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## Problems in applying dynamic panel data models: Theoretical and empirical findings

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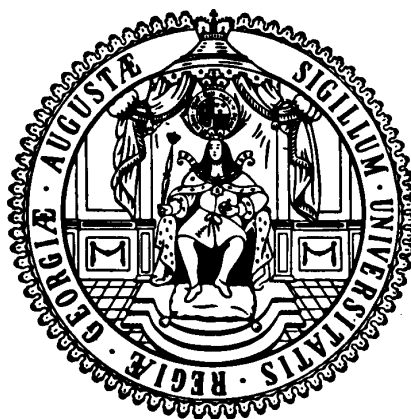
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**Problems in Applying Dynamic Panel Data Models:  
Theoretical and Empirical Findings**

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By

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**Abstract**

The objective of this paper is twofold: First, the applicability of a widely used dynamic model, the autoregressive distributed lag model (ARDL), is scrutinized in a panel data setting. Second, Chile's development of market shares in the EU market in the period of 1988 to 2002 is then analyzed in this dynamic framework, testing for the impact of price competitiveness on market shares and searching for estimation methods that allow dealing with the problem of inter-temporal and cross-section correlation of the disturbances. To estimate the coefficients of the ARDL model, FGLS is utilized within the Three Stage Feasible Generalized Least Squares (3SFGLS) and the system Generalized Method of Moments (system GMM) methods. A computation of errors is added to highlight the susceptibility of the model to problems related to underlying model assumptions.

**Keywords:**

dynamic panel data model, autoregressive distributed lag model; pooled 3Stage Feasible Generalized Least Squares estimation, panel GMM estimation, market shares

JEL: F14, F17, C23

## **Problems in Applying Dynamic Panel Data Models: Theoretical and Empirical Findings**

### **1. Introduction**

In this paper we utilize an autoregressive distributed lag model (ARDL) to estimate the dynamics of Chile's market shares in the EU market. This dynamic model has been adapted from studies of inter alia Balestra and Nerlove (1966), Baltagi and Levin (1986), Arellano and Bond (1991), Blundell et al. (1992), Islam (1995), Ziliak (1997). Cable (1997) applied an ARDL to market share behavior and mobility in the UK daily newspaper market. A common feature of all these studies (and many more studies of this kind) is that the dynamic relationship between dependent and independent variables is captured by a lagged dependent variable thus leading to an autoregressive distributed lag models. This is "the" standard dynamic model that is applied to panel data, as described in Baltagi (2005).

The main aim of this paper is to examine the applicability of the ARDL from a theoretical and an empirical point of view. From a theoretical point of view, the structure and origin of this widely used autoregressive distributed lag model are analyzed. From an empirical point of view estimation problems of the ARDL are illustrated by an empirical application to Chile's market shares in the EU market. We distinguish three types of caveats. The first caveat is related to the theory and refers to the underlying assumptions of the ARDL and the underlying geometric lag structure. The second caveat deals with the time series properties of the series and the autocorrelation problem present in most panel data sets. Finally, the third caveat centers around the endogeneity of the lagged dependent variable on the right hand side and the endogeneity of standard instrumental variables in the presence of serial autocorrelation.

The first type of problems arises because the ARDL is derived from a geometric lag (Koyck lag) model which presumes that all right hand side variables impact on the dependent variable in exactly this geometric form (Koyck, 1954). The reason for transforming the geometric lag model into an ARDL is that the geometric lag model is non-linear in its parameters. Non-linearity in the parameters was considered problematic for estimation in former times. Nowadays, modern computer software allows one to apply non-linear least squares to the Koyck-lag model so that this transformation could be regarded as superfluous. Nonetheless, ARDL continues to be "the" preferred dynamic model since it is so appealing to summarize the impact of all regressors (lagged and unlagged) in just one variable, namely the lagged dependent variable! However, derivation of the ARDL from the geometric lag model clarifies how restrictive the autoregressive ARDL could be.

The second type of problems is basically due to non-stationarity of the data entering the panel analysis. Non-stationarity leads to serial correlation, a problem that has to be dealt with if present. Panel unit root test and panel autocorrelation test must therefore be applied before running regressions to check for the presence of autocorrelated disturbances.

The third type of problems arises only when problem 2 applies. In the presence of autocorrelated error terms additional estimation problems caused by "derived endogeneity" appear. The lack of exogeneity of the lagged dependent variable and/or standard instrumental variables is the logical consequence of serial correlation. To tackle these estimation problems, the dynamic panel data model of Chile's market shares is estimated by both the Three Stage Least Squares (3SLS) and the Generalized Method of Moments (GMM) in combination with Feasible Generalized Least Squares (FGLS) to deal with the problem of endogeneity and of autocorrelation of the residuals across cross-sections and over time.

The critical examination of the preconditions, the applicability on panel data and the problematic nature of ARDL is considered as the main task of the paper and is pursued in three steps: First, we strive to clarify what it means to have the geometric lag as underlying lag structure and to outline the conditions under which a transformation from a Koyck-lag model into an ARDL would be possible. Second, the estimation problems surrounding the ARDL in the presence of autocorrelated disturbances, taking for granted that the ARDL is the true model, are discussed and two estimation methods 3SLS and system GMM are proposed. Third, ARDL is then actually applied to panel data, even though one has to be careful doing so. This last step is completed with an error analysis.

From an applied economist's point of view the objective of the paper is to analyze Chile's market share in the EU-market on a sectoral level in the period of 1988 to 2002 by applying panel time-series techniques. The widely used ARDL model is built with six cross-sections (EU countries) and fifteen annual observations for the seven most important export sectors of Chile (fish, fruit, wine, ores, wood, pulp of wood and copper). According to this model market shares are determined by Chile's and its main competitors' relative prices in the EU countries and an unobserved variable, such as strategic behavior. Price competitiveness is considered a decisive determinant of Chile's market shares since Chile's successful export products are rather homogeneous products (fish, fruit, beverages, ores, copper, and wood and products thereof).

The paper is set up as follows. In section 2 the derivation of the model and the assumptions of the ARDL are analyzed and discussed. Section 3 contains some background information on

Chile's market shares in the EU to motivate the model and its empirical application. Section 4 presents the application of the ARDL to Chilean market share data and an error analysis. Section 5 concludes.

## **2. Building an ARDL with Panel Market Share Data: Some Caveats**

### **2.1 How to Model Market Shares? Econometric Model Versus Purely Stochastic Model**

Following Sutton (2004), there are two contradicting views on the development of market shares over time: The first goes back to Alfred Chandler and asserts that market shares are robust over time and that leadership tends to persist for a 'long' time. The second view, propagated by Schumpeter, emphasizes the transience of leadership positions. Schumpeter labels those positions temporary monopolies created by invention and innovation. However, there is no benchmark for long or short leadership positions (2002 Japan Conference, 2005). We will test the relevance of these hypotheses by means of panel unit root tests. If market shares turn out to be stationary ( $I(0)$ ), this will indicate that they are robust and persistent during the period of 1988 to 2002. However, if they result to be non-stationary, then we will conclude that the Schumpeter hypothesis cannot be rejected by the 1988-2002 data.

There are also two approaches of modeling market shares: According to the first approach, market shares are basically purely stochastic, according to the second approach market shares are influenced by hard economic factors such as prices, marketing expenditure, number and strength of competitors etc. When modeling market shares, Sutton (2004) chooses an eclectic approach. Favoring the idea of building a stochastic model, he enriches the model by industry-specific features (e.g. a strategic representation of firms' competitive responses to market share changes). However, it has to be kept in mind that strategic behavior is very often intrinsically unobservable. In contrast to Sutton, we put less emphasis on the stochastic nature of market shares and stress the role played by sectoral real effective exchange rates that can be treated as an industry-specific feature. We believe that exchange rates, cost differentials, tariffs and subsidies are important 'hard' factors explaining market shares over time. Therefore, we will build a dynamic econometric model in which price competitiveness is considered as decisive for the competitive position. Since strategic behavior is difficult to model, we assume that strategic behavior and sector-specific characteristics are incorporated in the residuals of the regression model.



## 2.2 The Dynamic Econometric Market Share Model: The ARDL and the Restrictiveness of its Assumptions

An autoregressive distributed lag model will be utilized as dynamic model. Since this model serves as standard dynamic model in panel data analysis, its (general) applicability will be carefully scrutinized. Our objective is to discuss the preconditions for its applicability and its limitations by deriving this model. The ARDL approach has been applied in a multitude of cases and to diverse issues, such as the dynamic demand for natural gas, the dynamic demand for drug-like products, such as cigarettes, a dynamic model of employment, a dynamic model for growth convergence, a dynamic lifecycle labor supply model or a dynamic gravity model (see Balestra and Nerlove (1966), Baltagi and Levin (1986), Arellano and Bond (1991), Blundell et al. (1992), Islam (1995), Ziliak (1997), Kim et al. (2003)). Finally, it has also been applied to market share behavior by Cables (1997).

Cable (1997) proposes to model market shares using an autoregressive distributive lag model (ARDL)<sup>1</sup>. He selects a first order autoregressive model with a 1-period lagged endogenous variable<sup>2</sup>, in which prices and advertising share are the explanatory variables for UK's national daily newspapers.

We utilize and modify this model in the following way: Chile's market share in a specific sector is determined by Chile's price advantage (in terms of EU-Chilean producer prices and EU protection) and Chile's competitors price advantage in the EU market. In this model, changes in the real effective exchange rate in the more distant past have a smaller impact on changes in market shares than exchange rate changes of the more recent past. This assumption can be very plausible, but must be verified by the underlying data. As will be shown this model originates from a geometric lag model (Equation (1)) and enables one to model the reaction of market shares in the short, medium and long run. The lag length is expressed by  $k$  in our model.

Chile's market share in country  $i$  in sector  $s$  at time  $t$  in the geometric lag approach is modelled using a log-log-specification:

$$lshw_{ist} = \alpha_{is} + \beta_0 \lambda^0 lreer_{ist} + \dots + \beta_0 \lambda^k lreer_{ist-k} + \gamma_0 \lambda^0 lreer^*_{ist} + \dots + \gamma_0 \lambda^k lreer^*_{ist-k} + \mu_{ist} \quad (1)$$

where

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<sup>1</sup> First order autoregressive model.

<sup>2</sup> There are two types of autoregressive distributed lag models: the geometric lag model and the transfer function model, also known as ARMAX model (for a good description see Greene, 2000)

$i = 1, 2, \dots, 6$  represents the cross-sections: FRA, NDL, DEU, ITA, GBR and ESP (according to World Bank abbreviations);

$t = 1988, 1989, \dots, 2002$  are years (annual observations)

$s = 03, 08, 22, 26, 44, 47$  and  $74$  are the sectors (according to the two digit HS classification)

$lshw_{ist}$  stands for Chile's market share in EU country  $i$  in sector  $s$  at point  $t$ .  $lreer_{ist}$  is Chile's real effective exchange rate, prevailing in country  $i$  and in sector  $s$  and  $lreer^*_{ist}$  is Chile's competitor (\*) real effective exchange rate, prevailing in country  $i$  and in sector  $s$ .

Market shares in a specific sector ( $s$ ) are computed as ratio of Chile's sectoral exports ( $X$  in the numerator) and EU country  $i$ 's imports from the world  $M_i = M_{EU} + M_{non-EU}$  (in the denominator). Due to unsubstantial trade volumes, we consider only Chile's market shares in France (FRA), the Netherlands (NDL), Germany (DEU), Italy (ITA), UK (GBR), and Spain (ESP). Market shares are computed for seven sectors at the two-digit HS chapters, namely fish (03), fruit (08), beverages (22), ores (26), wood (44), pulp of wood (47) and copper (74). Sources of the data and generation of the data are described in Appendix 1. The period covered goes from 1988 to 2002. Thus, we obtain a maximum of 6 cross-sections and 15 years, resulting in a maximum of 90 observations per sector. The number of observations varies depending on the sector studied.

As to the coefficients and the disturbance in this type of model it is assumed that:  $0 < \lambda < 1$  and that  $\lambda$  is the same for all regressors. Having the same  $\lambda$  for all the regressors we can transform eq. (1) into an autoregressive distributed lag model, otherwise this will not be possible. Besides, if  $\lambda$  is the same, lag length  $k$  must be the same for all regressors, too (see Figure 1).

It is furthermore assumed that  $\beta_i = \beta_0 \lambda^i$ ,  $\gamma_i = \gamma_0 \lambda^i$  and  $\mu_{ist} \sim N(0; \sigma_\mu^2)$ .

A model that follows the above-mentioned restrictions can be transformed into the so-called first order autoregressive model which is characterized by a lagged endogenous variable on the right hand side (see Kelejian and Oates, 1981; Greene, 2000 and Nowak-Lehmann D., 2004).

By lagging eq. (1) by 1 period, multiplying through with  $\lambda$  we obtain

$$\begin{aligned} \lambda lshw_{ist-1} = & \alpha_{is} \lambda + \beta_0 \lambda^1 lreer_{ist-1} + \dots + \beta_0 \lambda^{k+1} lreer_{ist-k-1} + \gamma_0 \lambda^1 lreer^*_{ist-1} + \dots \\ & + \gamma_0 \lambda^{k+1} lreer^*_{ist-k-1} + \mu_{ist-1} \lambda \end{aligned} \quad (1')$$

By subtracting (1') from (1) and by suppressing  $\beta_0 \lambda^{k+1} lreer_{ist-k-1}$  and  $\gamma_0 \lambda^{k+1} lreer^*_{ist-k-1}$  since both terms become very, very small with large k, we obtain an autoregressive distributed lag model (eq. (2)) which is very similar to the partial adjustment model<sup>3</sup> (Kim et al., 2003):

$$lshw_{ist} = \alpha^*_{is} + \beta_{0is} lreer_{ist} + \gamma_{0is} lreer^*_{ist} + \lambda_{is} lshw_{ist-1} + v_{ist} \quad (2)$$

with  $\alpha^*_{is} = \alpha_{is}(1 - \lambda)$  and  $v_{ist} = \mu_{ist} - \lambda \mu_{ist-1}$  following a normal distribution  $N(0; \sigma_v^2)$ .

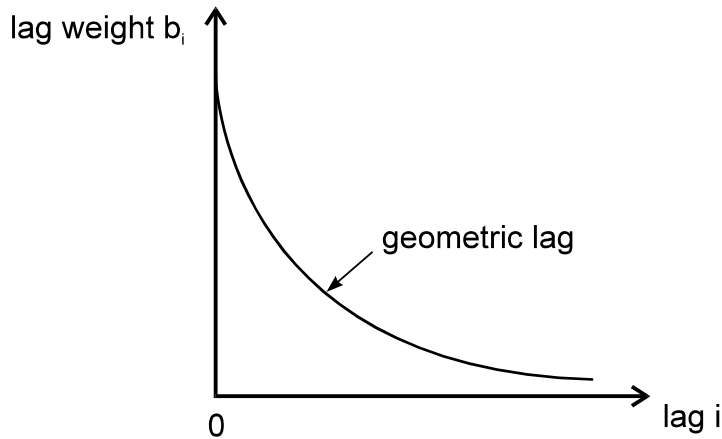
However, if  $\lambda$  becomes relatively large (say  $\lambda = 0.9$ ) and if the lag length k is short (say k = 2), suppression of the above-mentioned terms turns out to be very problematic since about 70 % (i.e.  $0.9^3$ ) of the impact of the lagged variables would be neglected. This will be shown in detail in section 4.1 and 4.2 in tables 4 and 6 which contain the error analysis.

A short lag length might constitute a problem when working with annual data, but might be of minor importance when working with monthly or daily data where the lag length is usually larger.

Besides and most important, eq. (2) is very restrictive, since the underlying model is a geometric lag model (eq. (1)) which is known to be of the following form.

**Figure 1:**

**The geometric lag distribution for a parameter  $b_i$**



Model (2) assumes not only a geometric reaction of the market share (lshw) with respect to relative prices ( $\beta_i$  and  $\gamma_i$  must follow a geometric lag) in all six importing countries i under

<sup>3</sup> The partial adjustment model would look like eq. (2\*):

investigation, but it assumes exactly the same (as measured by  $\lambda_i$ ) geometric reaction of  $lshw$  with respect to changes of all the regressors (both  $lreer$  and  $lreer^*$ ). In our case, as well as in many other studies using the ARDL, this assumption cannot be justified by the data for all regressors. Also, this specific geometric reaction does not always apply to all countries under study. These issues become even more crucial when the number of cross-sections gets bigger and when we have some more explanatory variables in the model (a model with e.g. 100 countries and 5 regressors).

Moreover, there are many instances in which the assumption of a geometric lag itself will not be fulfilled. This will be especially the case when reaction lags are present and when therefore the impact of changes in the current and the preceding periods is smaller than the impact of changes of earlier periods. In those cases the dynamic model chosen should be a polynomial lag model which allows one to estimate any lag structure that can be depicted by a polynomial of order 1, 2, ..., p.

Therefore, before applying model (1) or its linear transformation (2) the existence of a geometric relationship of the coefficients of the independent variables must be scrutinized very carefully. Incompatibility of the model assumptions with the data will necessarily lead to inconsistent estimates.

The question that remains unanswered is whether it is more convenient to estimate eq. (1), the more general geometric lag model, rather than eq. (2), the restricted model. As stated above, Eq. (1) is non-linear in its parameters, but can be estimated by Non-linear Least Squares (NLS). By estimating eq. (1) with Non-Linear Least Squares (NLS) together with SUR and FGLS one will obtain unbiased and efficient estimates if the relative prices ( $lreer$  and  $lreer^*$ ) are exogenous. That is eq. (1) involves no additional estimation problems (beyond the cross-section and serial correlation) since endogeneity of the right hand side variables does not arise if  $lreer$  and  $lreer^*$  are exogenous. However, Eq. (1) and eq. (2) have in common that the assumption of a geometric lag must be fulfilled. Non-fulfillment of this assumption will lead to biased estimates in both models.

### 2.3 Estimation Techniques for Non-Stationary Panel Data in an ARDL

Assuming for the moment that the underlying assumptions with respect to the geometric lag of the ARDL model are fulfilled, the time series properties of the series should be checked

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$lshw_{ist} = \lambda \alpha_{is} + \lambda \beta_{0is} lreer_{ist} + \lambda \gamma_{0is} lreer^*_{ist} + (1 - \lambda_{is}) lshw_{ist-1} + v_{ist}$ ; Here it is assumed that the adjustment to the desired equilibrium level of market share follows a geometric lag.

and a test of autocorrelation of the disturbances should be applied. We proceeded in several steps:

First, we test the time series properties of the data (all in natural logs). All series, i.e. market shares (lshw), Chile's real effective exchange rate (lreer) and Chile's competitors' real effective exchange rates (lreer\*) for all country-pairs are subject to tests on non-stationarity (panel unit root tests) in a first step. This procedure is applied to all seven sectors under investigation. The possible existence of structural breaks in the series is neglected because neither fundamental, abrupt changes in economic policy nor tremendous exogenous shocks could be detected in the period of 1988-2002. The governments of Aylwin, Frei and Lagos continued the economic policy of the Pinochet government. Consequently, the time series display no sign of a significant structural shift.

In the statistical analysis we allow for different unit root processes in the panel, i.e. cross-section specific (country-specific) unit roots. We apply the Im, Pesaran and Shin (2003) panel unit root test on all series thus considering the possibility of individual unit roots of our panel data. All variables (lshw, lreer, and lreer\*) are non-stationary, integrated of order one (I(1)) with a p-value of 0.00 (exception: lrpcopper with  $p = 0.02$ ). With respect to market shares, this finding supports more Schumpeter's view. According to Schumpeter, gains in market shares are temporary. Monopolistic positions have to be defended, otherwise they are lost quite fast. This view seems to especially apply to the fish, fruit, beverages, ores, and the copper sector. In the wood sectors (44 and 47), market shares appeared more stable (see figures 5-6 in Appendix 2), but non-stationary according to the tests. Table 1 presents the results.

**Table 1: Results from the Im, Pesaran, Shin (2003) Panel Unit Root Test stating t-bar values**

| <b>IPS Panel Unit Root Test Based on Individual Unit Roots</b>          |                                       |         |                     |
|---|---------------------------------------|---------|---------------------|
| <b>H<sub>0</sub>: Series has a unit root (series is non-stationary)</b> |                                       |         |                     |
| <b>Sector 03</b>  | <b>Fish and crustaceans, molluscs</b> |         |                     |
|   | Lshw03                                | Lreer03 | Lreer03*=Lreer03nor |
| Series in levels  | -1.81                                 | -1.58   | -1.94               |
| Δ Series  | -4.36                                 | -3.42   | -3.47               |
| <b>Sector 08</b>  | <b>Edible Fruit and nuts</b>          |         |                     |
|   | Lshw08                                | Lreer08 | Lreer08*=Lreer08aus |
| Series in levels  | -1.68                                 | -1.58   | -2.53               |

|                  |                                       |                        |                     |
|------------------|---------------------------------------|------------------------|---------------------|
| $\Delta$ Series  | -5.90                                 | -3.42                  | -4.11               |
| <b>Sector 22</b> | <b>Beverages, spirits and vinegar</b> |                        |                     |
|                  | Lshw22                                | Lreer22                | Lreer22*=Lreer08saf |
| Series in levels | -1.62                                 | -1.58                  | -0.92               |
| $\Delta$ Series  | -4.25                                 | -3.42                  | -3.34               |
| <b>Sector 26</b> | <b>Ores, slag and ash</b>             |                        |                     |
|                  | Lshw26                                | Lreer26                | Lreer26*=Lreer26bra |
| Series in levels | -1.29                                 | -1.58                  | -2.26               |
| $\Delta$ Series  | -4.18                                 | -3.42                  | -7.43               |
| <b>Sector 44</b> | <b>Wood and articles of wood</b>      |                        |                     |
|                  | Lshw44                                | Lreer44                | Lreer44*=Lreer44nor |
| Series in levels | -1.83                                 | -1.58                  | -1.94               |
| $\Delta$ Series  | -2.80                                 | -3.42                  | -3.47               |
| <b>Sector 47</b> | <b>Pulp of wood</b>                   |                        |                     |
|                  | Lshw47                                | Lreer47                | Lreer47*=Lreer47nor |
| Series in levels | -1.68                                 | -1.58                  | -1.94               |
| $\Delta$ Series  | -2.93                                 | -3.42                  | -3.47               |
| <b>Sector 74</b> | <b>Copper and articles of copper</b>  |                        |                     |
|                  | Lshw74                                | Lrpcopper <sup>4</sup> |                     |
| Series in levels | -1.34                                 | -1.58                  | -----               |
| $\Delta$ Series  | -4.22                                 | -3.42                  |                     |

Note: lshw = market share, lreer = Chile's real effective exchange rate, lreer\* = Chile's competitor real effective exchange rate in sectors 03, 08, 22,26,44,47,and 74.

Since all variables are I(1) one could proceed with cointegration analysis and panel cointegration tests (Pedroni, 1999; Pedroni, 2004). However, cointegration is a long-term concept, which is not applicable to our short time span. Moreover, with fifteen annual observations, the power of panel cointegration tests would be too low. But cointegration analysis is not the only approach that deals with non-stationary series and yields unbiased and efficient estimates in a dynamic model. FGLS is another possibility as is known from time series analysis. We exploit the special suitability of FGLS for estimating dynamic models with panel data (see Stock and Watson, 2003).

<sup>4</sup> Lrpcopper serves as an indicator of Chile's real copper production costs. It is used instead of lreer in the market share analysis.

FGLS in a panel analysis setting works analogously to the one in the time series setting. The idea remains the same: Non-stationarity of the series in a regression equation is reflected in the autocorrelation  $\rho$  of the residuals over time. When utilizing annual data first order autocorrelation is usually at work. This finding found statistical support in our sample.<sup>5</sup>

The procedure will be described below by abstracting from sectors for a moment. We tested eq. (3) below, after having computed the residuals  $\hat{v}_{it}$  from the ARDL model (eq. (2))

$$\hat{v}_{it} = \sum_{k=1}^K \rho_{ik} \hat{v}_{it-k} + e_{it} \quad (3),$$

with  $e_{it} \sim N(0; \sigma_{ei}^2)$  and  $k = 1, 2, \dots, K$  number of lags. Autocorrelation of the residuals is the mirror image of non-stationary series. The autocorrelation coefficient  $\rho_{ik}$ <sup>6</sup> in a way captures the autoregressive processes (expressed by  $\rho_{ik}'$ ,  $\rho_{ik}''$  and  $\rho_{ik}'''$ ) prevailing in the series (see equations (4)-(7)).

In theory we have:

$$lshw_{it} = \sum_{k=1}^K \rho_{ik}' lshw_{it-k} + e'_{it} \quad (4)$$

$$lreer_{it} = \sum_{k=1}^K \rho_{ik}'' lreer_{it-k} + e''_{it} \quad (5)$$

$$lreer^*_{it} = \sum_{k=1}^K \rho_{ik}''' lreer^*_{it-k} + e'''_{it} \quad (6)$$

$$lshw_{it-1} = \sum_{k=1}^K \rho_{ik}^{iv} lshw_{it-k-1} + e^{iv}_{it-1} \quad (7)$$

Note that FGLS uses a common  $\hat{\rho}_{ik}$  in equations (4)-(7) and transforms the variables correspondingly.

The FGLS method is applied in three steps: First, eq. (2) is estimated by SUR and the residuals are computed. Second, the order (first order, second order, or p-order) of autocorrelation  $\hat{\rho}_{ik}$  is estimated applying SUR and significance is tested in eq. (3). 1st order autocorrelation of the type  $\hat{v}_{it} = \hat{\rho}_{i1} \hat{v}_{it-1}$  turns out to be present and dominant.  $\hat{\rho}_{i1}$  expresses 1<sup>st</sup> order autocorrelation. Third, the variables of eq.(1) and (2) are transformed into

$$lshwz_{it} = lshw_{it} - \hat{\rho}_i lshw_{it-1},$$

$$lreerz_{it} = lreer_{it} - \hat{\rho}_i lreer_{it-1},$$

---

<sup>5</sup>  $\rho$  is usually well below 1 so that first differencing is a very rough method to get rid of stationarity.

$$\text{lrerz}_{it}^* = \text{lrer}_{it}^* - \hat{\rho}_i \text{lrer}_{it-1}^*,$$

$$\text{lshwz}_{it-1} = \text{lshw}_{it-1} - \hat{\rho}_i \text{lshw}_{it-2} \quad \text{and}$$

$$\varepsilon_{it} = \hat{v}_{it} - \hat{\rho}_i \hat{v}_{it-1}$$

thus generating variables in soft or quasi first differences. Eq. (2) is then estimated on basis of the transformed variables applying SUR (see Stock and Watson, 2003).

In contrast to the dynamic panel analysis literature (Baltagi, 2005), we stress the time series properties of the series more than it is usually done. The dynamic panel analysis literature usually abstracts from autocorrelation of the disturbances in order to elaborate more on the characteristics of one-way error or two-way error component models in which cross-section specific and time-specific random effects are present.

We take a different route for several reasons: First, we decide to work with a fixed effects model since our cross-sections are not randomly drawn, but selected on purpose. Second, we try to account for time series properties because our time dimension exceeds our cross-section dimension and therefore time series problems should obtain more weight.

Even though serial correlation in dynamic panel data models is only rarely dealt with in the econometric literature, the studies by Hujer et al. (2005), Kim et al. (2003), Sevestre and Trognon (1996) and Keane and Runkle (1992) dwell on this issue. Keane and Runkle (1992) and Kim et al. (2003) use the forward filtering 2SLS method (KR estimate), which treats unknown serial correlation in residual disturbance. This method pretends serial correlation to be one, which is a very rough estimate. Kim et al. (2003) refine the KR method and work with the variables in first differences. We, in contrast, estimate the extent of serial correlation in the sample (our  $\hat{\rho}_{ik}$ )<sup>7</sup> and then transform the variables correspondingly (in soft or quasi first differences). Hujer et al. (2005) assume that the residual term follows a moving average process (eg. MA(1), MA(2)). According to our data however, the residual term follows clearly an AR(1) process and not an MA(1) process. Panel analyses with macroeconomic data usually show unit-roots in the series and usually show an autoregressive error process. Therefore, time series tests on the series and the residuals are a must before starting estimation of the model.

The AR-error structure has severe consequences on the endogeneity of the instruments that can be used in the 3SLS and the GMM routine. These considerations lead us to an alternative

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<sup>6</sup> Which is to be estimated since it is unknown.



method of dealing with non-stationary series in a panel regression framework, namely to FGLS estimation techniques in combination with 3SLS and a GMM with self-selected instruments. Before interpreting the regression results we will present some facts on Chile's market shares for its most important export sectors and emphasize the role of EU and extra-EU competition. For each sector separate panel ARDLs will be run over the time period of 1988 to 2002, with the EU countries acting as cross-sections in the panel analysis.

### **3. Economic Background to the Dynamic Model:**

#### **3.1 Chile's Sectoral Market Shares in a Highly Competitive EU Market**

Based on 2003 data, the EU is Chile's first world-wide trading partner. 25% of Chile's exports go to the EU and 19% of its imports come from the EU. During the first semester of 2003, mining (predominantly copper) still represented 46% of total Chilean goods exports, while agriculture, farming, forestry and fishing products represented 13.02%. Trade with Chile represents 0.45% of total EU trade, placing Chile as 41st in the ranking of EU main trading partners. Between 1980 and 2002, EU imports from Chile increased from EUR 1.5 billion to EUR 4.8 billion, whilst EU exports to Chile increased from EUR 0.7 billion to EUR 3.1 billion (EU Commission, 2005).

Given the importance of the EU market to the Chilean export industry, Chile was eager to sign a Free Trade Agreement (FTA) with the EU (3 October 2002) in order to improve its market access to the EU. From Chile's point of view, the agreement can be clearly considered as a means to maintain and/or strengthen its competitive position in the EU market. In the short run, a reduction or elimination of trade barriers through a FTA and its impact on relative prices will improve Chile's competitive position not only with respect to the EU countries but also with respect to third countries which do not have a FTA with the EU. In the medium to long run however, the effect of the FTA will be eroded if the EU decides to conclude also FTAs with e.g. the MERCOSUR's full members and perhaps some Asian countries.

Given that Chile's main export commodities comprise copper, fish, fruits, paper and pulp, and wine and are thus heavily natural resource based, Chile's actual competitors are already numerous<sup>8</sup>: Norway, Russia, Indonesia, Malaysia, the Philippines and Thailand are much like Chile exporters of timber and rubber. Besides, the South East Asian countries were able to

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<sup>7</sup> In FGLS the unknown serial correlation coefficient is estimated as described in section 2.

<sup>8</sup> Even though Chile can still be considered the most competitive and the least corrupted economy in Latin America.

strongly increase their light manufactured exports to industrial countries in the last decade. South Africa, Australia and New Zealand, in the Southern Hemisphere, threaten Chile's position as a successful fruit and wine exporter. As far as agricultural products are concerned, Chile faces stiff competition from the EU countries. UK, Ireland and Norway are Chile's main competitors as far as fish exports are concerned. Moreover, China, enjoying low labor costs, has become a strong exporter of machinery and equipment, textiles and clothing, footwear, toys and sporting goods and mineral fuels, thus reversing in general terms Latin America's competitiveness in textile, clothing and shoe exports. When analyzing the determination of market shares (section 4, Eq. (2)) we will take account of EU and extra-EU competition.

### 3.2 Chile's Market Shares in the period of 1988 to 2002

In Table 2 we list Chile's largest export sectors, its export shares and its market shares in the EU market. In this table the EU market is considered as one market. However, in the empirical analysis we investigate Chile's sectoral market shares in specific EU countries.

**Table 2: Chile's seven most important export sectors and their competitive position**

| HS code | Sector                         | Annual percentage change of exports (1988-2002) | Export share in 2002 <sup>9</sup> | Potential extra-EU competitor <sup>10</sup> | Average Market Share in the EU <sup>11</sup> (1988-2002) |
|---------|--------------------------------|---|-----------------------------------|---|--|
| 03      | Fish and crustaceans, molluscs | 7.2 %   | 5.2 %                             | Norway                                      | 1.22 %   |
| 08      | Edible fruit and nuts          | 7.5 %   | 10.0 %                            | Australia, South Africa, New Zealand        | 2.62 %   |
| 22      | Beverages, spirits and         | 44.6 %  | 7.8 %                             | South Africa,                               | 0.77 %   |

<sup>9</sup> Share of Chile's sectoral exports in total Chilean exports.

<sup>10</sup> According to TradeCAN (World Bank, 2002)

<sup>11</sup> Share of EU imports from Chile in total EU imports (total EU imports include intra-EU trade).

|    |                             |        |        |   |        |
|----|-----------------------------|--------|--------|---|--------|
|    | vinegar                     |        |        | Australia                                   |        |
| 26 | Ores, slag and ash          | 11.9 % | 9.1 %  | Brazil, Australia, China                    | 3.75 % |
| 44 | Wood and articles of wood   | 12.4 % | 1.5 %  | Norway, Russia, Canada, Malaysia, Indonesia | 0.26 % |
| 47 | Pulp of wood                | 13.9 % | 6.6 %  | Norway, Canada, Russia                      | 2.89 % |
| 74 | Copper and articles thereof | 5.4 %  | 37.0 % | South Africa, Canada                        | 10.34% |

**Source:** EUROSTAT (2003); COMEXT CD ROM, 'Intra- and Extra-EU Trade, Annual data, Combined Nomenclature', European Commission ; own calculations.

All seven sectors experienced remarkable export growth, beverages being the most dynamic sector. It should be clarified, however, that 'beverages' started from a lower level in 1988 than the more traditional sectors such as fruit, wood, pulp of wood, and copper. Copper had the biggest market share in EU imports with 10.34 %, followed by ores (3.75 %), pulp of wood (2.89 %), and fruit (2.62 %) in the period of 1988 to 2002.

The development of Chile's market shares was subject to up and downs in most of the export sectors. Defending its market shares was no easy business for Chile in the sectors 'fish', 'fruit', and 'ores'. As to the sectors 'beverages', 'wood', 'pulp of wood' and 'copper' Chile could maintain or even strengthen its competitive position (see figures 1-7 in Appendix 2).

#### **4. Empirical Analysis of Market Shares within the ARDL**

We estimate eq. (2) as a fixed effect model allowing for cross-section specific intercepts ( $\alpha_i$ ). This model can be applied in its unrestricted form (see eq. (2)) by estimating cross-section specific slope parameters for  $lreer_{it}$ ,  $lreer_{it}^*$  and  $lshw_{it-1}$  ( $\beta_{0i}$ ,  $\gamma_{0i}$  and  $\lambda_i$ ) but given our limited number of observations in each cross-section we stick to common slope parameters in all countries. We capture country-specific effects only through cross-section specific

intercepts ( $\alpha_i$ ) and try to save degrees of freedom by modeling common slope parameters ( $\beta_0, \gamma_0$  and  $\lambda$ ) thus estimating eq. (8) for each of the seven sectors:

$$lshw_{it} = \alpha_i + \beta_0 lreer_{it} + \gamma_0 lreer^*_{it} + \lambda lshw_{it-1} + v_{it} \quad (8)$$

However, as we have seen before, the advantage of having a linear model is at the cost of having a lagged endogenous variable that is correlated with the disturbance term due to autocorrelation. When a lagged endogenous variable appears at the right hand side of a regression equation (as in the geometric lag model of eq. (2) or eq. (8)) and when the disturbances are autocorrelated (see eq. (3)), the lagged endogenous variable will be automatically correlated with the disturbance term and thus becomes endogenous. The endogeneity problem of the lagged dependent variable ( $lshw_{it-1}$ ), which is caused by first order AR-correlation of the residuals due to non-stationarity of the series, requires either the use of the Three-Stage Least Squares<sup>12</sup> or the use of the GMM (Generalized Method of Moments) technique. Modern computer programs allow one to generate the variables in soft first differences directly by adding e.g. an AR(1) term for first order autocorrelation and to simultaneously apply methods that control for the endogeneity of the regressors.

#### **4.1 Estimating the Impact of Price Competition on Market Shares Utilizing the 3SLS Approach in the ARDL model**

The choice of instruments is crucial for getting consistent estimates in any model, also in the market share model. We used an indicator of production capacity in real terms as an instrument for lagged market share ( $lshw_{it-1}$ ), the difference in PPP-income between Chile and the importing country as an instrument for  $lreer_{it}$ , and the competitor's real exchange rate in a transformation that is generally used in polynomial lag models as an instrument for  $lreer^*_{it}$ . In Table 3 the impact of price competitiveness on market shares being estimated by Three Stage Least Squares (3-SLS) is summarized.

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<sup>12</sup> Three-Stage Least Squares (3SLS) technique is the SUR version of Two-Stage Least Squares (see EViews 5: User's Guide, 2004, p. 700)

**Table 3: Results for the ARDL market share model estimated by panel-3 SLS**

|                             | <b>Regression coefficients*</b><br><b>Equation (2)</b> |   |  |                     | <b>Goodness of fit measures*</b> |                               |                                    |
|-----------------------------|--|---|--|---------------------|----------------------------------|-------------------------------|------------------------------------|
| <b>Sector-<br/>results</b>  | <b>Impact of<br/>Ireer</b><br>$\beta_{03SLS}$          | <b>Impact<br/>of Ireer*</b><br>$\gamma_{03SLS}$ | <b>Adjustm.<br/>Coeff.</b><br>$\lambda_{3SLS}$ | <b>AR-<br/>term</b> | <b>R<sup>2</sup>adjusted</b>     | <b>S.E. of<br/>regression</b> | <b>Durbin<br/>Watson<br/>stat.</b> |
| <b>03<br/>short<br/>run</b> | 0.82**<br>(0.02)                                       | -0.72<br>(0.19)                                 | -0.19<br>(0.20)                                | 0.68***<br>(0.00)   | 0.97                             | 1.02                          | 2.15                               |
| <b>08<br/>short<br/>run</b> | 1.82**<br>(0.02)                                       | -0.14<br>(0.85)                                 | -0.07<br>(0.70)                                | 0.69***<br>(0.00)   | 0.99                             | 1.05                          | 1.99                               |
| <b>22<br/>short<br/>run</b> | -2.09***<br>(0.01)                                     | 2.01***<br>(0.01)                               | 0.62***<br>(0.00)                              | -0.08<br>(0.64)     | 0.98                             | 1.05                          | 2.04                               |
| <b>22 long<br/>run</b>      | -6.96***   | 6.04***   | -----  | -----               | 0.98                             | 1.05                          | 2.04                               |
| <b>26<br/>short<br/>run</b> | 1.83***<br>(0.00)                                      | 0.06<br>(0.42)                                  | 0.70***<br>(0.00)                              | -0.29*<br>(0.07)    | 0.96                             | 1.02                          | 2.06                               |
| <b>26 long<br/>run</b>      | 6.10***  | 0.20  | -----  | -----               | 0.96                             | 1.02                          | 2.06                               |
| <b>44<br/>short<br/>run</b> | 0.35<br>(0.76)   | -2.35<br>(0.13)                                 | 0.46***<br>(0.00)                              | 0.60***<br>(0.00)   | 0.94                             | 1.06                          | 2.36                               |

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\* p-values in brackets.

♦ In 3SLS the adjusted R<sup>2</sup> is negative at times. It is unclear how the goodness of fit measures of the different cross-sections are to be weighted in order to derive an overall goodness of fit measure. Therefore, the figures listed should only signal the trend.

|                     |                    |                 |                   |                 |      |      |      |
|---------------------|--------------------|-----------------|-------------------|-----------------|------|------|------|
| <b>44 long run</b>  | 0.65               | -4.37           | -----             | -----           | 0.94 | 1.06 | 2.36 |
| <b>47 short run</b> | -1.20***<br>(0.00) | -0.27<br>(0.42) | 0.37***<br>(0.00) | 0.01<br>(0.91)  | 0.99 | 1.07 | 1.87 |
| <b>47 long run</b>  | -1.90***           | -0.43           | -----             | -----           | 0.99 | 1.07 | 1.87 |
| <b>74 short run</b> | -0.45***<br>(0.00) | -----           | 0.80***<br>(0.00) | -0.07<br>(0.66) | 0.99 | 1.04 | 2.16 |
| <b>74 long run</b>  | -2.25***           | -----           | -----             | -----           | 0.99 | 1.04 | 2.16 |

Under the assumption that the data follow an ARDL model, we find a significant positive impact of increased Chilean price competition on market shares in the fish (03), the fruit (08) and the ores (26) sector but no significant negative impact of *foreign* price competition on market shares in the seven sectors under study. As to beverages, we find a negative impact of competitive (low) Chilean prices and a positive impact of low foreign prices on market shares. Adjustment to the long-run equilibrium was significant in the beverages (22), the ores (26), the wood (44), the pulp of wood (47) and the copper (74) sector whereas no significant adjustment took place in the fish (03) and the fruit (08) sector. However, this interpretation of the results must still be followed with caution, as the error analysis below (Table 4) will show.

**Table 4: Error analysis in the 3SLS framework**

| Sector    | Computed adjustment coefficient<br>$\lambda_{3SLS}$ | Error if $k_{\max}=1$ :<br>$\lambda_{3SLS}^2$ | Error if $k_{\max}=2$ :<br>$\lambda_{3SLS}^3$ |
|-----------|---|---|---|
| Fish (03) | -0.19   | ---   | ---   |

|                   |         |      |      |
|-------------------|---------|------|------|
| Fruit (08)        | -0.07   | ---  | ---  |
| Beverages (22)    | 0.62*** | 0.38 | 0.24 |
| Ores (26)         | 0.70*** | 0.49 | 0.34 |
| Wood (44)         | 0.46*** | 0.21 | 0.10 |
| Pulp of wood (47) | 0.37*** | 0.14 | 0.05 |
| Copper (74)       | 0.80*** | 0.64 | 0.51 |

We can draw several conclusions from the error analysis in Table 4:

(1) The data do not fit the autoregressive lag model in the fish and in the fruit sector. The  $\lambda$ s there carry the wrong sign and are insignificant, but the ARDL requires significant positive  $\lambda$ s that lie in an interval  $]0;1[$ .

(2) The data can be explained by an ARDL in the rest of the sectors by and large since the  $\lambda$ s lie in an interval  $]0;1[$ . However, since we work with annual data where the maximum lag length is usually short ( $k_{\max} = 2$  is very realistic according to the cross-correlations), large errors will result in the beverages, the ores and the copper sectors where  $\lambda$  is relatively big and omission of the terms  $\beta_0 \lambda_{k+1} \text{lrer}$  and  $\gamma_0 \lambda^{k+1} \text{lrer}^*$  will therefore result in a large error. For example in the copper sector the error is 64% if  $k_{\max}$  is 1 and 51% if  $k_{\max}$  is two. I.e. 64% or 51% of the impact of copper prices on the market share in copper are neglected.

(3) Note that the errors are even bigger than computed when we have reasons to assume that the geometric lag structure does not apply at all instances. Computation of errors in this case would require that we know the true model.

#### 4.2 Estimating the Impact of Price Competition on Market Shares Utilizing the GMM-Approach in an ARDL

Alternatively to 3SLS, we estimate the dynamic model by GMM (Holtz-Eakin et al., 1988; Arellano and Bond, 1991; Caselli, Esquivel, Lefort, 1996; Durlauf et al., 2004). The special Arellano and Bond (1991) estimator which is based on the model in first differences is not

applicable in our case since the number of instruments created by the GMM technique would exceed the number of observations. Nonetheless, the classical GMM technique (in levels) allows one to control for the correlation between the lagged endogenous variable and the autocorrelated error terms. Judging from the way GMM works, this approach does have a comparative advantage over 3SLS at controlling endogeneity. Control of endogeneity is 100% due to specific model restrictions and therefore a gain in unbiasedness is obtained. However, efficiency is lost by creating a tremendous amount of moment conditions that have to be respected. In our case we get 210 moment conditions, i.e. 210 restrictions<sup>13</sup>, highlighting the computational burden of this approach (Schmidt et al., 1992).

The classical GMM approach uses lagged variables as instruments for endogenous regressors. This procedure, however, must be avoided in the presence of autocorrelation of the disturbances since it will not eliminate the problem of endogeneity under this condition (Durlauf et al., 2004). Therefore, we do not use lagged variables as instruments of endogenous regressors, but the instruments of the previous section, such as the difference in PPP-income between Chile and the importing country, an indicator of production capacity in real terms and the real exchange rate in a transformation that is generally used in polynomial lag models.

**Table 5: Results for the ARDL market share model estimated by panel-GMM**

|                             | Regression coefficients*             |  |                                       |                   | Goodness of fit measures |                       |                           |
|-----------------------------|--------------------------------------|--|---------------------------------------|-------------------|--------------------------|-----------------------|---------------------------|
|                             | Equation 2                           |  |                                       |                   |                          |                       |                           |
| Sector-<br>results          | Impact of<br>lreer<br>$\beta_{0GMM}$ | Impact<br>of lreer*<br>$\gamma_{0GMM}$ | Adjustm.<br>Coeff.<br>$\lambda_{GMM}$ | AR-<br>term       | R <sup>2</sup> adjusted  | S.E. of<br>regression | Durbin<br>Watson<br>stat. |
| <b>03<br/>short<br/>run</b> | -0.20<br>(0.24)                      | -0.78***<br>(0.00)                     | 0.64***<br>(0.00)                     | -0.24**<br>(0.02) | 0.98                     | 1.04                  | 2.11                      |
| <b>03 long<br/>run</b>      | -0.55                                | -2.17***                               | -----                                 | -----             | 0.98                     | 1.04                  | 2.11                      |

<sup>13</sup> The number of restrictions is T(T-1) K/2.

\* p-values in brackets.



|                             |                    |                   |                   |                    |      |      |      |
|-----------------------------|--------------------|-------------------|-------------------|--------------------|------|------|------|
| <b>08<br/>short<br/>run</b> | 2.29*<br>(0.07)    | -0.15<br>(0.90)   | -0.15<br>(0.42)   | 0.69***<br>(0.00)  | 0.99 | 1.10 | 1.98 |
| <b>22<br/>short<br/>run</b> | -2.53***<br>(0.00) | 2.29***<br>(0.00) | 0.58***<br>(0.00) | -0.13<br>(0.41)    | 0.98 | 1.06 | 2.08 |
| <b>22 long<br/>run</b>      | -6.02***           | 5.45***           | -----             | -----              | 0.98 | 1.06 | 2.08 |
| <b>26<br/>short<br/>run</b> | 0.32<br>(0.52)     | -0.17<br>(0.13)   | 0.71***<br>(0.00) | -0.28*<br>(0.06)   | 0.89 | 1.04 | 2.04 |
| <b>26 long<br/>run</b>      | 1.10               | 0.24              | -----             | -----              | 0.89 | 1.04 | 2.04 |
| <b>44<br/>short<br/>run</b> | -1.22**<br>(0.04)  | -0.98<br>(0.14)   | 0.74***<br>(0.00) | -0.37***<br>(0.00) | 0.90 | 1.06 | 2.26 |
| <b>44 long<br/>run</b>      | -4.69**            | -3.77             | -----             | -----              | 0.90 | 1.06 | 2.26 |
| <b>47<br/>short<br/>run</b> | -1.07**<br>(0.05)  | -0.31<br>(0.52)   | 0.40***<br>(0.00) | -0.05<br>(0.80)    | 0.74 | 0.26 | 1.87 |
| <b>47 long<br/>run</b>      | -1.78**            | -0.52             | -----             | -----              | 0.74 | 0.26 | 1.87 |
| <b>74<br/>short<br/>run</b> | -1.45**<br>(0.02)  | -----             | 0.37***<br>(0.03) | 0.49***<br>(0.00)  | 0.99 | 1.18 | 2.01 |
| <b>74 long<br/>run</b>      | -2.30              |                   |                   |                    | 0.99 | 1.18 | 2.01 |

Under the assumption that the underlying assumptions of the autoregressive lag model are fulfilled we can conclude that there is a positive relationship between an increase in Chilean price competitiveness and market share in the fruit sector (08) and a negative relationship between low Chilean wine prices (sector 22) and high Chilean copper prices (sector 74) and respective market shares. Foreign relative prices have a significant impact in the fruit (03) and beverages (22) sector. In the latter sector the quality aspect in the wine sector is supposed to be dominant (see Table 5). The role of prices in the wood (44) and the pulp of wood (47) sector might be severely impeded by illegal logging and illegal imports of wood products. Illegal logging distorted official trade flows not only of all timber products (roundwood, sawnwood, veneer, plywood, boards, semi-finished and finished products, and furniture, but also of pulp, paper, printed products and cellulose)<sup>14</sup>. This latter statement applies also to the interpretation of the 3SLS estimation.

Again an error analysis (see Table 6) is made to take account of intolerable inaccuracy when the actual lag length is short.

**Table 6: Error analysis in the GMM framework**

| Sector               | Computed<br>adjustment<br>coefficient<br>$\lambda_{GMM}$ | Error if $k_{\max}=1$ :<br>$\lambda_{GMM}^2$ | Error if $k_{\max}=2$ :<br>$\lambda_{GMM}^3$ |
|----------------------|--|--|--|
| Fish (03)            | 0.64***  | 0.41   | 0.26   |
| Fruit (08)           | -0.15  | ---  | ---  |
| Beverages (22)       | 0.58***  | 0.34   | 0.20   |
| Ores (26)            | 0.71***  | 0.50   | 0.36   |
| Wood (44)            | 0.74***  | 0.55   | 0.40   |
| Pulp of wood<br>(47) | 0.40***  | 0.16   | 0.06   |

<sup>14</sup> Illegal logging is estimated to comprise up to 50% of all logging activity in the key countries of Eastern Europe and Russia, up to 94% in the key Asian countries, up to 80% in the key African countries and up to 80% in the key Latin American countries (WWF, 2005; FERN, 2004).

|             |         |      |      |
|-------------|---------|------|------|
| Copper (74) | 0.37*** | 0.14 | 0.05 |
|-------------|---------|------|------|

The error analysis of Table 6 reveals three things:

- (1) Again, the ARDL does not seem to be the right model to explain market shares in the fruit sector in a dynamic context.  $\lambda$  is negative and insignificant.
- (2) Large errors do occur in the beverages, the ores and the wood sectors given that  $\lambda$  is relatively large there (see columns 3 and 4).
- (3) The errors are even bigger than stated in Table 6 when we have reasons to assume that a geometric lag structure does not apply at all instances. However, computation of this additional source of errors is beyond the scope of this paper.

To sum up:

On the one hand, we have the finding that the ARDL-estimations in sections 4.1 and 4.2 have very respectable adjusted  $R^2$  measures and Durbin-Watson (DW) statistics around 2.<sup>15</sup>

On the other hand, the standard errors of the regressions are relatively high. Moreover, the error analysis makes clear that the simple dynamic specification in the form of an ARDL suffers from some drawbacks. The autoregressive lag specification does not seem to apply in the fish and the fruit sector. Statements in the beverages, the ores, the wood and the copper sectors are subject to relatively large errors by neglecting the term  $\lambda^{k+1}$ , the impact of changes in prices and protection<sup>16</sup>, in the autoregressive transformation.

The estimation results of 3SLS and GMM differ a great deal. This result is puzzling since exactly the same instrumental variables are utilized in both estimation procedures. However, 3SLS and GMM differ in the number of restrictions that are applied. 3SLS basically works under the condition to minimize the squared residuals of eq. (2) with IV replacing the right hand side variables. GMM estimation is built around a multitude of moment conditions (210 conditions) of which some will be relevant and others just irrelevant. A search for relevant moment conditions does not take place in the GMM routine so that some far off moment conditions can become binding (see Ziliak, 1997).

## 5. Conclusions

Assuming that the underlying geometric lag specification can be applied to the data, the ARDL specification allows one to draw correct inferences about the short, the medium and the long run. The ARDL specification can be combined with the FGLS technique and is therefore able to deal with a couple of estimation problems resulting from autocorrelation, heteroscedasticity and cross-section correlation of the disturbances. Applied to a system of equations, this technique transforms the variables in the regression equation through weighting the regressor matrix with a weight matrix that can control for autocorrelation of the disturbances, for heteroscedasticity of the variance of the residuals and for cross-section correlation of the disturbances. The endogeneity problem is solved with instrumental variables (IV) in either a 3SLS or a GMM routine. Unlagged IV are utilized to get rid of the endogeneity problem and to obtain unbiased estimates. Furthermore, the 3SLS and the GMM- technique are able to produce efficient and consistent estimates if ARDL is the true model.

Violation of the geometric lag assumption is to be expected in particular when working with heterogenous panel data and with multivariate regression models. In this case a polynomial lag model could be the model of choice if there is not excessive cross-section heterogeneity. Estimations in the framework of panel error correction models and panel DOLS could be well advisable, even though these models require much longer time spans to allow for meaningful panel unit root and panel cointegration tests. Further research is needed on this topic.

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<sup>15</sup> Even though the DW must be adjusted in the presence of a lagged endogenous, the DW statistic is still able to roughly indicate problems of autocorrelation and misspecification.

<sup>16</sup> All our prices contain sector-specific protection whenever relevant.

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# Appendix 1

## Description of Data

In the following, the variables: sheu, shnoneu, shw, lreer, and lreer\* will be described in original form (not in logs). All data run from 1988 to 2002. Export data (to compute market shares) were taken from EUROSTAT: Intra- and extra –EU trade, Supplement 2, 2003.

In our case, six cross-sections (6 EU countries: Germany, Spain, France, UK, Italy, the Netherlands) had basically complete time series.<sup>17</sup>

### (1a) Chile's market share in the EU with respect to the EU countries: sheu

sheu<sub>ist</sub> measures the share of Chilean exports (x) of sector s in EU country i at time t when competing against imports (m) from EU countries only:

$$Sheu_{ist} = x_{ist}/m_{EUist}$$

### (1b) Chile's market share in the EU with respect to the non-EU countries: shnoneu

shnoneu<sub>ist</sub> measures the share of Chilean exports of sector s in EU country i at time t when competing against imports (m) from non-EU countries only:

$$shnoneu_{ist} = x_{ist}/m_{non-EUist}$$

### (1c) Chile's market share in the EU with respect to the world (EU and non-EU countries): shw

shw<sub>ist</sub> measures the share of Chilean exports of sector s in EU country i at time t when competing against imports (m) from EU and non-EU countries:

$$shw_{ist} = x_{ist}/m_{EU+non-EUist}$$

### (2) The Chilean real effective exchange rate: reer

reer is the bilateral real effective exchange rate between Chile and the EU countries (price quotation system), taking Chile's point of view. It consists of the real exchange rate (rer) and basic indicators of EU protection such as EU-tariffs (t) and EU-subsidies (s).

It is computed (all data for 'rer' are taken from World Development Indicators CD ROM of 2005) as:

$$rer = e \cdot P_{EU}/P_{Chile} \quad \text{with}$$

rer = real bilateral exchange rate between Chile and relevant EU country

e = nominal exchange rate (x Chilean Peso/1EUR) between Chile and relevant EU country

P<sub>EU</sub> = GDP deflator of the EU country under consideration with 1995 as base year (1995 = 100)

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<sup>17</sup> Due to missing data, Austria, Belgium, Finland, Luxemburg and Sweden were excluded from the analysis.



$P_{\text{Chile}}$  = GDP deflator of Chile with 1995 as base year ( $1995 \triangleq 100$ )

rer has been adjusted for EU tariff protection (in terms of average EU tariff rate (t)) and non-tariff protection (in terms of EU subsidy rate (s)). Tariff rates prevailing in the EU can be found in Trade Policy Review European Union, Volume 1, 2000, pp. 88-101 (WTO) and rough subsidy equivalents are based on qualitative information on non-tariff protection collected, explained and nicely put together for UNCTAD by Supper (2001).

So we get:

$$\text{reer} = \text{rer} \cdot (1-s)/(1+t)$$

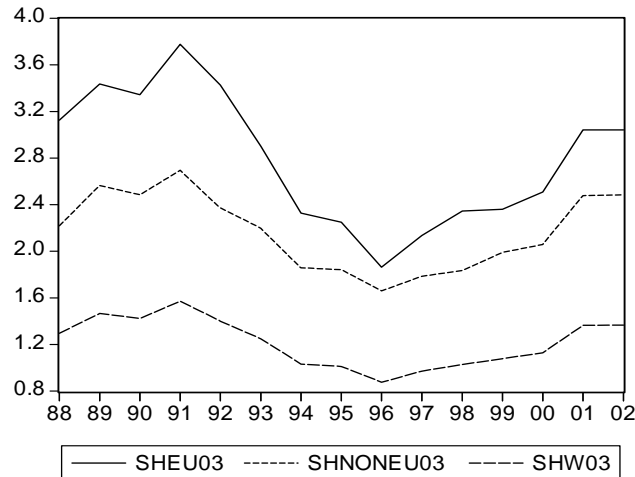
For the simulations, we assume that the FTA between Chile and the EU brings tariffs down to zero.

### **(3) Chile's competitors (\*) real effective exchange rates :reer\***

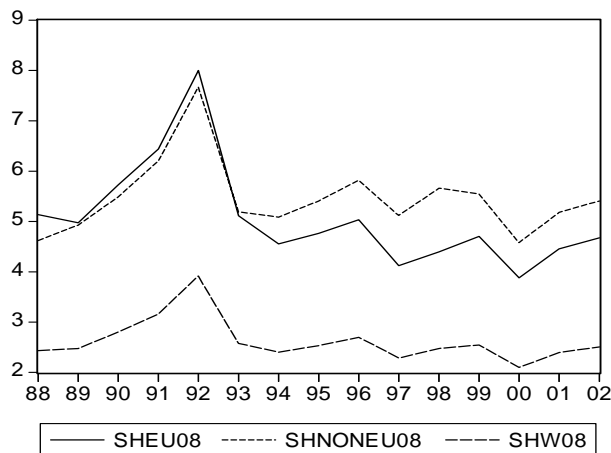
In analogy to (2) the real effective exchange rates of Chile's main competitors Norway, Australia, South Africa, Brazil are computed. Nominal exchange rates, Norway's, Australia's, South Africa's, and Brazil's GDP deflators are computed from World Development Indicators CD ROM 2005. Tariff and subsidy rates are borrowed from WTO and UNCTAD (see (2)).

## Appendix 2

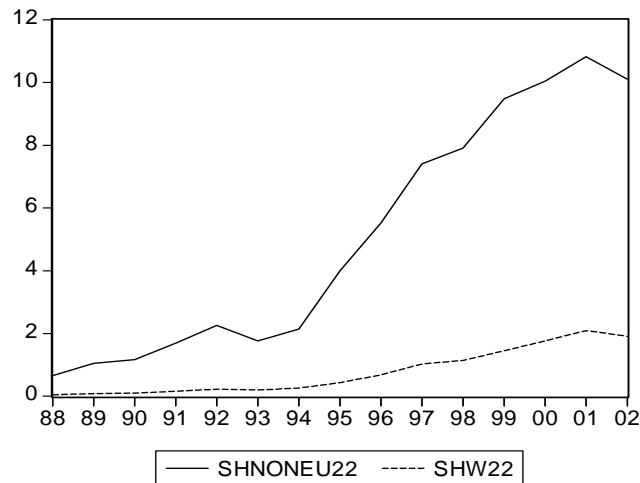
**Figure 1: Chile's market share in EU's fish imports with respect to EU and non-EU competitors in the period of 1988 to 2002**



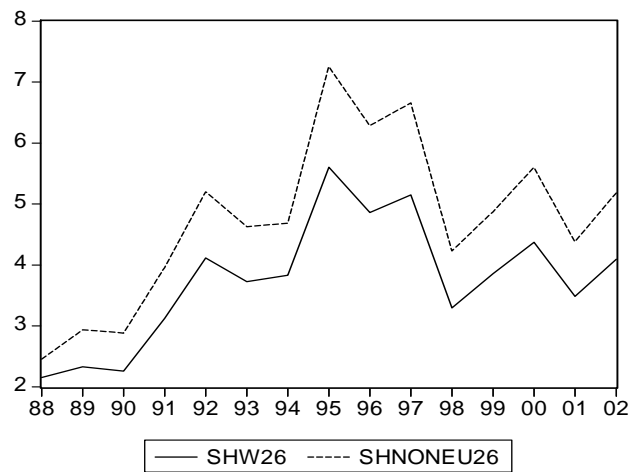
**Figure 2: Chile's market share in EU's fruit imports with respect to EU and non-EU competitors in the period of 1988 to 2002**



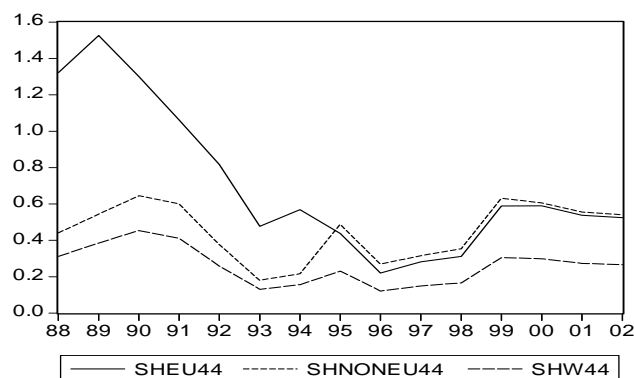
**Figure 3: Chile's market share in EU's imports of beverages with respect to EU and non-EU competitors in the period of 1988 to 2002**



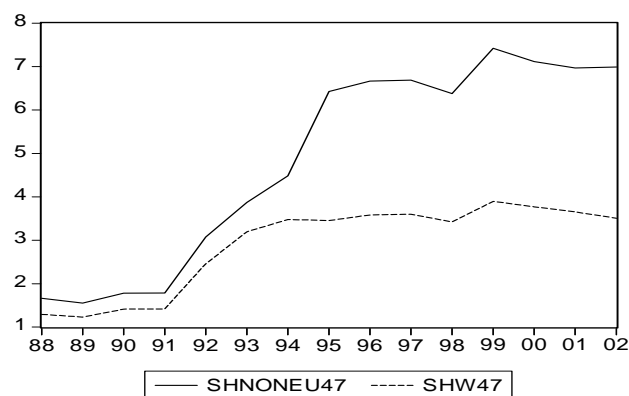
**Figure 4: Chile's market share in EU's imports of ores, slag and ash with respect to EU and non-EU competitors in the period of 1988 to 2002**



**Figure 5: Chile's market share in EU's imports of wood thereof (44) with respect to EU and non-EU competitors in the period of 1988 to 2002**



**Figure 6: Chile's market share in EU's imports of pulp of wood (47) with respect to non-EU and world-wide competitors in the period of 1988 to 2002**



**Figure 7: Chile's market share in EU's imports of copper (74) with respect to non-EU and world-wide competitors in the period of 1988 to 2002**

