

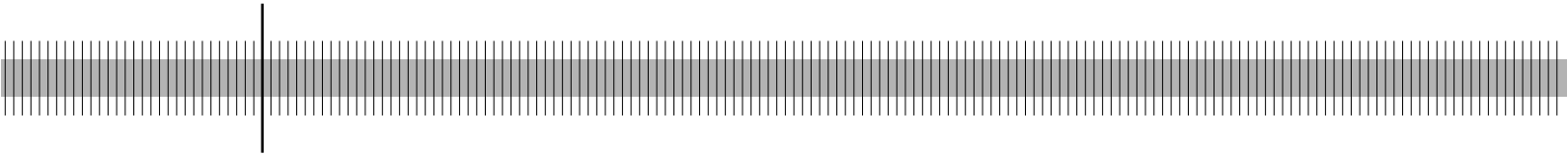
## **Interbank tiering and money center banks**

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**Abstract:**

This paper provides evidence that interbank markets are tiered rather than flat, in the sense that most banks do not lend to each other directly but through money center banks acting as intermediaries. We capture the concept of tiering by developing a core-periphery model, and devise a procedure for fitting the model to real-world networks. Using Bundesbank data on bilateral interbank exposures among 1800 banks, we find strong evidence of tiering in the German banking system. Moreover, bank-specific features, such as balance sheet size, predict how banks position themselves in the interbank market. This link provides a promising avenue for understanding the formation of financial networks.

**Keywords:**

Interbank markets, intermediation, networks, tiering, core and periphery, market structure

**JEL-Classification:**

G21, L14, D85, C63

## Non-technical summary

This paper defines interbank tiering and provides a network characterization founded on intermediation. The interbank market is tiered when some banks intermediate between banks that do not extend credit among themselves. We capture this market structure by formulating a core-periphery model and devise a procedure for fitting the model to real-world networks. This can be thought of as running a regression, but instead of estimating a parameter that achieves the best linear fit, one determines the optimal set of core banks that achieves the best structural match between the observed network and a tiered structure of the same dimension. We show that our procedure delivers a core which is a strict subset of intermediaries, excluding those banks that play no essential role in holding together the interbank market. It also yields a measure of distance that aggregates the structural inconsistencies between the observed network and the nearest tiering model. We use this statistic to test formally whether the extent of tiering observed in the interbank market is significantly greater than what emerges in networks formed by random processes.

Our empirical work relies on comprehensive Bundesbank statistics, which we use to construct the network of bilateral interbank positions between more than 2000 banks. While most banks simultaneously borrow and lend in the interbank market, we find that the core comprises only 2.7% of such intermediaries. Tiering thus delivers a strong refinement of the concept of intermediation. Throughout the available time span (1999Q1–2007Q4), the size and composition of the optimal core remain stable. This supports the view that we have identified a truly structural feature. Moreover, we show that the extent of tiering observed in the German interbank market cannot be replicated by standard random processes of network formation.

The final part of the paper explores why the banking system organizes itself around a core of money center banks by testing whether balance sheet variables predict which kind of banks form the core. The probit regressions confirm that (only) large banks tend to belong to the core, even though economies of scale and scope play a limited role. Other bank-specific variables, such as systemic importance, similarly predict reliably the way a bank chooses to position itself in the interbank network. We also show that the core of the banking system can be predicted by means of a regression that uses only balance sheet variables, which is helpful since most countries do not collect bilateral interbank data.

We show that the interbank market looks very different from what banking theory

imagines. The market is not a centralized exchange, but a sparse network, centered around a tight set of core banks, which intermediate between numerous smaller banks in the periphery. We also make novel use of network concepts that could be of broader interest in the areas of finance and industrial organization. Our approach allows us to measure how far a decentralized market is from a particular benchmark structure. To make a structural quality of interest amenable to quantitative treatment, we formulate a procedure – based on blockmodeling techniques – for fitting a theoretical structure to an observed network. Finally, the econometric part of the paper bridges two largely distinct literatures on individual banks and on network formation. In line with the view that different kinds of banks build systematically different patterns of linkages, we find that bank balance sheets reliably predict which banks position themselves in the core and which remain in the periphery. This link could be of practical use for central banks and regulators wishing to study their domestic interbank networks, for it provides a structured alternative to the entropy method usually employed when no bilateral data are available.

## Nicht-technische Zusammenfassung

In der vorliegenden Studie wird die Schichtung des Interbankenmarkts („Tiering“) definiert und eine auf Intermediation gegründete Netzwerkcharakterisierung vorgenommen. Der Interbankenmarkt untergliedert sich in Ebenen, wenn einige Banken für andere Banken, die einander keine Kredite gewähren, als Intermediär fungieren. Wir bilden diese Marktstruktur ab, indem wir ein Kern-Peripherie-Modell formulieren und ein Verfahren zur Anpassung des Modells an die Netzwerke der realen Welt entwickeln. Dies kann als Regressionsanalyse betrachtet werden, wobei anstatt der Schätzung eines Parameters, der die beste lineare Anpassung gewährleistet, der optimale Kreis von Kernbanken bestimmt wird, der die größte strukturelle Übereinstimmung zwischen dem untersuchten Netzwerk und einer geschichteten Struktur derselben Dimension bietet. Wir zeigen, dass unser Verfahren einen Kern hervorbringt, der eine strikte Teilgruppe von Intermediären darstellt und jene Banken ausnimmt, die für den Zusammenhalt des Interbankenmarkts keine wesentliche Rolle spielen. Das Verfahren führt außerdem zu einer Messgröße der Distanz, bei der die strukturellen Inkonsistenzen zwischen dem untersuchten Netzwerk und dem nächsten Tiering-Modell aggregiert werden. Wir verwenden diese Statistik, um formal zu testen, ob der am Interbankenmarkt beobachtete Grad der Schichtung signifikant höher ist als bei Netzwerken, die auf der Grundlage von Zufallsverfahren gebildet wurden.

Unsere empirischen Untersuchungen beruhen auf umfassenden Statistiken der Bundesbank, die wir zur Erstellung des Netzwerks bilateraler Interbankpositionen unter mehr als 2 000 Banken einsetzen. Während die meisten Institute gleichzeitig als Kreditgeber und Kreditnehmer am Interbankenmarkt agieren, umfasst der Kern nach unseren Erkenntnissen lediglich 2,7 % solcher Intermediäre. Die Schichtung ermöglicht somit eine deutliche Verfeinerung des Konzepts der Intermediation. Die Größe und Zusammensetzung des optimalen Kerns bleiben über die gesamte verfügbare Zeitspanne (1999Q1 – 2007Q4) stabil. Dies stützt die Annahme, dass wir ein wirklich strukturelles Merkmal identifiziert haben. Wir weisen zudem nach, dass sich der Gliederungsgrad des deutschen Interbankenmarkts nicht durch standardmäßige Zufallsverfahren der Netzwerkbildung replizieren lässt.

Im abschließenden Teil der Studie wird untersucht, warum sich das Bankensystem um einen Kern sogenannter Money Center Banks, organisiert. Zu diesem Zweck prüfen wir, ob sich anhand von Bilanzkennzahlen vorhersagen lässt, welche Art von Banken den Kern bilden. Die Probit-Regressionen bestätigen, dass tenden-

ziell (nur) Großbanken zum Kern gehören, wenngleich Skalen- und Verbundeffekte lediglich eine untergeordnete Rolle spielen. Auch anhand anderer bankspezifischer Variablen wie etwa der Systemrelevanz lässt sich zuverlässig vorausschätzen, wie sich eine Bank im Interbankennetzwerk positionieren möchte. Ferner weisen wir nach, dass der Kern des Bankensystems mittels einer Regression, bei der ausschließlich Bilanzkennzahlen zugrunde gelegt werden, vorhergesagt werden kann. Dies ist insofern hilfreich, als die meisten Länder keine bilateralen Interbankdaten erheben.

Wir zeigen, dass sich der Interbankenmarkt sehr stark von den Vorstellungen der Banktheorie unterscheidet. Es handelt sich nicht um einen zentralisierten Markt, sondern um ein weitmaschiges Netz mit einigen wenigen Kernbanken im Zentrum, die als Intermediär zwischen zahlreichen kleineren, in der Peripherie angesiedelten Banken fungieren. Wir bringen auch erstmals Netzwerkkonzepte zum Einsatz, die im Bereich der Finanz- und Industrieorganisation von allgemeinem Interesse sein könnten. Mit unserem Ansatz lässt sich messen, wie weit ein dezentraler Markt von einer spezifischen Benchmark-Struktur entfernt ist. Um eine bestimmte strukturelle Eigenschaft einer quantitativen Behandlung zugänglich zu machen, formulieren wir auf Basis von Blockmodellmethoden ein Verfahren zur Anpassung einer theoretischen Struktur an ein untersuchtes Netzwerk. Abschließend wird im ökonometrischen Teil der Studie eine Brücke zwischen zwei weitgehend unterschiedlichen Zweigen der Fachliteratur zu einzelnen Banken und zur Bildung von Netzwerken geschlagen. Im Einklang mit der Auffassung, dass verschiedene Arten von Banken systematisch unterschiedliche Verbindungsstrukturen aufbauen, stellen wir fest, dass sich anhand von Bankbilanzen zuverlässig vorhersagen lässt, welche Banken sich im Kern positionieren und welche in der Peripherie verbleiben. Dieser Zusammenhang könnte für Zentralbanken und Regulierungsbehörden bei der Untersuchung ihrer inländischen Bankennetzwerke von praktischem Nutzen sein, bildet er doch eine strukturierte Alternative zur Entropiemethode, die üblicherweise angewandt wird, wenn keine bilateralen Daten verfügbar sind.





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# Interbank Tiering and Money Center Banks<sup>1</sup>

## 1 Introduction

This paper proposes the view that interbank markets are tiered, operating in a hierarchical fashion where lower-tier banks deal with each other primarily through money center banks. It may seem peculiar to focus on intermediation between banks; intermediation is traditionally regarded as the activity that banks perform on behalf of non-banks, such as depositors and firms (Gurley and Shaw (1956), Diamond (1984)). The notion that banks themselves rely on another layer of intermediation goes largely unnoticed in the formal banking literature. Yet such hierarchical structures appear to be common in financial markets well beyond banking.

The interbank market is often modeled in the literature as a centralized exchange in which banks smooth liquidity shocks (e.g. Ho and Saunders (1985), Bhattacharya and Gale (1987), or Freixas and Holthausen (2005)). In reality, the interbank market is decentralized: deals are struck bilaterally between pairs of banks, not against a central counterparty (Stigum and Crescenzi (2007)). This defining feature of over-the-counter markets is known to give rise to intermediaries (Duffie et al. (2005), Gale and Kariv (2007)). While some recent models recognize the bilateral nature of the interbank market (e.g. Allen and Gale (2000), Freixas et al. (2000), and Leitner (2005)), the presence of intermediaries, and hence the tiered character of this market,

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<sup>1</sup>The views expressed in this paper do not necessarily reflect those of Deutsche Bundesbank, the Bank of International Settlements, the Federal Reserve Bank of Cleveland, nor the Board of Governors of the Federal Reserve System. We thank the Forschungszentrum der Deutschen Bundesbank for granting access to several sets of German banking statistics. We are grateful to Christian Upper for his input at an early stage of this project. We also thank Charles Calomiris, Fabio Castiglionesi, Marco Galbiati, Jacob Gyntelberg, Carl-Christoph Hedrich, Sujit Kapadia, Sheri Markose, Perry Mehring, Steven Ongena, Nikola Tarashev, Kostas Tsatsaronis, and especially Heinz Herrmann as well as our discussant Rod Garratt. Seminar participants at the Bank of England, Deutsche Bundesbank, the Federal Reserve Bank of Cleveland, the Frankfurt School of Finance and Management, and the Bank for International Settlements also provided helpful comments. Craig: Federal Reserve Bank of Cleveland, Deutsche Bundesbank, and adjunct at the European Business School. Address: P.O. Box 6387, Cleveland, Ohio 44101. Email: ben.r.craig@clev.frb.org; Tel: + 1 216 579 2061. von Peter: Bank for International Settlements, Address: Centralbahnplatz, CH-4002 Basel. Email: Goetz.von.Peter@bis.org. Tel: +41 61 280 8840.

has not been analyzed in any rigorous way. Yet the financial crisis highlighted the need to understand financial market structure, and doing so is a prerequisite for regulatory reform and macroprudential concepts addressing the "too-connected-to-fail" problem.

This paper defines interbank tiering and provides a network characterization founded on intermediation. The interbank market is tiered when some banks intermediate between banks that do not extend credit among themselves. We capture this market structure by formulating a core-periphery model and devise a procedure for fitting the model to real-world networks. This can be thought of as running a regression, but instead of estimating a parameter that achieves the best linear fit, one determines the optimal set of core banks that achieves the best structural match between the observed network and a tiered structure of the same dimension. We show that our procedure delivers a core which is a strict subset of intermediaries, excluding those banks that play no essential role in holding together the interbank market. It also yields a measure of distance that aggregates the structural inconsistencies between the observed network and the nearest tiering model. We use this statistic to test formally whether the extent of tiering observed in the interbank market is significantly greater than what emerges in networks formed by random processes.

Our empirical work relies on comprehensive Bundesbank statistics, which we use to construct the network of bilateral interbank positions between more than 2000 banks. While most banks simultaneously borrow and lend in the interbank market, we find that the core comprises only 2.7% of such intermediaries. Tiering thus delivers a strong refinement of the concept of intermediation. Throughout the available time span (1999Q1–2007Q4), the size and composition of the optimal core remain stable. This supports the view that we have identified a truly structural feature, one that has hitherto only been described in qualitative terms using aggregate data (Ehrmann and Worms (2004), Upper and Worms (2004)). Moreover, we show that the extent of tiering observed in the German interbank market cannot be replicated by standard random processes of network formation. The German interbank network fits the core-periphery model eight times better than Erdős-Rényi random graphs and about two times better than scale-free networks of the same dimension and density.

If tiering is not the result of random processes but of purposeful behavior, there must be economic reasons why the banking system organizes itself around a core of money center banks. The final part of the paper explores this idea by testing whether balance sheet variables predict which kind of banks form the core. The probit

regressions confirm that (only) large banks tend to belong to the core, even though economies of scale and scope play a limited role. Other bank-specific variables, such as systemic importance, similarly predict reliably the way a bank chooses to position itself in the interbank network. We also show that the core of the banking system can be predicted by means of a regression that uses only balance sheet variables, which is helpful since most countries do not collect bilateral interbank data.

Our work makes several contributions. First, we show that the interbank market looks very different from what banking theory imagines. The market is not a centralized exchange, but a sparse network, centered around a tight set of core banks, which intermediate between numerous smaller banks in the periphery. This raises the question of why financial intermediaries build yet another layer of intermediation between themselves. One possibility is the importance of intermediaries for the transmission of information. This function of networks has recently been studied in the social network literature (notably by Calvo-Armengol and Jackson (2004) and Galeotti and Goyal (2010) in this journal). A related issue is that persistence of the hierarchical structure we find could call into question the common assumption that random liquidity shocks are a sufficient basis for explaining interbank activity.

Second, we make novel use of network concepts that could be of broader interest in the areas of finance and industrial organization. Our approach allows us to measure how far a decentralized market is from a particular benchmark structure. To make a structural quality of interest amenable to quantitative treatment, we formulate a procedure – based on blockmodeling techniques – for fitting a theoretical structure to an observed network. We solve this combinatorial problem by an optimization algorithm and devise a new method of hypothesis testing to examine whether the structural quality under study can be expected to arise randomly. The procedure fits any observed network and can be adapted to other theoretical market structures. Our specific choice of a core-periphery structure is based on economic reasoning and delivers a refinement of intermediation. This contrasts with other network papers that often report network measures unrelated to any concepts in banking and finance.

Finally, the econometric part of the paper bridges two largely distinct literatures on individual banks and on network formation. In line with the view that different kinds of banks build systematically different patterns of linkages, we find that bank balance sheets reliably predict which banks position themselves in the core and which remain in the periphery. In other words, the observed network structure is the result

of purposeful behavior, which is driven by factors that are reflected in bank balance sheets. This link could be of practical use for central banks and regulators wishing to study their domestic interbank networks, for it provides a structured alternative to the entropy method usually employed when no bilateral data are available. More generally, this link – between banking-specific features and network structure – is a promising avenue for a better understanding of the formation of financial networks.

## 2 Tiering in the interbank market

This section provides a network characterization of the concept of interbank tiering. It then develops a procedure for fitting the model to real-world networks and implements it through a fast algorithm. The concepts are illustrated by a simple example, and the procedure and hypothesis tests are applied to the large German interbank market. But first we motivate and define interbank tiering.

Note that in defining tiering in terms of interbank credit relations, we focus on a meaningful economic choice. Interbank activity is based on relationships (Cocco et al. (2009)). In order to lend, a bank typically has to run creditworthiness checks (e.g. Broecker (1990)), the cost of which will limit the number of counterparties. As such, a credit exposure is more likely to reflect an economic relationship than many other transactions, such as the submission of a payment. The payments literature uses the term tiering in related sense, to describe access to payment and settlement systems (CPSS (2003), Kahn and Roberds (2009)): in some systems, only few banks are direct members, and other banks have to transact through members to settle payments with each other (e.g. CHAPS in the United Kingdom).<sup>2</sup> However, the routing of payments (on behalf of customers) differs from the extension of credit between banks. Exposures, unlike payments, do not cease to exist after they have been made, so the structure of the resulting network is of greater relevance for financial stability.

### 2.1 From intermediation to tiering

Banks may rely on intermediaries for a variety of functions. One is liquidity distribution, the process of channeling funds from surplus banks to deficit banks (e.g. Niehans

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<sup>2</sup>This literature focuses on the determinants of membership (Kahn and Roberds (2009) and Galbiati and Giansante (2009)). In practice, this involves legal and technological factors as much as economic considerations.

and Hewson (1976), Bruche and Suarez (2010)). Another is risk management: banks may place interbank deposits for purposes of diversification, risk-sharing, and insurance (e.g. Allen and Gale (2000), Leitner (2005)). Banks may also take and place funds in different maturities to alter their maturity profile (e.g. Diamond (1991), Hellwig (1994)). For these and other functions (including custodian or settlement services), banks rely on intermediaries in ways that give rise to interbank credit exposures.

**Definition 1: Interbank intermediation.** *An interbank intermediary is a bank acting both as lender and borrower in the interbank market.*

This is the standard concept of financial intermediation, applied more narrowly to the banking market. The set of interbank intermediaries can be identified from existing banking data as the subset of banks recording both claims *and* liabilities vis-à-vis other banks on their balance sheet. Our concept of interbank tiering describes the interbank structure that arises when *some* banks intermediate between banks that *do not* extend credit among themselves.

**Definition 2: Interbank tiering.** *Some banks (the top tier) lend to each other and intermediate between other banks, which participate in the interbank market only via these top-tier banks.*

An interbank market is tiered when it is organized in layers, which we call tiers to evoke the hierarchical nature of the concept – in contrast with a "flat" structure without intermediaries. This can be expressed in terms of bilateral relations between top-tier and lower-tier banks:

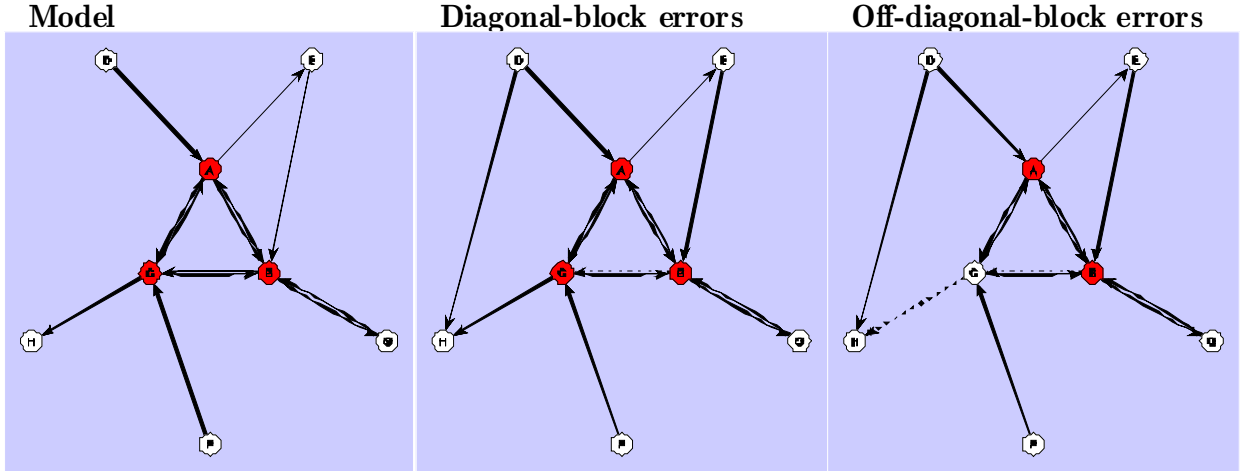
$$\left\{ \begin{array}{l} 1. \text{ Top-tier banks lend to each other,} \\ 2. \text{ lower-tier banks do not lend to each other,} \\ 3. \text{ top-tier banks lend to (some) lower-tier banks, and} \\ 4. \text{ top-tier banks borrow from (some) lower-tier banks.} \end{array} \right. \quad (1)$$

This formulation conveys several important points. Tiering is a structural property of the *system*, not a property of any individual bank. Furthermore, tiering is a *network* concept: the banks in the system are partitioned into two sets based on their *bilateral relations* with each other. At the same time, unlike other network concepts, tiering is founded on an *economic* concept that is central to banking and finance, intermediation. In fact, tiering is a refinement of intermediation: top-tier banks are special intermediaries that play a central role in holding together the interbank market.

Before developing a formal characterization, we provide a simple illustration of interbank tiering.

**Example.** Consider the left panel of Figure 1 (the other panels will be discussed later). Banks  $\{D, F, H\}$  are either lenders or borrowers, not both. The set of intermediaries thus consists of the remaining banks  $\{A, B, C, E, G\}$ . Bank  $C$ , for instance, intermediates from lender  $F$  to borrower  $H$ . It takes a chain of banks (involving  $A$  and  $C$ ) to intermediate from  $D$  to  $H$ . The top tier consists of a strict subset of intermediaries, namely  $\{A, B, C\}$  shown in solid color, while the remaining banks constitute the lower tier. For this partition of banks, the relations within and between the two sets exactly match the relations listed in (1). Banks  $E$  and  $G$  are intermediaries, but they belong to the lower tier because they are not sufficiently connected with other banks to qualify for the top tier (where they would violate the relations 1, 3 and 4). This reflects the fact that these two banks play no role in connecting lower-tier banks to the interbank market.





The left panel illustrates a perfectly tiered interbank structure in a stylized interbank market comprising 8 banks. The arrows represent the direction of credit exposure, e.g. bank D lends to A. The middle and right panels depict examples of networks that are not perfectly tiered.

Figure 1: Stylized example of an interbank market

This example illustrates a perfectly tiered interbank structure. In reality, the presence of tiering will be a matter of degree. Much of what follows serves to develop methods that formalize how to think about the distance between real-world networks and perfectly tiered structures.

## 2.2 Network characterization of tiering

This section develops a structural representation for our definition of interbank tiering. This will serve as a benchmark model against which empirical interbank market structures can be assessed. A network consists of a set of nodes that are connected by links. Taking each bank as a node, the interbank positions between them constitute the network, which can be represented as a square matrix of dimension  $n$  equal to the number of banks in the system. The typical element  $(i, j)$  of this matrix represents a gross interbank claim, the value of credit extended by bank  $i$  to bank  $j$ . Row  $i$  thus shows bank  $i$ 's bilateral interbank claims, and column  $i$  shows the same bank's interbank liabilities to each of the banks in the system. The diagonal elements  $(i, i)$  are zero when treating banks as consolidated entities (with intragroup exposures netted out). Off-diagonal elements are positive, or zero in the absence of a bilateral

position. Real-world interbank data typically give rise to directed, sparse and valued networks.<sup>3</sup> Since the concept of tiering is about the bilateral *structure* of linkages, we code the presence or absence of a link by 1 or 0, as is common practice in network analysis. Thus, non-symmetric binary matrices will be used to represent the model and the empirical interbank network in our application.

We characterize a perfectly tiered structure in the shape of a network. The bilateral relations (1) consistent with our definition of tiering are mapped into a matrix,  $M$ , with top-tier banks ordered first. For reasons that will become clear shortly, we shall call the set of top-tier banks "the core" ( $C$ ), and the set of lower-tier banks "the periphery" ( $P$ ). The nodes within each tier are equivalent with respect to the nature of their linkages with other nodes. Hence it suffices to specify the generic relations within and between the two tiers as a *blockmodel*,<sup>4</sup>

$$M = \begin{pmatrix} CC & CP \\ PC & PP \end{pmatrix}.$$

The block denoted by  $CC$  ("core to core") specifies how top-tier banks relate to other core banks: when they all lend to each other, as specified in (1),  $CC$  is a block of ones (ignoring the zero diagonal). Likewise, periphery banks *not* lending to each other makes  $PP$  a square matrix of zeros. Core banks lending to some banks in the periphery means that  $CP$  must be "row regular", meaning that it contains at least one link in every row. Similarly, when all core banks borrow from at least one periphery bank,  $PC$  is a "column regular" matrix with at least one 1 in every column.

Our definition of tiering therefore translates into the choice and location of specific block types. (Other theories would require different block types, but our procedure for estimating the implied market structure would still apply.) The blockmodel of tiering consists of a complete block (denoted  $\mathbf{1}$ ) and a zero block ( $\mathbf{0}$ ) on the diagonal, which specifies relations within the tiers, and two off-diagonal blocks specifying relations

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<sup>3</sup>The networks are directed, because a claim of bank  $i$  on  $j$  (an asset of  $i$ ) is not the same as a claim of  $j$  on  $i$  (a liability of  $i$ ). They are sparse as only a small share of the  $n(n - 1)$  potential bilateral links are used at any point in time. Finally, interbank networks are valued because interbank positions are reported in monetary values, as opposed to 1 or 0 indicating the presence or absence of a claim.

<sup>4</sup>Blockmodels are theoretical reductions of networks and have a long tradition in the analysis of social roles (Wasserman and Faust (1994)).

between the tiers:  $CP$  must be row-regular ( $\mathbf{RR}$ ), and  $PC$  column-regular ( $\mathbf{CR}$ ).<sup>5</sup>

$$M = \begin{pmatrix} \mathbf{1} & \mathbf{RR} \\ \mathbf{CR} & \mathbf{0} \end{pmatrix}. \quad (2)$$

This model specifies the market *structure* only – the overall size of  $M$  and its blocks will be determined once we set the number and identity of banks allocated to each tier. If  $c$  banks end up in the core, then the block  $CP$ , for instance, will be a matrix of dimension  $c \times (n - c)$ . One easily verifies that our simple example of tiering (Figure 1, left panel) conforms with the blockmodel  $M$  (with  $n = 8$ ,  $c = 3$ ),

$$\begin{pmatrix} \mathbf{1} & \mathbf{RR} \\ \mathbf{CR} & \mathbf{0} \end{pmatrix} = \left( \begin{array}{ccc|cccc} 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \\ \hline 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array} \right).$$

Our network characterization of tiering is a refinement of the general *core-periphery* model in sociology. In social network analysis, this label is attached to any network with a dense cohesive core and a sparse periphery (Borgatti and Everett (1999)), as reflected in the diagonal blocks  $\mathbf{1}$  and  $\mathbf{0}$  in (2). However, the core-periphery model in this literature does *not* specify how the core and periphery are related to each other; the blocks on the off-diagonal could be of any type and are often ignored in the analysis (as recommended by Borgatti and Everett (1999)). In building on intermediation, our model of tiering does specify how the core and periphery should be related: core banks borrow from, and lend to, at least one bank in the periphery; they *intermediate* between banks in the periphery and thereby hold together the entire interbank market.

This particular focus on how the core and periphery are related is based on an economic rationale that seems appropriate for the interbank market. Core banks are in the market at all times and incur interbank positions with important counterparties in the normal course of business (hence  $CC = \mathbf{1}$ ). Periphery banks, on the other hand, might only lend, or borrow, or might not participate in the interbank market at all

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<sup>5</sup>These terms come from the literature on generalized blockmodeling (Doreian et al. (2005)). A column-regular block,  $\mathbf{CR}$ , has each column (but not necessarily each row) covered by at least one 1; the  $\mathbf{RR}$  block has each row covered by at least one 1.

when they have no deficits or risks to cover at that moment. It would be too restrictive to require that every bank in the periphery has to be connected;<sup>6</sup> but the periphery as a whole should certainly be linked to the core, or else there would not be a single cohesive interbank market.<sup>7</sup> The choice of row- and column-regular blocks on the off-diagonal of  $M$  finds the right balance by placing strong restrictions only on core banks: every core bank must be connected to at least one bank in the periphery, but the converse need not hold.

## 2.3 Testing for structure

We now focus on how to determine the extent to which an observed real-world network exhibits tiering. How does one test for the entire structure in a network? Visual inspection is instructive but inconclusive for large networks, and traditional network statistics do not relate to any underlying model, tiered or otherwise. Our approach is to compare the network of interest with the model in terms of a measure of distance that aggregates the structural inconsistencies between them. If the observed network and the best-fitting tiering model remain at great distance from each other, then the network does not have a tiered structure.

We formulate a procedure for fitting the model  $M$  to an observed network  $N$ . This can be thought of as running a regression, but instead of estimating the parameter  $\beta$  that achieves the best linear fit, one determines the optimal set of core banks that achieves the best structural match between  $N$  and  $M$ , a perfectly tiered structure. We show that the solution has the desirable property that the core is a strict subset of all intermediaries. Finding this solution is a large-scale problem in combinatorial optimization for which we develop a fast algorithm. We then evaluate the degree of tiering in the observed network by testing the goodness of fit against the distribution obtained from fitting random networks for which tiering is not expected to emerge.

### 2.3.1 Fitting the model to a network

The tiering model  $M$  serves as the benchmark for assessing the extent of tiering inherent in an observed interbank network  $N$ . These two objects have to be made

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<sup>6</sup>This would be the result of defining  $CP$  and  $PC$  as complete ( $\mathbf{1}$ ) or regular blocks. A regular block has at least one 1 in every row *and* column, implying that every periphery bank lends to, *and* borrows from, some bank in the core (which would make all banks in the system intermediaries).

<sup>7</sup>This degenerate case of an unconnected periphery is permitted in the weak core-periphery model (with  $CP$  and  $PC$  zero blocks) discussed by Borgatti and Everett (1999).

comparable. The observed network  $N$  is a square matrix of dimension  $n$  equal to the number of banks, with  $N_{ij} = 1$  if bank  $i$  lends to bank  $j \neq i$ , and  $N_{ij} = 0$  otherwise. The model  $M$ , on the other hand, is a generic structure that embodies the relations in (1) for any dimension. The fitting procedure involves two steps: first, we define a measure of distance between the network and the model  $M$  of the same dimension, using (2) as the matching criterion; then, we solve for the optimal (distance-minimizing) partition of banks into core and periphery. Working with the optimal fit takes care of the problem that tiering is a qualitative concept that does not depend on the exact size of the core (or periphery) as long as there are two tiers.

The measure of distance we adopt, following the generalized blockmodeling approach of Doreian et al. (2005), is a total error score. It aggregates the number of inconsistencies between the observed network and the chosen model. Consider an arbitrary partition where  $c$  banks are considered for the core, leaving  $(n - c)$  banks in the periphery. Denote the set of core banks by  $C$ ; ordering core banks first (and rearranging  $N$  by permutation accordingly) makes  $C = \{1, 2, \dots, c\}$ . This partition divides the observed matrix  $N$  into four blocks, and the model  $M$  predicts how each block should look in a perfectly tiered network of the same dimension. In particular, the top tier  $CC$  should be a complete block  $\mathbf{1}$  of size  $c^2$ , so any missing link (outside the diagonal) presents an inconsistency with the model (2), as one core bank has no exposure to another. Likewise, any observed link within the periphery ( $PP$ ) constitutes an error relative to  $M$ , as periphery banks should not transact directly with each other in a perfectly tiered market. Errors in the off-diagonal blocks penalize zero rows (columns), because these are inconsistent with row-regularity (column-regularity, respectively): a zero row in  $CP$  indicates that a core bank fails to lend to *any* of the  $(n - c)$  banks in the periphery, violating a defining feature of core banks. Similarly, a zero column in  $PC$  shows that the corresponding core bank does not borrow at all from the periphery, producing as many errors as there are banks in the periphery  $(n - c)$ . The aggregate errors in each of these blocks are thus given by the following sums,

$$E = \begin{pmatrix} c(c-1) - \sum_{i \in C} \sum_{j \in C} N_{ij} & (n-c) \sum_{i \in C} \max\{0, 1 - \sum_{j \notin C} N_{ij}\} \\ (n-c) \sum_{j \in C} \max\{0, 1 - \sum_{i \notin C} N_{ij}\} & \sum_{i \notin C} \sum_{j \notin C} N_{ij} \end{pmatrix}. \quad (3)$$

The total error score aggregates the errors across the four blocks.<sup>8</sup> We normalize the

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<sup>8</sup>The aggregation of errors can be adapted to cases in which one type of error is more consequential

error score by the total number of links in the observed network,

$$e = \frac{E_{11} + E_{22} + (E_{12} + E_{21})}{\sum_i \sum_j N_{ij}}. \quad (4)$$

The total error score is our measure of distance; it is a function since every possible partition into two tiers is associated with a particular value of  $e$ . Denote this function by  $e(C)$ , where  $C$  stands for the set of banks under consideration for the core. The optimal core,  $C^*$ , is the set(s) of banks that produces the smallest distance to the model  $M$  of the same dimension,

$$\begin{aligned} C^* &= \arg \min e(C) \\ &= \{C \in \Gamma \mid e(C) \leq e(c) \forall c \in \Gamma\}, \end{aligned} \quad (5)$$

where  $\Gamma$  denotes all strict and non-empty subsets of the population  $\{1, 2, \dots, n\}$ . Intuitively, the expression (5) determines the number and identity of banks in  $N$  that are core banks in the sense of the interbank tiering model. The following example illustrates in a simple way how structural inconsistencies between  $N$  and  $M$  are measured by the distance function and minimized by the optimal core.

**Example.** Consider Figure 1, where the left panel shows our earlier example of a tiered structure ( $M$ ). The other panels depict examples of networks that are not perfectly tiered ( $N$ ). In the middle panel, suppose we knew that banks  $\{A, B, C\}$  are good candidates for the core. If so, however, we observe that one core bank ( $B$ ) does not lend to another core bank  $C$ , and periphery bank  $D$  lends directly to another ( $H$ ). Accordingly, the matrix (3) yields one error in each of the diagonal blocks  $CC$  and  $PP$ . As no other partition attains a lower error score,  $\{A, B, C\}$  remains the optimal core, as it minimizes the total error score to  $e(C^*) = 2/13$ .

Suppose we conjecture that  $\{A, B, C\}$  also forms the core of the network in the right panel. We observe that one putative core bank does not lend to the periphery at all; this immediately generates 5 fitting errors in block  $CP$  for  $C$ 's failure to lend to *any* of the 5 banks in the periphery. Moving  $C$  to the periphery instead causes a single error (its continued link with periphery bank  $F$ ), in addition to the existing error ( $D$  lending to  $H$ ). The distance between the network and the model can

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than another. E.g. multiplying  $(E_{12} + E_{21})$  by a parameter below unity deemphasizes the relation between core and periphery; multiplying  $E_{11}$  by a number above unity will yield a solution with a smaller, tightly connected core. As no theoretical priors on intermediation suggest otherwise, we use the equally weighted aggregation of errors, in line with the overall dimension of the network.

thus be reduced by placing bank  $C$  in the periphery, i.e. by considering a tiering model with only two nodes in the core (and six in the periphery). The optimal fit yields two errors in the (enlarged) periphery, none in the (reduced) core  $\{A, B\}$ , and none again in the off-diagonal blocks, for a total score of  $e(C^*) = 2/12$ . The new core excludes bank  $C$ , which obviously remains an intermediary, illustrating that the core comprises only those intermediaries that intermediate between banks in the periphery, as required by Definition 2.

Real-world network are far more complex than this example suggests, with structures that may be arbitrarily far removed from that of a tiered market. This makes it essential to understand the properties of the optimal fit and to develop an efficient procedure for arriving at this solution. We now show that the solution preserves the main features illustrated in this simple example.

### 2.3.2 Properties of the solution

The procedure of minimizing the distance between model  $M$  and network  $N$  delivers the optimal partition of banks into core and periphery. Based on our definition of distance (3)-(4), the solution has the following properties:

**Proposition 1:**

- (a) The presence of intermediaries is necessary and sufficient for a core-periphery structure:
  - (i) A network without intermediaries has no core.
  - (ii) A network with intermediaries has a core (and a periphery under one weak condition).
- (b) The core is a (strict) subset of the set of intermediaries:
  - (i) All core banks are intermediaries, but
  - (ii) Intermediaries are not part of the core if they do not lend to, *or* do not borrow from, the periphery.

Proof: see Appendix A. The first property relates to existence and shows that the distance-minimizing procedure can identify a core-periphery structure in virtually all networks. The sufficient condition for a core is the presence of at least one intermediary. A periphery always exists under the weak (and sufficient) condition that the network contains either unattached banks, or one missing bilateral link. This is intuitive, since an interbank market in which every bank lends to all other banks, as

in Allen and Gale (2000), cannot be regarded as tiered but must be viewed as "flat", since banks are all equal in their connection patterns. The core-periphery model can be fitted under conditions that are satisfied by all realistic interbank networks.

The second property shows that our concept of tiering delivers a useful refinement on the concept of intermediation: the core is a strict subset of all intermediaries. Core banks are special intermediaries that connect banks in the periphery. While this property is, of course, in line with our definition of tiering (and thus embodied in  $M$ ), the result states that this property carries over one-for-one to the solution when fitting  $M$  to an observed network  $N$ . This is remarkable, because one would expect any statistical fitting procedure on a large network to produce some errors in every block of (3). However, the off-diagonal blocks governing the relations between core and periphery have error scores of exactly zero. Consequently, the error score (4) at the optimum takes the simple form

$$e(C^*) = \frac{E_{11} + E_{22}}{\sum_i \sum_j N_{ij}}. \quad (6)$$

We have encountered these properties of the solution in the example above, where off-diagonal errors were zero and the optimal core  $\{A, B\}$  was a strict subset of all intermediaries  $\{A, B, C, E, G\}$ . The traditional core-periphery model, which disregards off-diagonal blocks (Borgatti and Everett (1999)), would have retained bank  $C$  in the core (in Figure 1, right panel), even though  $C$  no longer intermediates between banks in the periphery.

### 2.3.3 Implementation

Fitting the model to a real-world network is a large-scale problem in combinatorial optimization. Only for very small networks can the solution be found by exhaustive search. In our example with 8 banks, for instance, computing the total error scores for each of the  $2^8 = 256$  possible partitions confirms that  $\{A, B\}$  is indeed the (unique) solution that minimizes the error function. This brute-force approach becomes infeasible for larger networks. A medium-sized banking system of some 250 banks already requires on the order of  $10^{78}$  possible subsets ( $2^n$ ) to be evaluated for determining the optimal core. The problem of finding an optimal subset – which our paper shares with Kirman et al. (2007) and Ballester et al. (2010) – is *NP-hard*. The computational complexity of such problems rises exponentially with  $n$ , so that they cannot be solved by exhaustive search. The goal of fitting the model to realistic



networks, such as the German interbank market with close to 2000 active banks, calls for a more pragmatic procedure.

Our implementation thus relies on a sequential optimization algorithm, which follows closely the switching logic employed in our proof of Proposition 1. An initial random partition is evaluated and improved upon by moving banks between the core and periphery until the total error score (4) can no longer be reduced. The greedy version of our algorithm follows the steepest descent, switching from one tier to another the bank that contributes most to the error score at each iteration. To avoid running into local optima, a second version employs simulated annealing, which allows for a degree of randomness when moving banks, which declines monotonically as the optimum is being approached. One way to test whether the procedure returns a global optimum is by inspecting the associated  $E$ , since we know from Proposition 1 that a genuine solution necessarily comes with a diagonal error matrix. Appendix B describes the robustness checks we performed to ascertain that the procedure converges to a global optimum. The main programming challenge consisted of reducing the algorithm’s polynomial running time from order  $n^3$  to  $n^1$ . This made the algorithm sufficiently fast for the repeated applications necessary for hypothesis testing.

### 2.3.4 Hypothesis test against random networks

Having shown how to fit the model, we address the issue of significance: how can one evaluate the extent to which the observed network exhibits tiering? The closer the network resembles a tiered structure, the lower will be the error score (6). For a formal test, one must compare the distance between the network and the model to some benchmark. Selecting a benchmark, however, is not straightforward since we are assessing a *qualitative* feature relating to market structure. Moreover, it would be questionable – as in econometrics – to change, without a theoretical basis, the underlying model only to improve the statistical fit. It is easy to reduce the total error score by choice of a weaker model, for instance by replacing the complete block  $\mathbf{1}$  in (2) by a (more accommodative) regular block.<sup>9</sup> Such an ad hoc change in the structure would undermine the theoretical arguments advanced in Section 1.2, which led to this particular model. We therefore adopt a different strategy for evaluating

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<sup>9</sup>Model selection remains an underexplored area in blockmodeling. Doreian et al. (2005) provide no clear guidance, although they rightly caution against selecting among block types to minimize the number of structural inconsistencies.

significance.<sup>10</sup>

In a first step, we assess whether a tiering model is worth fitting at all. Recall that our measure of distance (4)-(6) normalizes the aggregate error by the total number of links in the observed network,  $\Sigma\Sigma N_{ij}$ . This is also the maximum error under the alternative hypothesis that the network comprises only a periphery. The minimum distance  $e(C^*)$  can therefore be used in a basic test, similar in spirit to an F-test of joint significance which tests whether it is worth including regressors at all.<sup>11</sup> If  $e(C^*) \geq 1$ , then there is no value in fitting a tiering model: doing so generates more structural inconsistencies than does a "flat" model with a periphery alone. In that case there is no evidence of a core standing out as a separate tier.<sup>12</sup> We require that  $e(C^*)$  attain a value well below unity to proceed.

In the second step, our strategy is to vary the data rather than the model: we test the total error score against the Monte Carlo distribution function from a data-generating process in which tiering is not expected to emerge. In particular, the error  $e(C^*)$  associated with the observed network  $N$  is tested against the error distribution obtained by fitting simulated networks where links are formed by exogenous statistical processes. The standard classes are *random graphs* introduced by Erdős and Rényi and *scale-free networks* popularized by Albert and Barabási and widely observed in the natural sciences (Newman et al. (2006)):

- A *random graph* is obtained by connecting any two nodes with a fixed and independent probability  $p$ . Any realization of such a network also has an expected density of  $p$ . A node can be expected to have a *degree*, or number of links, of  $p(n - 1)$  on each side in the case of a directed network. The expected degree distribution around this characteristic value is Binomial, converging to Poisson for large  $n$ .

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<sup>10</sup>Our approach of comparing a network to a *specific model* contrasts with the maximum likelihood method developed by Copic et al. (2009), which finds the partition with the highest probability of producing the observed network. (Wetherilt et al. (2009) apply this method to the 13 banks observed in the UK large-value payment system CHAPS.) In contrast to our approach of fitting an underlying model, their method *specifies* the likeliest community structure, defined as groups of nodes more likely to connect within than across groups. However, community structure differs from our core-periphery notion: periphery banks are in the lower tier precisely because they are *unlikely* to connect to each other.

<sup>11</sup>This test requires no distribution, since the observed network comprises the full population (not only a sample) of nodes.

<sup>12</sup>The other side of the test (a "flat" model with only a core) can be disregarded, except in the unusual case where the density of the observed network exceeds 50%.

- A *scale-free network*, on the other hand, has no characteristic scale: nodes with a lower degree are proportionately more likely than nodes with  $k$  times that degree, for any  $k$ . The degree distribution thus follows a power law. One statistical process giving rise to scale-free networks is known as *preferential attachment*, whereby new nodes attach to existing nodes with a probability proportional to the latter's degrees. This formation process tends to produce a few highly connected hubs, suggesting that scale-free networks match interbank networks more closely than do random graphs.

Random and scale-free models are not hierarchical in nature (Ravasz and Barabási (2003)). The purely statistical nature of these network formation processes is at odds with the idea that banks, by purposeful economic choice, organize themselves around a core of intermediaries, giving rise to interbank tiering. We therefore generate 1000 random networks of the same dimension and density as the observed network  $N$ , and fit the model  $M$  to *every* realization. This allows us to trace out an empirical distribution function  $F_e$  for the error score in an environment where tiering occurs only by chance. We say that  $N$  exhibits a significant degree of tiering if the associated test statistic  $e(C^*)$  is closer to zero than the bottom percentile of the distribution function found for random networks,

$$\text{Reject } H_0 \text{ if: } e(C^*) < F_e(0.01).$$

This significance test can be conducted separately for each class of random networks, Erdős-Rényi and scale-free. It can also be understood as rejecting the hypothesis that networks formed by standard random processes would produce the extent of tiering observed in  $N$ . As tiering is not expected to arise in such networks, it must be the result of incentives of banks for linking to each other in this particular way. Following our application, we explore this direction in the final section.

## 3 Application to the German banking system

### 3.1 Constructing the interbank network

We employ a set of comprehensive banking statistics known as the “*Gross- und Millionenkreditstatistik*” (statistics on large loans and concentrated exposures). The data are compiled by the Evidenzzentrale der Deutschen Bundesbank. According to the

Banking Act of 1998, financial institutions located in Germany must report on a quarterly basis each counterparty to whom they have extended credit in the amount of at least €1.5 million or 10% of their liable capital. If either threshold is exceeded at any time during the quarter, the lender reports outstanding claims (of any maturity) as they stand at the end of the quarter. From these reports, the Bundesbank assembles the central credit register, which is employed by reporting institutions for monitoring borrower indebtedness and by the authorities for monitoring individual exposures and the overall financial system.

The nature of these data presents several advantages. Claims are reported with a full counterparty breakdown vis-à-vis thousands of banks and firms. The bilateral positions are therefore directly observed and need not be estimated as in many other studies.<sup>13</sup> This makes it legitimate to apply network methods. Second, positions are quoted in monetary values (in millions of euros), indicating both the presence and strength of bilateral links. As the concept of tiering is about the structure of linkages, however, the monetary values are used here only to indicate the presence of a credit exposure. Third, the data are available on a quarterly basis since 1999Q1, which allows us to observe the structure of the network over time.

We gathered all reported bilateral positions between banks to construct the interbank network. To capture relations between legal entities (rather than internal markets), we consolidated banks by ownership at the level of the Konzern (bank holding company), thereby purging intragroup positions. We also excluded cross-border linkages in order to obtain a self-contained network (since further linkages of counterparties abroad remain unobserved). The resulting network is represented as a square matrix  $N$  with 4.76 million cells containing the bilateral interbank exposures among 2182 banks (including subsidiaries of foreign banks) located in Germany.

Some basic statistics convey a first impression. The German banking system is one of the largest in the world, with assets totaling €7.6 trillion (\$11 trillion) at the end of 2007. Reflecting the key role of the interbank market, consolidated domestic interbank positions sum to €1.056 trillion, making up a sizeable share of banks' balance sheets. Even after Konzern-level consolidation, the number of active banks

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<sup>13</sup>Bilateral interbank positions often have to be either reconstructed from payment flows (e.g. Furfine (2003), Bech and Atalay (2010), and Wetherilt et al. (2009)), or estimated from balance sheet data using entropy methods (Upper and Worms (2004), Boss et al. (2004)). Mistrulli (2007) documents the resulting bias when estimating contagion (see Degryse et al. (2009) for a survey). More importantly for our purposes, the entropy method spreads linkages so evenly that essential qualitative features of the network structure would disappear.

in the interbank market varies between 1760 to 1802 for our sample period. This set comprises, on average, 40 private credit banks (Kreditbanken), 400 savings banks (Sparkassen), 1150 credit unions (Kreditgenossenschaften), and 200 special purpose banks. Yet the network is sparse, with a density on the order of 0.41% of possible links (0.61% when excluding banks with no interbank borrowing or lending).<sup>14</sup> This sparsity suggests the presence of a discernible structure. The German banking system thus represents a network of interest not only in its own right, but also affords an opportunity to test whether a network of this size can be characterized with a simple core-periphery structure.

### 3.2 Fitting the core-periphery model

We now fit the tiered structure  $M$  to the German interbank network. The first results focus on a representative mid-sample quarter, 2003 Q2, in which 1802 banks (out of 2182) participated in the interbank market, 1671 as intermediaries, 67 as lenders only, and 64 as borrowers only. The fact that a large share (76.6%) of banks both lend and borrow is not unique to the German interbank market (e.g. 66% of banks in the Portuguese interbank market do so, see Cocco et al. (2009)). Using the procedure developed above, the optimal core was found to include 45 banks.<sup>15</sup> This is indeed a strict subset, comprising only 2.7% of intermediaries. As expected from Proposition 1, the core includes only those intermediaries that borrow from, and lend to, the periphery (the lower tier). The core excludes all those banks that appear as intermediaries in the data but play no essential role in the market. Many banks simply transform their maturity profile by taking and placing funds in different maturities, often with a single counterparty in the core (see also Ehrmann and Worms (2004)).

This finding confirms that the core is a strong refinement of the concept of intermediation. The core here is much smaller than what is sometimes called the core in other network studies.<sup>16</sup> By building on intermediation, our model of tiering leads to

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<sup>14</sup>Further network measures for the German interbank market are reported in Craig, Fecht, and von Borstel (2010).

<sup>15</sup>The optimal fit was robust across algorithms, as described in Appendix B.

<sup>16</sup>For Broder et al. (2000), the core of the worldwide web is the *giant strongly connected component* (GSCC), the set of pages that can reach one another through hyperlinks in both directions. Pages that can reach (or can be reached by) the core make up the *giant in-component* (or *out-component*, respectively). Broder et al. (2000) and subsequent studies thus use the core-periphery notion in a weaker sense of "reachability", regardless of how many links (and thus intermediaries) it takes for

a tighter core, comprising only 2% of banks in the network (see Figure 2). Yet the interbank market would not be a single market without this core. The exact size of the core, however, is less important than its existence in the first place; the core would contain fewer banks, for instance, if one attached a higher penalty on errors within the *CC* block than on those in other blocks. The total error score (4) of the optimal fit

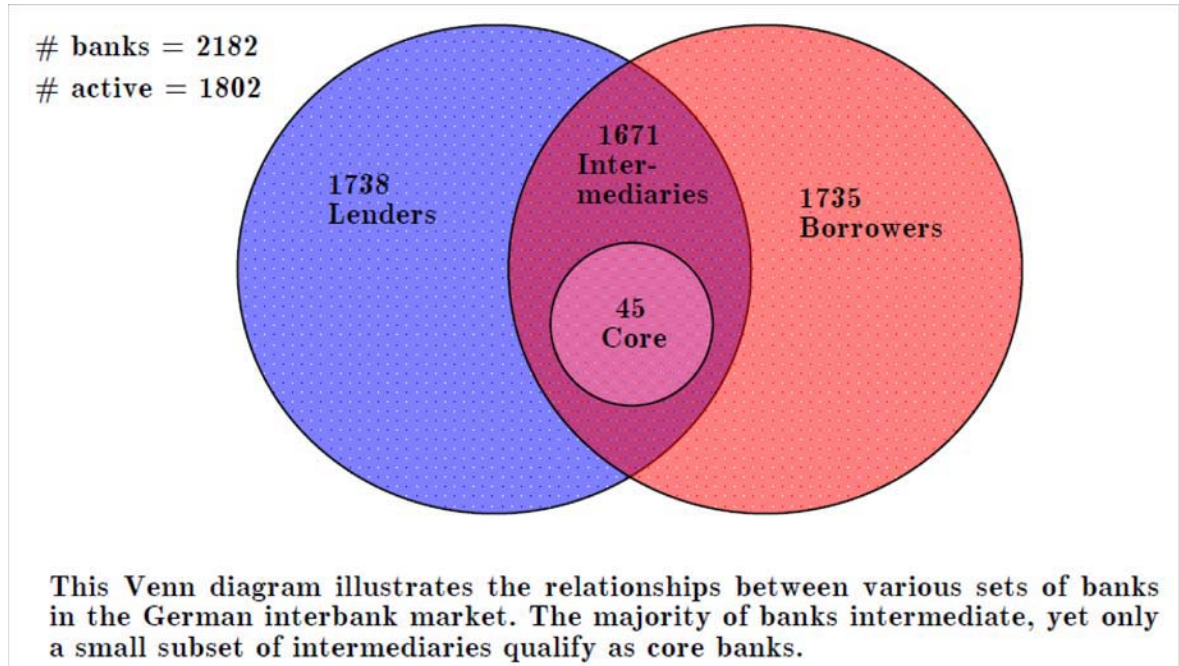


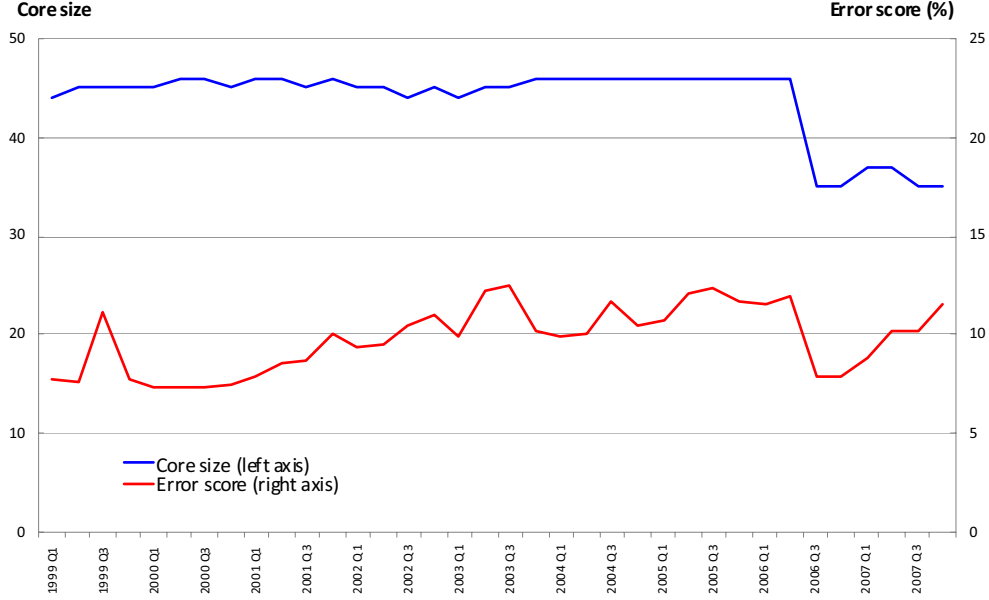
Figure 2: Tiering as a refinement of intermediation

came to 12.2% of network links. This is an average of 1.3 errors per bank, compared to an average of 11 links per active bank. Normalizing instead by the dimension of the network ( $= n(n - 1)$ ) shows that only 0.074% of all cells prove inconsistent with the model  $M$ . The total number of errors reached its minimum at 2406, comprising 683 errors (missing interbank links) within the core. The density of the core is still 66%, more than 100 times greater than the overall density of the network. The error matrix (3) inevitably features no errors in the off-diagonal blocks, consistent with the theoretical properties derived in Proposition 1. The majority of errors (1723) therefore occur because there are direct transactions taking place among banks in the

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one page to reach another. As a result, their core is a large subset (28%) of all pages in the sample. Applied to the Fedwire payment network, Soramäki et al. (2007) find the GSCC to comprise nearly 80% of banks in the network.

periphery. We track the evolution of the network on a quarterly basis from 1999Q1



The figure shows the size of the estimated core (number of banks, left axis) and the total error score (expressed as a percentage of links as in equation (4), right axis) for the German interbank network on a quarterly basis.

Figure 3: Structural stability over time

through 2007Q4. The structure we identified is highly persistent. First, the size of the core and the associated error score are stable over time (see Figure 3). The exception is the apparent break in series in 2006Q3, where a number of mergers reduced the size from 44-46 banks prior to this date, to 35-37 banks thereafter.<sup>17</sup> Importantly, the composition of banks within the core also remains remarkably stable over time. This can be shown by means of the estimated transition matrix,

$$P(s|s') = \begin{pmatrix} & \text{Core} & \text{Periphery} & \text{Exit} \\ \text{Core} & 0.940 & 0.049 & 0.011 \\ \text{Periphery} & 0.001 & 0.991 & 0.008 \\ \text{Exit} & 0 & 0 & 1 \end{pmatrix}. \quad (7)$$

<sup>17</sup>A number of mergers among banks in the core occurred, so the new core became a subset of the old core including the consolidated banks.

The element  $P_{\text{Core-Periphery}}$  represents the frequency with which core banks move to the periphery over time. The third state (outside the sample) takes care of exits from the banking population. The fact that the values on the diagonal are close to unity confirms that banks tend to remain in the same tier (core or periphery). Estimating a separate transition matrix for each quarter demonstrates its stability over time (Figure 4).<sup>18</sup>

These findings support the idea that we have identified a truly structural feature of the interbank market. The persistence of this tiered structure poses a challenge to interbank theories that build on Diamond and Dybvig (1983). If unexpected liquidity shocks were the basis for interbank activity, should the observed linkages not be as random as the shocks? Should the observed network not change unpredictably every period? If this were the case, it would make little sense for central banks and regulatory authorities to run interbank simulations gauging future contagion risks. The stability of the observed interbank structure suggests otherwise.

### 3.2.1 Robustness

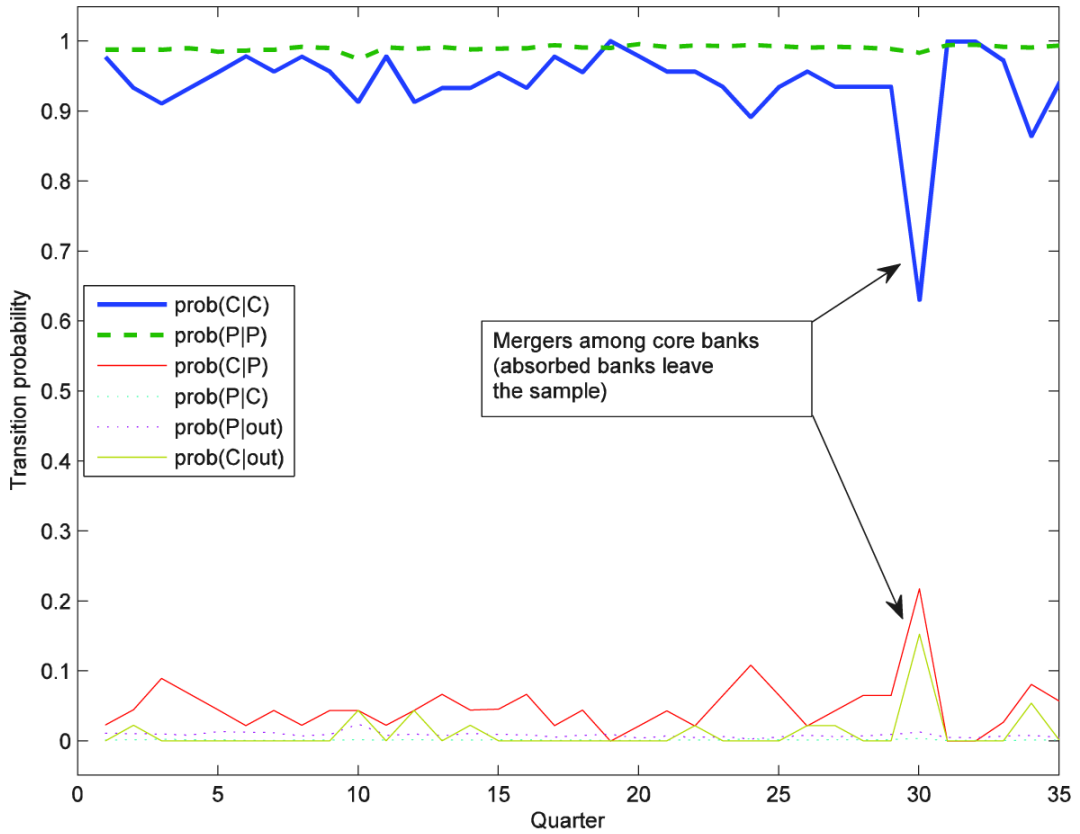
Before evaluating the statistical significance of tiering, it is important to address potential caveats. One concern relates to the way the banking statistics are collected: could the reporting threshold (€1.5 million or 10% of liable capital) bias the results? To test this possibility, we performed a censoring test whereby the model was fitted to networks defined by successively higher thresholds (from €1.5 to 100 millions, where only 50% of the value of reported positions remained in the network). The tiered structure remained unaffected, and the error score declined with each iteration. Apparently, much of the direct lending within the periphery is in smaller denominations, which dropped out as the censoring threshold increased. Indeed, the value of lending within the periphery accounts for less than 2% of total interbank credit. Applying this logic in reverse suggests that one would still observe a tiered structure if the reporting threshold were zero, although with more direct lending within in the periphery.

A more important question is whether legal structure and public ownership determine the network properties of the German banking system. The public savings banks have a special relationship with their respective *Landesbanken*, which provide them with borrowing and lending services (Schlierbach and Püttner (2003)). In a

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<sup>18</sup>The said merger activity among core banks makes the first row of  $P$  become ( 0.63 0.22 0.15 ) for the single quarter 2006Q3 (see Figure 4).





This figure shows the transition probabilities for each quarter over the sample period (1999 Q1 – 2007 Q4). The lines trace out the two top rows in equation (7) over time. For instance,  $\text{prob}(C|P)$ , shown in red, represents the frequency with which banks switch from the core to the periphery.

Figure 4: Transition Probabilities over Time

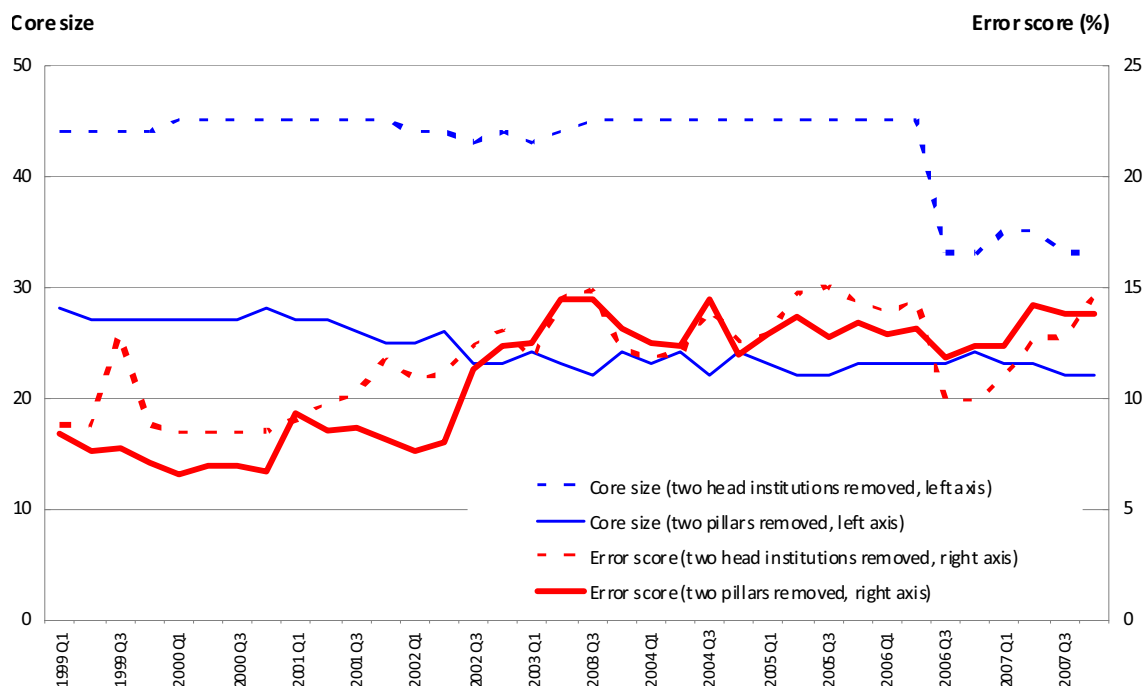
less prescriptive way, credit union banks also have a special relationship with their central cooperative banks. These pillars, and the tiering within them, are widely noted features of the German banking system. They are discussed in the interbank context by Ehrmann and Worms (2004) and Upper and Worms (2004). However, the observed network is not simply an institutional artifact but is rooted in economic choices. With few exceptions, banks are free to lend and borrow from other banks throughout the entire system – the data indeed show many direct linkages between periphery banks across different pillars. Moreover, the tiered network structure we identified predates subsequent legal developments: Guinnane (2002) describes how the regional head institutions arose to provide much-needed intermediation and payment services to the regionally dispersed credit unions and savings banks in the 19th century, well before the legal developments of the postwar period.

The view that economic motives, not only institutional factors, give rise to a core-periphery structure can also be examined by removing various segments, or their respective head institutions, from the network (Figure 5). First, the two most connected banks (head institutions) were removed from the network along with all of their links. These two banks together maintain so many links that their number exceeds the total links of the next fifteen banks and so could greatly affect the error score. The estimated core of the reduced network reveals a time series of cores with essentially the same properties and banks as the original network. Other configurations of bank deletions yielded similar results.

The most drastic experiment was the entire removal of the two pillars most likely to be shaped by legal factors, the savings banks and credit cooperatives. This was to test whether tiering would occur in the remaining – and least regulated – segment of the German banking system. Once again, the presence of a core remains a consistent feature, varying quite smoothly between 22 and 27 during the 36 quarters (Figure 5, solid lines). This is in spite of considerable merger activity in this segment of the banking industry over the sample period.<sup>19</sup> A more general concern could be that our model is not sufficiently sophisticated to capture the structure of the German (or any other) banking system. Our preference for the simple core-periphery model  $M$  is that it builds on intermediation. However, the fitting procedure we develop can also serve for estimating alternative market structures defined by other block

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<sup>19</sup>Interestingly, the structural break in 2006Q3 for the entire bank population is now absent; this is an indication that it occurred within the cooperative and savings bank sectors.



The figure shows the number of banks in the estimated core (in blue, left axis) and the total error score (in red, right axis) over time for two different experiments. In the first, shown with dashed lines, the two most connected banks (head institutions) are removed from the network. In the second experiment, shown with solid lines, all saving banks and credit cooperatives (pillars) are removed.

Figure 5: Robustness checks

types. To adapt the model to the vertical pillar structure of the German banking system, for instance, one replaces the row- and column-regular blocks in (2) by row- and column-*functional* blocks.<sup>20</sup> To generalize the model to three tiers, one would extend the model to 9 blocks to include a semi-periphery. Doing so for the German system would help distinguish regional intermediaries from the (few) genuine core banks intermediating across the entire country.<sup>21</sup>

<sup>20</sup>A row-functional block (Doreian et al. (2005)) in our context implies that every bank in the periphery relates to a *single* bank in the core.

<sup>21</sup>One indication suggestive of a three-tier system is the simple experiment of fitting the model once more on the subnetwork among core banks. This delivers an "inner core" of 28 banks with an error of 221 (17% of links).

### 3.2.2 Significance

The core-periphery structure appears robust and stable over time, but is the fit sufficiently tight to conclude that the interbank market is genuinely tiered? The screening test described in Section 1.3.4 is easily passed:  $e(C^*) = 0.122$  falls well below unity. That small a distance between the network and the model demonstrates that the tiered structure is a superior benchmark than the alternative, which comprised only a periphery.

In the second step, we test this score against the error distributions from fitting random networks. We generated 1000 Erdős-Rényi random graphs and 1000 scale-free networks of the same dimension and density as the German interbank network ( $n = 1802; d = 0.61\%$ ). We then fitted  $M$  to each realization, and traced out the distributions  $F_e$  against which to assess the error score of the German network. Figure 6 shows the histograms of the normalized error scores (4) for each class of random networks separately.<sup>22</sup>

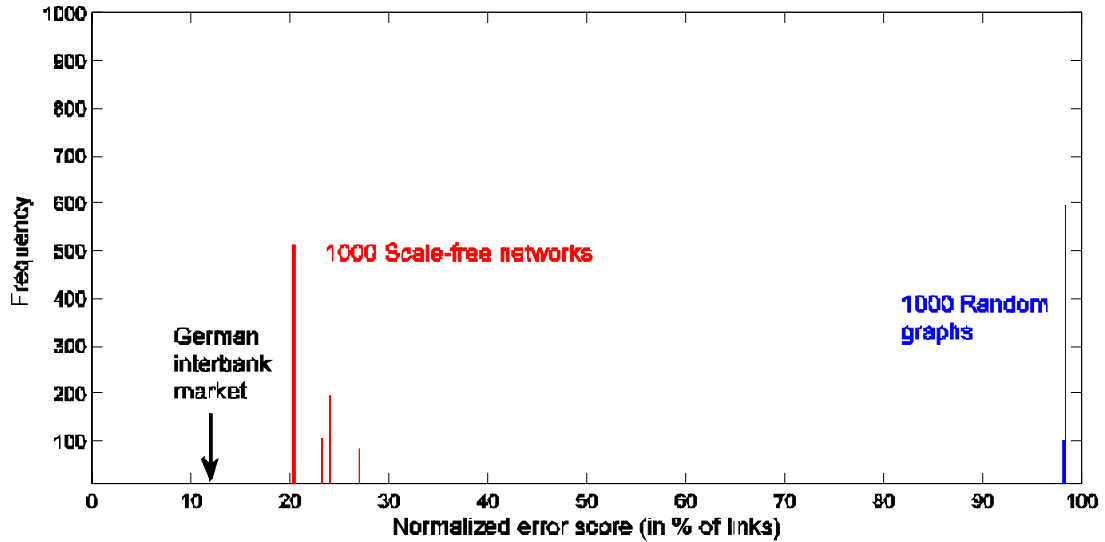
The error score distributions show that both classes of random networks exhibit tight statistical properties.<sup>23</sup> The Erdős-Rényi random graphs show error scores highly concentrated around 0.983. This is so close to unity that there is really no value in identifying a core in random networks. Importantly, even the best-fitting realization of 1000 networks produced an error score of 0.981, more than 8 times that of the German interbank network. The scale-free networks come much closer.<sup>24</sup> This was to be expected, since scale-free networks are known to produce hubs that characterize many real networks, including interbank markets (Boss et al. (2004)). Even so, *none* of the 1000 realizations of scale-free networks produced an error score of less than 0.204, a distance that remains by a factor of 1.8 larger than that of the German network. The goodness of fit for the German interbank network thus lies outside any conceivable percentile of the error distribution for both classes of random networks. We can therefore reject the hypothesis that random networks produce the extent of tiering evidenced by the German banking system. Put differently, the core-periphery

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<sup>22</sup>See Appendix B on the robustness checks we used to ascertain that the test distributions reflect the intrinsic randomness of networks, rather than stochastic output from an unreliable procedure.

<sup>23</sup>Scale-free networks consistently produced cores of size 55-57. Random graphs featured cores of size 17 or 18, in 86% and 14% of cases, respectively.

<sup>24</sup>Interestingly, the Monte Carlo experiments produced binning into four distinct error score classes (red in Figure 6). We made considerable efforts to ensure that these were not local minima, especially for the clusters around higher error scores (see Appendix B). More work is needed to uncover the reasons behind this phenomenon.



This figure compares the total error score from fitting the tiering model to the German interbank network (12.2% of links, shown as an arrow) to the normalized error scores, as defined as in equation (4), from fitting two types of random networks of the same dimension. The red bars show the histogram of error scores from fitting 1000 scale-free networks, whereas the blue bars represent the histogram from fitting 1000 Erdős-Rényi random graphs.

Figure 6: German Fit against simulated Error Score Densities

model is a much better description of the German interbank network than of random networks. We conclude that the tiering observed among German banks does not result from standard random processes. Indeed, the statistical approach to network formation is ill-suited for social and economic networks, which are the result of purposeful activity by agents weighing the costs and benefits of forming links (Goyal (2007) and Jackson (2008)). One should therefore expect different kinds of banks to build systematically different patterns of linkages – a direction we explore next.

## 4 Interbank tiering and money center banks

The concept of tiering captures a structural quality of the interbank market that allocates banks into a core and a periphery. As is characteristic for network analysis, this allocation is derived from the pattern of linkages alone: network statistics are calculated disregarding any other information on individual nodes. But one would expect that a bank’s network position would be related to bank-specific features, such as its size, location, business model, or funding sources. We regard this unexplored link as a promising bridge between banking theory and network analysis, essential for a better understanding of the formation of interbank networks.

### 4.1 What makes a core bank?

In this section, we explore whether individual bank features help explain how banks position themselves in the interbank market. In particular, what kind of banks make up the core of the network? To test whether a bank’s membership in the core can be predicted by bank-specific features, we assembled balance sheet variables for the 1802 active banks in the German interbank network in the mid-sample quarter 2003 Q2, using the monthly banking data collected by the Bundesbank’s statistics department (*monatliche Bilanzstatistik*).<sup>25</sup> These variables serve as regressors in a probit regression, where the binary dependent variable is core membership:  $b_i = 1$  if bank  $i$  was found to be part of the core in the previous section, and  $b_i = 0$  otherwise,

$$\text{prob}(b_i = 1) = \Phi(x_i'\beta).$$

The first column of Table 1 reports the simplest regression using bank size as the sole explanatory variable. The log of total bank assets is highly significant; a marginal increase in size from the average balance sheet of €230 million raises the probability of belonging to the core by a sixth of a percent. Indeed, size is a fairly reliable classifier. The average size of banks in the core is 51 times that of banks in the periphery. Hence, large banks tend to be in the core, while small banks are found in the periphery of the interbank network.

This intuitive result is in line with earlier studies on interbank markets. For instance, Cocco et al. (2009) find that small interbank borrowers rely more on relationships, preferably with larger banks. Interbank markets typically have natural

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<sup>25</sup>This test is in the spirit of the industrial organization approach to banking (surveyed in Degryse et al. (2009)), but focuses on overall market structure rather than on individual bank performance.

lenders and borrowers (Stigum and Crescenzi (2007)); in the federal funds market, small banks tend to turn over surplus funds to large banks that distribute or invest the funds (Ho and Saunders (1985), Allen and Saunders (1986), Bech and Atalay (2010)). Further back in US monetary history, small rural banks cleared at money centers that, in turn, were dealing with each other and with the large New York banks, a process known as reserve pyramiding (White (1983)). These observations are all consistent with our view that interbank markets have a tiered structure.

Is the importance of bank size for network position an expression of economies of scale and scope? This question should be addressed with a definition of size that is unrelated to a bank's interbank activity. The intermediary function that core banks perform, by borrowing and lending in the interbank market, of course contributes to their reported balance sheet size. We thus compute the *intrinsic size* of a bank as (the logarithm of) total assets excluding interbank lending. This measure captures all positions relating to the bank's *other* business lines, including that of affiliated entities consolidated into its balance sheet. Intrinsic size, when used alone, delivers a poor fit and the coefficient – although significant – is too small to identify core banks at the default threshold (column 1b). The variable remains significant but adds little explanatory power when used jointly with others (not reported). Economies of scale and scope per se seem to play a limited role in explaining a bank's position in the interbank market. This may reflect a degree of specialization among banks: some very large universal banks focus their other business to a greater extent on capital markets and on international activity, which lies beyond the observed (domestic) network.

The single most effective regressor will be one that takes network data into account. Column 2a shows that a bank's connectedness predicts quite reliably whether or not it is in the core, where we measure connectedness by *betweenness centrality*, a concept borrowed from sociology (Freeman (1979)). Betweenness is the probability with which a node lies on the shortest path between any two unconnected nodes. The probit regression makes clear that connectedness predicts core membership better than does bank size. This is not surprising when one recognizes tiering as a "group version" of betweenness: the core comprises the banks that jointly inter-mediate between the periphery, so a bank that helps to link pairs of unconnected banks also contributes to the core performing this role for the market as a whole. More intriguing is the presence of outliers: for reasons of specialization, some very large banks were found to be far less connected than their size and presence in the core

would suggest. This touches on the open question of whether "too-big-to-fail" or "too-connected-to-fail" is the relevant criterion for financial stability.

To examine this link directly, we estimate each bank's systemic importance using the approach taken in the interbank contagion literature. Systemic importance is measured by the damage a bank's failure inflicts upon the rest of the system (e.g. Upper and Worms (2004)). Such simulations often require a loss-given-default (LGD) which is generally unknown. Craig, Fecht, and von Borstel (2010) proceed to solve for the LGD that would be required for a bank's failure to cause a systemic crisis (defined as 25% of system assets in default). The variable *systemic importance* used in regression 2b is the inverse of this value, because more important banks bring down the system already at smaller LGDs. Systemic importance is highly correlated with a bank's network position: it is extremely unlikely that a systemically important bank would not be in the core, as indicated by the low rate of false core predictions, Prob(c|P). But the moderate fit also suggests that a bank's position in the network is something that goes beyond its systemic importance.

In practice, a major problem for central banks and regulators is that the *bilateral* interbank exposures for conducting network analysis and assessing systemic risk are unavailable in most countries. Is it possible to identify the core of the interbank market with a regression that uses only individual balance sheet variables? Columns 3 (and 1) present probit regressions excluding those regressors for which network data are required (those shaded in Table 1). *Interbank liabilities* help predict core membership quite well, although total bank size performed a little better, in part due to economies of scale and scope (column 3a). However, the prediction can be further improved by focusing on the size of interbank intermediation activity. The variable *intermediation* measures the volume each bank intermediates, by taking the minimum between its borrowing and lending in the interbank market. (It would be zero for banks that *only* borrow or lend, regardless of the volume.) Column 3b shows that this variable predicts core membership nearly as reliably as connectedness, and better than systemic importance, without requiring the bilateral data necessary for these two regressors.

Finally, we include the aforementioned variables jointly to examine their respective explanatory power. In regression 4a, it is clear that each regressor remains significant in concert with the others: bank size, betweenness, and systemic importance all contribute significantly to explaining which banks form the core. Each variable adds



a facet to core membership that is related to – but distinct from – the other two. The final regression, 4b, indicates that the explanatory power of systemic importance falls (to 8% significance) when interbank intermediation and betweenness are included together, suggesting that a bank’s interbank position and the volume it intermediates in the interbank market jointly contain most of the information embodied in systemic importance.

All in all, the results of Table 1 show that network position is predictable by bank-specific features. Banks are in the core because they are well-connected, both when measured by connectedness (betweenness centrality) and in terms of contagion (systemic importance); they are also in the core due to their ability to carry out large transactions, as measured by their balance sheet size or by the volume of interbank intermediation they perform. None of these concepts by itself fully explains core membership, but each adds to the qualities that make up a core bank.

A bank in the core of a tiered interbank market can therefore be regarded as a *money center bank*. This term is generally associated with large banks that dominate wholesale activity in money markets; in addition to running traditional banking operations, money center banks provide clearing and correspondent banking services, and act as dealers in a broad range of markets, including government securities, FX, derivatives, and offshore markets (Stigum and Crescenzi (2007)). As money market makers, they do interdealer business among themselves, inside the spread they quote to other, more peripheral banks. As such, money center banks are those intermediaries occupying the special network position we identify as the core. In this network sense, money center banks play a central role among banks, in dealing among themselves and tying in the periphery.

## 4.2 Concluding remarks: bridging two literatures

In relating network position to bank-specific features, our paper bridges two literatures. The banking literature, elegantly summarized by Freixas and Rochet (2008), examines individual bank incentives with no concern for how banks position themselves in a larger network. The literature on network formation, on the other hand, often relies on random processes from statistical mechanics (e.g. Newman et al. (2006)). Even recent game-theoretic models of strategic network formation (Goyal (2007) and Jackson (2008) provide excellent surveys) disregard the features of individual nodes. In our view, this severely limits what such models can predict in the

way of network formation. For instance, in some network formation games the pure star emerges as the unique equilibrium architecture (Bala and Goyal (2000), Goyal and Vega-Redondo (2007), Hojman and Szeidl (2008)); but since these theories cannot predict *which* node will form the center of the network, they must be regarded, in a sense, as indeterminate.

Our findings suggests that bank-specific features help explain how banks position themselves in the interbank market, as evidenced by the regression results. Balance sheet variables also help predict interbank relations in other studies (Cocco et al. (2009)), with implications for overall market structure. As tiering is not random but behavioral, there are economic reasons why the banking system organizes itself around a core of money center banks. The strong correlation with size suggests the presence of fixed costs, possibly with economies of scale and scope. To better understand financial networks, we argue that the way forward should focus more on the features of the nodes that make up the network. In the context of banking, this provides clues for theoretical modeling efforts as to how different banks choose to make network connections.

A class of recent banking models does take into account the fact that interbank markets operate as networks rather than centralized exchanges. Allen and Gale (2000) propose a framework in which banks of different regions (or sectors) face opposite liquidity shocks. This provides an incentive for banks to insure each other *ex ante*, which can be done through interbank deposits. In a related model, Leitner (2005) demonstrates that interbank deposits help induce banks to bail each other out. Similarly, Babus (2009) shows that it is optimal for banks to exchange deposits with all banks facing opposite liquidity shocks.<sup>26</sup> However, this approach predicts *dense* networks, contrary to the core-periphery structure we detected for the German interbank network. That core-periphery structure is also highly *persistent*, which clashes with the view that random liquidity shocks are the basis for understanding interbank activity. Moreover, the interbank market in these models is essentially *flat* – there is no role for intermediation. Banks are identical *ex ante*, including in the way they connect to each other. There is no reason in these models why banks, the main intermediaries in the economy, would build yet another layer of intermediation between them.

To explain the tiered structures we explored in this paper, a model would require

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<sup>26</sup>It is unclear whether this theory predicts a network of interbank deposits. Other instruments are available for implementing risk-sharing, including insurance contracts, derivatives, and credit lines.

some asymmetry or specialization. Two existing models do so by assumption. In the two-tier bank model of Qi (2008), the "correspondent" bank is assumed to be different: its ability to borrow costlessly makes other banks use it as a liquidity pool, much like a central bank. However, the central bank is not the only interbank intermediary, as is apparent from the German interbank network. Freixas et al. (2000) provide an example of such a case, obtained by assuming that all travelers pass through a single location.<sup>27</sup> The bank located there receives and extends lines vis-à-vis banks in all other locations (which are not connected to each other). Though both settings are constructed rather than derived, they lead to pure star networks with a single money center bank at the core. The core-periphery network is a generalization of the star network with several interconnected centers. To better understand the formation of such networks, it would therefore seem promising to start out from a model featuring a variety of diverse banking firms.

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<sup>27</sup>Consumers of different regions face uncertainty about where to consume. Interbank credit lines between banks in these regions help economize on reserves, so travelers need not move any goods or cash.

# Appendix

## Appendix A: Proofs

**Part a)** To show that the presence of intermediaries is necessary, consider a network  $N$  of dimension  $n$  in which there are *no* intermediaries in the sense of Definition 1. Banks are either lenders ( $\lambda$  in number), or borrowers ( $\beta$  in number), or neither of the two ( $n - \lambda - \beta \geq 0$ ). We first show that the latter group, the unattached banks, must be in the periphery, because each unattached bank causes fewer errors in (3) relative to the model (2) when allocated to the periphery. To see this, suppose there is an unattached bank among the  $c$  banks in the core. This causes exactly  $2(c - 1)$  errors in the  $CC$  block, and  $(n - c)$  errors in each of the blocks  $CP$  and  $PC$  of (3). The same bank placed in the periphery would cause no errors in  $CC$  (nor in  $PP$ ), but could add up to  $2(c - 1)$  errors for expanding the  $CP$  and  $PC$  blocks (if all remaining core banks are not linked to the periphery). Switching the unattached bank from core to periphery thus leads to a net reduction in the total number of errors of *at least*  $2(n - c)$ , which is always positive (and zero if the periphery is empty). The move thus weakly dominates for the first unattached, and strictly dominates for each subsequent unattached bank and every combination of unattached banks. Therefore, it is optimal to allocate all unattached banks to the periphery.

We proceed to show that the same argument holds for the remaining core banks, which must be either lenders or borrowers (not both). Suppose that  $\lambda_C$  lenders and  $\beta_C$  borrowers are in the core (so that  $\lambda_C + \beta_C = c$ , with  $0 \leq \lambda_C \leq \lambda$ ,  $0 \leq \beta_C \leq \beta$ ). Without loss of generality, reorder the nodes in each tier such that the lenders appear first, followed by the borrowers and the unattached. This divides each of the four blocks as shown in (8). The absence of intermediaries implies many zero blocks, since lenders borrow from no one, borrowers lend to no one, and the remaining banks are unattached. The nonzero entries show dimensions of sub-blocks that may be nonzero.

$$\begin{array}{cc|ccc}
 0 & \lambda_C \beta_C & 0 & \lambda_C \beta_P & 0 \\
 0 & 0 & 0 & 0 & 0 \\
 \hline
 0 & \lambda_P \beta_C & 0 & \lambda_P \beta_P & 0 \\
 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0
 \end{array} \tag{8}$$

Now, the number of errors of this (arbitrary) allocation can be reduced as long as there are banks left in the core. Applying (3) to (8) shows that the  $CC$  block generates at

least  $\lambda_C(\lambda_C - 1) + \beta_C(\beta_C - 1) + \lambda_C\beta_C$  errors, the number of zero entries in the top left block, and more if the sub-block  $\lambda_C\beta_C$  is not complete with ones. The  $CP$  block (top right) comprises at least  $\beta_C(n - \lambda_C - \beta_C)$  errors, where the term in brackets is the dimension of the periphery (of which  $\beta_P \equiv \beta - \beta_C$  are borrowers). Likewise, the  $PC$  block counts at least  $\lambda_C(n - \lambda_C - \beta_C)$  errors, and more if the sub-block  $\lambda_P\beta_C$  is not column-regular as required by (2). This allocation thus produces, for these three blocks, at least

$$(n - 1)(\lambda_C + \beta_C) + \lambda_C\beta_C \quad (9)$$

errors, plus the number of nonzeros in the sub-block  $\lambda_P\beta_P$ , denoted by  $\#(\lambda_P\beta_P)$ . If all banks were placed in the periphery instead, the errors would equal the number of nonzeros, which cannot exceed  $\lambda\beta$ . Expanding  $\lambda\beta$  (using  $\lambda \equiv \lambda_C + \lambda_P$ ) shows that (9) exceeds  $\#(\lambda\beta)$  provided

$$\lambda_C[(n - 1) - \beta_P] + \beta_C[(n - 1) - \lambda_P] > 0. \quad (10)$$

The terms in square brackets are always positive when there is one or more unattached banks in the network (implying  $(n - 1) > \beta + \lambda$ ); in that case, the error score can always be reduced by placing all banks in the periphery, i.e. until  $\lambda_C = \beta_C = 0$ . If there are no unattached banks, the same conclusion holds for all but one peculiar network for which the net gain in (10) would be zero.<sup>28</sup> Since moving all banks to the periphery is strictly dominant for all networks (and weakly dominant for one peculiar network), the absence of intermediaries implies an empty core.

To show sufficiency, i.e. that a network containing intermediaries gives rise to a non-empty core, assume to the contrary that the core is empty and at least one bank, say bank  $i$ , intermediates. Since all banks are in the periphery, the presence of  $i$  contributes at least two errors to  $PP$ . Allowing bank  $i$  to form a core by itself removes both errors without producing any new errors in the three new blocks of (3). By the same argument, adding more intermediaries to  $N$  can expand, but cannot reduce, the size of the core. Thus the presence of intermediaries produces a core.

What remains to be checked is that the periphery does not vanish. The core is potentially largest when all banks lend to each other: placing  $n - 1$  banks in the core will minimize the error score to zero. The same score can be also attained by

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<sup>28</sup>If a *single* bank lends to *all* other banks in the system ( $\beta_P = n - 1$ , and  $\beta_C = 0$ ), then the total error score is unaffected by whether that lender is in the core or the periphery. (The same holds for the single-borrower case, where  $\lambda_P = n - 1$ , and  $\lambda_C = 0$ .)



$CC$  block shrinks, transferring its column  $i$  to  $CP$  and row  $i$  to  $PC$ , respectively; and  $PP$  expands, taking column  $i$  from  $PC$  and row  $i$  from  $CP$ , respectively. The first transfer removes all the errors that  $i$  had caused in  $CC$  and may add new errors to  $CP$  and  $PC$  that are strictly fewer in number than those saved  $CC$ . (There is one possible exception where the net gain reaches zero. This occurs only if none of the remaining core banks borrow from any periphery banks ( $c-1$  errors), and either some core banks do not lend to the periphery or bank  $i$  borrows from all core banks.) The second transfer also delivers a net improvement: the  $(n-c)$  errors formerly in  $CP$  no longer count as errors when moved to  $PP$ , but column  $i$  now in  $PP$  may add errors if it contains ones; the net reduction in errors is again strictly positive, except in the one case where bank  $i$  happens to borrow from *all*  $(n-c)$  banks in the periphery.

Combining these error reductions shows that the distance-minimizing procedure will move bank  $i$  to the periphery, contradicting the initial claim that a nonintermediary can be in the core. (The one exception for which there is weak dominance can occur only if  $i$  borrows from all banks, or some other core banks do not intermediate between periphery banks, a case considered in what follows.) Thus all core banks are intermediaries.

The converse, that all intermediaries are also core banks, does not hold. Suppose bank  $i$  is in the core but intermediates only among core banks. It is straightforward to show, with the approach just used, that moving  $i$  to the periphery always produces a net reduction of at least  $2(n-c)$  errors (which had been in  $CP$  and  $PC$  but no longer count as errors when part of  $PP$ ). Hence, not every intermediary is a core bank.

We generalize this case by showing that a core bank that does not lend to (or does not borrow from) the periphery will not be in the core. Suppose bank  $i$  does not lend to any bank in the periphery. Its presence in the core contributes  $(n-c)$  errors to  $CP$  and  $x \geq 0$  errors to  $CC$  for any missing links with other core banks. Moving bank  $i$  to the periphery again leads to a net reduction in errors. The argument follows exactly the one just advanced for nonintermediaries, the only difference being that the number of errors involved in the first transfer, now  $x$ , need not exceed  $(c-1)$ . The result carries through that moving  $i$  to the periphery is strictly dominant, again with one exception where it is weakly dominant. The analogous case of a bank that does not *borrow* from the periphery can be shown by symmetry. Therefore, the core excludes intermediaries that do not lend to (or do not borrow from) the periphery.

## Appendix B: Computational methods

As stated, fitting a core-periphery model to a real-world network is a large-scale problem in combinatorial optimization, which we solve by means of a sequential algorithm. This way, the search for the optimal core leads to a solution in polynomial time, rather than in exponential time ( $2^n$ ) required by exhaustive search. Section 1.3.3 described two versions of the algorithm that we designed for this task, both running in polynomial time (order  $n^1$ ).<sup>31</sup> In our application to the German network ( $n = 1802$ ), the algorithm converged in 70 seconds on a standard IntelCore 2 duo processor (2.4GHz).

For NP-hard problems of this dimension, it is not possible to prove that the solution returned by any procedure is indeed the global optimum. We therefore performed several robustness checks to dispel doubts. First, we backtested our algorithm against existing blockmodeling routines, and obtained the same solutions for small example networks.<sup>32</sup> We also tested that the algorithm finds the optimum for cases where the true solution is known: we generated artificial networks (of the same dimension and density as the German system) with a *perfectly* tiered structure, for which the minimum error score (4) must be zero, by construction. The algorithm consistently returned the correct set of core banks with zero errors. Second, we know from Proposition 1 that any solution returning nonzero elements on the off-diagonal of the error matrix  $E$  cannot be an optimum – in practice, the procedure never returned solutions failing this criterion. However, as this is a necessary (not a sufficient) condition, one cannot rely on this test alone to rule out all local optima. Our third and main robustness check therefore consisted of repeated application and careful comparison of the results generated by two algorithms (see section 1.3.3).

This was straightforward to do for the single application to the German inter-bank network, and reliably yielded the solution reported in the text. To prepare the thousands of runs necessary for hypothesis testing, we compared the error scores calculated with simulated annealing programs with various "cooling" parameters and many different initial partitions, with the greedy algorithms using different initial conditions. For avoiding local optima it turned out to be helpful to start the greedy algorithm sufficiently far from an approximate solution to give it time to converge to the error-minimizing core. The best simulated annealing algorithms gave error scores

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<sup>31</sup>The MATLAB code is available upon request from the authors.

<sup>32</sup>The software *Pajek* (Batagelj et al. (2003)) implements generalized blockmodeling for networks of up to 256 nodes.



very close to a greedy algorithm with initial partitions that assigned a random half of the banks to the core. The local optima that did occur were easily identified by their extremely high error score, which would fall to the normal range when fitting the same network again.

The distributions shown in Figure 6, using the greedy algorithm with random initial partitions, offered consistently the minimum error score, always close to the best solution of any of the algorithms we tried. We performed robustness checks on the algorithm to make sure that the initial conditions and parameters were consistent with generating the minimum error scores for both types of random networks (see Appendix B). The core sizes did not vary between the algorithms, although the error scores did fluctuate in a narrow range for different initial conditions. Taken together, these robustness tests assured us that the distributions generated for the hypothesis tests reflect the intrinsic randomness of random networks, rather than stochastic output from an unreliable procedure. The random networks were generated in Matlab, using the routine of Muchnik et al. (2007) for obtaining directed scale-free networks.

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**Table 1: Core membership and bank-specific variables**

The table reports the results of probit regressions testing whether network position can be predicted by individual bank balance sheet variables. The binary variable *core membership* takes the value 1 for banks that were determined to be in the core, and 0 for the remaining banks. It is regressed on a constant and the regressors shown in the rows, which rely only on individual bank data (except for the shaded variables, which require the network data). The columns show the different regressions, each comprising 1802 observations. The cells show the maximum likelihood estimates of the coefficients. The marginal effects are shown in parentheses, evaluated at the multivariate point of means. Significance is denoted by \*(5%) and \*\*(1%).

*Bank size* is the natural logarithm of total assets (in € thousands plus 1); *Intrinsic size* excludes interbank claims from total assets before taking the logarithm. *Interbank liabilities* is the logarithm of (interbank liabilities+1). The fit with interbank liabilities was slightly better than that with interbank assets (not reported). *Intermediation* is the logarithm of interbank liabilities that a bank in turn lends out on the interbank market, i.e.  $\ln(\min\{\text{interbank assets, interbank liabilities}\} + 1)$ . *Connectedness* is normalized betweenness centrality (Freeman (1979)). *Systemic importance* of an institution is measured here as the (inverse) loss-given-default necessary such that the failure of the institution leads to a systemic crisis (a quarter of the banking system in default). The probabilities in the final rows are evaluated at the default threshold of 0.5.  $\text{Prob}(c|C)$  = probability (in %) that a bank predicted to be in the core is indeed in the core (=100- $\text{Prob}(p|C)$ ).  $\text{Prob}(c|P)$  = rate of false core predictions.

<i>Regressors</i>	<b>1a</b>	<b>1b</b>	<b>2a</b>	<b>2b</b>	<b>3a</b>	<b>3b</b>	<b>4a</b>	<b>4b</b>
<i>Bank size</i>	0.903** (0.0014)						0.361** (0.0821)	
<i>Intrinsic size</i>		0.149** (0.0073)						
<i>Interbank liabilities</i>					0.667** (0.0006)			
<i>Intermediation</i>						0.718** (0.00014)		0.455** (0.0557)
<i>Connectedness</i>			3962** (1581)				2931** (666)	3393** (415)
<i>Systemic importance</i>				4.737** (0.1193)			3.292* (0.748)	2.206 (0.270)
<i>Pseudo-R<sup>2</sup></i>	0.573	0.073	0.654	0.475	0.542	0.579	0.736	0.765
<i>% correctly classified</i>	98.5%	97.5%	98.8%	98.5%	98.0%	98.7%	99.0%	99.1%
<i>Prob(c C) core correct</i>	48.9%	0%	60.0%	42.2%	42.2%	51.1%	68.9%	71.1%
<i>Prob(c P) core false</i>	0.17%	0%	0.17%	0.06%	0.57%	0.06%	0.17%	0.23%

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