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Seibold, Arthur; Seitz, Sebastian; Siegloch, Sebastian

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PRIVATIZING DISABILITY INSURANCE

ARTHUR SEIBOLD

Department of Economics, Ludwig-Maximilians University Munich and CEPR

SEBASTIAN SEITZ

Department of Economics, University of Manchester and ZEW

SEBASTIAN SIEGLOCH

Department of Economics, University of Cologne, CEPR, and ZEW

Public disability insurance (DI) programs in many countries face growing fiscal pressures, prompting efforts to reduce spending. In this paper, we investigate the welfare effects of expanding the role of private insurance markets in the face of public DI cuts. We exploit a reform that abolished one part of German public DI and use unique data from a large insurer. We document modest crowding-out effects of the reform, such that private DI take-up remains incomplete. We find no adverse selection in the private DI market. Instead, private DI tends to attract individuals with high income, high education, and low disability risk. Using a revealed preference approach, we estimate individual insurance valuations. Our welfare analysis finds that partial DI provision via the voluntary private market can improve welfare. However, distributional concerns may justify a full public DI mandate.

KEYWORDS: Disability insurance, social insurance, privatization, risk-based selection.

1. INTRODUCTION

ACROSS THE DEVELOPED WORLD, the number of individuals receiving public disability insurance (DI) benefits has risen rapidly over the past decades. This has made DI one of the largest social insurance programs in OECD countries (OECD (2024)). Due to the increasing fiscal burden, governments face pressure to enact reforms reducing the generosity of public DI programs. While such reforms help improve fiscal sustainability, they naturally come at the cost of providing less insurance to individuals at risk of disability.

As a consequence, some economists and policymakers have proposed a larger role of *private* DI (e.g., GAO (2018)). Sizable private DI markets already exist in many countries, including the U.S. and Germany. However, private DI provision faces several potential problems, including market failures due to adverse selection and equity concerns

Arthur Seibold: arthur.seibold@econ.lmu.de Sebastian Seitz: sebastian.seitz@manchester.ac.uk Sebastian Siegloch: siegloch@wiso.uni-koeln.de

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(Liebman (2015)). Despite the significance of this policy debate, there is remarkably little empirical evidence on the functioning of private DI markets.¹

In this paper, we break new empirical ground on these issues. We investigate key features of private DI markets and study the welfare consequences of expanding the role of private DI. We exploit a unique reform that abolished one part of public DI for German workers. Our analysis is based on novel microdata from a large private insurer and administrative data on the universe of public DI claims. This setting and data allow us to obtain three pieces of empirical evidence that govern the welfare impact of private DI provision. First, we estimate crowding-out effects between public and private DI. Second, we document substantial heterogeneity in private DI take-up, which raises distributional concerns. Third, we carefully test for risk-based selection, which provides crucial information about the efficiency of the private DI market. We adopt a revealed preference approach to estimate individual insurance valuations based on these empirical facts. Our welfare analysis shows that partly privatizing DI can improve welfare. However, a full public DI mandate could be justified by equity concerns.

Assessing the potential of private DI to complement public DI is challenging for two reasons. First, suitable variation in public DI coverage is needed. Second, comprehensive and reliable data on private insurance is necessary to quantify the interaction between public and private DI. This paper is the first to overcome both of these challenges.

We exploit exogenous variation induced by a reform that removed one part of German public DI and replaced it with a voluntary private DI market. Specifically, the reform of 2001 privatized *own-occupation* DI for younger workers. Receiving own-occupation DI benefits requires workers to be unable to work in their previous occupation. In contrast, general DI benefits are based on stricter eligibility criteria: being unable to work in any occupation. Before the reform, both own-occupation and general DI were part of the social insurance system. The reform completely removed public own-occupation DI for birth cohorts 1961 and younger. Importantly, the German private DI market offers contracts including own-occupation DI coverage, for which workers can opt if they wish to compensate for the loss of public DI coverage.

To address the second challenge, we obtained a novel data set on all private DI contracts issued by a top-10 insurer in the German private DI market. This data contains high-quality information on private DI coverage, prices, and individual characteristics, which are critical inputs into our empirical analysis. We demonstrate that the insurer microdata is representative of the overall private DI market in key dimensions using aggregate data on the entire private DI market from a leading rating agency and representative household survey data. Complementing the data on private DI, we use administrative data on the universe of public DI claims.

We provide three pieces of empirical evidence on the private DI market. First, we study crowding-out effects of the reform, that is, the impact of public DI cuts on private DI take-up. On aggregate, we find substantial growth in the private DI market after the reform. To identify a causal effect, we use a difference-in-difference strategy exploiting the cohort cutoff of the reform. We find that treated individuals born above the cutoff significantly increase private DI purchases compared to control cohorts below the cutoff. Yet, even 15 years after the reform, overall take-up remains modest, as only 26% of workers have private DI. Thus, crowding-out is far from complete.

¹For instance, in their report to Congress, the U.S. Government Accountability Office (GAO (2018)) concludes that the implications of various proposals to expand private DI cannot be fully assessed due to "an array of complex factors that could influence private DI expansions and SSDI cost savings—factors for which data, methods, and assumptions [...] are either unreliable, unsupported, or unavailable."

Second, we document substantial heterogeneity in private DI take-up. Modest overall private DI take-up is mainly driven by low take-up among individuals with low income and low education. For instance, take-up is 65% in the top income quintile but only 7% to 12% in the bottom three quintiles. Moreover, there is important heterogeneity in take-up by priced risk groups, which insurers assign to workers based on occupations. Individuals in high-risk groups facing higher premiums are much less likely to take up insurance. These patterns indicate potential equity issues in the private DI market.

Third, we carefully investigate risk-based selection into private DI using two complementary empirical strategies. The first strategy is a "positive correlation test" (Chiappori and Salanié (2000)), regressing private DI take-up on disability risk at the level of finegrained occupations. As a second strategy, we conduct a "cost curve test" (Einav, Finkelstein, and Cullen (2010)), which exploits variation in private DI premiums over time to test for differences in risk across individuals. We do not find any evidence of adverse selection. In both empirical designs, risk-based selection is of a small and insignificant degree. At first glance, the lack of adverse selection may be surprising, as insurance should, in principle, be more valuable to higher-risk individuals. We discuss several potential explanations for this result. For instance, there could be heterogeneous preferences for insurance that are negatively correlated with risk. In particular, the fact that individuals with high education and high income are more likely to purchase private DI seems to counter adverse selection. We also explore the possibility of heterogeneous earnings losses upon disability that could make private DI more valuable for workers in high-skill occupations.

We then turn to the welfare consequences of privatizing DI provision. The analysis builds on Einav, Finkelstein, and Cullen (2010), who show that insurance demand and cost curves are sufficient statistics to assess welfare in insurance markets. Our setting with insurance choice provides a unique opportunity to implement a revealed preference approach and directly estimate individuals' willingness to pay for the DI coverage offered by the private market. To trace out the slope of the private DI demand curve, we implement an event study design around occupation reclassifications, which entail large changes in private DI premiums. This estimation yields a demand elasticity of -1.06.

Our counterfactual analysis compares the post-reform status quo, where DI is partly provided via the private market, to a full public DI mandate, including this extra coverage. We consider two welfare measures: (i) the net value of DI, which expresses the value of DI relative to its direct cost, and (ii) the marginal value of public funds (Hendren and Sprung-Keyser (2020)). For the latter, we calibrate additional indirect fiscal effects based on our data and estimates from the literature. Our main net value estimate implies that revealed insurance valuations among individuals receiving extra coverage amount to only 70.5% of the direct cost of insurance. Similarly, the marginal value of public funds of a mandate is 0.617.

This initial welfare analysis ignores distributional concerns. In an extension, we incorporate welfare weights based on a Utilitarian social welfare function. We find that a full public DI mandate has a social value exceeding its costs, even under small degrees of equity concern. Importantly, redistributive effects hinge on the design of social insurance. A *private* DI mandate does not increase social welfare since insurance benefits to high-risk groups are counteracted by risk-rated premiums. In contrast, a *public* DI mandate financed by income-based social insurance contributions effectively redistributes to low-income, high-risk individuals.

Overall, this paper shows that several market failures discussed in prior literature cannot justify mandating extra DI coverage in this context. Most importantly, we do not find any evidence of adverse selection in the private DI market, which is often considered

the canonical rationale for a public DI mandate. We also account for market power and administrative costs, which contribute to low take-up in other private insurance markets (Braun, Kopecky, and Koreshkova (2019)), and we calibrate several potential externalities. We find that none of these factors warrant a mandate in our setting. Hence, the private market covers the majority of individuals with a sufficiently high willingness to pay, and a mandate would predominantly enroll those with valuations below marginal cost. It is important to note that our welfare analysis follows existing literature and maintains the assumptions of the revealed preference approach, which abstracts from behavioral biases. Studying such biases is beyond the scope of this paper.

We argue that our findings are relevant beyond the German context for two main reasons. First, our systematic review of DI systems across countries reveals that both the German public DI system and the German private DI market share key characteristics with other countries, making our setting a broadly representative case study of privatizing DI. We also provide evidence that our results are not driven by specific institutional features, such as means-tested social assistance. Second, own-occupation disability risk—the subrisk our setting centers on—is strongly positively correlated with overall disability risk in the data. Hence, the types of individuals who would benefit from private DI tend to be those who would benefit from DI more generally. One may therefore expect similar patterns to emerge in other settings, including those where the details of DI coverage differ. Indeed, the limited existing evidence on private DI take-up from other countries points in this direction.²

This paper contributes to a large and growing literature on DI (see Low and Pistaferri (2020), for a review). Much of this literature focuses on public DI and its effect on labor supply and claiming decisions (Bound (1989), Gruber (2000), Autor and Duggan (2003, 2006, 2007), Chen and van der Klaauw (2008), Autor, Duggan, and Lyle (2011), Staubli (2011), von Wachter, Song, and Manchester (2011), Marie and Vall Castello (2012), Maestas, Mullen, and Strand (2013), French and Song (2014), Kostol and Mogstad (2014), Borghans, Gielen, and Luttmer (2014), Koning and Lindeboom (2015), Liebman (2015), Autor, Duggan, Greenberg, and Lyle (2016), Burkhauser, Daly, and Ziebarth (2016), Deshpande (2016a,b), Mullen and Staubli (2016), Gelber, Moore, and Strand (2017), Autor, Kostol, Mogstad, and Setzler (2019), Ruh and Staubli (2019)). In contrast, there is much less prior work on private DI markets. Exceptions include Autor, Duggan, and Gruber (2014), Stepner (2021), and Seitz (2021), who analyze moral hazard effects of private DI. A recent working paper by Fischer, Geyer, and Ziebarth (2024) also investigates the German reform of 2001. Their approach is complementary to ours, combining survey data with a general equilibrium model of the private DI market. Similar to our results, they find modest private DI take-up after the reform, particularly among low-income groups. While our welfare analysis focuses on the trade-off between private and public DI provision, they emphasize the role of supply-side factors for take-up and welfare within the private DI market.

We make three main contributions to this literature. First, exploiting our unique data and setting, we provide novel empirical evidence on crowding-out and selection in private DI markets. Our findings constitute the first direct empirical evidence on these issues, which are key in assessing the welfare impact of policies expanding the role of private markets and choice in DI. Second, we further exploit our setting with insurance choice to estimate willingness to pay for DI in a revealed preference approach. So far, little is

²For instance, Autor, Duggan, and Gruber (2014) and GAO (2018) report that private DI take-up increases with income in U.S. data, similar to our findings.

known about how individuals value DI. One exception is Cabral and Cullen (2019), who estimate willingness to pay for supplemental DI coverage within a U.S. firm and derive a lower bound on public DI valuations.³ Our third contribution is to assess the welfare consequences of partial private DI provision vs. a full public mandate. This complements and extends existing work analyzing welfare and the insurance-incentive trade-off within public DI (Diamond and Sheshinski (1995), Low and Pistaferri (2015), Meyer and Mok (2019), Haller, Staubli, and Zweimüller (2024)).

More broadly, our work builds on a rich literature testing for risk-based selection in social insurance settings. In Supplemental Appendix D (Seibold, Seitz, and Siegloch (2025)), we provide a more detailed review of this literature and conduct a meta-analysis of studies on risk-based selection published in leading economics journals since 2000. A large majority of existing work focuses on health insurance. Several papers have examined long-term care insurance (LTCI), pension annuities, and unemployment insurance. Evidence on risk-based selection in DI is particularly scarce. The only exception is Hendren (2013), who provides indirect evidence on potential risk-based selection in DI by documenting that individuals have private information about their disability risk.

While prior work on health insurance, pension annuities, and unemployment insurance tends to find evidence of adverse selection, our analysis of DI shows some interesting parallels to LTCI. DI and LTCI share several features, including risks predominantly occurring later in life, strong risk-rating in the private market, and the coexistence of public and private schemes. Like us, Finkelstein and McGarry (2006) and Boyer, De Donder, Fluet, Leroux, and Michaud (2020) find no adverse selection in private LTCI, with point estimates indicating advantageous selection. Braun, Kopecky, and Koreshkova (2019) investigate the interplay of asymmetric information, market power on the supply side, and other transfer programs in explaining low observed LTCI take-up.

Finally, this paper contributes to a nascent literature investigating the welfare effects of universal mandates versus voluntary markets in social insurance settings. Existing studies on these issues include work on health insurance (e.g., Einav, Finkelstein, and Cullen (2010), Finkelstein, Hendren, and Shepard (2019)), unemployment insurance (Landais, Nekoei, Nilsson, Seim, and Spinnewijn (2021), Hendren, Landais, and Spinnewijn (2021)), and workers' compensation (Cabral, Cui, and Dworsky (2022)). Our main contribution to this wider literature is that we provide the first welfare analysis of a private market with choice versus a full public mandate in the context of DI, one of the most important social insurance programs.

The remainder of this paper is organized as follows. Section 2 outlines context and data, Section 3 presents evidence on crowding-out, Section 4 discusses heterogeneity in private DI take-up, Section 5 tests for risk-based selection, Section 6 presents the demand and cost estimation, Section 7 shows the welfare analysis, and finally Section 8 concludes.

2. INSTITUTIONAL BACKGROUND AND DATA

2.1. Disability Insurance in Germany

Public Disability Insurance. In Germany, public disability insurance (DI) is administered by the State Pension Fund. Enrollment is mandatory for all employed individuals, while most self-employed workers and civil servants are exempt. DI contributions are

³In addition, a few studies use indirect consumption-based methods to quantify the insurance value of public DI (e.g., Meyer and Mok (2019), Deshpande and Lockwood (2022)).

levied as payroll taxes together with old-age pension contributions. Enrolled workers become eligible for DI benefits in the event of a long-term disability limiting their work capacity. Moreover, eligibility requires having contributed for at least 5 years in total and at least 3 out of the 5 years before the onset of disability. Upon application, a medical and work capacity assessment is carried out by the Pension Fund. Benefits are a function of workers' contributions, assuming they would have kept contributing according to their average predisability earnings until age 63. Public DI benefits are thus roughly proportional to individuals' predisability earnings, with an average gross replacement rate of 39%. Benefits can be paid until a worker reaches the normal retirement age, when they are converted into an old-age pension. According to our administrative data, 25.1% of German workers become disabled and claim public DI throughout their lifetime.

Crucially for our purposes, the public DI system consists of two separate tiers, general DI and own-occupation DI. The first tier pays benefits to workers suffering from a general disability (Erwerbsunfähigkeit), such that they are unable to work in any occupation for more than 3 hours per day. Common conditions leading to general disability include degenerative disc disease or severe depression/burn-out. The second tier, on the other hand, requires an own-occupation disability (Berufsunfähigkeit), defined as being unable to work in one's previous occupation. For instance, a bus driver suffering from vision impairment is unable to work in their occupation but may be able to work in other jobs. The two DI tiers require separate applications. Workers on own-occupation DI receive two-thirds of general DI benefits but face a less stringent earnings test. Own-occupation DI cases make up 13.2% of all public DI claims.

The Reform of 2001. Before 2001, all workers were covered both by general and own-occupation DI as part of the public DI mandate. However, rising expenditure on DI benefits stoked concerns about the fiscal sustainability of the program in the 1990s. This motivated a major reform in 2001 aimed at reducing public DI spending. Most importantly, the reform featured a sharp, cohort-based change in the scope of public DI: own-occupation DI coverage was completely removed for birth cohorts 1961 and younger from 2001 onward. Besides this main element, the reform featured further changes equally affecting all cohorts, including gradually phased-in changes to benefit calculation.⁵

The timing of the reform was noteworthy. Initially, the reform was announced in December 1997 to take effect in January 1999. The initial reform proposal intended to abolish own-occupation DI for all workers, not only for younger cohorts. After a change of federal government, the reform was retracted in late 1998. However, in December 2000, the reform was reannounced in its final form featuring the cohort cutoff, and the changes took effect in January 2001.

Private Disability Insurance. According to our rating agency data, at least 73 insurance companies offer private DI contracts. In 2015, the top 3 providers had a combined market

⁴General DI benefits are reduced for monthly earnings above EUR 400, whereas workers on own-occupation DI are allowed to earn at least EUR 700, depending on their prior earnings. Note that these earnings test thresholds are adjusted every few years. The aforementioned figures apply between 2008 and 2017.

⁵More precisely, the reform altered two elements of benefit calculation. First, an adjustment factor was gradually introduced, featuring negative benefit adjustments similar to penalties for early old-age pension claims. Second, the hypothetical contribution period used for benefit calculation was gradually extended, somewhat counteracting the new penalties. In addition, the reform introduced the possibility of claiming partial DI benefits for individuals with a general disability who can work between 3 and 6 hours per day. Finally, work capacity reassessments were introduced, but in practice, most beneficiaries still receive benefits permanently.

share of 34.2%, and the top 10 providers had a market share of 62.7%. Crucially, private DI always includes coverage of own-occupation disability risk, closely mirroring the prereform public DI system. Thus, workers affected by the reform can choose to purchase private DI in order to compensate for the removal of public own-occupation DI. Private DI payouts are independent of the public DI system, such that they can also serve as a top-up in case a worker is awarded public DI benefits. Before 2001, private DI purely served as such top-up insurance.

An important difference to the public DI system is that private DI premiums are riskbased. The primary determinant of private DI premiums are individuals' occupations, whereby insurers map occupations into a discrete number of risk groups (see below). Furthermore, insurance premiums can be adjusted for preexisting medical conditions and risky leisure activities, but this occurs infrequently.⁶ Finally, monthly premiums are actuarially adjusted to the individual's contract start and end date. This pricing practice has remained largely unchanged throughout our sample period and applies to all buyers. Private DI contracts typically specify a fixed amount of insured benefits, which can be set individually. In practice, monthly private DI payouts are of a similar magnitude to public DI benefits (see Section 2.3). German private DI is largely a nongroup market: the majority of 85% of contracts are purchased individually, and the remainder are obtained via employers (FAZ (2012)). Except a few niche providers, insurers generally offer contracts to all occupations. According to official statistics, only 3% of contract applications are denied by insurers (GDV (2023)).7 In terms of primary features, including the definition of disability, benefit levels, and contract duration, private DI contracts are quite homogenous across providers.⁸ Private DI can be bought either as a stand-alone product or bundled with other types of insurance, most commonly life insurance.

Table I provides summary information about private DI premiums and risk groups. The average monthly premium to insure EUR 1000 of monthly benefits is around EUR 73 for a contract start age of 25 and EUR 98 for a start age of 45. Following standard practice in the industry, the insurer from which our microdata originates uses five risk groups to price DI contracts. Appendix Table A1 shows frequent occupations in each risk group. Examples of occupations classified as low-risk include medical doctors, computer scientists, and accountants. Medium-risk occupations include high-school teachers, secretaries, and electrical engineers; high-risk occupations include bakers, firefighters, and warehouse workers. Private DI premiums differ strongly across risk groups: for instance, an individual in the lowest-risk group 1 is charged EUR 32 at age 25, while premiums rise up to EUR 155 for the highest-risk group 5. This variation in premiums is roughly in line with differences in disability risk across occupations. According to our administrative data, the lifetime disability risk of individuals in risk group 1 is less than 5%, while it is 24% in risk

⁶Premiums are adjusted beyond risk-group specific prices in only 4% of private DI contracts (GDV (2023)).

⁷This includes a few extremely risky occupations such as circus artists and explosives workers, as well as rejections due to preexisting conditions or risky leisure activities. Besides coverage denials, another 12% of private DI contracts feature exclusion clauses for preexisting conditions. The relatively low denial and exclusion rates are an important difference to U.S. nongroup insurance markets, where these are more frequent and can affect broader sets of occupations and income groups (Hendren (2013), Braun, Kopecky, and Koreshkova (2019)).

⁸The well-known consumer advice organization Stiftung Warentest (2024) finds in their latest report that contracts offered by 67 private DI providers are essentially homogenous in these primary characteristics. Even on secondary characteristics such as waiting periods, retroactive benefit adjustments, and rules on occupation switches, contracts are quite similar: the average provider satisfies 86% of secondary criteria set by the report. Ultimately, 85% of providers receive the highest ("very good") or second-highest ("good") rating.

Risk group	(1) Share of	(2) Lifetime disability risk	(3) Share of own-occupation DI claims	(4) (5) (6) Monthly insurance premium for contract start at		
	labor force			age 25	age 35	age 45
All	100.00%	25.06%	13.20%	72.84	83.54	98.15
Risk Group 1	9.72%	4.81%	10.85%	31.61	35.95	43.22
Risk Group 2	16.99%	15.35%	8.06%	41.72	49.08	57.49
Risk Group 3	35.12%	23.77%	12.56%	68.14	79.90	93.73
Risk Group 4	37.56%	31.01%	15.74%	100.60	113.31	133.03
Risk Group 5	0.62%	39.92%	31.94%	155.24	175.78	210.68

TABLE I Risk groups, disability risk, and private DI premiums.

Note: The table shows information on disability risk and private DI premiums by risk group. Risk groups are assigned by the insurer to individuals based on their occupations. See Appendix Table A1 for frequent occupations in each risk group. Column (1) shows the share of each risk group out of the labor force. Column (2) shows the fraction of individuals ever claiming public DI benefits in each group. Column (3) shows the share of own-occupation DI claims out of all DI claims. Columns (4) to (6) show the monthly premium (in EUR) charged to an individual insuring EUR 1000 of monthly benefits by contract start age, for a fixed contract end age of 65. The information in columns (1) to (3) is from our administrative data, and premiums are based on the insurer microdata.

group 3, and 40% in risk group 5.9 Own-occupation disability risk is strongly positively correlated with overall disability risk and increases even faster across risk groups. For instance, 8% to 11% of all disability cases in risk groups 1 and 2 are due to own-occupation disability, but the share increases to 32% for risk group 5. Finally, we note that risk groups differ in size, where risk group 1 and especially risk group 5 make up a smaller share of the labor force than the middle groups.

Other Safety Net Programs. In the German context, a number of other safety net programs are potentially available to individuals who are unable to work. Most importantly, means-tested social assistance (Arbeitslosengeld II) pays a flat benefit to individuals at risk of poverty, which could provide an alternative to DI benefits for some workers. Other transfer programs, including unemployment, sickness, and accident insurance, have a maximum benefit duration of up to 2 years, and thus cannot substitute DI for permanently disabled workers. Since a large welfare reform in 2005, social assistance benefits have been relatively low; for instance, the average beneficiary received EUR 469 per month in 2015. Social assistance is also subject to a strict means test at the household level: households owning any assets worth more than EUR 10k are ineligible, and transfers are withdrawn at a rate of 80% for household income exceeding EUR 100 per month. Moreover, benefit receipt requires actively searching for a job. Thus, social assistance is unlikely to be a meaningful substitute for DI for most workers, except perhaps for those in very low-income, low-asset households. We return to this discussion in Sections 3.2 and 4.2, where we show that the availability of social assistance cannot explain much of our results.

⁹Note that we calculate disability risk among cohorts 1960 and older, who are observed under full public DI coverage, including own-occupation DI. Thus, our risk measure is not confounded by endogenous claiming responses to the 2001 reform (see also Section 5).

2.2. Comparison to Other Countries

To assess the external validity of our analysis, it is useful to understand to what extent the German setting resembles DI provision in other countries. In Supplemental Appendix E, we present a detailed survey of public DI systems and private DI markets in selected OECD countries, including Austria, Canada, Denmark, France, Norway, the Netherlands, Spain, the U.K., and the U.S.

Overall, DI in Germany shares many key characteristics with DI in other settings. Across all countries included in our survey, public DI is a mandatory social security program for private-sector employees, and benefits are paid in case of a long-term disability that substantially reduces an individual's work or earnings capacity. Like in Germany, public DI benefits are a function of prior contributions in most countries, while lump-sum benefits are less common. Replacement rates vary, with Germany being at the lower end of public DI generosity. Nowadays, most public DI systems focus only on providing general DI, requiring claimants to be unable to work in any occupation. Interestingly, the evolution of public DI in several countries (e.g., Canada, the Netherlands, and the U.K.) closely mirrors the German setting, where own-occupation coverage was removed from public DI through reforms aimed at curbing public expenditure. In some cases, such as Austria and Spain, a subset of workers still qualify for own-occupation DI.

Furthermore, the structure of private DI markets in other countries is largely similar to Germany. In all countries we surveyed, there are individual private DI markets; although in a few cases (e.g., Denmark and the U.S.), private DI is predominantly sold as group insurance. Insurers offer own-occupation DI in all countries. Sometimes, workers can choose between own-occupation and general DI. As in Germany, private DI benefits can be set individually, and public and private DI payouts are independent in most countries. Private DI markets differ substantially in size: overall take-up varies between 4% in Austria and 85% in Denmark. Interestingly, private DI markets tend to be larger in countries with less generous public DI, which may be indicative of the type of crowding-out effects we study in Section 3.

2.3. Data

An important challenge in studying private DI is that comprehensive, high-quality data on private insurance take-up and contract characteristics is not readily available. We tackle this challenge by combining a number of data sources.

Private Insurer Microdata. First, we obtained a unique data set on all private DI contracts issued by a large insurance company (Anonymous Firm (2019)). The insurer is among the top 10 in the private DI market, with a market share between 3% and 6%. ¹¹ We observe contracts existing in any of the years between 2012 and 2017, irrespective of their start date. The data contains information on key contract characteristics and some limited sociodemographic information. Unfortunately, individual income and education are not included in the microdata. We thus match it with information on average income by occupation, age, and gender from the German Structure of Earnings Survey (Destatis

¹⁰An exception is given by the U.S. and Canada, where private DI providers are secondary payers and require claimants to apply for public DI. In Denmark, public DI benefits are means-tested against private DI payouts.

¹¹For confidentiality reasons, we cannot name the insurer or specify its market share more precisely.

(2019b)). Similarly, we add information on education from our administrative data. Appendix Table A2 shows summary statistics of the insurer microdata. Our main sample, which excludes contracts held by self-employed and civil servants, contains a high six-digit number of contracts. With an average purchase age of 31 and an end age of 61, private DI contracts tend to cover the bulk of individuals working lives. 60% of contract holders are male, average monthly premiums are EUR 86, and insured monthly benefits are EUR 1494, corresponding to a 35% replacement rate. 54% of contracts were sold as a stand-alone product.

An important question for the validity of our results is how representative the insurer providing our microdata is for the overall private DI market. We show that the insurer reflects the market well in many key dimensions. First, as we discussed above, private DI contracts are similar across providers regarding their primary features. Second, the pricing of private DI contracts follows common industry practice, assigning individuals to risk groups primarily based on occupations. As we show in Section 4.3, this results in similar relative prices across risk groups charged by different providers. Third, our insurer offers private DI to individuals in all occupations and industries. Thus, we observe private DI contracts of workers in 322 out of 334 3-digit occupations in the microdata. Fourth, the insurer has a countrywide presence and does not appear to specialize in particular geographic areas. In web-scraped data, we find that the insurer has local agencies across all states and in all major cities, as well as in many rural locations across the country. 93% of the German population has a local agency of the insurer in their county of residence or the neighboring county, and the remainder has access to its products via independent brokers or online. In addition, we present quantitative validation checks of our main results using independent, representative data sources in Section 4.3, which yield similar empirical patterns to the insurer microdata.

Administrative Data. Our second main data source is administrative data on the universe of public DI claims between 1992 and 2014 provided by the German State Pension Fund (FDZ-RV (2015)). This data contains information on the timing and type of DI claims, benefit amounts, individual earnings histories, and some sociodemographics such as age, marital status, and gender. Appendix Table A3 shows summary statistics of the administrative data. 59% of all DI claimants are male, and the average claiming age is around 52. Monthly DI benefits are EUR 1075 on average. Claimants' monthly earnings were EUR 2295 over all periods and EUR 1306 in the year before claiming. Compared to all DI cases, own-occupation DI claimants are more likely to be male and married, and their age and income tend to be slightly higher.

Other Data Sources. As an additional source of information on private DI, we obtained aggregate data on the entire private DI market from a leading rating agency (Morgen & Morgen (2021)). The agency rates insurance companies and collects data from all private insurers for this purpose. This data, on which we draw mainly for the aggregate patterns shown in Sections 3 and 4, contains time-series information on the total number of private DI contracts and a breakdown by contract type, risk group, and age group.

We also use data from the Income and Expenditure Survey (EVS), a representative household survey conducted by the German Federal Statistical Office (Destatis

¹²See Seitz (2021) for details of the insurer microdata and the matching procedure.

¹³The data on public DI claims is a subset of administrative data on all public pension claims first used by Seibold (2021). We also use the full data set on all pension claims to calculate some aggregate statistics, such as the distribution of occupations, risk groups, income and education.

(2019a)). We focus on the 2013 survey wave, which contains information on households' private DI take-up. We use this data for complementary analyses, particularly for the validation exercises presented in Section 4.3. Appendix Table A4 shows summary statistics of the survey data. 31% of households had private DI in 2013. Households' average labor income is EUR 2185 per month, and the average age of the main earner is 44. 59% of main earners are male, and the average household size is just above two.

3. CROWDING-OUT BETWEEN PUBLIC AND PRIVATE DI

The 2001 reform removes public own-occupation DI for younger birth cohorts. Affected individuals could compensate for this by purchasing private DI, which covers this risk. In this section, we study the effect of the reform on overall private DI take-up. We refer to the response of private insurance take-up to public DI cuts as a crowding-out effect, analogously to social insurance expansions studied in the literature (e.g., Cutler and Gruber (1996), Brown and Finkelstein (2008)).

3.1. Overall Private DI Take-up

We begin by showing aggregate patterns in public DI claims and private DI take-up in Figure 1. Panel (a) depicts the total number of public own-occupation DI claims per month in our administrative data. Precisely at the time of the reform, there is a sharp drop in claims, reflecting that younger cohorts affected by the reform immediately lose access to public own-occupation DI. Moreover, the figure indicates a continuing downward trend in claims over the years after the reform, as the share of workers in the older cohorts who are still eligible for own-occupation DI keeps declining. There is also some retiming of claims in the months just before the reform. Even though the spike just before January 2001 is sharp, the magnitude of these excess claims is small relative to the permanent reduction in claims after the reform.

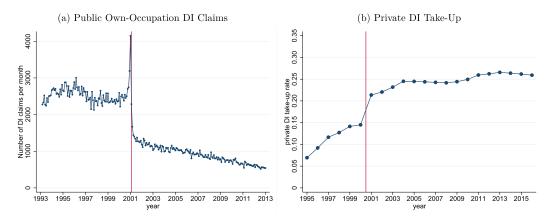


FIGURE 1.—Crowding-Out: Descriptive Evidence. Notes: Panel (a) of the figure shows the number of monthly public own-occupation DI claims. Panel (b) shows the overall private DI take-up rate, that is, the fraction of workers covered by private DI, by year. In both panels, the vertical line demarcates the 2001 reform.

¹⁴In addition, we use a number of auxiliary data sets. See Supplemental Appendix C for a complete list of all data sources.

Panel (b) of Figure 1 shows overall private DI take-up over time. We calculate the take-up rate as the number of contracts in the entire market from the rating agency data, divided by the total number of individuals contributing to social insurance from official statistics. The figure shows a clear jump in private DI take-up around the time of the reform. By 2015, 26% of workers have private DI, compared to below 10% before the first reform announcement in 1997. The substantial growth of the private DI market provides first, suggestive evidence of crowding-out between public and private DI. Yet, the modest level of private DI take-up 15 years after the reform indicates that this crowding-out is far from complete.

3.2. Difference-in-Difference Estimation

The evidence above suggests a crowding-out effect of the 2001 reform, but overall growth in the private DI market could be due to general trends in insurance demand or other factors. To isolate a causal effect, we follow a difference-in-difference strategy exploiting the cohort cutoff of the reform. We run regressions of the following form:

$$Y_{ct} = \beta_0 + \beta_1 treat_c + \beta_2 treat_c \cdot post_t + \delta_t + \epsilon_{ct}, \tag{1}$$

where Y_{ct} denotes an outcome of cohort c in month t, $treat_c$ is an indicator for treated cohorts 1961 and younger, $post_t$ is an indicator for post-reform periods January 2001 and later, δ_t is a month-by-year fixed effect, and ϵ_{ct} is an error term. The coefficient β_2 yields the difference-in-difference effect of interest. In the baseline specification, we focus on a narrow cohort window around the reform cutoff, comparing treated cohorts 1961–1962 to control cohorts 1959–1960.

Figure 2 illustrates our difference-in-difference results. In order to ease visual interpretation, the figure depicts graphical patterns at yearly frequency, while estimation results at monthly frequency are shown in Table II. We begin by investigating the effect of the reform on public own-occupation DI claims in Panel (a) of Figure 2. Before 2001,

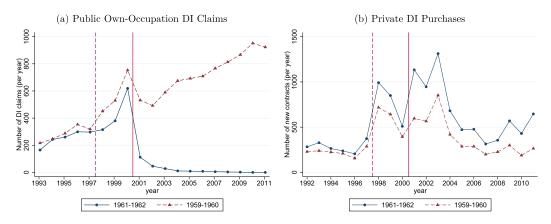


FIGURE 2.—Crowding-Out: Difference-in-Differences. Notes: The figure shows the number of public own-occupation DI claims (Panel a) and private DI purchases (Panel b) of individuals born in 1961–1962 (treated cohorts) versus 1959–1960 (control cohorts) at yearly frequency. In both panels, the dashed vertical line demarcates the time when the reform was first announced (December 1997), and the solid vertical line demarcates the time when the reform took effect (January 2001). See Table II for corresponding difference-in-difference estimates at monthly frequency.

	(1)	(2)	(2)	(4)	(5)	
	(1) (2) Public DI Claims		(3) (4) (5) Private DI Contracts			
	Own-Occupation All Public		Number of Purchases		Insured Benefits	
	DI Claims	DI Claims	All Contracts	Stand-Alone	(All Contracts)	
$\overline{\text{Treated} \times \text{post}}$	-53.37 (1.677)	-116.3 (5.734)	15.11 (2.739)	13.22 (1.676)	-462.2 (384.1)	
Observations	480	480	480	480	480	
R-squared	0.929	0.993	0.939	0.939	0.926	
Mean (pre-reform)	51.60	514.7	23.49	6.639	10,236	
Month-by-year FE	yes	yes	yes	yes	yes	

TABLE II Crowding-out: Difference-in-differences.

Note: The table shows results from the main difference-in-difference estimation described by equation (1). Outcomes are indicated by the respective column titles. Regressions are run at the level of cohort \times month cells. Prereform means are calculated in the year 2000 for columns (1) and (2), and in the years 1992 to 1997 for columns (3) to (5). Robust standard errors are in parentheses.

claims by treated and control cohorts follow a similar increasing trend. In 2001, there is a sharp differential drop in claims by treated cohorts virtually to zero, while claims by the control group continue to increase. Column (1) of Table II shows a highly significant difference-in-difference coefficient of -53.4, corresponding roughly to the number of monthly claims by treated cohorts just before the reform. As expected, this result confirms that the 2001 reform immediately and completely removes public own-occupation DI coverage for younger workers. In addition, column (2) of the table shows that the reform does not lead to an increased propensity to claim the other tier of public DI. The estimated effect on *any* type of public DI claims is in fact larger than the effect on own-occupation DI claims. This lack of benefit substitution towards general DI suggests that the disability screening process is able to distinguish between the two types of disability.

Next, the main outcome of interest is the number of private DI purchases. To analyze these, we turn to the insurer microdata, where we can observe individual characteristics. Panel (b) of Figure 2 depicts the number of private DI purchases by cohorts 1961–1962 versus 1959–1960 over time. Before the first announcement of the reform demarcated by the dashed vertical line, purchases by treated and control cohorts follow a very similar trend. After the announcement, there is an increase in private DI purchases by both groups. This is consistent with the initial reform proposal affecting all cohorts. However, a clear differential increase in purchases by the treated cohorts occurs when the reform is implemented in 2001. The impact on private DI purchases peaks in the third year post-reform and persists until the end of our sample period. Column (3) of Table II presents the

¹⁵Claims by the treated cohorts do not drop precisely to zero in 2001 due to delays in processing claims made before the reform.

¹⁶If anything, the estimate in column (2) would imply that general DI claims also decreased among treated cohorts. Potential reasons for such a negative spillover may include confusion about the reform or a general deterrence effect.

¹⁷Interestingly, older workers born before 1961 also seem to purchase more private DI contracts after 2001. This could be due to other reform elements affecting all cohorts. Moreover, increased marketing and sales efforts by insurers may not perfectly distinguish between treated and control cohorts around the cutoff. In the presence of such positive spillovers on the control group, our difference-in-difference would yield a lower bound on crowding-out effects.

estimated effect on monthly private DI purchases, pooling over the post-reform period. The coefficient of 15.1 is highly significant and corresponds to a 64% increase relative to prereform purchases. Column (4) shows that the effect is almost exclusively driven by newly purchased stand-alone DI contracts. This suggests that individuals specifically buy additional DI contracts after the reform rather than bundling DI with other insurance types. Finally, column (5) shows the estimated effect on the amount of benefits insured in new private DI contracts. We find no significant effect along this "intensive margin" of private DI. This motivates our focus on the extensive margin given by private DI take-up throughout the paper.¹⁸

Our baseline difference-in-difference estimation focuses on a narrow cohort window around the reform cutoff. This has the advantage of comparing relatively similar treated and control cohorts over time. However, this strategy likely leads to conservative estimates due to the age composition of the treatment group. Cohorts 1961–1962 are 39 to 40 years old at the time of the reform, while most individuals purchase private DI at younger ages. In the full sample, the average purchase age is around 31 (see Appendix Table A2). We repeat the difference-in-difference estimation for a broader set of cohorts to assess how the reform affects younger workers. Figure 3 shows estimated coefficients by cohort, where we replace the treated group in equation (1) by the respective cohorts denoted on the horizontal axis. Two main results emerge from the figure. First, the reform effect appears to be strongly increasing among younger cohorts. For instance, workers aged 29 to 30 at the time of the reform (cohorts 1971 to 1972) exhibit a roughly five times larger increase in the number of private DI purchases than the baseline treatment group. Second, the figure shows small differences in private DI purchases between cohorts born before

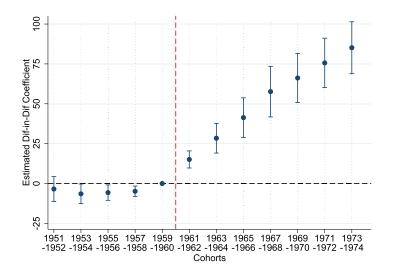


FIGURE 3.—Difference-in-Difference Effects by Cohort. Notes: The figure shows difference-in-difference estimates of the effect of the 2001 reform on private DI purchases for a range of cohorts. The estimates correspond to coefficient β_2 from equation (1), where the respective treatment group is given by the cohorts reported on the horizontal axis. Point estimates are shown along with 95% confidence intervals. The vertical line denotes the cohort cutoff of the 2001 reform, such that the cohorts to the right of the line are affected by the reform.

¹⁸In addition, Appendix Figure A1 presents graphical results corresponding to columns (2), (4), and (5) of Table II. Appendix Table A5 shows that our difference-in-difference results remain robust under various alternative specifications, including cohort-specific linear trends and a range of timing assumptions.

the reform cutoff. Only our baseline control group exhibits a very small increase relative to older cohorts, but there are no differential trends in insurance purchases between cohorts further below the cutoff.

Quantifying Crowding-out. Our difference-in-difference analysis reveals a significant impact of the 2001 reform on private DI purchases. To understand how this maps into crowding-out effects on the level of private DI take-up, we can perform a simple back-of-the-envelope calculation. We compute the predicted number of contracts held by cohorts 1961–1962 in 2015 based on pre-reform mean purchases and add the cumulative causal impact over the post-reform period implied by our estimates. This results in a 26% increase in the stock of private DI contracts held by the baseline treatment group who were treated at ages 39 to 40. Performing a similar calculation among the full set of treated cohorts from Figure 3 suggests a substantially larger rise in average private DI take-up by 194%. Applying this estimate to the pre-reform take-up rate from Figure 1 yields a crowding-out effect of 18 percentage points, similar to the observed increase in overall take-up. This implies that much of the growth of the private market can be attributed to a causal effect of the reform, while confirming that the magnitude of crowding-out between public and private DI is modest.

Alternative Strategy: Regression Discontinuity Design. As an alternative empirical strategy, the cohort cutoff of the reform could be exploited to implement a regression discontinuity design (RDD). Our difference-in-difference strategy has the advantage of providing higher statistical power, particularly for subgroup analyses. Nevertheless, Appendix Figure A2 shows that an RDD would yield results similar to our main specification. The figure depicts a sharp jump in the number of private DI contracts held by individuals precisely at the January 1961 cutoff. The RDD estimate is highly significant and corresponds to an increase of 25% relative to average take-up among control cohorts. This is almost perfectly in line with the 26% increase in the stock of private DI contracts implied by our baseline difference-in-difference result.

The Welfare Reform of 2005. As we explained in Section 2.1, another important safety net reform occurred in 2005. The reform made social assistance substantially less generous, replacing the prior income-dependent welfare system with a lower, flat benefit. Moreover, strict means testing was introduced, and benefit receipt was made conditional on active job search (see, e.g., Bradley and Kuegler (2019)). For our purposes, the 2005 reform presents a valuable opportunity to test the potential role of social assistance in determining private DI take-up. If social assistance served as a substitute for private DI, one might expect private DI take-up to increase after 2005, when benefit levels were reduced and many workers became ineligible for social assistance. However, Figure 1 suggests that much of the growth in private DI take-up occurs right around 2001, with no further change after 2005. Similarly, Figure 2 provides no indication that treated cohorts increase private DI purchases after 2005. To test this more formally, Appendix Table A5 performs a difference-in-difference estimation around the 2005 reform, resulting in a small and insignificant effect on private DI purchases. This suggests that the generosity of social assistance is not a major driver of private DI take-up.

4. HETEROGENEITY IN PRIVATE DI TAKE-UP

In this section, we study which types of individuals take up private DI. The main challenge in doing so is that comprehensive microdata on the overall private DI market is not

available. This challenge is faced by much of the literature investigating private insurance markets, which often uses data from a specific insurer or employer (e.g., Finkelstein and Poterba (2004, 2014), Einav, Finkelstein, and Cullen (2010), Autor, Duggan, and Gruber (2014), Cabral and Cullen (2019)). We follow a similar approach and resort to the insurer microdata. Supplemental Appendix B.1 describes in detail how we use this data in combination with administrative data and official social insurance statistics to calculate private DI take-up of subgroups. Importantly, our approach requires the assumption that the market share of the insurer is constant across subgroups (within contract type and year). This assumption is not innocuous and its validity hinges on how representative the insurer is for the overall market. In Section 2.3, we argued that the insurer reflects the market well in terms of contract design, pricing, occupational coverage, and geographic coverage. Moreover, we present comprehensive validation checks of the resulting take-up rates using representative household survey data and other independent data sources in Section 4.3.

4.1. Private DI Take-up Across Groups

In Figure 4, we begin by providing descriptive evidence on heterogeneity in private DI take-up in 2015. Panel (a) displays a strong positive correlation between private DI take-up and income. In the top income quintile, almost two-thirds (65%) of individuals have private DI. Private DI take-up is 30% in the fourth quintile, 11% to 12% in the second and third quintiles, and only 7% in the bottom quintile. Panel (b) shows a similar gradient of private DI take-up by education. 80% of individuals in the highest education quintile have private DI, while take-up is 26% in the fourth quintile and only 5% to 8% in the bottom three quintiles.

Panel (c) depicts private DI take-up by type of occupation. We use the task-based classification by Dengler, Matthes, and Paulus (2014) who adapt the method of Autor, Levy, and Murnane (2003) and distinguish between cognitive (analytical or interactive) versus manual tasks and routine versus nonroutine tasks. With 77% and 45%, respectively, workers in occupations performing analytical or interactive nonroutine tasks display the highest private DI take-up rates. In cognitive routine occupations, 20% of individuals have private DI, while take-up in manual occupations is only 8%.

Panel (d) finally investigates private DI take-up by risk group. Recall that the insurer assigns individuals to one of five risk groups based on occupations, and these risk groups are the primary determinant of private DI premiums. We find that lower-risk workers facing lower insurance premiums are much more likely to purchase private DI. In the lowest-risk groups 1 and 2, 58% and 56% of individuals have private DI, respectively. Among risk group 3, private DI take-up is 20%, and only 7% to 8% of individuals in risk groups 4 and 5 have private DI.

Heterogeneous Impact of the 2001 Reform. To understand how the 2001 reform affects private DI take-up across groups, we provide two additional pieces of evidence. First, Appendix Figure A3 shows private DI take-up rates before the reform (in 1997). Differences in take-up before the reform are qualitatively similar to Figure 4, but much less pronounced. For instance, 17% to 18% of individuals in the top two income quintiles have private DI, compared to 6% to 9% in the bottom three quintiles. Second, Appendix Figure A4 shows results from a causal analysis estimating heterogeneous effects of the 2001 reform. For this purpose, we repeat the difference-in-difference estimation from equation (1) separately for each subgroup. To increase statistical power, we extend the

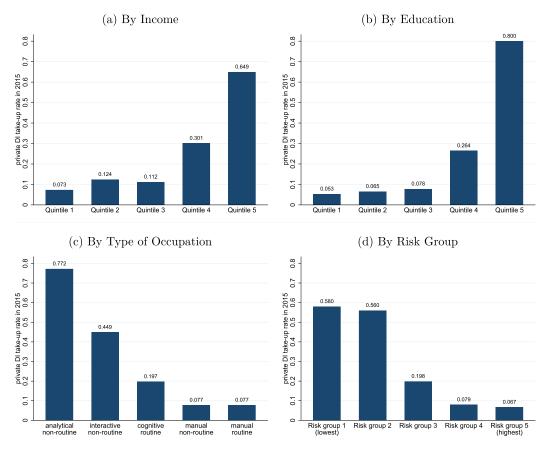


FIGURE 4.—*Private DI Take-Up across Groups. Notes*: The figure shows private DI take-up rates in 2015 by income quintile (panel a), education quintile (panel b), type of occupation (panel c), and risk group (panel d). In panel (b), education is defined as years of schooling. In panel (c), we use the task-based classification by Dengler, Matthes, and Paulus (2014) to group occupations. Take-up rates are calculated among all cohorts; see Supplemental Appendix B.1 for details.

cohort window used in the estimation to 1957–1964. The relative effects by subgroup are very similar to the descriptive patterns from Figure 4. For instance, we estimate that the impact on private DI purchases of the top income quintile is about double that for the fourth quintile, while effects for the bottom three quintiles are very small. The impact of the reform on take-up also strongly increases with education and nonroutine occupations, but decreases with risk groups. These results suggest that the causal impact of the 2001 reform by subgroup is closely in line with the observed post-reform heterogeneity in private DI take-up. ¹⁹

Multivariate Heterogeneity. Our main heterogeneity analysis shows that private DI take-up exhibits strong unconditional correlations with income, education, type of oc-

¹⁹In addition, Appendix Table A2 shows summary statistics of private DI contracts by time of purchase. Characteristics of pre- versus post-reform buyers align with the heterogeneity analysis presented here. Individuals who took up private DI between the first reform announcement and its final implementation (1998 to 2000) display similar characteristics to prereform buyers more broadly.

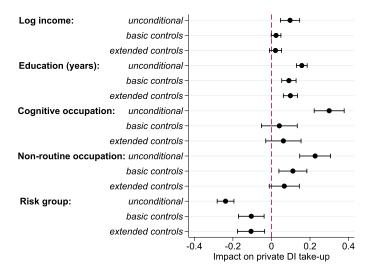


FIGURE 5.—Determinants of Private DI Take-Up. Notes: The figure displays results from regressions of private DI take-up rates on individual characteristics at the three-digit occupation level. The coefficients show the estimated impact of the respective variable with 95% confidence intervals. "Basic controls" are the set of characteristics from the figure, that is, log income, education (years), indicators for cognitive and non-routine occupations, and risk groups. "Extended controls" include these variables plus gender, marital status, an indicator for economic training and residence in East Germany. See Appendix Table A7 for full regression results.

cupation, and priced risk groups. To further unpack this heterogeneity, Figure 5 displays results from regressions of private DI take-up on these characteristics, controlling for varying sets of individual and occupational characteristics. One key result from these multivariate specifications is that income is not a significant determinant of private DI take-up once education and other characteristics are controlled for. Thus, while the unconditional take-up gradient by income is important for distributional considerations (see Section 7.2), income per se does not seem to drive heterogeneous private DI demand. On the contrary, Figure 5 shows that private DI take-up remains significantly correlated with education, risk groups, and working in a nonroutine occupation in all specifications.

4.2. Private DI Take-up, Disability Risk, and Risk Protection Benefit

Both descriptive patterns and difference-in-difference results suggest that private DI take-up *decreases* with risk groups. This raises a potential puzzle, as, in principle, one would expect higher-risk individuals to place a higher valuation on insurance. Note that risk-rated premiums alone cannot explain this finding. Private DI premiums increase across risk groups in a manner not far from actuarially fair. Thus, while one may not necessarily expect private DI take-up to increase with risk groups, the pricing scheme cannot explain the decreasing pattern.²⁰ To explore what could explain low private DI take-up among high-risk workers, we calibrate a comprehensive measure of the potential insurance value of private DI. Our *risk protection benefit* measure takes into account a variety

²⁰This point is closely related to our test for risk-based selection in Section 5. Once we control for insurance prices, we find that the correlation between private DI take-up and disability risk becomes flat but does not turn positive, as one would expect under standard models of adverse selection.

of factors beyond lifetime disability risk, including heterogeneity in the timing and subrisk composition of disability events, other safety net programs, and consumption drops upon disability.

Building on existing approaches in the insurance literature, particularly Mitchell, Poterba, Warshawsky, and Brown (1999) and Finkelstein and McKnight (2008), we set out an expected lifetime utility framework in Supplemental Appendix B.3. In this framework, individuals face some risk of disability in each period, and they may qualify for public DI benefits or social assistance in case of disability. We use the model to calibrate the certainty equivalent utility gain that risk-averse individuals would derive from private DI. To perform the calibrations, we combine the information on dynamic disability risk paths, income, and private DI parameters contained in our various data sources, and we rely on a range of assumptions about consumption drops upon disability and the probability of receiving public DI benefits.²¹ In all specifications, individuals can receive basic social assistance if their income is sufficiently low. We initially assume that consumption losses and risk preferences are homogeneous across groups, but relax these assumptions later. Figure 6 displays the calibrated risk protection benefit by risk group under selected specifications, along with private DI take-up and lifetime disability risk. Full calibration results are shown in Appendix Table A8.

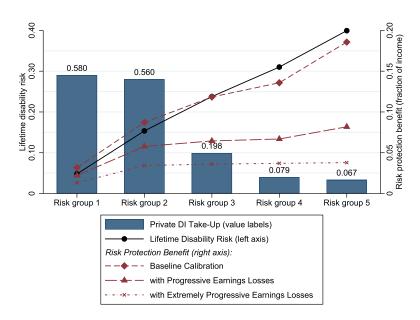


FIGURE 6.—Private DI Take-Up, Disability Risk, and Risk Protection Benefit. Notes: The figure shows private DI take-up rates, disability risk, and the risk protection benefit of private DI by risk group. The vertical bars depict private DI take-up rates for each group, calculated among all cohorts in 2015. The solid line shows lifetime disability risk by group. The dashed lines show the risk protection benefit of private DI as a fraction of income under three selected calibration scenarios, namely (i) under our baseline assumptions, (ii) in a scenario where income losses upon own-occupation disability increase somewhat progressively with income, and (iii) in a scenario with extremely progressive income losses. See Appendix Table A8 for detailed calibration results.

²¹Since no estimates of consumption losses upon disability are available in the German context, we rely on results from the U.S. by Meyer and Mok (2019) and results from Denmark by Humlum, Munch, and Plato (2025) in the calibration.

Under the baseline calibration scenario, which assumes a coefficient of relative risk aversion of three, we find that the expected utility gain from private DI increases monotonically from 3.2% of income for risk group 1 to 19% for risk group 5. These relative magnitudes are roughly aligned with the simple risk measure, which implies that taking into account full dynamic disability risk paths and the composition of claims does not substantially change the relative utility gain from private DI.²² In Appendix Table A8, the gradient of the risk protection benefit across groups remains similar under alternative assumptions about risk aversion, public DI rejections, and the size of consumption losses.

Next, the availability of other safety net programs has been shown to play a role for insurance choices, for example, in long-term care insurance (Braun, Kopecky, and Koreshkova (2019)). In our setting, two key programs could matter for private DI take-up. First, basic social assistance pays a flat benefit, which could provide some implicit insurance particularly for high-risk groups, given their lower average income (see Fischer, Geyer, and Ziebarth (2024)). In Figure 6, the calibrated risk protection benefit indeed increases less steeply than the simple risk measure for the highest risk groups 4 and 5, but this effect is quantitatively small. A limited role of social assistance is in line with the low implicit replacement rate of the program and with the evidence from Section 3.2, where we show that a large welfare reform hardly affects private DI take-up. Second, the availability of public DI benefits could influence private DI take-up. However, post-reform public DI only covers general disability risk and pays an approximately constant replacement rate to all groups. Thus, it is unlikely to induce differential private DI demand. This is confirmed by Appendix Table A8, where varying the probability of qualifying for public DI (rejection rates) hardly impacts the relative benefit of private DI across risk groups.

Our baseline calibration assumes that consumption losses upon disability are a constant percentage of income for all risk groups. However, the consequences of own-occupation disability may vary. In particular, low-risk occupations are more likely to perform cognitive nonroutine tasks, which tend to require specialized skills (see Dengler, Matthes, and Paulus (2014)). It is thus possible that workers in low-risk groups experience larger earnings losses if an own-occupation disability necessitates switching to a different occupation.²³ Unfortunately, we do not know of any existing estimates of heterogeneous consumption losses upon disability across occupations or risk groups. Hence, we consider two calibration scenarios to examine this channel. As a benchmark, we make the extreme assumption that in the event of own-occupation disability, all individuals are only able to work in a basic low-skill occupation where they earn the average bottom-quintile income. We also consider an intermediate scenario in between this extreme case and our baseline specification. Figure 6 shows that such "progressive" earnings losses can substantially modify the relative benefit of private DI. Under the intermediate scenario, the risk protection benefit increases less steeply with risk groups, and under the extreme scenario, it becomes virtually flat.

Finally, observed private DI take-up patterns could be explained by heterogeneous risk preferences. In particular, high-risk workers may have lower risk aversion. One potential reason behind a negative correlation between disability risk and risk aversion could be that workers select into more or less risky occupations based on their risk tolerance. To

²²Two key calibration inputs illustrate why this occurs. Appendix Figure A5 shows that the timing of disability events is similar across risk groups. Table I shows that, in addition to overall disability risk, the share of own-occupation claims also increases with risk groups.

²³This would be consistent with evidence from the literature on earnings losses upon job displacement. For instance, Huckfeldt (2022) documents particularly large losses for workers with specific human capital who find reemployment in a different occupation with lower skill requirements.

assess whether plausible variation in risk preferences could explain heterogeneous private DI take-up, we calibrate the degree of risk aversion that would make individuals indifferent between lifetime expected utility with and without private DI at market premiums. This yields an implied coefficient of relative risk aversion for the marginal buyer in each risk group. Details of the calibration are shown in Supplemental Appendix B.4, and results are displayed in Appendix Table A8. Across calibration scenarios with proportional consumption drops, the implied coefficient of risk aversion is between 1.09 and 4.96 for risk group 1 and between 0.66 and 2.87 for risk groups 4 and 5. Even when allowing for progressive earnings losses, implied risk aversion of higher-risk groups remains below that of risk group 1.²⁴ This suggests that lower risk aversion among high-risk groups could indeed explain their lack of private DI demand. Our risk aversion estimates for these groups are low but not implausibly far from results in the literature.²⁵

Implications for Welfare Analysis. Our baseline calibrations suggest that, given the size and structure of disability risk and the low level of social assistance in the German context, workers in high-risk groups should benefit substantially from private DI. However, low take-up among these workers could be explained by heterogeneous earnings losses upon own-occupation disability or by heterogeneous risk preferences. A key advantage of the revealed preference approach we follow later on is that the underlying reasons behind individual choices will not matter for the welfare implications, as long as observed private DI take-up reflects workers' true insurance valuations. Besides the factors discussed above, behavioral biases could be another potential reason for low insurance take-up among certain groups. Studying such biases is outside the scope of this paper. We briefly return to this discussion in our conclusion.

4.3. Validation Checks

Our empirical results on heterogeneity rely on the insurer microdata, as individuallevel data on the entire market is not available. As we discussed before, the validity of these findings depends on how representative the insurer is of the overall market. In this section, we present several validation checks using additional, independent data sources.

To begin with, overall private DI take-up in our data is very similar to estimates from other sources. A survey conducted by TNS Infratest (2015), a private survey company, finds that 26% of working adults had private DI in 2015, corresponding precisely to our main take-up rate estimate for the same year from Section 3.1. In the representative EVS survey data, overall private DI take-up by German households was 31% in 2013. Household-level take-up is naturally higher than our individual-level estimate since the average household has around two members (see Appendix Table A4).

Other data sources also suggest qualitatively similar private DI take-up patterns by subgroups. Appendix Figure A6 shows that take-up rates clearly increase with income in the household survey, albeit with a somewhat flatter gradient. We match take-up rates by gender well, considering that the survey figures are at the household level. To validate

²⁴Interestingly, calibrated risk aversion does not decrease monotonically with risk groups. In particular, risk aversion of the marginal buyer in group 5 tends to be higher than in groups 2 to 4. This likely occurs due to a combination of social assistance providing more sizable implicit insurance and relatively high private DI premiums charged to this group.

²⁵Studies on insurance choices typically yield estimates of relative risk aversion ranging between 1 and 8 (e.g., French (2005), Lockwood (2018), Jacobs (2023), Landais and Spinnewijn (2021)). Some work implies larger values (e.g., Cohen and Einav (2007), Sydnor (2010)).

private DI take-up rates by risk group, we use the rating agency data, which includes a breakdown by "harmonized" risk groups for the entire market. This information is based on insurers reporting the number of contracts in four risk groups defined by the rating agency. Harmonized groups correspond roughly to the risk groups used by the insurer providing our microdata, but the insurer additionally differentiates among the highest risks. Our main take-up estimates for the largest risk groups 2 and 3 are virtually the same as those from the rating agency data. For the lowest and highest-risk groups, the rating agency data displays even stronger heterogeneity in take-up than our main results.

Finally, as an additional piece of evidence, we present a comparison of private DI pricing by different insurers. For this exercise, we collect data on prices charged to the 10 most frequent occupations in each risk group for those of the top 10 insurers offering online price calculators. Appendix Figure A6 plots the average monthly premium by risk group for the insurer providing our microdata and four large competitors. Relative prices charged to different occupations are fairly similar across insurers. This suggests that different risk groups should have little reason to select specifically into the insurer providing our microdata, as its pricing reflects the overall market.

5. RISK-BASED SELECTION: POSITIVE CORRELATION TEST

A crucial question for the efficient functioning of private DI markets is whether and how individuals select into purchasing insurance based on their disability risk. Standard adverse selection models predict that high-risk individuals are more likely to purchase insurance, which can lead to underprovision of insurance or even complete market unraveling (Akerlof (1970), Rothschild and Stiglitz (1976)). To formally test for risk-based selection, we implement a *positive correlation test* (Chiappori and Salanié (2000)) in this section. Later, we provide additional evidence from a cost curve test (see Section 6.2).

Our aim is to test for a positive correlation between private DI take-up and disability risk, which would indicate adverse selection. Specifically, we run the following regression:

$$Q_{j} = \beta_{0} + \beta_{1}\pi_{j} + \sum_{k=2}^{5} \gamma^{k} \mathbb{1}(risk group_{j} = k) + \epsilon_{j},$$
(2)

where Q_j denotes private DI take-up of individuals in three-digit occupation j in 2015, π_j is lifetime disability risk measured in administrative data, and $\mathbb{1}(risk \ group_j = k)$ is an indicator for occupation j being assigned to risk group k by the insurer. Note that we define π_j as total risk (including both own-occupation DI and general DI top-up payouts), as this is the relevant risk measure from the perspective of insurer cost.

Our setting and data enable us to address two key challenges often faced by similar positive correlation tests in the literature. First, in assessing whether there is adverse selection, it is important to estimate the correlation between private DI take-up and risk within groups of individuals facing the same insurance prices. Indeed, we found a strong negative correlation between private DI take-up and risk groups in the previous section. Risk groups reflect an observed component of risk based on which insurance contracts are priced. In equation (2), we control flexibly for prices by including a set of risk group dummies, such that we can interpret β_1 as capturing selection on *unpriced risk*. Second,

 $^{^{26}}$ More precisely, we measure $risk\ group_j$ as the modal risk group in an occupation. Risk groups are not necessarily the same for all individuals within a three-digit occupation in the data because the insurer sometimes changes risk group assignment over time (see Section 6.2).

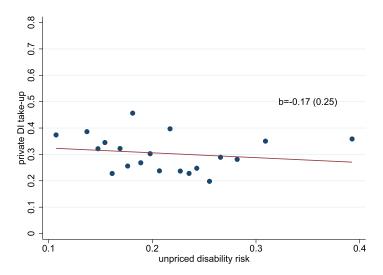


FIGURE 7.—Risk-Based Selection: Positive Correlation Test. Notes: The figure shows a binned scatterplot depicting the correlation between private DI take-up and residual (unpriced) disability risk, controlling for private DI premiums. We run the regression at the level of three-digit occupations. As explained in Section 5, take-up rates are calculated among treated cohorts in 2015, while disability risk is measured only among control cohorts. The figure also includes the estimated slope coefficient b with its standard error in parentheses. See Appendix Table A9 for details of the corresponding regression results.

a well-known difficulty with the positive correlation test is that ex post measures of risk based on observed insurance claims may confound selection on ex ante risk and moral hazard responses (see, e.g., Landais et al. 2021). A correlation of DI take-up and ex post claiming probabilities may be driven by certain risk types selecting into insurance (selection) or those with more insurance coverage becoming more likely to claim (moral hazard). To address this challenge and isolate risk-based selection, we calculate take-up among the treated cohorts 1961 and younger but measure disability risk π_j as the fraction claiming DI only among the control cohorts 1960 and older. This risk measure should not be confounded by moral hazard responses to differential take-up among treated cohorts since all individuals in the control cohorts are observed under full public DI coverage.

Figure 7 depicts the estimation results in a binned scatter plot. There is considerable residual unpriced variation in disability risk along the horizontal axis. Crucially, the estimated relationship between occupation-level private DI take-up and unpriced risk is quite flat, and the estimated slope coefficient corresponding to β_1 in equation (2) is small and statistically insignificant. In other words, we do not find any adverse selection from the point of view of the insurer: within priced risk groups, individuals with higher risk are no more likely to select into purchasing insurance. The point estimate on risk is negative, which would imply slightly advantageous selection into private DI, if anything.

At first glance, the lack of adverse selection may seem surprising, as insurance should in principle be more valuable to higher-risk individuals. However, some of the factors we discussed in Section 4.2 could explain this empirical finding. Evidence from other insurance markets points to heterogeneity in nonrisk related components of individual insurance valuations. If these correlate negatively with underlying risk, they can undo potential adverse selection (e.g., Finkelstein and McGarry 2006, Cutler, Finkelstein, and McGarry 2008). Our finding that high-income and highly educated individuals are more likely to purchase private DI could, for instance, reflect heterogeneous risk aversion or earnings

losses that are negatively correlated with risk. Appendix Table A9 presents further suggestive evidence along these lines by exploring how risk-based selection changes conditional on different sets of observables. In particular, we find that the coefficient turns positive (but remains insignificant) once we control for education. This suggests that not conditioning prices on education induces some advantageous selection, countering potential adverse selection within risk groups. Hence, even though it is somewhat coarse, the pricing scheme devised by insurers seems to be an important factor in preventing adverse selection.²⁷

6. VALUE AND COST OF DI

6.1. Basic Conceptual Framework

Next, our aim is to quantify the value and cost of the DI coverage offered by the private market. These two are the main components entering our welfare analysis later on. Our conceptual approach builds on Einav, Finkelstein, and Cullen (2010), who show that in order to evaluate welfare in insurance markets, the key sufficient statistics are given by insurance demand and cost curves. Similar frameworks have been used in a number of social insurance settings (Hendren, Landais, and Spinnewijn (2021), Einav and Finkelstein (2023)).

We consider a population of heterogeneous individuals indexed by θ_i , where $F(\theta_i)$ denotes the distribution of types. Heterogeneity may include variation both in individual disability risk and in other factors influencing DI valuations, such as risk aversion. The first key component for our welfare analysis is demand for DI. Denote by $v(\theta_i)$ the utility of consumer i from DI, and by p_k the insurance premium charged to individuals in risk group k. In a private market with insurance choice, the individual purchases DI if their willingness to pay exceeds the premium, $v(\theta_i) \geq p_k$. Aggregate demand for private DI in group k can be written as

$$D_k(p_k) = \int \mathbb{1}(v(\theta) \ge p_k) dF_k(\theta) = \Pr_k(v(\theta_i) \ge p_k).$$

The second component we require is the cost of providing DI. We denote by $c(\theta_i)$ the expected cost of insuring individual *i*'s risk. The average cost at price p_k is

$$AC_k(p_k) = \frac{1}{D_k(p_k)} \int c(\theta) \mathbb{1}(v(\theta) \ge p_k) dF_k(\theta) = \mathbb{E}_k(c(\theta_i)|v(\theta_i) \ge p_k).$$

In addition, we can write marginal cost as $MC_k(p_k) = \mathbb{E}_k(c(\theta_i)|v(\theta_i) = p_k)$.

Before we proceed to the empirical implementation, three aspects are worth noting. First, we assume that individuals make a discrete choice whether to buy insurance, and we abstract from the choice of insured benefit amounts in private DI contracts. This assumption is motivated by our results from Section 3.2, which suggest that this extensive margin is the empirically relevant dimension of insurance choice. Second, our main analysis follows the literature regarding the cost of providing DI and abstracts from any other cost incurred by insurers. We discuss the potential role of administrative cost in Section 7.3. Third, since insurance prices depend on risk groups to which insurers assign individuals

²⁷In line with this argument, Bundorf, Levin, and Mahoney (2012) show that risk-rated premiums can improve efficiency by limiting risk-based selection into health insurance.

based on observable characteristics (occupations), we conduct the analysis separately for each risk group. In other words, the insurance demand and cost curves described above apply within risk groups where individuals vary only in unpriced characteristics.

6.2. Estimating Demand and Cost

Our post-reform setting with insurance choice provides a unique opportunity to implement a revealed preference approach and directly measure individual valuations of the DI coverage offered by the private market. In order to estimate private DI demand, we exploit discrete price changes due to periodic updates in insurers' "risk tables," which determine the mapping of occupations to risk groups. According to conversations with industry experts, such reclassifications typically occur when an insurer gains access to improved data or analysis tools, or they can be induced by competitive pressure. In our insurer microdata, 9.8% of occupations are reclassified into a different risk group per year. We exploit this price variation to implement an event study design, pooling reclassifications that occur in the post-reform period. We estimate the causal effect of price changes on private DI purchases, which we can translate into demand elasticities. We also analyze the effect on the probability of claiming DI benefits, which allows us to perform a *cost curve test* for risk-based selection complementing the positive correlation test from Section 5.

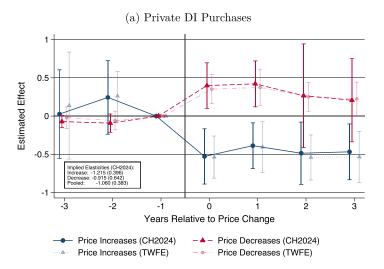
We set up a standard event study model, regressing outcome $Y_{j,t}$ of three-digit occupation j in year t on leads and lags of dummy variables indicating a price change due to reclassification. We consider both price increases (253 events between 2001 and 2015) and price decreases (272 events). When analyzing price decreases, we exclude occupations that experience a price increase from the sample, and vice versa; hence, we always use the same control group of never-treated occupations. We define an event window with three lags and three leads, and bin event indicators at the endpoints of the window, capturing average long-run impacts (Schmidheiny and Siegloch (2023)). Let $D_{j,t}$ be an indicator for a price increase or decrease as a result of reclassification. The empirical model is

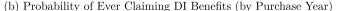
$$Y_{j,t} = \beta_{-3} \sum_{s=-\infty}^{-3} D_{j,t-s} + \sum_{\ell=-2}^{2} \beta_{\ell} D_{j,t-\ell} + \beta_{3} \sum_{s=3}^{\infty} D_{j,t-s} + \mu_{j} + \theta_{t} + \epsilon_{j,t},$$
(3)

where θ_t and μ_j are event-year and occupation fixed effects. Equation (3) specifies a two-way fixed effects (TWFE) model in a staggered-adoption design. This strategy requires two identification assumptions. The first is the standard parallel trends assumption: In the absence of the price change, average outcomes for treated and control occupations would have evolved similarly over time. The second identification assumption is that treatment effects are constant over time. Recent literature cautions against possible violations of this constant-effects assumption, which can lead to biased TWFE estimates. Hence, we use the heterogeneity-robust estimator by de Chaisemartin and D'Haultfoeuille (2020, 2024) as our baseline method and show standard TWFE estimates as additional results.

Figure 8 and Table III display results. Due to the discreteness of private DI pricing across risk groups, price changes implied by reclassifications are large: on average, prices change by 36.9%. Panel (a) of Figure 8 shows that yearly private DI purchases respond sharply and quite symmetrically to price increases and decreases. Pooling across all price

²⁸Note that these reclassifications only apply to new private DI contracts. Premiums charged to existing contracts are unaffected.





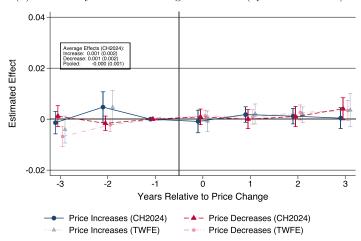


FIGURE 8.—Demand and Cost Estimation: Event Study Approach. Notes: The figure shows results from an event study around price changes due to occupation reclassifications. Panel (a) displays estimated dynamic effects on private DI purchases (relative to baseline purchases). Panel (b) shows the estimated impact on the probability of ever claiming DI benefits within the sample period, by year of purchase. In both panels, effects are shown separately for price increases and price decreases. In addition to the baseline estimates using the method by de Chaisemartin and D'Haultfoeuille (2024), we also show estimates from a standard two-way fixed effects (TWFE) specification in lighter color. Point estimates are displayed along with 95% confidence intervals for all specifications. In panel (a), the text box shows demand elasticities implied by the average effect on purchases for price increases, decreases, and pooling all price changes, with standard errors in parentheses. In panel (b), the text box shows average effects on claims, with standard errors in parentheses.

changes, the estimated impact on private DI demand is -39.3%, which implies a demand elasticity of -1.06. When estimated separately, the elasticity is -1.22 for price increases and -0.92 for price decreases, but the two estimates are statistically indistinguishable. Both de Chaisemartin and D'Haultfoeuille (2024) and TWFE estimators yield very similar point estimates. Furthermore, the figure displays only quantitatively small pretreat-

	(1)	(2)	(3)	(4)	(5)
	Pooled	Groups 1–2	Groups 2–3	Groups 3–4	Groups 4–5
dp/p	0.369	0.279	0.496	0.391	0.434
	(0.002)	(0.001)	(0.001)	(0.001)	(0.000)
dQ/Q	-0.393	-0.350	-0.444	-0.375	-1.246
	(0.065)	(0.029)	(0.034)	(0.046)	(0.485)
Elasticity	-1.060	$-1.25\acute{6}$	-0.895	-0.961	-2.873
	(0.174)	(0.104)	(0.069)	(0.117)	(1.117)
Observations	4022	1605	1988	2476	1423

TABLE III
DEMAND ELASTICITY ESTIMATION.

Note: The table displays results from our main demand elasticity estimation based on the event study approach. The first row shows the estimated change in private DI premiums upon occupation reclassifications. The second row displays the estimated response of private DI take-up. The third row shows implied demand elasticities. For each outcome, column (1) shows estimates pooling all risk groups, and columns (2) to (5) show results separately for each risk group pair. Standard errors based on the delta method are shown in parentheses.

ment trends in purchases under the de Chaisemartin and D'Haultfoeuille (2024) estimator, which suggests that differential trends in insurance demand across occupations do not drive reclassifications.

Columns (2) to (5) of Table III additionally report results separately by risk groups. For instance, the estimates in column (2) only use reclassifications from risk group 1 to risk group 2 or vice versa. Demand responses of different groups translate into relatively constant elasticities, even though the estimates are obtained across a wide range of baseline private DI take-up levels (except the larger but imprecisely estimate for risk groups 4 to 5). This pattern, which also arises under our alternative estimation strategy described below, motivates the assumption of a constant elasticity along the demand curve that we make later.

Next, we examine how private DI claims respond to price changes. Our outcome measure is the probability of ever claiming private DI benefits among individuals who purchased a contract in the event year. Note that this measure is not limited to claims during the time horizon of our event study itself, but takes into account all future claims occurring within our sample period. Panel (b) of Figure 8 depicts results. We find that despite the large observed demand response, there is no significant change in claims. The pooled point estimate is a precisely estimated zero effect, and we can exclude effects larger than 0.2 percentage points based on the confidence interval.²⁹ Separate estimates for price increases and decreases are also insignificant and close to zero. Again, we find no significant pretrends in claims, supporting the parallel trends assumption.

Estimating the effect on DI claims corresponds to the cost curve test for risk-based selection (Einav, Finkelstein, and Cullen (2010)). Intuitively, the impact of a price change on claims is informative about the cost associated with insuring marginal individuals induced to buy private DI compared to inframarginal buyers. Thus, the slope of the marginal cost curve can be derived from the estimated effect on claims. Our finding of a zero effect implies that the marginal cost curve is flat, that is, no significant risk-based

²⁹The point estimate for the third post-event year after price decreases, which is the binned endpoint capturing purchases three or more years after the event, is small and positive. Like the point estimate of our positive correlation test, this would suggest slightly advantageous selection, if anything.

selection. This result is consistent with the positive correlation test from Section 5, reinforcing our conclusion of no adverse selection in the private DI market.

Alternative Strategy: Quasidiscontinuity Approach. To complement these results, we implement a second demand estimation strategy, which relies on a different source of identifying price variation. Our alternative strategy directly exploits the discreteness in the pricing of private DI contracts, which creates jumps ("quasidiscontinuities") in premiums between risk groups. As we explain in detail in Supplemental Appendix B.2, this results in large price differences between some occupations with virtually identical underlying disability risk. Empirically observed changes in private DI take-up at the risk group boundaries can be interpreted as a response to local variation in insurance premiums. Results from this estimation strategy are shown in Appendix Table A10. The average price difference between adjacent risk groups is 42.0%, and the average conditional jump in private DI take-up corresponds to a 48.4% reduction in insurance demand. This implies an average demand elasticity of -1.11, which is reassuringly close to our estimate from the event study approach in Table III.

6.3. Constructing Demand and Cost Curves

Demand. We construct risk-group specific demand curves based on two empirical moments. First, their slope is pinned down by our demand elasticity estimates from above. Second, the level of demand is anchored by observed post-reform private DI take-up. We assume a constant elasticity of demand within risk groups, which is motivated by our elasticity estimates across different take-up levels.³⁰ For our main welfare analysis, we use the pooled elasticity estimate from the event study approach, but results remain very similar when considering group-specific elasticities instead.

We scale willingness to pay and prices in terms of expected insurance premiums paid by individuals and received by the insurer:

$$p_{i,k} = \sum_{t=0}^{T_i} (1 - \Pi_{k,t}) \tilde{p}_k \delta_t,$$
 (4)

where T_i is the contract end date relative to a start date normalized to zero, \tilde{p}_k is the per-period premium charged to risk group k, $\Pi_{k,t}$ is cumulative disability risk in period t, and $\delta_t = \frac{1}{(1+r)^t}$ is a discount factor. We use a discount rate of r=3%, and as before, we measure disability risk as the total claiming risk in the administrative data. Appendix Figure A5 displays empirical risk paths. As we know from Table I, lifetime disability risk increases strongly with risk groups. Risk paths by age evolve quite similarly across groups, with most DI claims occurring between ages 45 and 60. We calculate $p_{i,k}$ for each individual in the insurer microdata and take average expected premiums by risk group, $p_k = \mathbb{E}_k(p_{i,k})$. Thus, willingness to pay and the welfare measures described below are expressed in terms of certainty equivalents.

Cost. In an Einav, Finkelstein, and Cullen (2010)-type framework, the shape of cost curves is determined by the nature of risk-based selection. We found no significant risk-

³⁰Alternatively, the literature often assumes a linear demand curve (e.g., Einav, Finkelstein, and Cullen (2010), Landais et al. (2021)). In our case, demand responses estimated across different take-up levels suggest that a constant elasticity is a better approximation than a linear curve.

based selection in the positive correlation test and the cost curve test, implying a flat marginal cost curve. Moreover, as marginal costs are constant, marginal and average cost curves coincide.

We calculate the expected cost of providing the DI coverage offered by the private market to individual i in risk group k as

$$c_{i,k} = \sum_{t=0}^{T_i} \Pi_{k,t} b_i \delta_t, \tag{5}$$

where b_i is the level of insured benefits. Again, we calculate $c_{i,k}$ for each individual in the insurer microdata and then take the average expected cost within risk groups. Two additional features of our cost curves are worth noting. First, the cost estimates can be interpreted as inclusive of a fiscal externality due to moral hazard responses to insurance since our risk measure is based on ex post observed claims. Second, we assume that the cost of providing a given level of insurance coverage is the same across private and public DI systems.³¹

Results. Figure 9 plots empirical demand and cost curves by risk group. In each panel, the horizontal axis denotes the fraction of the group covered by private DI, ranging from zero to one. Demand curves rank individuals from high to low willingness to pay along the horizontal axis. Cost curves show the marginal/average cost associated with insuring the set of individuals willing to purchase insurance at a given price. In each panel, point A denotes empirically observed private DI take-up, and B denotes the intersection of demand and cost curves.³² In panel (a), the expected cost of insuring individuals in risk group 1 is low as this group faces the lowest disability risk. The estimated willingness to pay is above the cost at any level of take-up. Panel (b) shows corresponding results for risk group 2, for whom the cost is substantially higher. The demand curve also indicates a higher willingness to pay for DI, but demand and cost curves intersect at a take-up rate of 68%. Thus, willingness to pay is below cost for 32% of individuals. In panel (c), the cost of insuring risk group 3 is higher, while the demand curve is lower than that of risk group 2. In fact, willingness to pay is above cost for only 29% of individuals in risk group 3. Similarly, in panels (d) and (e), risk groups 4 and 5 are even costlier to insure, but the estimated willingness to pay is below cost for around 86% of individuals.

We further quantify estimated demand and cost in Appendix Table A11. We calculate both for a private DI contract insuring a 30% gross income replacement rate and scale magnitudes relative to income. Across all groups, median willingness to pay for the coverage offered by the private DI market is around 0.9% of income, and expected cost is 1.5% of income. In line with strongly varying disability risk, we estimate group-specific insurance costs between 0.3% of income in risk group 1 and 2.1% in risk group 5. In contrast, valuations do not increase with risk. Our estimates suggest a willingness to pay for private DI of 1.2% of income in risk group 1 and 1.5% in risk group 2, but only between 0.5%

³¹Unfortunately, the insurer microdata does not provide information on claims over a sufficiently long period to fully compare private and public DI claims. However, some aggregate calculations on private DI claiming risk are provided by the German Actuarial Society (DAV (2018)). Appendix Figure A5 includes private DI claiming risk from this source, calculated for a representative individual. There are some differences in the timing of claims, but overall disability risk is similar to observed public DI claims, suggesting that our assumption of equal cost is a good approximation.

 $^{^{32}}$ We use observed take-up only among treated cohorts to anchor the level of demand. Thus, empirical take-up denoted by points A is slightly higher than the rates shown in Figure 4.

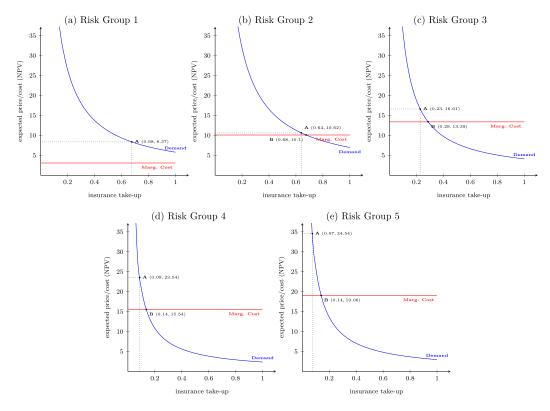


FIGURE 9.—Demand and Cost Curves. Notes: The figure presents private DI demand and cost curves estimated in Section 6.2. The horizontal axes display private DI take-up rates between zero and one, and the vertical axes show expected prices and cost as defined in equations (4) and (5). Each panel shows the demand curve and the marginal/average cost curve for the risk group indicated in the panel title. Point A denotes the private market equilibrium in each risk group, with associated insurance take-up and price in parentheses. Point B denotes the intersection of demand and marginal cost curves, with associated take-up and price in parentheses.

and 0.9% for risk groups 3 to 5. These quantitative results echo the large differences in observed private DI take-up across risk groups.

Conceptually, our analysis is closely related to Cabral and Cullen (2019), who use a similar framework to estimate workers' willingness to pay for supplemental private DI coverage at a U.S. firm. One key difference is that in their setting, private DI is a pure top-up insurance covering the same risk as public DI, whereas German private DI covers a different sub-risk since the 2001 reform. Yet, Cabral and Cullen (2019) find that workers are willing to pay 0.3% of annual earnings per 10% replacement rate, which is quite similar to our median private DI valuation estimate from above.

7. WELFARE EFFECTS OF PRIVATIZING DI

7.1. Baseline Welfare Calculations

Based on the estimated demand and cost curves, we can assess welfare in the private DI market. As our baseline welfare measure, we define the *net value* of DI as its value to

the insured relative to the cost to the insurer. Net value in the private market is

$$NV^{\text{priv}} = \frac{\sum_{k} n_{k} \left[\int v(\theta) \mathbb{1} \left(v(\theta) \ge p_{k} \right) dF_{k}(\theta) \right]}{\sum_{k} n_{k} \left[\int c(\theta) \mathbb{1} \left(v(\theta) \ge p_{k} \right) dF_{k}(\theta) \right]}, \tag{6}$$

where n_k denotes the size of risk group k. In the private market, the net value is given by the value to those who choose to purchase DI, that is, for whom $v(\theta) \ge p_k$, divided by the cost of providing DI to them. Since we estimate private DI valuations in the presence of baseline public DI coverage, NV^{priv} should be interpreted as the net value of the additional coverage offered by the private market.

Our main counterfactual of interest is the introduction of an insurance mandate providing the coverage offered by private DI to all workers.³³ Starting from the private market equilibrium, the net value of introducing the mandate is

$$\Delta NV^{\text{mand}} = \frac{\sum_{k} n_{k} \left[\int v(\theta) \mathbb{1} \left(v(\theta) < p_{k} \right) dF_{k}(\theta) \right]}{\sum_{k} n_{k} \left[\int c(\theta) \mathbb{1} \left(v(\theta) < p_{k} \right) dF_{k}(\theta) \right]}.$$
 (7)

Individuals with willingness to pay above the market price already purchased private DI when they had the choice. Thus, a mandate expands coverage to those individuals whose willingness to pay is below the price.

Based on this welfare measure, a reform is welfare-improving if its net value is greater than one; that is, it generates value exceeding its cost. For our counterfactual, $\Delta NV^{\rm mand} > 1$ would imply that mandating private DI coverage is welfare-improving. In contrast, $\Delta NV^{\rm mand} < 1$ would mean that leaving this coverage to the voluntary private market is preferable.

Our baseline welfare analysis follows Einav, Finkelstein, and Cullen (2010) and focuses on the direct value and cost of providing extra DI. However, various types of indirect effects could be associated with DI provision. To account for these as much as possible, we also calculate a marginal value of public funds (MVPF) measure (Hendren and Sprung-Keyser (2020), Finkelstein and Hendren (2020)). To do this, we augment equation (7) and include relevant fiscal externalities in the denominator.³⁴ As a first externality, mandating private DI coverage is likely to impose indirect moral hazard costs onto public DI, since top-up insurance in case the worker also qualifies for

³³While there might be alternative policies of interest, for example, mandating parts of private DI coverage, we focus on this counterfactual for two reasons. First, the fairest comparison is arguably between two policies providing the same insurance coverage, so it is natural to consider a mandate of actual private DI coverage. Second, our empirical estimates are directly related to this counterfactual since we quantify selection, insurance demand, and cost for the coverage provided by the private DI market. Thus, we consider a counterfactual based on actual private DI coverage the most empirically credible.

³⁴We continue using the entire estimated demand and cost curves when calculating the MVPF, as in equations (6) and (7). This is important because our counterfactual is a large reform moving insurance take-up to 100%, such that the approximation of willingness to pay based on the envelope theorem often used in MVPF calculations would not be appropriate.

public (general) DI benefits is included. To quantify this channel, we use the estimate of Seitz (2021), who finds that private DI increases public DI claims by 8.6%. Second, a fiscal externality may arise because additional DI claims entail reductions in labor supply, which in turn lower tax revenue. Unfortunately, empirical estimates of the labor supply effects of DI are not available in the German context, so we use an average of estimates from the literature. Third, covering all workers with private DI may reduce their propensity to claim social assistance if they become unable to work, implying a positive fiscal externality. Supplemental Appendix B.5 provides full details on how we calibrate each channel based on our data and estimates from the literature.

Welfare in the private DI market can be graphically illustrated using our estimated demand and cost curves. Panel (a) of Figure 10 depicts net value in the private DI market for the case of risk group 3. The total area under the demand curve up to equilibrium take-up corresponds to the numerator in equation (6), and the area under the marginal cost curve corresponds to the denominator. In addition, the figure shows a decomposition of willingness to pay into consumer surplus (area A), producer surplus (B), and cost (C). Appendix Figure A8 shows analogous graphs for all risk groups. Overall, the private DI market generates a large surplus, as individuals with the highest willingness to pay choose to purchase private DI. Consumer surplus is particularly sizable in risk groups 1 and 2, where individuals exhibit the highest insurance valuations. Producers receive the largest surplus from risk groups 1, 4, and 5, where markups over marginal cost are highest (see Section 7.3).

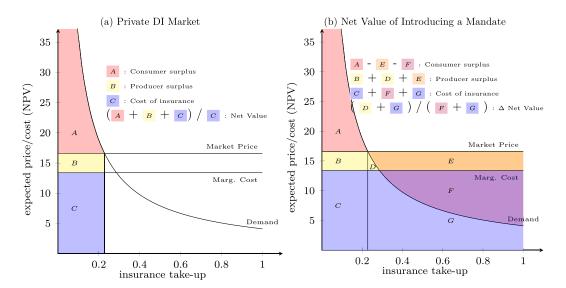


FIGURE 10.—Welfare Calculations. Notes: The figure illustrates our welfare calculations for the case of risk group 3. Panel (a) depicts welfare in the private DI market, where the net value is given by the total area under the demand curve (A+B+C) divided by the area under the cost curve (C). Panel (b) illustrates the net value of a reform mandating private DI coverage. The mandate increases DI take-up from the market equilibrium to 1. The net value of the reform is given by the additional area under the demand curve (D+G) divided by the additional cost (F+G). In both panels, the net value can be further decomposed, as explained in the respective legend. Appendix Figures A8 and A9 show corresponding graphs for all risk groups.

TABLE IV
WELFARE EFFECTS OF INSURANCE MANDATES.

	(1) (2) Private DI Mandate (Risk-Based Premiums)		(3) (4) Public DI Mandate (Income-Based Contributions)	
	Net Value	MVPF	Net Value	MVPF
Baseline value	0.705	0.617	0.705	0.617
Social value by risk aversion σ				
$\sigma = 1$	0.634	0.553	1.215	1.057
$\sigma = 2$	0.575	0.499	1.547	1.343
$\sigma = 3$	0.527	0.455	1.749	1.518
$\sigma = 5$	0.459	0.393	1.936	1.678
$\sigma = 8$	0.395	0.333	2.010	1.742

Note: The table shows the welfare effects of mandating the DI coverage offered by the private insurance market. Column (1) presents net value estimates for a private DI mandate and column (3) presents estimates for a full public DI mandate financed by income-based social insurance contributions. Columns (2) and (4) present marginal value of public funds (MVPF) estimates for the same mandates, taking into account fiscal externalities. The first row shows the baseline value calculated as in equation (7). The remaining rows show the social value calculated as in equations (8) and (9), using welfare weights from a Utilitarian social welfare function under different values of the coefficient of relative risk aversion σ .

Panel (b) of Figure 10 illustrates the welfare effects of a mandate, again for the case of risk group 3. Starting from the private market status quo, insuring all individuals entails additional costs given by the area under the cost curve between equilibrium take-up and mandated take-up of 100% (areas F+G). Expanding insurance yields additional value (D+G), but this is exceeded by additional premium payments (D+E+F+G), implying a net loss in consumer surplus. Insurers, on the other hand, gain surplus (D+E). Thus, the overall net value of the mandate is given by D+G over F+G, which is clearly below one. Appendix Figure A9 shows that the net value of a mandate is below one for all risk groups except group 1.

The first row of Table IV quantifies these welfare results. We find an overall net value of introducing a private DI mandate of 0.705. This implies that partial DI privatization, similar to the 2001 reform, is welfare-improving compared to a full public DI mandate. Similarly, we find an MVPF of a mandate of 0.617. This reflects that the joint effect of fiscal externalities increases the net cost of providing extra DI, reinforcing our conclusion that the private DI market is welfare-improving.³⁵

7.2. The Social Value of a DI Mandate

As an extension of the welfare analysis, we introduce distributional concerns. Recall that the private DI market disproportionately covers high-income and low-risk individuals. A mandate would thus extend coverage to more low-income and high-risk individuals, on whom a social planner concerned with equity would place particular weight. We write

³⁵As a point of comparison, Hendren and Sprung-Keyser (2020) report similar MVPF estimates for marginal reforms providing additional DI benefits between 0.74 and 0.96.

the social net value of introducing a mandate as

 $\Delta SNV^{\rm mand}$

$$= \frac{\sum_{k} n_{k} \left[\lambda_{k} \overbrace{\int (v(\theta) - p_{k}) \mathbb{1}(v(\theta) < p_{k}) dF_{k}(\theta)} + \overbrace{\int p_{k} \mathbb{1}(v(\theta) < p_{k}) dF_{k}(\theta)}^{\text{Insurer revenue}} \right]}{\sum_{k} n_{k} \left[\int c(\theta) \mathbb{1}(v(\theta) < p_{k}) dF_{k}(\theta) \right]}.$$
 (8)

The first term in the numerator captures the additional net utility individuals in risk group k derive under a mandate, corresponding to their valuation minus the price of extra DI. The change in consumer surplus among risk group k is multiplied by λ_k , the social welfare weight of individuals in this group. The second term in the numerator reflects additional revenue to the insurer. The social net value then relates the sum of these two terms to the additional cost of providing insurance.³⁶

Equation (8) considers a private insurance mandate where individuals are compelled to purchase private DI at market prices. However, in our setting, extra DI coverage was provided via the social insurance system before the 2001 reform, where individuals are mandated to participate and pay social insurance contributions. To evaluate such a public DI mandate, we have to consider that contributions can differ from risk-rated private DI premiums p_k . Formally, the social net value of a public DI mandate is given by

 $\Delta SNV^{\mathrm{pub}}$

$$= \left(\sum_{k} n_{k} \left\{ \lambda_{k} \left[\int \left(v(\theta) - p_{k} \right) \mathbb{1} \left(v(\theta) < p_{k} \right) dF_{k}(\theta) + \int \left(p_{k} - p_{k}^{\text{pub}} \right) dF_{k}(\theta) \right] \right. \\ + \left. \int p_{k}^{\text{pub}} \mathbb{1} \left(v(\theta) < p_{k} \right) dF_{k}(\theta) \right\} \right) / \left(\sum_{k} n_{k} \left[\int c(\theta) \mathbb{1} \left(v(\theta) < p_{k} \right) dF_{k}(\theta) \right] \right), \quad (9)$$

where p_k^{pub} denotes contributions paid by individuals in risk group k. Compared to equation (8), a public DI mandate thus entails an additional pricing effect entering consumer surplus. Specifically, we suppose that contributions are levied as a proportion of an individual's gross income, as is the case in our setting and other social insurance systems. We calculate the required contribution rate such that total contributions equal the cost of providing the extra coverage to all individuals.

In order to obtain welfare weights, we require a social welfare function. As is common in the literature, we assume Utilitarian social welfare, such that welfare weights are given by marginal utility from consumption. Moreover, we assume constant relative risk aversion utility. We calculate social welfare weights for each risk group based on expected lifetime income. Appendix Table A12 shows information on income and resulting social welfare weights by group. Expected income decreases monotonically with risk groups. On average, individuals in risk group 1 earn more than double the income of those in risk

³⁶Insurer revenue and cost carry a weight of one, corresponding to the average social welfare weight in the population.

group 5. We consider a range of values of the coefficient of relative risk aversion σ between 1 and 8, where a higher σ implies stronger equity concern, and thus larger welfare weights on higher-risk groups.

Results from the social net value calculations are shown in Table IV. Column (1) suggests that a private DI mandate would lower welfare under any degree of equity concern. Stronger equity concern decreases the social net value, indicating that a private DI mandate would be a regressive policy. As can be seen in Appendix Figure A9, forcing all individuals to purchase insurance at market prices entails larger reductions in consumer surplus among higher-risk groups, since they have to pay higher prices relative to a low willingness to pay. Column (3) shows the welfare effects of a public DI mandate with income-based contributions. In our baseline net value calculations shown in the first row of the table, the welfare impact of a public DI mandate is the same as that of a private DI mandate because the difference in pricing does not affect total surplus. However, in the presence of equity concerns, a public DI mandate improves welfare relative to the private market. Intuitively, the social insurance system with income-based contributions raises revenue from low-risk, high-income groups and redistributes towards high-risk, low-income groups by providing them with additional insurance at prices below risk-rated premiums. This redistribution is highly valued by the social planner. Even under low risk aversion of $\sigma = 1$, the social net value is already 1.215. As expected, the social net value rises with the degree of equity concern; for instance, it becomes 1.749 under $\sigma = 3$ and 2.010 under $\sigma = 8$.

We also calculate an analogous "social" MVPF measure. To this end, we augment equations (8) and (9) and include the various fiscal externalities described in Section 7.1. Table IV shows that the social MVPF is generally somewhat lower than the social net value. As before, this occurs because the joint effect of fiscal externalities increases net cost. However, our main welfare results remain similar: the social MVPF of a private DI mandate is far below one, whereas the social MVPF of a public DI mandate is between 1.057 and 1.742.

Extensions and Robustness. Appendix Table A13 shows results from three extensions to our welfare analysis. First, we separate the effects of the different types of indirect costs included in our MVPF calculations. As expected, moral hazard spillovers onto public DI and the fiscal externality due to reduced labor supply lower the value of a mandate, but the positive externality due to reduced social assistance claims increases its value. Second, we check whether our results are robust to relaxing the assumption of a constant demand elasticity across risk groups. We find that results are qualitatively unaffected when using the point estimates for each risk group instead. Third, we allow for some risk-based selection in the private DI market. To quantify the potential range of cost curve slopes, we use the 95% confidence interval around the claim effect from panel (b) of Figure 8. Converted into lifetime claiming probabilities, the confidence interval ranges from adverse selection with a 6.9% difference in costs between insured and uninsured individuals to advantageous selection with a -11.1% difference. Adverse selection somewhat increases the net value of a mandate, and advantageous selection somewhat decreases it, but again, results remain similar.

7.3. Supply-Side Factors: Market Power and Administrative Costs

Our welfare analysis relies on the sufficient-statistics framework by Einav, Finkelstein, and Cullen (2010), which takes insurance supply and the characteristics of insurance con-

tracts as given. Evidence from other insurance markets, in particular long-term care insurance, suggests that the supply side can matter for take-up and welfare (Braun, Kopecky, and Koreshkova (2019)). Key supply-side factors emphasized by prior literature include the degree of market power and the extent of administrative costs.

Several empirical observations suggest that both market power and administrative costs are less critical issues in our setting. First, the German private DI market is relatively competitive: the top 3 providers have a combined market share of 34.2%. This is substantially lower than in other markets, for example, Braun, Kopecky, and Koreshkova (2019) report a top-3 market share of 66% in U.S. long-term care insurance. Second, administrative costs are modest in German private DI. According to Fischer, Geyer, and Ziebarth (2024), fixed and variable administrative costs amount to 3% and 10% of premiums, respectively, compared to 20% and 13% in Braun, Kopecky, and Koreshkova (2019). Third, coverage denials, which can result from administrative costs, are infrequent in our setting. The overall denial rate is only 3% (see Section 2.1), versus 56% in U.S. long-term care insurance (Braun, Kopecky, and Koreshkova (2019)) and up to 64% in U.S. private DI (Hendren (2013)).

These empirical facts translate into modest insurance loads, a commonly used metric combining insurer profits and administrative costs.³⁷ Across all risk groups, we find an average load of 0.27, implying that insured individuals can expect to receive 73% of premiums in benefits. This is considerably lower than the average load of 0.42 reported in Braun, Kopecky, and Koreshkova (2019). Note that these loads are already implicitly incorporated in our main welfare analysis. Market power and administrative costs can lead to inefficiently low private DI take-up, which policy interventions aimed at increasing take-up such as a mandate can address. However, our welfare results imply empirical insurance loads are not sufficiently large to justify a mandate.

To shed more light on the role of administrative costs for private DI take-up and welfare, we nonetheless perform an additional counterfactual simulation building on Braun, Kopecky, and Koreshkova (2019) and Fischer, Geyer, and Ziebarth (2024). Some proponents of regulatory tools such as minimum benefit ratios argue that these could reduce administrative costs. In the counterfactual, we set administrative costs to zero and assume that this cost reduction is fully passed through to consumers. As it is unlikely that such an extreme reduction can be achieved in practice, we interpret the results from this simulation as an upper bound on the potential impact of administrative costs. Appendix Table A14 shows that the decrease in private DI premiums due to the removal of administrative costs leads to a modest rise in private DI take-up to 33%. The positive impact on consumer surplus and insurer profits exceeds the additional (direct) costs of providing DI, such that the net value of the counterfactual is 1.359, indicating an improvement in overall welfare. While these results are qualitatively unsurprising, they confirm that the impact of administrative costs is limited in our setting.

8. CONCLUSION

In this paper, we provide novel empirical evidence on the functioning of private DI markets. We document significant crowding-out after a reform that cut public DI coverage. Yet, private DI take-up remains far from complete, especially among low-income,

³⁷We follow Brown and Finkelstein (2008) and calculate insurance loads as $1 - (\mathbb{E}(c_{i,k})/\mathbb{E}(p_{i,k}))$, where $c_{i,k}$ are expected DI benefits (corresponding to the direct cost of providing insurance) from equation (5) and $p_{i,k}$ are expected insurance premium payments from equation (4).

low-educated, and high-risk individuals. Our welfare analysis highlights the policy implications of these findings. Our baseline welfare result is that leaving private DI coverage to the voluntary market is welfare-improving. This is closely related to our main empirical findings. First, we do not find adverse selection, which would lead to inefficiently low insurance take-up in the private market and which would be the canonical rationale for a mandate. Second, the value of extra DI coverage revealed by insurance choices is low for many individuals, especially in higher-risk groups, and our sizable demand elasticity estimates imply that insurance valuations decline fast among the uninsured. Third, market power and administrative costs are of insufficient magnitude to justify a mandate. In other words, the private DI market covers the majority of individuals whose willingness to pay is above marginal cost.

However, equity concerns can provide a rationale for including the DI coverage currently offered by the private market in the public DI mandate. For such a reform to improve social welfare, it is crucial to implement income-based contributions as in real-world social insurance systems. Such a mandate redistributes not only from high- to low-income groups but also from low- to high-risk groups. Importantly, this analysis takes the design of other tax and transfer schemes as given. If the government aims at redistributing across income levels, there are likely more efficient ways to achieve equity gains. Nevertheless, redistribution across disability risk types is a distinctive feature of public DI. It would be worthwhile for future research to explore these trade-offs further.

Throughout the welfare analysis, we follow the literature on mandates versus markets in social insurance settings and maintain the assumptions of the revealed preference approach (Einav, Finkelstein, and Cullen (2010), Finkelstein, Hendren, and Shepard (2019), Landais et al. (2021), Cabral, Cui, and Dworsky (2022)). Crucially, this includes the assumption that individuals make optimal private DI purchase decisions, such that observed demand reflects individuals' true insurance valuations. As discussed in Section 4.2, observed private DI take-up could be explained by several factors consistent with revealed preferences. However, if behavioral biases lead to inefficient underinsurance for some workers, this could potentially provide an alternative rationale for a mandate beyond the classic market failures considered by the revealed preference approach. Studying such biases is outside the scope of this paper, but this may be another area where future work is needed to inform policy.³⁸

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³⁸In an earlier version of this paper (Seibold, Seitz, and Siegloch (2022)), we considered behavioral biases as an alternative rationale for a mandate more explicitly. As it is difficult to directly quantify such biases in our data, we defer this topic to future work.

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The replication package for this paper is available at https://doi.org/10.5281/zenodo.15363634. The authors were granted an exemption to publish parts of their data because either access to these data is restricted or the authors do not have the right to republish them. However, the authors included in the package, on top of the codes and the parts of the data that are not subject to the exemption, a simulated or synthetic dataset that allows running the codes. The Journal checked the data and the codes for their ability to generate all tables and figures in the paper and approved online appendices. Whenever the available data allowed, the Journal also checked for their ability to reproduce the results. However, the synthetic/simulated data are not designed to produce the same results.