Bandyopadhyay, Subhayu; Wall, Howard J.

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Subhayu Bandyopadhyay
Howard J. Wall

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Subhayu Bandyopadhyay
*Federal Reserve Bank of St. Louis*
and IZA

Howard J. Wall
*Federal Reserve Bank of St. Louis*

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IZA
P.O. Box 7240
53072 Bonn
Germany

Phone: +49-228-3894-0
Fax: +49-228-3894-180
E-mail: iza@iza.org

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ABSTRACT

Is There Too Little Immigration?*

This paper presents a model of legal migration from one source country to two host countries, both of which can control their levels of immigration. Because of complementarities between capital and labor, the return on capital is positively related to the level of immigration. Consequently, when capital is immobile, host nations’ optimal levels of immigration are positively related to their capital endowments. Further, when capital is mobile between the two host nations, the common return on capital is a function of the levels of immigration in both countries, meaning that immigration is a public good. As a result, when immigration imposes costs on host countries, the Nash equilibrium results in free riding and less immigration than would occur in the cooperative equilibrium. These results are qualitatively unaltered when capital mobility extends to the source nation.

JEL Classification: F22, J61

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Corresponding author:

Subhayu Bandyopadhyay
Research Division
Federal Reserve Bank of St. Louis
PO Box 442
St. Louis, MO 63166-0442
USA
E-mail: bandysub@gmail.com

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1. Introduction

Immigration policy occupies a central place in policy discussions for most developed nations. Increasing globalization has also meant increased movement of skilled labor from developing to developed nations. For example, nations like China and India have abundant skilled labor, but lack infrastructure and complementary inputs. This has kept wages much lower than in developed nations and has led to employers in labor-scarce nations to pressure for the relaxation of immigration restrictions. It is well known, for example, that major U.S. firms like Microsoft lobby the government to relax the quota imposed by H1 type visas for temporary workers. A quote from Bhagwati (2003) summarizes the situation aptly:

“…developed countries’ appetite for skilled migrants has grown – just look at Silicon Valley’s large supply of successful Indian and Taiwanese computer scientists and venture capitalists. The enhanced appetite for such professionals reflects the shift to a globalized economy in which countries compete for markets by creating and attracting technically skilled talent. Governments also perceive these workers to be more likely to assimilate quickly into their new societies.”

Borjas (2000) mirrors this view in his analysis of the effects of skilled immigration through complementary effects on native capital and knowledge externalities to native workers.¹

¹ The importance of immigration in terms of its impact on the host economy is highlighted in Freeman (2004). He suggests that for several reasons immigration may have more significant effects than trade flows. One reason is the presence of non-traded goods in the product mix. Another is that a large volume of trade occurs between developed nations with similar factor endowments and thereby not contributing to factor price equalization as predicted by neo-classical trade theory. On the other hand, immigration happens more from developing to developed nations, significantly affecting the mix of skilled to unskilled labor in the host nation. This issue is not the focus of this paper, but it does go to show the importance of immigration in framing economic policy.
This paper addresses this interdependence in immigration policy, especially in the context of skilled immigrants who are perceived to be temporary workers. While immigration policy in the United States is largely considered to be a bilateral issue between the source nation (say India) and the host nation (U.S.), it is clear that immigration of skilled labor to the United States has spillover effects on other potential host nations and *vice versa*. If immigration raises the return on capital, capital will flow into that nation. The capital outflow from the other developed nations will affect both their wages and national income. Thus, the immigration level chosen by one host nation affects another. Although this is recognized in the literature, its analysis has not developed at a sufficient level.²

We address the issue of interdependence between host nations with a three-nation model where immigrants from a source developing nation (say $S$) migrate to two developed host nations ($H$ and $F$). $H$ and $F$ are developed nations with superior technology (relative to $S$) associated with higher marginal product of labor and consequently higher wages. Immigration policy is determined through a government quota and, as a result, there is a wedge between wages in the host and source nations. For simplicity, we also assume that there is no wage discrimination in the host nation. That is, immigrants and natives earn the same wage.

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² For example, see Fuess (2003) for a discussion about the favorable sentiment in Japan in the 1990s towards skilled immigration to help the nation regain international competitiveness at a time when Japan was suffering from an economic slump. Also, although the context is different, Zimmermann’s (2005) focus on the necessity of EU-wide harmonization of immigration policies (for non-EU source nations) is related. For example, he aptly summarizes the interdependence of immigration polices as follows: “There is a need to harmonize the single-country migration policies across Europe…. An inflow of non-EU labour immigrants in one country may affect the economies in all European Union partner countries through externalities in immigration like illegal flows, forced mobility of the natives, or adjustments through the capital and goods markets.”
Host nations incur an assimilation cost in making an immigrant suitable for the domestic workplace. It is well documented in the literature that assimilation entails real resource costs for an economy. Consider, for example, proficiency in the host nation’s official language. Dustmann and van Soest (2002) write:

“…one question relevant to that issue is how strongly language proficiency influences economic assimilation. If good knowledge of the dominant language increases productivity by a sufficient amount, governments may find it advantageous to provide an appropriate infrastructure for language acquisition to support this process, and to encourage the immigrant population to learn the dominant language. It is therefore important to obtain an accurate estimate of the effect of language on earnings.”

Using German data, they find significant effects of acquisition of the German language on the earnings of immigrants. Along similar lines, Meng and Gregory (2005) look at the effect of inter-marriage between immigrants and natives to look for assimilation effects. They find that intermarried immigrants earn significantly higher incomes compared to nonintermarried ones. They control for other mitigating factors and conclude that this premium derives from better assimilation that intermarriage facilitates.

In the benchmark case in which capital is immobile, the immigration policies of the two host nations H and F are independent of each other. Each host nation chooses immigration levels that equate the marginal gains for domestic capitalists to the marginal social (or assimilation) costs of immigration. A rise in immigration to nation j reduces the capital-to-labor ratio and the wage rate. The loss to native labor is a transfer that accrues to domestic capital, so the transfer makes no difference in terms of national income.\(^3\) As the

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\(^3\) Note that this is completely consistent with the findings of Borjas (2003), among others, suggesting that immigration has a negative effect on the wages/employment opportunities of native workers. The point of departure here is that we consider the aggregate effect on the nation, and, therefore, a loss to the workers is washed out by a gain to employers. We should also note that, in the presence of complementarities between different types of workers, the effect of immigration on native workers need not be negative. In our model the immigrants and native workers are perfect substitutes as far as the production function goes. If one allows for imperfect substitutability in the production function, then, of course, the negative impact might be
wage rate falls, however, immigrants are paid less, leading to an effective terms-of-trade gain in the factor market. This gain accrues as higher return for domestic capital, resulting in a net marginal benefit from immigration for a host nation.

In the presence of capital mobility, there are two scenarios. First, capital may be mobile between the host nations but immobile between the host nations and the source nation. This might be due, for example, to significant barriers to international capital mobility in developing nations (like a lack of currency convertibility, restrictions on the participation of foreign holders in equity markets, etc.). The alternative scenario has freely mobile capital between the developed and developing nations. Section 3 of the paper analyzes the first scenario, while section 4 extends it to the second. Some ambiguities do arise in the latter case, but the main thrust of the results from section 3 is unaffected.

When capital is mobile between $H$ and $F$ only, a rise in the immigration quota by $H$ will raise the demand for capital as more of it will be required to complement immigrant labor at the prevailing capital intensity. This will raise the demand for capital in the global capital market and raise its price, leading to two effects. The first is a terms-of-trade benefit from a reduction in payment to immigrants (similar to the immobility case). The second effect comes into play through the capital market. If $H$ is a net exporter (importer) of capital, it will gain from a rise (fall) in the rental rate. At the optimal immigration level, the marginal gains from these two effects are equated to the marginal cost. The relaxation of the immigration quota by $H$ affects the other host nation $F$ through the effect on the global capital market. Nation $F$’s capitalists gain, prompting $F$ to adjust its optimal immigration level. In other words, $H$ and $F$’s immigration policies have positive spillover

mitigated. In a recent contribution, Ottaviano and Peri (2005) take this approach and find large positive effects of immigration on the wages of U.S.-born workers. It is the complementarities between immigrants and natives that drive their findings.
effects on each other. In the Nash equilibrium, immigration levels are too low from a cooperative point of view. Because the positive externalities created by one nation on the other are not internalized in the process of unilateral optimization, there is a coordination failure that is quite similar to the problems that have been noted in the tax competition or multi-country trade taxation literatures.4

If the production functions of the two nations are identical, the international rate of return on capital is a function of the joint immigration levels of $H$ and $F$. In other words, global immigration becomes a public good. In turn, this means that the marginal benefit of $H$ (or $F$) is a function of global immigration and is independent of its location. The marginal cost is, however, location-specific and, hence, private. The result is a typical free rider equilibrium in which only one nation allows immigration.

The remainder of the paper contains four sections. Section 2 presents the optimal choice of immigration in the absence of capital mobility. Section 3 considers capital mobility between the two host nations. Section 4 discusses the implications for capital mobility between the host and source nations. Section 5 concludes.

2. The Model with Immobile Capital

We present a standard single-good model that is used often to analyze factor mobility.5 This section analyzes the home nation alone because $H$ and $F$ are independent

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4 See for example Wilson (1999) for the tax competition issue. Regions set taxes too low in a competition to attract capital. The taxes are too low in the sense that each region ignores the negative (positive) externality of lowering (raising) taxes on a rival region. If this externality is internalized taxes are higher. In a different context, Panagariya and Schiff (1994), Rodrik (1995), and Bandyopadhyay (1996) note that taxation of primary commodity exports by one exporting nation drives up its price for others. In that sense, there are positive terms-of-trade externalities that are not internalized by Nash taxes. The resulting taxes are sub-optimal.

5 See for example Ethier (1986), Bond and Chen (1987), etc. for single-good models with a focus on the general equilibrium linkages between the goods and factor markets. Borjas (2001) also uses a one-good
in terms of their policy decisions in the absence of capital mobility, and the analysis for $F$ simply mirrors that of $H$. Country $H$ produces a single good $X$ using labor ($L$) and capital ($K$), and a constant returns to scale (CRS) technology:

$$X = X(L, K). \quad (1)$$

Let firms in $H$ be perfectly competitive. The first order conditions of profit maximization are

$$X_1 - w = 0 \Rightarrow w = X_1(1, k) \Rightarrow w = w(k), k = \frac{K}{L} \text{ and } \quad (2)$$

$$X_2 - r = 0 \Rightarrow r = X_2(1, k) \Rightarrow r = r(k). \quad (3)$$

Using CRS properties we get

$$w(k) = X(1, k) - kr(k). \quad (4)$$

Let $I$ be the level of immigration, while $\bar{L}$ and $\bar{K}$ are $H$’s endowments of labor and capital, respectively. Therefore,

$$L = \bar{L} + I \Rightarrow k = \frac{\bar{K}}{\bar{L} + I} \Rightarrow k = k(I), k' < 0. \quad (5)$$

Using (1) through (5) and assuming that the government does not include immigrant income in national income ($NI$), we have the following expression:6

$$NI = (\bar{L} + I)\{1, k(I)\} - w\{k(I)\}I - cI, \quad (6)$$

model to look at the effects of immigration when there are regional differences in wages. While it is not difficult to use a multi-good, multi-factor model, it complicates the analysis needlessly. Since our focus is on factor mobility, we abstract from that issue.

6 There is a well-established literature debating whether immigrant incomes should be included in economic analyses of national income. We assume that it is not included in national income. As far as the policy decision regarding immigration goes, this makes sense. This is because ex-ante, there is no reason why the government should care about immigrant incomes when it is trying to decide whether to let in another immigrant. At that stage, the immigrant is not yet part of the economy. However, ex-post, inclusion or exclusion may both be justified depending on the context.
where \( c \) is assumed to be the constant marginal cost of immigrant assimilation. From (6), the first-order condition for the maximization of national income (through the choice of an optimal immigration level) is

\[
\frac{dNI}{dl} = -I\left(\frac{dw}{dl}\right) - c = Ik\left(\frac{dr}{dl}\right) - c = 0 \Rightarrow Ik_{r} = c, \text{ where } r_{i} = \frac{dr}{dl}. \tag{7}
\]

A marginal increase in \( I \) reduces \( w \) and, therefore, the payment to labor, including immigrant labor. The fall in the wage rate implies a rise in the return on capital. The loss in income for native labor is offset completely by the gains to capital. In addition, domestic capital gains because of the loss in payments to the immigrants, which is a terms-of-trade gain in the factor market and shows up as a net marginal benefit from immigration on the left-hand side of the last equality in (7). At the optimum, this benefit equals the marginal cost of immigration. Relation (7) defines the optimal immigration level implicitly as

\[
I = I(c, \bar{L}, \bar{K}). \tag{8}
\]

Using (7) and (8),

\[
\frac{dl}{dc} = \frac{1}{SOC} < 0 \Rightarrow \frac{dk}{dc} > 0 \Rightarrow \frac{dr}{dc} < 0, \tag{9a}
\]

where SOC<0 is the second-order condition for the optimal immigration problem. Thus, a rise in the marginal cost of immigration will reduce its level and also reduce the return on capital. Furthermore,

\[
\frac{dl}{d\bar{K}} = -\frac{I_{r_{i}}\left(\frac{\partial k}{\partial \bar{K}}\right) + k\left(\frac{\partial r_{i}}{\partial \bar{K}}\right)}{SOC} > 0 \tag{9b}
\]

because, using (3) and (5) and ignoring the third derivative of the production function,
\[
\frac{\partial k}{\partial K} = \frac{1}{L + I} > 0, \text{ and } r_i = -k \frac{X_{22}}{L + I} \Rightarrow \frac{\partial r_i}{\partial K} = -\frac{X_{22}}{(L + I)^2} > 0.
\]

Therefore, a rise in the capital endowment will raise the optimal immigration level. Using (3) and (5), notice that

\[
r = r \left(\frac{K}{L + I}\right) \Rightarrow \frac{dr}{dK} = X_{22} \frac{dk}{dK}.
\]  

(10a)

It can be shown that\(^7\)

\[
\frac{dk}{dK} \frac{1 - k(dI/d\bar{K})}{L + I} < 0 \Rightarrow \frac{dr}{dK} > 0.
\]  

(10b)

This finding is interesting because it suggests that in a two-host-country setup, \textit{ceteris-paribus}, the nation having the larger endowment of capital has the higher return on capital. Thus, if \(H\) is capital-abundant it will have the incentive to import capital. This is counter-intuitive at first glance, but makes sense when one considers the complementarity between immigration and capital.\(^8\) From (9b) we see that a capital-abundant nation will have a higher optimal immigration level, which in turn raises the marginal product of capital and the rate of return on capital.

3. Capital Mobility between Host Nations

This section explores the consequences of capital mobility between \(H\) and \(F\) and assumes that \(S\) is not connected to the global capital market (an assumption that is relaxed in the next section). It is useful to look at the current context for two reasons. The first is the analytical simplicity it offers and therefore the clarity of the results that we can obtain.

\(^7\) The proof is available from the authors on request.

\(^8\) This is consistent with Freeman (2004) who writes: “In theory, global capital markets send capital from advanced countries to poor countries…the major importer of foreign capital has been the US, whose stability and technological progress has attracted foreign investment…”
The second is that for many developing nations capital mobility suffers from several barriers, so the abstraction from universal capital mobility has an element of realism. All F-nation variables are marked by an asterisk.

The capital market equilibrium condition is

\[ K + K^* = \overline{K} + \overline{K}^* = K^w \Rightarrow (\bar{L} + I)k(r) + (\bar{L} + I^*)k^*(r) = K^w \Rightarrow r = r(I, I^*), \]  

where

\[ \frac{\partial r}{\partial I} = r_i = -\frac{k}{(\bar{L} + I)k'(r) + (\bar{L}^* + I^*)k''(r)} > 0 \]

because \( k'(r) = dk/dr < 0 \) and \( k'' = dk^*/dr < 0 \) (since \( X_{22} < 0 \) and \( X_{22}^* < 0 \)). Similarly,

\[ \frac{\partial r}{\partial I^*} = r_i^* = -\frac{k^*}{(\bar{L} + I)k'(r) + (\bar{L}^* + I^*)k''(r)} > 0 . \]

Under capital mobility H’s national income is

\[ NI = (\bar{L} + I)X[1,k\{r(I, I^*)\}] - w[k\{r(I, I^*)\}]I - cL + rK_E, \]

where \( K_E = \overline{K} - K = \overline{K} - (\bar{L} + I)k \) is the net exports of capital by H to F. We assume that \( I \) and \( I^* \) are chosen simultaneously by H and F under the Nash assumption that \( I^* \) is given when choosing its optimal \( I \). Assuming an interior solution, national income in H is maximized when

\[ (Ik + K_E)r_i - c = 0 . \]  

A rise in immigration raises the return on capital, which benefits H on two counts: As in the previous section, a rise in the rental rate is beneficial because it lowers the wage bill, an effect measured by the term \( Ik r_i \). In addition, there is a gain (or loss) from capital exports

\[ \text{Consider the case of India, which, for a long time had quite closed trade and capital markets. With recent liberalization, that is changing, but there are still a lot of restrictions in the capital market. Foreign equity participation is limited, currency convertibility in the capital account is pending, and direct foreign investment is carefully monitored. Many other developing nations share such restrictions.} \]
(or imports), which is measured by \( K_r r_v \). In equilibrium, the sum of these two effects is balanced against \( c \), \( H \)'s marginal cost of immigration.

Relation (13a) defines \( H \)'s Nash reaction function implicitly:

\[
I = I(I^*; c, \bar{K}, \bar{L}). \tag{13b}
\]

Analogously, \( F \)'s first-order condition and Nash reaction function are, respectively,

\[
(I^* k^* + K^* r_v) r_v - c^* = 0 \quad \text{and} \quad I^* = I^*(I; c^*, \bar{K}, \bar{L}). \tag{14b}
\]

Simultaneous solution of (13a) and (14a) yields the Nash equilibrium \((I^*_N, I^*_N)\). Note that

\[
\frac{\partial I}{\partial l} = \frac{\partial^2 NI}{\partial l^2} \Rightarrow \text{sign} \left( \frac{\partial I}{\partial l} \right) = \text{sign} \left( \frac{\partial^2 NI}{\partial l^2} \right) \quad \text{and} \quad \frac{\partial I^*}{\partial l} = \frac{\partial^2 NI^*}{\partial I^* \partial I} \Rightarrow \text{sign} \left( \frac{\partial I^*}{\partial l} \right) = \text{sign} \left( \frac{\partial^2 NI^*}{\partial I^* \partial I} \right). \tag{15b}
\]

Further, it can be shown that

\[
\frac{\partial^2 NI}{\partial l^2} = (Ik + K_r) r_v - r_v r_v \bar{L} k' \quad \text{and} \quad \frac{\partial^2 NI^*}{\partial I^* \partial I} = (I^* k^* + K^* r_v) r_v - r_v r_v \bar{L} k^* \hat{r}. \tag{16b}
\]

Using (11), we know that \( r_v \) and \( r_v \) are both positive. Thus, because \( k' \) and \( k^* \hat{r} \) are both negative, the second terms on the right-hand sides of (16a) and (16b) are positive. It can be shown that

\[
r_v r_v \left( \frac{k'}{k} + \frac{k^* \hat{r}}{k} \right) < 0. \tag{17}
\]
The first-order conditions imply that \((Ik + K_E)\) and \((I^*k^* + K^*_E)\) are both positive. Using (16a), (16b), and (17), it is clear that the reaction functions can be either positively or negatively sloped.

Let us now explore the incentives for \(H\) to pre-commit. Using (12) and (14b),

\[
NI = NI\{I, I^*(I)\} \Rightarrow \frac{dNI}{dI} = \frac{\partial NI}{\partial I} + \left(\frac{\partial NI}{\partial I^*}\right)\left(\frac{\partial I^*}{\partial I}\right).
\]

Evaluating (18a) at the Nash equilibrium [i.e., where \(\partial NI / \partial I = 0\)],

\[
\frac{dNI}{dI} = \left(\frac{\partial NI}{\partial I^*}\right)\left(\frac{\partial I^*}{\partial I}\right);
\]

It can be shown that

\[
\frac{\partial NI}{\partial I^*} = (Ik + K_E)r_I > 0,
\]

so, using (18b) and (19), it is clear that at the Nash equilibrium

\[
\frac{dNI}{dI} = \left(\frac{\partial NI}{\partial I^*}\right)\left(\frac{\partial I^*}{\partial I}\right) > 0(< 0) \text{ as } \frac{\partial I^*}{\partial I} > 0(< 0).
\]

From (20), in the Nash equilibrium \(H\) has a local incentive to pre-commit to a higher (lower) immigration level if \(F\) views \(I\) as a strategic complement (substitute) for \(I^*\). Using (16b) and (17), \(I\) is a strategic complement for \(I^*\) if and only if

\[
(I^*k^* + K^*_E)\left(\frac{k^*}{k} + \frac{k^*}{k^*}\right) > Lk^*.
\]

Finally, it is worth noting that because of positive spillovers, Nash-equilibrium immigration levels are likely to be too low compared to the cooperative levels. Consider, for example, the joint national income of \(H\) and \(F\):

\[
NI^w(I, I^*) = NI(I, I^*) + NI^*(I, I^*).
\]
Partials of the joint national income are
\[ \frac{\partial NI^w(I, I^*)}{\partial I} = \frac{\partial NI(I, I^*)}{\partial I} + \frac{\partial NI^*(I, I^*)}{\partial I} \quad \text{and} \quad \frac{\partial NI^w(I, I^*)}{\partial I^*} = \frac{\partial NI(I, I^*)}{\partial I^*} + \frac{\partial NI^*(I, I^*)}{\partial I^*}. \]

Evaluated at the Nash equilibrium, these reduce to
\[ \frac{\partial NI^w(I, I^*)}{\partial I} = \frac{\partial NI(I, I^*)}{\partial I} = (I^* k^* + K^*_k)r_i > 0 \quad \text{and} \quad \frac{\partial NI^w(I, I^*)}{\partial I^*} = \frac{\partial NI(I, I^*)}{\partial I^*} = (I k + K^*_K)r_i > 0. \]

From (24a) and (24b), it is clear that, starting from the Nash equilibrium, there is a local incentive to raise both \( I \) and \( I^* \) to achieve a cooperative equilibrium.

Turning our attention to the special case of identical production functions in \( H \) and \( F \), (11) can be written as
\[ k(r)(\bar{L} + \bar{L} + I + I^*) = \bar{K} \Rightarrow r = r(I + I^*) \Rightarrow r_i = r_j(I + I^*) = r_i. \]

For \( H \), the marginal benefit from immigration is
\[ MB^H = (I k + K^*_k)r_i = [\bar{K} - \bar{K} k \{r(I + I^*)\}]r_j(I + I^*) \Rightarrow MB^H = MB^H(I + I^*). \]

Similarly, for \( F \),
\[ MB^F = [\bar{K}^* - \bar{K}^* k \{r(I + I^*)\}]r_j(I + I^*) \Rightarrow MB^F = MB^F(I + I^*). \]

In this case we have the possibility of a corner solution. Suppose that \( H \) and \( F \) have identical marginal costs of immigration (i.e., \( c = c^* \)). Also assume that \( H \) has larger endowments of both labor and capital compared to \( F \). In this case, \( H \) will have an interior solution and \( F \) will have a corner solution (i.e., \( I^* = 0 \)) if and only if
\[ MB^H > MB^F \Rightarrow \bar{K} - \bar{L}k > \bar{K}^* - \bar{L}k \Rightarrow k < \frac{\bar{K} - \bar{K}^*}{\bar{L} - \bar{L}^*}. \]  

This is a Nash equilibrium where the optimal immigration for \( F \) is zero.\(^{10}\) Notice, however, that if \( F \) added a unit of immigration at the margin, the sum of the benefit from it for \( H \) and \( F \) would have exceeded the marginal cost to \( F \). Thus, we have a free rider problem (as in the case of a public good). Because \( r \) is a function of the sum of the two nations’ immigration levels, global immigration is a pure pubic good and is underprovided. Figure 1 illustrates this free-riding equilibrium for \( c = c^* \).

Notice from (25) that
\[ k(r) = \frac{\bar{K}^w}{\bar{L}^w + I^w}, \text{ where, } \bar{L}^w = \bar{L} + \bar{L}^*, \text{ and, } I^w = I + I^*. \]  

Using (27) and (28), the condition for \( MB^H > MB^F \) boils down to
\[ I^w > 2(\bar{K}^* \bar{L} - \bar{K} \bar{L}^*) / ((\bar{K} - \bar{K}^*)). \]  

If global immigration is positive, then a sufficient condition for (29) to be satisfied is
\[ \bar{K}^* \bar{L} - \bar{K} \bar{L}^* < 0 \Rightarrow \frac{\bar{K}}{\bar{L}} > \frac{\bar{K}^*}{\bar{L}^*}, \text{ assuming } \bar{K} > \bar{K}^*. \]  

Therefore, (30) suggests that if \( H \) is larger than \( F \) in terms of their endowments, then a sufficient condition for \( H \) to provide for global immigration while \( F \) free rides is that \( H \) is capital-abundant relative to \( F \). In the general case in which the marginal costs might differ, \( H \) will provide immigration and \( F \) will free ride if and only if
\[ MB^H - MB^F > c - c^* \Rightarrow k < \frac{\bar{K} - \bar{K}^* + (c^* - c)}{\bar{L} - \bar{L}^*} \cdot \]  

\(^{10}\) The corner solution in which one country will allow zero immigration in equilibrium is rather implausible and follows from our assumption of constant marginal assimilation costs. If we instead had increasing marginal assimilation costs, we could obtain interior solutions for both host countries. Immigration levels would still be sub-optimal because of the public good aspect of the model.
4. Capital Mobility between Host and Source Nations

It is useful to see how capital mobility among $H$, $F$, and $S$ affects our findings. In what follows, all variables are denoted as in the previous sections and the superscript $S$ refers to nation $S$. Let the production function in $S$ be CRS in labor and capital and be of the following form:

$$X^S = X^S(L^S, K^S), \text{ where, } L^S = L^S - (I + I^*) \text{ and } K^S = K^S - K^S_E.$$

(32)

Using (32) the capital market equilibrium is

$$K + K^* + K^S = K + K^S + K^S = K^W \Rightarrow$$

$$(L + I)k(r) + (L + I^*)k^*(r) + \{L^S - (I + I^*)\}k^S = K^W \Rightarrow r = r(I, I^*).$$

(33)

Using (33),

$$r_i = -\frac{k - k^S}{(L + I)k'(r) + (L + I^*)k''(r) + \{L^S - (I + I^*)\}k^S} > (or <) 0 \text{ as } k > (or <) k^S. \tag{34a}$$

Similarly,

$$r_{i^*} = -\frac{k^* - k^S}{(L + I)k'(r) + (L + I^*)k''(r) + \{L^S - (I + I^*)\}k^S} > (or <) 0 \text{ as } k^* > (or <) k^S. \tag{34b}$$

From (34a) and (34b), we can see that there is an ambiguity about the effect of a rise in the immigration quotas on the international rate of return on capital. If capital intensity in $S$ is higher than that in $H$ and $F$, then the effect of the immigration quotas on the return on capital is reversed. It is probably more realistic, however, to concentrate on the case where the developed host nations have a higher capital intensity compared to $S$. In that case, the effect of immigration on $r$ is as in the previous analysis, and the thrust of the results is unaffected. Finally, let us note that if the host nations have identical technology, then (33) may be written as
Expression (35) is similar to (25) in that the rental function is additive in its arguments. This implies that the public good nature of global immigration obtains even in this case. This results in a free riding and globally sub-optimal immigration equilibrium.

5. Concluding Remarks

This paper considered optimal immigration policy when mobile capital and capital-labor interdependencies mean that host countries’ policies are interdependent. As a result, market failures associated with externality and public good problems arise when host nations do not coordinate their immigration policies. While our context is somewhat distinct from Zimmermann’s (2005) discussion on the coordination problems within the European Union, the analysis should shed light on the European context. Although we focus on legal immigration, it would also be interesting to explore the coordination of policies toward illegal immigrants. Zimmermann (2005) discusses this issue, but we have not seen a formal analysis of it.
References


$$c = c^*$$

Figure 1