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SFB 649 Discussion Paper 2012-026

# Explaining regional unemployment differences in Germany: a spatial panel data analysis

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# Explaining regional unemployment differences in Germany: a spatial panel data analysis

Franziska Lottmann\*

## Abstract

This paper analyzes determinants for regional differences in German unemployment rates. We specify a spatial panel model to avoid biased and inefficient estimates due to spatial dependence. Additionally, we control for temporal dynamics in the data. Our study covers the whole of Germany as well as East and West Germany separately. We exploit district-level data on 24 possible explanatory variables for the period from 1999 until 2007. Our results suggest that the spatial dynamic panel model is the best model for this analysis. Furthermore, we find that German regional unemployment is of disequilibrium nature, which justifies political interventions.

**Keywords:** regional unemployment, spatial dependence, spatial panel models, Germany

**JEL classification:** C23, R12, R23

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# 1 Introduction

The unemployment rate is a widely used and often discussed indicator for the economic well-being of a country. However, the discussion is mostly concentrated on national unemployment rates which give no information about the regional structure of unemployment. Though, data on regional unemployment rates show substantial differences between regions. According to Taylor and Bradley (1997), regional differences within a country are stronger than differences between countries. Regional differences are of particular interest in Germany due to the specific history of the country. Until 1990, Germany was divided into two separate countries with different economic systems. The division of Germany caused structural differences resulting in adjustment processes which have not been fully completed until today.

This paper analyzes determinants for regional differences in German unemployment rates using spatial econometric methods. We identify the driving factors in the whole of Germany as well as in East and West Germany separately. Twenty years after German reunification, this study is, to our best knowledge, the first contribution investigating regional unemployment in Germany.

A specific feature of regional labor markets is their correlatedness over space. The presence of spatial (auto-)correlation implies that the level of regional unemployment in one particular region is correlated with that of neighboring regions. On the one hand, firms do not restrict their recruiting activities to their resident location and, on the other hand, job searchers might accept a job in a different area. The spatial econometric literature shows that ignoring spatial effects yields biased and inefficient estimates (see Anselin and Bera (1998) among others). Therefore, we apply a spatial econometric model to avoid these shortcomings.

To model regional unemployment, we take into account 24 possible explanatory variables containing equilibrium and disequilibrium and derive our set of regressors by

model selection. We have panel data on 412 German districts coresponding to German NUTS<sup>1</sup> III regions for the period from 1999 until 2007. As labor market data exhibit not only spatial but also temporal dynamics, we utilize both a static and a dynamic modeling approach while most contributions in the literature consider only static model specifications. Both applying a spatial panel model and a dynamic modeling to the context of regional unemployment are novel to the literature.

Regional unemployment differentials have been subject of intensive research in the literature. From a methodological point of view, the empirical literature can be divided into two strands of literature. On the one hand, models for regional unemployment are estimated using (non-spatial) panel data techniques. Examples are Partridge and Rickman (1997) who use data on state unemployment for the United States, and Taylor and Bradley (1997) who provide a comparative study for regional unemployment disparities in Germany, Italy and the United Kingdom. Their data for Germany covers only the Western part for the period from 1984 until 1994. They use data on the level of German *Länder* which correspond to the NUTS I level. On the other hand, contributions apply spatial econometric models in a cross-sectional setting. The first contribution in this direction is by Molho (1995) in which he provides evidence for the presence of significant spillovers in the adjustment to local shocks using data on 280 Local Labor Market Areas in Great Britain. Further examples for this strand of literature are Aragon et al. (2003) who analyze district-level data for the Midi-Pyrénées region of France and Cracolici et al. (2007) who explore the geographical distribution of unemployment in Italy. Finally, Elhorst (2003) provides a survey on theoretical models and explanatory variables for regional unemployment differences.

We contribute to the existing literature by the following two aspects: Firstly, we apply both a static and a dynamic spatial panel model. Furthermore, we exploit the panel

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<sup>1</sup>NUTS (French abbreviation) stands for "Nomenclature of Territorial Units for Statistics", and it is a hierarchical classification of regional units for statistical purposes.

dimension of the data and, in addition to that, we account for both spatial and temporal dependence in the data. Our results show that the spatial dynamic panel model fits our data in the best way. Secondly, we provide evidence that regional unemployment in Germany is of disequilibrium nature which provides a justification for political interventions on regional labor markets.

The structure of this paper is as follows: The second section briefly reviews theoretical explanations for regional unemployment differentials while the third presents the data set and explains how the spatial weights matrix is defined. The econometric model is introduced in the fourth section which covers model selection, specification testing and spatial econometric modeling. The fifth section is dedicated to the estimation results for the whole of Germany as well as for East and West Germany individually. Finally, the last section concludes.

## **2 Theoretical explanations for regional unemployment differentials**

Classical economic theory suggests that differences in regional unemployment should not occur because unemployed living in a region with high unemployment are expected to move to an area with lower unemployment. A similar reasoning holds for firms which are assumed to move from low-unemployment to high-unemployment regions because they can benefit from a larger pool of workers. However, regional unemployment data shows substantial differences.

### **2.1 Why do regional unemployment rates differ?**

The literature provides different explanations for the existence of regional unemployment differentials which can be summarized into two different views. The equilibrium view assumes the existence of a stable equilibrium in which regions have differ-

ent unemployment rates. According to Molho (1995), this equilibrium is characterized by “uniform utility across areas for homogeneous labor group” (p. 642). In this setting, there is no incentive for further migration. Hence, households (and firms) need to be compensated for high (low) unemployment by other positive factors, so-called amenities. Such amenities are, for example, better climate, reasonable housing prices or higher quality of life. Hence, the equilibrium rate of unemployment in region  $i$  is a function of the amenity endowment in this region (Marston (1985)). The equilibrium view has received theoretical and empirical support from (among others) Marston (1985) drawing on ideas from Hall (1970).

Contrary to the equilibrium view, the disequilibrium view assumes that regional unemployment will equalize in the long run. However, the adjustment process might be slow. The speed of adjustment depends on different factors that are connected to both labor supply and labor demand. Such factors are, for example, the age structure and the educational attainment of the population. Young people are more likely to migrate as they have lower opportunity costs and are less risk averse (Aragon et al. (2003)). People holding a degree of higher education are also more likely to move because the labor market for high-skilled workers is larger and these persons are expected to be better informed (Aragon et al. (2003)). The structure of the labor force also influences the relocation behavior of firms. Moreover, population density also affects the adjustment process to the long-run equilibrium. Unemployment is expected to be lower in urban areas because the matching process between unemployed and vacant jobs is more efficient. Furthermore, the migration behavior of people is clearly influenced by migration costs. For example, housing prices and the structure of the housing market influence how easy it is for a household to change its location.

These explanations for regional unemployment differences give rise to different conclusions for policy makers. According to Marston (1985), government efforts to reduce regional unemployment differentials are “useless” (p. 58) since they cannot reduce un-

employment anywhere for long when the level of regional unemployment can be considered as equilibrium state. By contrast, the disequilibrium view delivers an “implicit justification for programs that target government funds to depressed areas” (Marston (1985), p. 58). In light of these different consequences for policy, it is important to assess whether regional unemployment can be considered as equilibrium phenomenon or not.

However, both explanatory approaches for regional unemployment are not necessarily mutually exclusive. Marston (1985) states that “it may be that an equilibrium relationship exists, but that equilibrating forces are so weak that individual areas spend a long period of time away from their equilibrium” (p. 59). For the German case, there are arguments for both theoretical approaches to explain the regional labor market situation. On the one hand, about twenty years after German reunification, the economic catching-up process of East Germany is not yet complete. But, on the other hand, regional unemployment rates are not expected to equalize in the long run because of structural differences between regions. There exist structural differences not only between East and West Germany but also within East and West Germany and other areas.

Partridge and Rickman (1997) combine both approaches and extend the set of factors that might influence regional unemployment. In contrast to the equilibrium view, they do not assume that household utility in terms of income and amenities will equalize across areas in equilibrium. They add monetary and psychological costs of household relocation to the household utility function. These costs can be sufficiently high such that moving of households is limited. As regional unemployment in Germany has both equilibrium and disequilibrium aspects, we base our empirical analysis on Partridge and Rickman (1997).



## **2.2 Set of possible determining factors**

Following Partridge and Rickman (1997), we assume that unemployment in region  $i$  in year  $t$  depends on disequilibrium variables and an equilibrium component which is a function of market equilibrium effects, demographic characteristics as well as producer and consumer amenities. For the choice of the actual variables in these categories we take into account the empirical regional unemployment literature. However, the set of our variables is limited by data availability.

### **Disequilibrium effects**

We use the employment growth rate which, according to the literature, has turned out to be an important determinant for regional unemployment. This is not surprising because the change in employment directly affects unemployment.<sup>2</sup> Another variable capturing disequilibrium effects are wages or unit labor costs. Unfortunately, this data is not available on the desired regional level for our analysis.

### **Market equilibrium effects**

To account for the sectoral structure of regions, we use employment shares of different sectors. According to Martin (1997), industrial composition effects are a “primary reason” (p. 244) for labor demand and regional unemployment to differ across regions.

### **Demographic characteristics**

Demographic characteristics influence both labor demand and labor supply by affecting the number of new hires, quits, and workers leaving the labor force (Partridge and Rickman (1997)). We use the share of young and older persons to account for the age structure of the labor force. In contrast to studies on other countries, as for example the United States, German labor market data does not contain any information on ethnicity in general. However, we have data on the share of foreigners in the labor force. Another important demographic variable is labor force participation, especially female

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<sup>2</sup>It would be interesting to analyze the impact of (temporally) lagged values of employment growth on regional unemployment. However, to our best knowledge, employment data on periods prior to 1999 is not available on the level of districts.

labor force participation. Due to different social roles of women in both German countries before 1990, labor force participation of women differs substantially between East and West Germany. Unfortunately, the data on female labor force participation is only available on the level of *Regierungsbezirke* which partly correspond to the NUTS II regions of Germany, i.e. this variable exhibits less regional variation than the others. To include information on human capital, we utilize data providing three levels of educational attainment which are a university degree, a vocational qualification and no professional qualification at all. Furthermore, we use the balance of incoming and outgoing commuters of district  $i$  to control for a region's linkages with other regions. A positive commuting balance in region  $i$  indicates that labor supply in region  $i$  increases by incoming commuters. Moreover, a positive commuting balance gives an indication for positive demand for labor in region  $i$ .

### **Amenities**

On the one hand, the impact of amenities is captured by population density. It is a proxy for consumer and producer amenities because urban areas provide more amenities than rural areas. Unemployed persons have more employment opportunities and the matching process is expected to be more efficient in urban areas. However, urban areas are also associated with pollution and congestion. On the other hand, we consider three amenity variables which, to our best knowledge, have not been considered in the regional unemployment literature so far. First, we use the public debt ratio of a district because high public debts in relation to gross domestic product (GDP) are an indication for a deficient ability of a region to finance public goods and subsidies. Additionally, strongly indebted communities are not attractive for firms to create new businesses. Second, we utilize data on the number of business registrations. This variable is a proxy for producer amenities. A higher number of new businesses will result in a higher demand for labor. Third, we use the number of overnight stays to capture a region's attractiveness to tourists. Additionally, a high number of overnight stays may

be related to high business activities.<sup>3</sup>

### 3 Data and spatial weights matrix

#### 3.1 Regional unemployment and its determining factors

The data on regional unemployment rates used in this analysis are provided online by the Federal Employment Office (*Bundesagentur für Arbeit*). As it is official data, the underlying definition of unemployment corresponds to regulations in German Social Security Code (*Sozialgesetzbuch*). Moreover, we utilize a huge regional data set of possible explanatory variables. All these variables are taken from the regional database of the Federal Statistical Office of Germany (*Statistisches Bundesamt*). Since there were some values missing in this database, we requested them directly from the corresponding regional statistical institutions. A detailed description of the data and sources can be found in Table 12 in the appendix. Our data set covers the period from 1999 until 2007.<sup>4</sup> The end of our sample period is determined by a change in the sectoral classification in 2008, i.e. data on employment in different industries is not comparable before and after this change of classification. The data is available for all 412 German districts (*Landkreise* and *kreisfreie Städte*) which correspond to German NUTS III regions.<sup>5</sup> During our sample period, there are two reforms of district allocation. We allocate the data for the whole period in such a way that it corresponds to the situation after these reforms. Details on the district reforms can be found in the appendix.

To visualize regional differences in unemployment rates of German districts, Fig-

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<sup>3</sup>In contrast to other studies (as Cracolici et al. (2007) or Molho (1995)), we do not consider housing prices in our analysis because the majority of Germans lives in rented apartments. In 2006, 58% of the German population lived in rented apartments (see Timm (2008)). Until now, there exists no comprehensive data base for rental prices in German districts.

<sup>4</sup>In 2005, a labor market reform ("Hartz reform") became effective which changed the definition of unemployment. Therefore, the number of unemployed increased by definition in this year.

<sup>5</sup>Baddeley et al. (1998) state that NUTS III regions "most closely approximate meaningful labor markets" (p. 204). However, Eckey et al. (2007b) explain that travel-to-work areas are the relevant regional level for analyses of regional production and unemployment.

ure 1 presents a map of Germany which is colored according to the extent of regional unemployment in 2009.<sup>6</sup> Additionally, Table 3 shows summary statistics of regional unemployment rates over time. Based on these exploratory tools, we can summarize the following major facts. First, there is substantial variation in regional unemployment rates in Germany. In 2004, the district with lowest unemployment exhibited a rate of 4.4 % (Eichstätt district) while the highest regional unemployment rate amounted to 31.4 % (Uecker-Randow district). Second, the German labor market is characterized by strong differences between East and West Germany which still can be considered as consequences of German division. Regional unemployment rates are higher in East Germany. However, in a ranking of German districts with respect to unemployment, there are some East German districts that are placed ahead of West German districts. Third, besides the East-West differences, there is a slight North-South divide.

To test for stationarity of the data, we apply panel unit root tests. The results of the Im et al. (2003) (IPS) test and the Fisher-type (ADF) test which was proposed in Maddala and Wu (1999) and in Choi (2001) clearly reject the hypothesis of a unit root in regional unemployment rates at all reasonable significance levels. In addition to that, we apply the IPS test and the Fisher-type (ADF) test to our set of explanatory variables and find that all explanatory variables are stationary as well. However, Baltagi et al. (2007a) show that there can be considerable size distortions in panel unit root tests when the true model exhibits spatial error correlation. Hence, these test results can only serve as a slight indication regarding stationarity of the data.

### **3.2 Spatial autocorrelation on German labor markets**

An important component of spatial econometric models is the spatial weights matrix. It is a nonstochastic matrix that specifies exogenously the spatial relations between ob-

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<sup>6</sup>The map of Germany shows that some of the NUTS III regions lie within others, i.e. these districts have only one physical neighbor.

Table 1: Summary statistics of geographic distances (in kilometers) between centroids of German districts

Min	1st Qu.	Median	Mean	3rd Qu.	Max	Std. dev.
1.18	191.7	298	310.6	417.1	845.6	155.52

servations. Hence, the spatial weights matrix determines the neighborhood of district  $i$ . Accordingly, the term ‘neighboring’ always refers to the neighborhood set defined by the corresponding spatial weights matrix. On the one hand, we use a binary spatial weights matrix with entries zero and one and, on the other hand, matrices with general weights.

The simplest version of a spatial weights matrix is the binary contiguity matrix. When two districts share a common border, the corresponding entry in the spatial weights matrix is one and zero otherwise. The elements on the main diagonal are zero by definition. This matrix induces a simple spatial structure which might not reflect actual spatial linkages in an appropriate way. Therefore, we construct spatial weights matrices with general weights. On the one hand, we utilize data on geographic distances between districts and, on the other hand, we use a combination of geographic distance and size, as proposed in Molho (1995), to define spatial weights.

Geographic distance has frictional effects on labor market activity. Workers prefer to find a job in their closer environment because commuting and moving entail monetary and psychological costs. Therefore, we use great circle distances between centroids of districts to define the entries of the spatial weights matrix. Summary statistics of the geographic distances are provided in Table 1.

The weights of the distance-based matrix are defined by

$$w_{ij} = \begin{cases} \exp(-\tau d_{ij}) & \text{for } i \neq j \\ 0 & \text{for } i = j, \end{cases} \quad (1)$$

where  $\tau$  is a distance decay parameter and  $d_{ij}$  is the geographic distance between districts  $i$  and  $j$ . The resulting spatial weights matrix crucially depends on the choice of  $\tau$ . To determine the distance decay parameter, we use a grid search with different values for  $\tau$  and decide according to the Bayesian and Akaike's information criterion which parameter value is most suitable for our data. Niebuhr (2003) also uses this distance decay function to define the weights for her analysis of regional unemployment in Europe.

However, the distance decay function neglects the labor market size of districts. Spatial dependence differs when the extent of employment opportunities differs although distances between districts are the same. We expect that the spatial impact of a district with high employment on a low-employment district is stronger than vice versa. Therefore, we utilize the weighting scheme proposed by Molho (1995) which combines size with the distance decay effect. According to Molho (1995), the spatial weights are defined by

$$w_{ij} = \begin{cases} \frac{E_j \exp(-\eta d_{ij})}{\sum_{k \neq i} E_k \exp(-\eta d_{ik})} & \text{for } i \neq j \\ 0 & \text{for } i = j, \end{cases} \quad (2)$$

where  $E$  denotes the employment level and  $\eta$  is the distance decay parameter. As Molho (1995) points out, this weighting scheme implies that the spillover effect of the labor market situation in region  $j$  on the setting in region  $i$  increases with size of region  $j$  (measured in terms of employment) and decreases with the distance between both districts. Again, the impact of distance on the strength of the spatial relation crucially depends on the distance decay parameter  $\eta$ . We perform a grid search for  $\eta$  and decide on the appropriate value for our model according to information criteria.

Labor market activity and hence labor market data is expected to be correlated over space. To justify this aspect, we perform the Moran  $I$  test for spatial autocorrelation using regional unemployment rates. As this test is not specified for a particular spatial

process, we can apply it directly to our data. The null hypothesis of this test is the absence of spatial autocorrelation while the alternative is not exactly specified. The test statistic can be expressed by (Moran (1950))

$$I = \frac{\sum_i^n \sum_j^n w_{ij} (u_i - \bar{u})(u_j - \bar{u})}{\sum_{i=1}^n (u_i - \bar{u})^2} \quad (3)$$

where  $u_i$  and  $u_j$  are the regional levels of unemployment in district  $i$  and  $j$ .  $\bar{u}$  is defined by  $\bar{u} = \frac{1}{n} \sum_{i=1}^n u_i$  and  $w_{ij}$  is the element of the spatial weights matrix indicating the spatial impact of region  $j$  on region  $i$ . For the computation of the Moran  $I$  statistic we use the binary contiguity matrix.<sup>7</sup>

As the Moran  $I$  statistic is designed to detect spatial autocorrelation in cross-sectional data, we compute it for every year of our sample separately. The results of the Moran  $I$  test are presented in Table 2. They show that regional unemployment rates are positively spatially autocorrelated during the period from 1999 until 2007. Furthermore, they show a decreasing trend in the values of the Moran  $I$  statistic, i.e. the extent of spatial autocorrelation in regional unemployment rates decreases during 1999 and 2007.

## 4 Econometric Model

In order to control for spatial autocorrelation in the data, we specify a spatial econometric model for our analysis of regional unemployment. We apply a panel data model which allows to account for unobserved individual heterogeneity in the data. We obtain our model in two steps: Firstly, we use a model selection procedure to decide which variables from our set of possible explanatory variables actually have a significant impact on regional unemployment. Secondly, we use the specification test by Debarsy

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<sup>7</sup>We also tried the other spatial weights matrix to compute the Moran  $I$  statistic and got qualitatively the same results.

Table 2: Results of the Moran  $I$  test for spatial autocorrelation (1999-2007)

	Moran $I$	$Z$	$p$ -value
1999	0.874	26.48	0
2000	0.875	29.02	0
2001	0.890	29.51	0
2002	0.882	29.25	0
2003	0.863	28.61	0
2004	0.846	28.05	0
2005	0.799	26.5	0
2006	0.810	26.86	0
2007	0.793	26.29	0

Notes:  $Z$  denotes the standard deviate of the Moran  $I$  statistic, i.e.  $Z = \frac{I - E[I]}{sd(I)}$ . The null hypothesis is the absence of spatial autocorrelation whereas the alternative is positive spatial autocorrelation. The Moran  $I$  values are computed assuming normality.

Table 3: Summary statistics of regional unemployment rates (1999-2009)

	Min	1st Qu.	Median	Mean	3rd Qu.	Max	Std.dev.	national
1999	4	7.8	10	11.41	14.3	24.8	4.815	11.7
2000	3	6.7	8.8	10.46	13.3	25.6	5.158	10.7
2001	3	6.3	8.4	10.19	12.7	26.7	5.356	10.3
2002	3.9	6.9	9	10.69	12.9	27.6	5.279	10.8
2003	4.6	7.7	9.8	11.57	13.9	29.7	5.424	11.6
2004	4.4	7.7	9.8	11.66	14	31.4	5.467	11.7
2005	4.7	8.7	11.4	12.84	16.1	29.7	5.323	13
2006	3.7	7.7	10.5	11.81	15	27.6	5.084	12
2007	2.4	6.1	8.5	9.868	12.6	24.2	4.733	10.1
2008	1.9	4.8	7.2	8.435	11	21.5	4.306	8.7
2009	2.5	5.7	7.9	8.843	11.4	20.1	3.908	9.1



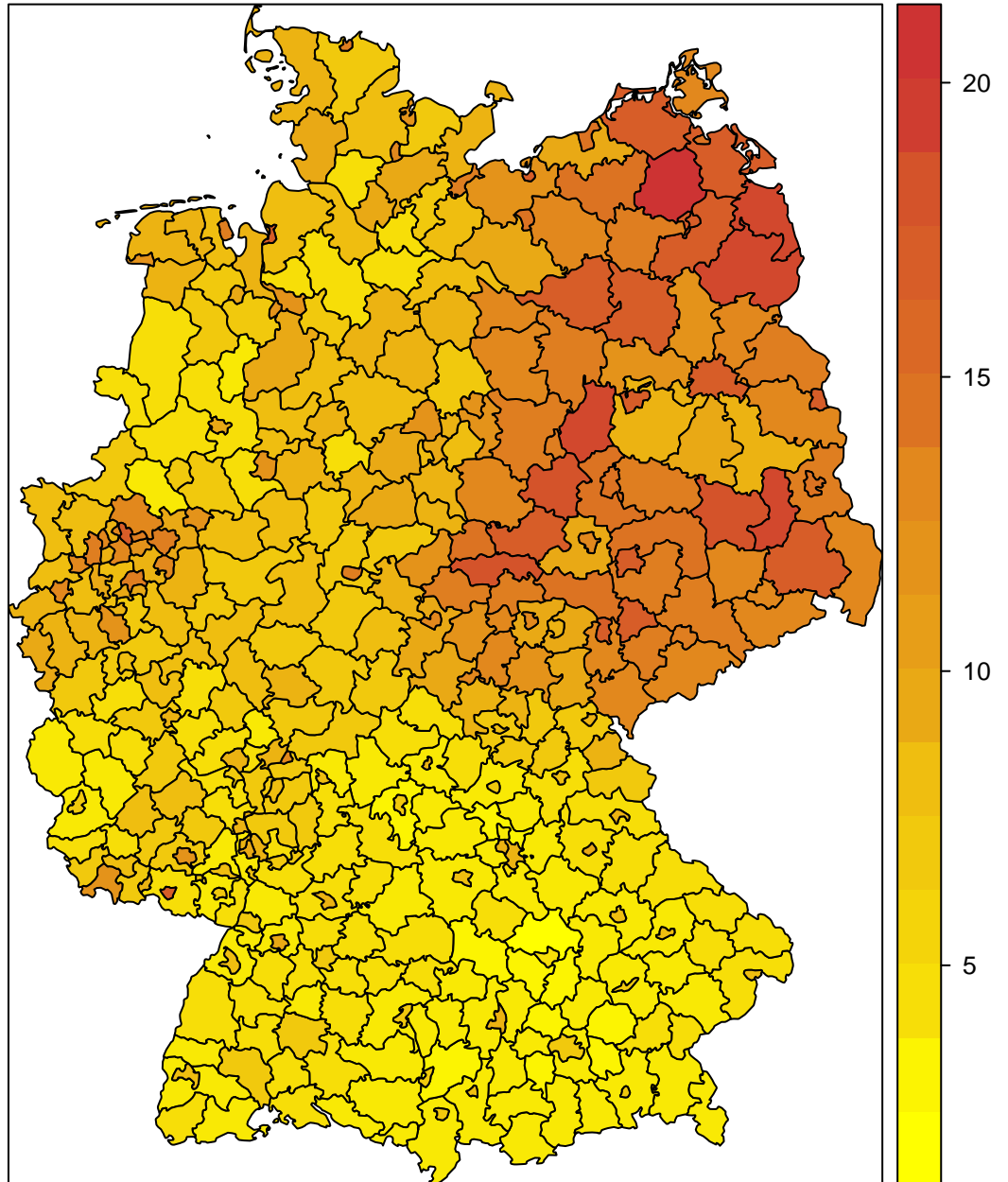


Figure 1: Regional unemployment in Germany in 2009

and Ertur (2010) to assess which spatial process captures the spatial dynamics in our data in the best way.

#### 4.1 Model selection

Our model selection procedure is based on the standard two-way fixed effects panel model (Baltagi (2008)), i.e.

$$u_{it} = \sum_{k=1}^K \beta_k x_{kit} + \mu_i + \alpha_t + \epsilon_{it}; \quad i = 1, \dots, N; \quad t = 1, \dots, T, \quad (4)$$

where  $u_{it}$  is the regional unemployment rate,  $\beta_k$  are unknown parameters and  $x_{kit}$  are the values of  $K$  explanatory variables.  $\mu_i$  denotes district-specific effects and  $\alpha_t$  represent time effects. We assume the district-specific effects to be fixed as our data set contains information on all German districts. The time effects capture national factors as, for example, business cycle effects that affect all regions in the same way.  $\epsilon_{it}$  are the disturbances for which it is assumed that  $\epsilon_{it} \sim (0, \sigma_\epsilon^2)$ . The indices of the variables denote district  $i$  and year  $t$ .

Model (4) controls neither for spatial autocorrelation nor for temporal dynamics in the data. Therefore, we refer to this model as basic model. If spatial dependence in the data is ignored, standard OLS regression will provide biased parameter estimates in case of spatial lag dependence and in case of spatially lagged exogenous variables. However, OLS estimation produces unbiased and inefficient estimates for the spatial error model. Neglecting a spatial lag term is similar to an omitted variable bias (Franzese and Hays (2007)). As the spatial lag term is correlated with the error term, OLS estimation of the associated coefficient will be inconsistent (Franzese and Hays (2007), Anselin and Bera (1998)).

In order to choose the relevant variables, we divide our set of explanatory variables into three groups according to theoretical importance. Then, we regress regional un-

employment rates on different combinations of variables where the variables with the strongest theoretical support are always contained. To keep computational effort manageable, we base these regressions on the basic model (equation (4)), although OLS estimation produces biased and/or inefficient results for spatially autocorrelated data. Finally, we compute Akaike's (AIC) and the Bayesian information criterion (BIC) to assess the goodness-of-fit of the regressions.

Table 4 provides an overview of the division of explanatory variables into these groups. The first group of variables contains variables which are essential for our model. We include in this group the employment share in manufacturing and in the construction industry (*%IND* and *%CON*), the age-related demographic variables (*YOUNG* and *OLD*) as well as one of the human capital variables (*H0*). Additionally, we include employment growth (*EG*) in this group to account for disequilibrium effects.<sup>8</sup> The second group contains variables that are expected to be important for the explanation of regional unemployment rates. We assign to this group our amenity variables (*DENS*, *DEBTR*, *STAY* and *REG*). Furthermore, we consider the employment shares of agriculture (*%AGR*), electricity, gas and water supply (*%ENERW*), financial business (*%FIN*), transport, storage and communication (*%TRANS*), real estate (*%REAL*) and public administration (*%PUB*) for this group. Moreover, female labor force participation (*FP*) as well as the remaining educational variables are part of this group (*H1* and *H2*). The last group consists of variables that are expected to have a weaker influence on regional unemployment. These variables are the share of foreign employed persons (*FOREIGN*) and the employment shares of mining and quarrying (*%MINE*), wholesale and retail trade (*%TRADE*), hotels and restaurants (*%HOT*) as well as education, health and social work (*%EDUHEALTH*).

Our model selection procedure selects a model containing thirteen variables. The

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<sup>8</sup>Note that we have not assigned female labor force participation to this group as its regional variation is small because of limited data availability.

summary statistics of these variables are in Table 10 in the appendix. To check for possible multicollinearity in our model, we analyze both the correlation matrix of the regressors and variance inflation factors where both give no indication for multicollinearity. Hence, our final best model is

$$\begin{aligned}
u_{it} = & \beta_1 EG_{it} + \beta_2 \%IND_{it} + \beta_3 \%ENERW_{it} + \beta_4 \%CON_{it} + \beta_5 \%HOT_{it} \\
& + \beta_6 \%FIN_{it} + \beta_7 \%PUB_{it} + \beta_8 YOUNG_{it} + \beta_9 OLD_{it} + \beta_{10} H0_{it} \\
& + \beta_{10} H1_{it} + \beta_{12} REG_{it} + \beta_{13} DEBTR_{it} + \mu_i + \alpha_t + \epsilon_{it}; \\
& i = 1, \dots, n; \quad t = 1, \dots, T, \quad (5)
\end{aligned}$$

where the variables are defined as before. The time effects ( $\alpha_t$ ) are strongly correlated with the national unemployment rate (correlation: 0.95).

Our final model contains all variables of group one. The model selection procedure selects the share of employed persons holding a vocational qualification as additional demographic variable. Hence, we account for two of three educational variables. Only the public debt ratio and the number of business registrations of our amenity variables are contained in our model. Hence, our model selection results reveal a first indication that regional unemployment is a disequilibrium phenomenon. Furthermore, the age-related demographic variables and the educational variables are contained in our final model. Regarding the market equilibrium effects, employment shares in electricity, gas and water supply, hotels and restaurants, financial business and public administration are selected into our model in addition to the sectoral variables of group one. The significance of the employment share in hotels and restaurants can be explained by the fact that a significant part of the work in this industry is done by persons holding no specific training qualification for this field. Hence, it might be easier for unemployed persons to get a job in this field.

Table 4: Division of explanatory variables for model selection

group 1	group 2	group 3
<ul style="list-style-type: none"> <li>- employment growth (<i>EG</i>)</li> <li>share of persons working</li> <li>- in manufacturing (<i>%IND</i>)</li> <li>- and in construction industry (<i>%CON</i>)</li> <li>share of</li> <li>- young (<i>YOUNG</i>)</li> <li>- and old persons (<i>OLD</i>)</li> <li>- employed persons without any vocational training (<i>H0</i>)</li> </ul>	<ul style="list-style-type: none"> <li>- female labor force participation (<i>FP</i>)</li> <li>share of employed persons</li> <li>- with vocational training (<i>H1</i>)</li> <li>- and with university degree (<i>H2</i>)</li> <li>- population density (<i>DENS</i>)</li> <li>- public debt ratio (<i>DEBTR</i>)</li> <li>- business registrations (<i>REG</i>)</li> <li>- number of overnight stays (<i>STAY</i>)</li> <li>share of persons working</li> <li>- in agriculture, hunting and forestry (<i>%AGR</i>),</li> <li>- in electricity, gas and water supply (<i>%ENERW</i>),</li> <li>- in transport, storage and communication (<i>%TRANS</i>),</li> <li>- in financial business (<i>%FIN</i>),</li> <li>- in real estate, renting and business activities (<i>%REAL</i>),</li> <li>- in public administration and defence; compulsory social security (<i>%PUB</i>)</li> </ul>	<ul style="list-style-type: none"> <li>- share of foreign employed persons (<i>FOREIGN</i>)</li> <li>share of persons working</li> <li>- in mining and quarrying (<i>%MINE</i>),</li> <li>- in hotels and restaurants (<i>%HOT</i>),</li> <li>- in wholesale and retail trade (<i>%TRADE</i>),</li> <li>- in education, health and social work (<i>%EDUHEALTH</i>)</li> </ul>

## 4.2 Spatial econometric modeling

To capture the spatial dependence in the data, we specify a spatial panel model. The spatial econometric literature provides different models for data with spatial autocorrelation: the model with spatially lagged exogenous variables (*SLX* model), the spatial error model, the spatial lag model and combinations of them. The *SLX* model is, from a methodological perspective, the simplest model because the additional regressors are exogenous and the error term remains spherical. We estimated this model for our data and found that the coefficients of all spatially lagged regressors are not significant. Furthermore, the results are, according to information criteria, slightly worse than those of the basic model.<sup>9</sup>

### 4.2.1 Testing for the spatial model specification

As the model with spatially lagged exogenous variables is not appropriate for our data, we need to specify one of the other spatial processes. Hence, we perform the specification test by Debarsy and Ertur (2010) to differentiate between the spatial models. To our best knowledge, the test by Debarsy and Ertur (2010) is the only specification test that allows to discriminate between the spatial lag model, the spatial error model and the model including both a spatial lag and spatially autocorrelated errors. Baltagi et al. (2003) extend the langrange multiplier (LM) test by Breusch and Pagan (1980) to the spatial error component model to test simultaneously for the existence of spatial error correlation as well as for random region effects. Additionally, they derive conditional tests for spatial error correlation and random region effects. Baltagi et al. (2007b) generalize the underlying model to a spatial panel model that controls for serial correlation over time for each spatial unit. We use this test to motivate our spatial dynamic model. Finally, Baltagi and Liu (2008) derive a test for autoregressive spatial lag dependence instead of spatial error terms.

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<sup>9</sup>The results can be obtained from the author upon request.

The starting point of the test by Debarsy and Ertur (2010) is the model with both a spatial lag term and spatially autocorrelated errors including fixed effects. It is called spatial autoregressive model with spatially autocorrelated disturbances of order (1,1) (SARAR (1,1) model) and can be described by

$$U_t = \lambda WU_t + X_t\beta + \mu + V_t; \quad V_t = \rho WV_t + \Xi_t; \quad t = 1, \dots, T, \quad (6)$$

where  $U_t = (u_{1,t}, u_{2,t}, \dots, u_{n,t})'$  is a  $(n \times 1)$  vector containing regional unemployment rates.  $X_t$  is the  $(n \times k)$  matrix containing all explanatory variables from our selected model (equation (5)),  $\beta$  is the  $(k \times 1)$  coefficient vector and  $\mu = (\mu_1, \dots, \mu_N)'$ .  $W$  is the  $(n \times n)$  spatial weights matrix.<sup>10</sup>  $\Xi_t = (\xi_{1,t}, \dots, \xi_{n,t})'$  is the  $(n \times 1)$  vector of innovations where  $\xi_{i,t}$  are i.i.d. across  $i$  and  $t$  and  $\xi_{i,t} \sim (0, \sigma_\xi^2)$ . Finally,  $\lambda$  is the spatial autoregressive coefficient and  $\rho$  is the spatial autocorrelation coefficient.

Debarsy and Ertur (2010) consider five different hypotheses in their paper:

- $H_0^a : \rho = \lambda = 0$ . This joint hypothesis tests whether there is spatial dependence in the data at all. If it cannot be rejected, there is no need for a spatial econometric model.
- $H_0^b : \lambda = 0$ . Under the alternative, the specification is the spatial lag model. However, spatial errors may exist.
- $H_0^c : \rho = 0$ . Under the alternative, the model contains spatially autocorrelated errors. However, a spatial lag term may exist.
- $H_0^d : \rho = 0$ , with  $\lambda$  possibly different from 0. Under the alternative, the general specification (equation 6) has to be estimated.

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<sup>10</sup>Debarsy and Ertur (2010) specify the model in their original contribution using different spatial weights matrices for the spatial lag and spatial error part. But they note that the test also works when these are equal.

Table 5: Test results of the specification test by Debarsy and Ertur (2010) using the binary contiguity matrix

	$H_0^a$	$H_0^b$	$H_0^c$	$H_0^d$	$H_0^e$
LM	1353.8	1285.7	967.19	7.86	3771.1
p-value	0	0	0	0.0051	0

- $H_0^e$  :  $\lambda = 0$ , with  $\rho$  possibly different from 0. Under the alternative, the general specification (equation 6) has to be estimated.

The test statistics for the hypotheses  $H_0^a$  until  $H_0^e$  are in the appendix. Table 5 shows the results of the Debarsy/Ertur (2010) test using the binary contiguity matrix.<sup>11</sup> According to the results, we can reject all five hypotheses even on the 1% significance level. Hence, the SARAR(1,1) model is the most appropriate model for our data.

#### 4.2.2 Static model specification

In accordance with the results of the test by Debarsy and Ertur (2010), we include a spatial lag term and spatially autocorrelated errors in our model. Additionally, we incorporate time effects in our static spatial panel model in order to have a two-way specification as in our basic model. The static model specification is

$$\begin{aligned}
 U_t = & \lambda WU_t + \beta_1 EG_t + \beta_2 \%IND_t + \beta_3 \%ENERW_t + \beta_4 \%CON_t + \beta_5 \%HOT_t \\
 & + \beta_6 \%FIN_t + \beta_7 \%PUB_t + \beta_8 YOUNG_t + \beta_9 OLD_t + \beta_{10} H0_t + \beta_{11} H1_t \\
 & + \beta_{12} REG_t + \beta_{13} DEBTR_t + \mu + \alpha_t \mathbb{1}_n + V_t; \quad V_t = \rho W V_t + \Xi_t; \quad t = 1, \dots, T, \quad (7)
 \end{aligned}$$

where the variables are defined as before. The elements of the  $(n \times 1)$  disturbance vector  $\Xi_t = (\xi_{1,t}, \dots, \xi_{n,t})'$  are assumed to be i.i.d. across  $i$  and  $t$  with zero mean and constant variance  $\sigma_\xi^2$ .  $\mathbb{1}_n$  denotes a  $(n \times 1)$  vector of ones.

<sup>11</sup>We also performed this test using the other spatial weights matrices and obtained qualitatively the same results.



Lee and Yu (2010b) show that for the (static) model with fixed individual and time effects the direct quasi-maximum likelihood estimation method yields inconsistent estimates for the common parameters unless  $n$  is large. In addition to that, they show that even in the case when both  $n$  and  $T$  are large, the distribution of the estimates of common parameters is not properly centered.

Moreover, Lee and Yu (2010b) show that the use of the typical within transformation to eliminate fixed effects causes the errors in the within-transformed model to be linearly dependent. Therefore, they apply an orthogonal transformation to eliminate the individual effects which produces independent error terms. The standard within transformation uses the deviation from time mean operator, i.e.  $J_T = I_T - \frac{1}{T}\mathbb{1}_T\mathbb{1}'_T$  where  $I_T$  is the identity matrix of dimension  $T$ . Lee and Yu (2010b) define the orthonormal eigenvector matrix of  $J_T$ , i.e.  $[F_{T,T-1}, \frac{1}{\sqrt{T}}\mathbb{1}_T]$ .  $F_{T,T-1}$  is the  $(T \times (T - 1))$  submatrix corresponding to the eigenvalues of one. They suggest to transform the original data by  $F_{T,T-1}$ , i.e.

$$[Y_{n1}^*, \dots, Y_{n,T-1}^*] = [Y_{n1}, \dots, Y_{nT}]F_{T,T-1}. \quad (8)$$

Note that the dimension of the transformed model is  $n(T - 1)$ . To remove the time effects from the model, they propose a similar transformation which is based on the orthogonal transformation using  $J_n = I_n - \frac{1}{n}\mathbb{1}_n\mathbb{1}'_n$ . Correspondingly, the model has dimension  $(n - 1)(T - 1)$  after both transformations. Lee and Yu apply this transformation approach in various contributions (Lee and Yu (2010a), Lee and Yu (2010b), Lee and Yu (2010c)). We apply it to both our static and our dynamic model. Finally, the transformed model can be estimated by quasi-maximum likelihood.<sup>12</sup>

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<sup>12</sup>For more details on the estimation methodology, see Lee and Yu (2010b).

### 4.2.3 Dynamic model specification

Labor market data is not only correlated over space but also over time. To motivate the dynamic approach, we use the test by Baltagi et al. (2007b) because it allows for serial correlation in the error terms (in addition to spatial autocorrelation). Details on hypotheses and test statistics are in the appendix. The test results clearly show the following three aspects of our data. Firstly, there is serial dependence in our data. Hence, a dynamic model specification is reasonable in our context. Secondly, the test results give an indication for the presence of spatially autocorrelated errors. This is in line with the results of the Moran  $I$  test that also show significant spatial autocorrelation in regional unemployment rates. Thirdly, the test results support our assumption of a fixed effects model because we cannot reject the hypothesis that the standard deviation of the fixed effects is equal to zero.

The literature on spatial dynamic panel models provides various model specifications. Elhorst (2012) provides a survey of the literature on specification and estimation of spatial dynamic panel data models. For our analysis of regional unemployment, we include a spatial lag term, a temporally lagged term as well as a combined spatially and temporally lagged term in our dynamic model. The resulting model can be described by

$$\begin{aligned} U_t = & \lambda WU_t + \gamma U_{t-1} + \delta WU_{t-1} + \beta_1 EG_t + \beta_2 \%IND_t + \beta_3 \%ENERW_t + \beta_4 \%CON_t \\ & + \beta_5 \%HOT_t + \beta_6 \%FIN_t + \beta_7 \%PUB_t + \beta_8 YOUNG_t + \beta_9 OLD_t \\ & + \beta_{10} H0_t + \beta_{11} H1_t + \beta_{12} REG_t + \beta_{13} DEBTR_t + \mu + \alpha_t \mathbb{1}_n + \Xi_t; \quad t = 1, \dots, T, \quad (9) \end{aligned}$$

where  $\gamma$  captures the pure time-dynamic effects and  $\delta$  captures the combined spatial-temporal effect. The assumptions about the error term  $\Xi_t$  are as before.

Yu et al. (2008) propose a bias corrected quasi-maximum likelihood estimator for the

spatial dynamic panel data model including a spatial lag, a temporal lag and a combined spatial-temporal term. However, they only allow for individual-specific fixed effects but not for fixed time effects. Lee and Yu (2010a) provide an estimator for the same model but extended to include time period fixed effects. Lee and Yu (2010a) show that direct quasi-maximum likelihood estimation of all parameters in the model with time effects yields an additional bias of order  $O(n^{-1})$ . They apply their transformation approach and show that it can avoid the additional bias with the same asymptotic efficiency as the direct quasi-maximum likelihood estimates when  $n$  is not relatively smaller than  $T$ . Furthermore, Lee and Yu (2010a) show that the direct estimates have a degenerate limit distribution while the transformed estimates are properly centered and asymptotically normal. Therefore, we apply the estimation methodology of Lee and Yu (2010a) to our dynamic model.

## 5 Estimation results

Firstly, we estimate the basic model, i.e. the model without any terms controlling for spatial or temporal dependence. The basic model is specified according to a two-way fixed effects panel data model and it is estimated using the standard within-estimator (see Baltagi (2008)). Secondly, we estimate the static spatial panel specification and, thirdly, the spatial dynamic model, both using the binary contiguity matrix, the distance decay matrix as well as the Molho (1995) weights matrix. Hence, we perform seven regressions for the whole of Germany. The regression results for the basic and the static model are in Table 6 and the results for the dynamic model are in Table 7. In addition to that, we perform the same regressions for the Eastern and Western part of Germany individually. Elhorst (2012) discusses stationarity issues and proposes stationarity conditions for spatial dynamic panel data models. These conditions as well as the conditions stated in Lee and Yu (2010c) are satisfied in the regression results for the

whole of Germany. However, the regression results for East and West Germany using the distance decay matrix do not meet the stationarity conditions. Therefore, we only present the results using the other spatial weights matrices for the separate analyses.

## **5.1 Results for the whole of Germany**

### **Economic interpretation**

As expected, regional unemployment rates are influenced negatively by employment growth. Furthermore, the shares of employed persons working in manufacturing and in the construction industry also have a negative impact on regional unemployment. Hence, districts that are specialized in these industries exhibit lower unemployment than districts with a different sectoral structure. Our estimation results reveal no indication for a discrimination of older workers as the associated coefficient is also negative. Though, this coefficient should not be overinterpreted because it can simply be related to effects of demographic change, i.e. an aging labor force. By contrast, the impact of younger employees on regional unemployment is positive. But this does not imply necessarily youth unemployment because the majority of persons aged 15 until 25 is still in the educational system. The share of employed persons without any professional qualification influences regional unemployment positively which is in line with expectation from theory. Interestingly, this also holds for the share of employed persons with vocational training.

Our model contains only a few of the amenity variables. Additionally, the signs of the amenity variables are against expectation from theory. According to the equilibrium view, consumers are expected to stay in regions with high unemployment when this region offers a great extent of amenities. Hence, high unemployment should be related negatively to public debt because heavily indebted districts are not able to finance public goods to improve life quality. If high public debts result from high investments in the past, consumers expect less expenditures in the future. However, our results show

a significant positive coefficient for the public debt ratio. A similar reasoning holds for producer amenities. Firms are expected to move to districts with high unemployment, i.e. the level of producer amenities should be higher when regional unemployment is lower. But the coefficient of business registrations is positive in our empirical results. Even if the public debt ratio is interpreted as a proxy for producer amenities, its coefficient has not the desired sign. Thus, our results reveal no indication for regional unemployment to be of equilibrium nature in Germany. Nonetheless, some of the market equilibrium variables, i.e. employment shares, are significant in our model.

### **Spatial econometric interpretation**

Ignoring spatial dependence in the data, results in biased and inefficient estimates. The estimated coefficients of the basic model are mostly upward-biased in absolute value in comparison with the results of the static model. In an earlier contribution (Lottmann (2012)) we get a similar result for the estimation of matching functions. The existence of this bias is theoretically shown in Franzese and Hays (2007). In addition to that, the information criteria show that the spatial models are more appropriate for our data than the basic one. Hence, a spatial model is needed for the analysis of regional unemployment.

The dynamic model fits our data better than the static model according to information criteria. Thus, in order to model regional unemployment, a dynamic modeling approach needs to be applied. To our best knowledge, most of the contributions to the regional unemployment literature apply only a static model. However, most of the explanatory variables are not significant in the dynamic model. Hence, the temporal lag is able to explain a lot of the variability in regional unemployment rates. Only employment growth, the employment shares of manufacturing, construction industry and electricity, gas and water supply as well as the age-related demographic variables have a significant impact on regional unemployment. Interestingly, the sign of the coefficient

for the share of people working in construction industry differs between the static and the dynamic model.

The spatial autoregressive ( $\lambda$ ) and the spatial autocorrelation coefficient ( $\rho$ ) measuring the spatial influence in our static spatial panel model are both significant while the influence of both coefficients is positive in most cases. Hence, district-level unemployment is influenced positively by unemployment in neighboring districts. The spatial autocorrelation coefficient indicates the impact of regional effects that affect a region consisting of more than one district. Examples in the context of regional unemployment are exogenous shocks as the closure of a production site. The spatial autoregressive coefficient of the dynamic model is also significant and positive. The same holds for the pure time-dynamic effect. This result underlines the fact that our data exhibit not only spatial but also temporal autocorrelation. Contrary to this, the combined spatial-time effect is negative and significant.

Furthermore, the results are fairly sensitive to the choice of the spatial weights matrix. In the spatial econometric literature, Bell and Bockstael (2000) (among others) find that estimation results are more sensitive to the specification of the spatial weights matrix than to the estimation technique. According to information criteria, the binary spatial weights matrix captures the spatial structure of the data in the best way for the static model while the distance decay function is most appropriate in case of the dynamic model.

## **5.2 Differences between East and West Germany**

Due to German history, it is worthwhile to analyze the differences between the Western and Eastern part of the country. We use a two-regime regression, i.e. we estimate the model for both parts separately. This procedure rests on the assumption that coefficients of the explanatory variables differ between East and West Germany. From an economic perspective, we find no reason why a particular coefficient, for example the

Table 6: Regression results of regional unemployment model - basic and static model specification for the period from 1999 until 2007

	dependent variable: $u_{it}$			
	basic	binary	static distance ( $\tau = 0.02$ )	static Molho (1995) ( $\eta = 0.01$ )
$EG_{it}$	-0.066*** (-7.12)	-0.033*** (-6.2)	-0.04*** (-5.41)	-0.05*** (-6.15)
%IND <sub>it</sub>	-0.11*** (-7.95)	-0.071*** (-7.35)	-0.08*** (-7.11)	-0.09*** (-7.05)
%ENERW <sub>it</sub>	0.17*** (2.6)	0.098** (1.98)	0.08 (1.47)	0.12* (1.93)
%CON <sub>it</sub>	-0.29*** (-11.85)	-0.133*** (-10.73)	-0.12*** (-5.58)	-0.17*** (-7.46)
%HOT <sub>it</sub>	0.16*** (2.96)	0.072* (1.95)	-0.01 (-0.17)	0.09* (1.96)
%FIN <sub>it</sub>	0.17*** (3.06)	0.046 (1.13)	0.102** (2.21)	0.14*** (2.75)
%PUB <sub>it</sub>	0.12*** (4.36)	0.053*** (2.74)	0.056** (2.49)	0.073*** (3.05)
YOUNG <sub>it</sub>	0.35*** (9.75)	0.021 (0.96)	-0.008 (-0.24)	0.057 (1.64)
OLD <sub>it</sub>	-0.16*** (-5.86)	-0.13*** (-7.28)	-0.2*** (-8.03)	-0.22*** (-8.73)
H0 <sub>it</sub>	0.103*** (3.8)	0.098*** (7.78)	0.088*** (4.52)	0.089*** (4.15)
H1 <sub>it</sub>	0.081*** (4.14)	0.081*** (7.56)	0.079*** (4.72)	0.084*** (4.74)
REG <sub>it</sub>	0.17*** (4.44)	0.08*** (3.35)	0.14*** (4.44)	0.11*** (3.96)
DEBTR <sub>it</sub>	0.054** (2.2)	0.015 (0.87)	0.02 (0.97)	0.026 (1.16)
$\lambda$	—	0.83*** (71.59)	0.79*** (16.41)	0.78*** (14.56)
$\rho$	—	-0.46*** (-13.68)	0.67*** (8.77)	0.71*** (9.06)
$\sigma^2$	0.61	0.34	0.44	0.5
log-likelihood	-4123.08	-3274.95	-3361.05	-3525.43
AIC	2.23	1.78	1.82	1.82
BIC	2.25	1.80	1.85	1.85
obs.	3708	3708	3708	3708

Notes:  $t$ -statistics are in parentheses.  $t$ -statistics for the static model are computed according to Anselin (1988).  $\lambda$  is the spatial autoregressive coefficient and  $\rho$  is the spatial autocorrelation coefficient. \*\*\*, \*\* and \* indicate coefficients that are significant at 1%, 5% and 10%, respectively.

Table 7: Regression results of regional unemployment model - dynamic model specification for the period from 1999 until 2007

	dependent variable: $u_{it}$		
	binary	distance ( $\tau = 0.02$ )	Molho (1995) ( $\eta = 0.01$ )
$EG_{it}$	-0.055*** (-7.93)	-0.063*** (-8.98)	-0.069*** (-9.23)
$\%IND_{it}$	-0.021** (-1.99)	-0.011 (-1.05)	-0.015 (-1.31)
$\%ENERW_{it}$	0.209*** (4.25)	0.23*** (4.63)	0.24*** (4.56)
$\%CON_{it}$	0.058*** (2.7)	0.019 (0.87)	0.047** (2.03)
$\%HOT_{it}$	-0.08* (-1.85)	-0.02 (-0.36)	-0.056 (-1.22)
$\%FIN_{it}$	0.055 (1.16)	0.07 (1.39)	0.065 (1.29)
$\%PUB_{it}$	0.0107 (0.53)	0.0095 (0.47)	0.0078 (0.36)
$YOUNG_{it}$	0.046* (1.74)	-0.0001 (-0.0039)	0.078*** (2.7)
$OLD_{it}$	-0.08*** (-3.8)	-0.104*** (-4.9)	-0.104*** (-4.61)
$H0_{it}$	0.006 (0.28)	0.0091 (0.43)	-0.016 (-0.71)
$H1_{it}$	-0.0149 (-0.97)	-0.014 (-0.91)	-0.029* (-1.73)
$REG_{it}$	0.0073 (0.28)	0.013 (0.51)	0.013 (0.48)
$DEBTR_{it}$	0.0088 (0.48)	0.0043 (0.23)	0.0081 (0.41)
$\lambda$	0.5*** (26.55)	0.88*** (42.41)	0.79*** (32.87)
$\gamma$	0.78*** (49.04)	0.78*** (52.11)	0.8*** (55.29)
$\delta$	-0.42*** (-15.98)	-0.68*** (-17.55)	-0.71*** (-14.31)
$\sigma^2$	0.27	0.27	0.31
log-likelihood	-2270.7	-1251.6	-1444.4
AIC	1.39	0.77	0.89
BIC	1.42	0.80	0.92
obs.	3296	3296	3296

Notes:  $t$ -statistics are in parentheses.  $t$ -statistics of the dynamic spatial panel model are computed using the asymptotic distribution derived in Lee and Yu (2010c).  $\lambda$  is the spatial autoregressive coefficient,  $\gamma$  captures the pure time effect and  $\delta$  captures the combined spatial-time effect. \*\*\*, \*\* and \* indicate coefficients that are significant at 1%, 5% and 10%, respectively. The reduced number of observations results from Lee and Yu's transformation approach.



coefficient of the employment share in manufacturing, should be similar in East and West Germany. We also tested for the coefficients to be different between East and West Germany. The test results show that most of the coefficients differ significantly between East and West Germany.

The Eastern part of Germany consists of 87 districts and the Western part consists of 325 districts. Note that the spatial model specifications of the separate regressions take only the spatial relations within the areas into account, but not the spatial interactions between them. The results for East Germany are in Table 8 while the results for Western Germany can be found in Table 9.

Employment growth and the employment share in manufacturing are negatively related to regional unemployment in both parts of Germany. Beyond that, the estimation results differ between East and West Germany. Firstly, the employment share of the construction industry has only a significant (negative) impact on regional unemployment rates in Eastern Germany. During the 1990s, economic growth in Eastern Germany was strongly driven by an expansion of the construction industry. Though, it contracted towards the end of the decade (Davies and Hallet (2001)). In 2000, the share of the construction industry in gross value added (using current prices) amounted to 8.1 per cent in Eastern Germany (including Berlin) whereas it amounted to only 4.7 per cent in Western Germany.<sup>13</sup> Secondly, regional unemployment in Eastern Germany is only influenced by some of the factors which we account for in our model. Only the educational variables, the number of business registrations and the employment share in hotels and restaurants have a significant (positive) impact on Eastern German regional unemployment rates. Contrary to this, the age variables as well as the employment shares in financial business and in public administration are significant in our model for Western Germany. Thirdly, the influence of the employment share in hotels and

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<sup>13</sup>The values are taken from *Volkswirtschaftliche Gesamtrechnungen der Länder*, [http://www.vgrdl.de/Arbeitskreis\\_VGR/](http://www.vgrdl.de/Arbeitskreis_VGR/).

restaurants is positive in East Germany while being negative in West Germany.

In line with our results for the whole country, we find that both spatial and temporal dynamics have to be accounted for when modeling regional unemployment. According to information criteria, the binary contiguity matrix captures the spatial relations in the best way for East Germany. Contrary to this, the binary contiguity matrix captures the spatial structure best for the static model while the Molho (1995) matrix is the best weights matrix in case of the dynamic model for Western Germany. The spatial coefficients are mostly significant for both parts of Germany. The signs of the coefficients are in line with the results for the whole country. Both the spatial autoregressive and the spatial autocorrelation coefficient are positive. Likewise, the pure time-dynamic is significant and positive while the combined space-time effect is negative and mostly significant.

## **6 Conclusion**

In this paper, we analyze the determinants for regional unemployment in Germany. Regional unemployment rates in Germany are characterized by substantial regional differences. We show that there are significant spatial spillovers in regional unemployment data. To avoid biased and inefficient estimates, we apply a spatial panel model to our data. In addition to spatial dependence, we also control for temporal dynamics in the data by specifying a dynamic model. Our analysis covers both the whole of Germany and East and West Germany separately.

Our results clearly show that the spatial panel model fits our data better than the basic model. Moreover, the dynamic modeling is more appropriate for our analysis of regional unemployment than the static one. Hence, the spatial dynamic panel model is the best model for the analysis of regional unemployment.

Our study leads to several conclusions for policy. Firstly, policy measures to reduce

Table 8: Regression results of East German regional unemployment model for period from 1999 until 2007

	dependent variable: $u_{it}$				
	basic	static		dynamic	
		binary	Molho (1995) ( $\eta = 0.01$ )	binary	Molho (1995) ( $\eta = 0.01$ )
$EG_{it}$	-0.084*** (-4.25)	-0.057*** (-3.6)	-0.078*** (-4.3)	-0.089*** (-5.71)	-0.1*** (-6.08)
% $IND_{it}$	-0.075** (-2.09)	-0.061** (-1.96)	-0.048 (-1.35)	0.0074 (0.25)	0.035 (1.11)
% $ENERW_{it}$	0.14 (0.7)	-0.12 (-0.68)	0.0059 (0.03)	0.21 (1.23)	0.23 (1.3)
% $CON_{it}$	-0.24*** (-4.11)	-0.23*** (-6.39)	-0.21*** (-4.63)	-0.0094 (-0.19)	-0.0061 (-0.12)
% $HOT_{it}$	0.27*** (3.64)	0.13** (1.97)	0.15** (2.01)	-0.021 (-0.32)	0.0035 (0.05)
% $FIN_{it}$	-0.098 (-0.45)	-0.35* (-1.88)	-0.23 (-1.09)	-0.26 (-1.59)	-0.27 (-1.55)
% $PUB_{it}$	0.066 (1.58)	0.0016 (-0.04)	0.029 (0.71)	-0.0024 (-0.08)	-0.0059 (-0.18)
$YOUNG_{it}$	0.036 (0.4)	0.12* (1.72)	0.045 (0.53)	-0.018 (-0.25)	-0.015 (-0.2)
$OLD_{it}$	-0.046 (-0.83)	-0.08* (-1.72)	-0.069 (-1.31)	-0.15*** (-3.42)	-0.16*** (-3.54)
$H0_{it}$	0.19** (2.35)	0.14** (2.22)	0.18** (2.36)	0.056 (0.89)	0.048 (0.73)
$H1_{it}$	0.092* (1.86)	0.069* (1.78)	0.12*** (2.64)	-0.014 (-0.37)	-0.015 (-0.38)
$REG_{it}$	0.086 (1.56)	0.083* (1.82)	0.13*** (2.89)	-0.029 (-0.74)	-0.026 (-0.62)
$DEBTR_{it}$	0.11** (2.01)	0.072 (1.49)	0.06 (1.09)	0.039 (0.89)	0.045 (0.96)
$\lambda$	—	0.67*** (13.84)	0.76*** (12.44)	0.38*** (8.83)	0.33*** (3.74)
$\rho$	—	-0.03 (-0.31)	0.42*** (2.73)	—	—
$\gamma$	—	—	—	0.74*** (21.24)	0.72*** (23.44)
$\delta$	—	—	—	-0.31*** (-5.29)	-0.15 (-1)
$\sigma^2$	0.79	0.59	0.75	0.37	0.41
log-like	-965.54	-824.36	-868.21	-594.99	-766.51
AIC	2.5	2.15	2.26	1.76	2.25
BIC	2.59	2.24	2.35	1.87	2.36
obs.	783	783	783	696	696

Notes:  $t$ -statistics are in parentheses.  $t$ -statistics for the static model are computed according to Anselin (1988).  $\lambda$  is the spatial autoregressive coefficient and  $\rho$  is the spatial autocorrelation coefficient. \*\*\*, \*\* and \* indicate coefficients that are significant at 1%, 5% and 10%, respectively.

Table 9: Regression results of West German regional unemployment model for period from 1999 until 2007

	dependent variable: $u_{it}$				
	basic	static		dynamic	
		binary	Molho (1995) ( $\eta = 0.01$ )	binary	Molho (1995) ( $\eta = 0.01$ )
$EG_{it}$	-0.043*** (-4.28)	-0.016** (-2.26)	-0.036*** (-4.05)	-0.06*** (-7.55)	-0.077*** (-9.34)
$\%IND_{it}$	-0.12*** (-8.9)	-0.051*** (-5.37)	-0.1*** (-8.26)	-0.012 (-1.12)	-0.0082 (-0.73)
$\%ENERW_{it}$	0.12* (1.91)	0.047 (1.11)	0.12** (2.11)	0.22*** (4.51)	0.25*** (4.9)
$\%CON_{it}$	-0.061* (-1.89)	0.0066 (0.29)	-0.052* (-1.82)	0.07** (2.5)	0.062** (2.11)
$\%HOT_{it}$	-0.28*** (-3.22)	-0.14** (-2.28)	-0.27*** (-3.42)	-0.064 (-0.92)	-0.063 (-0.87)
$\%FIN_{it}$	0.16*** (3.29)	0.07** (2.14)	0.13*** (2.86)	0.09* (1.92)	0.1** (2.06)
$\%PUB_{it}$	0.14*** (4.22)	0.08*** (3.46)	0.12*** (3.83)	0.021 (0.69)	0.0062 (0.2)
$YOUNG_{it}$	-0.04 (-0.73)	-0.12*** (-2.72)	-0.11** (-2.38)	0.072 (1.62)	0.07 (1.51)
$OLD_{it}$	-0.31*** (-10.12)	-0.25*** (-8.66)	-0.36*** (-11.79)	-0.01 (-0.4)	-0.03 (-1.12)
$H0_{it}$	0.034 (1.19)	0.065*** (3.31)	0.037* (1.72)	0.014 (0.6)	-0.0002 (-0.01)
$H1_{it}$	0.038* (1.88)	0.078*** (4.51)	0.081*** (4.54)	-0.034** (-2)	-0.054*** (-3.05)
$REG_{it}$	0.25*** (4.65)	0.08** (1.98)	0.2*** (4.37)	0.05 (1.25)	0.056 (1.35)
$DEBTR_{it}$	0.01 (0.41)	-0.0019 (-0.1)	0.0084 (0.36)	-0.0043 (-0.21)	-0.012 (-0.58)
$\lambda$	—	-0.62*** (-20.09)	0.76*** (16.52)	0.47*** (21.1)	0.83*** (33.95)
$\rho$	—	0.96*** (189.74)	0.6*** (6.72)	—	—
$\gamma$	—	—	—	0.805*** (44.66)	0.84*** (50.95)
$\delta$	—	—	—	-0.37*** (-11.5)	-0.84*** (-16.2)
$\sigma^2$	0.45	0.26	0.39	0.23	0.25
log-likelihood	-2820.29	-2404.88	-2457.77	-2028.3	-841.5
AIC	1.94	1.66	1.69	1.57	0.66
BIC	1.97	1.69	1.72	1.61	0.7
obs.	2925	2925	2925	2600	2600

Notes:  $t$ -statistics are in parentheses.  $t$ -statistics for the static model are computed according to Anselin (1988).  $\lambda$  is the spatial autoregressive coefficient and  $\rho$  is the spatial autocorrelation coefficient. \*\*\*, \*\* and \* indicate coefficients that are significant at 1%, 5% and 10%, respectively.

unemployment should account for regional differences in unemployment in Germany. In addition to framework conditions that are set on the national level, policy makers have to take regional differences in the economic structure into account. Secondly, according to our results, regional unemployment in Germany is of disequilibrium nature. Hence, our results provide a justification for policy makers to intervene on regional labor markets. However, thirdly, we find significant spatial spillovers, i.e. political decisions do not only affect the district on which they are targeted but also the neighboring districts. This aspect motivates political cooperations between different districts. The definition of labor market regions as, for example, proposed by Eckey et al. (2007a) can offer guidance for this process.

## Appendix

### District reforms

There are two district reforms during the period from 1999 until 2009. In the federal state of Saxony-Anhalt, the reform became effective as from July 1st, 2007. The reform reduced the number of districts from 21 to 11. The other reform affects the federal state of Saxony where it became effective as from August 1st, 2008. The reform resulted in a reduced number of districts from 29 to 13. As we want to use current map data of Germany, we aggregate the data according to the reforms. Hence, we use the regional structure after the reforms for the entire period. Regional unemployment rates of the 'new' district are weighted averages of the corresponding regional unemployment rates using the associated labor force as weights.

### Summary statistics of explanatory variables

	Min	1st Qu.	Median	Mean	3rd Qu.	Max	Std. dev.	unit
<i>EG</i>	-4.084	-0.859	-0.002	-0.234	0.537	2.724	1.178	%
<i>%IND</i>	3.455	19.580	26.350	27.650	35.990	67.240	11.254	%
<i>%ENERW</i>	0	0.478	0.739	0.904	1.074	7.974	0.732	%
<i>%CON</i>	2.130	5.681	7.559	7.938	10.1	17.4	3.035	%
<i>%HOT</i>	0.849	2.002	2.407	2.97	3.148	22.08	1.989	%
<i>%FIN</i>	0.445	2.096	2.612	2.941	3.232	16.95	1.73	%
<i>%PUB</i>	2.334	4.882	6.012	6.742	8.136	19.32	2.679	%
<i>YOUNG</i>	13.71	16.53	17.5	17.54	18.43	23.36	1.45	%
<i>OLD</i>	21.46	26.73	27.93	27.91	29.17	33.71	1.88	%
<i>H0</i>	7.351	14.44	17.91	17.1	20.32	30.57	4.63	%
<i>H1</i>	50.1	61.3	64.38	64.35	67.25	77.93	4.983	%
<i>REG</i>	0.335	0.923	1.404	1.992	2.258	39.27	2622	thousand
<i>DEBTR</i>	0.025	3.002	4.363	4.71	6.127	13.49	2.24	ratio

Table 10: Summary statistics of the explanatory variables of our model using averages over the period from 1999 until 2007

### Specification test by Debarsy and Ertur (2010)

Consider the SARAR(1,1) model<sup>14</sup>

$$Y_t = \lambda WY_t + X_t\beta + \mu + U_t; \quad U_t = \rho MU_t + V_t; \quad t = 1, \dots, T, \quad (10)$$

where  $Y_t = (y_{1,t}, y_{2,t}, \dots, y_{n,t})'$  is the  $(n \times 1)$  vector of the dependent variable for all individuals in period  $t$ ,  $X_t$  is the  $(n \times k)$  matrix of exogenous regressors and  $\beta$  is the associated vector of unknown regression coefficients.  $V_t = (v_{1,t}, \dots, v_{n,t})'$  is the innovation term where  $v_{i,t}$  is i.i.d. across  $i$  and  $t$  with zero mean and constant variance  $\sigma^2$ .  $\mu$  is the  $(n \times 1)$  vector of individual effects.  $W$  and  $M$  are  $(n \times n)$  spatial weights matrices,  $\lambda$  and  $\rho$  are the unknown spatial parameters. Applying the transformation approach by Lee and Yu yields the transformed model

$$Y_t^* = \lambda WY_t^* + X_t^*\beta + U_t^*; \quad U_t^* = \rho MU_t^* + V_t^*; \quad t = 1, \dots, T-1. \quad (11)$$

Denoting  $\theta' = [\beta', \rho, \lambda, \sigma^2]$  and  $\eta' = [\beta', \rho, \lambda]$ , the log-likelihood function is given by

$$l(\theta) = -\frac{n(T-1)}{2} \ln(2\pi) - \frac{n(T-1)}{2} \ln(\sigma^2) + (T-1) \ln|S(\lambda)| + (T-1) \ln|R(\rho)| - \frac{1}{2\sigma^2} \sum_{t=1}^{T-1} V_t^{*'}(\eta) V_t^*(\eta), \quad (12)$$

where  $S(\lambda) = I_n - \lambda W$ ,  $R(\rho) = I_n - \rho M$  and  $V_t^* = R(\rho)[S(\lambda)Y_t^* - X_t^*\beta]$ . Debarsy and Ertur (2010) consider five different hypotheses ( $H_0^a$  until  $H_0^e$ ) for their specification test.

#### Joint test statistic for $H_0^a : \rho = \lambda = 0$

Under the null hypothesis, the specification to be estimated is the standard fixed effects panel model. Debarsy and Ertur (2010) show that the transformed model can also be estimated by OLS. The joint LM statistic is then given by

$$LM_a = \tilde{Q}^{-1} [T_{22} \tilde{R}_y^2 - 2T_{12} \tilde{R}_v \tilde{R}_y + (\tilde{D} + T_{11}) \tilde{R}_v^2]; \quad (13)$$

where

$$\tilde{R}_v = \frac{\sum_{t=1}^{T-1} \tilde{V}_t^{*'} M \tilde{V}_t^*}{\tilde{\sigma}^2};$$

<sup>14</sup>All explanations are taken from the original paper by Debarsy and Ertur (2010).

$$\begin{aligned}\tilde{R}_y &= \frac{\sum_{t=1}^{T-1} \tilde{V}_t^{*'} W Y_t^*}{\tilde{\sigma}^2}; \\ \tilde{D} &= \tilde{\sigma}^{-2} \sum_{t=1}^{T-1} (W X_t^* \tilde{\beta})' M_{X^*} (W X_t^* \tilde{\beta}); \\ \tilde{Q} &= (\tilde{D} + T_{11}) T_{22} - T_{12}^2.\end{aligned}$$

Also,  $T_{11} = (T-1)tr[(W+W')W]$ ,  $T_{22} = (T-1)tr[(M+M')M]$ ,  $T_{12} = (T-1)tr((M'+M)W)$  and  $M_{X^*} = I_n - X_t^*(X_t^{*'}X_t^*)^{-1}X_t^{*'}$ . Finally,  $\tilde{V}_t^* = Y_t^* - X_t^*\tilde{\beta}$  is the residual of the constrained model and  $\tilde{\sigma}^2$  is the associated OLS residual variance.  $LM_a$  is expected to be asymptotically distributed as  $\chi_2^2$  under the joint null hypothesis  $H_0^a$ .

**Marginal test statistic for  $H_0^b : \lambda = 0$  (assuming  $\rho = 0$ )**

Under this hypothesis, the constrained model is

$$Y_t^* = X_t^*\beta + V_t^*; \quad t = 1, \dots, T-1, \quad (14)$$

where  $V_t^*$  is distributed according to a multivariate normal distribution with zero mean and the variance-covariance matrix  $\sigma^2 I_{n(T-1)}$ . The unconstrained model is

$$Y_t^* = \lambda W Y_t^* + X_t^*\beta + V_t^*; \quad t = 1, \dots, T-1, \quad (15)$$

and should be estimated using maximum likelihood. The  $LM$  statistic for this hypothesis is

$$LM_b = \frac{\sum_{t=1}^{T-1} (\tilde{V}_t^{*'} W Y_t^* / \tilde{\sigma}^2)^2}{\tilde{D} + T_{11}}, \quad (16)$$

where the variables are defined as before.  $\tilde{V}_t^*$  are the OLS residuals of equation (14). This  $LM$  statistic is asymptotically distributed as  $\chi_1^2$  under the null hypothesis.

**Marginal test statistic for  $H_0^c : \rho = 0$  (assuming  $\lambda = 0$ )**

For this test, the restricted model is again equation (14). The specification under the alternative is

$$Y_t^* = X_t^*\beta + U_t^*; \quad U_t^* = \rho M U_t^* + V_t^*; \quad t = 1, \dots, T-1. \quad (17)$$

The  $LM$  statistic for this hypothesis is



$$LM_c = \frac{\sum_{t=1}^{T-1} (\tilde{V}_t^{*'} M \tilde{V}_t^* / \tilde{\sigma}^2)^2}{T_{22}}. \quad (18)$$

Again,  $\tilde{V}_t^*$  are the residuals of equation (14) and  $\tilde{\sigma}^2$  is the estimate of the corresponding residual variance. Under the null hypothesis,  $LM_c$  is asymptotically distributed as  $\chi_1^2$ .

**Conditional test statistic for  $H_0^d : \rho = 0$  given  $\lambda \neq 0$**

The appropriate specification under the null is model (15). When the null is rejected, the correct specification is the general model (11). The disturbances of the restricted model are given by

$$V_t^* = S(\lambda)Y_t^* - X_t^*\beta; \quad t = 1, \dots, T-1. \quad (19)$$

These disturbances can be estimated by ML in model (15). The  $LM$  statistic for the conditional test for spatially autocorrelated errors in the presence of an endogenous spatial lag is given by

$$LM_d = \frac{(\sum_{t=1}^{T-1} \tilde{V}_t^{*'} M \tilde{V}_t^* / \tilde{\sigma}^2)^2}{T_{22} - (\tilde{T}_{\lambda\rho})^2 * var(\tilde{\rho})}, \quad (20)$$

where  $var(\tilde{\rho})$  is the variance of the autoregressive coefficient estimated under the constrained model and  $\tilde{T}_{\lambda\rho} = (T-1)tr[M'WS(\tilde{\rho})^{-1} + MWS(\tilde{\rho})^{-1}]$ .  $LM_d$  is asymptotically distributed as  $\chi_1^2$  under the null hypothesis.

**Conditional test statistic for  $H_0^e : \lambda = 0$  given  $\rho \neq 0$**

For this test, the unconstrained model is the general specification (equation 11) whereas the constrained model is equation (17). Its error term is given by

$$V_t^* = R(\rho)[Y_t^* - X_t^*\beta]; \quad t = 1, \dots, T-1. \quad (21)$$

The conditional  $LM$  statistic for the conditional test for an endogenous spatial lag in the presence of spatially autocorrelated errors is

$$LM_e = \frac{\sum_{t=1}^{T-1} (\tilde{V}_t^{*'} R(\tilde{\rho}) W Y_t^* / \tilde{\sigma}^2)^2}{\tilde{I}_{11} - \tilde{I}_{12} \tilde{I}_{22}^{-1} \tilde{I}_{21}} \quad (22)$$

with  $\tilde{I}_{22}$  being the variance-covariance matrix of the non-constrained parameters, namely  $\tilde{\rho}$ ,  $\tilde{\beta}$  and  $\tilde{\sigma}^2$ . The other terms are defined by

$$\begin{aligned} \tilde{I}_{11} = (T-1)tr(W)^2 + \frac{1}{\tilde{\sigma}^2} \sum_{t=1}^{T-1} [(R(\tilde{\rho})WX_t^*\tilde{\beta})'(R(\tilde{\rho})WX_t^*\tilde{\beta})] \\ + (T-1)tr[(R(\tilde{\rho})WR(\tilde{\rho})^{-1})'(R(\tilde{\rho})WR(\tilde{\rho})^{-1})]; \end{aligned} \quad (23)$$

$$\tilde{I}_{12} = \begin{bmatrix} \frac{1}{\tilde{\sigma}^2} \sum_{t=1}^{T-1} X_t^{*'} R(\tilde{\rho})' R(\tilde{\rho}) W X_t^* \tilde{\beta} \\ (T-1)tr[(MR(\tilde{\rho})^{-1})' R(\tilde{\rho}) W R(\tilde{\rho})^{-1} + MWR(\tilde{\rho})^{-1}] \\ 0 \end{bmatrix}. \quad (24)$$

All parameters involved in this test come from the constrained model. The  $LM_e$  statistic is asymptotically distributed as  $\chi_1^2$ .

**Test for serial correlation, spatial autocorrelation and random effects by Baltagi et al. (2007b)**

Consider the panel data model<sup>15</sup>

$$y_{ti} = x'_{ti}\beta + u_{ti}; \quad i = 1, \dots, n; \quad t = 1, \dots, T, \quad (25)$$

where  $y_{ti}$  is the observation of the  $i$ th region for the  $t$ th time period,  $x_{ti}$  denotes the  $(k \times 1)$  vector of observations on the nonstochastic regressors and  $u_{ti}$  is the regression disturbance. In vector form, the disturbance vector of equation (25) is assumed to have random region effects, spatially autocorrelated residual disturbances and a first-order autoregressive remainder disturbance term and it is written by

$$u_t = \mu + \epsilon_t \quad (26)$$

with

$$\epsilon_t = \lambda W \epsilon_t + v_t \quad (27)$$

and

$$v_t = \rho v_{t-1} + e_t, \quad (28)$$

where  $u'_t = (u_{t1}, \dots, u_{tN})$  and  $\epsilon_t, v_t$  and  $e_t$  are similarly defined.  $\mu = (\mu_1, \mu_2, \dots, \mu_N)'$  denote the vector of random region effects which are assumed to be  $IIN(0, \sigma_\mu^2)$ .  $\lambda$  is the scalar spatial autoregressive coefficient while  $\rho$  is the time-wise serial correlation coefficient.  $W$  is the  $(n \times n)$  spatial weights matrix.  $e_{ti} \sim IIN(0, \sigma_e^2)$  and  $v_{i,0} \sim N((0, \sigma_e^2)/(1 - \rho^2))$ .

Baltagi et al. (2007b) consider joint, marginal and conditional hypotheses for spatial error dependence, random region effects as well as for serial error dependence. Table 11 presents an overview of the hypotheses, test statistics and asymptotic distributions. To save space, we define all terms only once in the table.

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<sup>15</sup>All explanations are taken from the original paper by Baltagi et al. (2007b).

	Joint Test	One-dimensional marginal tests		
<b>Hypothesis</b>	$\rho = \lambda = \sigma_{\mu}^2 = 0$	$\lambda = 0$ (assuming $\rho = \sigma_{\mu}^2 = 0$ )	$\rho = 0$ (assuming $\lambda = \sigma_{\mu}^2 = 0$ )	$\sigma_{\mu}^2 = 0$ (assuming $\rho = \lambda = 0$ )
<b>LM statistic</b>	$\text{LM}_J = \frac{nT^2}{2(T-1)(T-2)} [A^2 - 4AF + 2TF^2] + \frac{n^2T}{b} H^2$ <p>where <math>A = \frac{\tilde{u}'(J_T \otimes L_n)\tilde{u}}{\tilde{u}'\tilde{u}} - 1</math>  <math>F = \frac{1}{2} \left( \frac{\tilde{u}'(G \otimes L_n)\tilde{u}}{\tilde{u}'\tilde{u}} \right)</math>  <math>H = \frac{1}{2} \left( \frac{\tilde{u}'(J_T \otimes (W+W))\tilde{u}}{\tilde{u}'\tilde{u}} \right)</math>  <math>b = \text{tr}(W+W')^2/2 = \text{tr}(W^2+W'W)</math>  <math>\tilde{u}</math> = OLS residuals  <math>G</math> = bidiagonal matrix with bidiagonal elements equal to one  <math>J_T</math> is a matrix of ones of dimension <math>T</math></p>	$\text{LM}_{\lambda} = \frac{n^2T}{b} H^2$	$\text{LM}_{\rho} = \frac{n^2T}{T-1} F^2$	$\text{LM}_{\mu} = \frac{nT}{2(T-1)} A^2$
<b>asymptotic distribution under <math>H_0</math></b>	$\chi_3^2$	$\chi_1^2$	$\chi_1^2$	$\chi_1^2$
<b>Two-dimensional marginal tests</b>				
<b>Hypothesis</b>	$\sigma_{\mu}^2 = \rho = 0$ (assuming $\lambda = 0$ )	$\lambda = \rho = 0$ (assuming $\sigma_{\mu}^2 = 0$ )	$\lambda = \sigma_{\mu}^2 = 0$ (assuming $\rho = 0$ )	
<b>LM statistic</b>	$\text{LM}_{\mu\rho} = \frac{nT^2}{2(T-1)(T-2)} [A^2 - 4AF + 2TF^2]$	$\text{LM}_{\lambda\rho} = \text{LM}_{\lambda} + \text{LM}_{\rho}$	$\text{LM}_{\lambda\mu} = \text{LM}_{\lambda} + \text{LM}_{\mu}$	
<b>asymptotic distribution under <math>H_0</math></b>	$\chi_2^2$	$\chi_2^2$	$\chi_2^2$	

	<b>One-dimensional conditional tests</b>
<p><b>Hypothesis</b></p> <p style="text-align: center;"><math>\lambda = 0</math> (allowing <math>\rho \neq 0</math> and <math>\sigma_\mu^2 &gt; 0</math>)</p> <p style="text-align: center;"><math>LM_{\lambda/\rho\mu} = \frac{\hat{D}(\lambda)^2}{b(T-2c\delta+c^2\delta^2)}</math></p> <p>where</p> <p><math>g = \text{tr}(V^{-1}J_T) = \frac{1}{\sigma_\varepsilon^2}(1-\rho)\{2+(T-2)(1-\rho)\}</math></p> <p><math>c = \frac{\sigma_\varepsilon^2\sigma_\eta^2}{\hat{\lambda}^2(1-\rho)^2\sigma_\eta^2+\sigma_\varepsilon^2}</math></p> <p><math>\hat{D}(\lambda) = \frac{\partial L}{\partial \lambda} \Big _{H_0} = \frac{1}{2}\hat{u}'(V^{-1}-2cV^{-1}J_TV^{-1}+c^2[V^{-1}J_T]^2V^{-1}) \otimes (W'+W)\hat{u}</math></p> <p><math>\hat{u}</math> are the restricted maximum likelihood residuals under <math>H_0</math>, and</p> <p><math>V^{-1} = \frac{1}{\sigma_\varepsilon^2}V_\rho^{-1}</math> with <math>V_\rho = \frac{1}{1-\rho^2}V_1</math> where</p> $V_1 = \begin{pmatrix} 1 & \rho & \rho^2 & \dots & \rho^{T-1} \\ \rho & 1 & \rho & \dots & \rho^{T-2} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \rho^{T-1} & \rho^{T-2} & \rho^{T-3} & \dots & 1 \end{pmatrix}$	
<p><b>LM statistic</b></p>	
<p><b>asymptotic distribution under <math>H_0</math></b></p>	$\chi_1^2$

Hypothesis	One-dimensional conditional tests continued $\rho = 0$ (allowing $\lambda \neq 0$ and $\sigma_\mu^2 > 0$ )
	$LM_{\rho/\lambda\mu} = \widehat{D}^2(\rho) J_{33}^{-1}$ <p>where</p> $\widehat{D}(\rho) = \frac{\partial L}{\partial \rho} \Big _{H_0}$ $= -\frac{(T-1)}{T} (\widehat{\sigma}_e^2 \text{tr}(Z_0(B'B)^{-1}) - n) + \frac{1}{2} \widehat{\sigma}_e^2 d' \left( \frac{1}{\widehat{\sigma}_e^2} (E_T' G E_T) \otimes (B'B) + \frac{1}{\widehat{\sigma}_e^2} (\bar{J}_T G \bar{J}_T) \otimes Z_0 + \frac{1}{\widehat{\sigma}_e^2} (E_T G \bar{J}_T) \otimes Z_0 + (\bar{J}_T G \bar{J}_T) \otimes Z_0 (B'B)^{-1} Z_0 \right) u$ <p>with</p> $Z_0 = (T\sigma_\mu^2 I_n + \sigma_e^2 (B'B)^{-1})^{-1}, \quad B = I_n - \lambda W, \quad \bar{J}_T = J_T / T, \quad J_T = \mathbb{1}_T \mathbb{1}_T', \quad \text{and} \quad E_T = I_T - \bar{J}_T$ <p><math>J_{33}^{-1}</math> is the (3,3) element of the inverse of the information matrix <math>\widehat{J}_\theta</math> evaluated under <math>H_0</math>.</p> $\widehat{J}_\theta = \begin{pmatrix} \frac{1}{2} \left( \frac{n(T-1)}{\widehat{\sigma}_e^4} + d_1 \right) & \frac{T}{2} d_2 & \frac{(T-1)}{T} (\widehat{\sigma}_e^2 d_1 - \frac{n}{\widehat{\sigma}_e^2}) & \frac{1}{2} \left[ \frac{(T-1)}{\widehat{\sigma}_e^2} d_3 + \widehat{\sigma}_e^2 d_4 \right] \\ \frac{T}{2} d_2 & \frac{T^2}{2} \text{tr}[Z_0]^2 & (T-1) \widehat{\sigma}_e^2 d_2 & \frac{T \widehat{\sigma}_e^2}{2} d_5 \\ \frac{T-1}{T} (\widehat{\sigma}_e^2 d_1 - \frac{n}{\widehat{\sigma}_e^2}) & (T-1) \widehat{\sigma}_e^2 d_2 & \widehat{J}_{\rho\rho} & \frac{T-1}{T} (\widehat{\sigma}_e^4 d_4 - d_3) \\ \frac{1}{2} \left( \frac{T-1}{\widehat{\sigma}_e^2} d_3 + \widehat{\sigma}_e^2 d_4 \right) & \frac{T \widehat{\sigma}_e^2}{2} d_5 & \frac{T-1}{T} (\widehat{\sigma}_e^4 d_4 - d_3) & \frac{1}{2} [(T-1) d_6 + \widehat{\sigma}_e^4 d_7] \end{pmatrix}$ <p>with</p> $d_1 = \text{tr}(Z_0(B'B)^{-1})^2$ $d_2 = \text{tr}(Z_0(B'B)^{-1} Z_0)$ $d_3 = \text{tr}((W'B + B'W)(B'B)^{-1})$ $d_4 = \text{tr}(Z_0(B'B)^{-1} (W'B + B'W)(B'B)^{-1} Z_0 (B'B)^{-1})$ $d_5 = \text{tr}(Z_0(B'B)^{-1} (W'B + B'W)(B'B)^{-1} Z_0)$ $d_6 = \text{tr}((W'B + B'W)(B'B)^{-1})^2$ $d_7 = \text{tr}(Z_0(B'B)^{-1} (W'B + B'W)(B'B)^{-1})^2$ <p>and <math>\widehat{J}_{\rho\rho} = \frac{n}{T^2} (T^3 - 3T^2 + 2T + 2) + \frac{2(T-1)^2 \widehat{\sigma}_e^4}{T^2} d_1</math></p>
asymptotic distribution under $H_0$	$\chi_1^2$



Two-dimensional conditional tests	
Hypothesis	$\lambda = \rho = 0 \text{ (allowing } \sigma_\mu^2 > 0)$
	$\text{LM}_{\lambda, \rho / \mu} = \widehat{D}'_\theta \widehat{\Gamma}_\theta^{-1} \widehat{D}_\theta = \frac{\widehat{D}(\rho)^2 n^2 T^2 (T-1)}{4\widehat{\sigma}_1^4 \widehat{\sigma}_e^2 \det[\widehat{J}(\theta_1)]} + \frac{\widehat{D}(\lambda)^2}{[(T-1) + \frac{\widehat{\sigma}_1^4}{\widehat{\sigma}_e^2}] b}$
	<p>with</p> $\widehat{D}(\rho) = \frac{\partial L}{\partial \rho} \Big _{H_0} = \frac{n(T-1)}{T} \left( \frac{\widehat{\sigma}_1^2 - \widehat{\sigma}_e^2}{\widehat{\sigma}_1^2} \right) + \frac{1}{2} \widehat{\sigma}_e^2 \hat{u}' \left[ (\widehat{J}_T / \widehat{\sigma}_1^2 + E_T / \widehat{\sigma}_e^2) G (\widehat{J}_T / \widehat{\sigma}_1^2 + E_T / \widehat{\sigma}_e^2) \otimes I_n \right] \hat{u}$ $\widehat{D}(\lambda) = \frac{\partial L}{\partial \lambda} \Big _{H_0} = \frac{1}{2} \hat{u}' \left[ \frac{\widehat{\sigma}_1^2}{\widehat{\sigma}_1^4} (\widehat{J}_T \otimes (W' + W)) + \frac{1}{\widehat{\sigma}_e^2} (E_T \otimes (W' + W)) \right] \hat{u}$ <p>where</p> $\widehat{\sigma}_1^2 = \hat{u}' (J_T \otimes I_n) \hat{u} / nT \quad \text{and} \quad \widehat{\sigma}_e^2 = \hat{u}' (E_T \otimes I_n) \hat{u} / n(T-1)$ <p>are the solutions of <math>\frac{\partial L}{\partial \mu} \Big _{H_0} = 0</math> and <math>\frac{\partial L}{\partial \sigma_e^2} \Big _{H_0} = 0</math>, respectively. <math>\hat{u}</math> are the restricted maximum likelihood residuals under <math>H_0</math>. <math>\widehat{J}(\theta_1)</math> is the block-diagonal information matrix with respect to the parameters <math>(\sigma_e^2, \sigma_\mu^2, \rho)</math>.</p>
LM statistic	$\widehat{J}_{\rho\rho} = n \begin{bmatrix} \frac{n}{2} \left( \frac{1}{\widehat{\sigma}_1^4} + \frac{T-1}{\widehat{\sigma}_e^2} \right) & \frac{nT}{2\widehat{\sigma}_1^4} & \frac{n(T-1)}{T} \widehat{\sigma}_e^2 \left( \frac{1}{\widehat{\sigma}_1^4} - \frac{1}{\widehat{\sigma}_e^2} \right) & 0 \\ \frac{nT}{2\widehat{\sigma}_1^4} & \frac{nT^2}{2\widehat{\sigma}_1^4} & \frac{n(T-1)\widehat{\sigma}_e^2}{\widehat{\sigma}_1^4} & 0 \\ \frac{n(T-1)}{T} \widehat{\sigma}_e^2 \left( \frac{1}{\widehat{\sigma}_1^4} - \frac{1}{\widehat{\sigma}_e^2} \right) & \frac{n(T-1)\widehat{\sigma}_e^2}{\widehat{\sigma}_1^4} & \widehat{J}_{\rho\rho} & 0 \\ 0 & 0 & 0 & (T-1)b + \frac{\widehat{\sigma}_1^4}{\widehat{\sigma}_e^2} b \end{bmatrix}$ <p>The information matrix is given by <math>\widehat{J}_\theta =</math></p>
	<p>where</p> $\widehat{J}_{\rho\rho} = n [2a^2(T-1)^2 + 2a(2T-3) + T-1] \quad \text{with } a = \frac{\widehat{\sigma}_e^2 - \widehat{\sigma}_1^2}{T\widehat{\sigma}_1^4}$
asymptotic distribution under $H_0$	$\chi_2^2$



Two-dimensional conditional tests continued	
Hypothesis	$\lambda = \sigma_\mu^2 = 0 \text{ (allowing } \rho \neq 0)$ $\text{LM}_{\lambda, \mu / \rho} = \widehat{D}'_\theta \widehat{\Gamma}^{-1} \widehat{D}_\theta = \frac{\widehat{D}^2(\sigma_\mu^2)}{\det[J(\theta_1)]} \frac{n^2}{\sigma_\epsilon^2(1-\rho^2)} \left\{ \frac{T}{2} (3\rho^2 - \rho^2 T + T - 1) - \rho^2 \right\} + \frac{\widehat{D}^2(\lambda)}{Tb}$ <p>where</p> $\widehat{D}(\sigma_\mu^2) = \frac{\partial L}{\partial \sigma_\mu^2} \Big _{H_0} = -\frac{n\delta}{2} + \frac{1}{2\sigma_\epsilon^2} \hat{u}' (V_\rho^{-1} J_\Gamma V_\rho^{-1} \otimes I_n) \hat{u}$ $\widehat{D}(\lambda) = \frac{\partial L}{\partial \lambda} \Big _{H_0} = \frac{1}{2\sigma_\epsilon^2} \hat{u}' (V_\rho^{-1} \otimes (W' + W)) \hat{u}$ <p>The information matrix is given by <math>\widehat{J}_\theta = \begin{pmatrix} \frac{nT}{2\sigma_\epsilon^2} &amp; \frac{n\delta}{2\sigma_\epsilon^2} &amp; \frac{n\rho}{\sigma_\epsilon^2(1-\rho^2)} &amp; 0 \\ \frac{n\delta}{2\sigma_\epsilon^2} &amp; \frac{n\delta^2}{2\sigma_\epsilon^2} &amp; \frac{n}{\sigma_\epsilon^2(1+\rho)} [(2-T)\rho^2 + \rho + (T-1)] &amp; 0 \\ \frac{n\rho}{\sigma_\epsilon^2(1-\rho^2)} &amp; \frac{n\rho}{\sigma_\epsilon^2(1-\rho^2)} &amp; \frac{n}{\sigma_\epsilon^2(1+\rho)} [(2-T)\rho^2 + \rho + (T-1)] &amp; 0 \\ 0 &amp; 0 &amp; 0 &amp; Tb \end{pmatrix}</math></p> <p><math>\hat{u}</math> are the restricted maximum likelihood residuals under <math>H_0</math></p> <p><math>J(\theta_1)</math> is the block-diagonal information matrix with respect to the parameters <math>(\sigma_\epsilon^2, \sigma_\mu^2, \rho)</math>.</p>
LM statistic	
asymptotic distribution under $H_0$	$\chi_2^2$

Two-dimensional conditional tests continued	
<b>Hypothesis</b>	$\sigma_\mu^2 = \rho = 0$ (allowing $\lambda \neq 0$ )
<b>LM statistic</b>	$\text{LM}_{\mu/\lambda} = \widehat{D}'_\theta \widehat{\Gamma}_\theta^{-1} \widehat{D}_\theta$ <p>where  <math>\widehat{D}'_\theta = (0, \widehat{D}(\sigma_\mu^2), \widehat{D}(\rho), 0)</math>  with  <math>\widehat{D}(\sigma_\mu^2) = \frac{\partial L}{\partial \sigma_\mu^2} \Big _{H_0} = -\frac{T}{2\sigma_\epsilon^2} \text{tr}(B'B) + \frac{1}{2\sigma_\epsilon^4} \hat{u}'(J_T \otimes (B'B)^2) \hat{u}</math>  <math>\widehat{D}(\rho) = \frac{\partial L}{\partial \rho} \Big _{H_0} = \frac{1}{2\sigma_\epsilon^2} \hat{u}' [G \otimes (B'B)] \hat{u}</math></p> <p>The information matrix is given by <math>J_\theta =</math></p> $\begin{pmatrix} \frac{nT}{2\sigma_\epsilon^2} \text{tr}(B'B) & 0 & \frac{T}{2\sigma_\epsilon^2} \text{tr}(B'B) & 0 & \frac{T}{2\sigma_\epsilon^2} d_3 \\ \frac{T}{2\sigma_\epsilon^2} \text{tr}(B'B) & 0 & \frac{T^2}{2\sigma_\epsilon^2} \text{tr}[(B'B)^2] & \frac{T-1}{\sigma_\epsilon^2} \text{tr}(B'B) & \frac{T}{2\sigma_\epsilon^2} \text{tr}[W'B + B'W] \\ 0 & 0 & \frac{T-1}{\sigma_\epsilon^2} \text{tr}(B'B) & n(T-1) & 0 \\ \frac{T}{2\sigma_\epsilon^2} d_3 & \frac{T}{2\sigma_\epsilon^2} \text{tr}[W'B + B'W] & 0 & 0 & \frac{T}{2\sigma_\epsilon^2} d_6 \end{pmatrix}$ <p><math>\hat{u}</math> are the restricted maximum likelihood residuals under <math>H_0</math></p>
<b>asymptotic distribution under <math>H_0</math></b>	$\chi_2^2$

Table 11: Hypotheses, LM statistics and asymptotic distributions of Baltagi et al. (2007b)

## Data description

Variable	Description	Data Source
<b>dependent variable</b>		
unemployment rate ( $u_{it}$ )	Regional unemployment rate at district level. Unemployment is defined according to regulations in Social Security Code, i.e. a person is officially registered as unemployed when certain requirements are fulfilled as this status is connected to the right to receive public benefits.	Federal Employment Office (Bundesagentur für Arbeit), data can be downloaded from regional data base of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ).
<b>explanatory variables</b>		
<i>market equilibrium effects</i>		
Industry mix ( $\%AGR_{it}$ , $\%IND_{it}$ , ...)	Number of employed persons which have a job that is subject to social insurance contribution according to the sector in which they are working in relation to the total number of employed persons with a job that is subject to social contributions. The classification of sectors in the version of 2003 is used which bases upon the European classification (NACE Rev. 1.1)). As there is a change in the sector classification in 2008, we only use data until 2007.	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ). Some values for the federal country of Saxony-Anhalt are missing in this database. We requested them directly from the regional statistical office of Saxony-Anhalt.
<i>demographic variables</i>		
Age structure of the population ( $OLD_{it}$ , $YOUNG_{it}$ )	Share of labor force aged 15 until 25 and older than 50 years, respectively. The labor force consists of employed and unemployed persons.	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ). Some values for the federal country of Saxony-Anhalt and Saxony are missing in this database. We requested them directly from the regional statistical office of Saxony-Anhalt and Saxony.
Foreigners ( $FOREIGN_{it}$ )	Extent of foreign labor force in relation to the whole labor force in district $i$ .	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ). Some values for the federal country of Saxony-Anhalt are missing in this database. We requested them directly from the regional statistical office of Saxony-Anhalt.

Variable	Description	Data Source
Female labor force participation ( $FP_{it}$ )	Ratio of female labor force (aged 15-65) to the female resident population in the same age.	Unfortunately, data on female labor force participation is only available on the level of <i>Regierungsbezirke</i> (partly corresponding to German NUTS II regions). The data source is the microcensus ( <i>Mikrozensus</i> ) which provides official representative statistics of the population and the labor market in Germany. However, data is only available until 2002. We obtained the missing values by extrapolation.
Educational attainment of population ( $H0_{it}, H1_{it}, H2_{it}$ )	Share of employed persons which have a job that is subject to social insurance contribution according to the level of education. Official statistics provide three levels of educational attainment: without any professional training, with a certificate of a vocational school or certificate of a university/university of applied sciences.	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ). Some values for the federal country of Saxony-Anhalt are missing in this database. We requested them directly from the regional statistical office of Saxony-Anhalt.
Commuting ( $COMM_{it}$ )	Balance of incoming and outgoing commuters of district $i$ , i.e. if the value is positive, there are more people that commute in the district than people that commute out of the district.	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ). Some values for the federal country of Saxony-Anhalt and Saxony are missing in this database. We requested them directly from the regional statistical office of Saxony-Anhalt and of Saxony.
<i>amenities</i>		
Population density ( $DENS_{it}$ )	Population density in persons per km <sup>2</sup> , values are calculated from the average population in every district divided by the area of every district.	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ).
Public debts of districts ( $DEBTR_{it}$ )	Sum of public debts of all communities belonging to district $i$ in relation to the regional domestic product of district $i$ .	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ).
Number of business registrations ( $REG_{it}$ )	Number of all newly registered businesses in district $i$ .	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ).
Number of overnight stays in hotels ( $STAY_{it}$ )	Number of persons that stay over night in hotels, hostels, etc.	Regional Database of Federal Statistical Office ( <a href="http://www.regionalstatistik.de">www.regionalstatistik.de</a> ).

Table 12: Descriptions and data sources of the dependent and all explanatory variables

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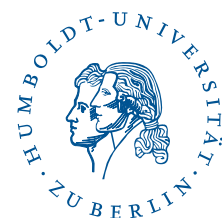
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