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**Working Paper**

## Impact of voucher design on public school performance: Evidence from Florida and Milwaukee voucher programs

Staff Report, No. 315

**Provided in Cooperation with:**

Federal Reserve Bank of New York

*Suggested Citation:* Chakrabarti, Rajashri (2008) : Impact of voucher design on public school performance: Evidence from Florida and Milwaukee voucher programs, Staff Report, No. 315, Federal Reserve Bank of New York, New York, NY

This Version is available at:

<https://hdl.handle.net/10419/60820>

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Federal Reserve Bank of New York  
Staff Reports

Impact of Voucher Design on Public School Performance:  
Evidence from Florida and Milwaukee Voucher Programs

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Staff Report no. 315  
January 2008

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**Impact of Voucher Design on Public School Performance:  
Evidence from Florida and Milwaukee Voucher Programs**

Rajashri Chakrabarti

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JEL classification: H40, I21, I28

**Abstract**

This paper examines the impact of vouchers in general and voucher design in particular on public school performance. It argues that all voucher programs are not created equal. There are often fundamental differences in voucher designs that affect public school incentives differently and induce different responses from them. It analyzes two voucher programs in the United States. The 1990 Milwaukee experiment can be looked upon as a “voucher shock” program that suddenly made low-income students eligible for vouchers. The 1999 Florida program can be looked upon as a “threat of voucher” program, in which schools getting an “F” grade for the first time are exposed to the threat of vouchers, but do not face vouchers unless and until they get a second “F” within the next three years. In the context of a formal theoretical model, the study argues that the threatened public schools will unambiguously improve under the Florida-type program, and this improvement will exceed that under the Milwaukee-type program. Using school-level scores from Florida and Wisconsin and a difference-in-differences estimation strategy in trends, it then shows that these predictions are validated empirically. These findings are reasonably robust in that they survive sensitivity checks including correcting for mean reversion and a regression discontinuity analysis.

Key words: vouchers, public school performance, regression discontinuity, mean reversion

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# 1 Introduction

The 1983 report “A Nation at Risk”<sup>1</sup> and a series of similar reports have led to continued concern that American public schools may be lagging behind their counterparts in other parts of the developed world. This has led to a wave of demands for public school reform. School choice and accountability in general, and vouchers in particular, are among the most hotly debated instruments of public school reform. This paper is motivated by the need to understand the effect of vouchers and, in particular, the designs of different kinds of vouchers on public school performance. It argues that all voucher programs are not created equal. There are often fundamental differences in voucher designs that affect public school incentives differently and in turn bring about different responses from them.

The first publicly funded voucher program in the U.S. was initiated in Milwaukee in 1990. This was followed by Cleveland in 1996 and Florida in 1999. Interestingly, there are crucial differences in the designs of these programs. The Milwaukee and Cleveland experiments are similar. (In the rest of the paper, I will concentrate on the Milwaukee experiment because of better data availability.) These two experiments can be looked upon as “voucher shock” programs with a sudden government announcement that the low-income public school population is eligible for vouchers. In particular, starting in the 1990-91 school year, the Milwaukee Parental Choice Program (MPCP) makes all public school students with family income at or below 175% of the poverty line eligible for vouchers to attend non-sectarian private schools.

On the other hand, the Florida program can be looked upon as a “threat of voucher” program, rather than a “voucher shock” program. Here the failing public schools are first threatened with vouchers and vouchers are implemented *only if* they fail to meet a government designated cutoff quality level. In particular, under the Florida opportunity scholarship program, all students of a public school become eligible for vouchers or “opportunity scholarships” if the school gets two “F” grades in a period of four years. Therefore, a school getting an “F” for the first time is exposed to the threat of vouchers but does not face vouchers unless and until it gets a second “F” within the next three years.<sup>2,3</sup> This paper argues

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<sup>1</sup> National Commission of Excellence in Education (1983), “A Nation at Risk: The Imperative for Educational Reform,” Washington, DC: U.S. Government Printing Office.

<sup>2</sup> The Florida Department of Education classifies schools according to five grades: -A, B, C, D, F (A-highest, F-lowest). The criteria for the assignment of the lower grades are discussed in section 4.2. For a detailed description of the two programs, see Figlio and Lucas (2004) for Florida, and Witte (2000) for Milwaukee.

<sup>3</sup> In 1999, 78 schools got an “F”. Students in 2 of those schools became eligible for vouchers. In 2000, 4 elementary schools got an F although none became eligible for vouchers. In 2001, no school got an F. In 2002, 64 schools got an F. Students in 10 of those schools became eligible for vouchers. In 2003 (2004), students in 9 (21) schools became eligible for vouchers.

that these differences in voucher designs will affect public school incentives differently and will induce very different responses from them. In particular, it argues that the Florida type “threat of voucher” program will have a much greater effect on public school response and performance than the Milwaukee type “voucher shock” program.

Apart from the above differences, the designs of the two programs are strikingly similar. In both the experiments, the private schools are not permitted, by law, to discriminate between students who apply with vouchers—they have to accept all students unless oversubscribed and have to pick students randomly once they are oversubscribed. The system of funding is also very similar. Under each program the average voucher amount equals the state aid per pupil, and the vouchers are financed by an equivalent reduction of state aid to the district. Thus state funding is directly tied to student enrollment and enrollment losses due to vouchers are reflected in a revenue loss for the public school.<sup>4</sup> The average voucher amounts under the Florida (1999-2000 through 2001-2002) and Milwaukee (1990-1991 through 1996-1997) programs have been respectively \$3,330 and \$3,346. During the corresponding periods, vouchers as a percentage of total revenue per pupil have been 41.55% in Florida and 45.23% in Milwaukee.

The paper develops its argument in the context of a formal theoretical model with three agents:—the public school, the households and the private schools. The demand for public school is endogenously determined from household behavior, giving micro-foundations to the public school payoff function. In an equilibrium framework, the model endogenously determines public school quality and its ingredients—public school effort and peer group quality. Both under complete information and under moral hazard (when public school effort is not observable), the model generates two empirically testable predictions that hold at the respective program equilibria—the threatened public schools will show an unambiguous improvement in quality under the Florida-type “threat of voucher” program and the improvement under the “threat of voucher” program will exceed that under the Milwaukee-type “voucher shock” program.

Using school-level test score data from Florida and Wisconsin, the paper next proceeds to test the two theoretical predictions. Implementing a difference-in-differences estimation strategy in trends, it estimates the program effects for each of the experiments by comparing the post-program improvement of the treated schools with an appropriate set of control schools. Controlling for potentially confounding

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<sup>4</sup> I will mainly focus on the Milwaukee experiment up to 1996-97. This is because following a 1998 Wisconsin Supreme Court ruling, there was a major shift in the program when religious private schools were allowed to participate in the program and the program entered into its second phase. Moreover, the financing of the Milwaukee program saw some crucial changes, so that the voucher amounts and the revenue loss per student due to vouchers were not comparable between Florida and second phase Milwaukee. Sections 4.5 and 6 discuss the implications of these changes and whether a comparison of the Florida program with Milwaukee second phase is legitimate.

pre-program time trends and post-program common shocks, the paper finds considerable evidence in favor of both the theoretical predictions. These findings are quite robust in that they continue to hold after controlling for other confounding factors such as mean reversion, possibility of a stigma effect and withstand several sensitivity tests. I use multiple strategies, including a regression discontinuity estimation strategy, to address the potential problem of mean reversion. The findings have strong policy implications from the point of view of public school reform.

A growing body of literature analyzes multiple issues relating to school vouchers. Nechyba (1996, 1999, 2000) analyzes distributional effects of alternative voucher policies in a general equilibrium framework that endogenizes residential choice. Hoyt and Lee (1998) and Chen and West (2000) investigate the political support for vouchers. Epple and Romano (1998) argue that vouchers lead to sorting by income and ability. They model private school and household behavior, but assume public schools to be passive. Epple and Romano (2002) examine how alternative voucher designs can affect stratification and technical efficiency. They allow for public school technical inefficiencies, but these inefficiencies are taken to be exogenous in their study. In particular, none of the above studies endogenize public school quality.

Nechyba (2003) allows for efficiency gain in the public schools facing competition from vouchers.<sup>5</sup> However, he does not model public school behavior. Manski (1992) considers the impact of vouchers on public school expenditure and social mobility, while allowing for rent-seeking public schools. But unlike the present paper, understanding the impact of different voucher designs on public school performance is not a concern in Manski. Modeling public school quality, McMillan (2002) shows that under certain circumstances, public schools may find it optimal to reduce productivity when a voucher is introduced. The main difference once again is that he considers the effect of traditional voucher experiments (“voucher shock” in my terminology) on public school response, while this study compares and contrasts the effects of two types of voucher experiments on public school performance. Second, unlike McMillan, this paper derives the demand for public school from equilibrium household behavior, thus providing micro-foundations to the public school payoff function. Third, unlike McMillan, this paper models peer quality, which is considered to be an essential input in the education production function.

A number of empirical studies look at the effect of vouchers on the performance of students who move to private schools with vouchers (the “choice students”). For a comprehensive review of this literature, see Hoxby (2003b) and Rouse (1998). The empirical literature on the impact of vouchers on public

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<sup>5</sup> He includes two constants in the public school production function that exogenously increase with a decrease in peer quality variance and an increase in the share of private school attendance respectively.

school performance has been relatively sparse. Greene (2001, 2003) finds positive effect of the Florida program on the performance of the treated schools. However, the classification into different treatment groups in Greene (2003) is based on post-program grades of schools and hence is susceptible to the endogeneity problem. In response to Greene's (2001) paper, a spurt of studies took place (Camilli and Bulkley (2001), Harris (2001), Kupermintz (2001)) that express doubt that the program effect in the Greene study is contaminated by mean reversion<sup>6</sup> and/or stigma effect of getting the lowest performing grade "F". However, all of the above studies are potentially afflicted by mean reversion.<sup>7</sup> This study gets rid of these problems by (i) arriving at the mean reversion effect using pre-program data and (ii) using a regression discontinuity analysis in Florida to estimate the program effect. Another problem with all the above studies is that they do not control for any pre-program trends, which once again can bias the program effects.

Analyzing the Florida program and using student level data from a subset of Florida districts, Figlio and Rouse (2004) find some evidence of improvement of the treated schools in the high stakes state tests, but these effects diminish in the low stakes, nationally norm-referenced test. Using student level data, West and Peterson (2005) study the effects of the revised Florida program (after the 2002 grading rule changes) as well as the NCLB Act on test performance of students in Florida public schools. They find that the former program has had positive and significant impacts on student performance, but they find no such effect for the latter. This study differs from the above two studies in some fundamental ways. First, the question posed here is different. The objective of this paper is to analyze whether voucher design matters as far as public school performance is concerned. For this purpose, it compares and contrasts the effects of two alternative voucher designs (Florida and Milwaukee designs) on public school performance. On the other hand, both Figlio and Rouse (2004) and West and Peterson (2005) focus on Florida. Second, this study combines a theoretical and an empirical counterpart, while both the above studies are essentially empirical. Third, the time periods under consideration are also different. West

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<sup>6</sup> For a discussion of the mean reversion problem in Florida-style programs that base rewards and/or sanctions on school scores, see Chay et al. (2003).

<sup>7</sup> In Florida, Greene (2001) argues that mean reversion is not a problem in his study as the gains achieved by low scoring F schools are similar to those of the high scoring F schools between 1999 and 2000. However, similar gains of low scoring and high scoring F schools do not imply an absence of mean reversion since 2000 is a post-program year. In fact, even in the presence of mean reversion, the coefficients of the high scoring and low scoring F schools can be similar if there are differential program effects between these two groups. The studies in response to Greene (2001) seek to arrive at mean reversion corrected program effect by subtracting the post-program (2000) score from the predicted score in 2000, where the predicted score is obtained from a regression of the 2000 score on the pre-program (1999) score. However, in this strategy, the mean reversion effect is confounded with the program effect (since 2000 is a post-program year) and the mean reversion correction gets rid of at least part of the program effect. (Harris (2001) and Kupermintz (2001) exclude the F schools in their predicted score regressions. However, it is not clear that any mean reversion effect from the other groups of schools can be attributed to the F schools.)

and Peterson study the impact of the revised Florida program (after the 2002 grading rule changes) and focus on the time period 2002-04. Figlio and Rouse study the effect of the 1999 Florida program, but they look at the effect of the program in 2000 only, that is, one year after program. This study also looks at the effect of the 1999 program in Florida, but the time period considered here is different. Given the nature of the Florida program, the 1999 threatened schools (that is, the schools that received an “F” grade in 1999) would be exposed to the threat of vouchers for the next three years only. Therefore, this study tracks the performance of the threatened schools (relative to the control schools) for three years after program—2000, 2001 and 2002—when the threat of vouchers would be in effect.

Hoxby (2003a, 2003b) analyzes the impact of the Milwaukee voucher program on public schools after the Wisconsin Supreme Court ruling of 1998. Since the MPS students eligible for free or reduced price lunches were the ones eligible for vouchers (see footnote 33), the extent of treatment of the Milwaukee schools depended on the percentages of their students eligible for free or reduced price lunches. Exploiting this, she classifies the Milwaukee schools into two treatment groups (“most treated” and “somewhat treated”) based on the percentages of their free or reduced price lunch students. Since all schools in Milwaukee are potentially affected by the program, she chooses, as her control group, a set of schools within Wisconsin but outside Milwaukee that are most similar to the Milwaukee schools. (Her treatment-control strategy is discussed in more detail in section 5.2 .) Using a difference-in-differences strategy, Hoxby (2003a) finds a positive productivity response to vouchers. Hoxby (2003b) controls for pre-program differences in trends (unlike Hoxby (2003a)), and analyzing post-program data up to 2002<sup>8</sup> (unlike 2000 in Hoxby (2003a)), finds evidence of a positive productivity response to vouchers in Milwaukee after the Wisconsin Supreme Court ruling.

This paper follows Hoxby in the treatment-control group classification in Milwaukee. However it differs from Hoxby (2003a, 2003b) in some fundamental ways. First the focus of this paper is different. Its objective is to analyze the impact of alternative voucher designs on public school performance. For this purpose, it compares the effect of the Florida program with that in Milwaukee, while Hoxby focuses on the Milwaukee program. Second, Hoxby looks at the Milwaukee program after the Supreme Court ruling of 1998. The focus of this paper is on the Milwaukee program before the court ruling (although it also considers the second phase). This is because, except the TOV and VS components, the program characteristics in Florida were most similar to the characteristics of the Milwaukee program in its first phase. Third, although the treatment-control strategy is based on Hoxby, it differs from Hoxby in

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<sup>8</sup> For the remainder of the paper, I will refer to school years by the calendar year of the spring semester.



several important ways.<sup>9</sup> Fourth, unlike Hoxby, the Milwaukee analysis in this paper controls for mean reversion (since the more treated schools in Milwaukee were also the lowest scoring schools), controls for the possibility that changes in student composition of schools may bias the program effects, and uses regression analysis to analyze the effect of the program separately over the various post-program years (unlike average annual effect in Hoxby).

However, the fundamental difference of the present paper from all the studies in the existing literature (both theoretical and empirical) is its focus on the impact of alternative voucher designs on public school performance.<sup>10</sup> In particular, there is no study thus far that seeks to compare the public school response to different voucher designs. This study fills this important gap. Moreover, unlike any of the papers in the existing literature, this paper combines a theoretical and an empirical part,—the theoretical part designed to model the basic features of the Florida and Milwaukee voucher programs and to compare and contrast the impacts of the two designs on public school performance and the empirical part aimed at testing the theoretical predictions.

## 2 The Model

There are three agents in the model: (i) the public school, (ii) the private schools, and (iii) the households. The public school is free and offers quality ( $q$ ) to all households that choose to attend it. Quality  $q$  is a composite of two factors: public school effort and public school peer-group quality. The objective of the public school is to maximize net revenue or “rent” which is simply defined as revenue minus costs. The school competition literature [Hoxby (2003a), Manski (1992), McMillan (2004)] typically assumes that public schools are net revenue maximizers. I adhere to this practice.<sup>11</sup> Public school revenue is given by  $p \cdot N$ ,<sup>12</sup> where  $p$  is the exogenously given per pupil revenue and  $N$  is the number of students in public

<sup>9</sup> This study uses two alternative strategies for sample formation. As in Hoxby, the first strategy classifies the Milwaukee schools into different treatment groups based on the percentages of their free or reduced price lunch eligible students. However, it classifies the Milwaukee schools into three treatment groups (unlike two in Hoxby) so that the treatment groups are both more homogeneous and starker from each other. Moreover, to test the robustness of the results, it also considers different samples that are constructed by varying the cutoffs that divide the Milwaukee schools into different treatment groups. A disadvantage of this treatment group strategy is that it constrains the program effect to be the same for all schools within a treatment group. Therefore I also use an alternative strategy. This second strategy uses a continuous treatment variable where the intensity of treatment is proxied by the schools’ percentage of free or reduced lunch population. I follow Hoxby in the control group classification also, although there are differences as discussed in section 5.2.

<sup>10</sup> Nechyba (2000) and Caucutt (2002) examine distributional and welfare consequences of targeting vouchers to low income types; Epple and Romano(2002) and Hoxby (2001) consider the effect of alternative voucher policies on stratification and equity. These papers relate to voucher design, but their concern is not its impact on public school performance.

<sup>11</sup> An alternative formulation could be to model the public school as a quality maximizer. However, in that case there would be no argument for voucher programs as far as improving public school quality is concerned.

<sup>12</sup> This formulation captures the fact that revenue is directly tied to the number of students under each of the programs as well as in the simple public-private (baseline) system. However, as discussed earlier, in both Florida and Milwaukee, the

school. Public school cost ( $C_p$ ) is given by  $C_p(N, e) = c_1 + c(N) + C(e)$ , where  $c_1$  is a fixed cost. Both  $c(\cdot)$  and  $C(\cdot)$  functions are assumed to be increasing and strictly convex in their respective arguments. I assume  $p - c_N > 0$ , that is the “net marginal revenue” per student is positive.

There is a continuum of private schools providing a continuum of quality levels. Private schools do not choose between students who apply with vouchers. This is in keeping with the feature of the U.S. voucher experiments, by which private schools are not allowed to discriminate between students. They have to accept all students unless oversubscribed and have to accept students randomly when oversubscribed.<sup>13</sup> Households pay a tuition  $T = t \cdot Q$  ( $t > 0$ ) to attend a private school of quality  $Q$ .<sup>14</sup>

Households are characterized by an income-ability tuple  $(y, \alpha)$ , where  $y \in [0, 1]$  and  $\alpha \in [0, 1]$ ;  $y$  and  $\alpha$  are assumed to be independently and uniformly distributed. A household obtains utility ( $U$ ) from the consumption of the numeraire good ( $x$ ), school quality ( $\theta$ ) and its ability ( $\alpha$ ). The household utility function is assumed to be continuous and twice differentiable and is given by  $U(x, \theta, \alpha) = h(x) + \alpha u(\theta)$ . The functions  $h$  and  $u$  are increasing and strictly concave in  $x$  and  $\theta$  respectively. It follows that households with higher ability have a higher preference (marginal valuation) for school quality,  $U_{\theta\alpha} > 0$ .<sup>15</sup>

School qualities available to a household are public school quality and a continuum of (exogenously given) private school qualities. Public school quality  $q = q(e, b)$  is a continuous, twice differentiable, increasing and concave function of public school effort  $e \in [e_{min}, e_{max}]$  and public school peer quality  $b$ . Public school peer quality is defined as the mean ability of the public school student body.<sup>16</sup> If a public school household decides to switch to a private school with vouchers, it incurs a positive switching or relocation cost  $c$ .

The paper models three alternative scenarios: (i) a simple public-private system (PP) without vouchers (the baseline), which can be thought of as the pre-program scenario for both programs; (ii) the Milwaukee-type “voucher shock” (VS) program; and (iii) the Florida-type “threat of voucher” (TOV) program. The simple public-private system consists of two stages. In the first stage, the public school

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public school loses only the state aid per pupil for each student lost due to vouchers. Therefore, a more appropriate formulation would be to model revenue as a more general function of enrollment  $p(N)$ . For simplicity, I assume a multiplicative form. All results continue to hold with the more general functional form  $p(N)$ ,  $p'(N) > 0$ .

<sup>13</sup> Chakrabarti (2005) shows that random selection has indeed taken place—the socioeconomic characteristics of the accepted and unaccepted applicants are very similar, both economically and statistically.

<sup>14</sup> Note that at equilibrium, private school quality will always exceed public school quality. Otherwise, no household would pay to attend a private school.

<sup>15</sup> The assumption  $U_{\alpha\alpha} = 0$  is made for simplicity. All results go through under  $U_{\alpha\alpha} < 0$ ,  $U_{\theta\alpha\alpha} < 0$  (and thrice differentiability).

<sup>16</sup> Public school quality can be thought of as being embodied in public school scores. The notion here is that public school scores reflect both public school effort and public school peer-group quality, which in turn depends on the abilities of the public school students. In other words, both public school characteristics and student characteristics contribute to school scores.

chooses effort. In stage 2, households choose between schools after observing the last stage public school effort. Peer-group quality and public school quality are simultaneously determined.

The Milwaukee program is analyzed in three stages. In the first stage, the government announces voucher  $v$ . In stage 2, facing  $v$ , the public school chooses effort. In stage 3, households choose between schools (after observing  $v$  and  $e$ ) and incur switching costs if they transfer out of public school. Peer-group quality and public school quality are simultaneously obtained.

The Florida program is modeled in four stages. In the first stage, the Government announces the program and a corresponding cutoff quality  $\bar{q}$  and voucher  $v$ . In stage 2, facing the program the public school chooses effort. Given the existing peer group quality,  $q$  is realized. In stage 3, the government imposes vouchers  $v$  if  $q < \bar{q}$ . No voucher is imposed if  $q \geq \bar{q}$ . In the last stage, households choose between schools (after observing effort and whether vouchers were imposed) and incur switching costs if they transfer out of public schools. Peer-group quality and public school quality are simultaneously realized.

Each of the systems constitutes a game between two players: the public school and the households. Facing the relevant program and correctly anticipating household behavior, public schools choose effort to maximize rent. In the last stage, after observing the program, public school effort and whether vouchers have been introduced, households anticipate a certain peer quality and choose between schools. At equilibrium, anticipated peer quality equals actual peer quality. This yields an equilibrium peer quality and a corresponding allocation of households between public and private sectors. Equilibrium public school quality (which is a composite of equilibrium public school effort and peer quality) is simultaneously obtained.

An equilibrium of the “threat of voucher” program is an effort-peer quality tuple  $(e_{TOV}, b_{TOV})$ , such that given the quality cutoff  $\bar{q}$  and voucher  $v$  (i)  $e_{TOV}$  is a public school equilibrium, given  $b_{TOV}$  and (ii)  $b_{TOV}$  is a household equilibrium, given  $e_{TOV}$ . The “voucher shock” equilibrium is a peer-group quality  $b_{VS}$  and an effort  $e_{VS}$  such that given voucher  $v$  (i)  $e_{VS}$  characterizes the public school equilibrium, given  $b_{VS}$  and (ii)  $b_{VS}$  characterizes the household equilibrium, given  $e_{VS}$ . The public-private equilibrium is characterized by an effort-peer quality tuple  $(e_{PP}, b_{PP})$ , where (i)  $e_{PP}$  is an equilibrium of the stage 1 game, given  $b_{PP}$  and (ii)  $b_{PP}$  is an equilibrium of the stage 2 game, given  $e_{PP}$ .

### 3 Characterization of the program equilibria

This section solves for the household and public school equilibria and compares the public school qualities under the PP, VS, and TOV equilibria.

#### 3.1 Household behavior

This subsection analyzes the household behavior under the three systems in a common framework. A household  $(y, \alpha)$  chooses private school iff  $h(y + v - t \cdot Q^* - c) + \alpha u(Q^*) > h(y) + \alpha u(q(e, b))$  where  $Q^*$  is the optimal private school quality choice of household  $(y, \alpha)$ . Define  $D = [h(y + v - t \cdot Q^* - c) + \alpha u(Q^*)] - [h(y) + \alpha u(q(e, b))]$ .<sup>17</sup> It can be easily seen that  $\frac{\delta D}{\delta y} > 0$  and  $\frac{\delta D}{\delta \alpha} > 0$  which imply stratification by income and ability respectively.

Suppose all households expect a peer group quality  $b^e \in [0, 1]$ .<sup>18</sup> Then for each  $y$  and given  $t, v, e, c$  and expected peer group quality  $b^e \in [0, 1]$ , there exists a unique household  $0 < \hat{\alpha} < 1$  such that all households with lower ability choose the public school and those with higher ability choose a private school. This  $\hat{\alpha}$  is the unique solution to the equation:

$$[h(y + v - t \cdot Q^* - c) + \alpha u(Q^*)] - [h(y) + \alpha u(q(e, b^e))] = 0 \quad (3.1.1)$$

where  $Q^*$  is the optimal private school quality choice of the household  $(y, \hat{\alpha}(y))$ .<sup>19</sup> Since the indirect utility and the  $q$  functions are continuously differentiable and  $D_\alpha > 0$ , by the implicit function theorem,

$$\hat{\alpha} = \hat{\alpha}(y; v, e, b^e, t, c) \quad (3.1.1a)$$

is a continuously differentiable function.<sup>20</sup> Using the implicit function theorem it is straightforward to check that for each income level, the cutoff ability level  $\hat{\alpha}$  is decreasing in  $v$  and increasing in  $e, b^e, t$  and  $c$ . Given all other parameters, the cutoff ability level varies inversely with  $y$ . Given  $b^e$ , peer group quality  $b$  is given by:

$$b = \frac{\int_0^1 \int_0^{\hat{\alpha}(y, b^e, \cdot)} \alpha d\alpha dy}{\int_0^1 \int_0^{\hat{\alpha}(y, b^e, \cdot)} d\alpha dy} \Rightarrow \frac{1}{2} \cdot \frac{\int_0^1 \hat{\alpha}^2(y, b^e, \cdot) dy}{\int_0^1 \hat{\alpha}(y, b^e, \cdot) dy} = g(b^e, e, v, t, c) \quad (3.1.2)$$

<sup>17</sup> The parameter  $v$  takes on a value of zero under the pre-program public-private system, and under the Florida TOV system if the public school escapes vouchers. On the other hand,  $v$  takes on an exogenously given positive value under the VS program, and under the TOV program if the public school fails to meet the cutoff and vouchers are introduced.

<sup>18</sup> I assume that there are always some households in the public and some households in the private sector at each income level. This assumption is made for simplicity. All results hold as long as there is at least one income for which this assumption holds.

<sup>19</sup> To save some notation the optimal private school quality choice of the corresponding household is always denoted by  $Q^*$ . It is obvious that the value of  $Q^*$  will change with income and ability.

<sup>20</sup> Similarly, for each  $\alpha$  and given  $t, v, e, c, b^e$  there exists a unique household  $\hat{y}$  such that all households with lower income choose public school and those with higher income choose private school.

At equilibrium  $b$  corroborates the initial conjecture  $b^e$ , that is,  $b = b^e$  (3.1.3)

In other words, if all households expect a peer-group quality, then at equilibrium this expectation has to be fulfilled. Mathematically, given parameters  $e, v, t, c$ , a fixed point in  $b$  is reached. A household equilibrium always exists.<sup>21</sup> From (3.1.1)-(3.1.3), the equilibrium peer quality satisfies the equation  $b^* = g(b^*, e, v, t, c)$ . The corresponding equilibrium allocation of households between public and private sectors is characterized by  $\hat{\alpha}(y, b^*, \cdot)$  for  $y \in [0, 1]$ .  $N(b^*, e, v, t, c) = \int_0^1 \int_0^{\hat{\alpha}(y, b^*, \cdot)} d\alpha dy = \int_0^1 \hat{\alpha}(y, b^*, \cdot) dy$  gives the corresponding number of students in public school at the household equilibrium  $b^*$ .

Equilibrium number of public school students decreases with vouchers and increases with public school effort. (The proof is in appendix A.) An increase in public school effort leads to an increase in the equilibrium cutoff ability level,  $\hat{\alpha}(y, b^*)$ , at each income level. This occurs through two channels. Given  $b^*$ , an increase in  $e$  induces households just above the cutoff at each income level to switch to the public school. This increases peer quality, leading to a further influx of higher ability households just above the cutoff from the private to the public sector. The consequence is an increase in the equilibrium number of students with effort. Vouchers acting directly as well as indirectly through peer quality induce a flight of high ability public school households at each income level to the private sector at equilibrium.<sup>22</sup>

### 3.2 Public School Behavior

The public school correctly anticipates behavior in all the future stages of the corresponding game, and chooses effort to maximize rent. The rent function is given by  $pN(e, v) - c_1 - c(N(e, v)) - C(e)$ .<sup>23</sup> Under the PP system there exists a unique effort  $e_{PP}$  such that it solves the first order condition  $\frac{\delta R(e, 0)}{\delta e} = (p - c_N)N_e(e, 0) - C_e(e) = 0$ . Similarly under the VS program, there exists a unique effort  $e_{VS}$  such that it solves  $\frac{\delta R(e, v)}{\delta e} = (p - c_N)N_e(e, v) - C_e(e) = 0$ .

**Proposition 1** *Equilibrium public school effort under the “voucher shock” program can be either greater or less than the pre-program public-private equilibrium.*

In the pre-program simple public-private equilibrium, marginal revenue equals marginal cost of effort at  $e_{PP}$ . Vouchers affect both marginal revenue and marginal cost in multiple ways and these effects together

<sup>21</sup> The proof of existence is in Appendix A. The equilibrium is unique if the marginal utility from peer quality is not too high. (See Appendix A.)

<sup>22</sup> The analysis here assumes that when vouchers are imposed, all households, irrespective of income, become eligible for them. Although this is the case in Florida, in Milwaukee vouchers are targeted only to the low-income population. I abstract from this here for simplicity. All results continue to hold under targeted vouchers and are available in Appendix D. Note that given other parameters  $(e, v, t, c)$ , the number of public school students is less in a household equilibrium where all households are eligible rather than where only the low-income are. The reason is that in the former case there is a flight of households at each income level, whereas in the latter case it is restricted only to a subset of income levels.

<sup>23</sup> I assume that  $|u_{\theta\theta}|$  is not very low, –this ensures strict concavity of the rent function. Also rents decrease with vouchers, since  $\frac{\delta R(e, v)}{\delta v} = (p - c_N)N_v < 0$

determine whether or not the public school increases effort. More precisely, equilibrium effort increases iff the following expression is positive:  $[(p - c_N)N_{ev} - c_{NN}N_vN_e]$  (3.2.1). Vouchers decrease the number of public school students. Since the cost function is convex in the number of students, vouchers decrease marginal cost on this account. This is captured by the second term in (3.2.1). The first term captures the change in net marginal revenue due to vouchers. Given that net marginal revenue per student  $(p - c_N)$  is positive, this depends on the effect of vouchers on the marginal number of students from a unit increase in effort ( $N_{ev}$ ). This can either increase or decrease with vouchers, thus rendering the effect on public school effort ambiguous.<sup>24</sup> Public school effort increases if either net marginal revenue increases or the decrease in marginal revenue is less than the decrease in marginal cost.

**Proposition 2** *For each voucher  $v$ , there exists a cutoff effort level  $\bar{e}$ <sup>25</sup> such that the equilibrium effort under the “threat of voucher” program,  $e_{TOV}$  exceeds both*

- (i) *the equilibrium effort under the “voucher shock” program,  $e_{VS}$  and*
- (ii) *the equilibrium effort under the public-private system,  $e_{PP}$ .*

The Florida-type TOV program affects public school incentives in a way very different from the Milwaukee-type VS program. A Florida public school facing the threat has two options: it can choose to meet the cutoff or it can choose not to meet the cutoff. In the latter case, it is in the same state as its counterpart under the VS program. It chooses the VS optimum effort  $e_{VS}$  and gets the VS rent,  $R(e_{VS}, v)$ . Since vouchers decrease rent, it follows that the school can be induced to satisfy a cutoff  $\bar{e}$  strictly higher than  $e_{VS}$ , where the rent from  $\bar{e}$  without vouchers exactly equals the rent from  $e_{VS}$  with vouchers. Thus, the fundamental feature of the TOV that induces a higher effort is that vouchers are not already imposed and a sufficient improvement can enable schools to escape vouchers.<sup>26</sup> Note that any cutoff in the range

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<sup>24</sup>  $N_{ev} = \int_0^1 \left[ \frac{\delta^2 \hat{\alpha}(y, b^*, \cdot)}{\delta e \delta v} + \frac{\delta^2 \hat{\alpha}(y, b^*, \cdot)}{\delta e \delta b} \frac{\delta b^*}{\delta v} \right] dy$ . There are two effects. The first is a direct effect whereby the marginal number of students that the school can gain with a unit increase in effort falls with vouchers. Vouchers lead to an exodus of relatively high-ability households (at each income level) to private schools, so that the new marginal household (who is indifferent between the public and private sectors) has a relatively lower marginal valuation of quality. Consequently, the number of students gained due to a marginal increase in effort is lower under vouchers. This is captured by the negative first term. The second is an indirect effect. Vouchers decrease peer quality ( $\frac{\delta b^*}{\delta v} < 0$ ) which in turn affects the marginal number of students. Since the marginal utility from school quality decreases with quality ( $u_{qq} < 0$ ) the marginal number of students due to an increase in effort decreases with an increase in peer quality ( $\frac{\delta^2 \hat{\alpha}(y, b^*, \cdot)}{\delta e \delta b} < 0$ ). Since vouchers lead to a fall in peer quality, the marginal number of students increases due to this factor (which is captured by the positive second term).

<sup>25</sup> Note that since peer quality is known, announcing a cutoff in terms of effort is equivalent to announcing a corresponding cutoff in terms of quality.

<sup>26</sup> The analysis here assumes that all households irrespective of income are eligible for vouchers under the VS program. However, this result also holds for vouchers targeted to the low-income population under the VS. The formal proof is available in Appendix D. The intuition can be laid down in two steps. Call the VS program where all students are eligible the “universal voucher shock” (UVS) program and where only the low-income students are eligible the “targeted voucher shock” (TVS) program and the corresponding equilibrium number of students and equilibrium effort  $N_{UVS}$ ,  $N_{TVS}$  and

$(e_{VS}, \bar{e}]$  induces an effort under the TOV program that is strictly higher than under the VS program. The intuition behind the second part of the proposition is similar. The Florida TOV program introduces a discontinuity in the rent function at the cutoff effort level. If the cutoff is set at  $e_{VS}$ , then meeting it gives a higher rent than choosing to accept vouchers. Since  $e_{PP}$  is the rent maximizing effort under  $v = 0$ , setting the cutoff at  $e_{PP}$  gives an even higher rent to the public school. Given the strict concavity of the rent function, this implies that there exists a cutoff  $\bar{e} > e_{PP}$  which satisfies the school's incentive constraint. Again, any cutoff in the range  $(e^*, \bar{e}]$  induces an effort under the TOV program that is strictly higher than under the PP program equilibrium.<sup>27</sup> As appendices B and C show, these results continue to hold when effort is not observable, but quality is and there is no one-to-one relationship between the two. But, as is obvious, the cutoff can no longer be set in terms of effort, which is now unobservable. Using propositions 1 and 2 and the properties of the household equilibrium (see proof of claim 1 in appendix), the result below follows.

**Corollary 1** *(i) Equilibrium public school quality under the “threat of voucher” equilibrium:*

*(a) exceeds the equilibrium quality under the pre-program public-private system.*

*(b) exceeds the equilibrium quality under the “voucher shock” program.*

*(ii) Equilibrium public school quality under the “voucher shock” program can be greater or less than the pre-program public-private equilibrium quality.*

## 4 Data

The data for this paper come from multiple sources. The Florida data consist of school-level data on test scores, grades, socio-economic characteristics of schools and school finances and are obtained from the Florida Department of Education (DOE). Data on socio-economic characteristics include data on sex-composition (1994-2002), percentage of students eligible for free or reduced-price lunches (1997-2002),

$e_{UVS}$ ,  $e_{TVS}$  respectively. First, note that the equilibrium rent under the TVS is greater than that under the UVS. Under the TVS, the school can attract  $N_{UVS}$  students by giving a lower effort than under the UVS and hence at a rent higher than under the UVS. Since the school chooses to attract  $N_{TVS}$ , it must be the case that rent is higher under the TVS. Second, if vouchers when imposed in the Florida-type TOV program took a targeted form, then following the argument in proposition 2, the program could implement a cutoff  $\bar{e} > e_{TVS}$ . But vouchers take the universal form in Florida, which implies that the rent would be smaller than the TVS rent if schools failed to meet the cutoff. This implies that there exists a cutoff  $\bar{e} > \bar{e} > e_{TVS}$  which satisfies the school's incentive constraint with equality and hence can be implemented by the TOV program. To summarize, there are two features in the design of the Florida TOV that induce a higher effort than the TVS: (i) vouchers are not already imposed and (ii) the potential loss of students is much greater. But, as is obvious from this discussion, the first factor is sufficient to induce a higher effort under the TOV.

<sup>27</sup> In the TOV program it may be reasonable to think that there is a stigma attached to being labeled as a ‘voucher public school’. For example, Maureen Backentoss, assistant superintendent of curriculum and instruction of Lake County School District refers to it as a “glass of cold water in the face”. In the presence of such a stigma, the public schools gain an additional utility if they are able to escape vouchers. This feature is absent in the VS program. Note that this will weigh results in favor of the TOV and will induce an even higher improvement under the TOV.

race-composition (1994-2002) and are obtained from the school indicators database of the Florida DOE. (As noted earlier, this paper refers to school years by the calendar year of the spring semester.) School finance data consist of several measures of school level and district level per pupil expenditures and are obtained from the school indicators database and the Office of Funding and Financial Reporting, Florida DOE.

School-level data on test scores are available on two tests: (i) the Florida Comprehensive Assessment Test Sunshine State Standards (FCAT-SSS) (This test will be referred to as the FCAT in the remainder of the paper.) (ii) the Stanford 9 test which the state calls the FCAT Norm Referenced test (FCAT-NRT). Following a field test given to all students in grades 4, 5, 8 and 10 in 1997<sup>28</sup>, the FCAT reading and math tests were administered in the year 1998. Mean scale scores (on a scale of 100-500) on grade 4 reading and grade 5 math are available for 1998-2002. Mean scale scores (on a scale of 1-6) on the Florida grade 4 writing test, which was first administered in 1993, are available from 1994-2002. School level mean scale scores (on a scale of 424-863) and NPR scores on the nationally normed Stanford 9 test, which was first administered in Florida in 2000, are available for grades 3-10 in reading and math from 2000-2002. (The FCAT is a high-stakes test, unlike the Stanford 9, because only the scores from the former enter the calculation of school grades.)

The Wisconsin data consist of school-level data on test scores, socio-economic characteristics of schools, and per pupil expenditure (both school-level and district-level). The data are obtained from the Wisconsin Department of Public Instruction (DPI), the Milwaukee Public Schools (MPS), and the Common Core of Data (CCD) of the National Center for Education Statistics. School-level data on test scores are available on three tests: (i) the Third Grade Reading Test (renamed the Wisconsin Reading Comprehension Test (WRCT) in 1996) and (ii) the grade 5 Iowa Test of Basic Skills (ITBS) and (iii) Wisconsin Knowledge and Concepts Examination (WKCE). School scores for WRCT, which was first administered in 1989, are reported in three “performance standard categories”: percentage of students below, percentage of students at, and percentage of students above the standard.<sup>29</sup> Data for these three categories are available for 1989-97. School-level ITBS reading data are available for 1987-1993; ITBS math data are available for 1987-1997. NPR scores for grade 4 WKCE (reading, math, language arts, science, social studies) are available for 1997-2002.

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<sup>28</sup>The 1997 test results were not made public.

<sup>29</sup> The mode of reporting ITBS math and WRCT reading scores changed in 1998. So I focus on pre-1998 scores.



## 5 Empirical Strategy

The empirical part of the paper seeks to test the following two predictions obtained from the theoretical model: (i) A Florida-type TOV program will induce threatened public schools to respond leading to an increase in their quality. (ii) Quality improvement of threatened public schools in the Florida-type program will exceed the improvement (if any) of treated public schools in the Milwaukee-type program. School quality is proxied by school scores.

### 5.1 Florida

In Florida, the schools that received an “F” grade in 1999 were directly exposed to the threat of vouchers since all their students would be eligible for vouchers if they received another F grade in the next three years. These schools constitute the group of treated schools and will be referred to as the “F schools”. The schools that received a D grade in 1999 were closest to the F schools in terms of grade but were not directly treated by the program. These schools will constitute the group of control schools and will be referred to as the “D schools”. The treatment and control groups respectively consist of 65 and 457 elementary<sup>30</sup> schools. Since the program was announced in June 1999 and the grades were based on the tests held in February 1999, the classification of schools into treatment and control groups is made here on the basis of their pre-program scores and grades.

The identifying assumption here is that if the F and D schools have similar trends in scores in the pre-program period, any shift of the F schools compared to the D schools in the post-program period can be attributed to the program. First, using only pre-program data, I test whether the F and D schools exhibit similar trends before the program. If they have similar pre-program trends, I use the following set of specifications to investigate whether the F schools demonstrate a higher improvement in test scores in the post-program era. If the treated F schools demonstrate a differential pre-program trend, in addition to estimating these specifications, I also estimate modified versions of them where I control for their pre-program differences in trends. I begin with a completely linear model:

$$s_{it} = f_i + \alpha_0 t + \alpha_1 v + \alpha_2 (F * v) + \alpha_3 (v * t) + \alpha_4 (F * v * t) + \alpha_5 X_{it} + \epsilon_{it} \quad (1)$$

where  $f_i$  denotes school fixed effects,  $t$  is time trend,  $v$  is the program dummy,  $v = 1$  if year  $> 1999$  and 0 otherwise. The variables  $v$  and  $v * t$  respectively control for post-program common intercept and trend shifts such as national, state and county level shifts. The coefficients on the interaction terms  $F * v$

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<sup>30</sup> I restrict my analysis to the elementary schools as there were too few middle and high schools that received a grade of “F” in 1999 (7 and 5 respectively) to justify analysis.

and  $F * v * t$  estimate the program effects— $\alpha_2$  captures the intercept shift and  $\alpha_4$  the trend shift of F schools.  $X_{it}$  denotes the set of school characteristics. All specifications I describe here are fixed effects regressions. I also estimate OLS counterparts of each of these specifications. All OLS regressions include a dummy for the treatment group F. The second model allows the trend in the comparison group to be non-linear while still constraining the year-to-year gains of the treated schools in the post-program period to be linear in addition to an intercept shift.

$$s_{it} = f_i + \sum_{i=1999}^{2002} \beta_i D_i + \beta_0(F * v) + \beta_1(F * v * t) + \beta_2 X_{it} + \epsilon_{it} \quad (2)$$

where  $D_i, i = \{1999, 2000, 2001, 2002\}$  are year dummies for 1999, 2000, 2001, and 2002 respectively.  $\beta_0$  and  $\beta_1$  capture the program effects. Finally, I estimate a completely unrestricted and non-linear model that includes year dummies to control for common year effects and interactions of post-program year dummies with the F school dummy to capture individual post-program year effects.

$$s_{it} = f_i + \sum_{i=1999}^{2002} \gamma_i D_i + \sum_{i=1999}^{2002} \gamma_{1i}(F * D_i) + \beta_2 X_{it} + \epsilon_{it} \quad (3)$$

This specification no longer constrains the post-program year-to-year gains of the F schools to be equal and allows the program effect to vary across the different years. The coefficients  $\gamma_{1i}, i = \{2000, 2001, 2002\}$  represents the effect of one, two and three years into the program respectively for the F schools.

The above specifications assume that the D schools are not affected by the program. Although the D schools do not face any direct threat from the program, they may face an indirect threat since they are close to getting “F”.<sup>31</sup> Therefore, I next allow the F and D schools to be different treated groups (with varying intensities of treatment) and compare their post-program improvements, if any, with 1999 C schools (C schools from now on) which were the next higher up in the grade scale using the above specifications after adjusting for another treatment group. It should be noted here that since both D and C schools may face the threat to some extent, my estimates may be underestimates (lower bounds), but not overestimates. Comparisons with A and B schools yield similar results but their pre-program trends are much more different from the F schools.<sup>32</sup>

## 5.2 Milwaukee

<sup>31</sup> In fact, there is some anecdotal evidence that D schools may have responded to the program. The superintendent of Hillsborough county, which had no F schools in 1999, announced that he would take a 5% pay cut if any of his 37 D schools received an F on the next school report card. (For more evidence, see Innerst, 2000).

<sup>32</sup> Moreover, these schools are also likely to be affected, since the program offered \$100 per student to all schools that got an “A” or improved their letter grades from one year to the next.

I employ two alternative strategies for sample formation. Both strategies use the basic intuition in the Hoxby studies that the extent of treatment of the Milwaukee public schools depends on their pre-program percentages of free or reduced price lunch eligible students.

**1. Classification into treatment groups:** This strategy is based on Hoxby (2003a) and is similar to hers. Since the free or reduced price lunch eligible students of the MPS were the ones eligible for vouchers, the extent of treatment of the Milwaukee schools depended on the percentages of their students eligible for free or reduced price lunches.<sup>33</sup> Exploiting this, Hoxby classifies the Milwaukee schools into two treatment groups based on the percentages of their free or reduced price lunch students—“most treated” (Milwaukee schools where at least two-thirds of the students were eligible for free or reduced price lunches in the pre-program period) and “somewhat treated” (Milwaukee schools where less than two-thirds of the students were eligible for free or reduced price lunches in the pre-program period).

I classify the schools into three treatment groups (unlike two in Hoxby) based on their pre-program (1989-90 school year) percentage of free or reduced price lunches. So the treatment groups here are more homogenous as well as starker from each other. Also, to test the robustness of the results, unlike Hoxby, I consider alternative samples that are obtained by varying the cutoffs that separate the different treatment groups. The 60-47 (66-47) sample classifies schools that have at least 60% (66%) of their students eligible for free or reduced-price lunch as “more treated”; schools with such population between 60% (66%) and 47% as “somewhat treated”; and schools with such population less than 47% as “less treated”. I also consider alternative classifications, such as “66” and “60” samples, where there are two treatment groups,—schools that have at least 66% (60%) of their students eligible for free or reduced-price lunches are designated as more treated schools, and schools with such population below 66%(60%) as somewhat treated schools. Since there were very few middle and high schools in the MPS and participation of students in the MPCP was mostly in the elementary grades, I restrict my analysis to elementary schools only.

The control group criteria used here is also based on Hoxby (2003a). Since all schools in Milwaukee were potentially affected by the program, she constructs a control group that consists of Wisconsin schools outside Milwaukee that satisfy the following criteria in the pre-program period: (i) had at least 25% of their population eligible for free or reduced-price lunch (ii) had black students compose at least

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<sup>33</sup> Under the Milwaukee program, all households at or below 175% of the poverty line are eligible to apply for vouchers. Households at or below 185% of the poverty line are eligible for free or reduced-price lunches. However the cutoff of 175% is not strictly enforced (Hoxby (2003b)) and households within this 10% margin are often allowed to apply. Also there were very few students who fell in the 175%-185% range, in fact 90% of the free/reduced price lunch eligible students qualified for free lunch. (Witte (2000)). Students below 135% of the poverty line qualify for free-lunch.

15% of the school population, and (iii) were urban. Her control group consists of 12 schools.

I designate schools that are located outside Milwaukee but within Wisconsin, satisfy the first two criteria above and have locales as similar as possible to the Milwaukee schools as my control schools. (Note that all these characteristics pertain to the pre-program school year 1989-90.) The locales of the Milwaukee schools fall in two categories,—locales 1 (large central city) and 3 (urban fringe of large central city) as classified by the CCD. No Wisconsin school outside Milwaukee has a locale code of 1. My controls schools have locale codes of 2 (middle-size central city), 3 and 4 (urban fringe of mid-size city). Most of them have locale codes of 2, very few have 3 and 4.<sup>34</sup> (See appendix table D.1 for control and more treated group characteristics.) The somewhat treated group in the 66-47 (60-47) consisted of 50.57% (50.99%) black, 3.68% (4.09%) hispanic and 53.6% (55.4%) free or reduced price lunch eligible students.

The control group of schools are demographically somewhat different from the treatment groups. So one can argue that in the absence of the program this group would have evolved differently from the others (Milwaukee schools). However, I have multiple years of pre-program data, and can check for any differences in pre-program trends of the treated and the control groups. This will not only get rid of any level differences between the treatment and control groups, but will also control for differences in pre-program trends, if any. It seems likely that once I control for differences in trends as well as in levels, any remaining difference between the treatment and the control groups will be minimal. In other words, my identifying assumption is that if the treated schools followed the same trends as the control schools in the immediate pre-program period, they would have evolved similarly in the immediate post-program period too. This undoubtedly is an advantage of this study over most other studies (described in the Introduction) since they use a difference-in-differences analysis in levels, which might bias the results.

Using each of these samples, I investigate how the different treatment groups in Milwaukee responded to the “voucher shock” program. For this purpose, I first test whether the pre-program trends of the untreated and the different treatment groups are the same. Second, I estimate OLS and fixed-effects versions of the three specifications (1)-(3) after adjusting for the relevant years, the number of treatment groups and controlling for differences in pre-program trends if there are any.

**2. Continuous treatment variable:** A disadvantage of the above strategy is that it constrains the program effect to be the same for all schools within a treatment group. Therefore, an alternative way to assess the impact of the program is to consider a continuous treatment variable. Here the intensity

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<sup>34</sup> The control group thus constructed contains 33 elementary schools. The 60-47 (66-47) sample consists of 42 (33) more treated, 42 (53) somewhat treated, and 21 less treated schools.

of treatment of schools is proxied by the percentage of their students eligible for free or reduced-price lunches in 1990. There is a wide variation among Milwaukee schools in the percentage of their free or reduced-price lunch students. In 1990, some schools had as few as 22% of their students eligible for free or reduced-price lunches, while others had as large as 93% of their students eligible. Exploiting this variation and using versions of the above three specifications appropriately adjusted for a continuous treatment variable, I investigate whether an increase in the intensity of treatment is associated with higher improvement.

### 5.3 Mean Reversion

There are several factors that might bias the results. I consider these and their potential solutions one by one. First is the issue of mean reversion. Mean-reversion is the statistical tendency whereby high or low scoring schools tend to score closer to the mean subsequently. Since the F schools were low scoring in 1999, a natural question to ask would be whether the improvement in Florida is driven by mean reversion rather than the program. Since I do a difference-in-differences analysis, my estimates will be contaminated by mean reversion only if F schools mean revert to a greater extent than the D schools and/or the C schools.

For a first pass at the mean-reversion issue, I investigate whether the schools that were low scoring in 1998 were also low scoring in 1999. Interestingly, in each of reading, math and writing, 70% of the schools that ranked in the bottom tenth percentile in 1998 also ranked in the bottom tenth percentile in 1999. This implies that although there may be mean reversion, it may not be a major problem.

A more direct way to approach mean-reversion would be to check by how much the schools that received an “F” grade in 1998 improved during 1998-1999 compared to those that received a “D” (or “C”) grade in 1998. Since this was the pre-program period, the gain can be taken to approximate the mean reversion effect and can be subtracted from the post-program gain of F schools compared to D schools (or C schools) to get at the mean-reversion corrected program effect.

The accountability system of assigning letter grades to schools started in the year 1999. The pre-1999 accountability system classified schools into four groups I-IV (I-low, IV-high). However, using the state grading criteria and data on percentage of students in different achievement levels in each of FCAT reading, math and writing, I was able to assign letter grades to schools in 1998.

The state assigned school grades based on FCAT reading, math and writing scores. In FCAT reading and math, it categorized students into five achievement levels (1-5) that correspond to specific ranges on

the raw-score scale. Using current year data, it designated a school an “F” if it was below the minimum criteria in reading, math and writing, a “D” if it is below the minimum criteria in one or two of the three subject areas, and “C” if it is above the minimum criteria in all three subjects but below the higher performing criteria in all three. In reading and math at least 60% (50%) of the students had to score level 2 (3) and above while in writing at least 50% (67%) had to score 3 and above to meet the minimum (higher performing) criteria in that respective subject.) The schools that were assigned grades “F”, “D” or “C” in 1998 using this criteria will henceforth be called the 98F schools, 98D schools, and 98C schools, respectively.

I also use an alternative strategy to get around the problem of mean reversion in Florida. In this strategy, I consider F and D schools that fail the minimum criteria in the same subject area in 1999 and compare their improvements in that subject area using specifications (1)-(3). I do this separately for reading, math and writing. The notion here is that the improvement (if any) of the F schools in a subject area when compared to similar scoring D schools in that subject area should not be contaminated by mean reversion. This is because mean reversion is likely to rise in a certain subject area only if the F schools are low scoring relative to the D schools.<sup>35</sup> The results obtained from this analysis are similar to the mean reversion corrected effects obtained from the above method and hence are not reported here.

Although the Milwaukee program is not conditional on low performance of schools, the more treated schools were also among the lowest scoring schools in each of the subject areas before the program. Therefore the treatment effect in Milwaukee can also be contaminated by mean reversion. To address the issue of mean reversion in Milwaukee, once again I use data from the pre-program period. I investigate whether the schools that in 1989 were similarly low scoring (details in next paragraph) as the more treated schools in 1990, improved relative to the control schools during 1989-90. If they did, then this improvement can be attributed to mean reversion as this was before the program.

To implement this strategy, I rank the Milwaukee schools on the basis of scores in each subject, and calculate mean reversion based on ranks of schools in that subject. For example, ranking schools in 1990 based on their reading scores, I note the ranks of the more treated, somewhat treated and less treated schools. Then I rank the schools in 1989 based on their 1989 reading scores and pick schools that have

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<sup>35</sup> Note that a potential problem here is that although F and D schools are both below the minimum criteria in the subject under consideration, their locations on the score scale may not be very similar. For example, if F schools are relatively low scoring compared to the relevant D schools in spite of both groups being below the cutoff, this strategy cannot completely purge the program effect of mean reversion. To take care of this problem I also compare F and D schools which are not only below the cutoff in the same subject area but also have similar scores in the relevant subject in 1999. The results remain very similar.

the same rank as the more treated schools in 1990 and call them the “low” group. Similarly I construct the “mid” and “high” groups in 1989 corresponding to the somewhat treated and less treated groups in 1990. If the “low” group thus constructed exhibit an improvement relative to the control schools in reading during 1989-90, I call this the mean reversion effect in reading and subtract it out from the more treated program effect in reading obtained earlier to arrive at the mean reversion corrected effect in reading. Similarly, based on ranks of schools in each of the other subjects in 1989 and 1990, I calculate the mean reversion corrected effect in the corresponding subjects.

#### 5.4 Regression Discontinuity Analysis

An alternative way to get around the problem of mean reversion is to do a regression discontinuity analysis.<sup>36</sup> The Florida program has created a highly non-linear and discontinuous relationship between school achievement and the probability that the school’s students would become eligible for vouchers in the near future. The regression discontinuity strategy here is to compare the improvement of F schools just below the cutoff between “F” and “D” with D schools just above the cutoff.

Based on the state grading criteria (see last page), I construct a discontinuity sample where both F and D schools fail to meet the minimum criteria in reading and math in 1999, while in writing, only F schools fail the minimum criteria. Here the probability of treatment varies discontinuously as a function of a smooth, continuous variable, the percentage of students scoring at or above 3 in 1999 FCAT writing. There is a sharp cutoff at 50%. Schools in this sample below 50% face a direct threat, while those above 50% face no such direct threat.

Using the sample of F and D schools that fail minimum criteria in both reading and math in 1999, Figure 3 Panel A illustrates the relationship between assignment to treatment (i.e. facing the threat of vouchers) and the schools’ percentages of students scoring at or above level 3 in FCAT writing. The figure shows that except one, all schools in this sample that had less than 50% of their students scoring below 3 recieved an F grade. Similarly, all schools (except one) in this sample that had 50 or a larger percentage of their students scoring at or above level 3 were assigned a D grade. Note that many of the dots correspond to more than one school,—Figure 3, Panel B illustrates the same relationship where the size of the dots are proportional to the number of schools at that point. The smallest dot corresponds to one school. These two panels show that in this sample, percentage of students scoring at or above 3

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<sup>36</sup> The regression discontinuity design was introduced by Thistlethwaite and Campbell (1960). This design has subsequently been developed and used by several papers such as Angrist and Lavy (1999), Hahn, Todd and Van der Klaauw (2001), Van der Klaauw (2002), Jacob and Lefgren (2004a, 2004b), Chay et al.(2003) etc.

in writing uniquely predicts (except two schools) assignment to treatment and there is a discrete change in the probability of treatment at the 50% mark.

Ranking schools in terms of percentage of students scoring above 3 in FCAT writing, I first pick schools that are within 8 points ( $\pm 8$ ) of the 50% cutoff and investigate the improvement of the F schools in this sample with that of the D schools. I call this sample discontinuity sample 1. It contains 33 F and 70 D schools. Next, I further shrink the sample and pick schools within  $\pm 5$  points of the cutoff (discontinuity sample 2).<sup>37</sup> This sample has 22 F and 53 D schools. I also consider two corresponding discontinuity samples where both groups fail the minimum criteria in reading and writing (math and writing). F schools fail the minimum criteria in math (reading) also, unlike D schools. In these samples, the probability of treatment changes discontinuously as a function of the percentage of students at or above level 2 in math (reading) and there is a sharp cutoff at 60%.

## 5.5 Stigma Effect of Getting the Lowest Performing Grade

A second concern in Florida is that there may be a stigma effect of getting the lowest performing grade F. If there is such a stigma, then the F schools will try to improve merely to avoid this stigma rather than in response to the program. I use several alternative strategies to investigate this issue. First, although the system of assigning letter grades to schools started in 1999, Florida had an accountability system in the pre-1999 period when schools were categorized into four groups 1-4 (1-low, 4-high) based on FCAT writing and reading and math norm referenced test scores. Using FCAT writing data for two years (1997 and 1998), I investigate whether the schools, which were categorized in group 1 in 1997, improved in relation to the 1997 group 2 and group 3 schools during the period 1997-98. The rationale here is that if there is a stigma effect of getting the lowest performing grade, the group 1 schools should improve in comparison to the group 2 and 3 schools even in the absence of the TOV program. I do not use the pre-1999 reading and math norm referenced test (NRT) scores for the following reasons. In reading and math, different districts used different norm referenced tests (NRTs) during this period, which varied in content and norms. Further, the same district often chose different NRTs in different years. Therefore these NRTs were not comparable across districts and across time. Moreover, since the districts could choose the specific NRT to administer (from among a set of NRTs) in each year, the choice is likely to be related to time varying (and also time-invariant) district unobservable characteristics which also affect test scores.

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<sup>37</sup> The intervals are picked so that the number of schools in each of the F and D categories are not too small.



Second, all the schools that received an F in 1999 received higher grades (A,B,C,D) in the years 2000, 2001, 2002. Therefore although the stigma effect on F schools may be operative in 2000, this is not likely to be the case in 2001 or 2002 since none of the F schools got an F in the preceding year (2000 or 2001 respectively). However the F schools would face threat of vouchers till 2002, so any improvement in 2001 and 2002 would provide evidence in favor of the TOV effect and against the stigma effect. Third, as I argue at the end of the results of the stigma effect exercise (page 29), it is not clear that stigma effect would dictate a relative improvement of F schools in comparison to the D schools in the first place, while threat of voucher would certainly drive/dictate such a difference.

## 5.6 Size of the Milwaukee Program

The Milwaukee program saw a major shift and entered into its second phase when following a 1998 Wisconsin Supreme Court ruling, the religious schools were allowed to accept choice students for the first time in the 1998-99 school year. (I will refer to the post-shift period as second phase Milwaukee or Milwaukee phase II.) As table 8 shows, this led to a massive increase in the number of MPCP schools and students and the MPS membership fell for the first time. The number of students allowed to participate in the MPCP was initially capped at 1% and subsequently raised to 1.5% in 1993-94 and 15% in 1996-97. Although this constraint was never binding, the number of private school seats was. Therefore with the entrance of the religious schools, there was a considerable expansion of the program. In the second phase, the number of voucher seats as well as the number of students allowed exceeded the number of applicants. Moreover, there was a considerable private school presence—27% of the public schools had at least 1-2 voucher schools within a one mile radius, 20% had 3-5, 30% had 6-10 and 13% had more than 11 voucher schools within a one mile radius.

It is tempting to compare the treatment effect in Florida with that in Milwaukee phase II also. However, it is not clear whether this comparison is legitimate. Except for the “TOV” versus “VS” component, the other features of the two programs were very similar and comparable between Florida and Milwaukee phase I (as described in the introduction). However this was not so in phase II. Due to some funding changes, the voucher amount (\$5,220 on average) as well as the revenue loss per student per year was much higher<sup>38</sup> in Milwaukee Phase II than in either Florida or Milwaukee Phase I. Moreover, in Florida we observe the effect of the program only in its first three years while in Milwaukee Phase II we observe the program 9-12 years after it was first implemented. It is reasonable to expect that adjustments

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<sup>38</sup> For an analysis of the changes in the voucher program in Milwaukee phase II and their effects, see Chakrabarti (2004)

and/or effects of adjustments take time to get reflected in test scores. Since each of these would indicate a higher response in Milwaukee Phase II, it is not clear that the effect of the Florida program will still be higher than that in Milwaukee Phase II. In spite of these problems, section 6 compares the treatment effect in Florida with that in Milwaukee Phase II, but the results should be interpreted with the above caveats in mind.

## 5.7 Sorting

Another issue relates to sorting in the context of Milwaukee. Vouchers affect public school quality not only through direct public school response but also through changes in student composition and peer quality brought about by sorting. All these three factors get reflected in the public school scores.<sup>39</sup> This issue is important in Milwaukee since over the years students have left the MPS with vouchers. In Florida, on the other hand, no school became eligible for vouchers in the years 2000 or 2001. Therefore the program effects in Florida (for each of the years 2000, 2001 and 2002) are not likely to be contaminated by this factor.<sup>40</sup> Moreover, the demographic compositions of the different groups of schools remain very similar for the different years under consideration (see the end of this subsection).

To consider the issue in Milwaukee, the following points may be noted. First, the empirical part of the paper seeks to test the theoretical prediction that the quality under the Florida program will exceed that under the Milwaukee program (Corollary 1), where quality is a combination of public school effort and peer quality, so there is a one to one correspondence between the theory and empirics. Second, each of the regressions control for demographic composition of schools (example, racial and sex compositions of schools and % of students eligible for free or reduced price lunches). However any change in student composition in terms of unobservable factors may not be controlled for by these factors. (It may be noted that inclusion of demographic controls do not change results by much, either in Florida or in Milwaukee.) Third, the number of students that left the MPS with vouchers, at least in the first phase, do not constitute a major part of the MPS population (see table 8) so that it is not likely to cause a major change in peer composition of schools.

Finally, to investigate this issue, I examine whether the demographic composition of the different Milwaukee treated groups changed over the years. I run the same three specifications as above except that the dependent variable of school scores is replaced by the respective demographic variable (% black,

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<sup>39</sup> See Hsieh and Urquiola (2003) for a discussion.

<sup>40</sup> Note that this does not mean that the Florida program was not credible. 10 schools got a second F in 2002, 9 schools in 2003 and 21 schools in 2004, and all their students became eligible for vouchers.

% hispanic etc.). The results are not reported here for lack of space but are available on request. I do not find evidence of changes in demographic composition of schools, in either phase I or phase II. Only a few of the coefficients are statistically significant and they are always very small in magnitude. They imply changes of less than 1%, more precisely, ranging between 0.22% and 0.80%. This provides suggestive evidence that sorting was not an important factor. It may be noted that I did the same exercise for Florida also,—there is no evidence of any relative shift of the demographic composition of the F schools in comparison to the D or C schools.

## 6 Results

### Florida

In Florida, investigation of pre-program trends for writing (1994-99), and reading and math (1998-99) reveal that F schools have no significant differences in trend compared to D schools in reading and math, although they exhibit a small negative differential trend in writing. (These results are not reported here but are available on request. Whenever there is a difference in pre-program trends, the regressions reported control for these differences by including interactions between trend and the respective treatment dummies.<sup>41</sup> Table 1 presents the effects of the Florida TOV program on F school reading, math and writing scores as compared to the D schools. For reading, the first two columns report results from the linear model 1, the next two columns from model 2 and the final two columns from the non-linear model 3. Both OLS and fixed effects (FE) estimates in the first two columns show positive intercept and trend shifts for the F schools, although the latter is not significant in the fixed-effects estimate. The results from model 2 corroborate this evidence. These effects are disaggregated in columns (5) and (6) where the coefficients reflect the effects of the program after one, two and three years. Both the OLS and fixed-effects estimates show positive and significant year effects in each of the years after program.

For math and writing, the first column reports results from the linear model 1, next column from model 2 and the final column from non-linear model 3.<sup>42</sup> In math, there is a positive, significant, large intercept shift after the program although there is no evidence of any trend shift. Column (9) shows

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<sup>41</sup> When data are available for only two years before program (for example, reading and math), the pre-program difference between treatment and control groups can be either a trend difference or a year effect. Specifications 1 and 2 control for this pre-program difference assuming it is a trend difference, and specification 3 controls for it assuming this difference is a year effect. Results from regressions without controlling for these pre-program differences are qualitatively similar.

<sup>42</sup> In many of the tables, only the fixed effects estimates are reported. The OLS results are very similar to the FE estimates and hence are omitted.

evidence of positive significant F school year effects in math in each of the three years after the program. In writing, columns (10)-(11) show positive and statistically significant intercept and trend shifts for the F schools. The last column shows positive, significant year effects in writing in each of the three years after the program. Figure 1 graphs the predicted values from OLS estimation of the linear model. It confirms that 1999 has been the watershed year. In each of reading, math and writing, the F schools have improved relative to the D schools after the program, and the gap between F schools and D schools has undoubtedly narrowed.

Next, considering D schools as an additional treatment group, table 2 looks at the effect of the program on F (more treated) and D (less treated) schools as compared to the C schools. For each of reading, math and writing, the first two columns present results from model 1, the last two columns from the unrestricted model 3.<sup>43</sup> (Results from model 2 are similar and hence are not reported.) In reading, F schools exhibit positive significant trend and intercept shifts that exceed the corresponding shifts of the D schools. In both math and writing, F schools exhibit positive, significant and large intercept shifts that are statistically greater than that of D schools. Columns (3)-(4), (7)-(8) and (11)-(12) show positive significant year effects in reading, math and writing for F schools in each of the years after program. Although many of the D school effects are also positive significant, the F school shifts are statistically larger in each of the years.<sup>44</sup>

To summarize, using different samples, different subjects, different specifications, and both OLS and FE estimates, the results above show considerable improvement of the F schools after the program in comparison to the control schools. Although D schools show non-negligible improvement (at least in reading and writing), their improvement is considerably smaller and also statistically different from those of F schools. However, as argued above, these effects may not necessarily reflect the effect of threat of vouchers, rather they may be contaminated by other factors such as mean reversion and stigma effect.

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<sup>43</sup> Compared to C schools, F schools exhibit a negative differential trend in reading and writing, but no significant differential trend in math. D schools exhibit a negative trend in reading and positive trend in math and writing in comparison to the C schools. Results are not reported here but are available on request.

<sup>44</sup> In 2002, although the state still continued to grade schools on the scale of "A" through "F", the grading criteria was changed to include value added scores in addition to levels. However, since the grades were still based on FCAT scores and the F schools anticipated vouchers if they got a second F in 2002, similar incentives continued to play in 2002. Also, the grading rule changes were announced in December 2001, while the tests were held in February and March 2002, so that there was very little time for schools to change their behavior in the wake of the new grading rule changes. Moreover, the results are very similar if the year 2002 is dropped and the analysis is repeated with data through 2001. Also, it should be noted here that the F schools and D schools (especially, the F schools) received additional funds from the state. However, all the results above are obtained after controlling for real per pupil expenditure. The results are not sensitive to inclusion of real per pupil expenditure, nor do they change after including a polynomial in real per pupil expenditure. Moreover, even in the pre-1999 period, the critically low performing schools received extra assistance,—however this did not result in improved performance of this group in this period, as table 7 shows in a different context.

I will consider these issues later.

### **Milwaukee**

Using the 66-47 sample, table 3 looks at the effect of the Milwaukee “voucher shock” program on WRCT (% above), ITBS reading, and ITBS math scores of different treatment groups.<sup>45</sup> Except the positive and statistically significant effect in WRCT reading in its second year, there is no other statistically significant evidence of any effect of the program.<sup>46</sup> Although many of the effects are positive, they are often not statistically significant and do not always have the right hierarchy (example, the somewhat treated effects often exceed the corresponding more treated effects). Although the second year somewhat treated effect in ITBS math is statistically significant, it is more than the corresponding more treated effect.<sup>47,48</sup> Figure 2 graphs the predicted values from the OLS regressions for the linear model using ITBS scores. As expected, there is no evidence of any program effect. The last column considers a continuous treatment variable and proxies the intensity of treatment of schools by its pre-program (1990) percentage of students who are eligible for free or reduced price lunches. It looks at the effect of an increase in treatment intensity on WRCT scores after one, two and three years after program. There is no evidence of any improvement with an increase in treatment intensity. (Results from the other models and OLS specifications are qualitatively similar.)

Thus the results in Milwaukee are mixed. However, it is safe to say that there is no evidence of any negative effect of the “voucher shock” program. The program seems to have had a positive and significant effect in the second year after program, at least in WRCT. These results seem to be robust in that they are replicated in the analysis with other samples. (These are not reported here but are available on request.)

### **Mean Reversion**

However, as argued above, the effects in both Florida and Milwaukee may be biased by mean reversion. Using data for 1998 and 1999 in Florida, Panel A of table 4 finds that in comparison to the 98D schools,

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<sup>45</sup> Estimation of pre-program trends (using 1987-90 for ITBS reading and math, and 1989-90 for WRCT reading) show no statistical difference in trends between the different treatment and control groups in any of the subject areas. These results are available on request.

<sup>46</sup> Results from model 2, OLS estimates of the three models and results from regressions using WRCT (% below) scores are similar and hence are not reported here. Results for the less treated group do not add any new insight and hence are omitted. These results are available on request.

<sup>47</sup> Since the ITBS was administered in Milwaukee as a district assessment program, I do not have data on non-Milwaukee Wisconsin schools for this test. As a result, my comparison group here will be the less treated group of schools. Since the comparison group is also treated to some extent, I expect my estimates for the ITBS to be underestimates.

<sup>48</sup> Note that although the more treated school effects are jointly significant for the WRCT scores in model 1 at 10% level, they are no longer jointly significant either in the non-linear model or for the ITBS reading and math scores, although the individual coefficients are often positive and non-negligible in magnitude.

the 98F schools show no evidence of mean reversion either in reading or math although there is mean reversion in writing. In comparison to the 98C schools (Panel B), there is no evidence of any mean reversion in reading; both 98D schools and 98F schools show comparable amounts of mean reversion in math; and only 98F schools show mean reversion in writing. There is no evidence of any mean reversion in Milwaukee so those results are not reported here.

### **Florida Versus Milwaukee**

Since Florida and Milwaukee belong to different regions, I first argue that the comparison of the program effect in Florida with that in Milwaukee is fair and reasonable. First, as shown in the introduction, apart from the TOV versus VS components in Florida and Milwaukee respectively, the other features of the program were very similar. In both programs, private schools could not discriminate between choice applicants. Also, the method of funding of the two programs, the average voucher amounts and the per pupil revenue losses from vouchers were very similar. Second, state and local revenues constituted very similar proportions of total revenue during the relevant periods,—the percentage of revenue coming from state and local sources were respectively 51% and 41% in Florida and 55% and 36% in Milwaukee. Third, as shown in table D.1, the demographic characteristics of the more treated and control schools in Florida were very similar, both economically and statistically, to those of the more treated and control schools in Milwaukee. Fourth, I also repeat my analysis by comparing the improvement in Milwaukee with that of a large urban district in Florida, Miami Dade County (which is also the largest school district in Florida). The results are very similar and hence not reported here. Finally, and perhaps most importantly, since I follow a difference-in-differences strategy in trends, any level or even trend differences between the two regions (that are common to schools in that region) are differenced out. It is unlikely, that any remaining difference, which differentially affects the trends in the two regions *only* in the post-program period, will be large.

Table 5 compares the effects of the Florida and Milwaukee programs on the respective more treated schools both before and after correcting for mean reversion. Table 5 figures are based on those in tables 2, 3 and 4 and all figures are expressed in terms of the respective sample standard deviations. The comparison results presented here correspond to the non-linear model, the results from the other models are similar. Pre-correction results show positive and significant effect sizes in each of the years and subject areas which always exceed the corresponding Milwaukee effect sizes (which are not significant except in second year reading). Mean reversion corrected effect sizes are obtained by subtracting the effect size attributed to mean reversion (obtained from expressing the relevant coefficients in table 4,

panel B in terms of respective standard deviations) from the F school effect sizes in each of the three years after program. The estimates in reading are the same as earlier. In math, although the effect sizes fall in Florida, they are still positive and considerably larger than those in Milwaukee.<sup>49</sup> The effect sizes in FCAT writing in the first, second, third years are respectively 0.74, 0.70 and 0.74 before correcting for mean reversion. No writing test data are available in Milwaukee during the relevant period. As seen in table 4, the mean reversion effect is largest in writing. Mean reversion correction leads to dampening of the estimates, but they are still positive and not small in magnitude—being 0.29, 0.25 and 0.29 in the first, second and third years after program respectively.<sup>50</sup> These results provide evidence in favor of both the theoretical predictions. It should be noted that since none of the F schools got an “F” in either 2000 or 2001, the mean reversion corrected effect sizes attributed to the Florida program in the second and third years may be underestimates.

### **Regression Discontinuity**

Next, I do a regression discontinuity analysis. The summary characteristics of the F schools and D schools in the discontinuity sample 1 are shown in Table 6A. The F schools and D schools in the discontinuity sample are strikingly similar to each other both in terms of pre-program demographic characteristics and scores. Using discontinuity sample 1, Figure 3, panels C-H show that for each of the years 2000 and 2001 and in each of the subject areas, there is a sharp drop at the cutoff suggesting a positive effect of the program on the treated schools. (The corresponding graphs for 2002 are similar and hence skipped.) Using discontinuity sample 1, table 6B shows the results from estimating most unrestricted specification (3). (Results for the other two specifications are similar and hence are not reported.) There are positive and statistically significant effects in all the three years after program. Interestingly, the results appear to be comparable or larger in reading and math and smaller in writing. This is consistent with the earlier finding of mean reversion in writing unlike in reading and math. The results reported here control for socioeconomic characteristics of schools. I also run alternative regressions that do not control for these

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<sup>49</sup>I also do a pair-wise non parametric test (sign test), where I ignore the significance of coefficients and consider only their signs. Under the null of equal effects the probability that any one effect size in Florida exceeds the corresponding one in Milwaukee is  $\frac{1}{2}$ . Under the null,  $D = \text{Florida effect} - \text{Milwaukee effect}$  follows a binomial distribution.  $D$  is positive in all cases. The probability of getting all positive  $D$  under the null is very small and hence the null of equal effects can be comfortably rejected.

<sup>50</sup> Consistent with the above findings, there is considerable anecdotal evidence that suggests that F schools have responded to the program. Escambia county implemented a 210-day extended school year in its F schools (typical duration was 180 days), implemented an extended school day at least twice a week, added small group tutoring in afternoons and Saturdays and longer time blocks for writing and math instruction. Palm Beach County targeted its fourth grade teachers for coaching and began more frequent and closer observations of teachers in its F schools. (For more evidence, see Innerst, 2000.) In the words of Carmen Varela-Russo, associate superintendent of technology, strategic planning and accountability, Broward County Public Schools, “People get lulled into complacency”. . . “the possibility of losing children to private schools or other districts was a strong message to the whole community.”

characteristics as well as regressions that control for a continuous measure of the selection variable (a polynomial in % of students scoring at or above level 3 in writing in 1999). The results are very similar. The results from the discontinuity sample 2 as well as those obtained from the other discontinuity samples described earlier are similar and hence are not reported here. These results further confirm that the F schools have responded to the program. (Note that the regression discontinuity analysis is likely to produce underestimates since D schools are treated to some extent, although indirectly.)

### **Stigma Effect**

Table 7 investigates whether there is a stigma effect of getting the lowest performing grade using pre-program FCAT writing scores. The logic, as outlined earlier, is that if there is such a stigma effect, then the lowest performing schools (group 1) should improve in relation to the group 2 and group 3 schools in the pre-program period 1997-98. Table 7 shows that there is no evidence that this has been the case.

Second, as shown earlier, the F schools showed strong gains in both 2001 and 2002. As discussed earlier, the stigma effect is not likely to have operated in these years, since the prior-year grade was not an F. This provides further evidence in favor of the TOV effect and against the stigma effect.

Third, note that the above discussion assumes that if there is a stigma effect associated with getting an F, this would induce a *relative improvement* of the F schools in comparison to the D schools. However, it is not clear that this would be the case in the first place. Stigma is the “bad” label that is associated with getting an F. Since the D schools are very close to getting F, and if F grade carries a stigma, then they should be threatened by the stigma effect also. In fact, one might argue that since D schools are unscarred while F schools are already scarred, the former will have a larger inducement to improve to avoid the scar. The bottomline is that even if there is a stigma effect, it should not dictate a relative improvement of the F schools in comparison to the D schools. Rather any such improvement should be the effect of TOV, because it is the F schools that are directly threatened by vouchers, not the D schools. It may be added that the regression discontinuity analysis considers D schools that are very close to getting F and literally at the margin of F. If there is a stigma effect associated with the F grade, then these D schools should certainly be affected by it. Since the regression discontinuity analysis shows an improvement of the F schools over D schools, it provides strong evidence in favor of the TOV effect, and against the stigma effect that the relative improvement of the F schools is driven by their relative response to stigma.

### **Size of the Milwaukee Program**

Since the competitive effect of the Milwaukee program is likely to have been larger in the second



phase than in the first,<sup>51</sup> table 9 compares the effect of the Florida program with that in Milwaukee phase II. The first four columns present estimates before correcting for mean reversion, while the last four columns present mean-reversion corrected estimates. All figures are in terms of sample standard deviations. The Florida effects are the same as earlier. The Milwaukee estimates correspond to non-linear regressions<sup>52</sup> run on the WKCE reading and math test scores (1997-2002) using the 66-47 sample. While interpreting these results, it should be remembered that the caveats mentioned earlier are likely to bias the Milwaukee phase II effects upwards. In spite of that, the Florida effects for each of the years and each of the subject areas, and both before and after mean reversion correction are larger than the corresponding Milwaukee estimates except second year reading (which are the same).

## 7 Other issues and robustness checks

### Has there been “teaching to the test” in Florida?

In Florida, FCAT is the high stakes test as its scores are used to calculate school grades. The above analysis focuses on high stakes test scores in Florida. Since the threat in the Florida program is given in terms of grade, the *response* of the Florida threatened schools should be assessed in terms of the high-stakes test. For example, even if it is found that there has been no improvement in the low stakes scores, it cannot be concluded that the public schools have not responded to the TOV program. The improvement will be reflected in the low stakes test only in so far as the gains in the high stakes test spill over to the low stakes test. In fact, any finding of teaching to the test, manipulation of the test-taking pool etc. are entirely consistent with the finding of F school response in this paper,—they would provide further evidence that the schools have responded to the program. The notion here is that if the public schools are found to unambiguously respond to the TOV program by increasing effort, then the other issues of teaching to the test, manipulation of the composition of the test taking population can be more easily taken care of by policy—for example, by broadening the curriculum to include all desirable areas and topics and using the test scores of all grades and students (for example, all special education and limited english proficient students also) for school grade computation purposes. Moreover, as Hanushek and Raymond (2003) argue, “teaching to the test” can only have a one-time effect on school scores.

Nevertheless, I investigate this issue by looking at the reading and math scores from the low stakes

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<sup>51</sup> Chakrabarti (2004) shows that the improvement in Milwaukee phase II has been larger than that in Milwaukee Phase I. The estimates for Milwaukee phase II are taken from that paper and are available on request.

<sup>52</sup> These regressions include year dummies and interactions of year dummies with more treated, somewhat treated and less treated group dummies. Mean reversion effects for Milwaukee phase II are computed using the same strategy as that for mean reversion in Milwaukee phase I except that the years 1989 and 1990 are replaced by 1997 and 1998 respectively.

Stanford 9 test, which was not used in the assignment of school grades. While the Stanford 9 test also contains multiple-choice questions, it places more emphasis on critical analysis in reading and problem-solving strategies, evaluating expressions, and solving linear equations in math compared to the FCAT. Table 9 uses data on Stanford 9 test scores for 2000-02. Since this test was first administered in 2000, no pre-program data are available. Prior to 2000, the districts used a variety of nationally normed tests which not only varied in content but the norms were also different.<sup>53</sup> As a result, these data are not comparable across districts, years, or with the post-program Stanford 9 data. Therefore, the pre-2000 data are not used here.

Table 10 panel A shows very high correlation between FCAT and Stanford 9 for both level scores and first difference in scores, for each of the subject areas tested and for each of the F schools, D schools, C schools, and all schools. The implication is that the FCAT results should be replicated in Stanford 9 also. Using Stanford 9 scores for 2000-02, panel B shows that F schools and D schools show positive and significant improvement in all grades and subjects and in most cases the F school effect exceeds the corresponding D school effect, even though the effects are not always statistically different between groups. Note that the effects are likely to be underestimates as all these results are relative to the 2000 gains (which judging from the FCAT estimates are quite high). The overall picture is consistent with the FCAT picture earlier. Up to 2001, the FCAT reading and math scores only in grades 4 and 5, respectively, were used for school grade computation. Interestingly, the 2001 F school improvement in reading is largest in grade 4. However for math, the 2001 F school gain is smallest in grade 5. To summarize, from the limited data that are available, the results are mixed. There is some evidence in favor of “teaching to the test”, but there is some evidence to the contrary also.

### **PAVE and Chapter 220 Programs**

Two other choice programs in Milwaukee are worth mentioning and it is important to rule them out as explanations for the pattern of results obtained. Chapter 220 Program, established in 1978 and further expanded in 1987, caters to the goal of metropolitan integration. It allows minority students from the MPS to attend public schools in the twenty four suburban districts, while white students from the suburbs may enroll in the MPS. The voucher program effects in Milwaukee are not likely to be contaminated by this program since this program started much before the MPCP, controlling for differences in pre-program trends between treatment and control schools gets rid of any effect of the Chapter 220 program, more so because the size of the latter program was relatively stable for the years

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<sup>53</sup> See the Florida department of education website at website <http://www.firn.edu/doe/sas/nrthome>

under consideration in this paper.

The PAVE (Partners Advancing Values in Education) program was established in 1992 and it came into operation from the 1992-93 school year. This is a privately funded school choice program that allows students at or below 185% (revised to 175% in 1995-96) of the poverty line in the city of Milwaukee (not just the MPS) to attend any private school in Milwaukee. Unlike the MPCP, PAVE covers only one-half of the private school tuition requiring the parents to match the other half. Although the initial participation in PAVE was not negligible, it petered out after the expansion of the Milwaukee program in 1998 and currently stands at approximately 700 students per year. However, the proportion of students transferring from the MPS is small, always constituting less than one-third of the total PAVE population, so that the number of students leaving the MPS under PAVE has always been much smaller than under MPCP. Moreover since PAVE required the scholarship to be topped up, overwhelmingly white and more advantaged households participated in the PAVE and the demographic composition of the PAVE students differed substantially from that of the MPCP students. The more-treated schools in this paper are predominantly black and hence are not likely to be strongly affected by PAVE. Moreover, there is no evidence of any trend shift in scores of the different treatment groups in 1992-93, the first year after PAVE. Finally, if anything PAVE will lead to overestimates, not underestimates, of the Milwaukee program.

## 8 Conclusion

This paper examines the role of vouchers as instruments of public school reform. It makes several important contributions in this context. First, it argues that voucher design matters,—differences in voucher designs affect public school incentives differently and hence induce different responses from them. Therefore, understanding the effect of different voucher designs is essential to the formulation of effective voucher policies. This study contributes in this direction by comparing the effects of two U.S. voucher programs—Florida and Milwaukee—that differ fundamentally in their designs. The Florida program is a “threat of voucher” program that first threatens the failing schools with vouchers and vouchers are introduced only if they fail to meet a certain government designated quality cutoff. The Milwaukee program, on the other hand, is a “voucher shock” program with a sudden government announcement that all low income public school students would be eligible for vouchers. In the context of an equilibrium theory of public school and household behavior, this paper argues that the Florida-type program should bring about an unambiguous improvement in public school performance and this improvement should

exceed the improvement (if any) in the Milwaukee-type program. Using data from Florida and Milwaukee, and a difference-in-differences estimation strategy in trends, it then demonstrates that these findings are validated empirically. These findings are reasonably robust to alternative specifications and samples, continue to hold after adjusting for mean-reversion and survive a regression discontinuity analysis.

Second, it also has important contributions from a theoretical point of view. It provides micro-foundations to the public school payoff function and derives the demand for public school from equilibrium household behavior. Moreover, it endogenously determines public school peer group quality, effort and quality at the respective program equilibria. Third, the findings have important policy implications which are all the more relevant in the context of the present concern over public school performance.

## Appendix A: Proofs of results

**Existence of Equilibrium:** *A Household Equilibrium always exists.*

**Proof.** This result can be proved in the following steps:

(i) Define  $\Phi : [0, 1] \rightarrow [0, 1]$  such that for all  $b' \in [0, 1]$ ,  $b = \Phi(b') = \frac{\int_0^1 \int_0^{\hat{\alpha}(y, b', \cdot)} \alpha d\alpha dy}{\int_0^1 \int_0^{\hat{\alpha}(y, b', \cdot)} d\alpha dy}$ .

Define a function  $F$  such that  $F(\hat{\alpha}) = \frac{\int_0^1 \int_0^{\hat{\alpha}} \alpha d\alpha dy}{\int_0^1 \int_0^{\hat{\alpha}} d\alpha dy} = \Phi(b')$ .

(ii)  $\hat{\alpha}(y, b', \cdot)$  is continuous in  $b'$  (from 3.1.1a).  $F(\hat{\alpha})$  is continuous in  $\hat{\alpha}$  (as both numerator and denominator are continuous in  $\hat{\alpha}$  and  $0 < \hat{\alpha} < 1$  ensures that the denominator is non-zero). Therefore  $\Phi$  is a continuous function from  $[0, 1] \rightarrow [0, 1]$ .

(iii) Since  $[0, 1]$  is non-empty, compact and convex and  $\Phi$  is continuous, there exists at least one fixed point  $b^* = \Phi(b^*)$  by Brouwer's fixed point theorem.

**Uniqueness of Equilibrium:**

While a household equilibrium always exists, it may not be unique. To see this differentiate (3.1.2) with respect to  $b^e$  to find that

$$\frac{\delta g}{\delta b^e} = \frac{1}{N(b^e, \cdot)} \int_0^1 (\hat{\alpha}(y, b^e, \cdot) - b) \cdot \frac{\delta \hat{\alpha}}{\delta b^e} dy \text{ where } N(b^e, \cdot) = \int_0^1 \hat{\alpha}(y, b^e, \cdot) dy$$

**Proof of  $\frac{\delta g}{\delta b^e} > 0$ :**

Consider the sign of:

$$\int_0^1 (\hat{\alpha}(y, b^e, \cdot) - b) dy = \int_0^1 [\hat{\alpha}(y, b^e, \cdot) - \frac{1}{N(b^e, \cdot)} \int_0^{\hat{\alpha}(y, b^e, \cdot)} \alpha d\alpha] dy \quad (\text{A.1}).$$

The sign of  $[\hat{\alpha}(y, b^e, \cdot) - \frac{1}{N(b^e, \cdot)} \int_0^{\hat{\alpha}(y, b^e, \cdot)} \alpha d\alpha]$  will be the same as

$[\hat{\alpha}(y, b^e, \cdot) \cdot N(b^e, \cdot) - \int_0^{\hat{\alpha}(y, b^e, \cdot)} \alpha d\alpha] = \hat{\alpha}(y, b^e, \cdot) [\int_0^1 \hat{\alpha}(y, b^e, \cdot) dy - \frac{\hat{\alpha}(y, b^e, \cdot)}{2}]$ . This is positive since

$\hat{\alpha}(y, b^e, \cdot) > 0$  and  $\int_0^1 \hat{\alpha}(y, b^e, \cdot) dy - \frac{\hat{\alpha}(y, b^e, \cdot)}{2} > 0$ . Therefore  $\int_0^1 (\hat{\alpha}(y, b^e, \cdot) - b) dy > 0$ . Intuitively, the

positive sign can be seen from (A.1). For each  $y$ ,  $\hat{\alpha}(y, b^e, \cdot) > \frac{\int_0^{\hat{\alpha}(y, b^e, \cdot)} \alpha d\alpha}{\int_0^{\hat{\alpha}(y, b^e, \cdot)} d\alpha} > \frac{\int_0^{\hat{\alpha}(y, b^e, \cdot)} \alpha d\alpha}{N(b^e, \cdot)}$ . The first inequality follows because the highest public school ability at a certain income exceeds average of all abilities at that income. The second inequality follows because  $N(b^e, \cdot) > \int_0^{\hat{\alpha}(y, b^e, \cdot)} d\alpha$ . The former sums all public school households at all incomes while the latter sums public school households at only one income.

Now,  $\frac{\delta^2 \hat{\alpha}}{\delta b^e \delta y} = -\frac{u_{b^e \alpha} \cdot (v_x^Q - v_x^g)}{(u_\alpha^Q - u_\alpha^g)^2} < 0$  since  $u_{\theta \alpha} > 0$ ,  $v_{xx} < 0$  and  $q_{b^e} > 0$ . Therefore due to an increase in  $b^e$  there is a higher increase in cutoff ability towards the lower incomes. Also  $\hat{\alpha}(y)$  is inversely related to  $y$ . Therefore higher positive values of  $\frac{\delta \hat{\alpha}}{\delta b^e}$  are multiplied with higher positive values of  $[\hat{\alpha}(y, b^e, \cdot) - b]$  so that  $\frac{\delta g}{\delta b^e}$  will be positive. Formally, if for some large  $y$ ,  $[\hat{\alpha}(y, b^e, \cdot) - b] < 0$ , then there must exist some  $y = y_1$  such that  $\hat{\alpha}(y_1, b^e, \cdot) = b$ . Then,

$$\begin{aligned} \int_0^{y_1} (\hat{\alpha}(y, b^e, \cdot) - b) dy &> \left| \int_{y_1}^1 (\hat{\alpha}(y, b^e, \cdot) - b^e) dy \right| \Rightarrow \int_0^{y_1} (\hat{\alpha}(y, b^e, \cdot) - b) \cdot \frac{\delta \hat{\alpha}(y_1, \cdot)}{\delta b^e} dy > \left| \int_{y_1}^1 (\hat{\alpha}(y, b^e, \cdot) - b) \cdot \frac{\delta \hat{\alpha}(y_1, \cdot)}{\delta b^e} dy \right| \\ &\Rightarrow \int_0^{y_1} (\hat{\alpha}(y, b^e, \cdot) - b) \cdot \frac{\delta \hat{\alpha}(y, \cdot)}{\delta b^e} dy > \int_0^{y_1} (\hat{\alpha}(y, b^e, \cdot) - b) \cdot \frac{\delta \hat{\alpha}(y_1, \cdot)}{\delta b^e} dy > \left| \int_{y_1}^1 (\hat{\alpha}(y, b^e, \cdot) - b) \cdot \frac{\delta \hat{\alpha}(y_1, \cdot)}{\delta b^e} dy \right| \\ &\quad \left| \int_{y_1}^1 (\hat{\alpha}(y, b^e, \cdot) - b) \cdot \frac{\delta \hat{\alpha}(y, \cdot)}{\delta b^e} dy \right| \end{aligned}$$

The last line follows because  $\frac{\delta \hat{\alpha}}{\delta b^e}$  is positive and is strictly decreasing in  $y$ . Therefore  $\frac{\delta g}{\delta b^e} > 0$ .

So the sign of  $\frac{\delta g}{\delta b^e}$  is positive. If it exceeds one, there are multiple equilibria. I henceforth restrict my attention to parameter values where  $b(0) > 0$  and  $\frac{\delta g}{\delta b^e} < 1$ . These are sufficient conditions that ensure a unique equilibrium. The first condition always holds since  $0 < \hat{\alpha}(\cdot) < 1$ . The second condition implies that a small increase (decrease) in anticipated peer quality leads to a less than proportionate increase (decrease) in actual peer quality.

**Claim 1:** *Equilibrium number of public school students falls with vouchers and increases with effort.*

**Proof. Step 1:** *Equilibrium peer-group quality falls with vouchers and increases with public school effort.*

*Effect of an increase in  $e$ :*

$$\frac{\delta b^*}{\delta e} = \frac{\frac{\delta g(b^*, \cdot)}{\delta e}}{1 - \frac{\delta g(b^*, \cdot)}{\delta b}} \text{ where } \frac{\delta g(b^*, \cdot)}{\delta e} = \frac{1}{N(b^*, \cdot)} \cdot \int_0^1 (\hat{\alpha}(y, b^*, \cdot) - b^*) \cdot \frac{\delta \hat{\alpha}}{\delta e} dy$$

The denominator is positive from uniqueness. Consider

$$\int_0^1 (\hat{\alpha}(\cdot) - b) dy = \int_0^1 \left[ \hat{\alpha}(\cdot) - \frac{1}{N(\cdot)} \cdot \int_0^{\hat{\alpha}(\cdot)} \alpha d\alpha \right] dy \quad (\text{A.1})$$

For any  $y$ ,  $[\hat{\alpha}(\cdot) \cdot N(\cdot) - \int_0^{\hat{\alpha}(\cdot)} \alpha d\alpha] = \hat{\alpha}(\cdot) \left[ \int_0^1 \hat{\alpha}(\cdot) dy - \frac{\hat{\alpha}(\cdot)}{2} \right]$ , which is positive. Therefore, A.1 > 0.

It can be easily checked that  $\frac{\delta^2 \hat{\alpha}}{\delta e \delta y} < 0$ .  $\hat{\alpha}(y)$  is inversely related to  $y$ . If for some large  $y$ ,  $[\hat{\alpha}(y, b^*, \cdot) - b^*] < 0$ , then there must exist some  $y = y_1$ ,  $y_1 \in (0, 1)$  such that  $\hat{\alpha}(y_1, b^*, \cdot) = b^*$ . Then,

$$\begin{aligned} & \int_0^{y_1} (\hat{\alpha}(y, b^*, \cdot) - b^*) dy > \left| \int_{y_1}^1 (\hat{\alpha}(y, b^*, \cdot) - b^*) dy \right| \\ \Rightarrow & \int_0^{y_1} (\hat{\alpha}(y, b^*, \cdot) - b^*) \cdot \frac{\delta \hat{\alpha}(y_1, \cdot)}{\delta e} dy > \left| \int_{y_1}^1 (\hat{\alpha}(y, b^*, \cdot) - b^*) \cdot \frac{\delta \hat{\alpha}(y_1, \cdot)}{\delta e} dy \right| \\ \Rightarrow & \int_0^{y_1} (\hat{\alpha}(y, b^*, \cdot) - b^*) \cdot \frac{\delta \hat{\alpha}(y, \cdot)}{\delta e} dy > \left| \int_{y_1}^1 (\hat{\alpha}(y, b^*, \cdot) - b^*) \cdot \frac{\delta \hat{\alpha}(y, \cdot)}{\delta e} dy \right|. \end{aligned}$$

Therefore  $\frac{\delta g}{\delta e} > 0$  and  $\frac{\delta b^*}{\delta e} > 0$ .

*Effect of an increase in  $v$ :*

$$\frac{\delta b^*}{\delta v} = \frac{\frac{\delta g(b^*, \cdot)}{\delta v}}{1 - \frac{\delta g(b^*, \cdot)}{\delta v}} \text{ where } \frac{\delta g(b^*, \cdot)}{\delta v} = \frac{1}{N(b^*, \cdot)} \cdot \int_0^1 (\hat{\alpha}(y, b^*, \cdot) - b^*) \cdot \frac{\delta \hat{\alpha}}{\delta v} dy$$

The denominator is positive from uniqueness. Since  $A.1 > 0$ ,  $\frac{\delta \hat{\alpha}}{\delta v} < 0$ ,  $\frac{\delta^2 \hat{\alpha}}{\delta v \delta y} > 0$  and  $\hat{\alpha}(y)$  is inversely related to  $y$ , the numerator is negative. Therefore,  $\frac{\delta b^*}{\delta v} < 0$ .

**Step 2:** *Equilibrium cutoff ability at each income level falls with vouchers and increases with effort.*

Follows from  $\frac{\delta \hat{\alpha}(y; b^*, \cdot)}{\delta e} = \frac{\delta \hat{\alpha}(y; b^*, \cdot)}{\delta e} |b^* + \frac{\delta \hat{\alpha}(y; b^*, \cdot)}{\delta b} \cdot \frac{\delta b^*}{\delta e}$  and  $\frac{\delta \hat{\alpha}(y; b^*, \cdot)}{\delta v} = \frac{\delta \hat{\alpha}(y; b^*, \cdot)}{\delta v} |b^* + \frac{\delta \hat{\alpha}(y; b^*, \cdot)}{\delta b} \cdot \frac{\delta b^*}{\delta v}$  and step 1.

From step 2 and definition of  $N(b^*, \cdot)$ , the proof follows.

**Proof of Proposition 1.**

Under the VS program,  $e_{VS}$  solves the first order condition:  $\frac{\delta R(e, v)}{\delta e} = (p - c_N)N_e(e, v) - C_e(e) = 0$ .

Comparative statics with respect to  $v$  yields:

$$\frac{\delta e}{\delta v} = \frac{-[(p - c_N)N_{ev} - c_{NN}N_v N_e]}{(p - c_N)N_{ee} - c_{NN}N_e^2 - C_{ee}} \quad A.2$$

The denominator is negative from the strict concavity of the rent function. Also  $p - c_N > 0$  and  $c_{NN}N_v N_e < 0$ .  $N_{ev} = \int_0^1 \left[ \frac{\delta^2 \hat{\alpha}(y, b^*, \cdot)}{\delta e \delta v} + \frac{\delta^2 \hat{\alpha}(y, b^*, \cdot)}{\delta e \delta b} \cdot \frac{\delta b^*}{\delta v} \right] dy$ .  $\frac{\delta b^*}{\delta v} < 0$  from claim 1. It can be easily seen that  $\frac{\delta^2 \hat{\alpha}(y, b^*, \cdot)}{\delta e \delta b} < 0$  and  $\frac{\delta^2 \hat{\alpha}(y, b^*, \cdot)}{\delta e \delta v} < 0$ . Therefore  $N_{ev} \geq 0$  which implies that A.2  $\geq 0$ . ■

**Proof of Proposition 2.**

**Proof to part (i):**

$pN(e_{VS}, 0) - c_1 - c(N(e_{VS}, 0)) - C(e_{VS}) > pN(e_{VS}, v) - c_1 - c(N(e_{VS}, v)) - C(e_{VS})$ , since vouchers decrease rent. By the strict concavity of the rent function,  $\exists \bar{e} > e_{VS}$  that satisfies the public school's incentive constraint under TOV with equality

$$pN(\bar{e}, 0) - c(N(\bar{e}, 0)) - C(\bar{e}) = pN(e_{VS}, v) - c(N(e_{VS}, v)) - C(e_{VS}).$$

**Proof to part(ii):**

$$pN(e_{PP}, 0) - c(N(e_{PP}, 0)) - C(e_{PP}) > pN(e_{VS}, 0) - c(N(e_{VS}, 0)) - C(e_{VS}) > pN(e_{VS}, v) - c(N(e_{VS}, v)) - C(e_{VS}, v)$$

The first inequality follows because  $e_{PP}$  is the rent maximizing effort under  $v = 0$ . Given strict concavity of the rent function,  $\exists \bar{e} > e^{PP}$  such that it satisfies the public school's incentive constraint under TOV with equality. ■

## Appendix B: Moral hazard problem – unobservable public school effort

This appendix relaxes the assumption of complete observability of public school effort and examines whether under unobservable public school effort, the equilibrium effort under the TOV program still exceeds those under the PP and the VS programs. Given public school effort  $e \in [e_{min}, e_{max}]$ , “effective effort”  $e'$  is realized according to the distribution  $F(e'/e)$ , where  $e' \in [e'_{min}, e'_{max}]$ . Although  $e$  is not publicly observable, all agents have complete knowledge of the set  $[e_{min}, e_{max}]$  and the family of conditional distributions  $F(e'/e)$  for  $e \in [e_{min}, e_{max}]$ . The corresponding density  $f(e'/e)$  satisfies the strict monotone likelihood ratio property (MLRP).  $F(e'/e)$  satisfies the convexity of the distribution function condition (CDFC) i.e  $F_{ee}(e'/e) > 0$  for all  $e' \in [e'_{min}, e'_{max}]$  and  $e \in [e_{min}, e_{max}]$ . Public school quality ( $q = q(e', b)$ ) is a composite of two factors: (i) “effective effort”  $e'$  and (ii) peer group quality (b) and can be thought of as being embodied in school scores.<sup>54</sup> All agents observe quality  $q$  but not the actual public school effort  $e$  that generated it.

Household behavior is basically the same as earlier, the only difference is that instead of using effort itself, they use a noisy representation of effort, effective effort  $e'$  to make their school choices. The public school anticipates household behavior and chooses  $e$  to maximize expected rent:

$$ER(v, \cdot) = \int_{e'_{min}}^{e'_{max}} [pN(e', v, b^*, \cdot) - c(N(e', v, b^*, \cdot))] f(e'/e) de' - c_1 - C(e) \text{ where } v = 0 \text{ under the}$$

public-private system. The expected rent function is strictly concave under CDFC. Equilibrium public school effort under the VS program can be either greater or less than the PP system. (Proof available on request.) The intuition behind this is as follows. With imposition of vouchers, rent falls at each realization of  $e'$ . An increase in  $e$  increases the probability of higher  $e'$  realizations. However, the above fall in rent can either increase or decrease in  $e'$ . This implies that vouchers may induce public schools to correspondingly decrease or increase effort in response to vouchers. Under the Florida TOV program

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<sup>54</sup> The uncertainty signifies the absence of any direct one-to-one relationship between the effort of teachers and administrators, and school scores.

the public school faces a quality cutoff  $\bar{q}$  or equivalently an “effective effort” cutoff  $\bar{e}'$  and chooses  $e$  to maximize its expected rent. The school’s expected rent under the TOV program is given by:

$$H = \int_{e'_{min}}^{\bar{e}'} [pN(e', v, \cdot) - c(N(e', v, \cdot))]f(e'/e)de' + \int_{\bar{e}'}^{e'_{max}} [pN(e', 0, \cdot) - c(N(e', 0, \cdot))]f(e'/e)de' - c_1 - C(e).$$

Under CDFC,  $H$  is strictly concave in  $e$ .

**Proposition 3** (i) *There exists  $e'_1, e'_{min} \leq e'_1 < E_1$  such that if the cutoff  $\bar{e}' \in [e'_1, e'_{max}]$  the effort under the “threat of voucher” program unambiguously exceeds that under the “voucher shock” program i.e.,  $e_{TOV} > e_{VS}$ . (ii) *There exists  $e'_2, E_2 < e'_2 \leq e'_{max}$  such that if the cutoff  $\bar{e}' \in [e'_{min}, e'_2]$  the effort under the “threat of voucher” program unambiguously exceeds that under the pre-program public-private equilibrium i.e.,  $e_{TOV} > e_{PP}$ .**

The intuitive argument behind this proposition is as follows. First consider the TOV and the VS programs. Facing the TOV program, if the school chooses  $e_{VS}$  (the equilibrium effort under the VS program), then at each realization of  $e' < \bar{e}'$ , its rent is the same as in the VS program. On the other hand, for each realization of  $e' \geq \bar{e}'$ , its rent is higher. Therefore the school chooses an effort strictly higher than  $e_{VS}$  to increase its probability of falling above  $\bar{e}'$  since it follows from the MLRP that an increase in effort increases the probability of higher  $e'$ s. The intuition behind  $\bar{e} > e_{PP}$  is similar.

Choosing  $e_{PP}$  under the TOV gives it the same rent as the PP program at each realization above  $\bar{e}'$  but lower rent at each realization below  $\bar{e}'$ . The school chooses an effort strictly above  $e_{PP}$  to increase (decrease) the probability of realizations above (below)  $\bar{e}'$ .<sup>55</sup> Thus, the results here parallel those in the complete information model (Proposition 2).

## Appendix C: Proof of Result in Appendix B

**Proof of Proposition 3. Proof to part (i):** Evaluating the first order condition under the TOV program at  $e_{VS}$ :

$$\frac{\delta H}{\delta e}|_{e_{VS}} = \frac{\delta H}{\delta e}|_{e_{VS}} - \frac{\delta ER(v, \cdot)}{\delta e}|_{e_{VS}} = \int_{\bar{e}'}^{e'_{max}} [r(e', 0) - r(e', v)]f_e(e'/e_{VS})de' = \int_{\bar{e}'}^{e'_{max}} \beta(e', v)f_e(e'/e_{VS})de'$$

where  $\beta(e', v) = [r(e', 0) - r(e', v)]$  and  $r(e', V) = pN(e', V) - c(N(e', V))$ ,  $V = \{0, v\}$ . MLRP implies that there exists  $E_1, f_e(e'/e_{VS}) \lesseqgtr 0$  according as  $e' \lesseqgtr E_1$ . Now if the cutoff  $\bar{e}' \geq E_1$  then  $\frac{\delta H}{\delta e}|_{e_{VS}} > 0$

<sup>55</sup> However, although rent falls at each realization of  $e'$  with vouchers, this fall (or alternatively, the gain in rent from avoiding vouchers) may either increase or decrease with  $e'$ . Depending on this, under certain circumstances, at very low levels of cutoff, the public school effort under TOV may be less than VS and at very high levels of cutoff, effort under TOV may be less than PP. The intuition is as follows. First consider TOV versus VS. If  $\bar{e}'$  is low, schools escape vouchers for low values of  $e'$  also. If it is the case that the gain in rent from avoiding vouchers is largest for lower values of  $e'$  then since an increase in effort decreases the probability of occurrence of lower values of  $e'$ , public school may find it profitable not to increase effort. Now consider TOV versus PP. If  $\bar{e}'$  is high, vouchers will be incurred at high values of  $e'$  also. If it is the case that the fall in rent due to vouchers is highest for high values of  $e'$ , then the school may not have an incentive to increase effort since an increase in effort increases the probability of occurrence of higher  $e'$ .



since  $\beta(e', v) > 0$  so that  $\bar{e} > e_{VS}$ . There are two cases if  $\bar{e}' < E_1$ . Let  $\int_{e'_{min}}^{e'_{max}} \beta(e', v) f_e(e'/e_{VS}) de' = A_1$ . Although  $f_e(e'/e_{VS}) \leq 0$  according as  $e' \leq E_1$ ,  $\beta(e', v)$  may be increasing or decreasing in  $e'$ . Therefore  $A_1 \geq 0$ . (Note that  $A_1 \leq 0$  implies  $e_{PP} \leq e_{VS}$ ).

Case 1: If  $A_1 > 0$  then for any  $\bar{e}' \in (e'_{min}, E_1)$ ,  $\frac{\delta H}{\delta e}|_{e_{VS}} > 0$  and  $e_{TOV} > e_{VS}$ .

Case 2: If  $A_1 < 0$  then  $\exists e'^1 \in (e'_{min}, E_1)$  such that

$|\int_{e'^1}^{E_1} \beta(e', v) f_e(e'/e_{VS}) de'| = \int_{E_1}^{e'^{max}} \beta(e', v) f_e(e'/e_{VS}) de'$  then for any  $\bar{e}' \in (e'^1, E_1)$ ,  $\frac{\delta H}{\delta e}|_{e_{VS}} > 0$  and  $e_{TOV} > e_{VS}$ .

Using cases (1) and (2) define  $e'_1 = [\min\{e' \in [e'_{min}, E_1] : \int_{e'}^{e'^{max}} \beta(e', v) f_e(e'/e_{VS}) de' > 0\}]$ . Then for any  $\bar{e}' \in [e'_1, e'^{max}]$ ,  $e_{TOV} > e_{VS}$ . Note that  $e'_1 \geq e'_{min}$  according as  $A_1 \leq 0$ .

### Proof to part (ii):

Evaluating the first order condition under the TOV program at  $e_{PP}$ :

$$\frac{\delta H}{\delta e}|_{e_{PP}} = \frac{\delta H}{\delta e}|_{e_{PP}} - \frac{\delta ER(0, \cdot)}{\delta e}|_{e_{PP}} = \int_{e'_{min}}^{\bar{e}'} [r(e', v) - r(e', 0)] f_e(e'/e_{PP}) de' = - \int_{e'_{min}}^{\bar{e}'} \beta(e', v) f_e(e'/e_{PP}) de'$$

MLRP implies that there exists  $E_2$ ,  $f_e(e'/e_{PP}) \leq 0$  according as  $e' \leq E_2$ . Now if the cutoff  $\bar{e}' \leq E_2$  then  $\frac{\delta H}{\delta e}|_{e_{PP}} > 0$  so that  $e_{TOV} > e_{PP}$ . There are two cases if  $\bar{e}' > E_2$ . Let  $A_2 = \int_{e'_{min}}^{e'^{max}} \beta(e', v) f_e(e'/e_{PP}) de'$ . Again similarly as above  $A_2 \geq 0$ . (Note that  $A_2 \geq 0$  implies  $e_{PP} \geq e_{VS}$ ).

Case 1: If  $A_2 < 0$  then for any  $\bar{e}' \in (E_2, e'^{max})$   $\frac{\delta H}{\delta e}|_{e_{PP}} > 0$  and  $e_{TOV} > e_{PP}$ .

Case 2: If  $A_2 > 0$  then  $\exists e'^2 \in (E_2, e'^{max})$  such that

$|\int_{e'_{min}}^{E_2} \beta(e', v) f_e(e'/e_{PP}) de'| = \int_{E_2}^{e'^2} \beta(e', v) f_e(e'/e_{PP}) de'$  then for any  $\bar{e}' \in (E_2, e'^2)$ ,  $\frac{\delta H}{\delta e}|_{e_{PP}} > 0$  and  $e_{TOV} > e_{PP}$ .

Using cases (1) and (2) define  $e'_2 = [\max\{e' \in [E_2, e'^{max}] : \int_{e'_{min}}^{e'} -\beta(e', v) f_e(e'/e_{PP}) de' > 0\}]$ . Then for any  $\bar{e}' \in [e'_{min}, e'_2]$ ,  $e_{TOV} > e_{PP}$ . Note that  $e'_2 \leq e'^{max}$  according as  $A_2 \geq 0$ . ■

## Appendix D: Targeted Vouchers

The analysis in the previous sections are based on the assumption that when vouchers are imposed, all households, irrespective of income, become eligible for them. In other words, vouchers take a universal form. Although this is the case in Florida, in Milwaukee only the low income households (say with  $y \leq y_T$ ) are eligible for vouchers, that is, vouchers take a targeted form. This section considers a voucher shock program where vouchers are targeted to the low income population only. It is referred to as the targeted voucher shock (TVS) program. To distinguish from the TVS, a voucher shock program where all households are eligible will be referred to as the universal voucher shock (UVS) program in this section. The TVS program is analyzed in three stages. In the first stage, the government

announces voucher  $v$  and income cutoff  $y_T$ . In stage 2, facing  $v$  and  $y_T$ , the public school chooses  $e \in [e_{min}, e_{max}]$ . In stage 3, households choose between schools and incur switching costs if they transfer out of public school. Peer group quality and public school quality are simultaneously obtained. The TVS equilibrium is a peer group quality  $b_T^*$  and an effort  $e_{TVS}$  such that given voucher  $v$  and income cutoff  $y_T$  (i)  $e_{TVS}$  characterizes the public school equilibrium given  $b_T^*$  and (ii)  $b_T^*$  characterizes the household equilibrium given the public school equilibrium.

### Household Behavior

I first characterize the household equilibrium under targeted vouchers and undertake a comparative static analysis to investigate how changes in the exogenous variables affect equilibrium peer quality, equilibrium allocation of households between public and private sectors and the equilibrium number of public school students.<sup>56</sup> Household equilibrium is characterized by the equations (A.1)-(A.3):

$$D = [v(y + v - t.Q^* - c) + u(Q^*, \alpha)] - [v(y) + u(q(e, b^e), \alpha)] = 0 \quad (\text{A.1})$$

Since households are eligible for vouchers only if their income is less than a certain cutoff  $y_T$ ,  $v = 0$  if  $y > y_T$ . For each income and given  $v, e, b^e, t, c$ , there exists a cutoff ability level  $\hat{\alpha}$ , which is obtained as a solution to A.1 such that all households with ability strictly above  $\hat{\alpha}$  prefer private school while those below prefer public. From the above equation  $\hat{\alpha}(\cdot)$  can be obtained as a continuously differentiable function of  $v, b^e, t, c$ <sup>57</sup> for each  $y$ . Given other parameters,  $\hat{\alpha}(\cdot)$  is continuously differentiable in  $y$  in the range  $[0, y_T)$  and  $(y_T, 1]$  with a discrete jump at  $y_T$ . Given  $b^e$ , peer group quality  $b$  is given by:

$$b = \frac{\int_0^{y_T} \int_0^{\hat{\alpha}(y, b^e, v, \cdot)} \alpha d\alpha dy + \int_{y_T}^1 \int_0^{\hat{\alpha}(y, b^e, 0, \cdot)} \alpha d\alpha dy}{\int_0^{y_T} \int_0^{\hat{\alpha}(y, b^e, v, \cdot)} d\alpha dy + \int_{y_T}^1 \int_0^{\hat{\alpha}(y, b^e, 0, \cdot)} d\alpha dy} = \frac{1}{2} \cdot \frac{\int_0^{y_T} \hat{\alpha}^2(y, b^e, v, \cdot) dy + \int_{y_T}^1 \hat{\alpha}^2(y, b^e, 0, \cdot) dy}{\int_0^{y_T} \hat{\alpha}(y, b^e, v, \cdot) dy + \int_{y_T}^1 \hat{\alpha}(y, b^e, 0, \cdot) dy} = F_T(\hat{\alpha}(\cdot), y_T) = g_T(b^e, e, v, t, c, y_T) \quad (\text{A.2})$$

At equilibrium  $b$  corroborates the initial conjecture  $b^e$ , that is,  $b = b^e$  (A.3)

A household equilibrium always exists under targeted vouchers.<sup>58</sup> However there may be multiple equilibria. To see this differentiate (A.2) to find that

$$\frac{\delta g_T}{\delta b^e} = \frac{1}{N_T} \left[ \int_0^{y_T} (\hat{\alpha}(v, \cdot) - b) \frac{\delta \hat{\alpha}}{\delta b^e}(v, \cdot) dy + \int_{y_T}^1 (\hat{\alpha}(0, \cdot) - b) \frac{\delta \hat{\alpha}}{\delta b^e}(0, \cdot) dy \right] \text{ where } N_T = y_T \frac{\hat{\alpha}(v, \cdot)}{2} + (1 - y_T) \frac{\hat{\alpha}(0, \cdot)}{2}$$

<sup>56</sup> To simplify analysis, this section assumes  $v_{xx} = 0$ .

<sup>57</sup> Using implicit function theorem, it can be easily seen that for each  $y$ ,  $\frac{\delta \hat{\alpha}}{\delta e} > 0$ ,  $\frac{\delta \hat{\alpha}}{\delta b^e} > 0$ ,  $\frac{\delta \hat{\alpha}}{\delta t} > 0$ ,  $\frac{\delta \hat{\alpha}}{\delta c} > 0$ ,  $\frac{\delta \hat{\alpha}}{\delta v} < 0$ , that is, the cutoff ability level increases with  $e, b^e, t, c$  and decreases with  $v$ .

<sup>58</sup> Define  $\Psi : [0, 1] \rightarrow [0, 1]$  such that for all  $b' \in [0, 1]$   $\Psi(b') = g_T(b', e, v, t, c, y_T)$ . By implicit function theorem  $\hat{\alpha}$  is continuous in  $b'$  (from A.1).  $F_T$  is continuous is  $\hat{\alpha}$  from A.2. Therefore  $\Psi$  is a continuous function from  $[0, 1] \rightarrow [0, 1]$ . By Brouwer's fixed point theorem, there exists at least one  $b^*$  such that  $b^* = \Psi(b^*)$ .

The sign of  $\frac{\delta g_T}{\delta b^e}$  is positive.<sup>59</sup> If it exceeds one, there may be multiple equilibria. Parameter values such that  $b(0) > 0$  and  $\frac{\delta g_T}{\delta b^e} < 1$  ensure a unique equilibrium. While  $0 < \hat{a} < 1$  ensures  $b(0) > 0$ , the second condition holds if the marginal utility from school quality and the marginal responsiveness of public school quality to peer quality are not too high.

**Lemma A.1** *Under targeted vouchers, peer group quality falls with vouchers and increases with public school effort.*

**Lemma A.2** *Under targeted vouchers, an increase in public school effort leads to reverse sorting by both income and ability. Targeted vouchers increase sorting by income and ability.<sup>60</sup>*

**Proposition A.1** *Equilibrium number of public school students decreases with targeted vouchers and increases with public school effort under targeted vouchers.*

The intuition behind lemmas A.1 and A.2 and proposition A.1 are exactly the same as earlier.

However, since vouchers are targeted here only to the low income population, high ability households only at each income level less than or equal to  $y_T$  switch to private schools with vouchers. An increase in effort however leads to an influx of high ability households at each income level similar to that in the universal vouchers case.

**Lemma A.3** *Given  $e, v, t, c$ , equilibrium number of public school students under targeted vouchers is greater than that under a universal vouchers system.*

Universal vouchers lead to a switch of high ability households at each income level whereas targeted vouchers leads to a flight of high ability households only for income levels less than or equal to  $y_T$ .

Therefore loss of students due to vouchers is greater under the universal than the targeted regime, given all other parameters.

### Public School Behavior

The public school correctly anticipates household behavior under targeted vouchers and chooses effort to maximize its rent  $R_T(e, v) = pN_T(e, v) - c(N_T(e, v)) - C(e)$ . There exists a unique effort  $e_{TVS}$  that solves its first order condition  $\frac{\delta R_T(e, v)}{\delta e} = (p - c_{N_T})\frac{\delta N_T(e, v)}{\delta e} - C_e(e) = 0$ . Since the imposition of targeted vouchers also leads to a flight of households from public school, it leads to a fall in public school rent.<sup>61</sup> Equilibrium public school effort under the TVS equilibrium can be either greater or less

<sup>59</sup> The proof is in appendix E. All proofs for this section are in appendix E.

<sup>60</sup> The proof follows on the same lines as above and hence is skipped.

<sup>61</sup>  $\frac{\delta R_T(e, v)}{\delta v} = (p - c_{N_T})\frac{\delta N_T(e, v)}{\delta v}$  which is negative because  $\frac{\delta N_T}{\delta v} < 0$  by proposition A.1 and  $(p - c_{N_T}) > 0$  by assumption.

than the pre-program public-private equilibrium. The proof and the intuition are exactly the same as in proposition 1 and hence is not repeated here.

**Lemma A.4** *Rent under the TVS equilibrium is greater than that under the UVS equilibrium.*

The intuitive argument is as follows. Under the targeted voucher shock program, the school can attract the same number of students as under the universal program,  $N(b^*, v)$ , by giving a lower effort than under the universal program (follows from lemma A.3 and proposition A.1) and hence at a lower cost and correspondingly higher rent (say  $\tilde{R}$ ) than the UVS. Since the school chooses to attract a different number of students under the targeted program,  $N_T(b^*, v)$ , it must be the case that the rent under TVS exceeds  $\tilde{R}$  and hence also the UVS rent.

**Proposition A.2** *For each voucher  $v$ , there exists a cutoff effort  $\bar{e}$  such that the equilibrium effort under the “threat of voucher” program exceeds the equilibrium effort under the “targeted voucher shock” equilibrium,  $e_{TVS}$ .*

To see the intuition, I start by assuming that vouchers if imposed in Florida also take a similar income targeted form as in Milwaukee. Then a Florida school choosing not to meet the cutoff chooses the TVS effort  $e_{TVS}$  and gets the TVS rent  $R_T(e_{TVS}, v)$ . Since vouchers decrease rent, the Florida school can be induced to satisfy a cutoff  $\bar{e} > e_{TVS}$ . However, vouchers actually take a universal form in Florida which implies that rent under vouchers in Florida is less than the  $R_T(e_{TVS}, v)$ . This implies that there exists a still higher cutoff  $\bar{e} > \bar{e} > e_{TVS}$  which can be induced by the Florida-type TOV program. Thus there are two features in the design of TOV that induce a higher effort than the TVS: (i) vouchers are not already imposed and a sufficient improvement can enable schools to escape vouchers (ii) the potential loss of students in the TOV is much greater.

**Corollary A.1** *Equilibrium public school quality under the “threat of voucher” equilibrium exceeds the equilibrium quality under the “targeted voucher shock” program.*

From Proposition A.2, the effort under the TOV program exceeds that under the TVS equilibrium. Noting that vouchers tend to lower peer quality and peer quality varies positively with effort, the corollary follows. Note that since the equilibrium effort under the TVS program can be greater or less than the pre-program public-private equilibrium, the same follows for equilibrium quality.

## Appendix E: Proofs of results in Appendix D

**Proof of  $\frac{\delta g_T}{\delta b^e} > 0$  :**

$$\frac{\delta g_T}{\delta b^e} = \frac{1}{N_T} \left[ \int_0^{y_T} (\hat{\alpha}(v, \cdot) - b) \frac{\delta \hat{\alpha}}{\delta b^e}(v, \cdot) dy + \int_{y_T}^1 (\hat{\alpha}(0, \cdot) - b) \frac{\delta \hat{\alpha}}{\delta b^e}(0, \cdot) dy \right] \text{ where } N_T = y_T \frac{\hat{\alpha}(v, \cdot)}{2} + (1 - y_T) \frac{\hat{\alpha}(0, \cdot)}{2}.$$

The proof consists of the following steps:

(i)  $\int_0^1 \hat{\alpha} dy - b$  is positive.

Noting that  $b = \frac{y_T}{N_T} \int_0^{\hat{\alpha}(v, \cdot)} \alpha d\alpha + \frac{(1-y_T)}{N_T} \int_0^{\hat{\alpha}(0, \cdot)} \alpha d\alpha$ , it follows that

$\int_0^1 \hat{\alpha} dy - b = y_T [\hat{\alpha}(v, \cdot) - \frac{\int_0^{\hat{\alpha}(v, \cdot)} \alpha d\alpha}{N_T}] + (1 - y_T) [\hat{\alpha}(0, \cdot) - \frac{\int_0^{\hat{\alpha}(0, \cdot)} \alpha d\alpha}{N_T}]$ . Since the expression in each of the square brackets is positive,  $\int_0^1 \hat{\alpha} dy - b$  is positive.

(ii)  $\frac{\hat{\alpha}(v, \cdot)}{2} < b < \frac{\hat{\alpha}(0, \cdot)}{2}$ .

From above,  $b = \frac{y_T \hat{\alpha}(v) \frac{\hat{\alpha}(v, \cdot)}{2} + (1-y_T) \hat{\alpha}(0, \cdot) \frac{\hat{\alpha}(0, \cdot)}{2}}{N_T}$ . Therefore  $b$  is a weighted average of  $\frac{\hat{\alpha}(v, \cdot)}{2}$  and  $\frac{\hat{\alpha}(0, \cdot)}{2}$ .

(iii) Now,

$$\frac{\delta g_T}{\delta b^e} = \frac{1}{N_T} [y_T (\hat{\alpha}(v, \cdot) - b) \frac{\delta \hat{\alpha}}{\delta b^e}(v, \cdot) dy + (1 - y_T) (\hat{\alpha}(0, \cdot) - b) \frac{\delta \hat{\alpha}}{\delta b^e}(0, \cdot) dy]$$

There are two possible cases:

Case (a):  $b < \hat{\alpha}(v, \cdot) < \hat{\alpha}(0, \cdot)$ . Then it follows that  $\frac{\delta g_T}{\delta b^e} > 0$ .

Case (b):  $\hat{\alpha}(v, \cdot) < b < \hat{\alpha}(0, \cdot)$ .

Now,  $\int_0^1 \hat{\alpha}(\cdot) dy - b > 0 \Rightarrow y_T \hat{\alpha}(v, \cdot) + (1 - y_T) \hat{\alpha}(0, \cdot) - b > 0 \Rightarrow y_T [\hat{\alpha}(v, \cdot) - b] + (1 - y_T) [\hat{\alpha}(0, \cdot) - b] > 0$ .

Then it must be the case that  $(1 - y_T) [\hat{\alpha}(0, \cdot) - b] > |y_T [\hat{\alpha}(v, \cdot) - b]|$ . Using equation A.1, it can be

easily seen that  $\frac{\delta^2 \hat{\alpha}}{\delta v \delta b^e} = \frac{u_{\alpha b^e}^q \frac{\delta \alpha}{\delta v}}{u_{\alpha}^q - u_{\alpha}^q} < 0$ . It follows therefore that

$(1 - y_T) [\hat{\alpha}(0, \cdot) - b] \frac{\delta \hat{\alpha}}{\delta b^e}(0, \cdot) > |y_T [\hat{\alpha}(v, \cdot) - b] \frac{\delta \hat{\alpha}}{\delta b^e}(v, \cdot)|$ . Hence  $\frac{\delta g_T}{\delta b^e} > 0$ .

**Proof of Lemma A.1.** At the household equilibrium under targeted vouchers,

$$b_T^* = g_T(b_T^*, e, v, t, c, y_T) \text{ where } b_T^* \text{ denotes the equilibrium peer quality under targeted vouchers.}$$

**Effect of an increase in  $e$ :**

$$\frac{\delta b_T^*}{\delta e} = \frac{\frac{\delta g_T(b_T^*, \cdot)}{\delta e}}{1 - \frac{\delta g_T(b_T^*, \cdot)}{\delta b}} \text{ where,}$$

The denominator is positive from the uniqueness condition. Consider the numerator.

$$\begin{aligned} \frac{\delta g_T(b_T^*, \cdot)}{\delta e} &= \frac{1}{N_T(b_T^*, \cdot)} \left[ \int_0^{y_T} (\hat{\alpha}(v, b_T^*, \cdot) - b_T^*) \frac{\delta \hat{\alpha}(v, b_T^*, \cdot)}{\delta e} dy + \int_{y_T}^1 (\hat{\alpha}(0) - b_T^*) \frac{\delta \hat{\alpha}(0, b_T^*, \cdot)}{\delta e} dy \right] \\ &= \frac{1}{N_T(b_T^*, \cdot)} \left[ y_T (\hat{\alpha}(v, b_T^*, \cdot) - b_T^*) \frac{\delta \hat{\alpha}(v, b_T^*, \cdot)}{\delta e} + (1 - y_T) (\hat{\alpha}(0) - b_T^*) \frac{\delta \hat{\alpha}(0, b_T^*, \cdot)}{\delta e} \right] \end{aligned}$$

The second line follows because  $v_{xx} = 0$ . Using equation A.1,  $\frac{\delta^2 \hat{\alpha}}{\delta v \delta e} = \frac{u_{\alpha e}^q \cdot \frac{\delta \alpha}{\delta v}}{u_{\alpha}^q - u_{\alpha}^q}$ , which is negative.

Therefore, it follows from the proof of  $\frac{\delta g_T}{\delta b^e} > 0$  that  $\frac{\delta g_T(b_T^*, \cdot)}{\delta e} > 0$ .

**Effect of an increase in  $v$ :**

$$\frac{\delta b_T^*}{\delta v} = \frac{\frac{\delta g_T(b_T^*, \cdot)}{\delta v}}{1 - \frac{\delta g_T(b_T^*, \cdot)}{\delta b}} \quad \text{where,}$$

$$\frac{\delta g_T(b_T^*, v, \cdot)}{\delta v} = \frac{1}{N_T} \left[ \int_0^{y_T} (\hat{\alpha}(v, \cdot) - b_T^*) \cdot \frac{\delta \hat{\alpha}(v, b_T^*, \cdot)}{\delta v} dy \right]$$

Starting from a status quo position of  $v = 0$  consider a marginal increase in  $v$  targeted to low income households with  $y \leq y_T$ . The denominator is positive. Consider the numerator.

$$\frac{\delta g_T(b_T^*(0), 0, \cdot)}{\delta v} = \frac{1}{N_T} \left[ \int_0^{y_T} (\hat{\alpha}(0, \cdot) - b_T^*(0)) \frac{\delta \hat{\alpha}(0, \cdot)}{\delta v} dy \right] = \frac{1}{N_T} y_T (\hat{\alpha}(0, \cdot) - b_T^*(0)) \frac{\delta \hat{\alpha}(0, \cdot)}{\delta v}$$

Note that  $\int_0^1 (\hat{\alpha}(0) - b_T^*(0)) = (\hat{\alpha}(0) - b_T^*(0)) > 0$ <sup>62</sup> since  $b_T^*(0) = \frac{\hat{\alpha}(0)}{2}$ . It follows that  $\frac{\delta g_T(b_T^*, 0, \cdot)}{\delta v} < 0$ . ■

**Proof of Proposition A.1.** Noting that  $N_T(e, v, \cdot) = \int_0^{y_T} \hat{\alpha}(e, v, \cdot) dy + \int_{y_T}^1 \hat{\alpha}(e, 0, \cdot) dy$ , the proof follows from lemma A.2. ■

**Proof of Lemma A.3.**

$$N(e, v, \cdot) = \int_0^{y_T} \int_0^{\hat{\alpha}(y, e, v, \cdot)} d\alpha dy + \int_{y_T}^1 \int_0^{\hat{\alpha}(y, e, v, \cdot)} d\alpha dy < \int_0^{y_T} \int_0^{\hat{\alpha}(y, e, v, \cdot)} d\alpha dy + \int_{y_T}^1 \int_0^{\hat{\alpha}(y, e, 0, \cdot)} d\alpha dy = N_T(e, v, \cdot)$$

The inequality follows from lemma A.2. ■

**Proof of Lemma A.4.** At the UVS equilibrium, the school chooses  $e_{VS}$ , attracts  $N(e_{VS}, v)$  and earns rent  $pN(e_{VS}, v) - c(N(e_{VS}, v)) - C(e)$ . Now  $N_T(e_{VS}, v) > N(e_{VS}, v)$ , (from lemma A.3). Therefore given  $v$ ,  $\exists \tilde{e} < e_{VS}$  such that  $N_T(\tilde{e}, v) = N(e_{VS}, v)$ , since  $\frac{\delta N_T}{\delta e} > 0$ . Then,

$$\begin{aligned} R(e_{VS}, v) &= pN(e_{VS}, v) - c(N(e_{VS}, v)) - C(e) < pN_T(\tilde{e}, v) - c(N_T(\tilde{e}, v)) - C(\tilde{e}) \\ &< pN_T(e_{TVS}, v) - c(N_T(e_{TVS}, v)) - C(e_{TVS}) = R_T(e_{TVS}, v) \end{aligned}$$

The first inequality follows because a lower effort generates smaller costs and hence higher rent, given revenue. The second inequality follows because  $e_{TVS}$  is the rent maximizing effort under targeted vouchers. ■

**Proof of Proposition A.2.**

The proof consists of two steps:

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<sup>62</sup> When  $v = 0$ ,  $b_T^*(0)$  is the same as  $b^*(0)$ .

**Step 1:** First assume that vouchers, if imposed under the TOV program, take a similar targeted form as in the TVS case. Then if the school decides not to meet the cutoff, it chooses  $e_{TVS}$  and gets the TVS equilibrium rent. Since vouchers decrease rent:

$$pN(e_{TVS}, 0) - c(N(e_{TVS}, 0)) - C(e_{TVS}) > pN_T(e_{TVS}, v) - c(N_T(e_{TVS}, v)) - C(e_{TVS}) = R_T(e_{TVS}, v)$$

Therefore,  $\exists \bar{e} > e_{TVS}$  such that the public school incentive constraint is satisfied with equality.

**Step 2:** However, since vouchers under the TOV program actually take the universal form rather than the targeted form, school chooses  $e_{VS}$  and gets rent  $R(e_{VS}, v)$  if it fails to meet the cutoff. Then it follows from step 1 and lemma A.4:

$$R(\bar{e}, 0) = R_T(e_{TVS}, v) > R(e_{VS}, v)$$

Therefore  $\exists \bar{e} > \bar{e} > e_{TVS}$  such that  $R(\bar{e}, 0) = R(e_{VS}, v)$ . ■

**Proof of Corollary A.1.**  $e_{TOV} > e_{TVS}$  from proposition A.2

$$\Rightarrow q(e_{TOV}, b^*(e_{TOV}, 0)) > q(e_{TVS}, b_T^*(e_{TVS}, 0)) > q(e_{TVS}, b_T^*(e_{TVS}, v)) \text{ since } q_e, q_b > 0 \text{ and } \frac{\delta b_T^*}{\delta e} > 0, \frac{\delta b_T^*}{\delta v} < 0. \quad \blacksquare$$

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**Table 1: Effect of “Threatened Status” on FCAT Reading (1998-2002), Math (1998-2002) and Writing (1994-2002) Scores**  
(Sample of treated F and control D schools in Florida)

	Grade 4 Reading						Grade 5 Math			Grade 4 Writing		
	OLS	FE	OLS	FE	OLS	FE	FE	FE	FE	FE	FE	
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
trend	-0.59 (0.57)	-0.20 (0.67)					12.80*** (0.76)				0.21*** (0.004)	
Program dummy	-5.25*** (1.46)	-5.30*** (0.84)					0.31 (0.91)				0.10*** (0.02)	
Program dummy * trend	5.35*** (0.57)	5.57*** (0.76)					-9.11*** (0.85)				-0.13*** (0.01)	
Treated * Program dummy	2.71* (1.60)	2.97* (1.78)	2.74* (1.65)	2.99* (1.80)			7.90** (2.29)	7.88*** (2.30)			0.30*** (0.05)	0.31*** (0.05)
Treated * Program dummy * trend	1.57** (0.74)	1.10 (1.00)	1.59** (0.76)	1.09 (1.00)			-0.71 (1.04)	-0.60 (1.06)			0.04** (0.02)	0.04** (0.02)
Treated * 1 year after program					4.85*** (1.49)	4.85*** (1.68)			6.78*** (1.63)			0.35*** (0.04)
Treated * 2 years after program					4.71*** (1.78)	3.30* (1.71)			7.25*** (1.82)			0.37*** (0.04)
Treated * 3 years after program					8.01*** (1.49)	7.08*** (1.78)			5.35*** (2.00)			0.43*** (0.05)
Year dummies	N	N	Y	Y	Y	Y	N	Y	Y	N	Y	Y
Controls	N	Y	N	Y	N	Y	Y	Y	Y	Y	Y	Y
Observations	2567	2550	2567	2550	2567	2550	2524	2524	2524	4476	4476	4476
R-squared	0.11	0.77	0.11	0.77	0.11	0.77	0.76	0.76	0.76	0.84	0.85	0.85
p-value <sup>1</sup>	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

\*, \*\*, \*\*\*: significant at the 10, 5, and 1 percent level, respectively. <sup>1</sup> p-value of F-test of the program effect on treated schools. Huber-White standard errors are in parentheses. All regressions are weighted by the number of students tested. The OLS columns include an F dummy and allow for correlations within districts. Columns (10)-(12) include an interaction term of treated dummy with trend. Controls include race, sex, percentage of students eligible for free or reduced-price lunches and real per pupil expenditure.

**Table 2: Effect of “Threatened Status” on FCAT Reading (1998-2002), Math (1998-2002) and Writing (1994-2002) Scores**  
(Sample of treated F, D and control C schools in Florida)

	Reading				Math				Writing			
	OLS	FE	OLS	FE	OLS	FE	OLS	FE	OLS	FE	OLS	FE
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
Less treated * program	1.70**	1.20			-0.23	-0.15			0.08***	0.08***		
	(0.84)	(1.00)			(0.92)	(1.09)			(0.02)	(0.02)		
More treated * program	4.88**	4.99**			9.05***††	9.02***††			0.38***††	0.37***††		
	(2.04)	(2.43)			(2.13)	(2.23)			(0.09)	(0.05)		
Less treated * program	5.22***	4.85***			0.29	0.30			-0.03	-0.03		
*trend	(0.81)	(0.93)			(0.60)	(1.04)			(0.02)	(0.02)		
More treated * program	7.73***	8.02***			0.91	0.54			0.01††	0.00		
*trend	(2.47)	(2.08)			(1.10)	(1.01)			(0.02)	(0.02)		
Less treated * 1 year after			4.13***	3.53***			1.06***	0.97			0.05**	0.05**
			(0.75)	(0.76)			(0.73)	(0.85)			(0.02)	(0.02)
Less treated * 2 years after			5.84***	5.52***			2.83**	2.54***			0.00	0.00
			(0.96)	(0.80)			(1.44)	(0.94)			(0.03)	(0.02)
Less treated * 3 years after			8.60***	7.94***			3.89***	3.47***			-0.03	-0.03
			(0.93)	(0.87)			(1.20)	(0.92)			(0.04)	(0.02)
More treated * 1 year after			9.45***††	9.32***††			9.56***††	8.96***††			0.40***††	0.39***††
			(1.92)	(1.87)			(2.02)	(1.59)			(0.07)	(0.04)
More treated * 2 years after			11.01***†	10.75***†			11.61***†††	11.00***††			0.39***†	0.37***†
			(2.39)	(1.87)			(2.99)	(1.77)			(0.07)	(0.04)
More treated * 3 years after			17.08***††	16.03***††			11.39***††	11.94***††			0.42***†	0.39***†
			(2.64)	(1.91)			(3.46)	(1.95)			(0.05)	(0.05)
Controls	N	Y	N	Y	N	Y	N	Y	N	Y	N	Y
Observations	6034	5933	6034	5933	6003	5909	6003	5909	10646	10587	10646	10587
R-squared	0.44	0.86	0.44	0.86	0.44	0.83	0.44	0.83	0.72	0.85	0.74	0.86
p-value <sup>1</sup>	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

\*, \*\*, \*\*\*: significant at the 10, 5, and 1 percent level, respectively. †, ††: more treated significantly different from less treated at 5 and 1 percent level respectively. <sup>1</sup> p-value of the F-test of program effect on treated schools. Huber-White standard errors are in parentheses. The OLS columns include more treated and less treated dummies and allow for correlations within districts. All regressions are weighted by the number of students tested. Columns (1)-(2), (5)-(6), (9)-(10) include program dummy, trend and an interaction of trend with program dummy while columns (3)-(4), (7)-(8), (11)-(12) contain year dummies. Columns (1)-(2), (5)-(6), (9)-(12) include interactions of trend with less treated and more treated dummies respectively and (3)-(4), (7)-(8) include interaction of  $D_1$  dummy ( $D_1 = 1$  if year > 1998) with less treated and more treated dummies respectively. Controls include race, sex, percentage of students eligible for free or reduced-price lunches and real per pupil expenditure.

**Table 3: Effect of the Milwaukee “Voucher Shock” Program**

	Using treatment groups						Cont. treatment var.
	WRCT (% above)		ITBS Reading		ITBS Math		WRCT (% above)
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Somewhat treated*program dummy	3.50		3.57		0.39		
	(2.59)		(5.24)		(2.81)		
More treated * program dummy	2.85		1.61		-2.97		
	(3.32)		(4.98)		(3.13)		
Somewhat treated*program dummy	0.64		1.34		0.61		
*trend	(0.47)		(0.34)		(0.54)		
More treated*program dummy*trend	0.67		0.94		0.50		
	(0.62)		(2.31)		(0.63)		
Somewhat treated * 1 year after program		2.03		4.15		-1.35	
		(2.81)		(4.49)		(2.94)	
Somewhat treated * 2 years after program		5.38**		7.83		6.14*	
		(2.43)		(5.17)		(3.38)	
Somewhat treated * 3 years after program		5.01		6.78		2.47	
		(3.03)		(5.31)		(3.31)	
More treated * 1 year after program		-0.92		1.12		-4.02	
		(3.33)		(3.86)		(3.26)	
More treated * 2 years after program		6.06*		6.59		4.36	
		(3.14)		(5.15)		(3.83)	
More treated * 3 years after program		5.69		2.85		-2.22	
		(3.98)		(5.18)		(3.54)	
Treatment * 1 year after program							-0.09
							( 0.09)
Treatment * 2 years after program							0.07
							(0.09)
Treatment * 3 years after program							0.03
							(0.11)
Year dummies	N	Y	N	Y	N	Y	Y
Observations	1195	1195	717	717	1127	1127	920
R-squared	0.50	0.58	0.55	0.55	0.58	0.60	0.55
p-value <sup>1</sup>	0.06	0.11	0.67	0.62	0.49	0.27	0.29

\*, \*\*, \*\*\*: significant at the 10, 5, and 1 percent level, respectively. <sup>1</sup> p-value of the F-test of joint significance of more treated shift coefficients. Huber-White standard errors are in parentheses. This table uses the 66-47 sample. All regressions include school fixed effects and control for race, sex, percentage of students eligible for free or reduced-price lunches and real per pupil expenditure. Columns (1), (3), (5) include program dummy, trend and an interaction of trend with program dummy.

Table 4: Mean Reversion of the 98F Schools Compared to 98D and 98C Schools, 1998-1999.

<b>Panel A: 98F and 98D Schools</b>		Dependent Variable: FCAT Score, 1998-99.					
	Reading		Math		Writing		
	(1)	(2)	(3)	(4)	(5)	(6)	
	OLS	FE	OLS	FE	OLS	FE	
trend	2.27***	2.01***	14.25***	14.02***	0.04***	0.04***	
	(0.67)	(0.43)	(0.65)	(0.49)	(0.01)	(0.01)	
98F*trend	-0.45	-0.65	1.03	1.17	0.14***	0.14***	
	(1.77)	(1.14)	(1.81)	(1.19)	(0.03)	(0.02)	
Observations	1353	1353	1354	1354	1355	1355	
R <sup>2</sup>	0.64	0.93	0.63	0.91	0.33	0.85	

<b>Panel B: 98F, 98D and 98C Schools</b>		Dependent Variable: FCAT Score, 1998-99.					
	Reading		Math		Writing		
	(1)	(2)	(3)	(4)	(5)	(6)	
	OLS	FE	OLS	FE	OLS	FE	
trend	1.76**	1.76***	9.57***	9.71***	0.03***	0.03***	
	(0.56)	(0.35)	(0.50)	(0.36)	(0.01)	(0.01)	
98F*trend	0.18	-0.55	4.67***	4.63***	0.14***	0.14***	
	(1.78)	(1.12)	(1.80)	(1.16)	(0.03)	(0.02)	
98D*trend	0.41	0.16	4.61***	4.22***	0.01	0.01	
	(0.88)	(0.54)	(0.82)	(0.58)	(0.02)	(0.01)	
Observations	2605	2605	2608	2608	2608	2608	
R <sup>2</sup>	0.76	0.96	0.76	0.94	0.38	0.87	

\*, \*\*, \*\*\*: significant at the 10, 5, and 1 percent level. All regressions include race, sex, % of students eligible for free or reduced-price lunches and real per pupil expenditure as controls. The OLS regressions include 98F and 98D dummies. Sample of 98F and 98D schools: s.d of FCAT reading, math and writing respectively are 18.9, 18.05, 0.30. Sample of 98F, 98D, 98C schools: s.d of FCAT reading, math and writing respectively are 21.16, 21.56 and 0.31.

**Table 5: Comparing the Impact of Florida “Threat of Voucher” and Milwaukee “Voucher Shock” Programs**

Using performance in reading test [WRCT (% above) 1989-97 and FCAT Reading 1998-2002] and math test [ITBS Math 1986-1997 and FCAT Math 1998-2002]

	Corrected for Mean Reversion							
	Reading		Math		Reading		Math	
	Wisconsin WRCT (1)	Florida FCAT (2)	Wisconsin ITBS (3)	Florida FCAT (4)	Wisconsin WRCT (5)	Florida FCAT (6)	Wisconsin ITBS (7)	Florida FCAT (8)
More Treated * 1 year after prog	-0.06	0.47***	-0.24	0.45***	-0.06	0.47***	-0.24	0.24***
More treated * 2 years after prog	0.38*	0.50 ***	0.26	0.55***	0.38*	0.50***	0.26	0.34***
More treated * 3 years after prog	0.35	0.80***	-0.13	0.60***	0.36	0.80***	-0.13	0.39***

\*, \*\*, \*\*\*: significant at the 10, 5, and 1 percent level, respectively. All figures are in terms of respective sample standard deviations. This table uses the 66-47 sample for Milwaukee. All figures are obtained from regressions that contain school fixed effects, year dummies, interactions of year dummies with the respective treatment dummies, race, sex, percentage of students eligible for free or reduced-price lunches and real per pupil expenditure. Standard deviation of FCAT reading scores = 20, Standard deviation of FCAT math scores = 20, Standard deviation of WRCT (% above) reading scores = 16, Standard deviation of ITBS reading scores = 18.45, Standard deviation of ITBS math scores = 16.71. For standard deviations corresponding to the mean reversion sample, see footnote for table 4.

**Table 6A: Pre-program Characteristics of Florida F and D schools  
in Regression Discontinuity Sample**

	F (std. dev.)	D (std. dev.)	F-D [p-value]
% black	64.68 (28.39)	64.08 (28.18)	0.60 [0.92]
% hispanic	17.99 (20.88)	20.16 (23.67)	-2.16 [0.66]
% white	16.42 (18.81)	14.31 (16.83)	2.11 [0.57]
% male	51.22 (4.00)	51.49 (5.43)	-0.27 [0.81]
% free-reduced lunch	86.30 (8.34)	83.60 (11.98)	2.64 [0.26]
FCAT Reading Score	253.97 (17.33)	254.18 (15.47)	-0.21 [0.95]
FCAT Math Score	274.25 (13.34)	275.64 (13.49)	-1.39 [0.63]
FCAT Writing Score	2.55 (0.11)	2.68 (0.11)	-0.02 [0.00]
Number of Schools	33	70	

**Table 6B: Regression Discontinuity Analysis in Florida**

	Reading FE (1)	Math FE (2)	Writing FE (3)
Treated * 1 year after Program	4.21* (2.46)	8.03*** (2.58)	0.19*** (0.06)
Treated * 2 years after Program	3.45* (2.06)	7.12** (3.04)	0.12* (0.06)
Treated * 3 years after Program	7.47** (3.06)	6.49** (3.26)	0.20*** (0.08)
Year dummies	Y	Y	Y
Observations	513	505	909
R-squared	0.76	0.76	0.87
p-value	0.01	0.00	0.00

\*, \*\*, \*\*\* denote significance at the 10, 5, and 1 percent levels respectively. Huber-White standard errors are in parentheses. All regressions are weighted by the number of students tested, include school fixed effects and control for race, sex, percentage of students eligible for free or reduced price lunches and real per pupil expenditure.

**Table 7. Is there a Stigma Effect of getting the Lowest Performing Grade?  
Effect of being Categorized in Group 1 on FCAT Writing Scores**

	Using FCAT Writing Scores, 1997-1998					
	Sample: Group 1, 2 Schools			Sample: Group 1, 2, 3 Schools		
	OLS (1)	FE (2)	FE (3)	OLS (4)	FE (5)	FE (6)
Trend	0.52*** (0.04)	0.52*** (0.03)	0.48*** (0.04)	0.48*** (0.02)	0.48*** (0.01)	0.46*** (0.02)
Group 1 * trend	-0.01 (0.08)	-0.02 (0.06)	-0.02 (0.06)	0.03 (0.07)	0.01 (0.05)	0.02 (0.05)
Group 2 * trend				0.03 (0.04)	0.04 (0.03)	0.04 (0.03)
Controls	N	N	Y	N	N	Y
Observations	314	314	314	1361	1361	1358
R-squared	0.49	0.84	0.85	0.52	0.87	0.87

\*, \*\*, \*\*\*: significant at the 10, 5, and 1 percent level, respectively. Huber-White standard errors are in parentheses. All regressions are weighted by the number of students tested and include race, sex, percentage of students eligible for free or reduced-price lunches and real per pupil expenditure as controls. The OLS regressions include group 1 and group 2 dummies.



**Table 8: Milwaukee Parental Choice Program: Membership**

Year	Number of Schools	Voucher* Students	MPS Students	Year	Number of Schools	Voucher* Students	MPS Students
1990-91	7	300		1997-98	23	1497	101,253
1991-92	6	512	93,381	1998-99	83	5761	99,814
1992-93	11	594	94,258	1999-00	90	7575	99,729
1993-94	12	704	95,258	2000-01	100	9238	97,985
1994-95	12	771	98,009	2000-01	100	9238	97,985
1995-96	17	1288	98,378	2001-02	102	10497	97,762
1996-97	20	1616	101,007	2002-03	102	11350	97,293

\* "Voucher Students" is calculated as the average of September and January FTE, plus summer school.

**Table 9: Comparing the impact of Florida and Milwaukee phase II programs**

Using reading [WKCE 1997-2002 and FCAT 1998-2002] and math test [WKCE 1997-2002 and FCAT 1998-2002]

	Reading		Math		Corrected for Mean Reversion			
					Reading		Math	
	Wisconsin WKCE (1)	Florida FCAT (2)	Wisconsin WKCE (3)	Florida FCAT (4)	Wisconsin WKCE (5)	Florida FCAT (6)	Wisconsin WKCE (7)	Florida FCAT (8)
More Treated * 1 year	0.20	0.47***	0.27	0.45***	0.20	0.47***	0.03	0.24***
More treated * 2 years	0.50***	0.50***	0.38***	0.55***	0.50***	0.50***	0.14***	0.34***
More treated * 3 years	0.53***	0.80***	0.57***	0.60***	0.53***	0.80***	0.33***	0.39***

All figures are in terms of respective sample standard deviations. All figures are obtained from regressions that contain school fixed effects, year dummies, interactions of year dummies with the respective treatment dummies, race, sex, free-reduced lunch percentage and real per pupil expenditure. Standard deviation of FCAT reading scores = 20, Standard deviation of FCAT Math Scores = 20, Standard deviation of WKCE reading scores = 13.07, Standard deviation of WKCE math scores = 15.01, Standard Deviation of WKCE Math for the mean reversion sample=14.4, Standard Deviation of FCAT Math for the mean reversion sample= 20.04

**Table 10: Has there been “Teaching to the Test” in Florida?**

Panel A	Correlation between FCAT and Stanford 9 NPR Scores			
	All Schools	F Schools	D Schools	C Schools
Grade 4 Reading, 2000	0.94 (1603)	0.85 (65)	0.87 (453)	0.85 (695)
Grade 4 Reading, 2001	0.96 (1651)	0.81 (64)	0.91 (451)	0.92 (694)
Grade 4 Reading, 2002	0.95 (1694)	0.85 (63)	0.88 (451)	0.91 (694)
Grade 5 Math, 2000	0.93 (1599)	0.81 (65)	0.85 (452)	0.84 (694)
Grade 5 Math, 2001	0.95 (1650)	0.89 (64)	0.91 (448)	0.91 (692)
Grade 5 Math, 2002	0.95 (1699)	0.85 (63)	0.90 (447)	0.92 (694)
Change in Grade 4 Reading, 2001-00	0.92	0.91	0.91	0.92
Change in Grade 4 Reading, 2002-01	0.94	0.92	0.93	0.95
Change in Grade 5 Math, 2001-00	0.93	0.93	0.92	0.92
Change in Grade 5 Math, 2002-01	0.95	0.94	0.94	0.94

Panel B	Dependent Variable = Stanford 9 NPR Scores					
	Reading			Math		
	Grade 3 (1)	Grade 4 (2)	Grade 5 (3)	Grade 3 (4)	Grade 4 (5)	Grade 5 (6)
More treated * 2001 year dummy	1.53*** (0.83)	3.41*** (0.82)	2.19*** (0.71)	3.08*** (1.00)	3.35*** (1.01)	3.06*** (1.08)
More treated * 2002 year dummy	2.58*** (0.91)	4.40***††† (0.89)	2.12*** (0.72)	4.62***† (1.12)	6.33***††† (1.09)	1.87* (1.10)
Less treated * 2001 year dummy	1.49*** (0.42)	2.59*** (0.41)	2.31*** (0.39)	1.75*** (0.48)	2.84*** (0.44)	2.45*** (0.49)
Less treated * 2002 year dummy	2.45*** (0.44)	2.49*** (0.43)	2.96 (0.42)	2.22*** (0.52)	3.24*** (0.47)	2.90*** (0.50)
Observations	3546	3545	3530	3546	3544	3530
R <sup>2</sup>	0.91	0.91	0.93	0.90	0.92	0.89
p-value	0.02	0.00	0.01	0.00	0.00	0.02

Panel A: All correlations are significantly different from zero at the 1% level. The number of schools in the corresponding category are in parentheses.

Panel B: \*, \*\*, \*\*\*: significant at the 10, 5, and 1 percent level, respectively. <sup>1</sup>p-value of the F-test for joint significance of post-program more treated year effects. Huber-White standard errors are in parentheses. All regressions are weighted by the number of students tested and include school fixed effects, year dummies, race, sex, percentage of students eligible for free or reduced-price lunches and real per pupil expenditure.

**Table D.1: Pre-program Demographic Characteristics of More Treated Schools and Control Schools in Florida and Wisconsin**

<b>Panel A</b>	Florida	Wisconsin		Florida–Wisconsin	
		66-47	60-47	66-47	60-47
<b>More treated Schools</b>	(std. dev.)	(std.dev.)	(std.dev.)	[p-value]	[p-value]
% black	62.79 (28.23)	66.55 (32.22)	62.90 (29.58)	-3.76 [0.56]	-0.10 [0.99]
% hispanic	18.95 (23.40)	18.07 (24.54)	14.81 (21.86)	0.88 [0.87]	4.14 [0.36]
% white	17.18 (19.54)	10.21 (10.68)	17.38 (16.55)	6.97 [0.07]	-0.20 [0.96]
%male	51.38 (4.84)	52.25 (2.60)	52.33 (2.58)	-0.87 [0.34]	-0.95 [0.22]
% free-reduced lunch	85.80 (9.95)	84.5 (6.48)	82.9 (9.04)	1.3 [0.50]	2.9 [0.12]

<b>Panel B</b>	Florida	Wisconsin	Florida–Wisconsin
<b>Control Schools</b>			
% black	18.12 (14.17)	22.37 (12.93)	-4.25 [0.10]
% hispanic	15.49 (21.23)	14.84 (6.02)	0.17 [0.86]
% white	63.59 (22.33)	60.85 (12.80)	2.73 [0.49]
% male	51.38 (4.84)	50.63 (2.29)	0.76 [0.43]
% free-reduced lunch	50.14 (17.51)	44.95 (11.66)	5.19 [0.10]

# FCAT Reading, Math and Writing-F,D Schools

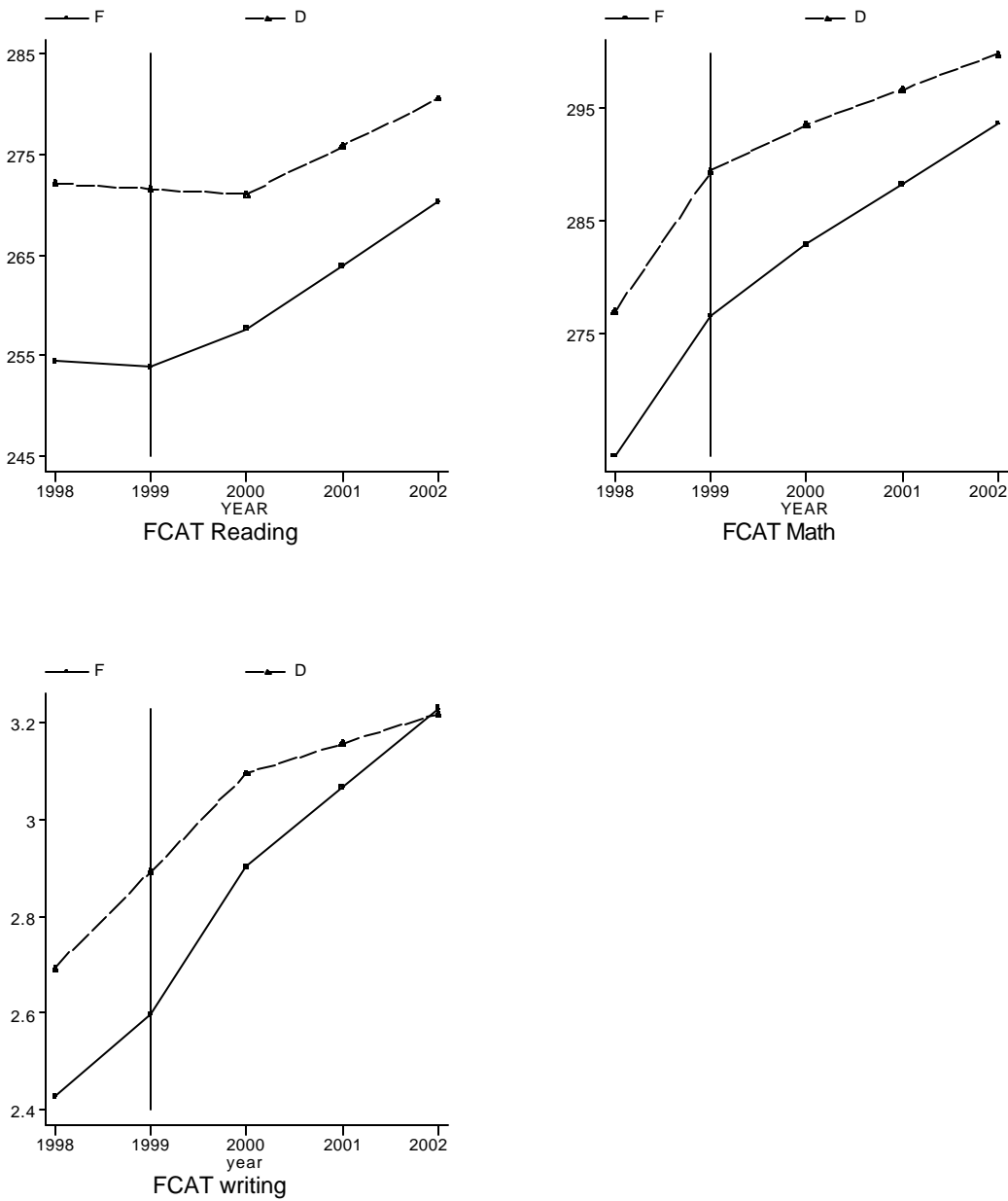


Figure 1. Florida 'threat of voucher' Program

### ITBS Reading and Math --MT, ST and LT

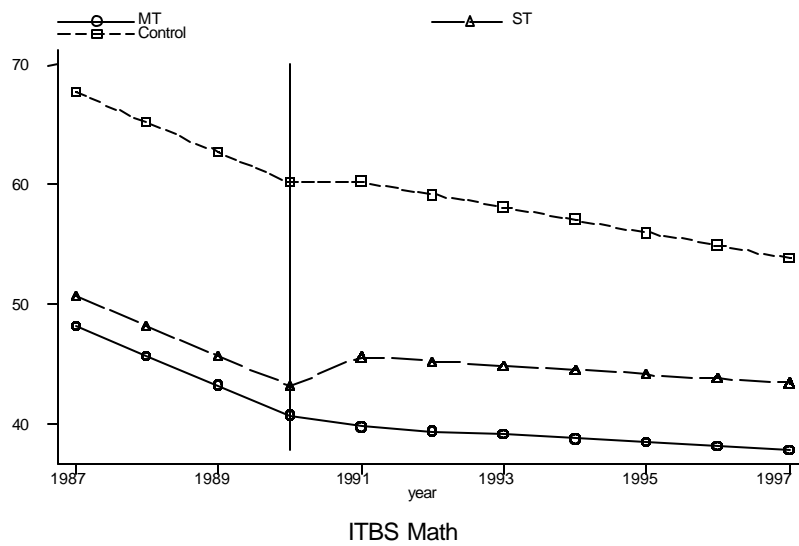
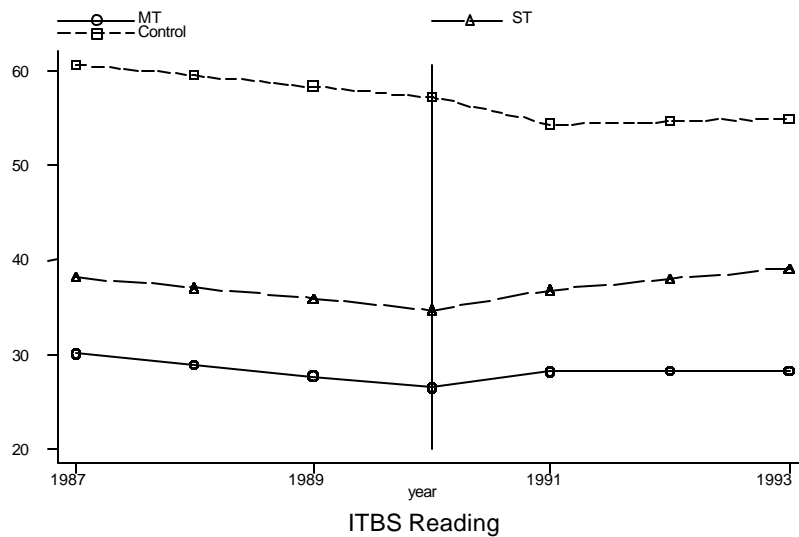
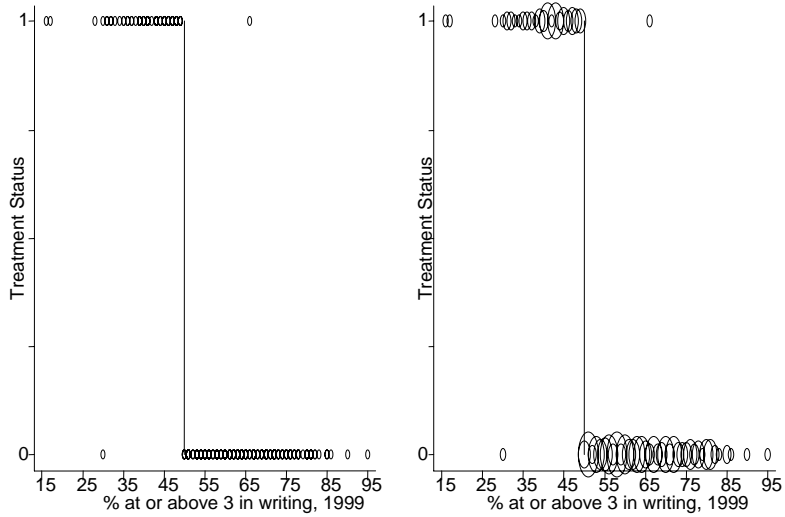
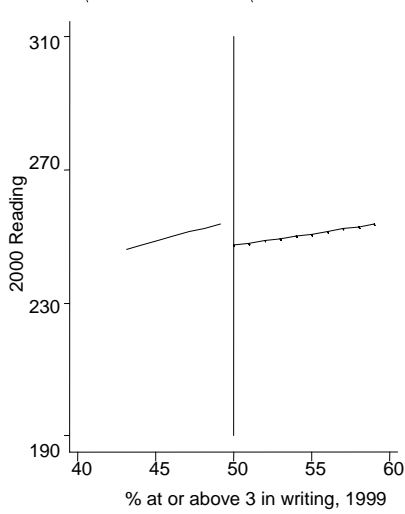


Figure 2. Milwaukee Voucher Shock Program

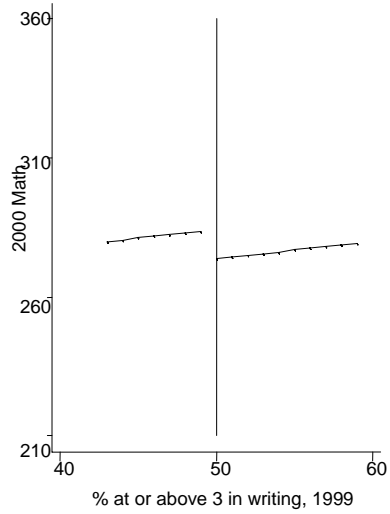


Panel A

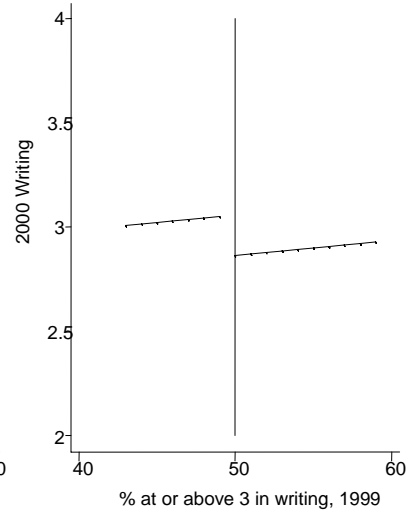
Panel B



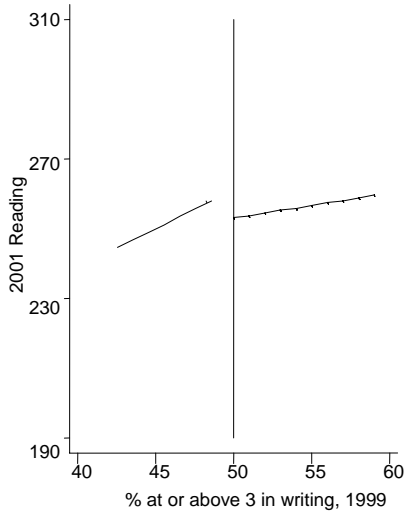
Panel C



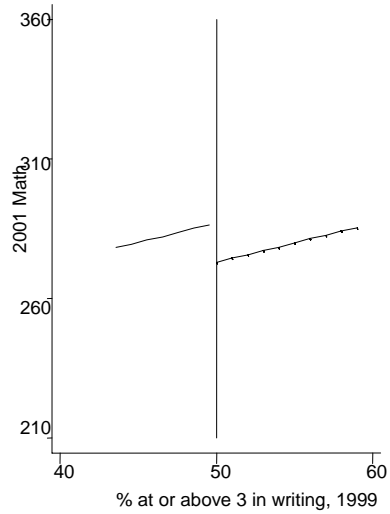
Panel D



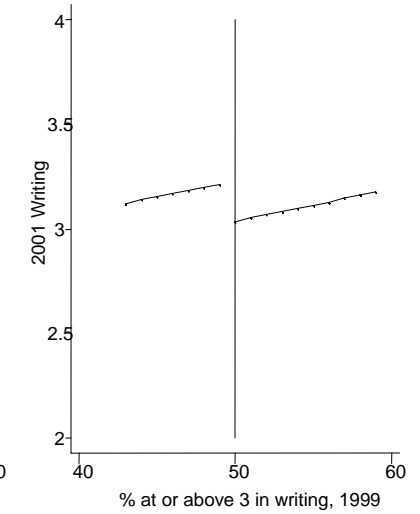
Panel E



Panel F



Panel G



Panel H

Figure 3. Regression Discontinuity Analysis