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Shaping Inequality and Intergenerational Persistence of Poverty: Free College or Better Schools*

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Abstract

We evaluate the aggregate, distributional and welfare consequences of alternative government education policies to encourage college completion, such as making college free and improving funding for public schooling. To do so, we construct a general equilibrium overlapping generations model with intergenerational linkages, a higher education choice as well as a multi-stage human capital production process during childhood and adolescence with parental and government schooling investments. The model features rich cross-sectional heterogeneity, distinguishes between single and married parents, and is disciplined by US household survey data on income, wealth, education and time use. Studying the transitions induced by unexpected policy reforms we show that the “free college” and the “better schools” reform generate significant welfare gains, which take time to materialize and are lower in general than in partial equilibrium. It is optimal to combine both reforms: tuition subsidies make college affordable even for children from poorer parental backgrounds and better schools increase human capital thereby reducing dropout risk.

Keywords: education spending, public transfers, welfare benefits, inequality, poverty, intergenerational persistence

J.E.L. Codes: D15, D31, E24, I24

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1 Introduction

In international comparison, the U.S. displays low intergenerational socio-economic mobility, with especially high persistence at the bottom of the income distribution. Achievement gaps between children of different socio-economic backgrounds appear early in life and persist into adulthood, and are associated with a strong parental income gradient of college attendance (Chetty et al. (2014)). Skill and achievement gaps during adolescence (i.e. before labor market entry) have been identified as a key factor determining differences in later life economic outcomes (see, e.g., Keane and Wolpin (1997); Carneiro and Heckman (2002); Huggett et al. (2011)), and a variety of policies have been proposed to lessen these disparities, most recently, a proposal by the current Biden administration to make at least community college free.¹

This paper aims at providing a joint analysis of policies targeted at the pre-college human capital accumulation stage (secondary school financing) on the one hand, and policies designed to make college education more financially affordable, on the other hand. Suppose that the main problem holding poor children back from successfully pursuing a college education is not that they cannot pay for it (i.e., the prevalence of binding credit constraints in the presence of high tuition costs), but rather that they arrive at college age ill-equipped to successfully apply and ultimately graduate from college. Then policies tackling this problem might be more appropriate tools to increase the average and reduce the cross-sectional dispersion and intergenerational persistence of college attendance, earnings and welfare. To evaluate and to compare such policies, we develop a dynamic general equilibrium model of childhood human capital and higher education decisions. We then assess the positive and normative implications of such policies designed to boost human capital accumulation and college attendance, especially of those children from disadvantaged socio-economic backgrounds.

Concretely, we develop a general equilibrium overlapping generations framework with intergenerational links through altruistically-motivated education and wealth transfers, in the spirit of Barro and Becker (1988), and with rich cross-sectional heterogeneity of labor productivity (and thus earnings), human capital, wealth and marital status. Human capital is accumulated at different stages of a child's development, depending on parental resource- and time investments as well as public education funding. Crucially, human capital acquired at earlier stages of child development determines the productivity of all future human capital investments. The human capital acquired prior to the higher education (college) stage determines both the chances to succeed in college and the expected returns from a college education. Altruistically motivated and rationally forward-looking parents respond to policies affecting the labor market stage of their children's life cycle. At the same time, parents react to education (financing) reforms by adjusting both their

¹As well as further initiatives to make higher education less costly.

own education choices and investments in their children. These interactions between education subsidies targeted at different stages of child and adolescent development and progressive taxation suggest that these policy reforms must be studied jointly. The dynastic modeling framework with intergenerational linkages allows us to evaluate the implications of policy reforms not only for cross-sectional inequality but also for intergenerational earnings- and education mobility.

Our policy analysis starts from an initial stationary equilibrium calibrated to the status quo of the US economy in the 2010's. We then investigate the impact of policy reforms along the transition of the economy towards a final steady state. Along this transition, the government may issue new government debt to finance education policies that in the long run raise human capital and thus the tax base (a fiscal externality), but take time to materialize their full impact. By issuing debt the government may thus smooth out the transitional costs of the policy reforms.

We evaluate a set of once-and-for-all policy reforms that are motivated by the current political discussion and that are comparable in the present discounted value of their government expenditure requirements. The first reform we consider is making college education free (motivated by President Biden's proposal to provide for universal free community college) which in our model is implemented by a 100% tertiary education subsidy by the government. This reform is then used as benchmark to determine the size of the other reforms to make those fiscally comparable. The alternative policy reform we consider focuses on human capital accumulation of younger children by increasing public spending for primary or secondary schools. Finally, we study whether there is scope for combining both reforms by characterizing the optimal mix of "better schools" and college tuition subsidies, holding the total fiscal cost of the policy reform on impact constant across all interventions considered.

Our findings can be summarized as follows. In terms of aggregates, both education reforms increase the share of a cohort having a college degree strongly (and roughly to the same degree in the long run), but the overall expansion of human capital is much more pronounced—and thus the college dropout share is substantially lower—under the pre-college school spending reform.² Because of the stronger increase in human capital in the long run, the net present discounted value of government revenues rises more substantially under the school expenditure expansion than under the 100% college subsidy reform. The expansion of the tax base is then larger in the former reform as well, to an extent that it is more than self-financing, in the sense that (if the government is allowed to issue new debt) the required permanent increase in the labor income tax rate to balance the intertemporal government budget is actually negative. Both reforms generate significant long-run welfare gains, in the order of 11-15% of permanent consumption,

²Importantly, the model-implied short-run partial equilibrium responses of college enrollment and high school graduation rates to small-scale expansions of both pre-college and college funding are consistent with the recent applied micro literature (see [Deming and Dynarski \(2009\)](#) and [Jackson and Mackevicius \(2023\)](#)).

when measured as consumption equivalent variation of newborn agents. Given the assumed altruism, these high welfare gains include the welfare benefits of children and all subsequent generations. Consistent with the more favorable human capital and tax revenue expansions, the welfare gain is larger by about 3 percentage points in the “better schools” reform than in the “free college” reform in the long run. The finding that the expansion of school spending results in large aggregate gains also aligns well with the recent empirical public economics literature that leveraging the link between local school spending, property taxes and property values concludes that both capital spending on schools (Cellini et al. (2010)) and “current expenditures” (i.e. mainly spending on teacher and personnel salaries, see Bayer et al. (2024)) are inefficiently low in the current US status quo.

Second, the two policy reforms have vastly different distributional consequences. Most crucially, the pre-college expenditure reform also benefits children from households who will not go to college even if they do not have to pay tuition, as is the case under the “free college” reform.³ This in turn has profound consequences for the intergenerational persistence of earnings and educational attainment. Perhaps the most striking contrast between the reforms is the differential impact on the educational attainment of the poorest children, which tend to be children growing up in a household with a single parent and low (less than high school) educational attainment. Although the “free college” reform is fairly successful in drawing these disadvantaged children into college, it does so at the cost of disproportionately high dropout rates and relatively low college wage premia.⁴ In contrast, the additional human capital accumulation these children obtain with the “better schools” reform, although insufficient in most cases to push them above the college threshold, strongly increases the chances of these children to at least complete high school, therefore strongly reducing the intergenerational persistence of dropping out of high school.

To isolate the importance of changes in endogenous interest rates and (relative) wages we also conduct a sequence of partial equilibrium exercises in which we hold these endogenous prices constant. We show, broadly speaking, that qualitatively, the aggregate and distributional conclusions discussed above also emerge in the absence of equilibrium price adjustments, but the welfare gains of the reforms are larger (as are the differences between the two reforms) in partial equilibrium. The most important general equilibrium effect in both types of reforms stems from the fact that the supply of labor, especially college labor (but also total labor in efficiency units), strongly increases, inducing a decline in the capital-labor ratio and therefore an increase in the

³At the same time, more generous high school financing additionally also benefits children even from most affluent backgrounds via increasing their post-graduation earnings. This is an important force driving the more beneficial fiscal implications of the “better schools” reform while the “free college” reform is completely ineffective for changing college decisions at the very top and simply provides a pure consumption transfer to these households.

⁴In the model, the college wage premium is not one parameter but follows a distribution that endogenously depends on the pre-college acquired human capital distribution.

real interest rate and a reduction in the real wage per labor efficiency units. Since the college wage premium also falls, relative to the long run BGP the wages of college graduates decline very substantially, whereas the wages of non-college labor mildly increase.⁵

It turns out that for the size of the general welfare gains, the reduction in wages (and especially, the wages of college graduates) is quantitatively most important. These general equilibrium wage impacts on welfare are broadly negative, but with a nuance. As discussed, the reduction in the capital-labor ratio leads to a decline in the wage per labor efficiency unit. However, the very significant increase in the share of college graduates induced by both reforms leads, over time, to a massive reduction in the college wage premium. Consequentially, college wages fall precipitously along the transition (and there is now a large share of individuals making these wages), in turn muting the increase in the college share in general equilibrium relative to partial equilibrium. In contrast, the wages of workers without a college degree actually slightly increase as the relative wage effect slightly dominates the absolute wage effect for this (shrinking) group of individuals or households. Since the policies lead to wage compression within the population, the distributional consequences for ex-ante lifetime utility are positive, partially compensating for the welfare losses from the decline in the absolute wage level. Finally, the (modest) increase in the real interest rate strengthens savings incentives; in the “better schools” reform it leads to a shift in the wealth distribution to the right over time and a larger capital stock; in the “free college” reform it mitigates the decline in private wealth accumulation that otherwise would have occurred in partial equilibrium due to the collapse in inter-vivos transfers. Overall, and relative to a world where all factor prices are constant, the long-run welfare gains for the “free college” reform are 3.1 percentage points lower in general than in partial equilibrium, respectively they are 4.6 percentage points lower for the “better schools” reform. Thus, endogenous factor price movements not only reduce the welfare gains from the reforms, but also reduce the gap in the welfare consequences across the two reforms.

Finally, and motivated by these results we study the optimal combination of both better school financing and college subsidies. To provide intuition for this analysis we develop a simple theoretical model —contained in Appendix D—, to establish the role of the two policy instruments as relative welfare substitutes —they both decrease the human capital threshold it takes to attend college— and as relative welfare complements —increasing human capital through increased school spending increases relative wages of college youngsters and reduces dropout probabilities. It is therefore a quantitative question whether our analysis of joint policies delivers a corner solution such that the “better schools” policy reform is the preferred policy choice, or an interior

⁵Although in partial equilibrium the “better schools” reform is effective in increasing college enrollment and graduation even for the poorest children, in general equilibrium the decline in the college wage premium and the higher costs of borrowing effectively mute this effect. The improvement in high school completion rates and post-graduation earnings, for a given education level, persist, however.

solution with an optimal mix of both instruments. We indeed find an interior optimum such that a policy that devotes ca. 1/3 of its budget to better schools and 2/3 to college subsidies maximizes aggregate welfare. This joint policy is almost as effective as the pure “free college” reform in drawing in additional students into college, but the higher average human capital upon entering college due to better schools limits the increase in dropout rates that the pure “free college” reform is inflicted by. The optimal policy is characterized by a higher weight on “free college” because it takes a sufficiently large college reform to draw a relevant mass of youngsters into college.

After briefly reviewing the extant literature, we describe the quantitative model and its equilibrium in Sections 2 and 3, respectively. Section 4 and 5 discusses calibration and validation of the model. In Section 6 we present the results of two policy reforms, and Section 7 discusses the optimal combination of both reforms. Section 8 concludes, and further details about the theory and quantification of the model, as well as additional results are contained in the appendix.

1.1 Related Literature

Our paper builds on a voluminous literature that has documented a prominent role of family income and family composition both in determining pre-college academic achievement (Dahl and Lochner (2012), Caucutt et al. (2017), Blandin and Herrington (2022), Ebrahimian (2023)), and college entry decisions and graduation outcomes (e.g. Belley and Lochner (2007)), even after controlling for initial conditions at high school graduation (see, e.g., Leukhina (2023)). Specifically, we seek to connect two broad literatures in macroeconomics and public finance for the study of currently proposed education finance and fiscal policy reforms. The first is concerned with (optimal) redistributive tax-transfer and education policies; see Benabou (2002), Hanushek et al. (2003) and Bovenberg and Jacobs (2005) for foundational papers. Recent papers in this genre focusing on education (financing) reform include Abbott et al. (2019), Caucutt and Lochner (2020), Stantcheva (2017), Capelle (2020), Fu et al. (2023) and also Athreya et al. (2019), Fogli et al. (2023) as well as our own work, Krueger and Ludwig (2016). An important part of this literature studies the impact of tax- and education policy on intergenerational mobility,⁶ see, e.g., Restuccia and Urrutia (2004), Holter (2015), Lee and Seshadri (2019), Koeniger and Prat (2018) and Koeniger and Zanella (2022), and a complementary and equally relevant literature studies (optimal) tax-transfer and poverty alleviation policy (transitions), see, e.g., Boar and Midrigan (2022), Dyrda and Pedroni (2023), Daruich and Fernández (2024), Floden (2001), Ortigueira

⁶Since intergenerational persistence in outcomes is impacted by intergenerational transfers, the empirical literature on these transfers in, e.g., Gale and Scholz (1994), Altonji et al. (1997) and especially Yang and Ripoll (2023) provides important references for the calibration of our the model.

and Siassi (2023), Guner et al. (2020) and Guner et al. (2021).⁷ In contrast to most of this existing literature, this project takes as central tenet that the heterogeneity in initial conditions at labor market entry with respect to human capital and wealth is an endogenous object that can be affected by education and fiscal policies. Thus, it considers education policies as additional means of redistribution, by reducing education and achievement gaps of children from different socio-economic backgrounds and at different stages of the skill formation process. In addition, we seek to contribute to the literature cited above by developing a framework that can distinguish between the incidence of pre-college versus college subsidies while explicitly modeling the complementarity between ability and educational attainment for wages (see Jacobs and Bovenberg (2011) or Stantcheva (2017)) and the dynamic complementarities in child human capital accumulation recently stressed by Cunha et al. (2010).

Therefore, into the above literature we seek to integrate an explicit modeling of life cycle choices with a production function for human capital at different stages of child development. In this regard, the paper builds on a second recent literature in empirical microeconomics and quantitative macroeconomics that models child skill formation and human capital accumulation endogenously, see, e.g., Cunha et al. (2006), Cunha and Heckman (2007), Cunha et al. (2010), Caucutt et al. (2020), Eckstein et al. (2019), Daruich (2022), Blandin and Herrington (2022), Bolt et al. (2023), Yum (2023), Adamopoulou et al. (2024), Bellue and Mahler (2024), and our own work, Fuchs-Schündeln et al. (2022) and Fuchs-Schündeln et al. (2023), to study the dynamic interactions between parental borrowing constraints and public education spending.⁸ On the modeling side we extend this literature by considering the endogenous time allocation choice for both parents between work, leisure and spending time with children of different ages. We also emphasize the importance of general equilibrium effects induced by the policy interventions. On the applied policy side, our main focus lies on the impact of (optimal) policy transitions (permitting government debt) on cross-sectional inequality and intergenerational persistence of economic outcomes, especially those at the lower end of the income and wealth distribution. This in turn requires the explicit model with intergenerational linkages and rich household heterogeneity especially with respect to family marital structure that we provide in this paper. It also highlights the importance of distinguishing the impact of policy reforms in the short run (early in the transition) and in the long run (in the final steady state).

⁷A complementary empirical literature studies the interaction of welfare programs and the education and human capital accumulation of children, see, e.g., Del Boca et al. (2014), Del Boca et al. (2016), National Academies of Sciences and Medicine (2019) and Bailey et al. (2023)

⁸The empirical literature on the impact of day care- and education spending and financing on education and economic outcomes, see, e.g., Havnes and Mogstad (2011), Abramitzky and Lavy (2014), Jackson et al. (2015), Deming and Walters (2017), Johnson and Jackson (2019), Jackson and Mackevicius (2021), Black et al. (2020), Duncan et al. (2022) and Flood et al. (2022) (as well as the survey by Handel and Hanushek (2022)) will provide key targets for our structural model.

2 The Quantitative Model

2.1 Overview

We employ a general equilibrium overlapping generations (OLG) model in which generations are linked through the intergenerational transmission of innate ability and financial wealth transfers. Parents are altruistic towards their children, solve a unitary decision problem and can invest time and monetary resources into the human capital accumulation of children when the latter are still living with their parents. In addition, parents can transfer wealth to children directly when they leave the parental household. The government collects taxes, runs a PAYGO social security system and finances exogenous government spending and endogenous education spending with taxes and government debt, subject to an intertemporal budget constraint and a period-per-period social security budget constraint. In general equilibrium the goods-, labor- and asset markets have to clear in every period along a policy-reform induced transition.

Relative to the standard quantitative life cycle literature our model contains three key additional features. First, households have children whose human capital accumulation during the transition from childhood to adolescence is endogenous and depends both on public schooling and private parental inputs. This element of the model is crucial for a study of education policies that differ in the extent to which primary/secondary and tertiary education is impacted and fiscal policies that impact the trade-off between market work (including participation) and time investment into children.⁹ Second, generations in our model are linked through “brains and bucks”, that is, human capital inputs and financial transfers from parents to children. With this model element, parents have endogenous margins of adjustment in direct response to education policy reforms. If college will be free, private inter-vivos transfers (and the accumulation of parents assets to make these transfers) will endogenously adjust. When public schools become better, private time and resource inputs can respond as well. Third, modeling both married households but also single mothers allows us to explicitly account for a group of children that disproportionately grow up in poverty and are the least likely to go to college, both because of financial constraints and due to poor pre-college academic achievement, at least on average.¹⁰

⁹The presence of government transfer- and social assistance programs whose importance varies by family structure renders the explicit modeling of an extensive margin (for both partners of a married couple) important as the recent work by [Guner et al. \(2012\)](#), [Bick and Fuchs-Schündeln \(2017\)](#) and [Holter et al. \(2023\)](#) suggests.

¹⁰The model abstracts from single fathers, given that this group constitutes a negligible share of the population in the data.

2.2 Individual State Variables

In order to meaningfully study the distributional consequences of the proposed policy reforms the model features rich cross-sectional heterogeneity, best described in terms of the individual state variables that characterize households. These are summarized in Table 1, including the range of values these state variables can take.

Table 1: Individual State Variables

State Var.	Values	Interpretation
j	$j \in \{0, 1, \dots, J\}$	Model Age
g	$g \in \{wo, ma\}$	Gender
h	$h > 0$	Human Capital
a	$a \geq -a(j, s)$	Financial Assets
s, s_p	$s \in \{hsd, hs, cod, co\}$	(Higher) Education
γ	$\gamma \in \{\gamma_l(s), \gamma_h(s)\}$	Fixed Productivity Component
η	$\eta \in \{\eta_l, \eta_h\}$	Persistent Productivity Shock
q	$q \in \{si, cpl\}$	Marital Status

Individuals differ by age j and young households start their independent economic life as singles and with four ex-ante predetermined state variables: gender (either being a woman or a man, $g \in \{wo, ma\}$), the education of their parents s_p (which determines their cost of attending college) initial human capital (h) and initial assets (a). Upon realization of the high school dropout shock and after an individual has taken its own higher education decision s , which is subject to college dropout risk, the highest completed education level also becomes a state variable (and that of the parent ceases to be relevant). Upon labor market entry, the acquired human capital stochastically translates into a discrete-valued fixed effect γ with education-specific support.¹¹ Labor productivity is also impacted by a persistent stochastic component η which is part of the state space. Finally, one period before children are born into a household, the marital status q of a household realizes and becomes a state variable, as a fraction of single households marry ($q = cpl$ for “couples”) while the rest remains single ($q = si$). Finally, when children are born into a household, their human capital h becomes a state variable as well.¹² In terms of notation, for married households the education and labor productivity of both partners are state variables, and the notation s_{-g} and γ_{-g} denotes the state variable of the “other” spouse.

¹¹The stochastic mapping from human capital h to the fixed labor productivity γ replaces the continuous state variable h with the discrete-valued variable γ , which reduces the dimensionality of the state space.

¹²At that time fixed productivity γ has replaced parental human capital, and thus there is no scope for confusion between parental and child human capital in a household.

2.3 Demographics, Timing and Economic Decisions

Time is discrete, indexed by t and extends to infinity, where each model period corresponds to four real years. In every period t the economy is populated by J overlapping generations. Individuals survive from age j to age $j + 1$ with probability ϕ_{j+1} . Before retirement survival is certain while from the exogenous retirement age j_r onward survival risk becomes relevant, and individuals live at most until age J . Assets of households that die at age j are distributed in a lump-sum fashion among all working age households.¹³ Transfers from accidental bequests are denoted by $Tr_{t,j}$.

Figure 1 provides a summary of the household lifecycle. Children are born at age $j = 0$, corresponding to biological age 2 (the first two years of a child's life cycle remain un-modelled). At parental fertility age j_f a number of $\varsigma(s(wo))$ identical children is born; that number depends on the education level $s(wo)$ of the mother. The initial human capital h_0 of each child is also a function of $(q, s(wo))$. Children stay in the parental household and accumulate human capital depending on their initial human capital and the time and resource input of their parents, for a given level of the public schooling input, as described below. These parental investments are referred to as private human capital investments. When children leave the parental household parents give them (non-negative) inter-vivos transfers b which can be used for consumption and/or for covering college expenses.

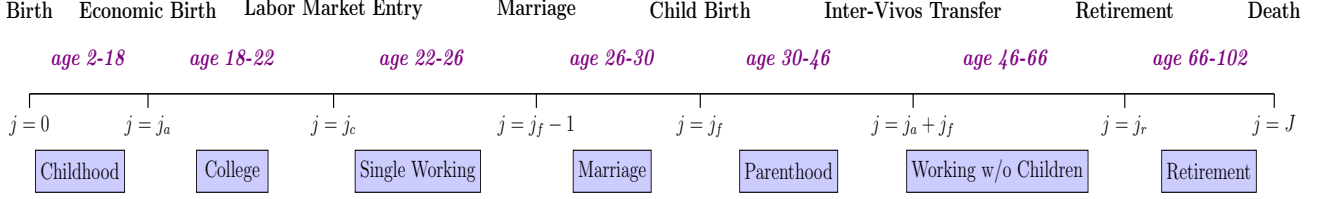
At model age j_a (biological age 18) children form their own households. They first graduate from high school with probability $\pi^{hs}(h)$ that depends on the human capital accumulated in school. Conditional on having a high-school diploma they then make their college enrollment decision. Young adults who choose college spend one model period for education, the other group starts working directly at age j_a . Dropping out of college is both a choice and subject to dropout risk, a shock, but given the four-year periodicity of the model both happen during the same time period, at age j_a . Specifically, conditional on choosing to enroll in college there is an additional decision to become a college dropout.¹⁴ Next, conditional on opting to continue, students successfully graduate with probability $\pi^{co}(h)$. College dropouts are assumed to have to pay only half of the tuition cost than college graduates, and they also face a correspondingly tighter borrowing limit.

After the education decision is taken all education groups draw a education group-specific fixed productivity component $\gamma(s)$ for the labor market, which, for each education group s , has two realizations, high and low. College students and dropouts can work-part time at high-

¹³To be more precise, what is redistributed among surviving households are the accidental bequests net of the amount needed to finance private college subsidies.

¹⁴In our model it is possible for individuals to have higher expected lifetime utility from becoming a college dropout than being only a high school graduate (because of higher wages) and than continuing with college (because of lower tuition cost and disutility from studying).

Figure 1: Lifecycle: Timeline



school wages during the college period.¹⁵ The probability of drawing a high realization of the fixed effect is an increasing function of acquired human capital h and education group specific, denoted by $\pi^\gamma(s, h)$. After education is completed all households enter the labor market. Upon labor market entry acquired human capital h ceases to be a state variable for all education groups. College graduates and college dropouts then redraw their fixed productivity component from a domain associated with their newly obtained higher education level.

During the working life, households make a discrete decision whether to work, and conditional on employment, make a continuous intensive margin hours choice. One period before the fertility age, at age $j_m = j_f - 1$ households face an exogenous (education specific) probability of marriage, and depending on the realization of the marriage shock continue to live either as singles or as couples. Table 2 summarizes all choice variables (and the ages at which these decisions are made).

Table 2: Decision Variables

Control Var.	Values	Decision Period	Interpretation
c	$c > 0$	$j \geq j_a$	Consumption
ℓ	$\ell \geq 0$	$j \geq j_a$	Hours worked (for couples $\ell(wo)$ and $\ell(ma)$)
a'	$a' \geq -a(j, s)$	$j \geq j_a$	Asset Accumulation
i^t	$i^t \geq 0$	$j \in \{j_f, \dots, j_f + j_a\}$	Time Investments (for couples $i^t(wo)$ and $i^t(ma)$)
i^m	$i^m \geq 0$	$j \in \{j_f, \dots, j_f + j_a\}$	Monetary Investments
b	$b \geq 0$	$j = j_f + j_a$	Monetary Inter-vivos Transfer
s	$s \in \{hsd, hs, cod, co\}$	$j = j_a$	(Higher) Education

Notes: List of decision variables of the economic model.

¹⁵This means that both the aggregate wage level as well as the fixed productivity component are the same as for high school graduate workers.

2.4 Human Capital

Human Capital Accumulation during Childhood. In every period during childhood human capital accumulation takes places according to the following production function:

$$h' = g(j, h, i^m, i^t, i^g), \quad (1)$$

where i^t and i^m denote parental time and monetary investment, while i^g denotes public investment. A subset of the parameters in the human capital production function will be allowed to vary by age j for calibration purposes, in order to capture differences in the relative importance of private time and resource inputs (as well as public schooling) at different stages of childhood. For married households the time investment i^t is a composite of the time inputs of both parents, which are assumed to be perfectly substitutable:

$$i^t = i^t(wo) + i^t(ma) \quad (2)$$

where $i^t(wo)$ and $i^t(ma)$ denote the time inputs of a woman and of a man, respectively.

2.5 Labor Productivity

The wage of a single household at age j , of gender g with an education level s and with a fixed productivity component realization $\gamma(s)$ is given by:

$$w(s, \gamma(s), g, j) = w(s) \cdot \gamma(s) \cdot \epsilon(s, g, j) \cdot \eta \quad (3)$$

where $w(s)$ is an aggregate education specific wage component, cf. Section 2.7, $\gamma(s)$ is a fixed household productivity component, $\epsilon(s, g, j)$ is a deterministic gender- and education-specific productivity profile, and η denotes a potentially persistent productivity shock.

2.6 Decision Problems

All household decision problems below are cast in recursive formulation, with variables expressed in per capita terms and detrended by the rate of technological progress μ .

2.6.1 Young Adults and the Education Decision at Age j_a

Since children born at age $j = 0$ are economically inactive until age $j = j_a - 1$ and simply accumulate human capital as a result of parental decisions, the youngest age at which economic choices are made is model age j_a (biological age 18) when children have become young adults and

have formed independent households. At that age their initial state is (j_a, g, s_p, a, h) , comprised of age j_a , gender g , parental education s_p , financial assets a and human capital h .

Now the tertiary education level is determined, partially by choice and partially by chance. It takes four values, as individuals can be high-school dropouts (hsd), high-school graduates (hs), college dropouts (cod) and college graduates (co). First, high school graduation is exogenous from the perspective of the newly founded household but stochastic: with probability $\pi^{hs}(h)$, with $\pi_h^{hs}(h) > 0$, the individual obtains a high-school diploma and with complementary probability it becomes a high-school dropout, with continuation lifetime utility $V_t(j_a, g, hsd; a, h)$, which does not depend on parental education s_p , because the latter only affects psychological (or, utility) costs of college attendance (see below).

A high-school graduate can choose to attend college, and conditional on enrollment may either graduate or drop out. Attending college is costly, both in terms of tuition (which is potentially subsidized by the government and can be financed by student loans and parental transfers) as well as in terms of the opportunity cost of time and the psychological (utility) cost of studying, which depend on their acquired human capital h and on the education of their parents s_p . For those deciding to try to graduate from college, their ability to do so is subject to exogenous (but human-capital dependent) drop-out risk: individuals succeed in college only with probability $\pi^{co}(h)$, with $\pi_h^{co}(h) > 0$. Individuals weigh these costs against the benefits of higher wages upon college graduation. College students (both those who will graduate and those who will drop out) can work part-time at high school wages, and thus during college the productivity $\gamma(hs)$ is a relevant state variable.¹⁶

The college attendance choice can then be written as¹⁷

$$s = \begin{cases} hs & \text{if } V_t(j_a, g, hs; a, h) \geq V_t(j_a, g, ce, s_p; a, h) \\ ce & \text{if } V_t(j_a, g, ce, s_p; a, h) > V_t(j_a, g, hs; a, h), \end{cases} \quad (4)$$

where only the college enrollment value function is indexed by parental education s_p , because of the dependency of psychological attendance costs on parental education, and where $V_t(j_a, g, ce; s_p, a, h)$ is the pre-dropout college *attendance* value function given by

$$V_t(j_a, g, ce, s_p; a, h) = \max_{s \in \{cod, co\}} \{V_t(j_a, g, cod, s_p; a, h), \pi^{co}(h) \cdot V_t(j_a, g, co, s_p; a, h) + (1 - \pi^{co}(h)) \cdot V_t(j_a, g, cod, s_p; a, h)\}, \quad (5)$$

¹⁶College drop-outs also pay smaller tuition costs and face a tighter borrowing limit than college graduates.

¹⁷In the computational implementation we apply Extreme Value Type I (Gumbel) taste shocks to smooth out this discrete decision problem (see e.g. [Iskhakov et al. \(2017\)](#) for a discussion of numerical advantages of Gumbel shocks in discrete-continuous dynamic applications). The taste shifters are purely a computational device, and the scale parameter of Gumbel shocks is set to 0.05.

so that individuals who prefer to drop out of college (from an ex-ante perspective) always do so. Finally, the pre-college enrollment decision value function at age j_a is given by

$$V_t(j_a, g, s_p; a, h) = (1 - \pi^{hs}(h)) \cdot V_t(j_a, g, hsd; a, h) + \pi^{hs}(h) \cdot \max_{s \in \{hs, ce\}} \{V_t(j_a, g, hs; a, h), V_t(j_a, g, ce, s_p; a, h)\}. \quad (6)$$

2.6.2 First Period of Working Life / College Period

At the beginning of the first period of independent economic life, realizations of the fixed productivity component and idiosyncratic productivity shocks are drawn. Thus, in the first period of economic life the decision problem can be split in two sub-periods. In the first sub-period, the fixed productivity component and the persistent income shock are drawn:

$$V_t(j_a, g, s, s_p; a, h) = \sum_{\gamma} \pi^{\gamma}(s, h) \sum_{\eta} \Pi(\eta) V_t(j_a, g, s, s_p; a, h; \gamma, \eta)$$

where γ denotes education-specific realizations of the fixed productivity component, and η is the persistent productivity shock realization. For households that neither enroll in college nor complete it, from this point in time onward acquired human capital ceases to be a state variable and is replaced by the fixed effect $\gamma(s)$. Since college students work at high school wages during the college phase, for them γ has to be redrawn at the end of the college period.

After the fixed effect is drawn, a standard consumption-savings problem with endogenous labor supply is solved. For households that choose not to enroll in college, the decision problem is identical to the one described in the next subsection 2.6.3. For households that complete college, the decision problem is slightly modified because they redraw the fixed productivity component given their newly obtained higher education level, incur psychological and financial costs of attending college, can work only up to maximum $\bar{\ell}^{ce}$ and also are allowed to borrow:

$$V_t(j_a, g, s, s_p; a, h; \gamma(hs), \eta) = \max_{c, a', \ell \leq \bar{\ell}^{ce}} \left\{ u(c, \ell) - F(g)_{\ell > 0} - p(s, s_p; h) + \beta \sum_{\gamma'} \pi^{\gamma'}(co, h) \sum_{\eta'} \pi(\eta' | \eta) V_{t+1}(j+1, g, s; a'; \gamma'(co), \eta') \right\}$$

subject to

$$\begin{aligned} a'(1 + \mu) + c(1 + \tau^c) + T(y(1 - 0.5\tau^p)) + \iota(1 - \vartheta - \vartheta^{pr}) &= (a + Tr_{t,j})(1 + r(1 - \tau^k)) + y(1 - \tau^p) \\ y &= w(s)\gamma(s)\epsilon(s, g, j)\eta\ell \\ a' &\geq -\underline{a}(s, j), c \geq 0, \ell \in [0, \bar{\ell}^{ce}]. \end{aligned}$$

where $p(s, s_p; h)$ is the psychological (utility) cost of attending college, and $\iota(1 - \vartheta - \vartheta^{pr})$ is the tuition cost net of public and private subsidies. $F(g)_{\ell > 0}$ denotes a fixed utility cost of working positive hours which depends on individual's gender.

Households that enroll in college but drop out solve the same problem as above with the only difference that they are assumed to pay only half of the tuition costs.

2.6.3 Working Life Before Marriage

After completing (or not) their tertiary education single individuals enter the labor market and make labor supply as well as consumption-saving choices (c, a', ℓ) , in light of their labor productivity, which is determined by the individual fixed effect γ , a deterministic education-, gender- and age-specific life cycle profile $\epsilon(s, g, j)$ and a persistent stochastic component η . With probability $\pi^\gamma(s; h)$ permanent productivity is $\gamma = \gamma_t(s)$ and with complementary productivity it is $\gamma = \gamma_h(s)$. The wage of a single individual is then given by $w(s) \cdot \gamma(s) \cdot \epsilon(s, g, j) \cdot \eta$, where $w(s)$ is the education-specific aggregate wage per efficiency unit of labor.

During working life, households make the discrete decision whether to work, and conditional on employment endogenously choose hours worked subject to a time endowment constraint. The decision problem of singles can then be written as

$$V_t(j, g, s; a; \gamma, \eta) = \max_{c, a', \ell} \left\{ u(c, \ell) - F(g)_{\ell > 0} + \beta \sum_{\eta'} \pi(\eta' | \eta) V_{t+1}(j + 1, g, s; a'; \gamma, \eta') \right\} \quad (7)$$

subject to

$$\begin{aligned} a'(1 + \mu) + c(1 + \tau^c) + T(y(1 - 0.5\tau^p)) &= (a + Tr_{t,j})(1 + r(1 - \tau^k)) + y(1 - \tau^p) \\ y &= w(s)\gamma(s)\epsilon(s, g, j)\eta\ell \\ a' &\geq -\underline{a}(s, j), c \geq 0, \ell \geq 0, \end{aligned}$$

where $\underline{a}(s, j)$ is an age- and education-specific borrowing limit and $F(g)_{\ell > 0}$ denotes a fixed, gender-specific utility cost of working positive hours. The household takes as given aggregate wages and interest rates $(w(s), r)$ as well as the proportional tax rates on consumption, asset income and labor income for social security (τ^c, τ^k, τ^p) , the nonlinear labor income tax schedule $T(\cdot)$ and well as the transfers Tr_j . Labor income taxes are levied on labor income net of employer contributions to social security $y(1 - 0.5\tau^p)$.

2.6.4 Marriage

Individuals remain single, until at age j_m (and at that age only) they face an exogenous, education-specific probability $\pi^m(s)$ of marriage, where we assume random matching so that the marriage probability only depends on own education s . Depending on the realization of the marriage shock individuals continue to live as singles or form a new married household. Since a married household is characterized by the education and wage fixed effect of both spouses as well as their combined financial asset positions (all of which are at least partially the result of endogenous choices), at age $j_m - 1$ a single individual has to form expectations over the type of spouse it might marry (and these expectations have to be confirmed in a rational expectations equilibrium, inducing an additional equilibrium fixed point problem). Recalling that state variables of the spouse of the opposite gender are indexed by $-g$, the decision problem at model age $j_m - 1$, in anticipation of potential marriage next period, is given by:

$$\begin{aligned}
V_t(j_m - 1, g, s; a; \gamma, \eta) = & \max_{c, a', \ell} \{ u(c, \ell) - F(g)_{\ell > 0} \\
& + \beta (\pi^m(s) \mathbf{E}_{s(-g), a'(-g), \gamma(s(-g))} \sum_{\eta'(wo)} \Pi(\eta'(wo)) \sum_{\eta'(ma)} \Pi(\eta'(ma)) \cdot \\
& V_{t+1}(j_m, cpl, s(wo), s(ma); a'(wo) + a'(ma); \gamma(s(wo)), \gamma(s(ma)), \eta'(wo), \eta'(ma)) \\
& \left. + (1 - \pi^m(s)) \cdot \sum_{\eta'} \pi(\eta' | \eta) V_{t+1}(j_m, si, g, s; a'; \gamma, \eta') \right\}
\end{aligned}$$

where $\mathbf{E}_{s(-g), a'(-g), \gamma(s(-g))}(\cdot) = \int (\cdot) d\Phi(j_m - 1, -g, s; a'(-g); \gamma(s(-g)))$, i.e. the expectation over the characteristics of potential spouses is determined by the cross-sectional measure and savings policy functions of the opposite gender households in period $j_m - 1$. The maximization problem is subject to the following constraints

$$\begin{aligned}
a'(1 + \mu) + c(1 + \tau^c) + T(y(1 - 0.5\tau^p)) &= (a + Tr_{t,j})(1 + r(1 - \tau^k)) + y(1 - \tau^p) \\
y &= w(s)\gamma(s)\epsilon(s, g, j)\eta\ell \\
a' &\geq -\underline{a}(s, j), c \geq 0, \ell \geq 0.
\end{aligned}$$

2.6.5 Parenthood and Child Human Capital Accumulation

At age $j_f > j_m$ children enter single women- and married households (single men do not live with children). The number of children per household is a function of the mother's marital status and education level, and is denoted by $\zeta(s(wo))$. All children of a household are assumed to be identical and characterized initially by a level of human capital h that depends on parental education and marriage status (s, q) . As long as children are present, parents invest time and

resources (i^m, i^t) into the production of new child human capital; we term these *private* human capital investments. For married couples, time investment is the sum of time devoted to their children by both partners, $i^t = i^t(wo) + i^t(ma)$. Time investments bear a utility cost for households, which depends on the number of children $\zeta(s(wo))$. The period utility function is therefore $u(c, \ell, i^t, s(wo))$. Finally, when children leave the household, parents can give them non-negative inter-vivos transfers b to finance tertiary education (or their consumption).

In every period during childhood private human capital investments are combined with *public* investment into schooling to transform existing child human capital h into new human capital h' according to the following age-dependent production function $h' = g(j, h, i^m, i^t, i^g)$. For single women, the decision problem during this stage of the life cycle then is

$$V_t(j, si, wo, s; a, h; \gamma, \eta) = \max_{c, i^m, i^t, a', h', \ell} \left\{ u(c, \ell, i^t, s(wo)) - F(wo)_{\ell > 0} + \beta \sum_{\eta'} \pi(\eta' | \eta) V_{t+1}(j + 1, si, wo, s; a', h'; \gamma, \eta') \right\} \quad (8)$$

$$\begin{aligned} a'(1 + \mu) + c(1 + \tau^c) + \zeta(s) \cdot i^m + T(y(1 - 0.5\tau^p)) &= (a + Tr_{t,j})(1 + r(1 - \tau^k)) + y(1 - \tau^p) \\ y &= w(s)\gamma(s)\epsilon(s, g, j)\eta\ell \\ a' &\geq -\underline{a}(j, s), c \geq 0, \ell \geq 0 \\ h' &= g(j, h, i(i^m, i^t, i^g)), i^m \geq 0, i^t \geq 0. \end{aligned}$$

Since single men are assumed not to have children present in the household, they solve the same maximization problem as in (7).

For couples, participation, hours worked and the time investment of both spouses are choice variables, and thus the dynamic programming problem of the household reads as:

$$\begin{aligned} V_t(j, cpl, s(wo), s(ma); a, h; \gamma((wo)), \gamma((ma)), \eta(wo), \eta(ma)) = \\ \max_{c, i^m, i^t(wo), i^t(ma), a', h', \ell(wo), \ell(ma)} \left\{ u(c, \ell(wo), \ell(ma), i^t(wo), i^t(ma), s(wo)) \right. \\ \left. - F(wo)_{\ell(wo) > 0} - F(ma)_{\ell(ma) > 0} + \beta \sum_{\eta'(wo)} \pi(\eta'(wo) | \eta(wo)) \sum_{\eta'(ma)} \pi(\eta'(ma) | \eta(ma)) \cdot \right. \\ \left. V_{t+1}(j, cpl, s(wo), s(ma); a', h'; \gamma(s(wo)), \gamma(s(ma)), \eta'(wo), \eta'(ma)) \right\} \end{aligned}$$

subject to

$$\begin{aligned}
a'(1 + \mu) + c(1 + \tau^c) + \varsigma(s(wo)) \cdot i^m + T^{cpl}(y(1 - 0.5\tau^p)) &= (a + 2 \cdot Tr_{t,j})(1 + r(1 - \tau^k)) + y(1 - \tau^p) \\
y &= w(s(wo))\gamma(s(wo))\epsilon(s(wo), wo, j)\eta(wo)\ell(wo) + w(s(ma))\gamma(s(ma))\epsilon(s(ma), ma, j)\eta(ma)\ell(ma) \\
a' &\geq -\underline{a}(j, \max(s(wo), s(ma))), c \geq 0, \ell(g) \geq 0 \text{ for } g \in \{ma, wo\} \\
h' &= g(j, h, i(i^m, i^t, i^g)), i^t = \sum_{g \in \{ma, wo\}} i^t(g), i^t(g) \geq 0 \text{ for } g \in \{ma, wo\}, i^m \geq 0,
\end{aligned}$$

where $T^{cpl}(\cdot)$ is the labor income tax function it faces.

2.6.6 Children Leaving the Household and Inter-Vivos Transfers

When children are of age j_a (and their parents of age $j_f + j_a$) they form their own households. At the beginning this period a one time inter-vivos transfer b can be made by the altruistically motivated parents; these transfers become assets of children within the same model period.¹⁸ In the interest of brevity, only the dynamic programs of single mothers are presented from this stage of the life cycle; the optimization problems of married couples are similar to those of singles. At age $j_a + j_f$ the dynamic program of single mothers is given by:

$$\begin{aligned}
V_t(j_a + j_f, si, wo, s; a, h; \gamma, \eta) &= \max_{c, b, a', \ell} \{u(c, \ell) - F(g)_{\ell > 0} \\
&+ \beta \sum_{\eta'} \pi(\eta' | \eta) V_{t+1}(j_a + j_f + 1, si, wo, s; a'; \gamma, \eta') \\
&+ \nu \mathbf{E}_{g^{ch}} V_t \left(j_a, si, g^{ch}, s; \frac{b}{1 + r(1 - \tau^k)}, h \right) \},
\end{aligned}$$

where $V_t \left(j_a, g^{ch}, s; \frac{b}{1 + r(1 - \tau^k)}, h \right)$ denotes the pre-education decision value function of a child with gender g^{ch} , parental education s , human capital h and assets $a = b/(1 + r(1 - \tau^k))$, noting that the transfer accrues to the newly independent child at the beginning of the current period and thus already earns interest concurrently. The parameter ν measures the strength of altruism of a parent. Maximization is subject to

$$\begin{aligned}
c(1 + \tau^c) + (1 + \mu)a' + \varsigma(s) \cdot b + T(y(1 - 0.5\tau^p)) &= (a + Tr_{t,j})(1 + r(1 - \tau^k)) + y(1 - \tau^p) \\
y &= w(s)\gamma(s)\epsilon(s, g, j)\eta\ell \\
a' &\geq -\underline{a}(s, j), c \geq 0, b \geq 0, \ell \geq 0.
\end{aligned}$$

¹⁸Since girls and boys have different expected lifetime utilities, parents may find it optimal to condition transfers on gender. In order to avoid having to carry child gender as a state variable, we assume that parents are constrained to treat girls and boys equally, or equivalently, learn the gender of children only when the leave the household. Thus, the expected lifetime utility of their offspring entails taking expectations with respect to the gender of the child.

After children have left the household, parental households continue solving a consumption-savings problem with endogenous labor supply until they reach retirement:

$$V_t(j, si, wo, s; a; \gamma, \eta) = \max_{c, a', \ell} \left\{ u(c, \ell) - F(g)_{\ell > 0} + \beta \sum_{\eta'} \pi(\eta' | \eta) V_{t+1}(j+1, si, wo, s; a'; \gamma, \eta') \right\}$$

subject to

$$\begin{aligned} a'(1 + \mu) + c(1 + \tau^c) + T(y(1 - 0.5\tau^p)) &= (a + Tr_{t,j})(1 + r(1 - \tau^k)) + y(1 - \tau^p) \\ y &= w(s)\gamma(s)\epsilon(s, g, j)\eta\ell \\ a' &\geq -\underline{a}(s, j), c \geq 0, \ell \geq 0. \end{aligned}$$

2.6.7 Retirement and Death

In retirement, that is after reaching the model age j_r , households solve a standard consumption-saving problem, receive social security benefits $pen(s, \gamma, \eta(j_r - 1))$ and face mortality risk (until they die for sure at maximal lifetime J). The problem is

$$V_t(j, si, g, s; a; \gamma, \eta) = \max_{c, a' \geq 0} \{u(c) + \beta\phi(j)V_{t+1}(j+1, si, g, s; a'; \gamma, \eta)\}$$

subject to

$$\begin{aligned} a'(1 + \mu) + c(1 + \tau^c) &= (a + Tr_{t,j})(1 + r(1 - \tau^k)) + pen(s, \gamma, \eta) \\ a' &\geq 0, c \geq 0, \end{aligned}$$

where $pen(s, \gamma, \eta(j_r - 1))$ is retirement income which depends on education-specific wages $w(s)$, the persistent shock realization in the last working period¹⁹ before retirement η , the education level s and the fixed productivity component γ .

2.7 Production

We assume exogenous labor augmenting technological progress through $\Upsilon_{t+1} = \Upsilon_t(1 + \mu)$, $\Upsilon_0 = 1$. A representative firm employs aggregate labor L_t and capital K_t to produce the final output good Y_t —both, K_t and Y_t are expressed in de-trended units—employing a neo-classical

¹⁹This construction allows us to capture the progressivity embedded in the actual US social security benefit formula without carrying around another continuous state variable during working age.

production function

$$Y_t = F(K_t, L_t). \quad (9)$$

Aggregate labor L_t at time t is the aggregate of college $L_{t,co}$ and non-college $L_{t,nc}$ labor

$$L_t = H(L_{t,nc}, L_{t,co}). \quad (10)$$

where $L_{t,nc} = L_{t,hsd} + L_{t,hs} + L_{t,cod}$ are the labor units jointly supplied by high-school dropouts, high-school graduates and college dropouts. Function $H(\cdot)$ captures imperfect substitutability across education groups nc and co giving rise to education specific aggregate wages $w(s)$.

2.8 Government

The government administers a progressive labor income tax code, pays transfers to households and collects linear taxes on consumption and capital income. Aggregate labor income tax revenues net of transfers are denoted by T_t . In addition, the government spends $\alpha_j i^g$ per child on primary and secondary school education. The age profile α_j permits us to differentiate between the cost of primary and secondary school and i^g measures the scale of public education spending, and will be one key policy choice by the government. Total spending on primary and secondary public schools is denoted by E_t . The government also subsidizes tertiary education, with the share ϑ of tuition covered by the government; ϑ is the second crucial policy choice variable, and a choice of $\vartheta = 1$ represents free college. We denote by E_t^{CL} the aggregate cost of college subsidies.

In addition to the endogenous streams of education expenditures (E_t, E_t^{CL}) for primary, secondary and tertiary education the government also needs to finance an exogenous stream of non-education related expenditures G_t . To do so, the government raises revenues from taxing labor- and capital income as well as consumption, and from issuing government debt B_t . The period t flow government budget constraint then is²⁰

$$E_t + E_t^{CL} + G_t + (1 + r_t)B_t = (1 + \mu)(1 + n_t)B_{t+1} + T_t + \tau_{c,t}C_t + \tau_{k,t}r_t(K_t + B_t) \quad (11)$$

The initial stock of government debt B_0 is an exogenously given initial condition (as is the initial aggregate capital stock K_0). Finally, the government also runs a pure pay-as-you-go social

²⁰Recall that we define all aggregate variables as de-trended objects, so that the debt level in period $t + 1$ needs to be trend-adjusted by the growth rate of aggregate variables, $(1 + n_t)(1 + \mu)$. Also note that the population growth rate is time varying, because of education specific fertility $\varsigma(s)$ and endogenously time varying education shares, cf. Appendix B.

security system whose budget equates payroll taxes (with tax rate τ^p) to all pension benefits paid out according to the benefit formula $pen(s, \gamma, \eta)$.

3 Equilibrium Definition and Computation

The key equilibrium object in our model is the cross-sectional measure Φ_t over household characteristics²¹ $(j, q, g, s; a, h; \gamma, \eta)$. For each time period t and age j we normalize the total measure $\Phi_t(j, \cdot)$ to 1 and denote by N_j the (time-invariant) size of age cohort j .

$$\int d\Phi_t(j, si, g, s; a, h; \gamma, \eta) + \int d\Phi_t(j, cpl, s(ma); a, h; \gamma(wo), \gamma(ma), \eta(wo), \eta(ma)) = 1 \quad (12)$$

In order to clarify the distinction between the partial- and the general equilibrium versions of the model it is necessary to give a somewhat formal definition of equilibrium.

3.1 Equilibrium Definition

For given initial physical capital stock and government debt (K_0, B_0) and initial cross-sectional distributions of singles $\{\Phi_0(j, si, \cdot)\}_{j_a}^J$ and couples $\{\Phi_0(j, cpl, \cdot)\}_{j_m}^J$ a competitive equilibrium is given by sequences of household value and policy functions (for consumption, assets, labor supply, child human capital investments and bequests), aggregate capital and labor inputs, tax and transfer policies and government debt levels, aggregate prices, accidental bequests as well as household measures such that

1. In each period, household value and policy functions solve the household optimization problems, given factor prices, government policies and accidental bequests.
2. Denoting the exogenous depreciation rate of capital by δ , factor prices for capital and college- as well as non-college labor per efficiency unit satisfy

$$r_t = F_K(K_t, G(L_{t,co}, L_{t,nc})) - \delta \quad (13a)$$

$$w_{s,t} = F_{L_{s,t}}(K_t, G(L_{t,co}, L_{t,nc})), \quad \text{for } s \in \{co, nc\}. \quad (13b)$$

²¹It is understood that, depending on the age j of the household as well as its marital status q , the household state space changes; for example, for couples it includes the education and fixed effect of both partners.

3. The government budget constraint (11) and the social security system budget constraint hold $\forall t$:

$$\tau_t^p \sum_{s \in \{co, nc\}} w_{s,t} L_{s,t} = \sum_{j=j_r}^J N_j \int pen_t(\cdot) d\Phi_t(j, \cdot) \quad (14)$$

4. Markets clear in all periods t ²²:

$$L_{co,t} = \sum_{j_a}^{j_r-1} N_j \int \gamma \epsilon(co, g, j) \eta \ell_t(j, co, \cdot) d\Phi_t(j, co, \cdot) \quad (15a)$$

$$L_{nc,t} = \sum_{j_a}^{j_r-1} N_j \sum_{s \in \{hsd, hs, cod\}} \int \gamma(s) \epsilon(s, \cdot, j) \eta \ell_t(j, s, \cdot) d\Phi_t(j, s, \cdot) \quad (15b)$$

$$K_{t+1} + B_{t+1} = \sum_{j=j_a}^J N_j^J \int a'_t(j, \cdot) d\Phi_t(j, \cdot) \quad (15c)$$

$$C_t + K_{t+1}(1 + n_t)(1 + \mu) + CE_t + E_t + G_t = F(K_t, L_t)L_t + (1 - \delta)K_t, \quad (15d)$$

where L_t was defined in (10) and CE_t are aggregate private education expenditures.

5. The marriage market clears:

$$\sum_{s(g) \in \{hsd, hs, cod, co\}} \pi^m(s(g)) \cdot \int \Phi_t(j_m - 1, si, g, s(g), \cdot) = \sum_{s(-g) \in \{hsd, hs, cod, co\}} \pi^m(s(-g)) \cdot \int \Phi_t(j_m - 1, si, -g, s(-g), \cdot).$$

6. The total accidental bequests received by the working age population in period $t + 1$ are equal to the total assets those passing away in period t net of private college subsidies

$$\sum N_{t+1, j_{j_a}^{j_r-1}} Tr_{t+1, j} = \sum N_{t, j_{j_r}^J} \int (1 - \phi_j) a'_t(j, \cdot) d\Phi_t(j, \cdot) \quad (16)$$

7. The cross-sectional measures of households evolve according to the laws of motion induced by exogenous population dynamics, the exogenous Markov processes for idiosyncratic labor productivity, the exogenous distribution of transitory shocks, endogenous asset and child human capital accumulation, higher education and inter-vivos transfer decisions, both at the age of marriage and at all other ages.

²²Recall that we need to trend adjust variables in period $t + 1$, cf. footnote 20.

8. The initial measure of newly formed households $\Phi_t(j_a, si, \cdot)$ at age j_a is consistent with inter-vivos transfers and human capital investment decisions of parents and the measure of economic newborns at age j_a after the higher education choice is made.
9. At age $j_m - 1$ prior to marriage expectations of singles about characteristics of future spouses are consistent with the cross-sectional distribution of the opposite gender at age $j_m - 1$.

3.2 Solution Algorithm

We propose to solve for (optimal) policy transitions in a model characterized by non-convex household maximization problems involving discrete and continuous decision variables as well as a sizable individual state space, and in which there are two nested fixed-point problems even in partial equilibrium, one emerging from the intergenerational linkages (the value function of children enters lifetime utility of their altruistic parents) and one from the marriage market equilibrium (types of pre-marriage singles are endogenous and have to match and conform to household expectations). The solution of market clearing prices in steady state and along the transition path is then relatively standard; our description here focusses on the more novel fixed point problems in steady state.²³

Modeling of marriage requires that the marriage market clears which results in a fixed point problem in distributions. Assuming rational expectations implies that before the marriage period expectation of assets and productivity of a future spouse should be consistent with the cross-sectional distribution of assets and productivity of the opposite gender, $\Phi(j_{m-1}, si, g, s; a; \gamma(s))$. Recall that due to explicitly modelled intergenerational altruism, the initial measure of economic newborns $\Phi(j_a, si, \cdot)$ must be consistent with inter-vivos transfers and human capital investment decisions of parents. This implies a second fixed point problem in distributions. Additionally, the value function of the child generation at age j_a should be consistent with the value function of the parental generation at age j_a which turns the finite horizon life cycle problem of each generation into an infinite horizon problem over time. Given that each iteration of the latter fixed point problem is affected by $\Phi(j_{m-1}, si, g, s, a, \gamma(s))$ the three fixed point problems (one in value functions and two in measures) have to be solved jointly. To deal with this multi-layer fixed point problem, we propose Algorithm 1.

²³The algorithm for the household problem is a combination of the discrete-continuous endogenous grid method described in [Iskhakov et al. \(2017\)](#)), embedded in a value function iteration algorithm that draws on [Druehl \(2021\)](#).

Algorithm 1 Nested Fixed Point Problem

- 1: **Step 1:** Guess distribution of assets, fixed productivity and education for both genders at the end of period j_{m-1} (for a given skill level s), $\Phi(j_m - 1, si, g, s; a; \gamma(s))$
 - 2: **Step 2:** For given $\Phi(j_{m-1}, si, g, s; a; \gamma(s))$, solve for intergenerational RE equilibrium:
 - 3: **2.1:** Solve fixed point problem in value functions (guess $V(j_a, si, \cdot)$, iterate until convergence)
 - 4: **2.1:** Solve fixed point problem in distributions (guess $\Phi(j_a, si, \cdot)$ iterate until convergence)
 - 5: **Step 3:** If $\|\Phi(j_{m-1}, si, g, s; a; \gamma(s))^{\text{update}} - \Phi(j_{m-1}, si, g, s; a; \gamma(s))^{\text{guess}}\| < \epsilon$, EXIT, else go back to Step 1 and continue until convergence.
-

4 Calibration

The model is calibrated to US aggregate and cross-sectional data, using a standard two-stage procedure in which a subset of the parameters is chosen outside the model based on values in the literature, and a second set of parameters is calibrated inside the model.

Specifically, while most demographic, aggregate technology and fiscal policy parameters as well as individual labor productivity parameters are set exogenously or directly estimated from the data, the key parameters governing preferences and the child human capital production function are calibrated internally so that the initial steady state general equilibrium of the model is consistent with the (child) age profile of parental time and resources investments, average hours worked, labor force participation, the cross-sectional wage- and education distributions, as well as the level of government spending and government debt.

4.1 Demographics

The population growth rate n is assumed to be 1% which is the average of the US annual population growth rate values in 2000s. The number of children per mother (fertility rate) differs by education level and is ca. 15% higher for households without a college degree, in accordance with the five most recent PSID waves. The marriage probability $\pi^m(s)$ is set to 0.51 for all education groups (average marriage rate for the age range 25-35 based on PSID 2011-2019).

4.2 Preferences

For single households, the per period utility function takes the following functional form:

$$u(c, \ell) = \frac{c^{1-\sigma}}{1-\sigma} - \phi \frac{\ell^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} \quad (17)$$

where $\sigma = 1$, i.e. assume logarithmic utility²⁴. Parameter ψ that can directly be interpreted as the Frisch elasticity of labor supply is set to 0.6 following [Kindermann and Krueger \(2014\)](#)²⁵. Finally, parameter ϕ is calibrated endogenously to match the average hours worked of 1/3 of the time endowment.

Households composed of couples experience disutility from hours worked of both partners:

$$u(c, \ell(wo), \ell(ma)) = \frac{c^{1-\sigma}}{1-\sigma} - \phi \frac{\ell(wo)^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} - \phi \frac{\ell(ma)^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}}. \quad (18)$$

The term capturing fixed costs of working positive hours $F_{\ell>0}$ is also calibrated endogenously to match the average share of non-participating and unemployed households of 25%.

During the model periods when children live in the parental household also time spent with children affects parental utility. We assume that the disutility from time with children enters the utility function of parents in an additively separable manner²⁶:

$$u(c, \ell, i^t, s(wo)) = \frac{c^{1-\theta}}{1-\theta} - \phi \frac{\ell^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} - \kappa \frac{\zeta(s(wo)) \cdot i^{t1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} \quad (19)$$

where κ is calibrated to match the average household time investment into children (per week per child), and $\zeta(s(wo))$ is the average number of children per household, which depends on the education of the mother.

For couple households, accordingly, there are additional terms capturing disutility from hours worked and time with children of the second partner:

$$u(c, \ell(wo), \ell(ma), i^t(wo), i^t(ma), s(wo)) = \frac{c^{1-\theta}}{1-\theta} - \phi \left(\frac{\ell(wo)^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} + \frac{\ell(ma)^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} \right) - \kappa \cdot \zeta(s(wo)) \cdot \left(\frac{i^t(wo)^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} + \frac{i^t(ma)^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}} \right) \quad (20)$$

When children attend college, they experience utility (psychological) costs determined by the following cost function

$$p(s, s_p; h) = \varrho(s, s_p) + \frac{1}{h}$$

²⁴Given the logarithmic utility assumption, the child equivalence scale parameter is irrelevant for the household problem and for brevity considerations is omitted.

²⁵As [Kindermann and Krueger \(2014\)](#) point out this value is based on the average of estimates for men and for women.

²⁶[Bastian and Lochner \(2020\)](#) based on females responses to EITC expansions point out that mothers increase their time with children not at the cost of hours worked but rather via reallocating their leisure time.

where $\varrho(s, s_p)$ is a calibration parameter which depends on parental education and is 50% smaller for college dropouts than for college graduates, due to the assumed lesser time these individuals spend in college. Specifically, $\varrho(s = co, s_p < co)$ is calibrated to match the average share of college graduates of 32% while $\varrho(s = co, s_p = co)$ is chosen such that the college enrollment rate conditional on parents being college graduates equals 92% (PSID 2011-2019). Observe that the psychological cost specification above implies that the utility costs are monotonically decreasing and convex in the acquired human capital h .

Households discount utility at rate β which is chosen such that in general equilibrium the implied interest rate equals 3.0%. Utility of future generations is discounted at rate ν which governs the degree of parental altruism. Parameter ν is chosen so that average per child inter vivos transfer is 61,200\$, as implied by the 2013 Rosters and Transfers Module of the PSID (based on monetary transfers from parents to children until age 26).

4.3 Human Capital Production Function

Initial Child Human Capital In the model innate human capital (at biological age 2) depends on parental education and marital status and for given parental background is exogenously given. The dependency of innate child ability on parental background is disciplined using child (Letter Word) test score data from the Child Development Supplement (CDS) to the PSID.

Human Capital Production Function At ages $j_0, \dots, j_a - 1$, children receive parents' human capital investments through money and time $i^m(j), i^t(j)$ and governmental (schooling) input i^g , respectively. Human capital is accumulated according to a multi-layer human capital production function with imperfectly substitutable inputs:

$$h'(j) = \left(\kappa_j^h h^{1-\frac{1}{\sigma^h}} + (1 - \kappa_j^h) i(j)^{1-\frac{1}{\sigma^h}} \right)^{\frac{1}{1-\frac{1}{\sigma^h}}} \quad (21a)$$

$$i(j) = \bar{A} \left(\tilde{\kappa}_j^g (i^g)^{1-\frac{1}{\sigma^g}} + (1 - \tilde{\kappa}_j^g) (i^p(j))^{1-\frac{1}{\sigma^g}} \right)^{\frac{1}{1-\frac{1}{\sigma^g}}} \quad (21b)$$

$$i^p(j) = \left(\tilde{\kappa}_j^m (i^m(j))^{1-\frac{1}{\sigma^m}} + (1 - \tilde{\kappa}_j^m) (i^t(j))^{1-\frac{1}{\sigma^m}} \right)^{\frac{1}{1-\frac{1}{\sigma^m}}} . \quad (21c)$$

The production function features partially age dependent parameters for calibration purposes - to reflect relative differences in importance of different inputs at different stages of childhood. All inputs are divided by their respective unconditional means which allows achieving unit independence (see [Cantore and Levine \(2012\)](#)). This normalization is accounted for by adjusting the weight parameters $\tilde{\kappa}_j^g$ and $\tilde{\kappa}_j^m$, respectively —see Appendix [B.2](#) for details.

In the outermost nest of the production function, existing human capital h is combined with aggregate investment $i(j)$ at age j . The substitution elasticity σ^h is set exogenously to 1 for all ages (implying a Cobb-Douglas specification). The age profile for the weight parameter κ_j^h is calibrated to match the age profile of (per child) parental time investment in the data. The average κ^h , in turn, is chosen such that the average short-run college enrollment elasticity with respect to high school spending generosity matches the midpoint of the range of empirical estimates reviewed in the meta-study by [Jackson and Mackevicius \(2023\)](#).

In the second nest of the production function public and private inputs $(i^g, i^p(j))$ are combined, with the substitution elasticity between the two inputs being denoted by σ^g and the age-specific weight parameters $\tilde{\kappa}^g(j)$. Our choice of i^g in the baseline calibration is described below in [Section 4.6](#) and $i^p(j)$ is the CES aggregate of parental inputs in the innermost nest. The substitution elasticity between both inputs is set exogenously to 2.43 using the estimate provided in [Kotera and Seshadri \(2017\)](#). For kindergarten ages, i.e. age bin 2-6, the weight parameter is calibrated endogenously to match average parental time investment at that age. For other ages, the weight parameter is also calibrated endogenously such that the inequality in acquired human capital by family background is close to the disparity in test scores in CDS-PSID at ages 17-19. \bar{A} is a normalization parameter which is chosen such that average acquired human capital at age 18 is equal to 1.

Finally, in the innermost nest parental time and resource inputs $(i^t(j), i^m(j))$ are combined, with a substitution elasticity that is denoted by σ^m and the age-dependent weight parameter $\tilde{\kappa}^m(j)$. The substitution elasticity σ^m is fixed exogenously at the value of 1 using the estimate provided in [Lee and Seshadri \(2019\)](#) whereas the weight parameter $\tilde{\kappa}^m(j)$ is calibrated endogenously to match the mean and the age profile of the parental monetary input.

4.4 High School and College Dropout

The high school completion probability takes the following functional form:

$$\pi^{hs}(h) = 1 - \exp(-\lambda^{hs}h), \quad (22)$$

where λ^{hs} is a parameter calibrated endogenously to match the average share of high school dropouts in PSID data²⁷ of 8%.

The college completion probability takes the same functional form:

$$\pi^c(h) = 1 - \exp(-\lambda^c h), \quad (23)$$

²⁷Education shares are based on the five recent waves of PSID: 2011, 2013, 2015, 2017 and 2019.

with parameter λ^c calibrated endogenously to match the average share of college dropouts in PSID data of 29%.

Observe that for $\lambda^h > 0$ and $\lambda^c > 0$ this functional form specification implies that the probability of both graduating from high school and finishing college is increasing in acquired human capital.

4.5 College Tuition Costs & Borrowing Constraint of Students

Based on NCES statistics, the net tuition cost ι (tuition, fees, room and board rates charged for full-time students in degree-granting post-secondary public institutions) for one year of college in constant 2010 dollars has been on average 15,500\$ during the time period 2000-2019. Following [Krueger and Ludwig \(2016\)](#), the maximum amount of publicly provided students loans per year is given by 11,397\$, which is the borrowing limit for college students in the model. For college dropouts, we assume that the borrowing limit is twice as tight as for college graduates. For all ages after the college period (i.e. for all $j > j_a$) we let

$$\underline{a}(j, s > hs) = \underline{a}(j - 1, s > hs)(1 + r) - rp$$

and compute rp such that the terminal condition $\underline{a}(j_r, s) = 0$ is met.

4.6 Education Spending

The government spends on schooling for children and pays the college subsidy for college students. According to NCES statistics, average per student spending on public schools is ca. $i^g = \$14,000$. The public college subsidy is set to $\vartheta\% = 38.8\%$ of average gross tuition costs, as in [Krueger and Ludwig \(2016\)](#). Additionally, we also explicitly model private subsidies that are paid from accidental bequests and constitute $\vartheta^{pr}\% = 16.6\%$ of the gross tuition cost in the baseline (see [Krueger and Ludwig \(2016\)](#)).

4.7 Labor Productivity

We use PSID data to regress by education of the household head log wages measured at the household level on a cubic in age of the household head, time dummies, family size, a dummy for marital status, and person fixed effects. Predicting the age polynomial gives our estimates of $\epsilon(s, g, j)$. We next compute log residuals and estimate moments of the earnings process by GMM and pool those across education categories and marital status. We assume a standard process of the log residuals according to a permanent and transitory shock specification, i.e., we

decompose log residual wages $\ln(y_t)$ as

$$\begin{aligned}\ln(y_t) &= \ln(z_t) + \ln(\varepsilon_t) \\ \ln(z_t) &= \rho \ln(z_{t-1}) + \ln(\nu_t)\end{aligned}$$

where $\varepsilon_t \sim_{i.i.d} \mathcal{D}_\varepsilon(0, \sigma_\varepsilon^2)$, $\nu_t \sim_{i.i.d} \mathcal{D}_\nu(0, \sigma_\nu^2)$ for density functions \mathcal{D} , and estimate this process pooled across education and marital status. To approximate this process in our model, we translate it into a 2-state Markov process targeting the conditional variance of y_t , conditional on y_{t-4} , $(1 + \rho^2 + \rho^4 + \rho^6)\sigma_\nu^2$ (accounting for the four year frequency of the model). The estimates and the moments of the approximation are reported in Table 3.

Table 3: Stochastic Wage Process

	Estimates			Markov Chain	
Parameter	ρ	σ_ν^2	σ_ε^2	$\pi_{hh} = \pi_{ll}$	$[\eta_l, \eta_h]$
Estimate	0.9559	0.0168	0.0566	0.8235	[0.6725, 1.3275]

Notes: This table contains the estimated parameters of the residual log wage process.

Acquired Human Capital and Wages The mapping of human capital into a fixed productivity component is probabilistic. The fixed effect $\gamma(s)$ can take two values, $\gamma^h(s)$ (high) and $\gamma^l(s)$ (low), respectively, for each education group. The probability of drawing a high realization $\gamma^h(s)$ is given by

$$\pi^h(h) = 1 - \exp(-h) \tag{24}$$

where h is child acquired human capital at age 18.

Education-specific permanent productivity parameters $\gamma^h(s)$ and $\gamma^l(s)$ are calibrated endogenously to ensure that for each of education group the average $\gamma(s)$ is equal to one²⁸, i.e.

$$\int (\pi^h(s, h)\gamma^h(s) + (1 - \pi^h(s, h))\gamma^l(s)) \Phi(dh, s) = 1. \tag{25}$$

The education-specific spreads $\Delta^\gamma(s)$ between $\gamma^h(s)$ and $\gamma^l(s)$ are calibrated as follows. For high school dropouts and high school graduates that serve as a reference group $\Delta^\gamma(s = hsd) = \Delta^\gamma(s = hs)$ is set such that the average variance of log wages equals 0.45 as implied by PSID 2011-2019. For the other two education groups, $\Delta^\gamma(s)$ parameters are scaled relative

²⁸This ensures that the skill premia are matched.

to $\Delta^\gamma(s < sco)$ such that the ratios of human capital gradients of (lifetime) wages of college graduates and the reference group, on the one hand, and college dropouts and the reference group, on other hand, estimated with NLSY79 data (in expectation, i.e. from an ex ante perspective) are matched. Specifically, estimates of education-specific human capital gradients $\hat{\rho}(s)$ are obtained by running the following regressions:

$$\ln(\omega(s)) = \rho(s) \cdot \frac{e}{\bar{e}} + v(s),$$

where $\omega(s)$ denotes age-free education-specific wages and e measures test scores of the Armed Forces Qualification Test (AFQT) which are normalized by their mean \bar{e} . Finally, $v(s)$ is an education group specific error term.

Table 4 shows the resulting estimates $\hat{\rho}(s)$. The estimated ability (human capital) gradient is strictly increasing in education reflecting a pronounced complementarity between ability (human capital) and education.

Table 4: Ability Gradient by Education Level

Education Level	Ability Gradient
(HS- & HS)	0.4248 (0.0481)
(CL-)	0.5786 (0.0245)
(CL & CL+)	0.7298 (0.0670)

Notes: Estimated ability gradient $\hat{\rho}(s)$, using NLSY79 as provided in replication files for [Abbott et al. \(2019\)](#). Standard errors in parentheses.

For $s > hs$, $\Delta^\gamma(sco)$ and $\Delta^\gamma(co)$ parameters are set such that

$$\frac{\int \left(\frac{\partial [\pi^h(s,h)\gamma^h(s) + (1-\pi^h(s,h))\gamma^l(s)]}{\partial h} \right) \Phi(dh, s)}{\int \left(\frac{\partial [\pi^h(s<co,h)\gamma^h(s<co) + (1-\pi^h(s<co,h))\gamma^l(s<co)]}{\partial h} \right) \Phi(dh, s < co)} = \frac{\hat{\rho}(s)}{\hat{\rho}(s < co)}.$$

Thus, for given acquired human capital distribution, the education-specific parameters $\gamma^h(s)$ and $\gamma^l(s)$ jointly determine the dispersion of wages as well as the degree of complementarity between human capital and education in wages. In other words, from an ex ante perspective these parameters determine the steepness of the expected college wage premium in human capital (in expectation), and from an ex post perspective they drive the realized dispersion of wages. The difference between wage dispersion of college- and non-college households is not targeted in the calibration.

4.8 Aggregate Production

We assume that (9) is a Cobb-Douglas production function

$$Y_t = F(K_t^\alpha (\Upsilon_t L_t)^{1-\alpha}),$$

where α determines the elasticity of output with respect to capital. In order to permit the possibility that a policy-induced change in the share of college graduates changes their relative wages we assume that non-college labor (including college dropouts) and college labor (i.e., college graduates) are imperfectly substitutable in production. Thus, the labor aggregator (10) is given by

$$L_t = (L_{t,nc}^\rho + L_{t,co}^\rho)^{\frac{1}{\rho}}$$

where ρ governs the elasticity of substitution between college $L_{t,co}$ and non-college labor $L_{t,nc} = L_{t,hsd} + L_{t,hs} + L_{t,cod}$.

The capital share parameter α is set to 1/3, a standard value in the literature, and the annual physical capital depreciation rate equals 5%. The rate of technological progress (and thus the long-run growth rate of per-capita income) μ equals 1%. Finally, the elasticity of substitution between skilled (college) and non-skilled (high school dropout, graduate and college dropout) labor is set to 3.3, following the estimate of [Abbott et al. \(2019\)](#).

4.9 Government

The government has to balance the budget of the general tax and transfer system as well as the budget of the pension system. In the scope of the general tax and transfer system budget, the government finances an exogenous stream of (non-education related) expenditures and an endogenous stream of education related expenditures (pre-tertiary and tertiary). The revenue side of the general tax and transfer system is comprised by taxes on consumption, capital and labor income. The consumption tax rate is set to 5% (see [Mendoza et al. \(1994\)](#)) while the capital income tax rate is fixed at 36%, following [Trabandt and Uhlig \(2011\)](#). Additionally, the government can issue debt.

Households that work positive hours in the labor market face the labor income tax schedule that is approximated using a two-parameter tax function as in [Heathcote et al. \(2017\)](#):

$$T(y, n > 0) = y - (1 - \tau)y^{1-\xi} \tag{26}$$

where τ is the level parameter, and ξ is the progressivity parameter. The progressivity parameter is exogenously set to 0.18 for all population groups, following [Heathcote et al. \(2017\)](#), while the level parameter is calibrated endogenously to match the government debt to GDP ratio of 100% in the baseline.

The non-participating and unemployed households have no labor income and thus do not pay labor income taxes but receive government transfers ω that are set to 20.2% of average (full-time) earnings (CEX 2001-2007; consumption of bottom 10%). Thus, for non-working singles and couples (i.e. both spouses do not work) the tax/transfer functions are given by:

$$T(q = si, 0) = -\omega \quad \text{and} \quad T(q = cpl, 0) = -2\omega.$$

If, however, only one spouse is non-working and the other spouse supplies positive hours, then the tax function is:

$$T(q = cpl, n(g) > 0, n(g^-) = 0, y) = y - (1 - \tau)y^{1-\xi} - \max\{0, 2\omega - (1 - \tau)y^{1-\xi}\}. \quad (27)$$

In other words, the government guarantees the minimum income of 2ω also to the couples with only one partner supplying positive hours.

Finally, as for the the pension system, the payroll tax τ^p is set to the current legislative level of 12.4% and the actual progressivity of the pension system is taken into account.

4.10 Calibration Summary

Table 16 in Appendix C.2 summarizes the subset of parameters calibrated exogenously outside the model, and Table 17, also in the appendix, provides an overview of the second stage parameters that are calibrated endogenously within the model.

5 Model Validation

There is substantial empirical evidence on the short-run impact of small-scale transfer program and education reforms; see [Bastian and Lochner \(2020\)](#), [García et al. \(2020\)](#) or the meta-study by [Jackson and Mackevicius \(2023\)](#) for the impact of the social safety net, early childhood interventions, and school funding on child achievement and later-life outcomes, as well as the meta study by [Deming and Dynarski \(2009\)](#) for the effect of college tuition grants on college enrollment and completion.

Before using the model for a counterfactual education policy analysis we view it as crucial to ensure that it has plausible predictions for comparable policy interventions empirically studied and surveyed by this literature. For that, it is important to decide what version and time horizon of our model to confront with these empirical estimates. For data reasons the empirical literature focuses on the short-run effects, and by their small-scale nature the experiments can plausibly be assumed to have no significant impact on the economy-wide interest rate as well as the aggregate and relative wages and the government budget. Therefore we contrast the short-run, partial equilibrium model response to this empirical evidence.²⁹ Since the range of the empirical estimates is fairly large, our goal is not to argue that our model matches any specific study, but rather to demonstrate that the model-based statistics fall into the empirical range and, especially, does not overstate the positive impact of the education policy reforms discussed in this paper.

5.1 College Tuition Subsidies

The empirical evidence on the short-run, small scale (quasi-)experimental effect of college tuition cost on attendance and completion is quite broad. [Deming and Dynarski \(2009\)](#) summarize the large literature on this topic, with the upshot that an \$1,000 increase in college subsidies leads to a 3-6 percentage point increase in college enrollment. Our model implies a response in college enrollment, in partial equilibrium, of 5.1 percentage points.

5.2 Increase in High School Spending

In their meta-study of a large number of empirical (quasi-)experimental studies, [Jackson and Mackevicius \(2023\)](#) report that an increase in public high school funding by \$1,000 per pupil for four years leads to an increase in high-school completion by 0.07-3.99 percentage points and an increase in college enrollment by 0.90-5.51 percentage points. We target the midpoint of the estimates for the impact of high-school funding for college enrollment when calibrating the model, but not the response of high school graduation rates to the same intervention, leaving this prediction of the model as an important dimension of model validation. In partial equilibrium of our model, the high school completion rate increases by 0.6 percentage points on impact of a \$1,000 increase in public high-school spending, towards the lower bound of the (arguably wide-ranged) empirical estimates, but indicating that in our model public schooling is not “overly” productive relative to the available empirical evidence.

²⁹Partial equilibrium means that wages and interest rates as well as tax rates are held fixed when the policy changes. In contrast, we continue to assume that the marriage market clears, that is, even in partial equilibrium households adjust their beliefs about the characteristics of potential future spouses in response to the policy change.

5.3 Discussion

The previous results indicate that our model-implied policy responses to small-scale reforms line up well with the empirical record. Alternatively put, the empirical results reported in the literature are consistent with our structural model, raising the question why we cannot simply extrapolate these empirical estimates of the short-run impact of small reforms to medium- or long-run outcomes at the aggregate, national scale, without any need for structural modeling?

The reasons are four-fold. First, policy transitions take time, and the short-run policy effect could be very different from long run impact of the policy since the distribution of the population (from the perspective of our model, with respect to initial assets, human capital and parental education) changes. Section 6.2 below shows that this is indeed the case in our model. Second, a large-scale reform might have important general equilibrium effects on (relative) wages of college and non-college labor as well as rates of returns that are not captured by small-scale quasi-experimental evidence. We show in Section 6.3.1 that these general equilibrium effects are indeed quantitatively very sizable. Third, for small-scale reforms the government budgetary consequences can plausibly be neglected, whereas for large-scale, economy-wide reforms the adjustment in taxes, transfers and/or government debt have to be considered explicitly, which requires articulating the intertemporal government budget constraint explicitly (and its adjustment, in the face of an education reform), as we do in Section 6.2.1.³⁰ Finally, and separately from the first three points that pertain to a *positive* policy analysis, for an assessment of the *normative* consequences of a hypothetical policy reform we need a utility-based structural approach.

6 Results for Two Pure Policy Reforms

6.1 The Thought Experiment

For each transition thought experiment we assume that the economy is in steady state calibrated to data from 1999 to 2019, and that the policy reform triggering the transition is completely unexpected, but that the government is henceforth fully committed to the policy reform. Our benchmark reform is “Free College”, a 100% subsidy of college tuition, financed by a permanent increase in the labor income tax rate τ . That is, this tax parameter adjusts once and for all to ensure that the intertemporal government budget constraint remains satisfied. In order to guarantee that the period-by-period budget constraint holds, government debt endogenously

³⁰The adjustments of taxes and transfers induced by the reforms potentially result in very different incidence of the full reform package as compared to pure reforms without any fiscal adjustments. Cf., e.g., [Kaplow \(2020\)](#) for a discussion of the importance of disentangling the distributional effects of a reform itself from those induced by the accompanying fiscal adjustments.

evolves along the transition from the old steady state towards its new steady state value (as a fraction of GDP). The corresponding “Better Schools” reform increases public (primary and secondary) school spending i^g permanently so that the extra expenditures have the same present discounted value as the “Free College” reform, making both interventions fiscally comparable.

We present our main results in Subsection 6.2, contrasting in turn the aggregate, welfare and distributional (cross-sectional and intergenerational socioeconomic persistence) consequences of the two reforms in general equilibrium. In order to isolate the importance of endogenous factor price movements, we study in Subsection 6.3.1 the same reforms in a partial equilibrium setting where wages and interest rates remain fixed (so that labor markets and the capital market need not clear, i.e., (15a)-(15c) need not hold). However, the government intertemporal government budget constraint (11) is required to be satisfied in all our thought experiments.³¹

6.2 Transitional Dynamics: Aggregates, Distribution and Welfare

In this section we summarize the transition results from our two main policy exercises; Table 10 in Appendix A provides a summary of comparison of the initial and the final steady states to which the policy transitions converges.

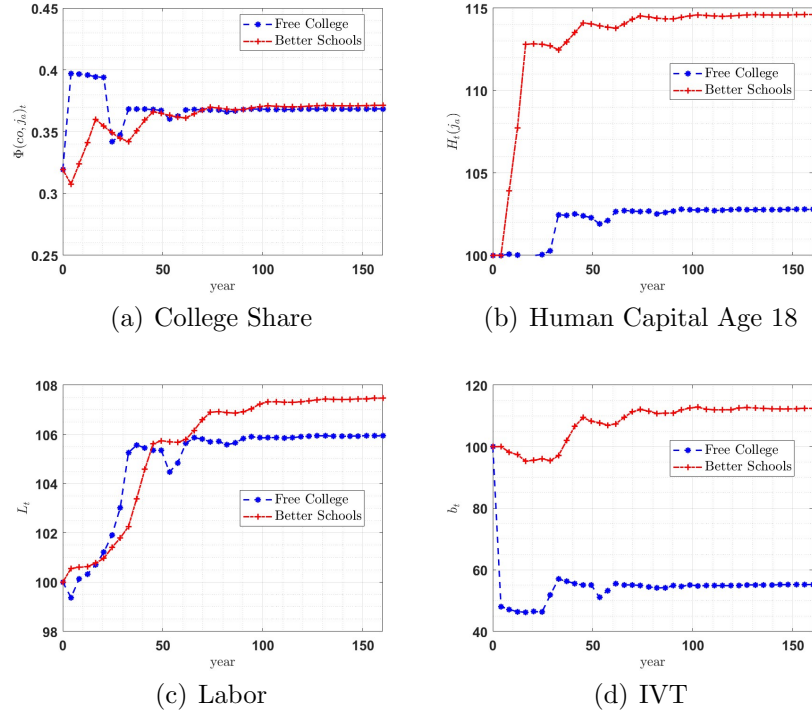
6.2.1 Aggregate Effects

In Figure 2 we display the dynamics of the college share, aggregate labor in efficiency units (L_t), average human capital at age 18 and aggregate inter-vivos transfers over time. Panel (a) of Figure 2 demonstrates that both policies are successful in inducing more individuals to attend college, although making college free does so to a larger extent in the short run. However, it also leads to many more college dropouts.³² Furthermore, it takes time for the full impact of the reforms to take hold. Only after the third generation born after the reform has made the higher education decision and completed college (i.e., roughly 50 years after the policy change, see Figure 4, panel a, below) does the share of the population with a college degree reach its new, higher steady state level. This broad observation, which also holds true for the other aggregate variables depicted in Figure 2, reinforces the need to model transitions explicitly.

³¹The progressive labor income tax code is specified as a two-parameter family following Benabou (2002) and Heathcote et al. (2017), and for the current thought experiments we fix the progressivity parameter and adjust the tax level parameter once and for all so that the intertemporal government budget constraint is satisfied. The sequence of government debt levels ensures that the flow government budget constraints are satisfied in every period.

³²There are also substantial differences in the underlying human capital and, thus, productivity distribution of the pool of new college students induced by each reforms. These differences will be discussed in Section 6.2.2 on the distributional impact of the reforms.

Figure 2: Aggregate Variables: General Equilibrium



Notes: Panel (a): Share of a given “birth” cohort that completes college; Panel (b): Average human capital of a given “birth” cohort at age 18 (Initial Steady State = 100); Panel (c): Aggregate labor efficiency units (Initial Steady State = 100); Panel (d) Aggregate Inter-vivos transfers (Initial Steady State = 100).

Panel (b) and (c) of Figure 2 indicate that the college expansion is achieved through very different channels in the two reforms. In the “free college” reform, as panel (b) of Figure 2 shows, there is only a very marginal positive human capital response within the lifespan of the first impacted generation (i.e. before the newly educated children become parents themselves). There are several conflicting forces at play that determine how parental incentives to invest in child human capital are affected by the generosity of the college subsidy. On the one hand, holding fixed the expected benefits from enrolling in college (in terms of graduation probability and earnings), the endogenous optimal human capital attendance threshold is decreasing in the college subsidy rate, which creates a disincentive for parents to invest in child pre-college human capital. On the other hand, the benefits from college (in terms of graduation probability and earnings) are increasing in the level of human capital and thus making college financially affordable creates an incentive for altruistic parents to increase their human capital investments in children so that the latter can take bigger advantage of attending college. Quantitatively, the positive and the negative investment incentive effects almost fully offset each other and acquired human capital increases only very marginally within the lifespan of one generation.

In the “better schools” reform there is a much more pronounced increase in child human capital accumulation, and some of the now better-schooled 18 year old teenagers choose to attend college when they used not to. Crucially, as panel (c) demonstrates, even those whose college attendance decisions are not affected by the reform now tend to have more human capital, and consequently are more productive in the labor market. Furthermore, since those attending college now have more human capital, under the “better schools” reform the college completion rate improves as well. Consequently, aggregate labor efficiency units rise more strongly under the “better schools” reform than under the “free college” reform.

Finally, panel (d) demonstrates that private parental adjustments also significantly differ: when college is free, private inter-vivos transfers (which are mainly used for financing college tuition) collapse, which in turn reduces overall asset accumulation by parental generations.³³ The strong response in the college share, in aggregate labor as well as aggregate savings also anticipates the finding that accounting for general equilibrium factor price adjustments will have quantitatively very important aggregate, distributional and welfare consequences.³⁴

6.2.2 Distributional Consequences

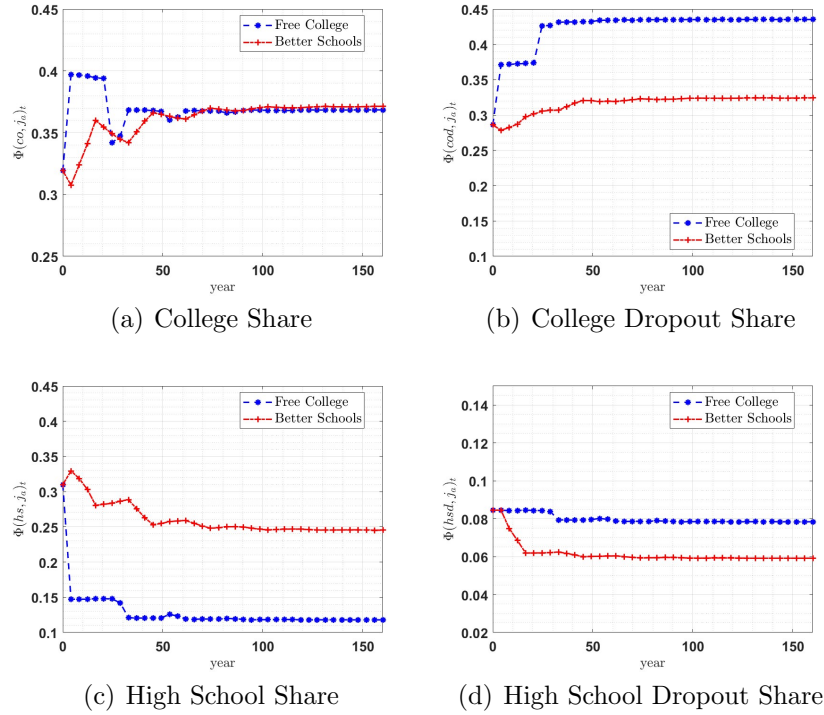
The two policy reforms also have substantially different distributional consequences. This is apparent from Figure 3 which complements panel (a) of Figure 2 and shows the evolution of the share of college dropouts in panel (a), those completing high-school in panel (b) and those with some, but not complete high school in panel (c). We highlight two key observations.

First, the “free college” reform does not change the share of children dropping out from high school by much (see panel (c)) even though the incentives of parents to invest time and resources into their children’s human capital (to make them potentially successful college students) have increased. For these children, predominantly from families with low parental educational background and often with only a single parent, the problem of college attainability prior to the reform is not (primarily) that it too expensive to attend college, but that their initial and acquired human capital during childhood would make it very strenuous to attend college (the utility cost of attending college is very high, given their human capital) and unlikely to succeed in obtaining a college degree. Anticipating that their children will not go to college, these parents see little reason to change their human capital investment decisions during the child’s primary and secondary education years, and thus the share of high-school dropouts only mildly declines under the “free college” reform. In contrast, the “better schools” reform leads to a decline in the share of

³³The importance of intergenerational transfers for (indivisible) human capital investment in the presence of credit market imperfections was already highlighted in Galor and Zeira (1993).

³⁴The adjustments of parental resource and time investments are shown in Appendix A. The quantitative importance of parental investment adjustments is somewhat limited due to a relatively large relative weight on public schooling in the calibration of the human capital production function.

Figure 3: Higher Education Shares: General Equilibrium



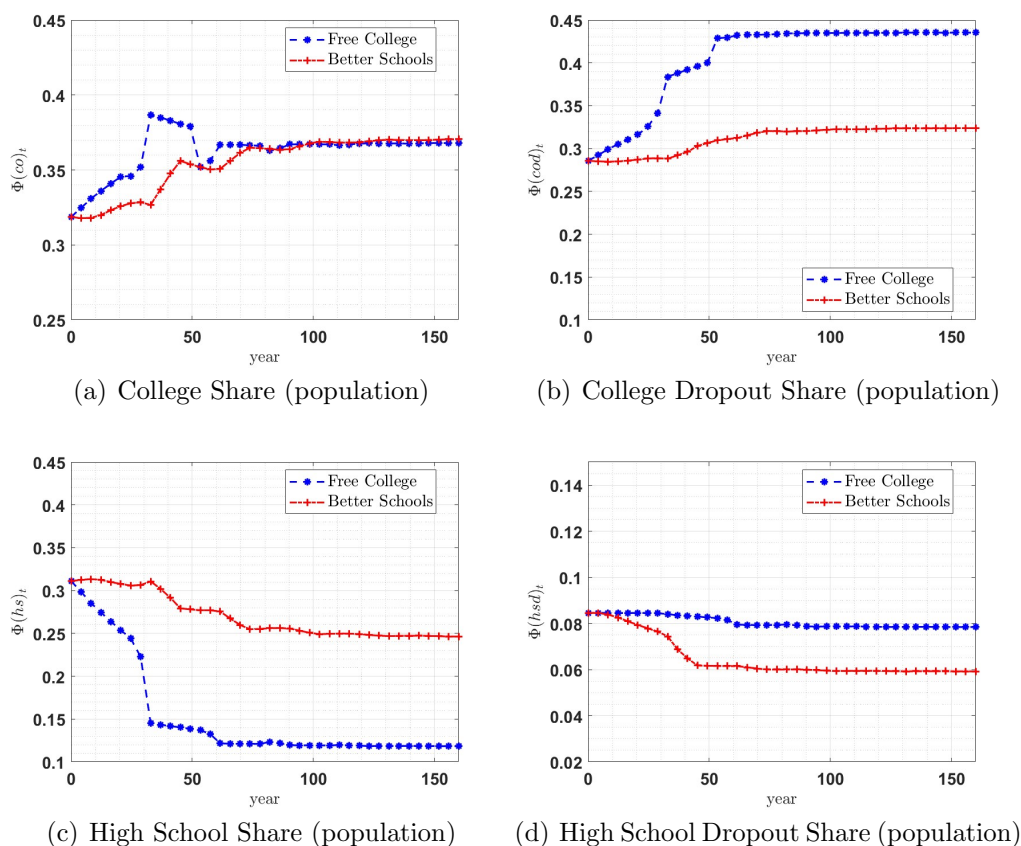
Notes: Panel (a): Share of a given “birth” cohort that completes college; Panel (b): Share of a given “birth” cohort that becomes a college dropout; Panel (c): Share of a given “birth” cohort that becomes a high school completer; Panel (d): Share of a given “birth” cohort that becomes a high school dropout.

high-school dropouts in the population by about three percentage points since the larger public investment into child human capital accumulation in school is only partially offset by lower private time and resource investments (see Appendix A.1) The improved human capital distribution at age 16 then results in a smaller share of the population dropping out of high school.

Second, many of the additional students drawn to college under the “free college” reform do not actually complete college (since their human capital from high school is relatively low and thus the chances of dropping out are high). In the long run (see Table 10 in the appendix), although the “free college” reform shifts 20 percentage points of previous high school graduates to college attendance, only about a quarter of these end up with a degree. In contrast, almost 60% of the new college attendees under the “better schools” reform (approximately 5 percentage points) graduate from college, suggesting that this reform uniformly shifts up the tertiary school

attainment distribution and benefits all segments of the distribution in terms of labor-market relevant skills.³⁵

Figure 4: Total Population Education Shares (general equilibrium)



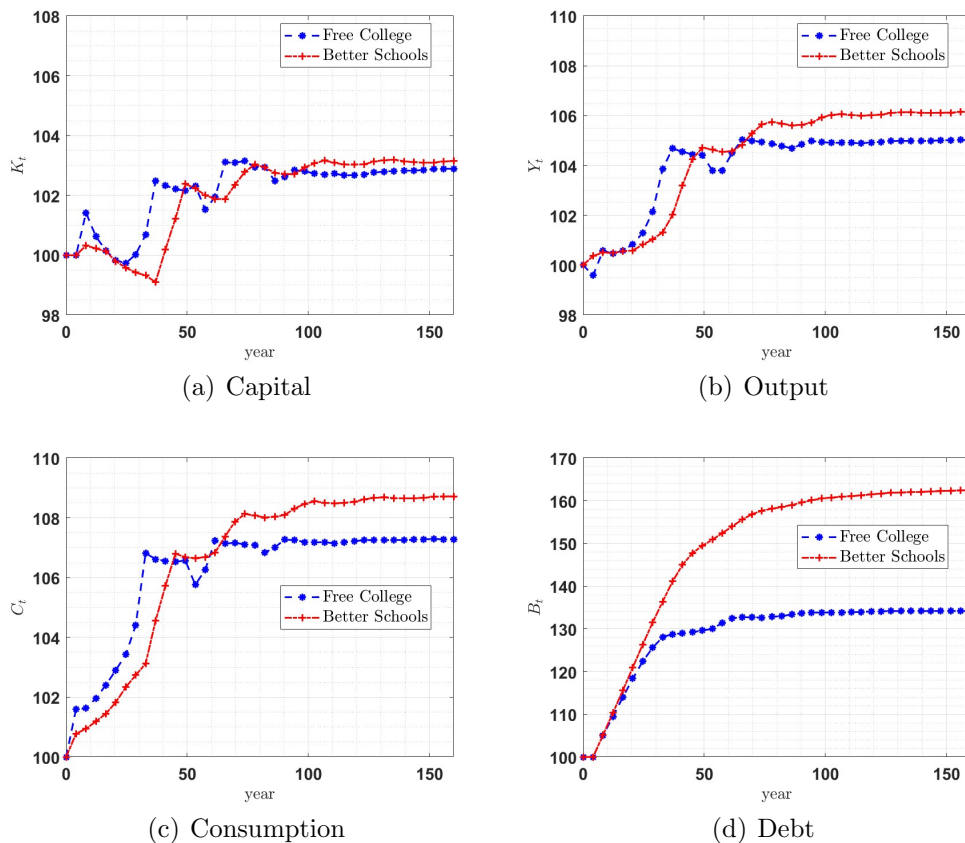
Notes: Panel (a): Population share of college completers; Panel (b): Population share of college dropouts; Panel (c): Population share of high-school completers; Panel (d): Population share of high-school dropouts.

Figure 4 shows the education *population* shares (as opposed to the education shares of a specific age cohort that was depicted in Figure 2). It displays a recurrent theme of this paper that the education reforms studied in this paper take time to materialize their full effect since the education expansion only directly impacts currently young generations that still have to go through school and/or make their higher education choices. Initially, this is a small share of the population, but over time these cohorts make an increasingly large share of the total labor force and thus the share of college-educated workers gradually increases (and that of individuals with only a high school degree declines). The extent to which this happens differs, of course, across the two reforms and is stronger for the “free college” thought experiment. In contrast, the

³⁵In partial equilibrium more than 70% of the new college attendees obtain a college degree under the “better schools reform”.

“better schools” reform over time reduces by about a quarter the share of the population without even a high school degree, although this takes three generations, with no such effect from the “free college” reform.

Figure 5: Aggregate Consumption, Production and Government Debt



Notes: Panel (a): Capital; Panel (b): Output; Panel (c): Consumption; Panel (d): Government debt.

Figure 5 displays the evolution of aggregate capital, output, consumption and government debt. Since capital is only mildly increasing along the transition, the time path of output roughly follows that of aggregate labor input; the same is true for aggregate consumption. For the same reason, the tax base increases gradually with labor along the transition, whereas the education cost in both reforms rises immediately on impact. Therefore, the government accumulates debt along the transition, and since the “better schools” reform delivers a larger output in the long run, the capacity to service debt is more substantial in this reform. See panel (d) of Figure 5.

We cast our model in general equilibrium, and therefore interest rates, wages and taxes adjust along the transition path to ensure that the labor markets for college-educated labor, non-college labor and the assets market clears. In Figure 6 we display the time paths of these equilibrium factor prices and taxes. We observe that on account of the increase in labor input (in efficiency units) induced by both education reforms, the capital-labor ratio falls, the interest rate increases

over time (see panel (a)), and wages per efficiency unit (not shown) fall over time. However, since college- and non-college labor are imperfect substitutes and non-college labor becomes scarcer relative to college labor, the college wage premium falls by nine percentage points under the “free college” reform, and almost eight percentage points under the “better schools” reform (see panel (b)) but wages of those without a college degree actually increase (see panel (c) of Figure 6).

In contrast, those with a college degree see their absolute wages decline substantially (relative to the long-run balanced growth path, of course). Panel (f) shows the (once and for all) adjustment in the labor income tax rate τ required to ensure that the intertemporal government budget constraint holds. It demonstrates that both reforms actually generate more fiscal space in that the reforms are self-financing and the labor income tax rate can actually fall, more so in the “better schools” reform.

6.2.3 Intergenerational Persistence

The policy reforms not only affect cross-sectional inequality, but also the intergenerational persistence of earnings and education. Table 5 displays one dimension of intergenerational mobility, showing how the earnings of children from different parental backgrounds (measured by parental education and marital status) change in response to the policy interventions. The first column shows the average lifetime earnings within a specific parental group, e.g., single parents without a high-school degree on average earn \$21,297. The second column shows the average earnings of children for each parental group under the baseline policy, and the remaining two columns show the percentage change in these child earnings induced by the two policy reforms.

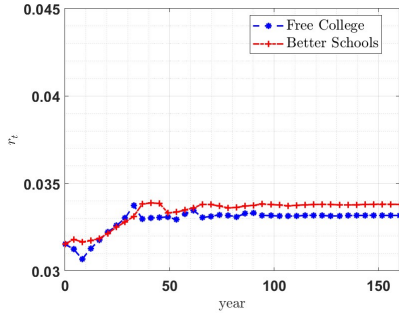
Table 5: Child Earnings % Change, by Parental Background

Parent Background	Baseline	FC, % Δ	BS, % Δ
Single, $s = hsd$ (\$21,297)	\$37,358	9.72	10.01
Single, $s = hs$ (\$37,153)	\$39,999	8.63	8.13
Single, $s = cod$ (\$44,951)	\$44,472	7.84	5.77
Single, $s = co$ (\$65,574)	\$59,187	-0.61	4.32
Couple, $s = hsd$ (\$27,043)	\$44,976	9.52	7.21
Couple, $s = hs$ (\$44,241)	\$47,799	7.19	5.05
Couple, $s = cod$ (\$59,484)	\$51,607	6.55	3.66
Couple, $s = co$ (\$88,968)	\$64,478	-0.17	3.62

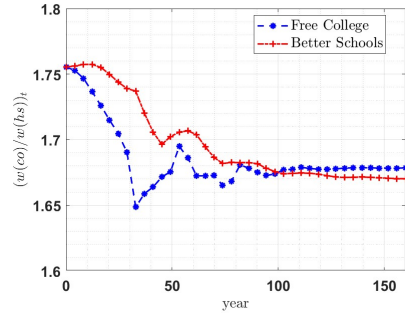
Notes: Annual gross earnings % change relative to the baseline, averaged over the working life. In parenthesis, own parental (annual, averaged over the working life) earnings are shown.

Table 5 shows that both reforms reduce the earnings gap between socio-economic groups. Interestingly, the reduction is larger in the “free college” reform than in the “better” schools

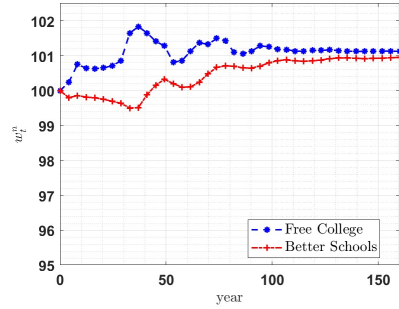
Figure 6: Prices and Taxes in General Equilibrium



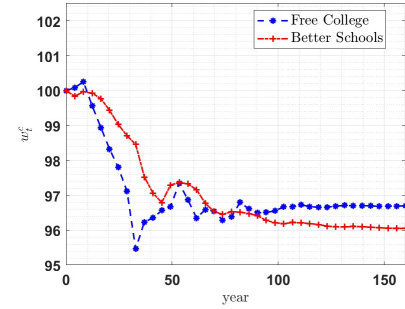
(a) Interest Rate



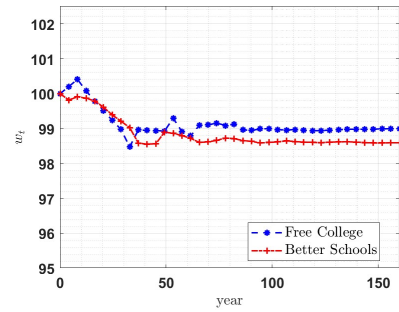
(b) College Wage Premium



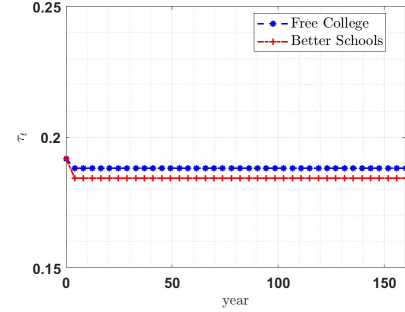
(c) Non-College Wage



(d) College Wage



(e) Average Wage Level



(f) Labor Income Tax Level Parameter τ

Notes: Panel (a): Interest rate; Panel (b): College wage premium; Panel (c): Non-college wage; Panel (d): College wage; Panel (e): Average wage level; Panel (f): Labor income tax parameter τ .

reform because children from the highest socio-economic group overwhelmingly attend college even without it being free, and thus this reform does not induce earnings gains for this group. The “better schools” reform in contrast elevates the accumulation of (earnings-relevant) human capital of all children (including those at the very top). As a result, this reform “raises all boats” and the resulting reduction of child earnings inequality is less pronounced.

Table 6: Intergenerational Education Transition Matrix: Initial Steady State

Single Parents				
	$s = hsd$	$s = hs$	$s = cod$	$s = co$
$s^p = hsd, q = si$	0.12	0.71	0.08	0.09
$s^p = hs, q = si$	0.10	0.68	0.10	0.12
$s^p = cod, q = si$	0.09	0.58	0.15	0.18
$s^p = co, q = si$	0.06	0.02	0.43	0.49
Married Parents				
	$s = hsd$	$s = hs$	$s = cod$	$sof = co$
$s^p = hsd, q = cpl$	0.11	0.68	0.11	0.12
$s^p = hs, q = cpl$	0.10	0.57	0.16	0.17
$s^p = cod, q = cpl$	0.09	0.47	0.21	0.23
$s^p = co, q = cpl$	0.06	0.02	0.43	0.49

Notes: Intergenerational education mobility: rows show parental background, columns show conditional child education shares.

Finally, Tables 6 and 7 display the intergenerational transition matrix of educational attainment as well as the changes induced by the policy reforms, separately for single parents (on average the poorest families in the population) and for married parents with dual earners. Table 6 shows the strong intergenerational persistence of education in the benchmark economy: the share of children from parents without a high school degree going to college (and succeeding or dropping out) is only 17% for those with single parents and 22% for those with married parents. In contrast, this number rises to 92% for those with parents that have a college degree (roughly independent of marital status of the parent).

Table 7 summarizes one key dimension of the distributional consequences of the educational policy reforms, by showing how the intergenerational education transmission matrices for children with single mothers (that is, the share of children with maternal education $s^p \in \{hsd, hs, cod, co\}$ that end up with own education s) are affected by both policies (in the long run, comparing steady states).^{36,37} Positive percentage point changes relative to the baseline are marked in red, negative changes are marked in blue. The table highlights the very different impact of both reforms on intergenerational persistence of education. A “free college” reform has virtually no impact on the share of children dropping out of high school (for any parental type). It is successful, however, in drawing a much larger share of those previously only completing high school into college, but

³⁶Note that the respective steady state is induced by the respective full policy transition.

³⁷The corresponding results for married parents are contained in Appendix A.3.

Table 7: Intergenerational Education Transition Matrix: Single Parents

Increased School Funding				
	$s = hsd$	$s = hs$	$s = cod$	$s = co$
$s^p = hsd, q = si$	-0.03	-0.10	0.08	0.05
$s^p = hs, q = si$	-0.03	-0.10	0.08	0.05
$s^p = cod, q = si$	-0.03	-0.09	0.10	0.02
$s^p = co, q = si$	-0.02	-0.01	-0.03	0.06
Free College				
	$s = hsd$	$s = hs$	$s = cod$	$s = co$
$s^p = hsd, q = si$	0.00	-0.36	0.27	0.09
$s^p = hs, q = si$	0.00	-0.37	0.29	0.08
$s^p = cod, q = si$	0.00	-0.34	0.28	0.05
$s^p = co, q = si$	0.00	-0.01	0.00	0.00

Notes: Changes in intergenerational education mobility: rows show parental background, columns show conditional child education shares. Table entries show absolute changes in conditional child education shares relative to the benchmark economy.

close to 3/4 of these additional college goers end up dropping out of college (see the last two columns of the lower panel of Table 7). Since for most teenagers dropping out of college is ex-post inefficient (had they known they would not succeed, they would have opted not to attend college in the first place), the reform is not a very effective intervention of raising the share of the population with a college degree.

In contrast, the “better schools” reform (upper panel of Table 7) significantly reduces high-school dropout rates (see first column of the table), but it is much less effective shifting previous high-school completers into attempting college. Conditional on going, however, the rise in the dropout rate is much less pronounced than in the free-college reform since teenagers under the “better schools” reform are much better prepared for college (in the sense of having higher human capital which translates into lower dropout probabilities). The results from both reforms displayed here also suggest that a mixed reform that uses some of the budget to improve schools to make children more college ready and make it cheaper to attend (albeit not necessarily free) could attain higher attendance without massively increasing dropout, and thus achieve the best of both worlds. This is in fact what we will demonstrate in Section 7 on the optimal (within a restricted policy set) policy reform.

6.2.4 The Welfare Consequences of the Reforms

Figure 7 displays the welfare consequences of both policy reform transitions, measured as consumption equivalent variation of economically newborn individuals (i.e., based on expected lifetime utility at age 18), and plotted as a function of the period of the transition at which these individuals enter the economy (i.e., $t = 0$ means individuals becoming economically active in the first

period of the transition). Specifically, we ask what uniform³⁸ increase of consumption households born into the old steady state would require to be indifferent between the status quo steady state and to being born into the transition induced by the policy reform. The left panels are for the “free college” reform and the right panels are for the expansion of public school funding.

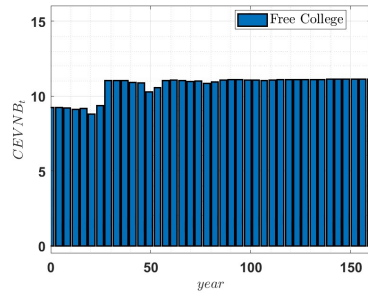
In order to distinguish the welfare gains originating from newborns living a better life (i.e., having a larger value function for a given initial state (a, h, s_p) of a newborn and facing an improved distribution of potential marriage partners) from an improved (or worsened) distribution over these initial state variables (Φ_t vs. Φ_0), in the lower panels we display the welfare consequences that would emerge if the (endogenous) distribution over initial characteristics were to remain unchanged at Φ_0 . Thus, the lower panel captures purely the welfare gains from higher lifetime utilities of the different types of economically newborn individuals, and the difference between the upper and the lower panels therefore reflects the welfare consequences of the endogenous and policy-induced shift in the distribution of the initial characteristics (human capital, financial wealth and parental education (a, h, s_p)) of the 18-year olds.³⁹

We highlight three qualitative points. First, both reforms entail substantial welfare gains for current newborns and future generations. In contrast to aggregate allocations, the welfare gains are fairly smooth across generations along the transition. The availability of government debt allows the government to smooth the short-run costs and use the long-run higher tax revenues from the education reform to make the transition “painless” for newborns (and the majority of the currently alive). Second, as a comparison between the upper and the lower left panel reveals, the direct benefits of “free college” for 18 year-olds are partially offset by the fact that they enter adult life with fewer assets as their parents respond to the policy by adjusting inter-vivos transfers. That is, the actual welfare gains for the youth are smaller compared to a scenario where the policy is evaluated under a fixed initial distribution of wealth (as well as human capital), at least early in the transition. Along the transition, the fact that young adults have better educated parents offsets this effect. Third, and in sharp contrast, a large part of the welfare gains with better school funding comes from an improved human capital and parental education distribution and these gains increase over time, as can be seen comparing the top and the bottom right panels. This reinforces the need for studying (debt financed) policy *transitions* when considering fundamental education reforms.

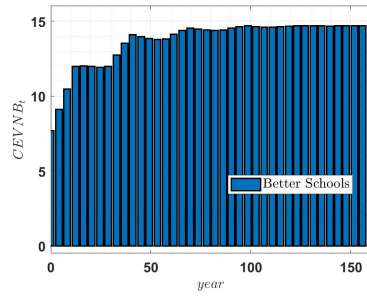
³⁸Uniform across individual types —initial assets, human capital and parental education— across time and states of the world.

³⁹It is understood that the lifetime utilities of newborns are also affected by changes in the marriage market distribution.

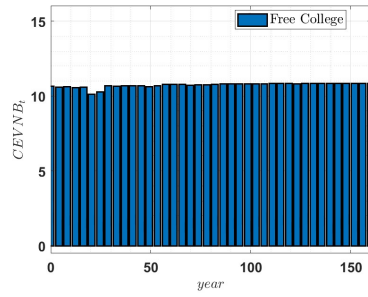
Figure 7: Welfare Gains of Newborns



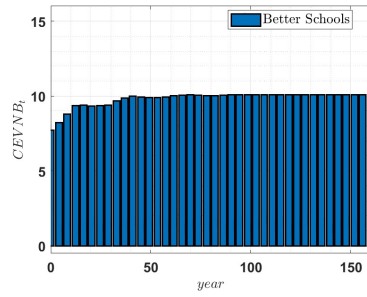
(a) CEV Newborns: Free College



(b) CEV Newborns: Pre-College Funding



(c) CEV NB: Free College, Φ_0

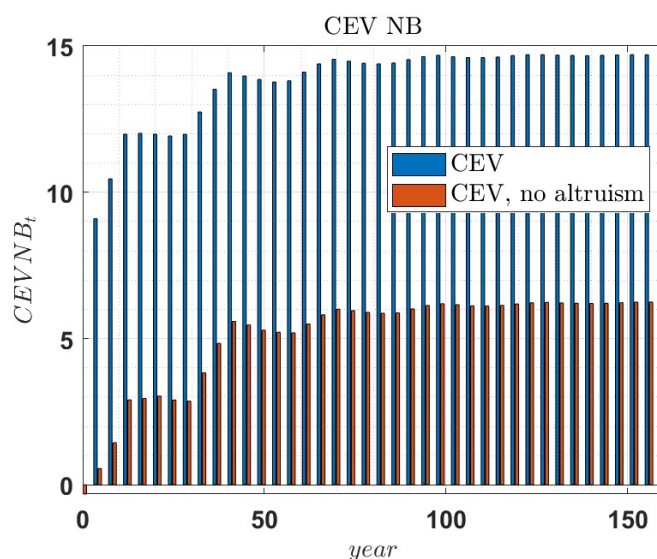


(d) CEV NB: Pre-College Funding, Φ_0

Notes: Panel (a) and Panel (b): newborn CEVs under actual period t cross-sectional distribution $\Phi_t(j_a, \cdot)$; Panel (c) and Panel (d): newborn CEVs under initial steady state period 0 cross-sectional distribution $\Phi_0(j_a, \cdot)$.

The magnitude of the welfare gains is perhaps surprisingly large, in the order of 10-15% of permanent consumption.⁴⁰ It is important to note here that in our model with parental altruism a potentially large part of these welfare gains, especially for generations born early in the transition, may come from the better lives these generations expect their children (and grandchildren) to have later during the transition and in the new steady state. Figure 8 shows that this is indeed the case, by displaying, by birth cohort, the welfare gains from the “better schools” reform documented in the upper right panel of Figure 7 as well as those welfare gains in the absence of intergenerational altruism.⁴¹ The key observation is that for early transition cohorts almost all of the welfare gains stem from better lives of their offspring, and even in the steady state this effects accounts for a large share (approximately 60%) of the overall welfare gains.

Figure 8: Better Schools Reform, Welfare Gains with and without Altruism



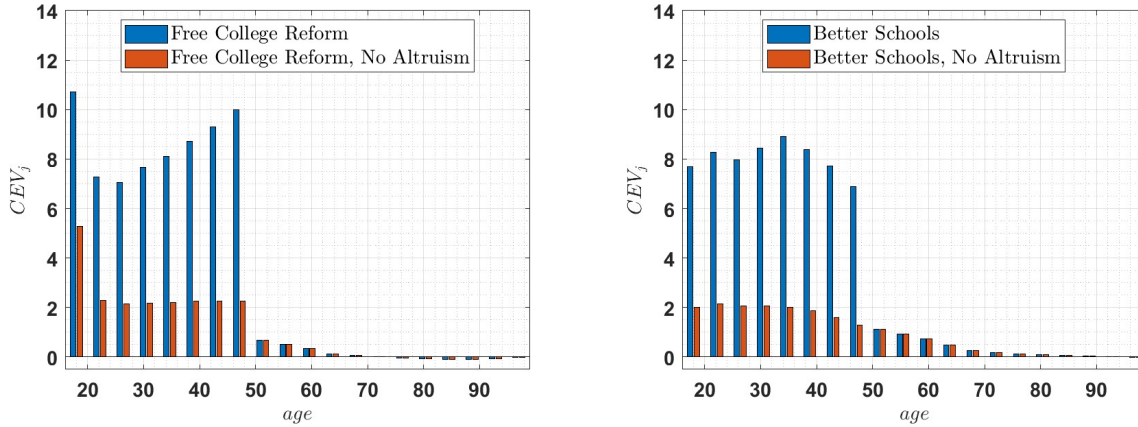
Notes: Newborn CEV under “Better Schools” reform under two welfare metrics: accounting for intergenerational altruism (blue bars), and ignoring utility from children (red bars).

Of course, welfare gains for academically newborn agents might partially come at the cost of welfare losses for existing (at the time of the policy reform) generations that do not benefit directly from the reforms since their human capital accumulation and tertiary education decisions lie in the past. However, since these generations are altruistically motivated toward their children, these generations might benefit indirectly through higher expected lifetime utility of their offspring. They are also affected by GE price and government budget adjustments.

⁴⁰Daruich and Fernández (2024) document welfare consequences of fundamental reforms of the welfare system in a model with intergenerational links and altruism that are of similar magnitude.

⁴¹For the latter, we use the same decision rules as in the benchmark, that is, households behave as if they are altruistic, but welfare is evaluated with preferences (and thus a value function) that abstracts from altruism, i.e., sets $\nu = 0$. The results for the “free college reform are qualitatively similar.

Figure 9: Welfare Gains of Currently Alive Population



(a) CEV Currently Alive, Total Population: “Free College” (b) CEV Currently Alive, Total Population: “Better Schools”

Notes: CEV of currently alive population by age (blue bars show the full welfare metric accounting for intergenerational altruism, red bars show the welfare outcomes without accounting for lifetime utility of children).

In Figure 9 we summarize the welfare consequences (again measured in terms of consumption equivalent variation) for these generations (by their age, and again averaged over their relevant state variables). Again the left panel is for the “free college” reform and right panel for the “better schools”; for both reforms we additionally show the welfare consequences when ignoring intergenerational altruism. We observe that younger generations with children still in the household also gain, mostly on account of the higher lifetime utility of their children, or the children they expect to have, in case of individuals that are younger than 26. This latter group also benefits from the fact that with some probability they will marry, and under the reform will marry someone with more human capital (and thus higher earnings which they get to share).

Older generations (those age 46 and older whose college education is completed and whose children have left the households) have smaller welfare gains, and if they are retired, might actually suffer welfare losses. This is due to general equilibrium effects: when wages fall, so do benefits from the PAYGO social security system, which offset (and for older households, dominate) the mild increase in asset returns and (if still in working age) the reduction in the labor income tax rate. Note, however, that these welfare losses are relatively mild. Thus, although neither reform constitutes a Pareto improvement (since the current old lose), it is conceivable that a reform that phases in the tax increases slowly might be sufficient to avoid the welfare losses for generations older than 46 at the time of the reform that Figure 9 documents.⁴²

⁴²Although not necessary here, in Section 7 we will introduce specific social welfare functions to aggregate the welfare gains and losses documented here, and to determine (according to those social welfare func-

6.3 Discussion of Key Modeling Elements

6.3.1 Importance of General Equilibrium

To isolate the importance of changes in endogenous interest rates and (relative) wages we also conduct a sequence of partial equilibrium exercises in which we hold these endogenous prices as well as the taxes required to balance the intertemporal government budget constant. As a summary, we show that qualitatively, the aggregate and to a large degree the distributional conclusions discussed above also emerge in the absence of equilibrium price adjustments. However, endogenous interest and (relative) wage adjustments in general equilibrium make the welfare gains for newborn generations smaller (relative to partial equilibrium) and reduce the difference between the two reforms.

The most important general equilibrium effects stem from the fact that inflow of more college-educated workers into the labor market (induced by the education reforms) and their higher human capital lowers both the capital-labor ratio and the college wage premium, in turn muting the increase in the college share in general equilibrium relative to partial equilibrium. The decline in the capital-labor ratio puts downward pressure on all wages (which hurts workers) but raises the interest rate. The *relative* wage effect, which provides welcome (from the perspective of ex-ante utility) redistribution across education types, is stronger in the school expenditure expansion reform since college enrollment decisions are more sensitive to the college wage premium in that thought experiment.

In addition, an increase in the interest rate induced by the reduction of the capital-labor ratio⁴³ in general equilibrium mutes the crowding-out effect of the “free college” reform on inter-vivos transfers and results in a larger crowding-in under the school expenditure reform. Overall, as a result of these general price movements and required tax adjustments, the welfare gains are smaller in general relative to partial equilibrium, and the *difference* between the two reforms is smaller in general equilibrium relative to partial equilibrium as well.

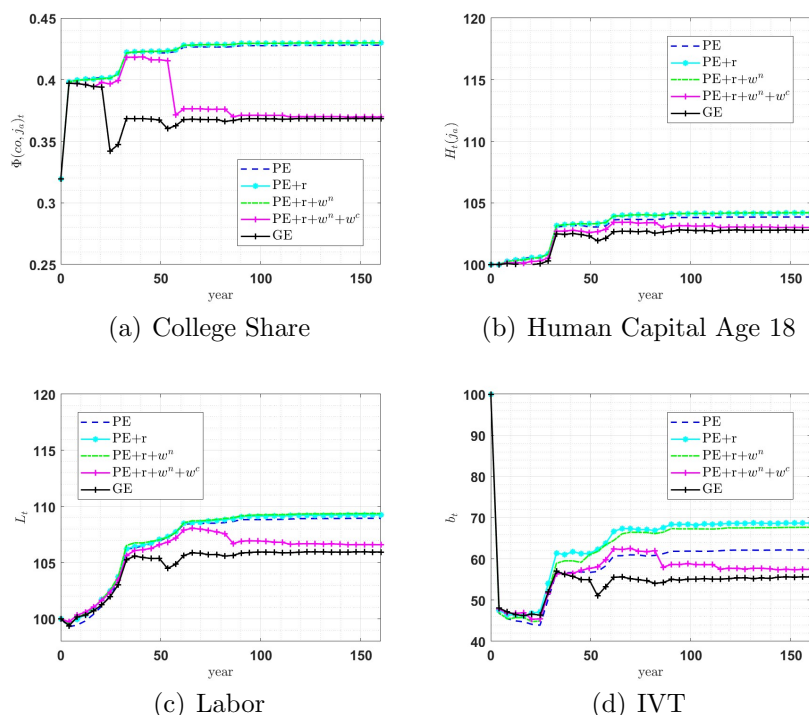
In Figure 10 we display the college share, human capital at age 18, aggregate efficiency units of labor as well as inter vivos transfers for the “free college” reform for five scenarios. The first is our general equilibrium benchmark experiment. The second scenario labeled partial equilibrium (“PE”) holds all prices (wages and interest rates) constant, but adjusts the level tax parameter τ once and for all so that the intertemporal government budget constraint continues to hold in partial equilibrium. The remaining three scenarios depart from the PE scenario, but

tions) the optimal mix of both policies. Not surprisingly, the aggregated welfare gains lie in between those experienced by the newborns and existing old generations.

⁴³The reduction of the capital-labor ration is in turn due to the increase in effective labor as well the reduced savings incentives for privately funded education expenditures and inter-vivos transfers and the shift from capital to government debt.

sequentially feed in the GE interest path (“PE+r”), then also the wage path for non-college labor (“PE+r+wⁿ”) and then also the wage for college labor (“PE+r+wⁿ+w^c”). The only difference between this last scenario and the “GE” scenario is that the latter has a higher labor income tax rate, relative to the tax level needed in partial equilibrium. These thought experiments seek to isolate the importance of changes in wages and changes in the real interest rate induced by the “free college” reform. Figure 11 does the same for the “Better Schools” reform.

Figure 10: Free College Reform, Aggregate Variables: GE Decomposition



Notes: Panel (a): Share of a given “birth” cohort that completes college; Panel (b): Average human capital of a given “birth” cohort at age 18 (Initial Steady State = 100); Panel (c): Aggregate labor efficiency units (Initial Steady State = 100); Panel (d) Aggregate Inter-vivos transfers (Initial Steady State = 100).

PE: partial equilibrium; GE: general equilibrium; PE+r: PE and the interest rate path from GE; PE+r+wⁿ: PE+r and the non-college wage path from GE; PE+r+wⁿ+w^c: PE+r+wⁿ and the college wage path from GE.

Very broadly, and with some nuance for a subset of the variables, the key general equilibrium effect comes from the endogenous adjustment of college-educated labor. This is apparent from the upper left panel of the figure. The partial equilibrium response of the college share is large and increasing over time, and adjustments in the interest rates do not change that finding (as the three lines are virtually on top of each other). However, when the college wage adjusts downward (as it does in GE), after an initial massive increase this share falls and settles down at a somewhat higher level relative to the pre-reform scenario. The general equilibrium wage effects

are also important for the intergenerational persistence of education: as Table 15 in Appendix A.4 shows, in partial equilibrium the “better schools” reform is actually quite successful drawing poor children with single mothers into college, but the decline in the college wage premium in general equilibrium largely offsets this effect (as we have shown above).

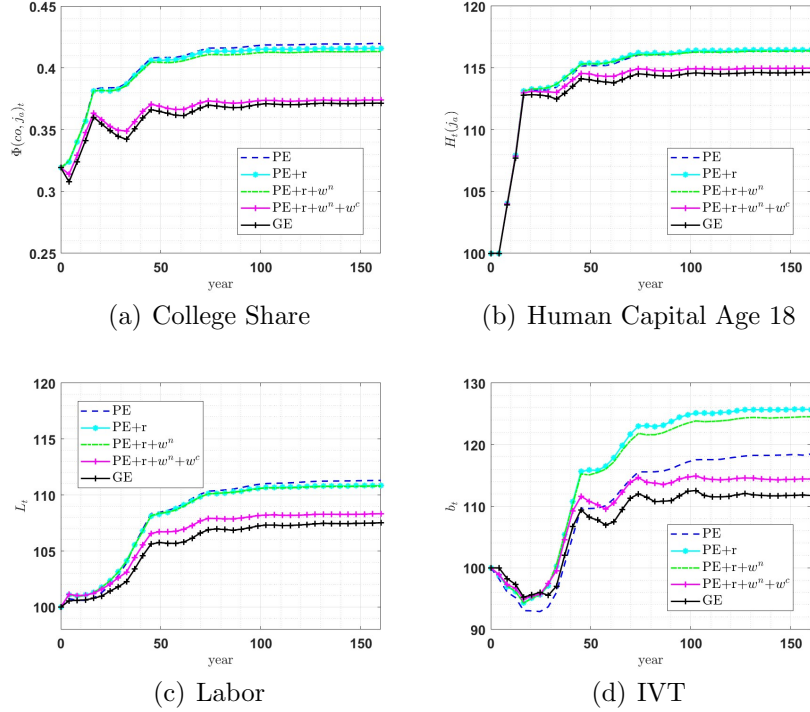
The (relatively small) change in the tax rate does not much affect this conclusion that it is the decline in the college wage (and thus the college wage premium) in general equilibrium that enacts the largest impact on the college share. This is also the driving force behind the smaller welfare gains of both reforms in general relative to partial equilibrium. Figures 14 and 15 as well as Table 10 in the Appendix show that, as a result of these general price movements, the welfare gains are 3.1-4.6 percentage points smaller, and the *difference* between the two reforms is also lower by 1.5 percentage points.

The endogenous interest rate increase (see again panel (a) of Figure 6) has only a minor effect on the college share, as the difference between the PE and the “PE+ r ” line in panel (a) is negligible. In contrast, the rise in the interest rate is more important for the intergenerational transmission of wealth, as panels (d) of Figures 10 and 11 display. Comparing the blue “PE” line with the cyan “PE+ r ” line shows that the increase in the interest rate in general equilibrium mitigates (but not fully offsets) the decline in inter-vivos transfers that the education reforms, especially the “free college” reform would otherwise have induced.

6.3.2 Importance of Government Debt

We have so far documented that both reforms are (more than) budget-neutral in an intertemporal sense, but required quite significant temporary deficits and thus an increase in government debt (relative to GDP) along the transition. In Appendix A.5 we analyze the quantitative importance of access to additional government debt, by considering a world in which the reform has to be financed period by period by tax changes which are sizable tax increases in the short run (see upper right panel of Figure 17). Without access to additional government debt the education reforms create recessions in the short run, in that labor input, GDP and aggregate consumption fall on impact on account of the reform-induced tax increases (see Figure 17) and the welfare gains for existing and future transitional generations are substantially smaller. Interestingly, if government debt is forced to be constant, relative to GDP, in the long run the economy has less debt and lower taxes than in the benchmark economy, and consequently the newborn steady state welfare gains from the education reform are actually larger in the absence of a reform induced debt expansion (see lower left panel of Figure 17 in the Appendix).

Figure 11: Better Schools Reform, Aggregate Variables: GE Decomposition



Notes: Panel (a): Share of a given “birth” cohort that completes college; Panel (b): Average human capital of a given “birth” cohort at age 18 (Initial Steady State = 100); Panel (c): Aggregate labor efficiency units (Initial Steady State = 100); Panel (d) Aggregate Inter-vivos transfers (Initial Steady State = 100). PE: partial equilibrium; GE: general equilibrium; PE+r: PE and the interest rate path from GE; PE+r+wⁿ: PE+r and the non-college wage path from GE; PE+r+wⁿ+w^c: PE+r+wⁿ and the college wage path from GE.

7 Optimal Policy

Thus far, we have considered two “pure” policy reforms in isolation and have seen that both generated significant welfare gains. We have also documented that especially for children from poor families college remains largely out of reach since under a “free college” reform the low human capital acquired in primary and secondary school translates into college failure rates that are so high to make college unattractive even if free. The pure “better schools” reform, in contrast, raises human capital of the entire population, including poor children, but without some college tuition subsidies going to college remains too expensive for the poorest children.

This raises the question whether a combination of both reforms raises human capital of these children sufficiently to make college success feasible while sufficiently reducing the cost to make it affordable. To provide guidance for such a joint policy analysis, we present in Appendix D a simple theoretical model, which establishes that the two policy instruments are relative welfare substitutes and relative welfare complements at the same time, as also transparently shown

in [Guerrieri \(2024\)](#). On the one hand, both instruments decrease the human capital threshold it takes to attend college. On the other hand, increasing human capital through increased school spending increases relative wages of college youngsters and reduces their dropout probabilities, and therefore a policy reform of increased school financing may complement a policy reform of reduced college fees. Due to this dual role of the policy instruments it is a quantitative question whether our analysis of joint policies delivers a corner solution such that the “better schools” policy reform is the preferred policy choice, or an interior solution with an optimal mix of both instruments.⁴⁴

When addressing this quantitative question in this section, we hold constant the total cost of the reform at the level in the previous section. Specifically, let Ω be the share of the total additional government education expenditures be allocated to “better school” financing and $1 - \Omega$ be the share devoted college tuition subsidies. The reforms in the previous section correspond to $\Omega = 0$ (“free college”) and $\Omega = 1$ (“better schools”). We now seek to find the $\Omega^* \in [0, 1]$ that maximizes social welfare $\mathcal{W}(\Omega)$.

7.1 Measurement of Social Welfare

In our life cycle economy with current and future generations and heterogeneity within generations the choice of the social welfare function $\mathcal{W}(\Omega)$ is not obvious. We will consider two alternatives, chosen again to highlight the potential distinction and conflict between the policy impact in the short- and in the long run. Our long-run welfare measure is the expected lifetime utility of economic newborns in the steady state, where as before expectations are taken under the veil of ignorance, that is, before the initial state (a, h, s_p) is realized. This was the welfare measure the discussion in the previous section has focused on.

The second alternative that captures the welfare consequences both for generations living through the transition and those born into the new steady state, is based on the lump-sum redistribution authority concept initially introduced by [Auerbach and Kotlikoff \(1987\)](#). Specifically, for each individual currently alive we compute the (possibly negative) wealth transfer required to make the individual indifferent between the status quo and a specific reform. We do the same for all newborn generations along the transition path and in the new steady state. We then aggregate these transfers using the populations shares in the initial steady state (for individuals already alive) and the relative size of newborn agents (relative to the population in the initial steady state), and discount transfers along the transition using the initial equilibrium interest rate (so that the discounting is the same for all policy reforms considered). Finally, for comparison

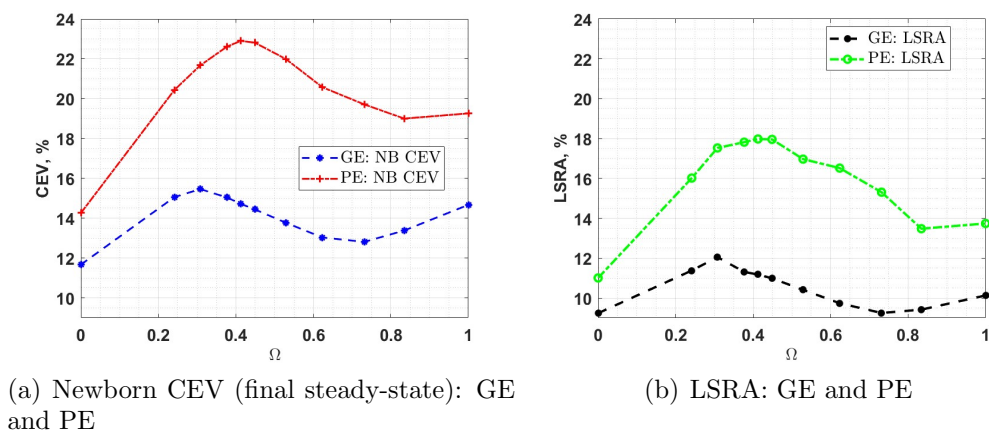
⁴⁴This also reemphasizes the crucial role of our model validation in Section 5 showing that the results of our calibrated model are consistent with empirical estimates of both instruments in raising college participation.

with other welfare measure we translate the aggregate wealth transfer into a flow consumption measure. For details how the LSRA welfare measure is constructed, see Appendix B.4.

7.2 The Optimal Policy Mix

In Figure 12 we plot the welfare gains, measured as CEV of newborns in the steady state and (flow-consumption based LSRA) as a function of the policy weight Ω , where again $\Omega = 0$ is the “free college” reform and $\Omega = 1$ corresponds to the “better schools” reforms discussed in the previous section. We do so for the general equilibrium benchmark model and, in order to interpret results, for the partial equilibrium version of the model.

Figure 12: Joint Reforms in GE and PE: Welfare



Notes: Ω (on the x-axis) denotes the relative weight on the i^g reform.

Although the precise optimum Ω^* evidently depends on the adopted welfare criterion, three robust findings emerge. First, and consistent with the previous section, for all weights Ω the welfare gains of the policy reforms are quite sizable (in the order of above 10% of lifetime consumption) and larger in partial equilibrium than in general equilibrium. Second, the CEV welfare measure that focuses on steady states shows larger gains than the ones that includes transitional generations (the LSRA measure), again confirming that the full welfare benefits of the reforms take time to materialize. Finally, and most importantly for the purpose of this section, the highest welfare is attained in the interior of the policy space and spends ca. $1/3$ of its budget on better schools and the remainder on subsidizing the cost of college. Thus, while aggregate welfare is higher under the pure “better schools” reform than under the “free college” reform, it takes a larger share of the spending share on college than on schools in the optimal mix. The reason is the discrete nature of the college decision: it takes a sufficiently large college reform to

move many individuals to complete college and to thereby effectively complement the schooling reform.⁴⁵

As Table 8 shows that, although all three reforms are successful in reducing the dispersion of wages and the poverty rate in the population (in the long run), relative to both extreme reforms the optimal policy mix leads to a larger reduction in the poverty rate, and has a similar effect on the variance of log wages as the better schools reform. The same is true for the intergenerational persistence of poverty, as the last column of Table 8 shows.

Table 8: Distributional Statistics: Benchmark Model and Policy Reforms

	Variance of Log Wages	Poverty Rate	Prob. of Stay in Q1
Baseline	0.4419	14.31%	21.54%
Free College	0.4326	12.82%	16.51%
Better Schools	0.4331	12.11%	15.59%
Optimal Policy	0.4381	11.54%	14.86%

Notes: The variance of log wages is computed on the sample of the entire working age population, i.e. ages 22-65. The poverty rate is computed based on the OECD poverty definition according to which the poverty threshold is set at 50% of median household disposable income, adjusted for the household size using the OECD household equivalence scale (0.5 for an additional adult, 0.3 for a child). The probability of staying in the lowest quintile of the income distribution is computed based on gross total household incomes.

Table 9 displays the change in intergenerational education persistence induced by the optimal policy mix; it is the counterpart of Table 7 and shows that the mixed reform is almost as successful as the pure “better schools” reform in curbing dropping out of high-school, while almost as successful as the “free college” reform in strengthening college completion, albeit at the cost of some additional college drop-outs (which is significantly less pronounced than in the pure “free college” reform). In this sense, and within the same fiscal budget, the mixed reform achieves the “best of both worlds”, with resulting welfare gains that surpass both pure reforms.

At the heart of this result is that one policy draws in more teenagers into college, and the other insures that these additional students are well-enough prepared so that dropout rates are kept in check. This is in line with our simple model presented in Appendix D.

8 Conclusion

In this paper we have studied the optimal combination of college tuition subsidies and school financing, for a given pre-specified budget for these reforms. To do so, we have developed a

⁴⁵Smaller spending on colleges instead mainly constitutes a consumption transfer to individuals that already attend college. It is then more efficient to spend this money on schools. This mechanism also explains the non-monotonicity in Figure 12 of the gains in the share parameter Ω .

Table 9: Intergenerational Education Transition Matrix: Optimal Mix

	Single Parents			
	$s = hsd$	$s = hs$	$s = cod$	$s = co$
$s^p = hsd, q = si$	-0.02	-0.20	0.14	0.09
$s^p = hs, q = si$	-0.02	-0.18	0.13	0.07
$s^p = cod, q = si$	-0.02	-0.17	0.13	0.06
$s^p = co, q = si$	-0.01	-0.01	-0.01	0.03

Notes: Changes in intergenerational education mobility: rows show parental background, columns show conditional child education shares. Table entries show absolute changes in conditional child education shares relative to the benchmark economy.

quantitative modeling framework that allows for a joint analysis of transitions induced by policies concerned with pre-labor market entry pre-distribution and post-labor market entry redistribution. Using this model we have evaluated the aggregate, distributional and welfare consequences of these reforms targeted at different stages of childhood and adolescence. We found that although individual reforms generate very significant welfare gains, a combination of both is most effective, in a welfare sense, of both curbing high-school dropout rates and encouraging college attendance without an overly large increase in college dropout rates.

Our analysis held the overall size of the education reforms constant. An analysis of the optimal size of the reform(s), both in the presence and the absence of a period-by-period budget balance assumption, would be informative about the importance of the “fiscal space” for the success of education reform. More broadly, we have taken the remainder of the fiscal constitution, that is, the tax-transfer system as given and invariant to the education policy reform. However, especially changes in the welfare system making transfers to the poor (which they might be used for additional education investments by the impacted families) could provide an alternative mobility enhancing policy. A quantitative analysis of a more comprehensive reform of the entire tax-transfer-education financing system, with specific focus on the performance of children of single mothers that constitute more than 20% of the current US child population⁴⁶ and are subject to particularly low upward mobility levels, would be especially relevant in this context. We defer this to ongoing and future work.

⁴⁶See e.g. the 2019 Pew Research Center study on “Religion and Living Arrangements Around the World”

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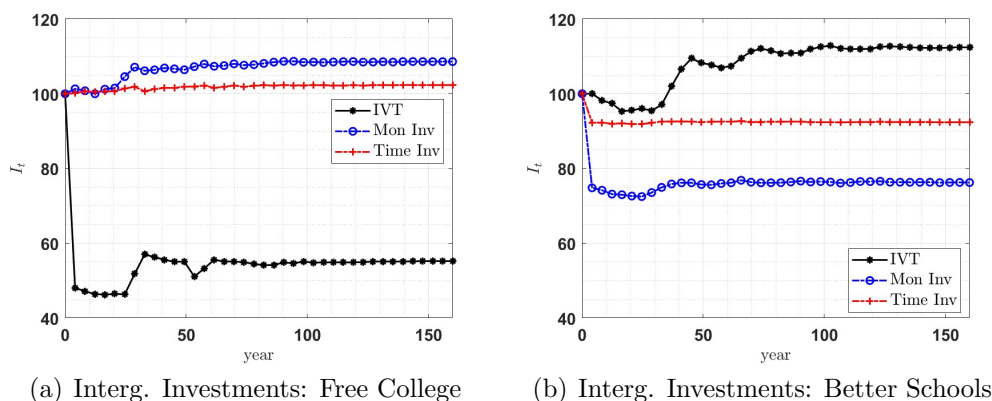
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A Additional Quantitative Results

A.1 Parental Investment Responses: “Free College” and “Better Schools”

The optimality condition linking parental resource and time input choices is derived in Appendix B. The plots below show the average per child parental inputs in terms of money, time as well as inter-vivos transfers for the two main reform scenarios. These are aggregate parental input adjustments in the education reform induced transitions. In both reform scenarios, resource investment in children responds stronger in the aggregate than the time investment. From the optimality condition linking monetary and time inputs, $\frac{i_m}{i_t^{1+\psi}}$ is a decreasing function of the marginal utility of consumption. This relation at the individual level, aggregated up, moves in the same direction as the aggregate consumption. Given the optimal consumption responses, the ratio $\frac{i_m}{i_t^{1+\psi}}$ moves up in the aggregate, but the ratio $\frac{i_m}{i_t}$ moves slightly down, i.e. the positive consumption response would need to be even stronger to make the $\frac{i_m}{i_t}$ ratio move upward.

Figure 13: Parental Investments



Notes: Intergenerational transfers under “Free College” (panel (a)) and “Better Schools” (panel (b)): inter-vivos transfers, monetary and time human capital investments in children.

A.2 Comparison of Steady States: Summary Tables

Table 10: Aggregates, Prices, Taxes and Welfare: Univariate Reforms

Variable	Initial SS	Δ GE FC	Δ PE FC	Δ GE i^g	Δ PE i^g
$\Phi(j_a, s = co)$	31.93%	4.92	10.87	5.23	10.04
$\Phi(j_a, s = cod)$	28.61%	14.92	10.06	3.85	3.64
$\Phi(j_a, s = hs)$	31.01%	-19.23	-20.15	-6.54	-10.88
$\Phi(j_a, s = hsd)$	8.45%	-0.61	-0.79	-2.54	-2.79
HK	1.00	2.78	3.86	14.64	16.41
L	8.85	5.94	8.90	7.57	11.34
Hours	0.28	1.09	1.83	2.36	3.77
C	7.70	7.35	9.67	8.74	11.59
K	12.55	2.00	-9.16	3.42	-9.62
B	3.38	36.54	64.30	58.54	89.23
Revenues	2.54	9.77	11.22	12.54	13.08
Y	13.22	4.72	3.46	6.31	4.93
r (annual)	3.14%	0.17	0.00	0.22	0.00
w	0.74	-1.28	0.00	-1.34	0.00
$\frac{w^c}{w^n}$	75.55%	-7.69	0.00	-8.57	0.00
w^n	0.97	1.11	0.00	1.01	0.00
w^c	1.70	-3.32	0.00	-3.92	0.00
τ	0.22	-1.72	-5.40	-3.24	-8.63
τ^P	12.40%	0.14	-0.06	-0.16	-0.43
$\frac{T(AE_0)}{Y}$	0.19	-0.40	-1.26	-0.76	-2.02
$\frac{AE_0}{Y}$	11.34%	0.28	1.16	0.23	0.98
CEV NB	0.00%	11.17	14.26	14.68	19.26
CEV alive	0.00%	4.49	5.26	4.34	5.58
LSRA	0.00%	9.24	11.01	10.13	13.74

Notes: The table summarizes long-run changes (induced by policy transitions) in the main aggregate variables, general equilibrium prices and taxes, and welfare. Changes for baseline variables initially stated in percentages are expressed in percentage points (%p), while changes for baseline variables initially in levels are shown as percentages (%).

GE refers to the full general equilibrium version of the model where wages and interest rate are endogenous as well as the government budget constraints are balanced. The PE version refers to a life cycle model with balanced government budgets, with aggregate physical capital being computed as: $K_t = A_t - B_t$, where A_t are total household assets, and B_t is debt stock (which is endogenous and results from re-balancing the intertemporal government budget constraint).

Table 11: Aggregates, Prices, Taxes and Welfare: Free College

Variable	Initial SS	Δ PE	Δ PE+r	Δ PE+r, $w(s < co)$	Δ PE+r, $w(s < co), w(co)$	Δ GE
$\Phi(j_a, s = co)$	31.93%	10.87	11.07	11.07	5.04	4.92
$\Phi(j_a, s = cod)$	28.61%	10.06	10.10	10.10	14.98	14.92
$\Phi(j_a, s = hs)$	31.01%	-20.15	-20.31	-20.30	-19.36	-19.23
$\Phi(j_a, s = hsd)$	8.45%	-0.79	-0.86	-0.86	-0.65	-0.61
HK	1.00	3.86	4.18	4.20	3.00	2.78
L	8.85	8.90	9.19	9.32	6.57	5.94
Hours	0.28	1.83	2.16	2.41	2.09	1.09
C	7.70	9.67	11.80	12.28	8.81	7.35
K	12.55	-9.16	0.67	1.57	-2.96	2.00
B	3.38	64.30	64.29	64.29	64.29	36.54
Revenues	2.54	11.22	15.60	16.61	8.68	9.77
Y	13.22	3.46	7.62	8.39	3.52	4.72
r (annual)	3.14%	0.00	0.17	0.17	0.17	0.17
w	0.74	0.00	0.00	0.00	-1.28	-1.28
$\frac{w^c}{w^n}$	75.55%	0.00	0.00	0.00	-7.69	-7.69
w^n	0.97	0.00	0.00	1.11	1.11	1.11
w^c	1.70	0.00	0.00	0.00	-3.32	-3.32
τ	0.22	-5.40	-3.24	-3.24	-3.24	-1.72
τ^p	12.40%	-0.06	-0.06	-0.06	-0.06	0.14
$\frac{T(AE_0)}{AE_0}$	0.19	-1.26	-0.76	-0.76	-0.76	-0.40
$\frac{Lab. Inc. Tax Rev}{Y}$	11.34%	1.16	0.71	0.76	0.15	0.28
CEV NB	0.00%	14.26	16.95	17.79	13.41	11.17
CEV alive	0.00%	5.26	5.90	6.15	5.35	4.49
LSRA	0.00%	11.01	12.88	14.08	10.61	9.24

Notes: The table summarizes long-run changes (induced by policy transitions) in the main aggregate variables, general equilibrium prices and taxes, and welfare. Changes for baseline variables initially stated in percentages are expressed in percentage points (%p), while changes for baseline variables initially in levels are shown as percentages (%).

GE refers to the full general equilibrium version of the model where wages and interest rate are endogenous as well as the government budget constraints are balanced. The PE version refers to a life cycle model with balanced government budgets, with aggregate physical capital being computed as: $K_t = A_t - B_t$, where A_t are total household assets, and B_t is debt stock (which is endogenous and results from re-balancing the intertemporal government budget constraint).

PE+r refers to the PE version where the interest rate path from the GE version is exogenously imposed - without any adjustments of other outer-loop variables. Therefore, the government budget constraints do not have to hold, and therefore the debt values (as well as the implied physical capital $K_t = A_t - B_t$ and thus also output are not shown, and marked as n/a.

PE+r, $w(s < co)$, $w(co)$ refers to the PE version where the interest rate and wages paths from the GE version are exogenously imposed - without any adjustments of other outer-loop variables.

Table 12: Aggregates, Prices, Taxes and Welfare: Better Schools

Variable	Initial SS	ΔPE	$\Delta PE+r$	$\Delta PE+r, w(s < co)$	$\Delta PE+r, w(s < co), w(co)$	ΔGE
$\Phi(j_a, s = co)$	31.93%	10.04	9.64	9.39	5.48	5.23
$\Phi(j_a, s = cod)$	28.61%	3.64	2.98	2.83	4.18	3.85
$\Phi(j_a, s = hs)$	31.01%	-10.88	-9.84	-9.45	-7.07	-6.54
$\Phi(j_a, s = hsd)$	8.45%	-2.79	-2.79	-2.78	-2.59	-2.54
HK	1.00	16.41	16.45	16.37	14.98	14.64
L	8.85	11.34	10.81	10.77	8.33	7.57
Hours	0.28	3.77	3.44	3.69	3.36	2.36
C	7.70	11.59	13.86	14.19	10.87	8.74
K	12.55	-9.62	2.92	3.68	-1.22	3.42
B	3.38	89.23	89.34	89.34	89.34	58.54
Revenues	2.54	13.08	17.69	18.35	10.62	12.54
Y	13.22	4.93	9.65	10.20	5.24	6.31
r (annual)	3.14%	0.00	0.22	0.22	0.22	0.22
w	0.74	0.00	0.00	0.00	-1.34	-1.34
$\frac{w^c}{w^n}$	75.55%	0.00	0.00	0.00	-8.57	-8.57
w^n	0.97	0.00	0.00	1.01	1.01	1.01
w^c	1.70	0.00	0.00	0.00	-3.92	-3.92
τ	0.22	-8.63	-8.63	-8.63	-8.63	-3.24
τ^p	12.40%	-0.43	-0.43	-0.43	-0.43	-0.16
$\frac{T(AE_0)}{Y}$	0.19	-2.02	-2.02	-2.02	-2.02	-0.76
$\frac{AE_0}{Lab. Inc. Tax Rev}$	11.34%	0.98	0.34	-0.04	-0.21	0.23
CEV NB	0.00%	19.26	22.42	23.05	18.27	14.68
CEV alive	0.00%	5.58	6.40	6.45	5.70	4.34
LSRA	0.00%	13.74	15.89	16.74	13.20	10.13

Notes: The table summarizes long-run changes (induced by policy transitions) in the main aggregate variables, general equilibrium prices and taxes, and welfare. Changes for baseline variables initially stated in percentages are expressed in percentage points (%p), while changes for baseline variables initially in levels are shown as percentages (%).

GE refers to the full general equilibrium version of the model where wages and interest rate are endogenous as well as the government budget constraints are balanced. The PE version refers to a life cycle model with balanced government budgets, with aggregate physical capital being computed as: $K_t = A_t - B_t$, where A_t are total household assets, and B_t is debt stock (which is endogenous and results from re-balancing the intertemporal government budget constraint).

PE+ r refers to the PE version where the interest rate path from the GE version is exogenously imposed - without any adjustments of other outer loop variables. Therefore, the government budget constraints do not have to hold, and therefore the debt values (as well as the implied physical capital $K_t = A_t - B_t$ and thus also output are not shown, and marked as n/a.

PE+ $r, w(s < co), w(co)$ refers to the PE version where the interest rate and wages paths from the GE version are exogenously imposed - without any adjustments of other outer loop variables.

Table 13: Aggregates, Prices, Taxes and Welfare: Optimal Mix

Variable	Initial SS	Δ PE	Δ PE+ r	Δ PE+ $r, w(s < co)$	Δ PE+ $r, w(s < co), w(co)$	Δ GE
$\Phi(j_a, s = co)$	31.93%	14.11	14.07	13.88	7.88	7.25
$\Phi(j_a, s = cod)$	28.61%	10.53	10.44	10.28	13.20	13.20
$\Phi(j_a, s = hs)$	31.01%	-22.79	-22.63	-22.30	-19.46	-18.95
$\Phi(j_a, s = hsd)$	8.45%	-1.85	-1.87	-1.86	-1.62	-1.51
HK	1.00	9.84	9.95	9.92	8.35	7.69
L	8.85	12.99	12.91	12.87	9.67	8.55
Hours	0.28	3.57	3.48	3.65	3.63	2.29
C	7.70	14.50	16.96	17.12	13.11	10.50
K	12.55	-9.00	3.23	3.71	-2.00	4.03
B	3.38	91.72	91.76	91.76	91.76	57.15
Revenues	2.54	13.15	18.00	18.32	9.59	12.12
Y	13.22	6.42	11.27	11.57	5.91	7.17
r (annual)	3.14%	0.00	0.23	0.23	0.23	0.23
w	0.74	0.00	0.00	0.00	-1.45	-1.45
$\frac{w^c}{w^n}$	75.55%	0.00	0.00	0.00	-8.54	-8.54
w^n	0.97	0.00	0.00	0.93	0.93	0.93
w^c	1.70	0.00	0.00	0.00	-3.97	-3.97
τ	0.22	-12.48	-12.48	-12.48	-12.48	-5.73
τ^p	12.40%	-0.24	-0.24	-0.24	-0.24	0.04
$\frac{T(AE_0)}{AE_0}$	0.19	-2.92	-2.92	-2.92	-2.92	-1.34
$\frac{\text{Lab. Inc. Tax Rev}}{Y}$	11.34	0.84	0.16	-0.16	-0.47	0.21
CEV NB	0.00%	21.67	24.84	25.18	20.27	15.48
CEV alive	0.00%	7.78	8.59	8.78	7.96	5.84
LSRA	0.00%	18.01	19.29	20.06	15.69	11.68

Notes: The table summarizes long-run changes (induced by policy transitions) in the main aggregate variables, general equilibrium prices and taxes, and welfare. Changes for baseline variables initially stated in percentages are expressed in percentage points (%p), while changes for baseline variables initially in levels are shown as percentages (%).

GE refers to the full general equilibrium version of the model where wages and interest rate are endogenous as well as the government budget constraints are balanced. The PE version refers to a life cycle model with balanced government budgets, with aggregate physical capital being computed as: $K_t = A_t - B_t$, where A_t are total household assets, and B_t is debt stock (which is endogenous and results from re-balancing the intertemporal government budget constraint).

PE+ r refers to the PE version where the interest rate path from the GE version is exogenously imposed - without any adjustments of other outer-loop variables. Therefore, the government budget constraints do not have to hold, and therefore the debt values (as well as the implied physical capital $K_t = A_t - B_t$ and thus also output are not shown, and marked as n/a.

PE+ $r, w(s < co), w(co)$ refers to the PE version where the interest rate and wages paths from the GE version are exogenously imposed - without any adjustments of other outer-loop variables.

A.3 Intergenerational Persistence of Education: Married Parents

Table 14 shows the change in the intergenerational education state transition matrix for children with married parents.⁴⁷ It shows the same qualitative pattern as for children with single parents that we report in the main text. Finally, it displays the additional general equilibrium decomposition for the optimal mixed reform referenced in the main text.

Table 14: Intergenerational Education Transition Matrix: Married Parents

Increased School Funding				
	$s = hsd$	$s = hs$	$s = cod$	$s = co$
$s^p = hsd, q = cpl$	-0.03	-0.05	0.05	0.03
$s^p = hs, q = cpl$	-0.03	0.00	0.03	-0.01
$s^p = cod, q = cpl$	-0.02	-0.01	0.05	-0.02
$s^p = co, q = cpl$	-0.02	-0.01	-0.02	0.04
Free College				
	$s = hsd$	$s = hs$	$s = cod$	$s = co$
$s^p = hsd, q = cpl$	0.00	-0.31	0.24	0.07
$s^p = hs, q = cpl$	0.00	-0.26	0.22	0.03
$s^p = cod, q = cpl$	-0.01	-0.27	0.26	0.02
$s^p = co, q = cpl$	0.00	-0.01	0.00	0.01

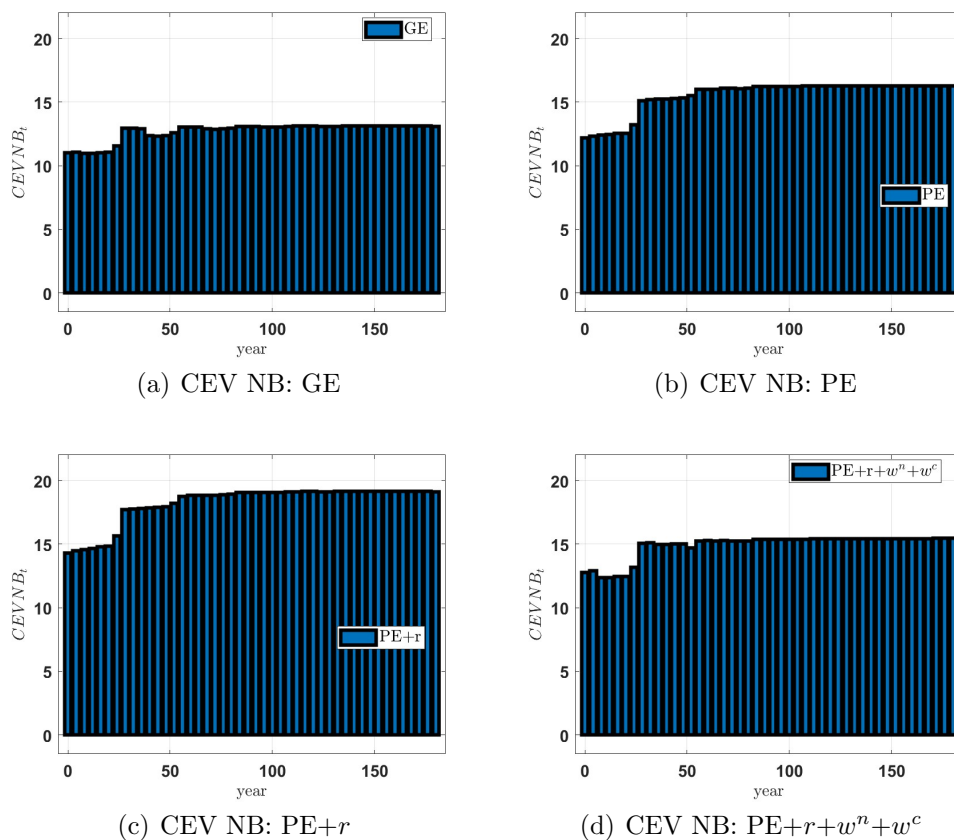
Notes: Changes in intergenerational education mobility: rows show parental background, columns show conditional child education shares. Table entries show absolute changes in conditional child education shares relative to the benchmark economy.

⁴⁷The education level of parental households is determined by the highest educational degree obtained by either of the two parents.

A.4 Partial vs. General Equilibrium: Additional Results

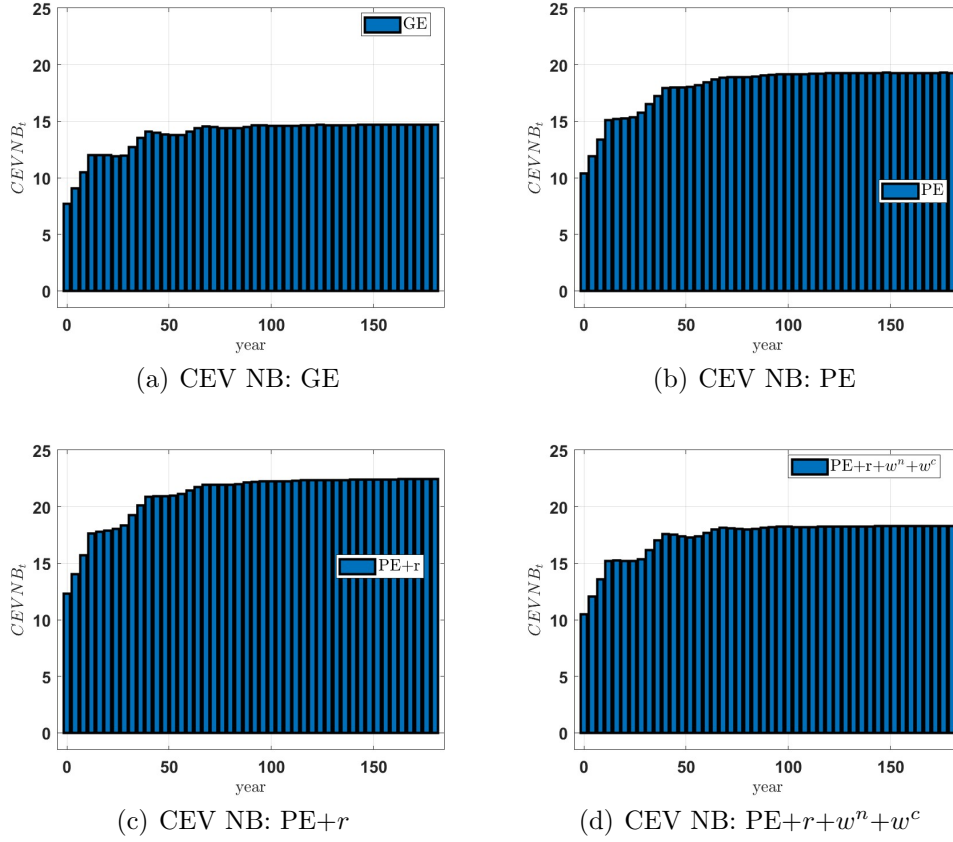
In this section we show the welfare consequences of both reforms in partial equilibrium and in general equilibrium. We also display the intergenerational education transition matrix for children with single parents in partial equilibrium for the “better schools” reform, since it shows the most marked difference to the general equilibrium results in the main text.

Figure 14: Free College Reform, Welfare Gains of Newborns



Notes: Newborn CEV. Panel (a): general equilibrium (GE); Panel (b): partial equilibrium (PE); Panel (c): PE and the interest rate path from GE (PE+r); Panel (d): PE+r and the wage paths from GE (PE+r + $w^n + w^c$).

Figure 15: “Better Schools” Reform, Welfare Gains of Newborns



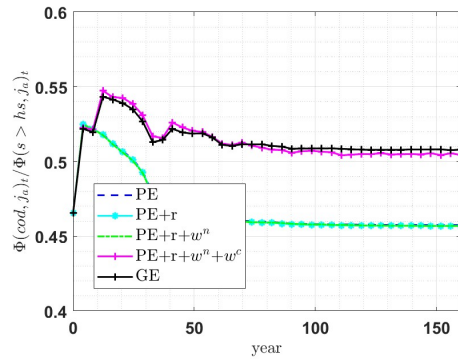
Notes: Newborn CEV. Panel (a): general equilibrium (GE); Panel (b): partial equilibrium (PE); Panel (c): PE and the interest rate path from GE (PE+r); Panel (d): PE+r and the wage paths from GE (PE+r + wⁿ + w^c).

Table 15: Intergenerational Education Transition Matrix: Single Parents in Partial Equilibrium, Change Relative to Baseline

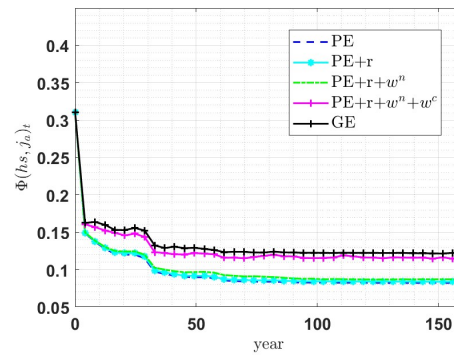
	“Better Schools”			
	$s = hsd$	$s = hs$	$s = cod$	$s = co$
$s^p = hsd, q = si$	-0.03	-0.12	0.06	0.09
$s^p = hs, q = si$	-0.03	-0.12	0.06	0.09
$s^p = cod, q = si$	-0.03	-0.13	0.06	0.10
$s^p = co, q = si$	-0.02	-0.01	-0.02	0.05

Notes: Changes in intergenerational education mobility: rows show parental background, columns show conditional child education shares. Table entries show absolute changes in conditional child education shares relative to the benchmark economy.

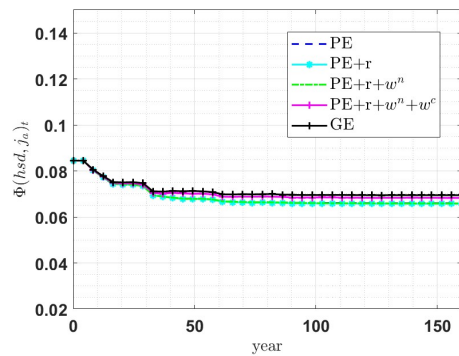
Figure 16: Mixed Reform, Education Shares



(a) College Dropout Share



(b) High School Share



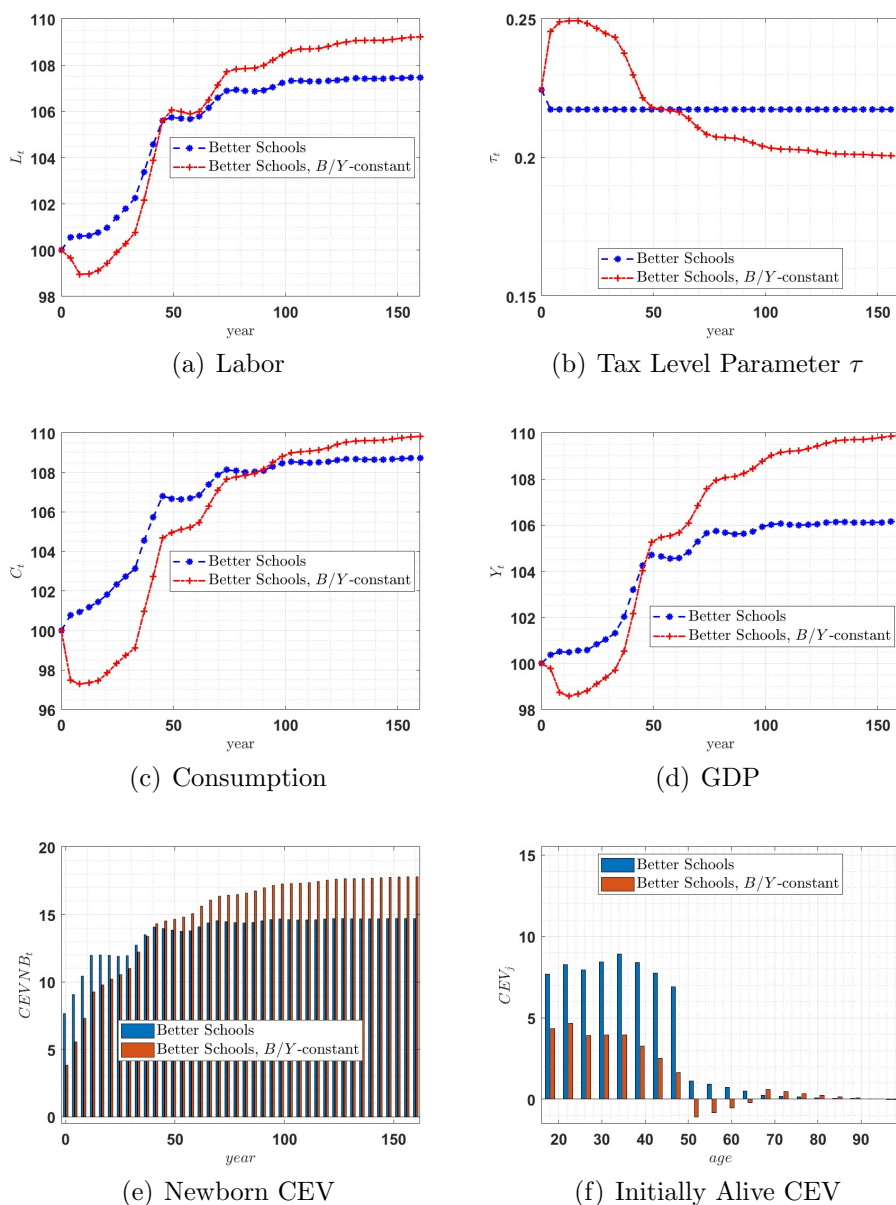
(c) High School Dropout Share

Notes: Panel (a): Share of a given “birth” cohort that becomes a college dropout; Panel (b): Share of a given “birth” cohort that becomes a high school completer; Panel (c): Share of a given “birth” cohort that becomes a high school dropout.

A.5 On The Importance of Government Debt

Figure 17 contrasts economic aggregates and welfare gains from the “Better Schools” reform with government debt adjustments (benchmark) and under the assumption of a constant debt to income ratio $\frac{B}{Y}$ which requires a period-by-period adjustment in the labor income tax rate.

Figure 17: Comparison between Debt vs. No Debt in the “Better Schools” Reform



Notes: The plots show transition paths of under the baseline specification (intertemporal government budget constraint), and with the specification where B/Y -ratio is being held constant at its baseline level. Panel (a): Aggregate efficiency units of labor; Panel (b): Tax function parameter τ ; Panel (c): Consumption; Panel (d): Output; Panel (e): Newborn CEV; Panel (f): Currently alive population CEV.

B Quantitative Model Appendix

B.1 Population Growth

With heterogeneous fertility rates by education, $\varsigma(s(wo))$, and an endogenous evolution of education shares along the transition, the total population growth is time varying and denoted by n_t . Recall that all parents are assumed to give birth to children at the same age j_f . Starting from retirement age j_r onward households face non-zero survival risk with ϕ_j denoting the survival probability from age j to age $j + 1$.

The population dynamics in every period evolve accordingly as

$$N_{t+1}(j_a) = \sum_s N_t(j_a + j_f, s, wo) \cdot \varsigma(s(wo)) \quad (28)$$

$$N_{t+1}(j + 1) = N_t(j) \cdot \phi_j \quad (29)$$

$$N_{t+1} = (1 + n_t)N_t \quad (30)$$

B.2 Human Capital Production Function: Normalization

The human capital production function has a multi-nested structure and is given by

$$h'(j) = \left(\kappa_j^h h^{1-\frac{1}{\sigma^h}} + (1 - \kappa_j^h) i(j)^{1-\frac{1}{\sigma^h}} \right)^{\frac{1}{1-\frac{1}{\sigma^h}}} \quad (31a)$$

$$i(j) = \bar{A} \left(\kappa_j^g \left(\frac{i^g}{\bar{i}^g} \right)^{1-\frac{1}{\sigma^g}} + (1 - \kappa_j^g) \left(\frac{i^p(j)}{\bar{i}^p} \right)^{1-\frac{1}{\sigma^g}} \right)^{\frac{1}{1-\frac{1}{\sigma^g}}} \quad (31b)$$

$$i^p(j) = \left(\kappa_j^m \left(\frac{i^m(j)}{\bar{i}^{m,d}} \right)^{1-\frac{1}{\sigma^m}} + (1 - \kappa_j^m) \left(\frac{i^t(j)}{\bar{i}^{t,d}} \right)^{1-\frac{1}{\sigma^m}} \right)^{\frac{1}{1-\frac{1}{\sigma^m}}} . \quad (31c)$$

The three inputs —public input i^g and parental money and time inputs $i^t(j)$ and $i^m(j)$ — are normalized throughout by their unconditional means (across all child ages/grades) to account for different units.

We can rewrite the second and third nests as

$$i(j) = \bar{A} \left(\Gamma^g \left(\frac{\kappa_j^g}{\Gamma^g (\bar{i}^g)^{1-\frac{1}{\sigma^g}}} (i^g)^{1-\frac{1}{\sigma^g}} + \frac{(1 - \kappa_j^g)}{\Gamma^g (\bar{i}^p)^{1-\frac{1}{\sigma^g}}} (i^p(j))^{1-\frac{1}{\sigma^g}} \right) \right)^{\frac{1}{1-\frac{1}{\sigma^g}}} \quad (32)$$

$$i^p(j) = \left(\Gamma \left(\frac{\kappa_j^m}{\Gamma (\bar{i}^{m,d})^{1-\frac{1}{\sigma^m}}} (i^m(j))^{1-\frac{1}{\sigma^m}} + \frac{(1 - \kappa_j^m)}{\Gamma (\bar{i}^{t,d})^{1-\frac{1}{\sigma^m}}} (i^t(j))^{1-\frac{1}{\sigma^m}} \right) \right)^{\frac{1}{1-\frac{1}{\sigma^m}}} , \quad (33)$$

respectively, for $\Gamma^g(\kappa_j^g, \bar{i}^g, \bar{i}^p, \sigma^g) \equiv \frac{\kappa_j^g}{(\bar{i}^g)^\rho} + \frac{(1-\kappa_j^g)}{(\bar{i}^p)^\rho}$ and $\Gamma(\kappa_j^m, \bar{i}^{m,d}, \bar{i}^{t,d}, \sigma^m) \equiv \frac{\kappa_j^m}{(\bar{i}^{m,d})^\rho} + \frac{(1-\kappa_j^m)}{(\bar{i}^{t,d})^\rho}$ where, in general, $\Gamma^g(\cdot) \neq 1$ and $\Gamma(\cdot) \neq 1$.

We can rewrite eq. (34) and eq. (35) further as

$$i(j) = \tilde{A}\tilde{\Gamma}^g \left(\tilde{\kappa}_j^g (i^g)^{1-\frac{1}{\sigma^g}} + (1 - \tilde{\kappa}_j^g) (i^p(j))^{1-\frac{1}{\sigma^g}} \right)^{\frac{1}{1-\frac{1}{\sigma^g}}} \quad (34)$$

$$i^p(j) = \tilde{\Gamma} \left(\tilde{\kappa}_j^m (i^m(j))^{1-\frac{1}{\sigma^m}} + (1 - \tilde{\kappa}_j^m) (i^t(j))^{1-\frac{1}{\sigma^m}} \right)^{\frac{1}{1-\frac{1}{\sigma^m}}}, \quad (35)$$

where $\tilde{\Gamma}^g = (\Gamma^g)^{1-\frac{1}{\sigma^g}}$ and $\tilde{\Gamma} = \Gamma^{1-\frac{1}{\sigma^m}}$. The normalized share parameters are accordingly defined as $\tilde{\kappa}_j^g = \frac{\kappa_j^g}{\Gamma^g(\bar{i}^g)^{1-\frac{1}{\sigma^g}}}$ and $\tilde{\kappa}_j^m = \frac{\kappa_j^m}{\Gamma(\bar{i}^{m,d})^{1-\frac{1}{\sigma^m}}}$.

B.3 Optimal Parental Human Capital Investments

Optimal Investment in Human Capital The intratemporal optimality condition for time with children is

$$\begin{aligned} \varsigma(si, s)(v^t)'(\varsigma(si, s) \cdot i^t) &= \lambda_i \frac{\partial i(i^m, i^t, i^g)}{\partial i^t} - \lambda_t \cdot \varsigma(si, s) = \lambda_h \frac{\partial g(h, i)}{\partial i} \frac{\partial i(i^m, i^t, i^g)}{\partial i^t} - \lambda_t \cdot \varsigma(si, s) \\ &= \beta \mathbf{E}_{\eta'|\eta} V_h(x'; a', h') \frac{\partial g(h, i)}{\partial i} \frac{\partial i(i^m, i^t, i^g)}{\partial i^t} \end{aligned}$$

The left hand side is the marginal cost of spending an additional time unit with children, the right hand side gives the discounted benefits, per child, of one additional unit of the final good being spent on education, where $\frac{\partial g(h, i)}{\partial i} \frac{\partial i(i^m, i^t, i^g)}{\partial i^m}$ is the marginal benefit of that spending on human capital tomorrow, and $\mathbf{E}_{\eta'|\eta} V_h(x'; a', h')$ is the expected marginal benefit of a smarter child.

The intertemporal optimality condition for resource investment in children is

$$\begin{aligned} \lambda_b \varsigma(si, s) &= \lambda_i \frac{\partial i(i^m, i^t, i^g)}{\partial i^m} = \lambda_h \frac{\partial g(h, i)}{\partial i} \frac{\partial i(i^m, i^t, i^g)}{\partial i^t} \\ \Leftrightarrow (\beta \mathbf{E}_{\eta'|\eta} V_a(x'; a', h') + \lambda_a) \varsigma(si, s) &= \beta \mathbf{E}_{\eta'|\eta} V_h(x'; a', h') \frac{\partial g(h, i)}{\partial i} \frac{\partial i(i^m, i^t, i^g)}{\partial i^m} \\ \Leftrightarrow \frac{u' \left(\frac{c}{1+\zeta_c \varsigma(si, s)} \right) \varsigma(si, s)}{1 + \zeta_c \varsigma(si, s) \quad 1 + \tau_c} &= \beta \mathbf{E}_{\eta'|\eta} V_h(x'; a', h') \frac{\partial g(h, i)}{\partial i} \frac{\partial i(i^m, i^t, i^g)}{\partial i^m} \end{aligned}$$

The left hand side is the marginal cost of reducing spending on consumption goods by one unit, and the right hand side again gives the discounted per child benefits.

Optimal Allocation between Time and Money Taking the ratio between the first order conditions for time and money inputs yields

$$\begin{aligned} \frac{(v^t)'(\zeta(si, s) \cdot i^t)}{\beta \mathbf{E}_{\eta'|\eta} V_a(x'; a', h') + \lambda_a} &= \frac{\frac{\partial i^p(j, i^m, i^t)}{\partial i^t}}{\frac{\partial i^p(j, i^m, i^t)}{\partial i^m}} \\ \Leftrightarrow (1 + \tau_c) \frac{(v^t)'(\zeta(si, s) \cdot i^t)}{\frac{u'(\frac{c}{1 + \zeta_c \zeta(si, s)})}{1 + \zeta_c \zeta(si, s)}} &= \frac{\frac{\partial i^p(j, i^m, i^t)}{\partial i^t}}{\frac{\partial i^p(j, i^m, i^t)}{\partial i^m}} \end{aligned} \quad (36)$$

This equation simply states that the marginal rate of substitution between time and consumption times its relative price (the consumption tax rate) equals the marginal rate of transformation in the production of inputs for human capital production.

Using the functional forms for per-period utility and human capital production function, the relation between optimal resource and time investments can be written as

$$\begin{aligned} \frac{i^m}{i^t} &= \left(\frac{1}{\chi} \kappa (\zeta(si, s) \cdot i^t)^{\frac{1}{\psi}} c(1 + \tau^c) \right)^{\sigma^m} \\ \Leftrightarrow \frac{i^m}{(i^t)^{1 + \frac{\sigma^m}{\psi}}} &= \left(\frac{1}{\chi} \kappa (\zeta(si, s))^{\frac{1}{\psi}} c(1 + \tau^c) \right)^{\sigma^m} \end{aligned} \quad (37)$$

B.4 Disentangling Efficiency and Redistribution when Measuring Welfare: The LSRA

To disentangle welfare benefits stemming from efficiency gains from those driven by redistribution, we use a wealth-based welfare criterion that follows the spirit of the lump-sum redistribution authority originally described in [Auerbach and Kotlikoff \(1987\)](#) and applied to a model with intragenerational heterogeneity in [Nishiyama and Smetters \(2005\)](#). Technically, our wealth-based measure is computed as follows. As a first step, individual-specific transfers are computed that would make the currently living households, including the period 0 newborns, indifferent between the status quo and the reform scenario. Denote those transfers by $\Psi_0(j, \cdot)$. These transfers are then aggregated up using the initial steady-state cross-sectional distribution and population shares. As a second step, for each newborn cohort in the transition and in the final steady state an ex-ante uniform transfer is computed that would make them indifferent between being born into the initial steady state or a given period of the transition (or a final steady state). We denote those transfers by Ψ_t . Finally, a present discounted value (based on the market discount rate) of these ex-ante transfers is computed and added up with the aggregate transfer to the initially

alive population. Thus, the total transfer is given by:

$$W = \int \Psi_0(\cdot) d\Phi_0(\cdot) + \sum_{t=1}^{\infty} \prod_{s=1}^t \left(\frac{1}{1 + r_s^{fc}} \right) \Psi_t \quad (38)$$

where we discount using the sequence of equilibrium interest rates of the free college reform, $\{r_t^{fc}\}_{t=1}^{\infty}$.

For expositional purposes, we follow the approach in [Kindermann and Krueger \(2014\)](#) and express the resulting aggregate monetary transfer as an annuity C paying a constant consumption flow in every transition period and in the final steady state:

$$C \cdot \sum_{t=0}^{\infty} \prod_{s=1}^t \left(\frac{1}{1 + r_s^{fc}} \right) = -W, \quad (39)$$

for $\prod_{s=1}^0 \left(\frac{1}{1 + r_s^{fc}} \right) = 1$.

Finally, we express the computed annuity value as percent of initial aggregate consumption:

$$\text{LSRA} = 100 \cdot \frac{C}{C_0} \quad (40)$$

C Model Calibration Appendix

C.1 Child Human Capital Production Function

Figure 18: Age Profiles of κ_j^h and κ_j^m

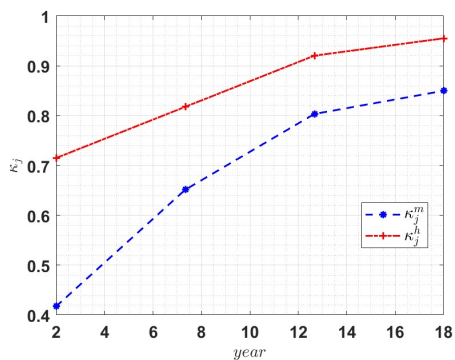
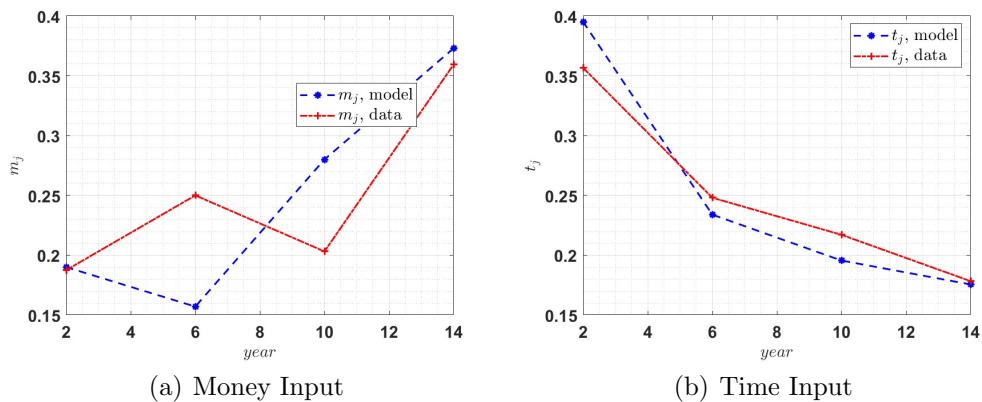


Figure 19: Age Profiles of Money and Time Parental Inputs: Model and Data



Notes: All variables are normalized by their respective means (over all age groups) which are directly targeted in the calibration.

C.2 Calibration: Summary Tables

Table 16: First Stage Calibration Parameters

Parameter	Interpretation	Value	Source (data/lit)
<i>Population</i>			
$j = 0$	Age at economic birth (age 2)	0	
j_a	Age at beginning of econ life (age 18)	4	
j_c	Age at finishing college (age 22)	5	
j_{f-1}	Marriage Age (age 26)	6	
j_f	Fertility Age (age 30)	7	
j_r	Retirement Age (age 66)	16	
J	Max. Lifetime (age bin 98-101)	24	
$\{\phi_j\}$	Survival Probabilities	see main text	Life Tables SSA
n	Population Growth Rate	1%	
$\frac{\zeta(s < co)}{\zeta(s = co)}$	Fertility Education Gradient	1.15	PSID 2011-2019
$\pi^m(s)$	Marriage probability	[0.51 0.51 0.51 0.51]	PSID 2011 - 2019
<i>Preferences</i>			
σ	Relative risk aversion parameter	1	
ψ	Frisch elasticity	0.6	
<i>Technology</i>			
μ	Technological growth rate	1%	
α	Capital share	33.3%	
δ	Depreciation rate	5%	
ρ	Subst. Elasticity $\frac{1}{1-\rho}$	3.3	
<i>Labor Productivity</i>			
$\{\epsilon(s, g, j)\}$	Age Profile	see main text	PSID 1968-2012
$[\eta_l, \eta_h]$	States of Markov process	[0.6725, 1.3275]	PSID 1968-2012
π_{hl}	Transition probability of Markov process	0.1765	PSID 1968-2012
<i>Ability/Human Capital and Education</i>			
ι	College tuition costs (annual, net of grants and subsidies)	15,500\$	NCES (average 2000-2019)
$\underline{a}(j \in [j_a], co)$	College borrowing limit	45,590\$	Krueger and Ludwig (2016)
σ^h	Elast of subst b/w human capital and CES inv. aggr.	1	Cunha et al. (2010)
σ^g	Elast of subst b/w public inv. and CES aggr. of private inv.	2.43	Kotera and Seshadri (2017)
σ^m	Elast of subst b/w monetary and time inv.	1	Lee and Seshadri (2019)
$\Phi(h(j=0) s_p)$	Innate ability dist-n of children by parental education	see main text	PSID CDS I
\underline{h}_0	Normalization parameter of initial dist-n of initial ability	0.1248	PSID CDS I-III
<i>Baseline Government policy</i>			
ϑ	Public subsidy of college education	38.8%	Krueger and Ludwig (2016)
ϑ^{pr}	Private subsidy of college education	16.6%	Krueger and Ludwig (2016)
i_j^g	Public high school education spending	$\approx 14,000$ \$	NCES (2000-2018)
τ_c	Consumption Tax Rate	5.0%	legislation
τ_k	Capital Income Tax Rate	36%	Trabandt and Uhlig (2011)
ξ	Labor Income Tax Progressivity	0.18	Heathcote et al. (2017)
ω	Income of non-working households	20.2% of average earnings	CEX 2001-2007 (see Holter et al. (2023))
τ^p	Soc Sec Payroll Tax	12.4%	legislation
G/Y	Government consumption to GDP	13.8%	current value

Notes: First stage parameters calibrated exogenously by reference to other studies and data.

Table 17: Second Stage Calibration Parameters

Parameter	Interpretation	Value	Data Moment & Source	Moment Value
<i>Preferences</i>				
β	Time discount rate	0.9949	Annual interest rate	3.00%
ν	Altruism parameter	0.5944	Average IVT transfer per child, 2013 Rosters and Transfers Module of PSID	\$61,200
ϕ	Weight on hours disutility	17.9718	Average hours per household, conditional on working	1/3
F	Fixed cost of working positive hours	0.2000	Employment rate age 25-54, U.S. Bureau of Labor Statistics	83%
<i>Labor Productivity</i>				
$\rho_0(s)$	Normalization parameter	[1.01, 1.01... ...0.98, 0.93]	Normalization $\mathbb{E}\gamma(s, h) = 1$	1.0
<i>Human Capital and Education</i>				
κ	Weight on disutility from time inv.	0.3473	Average time inv., CDS PSID I-III	23.77
κ_j^h	Share of human capital (outermost nest)	cf. Fig. 18	Slope of time inv. and i^g -elasticity, CDS PSID I-III, and Jackson and Mackevicius (2023)	cf. Fig. 19
κ_j^m	Share of monetary input (innermost nest)	cf. Fig. 18	Average monetary inv. and slope, CDS PSID I-III	cf. Fig. 19
$\kappa_j^g, j > 0$	Share of government input for ages 6 and older	0.8700	Test score disparity b/w "top" and "bottom" children at age 17-19, CDS PSID I-III	1.25
κ_0^g	Share of government input for age bin 2-6	0.7647	Average time inv. age bin 2-6, CDS PSID I-III	32.40
\bar{A}	Investment scale parameter	1.1989	Normalization of average HK at age j_a	1.00
λ^{hs}	Slope parameter of high school graduation probability function	2.6836	Share of high school dropouts, PSID 2011-2019	8%
λ^c	Slope parameter of college completion probability function	0.6881	Share of college dropouts, PSID 2011-2019	29%
$\varrho(s^p < co)$	Psychological (utility) costs $s = co, s^p < co$	3.3272	Share of college graduates, PSID 2011-2019	32%
$\varrho(s^p = co)$	Psychological (utility) costs $s = co, s^p = co$	0.9096	Conditional fraction of group $s > hs$ with $s^p = co$, PSID 2011-2019	92%
<i>Government policy</i>				
τ	Level parameter of HSV tax function	0.2246	B/Y -ratio	100%
ρ^p	Pension replacement rate	0.0883	Balance per period soc. sec. budget	

Notes: Second stage parameters calibrated endogenously by targeting selected data moments.

D The Simple Model

The purpose of the simple model is to illustrate the economic mechanisms through which two policy instruments, early childhood public education expenditures i^g and higher education subsidies ϑ , affect college participation decisions, earnings and welfare and how the two instruments interact. While there are no built-in complementarities through an assumption of a human capital production function that extends to the college period as in [Caucutt and Lochner \(2020\)](#), we highlight different forces of complementarities of the two policy instruments. The key force is that an education subsidy increases college participation and investing more into schools increases human capital thereby increasing wages of the better educated college graduates, respectively increasing the probability of students to complete college, thus achieving higher overall utility levels.

D.1 Setup

We assume a static model, where agents make a college participation decision $s \in \{hs, co\}$ — for *high school* and *college*— and consume resources c . Agents are born with productivity h_0 to produce human capital which is strictly positive, $h_0 > 0$, and distributed uniformly on the 0-1 interval $h_0 \sim (0, 1]$. The only other input into human capital formation is government investment i^g so that acquired human capital is

$$h = h_0 f(i^g) \tag{41}$$

where $f(i^g)$ is an at least twice continuously differentiable function with $f'(i^g) > 0$ and $f''(i^g) < 0$ for all $i^g > 0$.

Agents that do not attend college earn wage income $w(s = hs, h)$ with $w'(s = hs, h) > 0$ and $\lim_{h \rightarrow 0} w(s = hs, h) = 0$. Agents that do attend college earn wages $w(s = co, h) > w(s = hs, h) > 0$ for all $h > 0$ with $w'(s = co, h) > w'(s = hs, h)$ so that the college wage premium $\Delta w(h) \equiv \frac{w(s=co,h)}{w(s=hs,h)}$ is increasing in h . Consistent with our empirical estimates on which we base the calibration of the quantitative model, cf. [Section 4](#), we further assume that $w''(s, h) > 0$ for $s \in \{hs, co\}$.

College attendance also comes at a monetary cost of ι that is subsidized at rate ϑ so that college costs net of subsidies are $\iota(1 - \vartheta)$. There are additional psychological costs of attending college, which here are modeled as a monetary equivalent, $\varrho > 0$. These costs ensure that also in case of complete college subsidization, $\vartheta = 1$, aggregate college participation is bounded away from 1. Consumption, in this static model for post education decision state variables s, h , is

therefore given by

$$c(s, h) \leq (1 - \mathbf{1}_{s=co})w(s = hs, h) + \mathbf{1}_{s=co}w(s = co, h) - \mathbf{1}_{s=co}(\iota(1 - \vartheta) + \varrho). \quad (42)$$

Since in this simple model, we are not interested in evaluating welfare consequences of government insurance against h_0 -risk, we further assume a linear utility function

$$u(c) = c$$

and thus the weak inequality in (42) is replaced by a strict equality.

With the linear utility assumption, an alternative interpretation of the model is as follows. Rewrite $\Delta w(h)$ as $\Delta w(h) = 1 + \pi(h)\tilde{\Delta}w(h)$ so that college wages are $w(s = co, h) = w(s = hs, h) \left(1 + \pi(h)\tilde{\Delta}w(h)\right)$. $\pi(h)$ is a college completion probability with $\pi(h) \geq 0$ and $\pi'(h) \geq 0$, for all $h > 0$. Upon completion, agents earn the proportional premium $\tilde{\Delta}w(h) > 0$, for all h , $(\tilde{\Delta}w)'(h) \geq 0$ (where the inequality in either one of the two derivatives, $\pi'(h)$ or $(\tilde{\Delta}w)'(h)$, would have to be strict). In case of non-completion, agents earn non-college wages $w(s = hs, h)$.

We conclude the model description by assuming a government that evaluates policy choices i^g, ϑ by use of a social welfare function

$$W = \int u(c(h_0))dh_0. \quad (43)$$

D.2 Analysis

Agents choose to attend college iff⁴⁸

$$\begin{aligned} & w(s = co, h) - (\iota(1 - \vartheta) + \varrho) > w(s = hs, h) \\ \Leftrightarrow & \Delta w(h) > 1 + \frac{\iota(1 - \vartheta) + \varrho}{w(s = hs, h)}. \end{aligned} \quad (44)$$

Note that $\Delta w(h)$ is monotonically increasing in h and $w(s = hs, h)$ is monotonically increasing in h and, since in addition $\lim_{h \rightarrow 0} w(s = hs, h) = 0$, the LHS and the RHS cross at some $\bar{h} > 0$. This gives rise to a threshold level \bar{h} such that households with $h > \bar{h}(\vartheta)$ attend college and households with $h \leq \bar{h}(\vartheta)$ do not. Further, because ϑ decreases the RHS in (44), $\frac{\partial \bar{h}(\vartheta)}{\partial \vartheta} < 0$. By (41), this threshold property on h translates into a threshold for h_0 , or, likewise, for given h_0 ,

⁴⁸We accordingly break indifference by assuming that agents only attend college if the inequality in (44) is strict.

into a threshold for i^g .

$$\bar{h}_0(i^g, \vartheta) \equiv \frac{\bar{h}(\vartheta)}{f(i^g)}$$

and thus

$$\frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial \vartheta} = \frac{\partial \bar{h}(\vartheta)}{\partial \vartheta} \frac{1}{f(i^g)} < 0 \quad \text{and} \quad \frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial i^g} = -\bar{h}(\vartheta) \frac{1}{f(i^g)^2} f'(i^g) < 0.$$

Notice that \bar{h}_0 through its dependency on $\bar{h}(\vartheta)$ is also a function of the model parameters ι, ϱ . Throughout we assume a joint parametrization of $i^g, \vartheta; \iota, \varrho$ such that $\bar{h}_0 \in (0, 1)$. Then $\Psi(s = hs) = \bar{h}_0(i^g, \vartheta)$ is the non-college fraction of agents in the economy and $\Psi(s = co) = 1 - \bar{h}_0(i^g, \vartheta)$ is the fraction in college which increases in i^g and ϑ . Furthermore, note that

$$\frac{\partial^2 \bar{h}_0(i^g, \vartheta)}{\partial \vartheta \partial i^g} = \frac{\partial^2 \bar{h}_0(i^g, \vartheta)}{\partial i^g \partial \vartheta} = \frac{1}{\bar{h}_0(i^g, \vartheta)} \frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial i^g} \frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial \vartheta} = -\frac{\partial \bar{h}(\vartheta)}{\partial \vartheta} \frac{1}{f(i^g)^2} f'(i^g) > 0, \quad (45)$$

and thus the two instruments i^g and ϑ are substitutes in affecting college choice.

Having characterized the threshold $\bar{h}_0(i^g, \vartheta)$ and using (42) in (43) we can rewrite the social welfare function as

$$W = \underbrace{\int_0^{\bar{h}_0(i^g, \vartheta)} w(h(h_0), s = hs) dh_0}_{=A} + \underbrace{\int_{\bar{h}_0(i^g, \vartheta)}^1 w(h(h_0), s = co) dh_0}_{=B} - \underbrace{(\iota(1 - \vartheta) + \varrho)(1 - \bar{h}_0(i^g, \vartheta))}_{=C}. \quad (46)$$

To highlight the economic mechanisms of simple reforms to i^g and ϑ we now evaluate the derivatives of A, B, C in these policy instruments.

D.2.1 School Financing Reform

We note that

$$\frac{\partial A}{\partial i^g} = \underbrace{w(h(\bar{h}_0), s = hs) w'(h(\bar{h}_0), s = hs) f(i^g) \frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial i^g}}_{=(\frac{\partial A}{\partial i^g})_1 < 0} + \underbrace{\int_0^{\bar{h}_0(i^g, \vartheta)} w'(h(h_0), s = hs) f(i^g) dh_0}_{=(\frac{\partial A}{\partial i^g})_2 > 0}$$

and thus a school financing reform lifts more children into college, $(\frac{\partial A}{\partial i^g})_1 < 0$, and increases wages of non-college agents, $(\frac{\partial B}{\partial i^g})_2 > 0$. Likewise,

$$\frac{\partial B}{\partial i^g} = \underbrace{-w(h(\bar{h}_0), s = co)w'(h(\bar{h}_0), s = co)f(i^g)\frac{\partial \bar{h}_0}{\partial i^g}}_{=(\frac{\partial B}{\partial i^g})_1 > 0} + \underbrace{\int_0^{\bar{h}_0} w'(h(h_0), s = co)f(i^g)dh_0}_{=(\frac{\partial B}{\partial i^g})_2 > 0}$$

since a school financing reform lifts more children into college, $(\frac{\partial B}{\partial i^g})_1 > 0$, and increases wages of college youngsters, $(\frac{\partial B}{\partial i^g})_2 > 0$. Finally,

$$\frac{\partial C}{\partial i^g} = (\iota(1 - \vartheta) + \varrho) \frac{\partial \bar{h}_0}{\partial i^g} < 0$$

because an increase in the number of college youngsters increases the aggregate monetary college expenditures.

D.2.2 College Subsidy Reform

We note that

$$\begin{aligned} \frac{\partial A}{\partial \vartheta} &= w(h(\bar{h}_0), s = hs)w'(h(\bar{h}_0), s = hs)f(i^g)\frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial \vartheta} < 0 \\ \frac{\partial B}{\partial \vartheta} &= -w(h(\bar{h}_0), s = co)w'(h(\bar{h}_0), s = co)f(i^g)\frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial \vartheta} > 0 \end{aligned}$$

because a college reform only affects the threshold $\bar{h}_0(i^g, \vartheta)$, as well as

$$\frac{\partial C}{\partial \vartheta} = \underbrace{(\iota(1 - \vartheta) + \varrho) \frac{\partial \bar{h}_0(i^g, \vartheta)}{\partial \vartheta}}_{=(\frac{\partial C}{\partial \vartheta})_1 < 0} + \underbrace{\iota(1 - \bar{h}_0)}_{=(\frac{\partial C}{\partial \vartheta})_2 > 0}$$

Term $(\frac{\partial C}{\partial \vartheta})_1 < 0$ reflects the additional college cost from drawing in more students into college, where $(\frac{\partial C}{\partial \vartheta})_2 > 0$ captures the decreasing costs of college for all students. If and only if this second welfare enhancing effect dominates the first, then $\frac{\partial C}{\partial \vartheta} > 0$.

D.2.3 Joint Reform

Let us first turn to the most important force of complementarity of the two policy instruments we want to point out with this analysis. We find that

$$\frac{\partial^2 B}{\partial i^g \partial \vartheta} = \frac{\partial^2 B}{\partial \vartheta \partial i^g} = \underbrace{\left(\frac{\partial^2 B}{\partial i^g \partial \vartheta} \right)_1}_{<0} \underbrace{-w(h(\bar{h}_0), s = co)w'(h(\bar{h}_0), s = co)f'(i^g) \frac{\partial \bar{h}_0}{\partial i^g}}_{=\left(\frac{\partial^2 B}{\partial i^g \partial \vartheta} \right)_2 >0}$$

where

$$\begin{aligned} \frac{\partial^2 B}{\partial i^g \partial \vartheta} = & \underbrace{-w'(h(\bar{h}_0), s = co)^2 f(i^g)^2 \frac{\partial \bar{h}_0}{\partial i^g} \frac{\partial \bar{h}_0}{\partial \vartheta}}_{<0} \underbrace{-w(h(\bar{h}_0), s = co)w''(h(\bar{h}_0), s = co)f(i^g)^2 \frac{\partial \bar{h}_0}{\partial i^g} \frac{\partial \bar{h}_0}{\partial \vartheta}}_{<0} \\ & \underbrace{-w(h(\bar{h}_0), s = co)w'(h(\bar{h}_0), s = co)f(i^g) \frac{\partial^2 \bar{h}_0}{\partial i^g \partial \vartheta}}_{<0} \underbrace{-w(h(\bar{h}_0), s = co)w'(h(\bar{h}_0), s = co)f'(i^g) \frac{\partial \bar{h}_0}{\partial i^g}}_{>0}, \end{aligned}$$

i.e., the school finance reform becomes less effective in drawing youngsters with higher wages into college if a college subsidy reform comes on top. This reflects the partial substitutability of the two policy instruments. On the other hand, term $\left(\frac{\partial^2 B}{\partial i^g \partial \vartheta} \right)_2 > 0$ displays their partial complementarity: As derived above, the school financing reform increases wages of college youngsters, $\left(\frac{\partial B}{\partial i^g} \right)_2 > 0$, and the college subsidy reform draws students with higher wages and thus higher aggregate productivity into college. An alternative interpretation of this finding is that increasing subsidies draws more students into college and increasing their human capital increases the probability of these students to successfully complete college.

With respect to the remaining terms, we obtain, first, that

$$\frac{\partial^2 A}{\partial i^g \partial \vartheta} = \frac{\partial^2 A}{\partial \vartheta \partial i^g} = \underbrace{\left(\frac{\partial^2 A}{\partial i^g \partial \vartheta} \right)_1}_{>0} \underbrace{+ w(h(\bar{h}_0), s = hs)w'(h(\bar{h}_0), s = hs)f'(i^g) \frac{\partial \bar{h}_0}{\partial \vartheta}}_{=\left(\frac{\partial^2 A}{\partial i^g \partial \vartheta} \right)_2 <0},$$

where

$$\begin{aligned} \frac{\partial^2 A}{\partial i^g \partial \vartheta} = & \underbrace{(w'(h(\bar{h}_0), s = hs))^2 f(i^g)^2 \frac{\partial \bar{h}_0}{\partial i^g} \frac{\partial \bar{h}_0}{\partial \vartheta}}_{>0} \underbrace{+ w(h(\bar{h}_0), s = hs)w''(h(\bar{h}_0), s = hs)f(i^g)^2 \frac{\partial \bar{h}_0}{\partial i^g} \frac{\partial \bar{h}_0}{\partial \vartheta}}_{>0} \\ & \underbrace{+ w(h(\bar{h}_0), s = hs)w'(h(\bar{h}_0), s = hs)f(i^g) \frac{\partial^2 \bar{h}_0}{\partial \vartheta \partial i^g}}_{>0} \underbrace{+ w(h(\bar{h}_0), s = hs)w'(h(\bar{h}_0), s = hs)f'(i^g) \frac{\partial \bar{h}_0}{\partial \vartheta}}_{<0} \end{aligned}$$

is a complementarity of the two policy instruments, because the effectiveness of the i^g -reform in drawing students into college is diminished if education subsidies come on top so that, relative to a pure i^g -reform, more youngsters with higher wages remain non-college students.

Second, we find that

$$\frac{\partial^2 C}{\partial i^g \partial \vartheta} = \frac{\partial^2 C}{\partial \vartheta \partial i^g} = \underbrace{(\iota(1 - \vartheta) + \varrho) \frac{\partial \bar{h}_0}{\partial \vartheta \partial i^g}}_{=\left(\frac{\partial^2 C}{\partial i^g \partial \vartheta}\right)_1 > 0} \underbrace{-\iota \frac{\partial \bar{h}_0}{\partial i^g}}_{=\left(\frac{\partial^2 C}{\partial i^g \partial \vartheta}\right)_2 > 0} > 0,$$

which shows an additional complementarity of the two policy instruments. If the education subsidy reform comes on top of the schooling reform, then relatively fewer students (relative to the pure schooling reform) are drawn into college who have to pay the tuition cost, $\left(\frac{\partial^2 C}{\partial i^g \partial \vartheta}\right)_1 > 0$, and the aggregate tuition cost decreases because of the increasing subsidies, $\left(\frac{\partial^2 C}{\partial i^g \partial \vartheta}\right)_2 > 0$.