Reicher, Christopher Phillip

Working Paper
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Kiel Working Paper, No. 1543

Provided in Cooperation with:
Kiel Institute for the World Economy (IfW)

Suggested Citation: Reicher, Christopher Phillip (2009): Expectations, monetary policy, and labor markets: lessons from the Great Depression, Kiel Working Paper, No. 1543, Kiel Institute for the World Economy (IfW), Kiel

This Version is available at:
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Expectations, Monetary Policy, and Labor Markets: Lessons from the Great Depression

by Christopher P. Reicher

No. 1543 | August 2009
**Expectations, Monetary Policy, and Labor Markets: Lessons from the Great Depression**

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This paper estimates a series of shocks to hit the US economy during the Great Depression, using a New Keynesian model with unemployment and bargaining frictions. Shocks to long-run inflation expectations appear to account for much of the cyclical behavior of employment, while an increase in labor’s bargaining power also played an important role in deepening and lengthening the Depression. Government spending played very little role during the Hoover Administration and New Deal, until the rise in military spending effectively brought an end to the Depression in 1941. With the economy at or near the zero interest rate bound, interest rates and monetary aggregates provided a misleading indicator as to the true stance of inflation expectations; in fact, conditions were deflationary all throughout the 1930s in spite of high money growth and low interest rates. The experience of the 1930s offers lessons to modern policymakers who find themselves in a similar situation.

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I Introduction

Recent events have caused economists to revisit the Great Depression, in the hope that the Depression can provide lessons for policymakers and researchers. Like the current period, the Depression was characterized by low nominal interest rates and a fall in the velocity of money. The economy can behave unusually in this type of situation; Christiano, Eichenbaum, and Rebelo (2009) find that shocks to inflation expectations or to real demand can have large effects at the zero bound. Little work has gone into empirically evaluating the role of shocks to nominal expectations during the Depression, taking the zero bound into account. To fill this gap, this paper estimates a series of shocks to nominal expectations and interest rates during the interwar years using a New Keynesian model with inflexible interest rates, sticky wages, and search-based unemployment. It finds that these shocks can account for much of the evolution of employment and output during the 1930s. The model also investigates the role of shocks to government spending, productivity, and labor market policies.

This is not the first paper to look at the more general issue of expectations during the Depression. Eggertsson (2008) models the 1929-1933 contraction and 1933-1937 recovery periods as a transition between two separate policy regimes, one deflationary and one inflationary. He specifically examines fiscal policy and its potential implications for the price level, and he looks at happens when the economy is hit by an exogenous real interest rate shock. In comparison with Eggertsson, this paper looks at the role of expectations themselves as generating an impulse to money demand, and it models other aspects of labor markets and aggregate demand in more detail. Christiano, Motto, and Rostagno (2004) model the Depression as a response to a shock to currency demand, treating bank runs as a negative shock to the transactions technology. They do not model
expectations per se, but the issue of expected bank solvency lies in the background. Other researchers, such as Harrison and Weder (2006) explore the role of expectational shocks in models of real indeterminacy with increasing returns to scale. This is an interesting topic but this paper focuses on nominal indeterminacy and constant returns since these assumptions are more often used in the literature.

The specification of the labor market also allows for shocks to workers’ bargaining power and disutility from work. A number of authors have contended that the interventions of Presidents Hoover and Roosevelt, rather than improving conditions, may have in fact worsened the Depression. They argue that federal policies aimed at strengthening labor’s bargaining power and increasing labor income made it unprofitable for firms to hire workers and that this led to persistently depressed rates of employment and job creation. Bordo, Erceg, and Evans (2000), Ohanian (2007), Cole and Ohanian (1999, 2004), and Ebell and Ritschl (2008), to name a few, present narrative and quantitative evidence that this may have been the case. These policy interventions coincide with a drop in vacancy creation, a rise in labor’s share, and a fall in the Beveridge Curve, and these facts are only interpretable in a model with labor market frictions. A model with bargaining and with search-based unemployment can provide a natural context to talk about these issues and to disentangle them from the other disturbances to the economy. Including sticky wages allows one to better match the behavior of labor’s share during this time, as Bernanke and Carey (1996) argue.

This paper is structured as follows: Section II discusses the data used in the estimation exercise, and Section III lays out a medium-scale model of search-based unemployment in the presence of wage and price stickiness. Section IV discusses the
estimation procedure, and Section V presents the results. The results can be summarized as follows: Shocks to long-run nominal expectations and to interest rates explain the largest portions of the contractions of 1929-33 and 1937-38 but they do not explain the slow recovery after 1933. This is explained by shocks to labor’s bargaining power and, to a much lesser extent, a rise in the disutility from work. These shocks coincide with an increase in labor’s share of income and a persistent downward shift in the Beveridge Curve. Low productivity also exerted a moderate drag on employment, and a rise in government spending in 1941 accounts for the final recovery from the Depression but for very little of the employment dynamics before that.

These results also suggest that the money supply was a poor proxy for long-run nominal expectations, and that the dynamics of the post-1933 period were still profoundly deflationary. This is in sharp contrast with the analysis of Eggertsson. A narrow focus on monetary aggregates or on interest rates can cause policymakers to drastically misinterpret long-run expectations. In the current situation, the short-run money supply offers a poor indicator as to the long-run path of the nominal economy since the velocity of money can vary endogenously based on expectations about future actions. Policymakers also need to be aware that low interest rates can indicate long-term deflationary pressures, which appear to have been prevalent all throughout the 1930s.

II  The data

This paper makes use of linearly detrended quarterly observations on eleven variables related to real activity, job flows, and nominal variables from the first quarter of 1923 through the fourth quarter of 1941. Figures 1 and 2 show the data used in this
analysis. The GNP series comes from the National Income and Product Accounts and from Kendrick (1961), interpolated using industrial production and real department store sales. The price level is interpolated using the BLS’s wholesale price index and the price index for department store sales. Quality-adjusted labor input comes from Kendrick (1961), interpolated by the BLS’s series on the employment of production workers in manufacturing. Quarterly nominal investment and government spending come directly from Balke and Gordon (1986); the measure of investment spending used encompasses residential and nonresidential structures, equipment, and inventories. Interest rates are given by the banker’s acceptance rate in New York since this is a low-risk interest rate for which good data exist. The money supply comes from Friedman and Schwartz (1963) and equals the sum of adjusted demand deposits and currency held by the public. It is worth noting that the decline in the velocity of money equals the decline in nominal GDP; the real money supply did not change at all during the 1929-33 contraction.

The manufacturing separation and accession rates are those reported by Metropolitan Life and the BLS (from the NBER and various issues of Employment and Earnings). They are seasonally adjusted by the author in levels, and the pre-1930 series is spliced onto the post-1930 series after an amplitude and mean adjustment. Separations and accessions both played an important role in job flows during the 1930s. There is, unfortunately, a break in the way the data were calculated in 1929-30, so one must view these series with extreme caution. The detrended Metropolitan Life help wanted index (a proxy for vacancies) shows a dramatic decline throughout the sample; it showed higher than usual vacancy rates all throughout the 1920s and lower than usual vacancy rates throughout the 1930s. To illustrate this, Figure 3 shows the relationship between
unemployment and vacancies known as the Beveridge curve.\textsuperscript{1} In the late 1920s, the Beveridge curve shifted drastically downward. Zagorsky (1998) discusses the stability of this series and the related postwar Conference Board series, which held until the 1990s.

The labor share measure used in this paper is labor’s share of gross income from the corporate sector, interpolated to a quarterly frequency from annual data. The portion before 1929 was constructed on the basis of annual data provided by Moroney (1964), Osborne and Epstein (1956), Kuznets (1941), and Goldsmith (1955). The portion after 1929 is available in the NIPA. Throughout the 1930s, labor’s share seemed particularly high for a long period of time, a fact noted by Johnson (1954) and Solow (1958) and in contrast with the postwar experience. That this coincided with a fallen Beveridge Curve encourages the inclusion of labor market shocks in the model.\textsuperscript{2}

\textbf{III The model}

Walsh (2002, 2005), Trigari (2009), and Cooley and Quadrini (1999) present different models of labor matching in the presence of nominal rigidities, building upon the search and matching model of Mortensen and Pissarides (1994) and den Haan, Ramey, and Watson (2000). Gertler and Trigari (2009) extend this approach to include sticky nominal wages, finding that this modification can better account for cyclical movements in output and wages. This paper proceeds in the spirit of the latter model.

This model has seven disturbances: Disturbances to the money supply, government spending, productivity, the long-run price level, labor’s bargaining power, the disutility

\textsuperscript{1} Normally the Beveridge Curve shows unemployment instead of employment. Due to the unavailability of a reliable unemployment series, Figure 3 uses detrended employment instead, graphed from high to low.

\textsuperscript{2} Gomme and Rupert (2004) find that labor’s share has tended to rise at the beginning of postwar recessions as well. The unusual aspect of the labor share in this case is the persistently high labor share after 1933.
from work, and interest rates. On the household side, it consists of a continuum of infinitely lived consumers. Production and hiring take place in a firm-worker match, with wages responding sluggishly to the bargaining environment. A retail sector aggregates output from the wholesale sector and resets retail prices in a staggered manner. The monetary authority attempts to control the interest rate, but it has the inability to adjust the interest rate more than one-for-one with changes in expected inflation. Instead, short-run nominal variables are determined by a combination of an interest rate peg and expectations concerning the long-run price level. Government spending and fixed investment, with variable utilization, are the other sources of demand in this economy.

III.A The household sector

Individuals within households supply labor inelastically; they either work for a set number of hours per week or do not work at all. They also have the choice between consuming in a given period and investing in nominal bonds to consume in the future. They each seek to maximize the objective function

$$E_t \sum_{i=0}^{\infty} \beta^i \left[ \ln(C_{t+i} - hC_{t+i-1}) - \chi_{t+i}A_{t+i} \right],$$

where $C_{t+i}$ equals the household’s period-by-period real consumption and $\chi_{t+i}$ is an indicator variable equal to one if the household worked in a given period. Preferences are separable, exhibit habit persistence, and are consistent with balanced growth. For tractability, households are large and pool consumption efficiently.
Markets operate in three stages per period. In the first stage, after shocks are realized, financial markets open. People trade bonds and withdraw money in order to make their consumption purchases. In the second stage, the goods market opens and these purchases happen. In the third stage, income from the second stage is realized and factor payments are made. This delay introduces a cost channel into the model. This makes it possible for low nominal interest rates to directly stimulate production.

The quantity equation, which is normally motivated by forcing people to finance a portion of their spending (or factor incomes) with cash holdings, states that nominal consumption must not exceed end of period money holdings, allowing for variations in the transactions technology:

\[ P Y_t \leq V_t^{\text{TRANS}} M_{t+1}. \]  

(2)

In a low interest rate environment, this constraint may not bind since the cost channel no longer becomes operative. The reason for this is that in such a situation, households and firms can costlessly hold money in excess of their transactions demand for money. In standard New Keynesian models where the central bank follows an interest rate policy, this does not matter, since nominal spending is based purely on expectations regarding future inflation and interest rates. The observed speculative hoarding of money and the decoupling of different aggregates during the Depression provide an empirical basis for treating velocity as a forward looking ‘jump’ variable.  

The household’s budget constraint relates household money holdings, total income, bond purchases, money, taxes, and consumption. \( B_t \) equals the household’s purchases, at the beginning of the period, of one-period nominal bonds that mature at the

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3 Christiano, Motto, and Rostagno (2004) and Warburton (1945) present strong evidence that a depressed velocity of money played an important role in the Depression, with the former authors treating this as a structural shock to the composition and efficiency of money holdings.
beginning of the next period. They earn the gross nominal interest rate $R_t$. $T_t$ equals the level of net taxes paid by the household, with a Ricardian fiscal policy:

$$M_{t+1} + B_{t+1} + P_t C_t + P_t I_t = P_t Y_t + R_{t-1} B_t + M_t - P_t T_t.$$  

The household’s first-order conditions end up looking familiar. Optimization in bonds generates the usual intertemporal asset pricing relationship

$$\lambda_t = E_t \beta R_t \frac{P_t}{P_{t+1}} \lambda_{t+1},$$

where the household’s marginal utilities of consumption and wealth are equal:

$$\frac{1}{C_t - h C_{t-1}} - E_t \frac{\beta h}{C_{t+1} - h C_t} - \lambda_t = 0.$$

Because of market clearing, output equals consumption:

$$Y_t = C_t + G_t + I_t,$$

and the stochastic quantity equation holds, but merely as an accounting identity:

$$P_t Y_t = V_t M_{t+1}.$$  

### III.B The retail sector and sticky prices

Monopolistically competitive retailers buy output competitively from the wholesale sector and resell it at a markup. They aggregate it according to a Dixit-Stiglitz aggregator. Retailers buy their products $y_j$ competitively from wholesale producers who produce homogeneous intermediate goods. The aggregate level of output is given by

$$Y_t = \left[ \int_{0}^{t} y_j \rho \, dj \right]^{\frac{\theta}{\theta-1}},$$
for some substitutability parameter $\theta$ greater than one. From this expression, each individual retail firm faces a demand curve

$$y_p = \left( \frac{p_p}{p_t} \right)^{-\theta} Y_t,$$

(9)

where the aggregate price level $p_t$ equals the CES price index:

$$p_t = \left[ \int_0^1 p_{jt}^{1-\theta} dj \right]^{1/(1-\theta)}.$$

(10)

The retailers buy unfinished output from the wholesalers at a price $p_t^{W}$ and sell it at an aggregate markup $\mu_t \equiv P_t / p_t^{W}$. Each retailer, in the spirit of Calvo (1983), can only change its price with a probability $1 - \omega$.

Those firms that change their price in a given period do so symmetrically and reset their prices to $p_t^\ast$. They maximize expected discounted profits. Letting $D_{i,t+1}$ equal the discount factor $\beta(\lambda_{t+1}/\lambda_{t+1})$, the objective function for the price-changers equals

$$E_t \sum_{i=0}^\infty \omega^i D_{i,t+1} \left[ \left( \frac{p_t^\ast}{p_t} \right)^{-\theta} - \mu_t^{-1} \left( \frac{p_t^\ast}{p_t} \right)^{-\theta} \right] Y_{t+i}.$$

(11)

Long-run profit maximization results in the first order condition

$$\left( \frac{p_t^\ast}{p_t} \right) = \left( \frac{\theta}{\theta-1} \right) \frac{E_t \sum_{i=0}^\infty \omega^i D_{i,t+1} \mu_t^{-1} \left( \frac{p_t^\ast}{p_t} \right)^{\theta} Y_{t+i}}{E_t \sum_{i=0}^\infty \omega^i D_{i,t+1} \left( \frac{p_t^\ast}{p_t} \right)^{\theta-1} Y_{t+i}},$$

(12)

with the aggregate retail price index given by

$$p_t^{1-\theta} = (1 - \omega)(p_t^\ast)^{1-\theta} + \omega p_{t-1}^{1-\theta}.$$

(13)
Current prices are a weighted function of lagged prices and the prices set by those firms that could adjust. Conditions (12) and (13), when linearized and combined, describe a New Keynesian Phillips Curve relationship which relates current retail markups to current and expected future inflation.

**III.C The wholesale sector**

The wholesale sector distinguishes this model from typical sticky-price or sticky-wage models. Workers and firms separate for both exogenous and endogenous reasons, and firms search for workers based on expectations of future profitability.

Using standard notation, \( U_t = I - N_t \) equals the number of workers searching for a job at the beginning of the period, with the population normalized to one. There is a constant probability \( \rho \) that a match will end exogenously. The remaining \( (I - \rho)N_t \) matches experience an iid, idiosyncratic productivity shock \( a_{it} \) (with a distribution function \( F \)) and a systematic permanent productivity shock \( z_{it} \), all of which the worker and firm observe at the beginning of the period. Based on their realizations, the worker and firm decide whether to continue the relationship or to separate. If the relationship continues, the match produces \( y_{it} = (a_{it}z_{it})^{1-\alpha}k_{it}^{\alpha} \) which is sold at the wholesale price \( P_{it} \) to the retailers. If the relationship separates, production equals zero; the job is destroyed; and the worker becomes unemployed. All productivity shock processes have an unconditional mean of one and are iid over time. The idiosyncratic shocks are also independent and identically distributed over time and across agents, while the systematic productivity shocks are common to every agent.
Matches rent capital in a competitive rental market at a rate $\rho^k_t$, after all shocks are realized. Denoting the retailer’s gross markup $\mu_t$ as $P_t / P^w_t$, the surplus of a match at period $t$ equals the real value of the match’s product in time $t$, minus the disutility of work in product terms, plus the expected discounted continuation value of the match (denoted by $q_{it}$), minus the match’s capital rental payments. Income payments are discounted by the interest rate because of the cost channel induced by monetary frictions:

$$s_{it} = (a_{it}z_a)^{1-a}k_{it}^{-a} \frac{A_t}{\lambda_{it}} + q_{it} - \frac{\rho^k_t k_{it}}{R_t}.$$  

The value of $k_{it}$ is determined optimally by the match, so that:

$$k_{it} = (a_{it}z_a)^{1-a} \frac{\alpha}{(\mu_t \rho^k_t)^{1-a}}.$$  

As a result, firms and workers bargain over the worker’s marginal product:

$$s_{it} = \left(1 - \alpha \right) \frac{(a_{it}z_a)^{1-a} k_{it}^a}{\mu_t R_t} - \frac{A_t}{\lambda_{it}} + q_{it},$$  

so substituting in the firm’s capital demand,

$$s_{it} = \left(1 - \alpha \right) \frac{(a_{it}z_a)^{1-a} k_{it}^a}{\mu_t R_t} \left[ \frac{\alpha}{(\mu_t \rho^k_t)^{1-a}} \right] \frac{A_t}{\lambda_{it}} + q_{it}.$$  

After consolidating terms, one obtains the expression:

$$s_{it} = \left(1 - \alpha \right) \frac{1}{\mu_t R_t} \left[ \frac{\alpha}{(\mu_t \rho^k_t)^{1-a}} \right] \frac{A_t}{\lambda_{it}} + q_{it}. \quad (14)$$

Since only matches with a nonnegative surplus will continue, for a match to do so, it will require that $a_{it}$ exceed a certain cutoff value $\tilde{a}_t$. Since the shock $a_{it}$ is iid, the
continuation value of the surplus $q_i$ will equal the same value $q_t$ across matches. Setting (14) to zero gives the value of this cutoff:

$$\tilde{a}_i = \frac{1}{\mu^{1-\alpha}} R_i (A_i / \lambda_i - q_i) \left[ \frac{\rho_i^{\tilde{K}}}{\tilde{K}^{1-\alpha}} \right]^{1-\alpha} \frac{1}{1 - \alpha}. \quad (15)$$

If $a_{it}$ has the distribution $F$, then the endogenous separation probability $\rho^*_i$ equals $F(\tilde{a}_i)$ and the aggregate separation rate $\rho_i$ and the match survival rate $\phi_i$ are given by:

$$\rho_i = \rho^* + (1 - \rho^*) F(\tilde{a}_i), \quad (16)$$

and

$$\phi_i = (1 - \rho^*) [1 - F(\tilde{a}_i)] = (1 - \rho_i). \quad (17)$$

In most models of this sort, workers and firms bargain every period. This model instead exhibits wage stickiness. As in Gertler and Trigari (2009), wages are determined through staggered Nash bargaining. With probability $1 - \nu$, wages are bargained such that the worker receives a share $\eta_t$ of the bilateral surplus, and the firm receives the remainder. Otherwise, the nominal wage does not change. Newly hired workers receive a wage drawn at random from the prevailing wage distribution. In this situation the wage does not directly affect the bilateral surplus or the separation rate between firms and workers. It may have important spillover effects.

Firms can post vacancies at a fixed cost $p_i^{\nu}$ but face no other barriers to entry. These vacancies get filled at a gross rate $k_i^f$. A firm’s share of the surplus at any given date is denoted $s_i^f$. Equating the supply and demand for vacancies results in a condition equating the present value of a firm’s vacancy posting with the cost of vacancy posting:
\[ \mathcal{P}_t' = (1 - \rho^x)k_t' \beta E_\gamma \frac{\lambda_{x+1}}{\lambda_t} \int_{a_{t+1}}^\infty s_{a+t}dF(a_{t+1}). \]  
(18)

The probability of the worker actually finding a match equals \( k_t^w \), based on a matching function. These conditions give the continuation value of the surplus:

\[ q_t = (1 - \rho^x)\beta E_\gamma \frac{\lambda_{x+1}}{\lambda_t} (1 - k_t^w) \int_{a_{t+1}}^\infty s_{a+t}dF(a_{t+1}) + \frac{k_t^w \mathcal{P}_t'}{k_t'}. \]  
(19)

The cost of a vacancy has to grow with productivity in order to keep the vacancy-employment ratio stable over time. The exact way that this is done does not have a significant effect on the results, so posting costs are simply proportional to productivity:

\[ \mathcal{P}_t' = \mathcal{Q}_t. \]  
(20)

The firm’s share of the surplus is given by:

\[ s_t' = \frac{(1 - \alpha)(a_t, z_t)}{\mu R_t} k_t^\alpha - \frac{w_t}{R_t} + (1 - \rho^x)\beta E_\gamma \frac{\lambda_{x+1}}{\lambda_t} \int_{a_{t+1}}^\infty s_{a+t}dF(a_{t+1}). \]  
(21)

Aggregating things, the total number of unemployed in a period equals the starting stock of unemployed plus those who separate at the beginning of the period.

Abstracting from labor force entry and exit, this comes out to

\[ u_t \equiv U_t + \rho_t N_t = 1 - (1 - \rho_t)N_t. \]  
(22)

The number of vacancies posted in a given period equals \( v_t \). Given a constant-returns Cobb-Douglas matching function \( m(u_t, v_t) = a_t^\alpha v_t^{1-\alpha} \), the vacancy-filling rate is given by

\[ k_t^f = \frac{m(u_t, v_t)}{v_t}. \]  
(23)

and the worker’s job-finding rate is given by

\[ k_t^w = \frac{m(u_t, v_t)}{u_t}. \]  
(24)
The number of matches evolves according to the accounting identity

\[ N_{t+1} = (1 - \rho_t)N_t + m(u_t, v_t), \]  

(25)

and the gross output of the matched firms and workers is given by

\[ Q_t = \frac{(1 - \rho_t)N_t \bar{z}}{1 - F(\tilde{\alpha})} \left[ \int_0^\alpha a_t dF(a_t) \right] \left[ \frac{\alpha}{\mu \rho_t^k} \right]. \]  

(26)

Output (in value-added terms) equals gross output minus vacancy posting costs:

\[ Y_t = Q_t - p_t^i v_t. \]  

(27)

To solve for the rebargained real wage, one could note that those firms which pay the rebargained wage \( W_t^* \) have an average surplus of \((1 - \eta_i)s_i\). Since wages sometimes deviate from this, firms’ actual portion of the surplus may be higher or lower than this value. This difference, in the aggregate, is simply equal to the present value of the wage gap \( L_t \) after accounting for the cost channel:

\[ L_t = s_t' - (1 - \eta_i)s_i = E_t \sum_{i=0}^{\infty} \frac{\beta^i \lambda_{t+i}}{\lambda_{t+i}} \left( \frac{W_t^* - W_{t+i}}{R_{t+i}} \right). \]

This can be written as a difference equation:

\[ L_t = W_t^* - W_t \frac{R_t}{R_{t+1}} + E_t \frac{\beta \lambda_t \varphi_{t+1} L_{t+1}}{\lambda_t}, \]  

(28)

where the cumulative match survival probability is given for \( i > 0 \) by

\[ \varphi_{t+i} = \prod_{j=0}^{i} \varphi_{t+j}, \]

and is equal to one for \( i = 0 \). The average nominal wage rate is given by:

\[ P_t W_t = vP_{t-1} W_{t-1} + (1 - v)P_t W_t^*. \]  

(29)
Capital is subject to depreciation at a rate \( \delta (N_{K_{t+1}}) \) which reflects a positive relationship between depreciation and utilization. Capital holdings follow a first-order condition which comes from the household’s optimal choice of investment:

\[
1 = \beta E_t \left[ \frac{\lambda_{t+1}}{\lambda_t} \right] \left[ 1 + \frac{\phi K_{t+1} N_{K_{t+1}} - \delta (N_{K_{t+1}})^\rho}{R_{r+1}} \right].
\]

Finally, optimal utilization is given by:

\[
\rho_t^K = \delta \phi (N_{K_{t+1}})^{\rho-1}.
\]

### III.D Real driving processes

Letting \( \Gamma \) equal the long-run growth rate of productivity, it is convenient to assume that it follows a highly persistent AR(1) on top of a time trend:

\[
\ln(\bar{z}_t) - \Gamma t = \rho_t \left[ \ln(\bar{z}_{t-1}) - \Gamma (t-1) \right] + \varepsilon_t^\Gamma.
\]

The level of technology-adjusted government spending, \( G_t \), follows a stationary AR(1):

\[
\ln(G_t) = (1 - \rho_G) \ln(G) + (1 - \rho_G) \ln(\bar{z}_t) + \rho_G \ln(G_{t-1}) + \varepsilon_t^G.
\]

The bargaining weight \( \eta_t \) and the labor supply parameter \( A_t \) also follows an AR(1):

\[
\ln(\eta_t) = (1 - \rho_\eta) \ln(\eta) + \rho_\eta \ln(\eta_{t-1}) + \varepsilon_t^\eta,
\]

and

\[
\ln(A_t) = (1 - \rho_A) \ln(A) + \rho_A \ln(A_{t-1}) + \varepsilon_t^A.
\]

### III.E The monetary authority

During the interwar period, the Fed wished to stabilize nominal exchange rates and prices, concentrating upon the nominal price of gold and the dollar-sterling exchange
rate. Other branches of government such as the Treasury directed a large portion of monetary policy as well. With interest rates throughout the 1930s remaining extremely low and with the dollar fixed against the sterling, it seems accurate to treat the movement of interest rates as passive during this period. In particular this paper treats interest rates as following an exogenous persistent autoregressive process akin to an interest rate peg. Given an expected path of interest rates, current nominal variables are determined by expectations of the long-run price level.

This paper remains agnostic about the exact source of that long-run price level target. Eggertsson (2006, 2008), for instance, suggests that fiscal policy may have affected inflation expectations through a game that fiscal authorities play with their future selves. The Fiscal Theory of the Price Level views the price level as possibly evolving to ensure government solvency, to enforce consumers’ transversality conditions. Alternatively, Friedman (1963) argued that the collapse of the supply of inside money determined long run nominal expectations, while Bernanke and James (1991) emphasize the importance of the gold standard and governments’ decision of a nominal anchor. Alternatively, it is possible that these expectations were simply self-fulfilling. The model used here is consistent with each of these theories. What matters is that expectations are rational and that the long-run price level is well-defined.

Letting $\Theta_t$ equal the growth rate of the money supply from $t$ to $t+1$, the growth rate of the supply of inside money evolves according to the law of motion

$$\ln(\Theta_t) = (1 - \rho_m) \ln(\Theta) + \rho_m \ln(\Theta_{t-1}) + \epsilon_t^\Theta. \tag{36}$$

The short-run money supply does not matter in determining the equilibrium of the model since only long run expectations matter, but it is an interesting empirical question to see
how unexpected movements in the money supply are related to unexpected movements in nominal aggregates. This will indicate how well the monetarist view of the Depression can be reconciled with the New Keynesian view. Near the zero bound, it seems reasonable to treat interest rates as a highly persistent AR(1) process:

\[
\ln(R_t) = (1 - \rho_\kappa) \ln(R) + \rho_\kappa \ln(R_{t-1}) + \epsilon_t^R. \tag{37}
\]

Since interest rates cannot respond more than one-for-one to inflation, the model requires more assumptions for closure, or else there are too many valid rational expectations equilibria. To deal with this, this paper introduces an additional process, the expected long run price level, denoted by \( P_T \). Under the assumption of rational expectations, its logarithm must follow a random walk. The equilibrium is then determined by backward induction from the terminal price level, which is what an eigenvalue decomposition does.

For computational reasons, it is simpler to analyze the behavior of the nominal output gap. This gap is just defined as the difference between long-run and actual nominal output, given by \( \ln(J_t) = \ln(P_T) + \ln(Y_T) - \ln(P_t) - \ln(Y_t) \). Taking first differences, one can show, with a random walk long-run productivity process, that the nominal output gap \( J_t \) follows the law of motion:

\[
\ln(J_t) = \ln(J_{t-1}) - \ln\left(\frac{P_t}{P_{t-1}}\right) - \ln\left(\frac{Y_t}{Y_{t-1}}\right) + \epsilon_t^\nu + + \epsilon_t^\gamma. \tag{38}
\]

In the calculation of the rational expectations equilibrium, this equation generates a unit eigenvalue. Suppressing it ensures that the nominal output gap is strictly stationary, which enforces the definition of a nominal output gap. By generating the right number of unstable eigenvalues, this equation ensures saddle path stability and closes the model.
III.F Equilibrium and solution method

The aggregate household conditions (4) through (7), the New Keynesian retail conditions (12) and (13), the aggregated versions of (14) through (31) from the wholesale sector, and the driving processes (32) through (38) constitute a rational expectations equilibrium for this economy. The method used to estimate the shocks hitting this economy involves taking a log-linear approximation around a steady state. Based on this linearized system, it is possible to obtain feedback coefficients using the gensys.m program written and discussed by Sims (2002). In this particular situation, the equilibrium exists and is unique in the neighborhood around the steady state. While nonlinear methods may improve the accuracy of the model (ignoring the uncertainty surrounding functional forms and other sources of misspecification), they also impose the need to make additional assumptions about the ordering of shocks and their effects. In addition they are much more computationally intensive than linear methods since the model is high-dimensional.

IV Estimation strategy

IV.A State space approach

The linearized model conveniently lends itself to a state space representation. Given a set of feedback rules and quarterly data on eleven variables, it is fairly simple to use the Kalman Filter to estimate the underlying unobservable states. The filter also delivers the approximate Gaussian likelihood of the model. The first half of the state space approach consists of the reduced-rank VAR representation of the linearized model, of the form:
The second half of the state space approach consists of the observation equation relating the variables in the model to the eleven observed data series. One can label these series as \( x_i^* \). Algebraically, this idea can be represented by the observation equation:

\[
x_i^* = D_i x_i + \varepsilon_i^*,
\]

The iid (across time and variables) observation shocks \( \varepsilon_i^* \) consist of a combination of model misspecification and true observation errors, especially in the case of the vacancy and job flow data, but also in labor’s share and investment. They consist of those aspects of the data that the model does not perfectly explain. The variances of the observation errors are also estimated to maximize the likelihood function; they are bounded from below at 0.0001 for computational simplicity. The one exception is that the variance of the observation error on the inflation rate is set to 0.001 so that labor’s share is not mistakenly used to fit inflation instead.

### IV.B Calibrated and estimated parameter values

Most of the parameter values follow the calibrations used in Walsh (2002) or Gertler, Sala, and Trigari (2008), unless the data dictate another value. The values used for household preferences are within the range of standard values from the literature on postwar business cycles. Households have a habit persistence coefficient \( h \) of 0.7 based on the findings of Gertler et al. The nominal interest rate \( R \) equals 3.75 percent per year, based on real interest rates from 1923 through 1929. Output and consumption per capita grow at 1.7 percent per year. The rate of inflation is approximately zero on average. Investment (including residential structures but excluding consumer durables) is 15% of
output based on NIPA data; depreciation is 1.5% per quarter; and government spending is 8% of output. Steady state utilization is normalized to 1; it does not matter for the model.

Based on Walsh’s calibration, the gross retail markup $\mu$ equals 1.1, for a value of $\theta$ of 11. Retailers change their prices on average once every two quarters, for a value of $\omega$ of 0.5. This is based on Bils and Klenow’s (2004) estimate of about 0.5. Wages last one year, for a value of $\nu$ of 0.75, near the value used by Gertler and Trigari. The velocity of M1 shows no strong trend throughout the 1920s. This implies a per-capita nominal money growth rate of roughly 1.7 percent per year as well. This, combined with the real interest rate, implies a value of $\beta$ of 0.995.

Data on total job flows from the interwar period seem to indicate that hiring and firing in manufacturing have not changed much over the long run, so a conventional postwar calibration is used. The exogenous job separation rate $\rho^e$ equals 0.068 and the total job separation rate $\rho$ equals 0.10 per quarter. These values imply a value of $\rho^* = F(\bar{a})$ equal to 0.0343 per quarter. The idiosyncratic process $a_n$ is lognormal with an arithmetic mean of 1 and an estimated dispersion parameter $\sigma_a$ of 0.788, for a central location parameter $\mu_a$ of -0.3105. This delivers a value for $\bar{a}$ of 0.1746.

The likelihood of the model in the baseline setup favors vacancy posting costs equal to 1.83 percent of output; this is higher than the value of one percent used by Hairault (2002) and Andolfatto (1996). Not much solid external evidence exists on this parameter. The unemployment share $a$ of the matching function, in the baseline calibration, equals 0.2. Walsh cites Blanchard and Diamond (1989, 1991) who use postwar CPS data to derive an estimate of 0.4, but the joint behavior of the vacancy and accession rates during this period encourages a somewhat smaller value. This is also one
parameter which might be sensitive to linearization and the choice of a functional form
because the deviations of vacancies and unemployment are so large during the 1930s.

The steady-state unemployment rate $u$ (after separations) equals 0.06 based on
postwar values; no good unemployment data exist from this period. The worker-finding
rate $k^f$ equals 0.7 and the job-finding rate $k^w$ equals 0.6, both from Walsh’s calibration.
These imply that there are 0.0514 vacancies $v$ in the steady state. The baseline
calibration implies initial values of 0.2418 for labor’s bargaining power $\eta$ and 1.0735 for
the disutility of work $A/\lambda$. This equals 92.9% of the average wage.

The long-run productivity process has a coefficient of one, approximated as
0.99999 in order to avoid having the unit root suppressed when doing the eigenvalue
decomposition. Labor’s bargaining power and the disutility from work have a
persistence of 0.999 and 0.92, respectively, based on the likelihood function. Based on
observed data, money growth has a persistence $\rho_m$ of 0.75, while interest rates have an
autocorrelation of 0.96, and government spending has an autocorrelation of 0.96.

V Estimation results

V.A The driving processes and observation errors

The standard deviations of the seven driving processes and nine observation
error processes must be estimated by maximum likelihood. The estimated standard
deviations equal 0.0149 for the money supply shocks, 0.0958 for the government
spending shocks, 0.0183 for the productivity shocks, 0.0356 for the long-run price level
shocks, 0.2353 for the labor bargaining power shocks, 0.0089 for the labor supply shocks,
and 0.0010 for the interest rate shocks. The standard deviations of the observation error
processes are 0.001 for inflation (calibrated), 0.0037 for output, 0.0032 for employment, 0.0056 for money supply growth, 0.0004 for interest rates, 0.0283 for the log labor share, 0.1304 for vacancies, 0.2124 for the log separation rate, 0.2887 for the log accession rate, 0.0001 for government spending, and 0.1326 for investment.

Figures 1 and 2 show the real and nominal data as well as the estimated driving processes. The model matches the nominal variables as well as output and employment extremely closely. It also matches the separation rate and accession rates fairly well, but it predicts too many job flows in 1932 and too few in 1941. Even though these data are not of the best quality, they do seem to contain useful contain information about the economy of the 1920s and 1930s. The model matches the medium-run behavior of vacancies well, but the model predicts more short-run volatility than the data indicate. It also matches the high labor share during the contraction phase of the Depression; this is due to sticky nominal wages. The model matches the other variables very well.

V.B. Nominal shocks and their effects

Nominal factors appear to drive the cyclical behavior of labor markets during the Depression. The long run price level was relatively stable during the 1920s, with some deflationary pressure during the 1923 recession and some very mild inflationary pressure going into 1929. It then crashed and stayed persistently low after 1933. The data, narrative history, and model all agree that expectations of persistent price changes played a large role in the business cycle dynamics of the period. In contrast with Eggertsson (2008), this model indicates that the environment throughout the 1930s was still profoundly deflationary, primarily based on the low nominal interest rates. The intuition
for this form of deflationary bias in a liquidity trap is simple: With persistently low nominal interest rates and anything short of spectacular nominal stickiness, households’ intertemporal Euler Equation (4) demonstrates the Fisher Effect. Expected inflation tracks nominal interest rates, so as nominal interest rates decline in the long run, so does expected inflation. As Friedman (1963) noted, the low interest rates of this period appear to be a sign of deflationary, not inflationary, pressure.

Figures 4 and 5 show the cumulative effects of all the shocks in the model; the employment and output effects of the various shocks (save productivity) track each other closely. The estimated shocks from 1923 onward are fed into the model, and the effects after 1929 are shown in the charts (re-based to zero). The shocks to interest rates and to prices are taken together, since theory and measurement are silent as to their exact relationship. For both output and employment, these nominal shocks are the main drivers of the Depression. They contribute 15 points to the fall in output from trend and 19 points to the fall in employment from trend during the contraction phase of the Depression.

These shocks also account for two thirds of the 1937-38 recession in terms of the fall in output and almost the entire 1937-38 recession in terms of the fall in employment from trend, though the model does predict a longer recession than the one which actually occurred. Eggertsson and Pugsley (2006) argue that this recession was caused by the Fed’s deliberate engineering of low inflationary expectations, and the model and data are consistent with this interpretation of events. However, the model economy predicts a faster recovery from the initial onset of the Depression than the one which in fact occurred.

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4 Alternative relationships between shocks to the long run price level and interest rates were tried; they did not materially affect the total effects of these shocks, but they did affect the contribution of each shock to the total. As a result, only the total effects of the nominal shocks were reported.
happened; the model predicts recovery by the end of 1936. Since very little happened
with interest rates and with the long run price level after 1933, wage and price adjustment
should have brought the economy back to trend.

V.C. Evaluating the monetarist hypothesis

One might naturally ask the question, how well does money growth predict long-
run nominal output? Friedman and Schwartz (1963) and many authors since then assign
an important role to the money supply during the Depression period. A rough measure of
this correlation is given by regressing the forecast error of long run nominal output on the
forecast error of long run money. The coefficient obtained over the entire sample is 1.40,
with that coefficient rising to 1.61 beginning in the second quarter of 1933. It is clear
that the money supply was correlated with nominal output during this period; a simple
inspection of Figure 2 shows that they have broadly similar dynamics. This is the basis
for the monetarist claim that the money supply matters even in a liquidity trap, because
money and nominal output were positively correlated during that period.

To investigate the monetarist hypothesis, one can what happens when one takes
the additional information from the M1 money supply into account when estimating
shocks to nominal output. This is done by replacing equation (38) with the expression:

\[ \ln(J_t) = \ln(J_{t-1}) - \ln\left( \frac{P_t}{P_{t-1}} \right) - \ln\left( \frac{Y_t}{Y_{t-1}} \right) + \frac{1}{1 - \rho_M} \epsilon_{t}^{\Phi} + \epsilon_{t}^{\nu}, \]

(38M)

and reestimating the shock processes. This specification restricts nominal output in the
long run to be governed solely by the money supply and by a structural shock to the long-
run velocity of money. In a low interest rate environment, money supply need not feed
through into nominal output in every period (that is, velocity can vary endogenously in
the short run). In the long run, however, as conditions return to normal, one would expect velocity to revert to its long-run value. If the money supply were effective at providing a nominal anchor, then this is equivalent to saying that the quantity theory holds in the long run but not necessarily in the short run.

Figure 6 shows the results of this exercise. The effects of money supply shocks in this monetarist model mostly follow the underlying process of money growth. That is, money does exert a contractionary influence from 1929 through 1933. However, the money supply shot up after 1933, and the model predicts that by the end of 1933, output should have reverted to trend. Indeed, the model counterfactually predicts a very large boom during the mid-1930s. As a result of this anomalous behavior, the log likelihood of the monetarist model equals 1,983.4 versus 2,024.8 for the baseline model. The data strongly reject a monetarist interpretation of events of the entire decade. Not only were low interest rates an unreliable indicator of the stance of long-run monetary policy; it seems that the money supply was an unreliable indicator of the stance of long-run monetary policy.⁵ Nominal and real output growth simply did not automatically follow from money growth during the period of low interest rates.

V.D. The role of government spending and productivity shocks

A look at Figures 4 and 5 indicate a more moderate role for government spending and productivity shocks in comparison with nominal shocks. Contrary to popular wisdom, real government spending was mildly stimulative on average under the Hoover administration, adding about one percent each to employment and output between the

⁵ Taking the monetary base as the driver of long-run nominal output would only strengthen this conclusion, since the monetary base grew even more quickly than the broader aggregates during the 1930s. In fact the monetary base began to turn upward in late 1930; by this measure monetary policy was quite expansionary.
beginning of 1929 and the beginning of 1933. It did dip slightly in 1932, however. It continued to exert a mildly stimulative influence throughout the rest of the Depression, adding about 3% each to employment and output in mid-1936, and it accounted for only a tiny part of the 1937 recession. In conjunction with a moderation in deflationary expectations, war spending helped to pull the economy out of the Depression toward the end of 1941. The model and data seem to indicate that government spending (mainly in the form of military spending) played a decisive role in ending of the Depression, while it only played a limited role during the Hoover Administration and the New Deal. The changes in government spending before 1941 were simply too small to account for much, and this is in a situation with a fairly large government spending multiplier.\(^6\)

The model and data also indicate a moderate role for productivity, on the order of 7 percent of employment and 18 percent of output. The employment data used here are based on Kendrick (1961)'s quality-adjusted labor input measure. In comparison with an unadjusted measure of employment, this measure of labor input shows smaller productivity fluctuations. During this period there was a massive shift in the composition of the labor force away from manufacturing and into less-productive agriculture, and this measure accounts for much of that. The role ascribed here for movements in productivity should still be considered an upper bound on the effects of productivity shocks because of the difficulties inherent in measuring hours of work during this time, but it seems that unfavorable productivity shocks played a noticeable role in the behavior of output and employment during the contraction phase of the Depression.

\(^6\) The total cumulative multiplier (the output gain divided by the spending innovation) in this model equals 0.70 in total value, or 0.65 when taken in present value terms.
V.E. Labor market shocks and the slow recovery

The estimated bargaining power and labor supply shifters shifted upwards, persistently, for the entire Depression period. This indicates that there were disturbances that kept labor demand persistently low, apart from productivity and nominal shocks. Labor’s bargaining power shows slightly more cyclicality than does the labor supply shifter, while the latter made a one-time jump upward between 1933 and 1935. Figures 4 and 5 show that neither one matters much at a business cycle frequency. Their main contribution is toward the final collapse in employment in 1932 as well as the slow recovery; they also account for the persistent downward shift in the Beveridge Curve during the 1930s. Low vacancy creation precedes low employment, so while the shocks to labor’s bargaining power hit during the contraction, it took until the mid-1930s until their effects were completely felt. By contrast, labor supply remained fairly healthy until the New Deal and exerted a minor drag on employment thereafter. Overall, the circumstances in the 1930s reflect unusually sclerotic labor markets beyond what the usual nominal and real shocks would predict, and this coincides with a high labor share of income as well as a depressed Beveridge curve.

V.F The importance of the model parameters

Figures 7 through 9 show the effects of the nominal shocks under different values of the labor market parameters, after reestimating the structural shocks and holding other parameters constant. This exercise tends to overexaggerate the importance of individual parameter choices, but it offers insight into how the model works. Figure 7 shows what happens when one raises the share of vacancy posting costs to 2.2% and the standard
deviation of the idiosyncratic shocks to 1.4 (based on the likelihood function). In this case the model shows too much volatility but less persistence. Reducing vacancy posting costs to 0.7% and reducing the standard deviation of the idiosyncratic shocks to 0.19, by contrast, does not do much. Different values of the matching elasticity $a$ show the same pattern, with high values showing a deeper depression but a faster recovery, with lower values showing much smaller effects for nominal shocks. A higher value of $a$ is unlikely since that would imply a very large hiring rate due to high unemployment in 1932. The habit persistence parameter $h$ barely matters at all.

Figure 8 shows the influence of different capital market parameters. The presence and share of capital in the economy matter; a model with no capital has very little propagation of shocks, while the sensitivity of investment to interest rates magnifies the role of nominal shocks in economies with larger capital shares. A large share of investment (20%) shows similar patterns to a large share of vacancy posting costs since demand becomes more forward-looking in both cases. The specification of the depreciation and utilization schedules does not matter much. Finally, Figure 9 shows the importance of the nominal parameters. The model is sensitive to these parameters since without them nominal expectations are neutral. The model with a value of $\omega$ of 0 has only a small amount of propagation due to wage rigidity, while interestingly a sticky price parameter of 0.67 also shows somewhat fewer effects for nominal shocks. The wage stickiness parameter $\nu$ is absolutely crucial at explaining what happened during the Depression; the effect of wage rigidity on vacancy creation appears to be very important.

One can draw a few general conclusions as to how the model works based on these robustness checks. First of all, the presence of capital is crucial to get large
movements in employment and output; the forward looking parts of the model magnify demand shocks considerably. Vacancy posting costs and individual-level volatility also drive the model; without them there would be no job flows and no unemployment. The nominal stickiness parameters also matter; they provide the initial transmission mechanism from nominal shocks into real aggregates. While the exact numerical results of the model depend on the parameter values and upon model specification, the qualitative results are robust. In most cases, shocks to long run expectations can account for large portions of the recessions of 1929-33 and 1937-38, while they cannot account for the slow recovery in between. In every case, some other wedge appears to have shifted the Beveridge Curve downward.

VI Conclusion

Recent experiences with the zero bound have forced researchers and policymakers to reevaluate what actually drove the Great Depression, with the hope of not repeating it. This paper has shown that a modern model of unemployment, when fed with a series of plausible shocks to long-run expectations, can replicate much of the cyclical behavior of real aggregates during that period. However the model still relies on labor supply and vacancy wedges to account for the slow recovery after 1933. This is consistent with the view that restrictive labor market policies caused unemployment to remain structurally high, and it coincides with a drastic downward shift in the Beveridge Curve. If the Depression had been caused by nominal shocks alone, the US economy should have recovered quite well by the mid to late 1930s.
The results of these estimations also cast a revisionist view on the importance of the money supply and of inflationary expectations during the Depression. The money supply does show a positive relationship with the long-run price level during this period, but the model also rejects the view that exogenous changes in the money supply drove nominal output. Otherwise, 1934 through 1936 would have been years of great prosperity. This is consistent with New Keynesian thinking, whereby nominal spending is a purely forward-looking variable in conditions of slack money demand. Instead, the persistently low interest rates of the period indicate a profoundly deflationary environment, even after 1933.

The relative unimportance of monetary aggregates and the continued deflationary pressures indicated by low nominal interest rates are at odds with most traditional views of the 1930s, but they hold special relevance for policymakers faced with a low interest rate environment. In this type of situation the usual indicators of monetary policy are no longer reliable guides as to the evolution of nominal output, and expectations of the long run become particularly important in determining current outcomes. Policymakers need to take this into account when designing policies to cope with low interest rates; in a liquidity trap one should not mistake low interest rates and an expanding money supply for inflationary pressure.
Appendix A: Numerical solution to the model

A.1 Deriving the steady state from calibrated parameters

The state-space approach requires a specification for the state equation which comes from the linearized model. The linearized model in turn contains coefficients which depend on the steady state of the model. Deriving the steady state from the calibrated parameters while taking growth rates into account is fairly straightforward.

Given a nominal interest rate $R$, a balanced growth rate $\Gamma$, a gross inflation rate $\Pi$, and a risk aversion parameter $\sigma$, it is possible to calibrate the rate of time preference $\beta$ from equation (I.4) after noting that the costate variable $\lambda$ grows at rate $\Gamma$:

$$ R\Pi = \beta \Gamma. $$

(A1)

In a zero-inflation steady state with a driftless velocity, the money growth rate $\Theta$ simply equals the economic growth rate $\Gamma$. Given a markup $\mu$, one can solve the equation

$$ 1 - \frac{\theta}{\theta - 1} = \mu, $$

to get $\theta$.

Given a process for $a_t$ and total and exogenous separation rates $\rho$ and $\rho^x$, it is possible to derive the endogenous separation probability and the cutoff value for productivity:

$$ F(\tilde{a}) = \rho^e = \frac{\rho - \rho^x}{(1 - \rho^x)}. $$

(A2)

Given an observed unemployment rate $u$ as well as a total separation rate $\rho$, and job and worker finding rates $k^w$ and $k^f$, it is easy to find the number of employed (before separations):

$$ \text{employed} = u \frac{k^w}{k^f}. $$
the number of vacancies from the homogeneous matching function,

\[ k' v = k'' u , \]  

(A4)

and the retention rate:

\[ \varphi = (1 - \rho^s)[1 - F(\bar{a})] . \]  

(A5)

The capital evolution equation, given a steady state investment ratio and depreciation rate, determines the steady-state capital-output ratio:

\[ s_k = \frac{s_i}{(\Gamma - 1 + \delta)} , \]  

(A6)

and the intertemporal investment equation determines \( \rho_k \) and the depreciation elasticity parameter:

\[ \rho_k = R(R - 1) + \delta , \]  

(A7)

and

\[ \phi_k = \frac{\rho_k}{\delta} . \]  

(A8)

The demand for capital and the value of vacancy posting costs \( s_v \) determine the value of \( \alpha \):

\[ \alpha = \frac{P_c s_i \mu}{1 + s_v} . \]  

(A9)

Given the output equation, one can then find a value for gross output \( Q \):

\[ Q = \frac{(1 - \rho)N}{1 - F(\bar{a})} \left( \int_{\bar{a}}^{\infty} a dF(a) \right) \left[ \frac{\alpha}{\mu \rho_k} \right]^{\frac{\alpha}{1 - \alpha}} . \]  

(A10)

This gives values for \( Y \) and \( \gamma \) based on the equation for value added:
\[ Y = \frac{Q}{1 + s}, \quad (A11) \]

and
\[ \gamma^v = \frac{Q - Y}{v}. \quad (A12) \]

The average surplus is taken from integrating over output in excess over the reservation value:
\[ s = \frac{(1 - \alpha) \int_{a_1}^{a} (a_i - \bar{a}) dF(a_i) \left[ \frac{\alpha}{\mu_r^k} \right]^{v - \alpha}}{(1 - F(\bar{a})) \mu R}. \quad (A13) \]

The surplus equation a closed-form expression for \( q \):
\[ q = \frac{\varphi(1 - k^w) s + k^w \gamma^v}{R}, \quad (A14) \]

and the vacancy posting condition yields the firm’s share of the surplus:
\[ s^f = \frac{\gamma R \gamma^v}{k^f \varphi \kappa}. \quad (A15) \]

The real wage follows the form (in steady state):
\[ W = R \left( \frac{(1 - \alpha) Q}{\varphi N \mu R} - s^f + \frac{\gamma^v}{k^f} \right) \quad (A16) \]

and the rebargained wage is given by
\[ W^* = W \left( \frac{1 - \nu / \Gamma}{1 - \nu} \right). \quad (A17) \]

The initial value of the costate variable in consumption is determined by the first-order condition of the household’s optimization problem:
\[ \frac{1}{C - hC / \Gamma} - \frac{\beta h}{C - hC} - \lambda = 0, \quad (A18) \]
and the surplus equation yields $A$:

$$A = \left( \frac{(1 - \alpha)Q}{qN_{UR}} - s + q \right) \lambda. \tag{A19}$$

The price of vacancies can be normalized (by extension determining $\gamma$):

$$p^v = 1. \tag{A20}$$

The initial value of the velocity does not matter for the calibration of this model and can be set to one.

### A.2 Linearization around the steady state

Linearizing the quantity equation in first differences obtains the stochastic money demand relation (which determines velocity implicitly):

$$\hat{x}_t + \hat{y}_t - \hat{\Theta}_t - \Delta\hat{V}_t = \hat{\gamma}_{t-1}. \tag{A21}$$

The evolution of the number of matches comes from the accounting condition after substituting the relationship between matches and vacancy filling:

$$\dot{n}_{t+1} = \phi\dot{n}_t + \phi\hat{\phi}_t + \left( \frac{v_{k_f}}{N} \right) \hat{y}_t + \left( \frac{v_{k_f}}{N} \right) \hat{k}_{t+1}. \tag{A22}$$

The endogenous job destruction margin comes next:

$$\dot{\lambda}_t = \hat{\lambda}_t + \frac{1}{1 - \alpha} \hat{\mu}_t + \frac{\alpha}{1 - \alpha} \hat{\rho}_{t+1}^f - \hat{\zeta}_t - \left( \frac{q}{A/\lambda - q} \right) \hat{\gamma}_t,$$

$$+ \left( \frac{A/\lambda}{A/\lambda - q} \right) (\hat{\lambda}_t - \hat{\lambda}_t), \tag{A23}$$

followed by an expression for the job retention rate:

$$\hat{\phi}_t = \left( \frac{\rho^*}{1 - \rho^*} \right) e_{\rho^*} \hat{\lambda}_t, \tag{A24}$$
where $e_{Fa}$ equals the elasticity of $F$ with respect to $\tilde{a}$. The number of job seekers is approximated by the expression

$$\hat{n}_i = -\left(\frac{\varphi N}{u}\right)\hat{\phi}_i - \left(\frac{\varphi N}{u}\right)\hat{\mu}_i. \quad (A25)$$

The parameterization for the matching function ensures that the vacancy filling probability relates to vacancies and job searchers:

$$\hat{k}_i^v = a\hat{n}_i - a\hat{\nu}_i, \quad (A26)$$

and the job finding probability relates to the vacancy filling probability such that

$$\hat{k}_i^f + \hat{\nu}_i = \hat{k}_i^v + \hat{\mu}_i. \quad (A27)$$

Linearizing the job posting condition yields:

$$\hat{\dot{p}}_i^v = \hat{k}_i^f - \hat{r}_i + E_i\hat{\Phi}_{v+1} + E_i\hat{\Delta}_{v+1} + E_i\hat{\Phi}_{v+1}. \quad (A28)$$

Linearizing the output equation yields:

$$\hat{\dot{y}}_i = \left(\frac{Q}{Y}\right)(e_{Ha}\hat{a}_i + \phi_i + \hat{n}_i + \hat{\nu}_i = -\frac{\alpha}{1-\alpha}\hat{\mu}_i - \frac{\alpha}{1-\alpha}\hat{\rho}_i)$$

$$-\left(\frac{\rho p^+}{Y}\right)(\hat{\nu}_i + \hat{\rho}_i), \quad (A29)$$

where $e_{Ha}$ equals the elasticity of $H(\tilde{a}) = \frac{1}{1-F(\tilde{a})}\int_{\tilde{a}}^\infty a_i dF(a_i)$ with respect to $\tilde{a}$.

The asset pricing equation follows its typical form:

$$\hat{\lambda}_i = \hat{r}_i + E_i\hat{\lambda}_{v+1} - E_i\hat{\Phi}_{v+1}, \quad (A30)$$

and the first-order condition for consumption becomes:

$$\frac{\Gamma^2 + \beta h^2}{(\Gamma - h)^2} \hat{c}_i + \frac{\Gamma \beta h}{(\Gamma - h)^2} E_i\hat{c}_{v+1} - \frac{\Gamma h}{(\Gamma - h)^2} c + \hat{\lambda}_i = 0. \quad (A31)$$
The conditions for the retail sector give rise to a New Keynesian Phillips Curve linearized around a zero inflation steady state:

$$\frac{\omega}{R} E, \dot{x}_{t+1} = \omega \dot{x}_t + (1 - \omega) \left( 1 - \frac{\omega}{R} \right) \mu_t. \quad (A32)$$

The relationship between the continuation value of the surplus and future values of that surplus is approximated by the following:

$$q\dot{q}_t = \frac{\phi \Gamma s(1 - k_w)}{R} (E, \dot{\phi}_{t+1} - \dot{r}_t + E, \dot{x}_{t+1} + E, \dot{s}_{t+1})$$

$$+ \left( \frac{k_w p^v}{k} - \frac{\phi \Gamma s k_w}{R} \right) \dot{k}^v + \frac{k_w p^v}{k} (\dot{p}_t^v - \dot{k}_t^v). \quad (A33)$$

To get the factor shares and the continuation value of the match, it is helpful to have a linearized equation for the average surplus:

$$(s) = (1 - \alpha) \left( Y/Q, \dot{y}_t, \frac{\Gamma p^v}{Q} (\dot{v}_t, \dot{p}_t^v) - \phi_t - \dot{n}_t - \mu_t - \dot{r}_t \right)$$

$$- \frac{\alpha}{A} (\dot{\lambda}_t - \dot{\lambda}_t) + q\dot{q}_t, \quad (A34)$$

The surplus imbalance is linearized as follows (in levels, not log levels):

$$\dot{\lambda}_t = s^v \dot{s}^v_t - (1 - \eta)s\dot{s}_t + \eta s \dot{n}_t, \quad (A35)$$

and the transition equation for this expected imbalance, which determines the wage bargain, is linearized as:

$$\dot{\lambda}_t = \frac{W^*}{R} \dot{w}_t^* - \frac{W}{R} \dot{w}_t - \left( \frac{W^* - W}{R} + \frac{\phi \Gamma L}{R} \right) \dot{r}_t + \frac{\phi \Gamma L}{R} (E, \dot{\phi}_{t+1} + E, \dot{x}_{t+1})$$

$$+ \frac{\phi \Gamma}{R} E, \dot{\lambda}_{t+1}. \quad (A36)$$

The sticky wage equation becomes
The firm’s portion of the surplus, on average, is given as follows, after substituting in the job creation condition:

\[
s_t^{\prime} = \frac{(1-\alpha)Q_r}{\phi_N \mu R_t} - \frac{W}{R_t} + \frac{\gamma p_t^{\prime}}{k_t^{\prime}},
\]

so

\[
s_t^\prime \hat{y}_t = (1-\alpha)Y \hat{y}_t + \frac{(1-\alpha)\gamma p_t^{\prime} v_t}{\phi_N \mu R} - (1-\alpha)Q \hat{y}_t \left( \mu_t + \phi_t + \hat{n}_t \right)
- \frac{W}{R} \hat{w}_t + \left( \frac{\gamma p_t^{\prime}}{k_t^{\prime}} + \frac{1-\alpha)Y p_t^{\prime} v_t}{\phi_N \mu R} \right) \hat{p}_t^{\prime} - \frac{\gamma p_t^{\prime}}{k_t^{\prime}} \hat{k}_t^{\prime} + \left( \frac{W}{R} - \frac{(1-\alpha)Q}{\phi_N \mu R} \right) \hat{r}_t. \tag{A38}
\]

The resource constraint is linearized as

\[
\hat{y}_t = s_t \hat{c}_t + s_t \hat{i}_t + s_g \hat{g}_t, \tag{A39}
\]

and the capital transition equation is linearized as

\[
s_k \Gamma \hat{k}_{t+1} = s_k (1-s_s) \hat{k}_t - s_s s_k \phi \hat{n}_t^k + s_i \hat{i}. \tag{A40}
\]

The return to capital is given by

\[
\hat{\rho}_t^{\prime} = \frac{Q}{Y} \hat{y}_t + \frac{\gamma p_t^{\prime} v_t}{Y} \left( \hat{v}_t + \hat{p}_t^{\prime} \right) - \hat{k}_t - \hat{n}_t^k. \tag{A41}
\]

and the investment equation is given by

\[
R(\hat{r}_t - E_r \hat{r}_{t+1}) = \frac{\rho^k N_k}{R} - E_r \hat{p}_t^{\prime} + \left( \frac{\rho^k N_k - s_g \phi}{R} \right) E_r \hat{n}_t^{k+1}
- \frac{\rho^k N_k - s_g}{R} E_r \hat{r}_{t+1}, \tag{A42}
\]
while the utilization equation is given by

\[
\frac{d\hat{r}_t}{dt} = \frac{\rho^k N_k}{R} E_r \hat{p}_t^{\prime} - \left( \frac{\rho^k N_k - s_g \phi}{R} \right) E_r \hat{n}_t^{k+1}.
\]
\[ \hat{\rho}_i^k = (\phi - 1)\hat{n}_i^k. \]  

(A43)

Finally, it is necessary to include the seven linearized driving processes:

\[ \hat{\Theta}_i = \rho_n \hat{\Theta}_{i-1} + \epsilon_i^\Theta, \]  

(A44)

\[ \hat{g}_i = \rho_s \hat{g}_{i-1} + (1 - \rho_s)\hat{z}_{i-1} + \epsilon_i^g, \]  

(A45)

\[ \hat{z}_i = \rho_t \hat{z}_{i-1} + \epsilon_i^z, \]  

(A46)

\[ \hat{r}_i = \rho_r \hat{r}_{i-1} + \epsilon_i^r, \]  

(A47)

\[ \hat{\eta}_i = \rho_{\eta} \hat{\eta}_{i-1} + \epsilon_i^\eta, \]  

(A48)

\[ \hat{\Lambda}_i = \rho_{\Lambda} \hat{\Lambda}_{i-1} + \epsilon_i^\Lambda, \]  

(A49)

and

\[ \hat{J}_i = \hat{J}_{i-1} - \hat{\phi}_i - \hat{Y}_i + \epsilon_i^\phi + \epsilon_i^Y. \]  

(A50)

The end result of all of this is a reduced-rank VAR representation that provides the laws of motion for the underlying system for the state-observer setup.
Appendix B: Construction of the dataset

Constructing a consistent set of quarterly interwar labor market data required synthesizing a quarterly dataset from a number of different sources. This appendix contains details on the construction of these data elements and their sources:

1. The quarterly growth rate in the GNP deflator. The NIPA deflator post-1929 was used; the Kendrick (1961) deflator was used before that. They were interpolated using the growth rates of the price index for department store sales and of the BLS’s index of wholesale prices, both available from the NBER database.

2. The level of real output. The NIPA data were used post-1929 and the Kendrick (1961) data before that. These were interpolated using the FRB industrial production index and real department store sales. The former is available from the St. Louis Fed and from the Federal Reserve Board; the latter is available from the NBER database. This is taken to be at trend relative to population in 1923, 1928, and 1948. One appealing feature of using the Kendrick data is that he adjusts for long-run sectoral changes, avoiding much of the spurious choppiness that older fixed-weight indexes imposed on the data.

3. A measure of labor input. The Kendrick (1961) quality-adjusted labor input data were used. They were interpolated using the BLS’s series on employment for production workers. The main features of these data as opposed to quality-unadjusted data are that they scale down part-time workers to a full-time equivalent basis, and that they make some attempt to control for composition differences. During the mid-1930s, for instance, agricultural employment (particularly self-employment) did not significantly decrease while manufacturing employment stayed depressed. Not controlling for this
paints a misleading picture of productivity, since it is those less productive sectors which were less hit by the Depression. More historical work needs to be done in terms of measuring the hours of the self-employed and refining the quality adjustments for these labor series. It seems that adjusting for shorter workweeks and composition moves one in the right direction with regard to reconciling employment and output data. This is taken to be at trend, relative to population, in 1923, 1928, and 1948.

4. The growth rate in M1. The end-of-month data come from the appendices of Friedman and Schwartz (1963) via the NBER, with the money supply defined as currency plus adjusted demand deposits held by the public. These are then averaged throughout the quarter. These monthly averages, in turn, equal the average of the money supply at the end of the previous month and the money supply at the end of the current month.

5. A nominal interest rate. The banker’s acceptance rate is used (from the NBER) since it tracks the risk-free interest rate closely and provides consistent data for the entire period. There is no comparable series of short-term treasury notes available from that time.

6. A measure of labor’s share of output, corrected for changes in the sectoral composition of gross income, particularly the income of proprietors and government workers. Economywide compensation is first calculated as the labor share of corporate GDP less taxes on production and imports, times total GDP. To do this, an annual series is constructed for the corporate share of gross income originating from 1922 onward. Moroney (1964) and Osborne and Epstein (1956) report data on corporate net income originating, that is, income gross of direct corporate taxes but net of depreciation and indirect taxes (taxes on production and imports). Using data on corporate depreciation
allowances, investments treated as expenses, and inventory valuation adjustments published by Goldsmith (1955), an approximate capital consumption allowance is added back into these series using the national income accounting rules prevalent at the time. This yields a measure of corporate gross income originating, net of taxes on production and imports. Data for the post-1929 period come directly from the NIPA. Using 1958-vintage NIPA (U.S. Income and Output, 1958) data as a reality check, it appears that the data constructed by this method from the 1958 and 2009 vintages show similar behavior after 1929, with the 1958-vintage data showing slightly larger changes in labor’s share during the trough of the Contraction. In the interest of conservatism, the 2009-vintage series was used, ratio-spliced to the 1958-vintage series at 1929 where the 2009-vintage series begins. This composite series shows no clear trend in labor’s share from 1922 through 2009. This lack of trend contrasts with the long-run rise in labor’s share of economywide value added, reflecting the decline in proprietor’s income from agriculture and the increase in labor income from government.

Economywide compensation is then interpolated by using the FRB’s index of composite wages as well as manufacturing labor input. This way, compensation and income estimates are interpolated independently of each other. The labor share is calculated with compensation as the numerator and nominal GDP as the denominator.

7. A measure of vacancies. The Met Life help wanted series is used. It is seasonally adjusted at the source. The vacancy-employment ratio appears to be relatively stable, and it is taken to be at trend in 1948, with trend vacancies being determined by trend labor input. Zagorsky (1998) documents the long-run stability of this trend using data through the early 1990s. Most notably, vacancies remain above trend during the
1920s and then collapse right around the end of 1929. They fall below trend and remain there until the third quarter of 1942 when they shoot upward because of the effects of the war. Arithmetic percent deviations are taken from trend.

8. A measure of the separation rate of workers. These data come from the appendix to Woytinsky (1942) augmented by issues of Employment and Earnings from the 1970s. Woytinsky warns of a break in the methods used to compute the series between 1929 and 1930 but finds that these data, taken together, still provide a useful picture of interwar labor flows. The series behaves much as one would expect given the fact that recessions often come with a burst of job destruction and reductions in the accession rate. The pre-1930 series are also re-meaned and amplitude adjusted in order to match the post-1930 series in terms of overall levels. As it is, the inclusion or exclusion of these data and the specification of the measurement errors on the job flow variables will not particularly affect the results of the estimates in this paper. These data should not be taken too literally, but they provide some information about the cyclical behavior of job flows during this period. As with the quality-adjusted labor input data, this situation cries out for more historical work to be done.

9. A measure of the rate of new hiring, from the same sources as above. Calculations proceed in much the same way, and the same caveats apply.

10. Nominal government spending is taken from Balke and Gordon (1986). These data are divided by trend nominal GDP and taken as arithmetic percent deviations from trend.

11. Nominal investment is taken from Balke and Gordon (1986) and treated the same way. Investment consists of investment in inventories, residential and
nonresidential structures, and equipment. These items show the greatest deviations from
trend, with residential structures behaving mostly like investment and somewhat like
consumption, and with the narrowest definitions of investment turning negative in levels.
Durable goods behave more like consumption goods, so they are treated as such in the
model and data.
References


Figure 1 – Real variables (observed and smoothed)

Red ‘x’ lines denote observed data; blue solid lines denote smoothed data as described in the text. For details on data sources and calculations, see text.
Figure 2 – Nominal variables and driving processes (observed and smoothed)

Red ‘x’ lines denote observed data; blue solid lines denote smoothed data as described in the text. For details on data sources and calculations, see text.

Figure 3 – Beveridge Curve, pre and post-1929 (% deviation from trend)

Source: Same data as used for Figure 1. See text for details.
Figure 4 – Estimated effects of shocks on employment, baseline model

Source: Author’s calculations, 1929.1 set to 0.

Figure 5 – Estimated effects of shocks on output, baseline model

Source: Author’s calculations, 1929.1 set to 0.
Figure 6 – Estimated effects of nominal shocks on employment, monetarist model

[Graph showing estimated effects of nominal shocks on employment, monetarist model with various scenarios labeled: Baseline (All nominal shocks), Monetarist (M shocks only), Monetarist (All nominal shocks), Data.]

Source: Author’s calculations. See text for explanation.

Figure 7 – Estimated effects of nominal shocks on employment, various scenarios

[Graph showing estimated effects of nominal shocks on employment, various scenarios labeled: Baseline, s_v=2.2%; sigma_a=1.40, s_v=0.7%; sigma_a=0.19, a=0.1, a=0.4, habit=0, habit=-0.5, Data.]

Source: Author’s calculations. Baseline: s_v = 1.83%; h = 0.7; a = 0.2; σ_v=0.788.
Figure 8 – Estimated effects of nominal shocks on employment, various scenarios

Source: Author’s calculations. Baseline: $s_t = 15\%$; depreciation = 0.015.

Figure 9 – Estimated effects of nominal shocks on employment, various scenarios

Source: Author’s calculations. Baseline: $\omega = 0.5$; $\nu = 0.75$. 