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Structure and Temporal Change of Credit Network between Banks and Large Firms in Japan

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Abstract
Credit relationships between commercial banks and quoted firms are studied for the structure and its temporal change from the year 1980 to 2005. At each year, the credit network is regarded as a weighted bipartite graph where edges correspond to the relationships and weights refer to the amounts of loans. Reduction in the supply of credit affects firms as debtor, and failure of a firm influences banks as creditor. To quantify the dependency and influence between banks and firms, we propose to define a set of scores of banks and firms, which can be calculated by solving an eigenvalue problem determined the weight of the credit network. We found that a few largest eigenvalues and corresponding eigenvectors are significant by using a null hypothesis of random bipartite graphs, and that the scores can quantitatively describe the stability or fragility of the credit network during the 25 years.

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I. Introduction

Credit-debt relation between banks and firms is one of the most important relationships among economic agents. Credit is a source of profit for a bank, and it is a fuel for a firm to make growth. The flip side of the relation is, however, the path where failures take place and their propagation occur often at a nation-wide scale, and sometimes to a world-wide extent, as we experience today.

It is well known that the Japanese banking system had undergone a considerable deterioration in its financial conditions for a decade in 90’s. Financial institutions in private-sector had accumulated loan losses, more than 80 trillion yen (nearly 15% of GDP), which reduced the bank capitalization, and led to the failure of three major and other small banks. Even though two major banks were nationalized in 1997, and other political decisions were made in order to maintain the stability of financial system, most banks, major and minor, decrease the supply of credit immediately even by reducing existing loans to firms. A lot of firms, especially small and medium-sized firms, had eventually suffered the loss of funding. See Brewer et al. (2003).

Financial systems are, at an aggregate level, subject to the tails of distributions for economic variables. This perspective has been recognized extensively in economics; personal income, firm-size, number of relationships among firms and banks (ownership, supplier-customer, etc.), and so on. It has been recognized that distributions and fluctuations are the keys for understanding many phenomena in macro-economy (see Aoki and Yoshikawa (2007) and Delli Gatti et al. (2008)).

![Figure 1: Historical data of the total amount of debt from banks during the calendar years, 1980 to 2005. For large firms (filled circles) and for small and medium firms (squares).](image)

Fig. 1 shows the historical data of the total amount of debt from banks for large firms and for small and medium firms. For the year 2005, 1.25% (33,833) of domestic firms are the large firms according to the classification, while the rest 98.75% are the small-medium firms. Yet the total loans for the large firms amount to be 160 billion yen, which is nearly equal to those for the small-medium firms as shown in the figure. Thus, only a fractional

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1Source: 2008 white papers on small and medium enterprises in Japan, Small and Medium Enterprise Agency. Here large firms are the companies capitalized at 100 million yen or more, and small-medium firms are the others. Calendar years are used here and throughout this paper.

part of firms dominants a half of the entire loans. Conversely, as we shall show in this paper, a large part of loans is provided by a few large banks — the tail of another distribution.

Suppose a large firm is heavily indebted with banks. Then a failure of the firm, or a default, may cause a considerable effect on the balance sheets of the banks. If the banks reduce their supply of credit, then the total supply of loans will be decreased resulting in the adverse shocks to other firms. Therefore, the study of structure of credit relationships or credit network between banks and firms, and its temporal change would give us an insight to understand the financial stability or fragility. This is precisely the purpose of this paper.

There are several related works in the literature. For example, Ogawa et al. (2007) carried out an analysis of dependency of the number of long-term credit relationships on characteristics of firms. Uchida et al. (2008) studied the relation between bank-size and credit links. Kano et al. (2006) investigated the credit of small and medium-sized firms. Studies such as Ogawa et al. (2007) focus on multiple lending relationships. Recent development of complex network analysis (see Caldarelli (2007) and references therein) has been applied to financial systems (e.g., Inaoka et al. (2004), Iori et al. (2007), De Masi and Gallegati (2007), Imakubo and Soejima (2008), De Masi et al. (2008)). In this paper, we shall study on the credit network between banks and large firms by regarding the network as a weighted bipartite graph, develop quantification of fragility of banks, and apply it to credit networks in Japan for the past 25 years.

In Section II, we describe our dataset of credit network. In Section III.A, we consider a credit network as a weighted bipartite graph, and show several statistical properties of heavy-tailed distributions. Then, in Section III.B, we propose to define a set of scores for banks and firms which measure potential influences that one agent exerts on the other. It is shown that the scores can be calculated by solving an eigenvalue problem. In Section III.C, we apply this method to our dataset from the year 1980 to 2005. The results are discussed in Section IV.

II. Dataset

Our dataset is based on the survey of firms quoted in the Japanese stock-exchange markets (Tokyo, Osaka, Nagoya, Fukuoka and Sapporo, in the order of market size). The data were obtained through their financial statements and investigation by Nikkei Media Marketing, Inc. in Tokyo, and are commercially available. They include the information about each firm’s borrowing from financial institutions, the amounts of borrowing, classified into short-term and long-term borrowings. We examined the period from the years 1980 to 2005, for which incomplete data are few, and study the time development of credit relationships by using the total of long and short-term credit.

For financial institutions, we select commercial banks as a set of leading suppliers of credit. The set comprises long-term, city, regional (primary and secondary), trust banks, insurance companies and other institutions including credit associations. During the examined period, more than 200 commercial banks existed, which are summarized in Table 1. We remark that failed banks are included until the year of its failure, and that merger and acquisition of banks are processed consistently. For quoted firms, we choose only surviving firms that are quoted in the stock markets mentioned above.

The number of banks and firms in each year is summarized in Fig. 2. The classification of banks and industrial sectors of firms are shown in Table 1 and Table 2 respectively.

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3Based on the lists of surviving firms and quoted firms in September and December 2007 respectively. Firms registered on over-the-counter (OTC) market and/or on JASDAQ (the present OTC market) are excluded. The dataset include the OTC and JASDAQ data since 1996, so we exclude them also by checking the listing date of the firms added in the dataset.
III. Analysis of credit network

A. Credit network as a weighted bipartite graph

Each snapshot of credit network in our dataset can be regarded as a bipartite graph. Nodes are either banks or firms\(^4\). Banks and firms are denoted by Greek letters \(\mu (\mu = 1, \ldots, n)\) and Latin letters \(i (i = 1, \ldots, m)\) respectively. \(n\) is the number of banks, and \(m\) is that of firms. An edge between a bank \(\mu\) and a firm \(i\) is defined to be present if there is a credit relationship between them. In addition, a positive weight \(w_{\mu i}\) is associated with the edge, which is defined to be the amount of the credit. We can depict the network as shown in Fig. 3.

\[ w_{\mu i} = \text{the amount of lending by bank } \mu \text{ to firm } i, \] which precisely equals to the amount of borrowing by firm \(i\) from bank \(\mu\). The total amount of lending by bank \(\mu\) is

\[ w_\mu := \sum_i w_{\mu i}, \tag{1} \]

and the total amount of borrowing by firm \(i\) is

\[ w_i := \sum_\mu w_{\mu i}. \tag{2} \]

\(^4\)Note that banks are not included in the side of firms, even if they are borrowing from other banks, in our dataset. Thus interbank credit is not considered here.
We note that a same value $w_{i\mu}$ has different meanings as a weight to the bank $\mu$ and the firm $i$. For example, even if 90% of the total lending of the bank $\mu$ goes to the firm $i$, it may be the case that $i$ depends on $\mu$ by only 10% for all the loans from banks. It would be natural to define an $(n \times m)$ matrix $A$ whose component is given by

$$A_{i\mu} := \frac{w_{i\mu}}{w_\mu}.$$  

(3)

$A_{i\mu}$ represents the relative amount of lending by bank $\mu$ to firm $i$. We have

$$\sum_i A_{i\mu} = 1 \text{ for all } \mu .$$  

(4)

Similarly, we define an $(m \times n)$ matrix $B$ by

$$B_{i\mu} = \frac{w_{i\mu}}{w_i}.$$  

(5)

$B_{i\mu}$ represents the relative amount of borrowing by firm $i$ from bank $\mu$. We have

$$\sum_\mu B_{i\mu} = 1 \text{ for all } i .$$  

(6)

Degree $k_\mu$ of bank $\mu$ is the number of edges emanating from it to firms, and degree $k_i$ of firm $i$ is the number of edges to banks. When the weights $w_{i\mu}$ are all equal to 1, it is obvious that $k_\mu = w_\mu$ and $k_i = w_i$.

The distributions for $w_{i\mu}$, $w_i$, $k_\mu$, $k_i$ have long-tails. They are shown, for the data of credit relationships in the year 2005, from Fig. 4 (a) to (d). There is a significant correlation between $w_{i\mu}$ and $k_\mu$, in a natural way, and also for $w_i$ and $k_i$, as shown in (e) and (f) respectively. See De Masi et al. (2008) for extensive study on statistical properties.

B. Fragility and dependency scores of banks

A pair of bank and firm establish a credit relationship for obvious reasons. A bank supplies credit in anticipation of interest margin, and a firm demands for credit as an important source of financing in anticipation of growth in its business. An edge of credit, therefore, represents dependency of one agent on the other in twofold ways.

$A_{i\mu}$ quantifies the dependency of bank $\mu$ on firm $i$ as a source of profit. Also $B_{i\mu}$ is the dependency of firm $i$ on bank $\mu$ as a source of financing from financial institutions. The flip side of dependency is a potential influence which one agent exerts on the other. Suppose that bank $\mu$ shrinks the amount of its supplied credit, firm $i$ would be influenced to a certain extent that might be quantified by $B_{i\mu}$. Similarly, if firm $i$ fails or delays its repayment, then its effect to bank $\mu$ would propagate to an extent being measurable by $A_{i\mu}$.

From this consideration, it would be reasonable to define a set of scores on banks and firms in the following way. Assume that financial fragility can be quantified by a score — $x_\mu$ for bank $\mu$ and $y_i$ for firm $i$. The above consideration leads us to think about the influence from one score to the other by a set of equations that express the influence:

$$y \propto Bx ,$$  

(7)

$$x \propto Ay ,$$  

(8)

where $x$ and $y$ are the vectors with components, $x_\mu$ and $y_i$, respectively. It then follows that

$$P x = \lambda x ,$$  

(9)
Figure 4: (a) Cumulative distribution $P_{>}(w_{\mu})$ for banks’ lending $w_{\mu}$. (b) $P_{>}(w_{i})$ for firms’ borrowing. (c) $P_{>}(k_{\mu})$ for the number of banks’ lending relationships. (d) $P_{>}(k_{i})$ for the number of firms’ borrowing relationships. (e) Scatter plot for banks’ $w_{\mu}$ and $k_{\mu}$. (f) Scatter plot for firms’ $w_{i}$ and $k_{i}$. All the plots are for the data in the year 2005. In the plots (a),(c) and (e) for banks, the points are drawn according to the classification given in Table 1. Rank correlations (Kendall’s $\tau$) for (e) and (f) are $\tau = 0.825(16.0\sigma)$ and $\tau = 0.450(28.3\sigma)$ respectively ($\sigma$ calculated under the null hypothesis of statistical independence).
where \( P := AB \). \( \lambda \) is its eigenvalue and \( x \) is the corresponding eigenvector. We call \( x \) “fragility” scores of banks.

Alternatively, another set of scores could be defined, which we call “dependency” scores and represent the extent of dependency in our consideration above. Namely, they are \( u_\mu \) for bank \( \mu \) and \( v_i \) or firm \( i \) which satisfy

\[
\begin{align*}
    v & \propto A^T u , \\
    u & \propto B^T v .
\end{align*}
\]

This leads to another eigenvalue problem, \( P^T u = \lambda u \), or equivalently

\[
\begin{align*}
    u^T P &= \lambda u^T .
\end{align*}
\]

Here and hereafter \( T \) represents the transpose of a matrix or a vector, and we also suppose a vector as a column vector by convention.

Thus, the set \( x \) of fragility scores of banks is the right eigenvector of the weight matrix \( P \) as in Eq.(9), and the set \( u \) of dependency scores of banks satisfy the left eigenvector of \( P \) as in Eq.(12). Let us first prove mathematical properties on eigenvalues and eigenvectors, and show that the score \( u \) can be calculated directly from the score \( x \).

Eq.(9) is written explicitly in components as

\[
\frac{1}{w_\mu} \sum_{i,\nu} \frac{1}{w_i} w_{i \mu} w_{\nu i} x_\nu = \lambda x_\mu ,
\]

which we rewrite as

\[
\sum_{i,\nu} \frac{1}{w_i} w_{i \mu} w_{\nu i} x_\nu = \lambda w_\mu x_\mu .
\]

On the other hand, Eq.(12) is

\[
\sum_\mu u_\mu \frac{1}{w_\mu} \sum_i \frac{1}{w_i} w_{i \mu} w_{\nu i} x_\nu = \lambda u_\nu ,
\]

which, after exchanging \( \mu \leftrightarrow \nu \), reads as

\[
\sum_{i,\nu} \frac{1}{w_i} w_{i \mu} w_{\nu i} \frac{u_\nu}{w_\nu} = \lambda u_\mu .
\]

By comparing Eq.(14) and Eq.(16), we find that they are equivalent under the identification:

\[
u_\mu \propto w_\mu u_\mu .
\]

This also proves that left-eigenvalues and the right-eigenvalues have a same spectrum.

Let us consider two sets of eigenvalues and their corresponding eigenvectors, (\( \lambda^{(k)} \), \( u^{(k)} \), \( x^{(k)} \)) and (\( \lambda^{(\ell)} \), \( u^{(\ell)} \), \( x^{(\ell)} \)). We have

\[
u^{(k)}T P x^{(\ell)} = \lambda^{(k)} u^{(k)}T \cdot x^{(\ell)} = \lambda^{(\ell)} u^{(k)}T \cdot x^{(\ell)} .
\]

This means that

\[
0 = \left( \lambda^{(k)} - \lambda^{(\ell)} \right) u^{(k)}T \cdot x^{(\ell)} = \left( \lambda^{(k)} - \lambda^{(\ell)} \right) \sum_\mu u^{(k)}_\mu x^{(\ell)}_\mu .
\]
which, by the use of Eq.(17), implies that

$$0 = \left(\lambda^{(k)} - \lambda^{(f)}\right) \sum_\mu w_\mu x_\mu^{(k)} x_\mu^{(f)} .$$  \hfill (20)

Therefore, the eigenvectors should be orthonormal under the weight $w_\mu$ as a metric\(^5\). That is,

$$\sum_\mu w_\mu x_\mu^{(k)} x_\mu^{(f)} = \delta_{k\ell} .$$  \hfill (21)

It follows from Eq.(21) the orthonormality:

$$\sum_k w_\mu x_\mu^{(k)} x_\mu^{(k)} = \delta_{\mu\nu} .$$  \hfill (22)

This consideration of the inner product implies that we should take a look at the product of Eq.(14) and $x_\mu$. This leads us to

$$\lambda = \frac{\sum_i \frac{1}{w_i} \left(\sum_\mu w_\mu x_\mu^{i}\right)^2}{\sum_\mu w_\mu x_\mu^{2}} .$$  \hfill (23)

This proves that $\lambda$ is real and positive, although the matrix $P$ is not symmetric. Also we have the following inequality that holds for any value of $q$.

$$0 \leq \sum_\mu w_\mu (q - x_\mu)^2 = w_i q^2 - 2 \left(\sum_\mu w_\mu x_\mu\right) q + \sum_\mu w_\mu x_\mu^2 .$$  \hfill (24)

This leads to the inequality for the discriminant:

$$\left(\sum_\mu w_\mu x_\mu\right)^2 - w_i \sum_\mu w_\mu x_\mu^2 \leq 0 ,$$  \hfill (25)

from which it proves that the largest eigenvalue is 1.

$$0 < \lambda \leq 1 .$$  \hfill (26)

It is obvious from Eq.(23) that $\lambda = 1$ if and only if $x_\mu = q$. In fact, one can easily see, from Eq.(4) and Eq.(6) that $x_\mu = 1$ ($\mu = 1, \ldots, n$) is the eigenvector corresponding to $\lambda = 1$, provided that the bipartite graph is connected (i.e. any node of bank or firm is reachable from any other)\(^6\).

In addition, by applying the orthogonal relation in Eq.(22) to Eq.(14), it can be shown after a short calculation that the summation formula holds:

$$\sum_k \lambda_k = \sum_{\mu, i} A_{\mu i} B_{i\mu} = \text{tr} P .$$  \hfill (27)

---

\(^5\)Mathematically, $x$ is a covariant vector, $u$ is a contravariant vector, and the metric that connects them is given by $g_{\mu\nu} = \delta_{\mu\nu} w_\mu$. The orthogonalization of eigenvectors is done with respect to this metric.

\(^6\)For a disconnected graph, $x_\mu$ is constant in each connected components. The multiplicity of $\lambda = 1$ is equal to the number of the connected components.
To summarize, the eigenvector $u$ can be calculated directly from the eigenvector $x$. Also the eigenvalues satisfy $0 < \lambda \leq 1$, where the largest eigenvalue corresponds to a trivial eigenvector.

Now let us consider a perturbation, or an idiosyncratic shock, that occurs with a configuration $\delta x$ among banks. It is assumed that the shock propagates by Eq. (7) to generate $\delta y$ among firms, which in turn affects the banks by Eq. (8). Although we do not have knowledge on the time-scale for this diffusion process, it would be reasonable to assume that the structure of credit network does not change much in the meanwhile. Then the propagation of the perturbation, going back and forth from banks to themselves, could be described by the repetition of Eq. (7) and Eq. (8), or equivalently, $P^r$ for a number of iteration $r$.

Suppose that the eigenvalues are sorted in the decreasing order:

$$1 = \lambda_1 \geq \lambda_2 \geq \lambda_3 \cdots \lambda_n > 0.$$  

Ignore the subspace spanned by the trivial eigenvector $x^{(1)}$ from the perturbation, and expand the resulting vector $\tilde{x}$ with respect to the rest of eigenvectors as $\tilde{x} = \sum_{k=2}^n a_k x^{(k)}$, then

$$P^r \tilde{x} = \lambda_2^r a_2 x^{(2)} + \lambda_3^r a_3 x^{(3)} + \cdots + \lambda_n^r a_n x^{(n)}$$

$$= \lambda_2^r \left[ a_2 x^{(2)} + \left( \frac{\lambda_3}{\lambda_2} \right)^r a_3 x^{(3)} + \cdots + \left( \frac{\lambda_n}{\lambda_2} \right)^r a_n x^{(n)} \right].$$

This shows that the behavior of perturbation, in a long run $r \to \infty$, is determined mainly by the second largest eigenvalue and its corresponding eigenvector. For a finite $r$, it is suggested that one should consider only a few largest eigenvalues and the corresponding eigenvectors. On the other hand, the dependency scores, $u$, corresponding to the largest eigenvalue $\lambda = 1$ simply represents the total amount of loans, namely $u_\mu \propto w_\mu$, so we shall focus on non-trivial eigenvectors, $x^{(2)}$, $x^{(3)}$ and so on.

C. Results for the dataset

To determine significance of $\lambda_2, \lambda_3, \ldots$ and $x^{(2)}, x^{(3)}, \ldots$, we generate random bipartite graphs from the real data in the following way.

1. Cut every edge connecting bank $\mu$ and firm $i$. Then, for each original edge, we have two stubs that emanate from the bank and from the firm.
2. Retain the original weight $w_{\mu i}$ on the $k_\mu$ stubs emanating from the bank $\mu$.
3. Randomly choose a pair of a bank-stub and a firm-stub, and rewire the pair by an edge.

The procedure 3 is done so that there is no multiple edge between any pair of a bank and a firm. This rewiring procedure alters the weight as $w_{\mu i} \rightarrow w_{\mu j}$ if the edge emanating from $\mu$ to $i$ is randomly connected to $j$. Note that $w_{\mu}, k_\mu$ and $k_i$ are invariant for each $\mu$ and $i$ under rewiring, while $w_i$ becomes randomized. Therefore, the matrix $A$ has the same structure except a permutation of columns. This means that a same amount of credit is supplied by a bank to a different firm in randomly generated graphs.

The sum of eigenvalues satisfies Eq. (27). To compares the spectrum $\lambda$ with that for random graphs, one has to do so after a normalization. Define a normalized eigenvalue by

$$\tilde{\lambda}_k = \frac{\lambda_k}{\sum_{\ell=1}^n \lambda_\ell}.$$  

9
Figure 5: (a) Largest 20 eigenvalues $\tilde{\lambda}_k$ defined by Eq.(30). Squares are for the credit network in the year 2005. The points are averages for 10 realizations of random bipartite graphs with the standard deviation. (b) The components of eigenvector $|x^{(2)}_\mu|$ for the actual data in the year 2005 (solid lines). Dotted lines show absolute values of components averaged over the random graphs.

Fig. 5 (a) depicts the spectrum obtained for the credit network in the year 2005. By comparing with the spectrum for random graphs, we can say that only a few eigenvalues are significant. In this case, they are $\tilde{\lambda}_2$ and $\tilde{\lambda}_3$ (except $\tilde{\lambda}_1 = (\sum_k \lambda_k)^{-1}$), while $\tilde{\lambda}_7$ and smaller are indistinguishable from the spectrum for random graphs.

The corresponding eigenvectors $x^{(2)}, x^{(3)}, \ldots$ have components at a set of banks. To show this, $|x^{(2)}_\mu|$ is depicted in Fig. 5 (b). There are a few peaks at particular banks, while the same plot for random graphs (absolute value of each component averaged over 10 randomly generated graphs) is completely different from it.

This also demonstrates that such peaks of $|x^{(2)}_\mu|$ does not simply reflect the distribution for $w_\mu$, because under the randomization of bipartite graphs the configuration $w_\mu$ is not altered at all.

We also remark that if one simply takes into account of connectivity throwing away the information of weights, the resulting eigenvectors have quite different characteristics. This can be readily verified by assuming that $w_\mu = k_\mu$ and $w_i = k_i$, that is, by supposing that $w_{\mu i} = 1$ for each edge.
For the historical data from 1980 to 2005, we obtained the spectrum in each year to see how the eigenvalues change in time. The result is shown in Fig. 6 for the largest two eigenvalues $\lambda_2$ and $\lambda_3$ normalized by Eq.(30). There are a strong peak in the late 80’s and a drop in 1990; also two peaks around 1992 and in 1997. We also examined the components of eigenvectors, $x^{(2)}$ and $x^{(3)}$, in order to have a look at how stable or unstable the eigenstructure is during the same period of time. Fig. 7 shows the average of $|x^{(2)}_\mu|$ and $|x^{(3)}_\mu|$ for all the existed banks $\mu$ (horizontally) in the years from 1980 to 2005 (vertically from top to bottom). We can observe stable and unstable periods, and also peaks at particular banks. We shall discuss about the results in the next section.
IV. Discussion

Fig. 6 and Fig. 7 describe the temporal change of the Japanese credit network with respect to the eigenvalues and corresponding eigenvectors. In order to fully understand our propose scores of fragility for banks, one needs to compare the scores with the characteristics of financial conditions of banks, which can measure the level of financial deterioration. Yet it would be possible to relate the results with historical description on the Japanese banking system in the past 25 years.

The absolute values of the eigenvectors, in Fig. 7, have a relatively stable profile among banks from 1980 to 1986 and from 2000 to 2005. The profile has peaks at several banks, notably a few regional banks (in the middle-north geographical region). In the late 80’s, the profile is observed to be unstable, and spikes are present at two banks, from 1986 to 1989, which are in the middle-north region and are known to go financially deteriorated during the period. In the late 80’s to 90’s, the Bank of Japan (BOJ) altered monetary policy tightening the policy most notably in 1990. After the bubble collapse, during the 90’s, the profile changed into another configuration. A spike in the classification of \( h \) refers to the Credit associations (Shinkin banks). Then, in the latter half of 90’s, the profile went back to the previous one but with more peaks at other regional banks (especially at secondary regional banks). The spikes from 2003 to 2005 correspond to three banks in Okinawa.

Though we need more investigation beyond the anecdotal evidence, it is intriguing to note that several of the spikes in the profiles correspond to failed banks or banks that had been merged into larger banks.

Also we note that the peaks and spikes are present in same geographical regions as mentioned above. One of the authors (Y. F.) with collaborators recently showed that banks can be clustered into groups according to their patterns of lending to firms (De Masi et al., 2008). In fact, by defining the pattern for bank \( \mu \) by a vector \( \mathbf{a}_\mu \) that is equal to a column vector of the matrix \( A \):

\[
(a_\mu)_i := A_{\mu i}, \tag{31}
\]

it is possible to define a similarity in the lending patterns for a pair of banks \( \mu \) and \( \nu \), for example, by the inner product of the corresponding vectors \( \mathbf{a}_\mu \) and \( \mathbf{a}_\nu \). Then one can perform the clustering by clustering algorithms which include multi-dimensional scaling and hierarchical clustering. Indeed, De Masi et al. (2008) shows the minimum spanning tree (MST) calculated by a similarity measure ignoring the information of weight but considering only the connectivity from banks to firms. The resulting MST corresponds to clusters of co-financing relationships of banks, which strongly reflect the geographical regions especially for the regional banks. It would be interesting to investigate how the eigen-structure is related to those clusters.

It is also remarked that, as described in Section II, we did not include the firms that went into bankruptcy. It should be interesting to include them in the credit network in order to evaluate the effect to banks and to compare the evaluation with the structural change that followed after the bankruptcy. It would be possible to model such propagation based on our consideration in defining the scores.

V. Conclusion

We studied the structure and its temporal change of Japanese credit relationships between commercial banks and quoted firms for 25 years from 1980 to 2005. Each snapshot of credit network is regarded as a weighted bipartite graph, where each node is either a bank or a firm, and an edge between a bank and a firm is defined to be present if there is a credit relationship between them. The edge has a weight that represents the amount of credit.
Suppose that a bank shrinks the amount of its supplied credit, a firm as debtor would be influenced to a certain extent that might be quantified by a matrix that can be calculated by the weight. Similarly, if a firm fails, then its effect to a bank as debtor would propagate to an extent that is measurable from the weight. To quantify the propagation, we introduced a set of score named “fragility” and “dependency”, and proved a mathematical duality between them. The set of scores can be obtained by solving an eigenvalue problem.

By comparing the eigen-structure with that obtained in random bipartite graphs, which have same distributions for degrees of banks and firms and for normalized weight of banks, we found that the largest few (non-trivial) eigenvalues for the scores are significant. We performed historical analysis for our datasets, and showed that there are periods when the eigen-structure is stable or unstable, and that a particular set of banks, mostly a few regional banks, have large values of the fragility scores. Drastic change occurs in the late 80’s during the bubble and also at the epochs of financially unstable periods including the financial crisis. Further investigation might be necessary to relate our results based on the complex network analysis to the characteristic of banks, but we believe that our approach has a potential quantification in the structure and its development of credit relationships.
References


id | Classification                          | #  
---|----------------------------------------|----
 a | Long-term credit banks                 | 3  
 b | City banks                             | 16 
 c | Regional banks                         | 64 
 d | Secondary regional banks               | 71 
 e | Trust banks                            | 20 
 f | Life insurance companies               | 23 
 g | Non-life insurance companies           | 23 
 h | Credit associations (Shinkin banks)    | 4  
 i | Agricultural financial institutions    | 4  
 j | Shoko Chukin bank                      | 1  
 | Total                                   | 229

Table 1: Classification of commercial banks. # denotes the net number of institutions in each corresponding category during the years, 1980 to 2005. The leftmost column, a to j, is defined as a short-hand notation.

<table>
<thead>
<tr>
<th>manufacturing</th>
<th>#</th>
<th>non-manufacturing</th>
<th>#</th>
</tr>
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<td>Pulp &amp; paper</td>
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<td>Construction</td>
<td>148</td>
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<td>Chemicals</td>
<td>156</td>
<td>Wholesale trade</td>
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<td>Retail trade</td>
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<td>Securities</td>
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<td>Credit &amp; leasing</td>
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<tr>
<td>Ceramic, etc.</td>
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<td>Information Tech.</td>
<td>20</td>
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<td>Utilities (electric)</td>
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<td>Precision instruments</td>
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<td>Utilities (gas)</td>
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<tr>
<td>Other manufacturing</td>
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<td>Services</td>
<td>264</td>
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</table>

Table 2: Sectors of quoted firms in the dataset. # denotes the net number of firms in each sector during the years, 1980 to 2005. The total number of the firms amounts to 2,330.
Please note:

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