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On the Equivalence of Location Choice Models: Conditional Logit, Nested Logit and Poisson

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On the Equivalence of Location Choice Models: Conditional Logit, Nested Logit and Poisson

Abstract

It is well understood that the two most popular empirical models of location choice - conditional logit and Poisson - return identical coefficient estimates when the regressors are not individual specific. We show that these two models differ starkly in terms of their implied predictions. The conditional logit model represents a zero-sum world, in which one region's gain is the other regions' loss. In contrast, the Poisson model implies a positive-sum economy, in which one region's gain is no other region's loss. We also show that all intermediate cases can be represented as a nested logit model with a single outside option. The nested logit turns out to be a linear combination of the conditional logit and Poisson models. Conditional logit and Poisson elasticities mark the polar cases and can therefore serve as boundary values in applied research.

JEL Code: C25, R30, H73.

Keywords: firm location, residential choice, conditional logit, nested logit, Poisson count model.

July 14th, 2009

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1 Introduction

Location choices by households and firms are of interest to economists for numerous reasons, ranging from the determinants of residential segregation patterns in cities to the design of national tax policy. Given the discrete nature of such choices, they are typically modelled by empirical researchers through McFadden’s (1974) conditional logit framework.¹ The appeal of this approach lies in its formal link between the theoretical objective function of a representative location-seeking agent and the likelihood function of the empirical model.

Mostly out of a perception of greater computational ease, researchers have resorted to Poisson count estimation as an alternative approach to the conditional logit.² Guimaraes, Figueiredo and Woodward (2003), henceforth GFW, have shown that, with purely location-specific locational determinants or with determinants that are specific to locations and to groups of agents, the conditional logit and Poisson estimators return identical parameter estimates. In this sense, the two estimators are equivalent, and the rigorous link to the theory offered by the conditional logit model therefore applies identically to the Poisson. This useful result has already been applied widely in the location choice literature.³

We show that the identical coefficient estimates resulting from the two estimation strategies in fact have fundamentally different economic implications. The conditional logit model implies that the aggregate number of agents is fixed and that differences across locations affect only the distribution of those agents across those locations. Hence, an additional agent attracted to location \( j \) means one less agent among the other locations in the relevant set, \( i \neq j \).

In the Poisson model, however, an additional agent attracted to location \( j \) has no impact on the number of agents in the remaining locations and thus raises the aggregate number of agents, summed across \( i \) and \( j \), by one. Thus, the conditional logit model and the Poisson model can be viewed as polar cases, with the former representing zero-sum reallocations of firms or households across locations and the latter implying a positive-sum world.⁴

We also show that intermediate cases between these two extremes can be represented by a nested logit model featuring a generic outside option. This approach returns the same

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³Recent studies invoking the GFW equivalence result include Duranton, Gobillon and Overman (2006), Brüllhart, Jametti and Schmidheiny (2007), Arzaghi and Henderson (2008), Davis and Henderson (2008), and Coeurdacier, De Santis and Aviat (2009).

⁴For recent research on the cross-region effects of region-specific policies aimed at attracting firms, see, e.g., Greenstone and Moretti (2003), Chirinko and Wilson (2008), and Wilson (2009).
parameter estimates as the two other estimators. The nested logit in fact can be written as a linear combination of the conditional logit and Poisson models, with a single “rivalness parameter” representing the closeness of the nested logit to the conditional logit (and thus the distance from the Poisson). Conditional logit and Poisson elasticities mark the polar cases and can therefore serve as boundary values in applied research.

The paper is structured as follows. In Section 2, we formally derive the commonalities and differences among the conditional logit, Poisson and nested logit models. Empirical implications and an illustration are presented in Section 3. Section 4 concludes.

2 The models

We denote agents with \( f = 1, \ldots, N \) and regions with \( j = 1, \ldots, J \). For simplicity, we shall frame our discussion in terms of corporate location decisions, and therefore relate to \( f \) as “firms”.

Following GFW, we first assume the determinants of locational attractiveness to be purely region specific, such that they affect all firms symmetrically (case A). The \( K \) observable characteristics of each region are given by the \((K \times 1)\) vector \( x_j \). We then relax this assumption, and allow locational attractiveness to be region-industry specific (case B).

The random variable \( n_j \) represents the count of firms in region \( j \), whereas \( N_j \) denotes the number of firms actually observed in region \( j \). Analogously, the random variable \( n \) represents the total number of firms, whereas \( N \) denotes the observed total number of firms.

2.1 Case A: industry-invariant locational determinants

2.1.1 Conditional logit

Suppose that firm \( f \)’s profit in region \( j \) is determined by the linear model \( \pi_{fj} = x_j' \beta + \varepsilon_{fj} \), where \( \beta \) is a \((K \times 1)\) vector of coefficients. Then, the conditional logit model is defined by the assumption that the random term \( \varepsilon_{fj} \) is independent across \( f \) and \( j \) and follows an extreme-value type 1 distribution. With this assumption, the probability that a given firm \( f \) chooses region \( j \) rather than another region is given by

\[
P_{j|f} = P_j = \frac{e^{x_j' \beta}}{\sum_{i=1}^{J} e^{x_i' \beta}},
\]

where \( \sum_j P_{j|f} = 1 \) for all \( f \). Since locational characteristics \( x_j \) are assumed here to affect all firms symmetrically, this probability also represents the share of firms that will choose region \( j \).
The parameter $\beta$ can be estimated by maximum likelihood. We can write the log likelihood as

$$ \log L(\beta) = \sum_{j=1}^{J} N_j \log P_j = \sum_{j=1}^{J} N_j x'_j \beta - \sum_{j=1}^{J} N_j \log(\sum_{i=1}^{J} e^{x'_i \beta}). $$

(2)

The conditional logit model implicitly assumes that the total number of firms $n$ is given and does not depend on the locational characteristics $x$. The expected number of firms in region $j$, $E(n_j)$ is therefore simply

$$ E(n_j) = n P_j = n \frac{e^{x'_j \beta}}{\sum_{i=1}^{J} e^{x'_i \beta}}. $$

(3)

The percentage change in the expected number of firms in region $j$, $E(n_j)$, with respect to a unit change in the $k$-th locational characteristic of region $j$ itself is given respectively by the own-region semi-elasticity:

$$ \epsilon_{jj} = \frac{\partial \log E(n_j)}{\partial x_{jk}} = (1 - P_j) \beta_k. $$

(4)

Similarly, the percentage change in the expected number of firms in another region, $E(n_{i\neq j})$, with respect to a unit change in $j$’s $k$-th locational characteristic is given by the cross-region semi-elasticity:

$$ \epsilon_{ij} = \frac{\partial \log E(n_i)}{\partial x_{jk}} = -P_j \beta_k. $$

(5)

For simplicity, we shall henceforth refer to these and all subsequently presented semi-elasticities as “elasticities”. Hence, all “elasticities” derived and calculated in this paper in fact are semi-elasticities.

The own-region elasticity (4) shows that by enhancing its attractiveness a region will increase its expected number of firms, and the cross-region elasticity (5) implies that one region’s increased attractiveness to firms will reduce the number of firms choosing other regions: one region’s gain is another region’s loss. Moreover, a simple comparison of the two elasticities shows that small regions (in terms of $P_j$, the share of firms they host) are predicted by the conditional logit model to find their own firm counts to be relatively elastic to changes in their own locational characteristics, while not affecting firm counts in other regions as much as large regions.

We now turn from the viewpoint of individual regions to an analysis of what the conditional
logit model implies for the total number of firms among the $J$ regions. By definition, 

$$E(n) = \sum_{j=1}^{J} E(n_j) = n = N.$$  \hspace{1cm} (6)

Hence, the expected total number of firms is equal to the observed total, $N$, irrespective of regressors and parameters. This again shows the “zero sum” aspect of the conditional logit model, where the implied problem is one of allocating an exogenously fixed number of firms over a set of regions. It also follows logically that changes in the locational attractiveness of individual regions will not affect the total number of firms. Formally, the elasticity of the expected total firm count relative to a change in one of the $K$ locational characteristics of any particular region $j$ is zero:

$$\epsilon_j = \frac{\partial \log E(n)}{\partial x_{jk}} = 0.$$  

2.1.2 Poisson

The Poisson estimator is based on the assumption that $n_j$ is independently Poisson distributed with region-specific mean

$$E(n_j) = e^{\alpha + x_j^\beta}.$$  \hspace{1cm} (7)

Here too, $\beta$ can be estimated by maximum likelihood. We can write the concentrated log likelihood as

$$\log L(\beta) = \sum_{j=1}^{J} N_j x_j^\beta - \sum_{j=1}^{J} \left[ N_j \log \left( \sum_{i=1}^{J} e^{x_i^\beta} \right) \right] - \sum_{j=1}^{J} \log N_j! - N + N \log N.$$  \hspace{1cm} (8)

When comparing this to (2), the point made by GFW is plain to see: the log likelihood functions of the two models are identical up to a constant, and maximum likelihood estimation therefore yields identical parameter estimates $\hat{\beta}$.

The expected share of firms in region $j$ can be written as

$$P_j = \frac{E(n_j)}{\sum_{j=1}^{J} E(n_j)} = \frac{e^{\alpha + x_j^\beta}}{\sum_{i=1}^{J} e^{\alpha + x_i^\beta}} = \frac{e^{x_j^\beta}}{\sum_{i=1}^{J} e^{x_i^\beta}},$$  \hspace{1cm} (9)

which is exactly the same expression as (1), for the conditional logit model. This equivalence lies at the heart of the GFW result:

**Observation 1 (Guimaraes, Figueiredo and Woodward, 2003)** The log likelihood functions for the conditional logit and the Poisson model are identical up to a constant, and maximum likelihood estimation therefore yields identical parameter estimates $\hat{\beta}$. 

The elasticity of the expected number of firms in region \( j \), \( E(n_j) \), with respect to a change in the \( k \)-th locational characteristic of region \( j \) itself, and by that of another region \( i \neq j \), is given respectively by the own-region elasticity

\[
\epsilon_{jj} = \frac{\partial \log E(n_j)}{\partial x_{jk}} = \beta_k
\]

and by the cross-region elasticity

\[
\epsilon_{ij} = \frac{\partial \log E(n_i)}{\partial x_{jk}} = 0.
\]

Comparing these elasticities to their conditional-logit equivalents (4) and (5), we observe the following differences.

**Observation 2** The Poisson model implies more elastic responses by firm counts to given changes in own-region characteristics than the conditional logit model.

**Observation 3** Unlike in the conditional logit model, in the Poisson model, one region’s change in locational attractiveness has no impact on the number of firms located among any of the \( J - 1 \) other regions.

Hence, even though the estimated parameters \( \hat{\beta} \) will be invariant to the choice of model, their implied predictions differ starkly. The conditional logit model implies a zero-sum allocation process of a fixed number of firms over the \( J \) jurisdictions. In contrast, in the Poisson model new firms are non-rivalrous, in the sense that adjustment to one region’s locational characteristics works not through changes in firm numbers among the \( J - 1 \) other regions but from changes either in the supply of local entrepreneurship or in firms attracted from or repelled to somewhere outside the considered set of \( J \) regions.

Moving again from the viewpoint of individual regions to an analysis of the model’s implications for the total number of firms among the \( J \) regions, and using (7), we find that

\[
E(n) = \sum_{i=1}^{J} E(n_i) = \sum_{i=1}^{J} e^{\alpha + x'_i \beta} = e^\alpha \sum_{i=1}^{J} e^{x'_i \beta}.
\]

Comparing this expression with its conditional logit equivalent (6), we note that the expected total number of firms is now not generally equal to the observed total number of firms, \( N \), but depends on the regressors and parameters.\(^5\) The Poisson model thus implies that a change in a region’s locational attractiveness will affect the sum of firms active in the

---

\(^5\) Note that the predicted total number of firms at the estimated coefficients and actual data corresponds to the observed total of firms in the Poisson model just as it does in the conditional logit model. In symbols, \( E(n|\hat{\alpha}, \hat{\beta}) = N \).
J regions. Specifically, the elasticity of the expected total firm count with respect to a change in one of the K locational characteristics of any particular region \( j \) is given by

\[
\epsilon_j = \frac{\partial \log E(n)}{\partial x_{jk}} = \frac{e^{x_j^\prime \beta} \beta_k}{\sum_{i=1}^J e^{x_i^\prime \beta} \beta_k} = P_j \beta_k. \tag{6}
\]

**Observation 4** In the Poisson model, an increase (decrease) in one region’s locational attractiveness increases (decreases) the total of firms summed across the J regions. In the conditional logit model, a change in one region’s locational attractiveness leaves the total of firms summed across the J regions unchanged.

### 2.1.3 Nested logit

Observations 2, 3 and 4 show that the two models are the polar cases of a continuum of relative adjustment margins, ranging from reallocations purely within the set of alternatives considered (conditional logit) to reallocations purely between that set and some outside option (Poisson). We now turn to a micro-founded approach that covers this whole continuum and thus encompasses the polar cases.

Suppose that firms make two sequential choices. At the first stage, they choose between locating in one of the J regions considered (which could stand for “domestic” regions) and an outside option \( j = 0 \) (which could stand for locating “abroad” or for remaining inactive). At the second stage, they pick one of the J regions. Like in the conditional logit model, firm \( f \)'s profit in region \( j > 0 \) is determined by a linear function of the region-specific characteristics \( x_j \), such that \( \pi_{fj} = x_j^\prime \gamma + \nu_{fj} \). Firm \( f \)'s profit associated with the outside option is given by \( \pi_{f0} = \delta + \nu_{f0} \), where \( \delta \) summarizes the exogenously fixed locational attractiveness of the outside option. The stochastic term \( \nu_{f0} \) is assumed to follow a generalized extreme value distribution as in McFadden (1978).\(^7\) This leads to a nested logit model with one degenerate “nest” that includes \( j = 0 \) only and one other “nest” that includes all regions \( j > 0 \). This two-stage structure assumes independence between \( \nu_{f0} \) and \( \nu_{fj} \) for all \( j > 0 \), and non-negative correlation\((1 - \lambda^2)\) across \( \nu_{fj} \) for all \( j > 0 \); where \( 0 < \lambda \leq 1 \), sometimes called the “log-sum” coefficient, measures the importance of the domestic nest as a whole relative to the outside option.

In this setting, the probability that a particular firm \( f \) chooses the outside option \( j = 0 \) is given by

\[
P_0 = \frac{e^\delta}{e^\delta + (\sum_{j=1}^J e^{x_j^\prime \beta})^\lambda}, \tag{12}
\]

---

\(6\) We define \( P_j \equiv E(n_j)/E(n) \neq E(n_j/n) \) in the Poisson model. Using this definition, \( P_j = e^{x_j^\prime \beta} / \sum_{i=1}^J e^{x_i^\prime \beta} \) in both the conditional logit and the Poisson model.

\(7\) The specific density function assumed over \( \{0, J\} \) is \( F(\nu) = \exp \left[ -(\sum_{j=1}^J e^{-\nu_{fj} / \lambda})^\lambda - e^{-\nu_{f0}} \right] \).
and the probability that it chooses a particular region \( j > 0 \) among the \( J \) regions of interest is

\[
P_j = \frac{e^{x'_j \beta} \left( \sum_{i=1}^J e^{x'_i \beta} \right)^{\lambda-1}}{e^\delta + \left( \sum_{i=1}^J e^{x'_i \beta} \right)^\lambda} = P_{j>0} \cdot P_{j|j>0},
\]

where we reparametrize \( \beta = \gamma/\lambda \). This implies that, unlike in the conditional logit, the estimated regression parameters \( \hat{\beta} \) are not identical to the structural parameters of the underlying profit function.

The choice probabilities \( P_j \) can be decomposed into (a) the probability of choosing any of the \( J \) regions, \( P_{j>0} = 1 - P_0 \), and (b) the probability of choosing a specific region \( j \) given that the firm chooses to set up in one of the \( J \) regions,

\[
P_{j|j>0} = \frac{e^{x'_j \beta}}{\sum_{i=1}^J e^{x'_i \beta}}. \tag{13}
\]

The parameter \( \beta \) can again be estimated by maximum likelihood. We can write the concentrated log likelihood as

\[
\log L(\beta) = \sum_{j=1}^J \left[ N_j x'_j \beta - \sum_{j=1}^J \left[ N_j \log \left( \sum_{i=1}^J e^{x'_i \beta} \right) \right] \right] + N_0 \log(N_0) + N \log(N) - (N + N_0) \log(N + N_0),
\]

where \( \delta \) and \( \lambda \) cancel out when we substitute the first-order condition \( \partial \log L / \partial \delta = 0 \) into \( L(\beta, \delta, \lambda) \). N is the number of firms locating in any of the regions \( j > 0 \), and \( N_0 \) is the number of firms choosing the outside option \( j = 0 \). Note that \( \beta \) can be estimated without observing \( N_0 \).

**Observation 5** The log likelihood functions for the conditional logit, the Poisson and the nested logit model with a single outside option are identical up to a constant, and maximum likelihood estimation therefore yields identical parameter estimates \( \hat{\beta} \).

The ratio (13) is identical to its equivalents in the conditional logit and Poisson models, (1) and (9). This correspondence among the three models lies at the heart of Observation 5, which extends the GFW result to the nested logit case with a single outside option.

---

8This expression is obtained as follows:

\[
\log L(\beta, \delta, \lambda) = N_0 \log P_0 + \sum_{j=1}^J N_j \log P_j \\
= N_0 \log \left( \frac{e^\delta}{e^\delta + \left( \sum_{i=1}^J e^{x'_i \beta} \right)^\lambda} \right) + \sum_{j=1}^J \left[ N_j \log \left( \frac{e^{x'_j \beta} \left( \sum_{i=1}^J e^{x'_i \beta} \right)^{\lambda-1}}{e^\delta + \left( \sum_{i=1}^J e^{x'_i \beta} \right)^\lambda} \right) \right].
\]

The first-order condition with respect to \( \delta \) is \( \partial \log L / \partial \delta = N_0 - (N + N_0) e^\delta / \left[ e^\delta + \left( \sum_{i=1}^J e^{x'_i \beta} \right)^\lambda \right] = 0 \). The estimated \( \delta \) can therefore be expressed as a function of the estimated \( \beta \) and \( \lambda \): \( e^\delta = N_0 / N \cdot \left( \sum_{i=1}^J e^{x'_i \beta} \right)^\lambda \). When we substitute \( e^\delta \) in \( \log L(\beta, \delta, \lambda) \), \( \lambda \) also cancels out.
The expected number of firms in region $j > 0$ is

$$E(n_j) = (n + n_0)P_j = (n + n_0)\frac{e^{x_j^\beta}(\sum_{i=1}^J e^{x_i^\beta})^{\lambda-1}}{e^{\delta} + (\sum_{i=1}^J e^{x_i^\beta})^{\lambda}}. \quad (14)$$

The own-region elasticity of the expected number of firms, $E(n_j)$, relative to locational characteristics is given by

$$\epsilon_{jj} = \frac{\partial \log E(n_j)}{\partial x_{jk}} = [1 - P_{j|j>0}(1 - \lambda P_0)]\beta_k, \quad (15)$$

and the cross-region elasticity is given by

$$\epsilon_{ij} = \frac{\partial \log E(n_i)}{\partial x_{jk}} = -P_{j|j>0}(1 - \lambda P_0)\beta_k. \quad (16)$$

We can now compare the own- and cross-region elasticities of the three models. Simple inspection of elasticities (4), (5), (10), (11), (15) and (16) leads to the following observation.

**Observation 6** The nested-logit own-region and cross-region elasticities lie between their conditional logit and Poisson counterparts.

Once more, we now move from the analysis of firm counts in individual regions to the total number of firms that are active in the $J$ regions. Using (14) and (12), we find that

$$E(n) = (n + n_0)\frac{(\sum_{j=1}^J e^{x_j^\beta})^{\lambda}}{e^{\delta} + (\sum_{j=1}^J e^{x_j^\beta})^{\lambda}} = (n + n_0)P_{j>0}. \quad (12)$$

The expected total number of firms active in the $J$ regions is simply given by the share of potential firms that decide to become active in one of those regions. As in the Poisson model, the expected total number of firms is not generally equal to the observed total number of firms, $N$, but depends on the regressors and parameters, including those for the outside option.\(^9\)

The elasticity of the expected total firm count relative to a change in one of the $K$ locational characteristics of any particular region $j$ is given by

$$\epsilon_j = \frac{\partial \log E(n)}{\partial x_{jk}} = \lambda e^{x_{j}^\beta}(\sum_{i=1}^J e^{x_i^\beta})^{-1}\beta_k = \lambda P_0 P_{j|j>0}\beta_k. \quad (12)$$

**Observation 7** Like the Poisson, the nested logit model implies that a change in a region’s locational attractiveness will affect the total of firms summed across the $J$ regions.

Here, the responsiveness of the aggregate firm number is due to the effect on the decisions

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\(^9\) As in the Poisson and conditional logit models, the predicted total number of firms among the $J$ regions at the estimated coefficients and actual data corresponds to the observed total: $E(n|\beta, \delta, \lambda) = N$.\(^9\)
Table 1: Comparing implied elasticities (case A)

<table>
<thead>
<tr>
<th></th>
<th>Conditional Logit</th>
<th>Nested Logit</th>
<th>Poisson</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\epsilon_{jj}$</td>
<td>$(1 - P_{jj&gt;0})/\beta_k$</td>
<td>$[1 - P_{jj&gt;0}(1 - \lambda P_0)]/\beta_k$</td>
<td>$\beta_k$</td>
</tr>
<tr>
<td>$\epsilon_{ij}$</td>
<td>$-P_{ij&gt;0}/\beta_k$</td>
<td>$-P_{ij&gt;0}(1 - \lambda P_0)/\beta_k$</td>
<td>$0$</td>
</tr>
<tr>
<td>$\epsilon_{j}$</td>
<td>$0$</td>
<td>$\lambda P_0 P_{jj&gt;0}/\beta_k$</td>
<td>$P_{jj&gt;0}/\beta_k$</td>
</tr>
</tbody>
</table>

Notes: $P_{jj>0} = E(n_j)/E(n)$, $P_0 = E(n_0)/E(n + n_0)$

2.1.4 A synthesis of the three models

We can now pull together the salient features of the three models. First, we consider the impact of a change in the attractiveness of an individual region on the number of firms in that region and across the $J - 1$ remaining regions. Table 1 gathers the own-region, cross-region and aggregate elasticities implied by the three models.

In order to compare these elasticities, we define $\rho = 1 - \lambda P_0$ which satisfies $0 \leq \rho \leq 1$ under the standard nested logit assumption $0 < \lambda \leq 1$. We call $\rho$ the rivalness parameter. It allows us to write the nested logit elasticities as a linear combination of their conditional logit and Poisson equivalents: $\epsilon_{n\text{logit}}^{n\text{logit}} = \rho \epsilon_{c\text{logit}}^{c\text{logit}} + (1 - \rho) \epsilon_{n\text{Poisson}}$, $\epsilon_{jj}^{c\text{logit}} = \epsilon_{jj}^{c\text{logit}}$ and $\epsilon_{n\text{logit}}^{n\text{logit}} = (1 - \rho) \epsilon_{n\text{Poisson}}$. The rivalness parameter therefore acts as a summary measure of the position of the data generating process between the two polar cases, conditional logit ($\rho = 1$) and Poisson ($\rho = 0$). One may think of $\rho$ as capturing of the relative importance of the outside option: as $\rho \to 0$, competition among the $J$ regions becomes unimportant relative to the weight of the outside option, while with $\rho \to 1$, the outside option becomes negligible and any reallocations have to occur within the set of the $J$ regions.

We can also establish rankings of the elasticities implied by the three models. Provided that $\beta \neq 0$, the ranking of own-region elasticities is (c.f. Observations 2 and 6)

$$|\epsilon_{jj}^{\text{Poisson}}| > |\epsilon_{jj}^{n\text{logit}}| > |\epsilon_{jj}^{c\text{logit}}| > 0,$$

while the ranking of cross-regions elasticities is just the reverse (c.f. Observations 3 and 6),

$$|\epsilon_{ij}^{c\text{logit}}| > |\epsilon_{ij}^{n\text{logit}}| > |\epsilon_{ij}^{\text{Poisson}}| = 0.$$
and the ranking of aggregate elasticities is again (c.f. Observations 4 and 7)

$$|\epsilon^{\text{Poisson}}_j| > |\epsilon^{\text{nlogit}}_j| > |\epsilon^{\text{clogit}}_j| > 0.$$  

### 2.2 Case B: industry-specific locational determinants

Consider now that we observe $K$ characteristics $x_{sj}$ for every region $j$ and industry $s$. Hence, we again do not observe firm-specific regional attributes, but we now allow for these attributes to differ across groups of firms, best thought of as industries. We maintain the notation $x_j$ for the subset of locational determinants that are constant across industries. Furthermore, $n_{js}$ is the number of firms in region $j$ and industry $s$, $n_s$ is the observed number of industry-$s$ firms across all regions, $n$ is the total number of firms, and $N$ stands for the corresponding observed firm count in the sample.

The grouped conditional logit model is given by the probability that a given firm $f$ of industry $s$ chooses region $j$ rather than another region:

$$P_{j|f} = P_{j|s} = \frac{e^{x'_{sj}\beta}}{\sum_{i=1}^{J} e^{x'_{si}\beta}},$$

where $\sum_{j} P_{j|f} = 1$. $P_{j|s}$ is the probability for a particular firm to choose region $j$ given that the firm belongs to industry $s$.

The grouped Poisson model is given by

$$E(n_{sj}) = e^{\alpha_s + x'_{sj}\beta},$$

where $\alpha_s$ is an industry-specific constant.

Finally, the grouped nested logit model is given by the probability that a given firm $f$ of industry $s$ chooses either the outside option $j = 0$,

$$P_{0|s} = \frac{e^{\delta_s}}{e^{\delta_s} + (\sum_{j=1}^{J} e^{x'_{sj}\gamma/\lambda})^\lambda} = \frac{e^{\delta_s}}{e^{\delta_s} + (\sum_{j=1}^{J} e^{x'_{sj}\beta/\lambda})^\lambda},$$

or a particular domestic region $j > 0$,

$$P_{j|s} = \frac{e^{x'_{sj}\beta}(\sum_{i=1}^{J} e^{x'_{si}\beta})^{\lambda-1}}{e^{\delta_s} + (\sum_{i=1}^{J} e^{x'_{si}\beta})^\lambda} = P_{j>0|s} \cdot P_{j|j>0,s} = (1 - P_{0|s})P_{j|j>0,s},$$

where $\delta_s$ is an industry-specific constant, and $\beta = \gamma/\lambda$. $P_{j>0|s} = 1 - P_{0|s}$ is the probability
are (industry-specific) linear combinations of their conditional logit and Poisson equivalents: 

As in case A, the elasticities in the grouped nested logit model are observationally equivalent in a cross section of domestic firm choices and yield identical estimates for the parameter vector $\beta$. This has been shown by GFW for the grouped conditional logit and the grouped Poisson models, and we show it in the Appendix for the grouped nested logit model.

Table 2 summarizes the implied elasticities in the three grouped models (see the Appendix for derivations). As in case A, the elasticities in the grouped nested logit model are (industry-specific) linear combinations of their conditional logit and Poisson equivalents: 

$$
\epsilon^{\text{logit}} = \rho_s \epsilon^{\text{clogit}} + (1 - \rho_s) \epsilon^{\text{Poisson}} \quad \text{where} \quad \rho_s = 1 - \lambda P_{0|s}.
$$

<table>
<thead>
<tr>
<th>Region-industry specific regressor $x_{sjk}$:</th>
<th>Conditional Logit</th>
<th>Nested Logit</th>
<th>Poisson</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a) $\frac{\partial \log E(n_{sj})}{\partial x_{sjk}}$</td>
<td>$\beta_k (1 - P_{j</td>
<td>ij&gt;0,s})$</td>
<td>$\beta_k [1 - P_{j</td>
</tr>
<tr>
<td>(b) $\frac{\partial \log E(n_{sj})}{\partial x_{sjk}}$</td>
<td>$-\beta_k P_{ij&gt;0,s}$</td>
<td>$-\beta_k P_{ij&gt;0,s}(1 - \lambda P_{0</td>
<td>s})$</td>
</tr>
<tr>
<td>(c) $\frac{\partial \log E(n_{sj})}{\partial x_{sjk}}$</td>
<td>$0$</td>
<td>$\beta_k P_{ij&gt;0,s} \lambda P_{0</td>
<td>s}$</td>
</tr>
<tr>
<td>(d) $\frac{\partial \log E(n_{sj})}{\partial x_{sjk}}$</td>
<td>$\beta_k (1 - P_{j</td>
<td>ij&gt;0,s}) P_{s</td>
<td>ij}$</td>
</tr>
<tr>
<td>(e) $\frac{\partial \log E(n_{sj})}{\partial x_{sjk}}$</td>
<td>$-\beta_k P_{ij&gt;0,s} P_{s</td>
<td>i}$</td>
<td>$-\beta_k P_{ij&gt;0,s}(1 - \lambda P_{0</td>
</tr>
<tr>
<td>(f) $\frac{\partial \log E(n_{sj})}{\partial x_{sjk}}$</td>
<td>$0$</td>
<td>$\beta_k P_{s</td>
<td>ij} P_{j</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Region specific regressor $x_{jk}$:</th>
<th>Conditional Logit</th>
<th>Nested Logit</th>
<th>Poisson</th>
</tr>
</thead>
<tbody>
<tr>
<td>(g) $\frac{\partial \log E(n_{ij})}{\partial x_{jk}}$</td>
<td>$\beta_k \sum_{s=1}^{S} (1 - P_{j</td>
<td>ij&gt;0,s}) P_{s</td>
<td>ij}$</td>
</tr>
<tr>
<td>(h) $\frac{\partial \log E(n_{ij})}{\partial x_{jk}}$</td>
<td>$-\beta_k \sum_{s=1}^{S} P_{j</td>
<td>ij&gt;0,s} P_{s</td>
<td>i}$</td>
</tr>
<tr>
<td>(i) $\frac{\partial \log E(n_{ij})}{\partial x_{jk}}$</td>
<td>$0$</td>
<td>$\beta_k P_{j} \sum_{s=1}^{S} (\lambda P_{0</td>
<td>s} P_{s</td>
</tr>
</tbody>
</table>

Notes: $P_{j|ij>0,s} = E(n_{sj})/E(n_{s})$, $P_{0|s} = E(n_{s0})/E(n_{s} + n_{s0})$, $P_{s|ij} = E(n_{sj})/E(n_{j})$. $P_{s|ij}$ is the fraction of firms in industry $s$ in a given region $j$.

that a given industry-$s$ firm chooses any domestic region $j > 0$, and

$$
P_{j|ij>0,s} = \frac{e^{x_{ij}^s \beta}}{\sum_{i=1}^{J} e^{x_{ij}^s \beta}}
$$

is the probability that such a firm chooses a particular domestic region conditional on not choosing the outside option.
3 Estimation

3.1 Elasticity bounds

We have shown that estimation of any of the three models will yield identical parameter estimates \( \hat{\beta} \). The additional parameters \( \lambda, \delta \) and \( \alpha \) in the nested logit model are not identified but irrelevant for the estimation of \( \beta \). Hence, it is impossible to discriminate formally between these three model based on cross-section data. And yet, the implied elasticities differ substantially. In previous research, reported elasticities were based either on the conditional logit model or the Poisson model, without justification of the particular choice made or, mistakenly in this respect, by referring to the equivalence of the two models as established by GFW.

What can researchers do if they are not willing to make this choice by assumption but rely on cross-sectional data? We propose in this situation that one calculate the elasticities of both the conditional logit and the Poisson model and report these predictions as bounds for the true effects. As shown in Observation 6, intermediate values can be rationalized by a nested logit model.

The computation of both conditional logit and Poisson elasticities requires that one calculate predicted probabilities. In terms of case A (Table 1), the predicted probability is obtained as follows:

\[
\hat{P}_{j|j>0} = \frac{e^{x_j'\hat{\beta}}}{\sum_{i=1}^{J} e^{x_i'\hat{\beta}}},
\]

while for case B (Table 2), there are three predicted probabilities to be computed:

\[
\hat{P}_{j|j>0,s} = \frac{e^{x_{js}^r\hat{\beta}}}{\sum_{i=1}^{J} e^{x_{is}^r\hat{\beta}}},
\]

\[
\hat{P}_{s|j} = \frac{e^{x_{js}^r\hat{\beta}}}{\sum_{r=1}^{S} e^{x_{rj}^s\hat{\beta}}}, \text{ and}
\]

\[
\hat{P}_{j|j>0} = \frac{\sum_{s=1}^{S} e^{x_{js}^r\hat{\beta}}}{\sum_{r=1}^{S} \sum_{i=1}^{J} e^{x_{is}^r\hat{\beta}}},
\]

3.2 An example

By way of an illustration, we take the data on location choices in Portugal by foreign-owned plants used in Guimaraes et al. (2000, 2003), and we report the elasticities implied by the coefficients of their regression model. The data cover a cross section of 758 location choices among 275 Portuguese regions by firms belonging to one of 151 industries.\(^{10}\) Their region-industry level regressor of main interest, \( x_{sjk} \), is “industry-specific agglomeration”, defined as

\(^{10}\)We follow GFW by referring to industry-year pairs as “industries”. The 151 industries in their data set are combinations of 27 three-digit manufacturing sectors and seven sample years, ranging from 1985 to 1991.
Table 3: Comparing implied elasticities in an example of case B

<table>
<thead>
<tr>
<th>Region-industry specific regressor $x_{sjk}$:</th>
<th>large region $j$</th>
<th>small region $j$</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a) $\frac{\partial \log E(n_{sj})}{\partial x_{sjk}}$</td>
<td>2.9290</td>
<td>3.1883</td>
</tr>
<tr>
<td>(b) $\frac{\partial \log E(n_{si})}{\partial x_{sjk}}$</td>
<td>-0.2593</td>
<td>0</td>
</tr>
<tr>
<td>(c) $\frac{\partial \log E(n_{s})}{\partial x_{sjk}}$</td>
<td>0</td>
<td>0.2593</td>
</tr>
<tr>
<td>(d) $\frac{\partial \log E(n_{j})}{\partial x_{sjk}}$</td>
<td>0.1110</td>
<td>0.1208</td>
</tr>
<tr>
<td>(e) $\frac{\partial \log E(n_{i})}{\partial x_{sjk}}$</td>
<td>-0.0095</td>
<td>0</td>
</tr>
<tr>
<td>(f) $\frac{\partial \log E(n_{j})}{\partial x_{sjk}}$</td>
<td>0</td>
<td>0.0106</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Region specific regressor $x_{jk}$:</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>(g) $\frac{\partial \log E(n_{j})}{\partial x_{jk}}$</td>
<td>0.3873</td>
</tr>
<tr>
<td>(h) $\frac{\partial \log E(n_{i})}{\partial x_{jk}}$</td>
<td>-0.0378</td>
</tr>
<tr>
<td>(i) $\frac{\partial \log E(n_{j})}{\partial x_{jk}}$</td>
<td>0</td>
</tr>
</tbody>
</table>

Notes: large region: $j =$ Lisbon; small region: $j =$ Oleiros; $i =$ Porto in rows (e) and (h); $k =$ “industry-specific agglomeration” in rows (a) to (f), $k =$ “total manufacturing agglomeration” in rows (g) to (i); sector: $s =$ ISIC 351 (Industrial Chemicals) in 1989 in rows (a) to (f); any sector in rows (g) to (i).

the share of regional employment in the same industry as the relevant firm. Their region level regressor of main interest, $x_{jk}$, is “total manufacturing agglomeration”, defined as the log of aggregate manufacturing employment per square kilometer.

Taking their estimated parameters and computing the empirical probabilities (18)-(21), we can calculate all the implied elasticities of Table 2. Since the probabilities (18)-(21) vary by region and industry, we need to select specific cases for the computation of elasticities. We provide illustrations for two base regions $j$: Lisbon, the largest region in terms of $\hat{P}_{j|>0}$, and Oleiros, the smallest region in terms of $\hat{P}_{j|>0}$ that still had non-zero firm counts in the larger industry considered.\(^{11}\)

Table 3 shows the implied elasticities for changes in a region-industry specific regressor and in a region specific regressor. We can take these estimates to illustrate Observations 2 to 4.

- Observation 2: Own-region elasticities are larger in the Poisson model than in the

\(^{11}\)Where a comparison region $i$ needs to be specified for the computation of cross elasticities, we choose Porto, the second largest region in the data set. Where an industry $s$ needs to be specified, we choose Industrial Chemicals (ISIC 351) in 1989, the largest sector-year pair in the dataset (31 observed choices, i.e. 4 percent of the total of 758 choices).
conditional logit (rows (a), (d) and (g)). We can see that the difference between implied own-region elasticities is non-trivial for the large region (some 10 percent) but very small for the small region (less than 0.1 percent). This illustrates that the difference between implied own-region elasticities of the two models vanishes as the number of regions grows large and individual regions therefore become small.

- **Observation 3**: All Poisson cross-region elasticities are zero (rows (b), (e) and (h)).

- **Observation 4**: In the conditional logit model, the total number of firms (across all of Portugal) is invariant to changes in the values of \( x_{sjk} \) or \( x_{jk} \) whereas in the Poisson model the total changes with \( x_{sjk} \) or \( x_{jk} \) (rows (c), (f) and (i)). The effect on the total number of firms of a given change in \( x_{sjk} \) is stronger if the change occurs in a large region.

These computations illustrate the qualitatively different predictions implied by the conditional logit and Poisson models. With \( J = 275 \) spatial alternatives and \( s = 151 \) industries, the underlying data set is highly disaggregated, implying relatively modest quantitative differences between implied elasticities. Nonetheless, even here some of the differences are far from negligible. Perhaps the most striking difference appears in row (c) of Table 3. A one-unit change in \( x_{sjk} \) of Lisbon leaves the number of Portuguese plants in industry \( s \) unchanged in the conditional logit framework, while it increases by up to 29 percent in the Poisson model. Policy makers ought not to ignore a difference of such magnitude.

4 Conclusions

We show that the three standard location choice models - conditional logit, nested logit and Poisson - are observationally equivalent in terms of cross-section estimation yet imply starkly different predictions.

Take a corporate tax cut in a particular region. Provided that this is perceived by firms as making that region more attractive, all three models imply that the region itself will see an increase in its number of firms. We show that the magnitude of the implied increase differs: it is largest if the world is properly represented by the Poisson model, smallest if the world conforms with the conditional logit, and somewhere in-between if the world is nested logit. In a Poisson world, the tax cut will have no impact on firm counts in any other of regions within the data set. It will, however, pull firms away from other regions in the conditional logit and the nested logit cases. As the total number of firms is fixed in the conditional logit, the sum of the firms pulled away from the other regions is the same as the increase in the number
of firms in the tax-cutting region itself. The nested logit again represents an intermediate case, with some of the attracted firms relocating from elsewhere within the data set, implying that regional corporate tax bases are “rival”; and some firms appearing from outside that set, implying a “non-rival” tax base. The same logic can be applied to residential choices of private households with respect, for instance, to changes in local property tax rates.

Empirical researchers should be aware of the interpretational ambiguity affecting estimated parameters in standard location choice models, particularly if the number of locations and industries distinguished in the data is small. It can therefore be useful to report both conditional logit and Poisson elasticity estimates as bounds on the effects implied by the estimated parameters.

References


Appendix: Derivations for case B

Grouped conditional logit

The conditional logit model for grouped data is given by the probability that a given firm \( f \) of industry \( s \) chooses region \( j \)

\[
P_{j|f} = P_{j|s} = \frac{e^{x'_{sj}\beta}}{\sum_{i=1}^{J} e^{x'_{si}\beta}}.
\]

The log likelihood function is

\[
\log L(\beta) = \sum_{s=1}^{S} \sum_{j=1}^{J} N_{sj} P_{j|s} = \sum_{s=1}^{S} \left\{ \sum_{j=1}^{J} N_{sj} x'_{sj}\beta - \sum_{j=1}^{J} \left[ N_{sj} \log \sum_{i=1}^{J} e^{x'_{si}\beta} \right] \right\}.
\]

The expected number of firms in region \( j \) and industry \( s \) is

\[
E(n_{sj}) = n_{s} P_{j|s} = \frac{n_{s} e^{x'_{sj}\beta}}{\sum_{i=1}^{J} e^{x'_{si}\beta}};
\]

and the corresponding own-region and cross-region elasticities within industry \( s \) are, respectively,

\[
\frac{\partial \log E(n_{sj})}{\partial x_{sjk}} = (1 - P_{j|s})\beta_{k},
\]

\[
\frac{\partial \log E(n_{s})}{\partial x_{sjk}} = -P_{j|s}\beta_{k}.
\]

The expected number of firms in industry \( s \) is

\[
E(n_{s}) = \sum_{j=1}^{J} E(n_{sj}) = n_{s} = N_{s},
\]

and the corresponding elasticity within industry \( s \) is

\[
\frac{\partial \log E(n_{s})}{\partial x_{sjk}} = 0.
\]

The expected number of firms in region \( j \) is

\[
E(n_{j}) = \sum_{s=1}^{S} E(n_{sj}) = \sum_{s=1}^{S} n_{s} P_{j|s} = \sum_{s=1}^{S} \frac{n_{s} e^{x'_{sj}\beta}}{\sum_{i=1}^{J} e^{x'_{si}\beta}}.
\]

The corresponding own-region and cross-region elasticities for a region-industry specific shock \( x_{sjk} \) are

\[
\frac{\partial \log E(n_{j})}{\partial x_{sjk}} = \frac{\partial \log E(n_{sj})}{\partial x_{sjk}} \cdot \frac{E(n_{sj})}{E(n_{j})} = (1 - P_{j|s})P_{sj|j}/\beta_{k},
\]

\[
\frac{\partial \log E(n_{s})}{\partial x_{sjk}} = \frac{\partial \log E(n_{s})}{\partial x_{sjk}} \cdot \frac{E(n_{s})}{E(n_{j})} = -P_{j|s}P_{sj|j}/\beta_{k},
\]

where \( P_{sj|j} = E(n_{sj})/E(n_{j}) \).

The own-region and cross-region elasticities for a region-specific shock \( x_{jk} \) are

\[
\frac{\partial \log E(n_{j})}{\partial x_{jk}} = \sum_{s=1}^{S} \left[ \frac{\partial \log E(n_{sj})}{\partial x_{jk}} \cdot \frac{E(n_{sj})}{E(n_{j})} \right] = \beta_{k} \sum_{s=1}^{S} (1 - P_{j|s})P_{sj|j},
\]
\[
\frac{\partial \log E(n_i)}{\partial x_{jk}} = \sum_{s=1}^{S} \left[ \frac{\partial \log E(n_{si})}{\partial x_{jk}} \cdot \frac{E(n_{si})}{E(n_i)} \right] = -\beta_k \sum_{s=1}^{S} P_{j|s} p_{s|i}.
\]

The expected total number of firms in all regions and industries is
\[
E(n) = \sum_{s=1}^{S} \sum_{j=1}^{J} E(n_{js}) = \sum_{s=1}^{S} E(n_s) = n,
\]
and the corresponding elasticities for a region-industry specific shock \(x_{sjk}\) and a region-specific shock \(x_{jk}\) are, respectively,
\[
\frac{\partial \log E(n)}{\partial x_{sjk}} = 0, \quad \frac{\partial \log E(n)}{\partial x_{jk}} = 0.
\]

**Grouped Poisson**

The Poisson model for grouped data is given as
\[
E(n_{sj}) = \lambda_{sj} = e^{\alpha_s + x_{sj}' \beta},
\]
where \(\alpha_s\) is an industry-specific constant. The concentrated log likelihood function is
\[
\log L(\beta) = \sum_{s=1}^{S} \left\{ \sum_{j=1}^{J} N_{sj} x_{ij}' \beta - \sum_{j=1}^{J} [N_{sj} \log(\sum_{i=1}^{J} e^{x_{si}' \beta})] - \sum_{j=1}^{J} \log N_{sj}! + N_s \log N_s \right\} - N.
\]

The share of firms in region \(j\) for any given industry \(s\) is given by
\[
P_{j|s} = \frac{E(n_{sj})}{\sum_{i=1}^{J} E(n_{sj})} = \frac{e^{\alpha_s + x_{sj}' \beta}}{\sum_{i=1}^{J} e^{\alpha_s + x_{si}' \beta}} = \frac{e^{x_{sj}' \beta}}{\sum_{i=1}^{J} e^{x_{si}' \beta}}.
\]

The own-region and cross-region elasticities within industry \(s\) are, respectively,
\[
\frac{\partial \log E(n_{sj})}{\partial x_{sjk}} = \beta_k, \quad \frac{\partial \log E(n_{si})}{\partial x_{sjk}} = 0.
\]

The expected number of firms in industry \(s\) is
\[
E(n_s) = \sum_{i=1}^{J} E(n_{si}) = \sum_{i=1}^{J} e^{\alpha_s + x_{si}' \beta} = \sum_{i=1}^{J} E(n_{si}) = \sum_{i=1}^{J} e^{\alpha_s + x_{si}' \beta} = e^{\alpha_s} \sum_{i=1}^{J} e^{x_{si}' \beta},
\]
and the corresponding elasticity within industry \(s\) is
\[
\frac{\partial \log E(n_s)}{\partial x_{sjk}} = \frac{e^{x_{sj}}}{\sum_{i=1}^{J} e^{x_{si}' \beta}} \beta_k = P_{j|s} \beta_k.
\]

The expected number of firms in region \(j\) is
\[
E(n_j) = \sum_{s=1}^{S} E(n_{sj}) = \sum_{s=1}^{S} e^{\alpha_s + x_{sj}' \beta}.
\]

The corresponding own-region and cross-region elasticities for a region-industry specific shock
The expected number of firms in domestic region $j > 0$, the concentrated log likelihood function is

$$P_{sij} = \frac{E(n_{sj})}{E(n_j)},$$

where $P_{sij} = E(n_{sj})/E(n_j)$.
The own-region and cross-region elasticities for a region-specific shock $x_{jk}$ are

$$\frac{\partial \log E(n_{sj})}{\partial x_{sjk}} = \frac{\partial \log E(n_{sj})}{\partial x_{sjk}} \cdot \frac{E(n_{sj})}{E(n_j)} = P_{sij} \beta_k,$$

and the corresponding elasticities for a region-industry specific shock $x_{jk}$ are

$$\frac{\partial \log E(n_{sj})}{\partial x_{sjk}} = \sum_{s=1}^{S} \left[ \frac{\partial \log E(n_{sj})}{\partial x_{sjk}} \cdot \frac{E(n_{sj})}{E(n_j)} \right] = \beta_k,$$

where $P_j = E(n_j)/E(n)$.

**Grouped nested logit**

The nested logit model for grouped data is given by the probability that firm $f$ of industry $s$ chooses the outside option $j = 0$ or region $j > 0$: 

$$P_{0|s} = \frac{e^{\delta_s}}{e^{\delta_s} + (\sum_{j=1}^{J} e^{x_{sj}^\gamma/\lambda})^{\lambda}} = \frac{e^{\delta_s}}{e^{\delta_s} + (\sum_{j=1}^{J} e^{x_{sj}^\gamma/\lambda})^{\lambda}},$$

$$P_{j|s} = \frac{e^{x_{sj}^\beta}}{e^{\delta_s} + (\sum_{i=1}^{J} e^{x_{sj}^\beta})^{\lambda}} = P_{j>0|s} \cdot P_{j>0,s} = (1 - P_{0|s}) \cdot P_{j>0,s},$$

where $\delta_s$ is an industry-specific constant, $\beta = \gamma/\lambda$ and

$$P_{j>0,s} = \frac{e^{x_{sj}^\beta}}{\sum_{i=1}^{J} e^{x_{sj}^\beta}}.$$

The concentrated log likelihood function is

$$\log L(\beta) = \sum_{s=1}^{S} \left\{ \sum_{j=1}^{J} N_{sj} x_{sj}^\beta - \sum_{j=1}^{J} [N_{sj} \log \sum_{i=1}^{J} e^{x_{sj}^\beta}] + N_{s0} \log(N_{s0}) + N_s \log(N_s) - (N_s + N_{s0}) \log(N_s + N_{s0}) \right\}.$$

The expected number of firms in domestic region $j > 0$ and industry $s$ is

$$E(n_{sj}) = (n_s + n_{s0}) P_{j|s} = (n_s + n_{s0})(1 - P_{0|s}) P_{j>0,s},$$
and the corresponding own-region and cross-region elasticities within industry $s$ are, respectively,

$$\frac{\partial \log E(n_{sj})}{\partial x_{sjk}} = [1 - P_{j|j>0,s}(1 - \lambda P_{0|s})] \beta_k,$$

$$\frac{\partial \log E(n_{si})}{\partial x_{sjk}} = -P_{j|j>0,s}(1 - \lambda P_{0|s}) \beta_k.$$

The expected number of all domestic firms in industry $s$ is

$$E(n_s) = \sum_{j=1}^{J} E(n_{sj}) = (n_s + n_{s0})(1 - P_{0|s}),$$

and the corresponding elasticity within industry $s$ is

$$\frac{\partial \log E(n_s)}{\partial x_{sjk}} = \lambda P_{0|s} P_{j|j>0,s} \beta_k.$$

The expected number of firms in domestic region $j$ is

$$E(n_j) = \sum_{s=1}^{S} E(n_{sj}) = \sum_{s=1}^{S} (n_s + n_{s0}) P_{j|s},$$

The corresponding own-region and cross-region elasticities for a region-industry specific shock $x_{sjk}$ are

$$\frac{\partial \log E(n_{j})}{\partial x_{sjk}} = \frac{\partial \log E(n_{sj})}{\partial x_{sjk}} \cdot \frac{E(n_{sj})}{E(n_j)} = [1 - P_{j|j>0,s}(1 - \lambda P_{0|s})] P_{sj|j} \beta_k,$$

$$\frac{\partial \log E(n_{i})}{\partial x_{sjk}} = \frac{\partial \log E(n_{si})}{\partial x_{sjk}} \cdot \frac{E(n_{si})}{E(n_i)} = -P_{j|j>0,s}(1 - \lambda P_{0|s}) P_{sj|i} \beta_k,$$

where $P_{sj} = E(n_{sj})/E(n_j)$.

The own-region and cross-region elasticities for a region-specific shock $x_{jk}$ are

$$\frac{\partial \log E(n_{j})}{\partial x_{jk}} = \sum_{s=1}^{S} \left[ \frac{\partial \log E(n_{sj})}{\partial x_{jk}} \cdot \frac{E(n_{sj})}{E(n_j)} \right] = \beta_k \sum_{s=1}^{S} [1 - P_{j|j>0,s}(1 - \lambda P_{0|s})] P_{sj},$$

$$\frac{\partial \log E(n_{i})}{\partial x_{jk}} = \sum_{s=1}^{S} \left[ \frac{\partial \log E(n_{si})}{\partial x_{jk}} \cdot \frac{E(n_{si})}{E(n_i)} \right] = -\beta_k \sum_{s=1}^{S} P_{j|j>0,s}(1 - \lambda P_{0|s}) P_{sj|i}.$$

The expected total number of firms in all domestic regions and industries is

$$E(n) = \sum_{s=1}^{S} \sum_{j=1}^{J} E(n_{js}) = \sum_{j=1}^{J} E(n_j),$$

and the corresponding elasticities for a region-industry specific shock $x_{sjk}$ and a region-specific shock $x_{jk}$ are, respectively,

$$\frac{\partial \log E(n)}{\partial x_{sjk}} = \left[ \frac{\partial \log E(n_{sj})}{\partial x_{sjk}} + \sum_{i \neq j, i>0} \frac{\partial \log E(n_{si})}{\partial x_{sjk}} \right] \cdot \frac{E(n_{sj})}{E(n)} = \beta_k \lambda P_{0|s} P_{sj} P_{j},$$

$$\frac{\partial \log E(n)}{\partial x_{jk}} = \left[ \frac{\partial \log E(n_{j})}{\partial x_{jk}} + \sum_{i \neq j, i>0} \frac{\partial \log E(n_{i})}{\partial x_{jk}} \right] \cdot \frac{E(n_{j})}{E(n)} = \beta_k P_{j} \sum_{s=1}^{S} (\lambda P_{0|s} P_{sj}),$$

where $P_{j} = E(n_{j})/E(n)$.
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