tilde{y})dG(\tilde{y})$. Consider the following optimization problem with time evolving in discrete intervals of length $\Delta$.

$$W_{t}(y, w, F, a) = \max_{j \in \{0, 1\}} \left[ (1 - j)W^{u}(a + \hat{F}) + jW^{t}(y, \hat{w}, F, a) \right]$$  \quad (3)$$

$$s.t. -(1 - j)\hat{F} + jJ^{t}(y, \hat{w}, F, a) \geq \max\{-F, J^{t}(y, w, F, a)\}, \quad (4)$$

with

$$W^{t}(y, w, F, a) = \max_{c^{t}} u(c^{t})\Delta + \beta\mathbb{E}W^{e}(y', w, F, a')$$  \quad (5)$$

$$s.t. a' = a + (ra + w - c^{t})\Delta \quad (6)$$

and

$$J^{t}(y, w, F, a) = (y - w - \tau)\Delta + \beta\mathbb{E}J^{e}(y', w, F, a'). \quad (7)$$

$$J^{e}(y, w, F, a) = -(1 - j)\hat{F} + jJ^{t}(y, \hat{w}, F, a). \quad (8)$$

Equations (5)-(6) characterize the worker’s value function $W^{t}$ conditional on trade taking place in the current period. It equals the flow of utility from trading at the prevailing contract wage $w$ plus the expectation of the continuation payoff $W^{e}$ at the beginning of the next period. Correspondingly, equation (7) characterizes the firm value function $J^{t}$ with the caveat that the relevant wage for the firm is the pre-tax wage $w + \tau$.

In terms of the renegotiation game in Figure 1, $W^{t}$ and $J^{t}$ are the respective payoffs at stage n.2 conditionally on trade taking place at the prevailing wage. The contract $(w, F)$ is unchanged between the moment trade takes place and the beginning of the next period.

Consider now the worker’s optimization problem after the current productivity is drawn; i.e. at stage n.1 in Figure 1. The problem is characterized by equations (3)-(4). The worker can either propose to separate - $j = 0$ - with some side payment $\hat{F}$ or to trade - $j = 1$ - at some wage $\hat{w}$. If the worker’s proposal to separate is accepted the worker enters unemployment with wealth $a + \hat{F}$ and payoff $W^{u}(a + \hat{F})$. If the worker’s proposal
of some wage \( \hat{w} \) is accepted, \( \hat{w} \) becomes the current contract wage at which trade takes place in the current round. The associated worker’s payoff is \( W'(y, \hat{w}, F, a) \).

Equation (3) assumes that a worker’s proposal is accepted. This is the case if constraint (4), which requires that a proposal gives the firm its reservation payoff, is satisfied. The right hand side of equation (4) is the firm reservation payoff. The firm can secure a payoff of \(-F\) by paying the contractual severance payment and unilaterally firing the worker. Alternatively, it can obtain a payoff \(J'(y, w, F, a)\) by rejecting whatever worker’s proposal, in which case trade takes place in the current round at the unchanged contract wage \( w \). Therefore, if the worker proposes to separate - \( j = 0 \) - the associated firm payoff \(-\hat{F}\) must satisfy \(-\hat{F} \geq \max\{-F, J'(y, w, F, a)\}\). If the worker proposes to trade - \( j = 1 \) - the associated wage \( \hat{w} \) must give the firm a payoff \(J'(y, \hat{w}, F, a) \geq \max\{-F, J'(y, w, F, a)\}\). Equation (8) follows.

The following proposition establishes the equivalence between the value functions that solve the optimization problem (3)-(8) and the SSP payoffs of the renegotiation game.

**Proposition 1.** Let \( s \) and \( \Delta \) be given. A pair of functions \( W'(s), J'(s) \) is a SSP payoff profile for the renegotiation game if and only if it satisfies the system (3)-(8) with (4) holding as an equality.

The worker extracts all the surplus from the firm, as one would expect given that she is the only proposer.

The proposition also implies that a SSP strategy profile induces a stationary payoff profile which satisfies (3)-(8). Therefore, an equilibrium profile also induces a triplet of functions \((\hat{w}(s), \hat{F}(s), j(s))\) which, given the state, prescribes the outcome - trade, and at which contract wage, or separate, and with which severance payment - supporting such payoffs. We call such a triplet a SSP outcome.

We can now prove that the equilibrium outcome and payoffs are unique.

**Proposition 2.** Given \( s \) and \( \Delta \), the renegotiation game has a unique SSP outcome and payoff profile.

Finally, the following proposition characterizes the solution to system (3)-(8) in the limit as bargaining frictions become negligible.
Proposition 3. Let $s$ be given. As the interval between offers goes to zero ($\Delta \to 0$), the unique SSP payoff profile and outcome converge to

$$J^e(y, w, F) = \max \left\{ -F, \frac{y - w - \tau + \lambda \int_y^1 J^e(y', w, F) dG}{r + \lambda} \right\}, \quad (9)$$

$$W^e(y, w, F, a) = \max_{j \in \{0,1\}} (1 - j)W^u(a + \hat{F}) + jW^t(\hat{w}, F, a), \quad (10)$$

with

$$W^t(w, F, a) = \max_{c_t} u(c_t) + (ra + w - c_t)W^t_a + \lambda \int_y^1 W^e(y', w, F, a) dG \frac{1}{r + \lambda}, \quad (11)$$

and $\hat{F}(s) = -J^e(y, w, F)$, $\hat{w}(s) = \min\{w, \bar{w}(y, F)\}$,

$$\bar{w}(y, F) = y - \tau + rF + \lambda \int_y^1 \frac{1 - G(y)}{r + \lambda} dy. \quad (12)$$

The system of equations (9)-(11) is just the continuous-time limit, and compacted, counterpart of the corresponding system (3)-(8). The latter system is recursive with equations (7) and (8) alone determining the function $J^e$. Since neither equation contains worker’s wealth $a$, $J^e$ is independent of $a$. Equation (9) obtains from equations (7) and (8) and just restates that in the unique equilibrium the firm receives its reservation payoff.

It follows that if the match continues the equilibrium wage $\hat{w}$ equals the lower between the current contract wage $w$ and the firm’s reservation wage $\bar{w}(y, F)$ in equation (12). This is the wage that equates the two terms inside the maximum operator in equation (9). The associated value $W^t(\hat{w}, F, a)$ for the worker’s value function, in equation (10), is the expected utility from continuing the match at the new equilibrium contract wage $\hat{w}(s)$.

Similar reasoning applies to the determination of equilibrium severance payment $\hat{F}(s)$. Equation (10) characterizes the, Pareto optimal, separation decision given $\hat{F}$ and $\hat{w}$.

Finally, equation (11) is the Hamilton-Jacobi-Bellman equation for the worker’s value function in case trade takes place with $W^t_a$ denoting the partial derivative of $W^t$ with respect to wealth $a$. Note that since shocks are i.i.d., the firm’s productivity realization affects the worker’s expected utility $W^t$ conditional on the match surviving only through
It is worth pointing out that the equilibrium outcome in Proposition 3 implies no delay. Trade takes place in all periods as long as the match survives and the parties immediately agree to separate whenever it is Pareto optimal.

Equation (12) can be inverted to solve for the firm’s reservation productivity $\bar{y}(\sigma)$ as a function of the current contract; i.e.

$$w = \bar{y}(\sigma) - \tau + rF + \lambda \int_{\bar{y}(\sigma)}^{1} \frac{1 - G(y)}{r + \lambda} dy. \quad (13)$$

For given $F$, $\bar{y}(\sigma)$ is an increasing and concave function of $w$. The corresponding curve is drawn in Figure 2.

Consider now the joint reservation productivity $y_d$ below which the match is destroyed. This is the value of $y$ which equates $W^u(a + \bar{F})$ and $W^t(\hat{w}, F, a)$ in equation (10) - the worker’s utility from separation at the equilibrium severance pay and from continuation at the equilibrium wage. Proposition 3 implies that the joint reservation productivity is a function $y_d(\sigma, a)$ of the ruling contract $\sigma$ and the worker’s stock of wealth.

Figure 2 draws $y_d(\sigma, a)$ as a function of $w$, for given $(F, a)$. To understand how the two curves intersect consider the following thought experiment. For $w$ large enough it is $\hat{w}(s) = \bar{w}(y, F)$ for any $y$, as the firm’s outside option is binding - $J^c(y, \sigma) = -F$ - and the contract wage is renegotiated for any possible productivity realization. Therefore, the worker’s expected utility from continuing the match $W^t(\hat{w}, F, a)$ in equation (10)
is independent of $w$. For the same reason, also the worker’s return from separation in equation (10) is independent of $w$. It follows that $y_d$ is also independent of $w$ and strictly smaller than $\bar{y}$. Reducing $w$ has no effect on $y_d$, but reduces $\bar{y}$. Therefore there exists a unique critical value $w^*(F, a)$ of $w$ at which the two curves cross.

Given $(F, a)$, the two curves partition the set of possible $(y, w)$ pairs into the four, mutually exclusive, subsets in Figure 2. Together with $(F, a)$ the contract wage $w$ determines the equilibrium outcome given the productivity realization. In particular, the triplet $(w, F, a)$ determines whether $y_d < \bar{y}$ or not.

Consider, for example, the case in which $w < w^*(F, a)$; e.g. $w = w^1$ in Figure 2. This implies $y_d(w^1, F, a) > \bar{y}(w^1, F)$. The value of the productivity realization along the vertical line through $w^1$ determines the outcome. If $y < \bar{y}(w^1, F)$, the firm reservation payoff coincides with the return to firing the worker at the contractual cost $F$. If instead $y \geq \bar{y}(w^1, F)$, the firm prefers continuing to trade at $w^1$. Since $y_d(w^1, F, a) > \bar{y}(w^1, F)$ the contract wage is never renegotiated. Trade takes place at $w$ for any $y \geq y_d(w^1, F, a)$, the parties agree to renegotiate $F$ down and separate if $\bar{y}(w^1, F) < y < y_d(w^1, F, a)$ and the parties separate with a severance payment $F$ if $y \leq \bar{y}(w^1, F)$.

Suppose, instead, $w > w^*(F, a)$; e.g. $w = w^2$ in Figure 2. Unless $w$ is not renegotiated, the firm is better off paying $F$ and firing the worker whenever $y < \bar{y}(w^2, F)$. Since $\bar{y}(w^2, F, a) > y_d(w^2, F)$, the contractual severance payment $F$ is never renegotiated, but the wage is renegotiated down to $\bar{w}(y, F)$ - the inverse image of $\bar{y}$ along the segment AB - whenever $y_d(w^2, F, a) < y < \bar{y}(w^2, F)$.

The contract $(w, F)$ is never renegotiated and the transfers it establishes ex ante are realized ex post in all states if and only if $w = w^*(F, a)$.

We summarize the two possible set of outcomes in the following remark.

**Remark 1.** Given $(\sigma, a)$ one of two possible cases applies.

a. It is $y_d(\sigma, a) \geq \bar{y}(\sigma)$ and 1) trade takes place at the ruling wage $w$ in the current round if $y \geq y_d$; 2) the parties agree to renegotiate $F$ down to $\hat{F} = -J^e(y, \sigma)$ and separate if $\bar{y} < y < y_d$; 3) the parties agree to separate with a severance payment $F$ if $y \leq \bar{y}$; 4) $y_d$ satisfies

$$W^e(\sigma, a) = W^u(a - J^e(y_d, \sigma)).$$

(14)
b. It is $y_d(\sigma, a) < \bar{y}(\sigma)$ and 1) trade takes place at the ruling wage $w$ in the current round if $y \geq \bar{y}$; 2) the parties agree to renegotiate $w$ down to $\bar{w}(y, F)$ and trade in the current round if $y_d \leq y < \bar{y}$; 3) the parties agree to separate with a severance payment $F$ if $y < y_d$; 4) $y_d$ satisfies

$$W^d(\bar{w}(y_d, F), F, a) = W^u(a + F).$$  \hspace{1cm} (15)$$

The remark applies independently from whether the severance payment $F$ born by the firm is embodied in a private contract or mandated by legislation as renegotiating $F$ involves just exchanging a lower spot payment and labelling the separation either a quit or a voluntary redundancy.

### 3.2 Initial contract

A Pareto optimal initial contract maximises the present value of the firm’s expected profits at $t_0$ subject to the worker receiving a given level of utility. Alternative (efficient) bargaining solutions just select different values for the worker’s utility level. Among these, the axiomatic Nash bargaining solution is the most used in the matching literature. Furthermore, it is straightforward to adapt the proof of Proposition 2.4 in Rudanko (2006) to show that, in the environment of Section 4, the random matching equilibrium with Nash bargaining coincides with the competitive search equilibrium if Hosios’s (1990) condition, requiring workers’ Nash bargain share to coincide with the elasticity of the probability of filling a vacancy, is satisfied.

We therefore assume without much loss of generality that the initial contract satisfies the axiomatic Nash bargaining solution, or

**Assumption 1.** The optimal initial contract solves

$$\max_{\sigma} N = J^e(1, \sigma)^{1-\gamma} [W^e(1, \sigma, a) - W^u(a)]^{\gamma}$$

s.t. $W^e(1, \sigma, a) \geq W^u(a)$

$$J^e(1, \sigma) \geq 0$$

$$F \geq F_m.$$  \hspace{1cm} (16)$$
The first two constraints are the participation constraints for the worker and firm respectively. The third one is the institutional constraint on the privately contracted severance payment $F$ which applies in case the government mandates a minimum severance payment $F_m$.

The maximisation problem in equation (16) is continuous and differentiable in $\sigma$ on the interior of the feasible set. This, together with the fact that the Nash maximand is zero if either participation constraint is binding, implies that a privately optimal contract has to lie on the contract curve

$$\frac{\partial W^e(1,.)}{\partial F} = \frac{\partial J^e(1,.)}{\partial F}$$

and satisfy the surplus sharing condition

$$1 - \gamma \frac{W^e(1,.) - W^u(a)}{J^e(1,.)} = -\frac{\partial W^e(1,.)}{\partial w}$$

The following Lemma ensures that the two conditions are also sufficient for a unique global maximum.

**Lemma 1.** Given worker’s wealth, the Nash bargaining programme has a unique local and global maximum.

Uniqueness of the mapping from workers’ wealth to the optimal contract is necessary for equilibrium analysis, to which we now turn.

4 Equilibrium with CARA preferences

4.1 Steady state

We can now characterize market returns. To streamline notation we anticipate here that if workers’ have CARA preferences both the ex ante optimal contract $\sigma^*$ and the joint reservation productivity $y_d$ are independent of the worker’s stock of wealth $a$.

The asset value of an unfilled job $V_c$ satisfies the Bellman equation

$$rV_c = -m + q(\theta) \max\{J^e(1,\sigma^*) - V_c, 0\} = 0,$$
where \( J^c(1, \sigma^*) \) is the value to the firm of forming a new productive match with initial productivity equal to one and optimal contract \( \sigma^* \). The second equality follows from free entry.

The value function of an unemployed worker \( W^u \) is characterized in a similar way by the Hamilton-Jacobi-Bellman equation

\[
 rW^u(a) = \max_{c^u} u(c^u) + (ra + b - c^u)W_a^u + p(\theta) \max\{W^e(1, \sigma^*, a) - W^u(a), 0\}. \tag{20}
\]

The flow equivalent of being unemployed with wealth \( a \) equals the flow of utility from current consumption plus the expected capital gain. The latter has two components. First, the value of unemployment changes because the stock of wealth changes. The associated gain equals the change in wealth \( ra + b - c^u \) times the marginal utility of wealth \( W_a^u(a) \), where \( W_a^u \) denotes the partial derivative of \( W^u(a) \) with respect to wealth. Second, the worker meets a firm at rate \( p(\theta) \). If she accepts to form a match with a contract \( \sigma^* \), her lifetime expected utility is \( W^e(1, \sigma^*, a) \).

As in Mortensen and Pissarides (1994), the unemployment steady-state flow equilibrium condition is

\[
 \lambda G(\bar{y}_d) (1 - u) = p(\theta) u. \tag{21}
\]

Finally, balancing of the government budget requires the total gross unemployment benefit bill to equal total tax revenues, or

\[
 \tau = (b + \tau)u. \tag{22}
\]

In order to determine the firm and worker’s expected returns from matching, \( J^e(1, \sigma^*) \) and \( W^e(a, 1, \sigma^*) \), we need to solve for the optimal contract.

The equilibrium can be formally defined as follows.

**Definition** (Stationary equilibrium). Assume CARA preferences and no borrowing constraints. A stationary equilibrium is a set of policy functions \( \{c^f, c^a, \bar{y}, y_d\} \), value functions \( \{W^e, W^f, W^u, J^e, V^c\} \), an optimal contract \( \sigma^* \), market tightness \( \theta \), unemployment rate \( u \) and tax \( \tau \) such that: 1) \( c^f \) and \( c^a \) maximise (11) and (20); 2) \( \bar{y} \) satisfies (13) and \( y_d \) satisfies either (14) or (15); 3) \( \{W^e, W^f, J^e\} \) satisfy (9)-(12); 4) \( W^u \) satisfies (20); 5)
free entry implies $V_c = 0$ and $J^*(1, \sigma^*) = m/q(\theta)$; 6) $\sigma^*$ satisfies (16); 7) $u$ is given by (21); 8) $\tau$ satisfies (22).

In what follows we specialise the felicity function to the CARA form $u(c_t) = -\exp\{-\alpha c_t\}$ and impose solvency by means of a no-Ponzi game condition\textsuperscript{10}. The two assumptions imply that there is no lower bound on workers’ stock of wealth and that the workers’ attitude towards lotteries over non-capital income is independent of wealth. Together they make the problem tractable as the following proposition highlights.

**Proposition 4.** Assume CARA preferences and no borrowing constraints. Given $i = u, t$

1. workers’ value functions satisfy

$$W^i = \frac{u(c^i)}{r};$$

(23)

2. the saving functions $s^i$, the optimal contract $\sigma^*$ and the joint reservation productivity $y_d$ are independent of wealth.

The dynamic constraint implies $c^i = ra + w^i - s^i$. Since $s^i$ is independent of wealth, the latter enters the worker’s value functions only through the multiplicative term $\exp\{-\alpha(ra)\}$ which is independent of employment status. Therefore, workers’ wealth does not affect the maximand of the Nash product in (16) and the separation rules (14) and (15). It follows that all jobs have the same optimal contract and separation rule\textsuperscript{11}.

Finally, we can characterise the optimal contract.

**Proposition 5.** Assume CARA preferences and no borrowing constraints. If $F_m = -\infty$, the optimal contract $\sigma^*$ is never renegotiated and implies $c^i(\sigma^*, a) = c^u(a + F)$ and $s^i(\sigma^*) = 0$.

With CARA preferences and no legislated severance pay, an optimal contract is never renegotiated and provides full insurance against job loss. As discussed in Section 6.4, the

\textsuperscript{10}This requires debt to grow at a rate below the interest rate, $\lim_{t \to \infty} (1 + r)^{-t} a_t \geq 0$, with probability one.

\textsuperscript{11}If this were not the case, contracts and the joint reservation productivity $y_d$ would be indexed by wealth and the whole wealth distribution would be a state variable.
full insurance result is actually knife-edged and specific to CARA preferences. Since such preferences imply that instantaneous utility is proportional to its first derivative, it follows from Proposition 4 that equalising the marginal utility of a worker employed at wage \( w \) and that of a job loser receiving \( F \) equates their value functions and implies that the worker never renegotiates either component of the contract since she is indifferent between being fired and being employed at the original wage. More importantly, Proposition 5 implies the following corollary which provides a lower bound for the optimal severance payment.

**Corollary 1.** The privately optimal \( F \) is zero if and only if \( \gamma = 0 \) and exceeds \( F = (w - b)/(r + p(\theta)) \) if \( \gamma > 0 \).

Insurance against job loss requires a positive severance payment whenever employed workers enjoy rents over their unemployed counterparts. The optimal size of severance pay is bounded below by \( F \), the expected loss in lifetime income associated with transiting through unemployment. This equals the expected present value of the income loss \( w - b \) over the expected length of an unemployment spell.

The intuition is the following. Proposition 5 implies that consumption does not fall upon entering unemployment. Since the duration of unemployment is uncertain, the variability of future consumption for a job loser is higher than for her employed counterpart. The existence of a precautionary saving motive implies that, for consumption not to fall upon losing one’s job, the permanent income of a job loser has to exceed that of an employed worker.

If employed workers enjoy no rents over their unemployed counterparts, their participation constraint is binding, and a contract featuring \( w = b \) and no severance payment provides full insurance. Only in such case, the optimal severance payment coincides with its lower bound \( F \) and the latter equals zero.

Clearly, mandated employment protection matters only in so far as it exceeds privately optimal levels. In such a case the following proposition applies.

**Proposition 6.** If \( F_m \) is marginally above the privately optimal \( F \), the unique optimal contract features \( y_d > \bar{y} \).
Proposition 6 implies that if somebody, e.g. the government, imposes on the parties a severance payment in excess of the unconstrained privately optimal one then the parties adjust (reduce) wages in such a way that point \(a\) of Remark 1 applies for \(y \geq \bar{y}\). The wage component of the contract \(w\) is never renegotiated, while the parties agree to renegotiate the mandated severance payment down to \(-J^c(y, \sigma) > 0\) for \(y \in (\bar{y}, y_d)\). Excessive mandated intervention, overinsures job losers and calls for a fall in wages to reestablish ex ante shares. Furthermore, the ability of the government to impose higher than \textit{laissez-faire} job security is limited by renegotiation.

5 Quantitative implications

5.1 Actual versus optimal severance pay

Corollary 1 summarises the main message of the paper: when labour reallocation is a time-consuming process, severance payments are a necessary part of an optimal insurance contract whenever employed workers enjoy rents over their unemployed counterparts.

A key prediction of the model is the functional relationship between the lower bound \(F\) on the optimal severance pay on the one hand and wages, benefits and unemployment duration on the other. Severance payments are usually expressed as a function of the last wage. For this reason it is useful to define the variable \(f = F/w\) which measures the severance payment in units of per-period wage. The fact that in reality unemployment benefits \(b\) are a function \(\rho w\) of the last wage imply that in \textit{laissez-faire} equilibrium it is

\[
\underline{f} = (1 - \rho) / (r + p(\theta)),
\]

(24)

where \(\rho\) is the replacement rate.

Equation (24) implies that, as a share of wages, the lower bound on the optimal severance payment is fully determined by just three variables, the unemployment benefit replacement rate, the interest rate and unemployment duration. This implies that \(\underline{f}\) is an increasing function of all exogenous factors which increase equilibrium unemployment duration such as training and search costs, workers’ bargaining power and frictions in the matching process.
In expressing the lower bound on optimal severance pay as a function of observable quantities, equation (24) provides an operational metric which can usefully inform the debate on whether observed legislated job security measures are excessive.

To this effect, we choose an annual interest rate of 4 per cent and use data on unemployment duration and benefit replacement rates \(^{12}\) for seventeen OECD countries to construct a series for \(f\). The data with details of their sources are reported in Table 5 in Appendix A.2. For comparison, we have also constructed series for actual legislated dismissal payments and notice periods for blue and white collar workers assuming a representative worker with job tenure equal to the average completed job tenure derived from the worker-flow data in Nickell, Nunziata, Ochel and Quintini (2002). The resulting four series are reported in Table 5 in Appendix A.2. Since in a number of countries notice periods constitute the main bulk of dismissal costs for firms, our series for observed legislated severance payments add up dismissal payments and notice periods. The result are two series for legislated severance payments for white and blue collar workers.

\(^{12}\)The lower bound \(f\) should be a function of unemployment duration in the counterfactual *laissez-faire* equilibrium which is unobservable. Yet, as shown in Section 5.2, the distinction is not quantitatively important.
Figure 1 plots the lower bound $f$ on the horizontal axis against the two series for legislated severance payment for a worker of average tenure. In interpreting Figure 1 it is worth keeping in mind, that not only is $f$ a lower bound, but our series for legislated payments constitute an upper bound for actual legislated dismissal payment to the extent that the actual cost to firms of notice requirements falls short of total wage payments over the mandated notice period in so far as workers find a new job before the expiration of their notice. Hence, if legislated severance payments were in line with optimal private arrangements one should observe most data points to lie above the forty-five degree line.

The figure highlights that, for a number of countries, legislated payments are significantly below the level consistent with optimal insurance. In particular, legislated severance payments for all workers in Ireland and for blue collar workers in Belgium are significantly below their optimal level. Given the high duration of unemployment in these two countries over the sample period, legislated payments underinsure workers. The same is also true for France and New Zealand. Spain and Italy, two countries which are normally deemed to have extreme levels of employment protection, turn out to have legislated payments which exceed their optimal lower bound by respectively one and at most six months. This is not so surprising in the light of an average unemployment duration in excess of thirty months for Italy and forty months for Spain. The two starred observations for Italy refer to the period before 1991, the year in which the replacement rate was raised from three to forty per cent. They make clear the extent to which despite the very high levels of dismissal costs Italian workers were underinsured before the reform.

Portugal presents the most extreme case. The mandated level of severance payments exceeds its optimal lower bound by slightly more than eleven months. With effectively the same replacement rate but an unemployment duration roughly one third of the Spanish one, its optimal severance payment should also be roughly one third. Yet, observed legislated payment in Portugal are higher than in Spain. Also severance payments for white collar workers in Belgium exceed their optimal lower bound by eleven months. It is worth keeping in mind, though, that in the latter case, as for countries such as Denmark and Sweden, notice periods constitute the bulk of the legislated severance payment.
reported in the figure\textsuperscript{13}. Hence, the actual cost to firms and transfer to workers is likely to be lower.

The above discussion makes clear that if one judges legislated employment protection measures by how much insurance against the cost of job loss they imply then, with the possible exception of Portugal, there is little support for the view that Mediterranean countries, or indeed most OECD countries, feature levels of employment protections significantly in excess of privately optimal levels. There is an important caveat, though. Since our series for optimal severance payments has been constructed using observed unemployment duration the above comparison does not allow for the widely-debated possibility that the positive relationship between legislated employment protection measures and unemployment duration reflects the reverse causation going from high mandated job security to low job creation. We tackle this possibility in the next subsection.

5.2 Quantitative impact of excessive mandated job security.

We have been able to characterise the features of an optimal contract and obtain insight into the rationale for the existence of severance payments in an effectively partial equilibrium set up. Yet, the question of the allocational and welfare impact of excessive mandated job security is of an equilibrium nature and, given the model complexity, can only be answered numerically.

To this effect we calibrate our model economy to the Portuguese one. As noted in Section 5.1 Portugal is characterised by legislated dismissal costs dramatically in excess of the optimal lower bound predicted by the model. It is also one of the countries where severance pay constitutes the main bulk of dismissal costs. Therefore, it appears a natural benchmark to investigate the consequences of excessive government intervention.

We choose a Cobb-Douglas matching function \( m(U, V) = AU^\eta V^{1-\eta} \), where \( A \) indexes the efficiency of the matching process. The productivity distribution is assumed uniform on \([y_l, 1]\). With benefits equal to \( b = \rho w \) where \( \rho \) is the replacement ratio, the model has ten parameters: \( \{r, y_l, \rho, \alpha, \eta, \lambda, \gamma, f_c, m, A\} \).

All flow variables are per quarter. The interest rate is \( r = \phi = 0.01 \). The lower support

\textsuperscript{13}See the table in section A.2.
Table 1: Summary of calibration

<table>
<thead>
<tr>
<th></th>
<th>Portugal</th>
<th>Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Moments</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Unemployment rate (%)</td>
<td>6.5</td>
<td>6.5</td>
</tr>
<tr>
<td>Avg. unemployment duration (months)</td>
<td>17</td>
<td>17</td>
</tr>
</tbody>
</table>

Parameters

G(y) uniform on \([y_l,1]\), \(m(U,V) = AU^{\eta}V^{1-\eta}\), \(u(c) = \exp(-\alpha c)\).

\(r = .01, \gamma = \eta = .5, \rho = .65, f_c = 17, m = 10, \lambda = .014, y_l = .32, A = 0.18, \alpha = 1.7\).

of the distribution is set to \(y_l = 0.32\) to obtain a coefficient of variation for output shocks of 0.3 as in Blanchard and Portugal (2000). The Portuguese benefit replacement rate is \(\rho = 0.65\). The ratio between the legislated severance pay and the net quarterly wage is set to 5.7 which corresponds to its value of 17 months in Table 5\(^\text{14}\). The chosen value for the coefficient of absolute risk aversion is \(\alpha = 1.7\) which implies a coefficient of relative risk aversion of \(\sigma = \alpha c^\alpha(0) = 1.5\) for an unemployed worker with zero wealth. A value of 1.5 is in the middle of the range of available estimates for the coefficient of relative risk aversion. Results are reported also for \(\alpha = 3.5\) which corresponds to \(\sigma = 3\). The elasticity of the matching function \(\alpha\) is set to 0.5 consistently with the evidence in Petrongolo and Pissarides (2001). The chosen value for the coefficient of workers’ bargaining power \(\gamma\) is also 0.5. As noted in Section 3.2 this implies that the bargaining equilibrium coincides with the competitive search one. If workers are risk neutrals, it also implies that the decentralised equilibrium is efficient in the absence of unemployment benefits.

The cost of posting a vacancy \(m\) is set to 0.33 following Millard and Mortensen (1997). The remaining two parameters \(\lambda\) and \(A\) are set to 0.014 and 0.18 to match an average unemployment duration of 17 months and an unemployment rate of 6.5 per cent. The chosen value for unemployment duration comes from the OECD unemployment duration database\(^\text{15}\) (see Blanchard and Portugal (2000), figure 4). Table 1 summarises the calibration procedure.

\(^\text{14}\)The government budget constraint (22) implies that the tax born by the worker equals the total benefit bill net of taxes divided by the size of the employment pool. Therefore, it is legitimate to equate the net wage in the model with the wage net of payroll taxes in the data.

Table 2: Mandated severance payments (in months of net wages)

<table>
<thead>
<tr>
<th>Severance pay</th>
<th>( \sigma = 1.5 )</th>
<th>( \sigma = 3 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sigma )</td>
<td>1.5</td>
<td>3.0</td>
</tr>
<tr>
<td>Laissez-faire</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>Mandated</td>
<td>17</td>
<td>17</td>
</tr>
<tr>
<td>Laissez-faire</td>
<td>17</td>
<td>17</td>
</tr>
<tr>
<td>Mandated</td>
<td>30</td>
<td>30</td>
</tr>
</tbody>
</table>

| Job finding rate (%) | 17.4 | 17.8 | 18.1 | 17.7 | 17.8 | 17.9 |
| Job destruction (%)  | 1.2  | 1.2  | 1.2  | 1.2  | 1.2  | 1.2  |
| Unemployment rate (%)| 6.7  | 6.5  | 6.4  | 6.6  | 6.5  | 6.4  |
| Gross wage \( \times 100 \) | 93.3 | 89.4 | 85.9 | 93.3 | 89.4 | 85.9 |
| Net wage \( \times 100 \)  | 89.0 | 85.4 | 82.1 | 89.0 | 85.4 | 82.1 |
| Net output          | 100.0 | 100.2 | 100.3 | 100.0 | 100.1 | 100.1 |
| Welfare (employed)  | 100.0 | 100.0 | 99.8 | 100.0 | 99.9 | 99.3 |
| Welfare (unemployed) | 100.0 | 99.9  | 99.6 | 100.0 | 99.7 | 99.1 |
| Welfare (avg. job loser) | 100.0 | 103.4 | 106.2 | 100.0 | 103.2 | 105.7 |

We can now tackle the question of the employment and welfare costs of mandated employment protection. Table 2 summaries our findings for the benchmark case in which the coefficient of relative risk aversion equals 1.5 and for the more extreme one in which it equals 3. It shows the allocational and welfare impact of imposing mandated severance payments of respectively 17 and 30 months, against a privately optimal value of 6 months in the calibrated economy\(^\text{16}\). 17 months is the legislated value in Portugal used in our calibration. 30 months is an upper bound obtained by adding the size of the largest mandated severance payments in our dataset - 24 months - to the privately optimal value.

Clearly legislated severance payments below private optima are not binding and have no effect. Instead, rows three to ten in Table 2 report the labour allocation, wages and the percentage change, relative to \( \text{laissez-faire} \), in the present value of net output, and workers’ welfare\(^\text{17}\) associated with the three levels of severance pay considered.

The effect of legislated severance payment widely in excess of private optima on job destruction is negligible, as the legislated severance payment is renegotiated. As for the job finding rate, with \( \sigma = 1.5 \), it increases by 0.4 and 0.7 percentage points when

\(^{16}\)This is five per cent larger than 5.7 months, the value of the optimal lower bound \( f \) in our calibration.

\(^{17}\)The values of quantities with no meaningful unit of measurement have been normalised to 100 in the decentralised equilibrium. The present value of output is the shadow value of an unemployed worker which, as in Acemoglu and Shimer (1999), is maximised at a social optimum in the risk-neutral case. Workers’ welfare is measured in terms of the percentage of permanent consumption in the \( \text{laissez-faire} \) equilibrium which would give worker the same level of utility as in the equilibrium with government intervention.
severance payments exceed their *laissez-faire* value by respectively 11 and 24 months. The corresponding fall in the unemployment rate is 0.2 and 0.5 of a percent. The fall in unemployment duration is due to a fall in the gross (producer) wage $w + \tau$ equal to 4 and 12 percent respectively.

This fall in unemployment duration may appear surprising at first sight. Even if wages fall in response, government intervention by increasing income uncertainty should increase the cost to the firm of providing a given level of utility and reduce, rather than increase, job creation. A second, offsetting, effect is at play, though. At given benefit replacement rate, the reduction in wages reduces steady state unemployment benefits and workers’ threat point in bargaining thus increasing firms’ return to job creation. If the benefit replacement rate is sufficiently high the second effect prevails.

Net (consumer) wages fall slightly less than gross wages due to the fall in the payroll tax stemming from the fall in unemployment.

The fall in wages, unemployment duration and the unemployment rate is smaller in the case in which $\sigma = 3$. Higher risk aversion implies that workers’ are less willing to trade off a wage cut for overinsurance in case of job loss.

Independently from the degree of risk aversion, the increase in unemployment duration increases net output in our calibration, as unemployment benefits are inefficiently high and, job creation inefficiently low, in the calibrated economy. While the sign of the change in net output is specific to the choice of calibration parameters, though, its absolute value is not. In general, the change is very small, reflecting the marginal nature of the change in the allocation.

Turning to welfare, as legislated payments increase, the average job loser’s welfare increases significantly as the increase in the expected severance pay more than offsets the increased consumption variability. On the other hand, welfare falls for employed workers and unemployed job seekers. The fall in welfare is no larger than respectively one tenth ($\sigma = 1.5$) and one third ($\sigma = 3$) of one per cent for the case in which mandated payments equal 17 months of wages. If $\sigma = 3$ though, the maximum welfare loss is nearly one per cent when mandated payments equal 30 months.

It is instructive to conduct the same experiment starting from the constrained efficient equilibrium in which, as in Acemoglu and Shimer (1999), the social planner chooses one
The results of such experiment are reported in Table 3. Net output and welfare are reported as proportion of their corresponding value in the \textit{laissez-faire} equilibrium in Table 2.

The first interesting result is that, as far as efficiency is concerned, severance payments are no perfect substitute for unemployment benefits. The efficient replacement rate is respectively 0.05 and 0.1 depending on the risk aversion coefficient. The intuition is the same as in Acemoglu and Shimer (1999) and is clearest in the present CARA setup\footnote{The optimal replacement rate is roughly half than in Table 1 in Acemoglu and Shimer (1999) as their calibration features an average unemployment duration of 6.5 years against 17 months here.}, where given the absence of wealth effects, severance pay have no partial equilibrium effect on the bargaining outcome. Decreasing marginal utility implies that wages increase a worker’s surplus by less than they reduce a firm’s one. Therefore, if Hosios’s (1990) condition is satisfied, the firm’s share of surplus is inefficiently high in the absence of benefits. This result applies as long as workers marginal utility of consumption is decreasing.

Second, the optimal severance payment size is decreasing in the replacement rate. It is now roughly 10 months of wages against 6 months in Table 2. The larger income fall, relative to the calibrated benchmark economy, is less than offset by the general

\begin{table}[h]
\centering
\caption{Mandated severance payments (in months of net wages): efficient benefits}
\begin{tabular}{lccccccc}
\hline
\multicolumn{1}{l}{} & \multicolumn{6}{c}{\textit{$\sigma = 1.5$, $\rho = 0.05$}} & \multicolumn{2}{c}{\textit{\textit{$\sigma = 3$, $\rho = 0.1$}}} \\
\hline
Severance pay & \textit{Laissez-faire} & \textit{Mandated} & \textit{Laissez-faire} & \textit{Mandated} & \textit{Laissez-faire} & \textit{Mandated} & \textit{Laissez-faire} & \textit{Mandated} \\
\hline
Job finding rate (%) & 9.8 & 21 & 34 & 9.6 & 21 & 34 & 28.0 & 27.5 \\
Job destruction (%) & 28.7 & 28.3 & 28.1 & 28.6 & 28.0 & 27.5 & 28.0 & 27.5 \\
Unemployment rate (%) & 3.8 & 3.8 & 3.8 & 3.8 & 3.8 & 3.8 & 3.9 & 3.9 \\
Gross wage $\times$ 100 & 89.4 & 86.2 & 83.3 & 89.5 & 86.3 & 83.4 & 89.5 & 86.3 \\
Net wage $\times$ 100 & 89.2 & 86.0 & 83.1 & 89.1 & 85.9 & 83.0 & 89.1 & 85.9 \\
Net output$^\dagger$ & 101.9 & 101.9 & 101.9 & 101.9 & 101.9 & 101.9 & 101.9 & 101.9 \\
Welfare (employed)$^\dagger$ & 100.3 & 100.2 & 100.0 & 100.2 & 100.1 & 99.6 & 100.1 & 99.6 \\
Welfare (unemployed)$^\dagger$ & 99.0 & 98.9 & 98.6 & 99.0 & 98.8 & 98.3 & 99.0 & 98.8 \\
Welfare (avg. job loser)$^\dagger$ & 100.3 & 103.4 & 106.1 & 100.2 & 103.3 & 105.8 & 100.2 & 103.3 \\
\hline
\end{tabular}
\footnote{Relative to the corresponding value in \textit{laissez-faire} equilibrium with $\rho = 0.65$ in Table 2.}
\end{table}
equilibrium fall in unemployment duration.

Third, increasing severance payments by the same amount as in Table 2 - respectively 11 and 24 months - above their privately optimal value still has hardly any allocational effect, although the sign of the change in the duration of unemployment and its level is now reversed relative to Table 2. Given the small replacement rate, the fall in wages has now a smaller effect on the worker’s threat point relative to the previous case. Therefore the higher cost of providing a given level of utility to the worker is less than offset by the fall in her bargaining power. Job creation falls as a consequence, but the absolute value of the change is still negligible. The associated reduction in net output is less than second order (lower than a thousandth of a per cent) with respect to the change in unemployment while the fall in welfare is roughly the same as in Table 2.

Conversely, the efficiency cost of raising the replacement rate from its efficient level to 0.65 is large. Net output in the laissez-faire equilibrium with efficient benefits is 1.9% higher than in the corresponding equilibrium when $\rho = 0.65$. As for welfare, the increase in the replacement rate redistributes from employed, whose net wage falls due to the increase in the unemployment pool and the payroll tax, to unemployed workers.

Summing up, the robust insight of the paper is that, if firms and workers can write optimal contracts, however simple, legislated dismissal costs have very small allocational effects. The result implies that even in the absence of complete markets there is no causal relationship from legislated dismissal costs to high unemployment rates and duration and low job destruction. On the contrary, our findings imply that the causation goes the other way round, from factors, such as high workers’ bargaining power, or high matching frictions, that result in high unemployment duration to optimal severance payments. Also, the optimal severance payment is larger, the lower the amount of insurance provided by the state through unemployment benefits.

It is worth emphasising that the comparisons involve alternative steady states. So, while employed workers would be better off in the steady state of the laissez faire economy, they would lose if at a point in time excessive legislated job security measures were scrapped. Since contract wages are not renegotiated up as long as they remain above reservation wages in the post-reform equilibrium, employed workers would suffer a negative windfall given that their contract wages were fixed at a lower level in the past,
reflecting higher expected layoff payments. This is consistent with the fact that employed workers are often very opposed to reduction in mandated job security.

It also has to be pointed out that the size of the welfare losses derived reflects two extreme deviations from laissez faire. Figure 3 shows that for all but two countries in our dataset the difference between the lower bound $f$ and legislated severance payments is 5 months or less, rather than 11 months.

It is obviously of interest to know how sensitive the results are to changes in the key parameters. It turns out that, for a given difference between optimal and mandated severance pay, the result is remarkably robust to alternative parameterisations being driven by the optimal nature of contracts rather than any other features\footnote{Calibrating the model to the US economy produces very similar results. They are available upon request.}.

6 Extensions and discussion

This paper has relied on a number of simplifying assumptions to derive a closed form lower bound for the optimal severance pay wage ratio as a function of observable quantities. In what follows we discuss how relaxing such assumptions alters the main conclusions. The broad message can be anticipated here. The lower bound we have derived is remarkably robust. Also, provided wages are flexible and separation jointly optimal, the welfare losses derived in Section 5.2 are an upper bound on the corresponding losses under less restrictive assumptions.

6.1 Wage rigidity and no renegotiation\footnote{I am grateful to an anonymous referee and Ioana Marinescu for suggesting to explore respectively the rigid-wage and no-renegotiation cases.}

To better understand the near-neutrality result derived in the paper it may be useful to disentangle the relative role played by wage flexibility and ex post renegotiation of mandated severance payment.

Consider first the case in which the contract wage is rigid, but the severance payment is renegotiated. Standard manipulation of equation (9) allows writing the value of a new
job as

\[ J(1, \sigma) = \frac{1 - \bar{y}}{r + \lambda} - F, \]  

(25)

where \( \bar{y} \) satisfies (13).

It follows that, for given \( w \), the contractual or mandated severance payment \( F \) fully determines the firm’s return from job creation and, through equation (19), market tightness. An increase in \( F \), at given \( w \), reduces job creation. Importantly, since (19), (13) and (25) do not depend on workers’ preferences, the result applies to any matching model in which wages are exogenous.

The last column in Table 4 reports the allocation and welfare associated with increasing \( F \) while keeping \( w \) constant at its level in the laissez-faire benchmark in Section 5.2 in the case in which the coefficient of relative risk aversion equals 1.5. Increasing \( F \) to 17 months effectively exhausts any return to job creation and no equilibrium exists for higher values of the mandated severance payment. Job creation collapses to a fifth of its original value as the wage is prevented from reestablishing profitability of new jobs. Given constant returns in production, mandated severance payments have a large negative impact on the ex ante value of a job. Job destruction fall by 20 per cent as the increase in duration makes workers less willing to enter unemployment. All welfare measures also collapse. It follows that the flexibility of the average wage in response to policy parameters is crucial not only for mandated severance pay to have negligible welfare costs, but, much more generally, for the ability of calibrated matching models to generate reasonable changes in allocation and welfare in response to observed cross-country variation in policies.

Let us now turn to the opposite case in which the wage is endogenous, but the excessive mandated severance payment is not renegotiated. In such a case \( y_d \) no longer satisfies equation (14), but instead coincides with the firm’s reservation productivity \( \bar{y} \) even outside laissez faire. The wage is instead still determined by equation (18).

Columns 3 and 4 in Table 4 report the allocational and welfare changes when severance pay is increased relative to its laissez-faire value. The separation rate falls significantly as there is now (jointly) suboptimal labour hoarding. The producer wage, though, is effectively unchanged relative to Table 2. In fact, it falls marginally with higher severance
Table 4: Mandated severance payments (months of wages): \( \sigma = 1.5 \).

<table>
<thead>
<tr>
<th>Severance pay</th>
<th>Laissez-faire</th>
<th>Mandated Exog. ( F )</th>
<th>Mandated Exog. ( w )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Job finding rate (%)</td>
<td>17.4</td>
<td>17.7</td>
<td>17.8</td>
</tr>
<tr>
<td>Job destruction (%)</td>
<td>1.2</td>
<td>1.1</td>
<td>0.9</td>
</tr>
<tr>
<td>Unemployment rate (%)</td>
<td>6.7</td>
<td>5.7</td>
<td>4.8</td>
</tr>
<tr>
<td>Gross wage ( \times 100 )</td>
<td>93.3</td>
<td>89.5</td>
<td>86.0</td>
</tr>
<tr>
<td>Net wage ( \times 100 )</td>
<td>89.0</td>
<td>85.9</td>
<td>83.2</td>
</tr>
<tr>
<td>Net output</td>
<td>100.0</td>
<td>100.1</td>
<td>100.2</td>
</tr>
<tr>
<td>Welfare (employed)</td>
<td>100.0</td>
<td>100.3</td>
<td>99.8</td>
</tr>
<tr>
<td>Welfare (unemployed, ( f_c = 0 ))</td>
<td>100.0</td>
<td>100.2</td>
<td>99.6</td>
</tr>
<tr>
<td>Welfare (average job loser)</td>
<td>100.0</td>
<td>103.9</td>
<td>107.3</td>
</tr>
</tbody>
</table>

pay as, given the increase in job duration, a given wage cut implies a bigger fall in a worker’s permanent income and welfare. It follows that job creation is hardly affected and the unemployment rate falls significantly.

Net output still increases with the fall in unemployment, though marginally less than in the case in which separation is Pareto optimal. More surprising is the marginal increase in welfare for unemployed and employed workers when \( F \) is increased to 17 months of wages. The increase is fully accounted for by the fall in the lump sum tax, a positive externality, stemming from the lower unemployment level. Were it not for the tax reduction, consumption and welfare would actually fall. When \( F \) equals 30 months of wages though, the welfare loss is comparable to the corresponding one in Table 2, with the fall in taxes still accounting for the difference. Basically, the larger fall in taxes offsets the welfare cost associated with the private inefficiency of separation.

While less crucial than wage flexibility, the ability of the parties to negotiate Pareto optimal side payments is an important ingredient of the near-neutrality result, though it hardly matters for welfare.

There are numerous examples suggesting that negotiation of Pareto optimal transfers upon separation is more than a theoretical construct. One such instance is the frequency with which one reads or hears about voluntary redundancy packages and/or early retirement incentives offered by downsizing firms. By revealed preferences, these must be jointly optimal (if workers accept them) and if contracting firms make the effort to negotiate such packages the associated cost must be smaller than the, possibly shadow, cost.
of unilaterally laying workers off. Also, in Germany firms cannot legally carry out mass redundancies (i.e. the mandated layoff cost is infinite) unless they agree with workers’ representatives on a social plan covering procedures and compensation packages. For Italy, a country usually associated with extreme levels of employment protection, IDS (2000) reports that employers often negotiate incentive payments to induce employees to take voluntary redundancy and sign agreements waiving their right to take legal proceedings\textsuperscript{22}. Finally, Toharia and Ojeda (1999) document that it is common for Spanish firms to agree with workers to label economic dismissals as disciplinary ones to economise on advance notice and procedural costs. Between 60 and 70 per cent of all dismissals, over the 1987-97 period, took this form and involved bargaining over the size of termination payments.

6.2 Alternative preferences

CARA preferences and no lower bound on consumption, while analytically convenient, are unappealing for well-known reasons. The following proposition generalises the result in Proposition 4 to a larger class of preferences.

**Proposition 7.** If $u'''' > 0$, it is ex ante optimal to trade a higher $F$ for a lower $w$ at the actuarially fair rate as long as $c'^c(1, \sigma, a) > c''(a + F)$.

If consumers are prudent, the optimal contract requires that consumption in those states in which the worker enters unemployment and the severance payment is not renegotiated is no smaller than consumption in those states in which the worker is employed at the contract wage.

The proof of Proposition 7 assumes $\phi = r$, but the result easily generalises to the case in which $\phi > r$ and marginal utility is not strictly convex as long as a lower bound on consumption generates a precautionary saving motive\textsuperscript{23}.

A formal proof that the permanent income of a job loser receiving $F$ exceeds the permanent income of a worker employed at the contract wage is not available for the

\textsuperscript{22}The same source reports a total cost for individual redundancy of 10-12 months of wages for a worker paid around 2 million ITL a month.

\textsuperscript{23}It is straightforward to adapt the arguments in Aiyagari (1994) to show that, in a stationary equilibrium with a precautionary saving motive, the saving of a newly matched worker is positive even if $\phi > r$. 

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general case. Yet, the intuition behind Corollary 3 that, given that the contract provides insurance, the future consumption of an employed worker is less variable than that of a job loser suggests that the permanent income of the job loser must be higher for $c^*(a + F)$ not to be smaller than $c^*(1, \sigma, a)$.

Allowing for borrowing constraints is also unlikely to significantly change the results in Section 5. A previous version of this paper featuring hand-to-mouth consumers (but allowing for annuitization of severance payments) obtained similar results with only fractionally larger welfare costs.

### 6.3 Non-stationary benefits

With CARA preferences, allowing for the, realistic, possibility that workers entitlement to benefits falls over an unemployment spell or for the kind wage of losses in new occupations documented for example by Topel (1990) and Farber (2003) would leave unchanged the functional forms for the value functions and the first order condition for an optimal contract\(^{24}\). Proposition 5 and Corollary 1 would still apply. The fall in lifetime wealth associated with job loss would be larger though. The associated lower bound on the optimal severance payment would also be larger than in expression (24), if, as in our dataset, $\rho$ denotes the replacement rate upon job loss rather than its average\(^{25}\) value over an unemployment spell and benefits fall over time.

In fact, our argument that the privately optimal size of severance pay is strictly positive just relies on the average replacement rate being smaller than one. Not only is the latter the case in practice. The moral hazard associated with the conditional nature of benefits implies that the maximum, let alone the average, replacement rate along a socially optimal path is below one even when consumers cannot borrow or lend and the optimal time profile of benefits is non-stationary, as in Fredriksson and Holmlund (2001) and Coles and Masters (2006).


\(^{25}\)Where the average replacement rate is defined as the constant rate whose expected present value over an unemployment spell coincides with the present value of the path of actual replacement rates.
6.4 Imperfect insurance

In the above analysis, the optimal contract is never renegotiated in the *laissez-faire* equilibrium and insurance against match productivity shocks is perfect. As noted in Section 4 this is not true in general, though.

Consider, for example, the case in which the utility of leisure is positive. If the utility function is separable in consumption and leisure the contract curve is unchanged. Furthermore, it is easily shown that Proposition 4 still applies with the only difference that $W^u > u(c^u)/r$ if the utility of leisure is positive. It follows from Proposition 7 that under the optimal contract the lifetime utility of being employed at the contract wage is smaller than that of entering unemployment receiving the contracted severance payment $F$. Therefore, the latter must be renegotiated down with positive probability - $y_d > \bar{y}$ - and insurance is imperfect.

The same insight is likely to apply if workers have DARA preferences. Provided the optimal $w$ and $F$ are non-decreasing in wealth, it can be shown that DARA preferences imply $y_d > \bar{y}$ even if leisure yields no utility.

6.5 Alternating offer bargaining

The assumption that workers have all the bargaining power in the renegotiation game implies that workers capture all the surplus from separation. If instead firms capture a positive share of the surplus from separation, the agreed severance payment when $F$ is renegotiated is lower for given $w$ and $y$. Hence, the redistribution associated with excessive job security is smaller. This further reinforces the conclusion that the welfare loss derived in Section 5.2 is an upper bound.

One may also wonder to which extent the chosen bargaining protocol, which makes the offer to renegotiate the wage or the severance payment mutually exclusive, affects the solution. One natural alternative would be for the worker to propose to renegotiate the whole contract $(w, F)$, when offering to continue the match. The outcome would be

\footnote{DARA preferences do imply that the bargained wage is increasing in wealth in the static case. While the absence of a wealth effect on the bargaining outcome generalises from the static to dynamic case with CARA preferences, one can only conjecture that, with DARA preferences, the sign of the wealth effect is preserved in going from the static to the dynamic case.}
different, though, only if in equilibrium the ex ante contract were renegotiated for $y > y_d$. Yet, this is not the case with CARA preferences. Furthermore, we have argued in Section 6.4 that the same is true under a number of alternative assumption, including possibly DARA utility.

7 Conclusion

This paper characterises firms’ optimal provision of insurance by means of simple employment contracts when asset markets are incomplete and searching for a job is a costly activity. It establishes that positive severance payments are part of an optimal contract whenever employed workers enjoy positive rents. More importantly, the paper derives a lower bound on the optimal severance payment as a function of observable quantities. Such bound equals the fall in lifetime wealth associated with job loss and is therefore decreasing in unemployment benefit replacement rates and increasing in unemployment duration.

The paper makes no attempt to explain if and why severance payments should be enshrined in legislation rather than in written private, explicit contracts. In fact, firms have the same incentives to evade both legislated and privately contracted severance payments and courts face the same informational asymmetries in enforcing both types of measures. One possible explanation for excessive government intervention, along the lines of Saint-Paul (2002), is that it reflects the ability of a majority of employed insiders to extract a one-off welfare gain at the expense of the present and future generations of unemployed. Nevertheless, if the assumption is made that observed legislated measures reflect, to some extent, the degree to which private arrangements call for them the model predicts that there should be a direct relationship, *coeteris paribus*, between job security measures and the expected income loss associated with transiting through unemployment.

Indirect evidence consistent with the above assumption comes from Boeri, Borsch-Supan and Tabellini (2001) who find a negative correlation between an index of employment protection and a measure of benefit coverage. More direct evidence can be obtained

27The outcome is self-sustaining as new generations of insiders, whose contract wage was determined on the basis of the excessive mandated severance pay, would suffer a windfall be hurt by a subsequent reform which reduced the latter.
by regressing observed legislated dismissal costs against the expected income cost of job loss $f$. Estimating such relationship for blue and white collar workers separately yields\(^{28}\)

\[
f^{BC} = 1.84 + 0.55 f^* , \quad \bar{R}^2 = 0.23 \quad s.e. = 5.20
\]

and

\[
f^{WC} = 2.74 + 0.70 f^* , \quad \bar{R}^2 = 0.24 \quad s.e. = 6.39.
\]

There is a positive and statistically significant relationship between the series for $f^*$ and those for legislated dismissal costs for blue and white collar workers $f^{BC}$ and $f^{WC}$ in Table 5.

In principle, such positive correlation may reflect the reverse causation from high legislated job security to high unemployment duration which has been most emphasised in the literature on employment protection. Numerical simulations of our model, though, indicate that such reverse causation is unwarranted despite the lack of perfect insurance. Furthermore, optimal private contracting undoes the effects of excessive mandate job security to a great extent.

\(^{28}\)Standard errors in parenthesis.
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A Appendix

A.1 Proofs

Lemma 2. Let \( \Gamma_W = \Omega_w \cup \Omega_F \) denote the worker’s action set and \( A_W : S \to \Gamma_W \) and \( A_E : S \times \Gamma_W \to \{ \text{accept, layoff, reject} \} \) denote respectively a worker’s and firm stationary strategy. The set of SSP equilibria can be characterized in terms of a strategy profile

\[
A_W(s) = \begin{cases} 
F_n = \hat{F}(s) & \text{if } j(s) = 0 \text{ and } J^I(s) \geq -F, \\
w_n = \hat{w}(s) & \text{if } j(s) = 1 \text{ and } \hat{w}(s) \neq w, \\
w_n \in w \cup \overline{\Psi}_w(s) & \text{or } F_n > \hat{F}(s) & \text{otherwise},
\end{cases}
\]

and a payoff profile \( W^e(s), J^e(s) \) with \( W^e(s), J^e(s), j(s), \hat{w}(s), \hat{F}(s) \) satisfying the system (3)-(8).

Proof. Note that the system (3)-(4) implies \( \hat{w}(s) \in \Psi_w(s) \) and \( -\hat{F}(s) = \max\{-F, J^I(s)\} \). The latter follows from \( W^u(a) \) being continuous and strictly increasing.

Suppose a SSP strategy profile \( A_W, A_E \) exists and be \( W^e(s), J^e(s) \) the associated SSP payoff profile as of stage n+1.1, where \( n \) is arbitrary given stationarity. Let \( W^I(s), J^I(s) \) denote the SSP payoffs at stage n.2, conditionally on trade taking place at the prevailing wage. Given \( W^e(s), W^I(s) \) has to satisfy (5)-(6) since otherwise either \( W^I(s) \) is unattainable or the worker can improve upon it by choosing \( c_j(s) \) optimally. Similarly, given \( J^e(s), J^I(s) \) must trivially satisfy (7) as the firm does not choose any action until the next round.

Consider the firm optimal choice of action at n.2. If it rejects a proposal, \( \sigma \) is unchanged and the firm payoff is \( J^I(s) \). If it lays the worker off its payoff is \( -F \). If at n.1 the worker has chosen \( \Gamma_W = F_n \) and the firm accepts its payoff is \( -F_n \). Therefore is optimal for the firm to accept any \( F_n \leq \hat{F}(s) \) and reject otherwise. If instead at n.1 the worker
has chosen \( \Gamma_W = w_n \) and the firm accepts, the new contract wage is \( w' = w_n \) and the associated firm payoff is \( J'(y, w_n, F, a) \). Therefore, it is optimal for the firm to accept any wage offer \( w_n \in \Psi_w(s) \). When confronted with an offer \( w_n \notin \Psi_w(s) \) it is optimal for the firm to lay the worker off if \(-F > J'(s)\) and reject and obtain \( J'(s)\) otherwise.

Consider the worker’s optimal choice at stage n.1. Suppose the worker proposes some severance payment \( F_n \). If the firm accepts the worker’s payoff is \( W^u(a + F_n) \). Given the firm acceptance strategy, it is optimal for the worker to propose \( F_n = \hat{F}(s) \) if \( J'(s) \geq -F \). If instead \( J'(s) < -F \), it is \( \hat{F}(s) = F \). The same outcome - separation with a side payment equal to \( F \) - obtains whether the worker proposes \( F_n = \hat{F}(s) \) or whether she makes an unacceptable proposal. Conditional on separation being optimal - \( j = 0 \) - any such proposal is optimal. Suppose instead the worker proposes some wage \( w_n \). The worker payoff is \( W^t(y, w_n, F, a) \) if the firm accepts, \( W^t(s) \) if it rejects and \( W^u(a + F) \) if the firm lays the worker off. If \( \hat{w}(s) \neq w \), optimality requires the worker to propose \( w_n = \hat{w}(s) \).

Alternatively, if \( \hat{w}(s) = w \) it is \( J'(s) \geq -F \) and any proposal \( w_n \in w \cup \hat{W}_w(s) \) or \( F_n > \hat{F}(s) \) results in an unchanged contract wage \( w \). Conditional on continuation being optimal - \( j = 1 \) - any such proposal is optimal. In either case, the worker payoff is \( W^t(y, \hat{w}(s), F, a) \).

Finally, it is optimal for the worker to make a proposal which results in separation with \( \hat{F}(s) \) if \( W^u(a + \hat{F}(s)) > W^t(y, \hat{w}(s), F, a) \) or \( j(s) = 0 \) in (3) and to propose a wage which results in a contract wage \( \hat{w}(s) \) if \( W^u(a + \hat{F}(s)) \leq W^t(y, \hat{w}(s), F, a) \) or \( j(s) = 1 \) in (3). It follows that the payoff profile evaluated at n.1 must satisfy (3) and (8).

The proof follows from the above discussion noting that a deviation in a single stage does not affect continuation payoffs in a stationary equilibrium. \( \square \)

**Lemma 3.** The firm SSP payoff satisfies \( J^c(s) = \max\{J'(s), -F\} \).

**Proof.** The proof is in two steps.

First, it is \( J^c(s) = \min_{w} \max\{J'(y, w, F, a), J'(s), -F\} \) for all \( s \). For all \( s \) in which separation takes place - \( j(s) = 0 \) - this follows from Lemma 2 which implies \( J^c(s) = \hat{F}(s) = \max\{-F, J'(s)\} \). Consider instead those \( s \) for which the match survives - \( j(s) = 1 \). Lemma 2 implies that SSP equilibria induce a Pareto optimal outcome in all \( s \). By definition and strict monotonicity of the respective instantaneous utility functions the Pareto frontier

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is strictly decreasing in payoff space. Therefore, an optimal wage offer by the worker minimizes the firm’s payoff from acceptance subject to the firm receiving its reservation payoff $\max\{J'(s), -F\}$.

We now prove that $J^e(s) = \max\{-F, J'(s)\}$. Let $H$ denote the space of bounded continuous functions on $S$ taking values in $R$. $J^e(s) = \min_w \max\{J'(y, w, F, a), J'(s), -F\}$ together with (7) defines an operator $T$ mapping a function $J^e \in H$ into a new function also in $H$. Since the set $S$ is a convex Borel subset of $\mathbb{R}^4$, $[y, 1]$ is compact and the transition function for $y$ has the Feller property, it is straightforward to verify that $T$ satisfies Blackwell’s sufficient conditions and is therefore a contraction. Therefore the functional equation $J^e = T(J^e)$ has a unique solution. Since, $J^e(s) = \max\{J'(s), -F\}$ satisfies the functional equation it is the unique solution. \hfill \Box

**Proof of Proposition 1.**

**Necessity.** Lemma 3 together with equations (4) and (8) imply

\[-(1 - j)\hat{F} + jW^e(y, \hat{w}, F, a) = J^e(s).\]  

(28)

It follows from Lemma 2 that that a SSP payoff profile satisfies the system of Bellman equations.

**Sufficiency.** Assume a pair of functions $W^e(s), J^e(s)$ solving (3)-(8) - with (4) holding as an equality - exists. Be $j(s), \hat{w}(s), \hat{F}(s)$ the associated policy functions. Any strategy profile satisfying (26)-(27) can support $W^e(s), J^e(s)$ as a SSP equilibrium. \hfill \Box

**Proof of Proposition 2.** As in Merlo and Wilson (1995) we prove uniqueness by showing that the system of functional equations (3)-(8) has a unique fixed point. Lemma 3 implies that the system is recursive, with $J^e$ solving the functional equation

\[J^e(y, w, F, a) = \max\{-F, (y - w - \tau) \Delta + \beta E J^e(y', w, F, a')\}\]  

(29)

and $W^e$ solving the system formed by (3), (5) and (6) subject to (28).

The proof of Lemma 3 implies that (29) has a unique solution. The Pareto frontier is strictly decreasing in payoff space. Therefore, there is a unique mapping from the firm’s
to the worker’s payoff in all states. Given that \( J^e \) is unique so is \( W^e \).

Proving uniqueness of the SSP outcome amounts to proving that the policy functions are functions rather than correspondences. Since wealth \( a \) does not enter (29) \( J^e(s) \), \( J^t(s) \) are not functions of wealth and one can solve for

\[
J^t(y, w, F) = \frac{(y - w - \tau)\Delta + \beta \lambda \Delta \int_{y_l}^1 J^e(y', w, F) dG}{1 - \beta (1 - \lambda \Delta)},
\]

which is increasing in \( w \). It then follows from equation (3) subject to (28) that \( \hat{w}(s) \), \( \hat{F}(s) \) are unique since the left hand side of (28) is monotonic in \( \hat{F}(s), \hat{w}(s) \) and the right hand side is unique. The uniqueness of \( j(s) \) follows trivially.

**Proof of Proposition 3.** Using Lemma 3 and taking the limit of (30) as \( \Delta \to 0 \) yields (9). The firm’s reservation wage \( \hat{w}(y, F) \) is the value of \( w \) that equates the two terms inside the maximum operator in (9). Integrating the second term by parts and equating yields (12). \( \hat{F}(s) = -J^e(s) \) and \( \hat{w}(s) = \min\{w, \hat{w}(y, F)\} \) follow from (4) evaluated respectively at \( j = 0 \) and \( j = 1 \), and (8) and the definition of \( \hat{w} \). Finally, consider equation (5). It is \( \mathbb{E}W^e(y', w, F, a') = (1 - \lambda \Delta) W^e(y, w, F, a') + \lambda \Delta \int W^e(y', w, F, a') dG \).

Expanding \( W^e(., a') \) in \( a \) around \( W^e(., a) \), replacing in (5) and eliminating terms of order \( o(\Delta) \) gives

\[
W^t(y, w, F, a) = \max_{c_{\ell}} u(c_{\ell}')\Delta + \beta W^e(y, w, F, a) + W^e_a \Delta a +
\]

\[
\lambda \Delta \int_{y_l}^1 [W^e(y', w, F, a) - W^e(y, w, F, a)] dG.
\]

Noticing that if in a SSP equilibrium trade takes place at \( w \) in state \( (y, w, F, a) \) it is \( W^e(y, w, F, a) = W^t(y, w, F, a) \), replacing for \( \Delta a \) using (6) and taking the limit for \( \Delta \to 0 \) yields (11).

**Lemma 4.** It is \( W^e(1, \sigma^*, a) = W^t(\sigma^*, a) \) and \( J^e(1, \sigma^*) = J^t(1, \sigma^*) \).

**Proof.** Since a new match is viable by assumption, equation (10) implies \( W^e(1, \sigma^*, a) = W^t(\hat{w}(1, \sigma^*), F^*, a) > W^u(a - J^e(1, \sigma^*)) \). It remains to prove that \( \hat{w}(1, \sigma^*) = w^* \) or equivalently \( J^e(1, \sigma^*) > -F \). \( J^e(1, \sigma^*) = -F \) implies that \( J^e(y, \sigma) = -F \) and \( \hat{w}(y, \sigma^*) =...
\( \bar{w}(y, F) \), for any \( y \). It follows that risk-averse workers provide full insurance to risk-neutral firms which cannot be efficient.

**Proof of Lemma 1.** The programme (16) maximises \( W^c(1, \sigma, \alpha) \) subject to \( J^c(1, \sigma) \geq \bar{J} \). Since Lemma 4 implies \( J^c(1, \sigma^*) = J^t(1, \sigma^*) \) it can be easily derived that, in a neighbourhood of \( \sigma^* \),

\[
\frac{\partial J^c(1, \sigma)}{\partial w} = \frac{1}{r + \lambda G(\bar{y})}
\]

and that the firm (signed) marginal rate of substitution between \( w \) and \( F \) is given by

\[
-\frac{\partial J^c(1, \sigma)/\partial w}{\partial J^c(1, \sigma)/\partial F} = -\frac{1}{\lambda G(\bar{y})},
\]

where \( \bar{y} \) is shorthand for \( \bar{y}(\sigma) \). Since \( \bar{y} \) is increasing in \( w \), the firm indifference curves are convex to the origin and their lower contour set is convex. Hence, the programme (16) is non-concave in \( \sigma \). Yet, because workers are more risk-averse than firms their indifference curves are more convex to the origin than the firm ones at any \( \sigma \). Therefore a point of tangency is a local maximum and is unique. Existence and uniqueness are not affected by the constraint \( F \geq F_m \) being binding.

**Proof of Proposition 4.** Totally differentiating equations (20) and (11) with respect to wealth \( a \), using the FOCs \( W_i^a = u'(c^i), \ i = t, u, \) and noticing that Lemma 4 implies \( W^c_a(1, \sigma^*, a) = W^t_a(\sigma^*, a) \) one can write

\[
-W_{aa}^u(a)s^u(a) = p(\theta) \left[ W_{a}^t(\sigma^*, a) + \frac{\partial W^t d\sigma^*}{\partial \sigma^*} da - W_{a}^u(a) \right]
\]

and

\[
- W_{aa}^t(y, \sigma, a)s^t(\sigma, a) = \\
\lambda \left[ \int_{y_i}^{\bar{y}} W_{a}^t(\hat{w}, F, a)dG + \int_{y_i}^{\bar{y}} W_{a}^u(a - J^c(y', \sigma))dG - W_{a}^t(\sigma, a) \right],
\]

where \( \hat{w} = \min\{w, \bar{w}(y', F)\} \) and \( s^t(\sigma) \) denotes saving.

We guess and verify: 1) the value functions; 2) that \( d\sigma^*/da = 0 \). Suppose \( W^u(a) = -e^{-\alpha(\alpha + b - s^u)}/r \) and \( W^t(y, \sigma, a) = -e^{-\alpha|\alpha + w - s^t(\sigma)}/r \) with \( s^u \) and \( s^t(\sigma) \) unknown functions
independent of wealth. Replacing for $W^i_{aa}$ and $W^i_a$, it is easily verified that (35) and (36) form a system of functional equations in the two functions $s^u$ and $s^t$. It is evident that the solution is independent of $a$, for given $\sigma^*$. It remains to verify that $da^*/da = 0$ in equation (35). From Lemma 4 the worker’s surplus in the Nash maximand (16) is $W^c(\sigma^*, a) - W^u(a) = W^t(\sigma^*, a) - W^u(a) = -e^{-\alpha(\sigma^*)}(e^{-\alpha(w^*-s^t(\sigma^*))} - e^{-\alpha(b-s^u)})/r$. Since $s^t$ is independent of wealth, the latter does not enter the first order condition for $\sigma$. \hfill \Box

**Proof of Proposition 5.** Lemma 4 implies $W^c(1, \sigma^*, a) = W^t(\sigma^*, a)$. Using equation (11), Remark 1 and the FOC $u'(c^t) = W^t_a$, the worker’s marginal rate of substitution between $w$ and $F$ in a neighbourhood of $\sigma^*$ can be written as

$$\frac{\partial W^c(1, \sigma, a)}{\partial w} = -\frac{B/\lambda + J\beta(\bar{y})}{C/\lambda + J\beta(\bar{y})} = (37)$$

$$- \frac{u'(c^t)}{\partial F} s^t + \lambda \left[ \int_{\min(y, \bar{y})}^{\bar{y}} \frac{\partial W^c(y, \sigma, a)}{\partial F} dG - \int_0^{y^*} u'[c^u(a - J^c(y', \sigma)) \frac{\partial J^c(y', \sigma)}{\partial w} dG \right],$$

where $c^t, s^t, W^t_a$, are shorthand for $c^t(\sigma, a), s^t(\sigma), W^t_a(\sigma, a)$.

Given $(F, a)$ select $w$ such that $y_d(\sigma, a) = \bar{y}(\sigma)$. It follows from point 1 in Proposition 4 that $c^t(\sigma, a) = c^u(a + F)$ and, from Remark 1, that $w(y', F) = w, \forall y' > y_d, J^c(y', \sigma) = -F, \forall y' < \bar{y}$ and $c^t(\sigma, a) = c^u(a + F)$. Replacing in (36) gives $s^t(\sigma, a) = 0, \forall y > y_d$. Since the last integral in the square bracket on the denominator of (37) equals $G(\bar{y})u'[c^u(a + F)]$, it follows that the worker’s marginal rate of substitution in equation (37) coincides with the firm one in (34) and the contract is Pareto optimal. \hfill \Box

**Proof of Corollary 1.** If $\gamma \to 0$ it is $W^c(1, \sigma^*, a) = W^u(a)$. The contract $w = b$ and $F = 0$ is trivially optimal. If $\gamma > 0$, the Nash bargaining solution requires $W^c(1, \sigma, a) > W^u(a)$ and $w > b$, at the optimum. It remains to prove that $F > (w - b)/(p(\theta) + r)$. Proposition 5 implies $w = b + rF - s^u$. Hence, it needs to be proved that $s^u > -p(\theta)(w - b)/(p(\theta) + r)$. From Proposition 4, equation (35) can be rewritten as

$$s^u = \frac{p(\theta)}{r\alpha} \left[ e^{-\alpha(w-b+s^u)} - 1 \right]. \quad (38)$$

The left and right hand side of (38) are respectively increasing and decreasing in $s^u$. It is easily checked that $w > b$ implies that the left hand side is smaller than the right hand
Proof of Proposition 6. The left hand side of (18) is strictly increasing in both $F$ and $w$ while (33) and (37) imply that the right hand side of (18) equals $B$, the numerator on the right hand side of (37). Remark 1 or Figure 2 imply that an increase in $w$ at given $(F, a)$ increases $\bar{y}$ and reduces $\bar{y}$, starting from the private optimum characterized in Proposition 5. An increase in $F$ has the opposite effect. Therefore, at the private optimum, it is
\[
\partial B/\partial w = u''(c^t)(c^t/\partial w)^2 \text{ and } \partial B/\partial F < u''(c^t)(\partial c^t/\partial w)(1 - \partial c^t/\partial w),
\]
where normality both terms are negative as consumption is a normal good. It follows that the right hand side of (18) is strictly decreasing in $F$ and $w$ and, if $F$ increases, $w$ has to fall to satisfy (18). Equation (13) implies $\bar{y}$ falls as a result and, since positive discounting and uncertainty imply $F$ increases $c^u(a + F)$ more than $c^t(1, \sigma, a)$, it follows from Proposition 4 that $W^t(1, \sigma, a) < W^u(a + F)$ and $y_d$ increases.

Proof of Proposition 7. It needs to be proved that if $c^u(a + F) < c^t(\sigma, a)$ the worker’s marginal rate of substitution between $w$ and $F$ in equation (37), exceeds the firm’s one in equation (34). Replace on the right hand side of (37) for $\partial J^e(y, \sigma)/\partial w$ and $\partial J^e(y, \sigma)/\partial F$ using (33) and for $J(y, \sigma) = -F, \forall y < \bar{y}$. The condition to verify can then be written as
\[
\lambda G(\bar{y})[u'(c^t) - u'(c^u(a + F))] \leq \lambda \int_{\min\{y, \bar{y}\}}^{\bar{y}} \frac{\partial W^e(y, \cdot)}{\partial F} dF + s^t \left[ \frac{\partial W^t_a}{\partial F} - \lambda G(\bar{y}) \frac{\partial W^t_a}{\partial w} \right].
\]
Differentiating the FOC $W^t_a = u'(c^t)$ with respect to $w$ and $F$ and replacing for $\partial W^t_a/\partial w$ and $\partial W^t_a/\partial F$ one obtains
\[
\lambda G(\bar{y})[u'(c^t) - u'(c^u(a + F))] \leq \lambda \int_{\min\{y, \bar{y}\}}^{\bar{y}} \frac{\partial W^e(y, \cdot)}{\partial F} dF + s^t \left[ \frac{\partial c^t}{\partial F} - \lambda G(\bar{y}) \frac{\partial c^t}{\partial w} \right].
\]
where we have dropped the dependence of $c^t$ on $(\sigma, a)$ for space reason.

The left hand side of the inequality is negative by assumption. Since the first addendum on the right hand side of (40) is non-negative it is sufficient to show that so is the second addendum. Equation (36) implies $s^t \geq 0$, as $c^t(\sigma, a) > c^u(a + F)$ implies that the marginal utility of consumption is expected to increase. It remains to prove that
\[
-\lambda G(\bar{y}) \leq -(\partial c^t/\partial F)/(\partial c^t/\partial w).
\]
From (34) the left hand side of (41) is the actuarially fair rate of exchange \( dw/dF \). Trading a higher \( F \) for lower \( w \) at such rate leaves permanent income unchanged, but, given \( c'(\sigma, a) > c''(a + F) \), reduces future consumption variability. Since \( w'' > 0 \), \( c^t \) increases. Hence, the rate of change \( dw/dF \) that leaves \( c^t \) unchanged, the right hand side of (41), is smaller in absolute value.

\[ \square \]

A.2 Data and variables used in Section 5.1

This section contains the data used to construct Figure 3 in section 5.1. The data for the monthly exit rate from unemployment \( p(\theta) \) are from the OECD unemployment duration database. The benefit replacement rates \( \rho \) are from Nickell (1997) with the exception of the Italian replacement rate which has been updated on the basis of information in Office of Policy (2002). The average completed job tenure \( \text{ACJT} \) is from the dataset in Nickell et al. (2002). It is an average over each country’s sample period.

The notice periods and severance payments in columns 5 to 8 are obtained by applying the appropriate formulas for legislated notice and severance pay to a tenure equal to the average completed job tenure in column 4. The relevant formulas for the European countries come from Grubb and Wells (1993), with the exception of those for Austria, Finland, Norway, Sweden which are derived from IRS (Industrial Relations Service) (1989). The size of the legislated severance pay for Italy is the sum of the damages workers are entitled to if their dismissal is deemed unfair (5 months) plus the amount they are entitled to if they give up their right to reinstatement (15 months). Our value is consistent with the
Table 5: Legislated severance pay for blue and white collar workers.

<table>
<thead>
<tr>
<th>Country</th>
<th>$p(\theta)$</th>
<th>$\rho$</th>
<th>ACJT</th>
<th>$f_c$</th>
<th>Notice BC</th>
<th>Sev. pay BC</th>
<th>Notice WC</th>
<th>Sev. pay WC</th>
</tr>
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<tr>
<td></td>
<td>(monthly)</td>
<td>(%)</td>
<td>(yrs)</td>
<td>(months)</td>
<td>(months)</td>
<td>(months)</td>
<td>(months)</td>
<td>(months)</td>
</tr>
<tr>
<td>Australia</td>
<td>0.15</td>
<td>36</td>
<td>7.6</td>
<td>4.2</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>Belgium</td>
<td>0.04</td>
<td>60</td>
<td>24.4</td>
<td>9.2</td>
<td>1.9</td>
<td>-</td>
<td>21</td>
<td>-</td>
</tr>
<tr>
<td>Canada</td>
<td>0.29</td>
<td>59</td>
<td>3.5</td>
<td>1.4</td>
<td>0.5</td>
<td>0.25</td>
<td>0.5</td>
<td>0.25</td>
</tr>
<tr>
<td>Denmark</td>
<td>0.12</td>
<td>90</td>
<td>11.9</td>
<td>0.8</td>
<td>3</td>
<td>-</td>
<td>6</td>
<td>1</td>
</tr>
<tr>
<td>Finland</td>
<td>0.15</td>
<td>63</td>
<td>10.4</td>
<td>2.4</td>
<td>4</td>
<td>-</td>
<td>4</td>
<td>-</td>
</tr>
<tr>
<td>France</td>
<td>0.05</td>
<td>57</td>
<td>21.1</td>
<td>8</td>
<td>2</td>
<td>1.7</td>
<td>2</td>
<td>1.7</td>
</tr>
<tr>
<td>Germany</td>
<td>0.13</td>
<td>63</td>
<td>26.5</td>
<td>4.4</td>
<td>2</td>
<td>-</td>
<td>6</td>
<td>-</td>
</tr>
<tr>
<td>Ireland</td>
<td>0.03</td>
<td>37</td>
<td>11.4</td>
<td>19</td>
<td>1.5</td>
<td>1.4</td>
<td>1.5</td>
<td>1.4</td>
</tr>
<tr>
<td>Italy</td>
<td>0.03</td>
<td>40 (3)</td>
<td>41.2</td>
<td>18 (29)</td>
<td>0.5</td>
<td>20</td>
<td>4</td>
<td>20</td>
</tr>
<tr>
<td>Netherlands</td>
<td>0.05</td>
<td>70</td>
<td>15.3</td>
<td>5.6</td>
<td>3.3</td>
<td>-</td>
<td>3.3</td>
<td>-</td>
</tr>
<tr>
<td>Norway</td>
<td>0.25</td>
<td>65</td>
<td>11.6</td>
<td>1.4</td>
<td>3</td>
<td>-</td>
<td>3</td>
<td>-</td>
</tr>
<tr>
<td>New Zealand</td>
<td>0.17</td>
<td>30</td>
<td>6.8</td>
<td>4</td>
<td>1</td>
<td>-</td>
<td>1</td>
<td>-</td>
</tr>
<tr>
<td>Portugal</td>
<td>0.06</td>
<td>65</td>
<td>14.9</td>
<td>5.7</td>
<td>2</td>
<td>15</td>
<td>2</td>
<td>15</td>
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<tr>
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<td>12.9</td>
<td>3</td>
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<tr>
<td>Sweden</td>
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<td>80</td>
<td>10.6</td>
<td>0.8</td>
<td>4</td>
<td>-</td>
<td>4</td>
<td>-</td>
</tr>
<tr>
<td>UK</td>
<td>0.1</td>
<td>38</td>
<td>4.5</td>
<td>6</td>
<td>1.2</td>
<td>1.2</td>
<td>1.2</td>
<td>1.2</td>
</tr>
<tr>
<td>USA</td>
<td>0.33</td>
<td>50</td>
<td>3.1</td>
<td>1.5</td>
<td>2</td>
<td>-</td>
<td>2</td>
<td>-</td>
</tr>
</tbody>
</table>

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*a* 0.86 times length of service in years. This is an approximation of the Claeys formula in Grubb and Wells (1993).

*b* For Germany and Sweden the formulas are a function of both age and length of services. We assumed employment started at age 20.

*c* It applies only to large scale redundancies covered by the Worker Advanced Retraining Notification Act.

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estimates in Ichino (1996). The formula in Grubb and Wells (1993) wrongly treats as severance pay the *Trattamento di fine rapporto*, a form of forced saving workers are entitled to whatever the reason for termination\(^1\), including voluntary quit and summary dismissal. The data for Portugal and New Zealand come respectively from Foundation (2002) and CCH New Zealand Ltd (2002). The data for legislation in Australia, Canada and the United States are from Bertola, Boeri and Cazes (1999).

\(^{1}\)On this see Brandolini and Torrini (2002).