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Can crop yield risk be globally diversified?

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Can crop yield risk be globally diversified?*

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Abstract

In 2007 and 2008 world food markets observed a significant price boom. Crop failures simultaneously occurring in some of the world's major production regions have been quoted as one factor among others for the price boom. Against this background, we analyse the stochasticity of crop yields in major production areas. The analysis is exemplified for wheat, which is one of the most important crops worldwide. Particular attention is given to the stochastic dependence of yields in different regions. Thereby we address the question of whether local fluctuations of yields can be smoothed by international agricultural trade, i.e. by global diversification. The analysis is based on the copula approach, which requires less restrictive assumptions compared with linear correlations. The use of copulas allows for a more reliable estimation of extreme yield shortfalls, which are of particular interest in this application. Our calculations reveal that a production shortfall, such as in 2007, is not a once in a lifetime event. Instead, from a statistical point of view, similar production conditions will occur every 15 years.

JEL classification: C14; Q19

Keywords: crop yield risk, fully nested hierarchical Archimedean copulas (FNAC), price boom

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I Introduction

Agricultural commodity markets have been regulated for a long time by a variety of instruments, including intervention prices, fixed and variable tariffs, export subsidies and production quotas. Due to negotiations within the WTO, most agricultural markets have been deregulated during the last two decades throughout the world. This abolishment of price stabilizing measures led to an increase in price volatility on formerly regulated markets (Yang et al., 2001; Chavas and Kim, 2006). Although higher price fluctuations were expected, the crop price boom in 2007/2008 surprised market experts. This rise of agricultural commodity prices can be regarded from two perspectives. On the one hand, it quickened optimism in the agribusiness. For example, the end of the technological treadmill, which prevented an increase of farm incomes in the past, was proclaimed (von Witzke et al., 2008). On the other hand, the sharp increase of food prices shortened the food supply in low income countries and aggravated hunger and malnutrition among poor people. From a scientific point of view, two questions arise: what factors were responsible for the price boom and how likely is it that a similar constellation of price determining factors will occur again? It is widely accepted that multiple factors caused the recent increase in agricultural commodity prices. Sarris (2009) emphasizes three main factors: first, crop failures simultaneously occurred in major production region of the world; second, there was an increased demand for biofuels; and third, investors in agricultural commodity markets were involved in speculative activities. This article focuses on the first of these factors, i.e. stochastic shifts on the supply side. It is well known that agricultural yields, crop yields in particular, heavily depend on weather conditions. Thus, weather risks are immediately reflected in yield risks (e.g. Odening et al., 2008; Musshoff et al., 2009). When analysing the impact of yield fluctuations on agricultural prices, the choice of an appropriate perspective is important. For example, a regional analysis is not appropriate because poor harvests in one country can be compensated by imports (Lotze-Campen, 2007). In integrated markets, diversification by global trade has to be taken into account and thus a global analysis of agricultural yield risks is necessary. Against this background, we analyse the stochasticity of crop yields in the world's major production areas. The analysis is exemplified for wheat, which is one of the most important crops in the world in terms of production area and food security. Particular attention is given to the stochastic dependence of yields in different parts of the world. The spatial dependence structure is modelled using copulas. Compared with linear correlations, the application of copulas requires less restrictive assumptions and has advantages in the estimation of the joint occurrence of extreme events (c.f. Embrechts et al., 1999). Copulas became increasingly popular in the last decade and have been applied to various finance and insurance problems (Cherubini et al., 2004; Chen et al., 2009; Turgutlu and Ucer, 2010). Bianchi et al. (2009) integrated a copula approach in the Vector-Auto-Regression model (VAR) to model and forecast the dynamics of industrial production in the euro-zone. Applications in agricultural economics, however, are rare. Vedenov (2008) analyses the relationship between individual farm yields and area yields and Zhu *et al.* (2008) investigate the dependence of prices and yields in the context of revenue insurance.

The remainder of the article is divided into two main sections. Section II describes the methodological approach. We briefly review the concept of the copula and present the idea of a fully nested Archimedian copula for modelling high dimensional dependence structures. This concept is then applied to the estimation of joint yield risks of major wheat producers. Data and estimation results are presented in section III. The article ends with conclusions on the systemic risk of wheat production and the effectiveness of global trade to diversify this risk.

II Modelling Stochastic Dependence using Copulas

Theoretical framework

The outcome of multi-dimensional risks can be presented by using a multivariate distribution $F(x_1, \dots, x_d)$, in which x_i denotes the realization of the random variable X_i , $i=1,\dots,d$. Direct estimation of the joint distribution F usually fails due to insufficient data. Alternatively, the joint distribution F can be determined by linking the univariate marginal distribution $F_i(x_i)$ by means of the (linear) correlation coefficients between random variables. Yet, such kind of estimation of the joint distribution F is valid only for the family of elliptical multivariate distribution including multivariate normal distribution (cf. Embrechts et al., 2002). If this assumption does not hold then the associated (linear) correlation coefficients are not able to capture the complete information about the dependence structure between each single risk involved – particularly for the tail dependence, which plays an important role for the analysis of extreme events. Xu et al. (2010) showed with an example of weather risk how large the estimation error can be if linear correlation were applied instead of a more appropriate and sophisticated model.

The theoretical fundament of the copula concept is given by Sklar's Theorem (Sklar, 1959), which states that any d-dimensional distribution $F(x_1, \dots, x_d)$ can be described by using a copula function $C(\cdot)$:

$$F(x_1, ..., x_d) = C\{F_1(x_1), ..., F_d(x_d)\}, \quad \forall \ x_1, ..., x_d \in \overline{R}$$
 (1)

 $F_i(x_i)$ denotes the (univariate) marginal distribution and $u_i = F_i(x_i) \rightarrow [0,1]$ is therefore the uniform marginal distribution. Following Joe (1997), the copula function can be understood as a multivariate distribution function with all margins being uniformly distributed on [0,1]:

$$C(u_1, ..., u_d) = F\{F_1^{-1}(u_1), ..., F_d^{-1}(u_d)\}, \quad F_i^{-1}(u_i) = x_i$$
 (2)

Equation 1 allows us to decompose any d-dimensional joint distribution function $F(x_1,...,x_d)$ into its d marginal distributions $F_1(x_1),...,F_d(x_d)$, and a copula $C(\cdot)$, which describes the dependence structure among the d random variables. As with the estimation of any distribution function one can apply either parametric or nonparametric (e.g. kernel) approaches (Chen and Huang, 2007). Vedenov (2008) argues that a nonparametric copula is a natural choice since there is no constructive way to determine the optimal copula function and thus the danger of misspecifying

the copula is high. On the other hand, if valuable prior information is available, parametric methods can improve the estimation results (Charpentier *et al.*, 2007; Genest *et al.*, 1995). The main reason for using a parametric approach in this study is its superiority in simulating data from the copula. In fact, up to now there is no efficient method on simulation from the multivariate empirical distributions.

Parametric copulas can be classified into elliptical and Archimedean copulas. In the following, we concentrate only on Archimedean copulas, which can be described in a closed form. This property is convenient when applying simulation procedures. The general expression of Archimedean copulas is given by:

$$C(u_1, \dots, u_d) = \varphi^{-1}(\varphi(u_1) + \dots + \varphi(u_d))$$
(3)

where $\varphi(\cdot)$ is called the generator function with $\varphi(0) = 1$, $\varphi(\infty) = 0$ and φ^{-1} is its inverse. The family of Archimedean copulas includes three important types: the Gumbel, the Clayton and the Frank. The Gumbel copula is asymmetric and appropriate for presenting upper tail dependence which shows a stronger linkage between positive values, more variability and more mass in the positive tail than, for example, the Gaussian copula (Okhrin, 2007). In contrast to the Gumbel copula, the Clayton copula assigns a higher probability to joint extreme negative events than to joint extreme positive events. It displays lower tail dependence and is characterized by zero upper tail dependence (Nelsen, 2006, p. 215). Because of this feature, the Clayton copula has been widely used in financial applications and risk management (e.g., Junker and May, 2005; Blum *et al.*, 2002). The Frank copula is adequate to model symmetric dependence structures and exhibits both positive and negative dependence. In contrast to the Gumbel and the Clayton copula, the Frank copula implies tail independence (Nelsen, 2006, p. 215).

Hierarchical construction of a multi-dimensional dependence structure

Although the approach described above provides a relatively easy method to estimate and simulate the high-dimensional dependence structure, it is in fact extremely restrictive in the practical application of modelling a higher-dimensional case. The reason is that most multivariate Archimedean copula models present the whole dependence structure with only one single copula parameter θ , independent of the dimension of the model. Consequently, the substructure of the dependence is invisible. Furthermore, a multivariate Archimedean copula implicitly assumes that the order of margins u_i within the copula function is exchangeable. For instance, for a three dimensional case this means $C(u_1,u_2,u_3) = C(u_3,u_1,u_2)$. However, the implied permutation symmetry of the copula represents a very specialized dependence structure, which is not plausible for many applications (cf. McNeil *et al.*, 2005, p. 224; Savu and Trede, 2010).

In view of these shortcomings, attempts have been made to develop a more flexible and appropriate Archimedean model for capturing a high-dimensional dependence structure. One convincing method is the so-called Fully-Nested Archimedian Copulas (FNAC), which aggregates one dimension step by step starting from a low dimensional copula (Savu and Trede, 2010). The model for the d-dimensional dependence structure using the FNAC approach can be expressed as:

$$C(u_{1},...,u_{d}) = \varphi_{d-1}^{-1} \left\{ \varphi_{d-1} \circ \varphi_{d-2}^{-1} \left[... \left(\varphi_{2} \circ \varphi_{1}^{-1} \left[\varphi_{1}(u_{1}) + \varphi_{1}(u_{2}) \right] + \varphi_{2}(u_{3}) \right) + ... + \varphi_{d-2}(u_{d-1}) \right] + \varphi_{d-1}(u_{d}) \right\}$$

$$(4)$$

where $\varphi_1(\cdot),\ldots,\varphi_{d-1}(\cdot)$ are generator functions and their inverses $\varphi_1^{-1}(\cdot),\ldots,\varphi_{d-1}^{-1}(\cdot)$ capture the joint distribution of each aggregation step from low dimension (low level) to high dimension (high level). The symbol " \circ " is the composition operator. The FNAC method (Equation 4) is therefore characterized by up to d-1 copulas composed of d(d-1)/2 possible combinations of distinct bivariate marginal distributions $\left(F_i(x_i), F_j(x_j)\right)$ with $i \neq j$. The substructures of multidimensional dependence cluster $\varphi_{d-1} \circ \varphi_{d-2}^{-1}$ are expressed hierarchically (see Fig. 2 in Section III).

The construction of the multivariate dependence structure can be carried out with following steps: Initially at the lowest level, two variables with the largest copula parameter θ among all of the d(d-1)/2 pairs of variables will be combined by using a bivariate Archimedean copula. The first combination at the lowest level (two-dimensional dependence structure) can be described as:

$$z_1 = C_1(u_1, u_2) = \varphi_1^{-1} [\varphi_1(u_1) + \varphi_1(u_2)]$$
(5)

On the second level (three-dimensional dependence structure), the joint distribution z_1 with u_3 is nested by using $C_2(z_1, u_3)$:

$$C_2(z_1, u_3) = \varphi_2^{-1} \{ \varphi_2 \circ \varphi_1^{-1} [\varphi_1(u_1) + \varphi_1(u_2)] + \varphi_2(u_3) \} = \varphi_2^{-1} [\varphi_2(z_1) + \varphi_2(u_3)]$$
 (6)

This procedure will be repeated until the highest level has been reached. Since Equation 4 involves d-1 generator functions, there are total d-1 copula parameters to be estimated (in contrast to Equation 3).

Usually, all bivariate combinations within a FACN structure employ the same copula type, so that the copula models differ only in the copula parameters. These parameters must be strictly monotone decreasing from the lowest level to the highest level, $\theta_1 \geq \theta_2 \geq \cdots \geq \theta_{d-1}$. This condition, together with the use of the same copula type, ensures that the outcome of the combination of two copulas from different levels results again in a proper copula (Joe, 1997; Embrechts *et al.*, 2003).

Estimation and Goodness-of-Fit tests of copulas

In general, three approaches are available to estimate the parameters of a copula (cf. Cherubini et~al., 2004). The Exact Maximum Likelihood Method (EMLM) estimates the copula parameter θ and the parameters of the marginal distributions $\alpha_1, \dots, \alpha_d$ simultaneously. Alternatively, a two-step procedure can be used, where the parameters of the margins α are estimated first. Afterwards the copula parameters are determined, e.g. by maximum likelihood, treating the parameters of the margins as given. This procedure is called the inference for margin (IFM) method (Joe 1997). The IFM method is less efficient than the one-step maximum likelihood but computationally more attractive. An alternative semi-parametric estimation procedure is the Canonical Maximum-Likelihood (CML) (Haerdle et~al., 2008). The log-likelihood function is given by:

$$\hat{\theta} = \underset{\theta}{\operatorname{argmax}} \sum_{j=1}^{k} \ln[c\{\hat{F}_{1}(x_{1j}), \dots, \hat{F}_{d}(x_{dj}); \theta\}]$$
(7)

 $\hat{F}(x_{ij})$ is the i-th empirical marginal distribution based on the observations x_{ij} , $j=1,\cdots,k$. $\hat{\theta}$ is also called as Maximum-Pseudo-Likelihood-Estimator or rank-based Maximum-Likelihood-Estimator. The difference between CML and the two previously introduced methods, EMLM and IFM, is that the parametric marginal distribution is substituted by the empirical (rank-based) marginal distribution (Equation 10). The CML method is quite useful if the precise estimation of parametric margins is hampered by a limited number of observations. The CML method will be applied to the estimation of the copula parameter in this study.

Since different copula models imply very different dependence structures, it is important to apply the correct one that fits the empirical data the best. Although the underlying test problem is analogous to a Goodness-of-Fit (GoF) test for univariate distributions, it is more difficult applied to multidimensional distributions. In this context, Genest and Remillard (2008) propose a GoF-test belonging to the class of the dimension reduction approaches. Let C be the true d-dimensional copula for the empirical data, which is to be modelled and let C_{θ} be the underlying copula candidate to be tested. The subscript θ is the associated copula parameter. The testing hypothesis can be expressed as:

$$H_0: C \in \mathbf{C} = \{C_\theta; \theta \in \Theta\} \text{ vs. } H_1: C \notin \mathbf{C} = \{C_\theta; \theta \in \Theta\}$$
(8)

where Θ is the space of copula parameter. The GoF-test for Equation 8 is based on the Cramer-von-Mises Statistic \hat{T} , which measures the distance between empirical copula $\hat{C}(\cdot)$ and the candidate of parametric copula $C_{\theta}(\cdot)$.

$$\hat{T} = k \cdot \int_{[0,1]^d} \left[\hat{C}(Z) - C_{\theta}(Z) \right]^2 d\hat{C}(z) = \sum_{i=1}^k \left[\hat{C}(Z_i) - C_{\theta}(Z_i) \right]^2$$
(9)

Herein, Z denotes the d-dimensional empirical marginal distribution which can be described as

$$Z = (z_1, \dots, z_d) = \left(\frac{R_{1j}}{k+1}, \dots, \frac{R_{dj}}{k+1}\right), \quad j = 1, \dots, k$$
(10)

where k is the number of observations and R_{ij} is the rank of the observations x_{ij} amongst $(x_{11}, ..., x_{dk})$, $i \in (1, ..., d)$. The elements of Z are called pseudo-observations.

The empirical copula \hat{C} can then be expressed as

$$\hat{C}(Z) = \frac{1}{k} \sum_{j=1}^{k} I(z_{j1} \le u_{(1)}, \dots, z_{jd} \le u_{(d)}), (u_{(1)}, \dots, u_{(d)}) \in [0, 1]^{d}$$
(11)

where $I(\cdot)$ is an indicator function and $u_{(1)}, \dots, u_{(d)}$ are order statistics from the sample.

To obtain reliable p-value estimates, a parametric bootstrap procedure is needed, in which the calculation of Equation 9 is repeated for L times. The p-value for Equation 9 can be calculated by using the following expression:

$$p = \frac{1}{L+1} \sum_{l=1}^{L} I(T_l^* > \hat{T}), \ l = 1, \dots, L$$
 (12)

The random variable T_l^* is defined as:

$$T_l^* = \sum_{i=1}^k \left[C_l^*(Z_l^*) - C_{\theta_l^*}(Z_l^*) \right]^2, \ Z_l^* = (z_{1,j,l}, \dots, z_{d,j,l})$$
(13)

The bootstrap procedure for T_l^* is comprised of the following steps:

- a) the random sample $(x_{1,l}^*, \dots, x_{d,l}^*)$ from the hypothesized copula C_{θ} is generated and the associated pseudo-samples Z_l^* are calculated according to Equation 10;
- b) the parameters θ_l^* are estimated based on Z_l^* ;
- c) the empirical copula C_i^* is determined according to Equation 11;
- d) the steps from a) to c) will be repeated for L times; and
- e) the p-value is calculated, which is straightforward once C_l^* and θ_l^* are known.

Copula-based simulation of simultaneous risks

Once the marginal distributions and the copula have been determined and estimated parametrically, the realization of d-dimensional random variables, which follow the joint distribution $F(x_1, \dots, x_d)$ can be generated by employing the Monte-Carlo simulation method. In the context of multi-dimensional copulas, the "conditional inverse method" has been employed (Haerdle and Okhrin, 2009). The basic idea of this method is to generate the multi-dimensional random variables recursively according to the associated conditional distribution. First, the d-dimensional independent variables v_1, \dots, v_d are drawn from the uniform distribution $U \in [0,1]$. Afterwards the d-dimensional uniform-distributed variables u_1, \dots, u_d will be generated. In contrast to the generation of v_1, \dots, v_d , the d-dimensional variables u_1, \dots, u_d are stochastic dependent. The dependence structure of u_1, \dots, u_d is captured by the copulas $C(u_1, \dots, u_d)$. To achieve this, a recursive procedure is carried out. In the first step, the initial value of u_1 is equal to v_1 . The consecutive values u_2, \dots, u_d can be determined by the following procedure:

$$u_i = \Lambda^{-1}(v_i), \ i = 2, \cdots, d \tag{14}$$

The relationship between u_i and v_i can be determined by a certain function $\Lambda(\cdot)$ and through the inverse function of $\Lambda(\cdot)$ the independent uniform-distributed multivariate variables v_1, \ldots, v_d will be transformed to the dependent uniform-distributed multivariate variables u_1, \ldots, u_d . Therefore, the function $\Lambda(\cdot)$ also describes the dependence structure of u_1, \ldots, u_d . $\Lambda(\cdot)$ can be defined as:

$$\Lambda(u_{i}|u_{1},\dots,u_{i-1}) = P(U_{i} \leq u_{i}|U_{1} = u_{1},\dots,U_{i-1} = u_{i-1})$$

$$= \frac{\partial^{i-1}C_{i}(u_{1},\dots,u_{i})}{\partial u_{1},\dots,\partial u_{i-1}} / \frac{\partial^{i-1}C_{i-1}(u_{1},\dots,u_{i-1})}{\partial u_{1},\dots,\partial u_{i-1}}$$
(15)

 $C_i(\cdot)$ stands for the copula with i-th dimensional margins. In the last step, the realizations x_i associated with each random variable X_i can be generated by using

$$x_i = F_i^{-1}(u_i), \quad i = 1, \dots, d$$
 (16)

where $F_i^{-1}(u_i)$ is the inverse function of the marginal distribution $F_i(x_i)$. The resulting realizations x_1, \ldots, x_d , which are simulated by using the above-mentioned

procedure, follow the joint distribution $F(x_1,\dots,x_d)$, or more precisely they follow the copula $C(u_1, \dots, u_d)$.

III **Empirical Analysis of Shortfall Risk on Global Crop Production**

Data and modelling procedure

The empirical analysis is based on the yield data of wheat for the main producing countries worldwide. To limit computational work, the eight most important countries are selected: Canada, China, France, Germany, India, Pakistan, Turkey and the USA¹. In 2007, the amount of the wheat production in these countries share 58% of the total production worldwide. The empirical data of wheat yields for these countries is provided by FAO (http://faostat.fao.org) and is available from 1961 to 2007, comprising of 47 observations. The empirical analysis involves the following steps: First, the total amount of wheat yield is converted into per hectare yields. Using the hectare yields makes it easier to compare countries with different production scales. Moreover, changes of the acreage from year to year will not affect the analysis². Second, to eliminate the production trend caused by technical progress, the hectare yields are detrended by applying the following linear model:

$$y_{i,t} = m_i + \alpha_i \cdot t + \varepsilon_i, \quad i = 1, \dots, 8$$

where $y_{i,t}$ is the hectare yield (dt/hectare), m_i the constant term for country i, tdenotes time and α_i captures technical progress. The residual ε_i is the detrended hectare yield.

Table A1 in the appendix shows the detrended hectare ε yields for eight countries in ascending order. Note that yields realized in 2007 were the third worst yields since 1961 in four countries; however, this yield did not affect all eight countries. For example, in Pakistan a relatively good harvest was recorded in 2007. Furthermore, the figures provide an impression about the size of the yield volatility as well as their differences in each of the observed countries for each year.

Using the detrended yield data ε_i in Equation 17, univariate yield distributions are specified and estimated for each wheat producing country. The type of yield distribution is selected according to a χ^2 -test. A hierarchical Archimedean copula, FNAC, has then been estimated for the eight-dimensional detrended hectare yield, ε_i as described in the previous section. Once a hierarchical dependence structure is defined, the vector ε_i can be simulated by using conditional inverse method (see Equations 14 - 16). Finally, the total yield (tons) for the eight countries related to year 2007, $y_n^{sim,t}$, as well as the average yield (dt/hectare) for the eight countries,

 $\overline{y}_{i}^{sim,t}$, can be calculated by:

$$y_n^{sim,t} = \sum_{i=1}^{8} \left(\varepsilon_{i,n} + m_i + \alpha_i \cdot t \right) \cdot a_i, \quad i = 1, \dots, 8, \ t = 2007$$

$$(18)$$

¹ Although Russia belongs to the largest wheat producers, it had to be excluded from the analysis due to insufficient data.

The harvested areas of wheat are depicted in Fig. A1 in the appendix.

and

$$\overline{y}_n^{sim,t} = y_n^{sim,t} / \sum_{i=1}^8 a_i \tag{19}$$

n denotes the n-th simulation and a_i is the harvest area for country i. The simulation is carried out 10 000 times. The procedure results in an empirical distribution for the average yield and the total yield of wheat from which statistical parameters of interest can be derived.

Results

The results of the GoF-test for the marginal distributions of the detrended hectare yield, ε_i , are presented in Table A2 in the appendix. Apparently, the random yields in the various countries cannot be described by only one type of distribution. Instead, the yields follow different distributions, such as Weibull, Gaussian or Lognormal distributions. Similar results are reported by Moriondo *et. al.*, (2009) as well as Upadhyay and Smith (2005). This finding confirms that the joint yield distribution for all countries cannot be multivariate normal and hence the requirement for using linear correlations coefficients is not fulfilled.

The selection of the appropriate copula type is based on the GoF-test described in the previous section. The Clayton, the Gumbel and the Franck copula have been considered as candidates. The test was conducted for all 28 possible country pairs. In most cases the Clayton copula yields the best fit and thus this copula type was chosen for the entire FNAC. This result also indicates that the use of linear correlation would be inappropriate.

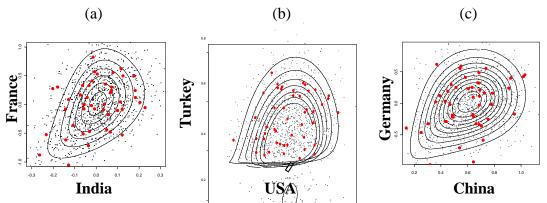


Fig. 1. Contour lines for the joint probability of the residual of wheat yield (dt/hectare) for (a) France and India, (b) Turkey and USA, (c) Germany and China. (Type of copula: Clayton; bold dots = observed; thin dots = simulated).

Fig. 1 illustrates the bivariate yield distributions for the following country pairs: a) France and India; b) Turkey and USA; and c) Germany and China. The contour lines of the bivariate distributions are obviously not symmetric and elliptical as implied by linear correlations.

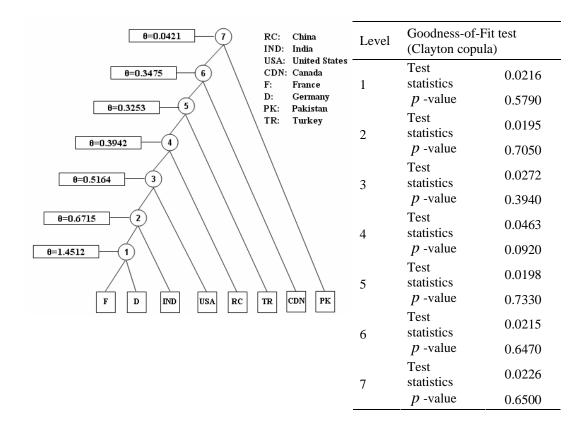
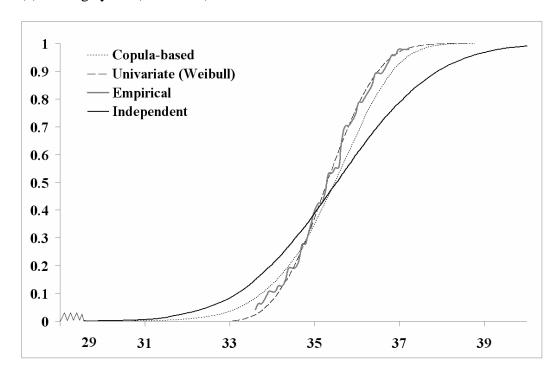


Fig. 2. Fully nested hierarchical structure of the Archimedean copula, FNAC

Next, the structure of the hierarchical copula is determined. The aggregation of countries rests on the test statistic of the GoF-test. Fig. 2 depicts the resulting dependence structure (left part) and presents the test statistics for the Clayton copula (right part). The estimates of the copula parameters decrease with increasing aggregation level, which is in accordance with theoretical requirements. An exception is the estimate on level six, which might be caused by the limited database that includes only 47 observations. As expected, the yields between neighbouring countries, for example between Germany and France, show a high stochastic dependence. On the other hand, it is surprising that the stochastic dependence between India and Germany is higher than the stochastic dependence between India in Pakistan. That means that stochastic dependence is not a simple function of distance as implied by commonly used decorrelation functions.

Fig. 3 and Table 1 present the main results of our analysis, namely the distribution function for per hectare yields (Fig. 3(a)) and for the total wheat production (Fig. 3(b)). Fig. 3(a) and Fig. 3(b) refer to the yield level (mean yield with trend) and acreage at the end of the observation period, i.e. 2007. The interpretation of Fig. 3(a) is rather difficult since the distribution is derived by aggregating very heterogeneous regions. Thus, is helpful to use the outcome of the extreme year 2007 as a reference point. In 2007, a per hectare yield of 33.52 decitons was realized. According to Fig. 3(a) the stochastic yields fall below this level with a probability of approximately 7%. In other words, the harvest observed in 2007 was a rare event, but statistically it will recur on average every 15 years under constant conditions.

(a) Average yield (dt/hectare)



(b) Total yield (100 million tons)

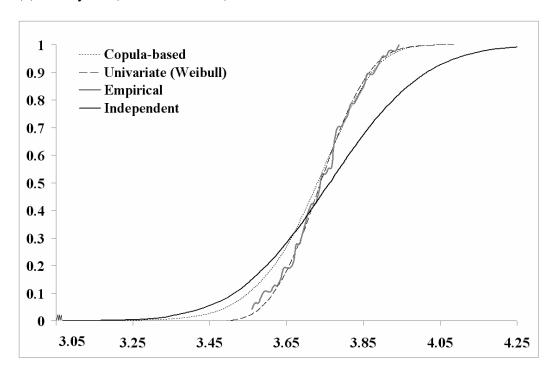


Fig. 3. Empirical and parametric distribution functions of global wheat production

We present two alternative estimates for the distribution function of global wheat production. First, a parametric distribution, namely a Weibull distribution, has been estimated. In contrast to the copula based approach, this distribution has been directly fitted to the aggregated production data. Moreover, an empirical (nonparametric) distribution function has been estimated. Though a direct estimation

of the distribution function is much simpler compared to the derivation from marginals and copulas, it has some obvious flaws. First, the estimation relies on only 47 observations and thus it will be plagued by low reliability, particularly in the tails. Second, the stochastic dependence structure of the various production regions is not revealed. Finally, it is questionable if different country-specific marginal yield distributions can be correctly represented by a single parametric distribution function. In light of these drawbacks, it is not surprising that the quantiles of the three distribution functions differ. Table 1 shows that the risk of global crop failures is underestimated by the direct estimation of the univariate distribution, though the means of all three distribution functions are almost equal. For example, the 1% quantile of the Weibull distribution for per hectare yield amounts to 33.37 dt/ha which is 1.28 dt/ha higher than the copula based estimate. The corresponding value of the empirical distribution cannot be uniquely determined due to its discrete nature.

Table 1. Parameters of the estimated distribution functions for wheat production (all regions for the year 2007)

| Quantile | Copula | -based | Univari (Weibu | | Empiric | al | Independent | | |
|----------|-----------------|----------|-------------------|-----------------|-----------------|----------|-----------------|----------|--|
| | AY ^a | TP^{b} | AY ^a | TP ^b | AY ^a | TP^{b} | AY ^a | TP^{b} | |
| 1% | 32.09 | 3.37 | 33.37 | 3.54 | n.a. | n.a. | 31.31 | 3.32 | |
| 5% | 33.22 | 3.50 | 33.84 | 3.58 | 33.64 | 3.55 | 32.47 | 3.44 | |
| 10% | 33.74 | 3.55 | 34.12 | 3.62 | 33.91 | 3.59 | 33.17 | 3.51 | |
| 50% | 35.47 | 3.61 | 35.29 | 3.74 | 35.29 | 3.74 | 35.52 | 3.76 | |
| Mean | 35.37 | 3.73 | 35.31 | 3.59 | 35.30 | 3.59 | 35.53 | 3.76 | |
| Variance | 1.47 | 0.0152 | 0.81 | 0.0084 | 0.86 | 0.0089 | 3.47 | 0.0389 | |

Notes: ^a Average yield in dt/ha. ^b Total production in 100 mill. tons.

To highlight the effect of global diversification of yield risk we present the results for the hypothetical scenario where yields are stochastically independent between all production regions. In this case, the distribution widens considerably and the variance increases by a factor of more than two (see Table 1 and Fig. 3). The effect of diversification is further elaborated in Fig. 4, which compares the variability of per hectare yields of different production regions. Apparently, the fluctuations of per hectare yields can be smoothed for most production regions by aggregation. This means that global trade can considerably reduce the shortfall risk for individual countries. It should be noted that a trade-off between average productivity and yield volatility exists. Intensive high tech production systems in Germany and France appears to be more sensitive to stochastic weather conditions compared to more extensive production systems in North America. Yield risk in India is similar to the global average, yet its average yields are relatively low.

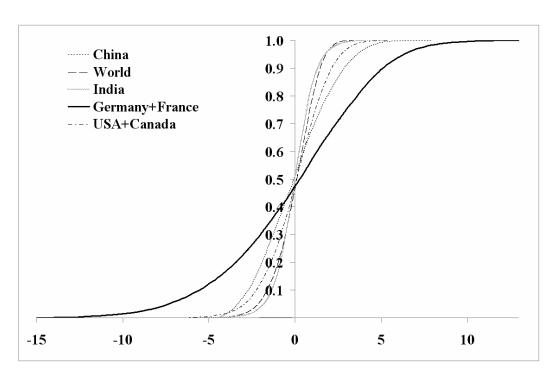


Fig. 4. Empirical and parametric distribution functions of wheat yields (deviations from mean in dt/hectare)

IV Conclusions

The main finding of the analysis is that yield risk for wheat as an important foodstuff can be reduced by pooling and aggregating production globally. This provides an argument for international agricultural trade, which is beyond deterministic welfare gains. It has been stated that price volatility for agricultural commodities in the EU increases due to the deregulation of markets (Britz and Heckelei, 2008). It should be stressed that the increase of price risk is a result of the abolishment of price protection measures and not a result of international trade. Based on our analysis we conjecture that price volatility in the EU would be even higher without a participation in international food markets. Nevertheless, global diversification cannot completely reduce yield risks. A shortfall, such as in 2007, is not a once in a lifetime event. From a statistical point of view, similar production conditions will occur every 15 years *ceteris paribus*.

However, a word of caution is necessary when interpreting our statistical findings. Our results do not allow for predictions about the scarcity of wheat (and hence price peaks) because the demand side was not taken into account. Clearly, the demand for wheat varies depending on population growth, income and the demand for biofuels. Furthermore, even our analysis of the supply side of the wheat market was incomplete since only eight countries were considered instead of all wheat producing countries. Moreover, the production of only a single year was analysed, ruling out time diversification. Usually food markets are short in supply if multiple poor harvests occur in a row and worldwide inventories are too small for smoothing this shortfall. This was the case in 2007/08. It should also be mentioned that our

probability statements refer to the yield level at the end of the observation period. An increase of the yield levels due to future technological progress has not been anticipated. Finally, one should recall that the production area depends on prices and thus is endogenous. For example, one could observe that farmers increased the acreage of wheat worldwide in 2008 as a response to the preceding price boom. Some of the aforementioned aspects could be handled in the framework of market equilibrium models. A linkage of existing market models with the presented stochastic analysis is a promising task for further research.

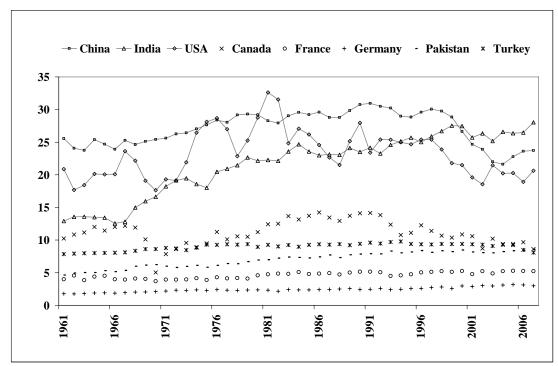
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Appendix



Source: FAO (2009)

Fig. A1. Harvest area of wheat (million hectares)

Table A1. Ranking of detrended per hectare yield of wheat (dt/hectare)

| Donle | Canada | | China | | France | | Germany | | India | | Pakistan | | Turkey | | USA | | Total | |
|-------|--------|------|-------|------|--------|------|---------|------|-------|------|----------|------|--------|------|-------|------|-------|------|
| Rank | Yield | Year | Yield | Year | Yield | Year | Yield | Year | Yield | Year | Yield | Year | Yield | Year | Yield | Year | Yield | Year |
| 1 | 6.13 | 1988 | 0.56 | 1977 | 14.85 | 2007 | 20.92 | 2003 | 4.66 | 2006 | 5.32 | 1987 | 8.68 | 1973 | 13.48 | 2002 | 9.39 | 2002 |
| 2 | 7.52 | 1961 | 1.67 | 2002 | 18.96 | 2003 | 21.35 | 2007 | 4.96 | 2005 | 5.62 | 1966 | 8.90 | 2007 | 15.05 | 2006 | 9.43 | 2007 |
| 3 | 8.97 | 2002 | 2.19 | 1980 | 20.73 | 2006 | 23.59 | 1976 | 5.03 | 2007 | 5.73 | 1984 | 8.97 | 1999 | 15.13 | 1989 | 10.13 | 2003 |
| 4 | 10.32 | 2001 | 2.34 | 2003 | 22.35 | 1976 | 24.80 | 2006 | 5.26 | 1980 | 5.74 | 1967 | 8.99 | 1994 | 15.13 | 1974 | 10.16 | 2006 |
| 5 | 10.85 | 1984 | 2.78 | 1973 | 23.36 | 1966 | 26.04 | 2002 | 5.50 | 1974 | 5.90 | 1994 | 9.08 | 1974 | 15.65 | 1991 | 10.20 | 1974 |
| 6 | 11.68 | 1989 | 2.85 | 2001 | 24.23 | 1961 | 26.75 | 1977 | 5.86 | 1964 | 6.31 | 1997 | 9.09 | 1961 | 15.70 | 1995 | 10.20 | 1977 |
| 7 | 11.86 | 1967 | 3.05 | 2000 | 24.26 | 2005 | 27.05 | 1966 | 5.88 | 1966 | 6.35 | 1996 | 9.28 | 1970 | 15.72 | 2007 | 10.36 | 2001 |
| 8 | 11.91 | 1974 | 3.48 | 1978 | 24.41 | 1975 | 27.28 | 1992 | 6.00 | 2003 | 6.42 | 2002 | 9.56 | 2001 | 15.77 | 1996 | 10.50 | 1961 |
| 9 | 12.19 | 1985 | 3.48 | 1981 | 24.71 | 2001 | 27.43 | 1989 | 6.00 | 1967 | 6.44 | 1978 | 9.58 | 2003 | 15.90 | 1967 | 10.66 | 1970 |
| 10 | 12.23 | 1979 | 3.55 | 1970 | 24.82 | 1963 | 27.44 | 1980 | 6.21 | 1977 | 6.56 | 1991 | 9.61 | 1968 | 16.07 | 1961 | 10.75 | 1980 |
| 11 | 12.73 | 2007 | 3.67 | 1974 | 25.12 | 1970 | 27.80 | 1970 | 6.56 | 2004 | 6.64 | 1985 | 9.67 | 1965 | 16.27 | 1988 | 10.80 | 2005 |
| 12 | 12.88 | 1980 | 3.81 | 1969 | 25.89 | 1977 | 27.80 | 1981 | 6.66 | 1978 | 6.67 | 1988 | 9.73 | 1964 | 16.46 | 1963 | 10.82 | 1988 |
| 13 | 12.92 | 1964 | 3.91 | 1971 | 27.75 | 1969 | 28.10 | 1965 | 6.68 | 1975 | 6.68 | 1999 | 9.94 | 2002 | 16.46 | 1966 | 10.87 | 1973 |
| 14 | 12.98 | 2003 | 4.01 | 1972 | 28.46 | 1971 | 28.48 | 1975 | 6.72 | 1987 | 6.74 | 2004 | 10.01 | 1995 | 16.56 | 1962 | 11.08 | 1978 |
| 15 | 13.07 | 1997 | 4.02 | 2005 | 28.60 | 1983 | 28.49 | 2005 | 6.73 | 1981 | 6.79 | 1990 | 10.04 | 1989 | 16.61 | 1964 | 11.17 | 1964 |
| 16 | 13.26 | 1968 | 4.07 | 1975 | 28.68 | 1986 | 28.57 | 1961 | 6.86 | 1982 | 6.82 | 1993 | 10.13 | 1969 | 16.68 | 1976 | 11.22 | 1975 |
| 17 | 13.35 | 1987 | 4.28 | 1998 | 28.69 | 1964 | 28.81 | 1972 | 6.93 | 1976 | 6.88 | 1971 | 10.29 | 1997 | 16.69 | 1977 | 11.28 | 1994 |
| 18 | 13.75 | 1994 | 4.55 | 1976 | 28.74 | 1987 | 28.87 | 1979 | 6.97 | 1973 | 7.05 | 1965 | 10.38 | 1996 | 16.87 | 1965 | 11.29 | 1967 |
| 19 | 13.96 | 1962 | 4.59 | 1991 | 28.77 | 1965 | 28.99 | 1983 | 6.97 | 1963 | 7.11 | 1964 | 10.55 | 1962 | 16.95 | 1978 | 11.30 | 1989 |
| 20 | 14.11 | 1998 | 4.66 | 2004 | 28.96 | 1997 | 30.38 | 1982 | 7.07 | 1979 | 7.28 | 2003 | 10.69 | 1966 | 17.01 | 1986 | 11.51 | 1969 |
| 21 | 14.14 | 1973 | 4.99 | 1968 | 29.32 | 1979 | 30.46 | 1969 | 7.10 | 1988 | 7.34 | 1974 | 10.85 | 1967 | 17.14 | 1975 | 11.53 | 1976 |
| 22 | 14.29 | 1972 | 5.21 | 1994 | 29.52 | 1981 | 30.47 | 1987 | 7.15 | 1998 | 7.35 | 1982 | 11.01 | 2004 | 17.15 | 1994 | 11.54 | 1995 |
| : | : | : | : | : | : | ÷ | : | : | : | : | : | : | : | : | : | : | : | ÷ |
| 45 | 17.34 | 2005 | 8.65 | 1983 | 35.74 | 1991 | 36.23 | 1991 | 9.12 | 2000 | 8.93 | 1986 | 13.82 | 1976 | 20.37 | 1971 | 13.09 | 1986 |
| 46 | 17.54 | 1976 | 9.32 | 1997 | 37.73 | 1998 | 36.60 | 2004 | 9.32 | 1995 | 8.98 | 2007 | 13.89 | 1979 | 20.41 | 1984 | 13.29 | 1983 |
| 47 | 17.60 | 1966 | 9.44 | 1984 | 40.88 | 1984 | 36.86 | 2001 | 9.56 | 1997 | 9.50 | 2000 | 14.59 | 1988 | 21.09 | 1983 | 13.60 | 1984 |

Source: FAO (2009)

Table A2. Marginal distributions of wheat yield (dt/hectare)

| Country | Marginal distribution | Parameters | | χ^2 test-statistics | p -value | |
|----------|-----------------------|------------|---------|--------------------------|----------|--|
| Canada | Logistio | location | 0.0243 | 2.1910 | 0.0495 | |
| Canada | Logistic | scale | 0.1382 | 2.1910 | 0.9485 | |
| | | shape | 3.4396 | | | |
| China | Weibull | scale | 0.6694 | 4.5740 | 0.7117 | |
| | | shift | -0.6022 | | | |
| Germany | Normal | mean | 0.0000 | 2.8700 | 0.8966 | |
| | Normal | SD | 0.3895 | 2.8700 | | |
| France | Normal | mean | 0.0000 | 8.6600 | 0.2780 | |
| | Normai | SD | 0.4975 | 8.0000 | 0.2700 | |
| India | Logistio | location | 0.0035 | 3.5530 | 0.8296 | |
| | Logistic | scale | 0.0690 | 3.3330 | | |
| Pakistan | | shape | 3.4666 | | | |
| | Weibull | scale | 0.3160 | 3.8940 | 0.7919 | |
| | | shift | -0.2842 | | | |
| Turkey | | shape | 1.7138 | | 0.6288 | |
| | Weibull | scale | 0.3280 | 5.2550 | | |
| | | shift | -0.2934 | | | |
| USA | | shape | 3.7793 | | | |
| | Weibull | scale | 0.6087 | 4.5740 | 0.7117 | |
| | | shift | -0.5498 | | | |

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