

A Service of



Leibniz-Informationszentrum Wirtschaft Leibniz Information Centre

Jeitschko, Thomas D.; Normann, Hans-Theo

Working Paper

Signaling in deterministic and stochastic settings

DICE Discussion Paper, No. 35

Provided in Cooperation with:

Düsseldorf Institute for Competition Economics (DICE), Heinrich Heine University Düsseldorf

Suggested Citation: Jeitschko, Thomas D.; Normann, Hans-Theo (2011): Signaling in deterministic and stochastic settings, DICE Discussion Paper, No. 35, ISBN 978-3-86304-034-5, Heinrich Heine University Düsseldorf, Düsseldorf Institute for Competition Economics (DICE), Düsseldorf

This Version is available at: https://hdl.handle.net/10419/51561

Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.





DISCUSSION PAPER

No 35

Signaling in Deterministic and Stochastic Settings

Thomas D. Jeitschko, Hans-Theo Normann

November 2011



IMPRINT

DICE DISCUSSION PAPER

Published by

Heinrich-Heine-Universität Düsseldorf, Department of Economics, Düsseldorf Institute for Competition Economics (DICE), Universitätsstraße 1, 40225 Düsseldorf, Germany

Editor:

Prof. Dr. Hans-Theo Normann

Düsseldorf Institute for Competition Economics (DICE)

Phone: +49(0) 211-81-15125, e-mail: normann@dice.uni-duesseldorf.de

DICE DISCUSSION PAPER

All rights reserved. Düsseldorf, Germany, 2011

ISSN 2190-9938 (online) - ISBN 978-3-86304-034-5

The working papers published in the Series constitute work in progress circulated to stimulate discussion and critical comments. Views expressed represent exclusively the authors' own opinions and do not necessarily reflect those of the editor.

Signaling in Deterministic and Stochastic Settings*

Thomas D. Jeitschko[†] Department of Economics Michigan State University HANS-THEO NORMANN[‡]
DICE
Düsseldorf University

November 1, 2011

Abstract

We contrast a standard deterministic signaling game with one where the signal-generating mechanism is stochastic. With stochastic signals a unique equilibrium emerges that involves separation and has intuitive comparative-static properties as the degree of signaling depends on the prior type distribution. With deterministic signals both pooling and separating configurations occur. Laboratory data support the theory: In the stochastic variant, there is more signaling behavior than with deterministic signals, and less frequent types distort their signals relatively more. Moreover, the degree of congruence between equilibrium and subject behavior is greater in stochastic settings compared to deterministic treatments.

Keywords: experiments, learning, noise, signaling, stochastic environments.

JEL classification: C7, C9, D8

^{*}The views expressed in this paper are those of the authors and are not purported to reflect the views of the U.S. Department of Justice. We would like to thank Tony Creane, Johannes Hörner, John Kagel, audience members at Seminars at the University of York, Royal Holloway College (University of London), University of Frankfurt, and Max-Planck-Institute Jena, DIW Berlin, Wissenschaftszentrum Berlin; as well as participants at the Midwest Economic Theory Meetings at Michigan State University, the Midwest Mathematical Economics Meetings at Ohio State University, and the Economic Science Association Meetings in Innsbruck for comments. We are grateful to the Max-Planck Institute for Research on Collective Goods (Bonn) for financial support.

[†]Present Address: Antitrust Division, U.S. Department of Justice, Washington, D.C. 20530, U.S.A., thomas.jeitschko@usdoj.gov; Phone: +1-202-532-4826; Fax.: +1-202-514-8862

 $^{^{\}ddagger}$ Present Address: Duesseldorf Institute for Competition Economics, (DICE), 40225 Düsseldorf, Germany, normann@dice.uni-duesseldorf.de

1 Introduction

Since the seminal work by Spence (1973, 1974), signaling—that is, the costly undertaking of actions in order to either convey or hide private information from others—has become the focus of much research within and beyond economics. In addition to the original work by Spence focusing on education, applications and variations have been seen in industrial organization (for example, entry deterrence through limit pricing (Milgrom and Roberts, 1982) or signaling of product quality (Milgrom and Roberts, 1986; Bagwell and Riordan, 1991)), monetary policy (Backus and Driffill, 1985) and the economics of litigation (Reinganum and Wilde, 1984), to name just a few; and outside of economics insights from signaling have found applications in biology (for example, Zahavi, 1975) and anthropology (Sosis and Ruffle, 2003).

Although these models greatly differ in their approaches and applications, there is one thing they have in common. In the vast majority of signaling games, the signal-generating mechanism is deterministic. The sender is able to perfectly control the signal, and the receiver precisely observes the signal that is sent. The receiver has no trouble interpreting the signal and can therefore correctly infer its cost. That is, there are no inaccuracies in sending or receiving the signal.

Even though standard, the assumption of deterministic signaling is not always plausible. For illustrative purposes, consider a Spence-type education-signaling game in which students signal their (unobservable) ability to potential employers through their choice of an (observable) level of education attained, and suppose that the signal that employers observe is a student's grade-point-average. Problems at the signal-generating stage may occur if, for instance, a student has a "bad day" (or a "good day," for that matter) during an exam. In this case, the sender is only imperfectly able to control the signal. Problems at the receiving end may occur if the employer cannot assess whether the classes taken by the student were particularly easy or hard. Similarly, education will also be a noisy signal for the receiver in a scenario where education is measured by the observable number of years of school attendance but where the education choice is affected by an intrinsic unobservable (dis)utility for education. As the receiver will be unaware of the utility of education, perfect inference of

the cost of the signal is no longer possible. In these examples, the signal-generating process is, in effect, stochastic.

Matthews and Mirman (1983) were the first to study such a stochastic setting. They consider a variation of the limit-pricing game introduced by Milgrom and Roberts (1982). In particular, they suppose that the incumbent monopolist chooses an unobservable output level before stochastic demand for the product is realized. This results in an observable but stochastic price which only imperfectly reveals the underlying output choice and hence the type of the incumbent. Another study, Hertzendorf (1993), adds noise to the Milgrom and Roberts (1986) advertising model. Hertzendorf argues that the recipients of advertising signals will only rarely be informed about the exact advertising budget of a company. Instead, people receive a noisy signal of the budget when observing advertisements.

Technically, what happens in stochastic signaling games is that any signal realization is consistent with any action taken by any type whenever the noise perturbing the signal has full support. Thus, signals are no longer invertible and therefore do not allow complete information about the underlying actions of the sender, even when agents of different types undertake different actions in equilibrium (that is, a separating equilibrium). The observable signals only allow incomplete inferences about the sender's true (unobservable) type. In other words, Bayesian updating leads to incremental information dissemination when agents undertake distinct actions, rather than immediate and complete learning.

A main result in noisy signaling games is that often a unique separating equilibrium emerges (Matthews and Mirman, 1983), instead of the large number of possible equilibrium configurations that emerge without noise and that differ quantitatively and qualitatively in deterministic games.¹ A second significant deviation of the equilibrium in noisy signaling games compared to deterministic versions is that the former admit a much richer comparative-statics analysis. In particular, in deterministic games actions are generally independent of the underlying distribution of types within a class of equilibrium configurations so that there are no meaningful comparative statics within a class with respect to prior beliefs. In contrast, in a noisy signaling model the unique equilibrium is sensitive to variations

¹Carlsson and Dasgupta (1997) use the stochastic game to suggest an equilibrium-selection criterion for deterministic signaling games when noise vanishes—demonstrating conditions for a unique noise-proof equilibrium to exist in deterministic games.

in the underlying distributions, which yields smooth comparative statics with respect to prior beliefs.

In the present paper we consider a sender-receiver signaling game similar to Matthews and Mirman (1983) and Carlsson and Dasgupta (1997) in which a sender chooses from a continuum of actions while the receiver only has two actions. However, in contrast to the former, we follow the latter in assuming a binary type-space rather than a continuum of types. We compare the equilibrium configurations in the deterministic and the stochastic signal-generating mechanisms and provide experimental data for this setup.

The theoretical analysis shows that there are many perfect Bayesian equilibrium constellations in the variant without noise. After the application of equilibrium refinements, one obtains a unique perfect Bayesian equilibrium. Depending on the prior, this unique equilibrium is either pooling or separating. For the stochastic case, even without resorting to refinements, one obtains a unique equilibrium which is separating. Thus, a first hypothesis (testable in the experiments) is that for certain priors pooling behavior should occur without noise as opposed to separating behavior with noise. A second implication of the noisy signaling framework is that players should always signal, that is, always choose actions that differ from their myopically optimal actions. This is in contrast to the deterministic case in which one type always chooses the myopic best action and does not engage in signaling.² Often, the impact of noise on players' decisions is ambiguous and depends on the prior beliefs and players' types. This sometimes leads to intriguing comparative-statics predictions that can be tested experimentally. For example, it is the less frequent type who chooses a message that is more strongly distorted away from the sender's myopic best action.

We complement the theoretical analysis with experimental data. Experimental research on signaling games has proven useful is assessing the relevance of the theory. For early contributions see for example Miller and Plott (1985), Brandts and Holt (1992), Potters and van Winden (1996) and Cooper, Garvin and Kagel (1997a, 1997b). More recent studies include Cooper and Kagel (2005, 2009) and Kübler et al. (2008). The case for studying a noisy signaling game seems particularly strong given the various propositions that differ

²In a separating equilibrium the "low" type chooses his myopic first-best action, and in a (refined) pooling equilibrium it is the "high" type who chooses his myopic first-best action.

markedly from the deterministic environment.

In our experiments we study treatments with two different priors (a "high" and "low" prior belief for the sender's type). For each of the two priors, we implement a deterministic and a noisy variant. We find that, as in previous experiments, our sessions do not completely converge to equilibrium.³ Nevertheless, our experimental results provide some clear confirmation of the theory. Regarding the key variables of our experiment (sender and receiver actions), the theory has predictive power. In addition, the hypotheses mentioned in the previous paragraph are supported by the data. Thus, for the high prior, there is more pooling behavior in the deterministic variant; we find indeed that there is significantly more signaling with noise. While there is no support for the hypothesis that the less frequent type signals more,⁴ in relative terms, this prediction is confirmed. Overall, the empirical data are closer to their equilibrium counterparts in the stochastic variant compared to the deterministic setting. We attribute this to the fact that noise in the model is similar to imperfect play by subjects leading to a greater congruence between equilibrium observations and subject behavior.

While our study is among the first experiments to analyze a noisy signaling game, de Haan, Offerman and Sloof (2011) also construct a model with noisy signals and run experiments. Their model differs from ours in that a pooling equilibrium may exist with noise, because the two sender types have the same first-best preferred action and the marginal cost of signaling is strictly positive. Their main focus is on varying levels of noise, whereas we examine how prior beliefs affect play in noisy and deterministic games. In particular, they find in their data that signaling expenditures increase with the level of noise. For low levels of noise, a separating equilibrium ceases to exist, however, subjects still coordinate on separation in the experiment.

 $^{^3}$ See Cooper and Kagel (2005, 2009), who convincingly argue that previous experimental signaling games do not immediately converge. Without repetitions or other mechanisms facilitating learning, equilibrium play emerges only gradually, if at all. They show that teams play dramatically more strategically than individuals.

⁴The reason for this failure is that, as is common in signaling-game experiments, the "low" types are much more prone to signaling than are the "high" types.

2 The Model and Equilibrium Behavior

There are two players who act in sequence. The first player to move is referred to as the sender (of male gender), and the second player is referred to as the receiver (of female gender). Before play begins, nature draws the sender's type. With probability $\rho_0 \in (0,1)$ the sender is the "high" type, denoted by \bar{t} and with complementary probability of $1 - \rho_0$ he is the "low" type denoted by \underline{t} ($<\bar{t}$).

The sender observes his type and then chooses a hidden/unobservable action a that affects his payoffs both directly and indirectly. The indirect effect comes about because the unobservable action a generates a (possibly noisy) signal s that triggers a payoff-relevant reaction r by the other player, the receiver. Specifically, the sender's (type-dependent) payoff is given by

$$u(a,r) = U - c(a-t)^2 + W r(s), \qquad t \in \{\underline{t}, \overline{t}\},$$

$$(1)$$

where U is a normalization parameter, $r \in \{0, 1\}$ is the receiver's response (based on the observed signal s), c > 0 is a scaling parameter, and W > 0 is a windfall that the sender obtains when r = 1.

The agent's most preferred (myopic best) action is thus a=t, and deviations from this (that is, $a \neq t$) entail signaling. Signaling may be undertaken in order to induce the receiver to take a response of r=1, rather than a response of r=0, as r=1 results in the agent obtaining the added windfall payment of W. The sender's type-dependent payoff as a function of the action is depicted in Figure 1, where, in order to observe signaling behavior in the equilibrium of the deterministic setting, we have restricted parameters such that $\bar{t} - \underline{t} < \sqrt{W/c}$.

The receiver does not know the type of the sender. Her prior beliefs are captured by ρ_0 . These prior beliefs are updated to ρ_1 upon observing the signal s on the basis of the relationship between the sender's actions a and the resulting signal s, given beliefs about how a sender's type t determines his action.

The receiver's payoffs are affected by her response $r \in \{0,1\}$ and are given by

$$v(r,t) = \begin{cases} V + B r, & \text{if } t = \overline{t} \\ V + B (1 - r), & \text{if } t = \underline{t}, \end{cases}$$
 (2)

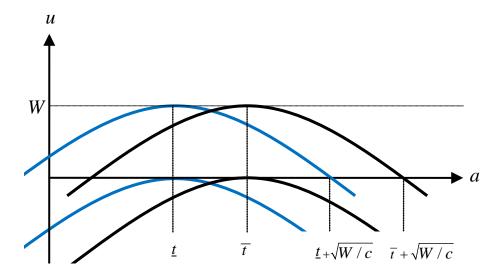


Figure 1: Sender's Payoff (with and without W; low type, left \square ; high type, right \square)

where V is some base-utility and B > 0 is a bonus that increases the weight of the decision variable r on the inference that the receiver has drawn about the agent's type. Given posterior belief $\rho_1(s)$, the receiver chooses $r \in \{0,1\}$ in order to maximize

$$Ev(r) = V + B \left[\rho_1 r + (1 - \rho_1)(1 - r) \right]. \tag{3}$$

Hence, the receiver responds with r = 0 whenever $\rho_1 \leq 1/2$, and chooses the response r = 1 otherwise.

We analyze the receiver's decision with switching strategies. That is, the receiver's response is determined by a critical threshold value of the signal \tilde{s} for which

$$r = \begin{cases} 1 & \text{if } s \ge \tilde{s} \\ 0 & \text{if } s < \tilde{s}. \end{cases}$$
 (4)

Using a switching point makes sense if the receiver thinks facing the higher type is more likely as the signal increases. This indeed occurs in the unique equilibrium of the noisy game, when noise has the monotone-likelihood-ratio property. The deterministic game can also be analyzed with switching strategies, although the game can also be studied without them, in which case the results change only marginally (as discussed below).

It is worth mentioning that compared to the model in Matthews and Mirman (1983) the sender's payoff itself is not subjected to noise in our model, only the signal is. Our

model is similar to Carlsson and Dasgupta (1997), but differs in that the receiver's payoff is strictly increasing in properly identifying the sender's type. That is, the receiver obtains B whenever she correctly identifies the sender's type. This is in contrast to many signaling games in which one response can be viewed as a risk-free alternative in that it gives a constant payoff independent of the sender's type (for example, not hiring the worker in Spence's model leads to a reservation payoff that is independent of the true type of the job applicant). Our setup corresponds to a scenario where a manager has to assign a worker to specific tasks within the firm (one requiring higher skills and therefore yielding greater compensation), and where the worker's subsequent performance correctly reveals his or her type in either case and thus may serve as a basis for the payment of the manager.

In summary, the sequence of events is:

- 1. after nature chooses the sender's hidden type $t \in \{\bar{t}, \underline{t}\}$ with $\Pr(t = \bar{t}) = \rho_0$, the sender chooses an unobservable action, denoted by \underline{a} for \underline{t} , and \overline{a} for \overline{t} ;
- 2. the unobservable action a generates the observable signal s, which the receiver uses to update her beliefs about the sender's type upon which she chooses a response $r \in \{0, 1\}$;
- 3. both players' payoffs are realized according to Equations (1) and (2).

The relationship between the sender's action a and the observed signal s depends on whether the signal-generating technology is deterministic or noisy. We analyze the two distinct environments in turn, concentrating on perfect Bayesian equilibrium solutions. In the deterministic setting the set of solutions is further refined, whereas in the noisy setting the perfect Bayesian equilibrium is unique and therefore does not require further refinement arguments.

2.1 Equilibrium with Deterministic Signals

In deterministic models the signal allows a perfect inference about the actions that were taken (that is, the signal-generating mechanism is invertible). Indeed, this is informationally equivalent to a setting in which the action itself is observable. Thus, we consider them to

be identical,

$$s \equiv a. \tag{5}$$

Restricting attention to pure-strategy equilibrium configurations, the action taken by the sender is either type-dependent and distinct for the two types (a separating equilibrium), or is independent of his type (a pooling equilibrium).

Separating Configurations. In a separating equilibrium the receiver infers the sender's type: the low type faces the unfavorable response of r=0, whereas the high type achieves the favorable response of r=1. As \underline{t} faces the unfavorable response he chooses his myopic first best action, that is, $\underline{a}^* = \underline{t}$, since any other action yields a lower payoff when his type is revealed. (See Figure 2 for illustration.) Incentive compatibility for the low type requires that he does not find it advantageous to trigger the favorable response of r=1 by choosing the high type's equilibrium action. This implies that $\overline{a}^* \notin \left[\underline{t} - \sqrt{W/c}, \ \underline{t} + \sqrt{W/c}\right]$. Moreover, individual rationality for the high type dictates that he does not prefer to accept the unfavorable response r=0 over taking the equilibrium action in order to obtain the favorable response of r=1. That is, $\overline{a}^* \in \left[\overline{t} - \sqrt{W/c}, \ \overline{t} + \sqrt{W/c}\right]$. Taking these considerations together yields a continuum of separating equilibrium constellations $\underline{a}^* = \underline{t}$ and $\overline{a}^* \in \left[\underline{t} + \sqrt{W/c}, \ \overline{t} + \sqrt{W/c}\right]$, with switching point $\tilde{s}^* = \overline{a}^*$.

Using Cho and Kreps' (1987) intuitive criterion, any separating equilibrium with $\tilde{s}^* > \underline{t} + \sqrt{W/c}$ can be upset. Specifically, suppose $\tilde{s}^* = \overline{a}^* > \underline{t} + \sqrt{W/c}$ and consider an out-of-equilibrium action $a \in \left[\underline{t} + \sqrt{W/c}, \tilde{s}^*\right]$. Such an action is dominated for \underline{t} . Even if the receiver responded with r = 1 to such an action, \underline{t} would still be strictly better off choosing $a = \underline{t}$ and getting the r = 0 response. Thus, the receiver should believe $\rho_1 = 1$ after such a deviation and then \overline{t} can profitably deviate to $\overline{a}' = \underline{t} + \sqrt{W/c}$. This leaves a unique separating equilibrium, the least-cost separating equilibrium, with $\underline{a}^* = \underline{t}$, $\overline{a}^* = \underline{t} + \sqrt{W/c}$ and $\tilde{s}^* = \overline{a}^*$.

Pooling Configurations. Note first that when $\rho_0 < 1/2$ there cannot be a pooling equilibrium. If types pool their actions with $\rho_0 < 1/2$, the receiver chooses the unfavorable response

⁵Note that, because we assume a switching point, all actions $a > \tilde{s}^* = \overline{a}^*$ trigger r = 1. Without a switching-point strategy, these signals may induce the response r = 0. However, neither type has an incentive to choose $a > \tilde{s}^*$, because this reduces the sender's payoff without affecting the receiver. Hence, the set of separating equilibrium actions is the same with and without a switching-point strategy.

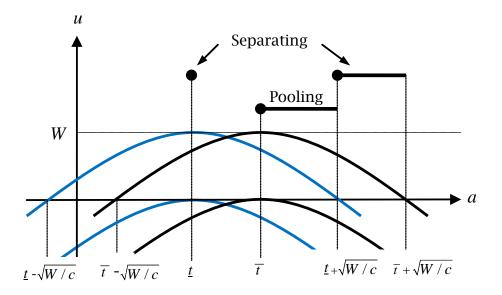


Figure 2: Separating and Pooling Equilibrium Configurations

of r=0. But then both types are no worse off by choosing their myopic best actions, which precludes them taking the same action so that a pooling equilibrium does not exist. With $\rho_0 \geq 1/2$ and pooling, the receiver chooses the favorable response of r=1, that is, both types get W in equilibrium. Because the receiver employs a switching point, there does not exist a pooling equilibrium with $\tilde{s}^* = \underline{a}^* = \overline{a}^* < \overline{t}$ as \overline{t} could profitably deviate to the myopically optimal $a=\overline{t}$ and still trigger r=1. There is a continuum of equilibrium pooling configurations with $\underline{a}^* = \overline{a}^* \in \left[\overline{t}, \ \underline{t} + \sqrt{W/c}\right]$ (having assumed that $\overline{t} - \underline{t} < \sqrt{W/c}$).

The equilibrium pooling configurations are strictly Pareto-rankable with lower actions strictly preferred by both types of sender. For that reason, the intuitive criterion does not refine the set of equilibrium configurations. (Whenever $\underline{a}^* = \overline{a}^* > \overline{t}$, both types would be better off choosing an out-of-equilibrium action of $a^* = \overline{t}$ if this triggered r = 1, thus, the out-of-equilibrium action is not equilibrium dominated and hence configurations with $a^* > \overline{t}$ survive.) However, one can select the efficient pooling equilibrium by applying Grossman and Perry's (1986) perfect sequential equilibrium or Mailath $et\ al$.'s (1993) undefeated equi-

⁶Analyzing the game without switching strategies, the set of equilibrium pooling configurations is larger, namely $\underline{a}^* = \overline{a}^* \in \left[\overline{t} - \sqrt{W/c}, \ \underline{t} + \sqrt{W/c}\right]$, which includes actions below the low-type's most preferred action. However, these additional configurations do not pass the intuitive criterion. We also note already at this point that subjects of either type in the experiment only rarely chose actions $a \in (\underline{t}, \overline{t})$ in the deterministic framework.

librium. Thus we obtain a unique pooling equilibrium (which is Pareto efficient) in which $\underline{a}^* = \overline{a}^* = \overline{t}.^7$

Note finally that when $\rho \geq 1/2$ the efficient pooling equilibrium with $\underline{a}^* = \overline{a}^* = \overline{t}$ also Pareto dominates the least-cost separating equilibrium from the sender's point of view. Specifically, in this pooling equilibrium \overline{t} has no incentive to separate himself by choosing some action $a > \overline{t}$ since \overline{t} already gets the maximum payoff in the pooling equilibrium. Applying the same equilibrium selection arguments as in footnote 7 leaves the efficient pooling equilibrium as the unique equilibrium if $\rho_0 \geq 1/2$. If p < 1/2, the least-cost separating equilibrium does survive the application of these additional refinements.

We summarize the refined equilibrium constellation for the deterministic case in Proposition 1 and Table 1.

Proposition 1 (Equilibrium in Deterministic Settings) If $\rho_0 < 1/2$, the unique perfect Bayesian equilibrium surviving equilibrium refinements is the least-cost separating equilibrium with $\underline{a}^* = \underline{t}$ and $\overline{a}^* = \underline{t} + \sqrt{W/c}$. If $\rho_0 \geq 1/2$, the unique perfect Bayesian equilibrium surviving equilibrium refinements is the pooling equilibrium with $a^* = \overline{t}$.

The predictions in Proposition 1 are based on the application of equilibrium refinements. The literature on the relevance of refinements in experiments (starting with Brandts and Holt, 1992, 1993) has not been conclusive and has not always found support for refinements. Thus, ex ante, it appears demanding to consider the above theoretical results as benchmarks for an experiment. Note, however, that in our setting the implications of the refinements are rather modest. They merely give preference to the least-cost separating equilibrium over Pareto inferior separating equilibria, and they select the Pareto efficient pooling equilibrium. The experimental results show that there is support for Proposition 1.

⁷Perfect sequential equilibrium (Grossman and Perry, 1986) requires that, for each out-of-equilibrium message, the receiver hypothesizes that the message was sent by some set of types of the sender and revises her beliefs conditional accordingly. If precisely the set of hypothesized players best responds by choosing the out-of-equilibrium message, the original equilibrium is upset. A similar rationale underlies Mailath *et al.*'s (1993) undefeated equilibrium except that the out-of-equilibrium message must be chosen with positive weight by some sender type in another perfect Bayesian equilibrium. To see the application of these refinements to our game, consider a pooling equilibrium with $\underline{a}^* = \overline{a}^* > \overline{t}$ (given $\rho_0 > 1/2$). Now assume an out-of-equilibrium action $a \in [\overline{t}, a^*)$. This is profitable for both \underline{t} and \overline{t} whenever the response is r = 1. While the equilibrium requires $\rho_1 = 0$ after the deviation, the refinements imply $\rho_1 = \rho_0 > 1/2$ since the deviation is profitable for both types provided r = 1 and both types have an incentive to deviate.

Prior Beliefs $\rho_0<1/2 \qquad \rho_0\geq 1/2$ Pooling $- \qquad \underline{a}^*=\overline{a}^*=\overline{t}$ Equilibrium Type $\underline{a}^*=\underline{t} \qquad -$ Separating $\overline{a}^*=\underline{t}+\sqrt{W/c} \qquad -$

Table 1: Refined Equilibrium Configurations with Deterministic Signals

2.2 Equilibrium with Noisy Signals

Consider now the case where the signal that the receiver observes is not invertible and therefore does not reveal the agent's action perfectly. As indicated in the introduction such noise may result because the sender does not have perfect control over the signal, or it may be that the receiver cannot clearly observe the action. In either case, the receiver must use statistical inference in order to update her beliefs about the action taken, and thus learn about the agent's type.

After we formalize the signal-generating mechanism, we consider the receiver's best response conditioned on her conjectures about the actions taken by the two types of sender. In anticipation of this response the optimal action of the sender is derived. The equilibrium is found by restricting beliefs of the receiver so that they are consistent with the actions taken by the sender.

The signal-generating mechanism is given by

$$s \equiv a + \epsilon, \tag{6}$$

where ϵ is an unobservable noise term that is distributed independently of a (that is, homoskedastically) according to a normal distribution (which has the monotone likelihood ratio property) with zero-mean and standard deviation of σ , i.e., $\epsilon \sim N(0, \sigma^2), \forall a$. We assume that the noise term is realized only after the sender has taken the action a. Thus, the sender

is unable to adjust his actions in light of the realization of noise and, hence,

$$s \sim N(a, \sigma^2).$$

We consider first the receiver's inference problem and best response. Let \underline{a}^c and \overline{a}^c , with $\underline{a}^c \neq \overline{a}^c$, denote the receiver's conjectures about which (unobservable) type-dependent actions are taken. As before ρ_1 denotes updated (posterior) beliefs. That is, ρ_1 is the receiver's subjective probability-assessment that the sender is a \overline{t} -type sender, conditional upon having observed the signal s, given the conjectures \overline{a}^c and \underline{a}^c .

Then, with $f(s|a) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(s-a)^2}{2\sigma^2}\right)$ denoting the normal density of the distribution of s with mean a, Bayes' Rule yields:

$$\rho_1(s|\underline{a}^c, \overline{a}^c) = \frac{\rho_0 f(s|a = \overline{a}^c)}{\rho_0 f(s|a = \overline{a}^c) + (1 - \rho_0) f(s|a = \underline{a}^c)}$$

$$= \frac{LR_0}{LR_0 + \exp\left(\frac{(\overline{a}^c - \underline{a}^c)(\overline{a}^c + \underline{a}^c - 2s)}{2\sigma^2}\right)},$$
(7)

where LR_0 denotes the likelihood ratio of prior beliefs, $\rho_0/(1-\rho_0)$.

Combining (7) with (3) yields the receiver's best response.

Lemma 1 (Best Response) Given the conjecture \overline{a}^c and \underline{a}^c , the receiver's best response is determined by a critical threshold value of s denoted by \tilde{s}^c . That is, $r^* = 1$ if and only if $s \geq \tilde{s}^c$ with

$$\tilde{s}^c = \frac{\overline{a}^c + \underline{a}^c}{2} - \ln(LR_0) \frac{\sigma^2}{\overline{a}^c - a^c}.$$

Notice that \tilde{s}^c has several intuitive properties. If $\rho_0 = 1/2$, then $\ln(LR_0) = 0$ and the critical threshold is simply the average of the conjectured actions of the two types of agent. As prior beliefs become strongly biased in favor of one or the other type of sender (that is, $\ln(LR_0) \to \pm \infty$), only extreme signals will lead to updating sufficiently strong to revise prior beliefs to change a response. Similarly, as the sender chooses a similar action regardless of type (that is, we approach a pooling equilibrium, so to speak, and $\bar{a} \approx \underline{a}$), again only extreme signals trigger a response by the receiver that differs from what prior beliefs indicate. Finally, the same holds true for increases in the variance of the noise σ^2 so that, for given beliefs about the senders' actions, a noisier environment leads to less updating.

Having characterized the receiver's learning and response, consider now the sender's optimal actions. Recall that the receiver's choice of r affects the sender's payoff (see (1)). Since the choice of r is governed by ρ_1 , which is a function of the sender's action a (see (7)), it is clear that the sender accounts for how a affects r. Since r is increasing in s, given \overline{a}^c and \underline{a}^c , both types of sender have an incentive to increase s. That is, both types would like to be identified as being a high type: the high type wants to set himself apart, and the low type wants to deceive.

Thus, given \overline{a}^c and \underline{a}^c (the sender's action affects only the signal s, but cannot affect the receiver's conjectures) and given Lemma 1, the sender's (type-dependent) objective is to choose a in order to maximize the value of Equation (1), viz.,

$$U - c(a - t)^{2} + W \Pr\left(s \ge \tilde{s}^{c} | a\right) =$$

$$U - c(a - t)^{2} + W \int_{\tilde{s}^{c}}^{\infty} \frac{1}{\sigma \sqrt{2\pi}} \exp\left(-\frac{(s - a)^{2}}{2\sigma^{2}}\right) ds, \qquad t \in \left\{\underline{t}, \overline{t}\right\}, \tag{8}$$

where \tilde{s}^c is given in Lemma 1. The (type-dependent) first-order condition is given by

$$2c(a-t) + \frac{W}{\sigma\sqrt{2\pi}} \int_{\bar{s}c}^{\infty} \frac{s-a}{\sigma^2} \exp\left(-\frac{(s-a)^2}{2\sigma^2}\right) ds = 0, \qquad t \in \{\underline{t}, \overline{t}\}.$$
 (9)

Hence,

Lemma 2 (Best Action) Given the receiver's response conditioned on her conjecture \overline{a}^c and \underline{a}^c , the sender's best action is implied by

$$2c(a-t) = \frac{W}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(\tilde{s}^c - a)^2}{2\sigma^2}\right), \qquad t \in \{\underline{t}, \overline{t}\},$$

where \tilde{s}^c is as before, given in Lemma 1.

Proof. Let $g(s,a) = -\frac{(s-a)^2}{2\sigma^2}$. Then $g_a = -g_s = \frac{s-a}{\sigma}$. Hence the term under the integral in the FOC (9) is $-g_s e^{g(s,a)}$ and therefore the integral itself is $e^{g(\tilde{s}^c,a)}$, since $\lim_{s\to\infty} e^{g(s,a)} = 0$.

Notice that Lemma 2 implies that both types of sender engage in signaling (that is, $a^* > t$ for both types), independent of the receiver's conjectures about the actions taken, provided $\overline{a}^c \neq \underline{a}^c$. This is a reflection of the fact that the marginal gain from signaling is positive, and hence the sender is willing to trade-off deviations of a from t in order to obtain the positive

marginal signaling gains. Specifically, the marginal cost of signaling is zero at t, whereas the marginal gains are strictly positive. Thus, in the noisy environment, players always signal.

In equilibrium the receiver is aware of the sender's desire to manipulate the flow of information. That is, she is aware that the high type will choose an action in the hopes of distinguishing himself from the low type and, similarly, that the low type will attempt to mimic the high type. As a consequence, she is aware of Lemma 2. This leads to consistent beliefs in which $\bar{a}^c = \bar{a}^*$ and $\underline{a}^c = \underline{a}^*$. Thus,

Proposition 2 (Equilibrium in Stochastic Settings) The equilibrium actions, \overline{a}^* and \underline{a}^* , are implied by the equations

$$2c\left(\overline{a}^* - \overline{t}\right) = \frac{W}{\sigma\sqrt{2\pi}} \exp\left(-\frac{1}{2\sigma^2} \left(\frac{\Delta a^*}{2} + \ln(LR_0)\frac{\sigma^2}{\Delta a^*}\right)^2\right),\tag{10}$$

$$2c\left(\underline{a}^* - \underline{t}\right) = \frac{W}{\sigma\sqrt{2\pi}} \exp\left(-\frac{1}{2\sigma^2} \left(\frac{\Delta a^*}{2} - \ln(LR_0)\frac{\sigma^2}{\Delta a^*}\right)^2\right);\tag{11}$$

where $\Delta a^* := \overline{a}^* - \underline{a}^*$. The equilibrium response is given in Lemma 1, with the \overline{a}^* and \underline{a}^* replacing \overline{a}^c and \underline{a}^c .

Notice that if $\rho_0 = 1/2$ so that $\ln(LR_0) = 0$, then both types will deviate from their myopic best actions by exactly the same amount, otherwise the relatively less likely type deviates (that is, signals) more.

3 Experimental design and procedures

The experiments were framed as an interaction of a worker and a personnel manager.⁸ In the instructions (see appendix), subjects were informed about the game as described above. The worker's decision was framed as an effort in a "test" which preceded the employment

⁸Because we use labels like manager, worker and effort, our frame is "meaningful." A "generic" frame would have avoided such labels and, instead, presented the game in abstract terms. Cooper and Kagel (2009) analyze cross-game learning in signaling games with meaningful and generic contexts and find that meaningful contexts can strongly support cross-game learning. However, a change in context, together with superficial changes which leave the underlying economic structure isomorphic to the original game leads to reduced learning. Two-person teams show substantially higher levels of strategic play in all of Cooper and Kagel's (2009) treatments.

decision. We made it clear that no real effort had to be invested, and we explained how the effort level chosen affected the worker's profit. The payoff information regarding the effort choice was given in a table.

As in the model, personnel managers then received the (deterministic or stochastic) signal derived from workers' effort levels in the test. Next, they had to decide whether or not to employ the worker for some (not specified) task. The descriptions of the payoffs explained that the manager is paid B if he or she employs a worker "suitable for the task" or if he or she does not employ a worker who is not suitable for the task. The suitability of the workers was randomly determined by the computer individually and in every period. Workers were paid W only if they were employed, in addition to the payoff from the effort choices.

The parameters we used for the experiment were U = 100, V = 0, W = B = 100, $c = \frac{1}{2}$, $\bar{t} = 50$ and $\underline{t} = 40$. Effort levels had to be chosen from the interval [25, 65]. These parameters yield the payoff table in the instructions (see appendix).

Our treatment variables are the noise parameter and the prior belief. Specifically, we compare games without noise to those with noise. In the sessions with noise, the noise was normally distributed with $\varepsilon \sim N(0, 5^2)$. Following Ashenfelter *et al.* (1992), subjects were not given the specific formal details of the normal distribution. Instead, they were given 100 "past realizations" of the noise term and were told that they should expect "similar distortions today" (see appendix). As for the prior belief, we deliberately ruled out a treatment in which both types are equally likely (which is the traditional set-up in signaling experiments) for two reasons. First, in the deterministic variant of the game a prior of one-half is exactly the threshold for switching from a pooling to a separating equilibrium and we wanted to have unambiguous predictions on behavior; and second, in the noisy variant we were specifically interested in the observation that the less-frequent type signals more, ruling out a prior under which types are equally likely. However, we also wanted to assure that neither type occurs too infrequently in any of the treatments. Thus, it was natural to settle on one prior in which the low type was twice as likely to occur as the high type and the other treatment with the reverse, that is, priors $\Pr(t = \bar{t}) = \rho_0$ of $^{1}/_{3}$ and $^{2}/_{3}$, respectively.

We use the labels *NoNoise.33*, *NoNoise.67*, *Noise.33* and *Noise.67* for the corresponding treatments. Table 2 summarizes the treatment design.

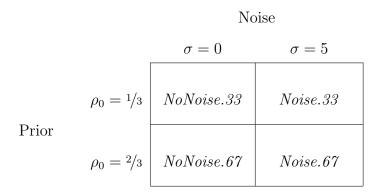


Table 2: Treatments

At the end of each period, subjects were given the following feedback: They were informed about the worker's type and the actual effort decision. In sessions with noise, they were also told the noisy signal that the personnel manager received. Further, they were reminded of the personnel manager's decision and were given the resulting payoffs of both players.

We decided to allow for many repetitions because learning is necessary in such complex situations—a supposition that is borne out by the data. Our experiments had a length of 40 periods.

Subjects were randomly rematched in every period in order to create an environment as close as possible to a single-period interaction between subjects. In each session, 20 subjects participated. The matching scheme was such that subjects interacted within a group of ten subjects. The rationale for this matching scheme is to generate more group-level observations that are independent; each session of 20 subjects thus consists of two independent groups.⁹ We have two sessions (40 participants) for each treatment, generating four independent groups per treatment. We used the same matching protocol in all sessions.

We applied role switching in this experiment. That is, participants acted both in the role of the worker and in the role of the personnel manager. Roles were switched every five periods, so all participants played either role four times for five periods. Many signaling experiments employ role switching; see Brandts and Holt (1992, 1993), Cooper et al. (1997a,b), Cooper

⁹It should be noted, however, that this can have the undesirable impact of making the within-group correlation greater since individuals within a matching group interact more frequently than if groups were formed from all session participants.

and Kagel (2005, 2009); Kübler *et al.* (2008), and Potters and van Winden (1996). One motive sometimes given in favor of role switching is that it may enhance learning because subjects may better understand the decision problem of the other players and therefore the overall game if they play in both roles.

Experiments were computerized. We used z-Tree, developed by Fischbacher (2007). Sessions were conducted at BonnEconLab, the University of Bonn's Experimental Economics Laboratory. In total, 160 subjects participated in eight sessions.

Sessions lasted between 60 and 75 minutes, including the time for reading the instructions, playing the experiment, answering a post-experimental questionnaire and paying the subjects. Earnings were denoted in "points." The exchange rate of one euro for 500 points was known. Subjects also received a show-up fee of four euros. Average earnings were about 13 euros, including the show-up fee.

4 Hypotheses

Given the experimental parameters ($U=100, V=0, W=B=100, c=\frac{1}{2}, \bar{t}=50$ and $\underline{t}=40$), we obtain the equilibrium benchmarks given in Table 3. Recall that \overline{a} and \underline{a} refer to \overline{t} 's and \underline{t} 's effort choices, respectively, and $\Delta a := \overline{a} - \underline{a}$ is the effort difference. Employment rates are denoted by \overline{e} and \underline{e} , and the average employment rate is $e := \rho_0 \overline{e} + (1 - \rho_0) \underline{e}$. Finally, \tilde{s} denotes the switching point, that is, the signal above which employers choose r=1. Equilibrium values are indicated by an asterisk (*) throughout.

Table 3 reveals that the predictions about the effects of our treatments are not always unambiguous. Consider, for example, the impact of noise on \underline{a} . In *Noise.33*, \underline{a} should be higher than in *NoNoise.33*, but it is exactly the other way round in *Noise.67* and *NoNoise.67*. For \overline{a} , the impact of noise is different again. Instead of unambiguous hypotheses, the impact of noise often depends on the prior (or *vice versa*) in theses cases. In what follows, we accordingly present hypotheses in the form of ordinal rankings of the relevant variable across all four treatments. We then use the non-parametric Jonckheere-Terpstra test, ¹⁰ testing the

¹⁰The Jonckheere-Terpstra test is a non-parametric test for more than two independent samples, like the Kruskal-Wallis test. Unlike Kruskal-Wallis, Jonckheere-Terpstra tests for ordered differences between treatments and hence requires an ordinal ranking of the test variable. See, for example, Hollander and Wolfe

	NoNoise	Noise
	$\underline{a}^* = 40.0, \overline{a}^* = 54.1, \Delta a^* = 14.1$	$\underline{a}^* = 42.5, \overline{a}^* = 55.0, \Delta a^* = 12.5$
$\rho_0 = 1/3$	$\underline{e}^* = 0, \overline{e}^* = 1, e^* = 0.33$	$\underline{e}^* = 0.06, \overline{e}^* = 0.83, e^* = 0.32$
	$\tilde{s}^* = 54.1$	$\tilde{s}^* = 50.2$
	$\underline{a}^* = 50.0, \overline{a}^* = 50.0, \Delta a^* = 0.0$	$\underline{a}^* = 48.0, \overline{a}^* = 54.0, \Delta a^* = 6.0$
$\rho_0 = 2/3$	$\underline{e}^* = 1, \overline{e}^* = 1, e^* = 1$	$\underline{e}^* = 0.49, \overline{e}^* = 0.88, e^* = 0.75$
	$\tilde{s}^* = 50.0$	$\tilde{s}^* = 48.1$

Table 3: Equilibrium Constellations Given the Experiment Parameters (figures are rounded)

null hypothesis that all treatments come from the same distribution against the predicted ranking of treatments.

We start with sender behavior. The first hypotheses are on the effort levels chosen by the low type \underline{a} , by the high type \overline{a} , and on the effort difference $\Delta a = \overline{a} - \underline{a}$. All of the hypotheses are obtained from Table 3.

Hypothesis 1 (Sender's Effort Choice) Concerning the senders' type-dependent equilibrium effort choices, the following rankings hold:

- (a) for the low-type's action a^* : NoNoise.33 < Noise.33 < Noise.67 < NoNoise.67;
- (b) for the high-type's action \bar{a}^* : NoNoise.67 < Noise.67 < NoNoise.33 < Noise.33;
- (c) for the difference in actions Δa^* : NoNoise.67 < Noise.67 < Noise.33 < NoNoise.33.

A general implication of noise is as follows.

Hypothesis 2 (Signaling with Noise) In the noisy treatments, senders should always signal, that is, they should always choose a > t.

For the treatments with noisy signaling, we have an intriguing hypothesis which we already noted following Proposition 2.

(1999).

Hypothesis 3 (Signaling Distortions with Noise) The sender whose type is less likely under the prior beliefs engages in more costly signaling efforts, that is, $\underline{a} - \underline{t} < \overline{a} - \overline{t}$ in Noise.33, and $\underline{a} - \underline{t} > \overline{a} - \overline{t}$ in Noise.67.

We now turn to the receiver's behavior. Table 3 contains the data for the type-dependent employment rates and also for the average employment rates per treatment.

Hypothesis 4 (Employment Rates) Concerning the senders' type-dependent equilibrium employment probabilities, the following rankings hold:

- (a) for the low type's employment rate \underline{e}^* : NoNoise.33 < Noise.33 < Noise.67 < NoNoise.67;
- (b) for the high type's employment rate \overline{e}^* : Noise.33 < Noise.67 < NoNoise.67 = NoNoise.33;
- (c) for the average employment rate e*: Noise.33 < NoNoise.33 < Noise.67 < NoNoise.67.

We finally turn to the receiver's equilibrium choice of switching points.

Hypothesis 5 (Switching Points) Regarding the receiver's switching points, \tilde{s}^* , the following ranking holds: Noise.67 < Noise.67 < Noise.33 < NoNoise.33.

5 Results of the Experiments

The results section is structured as follows. We begin with an analysis of the worker (sender) behavior. Then we move on to the managers (receivers), before analyzing workers and managers jointly to see how they respond to one another's actual behavior.

We usually employ non-parametric tests where we (conservatively) count one group of randomly matched participants as one observation. That is, we usually take the average action of all participants in one group as one observation (recall that we have have four entirely independent observations per treatment). Whenever we depart from this, we indicate how we deal with the possible non-independence of observations. Thus, we generally test directed hypotheses and report one-sided p-values, accordingly—except for the (unpredicted) time trends where we report two-sided p-values.

In signaling game experiments, it is common for learning to take place among subjects (see, for example, Cooper and Kagel, 2005, 2009). Therefore, our main data analysis is based on data from periods after learning has settled, that is, the second half of the experiment. We report on learning effects (which justify this selection) below.

5.1 Worker (sender) behavior

Table 4 and Figure 3 summarize the effort choices across the four treatments. Table 4 reports average effort choices and their standard deviation for the group averages. It also states the equilibrium benchmarks. Figure 3 displays the cumulative distribution functions of choices by types and treatment.

Prior	$No\Lambda$	loise	No	vise
	\underline{t}	\overline{t}	\underline{t}	\overline{t}
1/3	40.00	54.14	42.50	55.00
	44.34	51.57	45.19	52.77
	(1.41)	(1.40)	(0.91)	(0.49)
2/3	50.00	50.00	48.00	54.00
	46.93	50.96	45.67	51.50
	(1.96)	(0.92)	(1.72)	(1.19)

Table 4: Effort Levels (equilibrium values in italics, standard deviation in parenthesis)

As in previous signaling games, choices do not perfectly settle on the equilibrium benchmarks even in the second half of the experiment, as can be seen in Table 4. Figure 3 also indicates that there is no complete separating or pooling behavior in any treatment. Frequently, workers choose their myopic best action. While this is consistent with equilibrium behavior for one type in the *NoNoise* treatments, the frequency is nowhere near 100% for any type in any treatment. Another general observation is that the average signaling distortions (that is, the a-t margins) of the \underline{t} types are larger than those of the \overline{t} types in all treatments. Whereas \overline{t} generally provide too little effort compared to the equilibrium benchmark (except in *NoNoise.67*), t provide too much effort with the low prior and too little effort with the

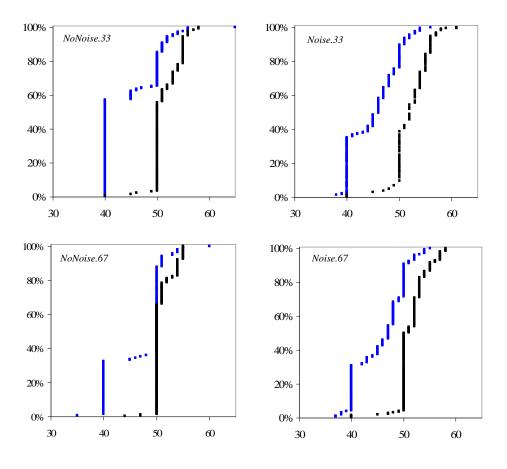


Figure 3: CDFs of Effort Choices (low type, left ■; high type, right ■)

high prior. Indeed, this is true right from the beginning, period $1.^{11,\,12}$

Figure 4 shows the time trends of the effort decisions for each treatment and type. The pattern in NoNoise.33 is typical for a signaling experiment where separating behavior emerges (see, for example, Cooper and Kagel, 2009): First, \underline{t} mimic \overline{t} 's effort levels; this appears to trigger the high types to increase their efforts, which eventually leads to a decline of low's efforts, with behavior having settled down for the second half of experiment. This is in stark contrast to NoNoise.67, in which pooling is predicted and no major time trends

¹¹The excess signaling of <u>t</u>-types may correspond to the phenomenon of over-investments in contests (for example, Fonseca, 2009; Sheremeta, 2010). It appears that subjects receive an extra utility from winning a contest. In our setup, getting employed is pretty much a forgone conclusion for high types, whereas low types may be willing to invest an excess effort for the sole purpose of getting employed.

 $^{^{12} \}mathrm{In}$ period 1 (where all effort choices are still completely independent), 30 of 44 high types choose $a=\bar{t}=50$ but only 14 of 36 low types $a=\underline{t}=40.$ A chi-square test indicates that the difference in proportions is significant (d.f. = 2, p = 0.009). Similarly, the 95% confidence interval of period-1 actions for the high type, [49.01, 50.94], includes the myopic best action, 50, whereas the confidence interval for \underline{t} , [41.54, 44.85], does not include 40. See also Figure 4.

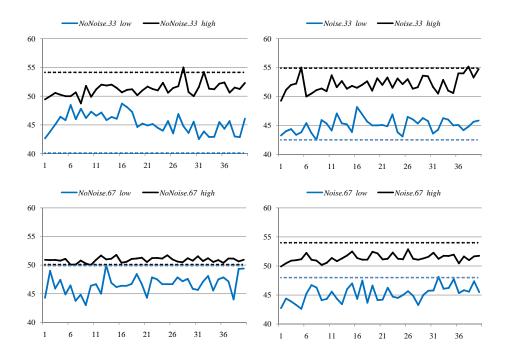


Figure 4: Effort over Time (low type, bottom □; high type, top □); equilibrium, dotted lines)

appear. In the treatments with noise, we observe increasing effort levels in the first half of the experiment but no tendencies over time in the second half (except for the effort increase of \underline{t} in Noise.67, see footnote 13 below). While we do recognize separating behavior in both Noise treatments, it is also apparent that the development over time is different from the pattern in NoNoise.33. We thus conclude some tentative support for our setup from Figure 4 in that both of our treatment variables seem to have the predicted effect, that is, pooling vs. separating in NoNoise, and qualitatively different separating behavior with both types signaling in Noise.¹³

We now formally test our Hypotheses. It turns out that while effort decisions do not perfectly converge, there are a number of observations that are consistent with the equilibrium benchmarks.

¹³We examine the correlations between experimental time periods and effort levels. In periods 1 to 20 three of eight possible correlations (two types × four treatments) were significant, whereas in periods 21 to 40 only one correlation was significant. In the first half of the experiment, \bar{t} -types increase their efforts over time in NoNoise.33 (Spearman's $\rho = 0.526$, p = 0.017), NoNoise.67 ($\rho = 0.390$, p = 0.090) and Noise.67 ($\rho = 0.606$, p = 0.005). In the second half of the experiment, \bar{t} -types increase their efforts over time in Noise.67 ($\rho = 0.496$, p = 0.026).

Table 4 shows that the ranking of effort averages across the four treatments is consistent with the theory. For \underline{t} , recall from Hypothesis 1(a) that the lowest effort benchmark (namely 40.0) should occur in NoNoise.33, next comes Noise.33 with a level of 42.5, followed by Noise.67 (48.0) and the highest effort levels for \underline{t} (50.0) should occur in NoNoise.67. The actual averages are ranked precisely in this way. A Jonckheere-Terpstra test rejects the null hypothesis (that effort averages of the \underline{t} type workers are drawn from the same distribution) at p=0.016 in favor of the alternative Hypothesis 1(a). Conducting the Jonckheere-Terpstra test for the ranking of effort choices by the \overline{t} types yields a similar result (p=0.031), rejecting the null in favor of Hypothesis 1(b).

Now consider the effort differential, $\Delta a = \overline{a} - \underline{a}$. The effort differential is the amount of separation between the types and therefore tells us something about the important pooling vs. separating issue. The impact of noise on this variable is ambiguous in theory. There is less separation with noise for the low prior but more separation with noise for the high prior. From Hypothesis 1(c), the theoretical benchmark for Δa^* (ranked in ascending order) is $\Delta a^* = 0.0$ in NoNoise.67 (the pooling case), 6.0 in Noise.67, 12.5 in Noise.33 and finally 14.1 in NoNoise.33. Figure 5 shows the average amount of separation between types for each group and the theoretical benchmark. The picture shows that the theory works well in organizing the data. The ranking of the group averages by treatment is the one predicted except that Noise.33 has a marginally higher average than NoNoise.33. Applying the Jonckheere-Terpstra test on the average effort differentials yields a highly significant rejection of the null hypothesis (p=0.006), therefore providing support for Hypothesis 1(c).

Part of Hypothesis 1(c) is the proposition that with $\rho_0 = 2/3$ pooling ($\Delta a^* = 0.0$) should occur without noise but separating ($\Delta a^* = 6.0$) with noise. This is an intriguing hypothesis which can be tested directly in a pairwise comparison of these treatments. A ranksum test confirms that the effort differential is smaller in NoNoise.67 than in Noise.67 (p=0.057, exact test). The CDFs in Figure 3 also provide evidence in this direction. For NoNoise.67, Figure 3 reveals that the pooling equilibrium effort level of 50 is the mode (60.25%). This is true for both types as \underline{t} workers choose a=50 in 51.5% and \overline{t} types in 64.8% of the cases. The frequency of a=50 effort choices is significantly smaller in Noise.67 and indeed in all of the other three treatments where $a^*=50$ should not occur in equilibrium (pairwise

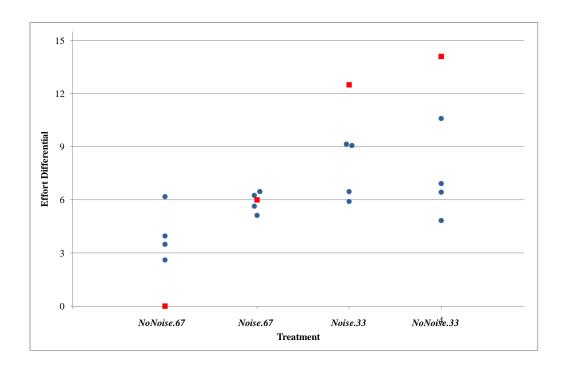


Figure 5: Effort Differentials $\Delta a = \overline{a} - \underline{a}$ (equilibrium: squares \blacksquare ; group data: bullets \bullet)

comparisons with exact rank-sum tests, all p=0.029 or smaller). This is support for the pooling vs. separating hypothesis with $\rho_0 = 2/3$. By contrast, if $\rho_0 = 1/3$ there should be separation both with and without noise and the prediction regarding the effort differential is 12.5 and 14.1 for Noise.33 and NoNoise.33, respectively. As there is separation either way and since the predicted effort differentials do not differ much, unsurprisingly, Noise.33 and NoNoise.33 do not differ significantly.¹⁴

Hypothesis 2 suggests that workers should always signal (that is, choose a > t) in treatments with noise. Specifically, \underline{t} should choose a > 40, and \overline{t} should choose a > 50 with noise. Whereas the CDFs show that in many cases workers do actually choose their myopic best actions, they also show that $\underline{a} = 40$ and $\overline{a} = 50$, respectively, are selected less frequently in the stochastic-signal treatments. Statistical support for this can be obtained by collecting the share of effort choices strictly larger than the (type-specific) myopic best action for each

 $^{^{14}}$ For the sake of completeness, the third pairwise comparison of Hypothesis 1(c), NoNoise.67 vs. NoNoise.33, confirms the theory in that we have a significant effect (p=0.057). Comparing Hypotheses 1(a) and (b) pairwise does not yield significant test results. Thus, while the Jonckheere-Terpstra omnibus test rejects the null hypothesis in these cases (Hypotheses 1(a) and (b)), we cannot identify a pair of treatments which (mainly) accounts for this rejection.

group. In the eight groups of the noisy treatments, 62.8% of the workers' actions have a > t but this is only the case in 47.8% of the deterministic treatments. A ranksum test reveals that this difference is significant (p=0.023). Note that we obtain this significant result even though one type is predicted to choose a > t also in the *NoNoise* treatments.

We can also check Hypothesis 2 for \underline{t} only. In the *Noise* treatments, \underline{t} 's equilibrium actions lie strictly between 40 (= \underline{t}) and 50 (= \overline{t}). By contrast, in the *NoNoise* treatments, the equilibrium actions for \underline{t} are 40 and 50, and moreover the worker is (at least in theory) revealed as being \underline{t} when choosing $a \in (40, 50)$. With noise, effort choices between 40 and 50 generate signals that only imperfectly reveal the worker as \underline{t} . These considerations are confirmed in the data. The CDFs show that 39.04% of the \underline{t} observations are in the $a \in (40, 50)$ interval with noise but, without noise, only 5.58% are. This difference is significant (rank-sum test, p < 0.001). The result suggests that subjects clearly understood the noisy signal-generating mechanism.

Finally, for the noise treatments, Hypothesis 3 states that signaling distortions (a-t) are larger for the less frequent type. At face value, this hypothesis is clearly rejected. As mentioned above (and as in other signaling experiments), the \underline{t} types distort more in all treatments compared to the \overline{t} types, and we find $\underline{a} - \underline{t} > \overline{a} - \overline{t}$ in all groups of all treatments. However, in relative terms, the prediction is supported. From Table 4, note that the \underline{t} types distort more with the high prior whereas the \overline{t} types distort more for the low prior. Testing this formally, the ratio $(\underline{a} - \underline{t})/(\overline{a} - \overline{t})$ is significantly smaller in Noise.33 than in Noise.67 (ranksum test, p=0.042). Interpreting the predictions in relative rather than absolute terms (which seems warranted as the \overline{t} types signal too little anyway, right from the first period on), we find support for Hypothesis 3.

5.2 Manager (receiver) behavior

Table 5 shows how frequently managers employ the workers. Compared to the equilibrium benchmark, \bar{t} is employed too rarely, and \underline{t} is employed too often. This finding is not particularly surprising given the above result that low types usually signal too much and high types sometimes too little. The hypothesis regarding \underline{t} , Hypothesis 4(a), turns out

to be supported by the data in that we reject the null hypothesis (Jonckheere-Terpstra, p=0.003). That is, even though quantitatively the predictions fail, the theory still yields a useful qualitative prediction regarding \underline{e} . Regarding the ranking of \overline{e} (the employment rates of \overline{t}), we cannot reject the null hypothesis that all treatments are drawn from the same distribution (Jonckheere-Terpstra, p=0.245), that is, we find no support for Hypothesis 4(b).¹⁵

Prior	NoNoise		Noise	
	\underline{t}	\overline{t}	\underline{t}	\overline{t}
1/3	$0.000 \\ 0.232 \\ (0.030)$	1.000 0.609 (0.066)	$0.060 \\ 0.272 \\ (0.036)$	0.833 0.609 (0.041)
2/3	$ \begin{array}{c} 1.000 \\ 0.470 \\ (0.057) \end{array} $	$ \begin{array}{c} 1.000 \\ 0.864 \\ (0.064) \end{array} $	$0.490 \\ 0.565 \\ (0.078)$	0.880 0.834 (0.056)

Table 5: Employment Rates (equilibrium values in italics, standard deviation in parenthesis)

Figure 6 shows that average employment rates across the two types, e, meet the equilibrium benchmarks rather accurately in three of the four treatments. That is, regarding average employment rates per treatment, the theory works well even in a quantitative sense. (The exception is *Noise.67*.) A Jonckheere-Terpstra test on the average employments rates confirms that the ranking we observe rejects the null hypothesis (p=0.004). This significant test result is in favor of Hypothesis 4(c). From Figure 6, it is evident that the differences are mainly driven by the prior rather than by noise.¹⁶

Employment decisions obviously depend on workers' effort levels. Figure 7 shows the

 $^{^{15}}$ Correlations over time for the employment decisions are as follows. \bar{t} -types are employed less frequently over time in NoNoise.33 (Spearman's $\rho=-0.488,\ p=0.029$), and more frequently in Noise.67 ($\rho=0.419,\ p=0.069$). In periods 21 to 40, \bar{t} -types' employment rates decrease over time in NoNoise.67 ($\rho=-0.472,\ p=0.036$). Time trends are perhaps less conclusive for the employment rates than for the effort decisions as employment rates can be quite volatile. The reason is that, depending on the chance move, the less frequent type (\bar{t} [t] in the .33 [.67] treatments), may occur only rarely in some period for some treatment (the minimum we find is two instances). Thus employment rates may vary substantially, indeed, in the Noise treatments this is predicted to occur in equilibrium.

 $^{^{16}}$ Indeed, if we compare our treatments pairwise, we find significant test results when we compare .33 and .67 treatments (ranksum tests, all p = 0.0105) but not when we compare NoNoise to Noise treatments. The results of these pairwise tests are the same for Hypotheses 4(a), (b) and (c).

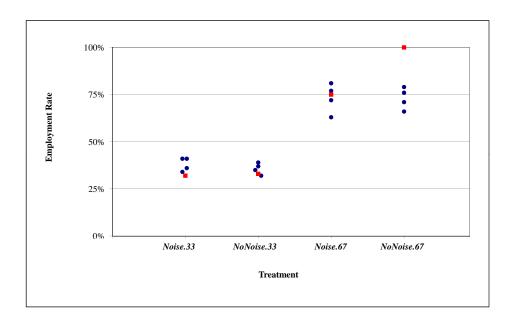


Figure 6: Employment Rates (equilibrium: squares ■; group data: bullets •)

likelihood of getting employed as a function of the effort signals. The probabilities are obtained from simple probit regressions where the response decision $r \in \{0, 1\}$ is a function of s, the signal received. For each treatment there is a separate regression. The probits are based on data from periods 21 to 40 and are clustered at the matching-group level (Wooldridge, 2003). As expected, the probability of an r = 1 choice increases with the received signal s. Indeed, in all treatments, most of the increase occurs between s = 40 and s = 55. In all four cases, both the constant and the marginal effects of the effort signal are significant at p < 0.001. All regressions are highly significant with the pseudo R^2 varying between 0.190 (Noise.67) and 0.413 (NoNoise.33).

There are two further intuitive observations from Figure 7. First, the employment likelihood is higher with $\rho_0 = 2/3$. Both with and without noise, r = 1 responses are more likely with the high prior. As can be seen in Figure 7, the $\rho_0 = 2/3$ treatments first-order stochastically dominate those with $\rho_0 = 1/3$. Second, the figure shows that the curves in the noise treatments are flatter than their *NoNoise* counterparts for the middle range of effort choices. For the $\rho_0 = 1/3$ prior, $\Pr(r = 1)$ is larger in the noise treatment for $s \le 49$ and smaller otherwise. Similarly, for the $\rho_0 = 2/3$ prior, $\Pr(r = 1)$ is larger with noise as long as $s \le 55$ and smaller otherwise. This is intuitive. A signal of, say, 45 is rather unlikely to have been

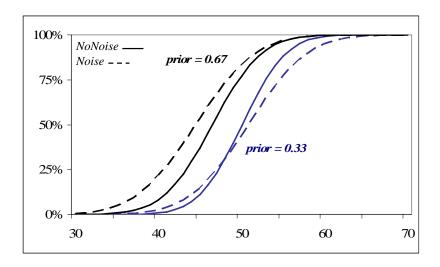


Figure 7: Probability of Employment as a Function of the Signal

sent by \bar{t} without noise. With noise, there is some chance \bar{t} 's choice was distorted negatively to the level of 45. The reverse is true for choices larger than, say, 50 and 55, respectively. Such high choices are almost surely sent by \bar{t} when there is no noise. With noise, there is still the chance that noise caused the high signal and thus managers are less likely to choose r = 1 compared to *NoNoise*, given the same effort choice.

Probit regressions (not reported here to economize on space) reveal that these two effects are significant. A dummy for the high prior has a significant impact on the likelihood of getting employed whereas a *Noise* regressor *per se* is positive but insignificant. Only when we include interaction terms does *Noise* become significant. The $Noise \times Effort$ interaction is negative and significant.

We also use probit regressions to test Hypothesis 5 which is on the switching strategies. Specifically, we run the probits mentioned in the previous paragraph above separately for each group and calculate the median accepted effort choice for each group, that is, the effort choice under which there is a 50% probability of being employed. We compare these median threshold effort levels (one for each group, four for each treatment) to the ranking of switching points given in Hypothesis 5. (If 100% of our subjects behaved consistently with the theory, they would reject every signal below the switching point and employ for every signal above that point, and thus the median signal that results in employment would be qual to the predicted switching point.) A Jonckheere-Terpstra rejects the null hypothesis

at p=0.001, supporting the ordinal ranking in Hypothesis 5.¹⁷ Figure 8 shows the empirical median switching points per group in conjunction with the equilibrium switching points.

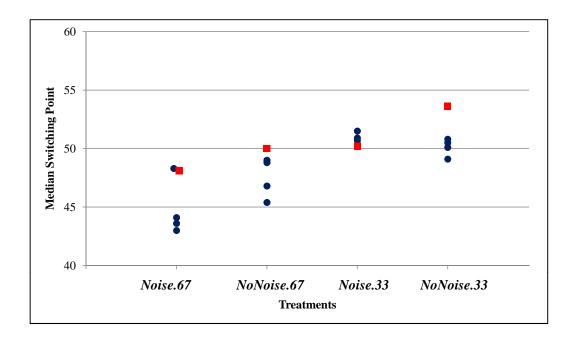


Figure 8: Switching Points (equilibrium: squares ■; group medians: bullets •)

5.3 How do players respond to others' empirical behavior?

Above, we saw that behavior does not seem to converge fully to equilibrium benchmarks. On the other hand, the support for some implications of the theory indicates that play is far from erratic. This raises the question of how subjects respond to the actual empirical behavior of the other subjects.

We first analyze how workers' actions correspond to the employment decisions. To do this, we determine the optimal effort level given managers' actual employment decisions in periods 21 to 40, separately for each treatment and type. Specifically, we use the acceptance probabilities from the probit regressions underlying Figure 7 and calculate workers' expected

¹⁷Testing pairwise, only the comparison of treatments *NoNoise.67* and *Noise.33* is significant (p = 0.029, exact ranksum test).

payoffs from this. For some effort level a,

$$100 - \frac{1}{2}(a-t)^2 + \Pr(r=1|a) \times 100$$

is t's expected payoff.

The main insight from this exercise is that average effort choices sometimes do not differ much from the value that maximizes expected payoffs and, whenever they do differ, this can be explained by "flat" expected payoff maxima. Table 6 shows the results.

Prior	NoNoise	Noise_
	\underline{t} t	\underline{t} t
1/3	$ 40.8 54.9 \\ +3.5 -3.3 $	$ 42.0 55.2 \\ +3.2 -2.4 $
2/3	$\begin{array}{ccc} 48.0 & 53.2 \\ -1.1 & -2.2 \end{array}$	$\begin{array}{ccc} 46.6 & 52.6 \\ -0.9 & -1.1 \end{array}$

Table 6: Optimal Effort Choices Given Employment Decisions (and difference between actual average effort and optimal choices)

There are eight cases, one for each treatment and each type. For example, the first entry (top left) indicates that, given the empirical receiver behavior in the second half of the experiment, \underline{t} 's optimal choice in NoNoise.33 was 40.8, yet the actual average choice was 3.5 higher (44.3) than the optimal choice of that type in that treatment (where the actual averages are obtained from Table 4). In three of eight cases, the (absolute) differences is 1.1 or less, suggesting a certain coincidence of optimal and actual average effort choices. Moreover, note that larger differences (say, three or more effort units) are subject to the disclaimer that differences in expected payoffs are truly minor. In Noise.33, the payoff loss from not playing optimally is merely 1.35% and 1.75% in NoNoise.33, for low and high types, respectively. The biggest loss in expected payoff (5.6%) occurs for \bar{t} in Noise.33. The fact that deviating from optimal behavior causes only minor losses of expected payoffs suggests that the discrepancy of optimal and actual average effort choices, if they occur at all, should be interpreted with caution (Harrison, 1989). The minor losses in expected payoffs also explain why play does not converge to equilibrium more quickly.

Table 6 reveals another result. The optimal effort choices given empirical behavior are sometimes surprisingly close to the equilibrium benchmarks (see Table 4). In *NoNoise.33* and *Noise.33*, they almost exactly coincide for both types. In *Noise.67*, the gap between optimal effort choices and the equilibrium benchmark is 1.4 for both types which does not seem to be too far off the mark. Only the pooling prediction in *NoNoise.67* differs from the optimal effort choices.

Next, we analyze how managers' decisions correspond to actual worker behavior. To this end, we calculate at which signal the probability that it was sent by \bar{t} is $^{1}/_{2}$ —this is the empirically optimal switching point for risk neutral receivers. This is done with probit regressions ($t = \bar{t}$ as a function of the observed s), separately for each treatment and based on the signals in periods 21 to 40. The actual switching point for each treatment is the lowest signal s that, based on the probits, leads to employment with probability of at least $^{1}/_{2}$. These actual switching points can be taken from Figure 7. Table 7 shows the results of this analysis. It reveals that, although the empirically optimal switching points are larger

Prior	NoNoise	Noise
1/3	$50.7 \\ -0.6$	$47.7 \\ -1.2$
2/3	$53.8 \\ -3.0$	$45.0 \\ -0.5$

Table 7: Optimal Switching Points Given Effort Decisions (and difference between actual median and optimal switching points)

than the actual switching points throughout, they do correspond closely to one another. In NoNoise.67 and Noise.33, they differ by only 0.5 and 0.6 units of effort, respectively, and in NoNoise.33 they differ by 1.2 only. In NoNoise.67 they differ by three units of effort. Again, the small differences between optimal and actual behavior are remarkable.

5.4 Does the theory perform better in stochastic settings?

A final issue that we discuss here is that, quantitatively, the theory appears to be more closely in line with behavior in the treatment with noise compared to the deterministic setting. To make this statement precise, consider the absolute difference between equilibrium values given in Table 3 and the treatment averages. As for the effort levels chosen (Table 4), the *Noise* treatment averages are closer to the equilibrium in three of four cases. In Table 5 (employment rates), the comparison reveals that the averages with noise are closer to the equilibrium in all four cases. Similarly, when we look at optimal decisions given empirical behavior of the other players, the noisy variants have a smaller gap between optimal choice and average choices in all four cases of Table 6 and in one of two cases in Table 7.¹⁸

What could be driving this result? One possibility is that because there are multiple equilibrium configurations in the deterministic case but a unique equilibrium in the stochastic version of our game, coordination on equilibrium might be easier in the noisy case. However, there is only limited evidence that subjects play any of the non-refined equilibria, as seen above. We believe that what may be driving the results is the fact that the stochastic variant captures aspects of decision making that the deterministic variant fails to address. Consider, for example, employment rates. In the deterministic game, in equilibrium, there are no errors in hiring, that is, in a separating equilibrium 100% of high types are employed and 0% of low types; whereas in a pooling equilibrium 100% of workers (that is, both types) are employed. However, in the data both Type-I errors and Type-II errors occur. That is, high types are sometimes erroneously not hired and low types are erroneously employed. In contrast, Type-I and Type-II errors are an equilibrium phenomenon in the noisy variant. Consequently employment rates are never extreme. Empirically, Type-I and Type-II errors are rather frequent—an aspect of the data that is well accounted for by the stochastic version of the model. Of course, the signaling model with noise does not take errors in decision making into account, but in the data Type-I and Type-II errors occur both because of noise and because of decision errors. Our point is, hence, that the stochastic model correctly predicts Type-I and Type-II errors even if, partly, they occur for the wrong reason. As a result, the theory performs better when noise is explicitly modeled.

¹⁸Since the noisy setup performs better in 12 of 14 cases, one could argue that a binomial test rejects the null hypothesis that theories perform equally well at p < 0.01.

6 Conclusion

We consider a sender-receiver signaling game in an environment in which the signal-generating mechanism is subject to homoskedastic noise. This noisy setup differs markedly from the standard deterministic case. With deterministic signals, a unique perfect Bayesian equilibrium can only be obtained after the application of equilibrium refinements and, depending on the prior belief, there is either a separating equilibrium or a pooling equilibrium. With noise, the unique equilibrium is separating and the equilibrium actions vary smoothly with the level of the noise and the prior belief.

We further contrast the differences between deterministic and noisy environments by reporting on subject behavior in experiments that we ran. Specifically, we study a frame where workers can choose effort levels as a signal and personnel managers decide whether to employ the workers. We compare games without noise to those with noise, and games with a "high" and "low" prior. Many predictions are confirmed in the data in qualitative terms and some are even relatively close in quantitative terms. In particular, the theory has predictive power regarding the main variables of interest, viz., effort levels, employment rates, and employment cut-offs (that is, switching points). As predicted, given a high prior there is more pooling behavior without noise compared to noisy environments. Also consistent with theory is that subjects choose their myopic best action less frequently in the noisy treatments. Absent ample learning opportunities, signaling experiments usually do not converge fully and often myopic choices and naive mimicking rather than sophisticated play is observed. However, even though we also do not see complete convergence in our data, we do find remarkable support for the theory, and where we find deviations these regularly result in near-negligible differences in payoffs compared to optimal play. In particular, subject behavior is distinct across treatments and in line with equilibrium differences of the two model specifications.

Furthermore, while the stochastic model may analytically be more challenging than the deterministic model, subject behavior seems more in line with the equilibrium in the stochastic treatment and model in contrast to a comparison of the empirical data of the deterministic treatment and the deterministic equilibrium. We conjecture that this is due to the fact that

stochastic (noisy) settings may be similar to stochastic (non-uniform) play by subjects, leading to greater congruence between the equilibrium of the stochastic game and the empirical data.

We see two avenues for future research. One interesting extension is to more closely examine the rate of convergence in subject behavior across the noisy and the deterministic treatments in order to ascertain how subject learning differs between the two settings. Also, cross-game learning (Cooper and Kagel, 2005, 2009) for two different priors or for noise vs. no noise may lead to interesting insights. Secondly, carefully eliciting beliefs should be intriguing for our game as the zero-one decision of the second mover is only a coarse measure of beliefs. Analyzing the first movers' second-order beliefs seems a further useful addition to our design as it may identify motives perhaps not captured by the theory. For example, first-movers may deliberately trade off a lower chance of being employed against lower effort cost beyond the extent suggested by theory. Of course, the learning and belief-elicitation issues nicely complement one another as the beliefs will be a useful indicator of learning.

References

- [1] Ashenfelter, O., Currie, J., Farber, H.S., Siegel, M., 1992. An experimental comparision of dispute rates in alternative arbitrage systems. Econometrica 60, 1407–1433.
- [2] Backus, D., Driffill, J., 1985. Inflation and reputation. Amer. Econ. Rev. 75(3), 530–38.
- [3] Bagwell, K., Riordan, M.H., 1991. High and declining prices signal product quality. Amer. Econ. Rev. 81(1), 224–239.
- [4] Brandts, J., Holt, C.H., 1992. An experimental test of equilibrium dominance in signaling games. Amer. Econ. Rev. 82, 1350–1365.
- [5] Brandts, J., Holt, C.H., 1993. Adjustment patterns and equilibrium selection in experimental signaling games. Int. J. Game Theory 22, 279–302.
- [6] Carlsson, H., Dasgupta, S., 1997. Noise-proof equilibria in two-action signaling games.J. Econ. Theory 77, 432–460.
- [7] Cho, I.-K., Kreps, D.M., 1987. Signaling games and stable equilibria. Quart. J. Econ. 102, 179–221.

- [8] Cooper, D.J., Garvin, S., Kagel, J.H., 1997a. Adaptive learning vs. equilibrium refinements in an entry limit pricing game. Econ. J. 107, 553–575.
- [9] Cooper, D.J., Garvin, S., Kagel, J.H., 1997b. Signaling and adaptive learning in an entry limit pricing game. RAND J. Econ. 28, 662–683.
- [10] Cooper, D.J., Kagel, J.H., 2005. Are two heads better than one? Team versus individual play in signaling games. Amer. Econ. Rev. 95, 477–509.
- [11] Cooper, D.J., Kagel, J.H., 2009. The Role of Context and Team Play in Cross-Game Learning. J. Europ. Econ. Assoc. 7, 1101–1139.
- [12] de Haan, T., Offerman, T., Sloof, R., 2011. Noisy signaling: theory and experiment. Games Econ. Behav., in press.
- [13] Fischbacher, U., 2007. Zurich toolbox for readymade economic experiments. Exper. Econ. 10, 171–178.
- [14] Fonseca, M., 2009. An experimental investigation of asymmetric contests, Int. J. Ind. Org. 27, 582–91.
- [15] Grossman, S., Perry, M., 1986. Perfect sequential equilibrium. J. Econ. Theory 39(1), 120–154.
- [16] Harrison, G., 1989. Theory and misbehavior of first-price auctions. Amer. Econ. Rev. 79, 749–762.
- [17] Hertzendorf, M.N., 1993. Im not a high-quality firm, but I play one on TV. RAND J. Econ. 24, 236-247.
- [18] Hollander, M., Wolfe, D.A., 1999. Nonparametric Statistical Methods. John Wiley and Sons, Hoboken, NJ.
- [19] Kübler, D., Müller, W., Normann, H.T., 2008. Job market signaling and screening: an experimental comparison. Games Econ. Behav. 64, 219–236.
- [20] Mailath, G.J., Okuno-Fujiwara, M., Postlewaite, A., 1993. Belief-based refinements in signaling games. J. Econ. Theory 60, 241–276.
- [21] Matthews, S., Mirman, L.J., 1983. Equilibrium limit pricing: The effects of private information and stochastic demand. Econometrica 51, 981–996.
- [22] Milgrom, P., Roberts, J., 1982. Limit pricing and entry under incomplete information. Econometrica 50, 443–459.

- [23] Milgrom, P., Roberts, J., 1986. Price and advertising signals of product quality. J. Polit. Economy 94, 796-821.
- [24] Miller, R., Plott, C., 1985. Product quality signaling in experimental markets. Econometrica 53, 837–872.
- [25] Potters, J., van Winden, F., 1996. Comparative statics of a signaling game: An experimental study. Int. J. Game Theory 25, 329–353.
- [26] Reinganum, J., Wilde, L., 1986. Settlement, litigation, and the allocation of legal costs. RAND J. Econ. 17, 557–566.
- [27] Sheremeta, R.M., 2010. Experimental comparison of multi-stage and one-stage contests. Games Econ. Behav. 68, 731–747.
- [28] Sosis, R.H., Ruffle, B.J., 2003. Religious ritual and cooperation: testing for a relation-ship on Israeli religious and secular kibbutzim. Current Anthropology 44(5), 713–722.
- [29] Spence, M., 1973. Job market signaling. Quart. J. Econ. 88, 355–74.
- [30] Spence, M., 1974. Market signaling—informational transfer in hiring and related processes. Harvard University Press, Cambridge.
- [31] Wooldridge, J.M., 2003. Cluster-sample methods in applied econometrics. Amer. Econ. Rev. 93(2), 133–138.
- [32] Zahavi, A., 1975. Mate selection—a selection for a handicap. J. Theoretical Biology 53, 205–214.

Appendix to Signaling in Deterministic and Stochastic Settings, by Jeitschko and Normann:

Instructions for *Noise.33*

Welcome to our experiment. Please read the following instructions carefully. Please do not talk to your neighbors during the experiment. Should you have any questions, please ask us. We will then come to your booth and answer the question privately.

In this experiment you can earn some real money. How much you will earn depends on your decisions and the decisions of the other participants. Your earnings will be denoted in "points". You payment at the end is equal to the sum of your earnings in each period plus a one-time payment of 4 Euros. For every 500 points, you will receive 1 Euro.

In total, there will be 40 periods.

In today's experiment, a worker and a personnel manager meet in every period. The worker can either be suitable for some task or not. Whether the worker is suitable is randomly decided by the computer in each period, and chances are 1/3 (or 33.33%) that the worker is suitable.

You will be worker or personnel manager, respectively, for five periods each time. Then roles are switched and you have the other role for five periods.

Workers and personnel managers will be randomly matched by the computer in every period. That is, you cannot tell whom you are matched with in each period.

Only the worker is informed whether or not he or she is suitable. The personnel manager has to decide whether or not to employ the worker without knowing if the worker is actually suitable. We will explain the details of your payoffs in detail below but, in principle, the worker gets 100 points if he is employed. The personnel manager gets 100 points if he employs a suitable worker; he also gets 100 points if he does not employ a non-suitable worker.

Before the personnel manager decides, the workers have to do a "test". For the purpose of this experiment, workers have to decide how much "effort" they want to invest when doing the test. We will simply ask for the amount of effort workers want to invest, but we will not do a real test with you. The personnel manager will be informed about the effort the worker invests in the test.

The effort in the test will affect the worker's payment. Have a look at the table below. The left column indicates the effort chosen; the middle column indicates the payoff from the test if the worker is suitable; and the middle column indicates the payoff from the test if the worker is not suitable. For example, an effort of 42 gives 68 points to the suitable worker and 98 points to the non-suitable worker; an effort of 56 yields 82 points to the suitable worker and a loss of 28 points to the non-suitable worker. The worker's payoffs in the table will be realized regardless of the personnel manager's decision.

The personnel manager will be informed of the worker's effort in the test, but not the payoff the effort level chosen yields for the worker. Note that the personnel manager will not be told the effort level chosen with perfect accuracy (more on this below). The personnel manager's payoff does not depend on the effort chosen by the worker.

After the personnel manager gets the information about the worker's effort in the test, he has to decide whether or not to employ the worker. The personnel manager gets paid for this as follows. He gets

- 100 points if he (a) employs a suitable worker or if he (b) does not employ a non-suitable worker,
- 0 points if he (c) does not employ a suitable worker, or if he (d) employs a non-suitable worker.

The worker gets

- the payoff (positive or negative) from the test in the table in every period,
- plus 100 points if he gets employed by the personnel manager and
- plus 0 points if not,

Worker's Payoff in the Test

Payoff in Points

Effort	Suitable Worker	Non-Suitable Worker
25	-212.50	-12.50
$\overset{-\circ}{26}$	-188.00	2.00
$\overline{27}$	-164.50	15.50
28	-142.00	28.00
29	-120.50	39.50
30	-100.00	50.00
31	-80.50	59.50
32	-62.00	68.00
33	-44.50	75.50
34	-28.00	82.00
35	-12.50	87.50
36	2.00	92.00
37	15.50	95.50
38	28.00	98.00
39	39.50	99.50
40	50.00	100.00
41	59.50	99.50
42	68.00	98.00
43	75.50	95.50
44	82.00	92.00
45	87.50	87.50
46	92.00	82.00
47	95.50	75.50
48	98.00	68.00
49	99.50	59.50
50	100.00	50.00
51	99.50	39.50
52	98.00	28.00
53	95.50	15.50
54	92.00	2.00
55	87.50	-12.50
56	82.00	-28.00
57	75.50	-44.50
58	68.00	-62.00
59	59.50	-80.50
60	50.00	-100.00
61 62	39.50	-120.50
62 63	28.00	-142.00 -164.50
64	15.50	-104.50 -188.00
	$\frac{2.00}{12.50}$	
65	-12.50	-212.50

no matter if he is suitable or not.

As mentioned, the worker's effort in the test will not be told the personnel manager with perfect accuracy. How the effort choice of the worker will be communicated to the personnel manager is subject to some random disturbances.

Consider an example. Suppose the worker's effort actual choice is 20. On top of this choice, the computer now adds, or subtracts, a random number. For example, the computer may subtract 4, in which case the personnel manager is told that the effort choice is 16 (rather than being told the actual choice, 20). Or the computer might add 2 on top of the chosen 20. In that case, an effort level 22 is communicated to the personnel manager.

Note that the actual effort level chosen in the test determines for the worker's payoff, not the disturbed effort level which the personnel manager learns.

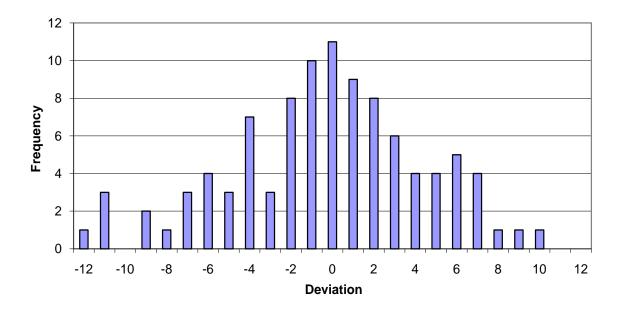
As a general rule, smaller distortions are more likely than larger ones, and disturbances are possible in either direction (adding to or subtracting from the effort level chosen).

For your information, the figure below shows the deviations from the actual choices in 100 cases in the past. You should expect similar distortions in today's experiment.

Note that the magnitude of the deviation does not depend on the effort level chosen. Indeed the level chosen has no impact whatsoever on the distortions the computer adds or subtracts. The figure shows the deviation from the true effort choice on the horizontal line and the frequency of these deviations (out of the 100 cases) with the help of the vertical bars.

In the figure you can see that, for example,

- in 4 of these 100 past cases, the computer added 4 to the chosen effort level
- in 1 of these 100 past cases, the computer added 9 to the chosen effort level
- in 3 of these 100 past cases, the computer subtracted 7 to the chosen effort level
- in 11 of these 100 past cases, the computer did not change the effort at all (the "0" column) so that the personnel manager learned the actual effort choice.



• deviations larger than +11 or smaller than -12 did not occur in 11 of these 100 past cases; such deviations are possible but unlikely.

The personnel manager will be informed about the randomly disturbed effort value before making the employment decision. The personnel manager will find out about the actual effort level chosen only at the end of a period.

Workers get their payments for the test according to their actual effort choice, not the disturbed message the personnel manager gets.

Let us summarize the experiment

- 1. The computer decides randomly whether or not the worker is suitable for the job. The chances for suitability are 1/3 (33.33%) for workers in each period. The worker (but not the personnel manager) is informed about the suitability of the worker.
- 2. The worker has to choose an effort level in the test (see the table), and the computer informs the personnel manager about the test effort. The effort level is subject to random disturbances.
- 3. The personnel manager decides whether or not to employ the worker
- 4. Payoffs are:

- If you are a worker: the payment from the effort choice in the test plus 100 points if you are employed
- If you are an personnel manager: 100 points if you employ a suitable worker, or if you do not employ a non-suitable worker

PREVIOUS DISCUSSION PAPERS

- Jeitschko, Thomas D. and Normann, Hans-Theo, Signaling in Deterministic and Stochastic Settings, November 2011.
- Christin, Cémence, Nicolai, Jean-Philippe and Pouyet, Jerome, The Role of Abatement Technologies for Allocating Free Allowances, October 2011.
- Keser, Claudia, Suleymanova, Irina and Wey, Christian, Technology Adoption in Markets with Network Effects: Theory and Experimental Evidence, October 2011.
- Catik, A. Nazif and Karaçuka, Mehmet, The Bank Lending Channel in Turkey: Has it Changed after the Low Inflation Regime?, September 2011.

 Forthcoming in: Applied Economics Letters.
- Hauck, Achim, Neyer, Ulrike and Vieten, Thomas, Reestablishing Stability and Avoiding a Credit Crunch: Comparing Different Bad Bank Schemes, August 2011.
- 30 Suleymanova, Irina and Wey, Christian, Bertrand Competition in Markets with Network Effects and Switching Costs, August 2011.
 Published in: B.E. Journal of Economic Analysis & Policy, Vol. 11, Issue 1 (Contributions), Article 56.
- 29 Stühmeier, Torben, Access Regulation with Asymmetric Termination Costs, July 2011.
- Dewenter, Ralf, Haucap, Justus and Wenzel, Tobias, On File Sharing with Indirect Network Effects Between Concert Ticket Sales and Music Recordings, July 2011.
- Von Schlippenbach, Vanessa and Wey, Christian, One-Stop Shopping Behavior, Buyer Power, and Upstream Merger Incentives, June 2011.
- Balsmeier, Benjamin, Buchwald, Achim and Peters, Heiko, Outside Board Memberships of CEOs: Expertise or Entrenchment?, June 2011.
- Clougherty, Joseph A. and Duso, Tomaso, Using Rival Effects to Identify Synergies and Improve Merger Typologies, June 2011.
 Published in: Strategic Organization, Volume 9, Issue 4 (November 2011), pp. 310-335.
- Heinz, Matthias, Juranek, Steffen and Rau, Holger A., Do Women Behave More Reciprocally than Men? Gender Differences in Real Effort Dictator Games, June 2011.
 Forthcoming in: Journal of Economic Behavior and Organization.
- Sapi, Geza and Suleymanova, Irina, Technology Licensing by Advertising Supported Media Platforms: An Application to Internet Search Engines, June 2011. Published in: The B. E. Journal of Economic Analysis & Policy 11 (2011), Article 37.
- Buccirossi, Paolo, Ciari, Lorenzo, Duso, Tomaso, Spagnolo Giancarlo and Vitale, Cristiana, Competition Policy and Productivity Growth: An Empirical Assessment, May 2011.
- 21 Karaçuka, Mehmet and Catik, A. Nazif, A Spatial Approach to Measure Productivity Spillovers of Foreign Affiliated Firms in Turkish Manufacturing Industries, May 2011. Forthcoming in: The Journal of Developing Areas.

- Catik, A. Nazif and Karaçuka, Mehmet, A Comparative Analysis of Alternative Univariate Time Series Models in Forecasting Turkish Inflation, May 2011. Forthcoming in: Journal of Business Economics and Management.
- Normann, Hans-Theo and Wallace, Brian, The Impact of the Termination Rule on Cooperation in a Prisoner's Dilemma Experiment, May 2011. Forthcoming in: International Journal of Game Theory.
- Baake, Pio and von Schlippenbach, Vanessa, Distortions in Vertical Relations, April 2011.
 Published in: Journal of Economics 103 (2011), pp. 149-169.
- Haucap, Justus and Schwalbe, Ulrich, Economic Principles of State Aid Control, April 2011.
- Haucap, Justus and Heimeshoff, Ulrich, Consumer Behavior towards On-net/Off-net Price Differentiation, January 2011.
 Published in: Telecommunication Policy 35 (2011), pp. 325-332.
- Duso, Tomaso, Gugler, Klaus, Yurtoglu, Burcin B., How Effective is European Merger Control? January 2011.

 Published in: European Economic Review, 55 (2011), pp. 980-1006.
- Haigner, Stefan D., Jenewein, Stefan, Müller, Hans Christian and Wakolbinger, Florian, The First shall be Last: Serial Position Effects in the Case Contestants evaluate Each Other, December 2010.
 Published in: Economics Bulletin 30 (2010), pp. 3170-3176.
- Suleymanova, Irina and Wey, Christian, On the Role of Consumer Expectations in Markets with Network Effects, November 2010 (first version July 2010). Forthcoming in: Journal of Economics.
- Haucap, Justus, Heimeshoff, Ulrich and Karacuka, Mehmet, Competition in the Turkish Mobile Telecommunications Market: Price Elasticities and Network Substitution, November 2010.

 Published in: Telecommunications Policy 35 (2011), pp. 202-210.
- Dewenter, Ralf, Haucap, Justus and Wenzel, Tobias, Semi-Collusion in Media Markets, November 2010.
 Published in: International Review of Law and Economics 31 (2011), pp. 92-98.
- Dewenter, Ralf and Kruse, Jörn, Calling Party Pays or Receiving Party Pays? The Diffusion of Mobile Telephony with Endogenous Regulation, October 2010. Published in: Information Economics and Policy 23 (2011), pp. 107-117.
- Hauck, Achim and Neyer, Ulrike, The Euro Area Interbank Market and the Liquidity Management of the Eurosystem in the Financial Crisis, September 2010.
- O8 Haucap, Justus, Heimeshoff, Ulrich and Luis Manuel Schultz, Legal and Illegal Cartels in Germany between 1958 and 2004, September 2010.
 Published in: H. J. Ramser & M. Stadler (eds.), Marktmacht. Wirtschaftswissenschaftliches Seminar Ottobeuren, Volume 39, Mohr Siebeck: Tübingen 2010, pp. 71-94.
- Herr, Annika, Quality and Welfare in a Mixed Duopoly with Regulated Prices: The Case of a Public and a Private Hospital, September 2010. Forthcoming in: German Economic Review.
- O6 Blanco, Mariana, Engelmann, Dirk and Normann, Hans-Theo, A Within-Subject Analysis of Other-Regarding Preferences, September 2010. Published in: Games and Economic Behavior 72 (2011), pp. 321-338.

- Normann, Hans-Theo, Vertical Mergers, Foreclosure and Raising Rivals' Costs Experimental Evidence, September 2010.

 Forthcoming in: The Journal of Industrial Economics.
- O4 Gu, Yiquan and Wenzel, Tobias, Transparency, Price-Dependent Demand and Product Variety, September 2010.
 Published in: Economics Letters 110 (2011), pp. 216-219.
- Wenzel, Tobias, Deregulation of Shopping Hours: The Impact on Independent Retailers and Chain Stores, September 2010.
 Published in: Scandinavian Journal of Economics 113 (2011), pp. 145-166.
- O2 Stühmeier, Torben and Wenzel, Tobias, Getting Beer During Commercials: Adverse Effects of Ad-Avoidance, September 2010.
 Published in: Information Economics and Policy 23 (2011), pp. 98-106.
- Inderst, Roman and Wey, Christian, Countervailing Power and Dynamic Efficiency,
 September 2010.
 Published in: Journal of the European Economic Association 9 (2011), pp. 702-720.

Heinrich-Heine-University of Düsseldorf Düsseldorf Institute for Competition Economics (DICE)

Universitätsstraße 1_ 40225 Düsseldorf www.dice.uni-duesseldorf.de