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Long-term nexus of macroeconomic and financial fundamentals with cryptocurrencies

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Long-Term Nexus of Macroeconomic and Financial Fundamentals with Cryptocurrencies

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Long-Term Nexus of Macroeconomic and Financial Fundamentals with Cryptocurrencies

Panayiotis M. Pourpourides*

September 8, 2023

Abstract

In this empirical study I examine the influence of macroeconomic and financial fundamentals on cryptocurrency metrics over the long term. Through both parametric and non-parametric estimation methods, I establish that the relative value of the US dollar and the price of gold consistently exert significant impact on cryptocurrency metrics. Analyzing daily and monthly data reveals a robust statistical correlation, resulting in adverse effects on cryptocurrency prices, market capitalizations, and Bitcoin's hash rate. These findings along with distinct features of Bitcoin resonate with the concept of Bitcoin as a digital asset analogous to physical gold, assuming a role similar to a substitute for the latter. Comparatively, Bitcoin's hash rate demonstrates heightened market exposure when contrasted with its price counterpart. While the value of the US dollar exerts negative effects on both gold and Bitcoin, the latter's response is notably greater. Moreover, the relationships of gold and Bitcoin with indicators such as the federal funds rate and the S&P 500 exhibit divergent patterns. While the US dollar primarily exerts downward pressure on Bitcoin's price and the gold price primarily influences the hash rate, over time the significance of both factors, though dominant, gradually diminishes.

JEL Classification Codes: E44; G10; G12; G19.

Keywords: Bitcoin; Cryptocurrencies; Blockchain; Macroeconomic and Financial Fundamentals.

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1 Introduction

Decentralized digital currencies, known as cryptocurrencies, have revolutionized electronic payments and financial services by leveraging innovative technologies that ensure data permanence and challenge traditional centralized financial systems. These cryptocurrencies, characterized by their secure encryption algorithms, offer accessible and cost-effective alternatives to traditional financial intermediaries, governments, and central banks. Cryptocurrencies operate on distributed ledger technologies (DLTs) -e.g. blockchains- which maintain a chronological record of transactions in a decentralized and tamper-resistant manner. This research delves into the profound long-run interplay between macroeconomic and financial fundamentals and cryptocurrency metrics, focusing specifically on the influential factors impacting cryptocurrency prices, market caps (capitalizations) and Bitcoin (BTC)'s hash rate. The research reveals that the relative strength of the US dollar, as measured by the DXY index, and the price of gold are two key factors negatively affecting the long-term variation of cryptocurrency metrics. Although there is an overall strong positive correlation between the prices of gold and BTC, after accounting for other factors, individual fluctuations in the gold price lead to a negative influence on the price of BTC. This aspect, along with BTC's fixed supply, network decentralization and security, underscores BTC as a digital store of value, reinforcing the concept that it can also function as a substitute for physical gold. While both gold and BTC respond negatively to a strengthened US dollar, BTC's reaction is notably stronger. In relation to BTC's price, its hash rate, reflecting mining activity, exhibits a broader market exposure. The study also demonstrates that while the value of the US dollar and the price of gold consistently drive variations in cryptocurrency prices and

BTC's hash rate, with dominant influence, their impact tends to diminish over time.

Despite the challenging economic landscape, Distributed Ledger Technologies (DLTs) are continuously evolving, serving as a transformative force within the financial services sector. Beyond reshaping the utilization of fiat currencies, DLTs have extended their disruptive influence to encompass traditional financial paradigms and may soon even impact central bank monetary policies. Benigno et al. (2022) theoretically emphasize the complexities of central bank monetary policy, in the presence of single solitary global cryptocurrency. These complexities are anticipated to intensify considerably in a more realistic multi-country setting, which includes multiple global cryptocurrencies. Benigno (2023), further shows that the government has control of the price level only if a privately issued currency is inflationary. It's crucial to recognize that cryptocurrencies often exhibit either transient inflationary characteristics or, in some instances, a lack of strict inflationary tendencies due to deflationary mechanisms embedded in their code.

A pivotal milestone occurred on June 9th, 2021, when the government of El Salvador enacted legislation recognizing BTC as legal tender. This unprecedented move marked the inaugural instance of a country adopting a cryptocurrency in such a manner. Subsequently, in a noteworthy development, the BTC Futures Exchange-Traded Fund (ETF) became the inaugural cryptocurrency ETF to be granted trading approval by the United States Securities and Exchange Commission (SEC), just over a month later. According to the 2022 Statista Global Consumer Survey (Statista, 2022b), encompassing 56 countries across diverse development levels and geographical regions, approximately 18% of respondents reported owning

or utilizing cryptocurrencies—an impressive 75% surge from 2019.¹ By October 2022, the collective market cap of the cryptocurrency sphere approximated 1 trillion USD, marking a reduction from the all-time high of nearly 3 trillion USD recorded in November 2021 (coinmarketcap.com). To provide context, the combined market cap of domestic firms listed on global stock exchanges reached around 105 trillion USD as of June 2022, growing to 122 trillion USD in 2021 (Statista, 2022a). This disparity underscores the rapid ascent of the cryptocurrency market, with an astounding 309% increase in overall market cap between 2019 and 2022, juxtaposed against a more modest 12.6% growth in the worldwide stock market. Remarkably, the growth span from 2019 to the pinnacle year of 2021 witnessed a staggering 980% expansion in cryptocurrency market cap, compared to the stock market’s 31% growth. As suggested by key surveys such as Bitstamp (2022) and Gemini (2022), perceived regulatory gaps have seemingly curtailed substantial institutional investments and broader adoption within the crypto sector. Critics contend that given the sector’s youthfulness, absence of centralized authority, and presence of smaller centralized entities, periods of economic turmoil make crashes, insolvencies, and bankruptcies an inevitable aspect of the cryptocurrency industry. Notably, the sector has persevered through significant crises, including the collapses of 2016 (MtGox) and 2022 (involving Terra Luna UST, Celsius, Voyager, Three Arrows Capital, FTX, and BlockFi).

In this research I examine a wide array of crypto-related metrics, encompassing the prices and market caps of layer one native coins as well as decentralized finance (DeFi) protocols

¹Notably, ownership or usage rates in 2022 for countries such as Nigeria and Thailand stood at 45% and 44% respectively, while in countries like Australia and the United States, they reached 18% and 16% respectively.

and BTC's hash rate. In conjunction with a representative collection of macroeconomic and financial indicators, I aim to foster a more profound empirical comprehension of the interplay between cryptocurrencies and the broader macroeconomic and financial landscape. The investigation encompasses both daily and monthly data frequencies, taking into account significant crypto-specific events. Through this comprehensive analysis, the research extends the existing literature and contributes to the elucidation of the intricate relationship between cryptocurrencies and macroeconomic and financial forces. The long-term relationships are estimated using both parametric (dynamic ordinary least squares) and non-parametric (fully modified ordinary least squares) methodologies. Estimation is augmented by robust standard errors to account for concerns regarding error autocorrelation and heteroskedasticity. The parametric and non-parametric estimates lead to the same conclusions. While all the independent variables demonstrate cointegration, only the price of gold and the value of the US dollar consistently exhibit statistically significant effects on BTC's price, hash rate, market cap, as well as the prices and market caps of other cryptocurrencies. To be specific, a one percentage point increase (decrease) in the price of gold corresponds to an approximate 3.6 percentage point decrease (increase) in the BTC price. While as a whole there is a high positive correlation between the prices of gold and BTC, after controlling for various other factors, variations in the price of gold cause a robust negative effect on the price of BTC. This specific aspect, coupled with BTC's fixed supply, proof of work (PoW) security, and decentralized network, underscores its position as a digital store of value, further bolstering the idea that it can function as a credible alternative to physical gold. ² Investors substi-

²A blockchain validates transactions through nodes, which are essentially individual computers or devices

tute one asset for the other rather than merely seeing them move in tandem. The impact of the US dollar's value, as assessed by the DXY index, has a notably stronger and more pronounced adverse influence—ranging from 21 to 27 times greater—on the price of BTC compared to the effect of the price of gold. Additionally, the negative impact of the DXY index on the price of gold is significantly smaller when compared with its influence on the price of BTC.

The estimates suggest that the hash rate of BTC, which reflects the mining activity on the BTC blockchain, exhibits a greater degree of general market exposure in comparison to the BTC price. Not only is the negative impact of the gold price on the hash rate estimated to be notably more substantial than its effect on its own price, but the hash rate is also positively influenced by fluctuations in the Federal Funds Rate and S&P 500, in contrast to the BTC price. This indicates that during a tighter Federal Reserve monetary policy, miners reduce BTC network activities. One reason could be their perception of tightened policy affirming high inflation and a move to safer assets, potentially lowering BTC's price. Moreover, a tighter monetary approach might signal increased energy costs to miners. While the S&P 500 is found to positively impact Bitcoin's price, mainly in daily frequencies, it yields the opposite effect on the hash rate. The latter effect might stem from miners' responsiveness that comprise the blockchain network. These nodes collaborate to verify and record new transactions on the blockchain. In a Proof of Work (PoW) consensus mechanism, miners compete against each other to process transactions on the network by solving a mathematical puzzle, for which they are rewarded. The node that successfully solves the puzzle adds the next block to the chain and receives new currency units. PoW serves as a highly secure consensus mechanism that progressively increases the network's difficulty over time, ultimately making it exceptionally resistant to hacking attempts.

to market dynamics. A thriving S&P 500 could lure attention and resources from BTC mining as miners chase potentially better returns elsewhere. Additional analyses indicate that price indices and market caps of two prominent DeFi protocols, namely Maker and Synthetix, display comparable patterns to BTC in response to the price of gold and the DXY index. Nevertheless, the impacts are somewhat less robust, as seen in instances such as the DXY index's influence on price and gold's effect on market cap. This could potentially be attributed to the constraints of limited time series data. Finally, I compute metrics of the daily contribution of the price of gold and the DXY index as well as their joint contribution in explaining the variation of the price and hash rate of BTC. These metrics affirm the significant contributions of both DXY and the price of gold to the decline in BTC's price and hash rate. Notably, DXY predominantly affects the price reduction, while the price of gold primarily drives the hash rate decrease. This study indicates that although these factors explain a significant portion of BTC's price and hash rate decline, their impact gradually diminishes.

While the literature addressing cryptocurrencies within the context of monetary theory and finance is relatively recent, it is continuously evolving. Theoretical efforts are predominantly centered on BTC and the proof-of-work (PoW) consensus mechanism. Notably, Garratt and Wallace (2018), Schilling and Uhlig (2019), Fernández-Villaverde and Sanches (2019), Cong et al. (2021), Pagnotta (2022), and Biais et al. (2023) illustrate the emergence of multiple equilibria (i.e., indeterminacy) when BTC is introduced into otherwise conventional monetary models.³ Benigno et al. (2022) and Benigno (2023) further emphasize the

³Garratt and Wallace (2018) highlight the significance of self-fulfilling beliefs about BTC, Schilling and

complexities of monetary policy in the presence of cryptocurrencies.

The empirical research examining the link between crypto and the macroeconomy has been relatively overlooked by the academic literature. An early work by Ciaian et al. (2016) uses an extended Barro (1979) type framework to derive an empirically estimable model of the BTC price. While they find that BTC specific characteristics such as the number of transactions, the number of addresses and views of Wikipedia drive the price at a daily frequency, they find little evidence that macroeconomic and financial factors such as Dow Jones, exchange rates and oil prices have an impact on the BTC price. Similar results are shown by Syafiqah and Basah (2021) using monthly data while Benigno and Rosa (2023) find that BTC is unresponsive to macroeconomic news, using a specific methodology and a small sample of high frequency data. Syafiqah and Basah (2021) however report evidence of cointegration between macroeconomic indicators and the price of XMR of the Monero blockchain. Lee and Rhee (2022) estimate a VECM using monthly data and find long-term relationships between BTC and macro indicators such as S&P 500, VIX, the 10-year treasury yield, CPI, the gold price and the dollar index. Carrick (2016) suggests that BTC complements other currencies, particularly those of emerging economies. Corelli (2018) not only finds a substantial connection between BTC and currencies of emerging economies but also establishes a relationship between the latter and five other high-market-cap cryptocurrencies. His findings further highlight the weaker links of cryptocurrencies and currencies

Uhlig (2019) explore the evolution of BTC's price and monetary policy, Fernández-Villaverde and Sanches (2019) emphasize currency competition, Cong et al. (2021) focus on the role of mining pools for miner risk sharing, Pagnotta (2022) emphasizes the security of blockchain technology, and Biais et al. (2023) underscore the role of sunspots in prices within a general equilibrium model.

of developed economies.⁴ The empirical finding of the link between crypto and currencies of emerging economies is justified by evidence reported in the Gemini (2022) survey which suggests that investors consider crypto as a good hedge against currency devaluations, especially in countries that experienced 50% or more devaluation of their currency against the USD over the last 10 years.

In this study, I refrain from analyzing the reaction to methodology-dependent macroeconomic news. Additionally, given the focus on the US economy using US indicators, and considering that most cryptocurrency transactions are tied to the US dollar as a primary benchmark, I choose not to include exchange rates from various countries. Instead, I focus on the impact of the relative value of the US dollar, as measured by the DXY index. The subsequent sections of this paper are structured as follows. Section 2 offers a concise historical review, tracing the technical evolution of cryptocurrencies. Section 3 encompasses the empirical analysis, including data description, analysis, estimation of long-run relationships, and illustration of dynamic effects. Finally, Section 4 provides the concluding remarks.

2 Crypto's technical evolution

The evolution of cryptocurrencies is closely interwoven with technological progress, particularly the groundbreaking concept of blockchain. This section delves into the key milestones that have shaped the technical landscape of cryptocurrencies, offering insights into their genesis, development, and the emergence of blockchain as a foundational building block. By

⁴Almansour et al. (2020) finds a weak connection only between BTC and the USD/GBP exchange rate but no significant links between BTC and exchange rates of other developed economies.

understanding the foundational elements of cryptocurrencies, we can make more informed connections between their technical evolution and their interactions with broader economic factors and the subsequent analysis of the interplay between cryptocurrencies and macroeconomic indicators.

Haber and Stornetta (1991) tackled the challenge of verifying the creation and modification times of a digital document. The proposed time-stamping approach guarantees prevention against retroactively or proactively altering sequentially occurring data, even when involving collusion with a time-stamping service. While the term "blockchain" is not explicitly referenced, this marks the initial introduction of a concept similar to a "blockchain". Szabo (1996) pioneered the formalization of "smart contracts" as digitally specified commitments, encompassing protocols governing their fulfillment. These contracts proved revolutionary, facilitating secure and efficient execution of diverse financial transactions. Szabo (1998) introduced "bit gold", a digital currency concept leveraging computational power costs within a decentralized framework. This involves generating bits via solving fluctuating computational equations, akin to the PoW consensus mechanism—initially proposed by Dwork and Naor (1992) to combat email spam. Szabo aimed to establish a secure, decentralized digital asset, minimizing reliance on central authorities. Decentralization resolves the trust issue in valuing money through third parties. Despite well-documented bit gold methodology, implementation never occurred. Subsequently, Konst (2000) proposed block theory, interlinking secure blocks, and employing cryptography to trace entry authenticity back to the origin.

In 2008, an individual or group using the alias Satoshi Nakamoto released a paper titled "Bitcoin: A Peer-to-Peer Electronic Cash System" (Nakamoto, 2008), marking the inception

of the first cryptocurrency.⁵ The paper merged concepts from prior research to propose a decentralized, distributed time-stamp system that generates computational evidence for transaction chronology. It introduced a network of validating computers (nodes) operating without a central authority, employing a PoW consensus mechanism. The total supply of BTC is capped at 21 million units, ensuring no more will ever exist.⁶ Nakamoto's paper outlines BTC's creation to address costly third-party mediation in transactions. The initial BTC block, termed the genesis block (or block 0), was mined on January 3rd, 2009, sparking a financial revolution. BTC's invention marked the inception of a decentralized money market and an alternative to inflationary fiat currencies, aiming to serve as a long-term inflation hedge. Athey et al. (2016) find BTC's main usage as an investment, consistent with Glaser et al.'s (2014) results. In the short term, BTC acts as a "risk-on" speculative asset, though the prevailing perception positions it primarily as a store of value, akin to physical gold despite differing properties. The findings presented in this study align with this perspective.

BTC possesses significant limitations. Firstly, despite adhering to key smart contract design principles outlined by Szabo (1996) and being a smart contracting platform, its scripting language presently doesn't support DApps (decentralized applications).⁷ Secondly, while the PoW consensus mechanism ensures robust security, it results in significant resource

⁵As of now, Satoshi Nakamoto's true identity remains undisclosed.

⁶BTC has a hard cap of 21 million coins, with a circulating supply of approximately 19.21 million as of November 2022. Coin release occurs gradually, halving the mining reward every four years. The initial 2009 reward was 50 BTC per block, valued around 850K USD at current prices (November 2022). BTC minting is projected to cease by 2140, with miners subsequently receiving transaction fees.

⁷In addition to the native coin of a distributed ledger technology (DLT), tokens can function as payment methods for DApps built on the DLT. Prominent examples of DApps include DeFi protocols.

wastage, with only a single miner being rewarded per block despite numerous miners expending resources to mine it. Moreover, scalability remains an issue; the BTC network struggles to handle substantial transaction volumes swiftly. Ethereum, an open-source blockchain introduced in July 2015 (Buterin, 2014), addressed the lack of DApps by incorporating smart contract functionality. Many distributed ledger technologies tackle resource wastage by employing proof of stake (PoS) consensus mechanisms for transaction validation or alternative approaches like efficient PoW. Ethereum, the second-largest blockchain by market cap, initially operated on a PoW consensus until September 15th, 2022, when it transitioned to PoS through the 'Merge'.⁸ Despite adopting the PoS model, the Ethereum blockchain still faces challenges related to scalability and high transaction costs. These constraints have triggered substantial growth within the blockchain industry, propelling initiatives to counter them through the implementation of Layer 2 (L2) protocols and the creation of new blockchains.

⁹ Presently, over 1,000 blockchains or, more generally, DLTs exist, with around 20,000 cryptocurrencies built atop them. Developers continually aim to enhance three primary attributes: decentralization, scalability, and security, collectively referred to as the 'Blockchain Trilemma'. This term arises due to the common trade-off between these attributes; for instance, heightened decentralization might sacrifice scalability, while prioritizing scalabil-

⁸In PoS, node owners validate blocks by staking their coins, such as ETH in this case, and receive rewards in return. As of May 2022, stateofthedapps.com reports nearly 3000 DApps developed on the Ethereum blockchain (out of a total of 4073 DApps across all blockchains), positioning it as the second-largest blockchain after BTC.

⁹L2 protocols operate atop parent blockchains or layer one (L1) blockchains (e.g., Ethereum and Bitcoin) with the goal of enhancing scalability and reducing transaction fees.

ity could compromise security. Beyond addressing the blockchain trilemma, where some blockchains assert partial solutions, a prevailing trend is interoperability—constructing infrastructure that facilitates active communication between diverse blockchain protocols.

3 Empirical Analysis

To estimate the long run relationship between cryptocurrencies and macroeconomic and financial indicators, I consider various measures of cryptocurrencies at different samples and frequencies.

3.1 Data

The effects on cryptocurrencies are measured via the construction of crypto indicators using closing prices and market caps of major coins as well as the hash rate of BTC.¹⁰ Apart from BTC, I collect and utilize price data for the following altcoins: ETH, Litecoin (LTC), BNB, XRP, DOGE, ADA, Maker (MKR), AAVE, UniSwap (UNI), Curve (CRV), PancakeSwap (CAKE), Synthetix (SNX), SushiSwap (SUSHI), Compound (COMP), Balancer (BAL), Yearn.finance (YFI) and the stablecoin USDT. The sample starting dates of each coin vary depending on data availability which implies that the sample periods of each indicator and thus the various indicator samples considered in estimation will vary. The reasoning behind the choice of the specific cryptocurrencies is the high market cap ranking in combination with the length of the available time series. Specifically, I consider the price

¹⁰The market cap of a cryptocurrency is defined as the product of a coin's circulating supply and its closing price.

of BTC (P_B), its hash rate (H_B) and its market cap (M_B) using daily data between the 29th of April 2013 and the 30th of November 2022. I use these variables as single indicators, not only because BTC has the highest market cap across all cryptocurrencies but also because it has the longest available time series.¹¹ Between the beginning and the end of the sample period, the rise of P_B and M_B has been explosive, with a 12692% and 22068% increase, respectively. As of the 30th of November 2022, P_B and M_B were sitting at 17 thousand USD and 330 billion USD, respectively. Within the same period, the H_B , a measure of computational power and an indicator of the network's health, also increased by 321 million %.¹² Within the same period, as a matter of comparison, the S&P 500 index increased by 156% with a market cap of about 31 trillion USD, while S&P 500's largest constituent, Apple Inc., had a market cap of 2.4 trillion USD. These numbers clearly indicate that the rise of the BTC technology that appeared in the scene only a decade ago without yet mass institutional adoption is outstanding at the very least.

Apart from BTC indicators, I consider two more sets of price and market cap indicators, one for layer-one native coins that incorporates DOGE and USDT, and another for DeFi protocols. Specifically, $P_{\overline{BL}}$ is a weighted average of the prices of *BTC*, *LTC*, *ETH*, *USDT*, *BNB*, *XRP* and *DOGE* and $M_{\overline{BL}}$ corresponds to the sum of the market caps of those cryptocurrencies. The sample is daily and spans from July 25th 2017 to November 30th 2022. Likewise, P_{MS} is the weighted average of the prices of *MKR* and *SNX*, while M_{MS}

¹¹Although the latter is also true for LTC, being one of the oldest cryptocurrencies while preserving its position among those with the highest market cap, I do not consider it separately or in a two-coin indicator with BTC because its market cap share relative to that of BTC is tiny; on average less than 3%.

¹²The hash rate increase between November 2022 and November 2021 was 70%.

is the corresponding market cap sum. The daily sample spans from March 16th 2018 to November 30th 2022. Finally, $P_{\overline{MS}}$ is an extended price indicator which corresponds to the weighted average of the prices of *MKR*, *SNX*, *AAVE*, *UNI*, *CRV*, *CAKE*, *SUSHI*, *COMP*, *BAL* and *YFI*, while $M_{\overline{MS}}$ is the matching market cap sum. In this case, the daily sample spans from October 5th 2020 to November 30th 2022.¹³ All the data series for cryptocurrencies were obtained from coinmarketcap.com. The weights of the price indicators are the time varying market cap shares of the coins that comprise the indicator, measured in US dollars. The daily data were also used to construct parallel samples with monthly data, apart from the cases of monthly $P_{\overline{MS}}$ and $M_{\overline{MS}}$ which are excluded due to their extremely short sample length (only 26 observations). Figure 1 displays the time series of the market cap shares for each of the three sets of composite indexes at daily frequencies. Although the share of BTC in the \overline{BL} indicator dominates the shares of the rest of the coins, jointly the remaining coins contribute significantly to the indicator as the mean of their combined share is 33% with the *ETH* share being the largest at 19%. In the two-coin aggregate indicator *MS*, the share of *SNX* is significantly low until the late 2019. Interestingly, the share of *SNX* looks like a mirror image of the share of *MKR*. In the aggregate indicator \overline{MS} , *UNI* clearly dominates between 20-50% as it is the largest DEX (decentralized exchange) in the crypto space.

¹³Between period July 2017 and November 2022, $P_{\overline{BL}}$ increased by 446% and $M_{\overline{BL}}$ increased by 786%, sitting at 642 billion USD as of the 30th of November 2022. Although respectively P_{MS} and $P_{\overline{MS}}$ decreased by 46% and 66% between the beginning and end of the sample, M_{MS} and $M_{\overline{MS}}$ increased by 153% and 327%, while as of 30/11/2022, M_{MS} and $M_{\overline{MS}}$ were sitting at 1,2 billion and 8 billion US dollars.

Table 1: Correlations of crypto variables

	P_B	$P_{\overline{BL}}$	P_{MS}	$P_{\overline{MS}}$	M_B	$M_{\overline{BL}}$	M_{MS}	$M_{\overline{MS}}$	H_B
P_B	1	0.99	0.72	0.79	1	0.99	0.94	0.90	0.89
$P_{\overline{BL}}$	0.96 (0.11)	1	0.67	0.79	0.99	0.96	0.93	0.80	0.69
P_{MS}	0.53 (0.43)	0.47 (0.46)	1	0.88	0.71	0.74	0.77	0.89	0.25
$P_{\overline{MS}}$	0.42 (0.48)	0.37 (0.49)	0.90 (0.19)	1	0.78	0.72	0.89	0.75	-0.48
M_B	1 (0.00)	0.96 (0.11)	0.53 (0.43)	0.42 (0.48)	1	0.99	0.94	0.90	0.90
$M_{\overline{BL}}$	0.97 (0.08)	0.88 (0.22)	0.57 (0.42)	0.46 (0.49)	0.97 (0.08)	1	0.94	0.93	0.66
M_{MS}	0.59 (0.40)	0.51 (0.44)	0.76 (0.38)	0.74 (0.35)	0.59 (0.40)	0.64 (0.38)	1	0.93	0.69
$M_{\overline{MS}}$	0.70 (0.32)	0.62 (0.36)	0.56 (0.43)	0.47 (0.49)	0.70 (0.32)	0.76 (0.28)	0.81 (0.25)	1	-0.18
H_B	0.01 (0.38)	0.01 (0.37)	0.04 (0.36)	0.08 (0.36)	0.01 (0.38)	0.03 (0.36)	0.05 (0.32)	0.08 (0.32)	1

Notes: All variables are expressed in logarithms prior to computing correlations using daily data. The upper triangular corresponds to correlations with a complete sample, and the lower triangular corresponds to mean correlations computed with 10-day rolling window. The numbers in parentheses are standard deviations.

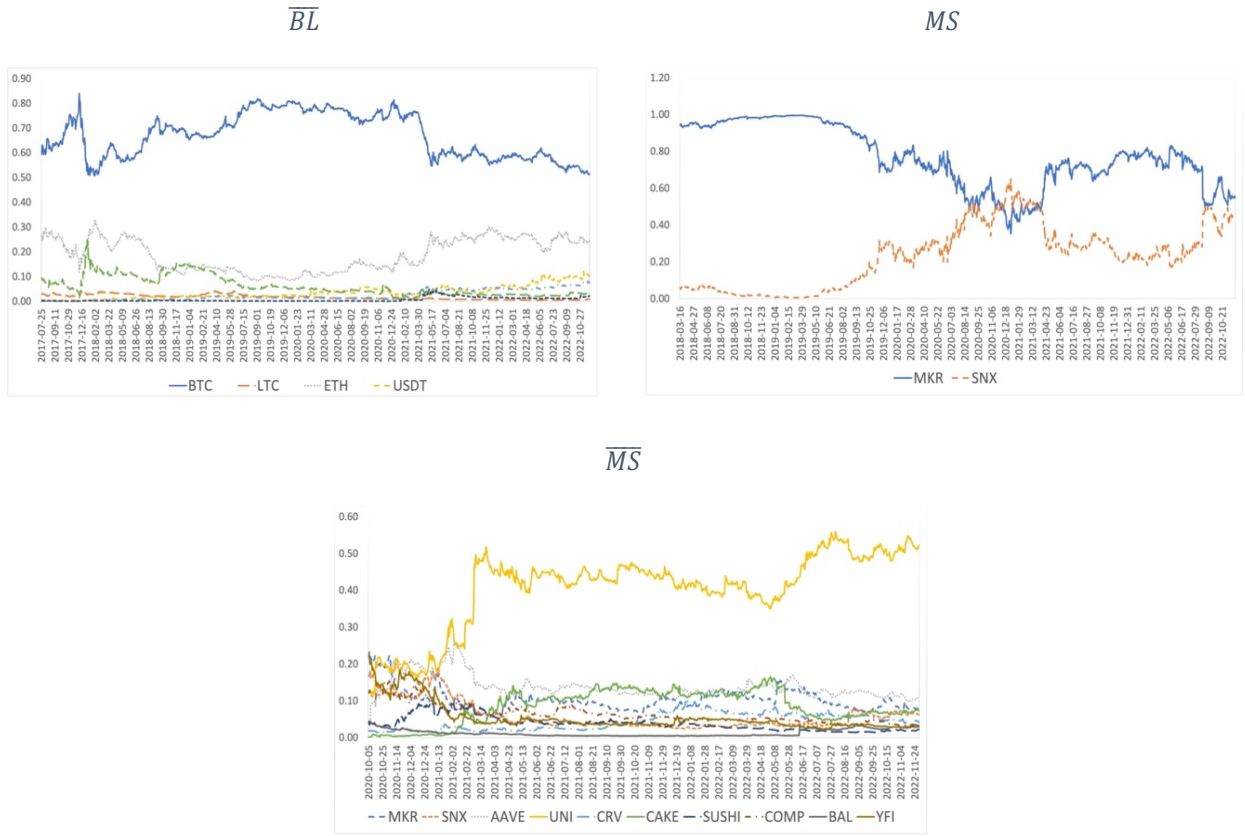


Figure 1: Market cap shares for \overline{BL} , MS and \overline{MS}

Figure 2, displays the time series of crypto prices and corresponding market caps. The figure shows that crypto prices as well as market caps exhibit a positive correlation. Table 1 gives a better insight into correlations by displaying the Pearson correlation coefficient between the crypto variables, expressed in logarithms, in two different ways using daily data. The upper triangular of the table exhibits cross correlations which are computed using complete samples, while the lower triangular exhibits the mean of rolling correlations (10-day window) along with standard deviations in parentheses. While the complete sample correlations is a good indicator of the relationship of two variables, it may also lead to cases

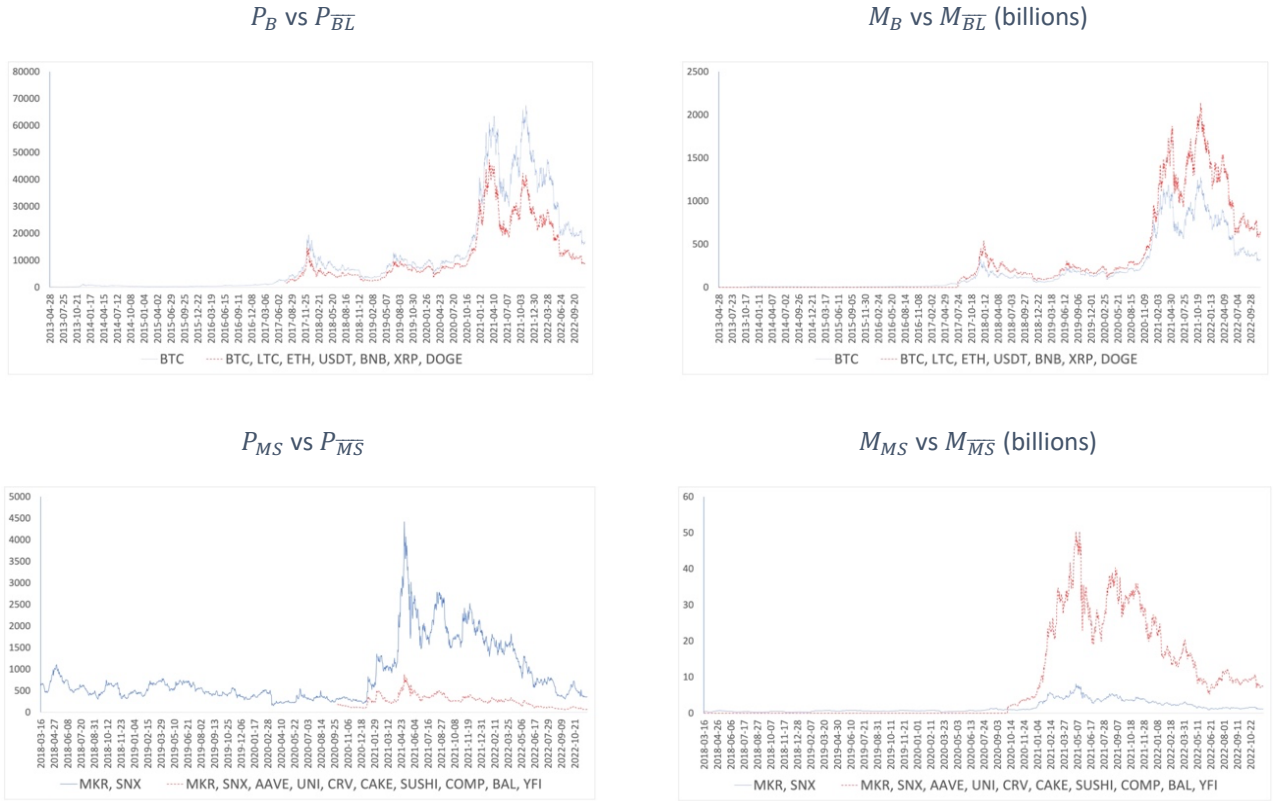


Figure 2: Prices and market caps of the crypto indicators

with biased outcomes under certain conditions. ¹⁴ The mean of rolling correlations with a 10-day window, along with the corresponding standard deviations, offers a more robust and nuanced approach. The rolling correlation methodology, captures the dynamic nature of the relationship between the variables over time and address aforementioned issues. The complete sample correlations suggest that, apart from the hash rate in a few cases, there is a strong positive co-movement between the variables. The rolling correlations indicate

¹⁴These cases encompass situations where there are nonlinear relationships between the variables, a few outliers that heavily influence the correlation result, and subgroups within the data that exhibit different correlation patterns.

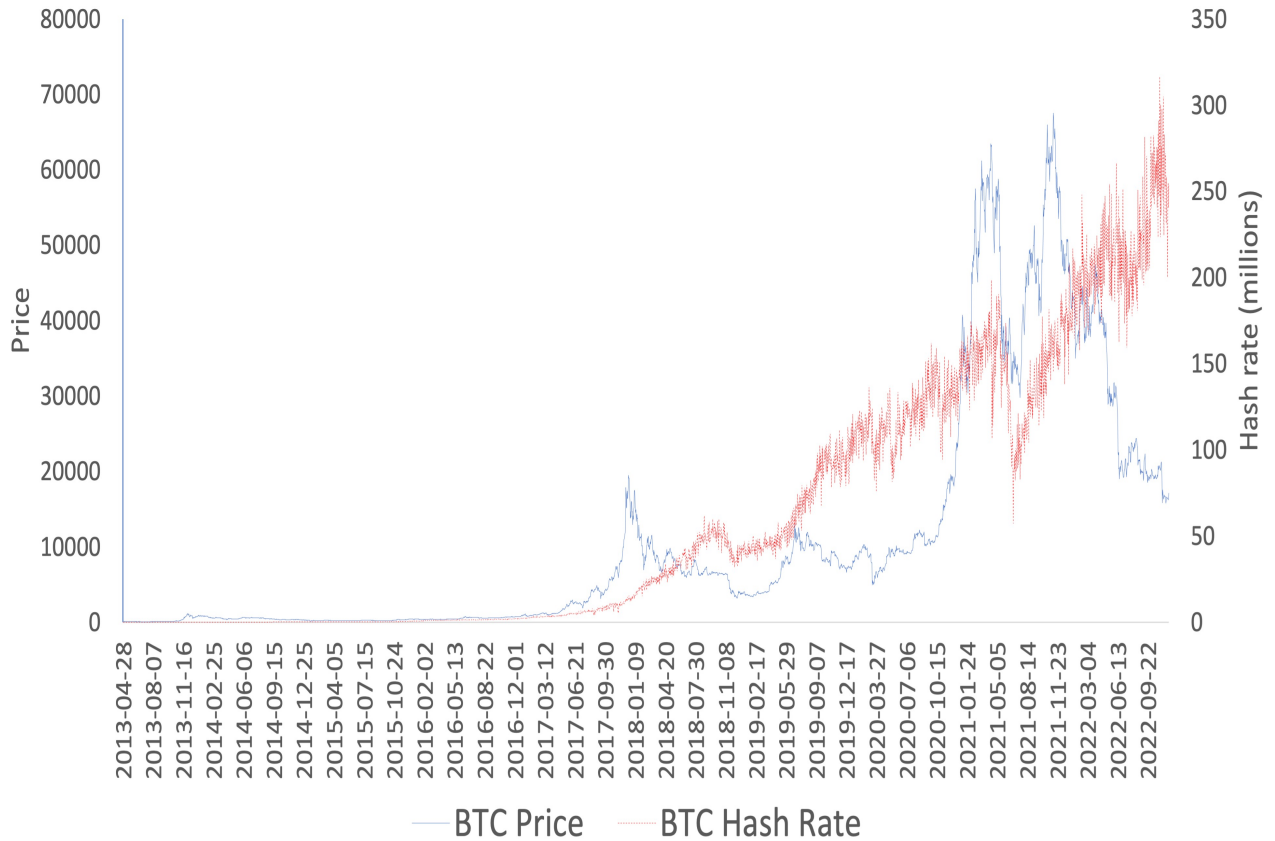


Figure 3: The price of BTC vs its hash rate

however that in most cases the correlations are not only significantly lower than those of complete samples but also very volatile. The fact that correlations reduce when one considers a rolling window is an indication that complete sample correlations are substantially driven by large swings due to systemic events that move most variables in the same direction. In the estimation the latter is taken into consideration as I control for major crypto-specific events which generate large swings to crypto prices with no effects on financial markets and macroeconomic variables. Exceptions are the correlations of the following pairs which preserve a correlation of at least 0.96 under both complete and rolling samples, with a low

standard deviation for the latter: (P_B, M_B) , $(P_B, P_{\overline{BL}})$, $(P_B, M_{\overline{BL}})$, $(M_B, M_{\overline{BL}})$ and $(P_{\overline{BL}}, M_B)$. It is worth noting that $P_{\overline{BL}}$ is fluctuating closely with P_B not only because BTC has a large share in the former but also because major layer one and large market cap coins tend to co-move with BTC. Given the large co-movements between the aforementioned series, I exclude variables M_B , $M_{\overline{BL}}$ and $P_{\overline{BL}}$ from the econometric model and the subsequent analysis.

An intriguing case is the hash rate of BTC. While H_B and P_B exhibit a correlation coefficient of 0.89 for the complete sample, the mean of the rolling correlation plummets to 1% with a standard deviation of 0.38. Furthermore, the means of all rolling correlations of H_B with the rest of the crypto prices are also around 1%-8% with large standard deviations, indicating zero co-movement despite the large positive correlations in complete samples. As shown on Figure 3, H_B is highly volatile with large common swings with P_B that evidently drive the large positive correlation in the complete sample. Despite the massive downward shifts of the price of BTC, its hash rate exhibits a clear upward exponential trend which reflects the expansion and health of the network. For instance, the drop of 32% of P_B between 8/11/2021 and 17/12/2021 is accompanied by an increase of 23% of H_B .

To evaluate the degree of interaction of crypto with macroeconomic and financial variables, I deploy a list of selected indicators. At daily frequencies, the latter consists of the S&P 500 (SP500) index, the DXY index, the price of gold (GOLD) and the federal funds effective rate (FFR).¹⁵ For convenience, I represent the set of macroeconomic and financial

¹⁵DXY measures the value of the US dollar versus a basket of six global currencies, the Euro, the UK Pound, the Canadian Dollar, the Japanese Yen, the Swedish Kroner and the Swiss Franc. GOLD corresponds to the price of gold per troy ounce. The data source for S&P 500 and FFR, is the Federal Reserve Economic

indicators as $X = [FFR, SP500, GOLD, DXY]'$. It is worth noting that apart from the pair $SP500$ and $GOLD$ where the two exhibit a correlation coefficient of 0.82, the correlation coefficients between the rest of the X indicators are less than 0.5. One issue in combining the crypto data with macro and financial indicators is the unbalanced sample due to the fact that cryptocurrencies are traded 24 hours per day in all days of the year, while data for macroeconomic and financial indicators are available only for working days and times. To construct a balanced sample, I adjust the sample of crypto variables by excluding the observations in days where data for macro and financial indicators are not available.

At the monthly frequency, I am keeping the same indicators, despite the fact that there is available data for $I(1)$ series such as the Consumer Price Index (CPI) and weekly earnings. The reason I do not incorporate these indicators into the system is because they are highly correlated with existing X indicators and may have a spurious relationship with the crypto variable, which can then lead to incorrect inference about the true long-run relationship.¹⁶ None of the indices is seasonally adjusted.¹⁷ The sample period of the macroeconomic and

Data (FRED) of the Federal Reserve Bank of St Louis. The data sources for $GOLD$ and DXY are gold.org and marketwatch.com, respectively.

¹⁶The correlation coefficient between CPI and $SP500$ is 0.93, while the correlation coefficient between weekly earnings and $SP500$ is 0.97. Weekly earnings correspond to seasonally adjusted average weekly earnings of all employees in the private sector (source: FRED of the Federal Reserve Bank of St Louis).

¹⁷Firstly, seasonal adjustment (SA) is typically less applicable to high-frequency data. Secondly, SA often necessitates a substantial historical dataset for accurately identifying seasonal patterns, a condition not met in the relatively recent cryptocurrency market. Thirdly, SA assumes that seasonal patterns remain relatively stable over time, which may be less likely in the highly volatile cryptocurrency market. Therefore, attempting to apply SA to existing cryptocurrency data may result in inaccuracies and misinterpretations.

financial indicators corresponds to the same sample period as the one for BTC that is, April 29th 2013 to November 30th 2022. Table A1 provides descriptive statistics.

3.2 Long-run relationships

The present study aims to investigate potential long-term associations between cryptocurrency variables and macroeconomic and financial indicators. To ensure an appropriate statistical specification of the model, I begin by assessing the order of integration of the variables through unit root tests. Based on the results of these tests, I proceed by presenting estimates of the long run relationship, if any, using the dynamic OLS (D-OLS) parametric approach of Stock and Watson (1993) and the fully modified OLS (FM-OLS) non-parametric approach of Phillips and Hansen (1990).

Tables 2A and 3A display various cases of stationarity tests for the daily and the monthly data series, respectively by employing the Augmented Dickey-Fuller (ADF), the Phillips-Perron (PP) and the Kwiatkowski-Phillips-Schmidt-Shin (KPSS) unit root tests. In the cases where the tests give conflicting results, I give more weight to the PP test over the ADF test, as the former accounts for serial correlation or heteroscedasticity while being more robust in the presence of structural breaks (case of FFR at monthly frequencies). The tests provide adequate evidence both at daily and monthly frequencies that the series P_B , P_{MS} , $P_{\overline{MS}}$, $M_{\overline{MS}}$, $M_{\overline{MS}}$, DXY , $GOLD$ and FFR are $I(1)$ processes. The results suggest that the series exhibit unit roots both with and without linear trends (*Trend*). In the case of $SP500$ at the daily frequency, the ADF and the PP tests suggest that the unit root hypothesis cannot be rejected when a linear trend is excluded but it is rejected at the 10% significance

level when a linear trend is included. However, the KPSS test rejects trend stationarity of *SP500* at the 1% significance level while both the ADF and PP tests cannot reject the unit root hypothesis even when the trend is included at the monthly frequency. For H_B , the unit root hypothesis is not rejected only when the intercept is excluded, which means that the H_B series is only a conditionally $I(1)$ process. Apart from the case of H_B , most of the other series have unit roots either with or without an intercept. In estimating long-run relationships, I am including the intercept to avoid possible spurious long-run relationships that may result from excluding fixed or structural factors, which can be captured by the intercept. Likewise, linear trends cannot be ignored either as they also appear to be statistically significant.

Having established the order of integration of the series, I next turn to testing for long-run relationships using robust standard errors which address problems of error autocorrelation and heteroskedasticity.¹⁸ Specifically, a model is employed in which the dependent variable is represented by one of the following variables: P_B , H_B , P_{MS} , $P_{\overline{MS}}$, $M_{\overline{MS}}$, and $M_{\overline{MS}}$. The fixed set of independent variables, excluding the constant and trend, comprise of *FFR*, *SP500*, *GOLD*, and *DEXY*. The model is estimated using dynamic ordinary least squares (D-

¹⁸The models that follow were also estimated and tested using control variables for six major crypto-specific events that caused significant adverse effects on crypto prices: (i) the Mt. Gox exchange hack; (ii) the Bitfinex exchange hack; (iii) the Luna UST stablecoin collapse; (iv) the froze of withdrawals, swaps and transfers by the crypto lender Celcius; (v) the failure of the crypto hedge fund Three Arrows Capital to meet its margin calls; (vi) the FTX exchange collapse. To do so I used standard dummies as well as dummy-type variables capturing the persistence of the effect in the daily frequency. The finding is that these control variables do not significantly change the main results. To save on space, I do not report these results which are available upon request.

OLS) which is the most commonly used and computational efficient estimation approach of long-run relationships. It eliminates endogeneity problems as well as error serial correlation. Furthermore, D-OLS, in contrast to a Vector Error Correction Model (VECM), does not necessitate any a priori structure specification, such as the ordering of variables, which can have significant implications on the estimation results. The fact that H_B is $I(0)$ while covariates DXY , $GOLD$, FFR and $SP500$ are $I(1)$ may give rise to the problem of an unbalanced regression which is subject to a non-standard distribution as the residuals could be non-stationary. However, this is not applicable in this context primarily due to the specific configuration of the model and the inherent characteristics of the data series. First, as demonstrated in Tables A2 and A3, the dependent variable, H_B , when combined with a linear trend, exhibits stationarity of order $I(0)$. Second, as demonstrated in Table 3, the regressors $GOLD$, DXY , FFR , and $SP500$ exhibit mutual cointegration at both daily and monthly frequencies. The results of the Engle–Granger cointegration test show that the null hypothesis is rejected (indicating the presence of cointegration) at the 5% significance level for the daily data and at the 10% significance level for the monthly data. Furthermore, the D-OLS and the fully modified ordinary least squares (FM-OLS) estimators confirm the existence of a long-run relationship among the four variables since all parameters exhibit statistical significance, with a minimum significance level of 5% for the daily data and a minimum significance level of 10% for the monthly data. Since the regression combines two $I(0)$ components—the first being H_B with a trend and the second being the mutually cointegrated variables $GOLD$, DXY , FFR , and $SP500$ —it produces stationary residuals, ensuring that the estimating equation is balanced for both daily and monthly frequencies.

To estimate the long-run relationship between the cryptocurrency variables and X , I utilize both the D-OLS estimator, which follows a parametric approach, and the FM-OLS estimator, which adopts a non-parametric approach, to enhance the robustness of the results. Table 2 presents the estimation results for the price and hash rate of BTC using the D-OLS and FM-OLS methodologies at both daily and monthly frequencies. The findings reveal that *GOLD* and the *DXY* are the dominant factors exerting significant influence on the price of BTC. *GOLD* demonstrates statistical significance at both daily and monthly frequencies across both estimation approaches, with significance levels ranging from 0.1% to 1%. Specifically, a 1% increase in the price of gold causes a 3.46-3.8% reduction in the price of Bitcoin on a daily basis, and a 3.15-3.97% decrease on a monthly basis. On average, across daily and monthly frequencies and based on both estimation methods, an increase of one percentage point in the price of gold is associated with a decrease of approximately 3.6 percentage points in the price of BTC. If one only considers the Pearson correlation coefficient between the prices of gold and BTC, which is as high as 0.77, they may end up with rather misleading conclusions regarding the relationship between the two assets. This relationship is actually robustly negative when other factors are taken into consideration. These observations reinforce the notion of BTC being akin to digital gold, which aligns with proponents' assertions. It could potentially embody an enhanced form of gold, proficiently serving as a store of value and an inflation hedge due to its fixed supply, security, and decentralization features. Additionally, it could even function as a viable alternative to traditional gold. As the demand for gold decreases, along with a decline in stock prices, investors who see BTC as a substitute or a digital version of gold choose to allocate their resources towards BTC.

This shift in investor sentiment and allocation leads to an increase in the demand for BTC, consequently exerting upward pressure on its price. Therefore, the negative relationship between the price of gold and BTC can be understood as a result of market dynamics and investor preferences between these two assets, where BTC competes with gold as a store of value. Contrary to the price of gold that exhibits a strong negative relationship with the federal funds rate, as shown in Table 3, the price of BTC does not exhibit a statistically significant relationship with the latter, either in daily or monthly frequencies. Furthermore, while the price of BTC exhibits a positive and statistically significant relationship with the S&P 500 at daily frequencies, similar to that of gold, it is noteworthy that this association fades out and becomes statistically insignificant when examining monthly frequencies, unlike gold.

In addition to the price of gold, the price of BTC is influenced, similar to gold, by the value of the US dollar, as measured by the *DXY* index. The impact of the *DXY* on the price of BTC however is significantly larger compared to its impact on the price of gold, ranging from 21 to 27 times greater. Specifically, a one percentage point increase in the *DXY* index is associated with a substantial decrease in the price of BTC of approximately 11 percentage points across both daily and monthly frequencies. In contrast, a percentage point increase in the *DXY* index is linked to a comparatively smaller decrease of approximately 0.42 and 0.47 percentage points in the price of gold across daily and monthly frequencies, respectively. Therefore, the strengthening of the US dollar exerts a much more pronounced negative influence on the demand for BTC compared to gold, resulting in substantial implications for its price.

Table 2: The long-run relationships of P_B & H_B with X

X	daily		monthly		daily		monthly	
	D-OLS	FM-OLS	D-OLS	FM-OLS	D-OLS	FM-OLS	D-OLS	FM-OLS
	BTC price (P_B)				BTC hash rate (H_B)			
FFR	0.039 (0.079)	0.015 (0.075)	0.048 (0.136)	0.028 (0.109)	-0.46 ^c (0.22)	-0.58 ^b (0.20)	-0.65 ^d (0.33)	-0.85 ^b (0.30)
SP500	1.58 ^c (0.80)	1.43 ^d (0.75)	1.78 (1.45)	1.66 (1.12)	-2.69 (2.22)	-3.60 ^d (1.98)	-7.90 ^c (3.76)	-5.39 ^d (3.11)
GOLD	-3.46 ^a (0.74)	-3.80 ^a (0.70)	-3.15 ^b (1.24)	-3.97 ^a (1.03)	-12.50 ^a (2.03)	-14.04 ^a (1.84)	-16.68 ^a (3.28)	-17.89 ^a (2.85)
DXY	-10.75 ^a (1.23)	-11.4 ^a (1.18)	-11.36 ^a (2.11)	-11.49 ^a (1.69)	-6.08 ^d (3.36)	-7.29 ^c (3.08)	-12.79 ^c (5.50)	-10.57 ^c (4.69)
C	65.4 ^a (13.7)	71.69 ^a (12.8)	68.50 ^b (24.85)	71.69 ^a (18.99)	144.42 ^a (38.37)	167.31 ^a (33.65)	241.97 ^a (66.88)	221.90 ^a (52.62)
Trend	0.003 ^a (0.000)	0.003 ^a (0.000)	0.069 ^a (0.019)	0.07 ^a (0.014)	0.009 ^a (0.001)	0.01 ^a (0.001)	0.26 ^a (0.05)	0.24 ^a (0.04)
adj R^2	0.96	0.96	0.97	0.96	0.93	0.92	0.99	0.92
Lags (AIC)	0		0		8		4	
Leads (AIC)	8		1		8		4	

Notes: The daily sample spans from 29 April 2013 to 30 November 2022 (2415 observations) and the monthly sample from April 2013 to November 2022 (116 observations). All regressions utilize robust Newey-West standard errors which are reported in parentheses. Lags and leads for D-OLS are chosen based on the Akaike information criterion (AIC). All three estimation approaches use the Bartlett kernel for calculating the long-run variance. The significance levels are denoted by 'a' for 0.1%, 'b' for 1%, 'c' for 5% and 'd' for 10%.

The hash rate of BTC, which indicates the mining activity on the BTC blockchain, demonstrates a higher level of market exposure compared to the BTC price. The impact of the gold price on the hash rate is estimated to be significantly higher than its effect on the price itself, with a range of 3.61-3.69 times greater at daily frequencies and 4.5-5.29 times greater at monthly frequencies. Specifically, a one-percentage-point increase in the price of gold corresponds to a 12.5-14.04 percent decrease in the hash rate on a daily basis, and to a 16.68-17.89 percent decrease on a monthly basis. The impact of the DXY index on the hash rate is comparable to its effect on the price. A one-percentage-point rise in the DXY index

leads to a 6.08-7.29 percent decline in the hash rate at daily frequencies, and a 10.57-12.79 percent decline at monthly frequencies. In contrast to the BTC price, the hash rate appears to also be influenced by the FFR and S&P 500. An increase of one percent in the FFR is associated with a decline in the hash rate of BTC by approximately 0.46-0.58 percent on a daily basis and 0.65-0.85 percent on a monthly basis. This suggests that when the Federal Reserve implements a tighter monetary policy, miners tend to reduce their mining activities on the BTC network. One possible explanation is that miners perceive a tightened monetary policy as a confirmation of high inflation and an investor shift towards less risky assets, resulting in a decrease in the price of BTC. Additionally, a tighter monetary policy may be seen by miners as confirmation of elevated energy prices, leading to higher mining costs. Interestingly, while the S&P 500 exhibits a positive effect on the price of BTC, particularly at daily frequencies, it has the opposite effect on the hash rate. However, it is important to note that this result holds significant at the 10% level on a daily basis and between 5% and 10% on a monthly basis. The positive influence of the stock market on the BTC price could be attributed to the perception that a bullish stock market environment signals overall economic growth and positive investor sentiment, leading to increased demand and higher prices for BTC. On the other hand, the negative impact of the S&P 500 on the BTC hash rate may be due to miners' reactions to market dynamics. Miners are primarily concerned with the profitability of their operations, which relies on various factors such as the cost of energy, mining difficulty, and block rewards. It is plausible that a rising S&P 500 indicates a flourishing traditional market, diverting attention and resources away from BTC mining as miners opt for potentially higher returns in other investment avenues. Consequently, the

Table 3: The long-run relationship of *GOLD* with *FFR*, *SP500* and *DXY*

	daily		monthly	
	D-OLS	FM-OLS	D-OLS	FM-OLS
FFR	-0.04 ^a (0.01)	-0.04 ^a (0.01)	-0.032 ^c (0.016)	-0.04 ^d (0.021)
SP500	0.56 ^a (0.04)	0.57 ^a (0.04)	0.55 ^a (0.05)	0.59 ^a (0.06)
DXY	-0.42 ^c (0.17)	-0.43 ^c (0.17)	-0.41 ^d (0.22)	-0.53 ^d (0.28)
C	4.72 ^a (0.68)	4.71 ^a (0.67)	4.77 ^a (0.88)	5.00 ^a (1.15)
adj R^2	0.78	0.77	0.92	0.78
Lags (AIC)	4		4	
Leads (AIC)	0		4	
	ADF	Engle-Granger	ADF	Engle-Granger
test statistic	-3.36		-3.14	
critical value				
5% sign. level		-3.34		-3.39
10% sign level		-3.05		-3.08

Notes: The daily sample spans from 29 April 2013 to 30 November 2022 (2415 observations) and the monthly sample from April 2013 to November 2022 (116 observations). All regressions utilize robust Newey-West standard errors which are reported in parentheses. Lags and leads for D-OLS are chosen based on the Akaike information criterion (AIC). All three estimation approaches use the Bartlett kernel for calculating the long-run variance. The significance levels are denoted by 'a' for 0.1%, 'b' for 1%, 'c' for 5% and 'd' for 10%.

BTC hash rate experiences a decline as miners shift their focus and resources, leading to a negative correlation with the S&P 500. However, further research is needed to delve deeper into the complex interplay between stock market indices, BTC prices, and mining activities to gain a comprehensive understanding of this phenomenon.

It is worth emphasizing that the relationship between the price of BTC and halving dates has been a subject of debate.¹⁹ Although only three halvings have occurred thus far,

¹⁹BTC halving, which occurs approximately every four years or after every 210,000 blocks are mined on

a similar pattern has been observed in the BTC price around each event. The price of BTC typically initiates an upward trend shortly before the halving, which gains momentum after the halving, ultimately reaching a peak 12 to 18 months later. However, it is important to note that there have been instances of upward trends in stock prices during the periods surrounding the three BTC halvings, which do not appear to be directly related to the halvings themselves. It is possible that the coinciding upward trends during the halvings were influenced by favorable macroeconomic and financial conditions, as well as increased liquidity in the market. Considering this perspective, it is plausible that the cycles in BTC prices may align more closely with liquidity cycles rather than halving cycles themselves. The notion that halvings amplify the perception of scarcity for BTC might have merely reinforced the more pronounced surges in Bitcoin's value during liquidity cycles, rather than serving as the primary driver behind them. Given the limited evidence for halving effects and the common pattern observed in crypto and stock prices around the halving period, the empirical analysis has deliberately avoided imposing any specific controls for halving cycles or effects. Introducing such controls could introduce biases into the results, potentially distorting the relationship between crypto prices and other variables.

Since the price indicator (P_{BL}) and market capitalization (M_{BL}) of major layer one coins the BTC blockchain, involves a reduction in the rewards received by miners for mining new BTC blocks. This reduction effectively decreases the rate at which new BTC enters circulation. The first halving took place on November 28, 2012, reducing the BTC block reward from 50 BTC to 25 BTC. The second halving occurred on July 9, 2016, further reducing the reward to 12.5 BTC. The third halving occurred on May 11, 2020, resulting in a block reward of 6.25 BTC. The upcoming fourth BTC halving is estimated to happen around block 840,000, expected to be mined in March or April 2024.

Table 4: Estimation of the long-run relationships of P_{MS} & M_{MS} with X

X	daily		monthly		daily		monthly	
	D-OLS	FM-OLS	D-OLS	FM-OLS	D-OLS	FM-OLS	D-OLS	FM-OLS
	P_{MS}				M_{MS}			
FFR	-0.09 (0.10)	-0.09 (0.09)	0.04 (0.14)	-0.09 (0.13)	0.05 (0.076)	0.01 (0.072)	0.23 ^a (0.04)	0.16 ^d (0.10)
SP500	4.17 ^a (0.96)	4.14 ^a (0.90)	-0.93 (1.35)	4.67 ^a (1.22)	1.87 ^b (0.72)	1.53 ^c (0.67)	-3.34 ^a (0.41)	1.24 (0.93)
GOLD	-3.87 ^a (1.06)	-4.04 ^a (1.00)	-3.78 ^c (1.62)	-4.37 ^b (1.34)	-1.51 ^d (0.80)	-1.61 ^c (0.77)	-3.50 ^a (0.43)	-1.50 (1.03)
DXY	-3.83 (2.57)	-4.25 ^d (2.41)	-15.80 ^a (3.83)	-4.22 (3.15)	-9.96 ^a (1.93)	-11.38 ^a (1.85)	-21.18 ^a (0.94)	-12.72 ^a (2.41)
C	18.51 (22.49)	21.76 (21.09)	111.40 ^a (28.68)	19.79 (28.27)	60.86 ^a (16.92)	70.60 ^a (16.16)	166.02 ^a (8.63)	77.97 ^a (21.65)
Trend	0.0004 (0.0009)	0.0005 (0.0008)	0.073 ^b (0.025)	0.008 (0.023)	0.002 ^a (0.0007)	0.003 ^a (0.0006)	0.14 ^a (0.007)	0.061 ^b (0.018)
adj R^2	0.72	0.70	0.97	0.72	0.89	0.89	0.97	0.90
Lags (AIC)	1		2		0		2	
Leads (AIC)	0		3		1		0	

Notes: The daily sample spans from 16 March 2018 to 30 November 2022 (1185 observations) and the monthly sample from March 2018 to November 2022 (57 observations). All regressions utilize robust Newey-West standard errors which are reported in parentheses. Lags and leads for D-OLS are chosen based on the Akaike information criterion (AIC). All three estimation approaches use the Bartlett kernel for calculating the long-run variance. The significance levels are denoted by 'a' for 0.1%, 'b' for 1%, 'c' for 5% and 'd' for 10%.

exhibit a strong positive correlation with the Bitcoin price, the aforementioned findings can be extended to encompass the major cryptocurrencies as a whole. However, it is important to acknowledge that consensus mechanisms, network security, and the level of decentralization in the alternative to BTC layer one blockchains diverge from those of BTC. Therefore, despite the notable price correlation, these underlying cryptocurrencies possess distinct features compared to BTC. Next, we direct our attention towards a specific category of tokens, specifically those within the DeFi sector. DeFi tokens operate within a distinct ecosystem that is specifically centered around decentralized financial applications and services. Unlike Bitcoin, which predominantly serves as a store of value and medium of exchange, DeFi tokens are purposefully designed to facilitate a wide range of financial activities, including lending, borrowing, trading, and yield farming. Furthermore, DeFi tokens often possess intrinsic utility within their corresponding decentralized applications, enabling functionalities such as governance rights, staking rewards, and access to specific features or services within the DeFi ecosystem. As a result, the underlying market dynamics and factors influencing DeFi tokens may diverge from those affecting BTC and other major layer one native coins. This is further evident in the relatively low correlations observed between the prices of DeFi protocols and BTC, as well as the correlations between their respective market caps. Additionally, it is important to note that the DeFi space is still in its early stages, characterized by high volatility and potential regulatory uncertainties. In order to examine the exposure of DeFi to macroeconomic and financial conditions, as well as its differences from Bitcoin and major layer one cryptocurrencies, I analyze a price index and the combined market capitalization of two prominent and well-established DeFi protocols, namely Maker and Synthetix. However,

it's crucial to acknowledge that the time series data for the Maker and Synthetix protocols is considerably shorter compared to that of Bitcoin, as these protocols were launched in 2017 and 2018, respectively. This should be taken into consideration, as the price and market capitalization of Maker and Synthetix may not fully capture the relationship with macroeconomic and financial indicators accurately. Hence, I approach the analysis of these indices with caution, recognizing the potential biases that may exist and the possibility of incomplete assessments.

Table 4 presents the estimation results for the regression analysis of P_{MS} and M_{MS} on the independent variables in X . Similar to the relationship of gold with the price and hash rate of BTC, gold demonstrates statistical significance as a driving factor for the MS index price. The magnitude of the effect is comparable to that observed in BTC, indicating that a one percentage-point increase in the gold price corresponds to a 3.87 - 4.04 percent decrease in P_{MS} at daily frequencies and a 3.78 - 4.37 percent decrease at monthly frequencies. The impact of DXY on P_{MS} is consistently negative and statistically significant, mirroring the findings observed in the case of BTC. However, this effect is only significant for the FM-OLS estimator at the 10% level when considering daily frequency and for the D-OLS estimator at the 0.1% level when considering monthly frequency. Notably, the D-OLS regression with monthly data demonstrates a superior fit, yielding an R^2 value of 0.97 compared to 0.70 of the FM-OLS regression with daily data. Therefore, I consider the monthly D-OLS estimates, which can also help average out the daily data noise, to be more reliable and representative.

²⁰ This preference stems not only from the superior goodness of fit in the regression and

²⁰DeFi ecosystems have a smaller market size and adoption relative to BTC. They are newer and more

the nature of monthly data but also due to the suitability of D-OLS in addressing concerns for the short sample and missing variables. By incorporating leads and lags of independent variables and eliminating correlations with the error term, D-OLS better tackles these issues. This is reinforced by the similarity between the D-OLS estimated coefficients with monthly data and corresponding estimates of the Bitcoin price regression displayed in Table 2. While FFR appears to be statistically insignificant across all cases, $SP500$ exhibits a positive and statistically significant relationship with P_{MS} , except for the case of D-OLS with monthly data.

The relationship between the market capitalization of the MS index and the price of gold generally demonstrates a negative association, except in the case of the FM-OLS estimation using monthly data. Additionally, irrespective of estimation methods and data frequencies, the market capitalization of MS exhibits a consistently strong negative relationship with the DXY . Furthermore, the variable M_{MS} displays a strong association with both the Federal Funds Rate (FFR) and the S&P 500 when considering the D-OLS estimator with monthly data. However, estimates pertaining to the S&P 500 diverge between daily and monthly data. While the analysis of daily data suggests a positive relationship between M_{MS} and the S&P 500, the monthly D-OLS estimation indicates a negative relationship. This discrepancy can be attributed to the inherent noise present in daily data, compounded by the relatively short time series sample. For completeness, despite the limited sample size, we have included the estimation results for the regression analysis of $P_{\overline{MS}}$ and $M_{\overline{MS}}$ using rapidly evolving, encompassing their own unique characteristics. The dynamic nature of the DeFi space increases the likelihood of missing variables in the regression model. Additionally, the shorter time series sample limit the availability of comprehensive and reliable data.

daily data in Table A4 of the appendix. Estimates using monthly samples are not reported due to the extremely limited length of the time series, consisting of only 26 observations. The findings consistently demonstrate a negative influence of DXY on both $P_{\overline{MS}}$ and $M_{\overline{MS}}$, while gold exhibits a negative impact solely on $M_{\overline{MS}}$. In contrast to the case for P_{MS} , FFR exhibits a negative impact on $P_{\overline{MS}}$ at the 10% significance level, while $S\&P500$ demonstrates a positive influence on $M_{\overline{MS}}$, also at the 10% significance level. Overall, it is crucial to exercise caution and approach the interpretation of the results obtained from very short samples with care.

3.3 Dynamic impact of DXY and gold

Thus far, I have established the statistical significance of the price of gold and the DXY index in explaining the long run movement of the price, the market cap, and the hash rate of BTC, as well as the prices and market caps of major layer one cryptocurrencies and major DeFi protocols. Specifically, I have obtained estimates of the long run partial elasticities of the crypto measures with respect to DXY and $GOLD$. The finding is that in the long run both DXY and $GOLD$ exhibit a robust negative influence on the price and hash rate of BTC as well as the rest of the crypto metrics. This section is dedicated to exploring the dynamic impact of the influence of DXY and $GOLD$ on the variables P_B and H_B , utilizing the long-run estimated elasticities as a reference point. Given the similarity between the D-OLS and FM-OLS estimates, I opt to solely employ the D-OLS estimates for this analysis. I represent the D-OLS fitted values of the gold price and the DXY index as $\hat{\beta}_{i,G}GOLD$ and $\hat{\beta}_{i,D}DXY$, respectively. Here, $\hat{\beta}_{i,D}$ and $\hat{\beta}_{i,G}$ denote the estimated coefficients, where

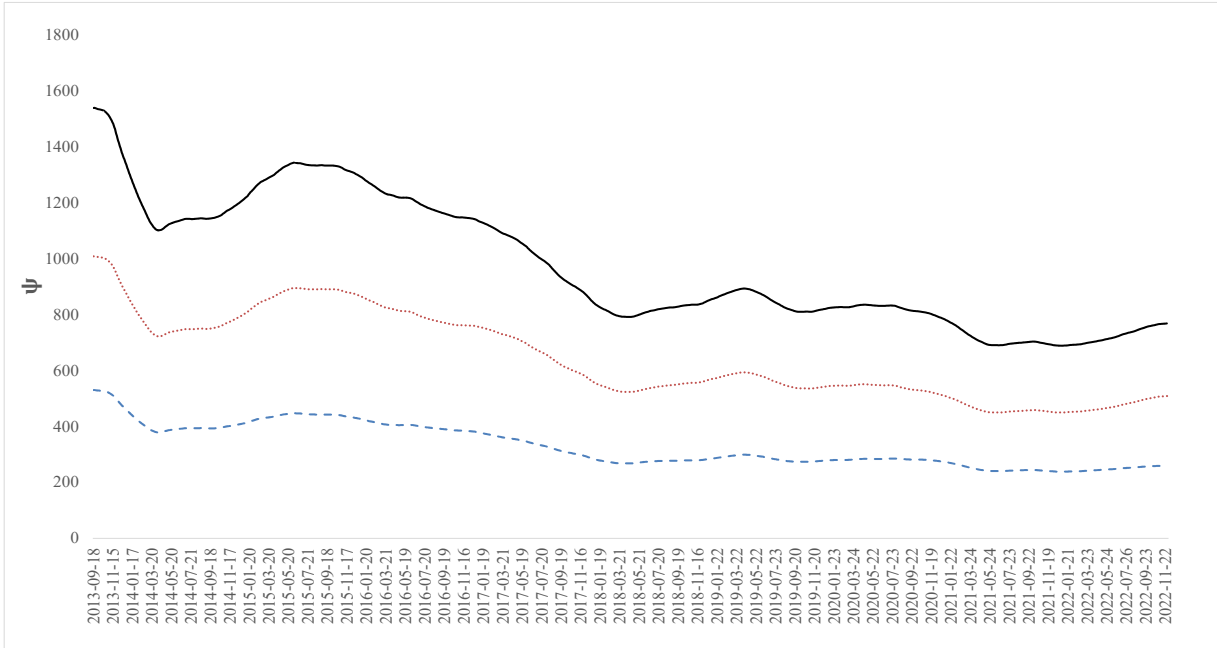
$i = B$ and $i = H$ correspond to the equations involving the BTC price and hash rate, respectively. Subsequently, I calculate adjusted measures of P_B and H_B that exclude the portions attributed to the long run effect of either DXY , $GOLD$, or both.²¹ The latter measures enable me to quantify the percentage shifts in P_B and H_B stemming from the influences of $GOLD$ and DXY . To put it differently, I ascertain the percentage long term alterations in P_B and H_B when $GOLD$, DXY , or both are omitted from the model that is,

$$\psi_{i,t}^G = -\frac{\hat{\beta}_{i,G}GOLD_t}{X_{B,t}}100, \psi_{i,t}^D = -\frac{\hat{\beta}_{i,D}DXY_t}{X_{B,t}}100, \psi_{i,t}^{G,D} = -\frac{\hat{\beta}_{i,G}GOLD_t + \hat{\beta}_{i,D}DXY_t}{X_{B,t}}100,$$

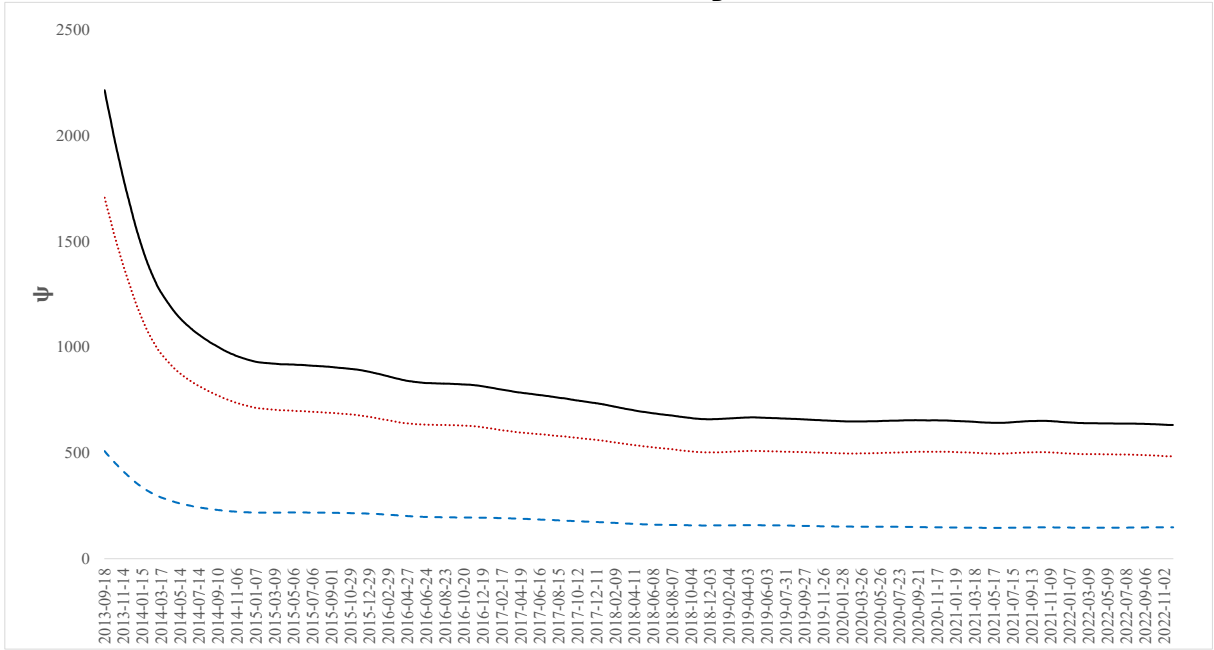
where $X = P$ with $i = B$, and $X = H$ with $i = H$. To simplify explanations, I will now refer to ψ_i^G , ψ_i^D , and $\psi_i^{G,D}$ as "omission ratios." Since our focus lies in understanding long-term effects, when analyzing the time series of these omission ratios, it is crucial to emphasize trends over static values. Static values become relevant primarily when comparing the contributions of gold and the DXY index at specific dates. To mitigate the impact of short-term fluctuations, I present the 100-day moving averages for the omission ratios. Given that the estimated elasticities $\hat{\beta}_{i,G}$ and $\hat{\beta}_{i,D}$ are strictly negative, a decreasing omission ratio over time suggests that the influence of the underlying factor(s) in explaining variations in the crypto metric is waning. Conversely, an increasing omission ratio implies that the contribution of the underlying factor(s) is strengthening over time. In Figure 4, you can observe the 100-day moving averages for the omission ratios for both the BTC price (I) and

²¹Respectively, $X_{B,t} - \hat{\beta}_{i,G}GOLD_t$, $X_{B,t} - \hat{\beta}_{i,D}DXY_t$ and $X_{B,t} - \hat{\beta}_{i,G}GOLD_t - \hat{\beta}_{i,D}DXY_t$, where $X = P$ with $i = B$, and $X = H$ with $i = H$.

its hash rate (II).



I. ψ_B^G — (blue), ψ_B^D ... (red), $\psi_B^{G,D}$ — (black)



II. ψ_H^D — (blue), ψ_H^G ... (red), $\psi_H^{G,D}$ — (black)

Figure 4: Percentage shifts of I. P_B and II. H_B due to DXY and $GOLD$

The initial observation drawn from Figure 4 is that the *DXY* index, in relation to the price of gold, is the primary factor influencing fluctuations in the BTC price, while the opposite holds true for the BTC hash rate. On average, the *DXY* index explains 95% more of the variation in the BTC price than the gold price, with a standard deviation of 4.92%. Conversely, the gold price, on average, accounts for 228% more variation in the BTC hash rate than the *DXY* index, with a standard deviation of 8.32%. Specifically, the *DXY*, causes a decline of 649% in the BTC price, while *GOLD* contributes to a 333% reduction. Likewise, *GOLD* causes a decrease of 639% in the BTC hash rate, compared to *DXY*'s contribution of 195%. The combined influence of *GOLD* and *DXY* leads to a decrease of 982% in the price and an 833% reduction in the hash rate.

The second observation drawn from the figure is the fact that the contribution of both factors to the variation in the BTC price and hash rate between the beginning and end of the sample decreases substantially. At the beginning of the sample, *DXY* and *GOLD* are jointly responsible for a 1460% reduction in the price of BTC while at the end of the sample they are jointly responsible for a 779% reduction. Likewise, at the beginning of the sample *DXY* and *GOLD* jointly reduce the price of BTC by 2711% while at the end of the sample they reduce it by 629%. Despite the prominent roles played by both *GOLD* and *DXY* in accounting for the fluctuations in P_B and H_B , their impact is gradually waning.

In summary, both *DXY* and *GOLD* significantly contribute to the decline in the price and hash rate of BTC. Specifically, *DXY* plays a pivotal role in the price reduction, whereas *GOLD* holds the primary responsibility for the hash rate decrease. The analysis indicates that while these two factors initially account for a substantial portion of the price and hash

rate reductions in BTC, their impact gradually diminishes.

4 Conclusion

In this research, I delved into the long-term impacts of macroeconomic and financial fundamentals on cryptocurrency metrics such as prices, market caps, and the hash rate of Bitcoin. The fact that the prices and market caps of most cryptocurrencies exhibit a robust correlation with the price of BTC, allows me to effectively narrow my focus on a small set of cryptocurrencies. To assess the long-run relationship of the latter with macroeconomic and financial fundamentals, I rely on indicators with daily available data such as the price of gold, the relative value of the US dollar as gauged by the DXY index, the S&P 500 index, and the federal funds rate. The long-term relationships are estimated employing both parametric (D-OLS) and non-parametric (FM-OLS) methods, yielding comparable results. Despite a high and positive Pearson correlation coefficient between BTC and gold prices, both the gold price and the DXY index consistently exhibit statistically significant adverse effects on BTC prices when accounting for other factors. These effects extend not only to the price and market cap of BTC, but also to the prices and market caps of other cryptocurrencies, and even the hash rate of BTC. The empirical evidence, combined with BTC's fixed supply, network security, and decentralization, further strengthens the notion of BTC as a digital alternative to gold—a store of value. However, disparities between gold and BTC interactions with the federal funds rate and the S&P 500 were observed. Moreover, BTC's response to the US dollar's value is notably amplified compared to gold. It is also noteworthy that the hash rate of Bitcoin is more sensitive to market dynamics compared to the price of BTC. The empirical

evidence further suggests that fluctuations in the value of the US dollar primarily influence the price of BTC, whereas fluctuations in the price of gold predominantly impact the hash rate of BTC. Nevertheless, the influence of these two factors as contributors to BTC metric variations tends to wane over time. In conclusion, this study unveils the intricate interplay between the price of gold and the relative value of the US dollar with cryptocurrency metrics, especially the price and hash rate of BTC. The findings illuminate Bitcoin's distinct status in the financial landscape, solidifying its reputation as a digital counterpart to a traditional store-of-value asset such as gold.

References

- [1] Almansour, B.Y., Almansour, A.Y., In'airat, M., 2020. The impact of exchange rates on bitcoin returns: Further evidence from a time series framework. *International Journal of Scientific and Technology Research* 9(2), 4577–4581.
- [2] Athey, S., Parashkevov, I., Sarukkai, V., Xia, J., 2016. Bitcoin Pricing, Adoption, and Usage: Theory and Evidence. Working Paper.
- [3] Barro, R.J., 1979. Money and the Price Level Under the Gold Standard. *The Economic Journal* 89 (353), 13–33.
- [4] Benigno, P., 2023. Monetary Policy in a World of Cryptocurrencies. *Journal of the European Economic Association* 21 (4), 1363–1396.

- [5] Benigno, G., Rosa, C., 2023. The Bitcoin–Macro Disconnect. Federal Reserve Bank of New York Staff Reports, no. 1052.
- [6] Benigno, P., Schilling, L.M., Uhlig, H., 2022. Cryptocurrencies, currency competition, and the impossible trinity. *Journal of International Economics* 136, 103601.
- [7] Biais, B., Bisiere, C., Bouvard, M., Casamatta, C., Menkveld, A.J., 2023. Equilibrium Bitcoin Pricing. *Journal of Finance* forthcoming
- [8] Bitstamp, 2022. Bitstamp Crypto Pulse.
- [9] Buterin, V., 2014. Ethereum: A Next-Generation Smart Contract and Decentralized Application Platform. Ethereum whitepaper.
- [10] Ciaian, P., Rajcaniova, M., d’A., Kancs, 2016. The economics of BitCoin price formation. *Applied Economics* 48(19),1799–815.
- [11] Carrick, J., 2016. Bitcoin as a complement to emerging market currencies. *Emerging Markets Finance and Trade* 52, 2321–2334.
- [12] Cong, L.W., He, Z., Li, J., 2021. Decentralized Mining in Centralized Pools. *Review of Financial Studies* 34 (3), 1191–1235.
- [13] Corelli, A., 2018. Cryptocurrencies and Exchange Rates: A Relationship and Causality Analysis. *Risks*, MDPI 6(4), 1-11.
- [14] Dwork, C., Naor, M. 1992. Pricing via processing or combatting junk mail.

- [15] Fernández-Villaverde, J., Sanches, D. R., 2019. Can Currency Competition Work? *Journal of Monetary Economics* 106, 1 - 15.
- [16] Garratt, R., Wallace, N., 2018. Bitcoin 1, bitcoin 2,: an experiment in privately issued outside monies. *Econ. Inq.* 56 (3), 1887–1897.
- [17] Gemini Global State of Crypto Report, 2022.
- [18] Glaser, F., Zimmermann, K., Haferkorn, M., Weber, M. C. , Siering, M., 2014. Bitcoin-asset or currency? Revealing users' hidden intentions. In *Twenty Second European Conference on Information Systems*, Tel Aviv.
- [19] Haber, S., Stornetta, W.S., 1991. How to time-stamp a digital document. *Journal of Cryptology* 3, 99–111.
- [20] Johansen, S., 2009. Cointegration: Overview and Development. *Handbook of Financial Time Series*, 671-693.
- [21] Konst, S., 2000. Secure log files based on cryptographically concatenated entries.
- [22] Kumar, S., 2022. Turn-of-the-month effect in cryptocurrencies. *Managerial Finance* 48 (5), 821-829.
- [23] Lee, Y., Rhee, J.H., 2022. A VECM analysis of Bitcoin price using time-varying cointegration approach. *Journal of Derivatives and Quantitative Studies* 30 (3).
- [24] Nakamoto, S., 2008. Bitcoin: A Peer-to-Peer Electronic Cash System.

- [25] Newey, W.K. , West, K.D. , 1994. Automatic Lag Selection in Covariance Matrix Estimation. *Review of Economic Studies* 61, 631–653.
- [26] Pagnotta, E., 2022. Decentralizing Money: Bitcoin Prices and Blockchain Security. *Review of Financial Studies* 35 (2), 866 – 907.
- [27] Phillips, P.C.B, Hansen, B.E., 1990. Statistical Inference in Instrumental Variables Regression with I(1) Processes. *Review of Economic Studies* 57 (1), 99–125.
- [28] Stock, J., Watson, M.W., 1993. A simple estimator of cointegrating vectors in higher order integrated systems. *Econometrica* 61(4), 783-820.
- [29] Schilling, L., Uhlig, H., 2019. Some simple bitcoin economics. *Journal of Monetary Economics* 106, 16 - 26.
- [30] Statista, 2022a. Total market capitalizations of domestic companies listed on stock exchanges worldwide from 2013 to June 2022.
- [31] Statista, 2022b. Share of Respondents Who Indicated They either Owned or Used Cryptocurrencies in 56 Countries and Territories Worldwide from 2019 to 2022.
- [32] Syafiqah, I., Basah, M.Y.A., 2021. An analysis on cryptocurrencies and macroeconomic variables using VECM, ASEAN. *Journal of Management and Business Studies* 3 (1), 8-15.
- [33] Szabo, N., 1996. Smart Contracts: Building Blocks for Digital Free Markets. *Extropy Journal of Transhuman Thought*, 16.

- [34] Szabo, N., 1997. Formalizing and Securing Relationships on Public Networks. First Monday, vol 2, number 9 - 1.
- [35] Szabo, N., 1998. Secure Property Titles with Owner Authority. Nick Szabo's Papers and Concise Tutorials.

Appendix

Table A1: Descriptive Statistics

	P_B	H_B	M_B	P_{BL}	M_{BL}	P_{MS}	M_{MS}	P_{MS}	M_{MS}
obs	2415	2415	2415	1347	1347	1185	1185	543	543
mean	11022	59594237	2.03E+11	12673	5.67E+11	855	1.62E+09	255	1.89E+10
median	4602	21739145	7.78E+10	7762	2.64E+11	573	8.08E+08	251	1.61E+10
max	67567	3.17E+08	1.27E+12	45457	2.14E+12	4419	8.15E+09	877	5.04E+10
min	68	67	7.78E+08	1559	7.01E+10	153	2.29E+08	60	1.63E+09
std. dev.	15667	73361272	2.96E+11	10789	5.34E+11	692	1.55E+09	140	1.18E+10
skewness	1.75	1.05	1.76	1.25	1.07	1.65	1.45	0.94	0.43
kurtosis	5.04	2.96	5.03	3.49	2.78	5.46	4.31	4.18	2.12

	DXY	$SP500$	$GOLD$	FFR
obs	2415	2415	2415	2415
mean	94	2772	1429	0.78
median	95	2630	1311	0.33
max	114	4797	2067	3.83
min	79	1573	1049	0.04
std. dev.	7	855	257	0.89
skewness	-0.39	0.71	0.73	1.08
kurtosis	3.39	2.37	2.06	3.11

Notes: All statistics were computed using raw daily data. The Jarque-Bera probability for all series is zero.

Table A2: Unit root tests - daily frequencies

	Level															
	no intercept				intercept & trend				no intercept				intercept & trend			
	ADF	PP	ADF	KPSS	ADF	PP	KPSS	ADF	PP	ADF	PP	KPSS	ADF	PP	KPSS	
P_B	1.26	1.35	-1.44	-1.30	5.48 ^a	-1.90	-1.70	0.26 ^a	-12.10 ^a	-50.97 ^a	-12.21 ^a	-50.93 ^a	-12.24 ^a	-50.92 ^a	0.08	
P_{MS}	-0.42	-0.42	-1.96	-1.94	1.26 ^a	-1.99	-1.96	0.40 ^a	-23.88 ^a	-36.74 ^a	-23.87 ^a	-36.73 ^a	-23.86 ^a	-36.72 ^a	0.09	
$P_{M\overline{MS}}$	-0.64	-0.65	-1.04	-1.14	1.14 ^a	-1.79	-1.86	0.55 ^a	-25.05 ^a	-25.02 ^a	-25.04 ^a	-25.01 ^a	-25.08 ^a	-25.06 ^a	0.02	
M_{MS}	0.36	0.33	-1.47	-1.50	3.08 ^a	-1.56	-1.66	0.41 ^a	-37.13 ^a	-37.13	-37.12 ^a	-37.12 ^a	-37.12 ^a	-37.12 ^a	0.08	
$M_{M\overline{MS}}$	0.79	0.80	-2.53	-2.54	0.55 ^b	-2.57	-2.60	0.55 ^a	-23.50 ^a	-23.50 ^a	-23.52 ^a	-23.52 ^a	-23.89 ^a	-23.89 ^a	0.17 ^b	
H_B	1.95	3.77	-9.87 ^a	-6.90 ^a	5.25 ^a	-6.98 ^a	-4.59 ^a	0.98 ^a	-4.93 ^a	-102.24 ^a	-5.77 ^a	-112.30 ^a	-7.18 ^a	-117.31 ^a	0.27 ^a	
DXY	1.25	1.24	-1.42	-1.46	2.36 ^a	-1.76	-1.82	0.58 ^a	-21.46 ^a	-48.90 ^a	-21.50 ^a	-48.94 ^a	-21.50 ^a	-48.93 ^a	0.10	
$SP500$	2.13	1.90	-1.02	-1.07	5.67 ^a	-3.27 ^c	-3.40 ^c	0.39 ^a	-10.06 ^a	-56.48 ^a	-10.29 ^a	-56.60 ^a	-10.29 ^a	-56.59 ^a	0.03	
$GOLD$	0.36	0.37	-1.05	-1.03	4.41 ^a	-3.04	-3.03	0.96 ^a	-50.48 ^a	-5.48 ^a	-50.48 ^a	-50.48 ^a	-12.27 ^a	-50.49 ^a	0.07	
FFR	1.72	1.89	0.89	1.03	1.32 ^a	0.27	0.37	0.57 ^a	-15.79 ^a	-51.94 ^a	-15.87 ^a	-51.98 ^a	-15.98 ^a	-52.05 ^a	0.37 ^a	

Notes: All variables except from FFR and UNE are expressed in natural logarithms. The table reports the Augmented Dickey-Fuller t-statistic, the Phillips-Perron adjusted t-statistic and the Kwiatkowski-Phillips-Schmidt-Shin (KPSS) LM statistic. For the Augmented Dickey-Fuller (ADF) test, the lags are determined using the Akaike Info Criterion (AIC). For the PP and the KPSS tests, I use the Bartlett kernel for the spectral estimation method, while the Newey-West bandwidth is selected using the method proposed by Newey and West (1994) which involves computing an optimal bandwidth that minimizes the mean squared error (MSE) of the estimated variance. The null hypothesis for the ADF and PP tests is that the series has a unit root while the null hypothesis for the KPSS test is that the series is stationary. Statistical significance is reported as follows: ^a 1% level, ^b 5% level, ^c 10% level.

Table A3: Unit root tests - monthly frequencies

	Level												First-differences					
	no intercept			intercept			intercept & trend			no intercept			intercept			intercept & trend		
	ADF	PP	KPSS	ADF	PP	KPSS	ADF	PP	KPSS	ADF	PP	KPSS	ADF	PP	KPSS	ADF	PP	KPSS
P_B	0.97	1.19	1.18 ^a	-1.57	-1.30	1.18 ^a	-2.45	-2.02	0.078	-6.89 ^a	-6.92 ^a	0.10	-7.06 ^a	-7.04 ^a	0.10	-7.09 ^a	-7.05 ^a	0.07
P_{MS}	-0.41	0.35	0.29	-1.94	-1.72	0.29	-1.94	-1.70	0.11	-2.99 ^a	-7.54 ^a	0.12	-2.97 ^b	-7.48 ^a	0.12	-2.96	-7.43	0.11
M_{MS}	0.36	0.48	0.65 ^b	-1.41	-1.38	0.65 ^b	-1.63	-1.43	0.11	-6.27 ^a	-6.27 ^a	0.14	-6.24 ^a	-6.24 ^a	0.14	-6.21 ^a	-6.21 ^a	0.12
H_B	0.83	1.85	1.17 ^a	-5.01 ^a	-6.06 ^a	1.17 ^a	-5.82 ^a	-4.59 ^a	0.27 ^a	-2.90 ^b	-2.39 ^b	0.68 ^b	-3.12 ^b	-3.06 ^b	0.68 ^b	-4.15 ^a	-4.47 ^a	0.14 ^c
DXY	1.04	1.20	0.59 ^b	-2.33	-1.46	0.59 ^b	-2.72	-1.95	0.15 ^b	-7.36 ^a	-7.50 ^a	0.09	-7.43 ^a	-7.56 ^a	0.09	-7.39 ^a	-7.53 ^a	0.09
$SP500$	2.35	2.54	1.20 ^a	-1.07	-1.07	1.20 ^a	-2.41	-2.55	0.12	-9.53 ^a	-9.53 ^a	0.08	-8.37 ^a	-9.90 ^a	0.08	-8.37 ^a	-9.86 ^a	0.07
$GOLD$	0.49	0.42	0.92 ^a	-0.93	-0.78	0.92 ^a	-2.75	-2.78	0.23 ^a	-8.35 ^a	-8.15 ^a	0.25	-8.33 ^a	-8.11 ^a	0.25	-8.36 ^a	-8.12 ^a	0.11
FFR	-0.50	0.02	0.33	-1.63	-0.84	0.33	-2.25	-1.27	0.14 ^c	-0.34	-3.81 ^a	0.19	-0.48	-4.04 ^a	0.19	-0.62	-4.25 ^a	0.13 ^c

Notes: All variables except from FFR are expressed in natural logarithms. The table reports the Augmented Dickey-Fuller t-statistic, the Phillips-Perron adjusted t-statistic and the Kwiatkowski-Phillips-Schmidt-Shim (KPSS) LM statistic. For the Augmented Dickey-Fuller (ADF) test, the lags are determined using the Akaike Info Criterion (AIC). For the PP and the KPSS tests, I use the Bartlett kernel for the spectral estimation method, while the Newey-West bandwidth is selected using the method proposed by Newey and West (1994) which involves computing an optimal bandwidth that minimizes the mean squared error (MSE) of the estimated variance. The null hypothesis for the ADF and PP tests is that the series has a unit root while the null hypothesis for the KPSS test is that the series is stationary. Statistical significance is reported as follows: ^a 1% level, ^b 5% level, ^c 10% level.

Table A4: Estimation of the long-run relationships, P_{MS} & M_{MS}

	P_{MS} (daily)		M_{MS} (daily)	
	D-OLS	FM-OLS	D-OLS	FM-OLS
FFR	-0.21 ^d (0.12)	-0.22 ^d (0.12)	-0.089 (0.16)	-0.10 (0.14)
SP500	1.35 (1.43)	0.90 (1.43)	3.35 ^d (1.79)	2.83 ^d (1.69)
GOLD	-1.48 (1.49)	-1.85 (1.49)	-9.26 ^a (1.87)	-10.35 ^a (1.76)
DXY	-7.29 ^c (3.53)	-9.00 ^c (3.54)	-13.71 ^b (4.47)	-15.84 ^a (4.19)
C	38.27 (31.47)	52.31 ^d (31.51)	126.49 ^b (39.47)	148.47 ^a (37.27)
Trend	0.002 (0.002)	0.003 (0.002)	0.004 ^c (0.002)	0.005 ^b (0.002)
adj R^2	0.73	0.72	0.81	0.79
Lags (AIC)	0		3	
Leads (AIC)	0		0	

Notes: The sample is daily and spans from 5 October 2020 to 30 November 2022 (543 observations). All regressions utilize robust Newey-West standard errors which are reported in parentheses. Lags and leads for D-OLS are chosen based on the Akaike information criterion (AIC). All three estimation approaches use the Bartlett kernel for calculating the long-run variance. The significance levels are denoted by 'a' for 0.1%, 'b' for 1%, 'c' for 5% and 'd' for 10%.