Atal, Vidya; Basu, Kaushik; Gray, John; Lee, Travis

Working Paper

Literacy traps: Society-wide education and individual skill premia

IZA discussion papers, No. 4047

Provided in Cooperation with:
Institute of Labor Economics (IZA)

Suggested Citation: Atal, Vidya; Basu, Kaushik; Gray, John; Lee, Travis (2009) : Literacy traps: Society-wide education and individual skill premia, IZA discussion papers, No. 4047, http://nbn-resolving.de/urn:nbn:de:101:1-20090323165

This Version is available at:
http://hdl.handle.net/10419/35454

Terms of use:
Documents in EconStor may be saved and copied for your personal and scholarly purposes.
You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.
If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.
Literacy Traps: Society-wide Education and Individual Skill Premia

Vidya Atal
Kaushik Basu
John Gray
Travis Lee

February 2009
Literacy Traps: Society-wide Education and Individual Skill Premia

Vidya Atal
Cornell University

Kaushik Basu
Cornell University and IZA

John Gray
Cornell University

Travis Lee
Cornell University

Discussion Paper No. 4047
February 2009

IZA
P.O. Box 7240
53072 Bonn
Germany

Phone: +49-228-3894-0
Fax: +49-228-3894-180
E-mail: iza@iza.org

Any opinions expressed here are those of the author(s) and not those of IZA. Research published in this series may include views on policy, but the institute itself takes no institutional policy positions.

The Institute for the Study of Labor (IZA) in Bonn is a local and virtual international research center and a place of communication between science, politics and business. IZA is an independent nonprofit organization supported by Deutsche Post Foundation. The center is associated with the University of Bonn and offers a stimulating research environment through its international network, workshops and conferences, data service, project support, research visits and doctoral program. IZA engages in (i) original and internationally competitive research in all fields of labor economics, (ii) development of policy concepts, and (iii) dissemination of research results and concepts to the interested public.

IZA Discussion Papers often represent preliminary work and are circulated to encourage discussion. Citation of such a paper should account for its provisional character. A revised version may be available directly from the author.
ABSTRACT

Literacy Traps: Society-wide Education and Individual Skill Premia

Using a model of O-ring production function, the paper demonstrates how certain communities can get caught in a low-literacy trap in which each individual finds it not worthwhile investing in higher skills because others are not high-skilled. The model sheds light on educational policy. It is shown that policy for promoting human capital has to take the form of a mechanism for solving the coordination failure in people’s choice of educational strategy.

JEL Classification: D20, I28, J31

Keywords: education, literacy, O-ring, skill formation, traps

Corresponding author:

Kaushik Basu
Department of Economics
Cornell University
Ithaca, New York 14853
USA
E-mail: kb40@cornell.edu
1 Introduction

The idea that an economy or a group of people can get caught in a low-level trap from which it is, in principle, possible to escape but no individual has it within his or her power to break out of it is an old one in economics, but its importance has remained undiminished. Among Tapan Mitra’s many fields of enquiry in economic theory, poverty traps has been a significant one. In 1995, in a joint paper with Mukul Majumdar, for instance, he explores the relation between increasing returns and poverty traps and how an economy can be caught in poverty, though once it is wrenched out of the trap it can grow unassisted (Majumdar and Mitra, 1995; see also Majumdar and Mitra, 1982; Dechert and Nishimura, 1983). This work is a natural extension of the idea of vicious circle of poverty to be found in Nurkse (1953) and Rosenstein-Rodan (1943) and also the idea that there is a close connection between underdevelopment and multiple equilibria (Basu, 1997).

While the dominant discussion of low-level traps has occurred in the context of a nation’s or a collectivity’s income, it is possible to carry the broad idea over to other indicators of a nation’s well-being (see Hoff and Stiglitz, 2001). In the present paper, we try to show that something similar may happen regarding literacy. A nation can get caught in a low-literacy or low-education trap. Once caught in this situation, it is not in the interest of any individual to incur cost and acquire a lot of skills. It is the skill-lessness of others that makes it not worthwhile for each individual to acquire much skills, and thus they are all trapped in a vicious circle.

Our analysis has important policy implications. A nation caught in a low-literacy trap cannot break out of it just by providing schools for it is not the supply of schools that is a bottleneck but the demand for higher education. Hence, the rather abstract model that we are about to construct can shed light on significant policy questions such as when do we need to make education compulsory and when will the simple act of making schools available take care of the problem of under-investment in human capital. The model sheds interesting light on how, in
a certain class of equilibria, giving a subsidy to education may have no effect on promoting education. In the process we get some insights into the design of policy that will be effective.

The core of our model is based on the idea of an O-ring production function, introduced in the literature by Kremer (1993) – see also Kremer and Maskin (1996). The idea is this. Since so much of today’s work takes the form of the assembly line, either literally, as in the manufacture of cars, or, in effect, as in software services, where small groups are engaged in doing different parts of a large job, that a malfunction in one part can undo the benefits of the other tasks that are done well. The metaphor is that of the space shuttle Challenger disaster in 1986, which was caused by the malfunctioning of a tiny component of the space-ship, the O-ring. The idea that there will be this kind of spillover effects of education among workers seems natural enough and there has been a lot of empirical and theoretical work on this (Rauch, 1993; Benabou, 1993; Redding, 1996; Acemoglu and Angrist, 2000; Kremer, Miguel and Thornton, 2004; Moretti, 2004).

In Kremer’s O-ring model, the skill that workers bring to their task is innate to the worker. If, however, we introduce education in the model, whereby each worker has the choice of incurring some cost (in terms of both time and money) and improving their skills and ability to do their jobs better, then interesting equilibria arise, including the possibility that workers will get caught in a low-education trap. This is the central idea that is pursued in this paper and while poverty traps are a pervasive topic in economics, low-literacy traps seem to have received much less attention. The work most related to our paper is that by Jones (2008). He constructs a random matching model in which there is endogenous human capital accumulation. Each individual faces the choice to be trained as a generalist or a specialist, with the value of being a specialist increasing as the density of specialists in the population rise. In Jones’ model, for certain parameter values, there is the possibility of multiple equilibria since the economy could be one of specialists or generalists. Another related exercise (Basu and Weibull,
2003; Horowitz, 2008) studies the punctuality traits of a collectivity, where each person benefits from other people’s punctuality and also the marginal return to increased individual punctuality rises with the level of other people’s punctuality. This strategic complementarity easily leads to multiple equilibria, whereby two societies of *a priori* identical individuals can get caught in, respectively, a tardy and a punctual equilibrium.

2 Model

2.1 A Primer on O-Rings

It is useful to begin by briefly summarizing the O-ring model, while at the same time adapting it a little to our present need. There is one consumer good in the economy. Its production takes place in factory units or, simply, factories. Each firm can own one or more factories. In each factory $n$ tasks ($n \geq 2$) are done, each task being done by one worker. Denote a worker’s skill by $q$ where $0 \leq q \leq 1$. We can interpret $q$ as the probability that the worker finishes his or her task successfully. Let $q_i$ be the skill-level that goes into task $i$, that is, the worker employed on task $i$ has a skill level $q_i$ and let $B$ be the output produced *per worker* in a factory when all tasks are performed successfully. The ‘production function’ in which $x$ denotes the expected output is as follows:

$$x = q_1 \cdot q_n nB \equiv \prod_{i=1}^{n} q_i nB. \quad (1)$$

It is easy to see that if all tasks are performed at skill level 1, then total output from the factory will be $nB$ and so the per worker output is $B$.

To start with, let us take the skill levels of workers to be exogenously given. The decision-making by the firms can be modeled in two different ways. The traditional route is to assume that there are many price-taking firms and free entry. Since there is a continuum of worker types, there is a continuum of wages, one for each type of worker. Let $w(q)$ be the market wage schedule exogenously given to the firms. We will throughout take the price of the product to be one.
In this case the firm’s problem is to choose \( n \) workers for operating a factory so as to maximize its profit. Hence, the firm’s problem is the following:

\[
\max_{\{q_i\}} \left[ \prod_{i=1}^{n} q_i nB - \sum_{i=1}^{n} w(q_i) \right].
\]

This gives us the following first-order condition for each task \( i \):

\[
w'(q_i^*) = \prod_{j \neq i} q_j^* nB. \tag{2}
\]

In addition, Kremer (1993) proved that it is always in the firm’s interest to have all its tasks done by workers of the same skill level. This is called the "skill-clustering theorem" in Basu (1997), where a short proof is available.

**Theorem 1 (Skill-Clustering)** If \((q_1^*, \ldots, q_n^*)\) maximize a firm’s profit, then (in addition to equation (2)) \(q_1^* = \ldots = q_n^*\).

In light of the skill-clustering theorem, equation (2) can be written as

\[
w'(q) = q^{n-1} nB,
\]

where \( q \) is the skill of labor chosen for each task by a firm.

Since, in equilibrium, each firm earns zero profit, a firm employing workers of skill \( q \) must satisfy

\[
q^n nB - nw(q) = 0
\]

or,

\[
w(q) = q^n B. \tag{3}
\]

Hence, we know that in equilibrium the wage schedule for different worker qualities will be given by this equation.

An alternative approach, which however will not be pursued here, is to assume that there are two or more firms and these are Bertrand oligopsonists. Each firm announces the wage it is willing to pay for each type of worker, and workers go to the firm offering the highest wage, ties being broken arbitrarily. The ‘equilibrium’ of this oligopsony is simply the Nash equilibrium of the normal-form game among
the firms. As we know from standard oligopsony, in equilibrium each firm will earn zero profit. The logic of this is obvious. If there is a firm that earns positive profit, then another firm could offer its workers a slightly higher wage and woo them away. So the initial outcome would not have been a Nash equilibrium. If, in addition, we assume away the integer problem, that is, assume that, for each wage announced by the firm, either no worker will agree to work or any number of workers will, then the wage schedule in equilibrium will be exactly as shown by the above equation (3).

We shall however go with the traditional approach of taking this to be a model of perfectly competitive firms with free entry.

2.2 Endogenizing Level of Education

Let us now allow for the possibility that individuals do not come with an immutable skill level but can acquire skill through education. To make it possible to conduct a formal analysis, we have to take a slightly novel route in developing the idea of an equilibrium. We shall assume that there are two-periods. In the first, workers choose their level of education and in the second period, with education as given, firms make their decisions as in a standard competitive model with free entry, in other words, exactly as described in the above section. In the first period, the workers essentially do a Nash-type calculation. That is, each worker calculates what would happen if he or she deviated and chose some other level of education. If she could not do better by any such deviation, then the existing choice of education for all workers is an ‘equilibrium’.

Formally, in the first period, each worker chooses to obtain a certain level of skill $q$ through education. We will assume that the cost of education that provides the level of skill $q$ is given by $c(q)$ with $c'(q) \geq 0$. In the second period, the firms take their decisions about what kinds of workers to hire for the different tasks, with wages being treated as exogenous by each firm. The second period equilibrium is reached when we find a wage schedule (that is, a wage of each level of skill) such that each firm maximizes profits and earns zero. In other words, the second
period works as described in the previous section (2.1). After the second period, firms earn their payoffs (we already know this will be zero in equilibrium) and each worker receives his or her payoff, which is equal to the wage earned by the worker minus the cost of education.

In defining the equilibrium formally in this two-period model, let us focus on a refinement of what was described informally above. The refinement is an outcome in which all workers voluntarily choose the same level of skill. We shall call this the ‘symmetric equilibrium’, with the frequent indulgence of dropping the epithet ‘symmetric’, since we are not going to talk about a non-symmetric equilibrium in this paper.

A skill level $q$ and a wage equal to $q^n B$ for each of these workers is a \textit{(symmetric) equilibrium} if and only if

1. $q^n B \geq c(q)$ and

2. for all $\hat{q}$, the wage that a worker who individually deviates to $\hat{q}$ earns is such that wage minus the cost of that education, namely, $c(\hat{q})$, is less than or equal to $q^n B - c(q)$.

In other words, all workers earn enough to cover their education cost and no worker by unilaterally deviating to some other level of education can do better.

To formalize condition (2), we need to describe what the wage a worker who unilaterally deviates to $\hat{q}$ when everybody else has chosen $q$, will earn. With a slight abuse of notation, denote this wage by $w(\hat{q}; q)$ and denote the profit of the firm hiring this person by $\pi(\hat{q}; q)$. Clearly,

$$\pi(\hat{q}; q) = \hat{q}q^{n-1} nB - (n - 1) w(q) - w(\hat{q}; q) = \hat{q}q^{n-1} nB - (n - 1) q^n B - w(\hat{q}; q).$$

The firm will hire this worker if and only if

$$\pi(\hat{q}; q) \geq \pi(q) = 0.$$
Therefore, \( w(\hat{q}; q) \) is the maximum possible wage the worker can get while ensuring that the above inequality is satisfied. Otherwise the firm will refuse to employ this worker. It is now easy to derive that when all other workers have skill \( q \), the wage of a worker with skill \( \hat{q} \) will be given by:

\[
w(\hat{q}; q) = \hat{q}q^{n-1}nB - (n - 1)q^nB.
\] (4)

What is interesting and makes our analysis easy to conduct is a property of \( w(\hat{q}; q) \). The property is the following. The graph of \( w(\hat{q}; q) \) as \( \hat{q} \) changes is always given by the straight line that is tangent to \( w(q) = q^nB \) at \( q \).

What we are now ready to demonstrate is that this model can have multiple symmetric equilibria. In other words, it is possible to have a very low level of education which is an equilibrium in the sense that if everybody chooses it, nobody can do better by deviating, and there is also a possibility of a very high level of education in equilibrium. A society can simply get caught in a low literacy trap. Between two societies, one highly skilled and another with rudimentary skills there may be no fundamental difference. They can be mere victims of their history. Using the property of \( w(\hat{q}; q) \) mentioned above, these results are easy to prove. This can be done with a few simple examples; and that is what we do presently. The last section of the paper goes into the large policy implications for what the government could do to promote education and the acquisition of human capital and skills.

3 Linear Cost Function and Literacy Trap

Consider a linear cost function for education as follows. Individuals are born with some level of skill, say \( z \). Alternatively, this is a level of skill that comes to us costlessly. Most human beings can perform basic tasks without having to undergo any formal training. To acquire skill beyond \( z \), a worker has to incur a cost, which increases linearly with the level of skill. To sum up, the cost of education for
attaining skill \(q\) is given by:

\[
c(q) = \begin{cases} 
0, & \text{for } 0 \leq q \leq z \\
a(q - z), & \text{for } z < q \leq 1
\end{cases}
\]  

(5)

where \(a\) is such that

\[
z^{n-1} < \frac{a}{nB} < 1 \quad \text{and} \quad \left(\frac{nz}{n-1}\right)^{n-1} \geq \frac{a}{nB}.
\]  

(6)

The first assumption guarantees that the cost of education is neither very high so that no one chooses to get more skill than \(z\), nor very low so that everyone chooses to become an expert. The second assumption guarantees that \(c(q) \leq w(q)\) for all \(q \in [0, 1]\).

Define \(\overline{q}\) such that

\[w'(\overline{q}) = a\]

or,

\[\overline{q} = \left(\frac{a}{nB}\right)^{\frac{1}{n-1}}.\]

\(\overline{q}\) is illustrated in Figure (1).

**Claim 1** Every worker acquiring skill \(\overline{q}\) and earning a wage of \(\overline{q}B\) is an equilibrium.

**Proof.** Suppose all workers have chosen \(\overline{q}\). We know that perfect competition among firms with free entry will drive wages to \(\overline{q}B\). It has already been seen earlier that firms offer the wage structure \(w(\cdot;\cdot)\) given by (4) optimally and none of the firms deviate from offering this.

Let us now check how a worker, who unilaterally deviates from \(\overline{q}\) will do. Note that by assumption (6), \(w(\overline{q}) \geq c(\overline{q})\) and \(z < \overline{q} < 1\). Now, from (4), we have

\[
\frac{\partial w(q;\overline{q})}{\partial q} = \overline{q}^{n-1}nB = w'(\overline{q}) = a.
\]

This implies that \(w(q;\overline{q})\) is parallel to \(c(q)\) for all \(q \in [z, 1]\). This in turn means that

\[w(q;\overline{q}) - c(q) = w(q;\overline{q}) - c(q)\]

for all \(q \in [z, 1]\).
But, \( w(q; \bar{q}) = w(\bar{q}) \). Therefore,

\[
w(q; \bar{q}) - c(q) \geq w(q; \bar{q}) - c(q) \quad \text{for all } q \in [0, 1].
\]

Hence, \( q \) is an equilibrium. It is interesting to note that deviations to the interval \([z, 1]\) leave the deviating worker exactly as well off as before, and all other deviations make the worker worse off. ■

![Figure 1: Linear cost function](image)

**Claim 2** In this example, with linear cost function given by (5), there are two other equilibria, one in which all workers choose \( q^* = z \) and another in which all workers choose \( q^* = 1 \).

**Proof.** First, suppose all workers choose \( q^* = 1 \) and one of them contemplates deviating from this common choice to a lower level of quality \( \tilde{q} < 1 \). Again the
tangent line to the graph of \( w(q) \) at \( q^* = 1 \) gives the wage for obtaining quality \( \hat{q} \). Now, for all \( \hat{q} < q^* \), the following is true:

\[
\frac{\partial w(\hat{q}; q^*)}{\partial \hat{q}} = w'(q^*) > w'(\hat{q}) = a.
\]

The inequality holds because \( w(q) \) is a convex function and \( q^* = 1 > \hat{q} \). Therefore, the loss in wages due to deviation to \( \hat{q} \) from \( q^* \) more than offsets the cost savings since \( w(\hat{q}; q^*) \) is more steeply sloped than the cost function. Thus deviation would lead to a lower payoff.

Similarly, if all workers choose \( q_* = z \), then deviation to \( \hat{q} > z \) is not advantageous since \( q_* = z < \hat{q} \) implies that

\[
\frac{\partial w(\hat{q}; q_*)}{\partial \hat{q}} = w'(q_*) < w'(\hat{q}) = a.
\]

Finally, deviation to \( \hat{q} < z \) lowers wages without reducing costs, so workers won’t do that.

It is easy to see that there does not exist any other equilibrium apart from the three described above in this model with the linear cost function given by (5).

### 3.1 Literacy Trap and Big Push

Note that, while \( \bar{q} \) is an equilibrium, it is not ‘stable’ in the following sense. In a society where all the workers are skilled upto level \( \bar{q} \), if it is possible to increase everyone’s skill a little bit, then each of the workers will deviate further away from \( \bar{q} \). That is, they will increase their skill; and note that this dynamic will continue till the equilibrium \( q^* \) is reached or gradually approached. On the other hand, if everybody’s skill was lowered a little, then a downward dynamic would start up and society could go all the way to the equilibrium \( q_* \).

Finally, we have a big ‘literacy trap’ at the education-level which provides skill \( q_* = z \). A ‘big push’ that drives the entire economy beyond the skill-level \( \bar{q} \) can start up innate forces that will then take the economy all the way to the good equilibrium. All smaller efforts will keep pulling workers back to \( q_* = z \). This has one heartening implication. In an economy with widespread illiteracy, the cost
of raising human capital may not be as much as appears at first sight. This is because the funding needed to promote education will not have to be sustained endlessly through time. As soon as a threshold is crossed, the accumulation of human capital and skills can be left to natural forces and will continue unabated.

4 More General Cost Function and Literacy Trap

Figure 2: Non-linear cost function with multiple equilibria

Though we illustrated our main results with the linear case, there is no need to confine the analysis to such cases. Virtually all results carry over to the more general, nonlinear cases. Consider the non-linear cost function as shown in Figure (2). As in case of linear cost function, suppose primary education that provides skill $z$ is free. Then the cost of education increases at an increasing rate. After some point, the behavior of the cost function changes and as someone gets more
educated, the less is his marginal cost of education. After a very high level of education, the marginal cost starts increasing again.

It is clear from the largely self-explanatory figure above that even with non-linear cost of education we may have multiple equilibria. In this particular example, we have two symmetric and strict Nash equilibria. As shown in Figure (2), $q_*$ and $q^*$ with firms offering wages $w(.)$ given by (3) are the two Nash equilibria and both are stable. Thus a literacy trap may occur in a society where all the workers optimally choose to attain the skill $q_*$.

5 Policy Interventions

Increasing literacy and the advancement of human capital has been a major focus of policy-making certainly in developing countries but also in developed nations. Evidently, there are two sides to this policy. There has to be a demand for education on the part of parents taking decisions for their children and young adults taking decisions for their own education. Secondly, there has to be a supply of schools so that parents who wish to educate their children can do so. In popular discourse, it is often said that poor parents do not want to educate their children. This has met, rightly, with strong criticism (see PROBE Team, 1999). However, this must not blind us to the fact that the intensity of demand for education can vary and this can make a difference to the literacy outcome of a nation (see PROBE Team, 1999; Drèze and Kingdon, 2001). It is believed that the rewards from education – the so-called ‘skill premium’ – have been rising in the developing world; and there is now some hard evidence on this (see Arbache, Dickerson and Green, 2004; Azam, 2009). When this happens, it is not surprising to find that the demand for getting education will also become stronger. It is now said in India, given that missionary schools had historically played a major role in the country, that all you have to do is to think of a good English name, like John or Thomas or Mary and add the prefix "Saint" and suffix "School" to it; and you will be in the education business with students flocking to you.
In our model, it is easy to see that the same country where the demand for education is low because the skill premium is low can change to an equilibrium with high premium and high demand for education. In Figure (1), if we start from a case where the country is caught at a low literacy trap at \( z \), it is not worthwhile for any individual to seek more education. The skill premium is just not high enough to make this worthwhile. If, on the other hand, education rises and goes past \( \bar{q} \) for everybody, then people will invest even more in education and the nation will come to rest at a very high level of education for all.

Our model allows us to separate out the demand and supply aspects quite neatly and so enables us to take a more sophisticated view on policy. We can think of government-subsidized education as an intervention which lowers the cost of education. This can have interesting effects depending on how it is done. Suppose government gives a small flat subsidy \( s \) for all levels of education. Contrary to what is presumed, this may have no effect on education. This will be true for all the equilibria depicted in Figures (1) and (2), excepting at \( z \) in Figure (1). To boost education, government has to vary the subsidy with respect to the level of education. In other words, the government needs to have a non-constant function \( s(q) \). The total cost of education is then given by \([c(q) - s(q)]\). By suitably altering the slope of \( s(q) \), the state can boost education. Indeed the net expenditure on education could be very small if the subsidy function is chosen artfully. If the economy is caught at equilibrium \( z \) in Figure (1), then a constant small subsidy will have a small positive effect on education. Beyond a critical point, it will have a huge effect, pushing skill acquisition all the way to the maximum value 1, with no need for any subsidy in the new equilibrium.

The model suggests that the fiscal burden of boosting education may not be too high, because all we need is a short period boost, after which the natural incentives in the system kick in and little further outside intervention is needed. For this same reason, it may be worthwhile for a country caught in a low-literacy equilibrium to have a policy of compulsory education, which forces parents to educate their children. If this can be sustained for a while, the need for force
will vanish since the high education of the rest of the population will raise the education premium for each individual.

References


