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The effect of classroom rank on learning throughout elementary school: experimental evidence from Ecuador

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Economic
and Social
Research Council

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Abstract

We study the impact of classroom rank on children's learning using a unique experiment from Ecuador. Within each school, students were randomly assigned to classrooms in every grade between kindergarten and 6th grade. Students with the same ability can have different classroom ranks because of the (random) peer composition of their classroom. Children with higher beginning-of-grade classroom rank have significantly higher test scores at the end of that grade. The impact of classroom rank is larger for younger children and grows over time. Higher classroom rank also improves executive function, child happiness, and teacher perceptions of student ability.

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1. Introduction

There are many settings in economics where relative rank concerns are important. They emerge naturally in tournaments (Lazear and Rosen 1981), they affect job satisfaction (Card et al. 2012), and can interact in interesting ways with social preferences (Bandiera et al. 2005). Although the idea that rank is important in education dates back to Marsh (1987), recent years have seen a growing literature quantifying its importance for a variety of outcomes (including Elsner and Isphording 2017 and 2018; Tincani 2018; Murphy and Weinhardt 2020; Elsner et al. 2021; Pagani et al. 2021; Comi et al. 2021; Bertoni and Nisticò 2023; Denning et al. 2023; Kiessling and Norris 2023; Delaney and Devereux 2022 provide an excellent survey of the recent literature), and showing medium- and long-term impacts on college major choice and attendance, earnings, and the probability of engaging in risky behaviors.²

In this paper, we investigate the impact of classroom rank on learning and other outcomes throughout elementary school. We use a unique experiment in elementary schools in Ecuador where, at the start of every grade, a cohort of students was randomly assigned across classrooms within a given school. Compliance with the random assignment was almost perfect, 98.9 percent on average over the 7 years of the experiment (Elsner et al. 2021 also explore random assignment of students to classrooms, although they consider higher education, whereas our focus is on elementary schools). Variation in peer groups resulting from randomly assigning students to classrooms means that two students with the same underlying ability and in the same school and grade will have different classroom ranks.

This experimental design generates substantial variation in classroom rank achievement, which we measure in percentiles (so rank is normalized to be between 0 and 1). For example, for individuals with median ability in their school (i.e., with a rank close to 0.5 within their school), classroom rank can be as low as 0.351 or as high as 0.593 depending on the classroom they are assigned to.³

We find that increasing a child's classroom rank at the start of a given grade, keeping own ability constant, raises end-of-grade achievement. Rank, however, is just a particular form of peer effects, which could influence outcomes in various ways. The experimental design we explore generates

² Existing papers show causal effects of rank on many domains. Murphy and Weinhardt (2020) and Cicala et al. (2018) show that rank can have positive effects on test scores in primary and secondary school. Elsner and Isphording (2017) and Elsner et al. (2021) document positive impacts of rank in high school on college enrolment and choice. Delaney and Devereux (2022) show that rank can partly explain the gender gap in the choice of STEM as a college major. In recent work, Denning et al. (2023) show that rank can also have long-term impacts on earnings later in life. Rank has also been shown to affect the likelihood of engaging in risky behaviors, as in Elsner and Isphording (2018). Pagani et al (2021) look at personality traits, Comi et al. (2021) focus on disruptive behaviours, and Kiessling and Norris (2023) study the relationship between rank and mental health.

³ Even for very high and very low levels of student ability, for which variation in rank is bound to be more limited, there can be rank differences of 0.1 (10 percentile points) or more depending on the classroom one is assigned to. This alleviates the type of concerns raised by Angrist (2014), who shows that experimental assignment of children to peer groups may generate weak variation in peer characteristics, making it difficult to study peer effects in those settings.

variation in other classroom-level characteristics that may affect learning. In order to isolate the impact of classroom rank from other peer influences, we estimate models that control for classroom-level characteristics in a flexible way, i.e. by including classroom fixed effects.

We show that the effects of classroom rank are entirely driven by classroom rank in math, rather than language. Focusing on classroom rank in math, we document that rank effects are concentrated in the upper half of the rank distribution. Consistent with this result, we also find that rank effects are larger for children with higher lagged achievement, for children who started kindergarten with higher levels of vocabulary and for children who attended preschool. We see no evidence that the effect of classroom rank varies with the gender of the child.

A central contribution of our paper is the focus on differences in the effects of classroom rank by grade, and how these evolve over time. For this purpose, we divide our sample into children in “early” grades (1st and 2nd grades), “middle” grades (3rd and 4th grades) and “late” grades (5th and 6th grades) in elementary school. We first show that classroom rank effects are largest in the early grades: moving a child from the 50th to the 75th percentile of classroom rank in 1st or 2nd grade increases her end-of-grade achievement by more than 1 percentile point of national achievement, while classroom rank in 5th and 6th grades has no effect on achievement. We reject the null that rank effects are the same in early, middle, and late grades (p -value=.025).

Our analysis then turns to the evolution of classroom rank effects over time. We show, remarkably, that the effects of early classroom math rank increase substantially as children age. After 4 lags the effect of classroom rank in 1st or 2nd grade is almost twice as large as it was originally. This result stands in sharp contrast with the effects of many other determinants of achievement, which tend to fade out.⁴

The fact that the medium-term effects of early classroom rank in math are larger than the short-term effects could occur for a number of reasons. One possibility is that students randomly assigned a high classroom rank in 1st (or 2nd) grade benefit from a virtuous cycle, where a high rank in grade t leads to higher learning and higher rank in grade $t + 1$, which in turn lead to higher learning and higher ranks in the following grades. We find, however, that our estimates are more consistent with an alternative model where, in addition to its direct effect on achievement, early math rank affects an unobserved trait—for example, academic self-concept—which affects learning in later grades, and which does not depreciate over time.

⁴ See, for example, Chetty, Friedman, and Rockoff (2014), and Jacob, Lefgren, and Sims (2010) for estimates of the fade-out of the effects of teacher quality, measured by teacher value added. For a review and discussion of fade-out in education interventions, with a particular focus on early childhood, see Bailey et al. (2020). For a recent example from a setting similar to ours, see Barrera-Orsorio et al. (2020) on the fade-out of information on student performance provided to parents in Colombia.

With this insight, we turn to other child outcomes. Between 1st and 4th grades, we collected data on child executive function (EF). EF refers to a set of skills that allow individuals to plan, focus attention, remember instructions, and juggle multiple tasks. It includes working memory, inhibitory control, and cognitive flexibility (Center for the Developing Child 2019). Executive function in childhood has been shown to predict a variety of outcomes in adulthood, including performance in the labor market, involvement in criminal activities, and health status, even after controlling for socioeconomic status in childhood (Moffitt et al. 2011). We show that randomly assigning a child to a classroom where her rank is higher during the early grades improves her executive function in the medium term.

We also have data on a number of non-cognitive outcomes. At the end of 1st grade, we asked children whether they were happy in school, and at the end of 6th grade, we collected data on child depression, self-esteem, grit, and growth mindset. We show that children with higher math classroom rank (at the start of 1st grade) are more likely to say they are always happy (at the end of that grade). However, we do not find significant impacts of classroom rank on non-cognitive skills measured at the end of 6th grade.

Finally, we analyze whether classroom rank affects teacher perceptions of whether each student ranks at the top or bottom of the class, which is another unique feature of our data. These perceptions are correlated with actual student ranks in test scores, but the correlation is not perfect, either because of measurement error, or because teacher perceptions reflect other student attributes beyond their performance on the test. Teacher perceptions of student ability or performance could be important if, for example, teachers pay more attention to children they consider higher-achieving—and if such teacher reactions, in turn, affect future achievement. We show that, controlling for own lagged achievement, students who have a higher classroom rank in one grade are more likely to be perceived to be at the top of the class (and less likely to be thought to be at the bottom of the class) by their teachers in subsequent grades.

In sum, children with higher classroom rank have higher end-of-grade achievement. The effects of early classroom rank in math in 1st and 2nd grade increase substantially over time. More highly ranked children also have higher executive function, exhibit higher levels of happiness, and are thought to be higher-achieving by their future teachers.

Our paper extends the economics literature on the impacts of rank in important ways. First, ours is the first paper that analyzes rank effects in elementary education using an experiment with multiple rounds of random assignment, with essentially perfect compliance, although Elsner et al. (2021) also explore the naturally occurring random assignment of students to college classes. The fact that we have

data on children randomly assigned to different classrooms in every grade in elementary school means that we can convincingly test whether classroom rank has larger effects in some grades than in others.

Second, because we follow children over the entire elementary school cycle, we can credibly estimate how the effects of classroom rank evolve over time. As we show, both of these considerations—differences across grades and changes in the impact of classroom rank over time—are important, at least in the setting that we study.

In addition, we have unusually rich data on, executive function, happiness, depression, self-esteem, grit, growth mindset and, more uniquely, of teacher perceptions of student ability. This helps us understand how teachers perceive rank, and how these perceptions may mediate the impact of student rank on outcomes.

Finally, unlike most of the literature on this topic, we conduct this study in a developing country context. In our setting, children come from very poor families, and they perform 1.7 standard deviations below the norm on a standardized vocabulary score (the TVIP, which is the Spanish language version of the Peabody Picture Vocabulary Test). This setting allows us to examine whether the magnitude of the impacts of rank on student outcomes observed in richer countries are similar in a context such as ours, where the perceptions of rank by students, families and teachers may be different than in much wealthier countries, as well as their reactions to such perceptions.

The rest of the paper proceeds as follows. In section 2 we describe the setting and data, in section 3 we discuss our empirical strategy. Results are in section 4, and we conclude in section 5.

2. Setting and data

A. Experimental setting and descriptives

We study the acquisition of math, language, executive function, and non-cognitive skills in Ecuador, a middle-income country in South America. As is the case in most other Latin American countries, educational achievement of young children in Ecuador is low (Berlinski and Schady 2015).

The data we use come from an experiment in 202 schools.⁵ Schools have at least two classrooms per grade (most have exactly two). An incoming cohort of children was randomly assigned to kindergarten classrooms within schools in the 2012 school year. These children were reassigned to 1st grade classrooms in 2013, to 2nd grade classrooms in 2014, to 3rd grade classrooms in 2015, to 4th grade classrooms in 2016, to 5th grade classrooms in 2017, and to 6th grade classrooms in 2018. Compliance with the assignment rules was very high—98.9 percent on average.

⁵ Araujo et al. (2016) discuss in detail the selection of schools in this study. They show that the characteristics of students and teachers in our sample are very similar to those of students and teachers in a nationally representative sample of schools in Ecuador.

Random assignment means that we can effectively deal with concerns about any purposeful matching of students with teachers and peers that often arise in non-experimental settings. We provide further details on the classroom assignment rules and compliance with randomization in Appendix A.

We have baseline data on maternal education, household wealth, whether a child attended preschool, and her vocabulary skills at the beginning of kindergarten. Table 1, Panel A, provides summary statistics for children in our sample. The table shows that children were 5 years of age on the first day of kindergarten, on average, and half of them are girls. Mothers were in their early 30s and fathers in their mid-30s. Both parents had on average just under 9 years of schooling, which corresponds to completed middle school. The average receptive vocabulary score of children in the sample is 1.7 SDs below the level of children that were used to norm the sample for the test.⁶

Table 1, Panel B, summarizes characteristics of classrooms and teachers. Average class size is 38. The average teacher in the sample has 18 years of experience. Eighty-two percent of teachers are women, and 82 percent are tenured. An important consideration in interpreting our results is that there is always one teacher per classroom, without a classroom aide, and that the same teacher is responsible for all academic subjects (all subjects other than physical education and, when they are available, art and music).

We collected data on math and language achievement at the end of each grade between kindergarten and 6th grade. For both subjects, tests were a mixture of material that teachers were meant to have covered explicitly in class—for example, in math, addition or subtraction; material that would have been covered, but probably in a somewhat different format—for example, simple word problems; and material that would not have been covered at all in class but that has been shown to predict current and future math achievement—for example, the Siegler number line task.⁷ We aggregate responses in math and, separately, language, by Item Response Theory (IRT), and calculate an average achievement score that gives the same weight to math and language.⁸

In every grade between kindergarten and 4th grade, we tested child executive function. EF includes a set of basic self-regulatory skills which involve various parts of the brain, but in particular the prefrontal

⁶ To measure baseline receptive vocabulary, we use the *Test de Vocabulario en Imágenes Peabody* (TVIP) (Dunn et al. 1986), the Spanish-speaking version of the much-used Peabody Picture Vocabulary Test (PPVT). The TVIP was normed on samples of Mexican and Puerto Rican children. It has been used widely to measure development among Latin American children. See Paxson and Schady (2007) for a comparison of vocabulary scores between children in Ecuador and the U.S., and Schady et al. (2015) for evidence on levels and socioeconomic gradients in the TVIP in five Latin American countries, including Ecuador.

⁷ The number line task works as follows. Children are shown a line with the two clearly marked endpoints—for example, in 1st grade, the left end of the line is marked with a 0, and the right end is marked with a 20. They are then asked to place various numbers on the line—for example, the number 2 or the number 18. The accuracy with which children place the numbers has been shown to predict general math achievement (see Siegler and Booth 2004).

⁸ Our results are very similar if, instead, we calculate a simple sum of correct responses within blocks of questions on the test, and give equal weight to each of these test sections (as in Araujo et al. 2016).

cortex.⁹ Executive function is generally thought of as having three domains: working memory, inhibitory control, and cognitive flexibility. It is an important determinant of how well young children adapt to and learn in school. Basic EF skills are needed to pay attention to a teacher; wait to take a turn or raise one's hand to ask a question; and remember steps in, and shift from one approach to another, when solving a math problem, among many other tasks that children are expected to learn and carry out in the classroom. Children with high EF levels are able to concentrate, stay on task, focus, be goal-directed, and make good use of learning opportunities. Low levels of EF are associated with low levels of self-control and “externalizing” behavior, including disruptive behavior, aggression, and inability to sit still and pay attention, which affects a child's own ability to learn, as well as that of her classmates (Séguin and Zelazo 2005).¹⁰

At the end of each grade, we asked teachers who were the 5 children with the highest achievement, and 5 with the lowest achievement.¹¹ In 1st grade, we asked children whether they were happy in school and in their classroom (two separate questions). In both cases, children had the option of answering “always”, “sometimes”, or “never”. Most children in the sample answered “always” to both questions, so we use their responses to construct a single variable for children who were always happy, almost always happy, or mostly happy.

In 6th grade, we collected data on child depression, self-esteem, growth mindset, and grit. To measure child depression, we used the Patient-Reported Outcomes Measurement Information System (PROMIS) Depression Scale for children aged 11-17 years, developed by the American Psychiatric Association.¹² To measure self-esteem, we selected 5 questions from the National Longitudinal Study of

⁹ Volumetric measures of prefrontal cortex size predict executive function skills; children and adults experiencing traumatic damage to the prefrontal cortex sustain immediate (and frequently irreversible) deficits in EF (Nelson and Sheridan 2011, cited in Obradovic et al. 2012).

¹⁰ Working memory measures the ability to retain and manipulate information; for example, 2nd grade child were asked to remember (increasingly long) strings of numbers and repeat them in order and then backwards. Cognitive flexibility measures the ability to shift attention between tasks and adapt to different rules; for example, 1st grade children were shown picture cards that had trucks or stars, red or blue, and were asked to first sort cards by *shape* (trucks versus stars), and then by *color* (red versus blue). Inhibitory control refers to the capacity to suppress impulsive responses; for example, kindergarten children were quickly shown a series of flash cards that had either a sun or a moon and were asked to say the word “day” when they saw the moon and “night” when they saw the sun. We calculate scores on each of the three domains in executive function, as well as a measure of overall EF scores that gives one-third of the weight to each individual domain. We do not have data on inhibitory control in 1st grade. In this grade, the overall measure of executive function includes only cognitive flexibility and working memory, with equal weight given to both.

¹¹ Importantly, these data are not disaggregated by subject—that is, we did not ask teachers who they thought were top and bottom performers in math and, separately, in language.

¹² Olinio et al. (2013), Klein et al. (2005), and Aylward et al. (2008) argue that the PROMIS depression scale has superior qualities (greater precision, more internal reliability, and more discriminant validity) than other commonly-used depression scales, including the Beck Depression Inventory (BDI), the Children's Depression Inventory (CDI), and the Center for Epidemiologic Studies-Depression (CES-D) scale.

Adolescent to Adult Health (Add Health).¹³ To measure Growth Mindset, we selected 10 of the 20 questions on the Dweck “Mindset Quiz”; growth mindset refers to the belief that intelligence is malleable, rather than fixed, and can be increased with effort (Blackwell, Trzesniewski, and Dweck 2007; Dweck 2008). Finally, to measure grit, we adapted 4 questions from the 8-item Grit Scale for children (Duckworth and Quinn 2009); grit refers to the capacity of individuals to persevere at a given task. For each of these 6th grade outcomes, we aggregated responses by factor analysis. We also calculate an overall non-cognitive score that gives the same weight to each of the individual tests.

Most of the tests were applied to children individually (as opposed to in a group setting) by specially trained enumerators.¹⁴ All tests, other than the non-cognitive tests applied in 6th grade, were applied in school. For all tests, to choose questions, we piloted the test; made changes as necessary; and selected questions that could be understood by children in our context, and which showed reasonable levels of variability in the pilot. Further details on child assessments are provided in Appendix B.

B. How much variation is there across classroom rank within school?

A potential concern could arise if there is limited variation in classroom rank across students with the same ability who are assigned to different classrooms as a result of the randomization. As illustrated in Angrist (2014), experimental designs that rely on random assignment of individuals to groups to identify peer effects may suffer from modest variation in peer characteristics, resulting in identification issues that are akin to a weak instruments problem. This empirical concern potentially applies to our setting, as we rely on random assignment of students to classrooms within schools to identify the causal effect of classroom rank on learning.

We show however that, in practice, our empirical work does not suffer from this problem. This problem is more likely to emerge in linear in means models that regress student outcomes on average peer characteristics. It is less important for examining the role of rank, which depends on the whole distribution of student characteristics in the classroom, and not only on its mean. In our dataset, two students with the same ability rank who attend the same school can have quite different classroom ranks.

We can graphically illustrate this point by plotting the distribution of classroom rank for students with the same level of ability, measured by an index of math and language. Figure 1, Panel A, relies on 1st grade data, and shows quantiles of the distribution of classroom rank (y-axis) for students with a given school rank (x-axis). In practice, to construct this figure, we plot different percentiles of classroom rank within each school rank ventile.

¹³ See Harris and Udry 2018 for a description of the Add Health data. The questions on self-esteem in Add Health build on the much-used Rosenberg Self-Esteem Scale (Rosenberg 1989).

¹⁴ The only exception is some of the achievement tests in 4th through 6th grades, which were applied in a group setting.

The figure shows that two 1st grade students with the same ability in the same school (and therefore, the same school rank), can have very different classroom ranks. For example, within the 10th ventile of school rank (with median value equal to 0.477), classroom rank varies between 0.351 (5th percentile) and 0.593 (95th percentile).

Another way to illustrate the same point is to plot percentiles of classroom rank against the residuals of a regression of national percentile rank in the math and language index (our measure of underlying ability) on school fixed effects. This is another way of normalizing ability within school (in Panel A, this was done by using school rank instead of actual test scores). The resulting figure is shown in Figure 1, Panel B, where we plot different percentiles of classroom rank within residualised national rank ventiles. Within the 10th ventile of residualised national rank, classroom rank varies between 0.322 (5th percentile) and 0.641 (95th percentile). A similar pattern is shown in Appendix Figures C1 and C2 for all other grades.

Another potential concern is that the students' perception of rank does not necessarily coincide with the measure of rank we use. This is an issue in this whole literature, and we do not have anything new to add. As argued in Murphy and Weinhardt (2020), the literature in psychology has established that students have accurate perceptions of their rank in a group even if they do not know their absolute ability. Furthermore, if individuals did not know their rank, we would not see an impact of rank on outcomes as we find in our paper, and as has been found in other papers on this subject.¹⁵

3. Empirical strategy

A. Main model

Our goal is to estimate the impact of child i 's classroom rank on her subsequent learning in elementary school. The dataset we use allows us to construct measures of classroom rank, lagged achievement, and achievement at the end of the current grade for children between 1st and 6th grades. With these data, we can investigate the impact of classroom rank in the short- and medium-run, starting as early as 1st grade.¹⁶

To begin our discussion, we focus on two questions. First, how should we measure rank, and which measure of rank is likely to be more relevant for future learning? Second, how do we identify the causal impact of rank on learning? The two issues are interlinked in our setting, so we discuss them together.

¹⁵ That said, it is true that the problem is one of measurement error, since objective rank may not correspond to perceived rank by students, families or teachers, which they use to make decisions, so our estimates could be biased. In fact, it is possible that multiple perceptions of rank on the same student by different individuals, families and teachers, are not only different from each other, but also operate in different ways.

¹⁶ We can construct measures of math and language achievement at the end, but not the beginning, of kindergarten. For this reason, our analysis focuses on 1st through 6th grades.

In the experiment we study, in each school, children were randomly assigned to classrooms at the start of every grade. As a result, every student has a randomly-assigned set of peers in each grade, so two students with the same underlying ability can nevertheless have different classroom ranks. Our study exploits this variation by estimating the impact of rank at the beginning of grade t on learning at the end of grade t , as well as on learning in subsequent grades (until the end of 6th grade). Achievement at the start of grade t is measured using tests administered at the end of grade $t - 1$. Beginning-of-grade classroom rank for each student is based on her achievement at the end of $t - 1$ and the achievement of her randomly-assigned classmates. From now on, we refer to this measure simply as classroom rank.¹⁷

Our approach assumes that students and teachers react to the beginning-of-grade student classroom rank. This makes most sense if they can perceive their rank, and act on it, fairly early during the school year. While we are not able to assess the impact of school rank as convincingly, since random assignment happens within schools, in Appendix G we explore impacts of school rank of achievement.

Throughout the paper we denote $Y_{i,s,c,t}$ as student i 's performance (measured by an index of math and language scores), at the end of grade t , in school s , and classroom c . To be consistent with the literature, we define $Y_{i,s,c,t}$ in terms of percentiles of national rank.¹⁸ $CR_{i,s,c,t}$ is student i 's classroom rank at the start of grade t , when the student is randomly assigned to classroom c . In our simplest model, we pool observations from all grades and estimate:

$$Y_{i,s,c,t} = \beta CR_{i,s,c,t} + g_t(Y_{i,s,c,t-1}) + \delta_{c,t} + \varepsilon_{i,s,c,t} \quad (3.1)$$

where $\delta_{c,t}$ is a classroom (by grade) fixed effect and $\varepsilon_{i,s,c,t}$ is a residual. This specification also allows us to address any concerns related to the fact that our experimental design generates variation in multiple factors (other than classroom rank) that could affect learning. This specification is analogous to the main approach in Murphy and Weinhardt (2020). As explained in their paper, there is variation in rank across individuals assigned to different classrooms that one can exploit even after accounting for classroom fixed effects, due to differences in the distribution of ability across classrooms.¹⁹

¹⁷ One issue we face is that we only observe end of grade $t - 1$ scores for students who were in a school in our sample in grade $t - 1$, which means that we do not know what these test scores are for students who arrived at the school in grade t . Therefore, we cannot compute grade t ranks for these students, and our measures of ranks for all other children ignore the fact that new entrants are in their classroom. This will introduce random measurement error in rank.

¹⁸ Percentile ranks normalize automatically by classroom (or school) size. The disadvantage of this is that being the first or last in a small or large classroom may mean something very different. In practice, however, we find no evidence that classroom rank measured in percentiles has different effects in smaller and larger classrooms.

¹⁹ Note that this is not equivalent to exploring within-classroom variation. In each classroom, individual ability and classroom rank are perfectly correlated, so one would not be able to estimate this model classroom by classroom (allowing

In this model, β is restricted to be the same across all grades, but all other parameters are allowed to be grade-specific. $g_t(Y_{i,s,c,t-1})$ is a third-order polynomial in $Y_{i,s,c,t-1}$.²⁰ We also estimate models in which, instead of pooling data for all six grades, we estimate separate coefficients on β for 1st and 2nd grades (“early” grades), 3rd and 4th grades (“middle” grades) and 5th and 6th grades (“late” grades).²¹

Next, we separately analyze the effects of classroom rank in math and language:

$$Y_{i,s,c,t}^k = \beta^k CR_{i,s,c,t}^k + g_t(Y_{i,s,c,t-1}^k) + \delta_{c,t}^k + \varepsilon_{i,s,c,t}^k \quad (3.2)$$

where the k superscript refers to a subject, math or language.

Up to this point, we have assumed that the effect of classroom rank on learning is linear in classroom rank. It is quite possible that this is not the case—it may be, for example, that rank has a different effect at the top and bottom of the (rank) distribution. Therefore, we also consider a version of equation (3.1) where the effect of classroom rank on learning is not constrained to be linear:

$$Y_{i,s,c,t} = \beta(CR_{i,s,c,t}) + g_t(Y_{i,s,c,t-1}) + \delta_{c,t} + \varepsilon_{i,s,c,t} \quad (3.3)$$

where $\beta(CR_{i,s,c,t})$ is now a flexible function of $CR_{i,s,c,t}$. In our preferred specification we discretize $CR_{i,s,c,t}$ into q values (forcing it to take $q = 10$ values, corresponding to 10 deciles of the distribution), so $\beta(CR_{i,s,c,t}) = \sum_{q=1}^{10} \beta_q CR_{i,s,c,t,q}$ (where $CR_{i,s,c,t,q}$ is an indicator variable that takes value 1 if $CR_{i,s,c,t}$ is in decile q).²²

B. Alternative models

Other papers in this literature use different measures of rank and different specifications. A leading example is Murphy and Weinhardt (2020), who study the impact of school rank at the end of elementary school on learning in secondary school. In contrast, we study the impact of classroom rank at the beginning of a

for classroom-specific parameters). The model is identified because it imposes that the impact of classroom rank is the same across classrooms. With this assumption, it would be identified even if we allowed for some restricted forms of interactive fixed effects, as in, for example, Bai (2009).

²⁰ As Murphy and Weinhardt (2020) emphasize, it is important to use flexible specifications for this function, to avoid the potential problem that β does not capture a true rank effect but is instead an artefact of the misspecification of this function. Our robustness checks show that considering polynomials in lagged scores of order higher than three, or controlling for lagged scores using percentiles of lagged national rank, does not lead to substantial changes in the results. For this reason, in our main empirical specification $g_t(Y_{i,s,c,t-1})$ is a cubic polynomial in its argument.

²¹ In Appendix E we also present estimates where β varies by grade in an unrestricted way, and therefore it is also indexed by t . Those estimates are noisier than the ones we focus on in the paper.

²² As pointed out by a referee, when the classroom rank of one student increases in a classroom the classroom rank of another student in the same classroom automatically decreases. This can induce another form of spillovers in the classroom. However, since we observe the classroom rank of every student, this is automatically accounted for in our models.

grade on learning occurring in that grade. Because in Murphy and Weinhardt (2020) rank is measured at the end of elementary school, it is a result of a student's position relative to her peers, but also of the student's reaction to her peers and any subsequent feedback, as well as other school shocks occurring between the beginning and the end of elementary school.²³ If we were to use the Murphy and Weinhardt (2020) specification instead of ours (and using classroom rank instead of school rank) we would estimate:

$$Y_{i,s,c,t} = \beta CR'_{i,s,c,t-1} + g_t(Y_{i,s,c,t-1}) + \delta_{c,t} + \varepsilon_{i,s,c,t} \quad (3.4)$$

where $CR'_{i,s,c,t-1}$ is the classroom rank at the end of grade $t - 1$, computed using scores at the end of $t - 1$ relative to peers in $t - 1$.

The main reason why we use equation (3.1), rather than (3.4), as our preferred specification is that it follows directly from our experimental design. Classroom ranks at the start of a grade are randomly assigned and cannot be modified by student effort or other unobserved shocks, whereas classroom ranks at the end of a grade are both a result of random assignment of peers, student effort, peer effort, and potentially even the responses of teachers and parents. Also, our approach estimates the effects of classroom rank experienced in the same year as we measure learning, which is arguably more relevant in the short run for a “big fish little pond” mechanism (as in Marsh 1987).²⁴ That said, students may not know their rank at the start of the grade and may take some time to learn about it. In contrast, in Murphy and Weinhardt (2020) students are more likely to have a reasonable perception of their rank since it is measured at the end of elementary school. Therefore, we present results from estimating (3.4) as a robustness check.

C. Dynamics

To estimate the dynamics of rank effects, we begin with specifications of the following form:

$$Y_{i,s,c,t+l} = \beta_{t,l} CR_{i,s,c,t} + g_{t+l}(Y_{i,s,c,t-1}) + \delta_{c,t} + \varepsilon_{i,s,c,t+l} \quad (3.5)$$

²³ Murphy and Weinhardt (2020) document the impact of this measure on future learning, when a student moves to another school and experiences a different set of peers. In their model students are motivated to work hard in secondary school because of the rank they experienced and perceived in their past school, as opposed to their rank in the current school.

²⁴ That said, one advantage of using end-of-grade rank in our setting would be that we can construct rank using everyone in the classroom at the end of the previous grade, while our preferred measure of beginning-of-grade rank excludes new school entrants for whom we do not have test scores at the end of the previous grade, introducing measurement error in our preferred measure of classroom rank (on average, 7.1 percent of students are new entrants in each classroom). However, as we show in the robustness checks below, our results are robust to a standard multiple imputation procedure for missing data.

We estimate these regressions separately for “early”, “middle”, and “late” grades, as discussed above. When $l = 0$, equation (3.5) is equivalent to (3.1) and provides estimates of the short-run impact of classroom rank at the start of grade t , $CR_{i,s,c,t}$, on learning at the end of that same grade, $Y_{i,s,c,t}$. We label this effect $\beta_{t,0}$. When $l > 0$, equation (3.5) provides estimates of the medium-term effect of classroom rank at various lags, which we label $\beta_{t,l}$.

$\beta_{t,l}$ (medium-run impact) and $\beta_{t,0}$ (short-run impact) are related through three main channels: (i) class rank in grade t affects learning at the end of that grade, and therefore also affects student achievement in grade $t + 1$ and in subsequent grades, through the function $g_{t+1}(Y_{i,s,c,t})$ in the $(t + 1)$ version of equation (3.1); (ii) since learning at the end of grade t is affected, classroom rank in $t + 1$ and subsequent grades is also affected, which can have a further impact on learning in those grades, captured by $\beta_{t+1,0}$ in equation (3.1); (iii) in addition, class rank in grade t may affect other skills not captured by our tests at the end of that grade (unobserved skills), but which nevertheless can affect learning in grades $t + 1$ and beyond.

To quantify the importance of these channels, we first estimate an additional equation relating classroom rank at the beginning of grade $t + 1$ with learning at the end of grade t , which we will assume can be approximated by the following linear relationship:

$$CR_{i,s,c,t+1} = \delta_{t+1} + \gamma_{t+1}Y_{i,s,c,t} + \tau_{c,t+1} + \eta_{i,s,c,t+1} \quad (3.6)$$

where $\tau_{c,t+1}$ is a classroom fixed effect, and $\eta_{i,s,c,t+1}$ is the variation coming from random assignment of students to different peer groups. In practice, as we show below, when $Y_{i,s,c,t}$ is the national percentile rank, $\gamma_{t+j} \approx 1$.

Suppose, for simplicity, that $g_t(Y_{i,s,c,t-1})$ is also linear: $g_t(Y_{i,s,c,t-1}) = \lambda_t Y_{i,s,c,t-1}$. Taking equations (3.1) and (3.6) together, and assuming that all medium-term impacts of rank on learning operate through observed tests scores and observed rank:

$$\begin{aligned} \frac{\partial Y_{i,s,c,t}}{\partial CR_{i,s,c,t}} &= \beta_{t,0} \\ \frac{\partial Y_{i,s,c,t+1}}{\partial CR_{i,s,c,t}} &= \left(\frac{\partial Y_{i,s,c,t+1}}{\partial CR_{i,s,c,t+1}} \frac{\partial CR_{i,s,c,t+1}}{\partial Y_{i,s,c,t}} + \frac{\partial Y_{i,s,c,t+1}}{\partial Y_{i,s,c,t}} \right) \frac{\partial Y_{i,s,c,t}}{\partial CR_{i,s,c,t}} \\ &= (\beta_{t+1,0} \gamma_{t+1} + \lambda_{t+1}) \beta_{t,0} \end{aligned}$$

Similarly:

$$\frac{\partial Y_{i,s,c,t+2}}{\partial CR_{i,s,c,t}} = (\beta_{t+2,0} \gamma_{t+2} + \lambda_{t+2})(\beta_{t+1,0} \gamma_{t+1} + \lambda_{t+1})\beta_{t,0}$$

Substituting these expressions, in subsequent grades we get:

$$\frac{\partial Y_{i,s,c,t+l}}{\partial CR_{i,s,c,t}} = \beta_{t,0} \prod_{j=1}^l (\beta_{t+j,0} \gamma_{t+j} + \lambda_{t+j}) \quad (3.7)$$

Equation (3.7) tells us how the medium-term impact of rank in grade t on learning in grade $t + j$ depends on the short-term impact of rank at the beginning of each grade on learning at the end of that grade ($\beta_{t,0}$), the impact of learning in one grade on learning in the subsequent grade (λ_t), and the impact of learning in one grade on classroom rank in the subsequent grade (γ_t). We also note that, because (as we show below) $\gamma_{t+j} \approx 1$, equation (3.7) indicates that it is possible that we may see little or no decay of rank effects over time. This is because a high classroom rank early in elementary school can in principle lead to a self-fulfilling cycle, where a high rank produces high learning, which in turn leads to a high rank, which in turn leads to high learning. Observed differences between estimates of actual medium-term impacts of rank ($\beta_{t,l}$), and $\frac{\partial Y_{i,s,c,t+l}}{\partial CR_{i,s,c,t}}$ from equation (3.7) tell us about the importance of unobserved skills as mediators of the medium-term impacts of rank.

D. Executive function, non-cognitive skills, and teacher perceptions

To estimate effects of ability classroom rank on happiness in 1st grade and non-cognitive skills in 6th grade, we run regressions comparable to (3.1), replacing achievement in grade t with the relevant outcome.²⁵ To estimate rank effects on executive function, we also use the model in (3.1), but add to this model a third-order polynomial in lagged EF (in addition to the polynomial in lagged achievement). These regressions use information in 1st through 4th grades, where data on current and lagged EF are available. Finally, as discussed above, we have data on teacher perceptions of students—specifically, a list of the 5 students each teacher thought had the highest, and lowest, achievement in their classrooms. We generate indicator variables for children who are seen to be at the top and, separately, bottom of their classroom by their teachers, and use them as outcomes. To assess medium-term effects of classroom rank on non-cognitive

²⁵ Child happiness is only available in 1st grade, so we run regressions of child happiness in 1st grade on math classroom rank at the beginning of 1st grade and the polynomial on math achievement at the end of kindergarten. Non-cognitive skills are only available at the end of 6th grade. We report the results of 6th grade non-cognitive skills on “early” (1st and 2nd grade), “middle” (3rd and 4th grade), and “late” (5th and 6th grade) math classroom rank.

skills, executive function and teacher perceptions we also run regressions analogous to (3.5), replacing achievement in grade $t + l$ with the relevant outcome.

4. Results

A. Graphical evidence

To motivate our analysis, we start with some simple figures. For this purpose, we first sort children into ventiles on the basis of their test scores in math and language at the end of grade $t - 1$ (say, end of kindergarten). Then, within each ventile, we calculate average test scores at the end of grade t (end of 1st grade) for two groups of children: those who, relative to other children in that ventile, were randomly assigned to classrooms where their rank at the beginning of t was “high”—classroom rank in the top 25 percent for that ventile—and those in classrooms where their rank was “low”—in the bottom 25 percent for that ventile. If classroom rank has a positive effect on test scores, we would expect the line that corresponds to high-ranked children to be above that which corresponds to low-ranked children.

Results are shown in Figure 2. Panel A focuses on the short-term effects of classroom rank in 1st grade. The figure shows that children with high classroom ranks have higher achievement than those with low classroom ranks, but only above the 40th percentile of the distribution of national rank. Panel B compares these two groups of children at the end of 3rd grade. The figure shows that the vertical distance between the two lines is larger than in Panel A, indicating that the effect of 1st grade classroom rank increases over time.

Panel C focuses on the short-term effects of classroom rank in 4th grade. Children with higher classroom ranks appear to have higher achievement at the end of 4th grade, but the difference is quite small. Panel D focuses on these same children at the end of 6th grade. The lines in this panel are very similar to those in Panel C, suggesting that the (modest) effects of 4th grade classroom rank do not grow over time. In sum, Figure 2 suggests that: the effects of classroom rank are larger in 1st grade than in 4th grade; the 1st grade effects are larger in the upper half of the distribution; and these effects increase over time.

B. Static model

Table 2 reports estimates of the effect of classroom rank on learning, measured by an index of math and language, using equation (3.1) above. Column (1) shows that the coefficient on β is .030, with a standard error of .008.²⁶ This implies that moving a child from the 50th to the 60th percentile of classroom rank increases her end-of-grade achievement by 0.30 percentiles of the national distribution. To get a sense of

²⁶ Standard errors for all models are clustered at the school level.

magnitude, we take all children who are in the same school and grade, who have the same value of lagged achievement in $t - 1$, but are assigned to different classrooms in grade t . The (absolute value) of the median difference in classroom rank between children in these pairs is 5.5 percentiles (that is, on average, in these pairs of identical children, one child has a classroom rank of 47.25 and the other has a rank of 52.75. At the 75th and 90th percentiles of the difference, the values are 9.8 and 14.7 percentiles, respectively).

In columns (2) and (3), we report estimates of the effects of classroom rank in math on achievement in math and language. In columns (4) and (5) we report estimates of the effects of classroom rank in language on achievement in language and math. Finally, in columns (6) and (7) we report estimates of the effects of classroom rank in math and classroom rank in language on achievement in language and math. The table shows that classroom rank in math affects math achievement (coefficient of .040, with a standard error of .010) and, to a lesser extent, language achievement; in contrast, classroom rank in language does not affect either math or language achievement. The results are robust to regressing math and language achievement on classroom rank in math and classroom rank in language in a joint fashion.²⁷

Appendix Table E1 reports the results from a number of robustness checks. To facilitate comparisons, column (1) reproduces the coefficient and standard error from column (2) in Table 2. Column (2) shows that, as expected given the random assignment, including controls for child gender, as well as age and its square, does not affect our results. Columns (3) to (6) report estimates where $g_t(Y_{i,s,c,t-1})$ is specified as a polynomial of orders 1, 2, and 4, and using dummies for percentiles of lagged national rank respectively (as opposed to our main estimates, in which we include a cubic in lagged achievement). The estimated classroom rank effects are larger when we include only linear or quadratic terms in lagged achievement. Reassuringly, however, the coefficient on classroom rank is essentially unchanged when we include a polynomial of order 4, or dummies for percentiles in lagged achievement as a control (rather than a polynomial of order 3).

In column (7), of Table E1 we present estimates of equation (3.4). As we discuss above, in this specification—which is similar in character to that used by Murphy and Weinhardt (2020)—classroom rank refers to rank at the end of $t - 1$, rather than at the beginning of t . Table E1 shows that these

²⁷ We do not know why math rank, but not language rank, affects achievement. It is in principle possible that classroom rank in math is more visible to students and teachers than is the case with language rank. However, we do not find strong evidence that this is the case in our setting. As we discuss below, teachers appear to place similar weights on math and language achievement in determining which students in their class have the highest and lowest achievement. We note that it is not uncommon in the literature to find larger effects of school-based interventions on math than on language (see the discussion in Fryer 2017). In the U.S., teachers have larger effects on math than on language achievement (Hanushek and Rivkin 2010).

estimates are substantially larger than those from our preferred specification.²⁸ The approach to classroom rank we take therefore yields conservative estimates of rank effects on learning.

At this point it is important to mention the potential impact of selective attrition on our estimates. There are between 14,322 (kindergarten) and 17,529 (5th grade) students per grade in our data. These are not always the same students. Typically, from one year to the next, between 7.5 and 10 percent of students leave our sample of schools (the exception is the transition from kindergarten to 1st grade, where this number is 15 percent).²⁹ Selective attrition out of our sample of schools could generate a correlation between $CR_{i,s,c,t}$ and $\varepsilon_{i,s,c,t}$, which may bias estimates of the effect of classroom rank. To assess whether our estimates are likely to be affected by these considerations, we use a standard multiple imputation procedure, as described, for example, in Little and Rubin (2019). We describe the implementation of the procedure in detail in Appendix D. We find that the main estimates of the effect of contemporaneous classroom rank in math on math achievement are robust to this procedure (estimated coefficient is .040 with a standard error of .015).³⁰

C. Heterogeneity

We begin our analysis of heterogeneity by estimating effects at different points in the distribution of classroom rank, again focusing on the effects of math classroom rank on math achievement. In Figure 3 we graph coefficients and confidence intervals on deciles 1 through 4, and 6 through 10 from equation (3.3) above, with decile 5 as the omitted category. The figure shows that there is essentially no impact of classroom rank in the bottom half of the distribution. For example, we cannot reject the null that being in the lowest decile of classroom math rank has the same effect on achievement as being in the middle of the distribution of rank. The coefficients that correspond to deciles 6 through 10, on the other hand, are all positive, and are generally larger in the higher deciles (so that the coefficient for the 10th decile is larger in magnitude than that for the 7th decile). In this case, we can reject the null that being in the highest decile of classroom math rank has the same effect on achievement as being in the middle of the distribution.

²⁸ It is interesting that classroom rank effects estimated by (3.4) are larger than those estimated by (3.1). As mentioned above, this could happen because children are more aware of end-of-grade rank than beginning-of-grade rank and therefore react more to it, or because end-of-grade rank captures other aspects of the school experience besides rank.

²⁹ Similarly, in any given grade, between 7 and 13 percent of students are new entrants to the sample (with the exception of 1st grade, where this value is 24 percent). New students are randomly assigned to classrooms just like any other students.

³⁰ Using the baseline data, we can conduct a balancing exercise to test for the presence of correlation between pre-determined child characteristics and classroom rank at the beginning of any given grade, which complement the random assignment tests in Appendix A. As in Denning et al (2023), Elsner et al (2021), or Elsner and Isphording (2018), we regress baseline variables on classroom rank and the remaining controls in our main models, as described above. Given the time discrepancy between the measurement of rank and the measurement of baseline characteristics, selective “attrition” (every year not only existing students move to another school, but new students enter the school and are incorporated in the randomization of students to classrooms) is an issue, so the balancing tests correct for it using multiple imputation. The results of this exercise are presented in Appendix Table D2.

In Table 3, we analyze other possible sources of heterogeneity in the effect of classroom rank. We first focus on gender. In theory, if girls have different levels of self-confidence than boys (as in Bordalo et al. 2019), or react differently to competition than boys (as in Niederle and Vesterlund 2011), it is possible that they react differently to rank. In the first column, we present estimates of a specification where all the coefficients in equation (3.2) for math are interacted with gender. Girls have significantly lower math scores than boys, but the impact of classroom rank on learning is the same for girls and boys.

We also interact classroom rank with vocabulary at the beginning of kindergarten, or with lagged achievement. These results show that classroom rank effects are substantially and significantly larger for children with higher baseline vocabulary levels, as well as for those with higher lagged achievement. In sum, and consistent with the results in Figure 3, Table 3 shows that classroom rank seems to have larger impacts for higher-achieving children. Finally, we interact classroom rank with variables capturing socio-economic status. Specifically, we run regressions in which we interact classroom rank in math with an indicator for mothers having less than secondary education, an indicator for whether the child attended preschool, and an indicator for household wealth being above the median. Table 3 shows that classroom rank effects are stronger among children who attended preschool.

D. Dynamics

We begin our analysis of dynamics by estimating effects of classroom rank separately for children in the “early” grades (1st and 2nd grade), “middle” grades (3rd and 4th grade), and “late” grades, both contemporaneously (without lags, as in equation (3.1) above) and at various lags (as in equation (3.5)). These results are in Table 4.³¹

Column (1) shows that the short-term effect of math classroom rank in the early and middle grades are both positive and of a comparable magnitude. On the other hand, classroom rank in 5th and 6th grades

³¹ In Appendix E we report results from estimating rank effects by grade, rather than by aggregating estimates into “early”, “middle”, and “late” grades.

has no effect on achievement.³² We test and reject the null that the coefficients on the early, middle, and late grades are the same (p-value: .025).³³

We next turn to the evolution of rank effects over time. Specifically, in columns (2) through (5), we report estimates of the effect of classroom math rank on math achievement after (up to) 1, 2, 3, and 4 lags, respectively. In the first row, corresponding to rank in the early grades, the coefficients increase monotonically over time—the impact after 4 lags is .109 (with a standard error of .021), almost twice as large as the short-term effect. We reject the null that the coefficients for lag 0 and lag 4 are the same (p-value: .069). On the other hand, the coefficients in the second row of the table show that the classroom rank effects in the middle grades decline, although we cannot reject the null that the coefficients for lag=0 and lag=2 are the same (p-value: .679).³⁴

Table 4 shows suggestive evidence that the effects of classroom rank in the early grades increase substantially over time.³⁵ Given these results, we now ask the following question: can we account for the increase in the effect of early classroom rank using estimates of $\beta_{t,0}$ (short-term impact of classroom rank), γ_t (impact of learning on future rank), and λ_t (impact of lagged skills on current skills)?

Estimates of $\beta_{t,0}$, γ_t , and λ_t for each grade t show that $\gamma_t \approx 1$ but $\beta_t + \lambda_t < 1$ for every grade, which means that, if rank operated primarily through short-term learning gains and the resulting improvement in subsequent rank, we should observe fade-out in the impacts of rank on learning.³⁶ As we

³² This result is perhaps surprising, and not shown before in other papers. It is possible that the impact of rank may depend on how long one has to learn about it and experience it, since what matters for the student's reaction to rank is his or her perception of rank. In our setting, but not in other settings where the effect of rank has been studied, there is annual reshuffling of peers, so it may be more difficult for children to learn about their rank. Therefore, the long-term impact of rank within a stable peer group could differ from the long-term impact of a rank that changes more frequently. In addition, potentially the peer group with which to compare oneself goes from the classroom to the entire school as one experiences more and more peers. One reason all this could dampen the measured impact of objective rank, is that it could blur the connection between perceived and objective rank. However, this also depends on the degree to which rank is perceived to be stable by the individual, and the extent to which they believe they can change rank. We have also estimated a specification where we look at school rather than classroom rank (Table G1 in Appendix G). Our results are similar to the ones shown here for classroom rank.

³³ Our results show a lack of effects of late classroom rank on achievement. This is somewhat in contrast with other papers in the literature, which find effects of rank on outcomes measured later in life (see Delaney and Devereux (2022) for a review of the literature). The impact of rank may depend on how much time a student has to learn about their rank and experience its effects. Therefore, the long-term impact of rank within a stable peer group may well differ from the long-term impact of a rank that changes more frequently, as is the case in our setting, where random assignment to a classroom happens at the beginning of every grade.

³⁴ We do not know why the effects of rank in the early grades increase, while those in the middle grades do not. We note, however, that some theories of human capital argue that earlier investments tend to have the largest effects (as in Cunha and Heckman 2007), in part because earlier investments allow children to better take advantage of later investments. It is possible that early classroom rank affects achievement in this way.

³⁵ Appendix Table D3 shows that the estimated effects of early classroom rank on later grade achievement are robust to a standard multiple imputation procedure (as in Little and Rubin (2019)) which corrects for selective attrition.

³⁶ One could think that the result that $\gamma_t \approx 1$ is an automatic consequence of random assignment. In principle this does not necessarily happen because national and classroom rank could have very different scales, especially if there is non-random sorting of students into schools. However, if schools look very similar in the types of students they get, it may

have seen in Table 4, this is not the case. Rather, our results suggest that classroom rank operates at least in part by producing sustainable changes in another unobserved skill, which has independent effects on learning.

A useful way to make this point is in Figure 4, which plots the implied change in learning in grades $t + l$, as a response to an exogenous change in early (1st or 2nd grade) achievement ($t = 0$) percentile rank by 10 points, under two scenarios: (i) using the estimates of β_{t+l} (for $l = 0, 1 \dots 4$) from equation (3.5), labeled *reduced form* in the figure; and (ii) using the estimates of γ_t , β_t and λ_t , (for several values of t) from equations (3.1) and (3.6), and then simulating the response to a particular change in rank using the equations (3.7), labeled *structural* in the figure. The figure shows that, under scenario (i), the effect of rank grows over time, while in scenario (ii) it does not.³⁷

In sum, Figure 4 suggests that early classroom rank affects future achievement through channels that are not modelled explicitly in our equations, such as through its impact on other unobservable skills. We examine impacts on non-academic skills in the next section.³⁸

In appendix Tables F1 and F2 we report results from additional exercises that exploit the panel nature of our dataset to examine the impacts of changes in classroom rank on national rank in math. The regressions in appendix Table F1 are run for “early” (1st and 2nd), “middle” (3rd and 4th) and “late” (5th and 6th) grades. Panel A of appendix Table F1 shows results from an exercise in which we regress national rank in math on contemporaneous classroom rank in math, lagged classroom rank in math and an interaction between the two, pooling data across grades. These regressions control for third-order polynomials in lagged national rank in math and in national rank in math measured in period $t - 2$, as well as classroom-by-grade fixed effects. Although all coefficients are positive, they are imprecisely estimated and we cannot reject that the model is linear in classroom rank.

Panel B of appendix Table F1 shows results from an exercise analogous to that in Elsner et al. (2021), estimating the impacts of changes in classroom rank over time on national rank in math. The results from this exercise show that, for middle grades, a positive change in classroom rank over time has a positive impact on national rank in math, while a negative change in classroom rank over time has a negative impact on national rank in math. Finally, appendix Table F2 shows results from another exercise analogous to

happen that the distribution of classroom and national rank look similar, and that random assignment leads automatically to $\gamma_t \approx 1$.

³⁷ For the purpose of illustration, we normalize the estimate of $\beta_{t,0}$ to be the same across the two scenarios.

³⁸ Throughout this analysis we assume that rank affects actual achievement as opposed to affecting only test-taking skills. Therefore, we interpret our results as saying that there is a virtuous cycle in learning as opposed to a virtuous cycle in test-taking confidence. In reality, we cannot distinguish the two. However, notice that the tests administered in our data are low stakes tests, and students may be relaxed when taking them. Furthermore, in the earlier grades, tests are administered individually by an enumerator, which may also help attenuate any issues related to test-taking confidence.

that in Elsner et al. (2021), estimating the cumulative impacts of changes in classroom rank between first and 6th grade on national rank in math at the end of 6th grade. We control for a third-order polynomial in national rank in math in kindergarten and classroom fixed effects. The results show positive and increasing cumulative effects of positive changes in classroom rank over time, and increasingly negative cumulative effects of negative changes in classroom rank over time.³⁹

Appendix Table G1 reports estimates to a model analogous to equation (3.5), but using school rank as our main regressor of interest (instead of classroom rank), and controlling for school-by-grade fixed effects (instead of classroom-by-grade fixed effects). While we do not have random assignment at the school level, we can estimate the impact of school rank on achievement assuming that conditional on lagged ability and the school fixed effect, a student’s rank within the school is random. As Table G1 shows, here too we find that the impact on achievement of rank in “early” grades is stronger than the impact of rank in “late” grades. In addition, we show that early school rank has persistent and growing impacts on achievement in later grades. These estimates are qualitatively similar to our main dynamic estimates presented in Table 4.⁴⁰ The fact that early rank has long-lasting effects on achievement may indicate that children learn about their rank during the first years of school, and their perception of their ranking persists over time.

E. Executive function, non-cognitive skills, and teacher perceptions

As discussed above, there is a large literature in child psychology that argues that executive function is a key determinant of learning (Anderson 2002; Espy 2004; Senn et al. 2004). In our data, too, EF in a given grade predicts future achievement.⁴¹ It is therefore of interest to analyze whether classroom rank improves executive function. Table 5 shows estimated effects of classroom rank in math on executive function (standardized to have mean zero and unit standard deviation) separately for children in the “early” and “middle” grades, both contemporaneously and at various lags.⁴² Below the standard errors in parentheses

³⁹ It is perhaps difficult to reconcile the results in tables F1 (panel B) and F2. However, notice that in F2 we are only controlling for first period ability in the regression, and therefore, changes in classroom rank capture both a change in rank due to a change to randomly assigned peers, and changes in rank due to changes in ability which can occur for several reasons, which could potentially affect the interpretation of these coefficients as measuring exclusively the impact of changes in rank.

⁴⁰ They are however larger in absolute value, which could perhaps suggest that school rank has a larger impact on learning than classroom rank.

⁴¹ We do not have the data to identify the causal effect of executive function on learning. Nevertheless, in a regression of achievement in grade t on executive function in grade $t - 1$, including school fixed effects, the coefficient on EF is .538 (with a standard error of .005). If, in addition, we control for achievement at the end of $t - 1$, the coefficient on EF is .096 (with a standard error of .002).

⁴² We did not apply executive function tests past 4th grade.

we report p-values computed based on the Romano-Wolf stepdown procedure using 5,000 bootstrap replications (see Romano and Wolf, 2005 and Clarke, Romano and Wolf, 2020).

The first column of Table 5 shows that the coefficients on contemporaneous classroom math rank are positive for both early and middle grades, albeit not significant. Looking across rows, we find that early classroom rank has a positive and significant effect on executive function after one lag. The estimated effect implies that an increase in early classroom rank from the 50th to the 60th percentile of the distribution improves executive function by 2.65 percent of a standard deviation. However, the effect of early classroom rank on executive function fades out after two lags (the estimated coefficient is .054 with a standard error of .077).

Table 6 reports the marginal effects from ordered probit regressions of child happiness on math classroom rank in 1st grade. These results show that moving a child from the 50th to the 60th percentile of the distribution of classroom rank increases the probability that a child says she is always happy in school by 1.3 percentage points.

Appendix Table H1 reports the results from regressions of 6th grade non-cognitive skills on math classroom rank in “early” (1st and 2nd), “middle” (3rd and 4th) and “late” (5th and 6th) grades. While all estimated coefficients are positive, they are not significant (with the exception of the effect of late classroom rank on the aggregate non-cognitive skills index, which is estimated to be .266 with a standard error of .157, and the self-esteem component, which is estimated to be .288 with a standard error of .149).

Finally, we turn to teacher perceptions. Teacher ratings are informative about student performance. Although the top (bottom) 5 students reported by the teacher are not always the 5 highest (lowest) performing students in the tests we administer, there is some overlap.⁴³ The fact that these two measures are only imperfectly correlated could in part be a result of measurement error in either one of them. It is also possible, however, that in assessing “achievement” teachers are in fact taking account of a broader or somewhat different construct, i.e., teacher perceptions do not measure exactly the same thing as the tests. Furthermore, if teachers perceive highly-ranked children to be particularly high achieving—even conditional on their actual ability—they may reinforce academic self-concept of highly-ranked children, and thus contribute to the impact of rank on learning outcomes we observe in both the short- and medium-run.

⁴³ There is no evidence that teachers make more use of math or language achievement in assessing who are top and bottom students: The correlations between being in the top 5 by measured math achievement and language achievement, on the one hand, and having a teacher report a student as being in the top 5 are 0.38 and 0.33, respectively, while the correlations between being in the bottom 5 by measured math achievement and language achievement, on the one hand, and having a teacher report a student as being in the bottom 5 are 0.38 and 0.41, respectively.

In Table 7 we report the results of regressions of teacher perceptions on (randomly assigned) classroom rank in math, conditional on achievement in math. We pool across “early” (1st and 2nd), “middle” (3rd and 4th), and “late” (5th and 6th) grades. Here too we report p-values computed based on the Romano-Wolf stepdown procedure using 5,000 bootstrap replications. In column 1 of Table 7, we show that, in a regression that controls for achievement at the end of $t - 1$, higher classroom rank at the start of grade t increases the probability that a child is seen as a top student by her teacher in $t + 1$ for early, middle and late grades. Moreover, in column (5) we show that higher classroom rank at the start of grade t in early grades reduces the probability that the student is seen as a bottom student by her teacher in $t + 1$. Looking across rows, we find that the effect of early and middle classroom rank on the probability of being seen as a top student by a teacher is positive and significant after several lags, but tends to fade out for early rank. Interestingly, a higher classroom rank in early grades significantly reduces the probability of being seen as a bottom student after 3 lags.⁴⁴

In sum, we show that children who, as a result of random assignment, have higher math classroom rank have higher levels of executive function, are more likely to be happy, and are also perceived to be higher-achieving by their future teachers.

5. Conclusion

This paper analyzes the impact of classroom ability rank measured at the start of the academic year on learning during that year and learning in subsequent years. In our data, which comes from a longitudinal study of students in elementary schools in Ecuador, two students with the same underlying ability and attending the same school can have different classroom ranks because they are randomly assigned to different classrooms, with slightly different peers.

We measure classroom rank and learning in math and language. Beginning-of-grade classroom rank and end-of-grade achievement are available for all grades from 1st to 6th grade. We also observe executive function in kindergarten through 4th grade, self-reported child happiness in 1st grade, and non-cognitive skills at the end of 6th grade. In addition, we have data on teacher perceptions of student ability in every grade between kindergarten and 6th grade.

We show that classroom rank has modest positive short-term effects on achievement. Estimated effects of classroom rank can be confounded by the effects of peer quality. Students randomly assigned to classrooms with better peers will in general have lower classroom ability rank, but potentially benefit from

⁴⁴ In table H2 in the appendix we include teacher perceptions of rank and student rank simultaneously in our model of learning. Both variables are important predictors of learning, and interestingly, the coefficient on student rank is only slightly affected by the inclusion of teacher perceptions of rank.

better peers. For this reason, our main model specification controls for classroom-by-grade fixed effects. The conflation of rank and peer quality effects is a feature of any study where both change at the same time, such as studies of the impact of selective schools, affirmative action, or neighbourhood effects.

We also show that classroom rank in math, but not language, affects achievement. The impact of classroom rank in math is larger for younger children and grows substantially over time. Moving a child from the 50th to the 60th percentile of classroom rank in 1st (2nd) grade increases her achievement in 5th (6th) grade by 1 percentile of the national distribution. The increase in the magnitude of rank effects is remarkable given the evidence that impacts of many other interventions in elementary school fade out over time. Exogenous changes in classroom math rank also improve executive function, happiness, and teacher perceptions of students. Changes in these skills, or others that we do not observe, are likely to be important in explaining how classroom rank raises child learning.

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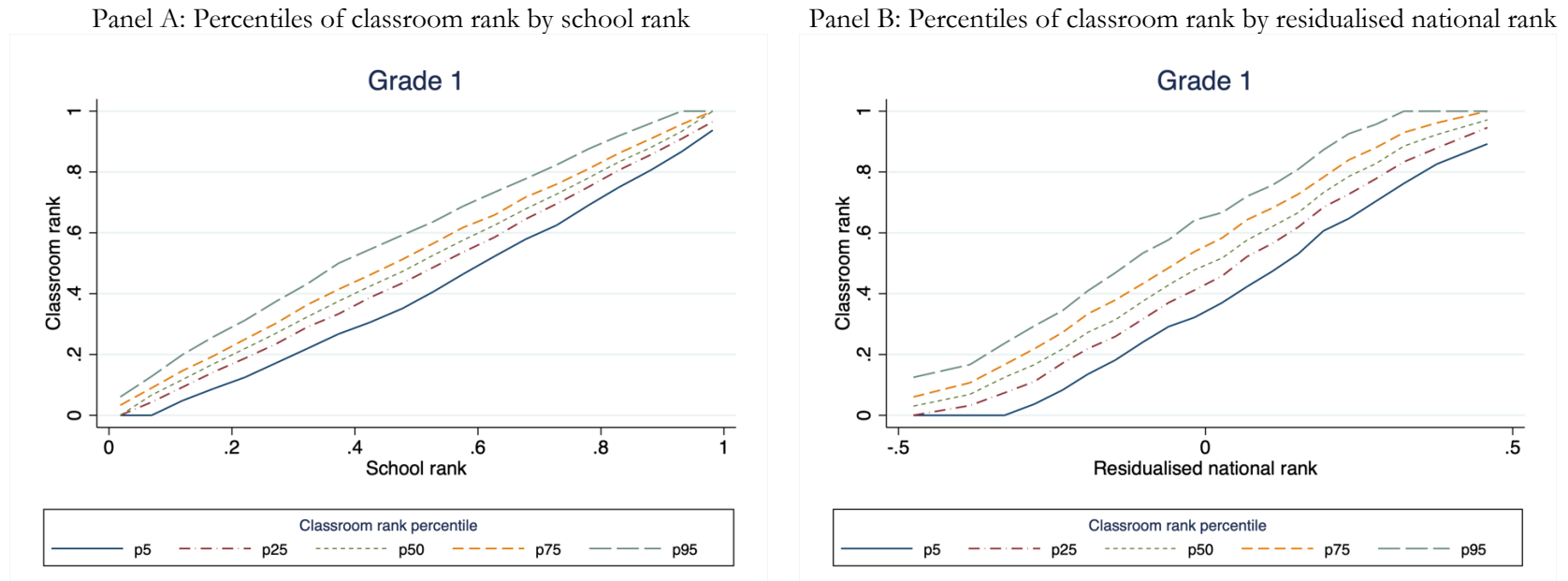
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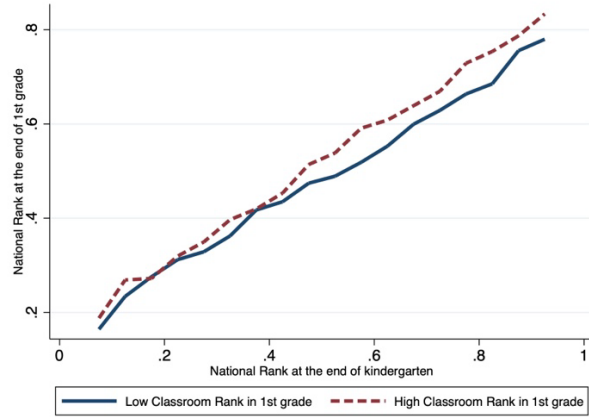
Figure 1: Variation in classroom rank within school



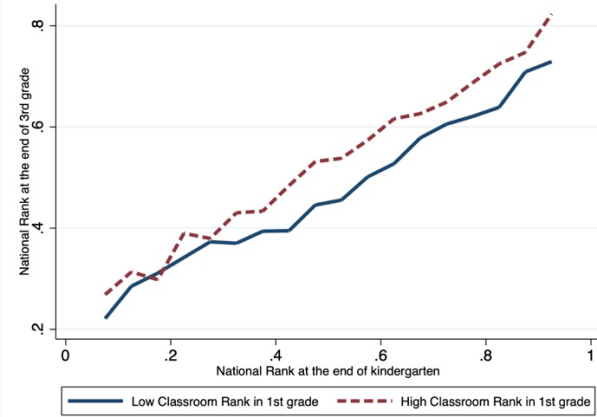
Notes: To construct the figure in Panel A we plot the 5th, 25th, 50th, 75th and 95th percentile of classroom rank within each ventile of school rank, against the median school rank in that ventile, measured by an index of math and language. To construct the figure in Panel B, we first regress national ability rank measured by an index of math and language on school fixed effects and derive residuals. Then we plot percentiles of classroom rank within each ventile of residualised national ability rank, against the median residualised national rank in that ventile.

Figure 2: Visual evidence of classroom rank effects on achievement

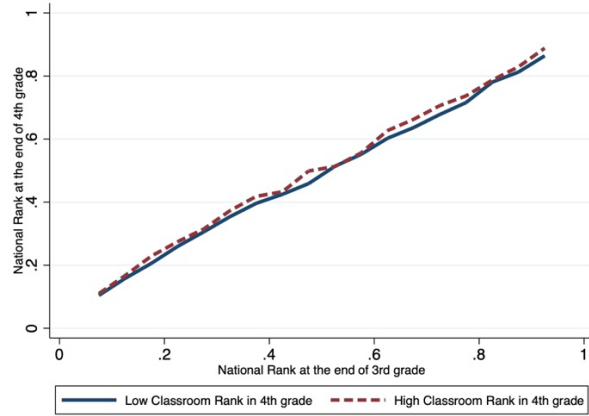
Panel A: Short-term effects of classroom rank in 1st grade



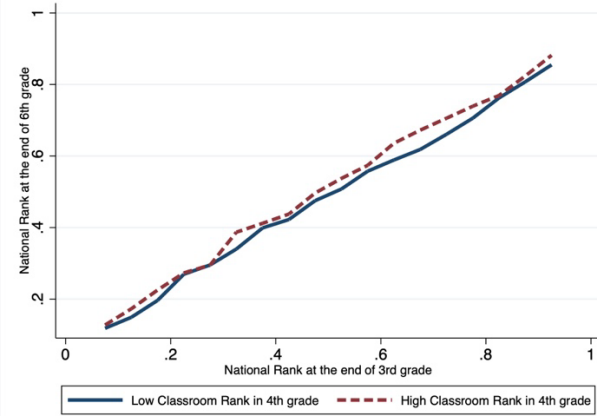
Panel B: Long-term effects of classroom rank in 1st grade



Panel C: Short-term effects of classroom rank in 4th grade

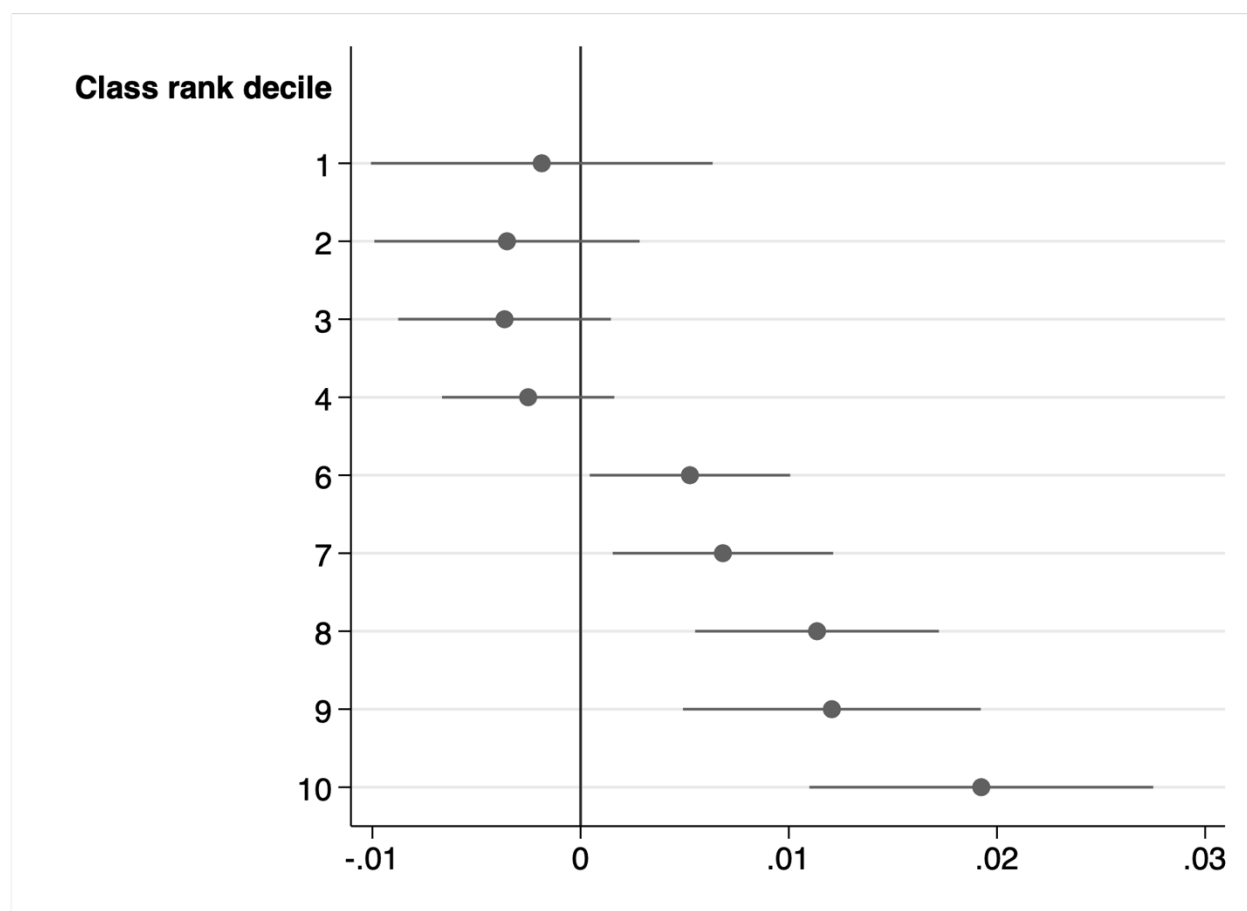


Panel D: Long-term effects of classroom rank in 4th grade



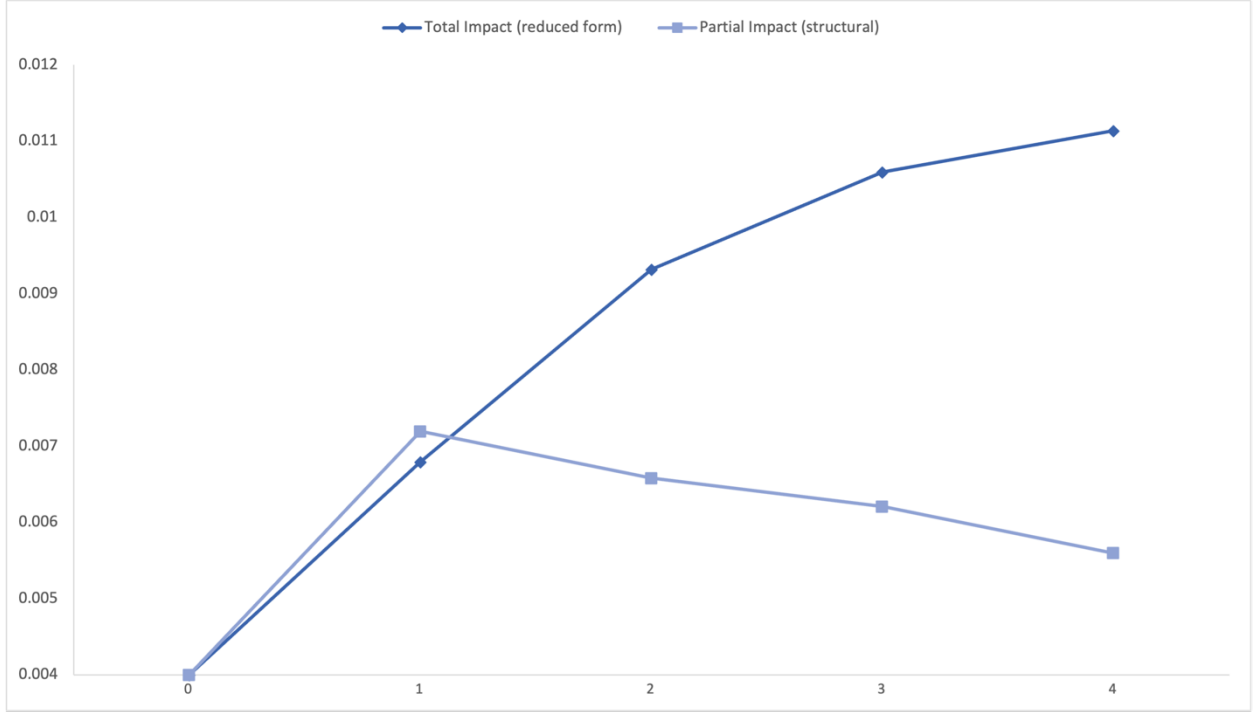
Notes: To generate this figure, we first sort children into ventiles on the basis of their test scores in math and language at the end of grade $t - 1$. Then, for each ventile, we calculate average test scores at the end of grade t for two groups of children: those who, relative to other children in that ventile, were randomly assigned to classrooms where their rank at the beginning of t was “high”—classroom rank in the top 25 percent for that ventile—and those in classrooms where their rank was “low”—in the bottom 25 percent for that ventile. Panel A focuses on the short-term effects of classroom rank in 1st grade, and Panel B compares these two groups of children at the end of 3rd grade. Panel C focuses on the short-term effects of classroom rank in 4th grade, and Panel D focuses on these same children at the end of 6th grade.

Figure 3: Classroom rank effects at different deciles of the distribution of achievement



Notes: To produce this figure we discretize classroom rank in math into 10 deciles and run regressions of math achievement on classroom rank deciles. We graph coefficients and 90 percent confidence intervals on deciles 1 through 4, and 6 through 10, with decile 5 as the omitted category. All regressions include a third order polynomial in lagged national rank and classroom-by-grade fixed effects. All regressions are limited to schools in which there are at least two classrooms per grade. Standard errors are clustered at the school level throughout.

Figure 4: Total and partial effects of rank on achievement



Notes: The figure plots the implied change in learning in grades $t + l$, as a response to an exogenous change in early (1st or 2nd grade) achievement ($t = 0$) percentile rank by 10 points, under two scenarios: (i) using the estimates of β_{t+l} (for $l=0, 1 \dots 4$) from equation (3.7) in the main text (“total impact”); and (ii) using the estimates of γ_t , β_t and λ_t , (for several values of t) from equations (3.1) and (3.8) in the main text, and then simulating the response to a particular change in rank using the equations (3.9) (“partial impact”). We normalize the estimate of $\beta_{t,0}$ to be the same across the two scenarios.

Table 1: Child, teacher, and classroom characteristics

| | Mean | Standard deviation | N |
|---------------------------------------|------|--------------------|--------|
| Child and household characteristics | | | |
| Age of child (months) | 60.3 | 4.9 | 13,877 |
| Gender of child | 0.49 | 0.50 | 14,519 |
| Receptive vocabulary score (TVIP) | 82.9 | 15.9 | 13,574 |
| Mother's years of completed schooling | 8.8 | 3.8 | 13,665 |
| Father's years of completed schooling | 8.5 | 3.8 | 10,623 |
| Mother's age | 30.2 | 6.6 | 13,675 |
| Father's age | 34.6 | 7.9 | 10,649 |
| Proportion who attended preschool | 0.61 | 0.49 | 14,506 |
| Household has piped water in home | 0.83 | 0.38 | 14,439 |
| Household has flush toilet in home | 0.46 | 0.50 | 14,439 |
| Teacher and classroom characteristics | | | |
| Proportion female | 0.82 | 0.38 | 2830 |
| Proportion tenured | 0.82 | 0.38 | 2818 |
| Years of experience | 18.1 | 10.5 | 2820 |
| Class size | 37.7 | 6.8 | 2839 |

Notes: The table reports means and standard deviations of the characteristics of children entering kindergarten in 2012, measured at the beginning of the school year, and of the teachers they had between kindergarten and 6th grade. The TVIP is the *Test de Vocabulario en Imágenes Peabody*, the Spanish version of the Peabody Picture Vocabulary Test (PPVT). The test is standardized using the tables provided by the test developers which set the mean at 100 and the standard deviation at 15 at each age.

Table 2: Classroom rank effects, math-language index and separating math and language

| | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
|---------------------------------------|---------------------|-------------------|-------------------|----------------|----------------|-------------------|-------------------|
| | Math+Language index | Math | Language | Math | Language | Math | Language |
| Classroom rank in math+language index | .030*** (.008) | | | | | | |
| Classroom rank in math | | .040*** (.010) | .030*** (.011) | | | .037*** (.009) | .024*** (.009) |
| Classroom rank in language | | | | .017 (.012) | .003 (.009) | -.000 (.009) | -.006 (.009) |
| N | 87,706 | 87,713 | 87,760 | 87,740 | 87,789 | 87,709 | 87,756 |

Notes: The table reports estimates from regressions of achievement national rank on classroom rank, pooling observations across grades. For the regression in Column (1), national rank and classroom rank are calculated on the basis of the index averaging across math and language scores, and a third-order polynomial in lagged national rank in the index averaging across math and language achievement is included as a control. For Columns (2) and (3), classroom rank is calculated on the basis of math test scores, and a third-order polynomial in lagged math achievement is included as a control. For the regressions in Columns (4) and (5), classroom rank is calculated on the basis of language test scores, and a third-order polynomial in lagged language achievement is included as a control. For the regressions in Columns (6) and (7), we include classroom rank calculated on the basis of math and language achievement, and a third-order polynomial in lagged math and language achievement is included as a control. All regressions control for classroom-by-grade fixed effects. All regressions are limited to schools in which there are at least two classrooms per grade. Standard errors are clustered at the school level throughout. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table 3: Heterogeneity of math classroom rank effects

| | (1) | (2) | (3) | (4) | (5) | (6) |
|------------------------------|--------------------|------------------------|-------------------------|---|-----------------------|-------------------------------------|
| | Gender | Baseline Vocabulary | Lagged national rank | Mother has less than secondary education | Attended preschool | Household wealth above median |
| Classroom rank | .039*** (.010) | .036*** (.012) | .010 (.016) | .041*** (.012) | .042*** (.012) | .046*** (.012) |
| Main covariate effect | -.006*** (.002) | .020*** (.001) | 1.02*** (.034) | -.022*** (.008) | -.021*** (.008) | .017*** (.002) |
| Interaction (rank*covariate) | .002 (.003) | .007*** (.003) | .060** (.026) | -.001 (.005) | .027** (.013) | -.007 (.004) |
| N | 87,700 | 61,178 | 87,713 | 59,572 | 63,270 | 62,433 |

Notes: The table reports estimates from regressions of national rank in math on classroom math rank and interactions. Observations are pooled across grades. Column (1) shows the results from a regression of national rank on classroom rank interacted with an indicator variable for girls. Column (2) shows the results from a regression of national rank on classroom rank interacted with baseline vocabulary. Column (3) shows the results from a regression of national rank on classroom rank interacted with lagged national rank. Column (4) shows the results from a regression of national rank on classroom rank interacted with an indicator variable for mother having less than secondary education. Column (5) shows the results from a regression of national rank on classroom rank interacted with an indicator variable for the child having attended preschool. Column (6) shows the results from a regression of national rank on classroom rank interacted with an indicator variable for the child belonging to a family with household wealth above the median. All regressions are limited to schools in which there are at least two classrooms. All regressions include a third order polynomial in lagged national rank in math and classroom-by-grade fixed effects. Standard errors are clustered at the school level. N is lower for columns (2), (4), (5) and (6) because we collected this information at the beginning of kindergarten, so it is not available for children who joined schools in our sample after the beginning of kindergarten. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table 4: Effects of math classroom rank on achievement, by grade and lag

| | Lags | | | | | Joint- test 1 | Joint- test 2 |
|--|-------------------|-------------------|-------------------|-------------------|-------------------|------------------|------------------|
| | 0 | 1 | 2 | 3 | 4 | | |
| Classroom rank "early" (1st & 2nd grades) | .064*** (.017) | .077*** (.019) | .090*** (.021) | .096*** (.022) | .109*** (.021) | [.486] | [.069] |
| Classroom rank "middle" (3rd & 4th grades) | .048*** (.017) | .038** (.019) | .040** (.019) | | | [.848] | [.679] |
| Classroom rank "late" (5th & 6th grades) | .005 (.015) | | | | | | |
| Joint-test 3 | [.025] | [.160] | [.098] | | | | |
| Joint-test 4 | [.011] | | | | | | |

Notes: The table reports estimates from regressions of national rank in math on classroom math rank for different lags of classroom rank, separately for children in the “early” (1st and 2nd), “middle” (3rd and 4th), and “late” grades (5th and 6th) grades. All regressions are limited to schools in which there are at least two classes. All regressions include a third order polynomial in lagged national rank in math and classroom-by-grade fixed effects. Standard errors are clustered at the school level. P-values for joint-tests of equality of coefficients (in square brackets) are calculated after running estimates by Seemingly Unrelated Regressions. Joint-test 1 is a test that the coefficient for all lags is the same, and Joint-test 2 is a test that the coefficient on lag=0 is the same as that on lag=4 (for the “early” grades) or lag=2 (for the “middle” grades). Joint-test 3 is a test that the coefficients on “early”, “middle”, and “late” grades are the same, and Joint-test 4 is a test that the “early” and “late” effects are the same. Standard errors are clustered at the school level throughout. N lag 0, “early”: 26,695. N lag 0, “middle”: 30,078. N lag 0, “late”: 30,940. N lag 1, “early”: 24,648. N lag 1, “middle”: 28,194. N lag 2, “early”: 23,199. N lag 2, “middle”: 26,706. N lag 3, “early”: 22,140. N lag 4, “early”: 21,210. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table 5: Math classroom rank effects on executive function

| | Lags | | |
|--|----------------|-------------------|----------------|
| | 0 | 1 | 2 |
| Classroom rank “early” (1 st & 2 nd grades) | .096 (.067) | .265*** (.078) | .054 (.077) |
| Classroom rank “middle” (3 rd & 4 th grades) | .096 (.071) | .000 | .338 |
| | .113 (.080) | | |

Notes: The table reports estimates from regressions of executive function, in SDs, on classroom achievement rank in math, for different lags of classroom rank, separately for children in the “early” (1st and 2nd) and “middle” (3rd and 4th) grades. All regressions include third order polynomials in lagged national rank in math, a third-order polynomial in lagged executive function, and classroom-by-grade fixed effects. Below the standard errors in brackets we report p-values computed according to the Romano and Wolf stepdown procedure (see Romano and Wolf, 2005 and Clarke, Romano and Wolf, 2020), using 5000 bootstrap replications. All regressions are limited to schools in which there are at least two classrooms per grade. We cannot assess the impact of classroom rank past 4th grade, as we did not apply executive function tests after that grade. Standard errors are clustered at the school level throughout. N lag 0, “early”: 26,696. N lag 0, “middle”: 30,065. N lag 1, “early”: 24,649. N lag 2, “early”: 23,199. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table 6: Math classroom rank effects on happiness

| | <u>Child happiness (1st grade)</u> | | |
|----------------|---|---------------------|-------------------|
| | Mostly happy | Almost always happy | Always happy |
| Classroom rank | -.070*** (.023) | -.057** (.019) | .127*** (.042) |

Notes: The table reports estimates from a regressions of child happiness in 1st grade on classroom achievement rank in math in 1st grade, estimated by ordered probit. All regressions include third order polynomials in kindergarten national rank in math and classroom fixed effects. All regressions are limited to schools in which there are at least two classrooms per grade. Standard errors are clustered at the student level throughout. N is 12,062. Standard errors are clustered at the school level throughout. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table 7: Math classroom rank effects on teacher perceptions

| | Top 5 student | | | | Bottom 5 student | | | |
|---|-------------------|-------------------|------------------|----------------|--------------------|-----------------|-----------------|-------------------|
| | Lags | | | | Lags | | | |
| | 0 | 1 | 2 | 3 | 0 | 1 | 2 | 3 |
| Rank “early” (1 st & 2 nd grade) | .099*** (.029) | .092*** (.026) | .060** (.025) | .027 (.027) | -.079*** (.028) | -.047 (.029) | -.021 (.026) | -.058** (.025) |
| | .000 | .000 | .021 | .534 | .004 | .162 | .617 | .021 |
| Rank “middle” (3 rd & 4 th grade) | .074** (.031) | .088*** (.031) | | | -.007 (.031) | -.019 (.032) | | |
| | .021 | .004 | | | .774 | .640 | | |
| Rank “late” (5 th & 6 th grade) | .083* (.042) | | | | -.056 (.042) | | | |
| | .065 | | | | .321 | | | |

Notes: The table reports the results from regressions of a child being reported to be among the top 5 (bottom 5) by achievement by her teachers in grade $t+1$ on classroom rank in grade t , controlling for a third-order polynomial in national achievement in math in grade $t-1$, and school-by-grade fixed effects, pooling across “early” (1st and 2nd), “middle” (3rd and 4th) and “late” (5th and 6th) grades. Below the standard errors in brackets we report p-values computed according to the Romano and Wolf stepdown procedure (see Romano and Wolf, 2005 and Clarke, Romano and Wolf, 2020), using 5000 bootstrap replications. All regressions are limited to schools in which there are at least two classrooms per grade. Standard errors are clustered at the school level throughout. N “early”: 27,794. N “middle”: 30,842. N “late”: 15,552. *Significant at 10%, **significant at 5%, ***significant at 1%.

Appendix A

An important assumption underlying our empirical strategy is that children’s classroom rank at the beginning of a given grade is random, due to random assignment of children to classrooms within schools in every year.¹ Random assignment is closely monitored, and compliance was very high, 98.9 percent on average. In this appendix, we present tests of random assignment using a methodology developed in Jochmans (2023).

First, we briefly discuss the procedure outlined in Jochmans (2023). Consider our setting, in which we observe data on S schools, and each school has n_1, \dots, n_S students. Within each school, children are assigned to a classroom—and therefore their peer group—every year. Let $x_{s,i}$ be an observable characteristic of child i in school s . If assignment to peer groups is random, $x_{s,i}$ will be uncorrelated with $x_{s,j}$, for all j belonging to the set of i ’s classroom peers. Let $\bar{x}_{s,j}$ be the average value of characteristic x among student i ’s peers. The procedure tests whether the correlation in a within-school regression of $x_{s,i}$ on $\bar{x}_{s,i}$ is statistically significantly different from zero (a methodology first proposed in Sacerdote (2001)), introducing a bias correction for the inclusion of group fixed effects (in our case, schools). It is important to control for school fixed effects, as randomization happens within schools, but there may be selection into a school based on individual characteristics. Jochmans (2023) shows that a fixed-effects regression of $x_{s,i}$ on $\bar{x}_{s,i}$ will yield biased estimates due to inconsistency of the within-group estimator. The proposed corrected estimator is given by

$$ts = \frac{\sum_{s=1}^S \sum_{i=1}^{n_s} \tilde{x}_{s,i} \left(\bar{x}_{s,j} + \frac{x_{s,i}}{n_s - 1} \right)}{\sqrt{\sum_{s=1}^S \left(\sum_{i=1}^{n_s} \tilde{x}_{s,i} \left(\bar{x}_{s,j} + \frac{x_{s,i}}{n_s - 1} \right) \right)^2}} \quad (\text{A. 1})$$

where $\tilde{x}_{s,i}$ is the deviation of $x_{s,i}$ from its within-school mean. The null hypothesis is thus absence of correlation between i ’s characteristics and those of her peers. To test the random assignment in our setting, we implement this procedure by testing for the presence of correlation between child i ’s scores measured at the end of grade $t - 1$ and the average end-of-grade scores in $t - 1$ of the classroom peers assigned to

¹ We use the word “random” as shorthand but, as discussed at length in Araujo et al. (2016), strictly speaking random assignment only occurred in 3rd through 6th grade. In the other grades, the assignment rules were as-good-as-random. Specifically, the assignment rules we implemented were as follows: In kindergarten, all children in each school were ordered by their last name and first name, and were then assigned to teachers in alternating order; in 1st grade, they were ordered by their date of birth, from oldest to youngest, and were then assigned to teachers in alternating order; in 2nd grade, they were divided by gender, ordered by their first name and last name, and then assigned in alternating order; in 3rd through 6th grades, they were divided by gender and then randomly assigned to one or another classroom.

her in a given grade t . We do so for each grade. We implement the test for all children in the sample, and restricting the sample to those children who have both end of grade $t - 1$ scores as well as end of grade t scores (as these will be the children that end up being included in the estimation of our models). The results are shown in tables A1 and A2, respectively. Our results show that we cannot reject the null hypothesis that there is no correlation between child i 's achievement and that of her classroom peers. This result is true for all grades and both samples. Hence, we conclude that random assignment was successful in our setting.

Table A1: Testing for random assignment of children to classrooms, full sample

| | Kindergarten | Grade 1 | Grade 2 | Grade 3 | Grade 4 | Grade 5 | Grade 6 |
|----------------|--------------|---------|---------|---------|---------|---------|---------|
| Test statistic | 1.36 | -.598 | .950 | .039 | -.668 | -.077 | .718 |
| P-value | .174 | .550 | .342 | .969 | .504 | .939 | .473 |

Notes: In this table, we report results for tests of random assignment of children to classrooms within schools using a methodology proposed by Jochmans (2023). The null hypothesis is absence of correlation between a child's ability measured at the end of the previous grade and the average ability of classroom peers assigned to her at the beginning of a given grade, conditional on school. The sample includes all children.

Table A2: Testing for random assignment of children to classrooms, restricted sample

| | Kindergarten | Grade 1 | Grade 2 | Grade 3 | Grade 4 | Grade 5 | Grade 6 |
|----------------|--------------|---------|---------|---------|---------|---------|---------|
| Test statistic | 1.39 | -.266 | 1.38 | .148 | -.202 | .208 | .815 |
| P-value | .164 | .791 | .169 | .883 | .840 | .835 | .415 |

Notes: In this table, we report results for tests of random assignment of children to classrooms within schools using a methodology proposed by Jochmans (2023). The null hypothesis is absence of correlation between a child's ability measured at the end of the previous grade and the average ability of classroom peers assigned to her at the beginning of a given grade, conditional on school. The sample is restricted to children who have available both beginning- and end-of-grade scores for a given grade.

Appendix B

This appendix presents additional information on test scores, executive function, and non-cognitive skills. Figure B1 presents the univariate densities of our achievement measures, separately by grade. The figure shows that most of the distributions appear to have a reasonable spread and are generally symmetric. One clear exception is math achievement in kindergarten, which is left-censored.

Figure B2 presents comparable densities for executive function. It shows that the distributions of inhibitory control and cognitive flexibility are often highly skewed. This is not surprising given the nature of the tests. As an example, we describe the executive function tests we applied in kindergarten.

In the inhibitory control test, kindergarten children were quickly shown a series of 14 flash cards that had either a sun or a moon and were asked to say the word “day” when they saw the moon and “night” when they saw the sun. Just over half (50.8 percent) of all children made no mistake on this test, so there is a concentration of mass at the highest value, while very few children (1.6 percent) answered all prompts incorrectly.

The cognitive flexibility test we applied in kindergarten worked as follows. Children were handed a series of picture cards, one by one. Cards had either a truck or a star, in red or blue. The enumerator asked the child to sort cards by *color*, or by *shape*. Specifically, in the first half of the test, the enumerator asked the child to play the “colors” game, handed her cards, indicating their color, and asked the child to place them in the correct pile (“this is a red card: where does it go?”). After 10 cards, the enumerator told the child that they would switch to the “shapes” game, and reminded the child that, in this game, trucks should be placed in one pile and stars in another. The enumerator then handed the child cards, indicating the shapes on the card, and asked her to place them in the correct pile (“this is a star: where does it go?”). In both the first and the second part of the test, if the child made three consecutive mistakes, the enumerator paused the test, reminded her what game they were playing (“remember we are playing the shapes game; in the shapes game, all trucks go in this pile, and all stars in this other pile”), and handed the child a new card with the corresponding instruction. A small proportion of children in kindergarten (7.5 percent) did not understand the game, despite repeated examples, and were given a score of 0; just under half of all children (47 percent) answered all prompts correctly in both the “colors” and “shapes” parts of the test; and just over a quarter (27.3 percent) of all children made no mistakes in the first part of the test (the “colors” game), but incorrectly classified every card in the second part of the test (the “shapes” game). These children were unable to switch rules, despite repeated promptings from the enumerator. The distribution of scores for this test therefore has a concentration of mass at two points, with much less mass at other points.

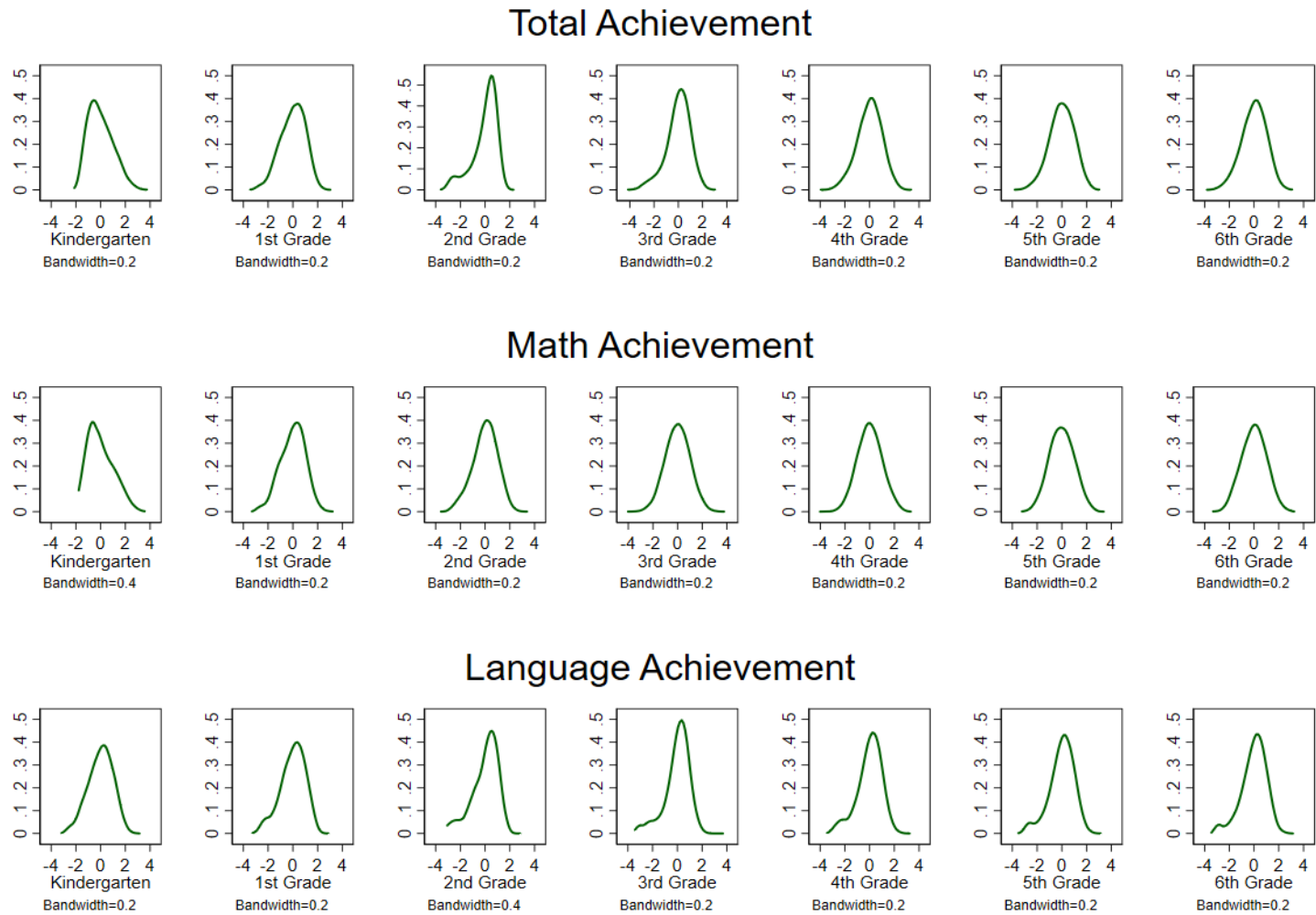
The working memory test had two parts. In the first part, children were given 2 minutes to find as many sequences of dog, house, and ball, in that order, on a sheet that has rows of dogs, houses, and balls in various possible sequences. The score on this part of the test is the number of correct sequences found by the child. In the second part of the test, the enumerator recited strings of numbers, and asked the child to repeat them, in the same order or backwards. Figure B2 shows that the aggregate working memory score is distributed smoothly, with little evidence of a concentration of mass at particular values.

In practice the correlations of the scores across the three dimensions in our sample are low—in the range of 0.21 to 0.32 between cognitive flexibility and working memory, between 0.17 and 0.33 between working memory and inhibitory control, and in the range of 0.12 to 0.15 between cognitive flexibility and inhibitory control—see Appendix Table B3.² When the scores across the three dimensions are averaged, the distributions of the total executive function score are generally smooth and symmetric.

Figure B3, finally, shows univariate densities of the four non-cognitive measures we applied in 6th grade. The figure shows that the distribution of the depression and grit scores appear to be right-censored. The distribution for the aggregate measure of non-cognitive outcomes, on the other hand, is smooth and symmetric. Table B4 shows that the different non-cognitive outcomes are positively correlated, although the correlations are far from unity—they range from 0.20 (between depression and grit) to 0.49 (between growth mindset and self-esteem).

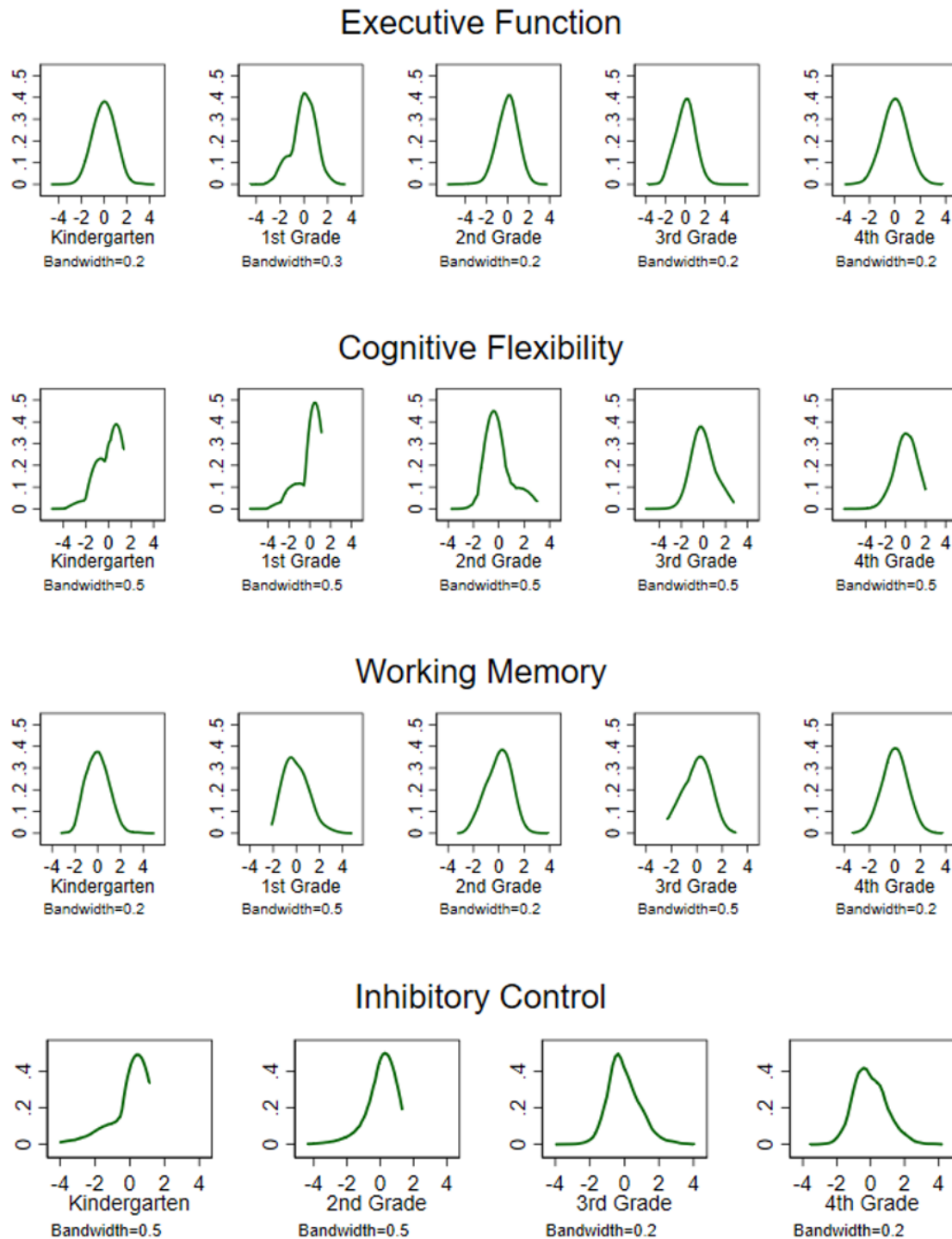
² The fact that these correlations are very low is likely to be a result of both measurement error and differences across the constructs that each domain measures.

Figure B1: Distributions of achievement, by grade



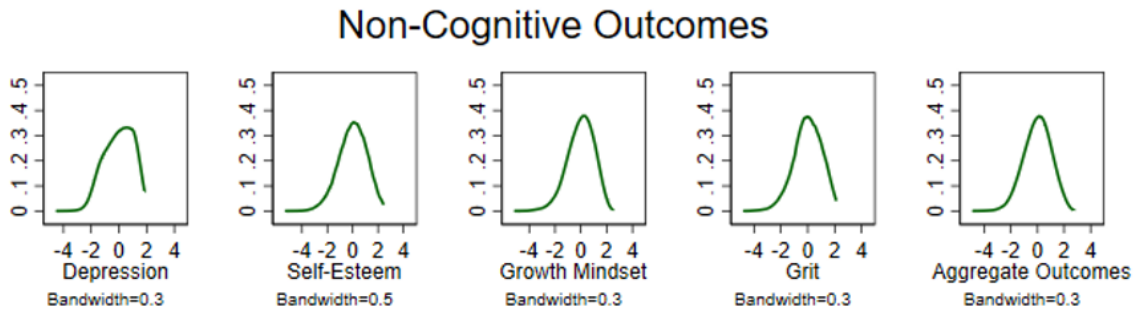
Notes: The figure shows univariate densities of achievement, in z-scores, by grade.

Figure B2: Distributions of executive function, by grade



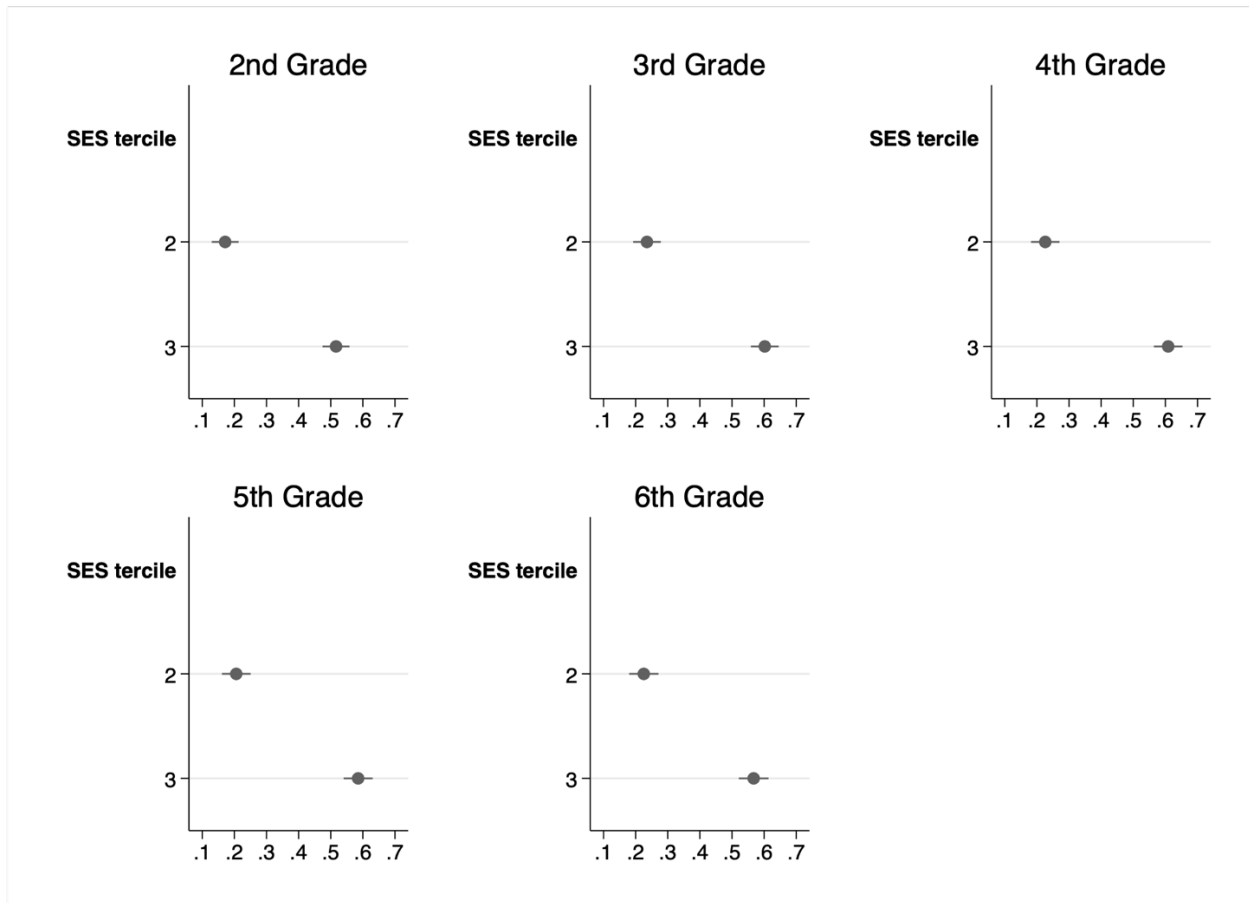
Notes: The figure shows univariate densities of executive function, in z-scores, by grade.

Figure B3: Distributions of non-cognitive outcomes



Notes: The figure shows univariate densities of non-cognitive outcomes at the end of 6th grade, in z-scores.

Figure B4: SES gradients in math test scores, by grade



Notes: The figure shows SES-gradients in math achievement in z-scores, by grade. SES is measured using a factor constructed using information at baseline on mother's education, father's education and household wealth.

Table B1: Summary statistics for score components

| Grade | Test | N | Mean | SD |
|---------------------------|----------------------------------|-------|------|------|
| Kindergarten | | | | |
| Executive Function | Memory | 14522 | .269 | .208 |
| | Card sorting | 14511 | .799 | .225 |
| | Day and night | 14506 | .848 | .242 |
| | Indicators comprehension | 14519 | .617 | .166 |
| Language | Letters and words identification | 14522 | .125 | .157 |
| | Initial sound identification | 14517 | .017 | .086 |
| | Oral comprehension | 14510 | .394 | .198 |
| | Knowledge of letter sounds | 14522 | .050 | .141 |
| | Vocabulary on images test "TVIP" | 14337 | .297 | .143 |
| Math | Number identification | 14522 | .372 | .229 |
| | Block rotation | 14522 | .805 | .156 |
| | Sequences | 14522 | .256 | .299 |
| | Word problems | 14512 | .252 | .163 |
| 1st Grade | | | | |
| Executive Function | Memory | 17227 | .310 | .186 |
| | Card sorting | 17227 | .857 | .247 |
| | Pair Cancellation | 16347 | .240 | .095 |
| | Matrix | 17227 | .485 | .294 |
| Language | Letters and words identification | 16364 | .741 | .265 |
| | Tales | 17265 | .297 | .256 |
| | Syllable identification | 17265 | .438 | .270 |
| | Vocabulary on images test "TVIP" | 16339 | .533 | .247 |
| Math | Number identification | 16158 | .653 | .175 |
| | Arithmetic | 17265 | .362 | .246 |
| | Word problems | 16353 | .491 | .254 |
| | Number line | 16368 | .782 | .123 |
| 2nd Grade | | | | |
| Executive Function | Memory | 16839 | .445 | .197 |
| | Card sorting | 18393 | .696 | .232 |
| | Pair Cancellation | 16848 | .370 | .114 |
| | Words and colors - Stroop | 14354 | .218 | .071 |
| | Numbers and amounts - Stroop | 18393 | .833 | .270 |
| Language | Letters and words identification | 18316 | .826 | .310 |
| | Tales | 18393 | .279 | .254 |
| | Writing fluency | 18393 | .598 | .313 |
| | Reading Comprehension | 18393 | .296 | .245 |
| | Vocabulary on images test "TVIP" | 16844 | .452 | .168 |
| Math | Sequences | 18481 | .399 | .234 |
| | Position Value | 16846 | .366 | .136 |
| | Arithmetic | 18481 | .406 | .230 |
| | Word problems | 18393 | .300 | .190 |
| | Number line | 16874 | .841 | .073 |
| 3rd Grade | | | | |
| Executive Function | Triangles and squares | 17518 | .695 | .163 |
| | Memory | 17518 | .425 | .202 |
| | Pair Cancellation | 17279 | .428 | .109 |
| | Words and colors - Stroop | 16142 | .240 | .061 |

| | | | | |
|---------------------------|----------------------------------|-------|------|------|
| Language | Letters and words identification | 17518 | .931 | .193 |
| | Writing fluency | 17521 | .676 | .246 |
| | Reading Comprehension | 17521 | .443 | .206 |
| | Vocabulary on images test "TVIP" | 17276 | .446 | .142 |
| Math | Sequences | 17521 | .496 | .231 |
| | Word problems | 17521 | .390 | .208 |
| | Position Value | 17521 | .386 | .182 |
| | Arithmetic | 17521 | .527 | .227 |
| | Number line | 17277 | .847 | .095 |
| 4th Grade | | | | |
| Executive Function | Triangles and squares | 17424 | .768 | .146 |
| | Memory | 17425 | .466 | .161 |
| | Pair Cancellation | 17434 | .454 | .112 |
| | Words and colors - Stroop | 16920 | .271 | .066 |
| Language | Reading fluency | 17428 | .783 | .078 |
| | Writing fluency | 17422 | .081 | .073 |
| | Reading Comprehension | 17425 | .113 | .147 |
| | Vocabulary on images test "TVIP" | 17434 | .345 | .162 |
| Math | Sequences | 17432 | .091 | .074 |
| | Word problems | 17424 | .078 | .101 |
| | Position Value | 17424 | .058 | .067 |
| | Arithmetic | 17426 | .205 | .150 |
| 5th Grade | | | | |
| Language | Reading fluency | 17529 | .443 | .145 |
| | Writing fluency | 17529 | .628 | .251 |
| | Reading Comprehension | 17529 | .454 | .171 |
| | Vocabulary on images test "TVIP" | 17529 | .686 | .140 |
| Math | Sequences | 17529 | .538 | .219 |
| | Word problems | 17529 | .481 | .208 |
| | Position Value | 17529 | .453 | .201 |
| | Arithmetic | 17529 | .455 | .220 |
| 6th Grade | | | | |
| Language | Reading fluency | 17265 | .519 | .162 |
| | Writing fluency | 17266 | .418 | .160 |
| | Reading Comprehension | 17266 | .535 | .132 |
| | Vocabulary on images test "TVIP" | 17266 | .476 | .164 |
| Math | Sequences | 17266 | .483 | .240 |
| | Word problems | 17266 | .411 | .178 |
| | Position Value | 17266 | .564 | .251 |
| | Arithmetic | 17266 | .466 | .209 |

Notes: The table reports summary statistics for each sub-component of the scores in executive function, language and math for each grade. The mean measures the proportion of students obtaining a correct score in each sub-component of the scores in executive function, language and math for each grade. We stop administering tests for executive function after 4th grade.

Table B2: Correlations math z-scores and lagged math z-scores, by grade

| | Grade | | | | |
|--------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| | 2 | 3 | 4 | 5 | 6 |
| Lagged score | .810*** (.005) | .837*** (.005) | .868*** (.004) | .878*** (.004) | .893*** (.004) |
| N | 14,766 | 15,301 | 15,850 | 16,077 | 16,105 |

Notes: Table presents the results from pairwise correlations between math z-scores at the end of each grade and lagged math z-scores. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table B3: Correlations across dimensions in executive function

| | Inhibitory Control | Cognitive Flexibility |
|-----------------------|--------------------|-----------------------|
| Kindergarten | | |
| Cognitive Flexibility | 0.13 | |
| Working Memory | 0.22 | 0.29 |
| 1 st Grade | | |
| Working Memory | | 0.23 |
| 2 nd Grade | | |
| Cognitive Flexibility | 0.15 | |
| Working Memory | 0.25 | 0.24 |
| 3 rd Grade | | |
| Cognitive Flexibility | 0.12 | |
| Working Memory | 0.17 | 0.21 |
| 4 th Grade | | |
| Cognitive Flexibility | 0.15 | |
| Working Memory | 0.33 | 0.32 |
| Pooled | | |
| Cognitive Flexibility | 0.14 | |
| Working Memory | 0.24 | 0.26 |

Notes: The table reports the pairwise correlations between executive function dimensions. All the correlations are significant at the 1 percent level.

Table B4: Correlations across non-cognitive outcomes

| | Depression | Self- Esteem | Growth Mindset |
|----------------|------------|--------------|----------------|
| Self- Esteem | 0.24 | | |
| Growth Mindset | 0.26 | 0.49 | |
| Grit | 0.20 | 0.45 | 0.38 |

Notes: Table presents the results from pairwise correlations between non-cognitive outcomes collected in 6th grade. All the correlations are significant at the 1 percent level.

Table B5: Correlations across national rank outcomes over time

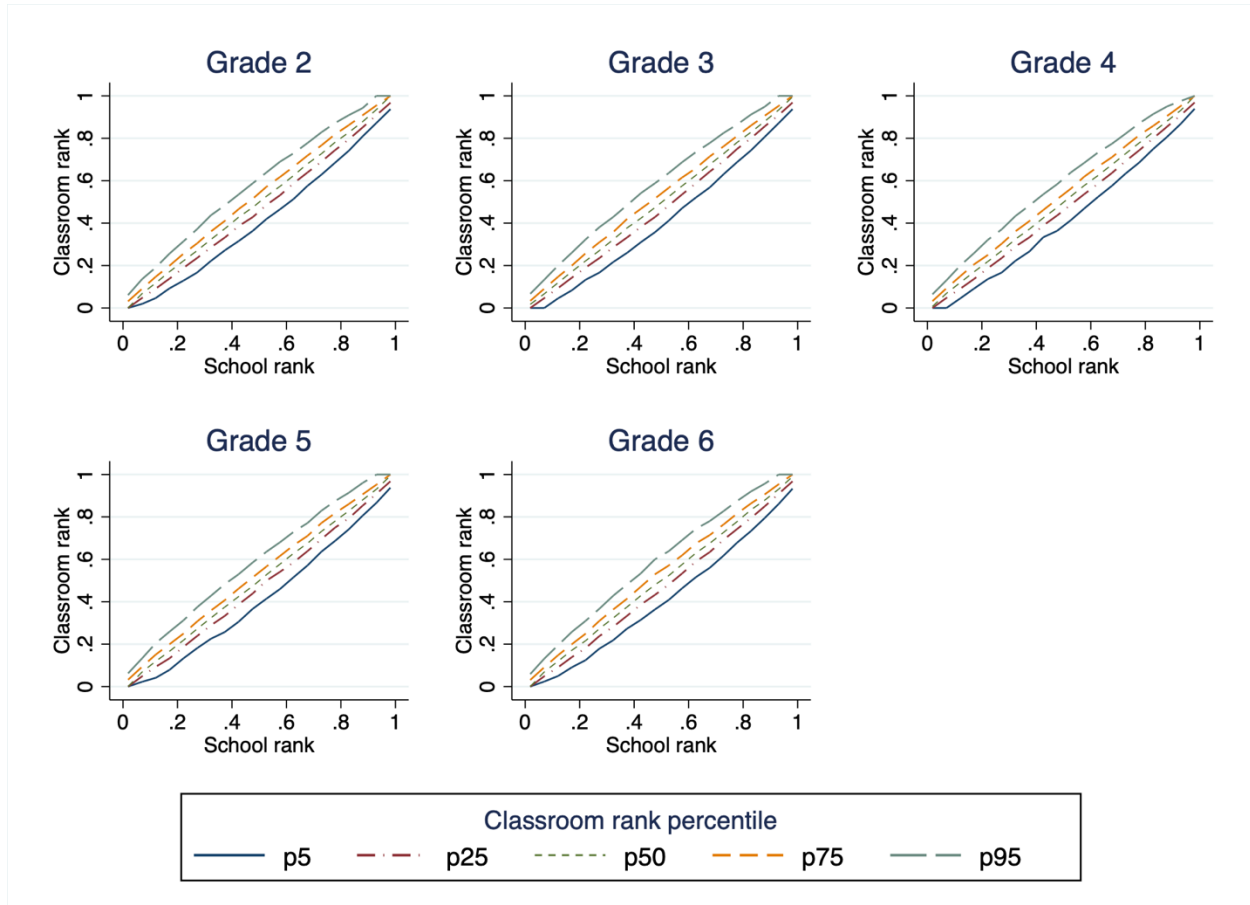
| | National rank math in t | National rank math in t-1 | National rank language in t |
|-------------------------------|-------------------------|---------------------------|-----------------------------|
| National rank math in t-1 | .815 | | |
| National rank language in t | .687 | .661 | |
| National rank language in t-1 | .654 | .684 | .773 |

Notes: Table presents the results from pairwise correlations between national rank in math (language) in a given grade and lagged national rank in math (language).

Appendix C

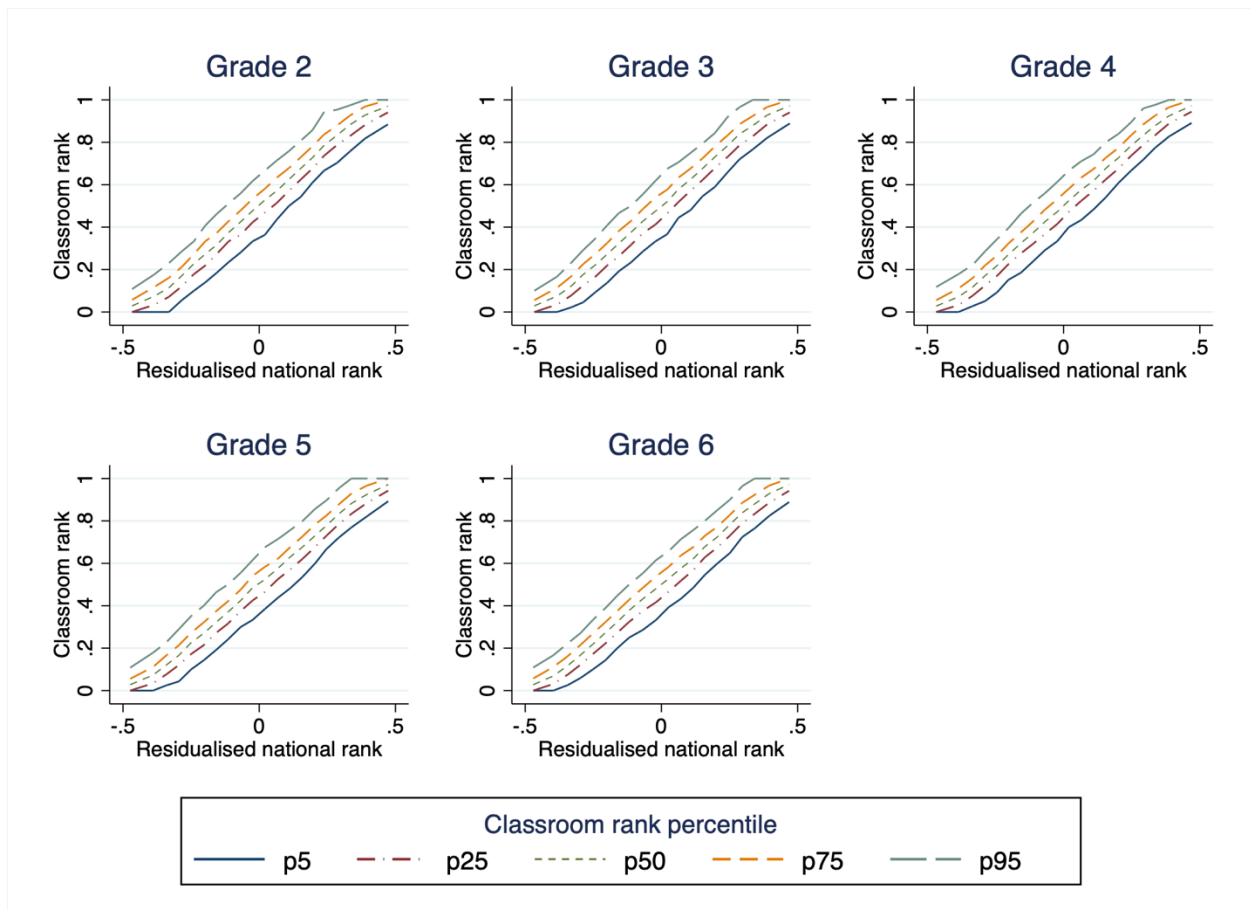
In this Appendix, we provide evidence of the variation in classroom achievement rank within school for Grades 2 to 6.

Figure C1: Percentiles of classroom rank by school rank, Grades 2 to 6



Notes: To construct this figure we plot the 5th, 25th, 50th, 75th and 95th percentile of classroom rank within each ventile of school rank, against the median school rank in that ventile, for each grade, measured by an index of math and language.

Figure C2: Percentiles of classroom rank by residualised national rank, Grades 2 to 6



Notes: To construct the figure, we first regress national ability rank on school fixed effects and derive residuals. Then we plot percentiles of classroom rank within each ventile of residualised national ability rank, against the median residualised national rank in that ventile, for each grade, measured by an index of math and language.

Appendix D

Our sample is characterized by the fact that, in each grade, students may leave a school (attritors), or join a school (new entrants). As a result, our regression samples change slightly across specifications. Table D1 shows that attritors and new entrants have significantly lower levels of learning, as measured by national rank in math. In table D1 Panel A, we regress learning in math at the end of last grade (and thus the last information on learning available at the beginning of a given grade) on a dummy for being an attritor at the beginning of a given grade. We do this for every grade. Our results suggest that students who leave the school have significantly lower levels of learning, compared to students who do not leave. Panel B of Table D1 shows results for a similar regression for new entrants, regressing learning at the end of the grade on a dummy for being a new entrant in that grade, for every grade. New entrants have significantly lower learning in math compared to regular students.

Next, we describe the multiple imputation procedure (as described in Little and Rubin, 2019) that we implement to investigate the sensitivity of our results to missing data. To describe this procedure, we start by recalling our main equation of interest, equation (3.1) for national rank in math:

$$Y_{i,s,c,t} = \beta CR_{i,s,c,t} + g_t(Y_{i,s,c,t-1}) + \delta_{ct} + \varepsilon_{i,s,c,t}$$

Selective attrition could generate a correlation between $CR_{i,s,c,t}$ and $\varepsilon_{i,s,c,t}$ that could lead to biased estimates of β . The imputation procedure we use assumes that attrition up to grade t is random conditional on the past test score, classroom assignment, and controls. More formally, assume that $P_{i,s,c,t} = 1$ if student j is still in the sample by the end of grade t . Denote $\varphi_t()$ as the density of $\varepsilon_{i,s,c,t}$. Then the assumption is:

$$\varphi_t(\varepsilon_{i,s,c,t} | CR_{i,s,c,t}, Y_{i,s,c,t-1}, P_{i,s,c,t} = 1) = \varphi_t(\varepsilon_{i,s,c,t} | CR_{i,s,c,t}, Y_{i,s,c,t-1}) \quad (\text{D.1})$$

D.1 Single imputation

We now explain what a single imputation procedure would do before we move on to the multiple imputation procedure we use, which builds on a single imputation procedure. The goal is to impute test scores for individuals who have left the sample at each date, and for those who are new entrants. We first describe the imputation for attritors. Note that, for attritors, one also needs to impute classroom assignments but that can be done trivially given that classrooms are assigned at random in every grade. To impute test scores, we start by estimating the parameters of the following model for test scores at the end of kindergarten:

$$Y_{j,s,c,1} = f_1^k(Y_{j,s,c,0}^k) + \zeta^1 X_{j,s,c,0} + \tau_{s,c,1}^1 + \kappa_{j,s,c,1} \quad (\text{D.2})$$

where $f_1^k(Y_{j,s,c,0}^k)$ is a third-order polynomial in lagged scores of skill k , $X_{j,s,c,0}$ is a vector of controls including age and gender of the student, and $\tau_{s,c,1}^1$ are classroom fixed effects. All parameters are indexed by superscript 1 to indicate they refer to kindergarten (the first year of elementary school). Using this model one can predict what $Y_{j,s,c,1}$ (test scores at the end of kindergarten) would be for those leaving the sample between the beginning and the end of kindergarten. A similar procedure can then be used to predict test scores at the end of 1st grade: $Y_{j,s,c,1}$. There are, however, now two types of attritors one needs to consider: A) those who started (but did not end) 1st grade in our sample, for whom we know classroom assignment; B) those who left the sample before the start of 1st grade, and for whom we therefore do not know what their classroom assignment would have been had they stayed in the sample. We estimate the following equation for test scores at the end of first grade:

$$Y_{j,s,c,2} = f_2^k(Y_{j,s,c,1}^k) + \zeta^2 X_{j,s,c,1} + \tau_{s,c,2}^2 + \kappa_{j,s,c,2} \quad (\text{D.3})$$

We use this equation to predict 1st grade test scores given all lagged scores and all lagged classroom assignments. For individuals in case A) above this equation can be readily used to predict their test scores. For individuals in case B), we need first to assign them a 1st grade classroom. We impute classroom assignment at random, consistent with the randomization procedure taking place in schools. Some of these students were also missing end-of-kindergarten test scores, because they left the sample before the end of kindergarten. In that case, we use the imputed value from the end-of-kindergarten imputation regression as their end-of-kindergarten score. Note that classroom ranks are updated to include the students who have now been assigned an imputed classroom and lagged score. We proceed analogously for the subsequent grades. The basic imputation equation for grade t is:

$$Y_{j,s,c,t} = f_t^k(Y_{j,s,c,t-1}^k) + \zeta^t X_{j,s,c,t-1} + \tau_{s,c,t}^t + \kappa_{j,s,c,t} \quad (\text{D.4})$$

The procedure for new entrants is analogous to the one just described for attritors, although in this case we impute scores "backwards". Note that, for new entrants, we do not need to impute classrooms, as we know their classroom assignment in the grade they appear. To impute lagged scores for new entrants, the basic imputation equation is given by:

$$Y_{j,s,c,t-1} = h_t^k(Y_{j,s,c,t}^k) + \mu^t X_{j,s,c,t} + \lambda_{s,c,t}^t + \eta_{j,s,c,t} \quad (\text{D.5})$$

D.2 Multiple imputation

This single imputation procedure is one step of the more complex multiple imputation procedure we implement in this paper.

Step 1: q imputations. The first step of this procedure is to generate m sets of imputed scores. The parameters of the imputation regressions described above, $\{f_t^k(), \zeta^t, \tau^t, h_t^k(), \mu^t, \lambda^t\}$, are estimated with error. The multiple imputation procedure takes into account this error by considering more than one set of imputed values for the missing data. The idea is to take q draws (in our case $q = 20$) from the joint distribution of $\{f_t^k(), \zeta^t, \tau^t, h_t^k(), \mu^t, \lambda^t\}$. Conceptually, one could do this by assuming they have a joint normal distribution. In practice, with a very high dimensional set of parameters, this is difficult. Another reason why this is difficult in our setting is because we have many imputation models, one for each grade, where the model for grade t uses imputed values in grade $t - 1$. Therefore, we instead bootstrap the single imputation procedure, using 20 replications, and using the parameters of these 20 replications as the 20 draws we need: $\{f_t^k(), \zeta^t, \tau^t, h_t^k(), \mu^t, \lambda^t\}^q$. Using each $\{f_t^k(), \zeta^t, \tau^t, h_t^k(), \mu^t, \lambda^t\}$, we can get q sets of imputed scores, $\{Y_{j,s,c,t}\}^q$. This allows to construct q sets of complete datasets, with no missing data, with randomly assigned classrooms (denoted $A_{j,t}$) used when needed: $\{Y_{j,s,c,t}, A_{j,t}\}^q$.

Step 2: estimate model q times and get q sets of estimated parameters. The second step is to estimate the model q times using the q complete datasets: $\{Y_{j,s,c,t}, A_{j,t}\}^q$. We estimate the model in the same fashion as the paper, but now including the children with imputed scores in our classroom rank measure. This gives us m sets of estimated parameters of equation 3.1, notably: $\{\beta_t\}^q$. From it we can also construct standard errors for each of these q estimates, which we label $\{\sigma_t^2\}^q$.

Step 3: integrate the q estimates. In order to integrate the q estimates and the corresponding variances we use the following results:

$$\beta_t = \frac{1}{q} \sum_{k=1}^q \beta_t^q \quad (\text{D.6})$$

$$\sigma_t^2 = \frac{1}{q} \sum_{k=1}^q \sigma_t^{2,q} + \frac{1}{q-1} \sum_{k=1}^q (\beta_t^q - \beta_t)^2 \quad (\text{D.7})$$

The estimated effects of contemporaneous classroom rank on end-of-grade achievement correcting for selective attrition using multiple imputation are virtually identical to those from our main model: the estimated coefficient is .040 (with standard error .015), compared to an estimated coefficient of .040 (with standard error .010) from our main estimates (reported in column 2, table 2 in the main body of the paper).

We adapt the multiple imputation procedure described above to perform two sets of robustness checks. First, we use multiple imputation to conduct a balancing exercise in which we test for the presence of correlation between pre-determined child characteristics and classroom rank at the beginning of a given grade. These pre-determined characteristics are national rank in *TVIP* scores measured at baseline, national rank in a factor capturing family-level characteristics at baseline (constructed using factor analysis on variables measuring mother's education, father's education and household wealth), child gender and age. To conduct the balancing exercise for national rank in *TVIP* scores and for the family factor (both measured at baseline), we need to complement the procedure described above by imputing these outcomes for new entrants using equation (D.5). The estimated model in this exercise regresses pre-determined child characteristics on classroom achievement rank pooling across grades, controlling for a third-order polynomial in lagged national achievement rank and classroom-by-grade fixed effects. The results from this exercise are presented in Table D2. We perform this exercise separately using classroom rank in the math+language index (Panel A), classroom rank in math (Panel B) and classroom rank in language (Panel C). Second, we use the multiple imputation procedure described above to verify the robustness of our dynamic estimates of the impact of early classroom rank on achievement in later grades. To this end, we impute later grade scores for attritors based on national rank in math at the end of kindergarten. Similarly, we impute national rank in math at the end of kindergarten for new entrants based on national rank in math in the grade they first appear in the sample. The estimated model in this exercise is a regression of the effects of early classroom rank on later grade achievement analogous to equation (3.7) in the main body of the paper. Results for this exercise are presented in Table D3, which compares results with and without multiple imputation. Panel A shows the results from our model estimates that include the data generated by the multiple imputation procedure, whereas Panel B reproduces the results in the first row of Table 4 in the main body of the paper. If anything, the magnitudes of the estimated coefficients are slightly larger when we correct for selective attrition using multiple imputation with respect to the estimates from our main model. The results on dynamic effects of early classroom rank on later grade achievement are qualitatively robust to correcting for selective attrition.

Table D1: Math performance of attritors and new entrants

| | Grade 1 | Grade 2 | Grade 3 | Grade 4 | Grade 5 | Grade 6 |
|-------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| Attritor | -.048*** (.007) | -.132*** (.007) | -.098*** (.007) | -.059*** (.008) | -.073*** (.008) | -.049*** (.008) |
| New entrant | -.028*** (.005) | -.020*** (.007) | -.011 (.007) | -.035*** (.008) | -.056*** (.008) | -.049*** (.009) |

Notes: Panel A displays coefficients from estimates of national rank in math at the beginning of a given grade on whether the student is an attritor in that grade. Different columns correspond to different grades. Panel B displays coefficients from estimates of national rank in math at the end of a given grade on whether the student is a new entrant in that grade. Different columns correspond to different grades. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table D2: Balancing exercise correcting for selective attrition using multiple imputation

| | TVIP | Family factor | Child is female | Child age |
|--|-----------------|-----------------|-----------------|-----------------|
| <i>Classroom rank in math+language index</i> | | | | |
| 1st Grade | .095 (.050) | .074 (.043) | -.039 (.080) | -.687 (1.50) |
| 2nd Grade | .046 (.037) | .073 (.041) | -.118 (.085) | -1.71 (1.57) |
| 3rd Grade | .017 (.039) | .027 (.041) | -.008 (.089) | -.580 (1.33) |
| 4th Grade | .025 (.047) | .018 (.042) | -.092 (.083) | -2.04 (1.79) |
| 5th Grade | -.012 (.053) | -.021 (.039) | -.087 (.094) | -.039 (1.69) |
| 6th Grade | .017 (.049) | -.008 (.043) | -.074 (.083) | 1.40 (1.67) |
| <i>Classroom rank in math</i> | | | | |
| 1st Grade | .100* (.052) | .014 (.044) | -.034 (.068) | .515 (1.50) |
| 2nd Grade | .072* (.043) | .059 (.038) | -.006 (.088) | -1.66 (1.36) |
| 3rd Grade | -.008 (.044) | .014 (.045) | -.040 (.085) | 1.28 (1.33) |
| 4th Grade | .031 (.046) | -.009 (.044) | -.082 (.077) | .233 (1.76) |
| 5th Grade | -.005 (.056) | -.015 (.042) | .058 (.088) | -1.18 (1.51) |
| 6th Grade | .033 (.049) | .008 (.045) | -.047 (.087) | .984 (1.61) |
| <i>Classroom rank in language</i> | | | | |
| 1st Grade | .061 (.052) | .038 (.053) | -.051 (.077) | 2.09 (1.93) |
| 2nd Grade | .054 (.037) | .067* (.035) | -.074 (.084) | -.027 (1.21) |
| 3rd Grade | .037 (.044) | .042 (.036) | -.026 (.080) | -1.91 (1.57) |
| 4th Grade | .012 (.045) | .031 (.045) | -.084 (.095) | -1.62 (1.50) |
| 5th Grade | .016 (.048) | -.051 (.041) | -.125 (.093) | .805 (1.57) |
| 6th Grade | .037 (.050) | -.024 (.053) | -.016 (.098) | 1.05 (1.65) |

Notes: This table presents estimated coefficients from a balancing exercise testing for the presence of correlation between pre-determined child characteristics and classroom rank at the beginning of a given grade, correcting for selective attrition using the multiple imputation procedure in Little and Rubin (2019) described in Appendix D. Column 1 uses national rank in TVIP scores measured at baseline as the outcome, column 2 uses national rank in a factor capturing family-level characteristics at baseline (constructed using factor analysis on variables measuring mother's education, father's education and household wealth) as the outcome, columns 3 and 4 use child gender and age as the outcomes, respectively. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table D3: Dynamics correcting for selective attrition using multiple imputation

| | Lags | | | | |
|---|-------------------|-------------------|-------------------|-------------------|-------------------|
| | 0 | 1 | 2 | 3 | 4 |
| Classroom rank "early" (1st & 2nd grades) | .084*** (.028) | .103*** (.032) | .112*** (.039) | .114*** (.038) | .124*** (.039) |
| Classroom rank "early" (1st & 2nd grades) | .064*** (.017) | .077*** (.019) | .090*** (.021) | .096*** (.022) | .109*** (.021) |

Notes: Panel A of the table reports estimates from regressions of national rank in math on classroom math rank for different lags of classroom rank for children in “early” (1st and 2nd) grades, correcting for selective attrition using the multiple imputation procedure in Little and Rubin (2019) described in Appendix D. Panel B of the table reproduces our main estimates from regressions of national rank in math on classroom math rank for different lags of classroom rank for children in “early” (1st and 2nd) grades, reported in Table 4 in the main body of the paper. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table D4: Effect of classroom rank excluding schools in the top 10% of the distribution of new entrants

| | Math |
|----------------|-------------------|
| Classroom rank | .044*** (.010) |

Notes: The table reports estimates from regressions of national rank in math on classroom math rank, pooling observations across grades. We exclude from the regression schools that are in the top 10% of the distribution of new entrants. In every grade, we count how many new entrants are in each school. Then, in the regression we exclude schools that are in the top 10% of the distribution of new entrants in each grade. We include a third-order polynomial in lagged math achievement as a control. The regression controls for classroom-by-grade fixed effects. The regression is limited to schools in which there are at least two classrooms per grade. Standard errors are clustered at the school level. N is 79,165. *Significant at 10%, **significant at 5%, ***significant at 1%.

Appendix E

Robustness checks: Table E1 presents robustness checks.

Table E1: Robustness checks, effects of math classroom rank on math achievement

| | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
|------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| Classroom rank in math | .040*** (.010) | .040*** (.010) | .063*** (.010) | .063*** (.010) | .040*** (.010) | .041*** (.010) | .107*** (.008) |
| N | 87,713 | 87,713 | 87,713 | 87,713 | 87,713 | 87,713 | 87,713 |
| Age and gender | | X | | | | | |

Notes: The table reports estimates from regressions of national rank in math on classroom math rank. Observations are pooled across grades. All estimates include classroom-by-grade fixed effects. Column (1) reproduces the result from column (2) of Table 2. Column (2) is comparable to column (1) but adds controls for child gender, age, and its square. In columns (3), (4), (5) and (6), lagged achievement in math enters the regression as a linear term, quadratic term, fourth-order polynomial or controlling for dummies of percentiles of lagged math achievement (as opposed to a cubic term). Column (7) corresponds to estimates of equation (3.4) in the main text. All regressions are limited to schools in which there are at least two classrooms per grade. Standard errors are clustered at the school level throughout. *Significant at 10%, **significant at 5%, ***significant at 1%.

Grade-specific estimates of effects of classroom rank: Table E2 presents estimates of math classroom rank effects, by grade (rather than when grades are aggregated into “early”, “middle” and “late” periods). These results are consistent with those in the first column of Table 4 in the main body of the paper, although they are noisier.

Table E2: Grade-specific estimates of effects of classroom rank

| | Grade | | | | | |
|----------------|-------------------|-----------------|----------------|-------------------|----------------|-----------------|
| | 1 | 2 | 3 | 4 | 5 | 6 |
| Classroom rank | .081*** (.025) | .045* (.023) | .030 (.024) | .065*** (.022) | .029 (.019) | -.019 (.022) |
| N | 12,161 | 14,534 | 14,823 | 15,255 | 15,350 | 15,590 |

Notes: The table reports estimates from regressions of national rank in math on classroom math rank, separately by grade. All regressions are limited to schools in which there are at least two classes. All regressions include a third order polynomial in lagged national rank in math and classroom-by-grade fixed effects. Standard errors are clustered at the school level. *Significant at 10%, **significant at 5%, ***significant at 1%.

Weighted effects of classroom rank across deciles of lagged national rank: Table E3 presents estimates of the weighted sum of effects of math classroom rank on national rank in math across deciles of lagged national rank in math. To derive this estimate, we estimate our main specification (equation 3.1) adding to the specification interactions of classroom rank in math with deciles of lagged national rank in math.

Table E3: Weighted sum of effects of math classroom rank across deciles of lagged national rank in math

| | Math |
|----------------|-------------------|
| Classroom rank | .041*** (.010) |

Notes: The table reports estimates of impacts of classroom rank in math on national rank in math using our main specification in equation (3.1), adding to the specification interactions of classroom rank in math with deciles of lagged national rank in math. We derive the weighted sum of effects of classroom rank across deciles of lagged national rank. Standard errors are clustered at the school level. *Significant at 10%, **significant at 5%, ***significant at 1%.

Effect of classroom rank controlling for mean of peer ability and standard deviation of peer ability:

Table E4 presents estimates of the effect of math classroom rank on national rank in math, controlling for the leave-one-out mean of classroom peer ability in math and for the leave-one-out standard deviation of classroom peer ability in math, as well as an interaction between the two.

Table E4: Effect of math classroom rank controlling for peer ability

| | (1) | (2) | (3) | (4) |
|--|------------------|------------------|------------------|------------------|
| Classroom rank | .026** (.010) | .024** (.010) | .023** (.010) | .023** (.010) |
| Leave-one-out mean of classroom peers * Lagged achievement | | -.019 (.022) | -.019 (.021) | -.159 (.151) |
| Leave-one-out SD of classroom peers * Lagged achievement | | | -.004 (.063) | -.289 (.311) |
| Interaction: Mean * SD * Lagged achievement | | | | .544 (.595) |

Notes: The table reports estimates from regressions of achievement national rank on classroom rank and the leave-one-out mean and standard deviation of classroom peer achievement, pooling observations across grades. In Column (1) we regress national rank on classroom rank at the beginning of the school year, including a third-order polynomial in lagged national rank. Column (2) combines classroom rank and the leave-one-out mean of classroom peers interacted with lagged achievement. Column (3) adds the leave-one-out standard deviation of classroom peer achievement, interacted with lagged achievement. Column (4) adds an interaction between the leave-one-out mean and standard deviation, also interacted with lagged achievement. All regressions include school-by-grade fixed effects. All regressions are limited to schools in which there are at least two classrooms per grade. Standard errors are clustered at the school level throughout. N is 87,713 observations in all columns. *Significant at 10%, **significant at 5%, ***significant at 1%.

Effect of classroom rank in age on national rank in math: Table E5 reports estimates of classroom rank in age on national rank in math, controlling for a third order polynomial in lagged national rank in math as well as child age and classroom-by-grade fixed effects.

Table E5: Effect of classroom rank in age on math ability

| | Math | |
|------------------------|-------------------|-------------------|
| Classroom rank in math | | .039*** (.010) |
| Classroom rank in age | .023*** (.004) | .023*** (.004) |

Notes: The table reports estimates of impacts of classroom rank in age on national rank in math. All regressions control for a third-order polynomial in lagged national rank in math, child age and classroom-by-grade fixed effects. N is 87,459. Standard errors are clustered at the school level throughout. *Significant at 10%, **significant at 5%, ***significant at 1%.

Appendix F

In this Appendix, we show results from additional exercises exploring dynamic effects of classroom rank, leveraging the panel structure of our dataset.

Table F1: Effects of changes in classroom rank on math achievement

| | Math |
|--|-----------------|
| Panel A | |
| Contemporaneous classroom rank | .009 (.012) |
| Lagged classroom rank | .016 (.011) |
| Interaction (Contemporaneous classroom rank * Lagged classroom rank) | .013 (.015) |
| Panel B | |
| Change in classroom rank is in bottom quartile | -.002 (.002) |
| Change in classroom rank is in top quartile | .001 (.002) |

Notes: Panel A reports estimates of the impacts of classroom achievement rank on national achievement rank, interacted with lagged classroom rank, pooling information across grades. The regression controls for a third-order polynomial in lagged national rank (i.e., period t-1) and a third-order polynomial in national rank in period t-2, as well as classroom-by-grade fixed effects. Panel B reports estimates of an exercise analogous to Elsner et al. (2021), which examines the impacts of changes in classroom achievement rank over time on national achievement rank, pooling information across grades. To construct these results, we take the difference in classroom ranks between subsequent grades. We create quartiles of the distribution of this difference. Then, we define two types of changes: rank goes up if a student is in the top quartile of the distribution of changes; rank goes down if a student is in the bottom quartile of the distribution of changes. Rank stays the same if the student is in the 2nd or 3rd quartile of the distribution. We regress national rank achievement on an indicator variable for whether the student's rank went up, an indicator variable for whether the student's rank went down, third-order polynomials in lagged national rank and national rank in period t-2 as well as classroom-by-grade fixed effects. Standard errors are clustered at the school level throughout. N is 66,917. *Significant at 10%, **significant at 5%, ***significant at 1%.

Table F2: Cumulative effects of changes in classroom rank on math achievement

| | Math 6th grade |
|--|--------------------|
| Panel A | |
| 1 positive change in classroom rank | .124*** (.006) |
| 2 positive changes in classroom rank | .231*** (.006) |
| 3 or more positive changes in classroom rank | .329*** (.011) |
| Panel B | |
| 1 negative change in classroom rank | -.117*** (.006) |
| 2 negative changes in classroom rank | -.221*** (.007) |
| 3 or more negative changes in classroom rank | -.318*** (.011) |

Notes: The table reports estimates of cumulative impacts of positive and negative changes in classroom rank in math between first and 6th grade on national rank in math at the end of 6th grade. Classroom rank changes are defined in the same way as for Table F1. The omitted category is no changes in classroom rank. The category “3 or more changes” subsumes the categories for 3 and 4 changes. The regression controls for a third-order polynomial in national rank in math in kindergarten, as well as classroom fixed effects. Standard errors are clustered at the school level. N is 9,352. *Significant at 10%, **significant at 5%, ***significant at 1%.

Appendix G

In this Appendix, we present results showing dynamic effects of school rank (instead of classroom rank) and controlling for school-by-grade fixed effects (instead of classroom-by-grade fixed effects). While we do not have random assignment at the school level, we can estimate the impact of school rank on achievement assuming that conditional on lagged ability and the school fixed effect, a student's rank within the school is random.

Table G1: Effects of math school rank on achievement, by grade and lag

| | Lags | | | | |
|---|-------------------|-------------------|-------------------|-------------------|-------------------|
| | 0 | 1 | 2 | 3 | 4 |
| School rank “early” (1 st & 2 nd grades) | .105*** (.023) | .150*** (.025) | .162*** (.025) | .173*** (.027) | .173*** (.026) |
| School rank “middle” (3 rd & 4 th grades) | .065*** (.021) | .073*** (.024) | .088*** (.025) | | |
| School rank “late” (5 th & 6 th grades) | .018 (.020) | | | | |

Notes: The table reports estimates from regressions of national rank in math on school math rank for different lags of school rank, separately for children in the “early” (1st and 2nd), “middle” (3rd and 4th), and “late” grades (5th and 6th) grades. All regressions are limited to schools in which there are at least two classes. All regressions include a third order polynomial in lagged national rank in math and school-by-grade fixed effects. Standard errors are clustered at the school level. Standard errors are clustered at the school level throughout. N lag 0, “early”: 26,695. N lag 0, “middle”: 30,078. N lag 0, “late”: 30,940. N lag 1, “early”: 24,648. N lag 1, “middle”: 28,194. N lag 2, “early”: 23,199. N lag 2, “middle”: 26,706. N lag 3, “early”: 22,140. N lag 4, “early”: 21,210. *Significant at 10%, **significant at 5%, ***significant at 1%.

Appendix H

Effects of classroom rank in math on non-cognitive skills: Table H1 shows the results from regressions of 6th grade non-cognitive skills on math classroom rank in “early” (1st and 2nd), “middle” (3rd and 4th) and “late” (5th and 6th) grades.

Table H1: Math classroom rank effect on non-cognitive skills

| | (1) | (2) | (3) | (4) | (5) |
|--|-------------------------|----------------|-----------------|----------------|----------------|
| | Non-cognitive aggregate | Depression | Self-esteem | Growth mindset | Grit |
| Classroom rank “early” (1 st & 2 nd grades) | .156 (.112) | .115 (.120) | .157 (.119) | .136 (.116) | .026 (.115) |
| Classroom rank “middle” (3 rd & 4 th grades) | .169 (.153) | .119 (.136) | .170 (.151) | .076 (.149) | .124 (.155) |
| Classroom rank “late” (5 th & 6 th grades) | .266* (.157) | .089 (.143) | .288* (.149) | .153 (.151) | .162 (.152) |

Notes: The table reports estimates from regressions of a given 6th grade non-cognitive skill, or the non-cognitive aggregate of all four skills, on classroom achievement rank in math in “early” (1st and 2nd), “middle” (3rd and 4th), and “late” grades (5th and 6th). All regressions include third order polynomials in lagged national rank in math and classroom-by-grade fixed effects. All regressions are limited to schools in which there are at least two classrooms per grade. N is 15,578. Standard errors are clustered at the school level throughout. *Significant at 10%, **significant at 5%, ***significant at 1%.

Effects of classroom rank in math and teacher perceptions of student ability on math ability: Table H2 shows effects of lagged classroom rank in math and teacher perceptions of student ability on national rank in math, pooling information for “early” (1st and 2nd), “middle” (3rd and 4th) and “late” (5th and 6th) grades.

Table H2: Effects of classroom rank and teacher perceptions of student ability on math achievement

| | Math | | | | | | | | |
|-----------------------|----------------------------|-------------------|--------------------|-----------------------------|-------------------|--------------------|---------------------------|-------------------|--------------------|
| | Early grades (1st and 2nd) | | | Middle grades (3rd and 4th) | | | Late grades (5th and 6th) | | |
| Classroom rank in t-1 | .077*** (.019) | .063*** (.019) | .074*** (.019) | .038** (.019) | .033* (.018) | .031* (.018) | .049** (.020) | .048** (.020) | .046** (.020) |
| Top 5 in t-1 | | .121*** (.004) | | | .081*** (.003) | | | .064*** (.004) | |
| Bottom 5 in t-1 | | | -.133*** (.005) | | | -.069*** (.004) | | | -.056*** (.004) |

Notes: The table reports estimates of the effects of lagged classroom rank in math and teacher perceptions of student ability on national rank in math, pooling information for “early” (1st and 2nd), “middle” (3rd and 4th) and “late” (5th and 6th) grades. Teacher perceptions of student ability are measured using indicator variables for the child being reported to be among the top 5 (bottom 5) by achievement by her teachers. All regressions control for a third-order polynomial in national rank in math in period t-2, as well as classroom-by-grade fixed effects. Standard errors are clustered at the school level throughout. N “early” 24,648. N “middle” 28,194. N “late” 14,329. *Significant at 10%, **significant at 5%, ***significant at 1%.