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An inexact science: Accounting for measurement error and downward bias in mode and location choice models

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An inexact science: Accounting for measurement error and downward bias in mode and location choice models*

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Abstract

Using commuting data for Brisbane, Australia, we find that accounting for measurement error in travel times causes the magnitude of parameters in mode and location choice models to increase approximately three-fold and 30–40%, respectively. Errors appear to be somewhat systematic, with travel times being underestimated for short journeys and vice versa for long journeys—especially by public transport. We find similar results when we use alternative transport cost measures and independent commuting data from London. Our findings are likely to have important implications for transport and land use policy as well as the many types of economic models in which travel times—and transport costs, more generally—occupy a central role.

Keywords: mode choice, location choice, travel times, measurement error, Australia

JEL-classification: C13, R14, R41.

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Although this may seem a paradox, all exact science is dominated by the idea of approximation.

Bertrand Russell
The Scientific Outlook

1. Introduction

Despite occupying a central role in the fields of spatial, urban, and transport economics, accurate data on travel times and transport costs are often hard to come by. Rarely do researchers observe actual travel times, with most data either self-reported by travellers—and hence affected by *errors of perception*—or imputed from imperfect information—and hence affected by *errors of imputation*.¹ Importantly, there is no a priori reason to expect that measurement error in travel times is a “neutral” statistical process. Indeed, Hausman’s “iron law of econometrics” posits that random measurement error will—via the statistical process of attenuation—cause estimated parameters to be biased towards zero (Hausman, 2001).² For these reasons, a growing body of transportation literature considers the effects of measurement error, especially differences in reported vis-à-vis imputed travel times (see, e.g. Walker et al., 2010; Yamamoto and Komori, 2010; Bhatta and Larsen, 2011; Varotto et al., 2017; Varela et al., 2018). As an example, Walker et al. (2010) finds that “...models that do not correct for measurement error may underestimate travelers’ values of time”—just as predicted by Hausman’s “iron law”.

Here, we study the second source of measurement error noted above, that is, so-called errors of imputation. Specifically, we consider how uncertainty in the home location of commuters within zones introduces measurement error into travel times and affects the estimated parameters in mode and location choice models. In doing so, we build on a body of literature that extends at least back to Train (1978). More recent studies treat the uncertainty that arises from spatial aggregation, or “zoning”, as an instance of the modifiable area unit problem, which they seek to mitigate by either more detailed zones

¹ Even travel time data sourced from individual mobile and Bluetooth devices are usually measured with error and/or aggregated to protect personal privacy.

² Other statistical processes—like publication selection effects, for example—can introduce positive bias to the magnitude of estimated parameters (see, e.g., Loken and Gelman, 2017; Andrews and Kasy, 2019).

(see, e.g. Chang et al., 2002; Guo and Bhat, 2004; Martínez et al., 2007), or individual travel time data (see, e.g. Lovelace et al., 2014; Kuehnel et al., 2020). Notwithstanding the merits of these methods, both can encounter problems with data availability and computational tractability. In contrast, we explicitly quantify measurement error in travel times and directly account for its effects. Our study is perhaps closest to Yamamoto and Komori (2010), who find that accounting for uncertainty in the distance from home to public transport (“PT”) stops biases the parameters in mode choice models towards zero. In contrast to Yamamoto and Komori (2010), however, we consider measurement error for both car and PT; for the whole commute between home and work; and in both mode and location choice models.

To frame our analysis, we estimate parts of the spatial general equilibrium (“SGE”) model developed in Ahlfeldt et al. (2015), hereafter “ARSW”, which has become a workhorse model in urban economics (see, e.g., Monte et al., 2018; Severen, 2021; Dericks and Koster, 2021). In ARSW, workers choose their transport mode and home/work locations in response to travel times by car and PT. To estimate the model, we link Census data on the home/work locations and main mode of travel for almost all workers in the city of Brisbane, Australia to car and PT travel times that are imputed from a journey planner, namely OpenStreetMap (2021). In doing so, we use sampling to characterise the variation in travel times that is introduced by uncertainty in the home location of commuters within zones. Like ARSW, we use these data to estimate mode and location choice models. Unlike ARSW, however, we account for measurement error in travel times. We find the latter yields significant improvements in model performance and causes parameter estimates to increase in magnitude. This bias does not appear to be easily addressed as a form of heterogeneity or endogeneity, nor is it driven by unusual observations, such as intra-zonal commutes or low-density zones. Measurement error appears to have a systematic component, with travel times for short commutes being underestimated, and vice versa for long commutes. We find similar results when we approximate measurement error as a percentage of the mean travel time, or when we use alternative transport cost measures and independent commuting data from London.

We note three important implications of these findings. First, models that do not account for measurement error seem likely to underestimate the causal effect of travel times—and transport costs, more generally—on mode and location choice. This bias seems sufficiently large that it may distort transport and land use policy settings. Second, we suggest that researchers judiciously allow for measurement errors in travel times and transport costs when estimating models, even when they lack detailed information

on the magnitude of these errors. Allowing for measurement error in an approximate fashion may be preferable to treating the data deterministically when it is not. Third, our findings highlight several areas for further research, including but not limited to quantifying the contribution of other sources of uncertainty and accounting for the effects of measurement error in other related economic settings—especially those characterised by heterogeneous geographies, multi-modal transport costs, and congestion.

This paper is structured as follows: Section 2 outlines the methodology and data, Section 3 presents the results, Section 4 discusses the findings, and Section 5 concludes.

2. Methodology

2.1. Models

In the SGE model developed in ARSW, car and PT travel times affect worker's choice of transport mode and, in turn, their home/work locations. In the following sub-sections, we summarise the parts of this model that are relevant to this study.

2.1.1. Location choice

Consider a representative worker, o , that is choosing their home/work locations i and j in accordance with preferences, U_{ijo} , which are represented by the utility function:

$$U_{ijo} = z_{ijo} \frac{B_i}{d_{ij}} \left(\frac{c_{ijo}}{\beta} \right)^\beta \left(\frac{l_{ijo}}{1 - \beta} \right)^{1-\beta}, \quad (1)$$

where z_{ijo} denotes the worker's idiosyncratic preference for locations i and j that we discuss in more detail below; B_i denotes the level of residential amenities in i ; d_{ij} denotes the dis-utility of commuting between i and j ; c_{ijo} denotes a composite consumption good; β is the share of expenditure on c_{ijo} ; and l_{ijo} denotes residential floor space.

ARSW assume that all workers supply one unit of labour and earn wage w_j . Let q_i denote the price of floor space, l_{ijo} , and assume the consumption good, c_{ijo} , is the numeraire,

such that its price is equal to one in all locations. Maximising Equation (1) subject to the budget constraint $w_{ij} = q_i l_{ijo} + c_{ijo}$ then yields the following indirect utility function:

$$u_{ijo} = z_{ijo} \frac{B_i w_j}{d_{ij} q_i^{1-\beta}}. \quad (2)$$

Equation (2) implies that a worker's preference for home/work locations i and j increases with amenities, B_i , and wages, w_j , but decreases with commuting costs, d_{ij} , and rents, $q_i^{1-\beta}$. Wages and rents w_j and q_i ; local amenities B_i ; and commuting costs d_{ij} , can adjust endogenously to leave workers indifferent between locations in spatial equilibrium.

ARSW assume that z_{ijo} observes a Frechét distribution $F(z_{ijo}) = \exp(-T_i E_j z_{ijo}^{-\varepsilon})$ and integrate over z_{ijo} to yield the probability, π_{ij} , that a worker lives in i and works in j :

$$\pi_{ij} = \frac{T_i E_j (d_{ij} q_i^{1-\beta})^{-\varepsilon} (B_i w_j)^\varepsilon}{\sum_{r=1}^S \sum_{s=1}^S T_r E_s (d_{rs} q_r^{1-\beta})^{-\varepsilon} (B_r w_s)^\varepsilon}, \quad (3)$$

where $T_i, E_j > 0$ are scale parameters and $\varepsilon > 1$ is a parameter to be estimated that denotes the degree of worker homogeneity. That is, larger values of ε imply that workers have more homogeneous preferences over locations. Equation (3) defines the model of worker location choice that sits at the heart of the SGE model developed in ARSW.

To proceed, ARSW assume commuting costs $d_{ij} = \exp(\kappa \bar{\tau}_{ij})$, where κ is a parameter to be estimated and $\bar{\tau}_{ij}$ denotes average travel time, which we discuss in more detail in Section 2.1.2. Equation (3) can then be readily manipulated to yield a reduced-form (Poisson) “gravity” model, $n_{ij} = \exp(\delta_i + \delta_j - \varepsilon \ln d_{ij}) = \exp(\delta_i + \delta_j - \nu \bar{\tau}_{ij})$. Here, n_{ij} denotes the number of workers that commute from i to j ; $\delta_i = \ln [T_i B_i^\varepsilon q_i^{-(1-\beta)\varepsilon}]$ and $\delta_j = \ln [E_j w_j^\varepsilon]$ denote origin and destination effects, respectively; and the composite semi-elasticity, $\nu \equiv \varepsilon \kappa$ defines the effect of $\bar{\tau}_{ij}$ on worker's choice of home/work location.

2.1.2. Mode choice

In a multi-modal setting, the average travel time between locations i and j , $\bar{\tau}_{ij}$, is defined by the mode-share weighted average of travel times by individual modes. ARSW consider

two modes—that is, car and PT—and subsequently define $\bar{\tau}_{ij}$ as follows:

$$\bar{\tau}_{ij} = \mathbb{E} \left[\hat{m}_i^c t_{ij}^c + \hat{m}_i^p t_{ij}^p \right] = \mathbb{E} \left[\hat{m}_i^c t_{ij}^c + (1 - \hat{m}_i^c) t_{ij}^p \right], \quad (4)$$

where \hat{m}_i^c, t_{ij}^c , \hat{m}_i^p , and t_{ij}^p denote mode shares and travel times for car and PT, respectively. ARSW use a logit model to predict \hat{m}_i^c over home locations, which is combined with data on t_{ij}^c and t_{ij}^p to compute $\bar{\tau}_{ij}$ per Equation (4) (cf. Supplementary Appendix S.6.3. Ahlfeldt et al., 2015). In doing so, \hat{m}_i^c , t_{ij}^c , t_{ij}^p , and, in turn, $\bar{\tau}_{ij}$ are treated deterministically.

We can, however, go further than ARSW in three ways. First, we use our data to estimate a logit mode choice model for individual home/work locations i and j , m_{ij}^c :

$$m_{ij}^c = \frac{n_{ij}^c}{n_{ij}} = \frac{\exp(\mu^c t_{ij}^c + \mu^p t_{ij}^p + \zeta_0)}{1 + \exp(\mu^c t_{ij}^c + \mu^p t_{ij}^p + \zeta_0)}, \quad (5)$$

where n_{ij}^c denotes the number of workers that commute by car between home/work locations i and j ; n_{ij} denotes the total number of commuters; μ^c and μ^p are parameters to be estimated, where we expect $\mu^c < 0$ and $\mu^p > 0$; and ζ_0 denotes an intercept.³ Second, per Section 2.2, we use methods to account for the measurement error in t_{ij}^c and t_{ij}^p and that, in turn, allow us to estimate the unobserved latent (“true”) car and PT travel times, t_{ij}^{c*} and t_{ij}^{p*} . Third, we treat t_{ij}^{c*} and t_{ij}^{p*} —and subsequent estimates of mode shares \hat{m}_{ij}^c and average travel times τ_{ij} —as random variables with their own distributions.

By extending ARSW in these three ways, we can define an alternative, more detailed measure for the distribution of average travel time, τ_{ij} :

$$\tau_{ij} = \hat{m}_{ij}^c t_{ij}^{c*} + (1 - \hat{m}_{ij}^c) t_{ij}^{p*}, \quad (6)$$

which differs from Equation (4) through the use of estimated mode shares for individual pairs of home/work locations, \hat{m}_{ij}^c ; the use of estimated latent travel times, t_{ij}^{c*} and t_{ij}^{p*} , and by treating \hat{m}_{ij}^c , t_{ij}^{c*} and t_{ij}^{p*} as random variables each with their own distributions. In contrast to ARSW, we use Equations (5) and (6) to compute a distribution for τ_{ij} , which we use to estimate the location choice model in Section 2.1.1.

³ That is, we expect that longer car travel times will lead to lower car mode share and vice versa for longer PT travel times. The mode share model in Equation 5 can be given microeconomic foundations in a random-utility framework in which individual workers choose modes in response to car and PT travel times, given idiosyncratic preferences for modes that are assumed to follow an EV1 distribution.

2.2. Methods

ARSW adopts a recursive process that, first, estimates the mode choice model; second, computes average travel times; and third, estimates the location choice model. To enable comparisons to ARSW and subsequent literature, we follow a similar recursive process.

Turning first to the conventional ARSW setting that does not allow for measurement error, we estimate variants of the following set of equations:

$$n_{ij}^c \sim \mathcal{B}(n_{ij}, \mu^c t_{ij}^c + \mu^p t_{ij}^p + \zeta_0) \quad (\text{Mode choice})$$

$$\bar{\tau}_{ij} = \mathbb{E} [\hat{m}_{ij}^c t_{ij}^c + (1 - \hat{m}_{ij}^c) t_{ij}^p] \quad (\text{Compute mean } \bar{\tau}_{ij})$$

$$n_{ij} \sim \mathcal{P}(\delta_i + \delta_j - \nu \bar{\tau}_{ij}) \quad (\text{Location choice})$$

First, we estimate the Binomial mode choice model, $n_{ij}^c \sim \mathcal{B}(\dots)$, with logit link. Second, we use the latter to estimate mode shares, \hat{m}_{ij}^c , which are combined with mean travel times, t_{ij}^c and t_{ij}^p , to compute the mean average travel times, $\bar{\tau}_{ij}$. Third, we use $\bar{\tau}_{ij}$ to estimate the Poisson location choice model, $n_{ij} \sim \mathcal{P}(\dots)$. In this setting, car and PT travel times, t_{ij}^c and t_{ij}^p , and the resulting estimates for $\bar{\tau}_{ij}$, are treated deterministically.

Second, we extend this set of equations to account for measurement errors in travel times and other parameters as follows:

$$n_{ij}^c \sim \mathcal{B}(n_{ij}, \mu^c t_{ij}^{c*} + \mu^p t_{ij}^{p*} + \zeta_0) \quad (\text{Mode choice})$$

$$t_{ij}^{c*} \sim \text{Logn}(t_{ij}^c, (s_{ij}^c)^2) \quad t_{ij}^{p*} \sim \text{Logn}(t_{ij}^p, (s_{ij}^p)^2)$$

$$\tau_{ij} = \hat{m}_{ij}^c t_{ij}^{c*} + (1 - \hat{m}_{ij}^c) t_{ij}^{p*} \quad (\text{Compute distribution of } \tau_{ij})$$

$$n_{ij} \sim \mathcal{P}(\delta_i + \delta_j - \nu \tau_{ij}^*) \quad (\text{Location choice})$$

$$\tau_{ij}^* \sim \text{Logn}(\bar{\tau}_{ij}, s_{\tau_{ij}}^2).$$

This departs from ARSW in three ways. First, when estimating the mode choice model, $n_{ij}^c \sim \mathcal{B}(\dots)$, we allow for measurement error in car and PT travel times, t_{ij}^c and t_{ij}^p . This yields two extra equations for the latent car and PT travel times, $t_{ij}^{c*} \sim \text{Logn}(\dots)$ and $t_{ij}^{p*} \sim \text{Logn}(\dots)$. We assume t_{ij}^{c*} and t_{ij}^{p*} follow Lognormal distributions with means t_{ij}^c and t_{ij}^p and standard deviations, s_{ij}^c and s_{ij}^p that we calculate from the data described in Section 2.3. This ensures the latent travel-times are constrained to be positive. Second, we compute a distribution for average travel time, τ_{ij} , that accounts for variation in estimates

for \hat{m}_{ij}^c , t_{ij}^{c*} , and t_{ij}^{p*} . Third, when estimating the location choice model, $n_{ij} \sim \mathcal{P}(\dots)$, we allow for measurement error in average travel time, τ_{ij} . Specifically, we assume the latent average travel time τ_{ij}^* follows a Lognormal distribution with mean $\bar{\tau}_{ij}$ and standard deviation, $s_{\tau_{ij}}$, that we compute from the estimated distribution for τ_{ij} .

We are primarily interested in the effects of measurement error in t_{ij}^c , t_{ij}^p , and τ_{ij} on estimates for the parameters μ^c , μ^p , ν , δ_i , and δ_j . To this end, we estimate all models using Bayesian methods, which allow us to directly account for measurement error in a systematic way.⁴ In doing so, we attempt to understand the effects of measurement error separately from other common sources of bias, such as heterogeneity and endogeneity. One disadvantage of Bayesian methods is their increased computational time, which can extend to several days for the more complex measurement error models.

2.3. Data

We draw on two main sources of data. First, we extract commuting data from the Australian Census that was undertaken on 9 August 2016 for all 236 SA2s in the Brisbane Greater Capital City Statistical Area (“GCCSA”). The Australian Bureau of Statistics (“ABS”) describes an SA2 as “... a community that interacts together socially and economically” whereas the GCCSA is designed to capture the extent of the labour market (ABS, 2021). In the 2016 Census, 2.3 million residents and 1.0 million workers were recorded in the Brisbane GCCSA, where SA2s have a median population of 8,715 and a median area of 7.3 square kilometres. For all 587,601 full-time workers, we extract the SA2s where they usually live and work—yielding $236 \times 236 = 55,696$ SA2-to-SA2 observations—as well as their main mode of travel, that is, private vehicle, PT, or walking/cycling. We exclude full-time workers that worked from home (“WFH”) on the day of the Census and remove observations associated with SA2s for which we do not observe any commutes, or that have fewer than 9 residents or jobs.⁵ This leaves us with $229 \times 233 = 53,357$ SA2-to-SA2 observations. The Census is a rich but incomplete source of data; we do not know, for example, workers’ precise home and work locations nor their departure time, commute frequency, or route—including intermediate destinations.

⁴ Specifically, all models are estimated using the statistical package R running in the RStudio environment with the brms package (R Core Team, 2023; RStudio Team, 2023; Bürkner, 2017).

⁵ More specifically, we remove observations that originate in Brisbane Port–Lytton (pop. 9), Lake Manchester–England Creek (pop. 0), Carole Park (pop. 7), New Chum (pop. 0), Mount Coot-tha (pop. 0), Greenbank Military Camp (pop. 0), and Enoggera Reservoir and also those observations that are destined for Enoggera Reservoir (emp. 5), Lake Manchester–England Creek (emp. 5), and Greenbank Military Camp (emp. 9).

Second, to these 53,357 observations, we append travel time data for August 2016 that are imputed from Open Street Maps, “OSM”, which is an open-access, multi-modal journey planner (OpenStreetMap, 2021).⁶ As we do not know the precise home location of commuters within SA2s, we randomly sample 20 points per SA2 based on the distribution of the population across smaller census “meshblocks”. For work locations, we adopt a more conventional deterministic approach: First, we snap geometric centroids to the nearest pedestrian link in OSM and, second, where necessary we manually adjust the destination to the approximate employment centroid as it appears from aerial imagery. As one might expect, such manual adjustments are more important in larger, less populated SA2s where employment is unevenly distributed. We then compute travel times by car and PT from each of the 20 origins per SA2 to each destination per SA2, which enables us to generate a distribution of travel times for each combination of home and work locations. Appendix A illustrates the results of this sampling process for one SA2-to-SA2 pair. For PT, we assume a 07:30am departure time and include access time, wait time, in-vehicle time, and egress time. We drop 920 observations associated with two SA2s that are inaccessible by car (Redland Islands and Scarborough–Newport–Moreton Islands) and 2,644 observations for which one or fewer PT travel time was returned, which were mainly associated with five remote, rural SA2s—namely, Boonah, Dayboro, Kilcoy, Woodford–D’Aguilar, and Mount Coot-tha. This leaves us with 49,793 observations for 227 home/work locations (SA2s) and 571,333 full-time workers, which represents 97.2% of those recorded as residing and working in Brisbane GSCCA on the day of the Census.

Figure 1 presents data that are relevant to the estimation of mode choice models. The top left and right panels present histograms of mean travel times by car and PT, t_{ij}^c and t_{ij}^p , for which the commute-weighted average is approximately 25 and 63 minutes, respectively. The bottom-left panel in Figure 1 then presents scatter plots of t_{ij}^c versus t_{ij}^p . Notwithstanding the positive correlation (0.754), we observe considerable variation that likely reflects the effects of geographic barriers—such as the Brisbane River, which carves a meandering path through the city—as well as mode-specific infrastructure/services, such as railways, busways, tunnels, bridges, and ferries.⁷ Our methodology exploits variation in travel times between modes within origin-destination pairs to identify their

⁶ We download 2016 data on the PT network in GTFS format from TransitFeeds (2021) and pedestrian network in OSM format from Geofabrik (2020). We manually edit the latter to add some missing links.

⁷ Perhaps the most notable—but by no means only—example is the Eleanor Schonell Bridge (“ESB”) that connects Dutton Park and St Lucia. The ESB is accessible only to those travelling by PT, walking, or cycling, who gain a considerable travel time advantage compared to driving. Charles-Edwards et al. (2015) use individual data to analyse travel patterns before and after the opening of the ESB in 2006 and find significant effects on non-car mode share and home locations. Inspection of our data confirms that PT travel times are most competitive for journeys that benefit from mode-specific infrastructure, like the ESB.

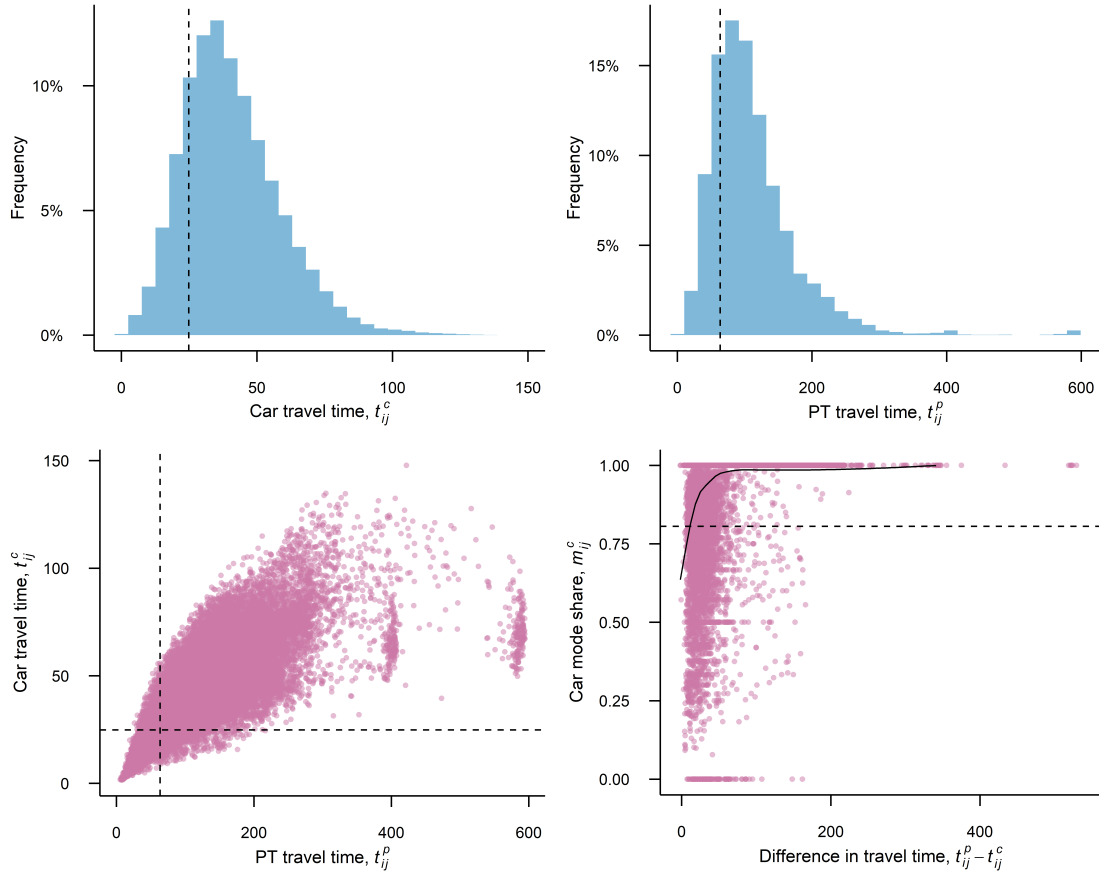


Figure 1: Top: Histograms of car (left) and PT (right) travel times, t_{ij}^c and t_{ij}^p , respectively. Bottom: Scatter plots of t_{ij}^c versus t_{ij}^p (left) and car mode share, m_{ij}^c versus $t_{ij}^p - t_{ij}^c$ (right), where the solid line denotes the smoothed trend. Dashed vertical and horizontal lines indicate the mean.

effects on mode choice. In later sections, we consider whether this variation is exogenous. The bottom-right panel in Figure 1 then plots car mode share, m_{ij}^c , versus the difference in travel times, $t_{ij}^p - t_{ij}^c$. We find considerable variation in car mode share m_{ij}^c , which is positively associated with the difference in travel times, $t_{ij}^p - t_{ij}^c$, as we might expect.

Figure 2 presents data that are relevant to the estimation of location choice models. In the left panel, we present a histogram of commuting flows, which reveals considerable heterogeneity, that is, our data comprise of a large number of small commuting flows and a small number of large commuting flows. In the right panel, we find the expected negative slope between $\ln n_{ij}$ and mean average travel time, $\bar{\tau}_{ij}$, where we compute the latter per Equation (4). To finish, Figure 3 illustrates a key aspect of our data: measurement error in travel times arising from uncertainty in the home location of

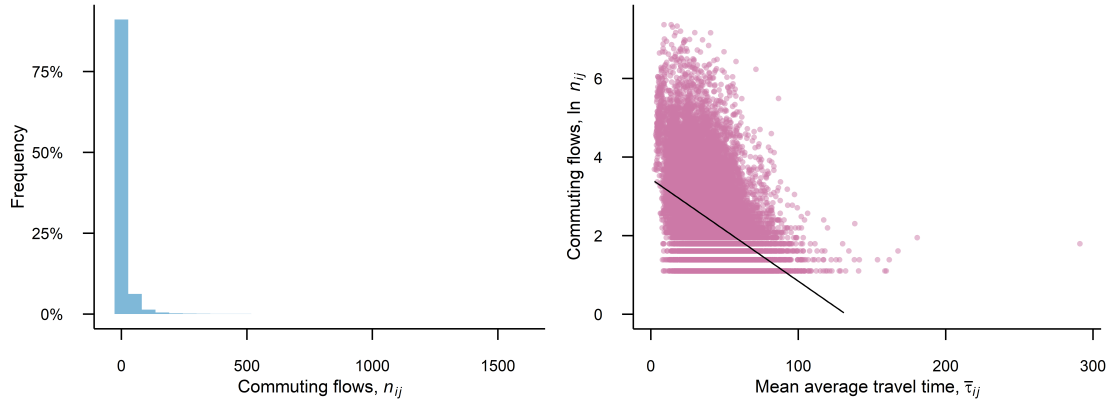


Figure 2: Left panel: Histogram of commuting flows, n_{ij} . Right panel: Commuting flows, $\ln n_{ij}$, versus average travel time, τ_{ij} , where we compute the latter as per Equation (4).

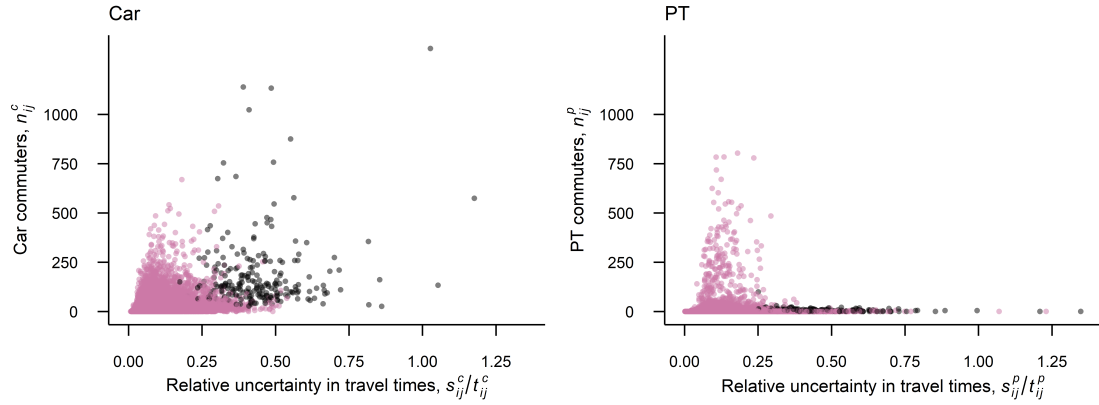


Figure 3: Commuting flows for car (left) and PT (right) versus relative uncertainty in travel times, where the latter is measured by the ratio of the standard error in travel times to the mean travel times, s_{ij} / t_{ij} , for each mode. Grey shaded points denote intra-zonal flows.

commuters within zones. Specifically, the left and right panels of Figure 3 plot commuting flows by car (n_{ij}^c) and PT (n_{ij}^p) versus relative uncertainty in travel times, which we define as the ratio of the estimated standard deviations and mean travel times, s_{ij} / t_{ij} . For car, we observe a positive association between s_{ij}^c / t_{ij}^c and n_{ij}^c , that is, large car commuting flows are associated with more uncertain travel times, especially for intra-zonal flows. For PT, in contrast, we observe no clear association between s_{ij}^p / t_{ij}^p and n_{ij}^p . This is the first hint that measurement error in travel times may have heterogeneous effects by mode. Indeed, the commute-weighted average s_{ij} / t_{ij} is approximately 10.0% and 13.4% for car and PT, respectively, which suggests that estimates of t_{ij}^p are relatively more uncertain than those for t_{ij}^c . This, in turn, likely reflects the effects of variation in access time, wait time, and in-vehicle time when travelling by PT from different home locations.

3. Results

3.1. Mode choice

3.1.1. Benchmark models

First, we estimate three mode choice models. **Model A** includes car and PT travel times, t_{ij}^c and t_{ij}^p , and an intercept, ζ_0 , in a Binomial model, $\mathcal{B}(\dots)$, with logit link:

$$n_{ij}^c \sim \mathcal{B}(n_{ij}, \mu^c t_{ij}^c + \mu^p t_{ij}^p + \zeta_0) \quad (\text{Model A})$$

where n_{ij}^c denotes the number of workers that commute by car (“successes”) between their home in i and their work in j ; n_{ij} denotes the total number of commuters (“trials”); and μ^c and μ^p are parameters to be estimated, where we expect $\mu^c < 0$ and $\mu^p > 0$.

To control for unobserved sources of heterogeneity that affect mode share, **Model B** adds group-level (“random”) effects for individual home/work locations, ζ_i and ζ_j :

$$\begin{aligned} n_{ij}^c &\sim \mathcal{B}(n_{ij}, \mu^c t_{ij}^c + \mu^p t_{ij}^p + \zeta_i + \zeta_j) \\ \zeta_i &\sim \mathcal{N}(0, \sigma_i^2) \quad \zeta_j \sim \mathcal{N}(0, \sigma_j^2). \end{aligned} \quad (\text{Model B})$$

Where we follow convention and assume the group-level effects ζ_i and ζ_j observe Normal distributions with variances σ_i^2 and σ_j^2 , respectively.

Third, **Model C** uses a control function to address concerns with endogeneity. In the first stage, we regress both car and PT travel times, t_{ij}^c and t_{ij}^p , against an instrument, Z_{ij} , and home and work group-level effects, ζ_i^z and ζ_j^z , using the following model:

$$\begin{aligned} t_{ij} &\sim \text{Logn}(\eta Z_{ij} + (1 + \eta_i Z_{ij})\zeta_i^z + (1 + \eta_j Z_{ij})\zeta_j^z) \\ \zeta_i^z &\sim \mathcal{N}(0, \sigma_{i^z}^2) \quad \zeta_j^z \sim \mathcal{N}(0, \sigma_{j^z}^2) \quad \eta_i \sim \mathcal{N}(0, \sigma_{\eta_i}^2) \quad \eta_j \sim \mathcal{N}(0, \sigma_{\eta_j}^2), \end{aligned} \quad (\text{Model C-CF})$$

where we assume t_{ij}^c and t_{ij}^p follow Lognormal distributions and we allow the effects of Z_{ij} to vary with ζ_i^z and ζ_j^z per the group-level parameters η_i and η_j . For Z_{ij} , we use the Euclidean distance between the centroids of i and j , which we assume to be exogenous. In the second stage, we include the two residuals from the first stage, z_{ij}^c and z_{ij}^p , in an

extended mode choice model:

$$\begin{aligned} n_{ij}^c &\sim \mathcal{B}(n_{ij}, \mu^c t_{ij}^c + \mu^p t_{ij}^p + v^c z_{ij}^c + v^p z_{ij}^p + \zeta_i + \zeta_j) \\ \zeta_i &\sim \mathcal{N}(0, \sigma_i^2) \quad \zeta_j \sim \mathcal{N}(0, \sigma_j^2), \end{aligned} \quad (\text{Model C})$$

If the parameters v^c and v^p are non-zero, then we have evidence of endogeneity.

To begin, we estimate Models A, B, and C without measurement error. Then we extend each of the three models to allow for measurement error in car and PT travel times, t_{ij}^c and t_{ij}^p . The measurement error version of Model A, for example, becomes:

$$\begin{aligned} n_{ij}^c &\sim \mathcal{B}(n_{ij}, \mu^c t_{ij}^{c*} + \mu^p t_{ij}^{p*} + \zeta_0) \\ t_{ij}^{c*} &\sim \text{Logn}(t_{ij}^c, (s_{ij}^c)^2) \quad t_{ij}^{p*} \sim \text{Logn}(t_{ij}^p, (s_{ij}^p)^2) \end{aligned} \quad (\text{Model A}^*)$$

where the parameters t_{ij}^{c*} and t_{ij}^{p*} denote unobserved latent car and PT travel times that are estimated along with the other model parameters. Here, we assume t_{ij}^{c*} and t_{ij}^{p*} follow Lognormal distributions with means, t_{ij}^c and t_{ij}^p , and variances, $(s_{ij}^c)^2$ and $(s_{ij}^p)^2$, respectively, where s_{ij}^c and s_{ij}^p denote the estimated standard errors from the sampled travel time data described in Section 2.3. We use an identical multi-level structure to extend Models B* and C* to allow for measurement error in car and PT travel times.

Table 1 presents regression results for these mode choice models, where columns 1–3 and 4–6 pertain to models without (Models A, B, and C) and with (Models A*, B*, and C*) measurement error, respectively.⁸ In all models, we standardise car and PT travel times, t_{ij}^c and t_{ij}^p , such that their parameters, μ^c and μ^p , measure the effect of a one standard deviation increase in travel time. Turning first to the summary statistics, we find Model C*—that is, Model C with measurement error—performs the best, per the leave-one-out information criterion (“loo-ic”).⁹ In terms of the parameters μ^c and μ^p , the models with measurement error (columns 4–6) return estimates that are, on average, approximately three-times larger in magnitude when compared to the same models without measurement error (columns 1–3). Interestingly, the attenuation bias introduced by measurement error is sufficiently large in our setting that estimates of μ^c are zero in Model B (column 2), which is contrary to expectations. This may imply that the attenuation bias introduced by measurement error can be especially severe in

⁸ We use weakly-informative priors, $\mathcal{N}(0, 1)$, for population- and group-level parameters, and defaults otherwise. As we have a large number of observations, the choice of priors has little effect on the results.

⁹ The loo-ic measures the out-of-sample performance of each model using efficient leave-one-out cross-validation (for details, see Vehtari et al., 2017). Lower values of loo-ic are preferred.

Model	Without measurement error			With measurement error		
	A	B	C	A*	B*	C*
Car, μ_c	-1.925 (0.011)	0.009 (0.025)	-1.593 (0.051)	-5.881 (0.073)	-2.574 (0.063)	-5.184 (0.106)
PT, μ_p	4.267 (0.021)	1.931 (0.044)	3.577 (0.090)	14.581 (0.164)	7.764 (0.135)	10.798 (0.201)
OD effects (ζ_i, ζ_j)	No	Yes	Yes	No	Yes	Yes
Control function	No	No	Yes	No	No	Yes
loo-ic	182,439	50,858	48,443	40,710	37,044	32,100
R^2	0.869	0.992	0.993	0.999	0.999	0.999

Table 1: Regression results for mode share models per Section 3.1.1 (s.e. in parentheses). In all models, the dependent variable is car commuting flows, n_{ij}^c ; we standardise car and PT travel times, t_{ij}^c and t_{ij}^p , so the parameters, μ^c and μ^p , denote the effect of a one standard deviation increase; and $n = 49,793$. Columns 1–3 and 4–6 report results without and with measurement error, respectively. Models A and A* include t_{ij}^c and t_{ij}^p —or, their latent counterparts, t_{ij}^{c*} and t_{ij}^{p*} —and an intercept; Models B and B* include group-level effects for home and work locations, ζ_i and ζ_j to control for unobserved heterogeneity; and Models C and C* use a control function to address endogeneity, where we instrument t_{ij}^c and t_{ij}^p with the crow-flies distance between the centroids of i and j , Z_{ij} .

multi-variate settings where the “true” parameter values have opposing signs. Notably, efforts to control for heterogeneity and endogeneity do not mitigate the attenuation bias, even if they do yield improved model performance. In general, these results suggest the estimation of mode choice models is sensitive to attenuation bias caused by measurement error in addition to the more common problems of heterogeneity and endogeneity.

3.1.2. Sensitivity tests

We subject Model C* to several sensitivity tests, for which the results are presented in Table 2.¹⁰ Like Table 1, columns 1–3 and 4–6 in Table 2 report results without and with measurement error, respectively. First, Models C-1 and C*-1 test whether the use of free-flow car travel times from OSM biases the results by including an estimate of the

¹⁰ For clarity, Model C* is specified as follows:

$$\begin{aligned}
n_{ij}^c &\sim \mathcal{B}(n_{ij}, \mu^c t_{ij}^{c*} + \mu^p t_{ij}^{p*} + v^c z_{ij}^c + v^p z_{ij}^p + \zeta_i + \zeta_j) \\
t_{ij}^{c*} &\sim \text{Logn}(t_{ij}^c, (s_{ij}^c)^2) \quad t_{ij}^{p*} \sim \text{Logn}(t_{ij}^p, (s_{ij}^p)^2) \\
\zeta_i &\sim \mathcal{N}(0, \sigma_i^2) \quad \zeta_j \sim \mathcal{N}(0, \sigma_j^2)
\end{aligned}
\tag{Model C*}$$

The first level defines the mode choice model; the second level defines the models of latent travel times, t_{ij}^{c*} and t_{ij}^{p*} ; and the third level defines the home/work group-level effects. We are interested in estimates of the parameters μ^c and μ^p , which denote the effects of t_{ij}^{c*} and t_{ij}^{p*} on mode choice, and t_{ij}^{c*} and t_{ij}^{p*} .

	Without measurement error			With measurement error		
	C-1	C-2	C-3	C*-1	C*-2	C*-3
Car, μ_c	-0.306 (0.074)	-1.663 (0.076)	-2.504 (0.109)	-4.972 (0.177)	-5.332 (0.107)	-5.613 (0.117)
PT, μ_p	4.451 (0.098)	3.181 (0.136)	4.808 (0.197)	10.892 (0.211)	11.176 (0.212)	11.703 (0.224)
Car congestion	Yes	No	No	Yes	No	No
Inter-zonal	No	Yes	No	No	Yes	No
Urban	No	No	Yes	No	No	Yes
loo-ic	47,536	42,357	33,994	32,093	29,848	26,336
R^2	0.993	0.994	0.992	0.999	0.998	0.998

Table 2: Regression results for mode share models per Section 3.1.2 (s.e. in parentheses). In all models, the dependent variable is car commuting flows, n_{ij}^c and we standardise car and PT travel times, t_{ij}^c and t_{ij}^p , so the parameters, μ^c and μ^p , denote the effect of a one standard deviation increase. Columns 1–3 and 4–6 report results without and with measurement error, respectively. To Model C*, Models C-1 and C*-1 ($n = 49,793$) add a measure of extra car travel time due to congestion. Models C-2 and C*-2 ($n = 49,566$) re-estimate Model C* for a sub-sample that includes only inter-zonal commutes, whereas Models C-3 and C*-3 ($n = 32,580$) includes only urban SA2s.

extra car travel time that is due to congestion in the morning and evening peak periods.¹¹ Controlling for congestion does not, however, affect the parameter estimates in Model C*-1 vis-à-vis Model C*, which may indicate that accounting for measurement error in free-flow travel times helps to control for congestion. Second, although Models C-2 and C*-2 limit the sample to inter-zonal commuting flows, we find parameter estimates that are essentially the same as Models C and C*, respectively. Third, and in a similar fashion, Models C-3 and C*-3 include only urban SA2s with population densities above 500 people per square kilometre. Both models return slightly larger parameter estimates, especially Model C-3 vis-à-vis Model C. This may indicate that excluding low-density zones helps to reduce, but not eliminate, the effects of measurement error. Nonetheless, all three sensitivity tests confirm that measurement error in travel times introduces significant attenuation bias into estimates of the parameters in mode choice models.

To conclude this section, we consider estimates of the latent travel times t_{ij}^* from Model C*. Figure 4 plots t_{ij}^* (vertical axes) versus sampled travel time, t_{ij} (horizontal axes) for car (left panel) and PT (right panel) for a random sample of 500 observations with non-zero commuting flows, that is, $n_{ij}^c > 0$ and $n_{ij}^p > 0$. The dashed diagonal lines denote where $t_{ij}^* = t_{ij}$; the size of points denotes the number of commuters, n_{ij} ; the grey bars denote the 95% credible interval of t_{ij}^* ; and the solid line indicates a non-parametric,

¹¹ These data are sourced from a commercial travel demand model owned by Veitch Lister Consulting. We are grateful to Michiel Jagersma and Azim Bhutta for their help in extracting these data.

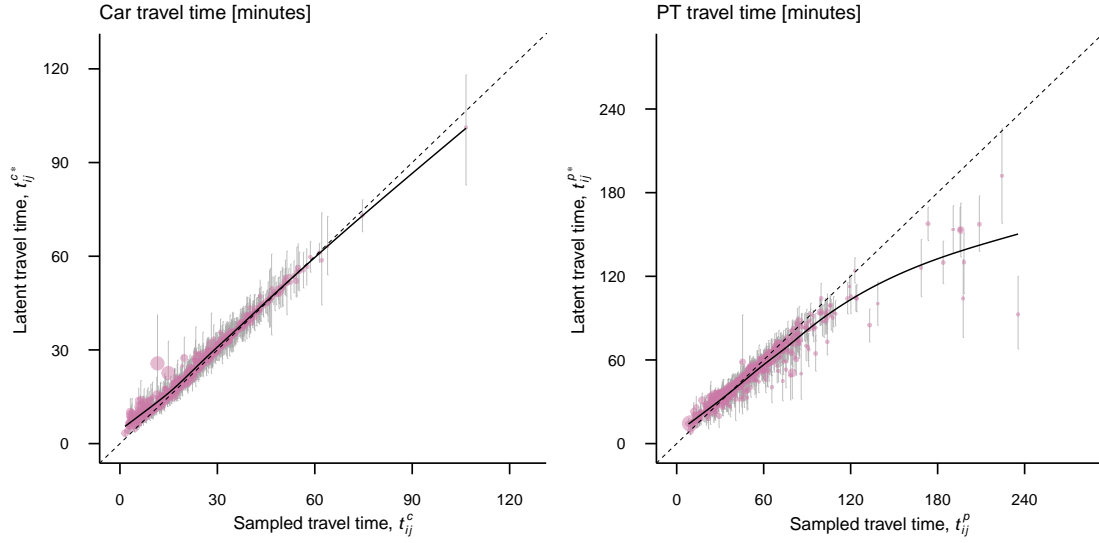


Figure 4: Latent t_{ij}^* (vertical axes) from Model C* versus sampled t_{ij} (horizontal axes) travel times for car (left panel) and PT (right panel) for a random sample of 500 observations with positive commuting flows, that is, $n_{ij}^C > 0$ and $n_{ij}^P > 0$. The dashed diagonal line denotes where $t_{ij}^* = t_{ij}$; the size of points denotes the number of commuters, n_{ij} ; and the vertical error bars denote the 95% credible intervals for t_{ij}^* . In both panels, we show non-parametric, non-linear GAM trend lines.

non-linear GAM trend line. In both panels, we observe subtle but systematic differences between latent and sampled travel times, with the former exceeding the latter at small values, and vice versa for large values—especially for PT. The relationships in Figure 4 provide preliminary evidence that the measurement error that affects our sampled travel time data may have a systematic component, rather than being purely random. Specifically, our method for sampling potential home locations within SA2s appears to systematically underestimate the travel time of short commutes and vice versa for long commutes. In Section 4, we discuss some of the underlying processes, such as parking and sorting, which may explain these systematic biases in travel time data.

3.2. Location choice

3.2.1. Benchmark models

To estimate location choice models, we first construct our measure of average travel time, τ_{ij} . From the preferred mode choice model, Model C*, we predict mode share, \hat{m}_{ij}^C , and extract posterior estimates of the latent car and PT travel times, t_{ij}^{C*} and t_{ij}^{P*} . We use these

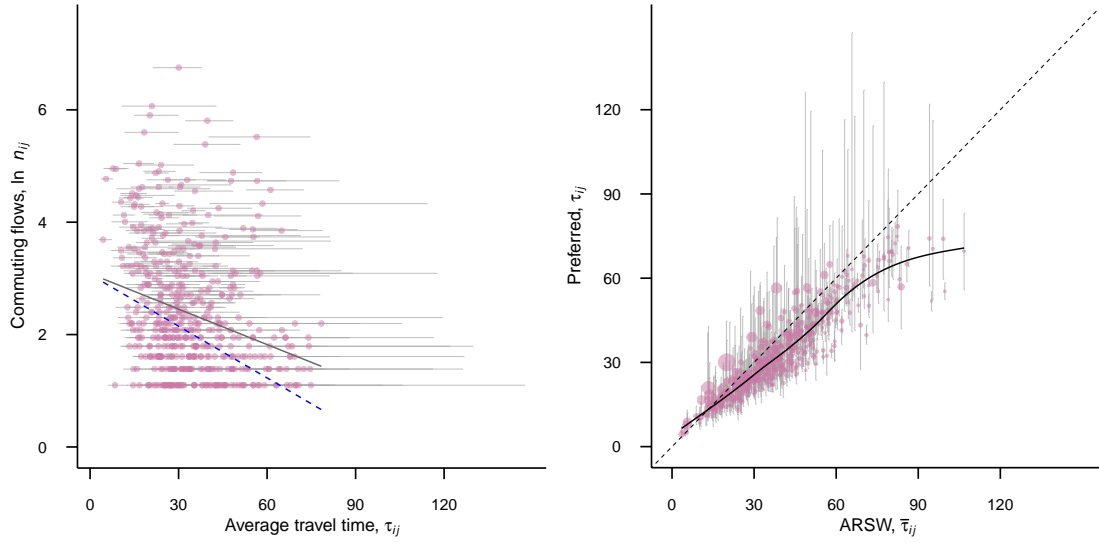


Figure 5: Comparing estimates of average travel time, τ_{ij} , for a random sample of 500 observations with positive commuting flows, $n_{ij} > 0$. Left panel: Commuting flows, $\ln n_{ij}$ (vertical axis), versus τ_{ij} (horizontal axis) and their 95% credible intervals. The solid (black) line shows a linear trend whereas the dashed (blue) line shows a weighted trend, with weights equal to the inverse of the estimated variance of τ_{ij} , that is, $1/s_{\tau_{ij}}^2$. Right panel: Estimates of τ_{ij} and their 95% credible intervals (vertical axis) versus the measure used in ARSW, $\bar{\tau}_{ij}$ (horizontal axis). The dashed diagonal line denotes where both measures are equal and the solid line denotes a GAM trend line.

data per Equation (6) to calculate a distribution for τ_{ij} . Figure 5 plots our estimates of τ_{ij} for a random sample of 500 observations with positive commuting flows, $n_{ij} > 0$. The left panel plots $\ln n_{ij}$ (vertical axis) versus our estimates of τ_{ij} (horizontal axis) and their 95% credible intervals. We add two lines: The solid (black) line shows a linear trend whereas the dashed (blue) line shows a weighted trend, with weights equal to the inverse of the variance of τ_{ij} , that is, $1/s_{\tau_{ij}}^2$. The latter has a more negative slope, which provides the first informal evidence that uncertainty in τ_{ij} may give rise to attenuation bias. The right panel of Figure 5 compares τ_{ij} (vertical axis) to that used in ARSW (horizontal axis). The former exceeds the latter at low values and vice versa at high values, like the differences between latent and sampled travel times that are evident in Figure 4. Uncertainty in τ_{ij} appears to be somewhat systematic, decreasing with $\ln n_{ij}$ and increasing with τ_{ij} .

Using our preferred measure of average travel time, τ_{ij} , we now estimate variants of the location choice model. First, Model D includes the mean $\bar{\tau}_{ij}$ and an intercept, δ_0 :

$$n_{ij} \sim \mathcal{P}(\delta_0 - \nu \bar{\tau}_{ij}), \quad (\text{Model D})$$

where the parameter $\nu \equiv \varepsilon \kappa$ is our focus. Second, Model E follows ARSW by including

home/work fixed effects, δ_i and δ_j , to control for heterogeneity between locations:

$$n_{ij} \sim \mathcal{P}(\delta_i + \delta_j - \nu \bar{\tau}_{ij}). \quad (\text{Model E})$$

Third, Model F uses a control function to address endogeneity in $\bar{\tau}_{ij}$. First, we regress $\bar{\tau}_{ij}$ against an instrument, Z_{ij} ; home/work location effects δ_i^z and δ_j^z ; and interaction terms between Z_{ij} , δ_i^z , and δ_j^z . We assume $\bar{\tau}_{ij}$ follows a Lognormal distribution and again use the Euclidean distance between the centroids of i and j for Z_{ij} , which yields:

$$\begin{aligned} \bar{\tau}_{ij} &\sim \text{Logn}(\eta Z_{ij} + (1 + \eta_i Z_{ij})\delta_i^z + (1 + \eta_j Z_{ij})\delta_j^z) \\ \delta_i^z &\sim \mathcal{N}(0, \sigma_{iz}^2) \quad \delta_j^z \sim \mathcal{N}(0, \sigma_{jz}^2) \quad \eta_i \sim \mathcal{N}(0, \sigma_{\eta_i}^2) \quad \eta_j \sim \mathcal{N}(0, \sigma_{\eta_j}^2), \end{aligned} \quad (\text{Model F-CF})$$

In the second stage, we include the residuals from the first stage, ϵ_{ij}^τ , to yield:

$$n_{ij} \sim \mathcal{P}(\delta_i + \delta_j - \nu \bar{\tau}_{ij} + v^\tau \epsilon_{ij}^\tau). \quad (\text{Model F})$$

As before, if the parameter v^τ is non-zero, then we have evidence of endogeneity.

Like Section 2.1.2, we first estimate Models D, E, and F without measurement error and, second, extend each model to allow for measurement error in average travel time, τ_{ij} . For example, Model D*—that is, the measurement error version of Model D—becomes:

$$\begin{aligned} n_{ij} &\sim \mathcal{P}(\delta_0 - \nu \tau_{ij}^*) \\ \tau_{ij}^* &\sim \text{Logn}(\bar{\tau}_{ij}, (s_{ij}^\tau)^2), \end{aligned} \quad (\text{Model D}^*)$$

where we compute the standard deviation in average travel times, s_{ij}^τ , from the distribution of estimates for τ_{ij} . Models F* and G* extend Models F and G using an identical multi-level structure to account for measurement error in average travel time, τ_{ij} .

In Table 3, columns 1–3 and 4–6 present results without (Models D, E, and F) and with (Models D*, E*, and F*) measurement error, respectively. Model F* (column 6) has the lowest loo-ic and yields an estimate for $\nu = 0.1607$ (s.e. 0.0005), which is approximately one-third larger than the same model without measurement error (Model F) and 50% larger than the model that is closest to ARSW (Model E). For the models without measurement error, the inclusion of controls for heterogeneity (Model E) and endogeneity (Model F) serve to significantly improve model performance and yield larger estimates for ν , but do not fully mitigate the attenuation bias that is introduced by measurement error. These results suggest the estimation of location choice models is

	Without measurement error			With measurement error		
	D	E	F	D*	E*	F*
ν	0.0550 (0.0001)	0.1056 (0.0001)	0.1203 (0.0002)	0.1854 (0.0003)	0.1422 (0.0004)	0.1607 (0.0005)
OD effects (δ_i, δ_j)	No	Yes	Yes	No	Yes	Yes
Control function	No	No	Yes	No	No	Yes
loo-ic	1,865,606	347,669	329,673	393,491	210,722	204,818
R^2	0.039	0.860	0.880	0.974	0.991	0.991

Table 3: Regression results for location choice models per Section 3.2.1 (s.e. in parentheses). In all models, the dependent variable is commuting flows, n_{ij} , and $n = 49,793$. Columns 1–3 and 4–6 report results without and with measurement error, respectively. Models D and D* include the average travel time, $\bar{\tau}_{ij}$ —or, its latent counterpart, τ_{ij}^* —and an intercept; Models E and E* control for unobserved heterogeneity by including fixed effects for home and work locations, δ_i and δ_j ; and Models F and F* use a control function to address endogeneity, where we instrument t_{ij}^c and t_{ij}^p with the crow-flies distance between the centroids of i and j , Z_{ij} .

sensitive to the attenuation bias introduced by measurement error, in addition to the more common problems of heterogeneity and endogeneity. That said, the level of this bias is an order of magnitude smaller than what we find for the mode choice models.

3.2.2. Sensitivity tests

We subject Models F and F* to several sensitivity tests, for which the results are presented in Table 4.¹² We structure Table 4 as before: Columns 1–3 and 4–6 report results without and with measurement error, respectively. First, Models F-1 and F*-1 use a sub-sample of the data that includes only inter-zonal commuting flows. Compared to Models F and F*, we find estimates for ν that are approximately 10% smaller. Second, and in a similar fashion, Models F-2 and F*-2 use a sub-sample of the data that includes only urban SA2s with population densities above 500 people per square kilometre. Here, the effect goes the other way: Compared to Models F and F*, we find estimates for ν that are approximately 10% larger. Third and finally, Models F-3 and F*-3 estimate zero-inflated models, which allow for additional binomial processes to give rise to more

¹² For clarity, Model F* is specified as follows:

$$\begin{aligned}
n_{ij} &\sim \mathcal{P}(\delta_i + \delta_j - \nu\tau_{ij}^* + v^\tau \epsilon_{ij}^\tau) \\
\tau_{ij}^* &\sim \text{Logn}(\bar{\tau}_{ij}, (s_{ij}^\tau)^2),
\end{aligned}
\tag{Model F*}$$

The first level defines the location choice model whereas the second level defines the model of latent average travel times. We are mainly interested in estimates of the parameters ν , τ_{ij}^* , δ_i and δ_j .

	Without measurement error			With measurement error		
	F-1	F-2	F-3	F*-1	F*-2	F*-3
ν	0.1125 (0.0002)	0.1282 (0.0003)	0.1077 (0.0002)	0.1429 (0.0005)	0.1712 (0.0007)	0.1339 (0.0005)
Inter-zonal	Yes	No	No	Yes	No	No
High density	No	Yes	No	No	Yes	No
Zero-inflated	No	No	Yes	No	No	Yes
loo-ic	267,885	232,514	298,623	196,384	148,941	198,303
R^2	0.925	0.893	0.701	0.992	0.992	0.878

Table 4: Regression results for location choice models per Section 3.2.2 (s.e. in parentheses). In all models, the dependent variable is commuting flows, n_{ij} . Columns 1–3 and 4–6 report results without and with measurement error, respectively. Compared to Models F and F*, Models F-1 and F*-1 ($n = 49,566$) use a sub-sample of the data that includes only inter-zonal commutes, whereas Models F-2 and F*-2 ($n = 32,580$) use a sub-sample that includes only urban SA2s. Models F-3 and F*-3 ($n = 49,793$) estimate zero-inflated Poisson models, which include an additional binomial process.

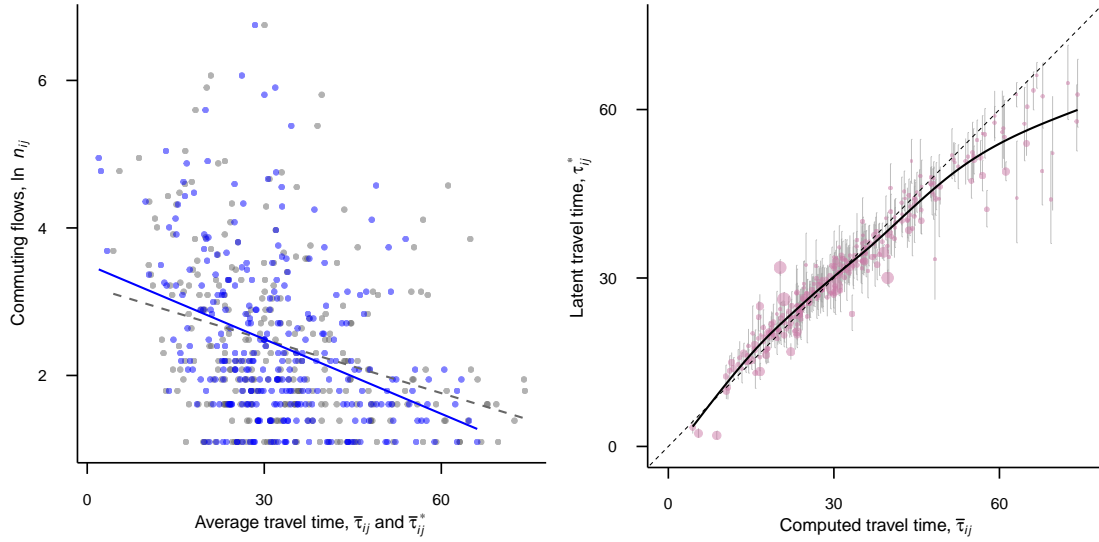


Figure 6: Analysing results for Model F*-3 for a random sample of 500 observations with positive commuting flows, $n_{ij} > 0$. The left panel shows $\ln n_{ij}$ (vertical axis) versus average travel time, τ_{ij} (horizontal axis). The dashed (grey) and solid (blue) lines show linear trends versus the means of the computed and latent estimates, $\bar{\tau}_{ij}$ and $\bar{\tau}_{ij}^*$, respectively. The right panel plots $\bar{\tau}_{ij}$ (horizontal axis) versus τ_{ij}^* (vertical axis) and its 95% credible intervals. The dashed diagonal line denotes where $\bar{\tau}_{ij} = \tau_{ij}^*$ and the solid line denotes a GAM trend line.

zeros than is generated by the Poisson processes alone.¹³ We find evidence to support zero-inflated models in our setting: Models F-3 and F*-3 perform better than Models

¹³ Zero-inflated Poisson models can be motivated on empirical and theoretical grounds. Empirically, the ABS randomly perturbs Census data to protect individual privacy, introducing extra zeros into data with small counts, like ours. And, from a theoretical perspective, additional zeros may be introduced when workers' choice of home/work locations is constrained by their schedules as well as their budget.

F and F*, respectively, and return smaller estimates for ν . Nonetheless, in all three tests, the models with measurement error (columns 4–6) return estimates for ν that are approximately 30–40% larger than those without (columns 1–3). To finish, Figure 6 analyses results for Model F*-3 for a random sample of 500 observations with positive commuting flows, $n_{ij} > 0$. The left panel shows $\ln n_{ij}$ (vertical axis) versus average travel time, τ_{ij} (horizontal axis), where the dashed (grey) and solid (blue) lines represent linear trends for computed ($\bar{\tau}_{ij}$) and latent estimates (τ_{ij}^*), respectively. The latter trend line has a steeper slope that is consistent with a larger coefficient for ν . The right panel of Figure 6 then plots $\bar{\tau}_{ij}$ (horizontal axis) versus τ_{ij}^* (vertical axis) and its 95% credible intervals. Like Figure 4, these results indicate that long commutes tend to be overestimated.

3.2.3. Approximating errors

Many existing models are likely to use data for which estimates of the associated measurement error are not available nor easily generated. This raises an interesting question: In the absence of this data, is it possible to approximate the measurement errors, s_{ij}^T ? To this end, Table 5 presents regression results for variants of Model F*-3 where we approximate s_{ij}^T as a percentage, F , of the mean average travel time, $\bar{\tau}_{ij}$ —that is, we set $s_{ij}^T = F \bar{\tau}_{ij}$ —where we let F vary from 0%–50%. In Table 5, $F = 30\%$ (column 4) has the lowest loo-ic, where $\nu = 0.1973$ (s.e. 0.0015). The latter is approximately twice that for Model F-3, which does not allow for measurement error, and 50% more than Model F*-3, which calculates s_{ij}^T from the distribution of estimates for τ_{ij} and where the commute-weighted average of $s_{ij}^T / \bar{\tau}_{ij} = 14.9\%$. The results in Table 5 are interesting for two reasons. First, approximating measurement error appears preferable to treating τ_{ij} deterministically—as can be seen by comparing the loo-ic values for the model where $F = 0\%$ to those that allow for measurement error. Second, the “true” level of measurement error and attenuation bias is likely to exceed our estimates—possibly because we only capture uncertainty in the home location of workers within zones—as can be seen by comparing the loo-ic for Model F*-3 (198,303) to those in Table 5.

To finish, we test whether our findings are robust to alternative data. First, we replace estimates of average travel time with estimates of average generalised costs (“AGCs”) that are sourced from a conventional (“four step”) travel demand model. AGCs seek to measure both the monetary and non-monetary costs of commuting. By replacing average travel time with AGCs, we can check whether our results are due to aspects

Model	Approximate measurement error, $s_{ij}^\tau = F \bar{\tau}_{ij}$					
	$F = 0\%$	$F = 10\%$	$F = 20\%$	$F = 30\%$	$F = 40\%$	$F = 50\%$
ν	0.1077 (0.0002)	0.1567 (0.0007)	0.1855 (0.0013)	0.1973 (0.0015)	0.2093 (0.0016)	0.2242 (0.0020)
loo-ic	298,623	190,518	174,961	174,070	175,028	176,251
R^2	0.701	0.924	0.972	0.986	0.989	0.990

Table 5: Regression results for location choice models per Section 3.2.3 (s.e. in parentheses). In all models, the dependent variable is commuting flows, n_{ij} , and $n = 49,793$. Column 1 (Model F-3) treats average travel time, $\bar{\tau}_{ij}$, deterministically. Columns 2–6 (Model F*-3) approximates measurement errors, $s_{ij}^\tau = F \bar{\tau}_{ij}$, where F varies from 10%–50% per the column headers.

of our methodology, such as the approach to sampling car and PT travel times, the somewhat simplistic mode choice model, or the construction of τ_{ij} . Appendix B, Table 6 presents results for location choice models estimated using AGCs, where we approximate measurement error as in Table 5. We find similar results to the latter, with $F = 30\%$ yielding the best model performance and an estimate for ν that is approximately twice as large as the deterministic version of the same model. Second, we use entirely independent data for London that is sourced from Dericks and Koster (2021) and for which results are presented in Appendix B, Table 7. When we treat $\bar{\tau}_{ij}$ deterministically (column 1), we estimate $\nu = 0.1003$ (s.e. 0.0002), which is close to the 0.1005 (s.e. 0.0006) reported in Table 4 of Dericks and Koster (2021). When we approximate measurement error, however, we find $F = 40\%$ (column 5) yields the best performance, for which $\nu = 0.2135$ (s.e. 0.0012). Thus, we find strikingly similar results when we estimate location choice models using alternative transport cost measures and independent data from London.

4. Discussion

First, we consider the policy implications of the downward bias in parameters found in Section 3. To do so, we compare the effects of a simple intervention, that is, a 5% reduction in travel times for PT.¹⁴ For mode choice, the model without measurement error (Model C) predicts that this intervention would cause the car mode share to decline by approximately 1.6 percentage points, from 80.6% to 79.0%, whereas the

¹⁴ A 5% reduction in PT travel times might be achieved via higher densities around PT stops/stations to reduce walk time (Loutzenheiser, 1997; F. Zhao et al., 2003); frequent, connected PT networks (Walker, 2012); priority measures, all-door boarding, and off-board fare collection for buses (Currie and Lai, 2008; Stewart and El-Geneidy, 2014; Tirachini, 2013); and shorter rail dwell-times (Kuipers et al., 2021).

model with measurement error (Model C*) predicts that car mode share would decline by 7.6 percentage points. For location choice, differences in the predicted change in population and employment between Models F*-3 and Model F-3—that is, with and without measurement error—are shown in Figure 7. Although these differences are more subtle, Model F*-3 predicts larger increases in employment in secondary locations outside the city centre.¹⁵ In general, these results indicate that mode choice models are more affected by attenuation bias. This may suggest that mode choice models are more susceptible to unobserved selection effects that, in turn, affect travel times. One such process is “intra-zonal sorting”, whereby workers select into locations within zones that have lower-than-average travel times. And, although location choice models are somewhat less biased, evidence finds that even small changes in the distribution of people and jobs (“land use”) can have significant effects on transport outcomes (see, e.g., Y. Zhao and Kockelman, 2002; Yang et al., 2013). For these reasons, we suggest the attenuation bias in mode and location choice models may be large enough to distort transport and land use policies. This includes, most obviously, the ex-ante economic appraisal of possible investments using cost-benefit analysis as well as the potential contribution of policies to wider strategic outcomes, like improved accessibility and reduced carbon emissions.

Second, we consider whether the bias that we find has implications for other model parameters. Specifically, in ARSW the home/work location effects, δ_i and δ_j , represent combinations of other structural model parameters—that is, $\delta_i = \ln [T_i B_i^\varepsilon q_i^{-(1-\beta)\varepsilon}] = \ln T_i + \varepsilon \ln B_i - \varepsilon(1 - \beta) \ln q_i$ and $\delta_j = \ln [E_j w_j^\varepsilon] = \ln E_j + \varepsilon \ln w_j$. As such, changes in estimates of δ_i and δ_j can have implications for these parameters. Similarly, spatial economic “sorting models” will often estimate a first-stage gravity model in which the origin/destination effects—also known as area-specific constants, or “ASCs”—represent the overall level of utility that is attached to locations (see, e.g., Teulings et al., 2018). The ASCs are often used in second-stage regressions to estimate related economic parameters, such as the willingness-to-pay for local amenities (see, e.g., Van Duijn and Rouwendal, 2013). To gain insight into whether measurement error affects estimates of δ_i and δ_j to an extent that it might bias subsequent analyses, Figure 10 in Appendix D plots δ_i and δ_j versus measures of rents, $\ln q_i$, and wages, $\ln w_j$ —that we also source from the Census. In ARSW’s model, the slope of the trend lines for δ_i versus $\ln q_i$ and δ_j versus $\ln w_j$ should approximate $-\varepsilon(1 - \beta)$ and ε , respectively. When we compare the results for models

¹⁵ Compared to the Base, Model F*-3 predicts that employment and population will centralise and suburbanise, respectively, per Appendix C, Figure 9. Here, we consider only the effects of changes in travel time and do not allow for subsequent effects on related markets, such as the housing and labour market. As such, this represents a partial equilibrium analysis that, in our view, is likely to overstate the land use response.

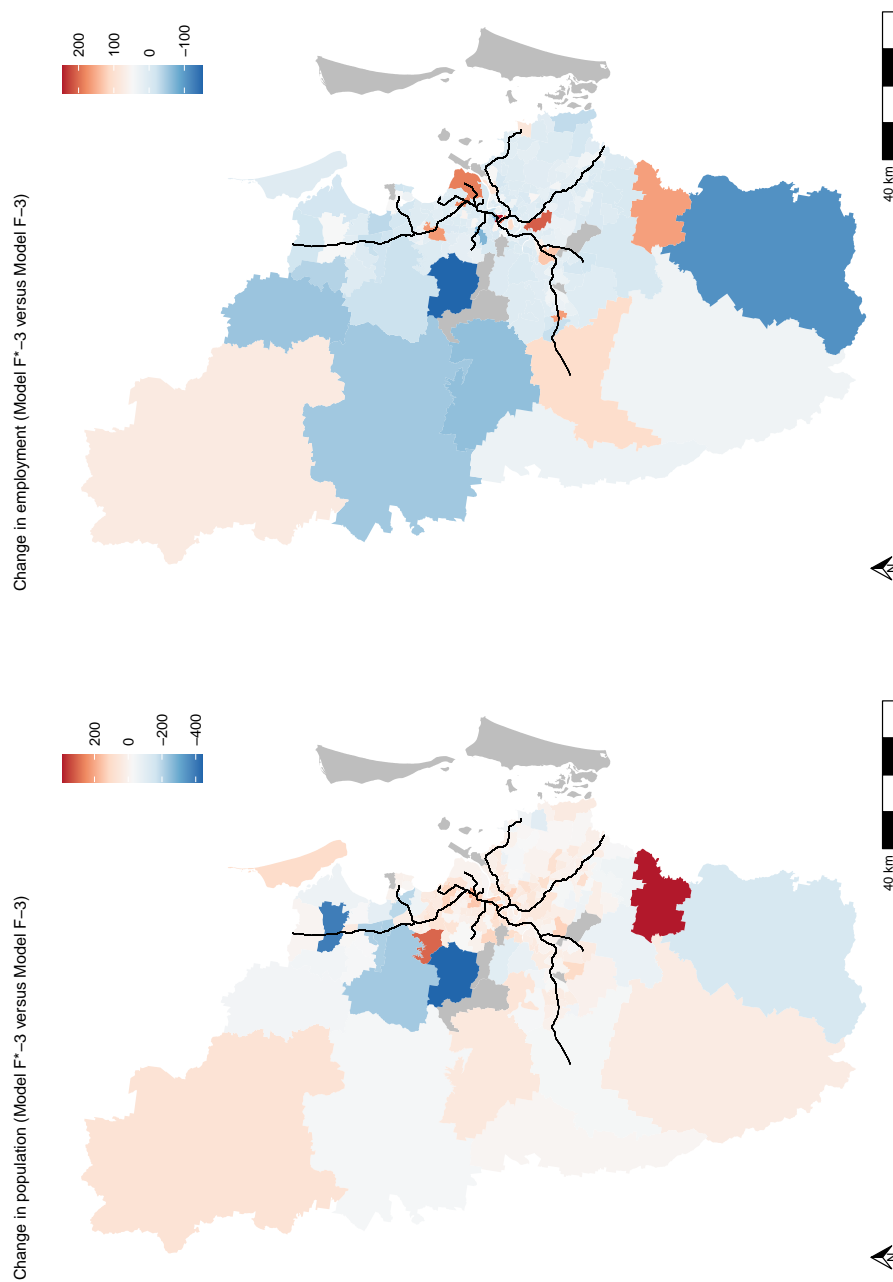


Figure 7: The difference in the change in population (bottom panel) and employment (top panel) caused by a 5% reduction in PT travel times between location choice models with (Model F*-3) and without (Model F-3) measurement error. Compared to Model F-3, Model F*-3 predicts larger increases in population in suburban areas with access to PT and secondary employment locations. The solid (black) lines illustrate the extent of urban passenger rail services.

with and without measurement error, however, we do not observe any obvious systematic differences in the implied relationships. This finding provides some solace, as it suggests that the downward bias in parameter estimates that is introduced by measurement error in travel times does not necessarily “spill over” into subsequent analyses that make use of the estimates for δ_i and δ_j . That said, we cannot preclude the presence of systematic bias in the home/work location effects and advise researchers to proceed with caution.

Third, we suggest it may be prudent for researchers to allow for measurement error in travel times—and transport costs, more generally—when estimating models, even if they lack detailed information on the magnitude of these errors. In Section 3.2.3 (cf. Table 5), we find approximating measurement error improves the performance of location choice models and yields larger parameters. We expect measurement error will be most relevant in settings that are characterised by spatially heterogeneous geographies, multi-modal transport networks, and congestion effects. In such environments, agents seem likely to adjust their behaviour over multiple unobserved margins that introduce uncertainty into imputed travel times. Although the use of smaller, more detailed zones might mitigate some sources of error, we do not expect it to eliminate it entirely. Indeed, the location choice models in Table 6 use AGCs that are sourced from a travel demand model with smaller zones than the SA2s that we use for our analyses, yet reveal similar levels of attenuation bias.¹⁶ Notwithstanding these findings, we caution that approximating measurement error treats the data-generating process for uncertainty in travel times as a “black box”. This may, in turn, amplify other problems, such as misspecification. For this reason, although we suggest that—in the absence of detailed data—researchers should consider approximating measurement error, it is important to do so judiciously. Specifically, where models are estimated using approximate measurement errors, then we recommend carefully inspecting estimates of the latent travel times to ensure they remain plausible. With sufficient care, allowing for measurement error in an approximate fashion is likely to be better than treating the data deterministically when it is not.

Finally, we note three related areas for further research. First, uncertainty in the home locations of workers within zones is only one potential source of measurement error in travel times. Further research could seek to quantify other sources of uncertainty—such as work location, departure time, commute frequency, and route choice—and investigate

¹⁶ Smaller zones may reduce positive bias in long PT journeys, which seems likely to arise when workers “sort” into home locations that are accessible to PT and have shorter travel times than is found from random sampling. That said, we suggest smaller zones are unlikely to reduce negative bias in short car journeys, especially if the latter reflects unobserved time spent searching for parking and subsequent access/egress.

their implications for model parameters. Second, we see a need for more research into how parking costs—both monetary and non-monetary—are best incorporated into travel demand models. Such research could adapt and extend the methods developed in Ostermeijer et al. (2019), which uses property transactions to estimate spatial variation in the implicit price of parking. Third, further research could consider whether other models in spatial, urban, and transport economics are also affected by measurement error. This includes models that are commonly used in transport economics, such as destination choice models (“distribution”), as well as spatial economic and international trade models (see, e.g., Allen and Arkolakis, 2014; Anderson and Van Wincoop, 2004, respectively).

5. Conclusions

Using commuting data for Brisbane, Australia, we find that accounting for measurement error in travel times causes the magnitude of parameters in mode and location choice models to increase approximately three-fold and 30–40%, respectively. Errors appear to be somewhat systematic, with travel times for short car journeys being underestimated and vice versa for long PT journeys. The biases are not readily addressed as a form of heterogeneity or endogeneity, nor are they due to unusual observations, such as intra-zonal commutes or low-density zones. Similar findings emerge when we approximate the level of error and use alternative transport cost measures or independent data from London. We note three main implications of our results. First, models that do not account for measurement error may underestimate the causal effect of travel times and transport costs, more generally, to an extent that it distorts transport and land use policy. Second, we advise researchers to judiciously allow for measurement errors in travel times and transport costs, even if they lack detailed information on the magnitude of the errors. And, third, our results highlight several promising areas for further research, including but not limited to quantifying the effects of other sources of uncertainty and accounting for measurement error in other economic models.

References

- ABS (2021). *Statistical Area Level 2 – Australian Statistical Geography Standard (ASGS)*. URL: <https://www.abs.gov.au/statistics/standards/australian-statistical-geography-standard-asgs-edition-3/jul2021-jun2026/main-structure-and-greater-capital-city-statistical-areas/statistical-area-level-2> (visited on 03/03/2023).
- Ahlfeldt, G. M., S. J. Redding, D. M. Sturm and N. Wolf (2015). 'The Economics of Density: Evidence from the Berlin Wall'. *Econometrica* 83.6, pp. 2127–2189.
- Allen, T. and C. Arkolakis (2014). 'Trade and the Topography of the Spatial Economy'. *The Quarterly Journal of Economics* 129.3, pp. 1085–1140.
- Anderson, J. E. and E. Van Wincoop (2004). 'Trade costs'. *Journal of Economic literature* 42.3, pp. 691–751.
- Andrews, I. and M. Kasy (2019). 'Identification of and correction for publication bias'. *American Economic Review* 109.8, pp. 2766–94.
- Bhatta, B. P. and O. I. Larsen (2011). 'Errors in variables in multinomial choice modeling: A simulation study applied to a multinomial logit model of travel mode choice'. *Transport Policy* 18.2, pp. 326–335.
- Bürkner, P.-C. (2017). 'brms: An R package for Bayesian multilevel models using Stan'. *Journal of Statistical Software* 80.1, pp. 1–28.
- Chang, K., Z. Khatib and Y. Ou (2002). 'Effects of zoning structure and network detail on traffic demand modeling'. *Environment and Planning B: Planning and Design* 29.1, pp. 37–52.
- Charles-Edwards, E., M. Bell and J. Corcoran (2015). 'Greening the Commute: Assessing the Impact of the Eleanor Schonell 'Green' Bridge on Travel to the University of Queensland, Australia'. *Urban Policy and Research* 33.1, pp. 61–78.
- Currie, G. and H. Lai (2008). 'Intermittent and dynamic transit lanes: Melbourne, Australia, Experience'. *Transportation Research Record* 2072.1, pp. 49–56.
- Dericks, G. H. and H. R. A. Koster (2021). 'The billion pound drop: the Blitz and agglomeration economies in London'. *Journal of Economic Geography* 21.6, pp. 869–897.
- Geofabrik (2020). *Our Download Server*. URL: <https://www.geofabrik.de/data/download.html> (visited on 15/10/2021).
- Guo, J. Y. and C. R. Bhat (2004). 'Modifiable areal units: Problem or perception in modeling of residential location choice?' *Transportation Research Record* 1898.1, pp. 138–147.
- Hausman, J. (2001). 'Mismeasured variables in econometric analysis: problems from the right and problems from the left'. *Journal of Economic Perspectives* 15.4, pp. 57–67.
- Kuehnel, N., D. Ziemke, R. Moeckel and K. Nagel (2020). 'The end of travel time matrices: Individual travel times in integrated land use/transport models'. *Journal of Transport Geography* 88, p. 102862.
- Kuipers, R. A., C.-W. Palmqvist, N. O. Olsson and L. Winslott Hiselius (2021). 'The passenger's influence on dwell times at station platforms: A literature review'. *Transport Reviews* 41.6, pp. 721–741.
- Loken, E. and A. Gelman (2017). 'Measurement error and the replication crisis'. *Science* 355.6325, pp. 584–585.
- Loutzenheiser, D. R. (1997). 'Pedestrian access to transit: Model of walk trips and their design and urban form determinants around bay area rapid transit stations'. *Transportation Research Record* 1604.1, pp. 40–49.
- Lovelace, R., D. Ballas and M. Watson (2014). 'A spatial microsimulation approach for the analysis of commuter patterns: From individual to regional levels'. *Journal of Transport Geography* 34, pp. 282–296.

- Martínez, L. M., J. M. Viegas and E. A. Silva (2007). 'Zoning decisions in transport planning and their impact on the precision of results'. *Transportation Research Record* 1994.1, pp. 58–65.
- Monte, F., S. J. Redding and E. Rossi-Hansberg (2018). 'Commuting, migration, and local employment elasticities'. *American Economic Review* 108.12, pp. 3855–90.
- OpenStreetMap (2021). *OpenStreetMap — Australia*. URL: <https://www.openstreetmap.org/#map=5/-28.111/133.242> (visited on 15/10/2021).
- Ostermeijer, F., H. R. Koster and J. van Ommeren (2019). 'Residential parking costs and car ownership: Implications for parking policy and automated vehicles'. *Regional Science and Urban Economics* 77, pp. 276–288.
- R Core Team (2023). *R: A Language and Environment for Statistical Computing*. Vienna, Austria: R Foundation for Statistical Computing.
- RStudio Team (2023). *RStudio: Integrated Development Environment for R*. Boston, MA.
- Severen, C. (2021). 'Commuting, Labor, and Housing Market Effects of Mass Transportation: Welfare and Identification'. *The Review of Economics and Statistics*, pp. 1–99.
- Stewart, C. and A. El-Geneidy (2014). 'All aboard at all doors: Route selection and running-time savings estimation for multiscenario all-door bus boarding'. *Transportation Research Record* 2418.1, pp. 39–48.
- Teulings, C. N., I. V. Ossokina and H. L. F. de Groot (2018). 'Land use, worker heterogeneity and welfare benefits of public goods'. *Journal of Urban Economics* 103, pp. 67–82.
- Tirachini, A. (2013). 'Bus dwell time: the effect of different fare collection systems, bus floor level and age of passengers'. *Transportmetrica A: Transport Science* 9.1, pp. 28–49.
- Train, K. E. (1978). 'The sensitivity of parameter estimates to data specification in mode choice models'. *Transportation* 7.3, pp. 301–309.
- TransitFeeds (2021). *TransLink SEQ GTFS*. URL: <https://transitfeeds.com/p/translink/21?p=17> (visited on 15/10/2021).
- Van Duijn, M. and J. Rouwendal (2013). 'Cultural heritage and the location choice of Dutch households in a residential sorting model'. *Journal of Economic Geography* 13.3, pp. 473–500.
- Varela, J. M. L., M. Börjesson and A. Daly (2018). 'Quantifying errors in travel time and cost by latent variables'. *Transportation Research Part B: Methodological* 117, pp. 520–541.
- Varotto, S. F., A. Glerum, A. Stathopoulos, M. Bierlaire and G. Longo (2017). 'Mitigating the impact of errors in travel time reporting on mode choice modelling'. *Journal of Transport Geography* 62, pp. 236–246.
- Vehtari, A., A. Gelman and J. Gabry (2017). 'Practical Bayesian model evaluation using leave-one-out cross-validation and WAIC'. *Statistics and Computing* 27.5, pp. 1413–1432.
- Walker, J. (2012). *Human transit: How clearer thinking about public transit can enrich our communities and our lives*. Island Press.
- Walker, J., J. Li, S. Srinivasan and D. Bolduc (2010). 'Travel demand models in the developing world: Correcting for measurement errors'. *Transportation Letters* 2.4, pp. 231–243.
- Yamamoto, T. and R. Komori (2010). 'Mode choice analysis with imprecise location information'. *Transportation* 37.3, pp. 491–503.
- Yang, C., A. Chen, X. Xu and S. Wong (2013). 'Sensitivity-based uncertainty analysis of a combined travel demand model'. *Transportation Research Part B: Methodological* 57, pp. 225–244.
- Zhao, F., L.-F. Chow, M.-T. Li, I. Ubaka and A. Gan (2003). 'Forecasting transit walk accessibility: Regression model alternative to buffer method'. *Transportation Research Record* 1835.1, pp. 34–41.
- Zhao, Y. and K. M. Kockelman (2002). 'The propagation of uncertainty through travel demand models: An exploratory analysis'. *The Annals of Regional Science* 36, pp. 145–163.

A. Appendix A: Example of sampled journeys

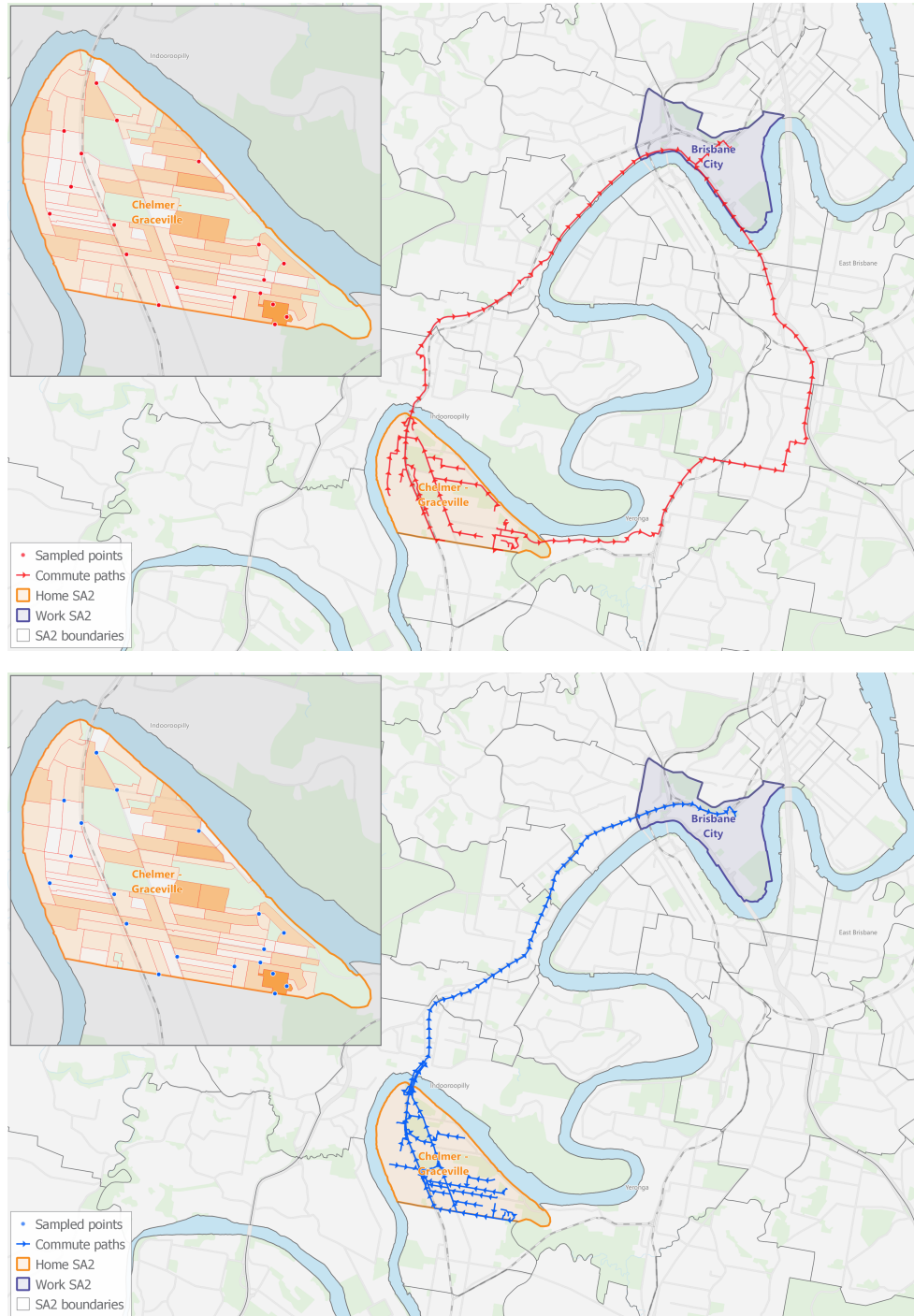


Figure 8: Sampled journeys by car (top) and PT (bottom) from Chelmer – Graceville to Brisbane City. The authors thank Azim Bhutta from Veitch Lister Consulting for making this map.

B. Appendix B: Additional regression results

Model	Approximate measurement error, $s_{ij}^T = F \bar{\tau}_{ij}$					
	$F = 0\%$	$F = 10\%$	$F = 20\%$	$F = 30\%$	$F = 40\%$	$F = 50\%$
ν	0.9386 (0.0199)	1.2999 (0.0042)	1.5865 (0.0080)	1.8846 (0.0138)	2.1740 (0.0199)	2.4009 (0.0277)
loo-ic	268,102	177,404	168,583	168,542	168,886	169,010
R^2	0.922	0.994	0.995	0.995	0.995	0.995

Table 6: Regression results for location choice models estimated using data from Brisbane (s.e. in parentheses). In all models, the dependent variable is commuting flows, n_{ij} ; we include home/work location fixed effects; and $n = 49,793$. We measure transport costs using AGCs that are sourced from a travel demand model that is calibrated to a normal weekday in 2016 using data from various sources, including but not limited to the Census. For each home/work location, we calculate AGCs as a weighted average across all workers that commute by car, PT, and walking/cycling for all time periods on a normal weekday. We aggregate AGCs from more detailed travel zones to SA2s, between which there exists a many-to-one relationship. As AGCs are measured on a different scale to travel times, the estimates for ν are not directly comparable between the two measures. Column 1 treats AGCs deterministically ($F = 0\%$). Columns 2–6 then approximate the magnitude of measurement error, $s_{ij}^T = F \bar{\tau}_{ij}$, where we allow F to vary from 10%–50% per the column headers. We find the lowest (best) loo-ic criterion for the model where $F = 30\%$ (column 4), for which the parameter estimate is twice as large as $F = 0\%$. We also note that models estimated using AGCs perform better than those estimated using travel times, which suggests travel demand models provide information that is relevant to modelling location choice.

Model	Approximate measurement error, $s_{ij}^T = F \bar{\tau}_{ij}$					
	$F = 0\%$	$F = 10\%$	$F = 20\%$	$F = 30\%$	$F = 40\%$	$F = 50\%$
ν	0.1003 (0.0002)	0.1309 (0.0004)	0.1654 (0.0007)	0.1916 (0.0009)	0.2135 (0.0012)	0.2324 (0.0016)
loo-ic	212,573	154,737	130,382	125,320	124,780	125,019
R^2	0.889	0.980	0.990	0.993	0.993	0.994

Table 7: Regression results for location choice models estimated using data from London sourced from Dericks and Koster (2021) (s.e. in parentheses). From the full sample of 966,289 observations used in Dericks and Koster (2021), we randomly sample $n = 50,000$ observations. In all models, the dependent variable is commuting flows, n_{ij} . Column 1 treats average travel time, $\bar{\tau}_{ij}$, deterministically ($F = 0\%$), which yields an estimate for $\nu = 0.1003$ (s.e. 0.0002) that is close to the 0.1005 (s.e. 0.0006) reported in Table 4 of Dericks and Koster, 2021. Columns 2–6 then approximate the magnitude of measurement error, $s_{ij}^T = F \bar{\tau}_{ij}$, where we allow F to vary from 10%–50% per the column headers. We find the lowest (best) loo-ic criterion when $F = 40\%$ (column 5), where $\nu = 0.2135$ (s.e. 0.0012). That is, more than twice that of the model without measurement error.

C. Appendix C: Change in population and employment

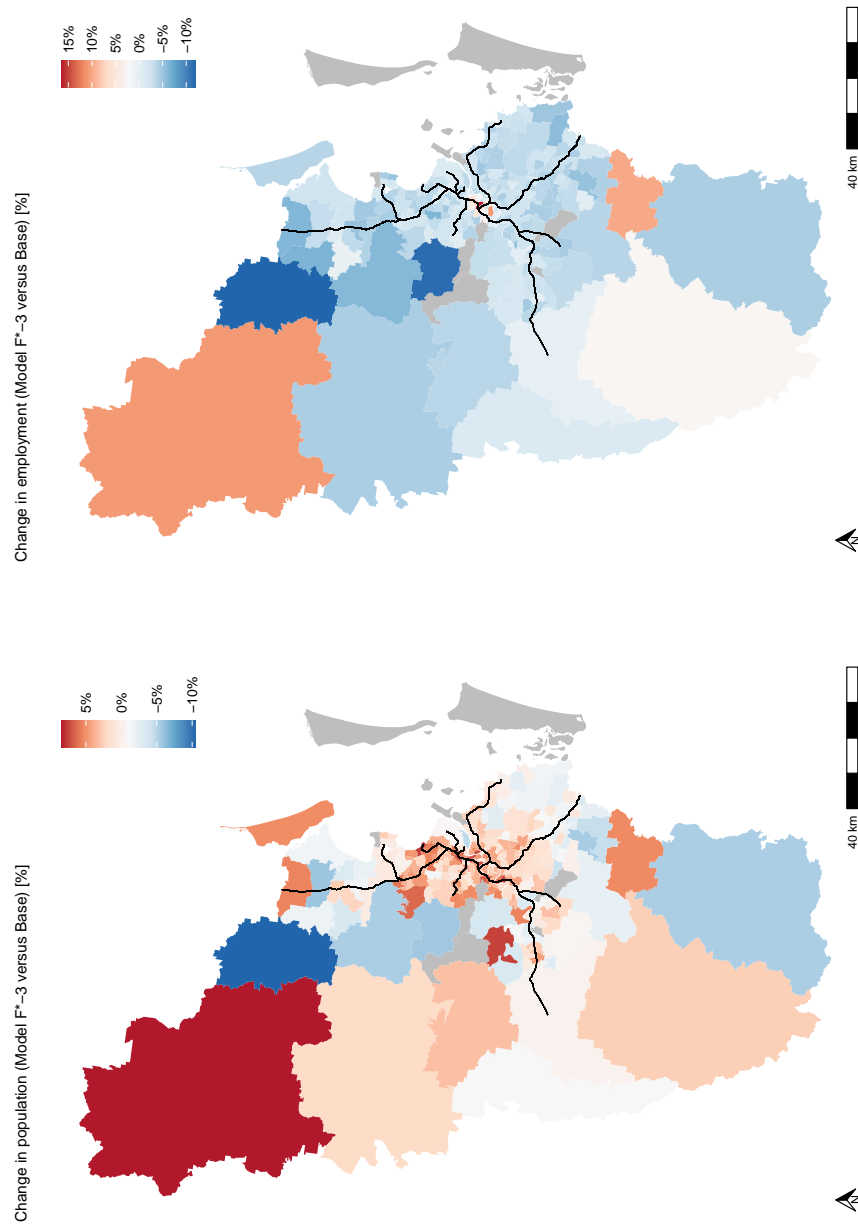


Figure 9: The percentage change in population (bottom panel) and employment (top panel) of full-time workers caused by a 5% reduction in PT travel times predicted by Model F*-3 compared to the Base. The population increase in suburban locations with access to PT and/or where walking/cycling is viable, whereas employment increases in locations around the city centre. The solid (black) lines illustrate the extent of urban passenger rail services.

D. Appendix D: Home and work location effects

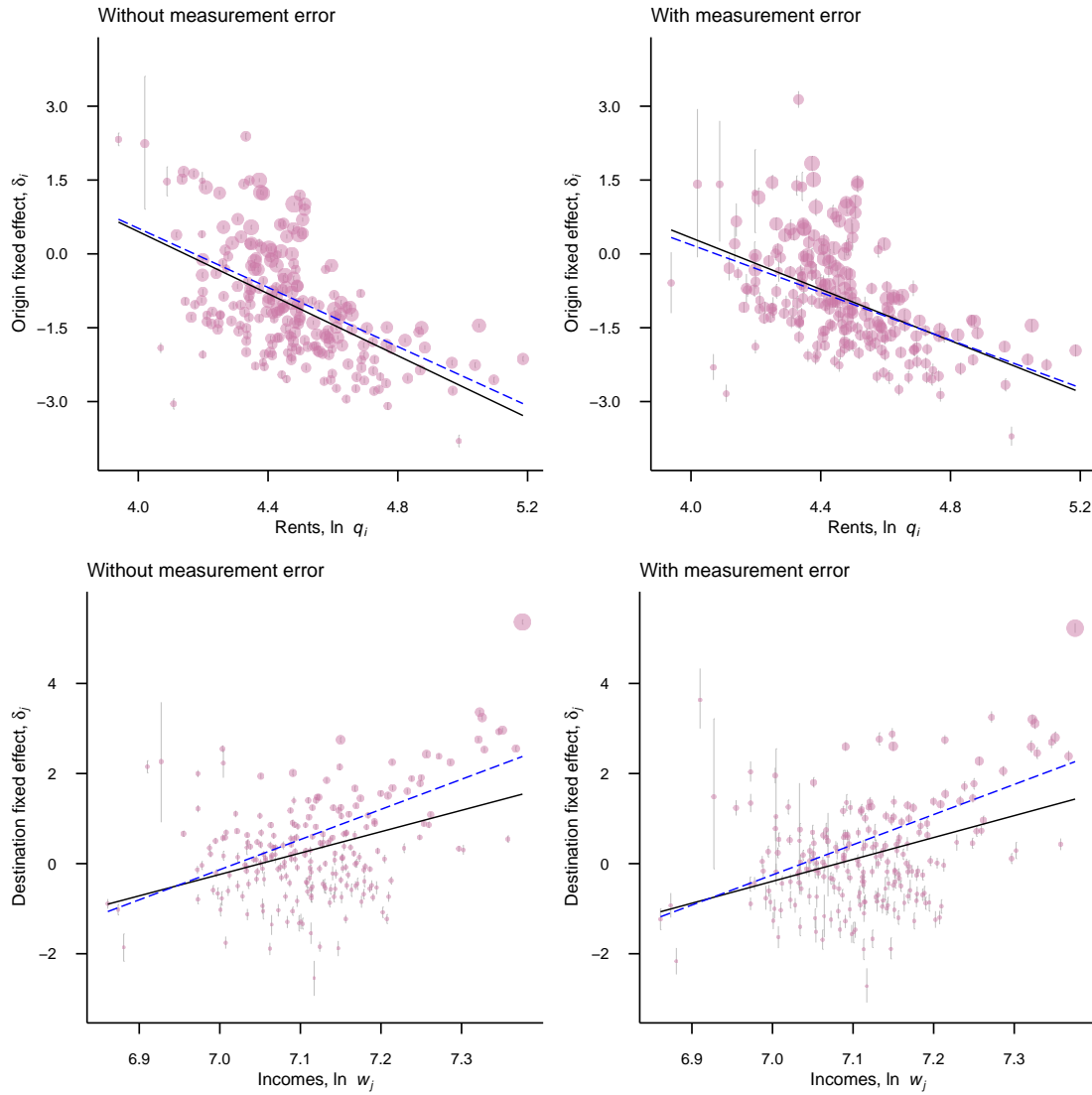


Figure 10: Estimates of δ_i (top panels) and δ_j (bottom panels) from models without (left panels) and with (right panels) measurement error, respectively, versus average rent, $\ln q_i$ (top panels) and income, $\ln w_j$ (bottom panels). We extract data on average rent per bedroom for occupied private dwellings and the average gross income for full-time workers per SA2 from the Census. The vertical error bars denote the 95% credible interval for the estimates of fixed effects and we add a normal linear trend line (solid black) and a weighted trend line (dashed blue), where weights are defined by the inverse of the variance of the estimates of each fixed effect. The size of the dots indicate the total number of commuters that live (top) and work (bottom) in each SA2.