

A Service of

ZBW

Leibniz-Informationszentrum Wirtschaft Leibniz Information Centre for Economics

van Roye, Björn; Wesselbaum, Dennis

#### Working Paper Capital, endogenous separations, and the business cycle

Kiel Working Paper, No. 1561

**Provided in Cooperation with:** Kiel Institute for the World Economy – Leibniz Center for Research on Global Economic Challenges

*Suggested Citation:* van Roye, Björn; Wesselbaum, Dennis (2009) : Capital, endogenous separations, and the business cycle, Kiel Working Paper, No. 1561, Kiel Institute for the World Economy (IfW), Kiel

This Version is available at: https://hdl.handle.net/10419/28388

#### Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

#### Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.



## WWW.ECONSTOR.EU



## Kiel Working Papers



Kiel Institute for the World Economy

# Capital, Endogenous Separations, and the Business Cycle

by Björn van Roye and Dennis Wesselbaum

No. 1561 | October 2009

Web: www.ifw-kiel.de

Kiel Working Paper No. 1561 | October 2009

#### Capital, Endogenous Separations, and the Business Cycle

Björn van Roye and Dennis Wesselbaum

Abstract:

We implement capital in an endogenous separations New Keynesian matching model. In contrast to the vintage capital theory, we suggest a more general approach, such that workers have unrestricted access to a proportional share of the capital stock. We find that the introduction of capital generates an important channel for the transmission of aggregate productivity shocks, using capital-labor trade-off. The model generates higher volatilities of key variables and therefore enhances the performance of the matching model to generate stylized facts in response to an aggregate productivity shock. However, there is almost no difference for monetary policy shocks.

Keywords: Capital, Endogenous Separations, Search and Matching.

JEL classification: E22, E32, J64.

Kiel Institute for the World Economy, Kiel University 24100 Kiel, Germany Telephone: +49-8814-300

E-mail: bjoern.vanroye@ifw-kiel.de denniswesselbaum@web.de

The responsibility for the contents of the working papers rests with the author, not the Institute. Since working papers are of a preliminary nature, it may be useful to contact the author of a particular working paper about results or caveats before referring to, or quoting, a paper. Any comments on working papers should be sent directly to the author.

 $Cover photo: \ uni\_com \ on \ photocase.com$ 

## Capital, Endogenous Separations, and the Business Cycle

Björn van Roye

Kiel Institute for the World Economy Dennis Wesselbaum

Kiel Institute for the World Economy and Kiel University

October 12, 2009

#### Abstract

We implement capital in an endogenous separations New Keynesian matching model. In contrast to the vintage capital theory, we suggest a more general approach, such that workers have unrestricted access to a proportional share of the capital stock. We find that the introduction of capital generates an important channel for the transmission of aggregate productivity shocks, using capital-labor trade-off. The model generates higher volatilities of key variables and therefore enhances the performance of the matching model to generate stylized facts in response to an aggregate productivity shock. However, there is almost no difference for monetary policy shocks.

**Keywords**: Capital, Endogenous Separations, Search and Matching. **JEL classification**: E22, E32, J64.

#### 1. Introduction

The ability of search and matching models to replicate stylized facts has been assessed by various authors. Shimer (2005) in his seminal contribution finds that the standard search and matching model with exogenous separations within a RBC partial equilibrium context is not able to replicate the fluctuations of key labor market variables. A promising solution approach was introduced by Hall (2005) implementing a real wage rigidity, increasing the surpluses of the firm over the cycle and increasing the response of vacancies. However, it appears that real wage rigidity on the one hand is not able to significantly improve the model's performance, as shown by Krause and Lubik (2007). Additionally, there is evidence that the wage of new entrants is not rigid as shown by Haefke et al. (2009). A different solution proposed by Hagedorn and Manovskii (2008) sets the value of leisure close to the wage and the worker's bargaining power close to zero. Therefore, firms relative profits are heavily affected from productivity changes, hence increasing the volatility. However, their approach shows an unrealistic high sensitivity of the unemployment rate with respect to unemployment benefit changes. It appears that a satisfying solution has not been found yet.

As proposed by Hornstein et al. (2005), the introduction of capital might be an important feature that has been rather neglected in the search and matching RBC and NKM literature. Capital, and to be more precisely the cost of investment, add an additional variable to the firm's decision problem. Fluctuations along this margin should also have an impact on the labor market decisions of the firm. In contrast to the recent literature, we do not assume that there is heterogeneity in matches, since we allow unrestricted access to capital and technology to all matches at any time. Therefore, we deviate from the vintage capital literature.<sup>1</sup> The vintage approach is based upon the seminal contribution from Caballero and Hammour (1991), assuming that due to the process of innovation jobs that contain the newest technologies are created, whereas outdated jobs are destructed. Along this line, Michelacci and Lopez-Salido (2007) and Costain and Reiter (2008) introduce the vintage theory to matching models in a RBC context with exogenous separations. Our approach has to be understood as a more general case of modelling capital and consistently as a starting point in the process of understanding the relevance of capital in matching models. In the

<sup>&</sup>lt;sup>1</sup>See e.g. Boucekkine et al. (2006), Eyigungor (2006) or Hornstein et al. (2007).

following, we build a New Keynesian DSGE model with search frictions, capital and purely endogenous separations. Although their is no consensus in the literature on the proper determination of the separation margin, following Fujita and Ramey (2007, 2008) and Ramey (2008) empirical evidence seems to favor endogenous separations. Balleer (2009) shows that the separation rate increases after a positive technology shock and that the standard model generates the volatility of these variables conditional on technology shocks. In addition, Barnichon (2009) finds that around business cycle turning points the separation rate is causative for most of unemployment movements.

Firms rent any desired quantity of capital on a frictionless capital market as in Pissarides (2000). We evaluate the performance along the labor market dimension. For this purpose, and to have a transparent judgement basis for later purpose, we scrutinize U.S. data and perform a statistical analysis.<sup>2</sup> Our findings are presented in Table 1.

#### - Table 1 about here -

The main findings can be summarized as follows

#### • Unemployment and Vacancies

Unemployment is almost 9 times as volatile as productivity, while vacancies are even 10 times as volatile. Labor market tightness is even 19 times as large as labor productivity, while the correlation between unemployment and vacancies is strongly negative.

#### • Job Finding Rates

The job finding rate is about twice as volatile as labor productivity, strongly autocorrelated and pro-cyclical.

#### • Job Creation and Destruction Rates

The job creation and destruction rates are negatively correlated (-0.36) and show much smaller standard deviations than unemployment or vacancies.<sup>3</sup>

We show that the introduction of capital adds an important channel for the transmission of aggregate productivity shocks. We create the empirical values of

 $<sup>^{2}</sup>$ To be consistent with the findings from Shimer (2005), we apply his methodology.

<sup>&</sup>lt;sup>3</sup>Values for the job creation and destruction rates are based on Krause and Lubik (2007), using HP filtered data from 1964:Q1 to 2002:Q3.

standard deviations for unemployment and vacancies in response to an aggregate productivity shock. However, we find that the transmission channel is less important for the propagation of monetary shocks.

The remainder is organized as follows. In the next section we derive the model for later analysis. In section 3 we calibrate and close the model while section 5 compares the performance of the capital model with a standard search and matching model. In section 6 we finally draw the conclusion.

#### 2. A Matching Model with Capital

In this section, we present a New Keynesian model with endogenous separations, search frictions and capital. Households maximize consumption by choosing the optimal consumption path of a CES aggregate of differentiated products and make the investment decision. Firms, acting on a monopolistically competitive market, maximize profits by setting prices - time-dependent pricing à la Rotemberg (1982) - and choosing the optimal levels of employment and capital subject to price adjustment costs, hiring costs and capital adjustment costs. Separations are driven by job-specific productivity shocks affecting new and old jobs generating a flow of worker. In addition, the monetary authority targets the nominal interest rate by a standard Taylor-rule.

#### 2.1. Consumer Preferences

We assume a discrete-time economy with an infinite living representative household who makes its investment decision and seeks to maximize its utility given by

$$U = E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{C_t^{1-\sigma} - 1}{1-\sigma} \right], \tag{1}$$

where  $C_t = \int_0^1 \left[ C_{it}^{\frac{\epsilon-1}{\epsilon}} di \right]^{\frac{\epsilon}{\epsilon-1}}$  is the Dixit-Stiglitz aggregator,  $\beta$  is the discount factor, and the degree of risk aversion is given by  $\sigma$ . We assume that a household consists of a continuum of members, inelastically suppling one unit of labor and being represented by the unit interval.

In addition, and following Merz (1995), Andolfatto (1996), and Poilly and Sahuc

(2008), we assume consumption pooling. The household maximizes consumption subject to the intertemporal budget constraint

$$C_t + \frac{B_t}{P_t} = \mathcal{W}_t + r_t^K K_t + R_{t-1} \frac{B_{t-1}}{P_t} + bu_t + \Pi_t + T_t,$$
(2)

where b is the value of home production, such that  $bu_t$  accordingly is the income of unemployed household members.  $\mathcal{W}_t$  is labor income,  $B_t$  is Bond holding which pays a gross interest rate  $R_t$ .  $\Pi_t$  are aggregate profits and  $T_t$  are real lump sum transfers from the government. The earnings from providing capital are given by  $r_t^K K_t$ , where  $r_t^K$  is the rental rate of the capital stock  $K_t$ . The rental rate of capital is derived by the corresponding cost minimization problem of the firm. By minimizing total expenditures, we obtain the demand function  $C_{it} = \left(\frac{P_{it}}{P_t}\right)^{-\epsilon} C_t$ and by solving the households maximization problem, we obtain the standard Euler equation for intertemporal consumption flows, i.e.

$$C_t^{-\sigma} = \beta R_t E_t \left[ \frac{P_t}{P_{t+1}} C_{t+1}^{-\sigma} \right].$$
(3)

#### 2.2. Entry and Exit Site

The firm searches for workers on a discrete and closed market. Trade in the labor market is uncoordinated, costly and time-consuming. Therefore, labor market frictions are modelled via a Cobb-Douglas type matching function with constant returns to scale, i.e.<sup>4</sup>

$$\Psi(u_t, v_t) = m(u_t)^{\mu} (v_t)^{1-\mu}.$$
(4)

The function gives the number of new employment relationships at the beginning of the next period. Where  $u_t$  is the number of unemployed worker and  $v_t$  is the number of open vacancies, assumed to lie on the unit interval  $v_t = \int_0^1 v_{it} di$ . Where  $\mu \in (0, 1)$  is the elasticity of the matching function with respect to unemployment and the matching efficiency is governed by m > 0. The matching function is homogenous of degree one, strictly increasing in each of its arguments, strictly concave and twice continuously differentiable. The homogeneity assumption leads to the probability of a vacancy being filled in the next period  $q(\theta_t) = m(\theta_t)^{-\mu}$ ,

<sup>&</sup>lt;sup>4</sup>In their empirical analysis Petrongolo and Pissarides (2001) find that the Cobb-Douglas function with constant returns to scale is the most appropriate specification.

where  $\theta_t = v_t/u_t$  corresponds to labor market tightness.

The firm's exit site is determined by endogenous separations only. Therefore, the total number of separations at firm *i* is given by  $\rho_{it} = F(\tilde{a}_t)$ , where  $\tilde{a}_{it}$  is an endogenously determined critical threshold. If the specific productivity of a job is below this threshold, it is not profitable and separation takes place. F(a) is a time-invariant distribution with positive support f(a). Connecting the results for job creation and the job destruction enables us to determine the evolution of employment at firm *i* as

$$n_{it+1} = (1 - \rho_{it+1})(n_{it} + v_{it}q(\theta_t)).$$
(5)

The firm adjusts employment by posting vacancies and by setting the critical threshold, which then influences the separation rate.

#### 2.3. Firm's Maximization

If the matching process has been successful, production commences along the production function given by

$$y_{it} = A_t K_{it}^{\alpha} \left[ n_{it} \int_{\tilde{a}_{it}} a \frac{f(a)}{1 - F(\tilde{a}_{it})} da \right]^{1 - \alpha} = A_t K_{it}^{\alpha} \left[ n_{it} H(\tilde{a}_{it}) \right]^{1 - \alpha}, \tag{6}$$

where  $\alpha < 1$ , aggregate productivity  $A_t$  is common to all firms, the specific productivity  $a_{it}$  is idiosyncratic and every period it is drawn in advance of the production process from the corresponding distribution function. The worker specific production function can then be written as

$$y_{jt} = A_t k_{ijt}^{\alpha} \tilde{a}_{jt}^{1-\alpha}, \tag{7}$$

where worker j's share of the overall capital in firm i is  $k_{ijt} = K_{it}/n_{it}$ . Since we assume homogeneity in matches, every worker has a proportional access to the capital stock.

The capital stock accumulates according to

$$K_{t+1} = (1 - \delta)K_t + I_t,$$
(8)

where  $\delta$  is the depreciation rate and  $I_t$  corresponds to investment following

$$I_t = I_{t-1} + \frac{1}{\vartheta}Q_t,\tag{9}$$

where  $\vartheta$  is the investment adjustment cost.<sup>5</sup> Tobin's Q is given by

$$Q_t = \frac{r^K}{r^K - 1 + \delta} r^K_{t+1} + \beta (1 - \delta) Q_{t+1} + \Lambda_{t+1}, \tag{10}$$

where  $\Lambda_{t+1} = \sigma(c_t - c_{t+1})$  is the linearized stochastic discount factor. The firm solves the following maximization problem

$$\Pi_{i0} = E_0 \sum_{t=0}^{\infty} \beta^t \frac{\lambda_t}{\lambda_0} \left[ \frac{P_{it}}{P_t} y_{it} - \mathcal{W}_{it} - cv_{it} - r_t^K K_t - \frac{\psi}{2} \left( \frac{P_{it}}{P_{it-1}} - \pi \right)^2 Y_t \right], \quad (11)$$

being real revenue depleted by total costs.<sup>6</sup> Due to the introduction of nominal and real frictions, total costs are also determined by vacancy posting costs (c > 0), capital rental costs and price adjustment costs ( $\psi \ge 0$ ).

The wage bill is given by the aggregate of individual wages

$$\mathcal{W}_{it} = n_{it} \int_{\tilde{a}_{it}} w_t(a) \frac{f(a)}{1 - F(\tilde{a}_{it})} da.$$
(12)

Using the first-order conditions from the firm's maximization problem gives the job creation condition

$$\frac{c}{q(\theta_t)} = E_t \beta_{t+1} (1 - \rho_{t+1}) \left[ (1 - \alpha) \varphi_{t+1} A_{t+1} K_{t+1}^{\alpha} n_{t+1}^{-\alpha} H(\tilde{a}_{t+1})^{1-\alpha} - \frac{\partial \mathcal{W}_{t+1}}{\partial n_{t+1}} + \frac{c}{q(\theta_{t+1})} \right] . (13)$$

This condition reflects the hiring decision as a trade-off between the costs of a vacancy and the expected return. Where  $1/q(\theta_t)$  is the duration of the relation-ship between firm and worker.

A key distinctiveness of New Keynesian models is their capability to elucidate the reciprocity of output and inflation. In these models inflation dynamics are

<sup>6</sup>Perfect capital markets imply that the firm discounts with the households subjective discount factor.

<sup>&</sup>lt;sup>5</sup>See Christiano et al. (2005) for a broader definition.

defined by the New Keynesian Phillips curve (NKPC, for short)

$$\hat{\pi}_t = \beta E_t \hat{\pi}_{t+1} + \kappa \hat{\varphi}_t, \tag{14}$$

where  $\kappa = (\epsilon - 1)/\psi$  and  $\hat{\varphi}_t$  reflects the marginal costs.

Subsequently, we will shed light on the wage setting process to derive an expression for the individual real wage which will allow us to study the firm's separation decision more precisely and further determine the critical threshold.

#### 2.4. Wage Setting

A successful match shares an economic rent which is splitted according to individual Nash bargaining. The firm-worker pair then solves the following problem

$$w_t = \operatorname*{argmax}_{w_t} \Big\{ (W_t - U_t)^{\eta} (J_t - V_t)^{1-\eta} \Big\},$$
(15)

where the first term is the worker's surplus, the latter term is the firm's surplus and  $0 \le \eta \le 1$  is the exogenously determined, constant relative bargaining power. It can be shown that the individual real wage satisfies the optimality condition

$$W_t(a_t) - U_t = \frac{\eta}{1 - \eta} J_t(a_t).$$
 (16)

To obtain an explicit expression for the individual real wage, we determine the asset value functions and substitute them into the Nash bargaining solution (16). For the firm the asset value of the job depends on the real revenue, the real wage and if the job is not destroyed, the discounted future value. Otherwise, the job is destroyed and hence has zero value. In terms of a Bellman equation the asset value is given by

$$J_t(a_t) = \varphi_t A_t k_t^{\alpha} a_t^{1-\alpha} - w_t(a_t) + E_t \beta_{t+1} \left( (1 - \rho_{t+1}) \int_{\tilde{a}_{t+1}} J_{t+1}(a) \frac{f(a)}{1 - F(\tilde{a}_{t+1})} da \right).$$
(17)

The asset value of being employed for the worker consists of the real wage, the discounted continuation value and in case of separation the value of being unem-

ployed

$$W_t(a_t) = w_t(a_t) + E_t \beta_{t+1} (1 - \rho_{t+1}) \int_{\tilde{a}_{t+1}} W_{t+1}(a) \frac{f(a)}{1 - F(\tilde{a}_{t+1})} da \quad (18)$$
  
+  $E_t \beta_{t+1} \rho_{t+1} U_{t+1}.$ 

Analogously, the asset value of a job seeker is given by

$$U_{t} = b + E_{t}\beta_{t+1}\theta_{t}q(\theta_{t})(1-\rho_{t+1})\int_{\tilde{a}_{t+1}}W_{t+1}\frac{f(a)}{1-F(\tilde{a}_{t+1})}da \qquad (19)$$
  
+  $E_{t}\beta_{t+1}(1-\theta_{t}q(\theta_{t})(1-\rho_{t+1}))U_{t+1}.$ 

Unemployed worker receive the value of home production b, the discounted continuation value of being unemployed and if she is matched she receives the value of future employment. Inserting these value functions into the Nash bargaining solution yields the individual real wage

$$w_t(a_t) = \eta(\varphi_t A_t k_t^{\alpha} a_t^{1-\alpha} + c\theta_t) + (1-\eta)b.$$

$$\tag{20}$$

The firm will endogenously separate from a worker, if and only if

$$J_t(a_t) < 0, \tag{21}$$

i.e. if the worker's asset value is smaller than zero. After some algebra, the threshold is given by

$$\tilde{a}_t = \left\{ \frac{1}{(1-\eta)\varphi_t A_t k_t^{\alpha}} \left[ (1-\eta)b + \eta c\theta_t - \frac{c}{q(\theta_t)} \right] \right\}^{\frac{1}{1-\alpha}}.$$
(22)

In the next section, we close our model by calibrating deep parameters and by defining monetary policy.

#### 3. Model Solution

#### 3.1. Closing the Model

The monetary authority targets the short-term nominal interest rate by following a standard Taylor rule, given by

$$r_t = \phi_\pi \pi_t + \phi_y Y_t + \varrho_t, \tag{23}$$

where  $\phi_{\pi}$  and  $\phi_{y}$  are the respective weights and the interest rate shock follows a standard AR(1), i.e.  $\rho_{t} = \rho_{\varrho} \rho_{t-1} + \alpha_{\varrho,t}$ . The aggregate productivity shock is formulated as

$$A_t = \rho_A A_{t-1} + \alpha_{A,t}.$$
(24)

The i.i.d. error term is  $\alpha_{A,t} \sim N(0, \sigma_A)$  with  $cov(A_{t-1}, \alpha_{A,t}) = 0 \forall t$ . The market clearing condition reads as

$$Y_t = C_t + I_t. (25)$$

Then the model is linearized around its deterministic steady state and simulated with the software package Dynare.

For the given stochastic processes  $\{A_t, \varrho_t\}_{t=0}^{\infty}$  and the interest rate  $\{r_t\}_{t=0}^{\infty}$  a determined equilibrium is a sequence of allocations and prices

 $\{\tilde{a}_t, C_t, I_t, jcr_t, jdr_t, K_t, m_t, n_t, \pi_t, \varphi_t, Q_t, \rho_t, r_t^K, \theta_t, u_t, v_t, w_t, y_t\}_{t=0}^{\infty}$ , which for given initial conditions, satisfies equations (3), (4), (5), (6), (8), (9), (10), (13), (14), (20), (22), (23), (24), (25), the definitions for labor market tightness, job destruction and creation rate, the interest rate shock, the law of motion for unemployment, the separation rate, and the firm's cost minimization solution.

#### 4. Calibration

We calibrate the model on a quarterly basis for the United States and set parameter values according to stylized facts and the relevant literature. We set the Taylor Rule parameters to standard values of 1.5 with respect to inflation  $(\phi_{\pi})$ 

and to 0.125 to output  $(\phi_y)$ . The discount factor is set to 0.98 percent which results into a steady state interest rate of approximately 2 percent. For the risk aversion parameter  $\sigma$  we choose to set the parameter to a value of 2. Following Krause and Lubik (2007), we set the price adjustment cost  $\psi$  to a value of 40 which coincides with a Calvo parameter that represents a price adjustment in every fourth quarter as in Taylor (1999). With regard to the labor market variables, we choose a steady-state employment rate of 0.88 which results in an equilibrium unemployment rate of 12 percent analogously to Krause and Lubik (2007). The separation rate is set to 0.10 according to Hall (2005) which is due to endogenous separations only. The distribution parameters  $\mu$  and  $\sigma_{ln}$  of the log-normal distribution are chosen to match the observed volatility of job destruction. We set the parameters to 0 resp. 0.12. The job filling rate is assumed to equal 0.7 which corresponds to a monthly rate of 0.3 which is consistent with U.S. data.<sup>7</sup>, whereas the probability for a worker of finding a job,  $\theta q(\theta)$  is equal to 0.6, which represents an unemployment average duration of 1.7 as in Cole and Rogerson (1999). In order to ensure a socially efficient outcome, we respect the Hosios (1990) rule, viz. the elasticity of matches with respect to unemployment  $\mu$  is set equal to the workers bargaining power  $\eta = 0.5$ . Missing parameter values are computed from the steady state. The coefficient with respect to the capital share is set to the standard value of 1/3, inducing a labor share of roughly 60 percent. In line with Christiano et al. (2005), investment adjustment costs are set to 2.48 and the depreciation rate is  $\delta = 0.025$ . The value of the autocorrelation of the aggregate productivity shock is set to 0.66, to balance the estimation results from Prescott (1986) and Altig et al. (2005). Prescott (1986) finds a value of 0.95, while Altig et al. (2005) find a value of 0.1 for a shock to capital embodied technology and 0.87 for a neutral technology shock. For the interest rate shock, we calibrate the persistence parameter to 0.49.

#### 5. Model Comparison

In this section, we analyze differences between a standard search and matching model with endogenous separations (baseline model, henceforth) and a model which additionally includes capital as developed above. At first, we consider an

<sup>&</sup>lt;sup>7</sup>See Blanchard and Galí (2007).

aggregate productivity shock. Subsequently, we scrutinize the dynamics to an expansionary monetary policy shock.

#### 5.1. Productivity shock

Figure 1 shows the impulse responses to an positive aggregate productivity shock for both models.

#### - Figure 1 about here -

In the baseline model, GDP increases persistently due to the rise of aggregate productivity, which boosts production. Simultaneously, marginal costs decrease and consistently, - via the NKPC - inflation decreases. The monetary authority lowers its interest rates, since it puts more weight on inflation than on output. The expansionary behaviour of the central bank acts as a supplementary increase in aggregate demand such that firms increase their labor demand.<sup>8</sup> As a consequence, the separation threshold decreases and firms aim to keep more workers in order to remedy increased demand. Analogously, job creation rises on impact, turns negative in the consecutive quarter, however.<sup>9</sup> As characteristic for endogenous separation models, we identify a separation driven adjustment mechanism. In contrast to the baseline model, and as a consequence of the capital-labor tradeoff, unemployment increases in the capital model, because firms substitute labor by capital. While in the baseline model the productivity of workers increases because aggregate productivity increases, the capital model suggests an additional channel, working along the per-worker capital stock, i.e.  $k_{iit}$ . The direct effect works through the increase in the capital stock, viz. an increased capital stock makes workers more productive. The indirect effect is a consequence of the substitution of labor. Since employment decreases, the capital share of worker *i* clearly increases, additionally increasing her productivity. This, in turn, also rises the incentive to separate from less productive workers.

Furthermore, the dynamic response of vacancies changes significantly in the model with capital. While in the baseline model vacancy postings drop on impact and

<sup>&</sup>lt;sup>8</sup>If inflation would not react on impact, employment would fall, because the firm would be capable of satisfying the unchanged demand with less workers.

<sup>&</sup>lt;sup>9</sup>This follows straightforward from the job creation condition. Initially, expected profits rise since productivity increases - but then hiring costs increase, driving the system back to the equilibrium.

converge from below to the steady state, in the capital model vacancies initially increase and converge from above. As before, the capital-labor trade-off causes this changed vacancy posting behavior. Consider the vacancy posting condition (13). Due to the increase in the capital stock and aggregate productivity, the expected profit from a vacancy increases. This is further enhanced by the same mechanism that we already identified. Because firms decrease employment, the per-worker capital stock significantly increases such that there is "capital left" for new workers, i.e. the expected profit from a posted vacancy is large, since the worker's productivity will be large due to (i) the large aggregate productivity and (ii) due to the large worker's capital share (especially, in relation to the steady state).

Our findings are mirrored in the second moments of our simulation (see Table 2).

#### - Table 2 about here -

With respect to our empirical analysis in the introduction, we show that the model with capital performes outstandingly. In particular, the standard deviations of vacancies and unemployment are in line with the evidence, such that there is no Shimer-puzzle. However, the volatility of labor market tightness is four times below the target value. In addition, except from the standard deviation of separations, all values are close to their empirical pendants. We admit that the challenge of the endogenous separation model, the separation driven adjustment mechanism, is still present in the capital model and causes the relatively bad performance of second moments. For instance, the fact that there is no Beveridge curve and the second moments with respect to the separation rate are not in line with empirical observations. In addition, in the capital model - and in contrast to the baseline model - the standard deviations of the job creation and destruction rates are too high compared to empirical estimates and there correlation is close to (plus) one (being around 0.5 in the baseline model). However, we find that the capital model produces higher persistence values. Unfortunately, this persistence is not endogenous in the sense that a one-off shock creates almost no persistence. Therefore, the model only generates higher persistence to an autocorrelated shock.

#### 5.2. Interest Rate Shock

Figure 2 presents the reactions of the aggregates to a reduction of the monetary authority's policy rate.

- Figure 2 about here -

The transmission of monetary policy shocks is not - heavily - affected by the introduction of capital. Our qualitative and quantitative results are quite similar. An expansionary measure of the monetary authority leads to a boost in aggregate demand and in inflation, due to the pressure on marginal costs. The significant decrease of unemployment is due to the sharp reduction of the job destruction rate which results from a strong decline in separations, i.e. the separation driven adjustment mechanism. Initially, job creation increases; however it already turns negative in the second quarter. Capital accumulation makes almost no difference with respect to monetary policy interventions. The reason is, that the monetary policy shock acts as a demand shock, hence increasing firms output. Because the capital-labor trade-off is less heavily activated - as it was compared to the consideration of the productivity shock -, the dynamic responses of both systems look identical. Although, the transmission channel is less present in this case, it still creates additional variability of labor market variables. Our simulations of the business cycle statistics in Table 3 confirm these results.

- Table 3 about here -

As we have seen, the capital model creates significantly higher values of standard deviations for unemployment and vacancies. However, with respect to the remaining values of standard deviation, we infer almost no change. In addition, this holds for the correlations between the labor market variables. The relationship between the volatilities of the job creation and destruction rate between the two models is of the same size as we have discussed in the precedent section.

#### 6. Robustness Issues

In what follows, we perform a robustness analysis of our results for the capital model and the productivity shock only. Setting the value of the autocorrelation of the shock to 0.89 (the empirical autocorrelation) significantly increases the fluctuations of all variables. However, our qualitative results remain unaffected and the nature of the shock allows us to choose a smaller value of the shock than normally employed in RBC models. Increasing the unemployment rate (0.3 in this example) leaves our quantitative and qualitative results unaffected. In particular, the standard deviations of the job creation and destruction rate are significantly reduced. Along this line, decreasing the unemployment rate (6 % in this example) increases the fluctuations of labor market variables. Since this is a well-known effect of matching models, we continue with the discussion of the steady state separation rate. Setting this value to 0.15 as in Andolfatto (1996) leaves our results completely unaffected. A value of  $\psi = 105$  decreases business cycle fluctuations.

The value of capital adjustment costs plays a major role for the dynamics of the capital model. Increasing this value (around five times, in this example) decreases the standard deviations of labor market variables, because the efficiency of the new transmission channel decreases with increasing capital adjustment costs.

#### 7. Conclusion

In this paper we have shown that the introduction of capital adds an important channel for the propagation of productivity shocks. We develop a New Keynesian model with search frictions, purely endogenous separations and capital. In deviating from the vintage capital theory, we consider a more general case of capital in DSGE models. In our model, workers have an unrestricted and proportional access to the firm's capital stock, i.e. we do not assume heterogeneity in matches. Within this framework we show that the dynamic adjustment path of the capital model deviates significantly from the baseline model to an aggregate productivity shock. The reason for the differences between these two models - and in fact the reason why there is no difference in response to the monetary policy shock - is the fact that the firm substitutes labor by capital. In addition, the main channel causing the discussed differences is the worker's capital share being affected (i) directly, by the increase of the capital stock, and (ii) indirectly, by the decrease of employment. While these channels are important for the transmission of the productivity shock, they only play a minor role for the propagation of the monetary policy shock. Consistently, in both cases the capital model creates larger - and

for the productivity shock even fits - the empirical fluctuations of unemployment and vacancies. We admit that the underlying challenge of endogenous separation models - the separation driven adjustment mechanism - is not resolved, such that the second moments are still not entirely in line with the evidence.

With our more general approach of implementing capital, and by proposing an additional transmission channel, we justify to further consider the role of capital, capital adjustment costs and the capital-labor trade-off in sticky price matching models. We believe that the consideration of specific shocks, e.g. match-specific or worker-specific, should be a fruitful area for future research.

#### A. References

Altig, David, Lawrence J. Christiano, Martin Eichenbaum, and Jesper Linde. 2005. "Firm-Specific Capital, Nominal Rigidities and the Business Cycle´." NBER Working Papers 11034.

Andolfatto, David. 1996. "Business Cycles and Labor Market Search." American Economic Review, Vol. 86(1): 112-132.

**Balleer, Almut.** 2009. "New Evidence, Old Puzzles: Technology Shocks and Labor Market Fluctuations." Kiel Working Paper, No. 1500.

**Barnichon, Régis.** 2009. "Vacancy posting, Job Separation and Unemployment Fluctuations." Mimeo.

**Blanchard, Olivier J. and Jordi Galí.** 2007. "A New Keynesian Model with Unemployment." Kiel Working Paper, No. 1335.

Boucekkine, Raouf, David de la Croix, and Omar Licandro. 2006. "Vintage Capital." Economics Working Papers ECO2006/8.

Caballero, Ricardo J., and Mohamad L. Hammour. 1994. "The Cleansing Effect of Recessions." *American Economic Review*, 84(5): 1350-1368.

Christiano, Lawrence J., Martin Eichenbaum, and Charles L. Evans. 2005. "Nominal Rigidities and the Dynamic Effects of a Shock to Monetary Policy." *Journal of Political Economy*, 113(1): 1-45.

Cole, Harold L. and Richard Rogerson. 1999. "Can the Mortensen-Pissarides Matching Model Match the Business-Cycle Facts?" International Economic Review, 40(4): 933-960.

Costain, James S., and Michael Reiter. 2008. "Business Cycles, Unemployment Insurance, and the Calibration of Matching Models." *Journal of Economic Dynamics and Control*, 32(4): 1120-1155.

**Eyigungor, Burcu.** 2006. "Specific Capital and Vintage Effects on the Dynamics of Unemployment and Vacancies." University of California, Los Angeles mimeo.

**Fujita, Shigeru, and Garey Ramey.** 2007. "Reassessing the Shimer Facts." Federal Reserve Bank of Philadelphia Working Paper, No. 07-2.

**Fujita, Shigeru and Garey Ramey.** 2008: "The Cyclicality of Separation and Job Finding Rates." Federal Reserve Bank of Philadelphia Working Paper, No. 07-19.

Haefke, Christian, Marcus Sonntag, and Thijs van Rens. 2009. "Wage Rigidity and Job Creation." Kiel Working Papers, No. 1504.

Hagedorn, Marcus, and Iourii Manovskii. 2008. "The Cyclical Behavior of Equilibrium Unemployment and Vacancies Revisited." *American Economic Review*, 98(4): 1692-1706.

Hall, Robert E. 2005. "Employment Fluctuations with Equilibrium Wage Stickiness." *American Economic Review*, 95(1): 50-65.

Hornstein, Andreas, Per Krusell, and Giovanni L. Violante 2005. "Unemployment and vacancy fluctuations in the matching model: inspecting the mechanism." *Economic Quarterly*, Federal Reserve Bank of Richmond, Summer Issue, pp. 19-50.

Hornstein, Andreas, Per Krusell, and Giovanni L. Violante 2007. "Modelling Capital in Matching Models: Implications for Unemployment Fluctuations." Mimeo.

Hosios, Arthur J. 1990. "On the Efficency of Matching and Related Models of Search and Unemployment." *Review of Economic Studies*, 57(2): 279-298.

Krause, Michael U., and Thomas A. Lubik. 2007. "The (Ir)relevance of Real Wage Rigidity in the New Keynesian Model with Search Frictions." *Journal of Monetary Economics*, 54(3): 706-727.

Merz, Monika. 1995. "Search in the Labor Market and the Real Business Cycle." *Journal of Monetary Economics*, 36(2): 269-300.

Michelacci, Claudio, and David Lopez-Salido. 2007. "Technology Shocks and Job Flows." *Review of Economic Studies*, 74(4): 1195-1227.

Petrongolo, Barbara, and Christopher A. Pissarides 2001. "Looking into the Black Box: A Survey of the Matching Function." *Journal of Economic Literature*, No. 39: 390-431.

**Pissarides, Christopher A.**. 2000. "Equilibrium Unemployment Theory." Cambridge, Mass.: MIT Press.

**Poilly, Céline, and Jean-Guillaume Sahuc.** 2008. "Welfare Implications of Heterogeneous Labor Markets in a Currency Area." Banque de France Working Paper, No. 199.

**Prescott, Edward.** 1986. "Theory Ahead of Business Cycle Measurement." *Federal Reserve Bank of Minneapolis Quarterly Review*, 10(Fall): 9-22.

Ramey, Garey. 2008. "Exogenous vs. Endogenous Separation." Mimeo.

**Rotemberg, Julio.** 1982. "Monopolistic Price Adjustment and Aggregate Output." *Review of Economic Studies*, 49(4): 517-531.

Shimer, Robert. 2005. "The Cyclical Behavior of Equilibrium Unemployment and Vacancies." *American Economic Review*, 95(1): 25-49.

**Taylor, John B.** 1999. "Staggered price and wage setting in macroeconomics." In: Taylor, John B. and Michael Woodford (Eds.), "Handbook of Macroeconomics." Elsevier Science B.V., Amsterdam.

### **Tables and Figures**



Figure 1: Impulse Responses to a 1 % Productivity Shock.



Figure 2: Impulse Responses to a 1 % Interest Rate Shock.

		u	V	$\theta$	jfr	ρ	р
Standard Deviation		0.1804	0.2034	0.3733	0.0339	0.0064	0.0202
Autocorrelation		0.9681	0.9741	0.9748	0.9244	0.8062	0.8948
	u	1	-0.8921	-0.9692	-0.9491	0.6774	-0.3793
Correlation Matrix	v	-	1	0.9759	0.8507	-0.7027	0.3972
	$\theta$	-	-	1	0.9221	-0.7102	0.3997
	jfr	-	-	-	1	-0.548	0.4094
	$\rho$	-	-	-	-	1	-0.4975
	р	-	-	-	-	-	1

Table 1: Business Cycle Properties of the U.S. Economy.

Notes: We use quarterly, seasonally adjusted, HP filtered ( $\lambda = 10^5$ ) data from 1955:Q1 to 2009:Q2 provided by the OECD and the BLS. All variables respond to log deviations.

Table 1	2: Busin	ess Cycl	e Properties	s of the	Matching	Models -	Productivity	Shock.
---------	----------	----------	--------------	----------	----------	----------	--------------	--------

	u	v	$\theta$	jfr	$\rho$	р
Standard Deviation						
	0.20	0.20	0.04	0.02	0.20	0.01
	0.02	0.02	0.004	0.002	0.02	0.01
	0.99	0.96	0.61	0.61	0.99	0.66
	0.66	0.65	0.64	0.64	0.59	0.66
u	1	0.98	-0.06	-0.06	0.99	0.12
v	-	1	0.14	0.14	0.99	0.30
$\theta$	-	-	1	1	0.01	0.95
jfr	-	-	-	1	0.01	0.95
ρ	-	-	-	-	1	0.18
р	-	-	-	-	-	1
u	1	0.99	0.99	0.99	0.99	1
v	-	1	0.99	0.99	0.99	-1
$\theta$	-	-	1	1	0.99	-0.99
jfr	-	-	_	1	0.99	-0.99
ρ	-	-	-	-	1	0.99
р	-	_	_	-	-	1
	$ \begin{array}{c} \mathbf{u} \\ \mathbf{v} \\ \theta \\ \mathbf{jfr} \\ \rho \\ \mathbf{u} \\ \mathbf{v} \\ \theta \\ \mathbf{jfr} \\ \rho \\ \mathbf{p} \\ \mathbf{p} \\ \mathbf{v} \\ \theta \\ \mathbf{p} \\ \mathbf{v} \\ \theta \\ \mathbf{p} \\ \mathbf$	u $0.20$ $0.02$ $0.99$ $0.66$ u         1           v         - $\theta$ -           jfr         -           p         -           u         1           v         - $\rho$ -           jfr         - $\theta$ -           jfr         - $\rho$ -           jfr         - $\rho$ -           jfr         - $\rho$ -	u         v $0.20$ $0.20$ $0.02$ $0.02$ $0.99$ $0.96$ $0.66$ $0.65$ u         1 $0.98$ v         -         1 $\theta$ -         - $\rho$ -         - $\rho$ -         - $\mu$ 1 $0.99$ $v$ -         1 $\theta$ -         - $\mu$ 1 $0.99$ $v$ -         1 $\theta$ -         - $\mu$ 1 $0.99$ $v$ -         1 $\theta$ -         - $ifr$ -         - $ifr$ -         - $\rho$ $\rho$ $\rho$ <t< td=""><td>u         v         <math>\theta</math>           0.20         0.20         0.04           0.02         0.02         0.004           0.99         0.96         0.61           0.66         0.65         0.64           u         1         0.98         -0.06           v         -         1         0.14           <math>\theta</math>         -         -         1           jfr         -         -         -           <math>\rho</math>         -         -         -           <math>\psi</math>         -         1         0.99           <math>\phi</math>         -         -           <math>\mu</math>         1         0.99         0.99           <math>\psi</math>         -         1         0.99           <math>\theta</math>         -         -         -           <math>\rho</math>         -         -         -           <math>\psi</math>         -         1         0.99           <math>\theta</math>         -         -         1           <math>\rho</math>         -         -         1           <math>\psi</math>         -         1         0.99           <math>\theta</math>         -         -         -           <math>\phi</math>         -         -</td><td>u         v         <math>\theta</math>         jfr           0.20         0.20         0.04         0.02           0.02         0.02         0.004         0.02           0.99         0.96         0.61         0.61           0.66         0.65         0.64         0.64           u         1         0.98         -0.06         -0.06           v         -         1         0.14         0.14           <math>\theta</math>         -         -         1         1           <math>\rho</math>         -         -         1         1           <math>\rho</math>         -         -         -         -           <math>\mu</math>         1         0.99         0.99         0.99           <math>\psi</math>         -         1         1         1           <math>\rho</math>         -         -         1         1           <math>\rho</math>         -         -         1         1           <math>\rho</math>         -         -         -<!--</td--><td>u         v         <math>\theta</math>         jfr         <math>\rho</math>           0.20         0.20         0.04         0.02         0.20           0.02         0.02         0.004         0.02         0.02           0.99         0.96         0.61         0.61         0.99           0.66         0.65         0.64         0.64         0.59           u         1         0.98         -0.06         -0.06         0.99           v         -         1         0.14         0.14         0.99           <math>\theta</math>         -         -         1         0.01           <math>\rho</math>         -         -         1         0.01           <math>\rho</math>         -         -         -         1         0.01           <math>\rho</math>         -         -         -         1         0.01           <math>\rho</math>         -         -         -         -         1           <math>\mu</math>         1         0.99         0.99         0.99         0.99           <math>\psi</math>         -         1         0.99         0.99         0.99           <math>\psi</math>         -         1         0.99         0.99         0.99           <math>\psi</math></td></td></t<>	u         v $\theta$ 0.20         0.20         0.04           0.02         0.02         0.004           0.99         0.96         0.61           0.66         0.65         0.64           u         1         0.98         -0.06           v         -         1         0.14 $\theta$ -         -         1           jfr         -         -         - $\rho$ -         -         - $\psi$ -         1         0.99 $\phi$ -         - $\mu$ 1         0.99         0.99 $\psi$ -         1         0.99 $\theta$ -         -         - $\rho$ -         -         - $\psi$ -         1         0.99 $\theta$ -         -         1 $\rho$ -         -         1 $\psi$ -         1         0.99 $\theta$ -         -         - $\phi$ -         -	u         v $\theta$ jfr           0.20         0.20         0.04         0.02           0.02         0.02         0.004         0.02           0.99         0.96         0.61         0.61           0.66         0.65         0.64         0.64           u         1         0.98         -0.06         -0.06           v         -         1         0.14         0.14 $\theta$ -         -         1         1 $\rho$ -         -         1         1 $\rho$ -         -         -         - $\mu$ 1         0.99         0.99         0.99 $\psi$ -         1         1         1 $\rho$ -         -         1         1 $\rho$ -         -         1         1 $\rho$ -         -         - </td <td>u         v         <math>\theta</math>         jfr         <math>\rho</math>           0.20         0.20         0.04         0.02         0.20           0.02         0.02         0.004         0.02         0.02           0.99         0.96         0.61         0.61         0.99           0.66         0.65         0.64         0.64         0.59           u         1         0.98         -0.06         -0.06         0.99           v         -         1         0.14         0.14         0.99           <math>\theta</math>         -         -         1         0.01           <math>\rho</math>         -         -         1         0.01           <math>\rho</math>         -         -         -         1         0.01           <math>\rho</math>         -         -         -         1         0.01           <math>\rho</math>         -         -         -         -         1           <math>\mu</math>         1         0.99         0.99         0.99         0.99           <math>\psi</math>         -         1         0.99         0.99         0.99           <math>\psi</math>         -         1         0.99         0.99         0.99           <math>\psi</math></td>	u         v $\theta$ jfr $\rho$ 0.20         0.20         0.04         0.02         0.20           0.02         0.02         0.004         0.02         0.02           0.99         0.96         0.61         0.61         0.99           0.66         0.65         0.64         0.64         0.59           u         1         0.98         -0.06         -0.06         0.99           v         -         1         0.14         0.14         0.99 $\theta$ -         -         1         0.01 $\rho$ -         -         1         0.01 $\rho$ -         -         -         1         0.01 $\rho$ -         -         -         1         0.01 $\rho$ -         -         -         -         1 $\mu$ 1         0.99         0.99         0.99         0.99 $\psi$ -         1         0.99         0.99         0.99 $\psi$ -         1         0.99         0.99         0.99 $\psi$

Notes: Theoretical Moments.

		u	v	$\theta$	jfr	ρ	р
Standard Deviation							
Capital Model		0.12	0.10	0.03	0.01	0.13	-
Baseline Model		0.09	0.06	0.03	0.02	0.10	-
Autocorrelation							
Capital Model		0.72	0.79	0.49	0.49	0.53	-
Baseline Model		0.49	0.47	0.52	0.52	0.20	-
	u	1	0.99	-0.85	-0.85	0.98	-
Correlation	v	-	1	-0.77	0.96	-0.77	-
Matrix	$\theta$	-	-	1	1	1	-
Capital	jfr	-	-	-	1	-0.85	-
Model	$\rho$	-	-	-	-	1	-
	р	-	-	-	-	-	-
	u	1	0.99	-0.99	-0.99	0.96	-
Correlation	v	-	1	-0.99	-0.99	0.96	-
Matrix	$\theta$	-	-	1	0.99	-0.94	-
Baseline	jfr	-	-	-	1	-0.95	_
Model	$\rho$	-	-	-	-	1	-
	р	-	-	-	-	-	-

Table 3: Business Cycle Properties of the Matching Models - Interest Rate Shock.

Notes: Theoretical Moments.