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The Impact of Iceberg Orders in Limit Order Books *

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Abstract

We examine the impact of iceberg orders on the price and order flow dynamics in limit order books. Iceberg orders allow traders to simultaneously hide a large portion of their order size and signal their interest in trading to the market. We show that when the market learns about iceberg orders they tend to strongly attract market orders consistent with iceberg orders facilitating the search for latent liquidity. The greater the fraction of an iceberg order that is executed the smaller its price impact consistent with liquidity rather than informed trading. The presence of iceberg orders is associated with increased trading consistent with a positive liquidity externality, but the reduced order book transparency associated with iceberg orders also creates an adverse selection cost for limit orders that may partly offset any gains.

Keywords: Hidden Liquidity; Iceberg Orders; Limit Order Markets; Transparency;

JEL Codes: G10, G14

A trader seeking to execute a large trade faces the problem that signalling his trading intentions to the market can both help and hurt the effective execution of his trade. A signal may help attract counterparties to reduce the time it takes to complete the trade and the trading cost. On the other hand, it may also attract opportunistic traders who make the completion less likely or more costly. Traders' solutions may include following dynamic order submission strategies or trading off the exchange because such strategies limit the amount of information that is revealed about their trading intentions. Many exchanges have offered their own solution by adopting a particular order type known as an *iceberg order*. We study the use of iceberg orders and their impact on price and order flow dynamics in limit order books. We find evidence that supports the view that iceberg orders allow traders to advertise their trading intentions and attract counterparties while limiting the expected price impact of their trades. Our evidence is consistent with iceberg orders attracting market orders that may otherwise have stayed on the sidelines. On the other hand, we also show that some of these gains come at the expense of limit orders who suffer an adverse selection cost due to the reduced order book transparency.

A trader submitting an iceberg order specifies a price, a total order size, and a *peak* (size) which is smaller than the total size. Initially only the peak is displayed in the order book and the rest of the order remains hidden. When the first peak has been fully executed, another peak is automatically displayed in the order book, and the hidden part is reduced by the corresponding number of shares.

Our understanding of the rationale for submitting iceberg orders and the desirability of market designs that allow such orders is still incomplete. The iceberg orders have a direct effect on order books, but, perhaps more interesting, is the indirect effect that they are likely to have on the strategic behavior of other market participants. To what extent can market participants detect the presence and predict the amount of hidden volume? If they can then what is the rationale for submitting iceberg orders? Are iceberg submitters motivated primarily by liquidity or information? What is the impact of iceberg orders on liquidity suppliers who use limit orders? We address these questions using a sample from the German Stock Exchange's Xetra platform that includes detailed information on iceberg orders.

In order to address these questions we need some way to approximate the information that market participants have about the existence and size of potential iceberg orders. The immediate automatic display of a new peak after the currently displayed peak is executed creates a distinct pattern in the order book updates that is observable to any market participant who monitors the order book closely. A market participant who detects an iceberg order cannot determine the iceberg order's size although its peak size may provide a signal. But as peaks are executed and new ones are displayed the participant can form more precise forecasts of the order's original size. Rather than disclose the information about the order size right away the iceberg order sequentially reveals more information as peaks are executed.

Building on these observations, we develop an algorithm for detecting iceberg orders that uses publicly available information on the order book and price dynamics. Conditional on a signal of detection, we use the observed peak size and the number of executed peaks to dynamically predict the hidden volume. We combine the detection algorithm's signals of icebergs with our actual iceberg observations to isolate the iceberg order's impact on the behavior of market participants from other factors that may influence the propensity to submit iceberg orders. Our sample exhibits a lot of variation in the peak sizes, the number of submitted peaks, and the number of executed peaks which implies that our methodology generates independent variation in the executed iceberg volume and the predicted hidden volume.

We are interested in the price impact of iceberg orders because they tend to be much larger than regular limit orders and hence they are likely to move prices for either liquidity or information reasons. Yet, several studies conclude that iceberg order have little price impact. We show that iceberg orders have a price impact that is increasing in their order size. But the observed price impact of an iceberg order of a given size depends critically on the fraction of the iceberg order that is eventually executed. Together this evidence supports the liquiditybased explanation. If the primary driver was information we would, on average, expect to observe a price movement in the direction of the iceberg orders regardless of how much of it was executed. Instead the observed pattern supports the view that it is the initially unknown latent liquidity demand, which eventually is discovered, that together with the iceberg order determine the price impact.

We examine how iceberg orders influence the order flow to better understand the potential dual objectives of hiding and signalling. We show that the detection status of an iceberg order, the predicted hidden volume, and the amount of iceberg volume already executed influence the likelihood and size of market orders. We find that detected iceberg orders are more likely to attract market orders that undetected iceberg orders; that the market order size is increasing in the iceberg order's size; and that the probability of additional market orders hitting the iceberg order is increasing in the iceberg volume that has already been executed.

Given that the iceberg orders appear to allow some traders to more effectively execute their transactions it is natural to ask if the benefit to this group of traders comes at the expense of some other traders. If we focus strictly on the trade executions then trading is a zero-sum game with the profits to liquidity suppliers corresponding to the transaction costs paid by the liquidity demanders. We measure the profits earned by liquidity suppliers using either iceberg or limit orders to assess the net effect for order books with iceberg orders. Our results show that iceberg orders are more profitable when they are either undetected or when the market underestimates their true size. This is consistent with the strategic advantage of iceberg orders coming from the submitter's ability to control the amount of information reveled. In aggregate, limit orders earn a profit in order books with no iceberg orders but suffer a loss in order books with iceberg orders. The losses partly stem from the fact that an iceberg order has a price impact which will, on average, cause limit orders on the wrong side to suffer losses. In addition, there is a 'crowding out' effect in that iceberg orders are large and effectively drive down the execution probability for limit orders on the 'right side' of the order book but behind the iceberg order.

A number of empirical studies including Boni and Leach (2004), Degryse (1999), Fleming and Mizrach (2008), Labys (2001), Pardo and Pascual (2007), and Tuttle (2006) document widespread use of iceberg orders or closely related order types such as reserve orders. Other studies including Aitken, Berkman, and Mak (2001), Harris (1996), Bessembinder, Panayides, and Venkataraman (2009) study the decision to submit iceberg orders. Theoretical treatments of iceberg orders include Buti and Rindi (2008), Esser and Mönch (2007) and Moinas (2007). The studies most closely related to ours are De Winne and D'Hondt (2007) and Bessembinder, Panayides, and Venkataraman (2009). Our approach to the iceberg order detection builds on their work and extends it by incorporating both the peak size and the number of executed peaks. Bessembinder, Panayides, and Venkataraman (2009) apply the implementation shortfall methodology to assess the costs and benefits of submitting iceberg orders. We focus instead on the impact of the iceberg orders on the behavior of other market participants and their payoffs. Our methodology allow us to extend the analysis of De Winne and D'Hondt (2007) who do not use the peak size, the number of executed peaks, nor control for variables the may influence the propensity to submit iceberg orders.

Our evidence on the information content of the iceberg orders for future mid-quotes adds to the growing literature that investigates the information content of the limit order book. Cao, Hansch, and Wang (2009) find that future prices to some extent can be predicted based on *visible* information in the order book and an experimental study by Bloomfield, O'Hara, and Saar (2005) shows that informed traders may often use limit orders providing a rational for an informative limit order book. Our evidence shows that other order book information including the hidden volume from iceberg orders and the history of order book updates also helps predict both future prices and quantities.

In the next section we develop our testable hypotheses. In Section 2 we present our sample and our methodology. In Section 3 we present our main empirical results for the price impact, the market order flow, and the order book profits. Section 4 provides some further interpretation of our results. Section 5 concludes. In the Appendix we provide more details on the computation of profits to liquidity suppliers, the detection algorithm, and estimation procedures.

1 Testable Hypotheses

In this section we develop and present our hypotheses for the iceberg orders impact on prices, the market order flow, and the order book profits of liquidity suppliers. An iceberg order specifies a price, a total size, and a peak size. The peak size is the maximum displayed volume. When a trader submits an iceberg order, the first peak size is displayed in the order book. At that time, the hidden volume of the order is equal to the order's total size minus its peak size. When the first peak size has been fully executed, another peak (size) is automatically displayed in the order book, and the hidden volume is reduced by the corresponding number of shares. The trading system automatically displays new peaks after additional executions until the final peak is displayed or the submitter cancels the iceberg order.

Initially an iceberg order is indistinguishable from a limit order with the same price and size. But over time the execution of displayed peaks and the display of new peaks allow market participants to learn about its existence and predict its size. In addition, any systematic relationship between the peak size, the number of peaks, and the iceberg order's total size imply that market participants can improve their forecasts of the iceberg order's size over time. Iceberg orders are often justified and promoted as an order type that facilitates the execution of large orders with minimal price impact, a property that should appeal to large liquidity traders. On the other hand, the more successful iceberg orders are in reducing the price impact for large orders the more they should appeal to informed traders. The existing evidence on the price impact of iceberg orders is mixed. A challenge in addressing the price impact question is that the iceberg order's price is fixed for each peak causing the short-term impact to be zero regardless of the order's ultimate impact. We focus on the price impact measured over a horizon that is longer than the duration of the iceberg order to overcome this challenge. The fixed iceberg order price also means that the full impact of public information, which is revealed while the iceberg order is outstanding, may only be reflected in prices with a delay.

The ability to hide a large portion of the order size may make iceberg orders appealing to informed traders. We would therefore expect iceberg orders to have a price impact and we would expect the price impact to be increasing in the iceberg order's size. Iceberg orders may also have a price impact if they are primarily submitted by large liquidity traders. The difference is that if the iceberg orders are primarily submitted by liquidity traders then we would expect the net price impact to depend on the latent demand for liquidity. Consider a buy iceberg order of a given size. If the order is primarily submitted by liquidity traders, we would expect the price impact to depend on the latent liquidity demand; lots of interest in selling may imply that the net impact of the buy iceberg order is small, little interest in selling produces a greater price impact. In contrast, if positive information is the reason for submitting the buy iceberg order, we would expect a higher future mid-quote regardless of the market order flow. To distinguish between these scenarios we consider the following two hypotheses:

Hypothesis 1: **Price Impact** The future mid-quote is increasing in the expected and actual size of a buy iceberg order and decreasing in the expected and actual size of a sell

iceberg order.

Hypothesis 2: **Price Impact-Liquidity.** For a given expected or actual size of an iceberg order, the future mid-quote is decreasing in the executed volume of a buy iceberg order and increasing in the executed volume of a sell iceberg order.

The expected fraction of the iceberg order that executes depends on the interaction between the iceberg order and the market order flow. A challenge in sorting out the interaction is that the iceberg order submissions may be opportunistically timed. For example, a trader may submit a buy iceberg order when the probability of a sell market order is high or the expected size of sell market orders is large or some combination of the two.¹ On the other hand, since the iceberg order can be detected by liquidity demanders and its peak size may act as a signal about its size, it is also possible that the iceberg order itself induces a change in the market order flow. For example, some liquidity demanders may wait until they detect an iceberg order on the other side of the market because they rather trade when there is greater depth on the other side of the market. The timing argument leads to the following hypothesis:

Hypothesis 3: **Timing.** An iceberg order on the bid side is associated with a greater likelihood of sell market orders and larger sell market orders, holding other things equal, with the corresponding prediction for iceberg orders on the ask side and buy market orders.

By timing the iceberg order submission the submitter increases the likelihood of filling the order. It also possible that potential counterparties react to signal of an iceberg order and perhaps react more strongly depending on the size of the iceberg order. The fact that iceberg orders are detectable makes signalling possible, and as long as there is some latent liquidity demand, there are potential counterparties who may react to the signal. The fact that the iceberg submitter could have stayed out of the order book and either submitted a

¹The results on the order aggressiveness in De Winne and D'Hondt (2007) illustrate this point. They find that a signal of an iceberg order increases the order aggressiveness, but the results are also consistent with the reverse explanation that the iceberg order was submitted in anticipation of greater order aggressiveness.

series of smaller limit orders or waited for suitable limit order to appear in the order book implies that she chose to follow a strategy that potentially reveals more information than some alternative strategies. Regardless of the intent we may have an effect that can be thought of as a signaling or advertising effect of the iceberg order. This leads us to our fourth hypothesis:

Hypothesis 4: Advertising Effect. A detected iceberg order on the bid side increases the likelihood of a sell market order and increases the expected size of sell market orders. Analogous predictions apply to the ask side of the order book and buy market orders.

Despite the fact that market participants may detect and react to iceberg orders, they clearly have less information and hence are subject to potential adverse selection. Liquidity demanders are exposed to the risk of trading with an iceberg order that turns out to be larger than expected. Conversely, liquidity demanders fare better if they trade with an iceberg order that turned out to be smaller than expected. So here the active side of the trade is exposed to an adverse selection risk that is similar to the one faced by the passive side in the Glosten (1994) model.

Liquidity suppliers who submit limit orders may suffer losses for the following reason. Any limit order behind the iceberg order in the order queue is very unlikely to be executed whereas limit orders on the other side are relatively more likely to be executed. If the iceberg order tends to move the prices, this means that limit orders are more likely to receive more unfavorable executions and less likely to received favorable executions. Like the risk for liquidity demanders this risk is more severe when the iceberg order is a surprise or when it is turns out to be larger than anticipated.

Hypothesis 5: Adverse Selection. Iceberg orders create an adverse selection risk for both liquidity demanders and suppliers. The risk is more severe when the iceberg order has not been detected or when it is larger than expected based on available information.

2 Our Sample and Methodology

2.1 Our Sample

Our sample is from Deutsche Börse's electronic trading platform Xetra. It covers all thirty stocks in the DAX-30 German blue chip index for the period January 2nd to March 31st, 2004. On Xetra, traders can, in addition to market and limit orders, submit iceberg orders. The order records identify iceberg orders so that we are able to reconstruct snapshots of both the displayed and hidden order books. We restrict our sample to continuous trading only. We present more details on the sample reconstruction in Appendix A4.

In the order book, an order is given priority according to price, display condition, and time. A sell order at a lower price has priority relative to any sell orders at higher prices, regardless of the order's time of submission or display condition. At the same price level, a displayed order has priority relative to any hidden orders regardless of the order's time of submission. Among displayed orders, an order submitted earlier has priority relative to any orders submitted later. When an iceberg order's displayed part is fully executed and the next peak converts from hidden to displayed status the newly displayed peak also receives a new time stamp which determines its time priority.

2.1.1 Iceberg Submissions

For the purpose of brevity we sort the stocks into three categories—large, medium, and small—based on trading activity and report all results for these three categories only. The large and medium categories have eight and seven stocks, respectively, with the remaining fifteen stocks being assigned to the small category. Table A1 in the appendix reports descriptive statistics for all thirty sample stocks.

Table I reports cross-sectional descriptive statistics for iceberg and limits orders with cross-sectional standard deviations in parentheses. Panel A shows that the iceberg orders' share of all non-marketable orders submitted ranges from 7 to 11% with an overall average of 9%. Iceberg orders represent a greater fraction of shares executed with the corresponding percentages ranging from 15 to 20% with an overall average of 16%. Panel B reports the Table I median distance between the order price and the best quote for iceberg orders and limit approxorders. The differences between iceberg and limit orders in the order price dimension appear imately to be small and unsystematic. here.

Panel C reports averages of the iceberg order's total size, peak size, the number of submitted peaks, and the number of executed peaks of iceberg orders whose first peak size was executed. The last row of the panel reports the average size of limit orders. Iceberg orders are on average 12 to 20 times larger than limit orders demonstrating that iceberg orders tend to be an order of magnitude larger than limit orders. Even the peak size is between 2.2 and 2.9 times larger, which further underscores the difference between iceberg orders and limit orders in order size.

The number of peaks is negatively correlated with the peak size since the product of their averages exceeds the average total size. We explore the relationship between peak size and the number of peaks in more detail below. The average number of executed peaks shows that conditional on the first peak being executed, on average, four new peaks will be displayed and approximately 80% of the executed shares originate from initially hidden volume for these orders.

Panel D reports statistics on the clustering of the total size, peak size, and the number of peaks. We report the percentage of all observations that are accounted for by the three most frequently observed values to illustrate the degree of clustering. The clustering is strongest for the peak size with 59% of all observed peak size values accounted for by the three most frequently observed values for a typical stock. The number of peaks is somewhat less clustered with a corresponding average frequency of 34%.

2.1.2 Iceberg Executions

Table II reports statistics on several dimensions of the iceberg execution. The first specification in Panel A is a regression of the realized profit for iceberg orders, with at least one executed peak, on the total order size, the executed volume, and the peak size. We normalize all variables so that the intercept captures the average realized spread for a typical iceberg order. The realized profit is measured as the signed difference between the iceberg order's Table II price and the mid-quote 30 minutes after the iceberg's last peak was executed. On average, approxthe per share realized profit is positive, and significantly different from zero, starting at imately 1.7 basis points for the large and increasing to 3.7 basis points for the small stock group. here.

The second specification includes both the total order size and the executed volume and this combination reveals an interesting regularity. Holding the executed volume constant, a larger iceberg order has a higher realized spread suggesting that the hidden size matters for the future mid-quote even though it may never be directly observed by market participants. The effect of the iceberg's peak size is more mixed with many stocks having a negative coefficient albeit not always significantly different from zero. The importance of the order size is evidence that the ability to hide the order size creates a strategic advantage. Conversely, it explains why other market participants may expend resources trying to detect iceberg orders and predict their total size.

Prior to the execution of its first peak the iceberg order resembles a limit order. To take into account the possible difference between the first and subsequent peaks we estimate models for both the probability of execution for the first peak and the execution percentage conditional on the first peak being executed. Panel B and C report the marginal effects for the two execution statistics. The negative marginal effect of the peak size for the execution probability is consistent with a larger peak size encouraging undercutting and hence reducing the probability of execution. On the other hand, Panel C shows that, conditional on one peak being executed, a larger peak size increases the percentage executed. Once a peak has

been executed, the iceberg order is likely to have been detected and at that stage a larger peak size facilitates a greater execution percentage because each added peak represents a larger fraction of the total order and minimize the opportunities for limit orders to gain priority by matching the price of the iceberg order. Both of these effects are consistent with the assumptions made regarding the peak size in Esser and Mönch (2007).

The distance to the best quote has, as expected, a large negative effect on the probability of execution, but conditional on an executed peak the initial distance to the best quote is no longer useful for predicting the percentage executed. The order size has a positive marginal effect for the probability of execution which is interesting since it is hidden. One interpretation is that traders submitting larger iceberg orders are more patient and therefore more likely to received at least one execution. The same variable has a negative marginal effect on the percentage executed, which is expected as, everything else equal, it is more difficult to fill a larger order.

2.2 Methodology

Our methodology consists of an algorithm for detecting iceberg orders and a model for predicting the hidden volume. The goal is to approximate the market participants' information set with respect to iceberg orders and hidden volume and to relate innovations in their information set to subsequent price and order flow dynamics. We presents each part of our methodology in more detail below.

The detection algorithm solves a problem that is similar to the one solved by researchers with limit order book datasets that lack the complete information on iceberg orders. For example, Biais, Hillion, and Spatt (1995) apply a method to determine that one trade out of eight is partially executed against an iceberg order using only information available to anyone observing the order book. De Winne and D'Hondt (2007) develop an algorithm similar to the one we use and apply to a dataset that includes iceberg order information. Bessembinder, Panayides, and Venkataraman (2009) show for a related dataset how other publicly observed variables can be used to generate informative predictions about iceberg orders even before any executions have occurred. We extend this line of inquiry by exploiting both information from both detected and undetected iceberg orders in our analysis. There is no priori work that we are aware of that generates dynamic predictions for hidden volume.

2.2.1 Detecting Iceberg Orders

A detection algorithm is a set of rules for generating predictions of whether or not a given order book contains iceberg orders based on publicly available data. The basic idea is that if an order book contains an iceberg at the best quote then a trade that exhausts all the displayed depth at the best quote prompts an immediate addition of new depth equal to the iceberg order's peak size. Following such an event the algorithm sets the indicator for an iceberg to one and based on the amount of added depth the algorithm will anticipate future depth changes for as long as the iceberg order remains in the order book. The algorithm remembers the indicator values for multiple prices so if the current best quote, which has a detected iceberg, is undercut but later becomes the best quote again the algorithm assumes that the iceberg order is still there until an anticipated update to the order book depth fails to occur. We provide a detailed example that illustrates how our algorithm works in Appendix A3.

Table III reports the average frequencies of the iceberg signals generated by the algorithm compared to the true iceberg states. Similar to our applications later, it only reports Table III results for the best quote only. The frequencies reported in the table are the cross-sectional approxaverages with cross-sectional standard errors reported in parentheses. The diagonal entries imately are the percentages of correct predictions; for 85 to 90% of the observations the algorithm here. correctly detects no iceberg order, and for 6 to 9% of the observations the algorithm correctly detects an iceberg. The top right entry in each panel is the percentage of observations for which the algorithm falsely detects an iceberg. These instances are relatively rare with the average frequency being around 1%. The bottom left entry in each panel is the percentage of observations for which the algorithm fails to detect an iceberg order. Between 3 and 5% of the observations fall in this category. The algorithm's relative weakness is the instances of iceberg orders that it fails to detect. These percentages suggest that iceberg orders may succeed in remaining hidden, albeit only for a limited amount of time.

The frequencies reported in Table III are for the ask side only. The results for the bid side are very similar. Furthermore, the correlation between icebergs on the bid and the ask side is low so the frequency of an iceberg signal for at least one side of the book is approximately twice the percentages in the bottom right of each panel.

It is difficult to determine how closely the predictions from our algorithm approximates the market participants' information about iceberg orders. Conversations with market participants suggest that it is reasonable to assume that active participants are able to discern this type of information from observing the order book dynamics or by using their own algorithms. It may also be the case that some market participants can generate even more accurate predictions using other signals.

2.2.2 Predicting Hidden Volume

Figure 1 shows a mosaic plot of the peak size and the total size for one representative stock (ticker: DPW). The widths of the boxes is proportional to the frequencies of the different peak size categories. Similarly the height of the resulting boxes is proportional to the frequencies of different total sizes given a peak size category. The shading of the boxes and the plus and minus signs indicate the strength of the deviation from the null hypothesis of independence.

Figure 1

approx-

The plot shows that the peak size and the total size are positively correlated although the imately total size is non-linear in the peak size and exhibits some discontinuities. For example, for here. both the 1K and 2K peak size category, the total size that is unusually frequent is 10K. On

the other hand, if we compare the smallest and the largest category of peak sizes, 1K versus 10K, we see that the total size categories do not overlap much with most of the distribution shifted to either 20K or 50K for the largest peak sizes. We observe some cross-sectional variation but all stocks exhibit both a general positive correlation between peak size and total size with some deviations that may reflect clustering on certain round numbers or a deliberate choice by the iceberg order submitters.

Market participants do not observe all the information in Figure 1, but they can identify the peak size and track the number of peaks executed for detected iceberg orders. We assume that market participants form rational expectations about the hidden volume based on this information. Table IV reports regression results for predicting the hidden volume Table IV at the best quote, conditional on an iceberg signal, using the peak size and the number of approxexecuted peaks. We report average parameter estimates and standard errors for a linear and imately a piecewise-linear specification. In both specifications the hidden volume and the peak size here. are normalized by the average peak size for each stock.

Regardless of the specification the predicted hidden volume is positive correlated with the peak size of the detected iceberg, and each executed peak reduces the predicted hidden volume by an amount that is smaller than the average peak size.

Figure 2 shows the observed average hidden volume as a function of the number of approxexecuted peaks for one of the sample stocks, DPW, and the four most commonly observed imately peak size categories. The average fitted values for the piecewise linear specification is plotted here. with a solid line in the graph. The hidden size has been normalized by the average peak size for each stock. The relationship between hidden volume and the number of executed peaks is, in general, negative, as expected, with a slope that is less than one; for each executed peak the expected hidden volume declines by less than one peak. We observe distinct jumps for all three stocks between four and five and between nine and ten executed peaks.

Figure 2

3 Empirical Results

We start by presenting our results for the impact of iceberg orders on future prices and the market order flow. We then present our results for the iceberg orders' impact on order book profits.

3.1 The Impact on Prices

Table V reports results for regressions with the mid-quote change as the dependent variable approand iceberg and hidden volume among the independent variables. We measure the midimate quote change over a thirty trade horizon that starts from the current trade. The first six here. rows of the table (above the dashed line) report parameter estimates with standard errors that capture a standard price impact of market orders which includes an intercept, a fixed parameter on the sign of the trade, and a trade-size dependent parameter. The parameter estimates for the fixed parameter are between two and three basis points and the parameter estimates for the trade-size dependent parameter are between one-half and one basis points.

In specification A we add two iceberg related variables to determine to what extent iceberg orders have any impact. The first is a signed indicator for a detected iceberg order; the indicator is positive for a buy iceberg and negative for a sell iceberg order. A positive coefficient on the indicator implies that the mid-quote tends to shift in the direction of the iceberg order. The second iceberg variable interacts the signed market order size with an unsigned indicator for a detected iceberg. The coefficient on this variable captures any differential price impact of market order size with iceberg orders in the book.

The parameter estimates on the signed iceberg indicator are positive and significantly different from zero for all three categories implying that, holding other things equal, the midquote tends to increase over the next 30 trades, if there is an iceberg at the bid side at time tand conversely decrease, if there is an iceberg at the ask side. The coefficient on the iceberg

Table V approximately indicator interacted with the signed market order size is negative for all categories and ranges from -0.2 to -0.3 basis points implying that the per unit price impact is approximately 30% smaller when there is an iceberg order in the order book; both the future mid-quote and the per unit price impact is different for order books with detected iceberg orders. Overall, the evidence suggests that the price impact is both statistically and economically different when iceberg orders have been detected.

In specification B we add the executed iceberg volume and predicted hidden volume. The executed iceberg volume is defined as the sum of all shares executed that originated from the iceberg order in the current iceberg sequence. The predicted hidden volume is obtained from the fitted values of the piecewise-linear specification in section 2.2.2. Both the executed iceberg volume and the predicted hidden volume are signed and normalized by the average market order size.

The positive parameters on the predicted hidden volume imply that, holding other things equal, greater expected hidden volume on the bid side is associated with a higher future price. The mean predicted hidden volume across the categories is between 7 and 10 units and produce a price impact that range from one to three basis points. A one standard deviation shock to the predicted hidden volume—which is between 3 and 5 units—translates into a change of between 0.5 to 1.5 basis points.

The estimated parameters on the executed iceberg volume are negative and range from -0.07 to -0.16 basis points. Across the three categories the mean value of the executed volume is between 7 and 9 units which translates into an average adjustment of between -0.5 to - 1.4 basis points. A one standard deviation shock to the executed iceberg volume—which is between 7 and 10 units—increase the magnitude of the adjustment to between -1.3 and -3 basis points. The evidence of the price impact being increasing in the order size is consistent with Hypothesis 1. The fact that the net price impact decreases, holding other things equal, in the executed iceberg volume supports the liquidity-based explanation of Hypothesis 2.

Specification C adds the 'surprise' in the hidden volume defined as the difference between the actual hidden volume and the predicted hidden volume. If market participants underestimate the amount of hidden volume, we expect the difference to eventually be reflected in prices either by market participants learning the truth as more peaks are displayed or indirectly through future order flow. In either case we would expect a greater than expected hidden volume on the bid side to predict a higher mid-quote and vice versa according to Hypothesis 1. The estimated parameter on the actual minus predicted hidden volume is between 0.15 and 0.36 basis points per unit and provides additional support for the hypothesis. A shock equal to one standard deviation of the surprise hidden volume, which has a mean of zero, is approximately equal to 8 units and that shock translates into an expected mid-quote adjustment of one to three basis points.

Specification D replaces the predicted hidden volume with the actual hidden volume to determine the importance of measurement errors from the prediction exercise. As expected the increased precision raises the estimated parameters on the actual hidden volume compared to those of the predicted hidden volume and reduces the parameters on the signed iceberg indicator. The estimated parameters on executed volume are nearly unchanged.

Overall, the results show that iceberg orders have an impact on prices, but the magnitude of the impact depends critically on the realization of the net liquidity demand. If a large fraction of the iceberg order is executed, it implies a smaller net liquidity demand shock—the demand from the iceberg was largely met by latent demand on the other side—resulting in a smaller price change. On the other hand, if there are few executions relative to the size of the iceberg order then we have a large net liquidity demand shock which generates a larger price changes which is increasing in the iceberg order's size. The fact that the impact of an iceberg order, holding its size constant, depends on the order flow realization suggests that the impact is more about the discovery of the net balance of liquidity demand than about trading on private information. If the primary reason for submitting the iceberg order was private information we would, on average, expect a price change that increases in its size but that is independent of the order flow realization.

3.2 The Impact on Market Order Flow

Table VI reports results for the market order size regressed on four indicators for detected approxand not detected iceberg orders, visible volume, executed iceberg volume, and predicted imately hidden volume. For all variables we distinguish between the effect on the side of the order here. book that is hit by the market order and the side that is not hit.

The estimated coefficients for the iceberg indicators are all positive and significantly different from zero implying that market order size and iceberg orders are positively correlated. The estimated parameters for market orders hitting detected icebergs are approximately 0.4 for specification A implying that the average market order size increases by approximately 40% when an iceberg has been detected iceberg. But, the magnitude of the parameter estimates for the corresponding not detected iceberg indicators are also positive and often of the same order of magnitude in line with the timing explanation of Hypothesis 3. The positive and significant albeit smaller coefficients for not hit indicators lend further support to this interpretation.

Specification B adds the visible order book volume which we normalize to have a mean of zero and a unit standard deviation. The estimated parameters on the visible volume on the hit side are between 0.3 and 0.4 implying that a one standard deviation increase in the visible volume increases the average market order size by approximately 30 to 40%. The effect is weaker for the not hit side of the order book with parameters between -0.02 and 0.05. In this specification the parameter estimates for the hit iceberg indicators are all smaller in magnitude and the change is greater for the not detected iceberg orders. Despite this effect the hit side effects for the indicators remain around 0.25 suggesting that the greater market order sizes are not simply a by-product of greater visible order book volume.

Specification C adds the executed iceberg and the predicted hidden volume. The parameter estimates on the executed volume on the hit side are positive and significantly different from zero with values approximately equal to 0.05. The corresponding parameters for the not hit side are negative. The positive hit side parameters are indicative of a feedback effect by which a greater volume executed against the iceberg order attracts larger market orders. The predicted hidden volume also has positive parameter estimates with larger and significant estimates for the hit side and positive but smaller estimates for the other side. The positive and greater hit side parameter estimates are consistent with larger predicted hidden volume attracting larger market orders. Overall, the results for specification C are consistent with an advertising effect of iceberg orders (Hypothesis 4).

Table VII reports results for a logit model of the probability of a buy market order condiapproxtional on iceberg indicators, visible volume, executed iceberg and predicted hidden volume. imately The reported figures are average marginal effects with standard errors in parentheses. In here. specification A we include indicators for detected and undetected icebergs on the bid and ask sides of the order book. The estimated marginal effects are between -0.17 and -0.19 for the bid side and 0.17 to 0.19 for the ask side implying that with an iceberg on the ask side of the order book we observe a shift in the probability of buy market order from 0.5 to approximately 0.7 with a corresponding effect for the other side. The marginal effects for the undetected iceberg indicators have the same sign but are less than one-third as large as the corresponding marginal effects for the detected iceberg orders. The larger marginal effect of the detected iceberg suggests that liquidity demanders are drawn to the iceberg order consistent with a advertising effect of Hypothesis 4.

Table VII

In specification B we add the visible volume for the ask and bid sides of the order book. The visible ask volume has a negative marginal effect of approximately -0.04 which counteracts the positive marginal effect of a detected iceberg on the ask side. Furthermore, the average visible volume is slightly positive when an iceberg is detected implying that a

visible ask volume that is one standard deviation above the mean value for detected iceberg states on the ask side reduces the probability of a buy market order from 0.71 to 0.55. This negative effect is consistent with existing evidence of market versus limit order submissions (see, e.g., Biais, Hillion, and Spatt (1995). It also means that the iceberg submitter who affects the visible volume by his choice of peak size faces a trade-off.

In specification C we drop the undetected iceberg order and add the executed iceberg and predicted hidden volume. We normalize the executed and predicted volumes to have a mean of zero and standard deviation of one, conditional on a value of one for the iceberg detection indicator. The marginal effect of executed ask volume is positive implying that, holding other things equal, the probability of a buy market order increases as the volume executed against the iceberg volume. Like the corresponding results above for the market order size this is in line with a feedback effect. Together, this is evidence of the iceberg order itself having an impact on the market order flow that is distinct from any timing effect.

The trading game is a zero-sum game with the profits or losses of liquidity suppliers with iceberg or limit orders jointly determining the transaction costs for liquidity demanders. To determine what the joint effects are of the above results on the price impact and the market order flow we examine the order book profits next.

3.3 The Impact on Order Book Profits

Table VIII reports the average estimates of the expected order book profits. The expected approxorder book profits are determined by the conditional probability of an order being executed imately multiplied by the signed difference between the order price and the expected mid-quote here. conditional on execution. We prefer to focus on the expected rather than the realized order book profits because we are interested in how the profits are split between different types of orders or traders something that is difficult to disentangle from the expect figures. In order to compute the order book profits we use the price impact function that we estimated above

Table VIII

(Table V), the market order size distribution (Table VI), and the probability of a buy market order (Table VII). We assume further that the market order size distribution is exponential with a conditional mean order size determined by as reported in Table VI. Appendix A2 provides more details on our procedure for computing the profits.

The overall average order book profits is between 0.5 and 1 basis points. When the books are split based on whether or not there is an iceberg order we observe greater profits without iceberg orders and smaller and sometimes negative profits with iceberg orders. Lower order book profits imply gains for liquidity demanders, which combined with the fact that we observe larger market orders, suggest that liquidity demanders overall fare better when there are iceberg orders in the order book.

Table IX reports the breakdown of the order book profit estimates for order books with approxiceberg orders. Panel A reports the estimates for books with detected iceberg orders split by the order type, iceberg order versus all limit orders, and for limit orders on the side of the here. iceberg order versus the opposite side. The *ex ante* profits for iceberg order do not vary much across the detected and not detected cases. In contrast, the *ex post* profits are substantially greater for the not detected cases ranging from 0.5 to 1 basis points for the ex post case versus approximately zero for the detected cases.

The limit order profits are negative across the books with detected and undetected iceberg orders. But, if we split the limit orders whether they are on the same or opposite side of the iceberg order, we observe that limit orders that are on the side of the iceberg order generate positive profit both for detected and undetected iceberg orders. The greater expected profits for unanticipated iceberg orders, the negative profits for limit orders on the opposite side as well as overall (ex post) provide evidence consistent with adverse selection (Hypothesis 5). Table X

Table X reports estimation results for regressions that relate the *ex post* expected profits approxaccruing to different orders—iceberg orders, limit orders, and market orders—to information imately about the iceberg orders and the remaining hidden volume. We are interested in how the here.

Table IX

imately

order book profits are split between the iceberg submitters, the liquidity providers who use limit orders, and the liquidity demanders. Neither the executed iceberg volume nor the surprise hidden volume are exogenously given so these regressions are simply used to illustrate how the profits accruing to different types of orders vary across different types of outcomes without implying any causal relationship.

The right-hand side variables have been normalized to have a mean of zero and standard deviation of one so that the intercept captures the mean profits. For books with detected iceberg orders the profit for iceberg orders is approximately zero, so the negative profit for limit orders implies a gain (profit) for the market orders. In contrast, for order books with undetected iceberg orders the iceberg orders, on average, capture a profit of 0.5 to 1.1 basis points, and since market orders also capture a small profit, the limit orders suffer a loss of 0.5 to 1.7 basis points.

The profits for iceberg orders are increasing in both the predicted hidden volume and the surprise hidden volume. The effect of the surprise hidden volume is between 1.1 and 2.6 basis points for a one standard deviation shock to the surprise hidden volume providing evidence that iceberg order that are surprisingly large earn higher profits and, of course, vice versa for smaller than expected iceberg orders.

The limit order submitters earn lower or even negative profits from order books with iceberg orders. In contrast they earned positive profits in books without iceberg orders. In particular, limit orders are exposed to losses driven by two factors. First, limit orders on the opposite side of iceberg orders suffer losses because iceberg orders have price impact; the losses are more severe when iceberg orders are undetected. Second, limit orders on the same side of the book as the iceberg orders would earn profits but execution is only likely if they match the iceberg order's price otherwise they are too far back in the queue.

The overall results for market order submitters are mixed. The main exception is the small stock group for which the average estimated profits are positive and significant regardless of whether the iceberg has been detected or not. In general, the profits accruing to market orders increase in the iceberg order size and in the amount of executed iceberg volume.

4 Interpretation

We interpret the evidence above as supporting the idea that iceberg orders have a price impact that depends on the net demand for liquidity. In submitting an iceberg order a trader balances the benefit of displaying more of her order size—the advertising effect—against the benefit of hiding more of it. Because it is the iceberg order's most salient feature the latter effect has naturally received the most attention. For example, the theoretical models to date start from the assumption that iceberg orders will be used so as to hide as effectively as possible. The fact that the observed iceberg order peak sizes deviate significantly from the typical limit order sizes and our main results all suggest that the advertising or signaling aspects of the iceberg order may be equally important.

The rationale for using iceberg orders is that *ex ante* the large traders by definition has limited information about the latent demand. Submitting an iceberg order is effectively a way for the trader to search for latent liquidity. If latent demand is discovered, the trader ends up trading a larger fraction of the order at a price that may compare favorably to alternative strategies. If no or only limited latent demand is discovered, the trader ends up executing only a fraction of the order and needs to resubmit or follow an alternative strategy to complete the trade. But, the greater transaction costs in the latter case are simply a reflection of market conditions and in some sense the trader is no worse off having searched for the latent demand using the iceberg order.

The welfare properties of market designs with iceberg orders is obviously an important question. Although we cannot address that question directly our results shed some light on the issues involved. The evidence of feedback effects with more executed iceberg volume attracting larger market orders and increasing the probability of market orders hitting the iceberg order are indicative of a potential positive externality of iceberg orders. On the other hand, other liquidity providers who submit limit orders do not fare well in order books with iceberg orders. They make up for that with higher profits in order books without iceberg orders but that means that it is hard to determine the net effect.

Our results have some implications for the way we think about the dynamic aspects of the iceberg strategy. In particular, the fixed price for each of the iceberg order's peaks is intriguing in the light of the above results. Both our price impact and market order flow results show that there are distinct time patterns and these patterns remain in the order book profit results. One can think of the iceberg order submitter as a seller who sequentially auctions off multiple peaks at a fixed price. One part of the auction literature documents and studies a phenomenon that is known as the declining price anomaly in multi-unit sequential auctions (see, for example, Bernhardt and Scoones (1993)). The anomaly is that prices for identical items sold in later auctions tend to be lower than those sold in earlier auctions. In the case of iceberg orders the puzzle is that the prices are fixed for each 'round' or peak but because new information is revealed with the execution of each peak it would appear that the value is changing. The question then is under what assumptions is an iceberg order with a fixed price per peak the optimal type of iceberg order? For example, why not have an iceberg order that moves the price to buy down marginally after each executed peak? Or an iceberg order whose peak size increases dynamically after detection? And, if the fixed price is optimal, then what is the optimal strategy for liquidity demanders?

5 Conclusions

We examine the impact of iceberg orders on the price and order flow dynamics in limit order books. One of our main findings is that we find strong support for an advertising or signalling effect of iceberg orders. Part of the effect is an artifact of the iceberg order type—the fact that it is detectable—but part of it is under the control of the iceberg order submitter through her choice of peak size. An important outstanding question is how the optimal peak size is determined for a given total order size.

In principle, the order updates generated by an iceberg order can also be replicated using a dynamic order submission strategy. What determines the choice between these two seemingly equivalent strategies? Does the fact that the iceberg order is in the limit order book increase its effectiveness in terms of signalling?

Even if we abstract from the signalling, the iceberg order itself is a pre-packaged dynamic order submission strategy. Likewise, a market order submitter who trades against a detected iceberg order solves a special dynamic order submission problem since the iceberg order temporarily makes the order book perfectly resilient after each executed peak. Under what assumptions can we rationalize these types of strategies in existing dynamic models of optimal trading such as Bertsimas and Lo (1998), Huberman and Stanzl (2005), Obizhaeva and Wang (2006)?

Addressing these questions as well as determining the welfare properties of market design with iceberg orders are all important topics for future research.

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Figure 1: A mosaic plot of the peak size (horizontal axis) against the total size (vertical axis) for DPW. We use the following cut-offs for peak size categories: 1-1,500 shares \Rightarrow 1K; 1,501-2,500 \Rightarrow 2K; 2,501-3,500 \Rightarrow 3K; 3,501-7,500 \Rightarrow 5K; 7,501+ \Rightarrow 10K; and total size categories: 1-7,500 shares \Rightarrow 5K; 7,501-12,500 \Rightarrow 10K; 12,501-17,500 \Rightarrow 15K; 17,501-35,000 \Rightarrow 20K; 35,001+ \Rightarrow 50K. The plot is constructed by dividing the unit interval into five segments whose lengths are proportional to the frequency of observed peak sizes that fall within each category. This determines the width of each 'box'. The height of each box is determined similarly by the frequencies of total sizes for a given peak size category. The shading reflects the deviation from the relationship expected under independence and is based on the standardized (Pearson) residuals; dark shading (large "+"), > 4; light shading (small "+"), 2 : 4; solid box 0 : 2; dashed box -2 : 0; dashed box (small "-") -4 : -2. Residuals in excess of 4 in absolute value correspond to a p-value of 0.0001 and residuals between 2 and 4 in absolute value to a p-value of 0.05 for a chi-square test with the null hypothesis of independence of peak and total size.



Figure 2: The graph shows the relationship between the number of executed peaks and the remaining hidden volume for *detected* iceberg orders. Each set of bars in the graph represent the average hidden volume at the best quote as a function of the number of executed peaks (up to 15 peaks) for different peak size categories for DPW. The counter for the number of executed peaks keeps track of the iceberg order history so that, if an iceberg after detection is undercut, but later reappears at the best quote the counter will remember the past executed peaks and only reset the counter when the iceberg leaves the book. The dots connected by the solid line represent the average fitted values for a regression that predicts the hidden volume based on the peak size and the number of executed peaks, see Section 2.2.2 and Table IV. The cut-offs used for the peak size are as follows: 1-1,500 shares \Rightarrow 1K; 1,501-2,500 \Rightarrow 2K; 2,501-3,500 \Rightarrow 3K; 3,501+ \Rightarrow 5K. The remaining hidden volume is scaled by the average peak size for all icebergs.

					<u> </u>				
	La	arge	Mee	lium	Sr	nall	1	All	
Panel A: Iceb	erg Or	ders' Sha	re of N	on-Mar	ketable	Orders [%]		
Percent of shares submitted	6.9	(1.1)	11.2	(4.9)	9.8	(3.2)	9.3	(3.6)	
Percent of shares executed	14.8	(3.1)	19.4	(3.8)	14.8	(5.2)	15.9	(4.7)	
Panel B: Median Dist	ance b	etween C	Order P	rice and	l Best G) uote [ba	sis poin	ts]	
Iceberg Orders	3.1	(1.5)	4.2	(2.2)	3.6	(1.9)	3.6	(1.9)	
Limit Orders	3.9	(1.1)	4.8	(1.9)	3.5	(2.1)	3.9	(1.9)	
Panel C: Average Size of Iceberg and Limit Orders									
Iceberg Orders									
Total Size [1000 shares]	17.3	(12.3)	19.2	(8.7)	14.0	(4.4)	16.1	(8.2)	
Peak Size [1000 shares]	3.1	(3.2)	3.2	(1.9)	2.0	(0.9)	2.6	(2.0)	
Submitted $\#$ of Peaks	7.3	(1.2)	7.1	(0.7)	7.9	(0.9)	7.6	(1.0)	
Executed $\#$ of Peaks	5.6	(0.6)	5.6	(0.3)	5.3	(0.5)	5.5	(0.5)	
Limit Orders [1000 shares]	1.4	(1.7)	1.3	(0.8)	0.7	(0.4)	1.0	(1.0)	
Panel D: Clustering	of Ice	berg Peal	x Size, '	Total Si	ze and	Number	of Peaks	3	
Total Size [%]	47.6	(10.1)	41.5	(2.4)	46.1	(6.1)	45.4	(7.0)	
Peak Size [%]	58.2	(14.7)	49.8	(6.6)	63.9	(15.0)	59.1	(14.3)	
Number of Peaks [%]	35.9	(8.6)	31.8	(6.2)	34.9	(6.6)	34.4	(7.0)	

 Table I: Iceberg Orders: Summary Statistics

Table I reports summary statistics for iceberg orders and limit orders. Panel A reports the percentage of submitted and executed (non-marketable) orders that are iceberg orders. Panel B reports the cross-sectional average of the median distance between the order price and the best quote on the same side of the order book for iceberg orders and limit orders. Panel C reports the average iceberg order total size (1000 shares), the average peak size (1000 shares), the average number of peaks submitted, and the average number of peaks executed for iceberg orders with at least one executed peak. The last row of Panel C reports the average limit order size (1000 shares). Panel D reports the percentage of all observations that are accounted for by the three most common values of the total size, peak size, and the number of peaks. The sum of the frequencies for the top three values are computed for each stock and then averaged within each category or across the three categories. Cross-sectional standard deviations are reported in parentheses.

	Panel A: Realized Profit [basis points]								
		Depende	nt Varia	able: Re	alized Pro	ofit Usin	g the M	id-Quote	
		Thirty	Minute	es After	the Execu	ution of	the Last	Peak	
OLS		Large			Medium			Small	
Intercept	1.66	1.66	1.66	2.78	2.78	2.78	3.74	3.74	3.74
	(0.72)	(0.72)	(0.72)	(0.82)	(0.82)	(0.82)	(1.50)	(1.50)	(1.50)
Order Size	0.60	5.59	5.98	1.19	7.47	7.85	1.06	7.16	7.89
	(0.72)	(1.04)	(1.10)	(0.82)	(1.23)	(1.30)	(1.50)	(1.86)	(2.01)
Executed Volume		-6.85	-6.67		-8.47	-8.28		-9.82	-9.53
		(1.04)	(1.05)		(1.23)	(1.25)		(1.86)	(1.89)
Peak Size			-0.95			-0.92			-1.89
			(0.87)			(1.01)			(1.77)
	Р	anel B: F	First Pea	ak Execu	ution Prol	oability	(Margin	al Effects	3)
Logit		Depend	dent Va	riable: I	Execution	Indicat	or for 1s	t Peak	
Order Size		3.55			3.68			2.70	
		(0.80)			(0.75)			(1.35)	
Peak Size		-1.50			-2.91			-2.61	
		(0.76)			(0.75)			(1.27)	
Distance to		-14.73			-14.38			-12.91	
Best Quote		(0.73)			(0.69)			(1.28)	
	Pa	anel C: C	ondition	nal Exec	ution Per	centage	(Margin	al Effect	s)
Ordered Logit		Γ	Depende	nt Varia	ble: Exec	ution P	ercentag	e	
Order Size		-6.27			-7.23			-8.33	
		(0.65)			(0.64)			(1.49)	
Peak Size		5.93			6.20			7.19	
		(0.75)			(0.74)			(0.11)	
Distance to		0.81			1.12			0.03	
Best Quote		(0.54)			(0.54)			(1.60)	

Table II: Iceberg Orders: Realized Profit and Executions

Table II reports regression results for the realized profit and executions of iceberg orders. Panel A reports estimates for a regression of the realized profit for icebergs with *at least one executed peak* on an intercept, the order size, the executed volume, and the peak size. For a buy iceberg order the realized profit is measured as the difference between the mid-quote 30 minutes after the order's last execution and the order price. The units are basis points. The regressions are estimated stock-by-stock and we report the average parameters estimates with average standard errors in parentheses. All variables are normalized to have a mean of zero and standard deviation of one. Panel B reports the marginal effects (in percent) for a logit model for the probability of the first peak being executed as a function of the order size, the peak size, and the distance between the order price and the best quote on the same side. Panel C reports the corresponding (combined) marginal effects for an ordered logit model of the total execution percentage conditional on execution of the 1st peak. The distance from the best quote is defined as the difference between the best (same side) quote and the iceberg order's price, in basis points, at the time of the order submission.

					-	-			
		Large			Mediur	n		Small	
	Predi	iction		Predi	ction		Predi	ction	
Truth	No	Yes	Sum	No	Yes	Sum	No	Yes	Sum
No	90.0	1.0	91.0	84.7	1.5	86.2	89.9	0.8	90.7
	(1.2)	(0.2)	(1.0)	(2.1)	(0.2)	(1.9)	(1.4)	(0.1)	(1.1)
Yes	2.9	6.1	9.0	4.6	9.2	13.8	3.1	6.1	9.3
	(0.5)	(0.5)	(1.0)	(0.8)	(1.1)	(1.9)	(0.4)	(0.8)	(1.3)
Sum	92.9	7.1	100.0	89.3	10.7	100.0	93.0	7.0	100.0
	(0.7)	(0.7)		(1.3)	(1.3)		(0.9)	(0.8)	
						'			

Table III: Detecting Iceberg Orders

Table III reports, for the best ask quote in the book, the cross-sectional averages for the predictions (yes/no) generated by the iceberg detection algorithm across the percentages of the true iceberg status (yes/no). The columns of each 2×2 matrix correspond to the algorithm's predictions and the rows correspond to the truth. Entries on the diagonal correspond to correct predictions. The cross-sectional standard errors of the means are reported in parentheses below each mean. The results for the bid side are similar with the largest difference being of the order of less than one-half percentage points.

	Lat	rge	Med	ium	Sm	all
Intercept	2.29	2.55	2.34	2.60	2.66	2.92
-	(0.08)	(0.09)	(0.08)	(0.09)	(0.20)	(0.21)
I_{5-9}^{peak}		-1.47		-1.30		-1.72
0.0		(0.11)		(0.12)		(0.25)
I_{10+}^{peak}		-0.98		-1.36		-1.19
101		(0.23)		(0.21)		(0.51)
Peak Size	2.28	2.22	2.26	2.22	2.72	2.67
	(0.06)	(0.06)	(0.06)	(0.06)	(0.16)	(0.16)
$\operatorname{Peak}_t - 1$	-0.21		-0.18		-0.25	
	(0.01)		(0.01)		(0.02)	
$I_{1-4}^{peak} \times (\text{Peak}_t - 1)$		-0.48		-0.45		-0.55
		(0.04)		(0.04)		(0.08)
$I_{5-9}^{peak} \times (\text{Peak}_t - 5)$		-0.37		-0.33		-0.43
		(0.04)		(0.05)		(0.10)
$I_{10+}^{peak} \times (\text{Peak}_t - 10)$		-0.11		-0.03		-0.16
		(0.06)		(0.05)		(0.14)
R^2	0.19	0.21	0.16	0.17	0.17	0.19

Table IV: Predicting Hidden VolumeDependent Variable: Hidden Volume at Best Quote

Table IV reports average parameter estimates for regressions of the hidden volume at the best quote on the number of peaks executed and the peak size of the iceberg order. The number of peaks is denoted by Peak_t and is defined as the number of peaks that have been fully executed at the current price since the iceberg was detected; the number of peaks restarts when a new iceberg is detected. The second specification allows for (i) shifts in the intercept via I_{5-9}^{peak} and I_{10+}^{peak} , and (ii) the slope via the indicators $I_{1-4}^{peak} - I_{10+}^{peak}$ interacted with the peak counter ($Peak_t$). Both the hidden volume and the peak size are normalized by the average peak size for each stock. We estimate the regressions stock-by-stock for all observations with a detected iceberg and report the average parameter estimates for the large, medium, and small categories with average standard errors in parentheses.

Table	V:	Impact	on	Prices
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Dependent Variable:		La	arge			Me	dium			$\mathbf{S}_{\mathbf{I}}$	mall	
Δ Mid-quote over next 30 Trades	А	В	\mathbf{C}	D	А	В	\mathbf{C}	D	А	В	\mathbf{C}	D
Intercept	-0.15	-0.15	-0.15	-0.15	-0.28	-0.28	-0.29	-0.29	-0.20	-0.21	-0.21	-0.21
	(0.03)	(0.03)	(0.03)	(0.03)	(0.05)	(0.05)	(0.05)	(0.05)	(0.07)) (0.07)	(0.07)	(0.07)
Signed Trade	1.80	1.80	1.79	1.79	2.54	2.53	2.52	2.51	3.19	3.17	3.15	3.14
	(0.02)	(0.02)	(0.02)	(0.02)	(0.03)	(0.03)	(0.03)	(0.03)	(0.04)) (0.04)	(0.04)	(0.04)
Signed Trade Size	0.42	0.42	0.44	0.44	0.57	0.58	0.60	0.61	0.89	0.90	0.93	0.93
	(0.01)	(0.01)	(0.01)	(0.01)	(0.02)	(0.02)	(0.02)	(0.02)	(0.02)) (0.02)	(0.02)	(0.02)
Signed Iceberg Indicator	0.71	0.42	$\bar{0.43}$	0.14	 $-\bar{0.78}^{-}$	-0.12	-0.28	-0.57	1.45	0.21	0.22	-0.28
	(0.06)	(0.12)	(0.12)	(0.08)	(0.10)	(0.25)	(0.25)	(0.13)	(0.15)) (0.32)	(0.34)	(0.21)
Iceb. Ind. \times Signed Trade Size	-0.16	-0.17	-0.16	-0.16	-0.16	-0.16	-0.15	-0.15	-0.29	-0.30	-0.29	-0.29
	(0.01)	(0.01)	(0.01)	(0.01)	(0.02)	(0.02)	(0.02)	(0.02)	(0.04)) (0.04)	(0.04)	(0.04)
Executed Iceberg Volume		-0.07	-0.07	-0.08		-0.08	-0.08	-0.08		-0.14	-0.15	-0.16
		(0.01)	(0.01)	(0.01)		(0.01)	(0.01)	(0.01)		(0.02)	(0.02)	(0.02)
Predicted Hidden Volume		0.10	0.10			0.20	0.24			0.27	0.28	
		(0.01)	(0.01)			(0.03)	(0.03)			(0.03)	(0.03)	
Actual-Predicted Hidden Volume			0.15				0.28				0.36	
			(0.00)				(0.01)				(0.01)	
Actual Hidden Volume				0.14				0.28			. ,	0.35
				(0.00)				(0.01)				(0.01)

Table V reports the parameter estimates for regressions of the mid-quote change over the next 30 trades on a constant, the sign of the trade, the signed trade size, a signed iceberg indicator, the iceberg indicator multiplied by the trade size, and, in specifications B and C, the executed iceberg volume, the predicted (remaining) hidden volume, the surprise hidden volume (actual-predicted), and, in specification D, the actual hidden volume. The signed iceberg indicator is defined as the indicator for an iceberg order on the bid side minus an indicator for an iceberg on the ask side of the order book. The iceberg indicator times the signed trade size is defined as the indicator for an iceberg on the bid or the ask side multiplied by the signed trade size. The units for the change in the mid-quote is basis points. The executed and predicted hidden volume are signed so that bid side volume is positive and ask side volume is negative.

Dependent Variable: Market Order Size		Large			Mediun	1		Small	
	А	В	\mathbf{C}	А	В	\mathbf{C}	А	В	\mathbf{C}
Intercept	0.950	0.960	0.972	0.919	0.939	0.961	0.934	0.952	0.968
	(0.001)	(0.001)	(0.001)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)
Variables Associated with the Order Boo	ok Side <u>I</u>	<u>Iit</u> by th	e Market	t Order					
Iceberg Detected	0.401	0.253	0.272	0.435	0.273	0.246	0.426	0.259	0.286
	(0.010)	(0.011)	(0.005)	(0.011)	(0.011)	(0.006)	(0.012)	(0.012)	(0.007)
Iceberg Not Detected	0.307	0.282		0.294	0.262		0.379	0.295	
	(0.005)	(0.005)		(0.006)	(0.006)		(0.007)	(0.007)	
Visible Volume		0.273	0.273		0.404	0.404		0.404	0.403
		(0.003)	(0.003)		(0.005)	(0.005)		(0.005)	(0.005)
Executed Iceberg Volume			0.051			0.045			0.064
			(0.008)			(0.009)			(0.011)
Predicted Hidden Volume			0.110			0.099			0.091
			(0.011)			(0.010)			(0.023)
Variables Associated with the Order Boo	ok Side <u>N</u>	<u>Not Hit</u> k	by the M	arket Order					
Iceberg Detected	0.111	0.080	0.032	0.183	0.136	0.068	0.212	0.183	0.069
	(0.009)	(0.009)	(0.007)	(0.010)	(0.010)	(0.008)	(0.011)	(0.011)	(0.009)
Iceberg Not Detected	0.074	0.035		0.154	0.076		0.138	0.073	
	(0.007)	(0.007)		(0.008)	(0.008)		(0.009)	(0.009)	
Visible Volume		-0.019	-0.018		0.030	0.034		0.051	0.054
		(0.002)	(0.002)		(0.002)	(0.002)		(0.002)	(0.002)
Executed Iceberg Volume			-0.022			-0.029			-0.054
			(0.008)			(0.008)			(0.008)
Predicted Hidden Volume			0.055			0.027			0.055
			(0.008)			(0.010)			(0.008)

Table VI: Impact on the Market Order Flow: The Market Order Size

Table VI reports results for regressions of the market order size on iceberg detection indicators, indicators for undetected iceberg orders, visible volume, executed iceberg volume, and predicted hidden volume for the side of the order book that is 'hit' by the incoming market order and the side that is 'not hit.'. We estimate the regressions stock-by-stock and report the average parameter estimates and standard errors. All order book volume variables are normalized to have a mean of zero and the market order size is normalized to have a mean of one.

							•		
		Large			Mediun	1		Small	
	А	В	\mathbf{C}	А	В	С	А	В	\mathbf{C}
Ask Side Variables									
Iceberg Detected	0.192	0.192	0.191	0.174	0.170	0.167	0.174	0.175	0.174
C C	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)
Iceberg Not Detected	0.052	0.072		0.044	0.061		0.022	0.039	
0	(0.001)	(0.001)		(0.001)	(0.001)		(0.000)	(0.001)	
Visible Volume		-0.043	-0.042		-0.051	-0.050	()	-0.042	-0.042
		(0.001)	(0.001)		(0.001)	(0.001)		(0.001)	(0.001)
Executed Iceberg Volume		(0.00-)	0.028		(0.00-)	0.028		(0.00-)	0.028
			(0.003)			(0.003)			(0.003)
Predicted Hidden Volume			-0.004			-0.001			0.005
			(0.002)			(0.001)			(0.003)
Bid Side Variables			(0.002)			(0.002)			(0.000)
Iceberg Detected	-0 192	-0 193	-0 191	-0.168	-0 165	-0 164	-0 177	-0 179	-0 178
	(0.002)	(0.002)	(0.002)	(0.002)	(0.100)	(0.002)	(0.002)	(0.002)	(0.002)
Iceberg Not Detected	-0.052	(0.002)	(0.002)	-0.035	(0.002)	(0.002)	-0.030	(0.002)	(0.002)
Teberg Not Detected	(0.002)	(0.001)		(0,000)	(0.000)		(0,000)	(0.043)	
Visible Volume	(0.001)	(0.001)	0 030	(0.000)	0.054	0.054	(0.000)	0.045	0.045
visible volume		(0.041)	(0.009)		(0.004)	(0.004)		(0.040)	(0.043)
Everyted Leeberg Volume		(0.001)	(0.001)		(0.001)	(0.001)		(0.001)	(0.001)
Executed Iceberg Volume			-0.023			-0.030			-0.030
			(0.003)			(0.003)			(0.003)
Predicted Hidden Volume			0.004			-0.003			-0.002
			(0.002)			(0.003)			(0.003)

Table VII: Impact on the Market Order Flow: The Probability of a Buy Market Order

Table VII reports the average marginal effects for three logit-model specifications for the probability of a buy market order with average standard errors in parentheses. The explanatory variables are the iceberg detection indicators, indicators for undetected icebergs, the visible volume, the executed iceberg volume, and the predicted hidden volume at the ask and bid sides.

	La	rge	Me	dium	Sn	nall
	Pane	lA: Ex	Ante			
All Books	0.67	(0.02)	1.13	(0.04)	0.96	(0.07)
Books without Icebergs	0.78	(0.02)	1.31	(0.04)	1.20	(0.07)
Books with Icebergs	0.18	$(\bar{0}.\bar{0}4)^{-}$	0.64	(0.07)	-0.01	(0.13)
- not detected	0.80	(0.03)	1.74	(0.06)	1.28	(0.09)
- detected	-0.11	(0.05)	0.10	(0.09)	-0.64	(0.18)
	Pane	el B: Ex	Post			
All Books	0.59	(0.02)	0.95	(0.04)	0.79	(0.07)
Books without Icebergs	0.76	(0.02)	1.29	(0.04)	1.16	(0.07)
Books with Icebergs	-0.14	$(\bar{0}.\bar{0}\bar{4})$	0.05	(0.07)	-0.73	(0.13)
- not detected	-0.04	(0.03)	0.08	(0.07)	-0.60	(0.09)
- detected	-0.18	(0.05)	0.04	(0.09)	-0.80	(0.18)

Table VIII: Impact on Order Book Profits

Table VIII reports the average estimates for the expected order book profits with standard errors in parentheses. We compute the order book profits across all limit and iceberg orders by defining the profits per market order arrival as the product of the probability of execution and the signed difference between the order price and the expected mid-quote conditional on execution. The calculations use our estimates for the price impact of market orders, the market order size distribution, and the conditional probability of buy versus sell market orders. Panel A reports the Ex Ante and Panel B the Ex Post figures. The differences between Ex Ante and Ex Post order book profits are that we include the surprise hidden volume and replace the predicted with the actual hidden volume in the Ex Post profit calculations. The order book profits are measured in basis points per market order arrival. The standard errors take into account the estimation errors from the first stage parameter estimates.

		La	arge	Mee	dium	Sn	nall
				. .			
		Panel A: <u>I</u>	<u>Detected</u>	Icebergs			
Iceberg Order	ex ante	-0.10	(0.04)	-0.18	(0.06)	-0.37	(0.11)
	ex post	0.01	(0.04)	0.03	(0.06)	-0.12	(0.11)
Limit Orders	ex ante	-0.01	$\bar{(0.04)}$	$0.\bar{28}$	$\overline{(0.06)}$	-0.28	(0.12)
	ex post	-0.20	(0.04)	0.00	(0.06)	-0.68	(0.12)
- side of Iceberg	ex ante	0.09	(0.01)	0.11	(0.02)	0.05	(0.02)
	ex post	0.14	(0.01)	0.24	(0.02)	0.17	(0.03)
- opposite	ex ante	-0.10	(0.04)	0.17	(0.06)	-0.33	(0.11)
	ex post	-0.34	(0.04)	-0.24	(0.06)	-0.85	(0.12)
	Pa	anel B: <u>No</u>	t Detect	<u>ed</u> Icebergs	3		
Iceberg Order	ex ante	-0.13	(0.01)	-0.14	(0.01)	-0.29	(0.02)
	ex post	0.40	(0.02)	0.71	(0.03)	1.00	(0.05)
Limit Orders	ex ante		$\bar{(0.02)}$	1.84	$\overline{(0.05)}$	1.56	(0.07)
	ex post	-0.44	(0.04)	-0.63	(0.06)	-1.58	(0.09)
- side of iceberg	ex ante	0.35	(0.01)	0.75	(0.02)	0.65	(0.02)
	ex post	0.21	(0.01)	0.36	(0.01)	0.28	(0.01)
- opposite	ex ante	0.57	(0.02)	1.09	(0.04)	0.90	(0.05)
	ex post	-0.64	(0.04)	-0.99	(0.06)	-1.86	(0.10)

Table IX: Breakdown of Profits for Order Books with Iceberg Orders

Table IX reports the breakdown of the order book profits for order book with iceberg orders, at the best quote, into two categories: order books with detected iceberg orders in Panel A and order books with undetected icebergs in Panel B. Each panels reports the profits by order type, iceberg versus limit order, by side of the order book for limit orders, side of iceberg versus opposite side, and by conditioning information, ex ante versus ex post. We compute the order book profits across all limit and iceberg orders by defining the profits per market order arrival as the product of the probability of execution and the signed difference between the order price and the expected mid-quote conditional on execution. The calculations use our estimates for the price impact of market orders, the market order size distribution, and the conditional probability of buy versus sell market orders. The differences between ex ante and ex post order book profits are that we include the surprise hidden volume and replace the predicted with the actual hidden volume in the ex post profit calculations. The order book profits are measured in basis points per market order arrival. We report standard errors in parentheses. The standard errors take into account the estimation errors from the first stage parameter estimates.

	Depe	endent Va	riable: Ex	Post Or	der Book	Profit
	Ĺa	rge	Mee	dium	Sn	nall
	Panel A: <u>l</u>	Detected	Icebergs			
Iceberg Orders						
Intercept	0.01	(0.04)	0.03	(0.06)	-0.12	(0.11)
Executed Iceberg Volume	-0.44	(0.04)	-0.44	(0.05)	-0.99	(0.09)
Predicted Hidden Volume	0.34	(0.03)	0.27	(0.04)	0.86	(0.11)
Surprise Hidden Volume	0.86	(0.03)	1.14	(0.03)	1.78	(0.06)
Limit Orders						
Intercept	-0.20	(0.04)	0.00	(0.06)	-0.68	(0.12)
Executed Iceberg Volume	0.28	(0.03)	0.07	(0.04)	0.27	(0.09)
Predicted Hidden Volume	-0.64	(0.05)	-0.98	(0.06)	-2.12	(0.16)
Surprise Hidden Volume	-1.27	(0.04)	-1.35	(0.04)	-3.08	(0.10)
Market Orders						
Intercept	0.18	(0.05)	-0.04	(0.09)	0.80	(0.18)
Executed Iceberg Volume	0.16	(0.02)	0.38	(0.02)	0.75	(0.05)
Predicted Hidden Volume	0.30	(0.03)	0.74	(0.04)	1.29	(0.12)
Surprise Hidden Volume	0.41	(0.03)	0.23	(0.02)	1.36	(0.08)
		_				
Pa	nel B: <u>No</u>	t Detecte	<u>ed</u> Icebergs	5		
Iceberg Orders						
Intercept	0.40	(0.02)	0.71	(0.03)	1.00	(0.05)
Surprise Hidden Volume	0.66	(0.02)	0.95	(0.03)	1.39	(0.04)
Limit Orders						
Intercept	-0.44	(0.04)	-0.63	(0.06)	-1.58	(0.09)
Surprise Hidden Volume	-1.45	(0.05)	-3.10	(0.08)	-3.22	(0.09)
Market Orders		-		·		
Intercept	0.04	(0.03)	-0.08	(0.07)	0.60	(0.09)
Surprise Hidden Volume	0.79	(0.03)	2.20	(0.06)	1.87	(0.05)

Table X: Determinants of Profits for Order Books with Iceberg Orders

Table X reports parameter estimates for regressions of the ex post profits with the executed iceberg volume, the predicted hidden volume, and the surprise hidden volumes as independent variables. We estimate a separate regression for iceberg orders, limit orders, and market orders for each stock and report average parameter estimates with standard errors in parentheses. The profits for market orders are defined as minus the total order book profits. Panel A reports the results for detected iceberg orders and Panel B reports the results for not detected iceberg orders. The right hand side variables have been normalized to have a mean of zero and unit standard deviation so that the intercept captures the mean profit. The units are basis points per share and market order arrival.

Appendices

$\mathbf{A1}$	Descriptive	Statistics	for	Sample	Stocks
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		MCAP	Trad. Vol.	Mid-Quote	Trades	Trade Size	Bid-	Ask Spread
	Ticker	[€b]	[€b]	[€]	[1000]	[1000 shrs]	[b.p.]	[cents]
Large	ALV	33.8	18.6	99.5	289.1	0.6	4.6	4.5
	DBK	38.2	19.8	67.6	253.4	1.2	4.0	2.7
	DCX	30.3	12.0	36.3	211.6	1.6	5.2	1.9
	DTE	34.9	22.4	15.6	284.4	5.0	7.1	1.1
	EOA	33.8	10.3	52.5	183.7	1.1	4.5	2.4
	MUV2	16.4	13.3	93.6	218.9	0.6	4.6	4.3
	SAP	27.4	11.8	131.0	179.4	0.5	4.6	6.0
	SIE	52.9	20.6	63.7	282.5	1.1	3.9	2.5
	Mean	33.5	16.1	70.0	237.9	1.5	4.8	3.2
Medium	BAS	25.4	8.0	43.1	165.1	1.1	4.7	2.0
	BAY	15.9	5.7	22.8	153.5	1.6	7.1	1.6
	BMW	12.2	5.6	34.7	134.9	1.2	5.6	1.9
	HVM	6.6	6.3	18.5	123.7	2.8	9.2	1.7
	IFX	4.8	9.4	11.6	179.0	4.5	10.0	1.2
	RWE	12.7	6.3	33.9	148.0	1.2	5.9	2.0
	VOW	9.7	6.7	39.2	162.8	1.0	5.2	2.0
	Mean	12.5	6.8	29.1	152.4	1.9	6.8	1.8
Small	ADS	4.1	2.0	92.5	62.6	0.4	6.7	6.1
	ALT	3.3	2.0	48.8	69.9	0.6	7.4	3.6
	CBK	7.6	3.4	15.3	92.7	2.4	9.6	1.5
	CONT	4.1	1.6	31.5	64.0	0.8	8.8	2.8
	DB1	4.8	2.3	47.0	62.8	0.8	7.0	3.3
	DPW	6.8	2.8	18.2	84.1	1.8	9.3	1.7
	FME	1.9	0.8	53.8	39.7	0.4	9.4	5.0
	HEN3	3.7	1.2	65.8	44.9	0.4	7.3	4.8
	LHA	4.5	2.8	14.1	86.5	2.3	10.6	1.5
	LIN	3.4	1.4	43.6	57.3	0.6	7.5	3.3
	MAN	2.4	1.8	27.7	67.6	0.9	9.1	2.5
	MEO	5.0	2.5	34.8	79.0	0.9	8.4	2.9
	SCH	7.1	3.3	41.0	97.4	0.8	6.7	2.7
	TKA	6.4	2.4	15.8	80.7	1.9	10.7	1.7
	TUI	2.0	1.7	18.7	67.8	1.3	11.5	2.1
	Mean	4.5	2.1	37.9	70.5	1.1	8.7	3.0

Table A1 reports the market capitalization, the trading volume, the average mid-quote, the total number of trades, the average trade size (1000 shares), and the average relative (basis points) and absolute (euro cents) bid-ask spreads for the sample stocks. The market capitalization is calculated using a free-float methodology, in billions of euros as of December 2003. The sample period is January 2nd to March 31st, 2004.

A2 Order Book Profit Calculation

In this appendix we show how we compute the expected order book profits discussed in section 3.3. Our set-up is similar to the one used by Sandås (2001) and Frey and Grammig (2006) in their tests of implications of the Glosten (1994) model. The main innovations are that we explicitly take into account the hidden volume in the order book and its effect on price and order flow dynamics.

Our econometric approach combines the specifications for the price impact, the market order size and the probability of a buy market order in a combined method of moments estimation. The moment equations are the score functions of the linear regression models, respectively the logit model for the buy probability.

Denote the change of the mid-quote from t to $t + \tau$ as Δp , the (unsigned) market order size as M and the indicator for a buy market order as d^+ .

We apply this notation to the vectors of exogenous variables $X_{\Delta p}$, X_M and X_{d^+} and to the parameter vectors $\theta_{\Delta p}$, θ_M and θ_{d^+} . This yields the following set of moments:

$$E\begin{bmatrix} \left(\Delta p - \theta'_{\Delta p} X_{\Delta p}\right) & \otimes & X_{\Delta p} \\ \left(M - \theta'_M X_M\right) & \otimes & X_M \\ \left(d^+ - \frac{e^{\left(\theta'_{d^+} X_{d^+}\right)}}{1 + e^{\left(\theta'_{d^+} X_{d^+}\right)}}\right) & \otimes & X_{d^+} \end{bmatrix} = 0.$$
(A 1)

The specification for the price impact $X_{\Delta p}$ changes depending on whether we estimate the profit with public information available at the time of trade, ex ante specification B in Table V, or if we estimate it after adding the surprise volume, ex post specification C in Table V. The specifications of exogenous variables for market order size, X_M (specification C in Table VI), and buy probability, X_{d^+} (specification C in Table VII), are identical for the calculation of ex ante and ex post profit.

To derive the expected profit of the limit order book we calculate upper- and lower-tail expectations to determine the expected revision in the stock price conditional on execution as in Glosten (1994).

Briefly, limit orders are executed in a discriminatory fashion. A limit sell order that is executed if a buy market order of size M arrives is also executed by any larger buy market order. Thus we compare the potential revenue to the expected price change for the whole range of potential market orders which could execute the limit order.

Consider a single unit at the ask side of the order book at queue position q. Its spread defined as the distance between its limit price and the current mid-quote is denoted as s(q). The expected profit $\pi(q)$ for the qth unit is given as:

$$\pi(q) = Pr(d^+|X_{d^+};\theta_{d^+}) \int_q^\infty \left[s(q) - \Delta p(M|X_{\Delta p}^{\setminus M};\theta_{\Delta p}) \right] f(M|X_M;\theta_M) \, dM, \tag{A 2}$$

with $Pr(d^+|.)$ denoting the probability of a buy market order, $\delta p(M|.)$ the expected price change of the market order with size M and f(M|.) the probability density function of the market order size. $X_{\Delta p}^{\setminus M}$ is the set of exogenous variables used in the price impact specification excluding the market order size.

The specification above is valid for any distribution of the market order size but can be solved

in closed-form for the case of an exponential distribution. Here the profit of a single unit equals:

$$\pi(q) = \frac{e^{(\theta'_d + X_d +)}}{1 + e^{(\theta'_d + X_d +)}} \left[s(q) - X_{\Delta p}^{\setminus (M,I)} \theta_{\Delta p}^{\setminus (M,I)} - (\theta_{\Delta p}^M + \theta_{\Delta p}^{I \times M} I)(\theta'_M X_M + q) \right] \left[1 - e^{-\left(\frac{q}{\theta'_M X_M}\right)} \right],$$
(A 3)

with *I* denoting the (unsigned) iceberg indicator, which interacts with the market order size in the specification of the expected price change. As above, $X_{\Delta p}^{\setminus (M,I)}$ and $\theta_{\Delta p}^{\setminus (M,I)}$ include the exogenous variables and parameters except the market order size and the iceberg indicator. The parameters $\theta_{\Delta p}^{M}$ and $\theta_{\Delta p}^{I \times M}$ refer to the market order size and the interaction between market order size and iceberg indicator.

For an aggregated block, for example, one order or all orders at a given price, with price distance s, which starts at queue position Q_s and ends at position Q_e the expected profit is denoted $\Pi(Q_e; Q_s) = \int_{Q_s}^{Q_e} \pi(q) dq$. Again, with exponentially distributed market orders the expected profits are determined as:

$$\Pi(Q_e;Q_s) = \frac{e^{(\theta'_{d+}X_{d+})}}{1+e^{(\theta'_{d+}X_{d+})}} \left\{ \left[s - X^{\setminus (M,I)}_{\Delta p} \theta^{\setminus (M,I)}_{\Delta p} - (\theta^M_{\Delta p} + \theta^{I\times M}_{\Delta p}I)\theta'_M X_M \right] \left[\phi(Q_s) - \phi(Q_e) \right] + (\theta^M_{\Delta p} + \theta^{I\times M}_{\Delta p}I) \left[\phi(Q_s)Q_s - \phi(Q_e)Q_e \right] \right\}$$
(A 4)

with $\phi(x) = e^{-\left(\frac{x}{\theta'_M X_M}\right)}$ denoting the complementary cdf of the exponential distribution.

For the standard errors of the expected profits we consider both the errors from the GMM estimation and the sampling error for the calculations from the order books in the sample. The uncertainty of the estimated parameters of the GMM model is considered via the delta method. We combine the two errors by assuming independence. Denote P as one of the terms in Tables VIII to X, then an estimator of the variance of P, σ_P^2 , is derived by the following expression:

$$\sigma_P^2 = \frac{\partial P}{\partial \theta'} V(\theta) \frac{\partial P}{\partial \theta} + s_P^2 \tag{A 5}$$

in which $V(\theta)$ denotes the estimated variance matrix of the model parameters and s_P^2 is the sampling variance of the profit term for Tables VIII and IX or the estimated variance for the regression parameters in Table X. The gradient vector of the profit term to the parameters $\frac{\partial P}{\partial \theta}$ is calculated numerically.

A3 Detection Algorithm: An Example

This appendix provides more details about algorithm that tries to replicate the modus operandi which allows professional traders to detect iceberg orders in the order book. The algorithm assumes an iceberg to be detected after the first replenishment. After the detection the algorithm keeps the detection state until all visible volume of the quote is cancelled or an expected replenishment has not occurred. It tracks the following properties: Iceberg detection state, peak volume of the detected iceberg, executed volume from the detected iceberg and the true hidden volume. Executed volume and peak volume are used to predict the hidden order volume of a detected iceberg. The algorithm assumes that market participant to compare the execution records with the observed order book before each trade and then keep track of updates of the order book thereafter. In case of a fast market with many orders clustering it may overstate the market participants' knowledge. On the other hand, there are several possible extensions to enhance the algorithm. Overall we consider the algorithm a good proxy for the information set of sophisticated traders.

The example below illustrates the detection algorithm.



The figure above depicts a simple order book configuration. The best bid and ask are both defined by one limit order, the visible volume variable \mathcal{V} equals the size of the limit orders and the iceberg indicator for the best quotes \mathcal{I} are zero.



A buy iceberg order with peak volume of 1000 and a total volume of 4000 is submitted at the best bid price level. The peak volume increases the visible volume, but the iceberg iceberg indicator at the best quote remains unchanged, as the iceberg is not detected. The hidden volume ($\mathcal{H} = 3000$) is only used for ex post calculations.



A sell market order for 2500 shares arrives. It executes first against the limit order and the peak volume of the iceberg order. Then shares from the hidden part of the order book enter the visible book and the remaining 500 shares are executed against the new peak. Due to this first replenishment the algorithm considers the iceberg to be detected and stores peak size \mathcal{P} and executed volume \mathcal{E} . Those are used to predict the hidden volume $\hat{\mathcal{H}}$ as specified in table IV.



A buy limit order with 1500 shares is submitted inside the spread. The new quote replaces the one with the iceberg order as the best bid. Accordingly both the visible volume and the iceberg indicator are adjusted. The algorithm still tracks the properties of the iceberg order deeper in the book.



A market order to sell 3000 shares is submitted. It executes first against the limit order at the best bid, another 500 shares execute against the remaining peak volume. It triggers another replenishment. As the iceberg was detected previously the iceberg indicator for the best bid is set again. The detection algorithm updates hidden and executed volumes and accordingly a new predicted hidden volume is applied.



Two events occurred in the meantime: First two additional buy limit orders with 1000 shares and 1500 shares were submitted at the best quote and then the iceberg order was cancelled. The iceberg indicator at the best quote is still equal to one, as the algorithm has not yet detected the cancellation.² Only the true hidden volume is updated.

Limit Order B	ook at t $=$	7:
Best Ask		
V=2000	$\mathcal{I}=0$	Sell
	-	
		8
Rest Rid		
Dest Dia	_	
$\mathcal{V}{=}1000$	$\mathcal{I}=0$	

Another sell market order with 1500 shares executes the first limit order and 500 shares of the second. As a replenishment was expected after 1000 shares executed from this quote the algorithm removes the iceberg state from this price level.

 $^{^{2}}$ An enhanced algorithm could take into account that the cancellation of 1000 shares potentially indicates a cancellation of the iceberg order.

A4 Estimation Details

This appendix reports further details on the empirical procedure used throughout the paper. It first covers the reconstruction of the limit order book and order histories from the XETRA log files. A discussion of the methods and adjustments in the estimation tables follows.

XETRA sample

- 1. Only observations from the continuous trading are used. All auctions (including volatility interruptions) are removed. For the reconstruction we take into account the effects that any order submissions, transactions, or cancellations in the auctions have on the state of the order book dring continuous trading.
- 2. On the 6th of February 2004 all XETRA trading was interrupted during the continuous trading. All observations of this day are excluded.³
- 3. From the order histories we reconstruct snapshots of the displayed and hidden order books 1/100th of a second before each transaction.
- 4. At the start of the day, after the midday auction and volatility interruptions the first ten transactions are removed (exceptions are the calculations for Tables I, II, and A1).

Table I

- 1. All included orders are exclusively from the continuous trading regime; these orders never contributed to the order book during an auction.
- 2. In Panel A partially marketable limit and iceberg orders only contribute with their non-marketable volumes.

Table II

- 1. Both in Panels B and C the marginal effects reported are the mean of the marginal effects evaluated at each observation (average marginal effects). The standard errors are derived from the standard errors of the logit parameters via the delta method.
- 2. In Panel C the execution percentage is modelled by an ordered logit with five classes (0-20%, 20-40%, 40-60%, 60-80%, 80-100%). The (combined) marginal effect is the sum of marginal effects of each class multiplied with the respective class mean.
- 3. Exogenous variables in all panels are normalized to zero mean and unit standard deviation.

Table III

The detection algorithm (see Appendix A3) tracks each price level separately. The table reports the percentages for the observations at each transaction. If there are several icebergs at each side, the volume variables (hidden and executed volumes) are combined. The peak volume, however, is always updated to the one with the latest replenishment of the peak.

Table IV and Figure 2

- 1. The specification ignores that the range for hidden volume is truncated at zero. The average percentage of negative predictions is very small (0.016% for large, 0.002% for medium, and 0.014\$ for small stocks).
- 2. Number of peaks executed is the ratio of executed volume from iceberg to peak size stored by the detection algorithm (see Appendix A3).

 $^{^{3}}$ Refer to XETRA Newsboard message 2004/02/06 11:03:35

http://deutsche-boerse.com/dbag/dispatch/de/xetraNewsboard/gdb_navigation/trading/10_trading_platforms/200_ xetra/100_xetra_newsboard?news=31872&venue=1

Tables V to VII

- 1. All specifications are estimated separately on an identical dataset for stock group. The score functions for Tables V, VI, and VII are given by the first, second, and third row of matrix A 1 in Appendix A2. Parameters are estimated by the method of moments (this equals the maximum likelihood estimation). Standard errors are derived by a heteroscedasticity autocorrelation covariance (HAC) estimator with a ten lags Bartlett kernel.
- 2. All observations are pooled by stock groups (as shown in Table A1). For the calculation of autocovariances only pairs of observation are used which belong to an uninterrupted period of continuous trading in the same stock. We verify the robustness of our findings by estimating all models separately by stock.
- 3. The variables labeled 'predicted hidden volume' and 'executed iceberg volume' are normalized differently in Table V compared to the others. To be comparable to the parameter of the trade size they are normalized as multiples of the average market order volume of the individual stock. In Tables VI and VII they are standardized (zero mean, unit standard deviation) on the sub-sample of detected iceberg observations of the individual stock. Another difference is that in Table V the variables are signed by side (bid volume positive, ask volume negative), whereas in the other tables there are individual estimators for each side.
- 4. Due to some extreme outliers for the visible quote volume in the sample we restrict the maximum visible volume to 25 times the average market order size (0.38% for large, 0.21% for medium, and 0.08% for small stocks). We replace (winsorize) the visible volume for those observations with the defined maximum.
- 5. Negative predicted hidden volume (see above) is replaced by a zero prediction.
- 6. The specification ignores that the market order size is truncated at zero. For the set of estimated parameters no observation with predicted negative market order size is observed.
- 7. Table V only: For the last 30 transactions of the trading day the closing price replaces the future mid-quote.
- 8. Table VII only: For the logit average marginal effects are reported. For the iceberg indicators the marginal effect is reported for a change from zero to one.

Tables VIII to X

- 1. All remarks for Tables V to VII are still valid here.
- 2. Specification of the estimated moments and the derivation of the expected profit is outlined in Appendix A2.
- 3. Profits are calculated for units up to the 4th best quote level. The addition of the 4th level itself contributed to the results only marginally.
- 4. For the calculation of ex-ante profits the predicted hidden volumes are considered, ex-post the true hidden volumes.
- 5. Table VIII only: Books without Icebergs include false detections of the iceberg detection algorithm.
- 6. Table IX only: The row "Iceberg Order" only includes the iceberg orders of the best quote (usually only one). For the calculation we track the ordering in the queue by maintaining a separate priority list of all orders at the best quote. The visible volume of iceberg orders at other quotes are subsumed under "Limit Orders".

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