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**Working Paper**

## Cyclical Earnings, Career and Employment Transitions

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# Cyclical Earnings, Career and Employment Transitions

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## ABSTRACT

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# Cyclical Earnings, Career and Employment Transitions\*

This paper studies the cyclical behaviour of earnings risk and career changes. We document that the procyclical skewness of the earnings growth distribution arises mostly from the earnings changes of employer and occupation switchers. To uncover their relative importance in driving cyclical earnings changes and whether this arises from changes in the returns to mobility or mobility shocks, we propose a multi-sector business cycle model with on-the-job search and endogenous occupational mobility. Idiosyncratic occupational mobility is the main driver of cyclical earnings risk, mainly due to cyclical shifts in the returns to this mobility. This is the main reason why the sullyng effects of recessions are long-lasting. These effects manifest themselves through a collapse of the job ladder and forgone lifetime earnings gains, especially for low-paid workers, and through large lifetime earnings losses among high-paid workers who experience forced occupational mobility and poor re-employment outcomes.

**JEL Classification:** E24, E30, J62, J63, J64

**Keywords:** earnings, unemployment, business cycle, search, occupational mobility

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# 1 Introduction

Understanding the nature of earnings risk is important because it impacts individuals' career path decisions, their consumption, savings and investment decisions, and ultimately inequality. In this paper we study the joint behaviour of earnings risk and career changes over the business cycle. It is well documented that during recessions those individuals who separate directly to another job face lower earnings gains, while those who lose their jobs suffer larger earnings losses relative to expansions (see Huckfeldt, 2022). These patterns are consistent with increasing evidence showing that the distribution of earnings growth exhibits procyclical skewness (see Guvenen, Ozkan and Song, 2014 and Busch, Domeij, Guvenen and Madera, 2021)<sup>1</sup> Less is known, however, about the type of job mobility that drives cyclical earnings risk and whether the latter is mainly caused by cyclical changes in the returns to mobility (i.e. the earnings change conditional on a transition), cyclical changes in the frequency of job loss and job finding and how workers' mobility decisions interacts with them both. Studying these features is important as they help determine the sources of idiosyncratic earnings risk and why this risk changes over the cycle. Without this understanding it remains difficult to evaluate, for example, whether governments should emphasise labour market policies that aim to bring individuals back to work quickly over longer duration re-training schemes that help individuals improve the type of their re-employment jobs.<sup>2</sup>

This paper shows that career changes, which we observe as occupational mobility, are the main driver behind the cyclical patterns of the earnings growth distribution. Moreover, it is occupational mobility due to workers' evolving idiosyncratic career prospects rather than occupation-wide productivity differences that makes occupational mobility the more important component. We also show that employer mobility on its own does not contribute as much as occupational mobility in shaping cyclical earnings risk. Further, worsening returns to (idiosyncratic) occupational mobility during recessions explain to a large extent the observe procyclical skewness of earnings changes. Our analysis demonstrate that the sullyng effects of recessions are long-lived. They manifest themselves through a collapse of the job ladder, particularly for occupation switchers, and forgone lifetime earnings gains especially for low-paid workers, and through the large lifetime earnings losses faced by high-paid workers who experience forced occupational mobility and poor re-employment outcomes.

To motivate our approach we use the Survey of Income and Program Participation (SIPP) to construct the annual earnings growth distribution both in the cross-section and over the business cycle. After showing that the earnings growth distribution in our data is also characterised by procyclical skewness as in Guvenen et al. (2014), and exhibits the same cross-sectional properties as documented

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<sup>1</sup>Procyclical skewness implies that the interquartile range of the distribution of earnings growth remains stable over the cycle, while the right tail compresses and the left tail expands in recessions and vice versa in expansions (Busch et al., 2021).

<sup>2</sup>For example, during the recent Covid-19 pandemic the UK Government ended up implemented unemployment benefits cuts to individuals who did not actively search for jobs outside their occupations after three months into their unemployment spell. This is similar to the Hartz reforms aimed at tackling high unemployment in Germany. These reforms imposed severe penalties on the level of unemployment benefits individuals could claim if they rejected a suitable job offer irrespectively of the industry/occupation.

in Guvenen, Karahan, Ozkan and Song (2021), we present novel evidence showing the importance of occupational mobility driving earnings growth. First we show that, among those individuals who changed employer, there is an increasing relationship between the size of the earnings change (positive or negative) and the probability of an occupational switch. This feature is observed among individuals who made a direct employer transition and among those who changed employers through a spell of unemployment. We then document our main empirical finding. The procyclical skewness of the earnings growth distribution arises mostly from the earnings changes of those individuals who switched employers and occupations at the same time. We find considerably stronger evidence of procyclical skewness among those who made an occupation switch and changed employers directly through a job-to-job transition or through unemployment relative to those who changed employer but did not switch occupation.

To interpret these data patterns, we propose a model of on-the-job search in which a job consists of two dimensions: the employer dimension (where the job is done) and the occupation dimension (the tasks involved in the job). We use this framework to investigate (i) whether cyclical changes in the earnings risk arise from the occupation or from the employer dimension, and (ii) whether the importance of each dimension arise from cyclical changes in the returns to mobility or from cyclical changes on worker flows. A simple decomposition of cyclical changes in observed worker flows and observed earnings changes conditional on flows does not allow us to answer these questions. Observed worker flows reflect worker choices in the face of changing returns, where workers could opt not to reallocate. Observed earnings changes reflect workers' acceptance decisions in the face of alternative employment possibilities, shaped also by the flows, and returns elsewhere. To untangle these forces we extend the canonical on-the-job search model originally proposed by Burdett (1978) to a multi-sector business cycle economy with endogenous employer and occupational mobility and cyclical fluctuations in job loss and job finding probabilities and offer distributions.

In our model, worker and earnings heterogeneity arises principally from two idiosyncratic productivity shocks. Essentially, workers search to improve on the two dimensions of job match quality, occupation- and firm-specific. Occupations are distinguished from one another by their workers' specific match quality and specific human capital as well as occupation-wide productivity differences. A key feature of our framework is that the decision to change employer or occupations is fundamentally different in terms the workers' information. As is standard in job ladder models, meetings with employers are treated akin to "inspection" goods. Once a worker encounters a firm, he knows enough to make a job acceptance decision. This assumption captures that typically many job interviews reveal enough information to the worker (and firm) to accept or reject the employment offer. As in many multi-sector models following Lucas and Prescott (1974), the decision to change occupations is instead treated akin to an "experience" good (see Carrillo-Tudela and Visschers, 2021, Pilossoph, 2021, Wiczer, 2015, among others). The worker does not know his labour market opportunities before starting the search for a job in the new occupation. This captures that when changing careers workers typically are able to re-build their employment contacts, learn about new employment opportunities and their job finding prospects only when they start searching for jobs in the new occupation. We

show that this structure is able to replicate the data very well.

We use simulated methods of moments to structurally estimate our model. The estimation reveals that workers' endogenous decisions to change employers and occupations with or without intervening spells of unemployment can reproduce the observed cyclical behaviour of the earnings growth distribution, the cyclical behaviour of worker mobility as well as a wide range of cross-sectional patterns that characterise earnings risk and worker mobility. In particular, our model reproduces the (i) job loss, re-employment and direct employer transition probabilities in the cross-section and over the business cycle; (ii) the gross occupational mobility patterns among employer stayers and movers in the cross-section and over the cycle, including the increasing relationship between the size of the earnings change and the probability of an occupation switch; (iii) the bilateral net mobility flows across occupations; (iv) the earnings growth distributions conditional on workers' employer and occupation transitions; (v) the cyclical change in the earnings growth distribution, characterised by its procyclical skewness; and (vi) the cyclical changes of the earnings growth distribution conditional on employer and occupation transitions, showing that the procyclical skewness arises from simultaneously changes in employers and occupations.

Our approach allow us to disentangle the separate effects of firm-worker and occupation-worker shocks in explaining the cyclicalities of earnings growth. We find that returns to idiosyncratic occupational mobility can explain nearly the entirety of the difference between the expansion and recessions earnings growth distributions, particularly between the 10<sup>th</sup> and 90<sup>th</sup> percentiles. Outside this range two major conclusions emerge. At the bottom tail, about 53% of the largest earnings losses we observe in recessions arise from those individuals who lost their jobs *and* had to change occupations. This type of events are similar to the “disaster” shocks in Guvenen et al. (2021) or “obsolescence” shocks in Huckfeldt (2022). At the top tail, the more abundant number of opportunities to improve the occupational dimension of a job becomes the more important, and can explain 26% of the largest earnings gains observed in expansions. The remainder is explained by cyclical changes in returns to occupational mobility.

Given the estimates in which both flows and returns respond to the cycle, we investigate the cost of business cycles. In particular, our model implies that cyclical changes in the returns to mobility and probabilities of job loss and job finding affect workers differently based on their positions in the employer and occupation dimensions of the job ladder. For example, by affecting their ability to climb the ladder and their outcomes after falling from it, workers might suffer differently from the sullyng effects of recessions (see Barlevy, 2002). We are interested in whether this sullyng effects persists over time. We find that low-paid workers suffer disproportionately more in terms of lifetime earnings during recessions from the reduced opportunities to climb the job ladder and the lower returns to mobility than do high-paid workers. However, we also find that it is high-paid workers who suffer disproportionately more in recessions from job transition through spells of unemployment than low-paid workers. A key result is that these costs arise primarily from the occupation dimension rather than the employer dimension of a job. This suggests that labour market policies that enable workers to achieve higher returns to occupation mobility through access to higher quality jobs could have a

significant impact in reducing cyclical earnings risk and the cost of recessions.

**Related Literature** This paper contributes to the literature investigating the properties of idiosyncratic earnings risk. Measures of the latter have been typically obtained using log-normal earnings processes and used in a wide variety of heterogeneous agent macroeconomic models. A set of recent papers, however, show that idiosyncratic earnings risk present non-Gaussian features. For example, Guvenen et al., (2021) using administrative data for the US find that the earnings growth distribution is left-skewed and has excess kurtosis (see also Arellano, Blundell and Bonhomme, 2017). Di Nardi et al. (2019), Halvorsen, Holter, Ozkan and Storesletten (2020) and Busch (2020) find similar features using data from the Netherlands, Norway and Germany. The former two also analyse the roles of changes in hours relative to hourly wages in shaping the earnings growth distribution. The main difference between these papers and ours is that we focus on understanding cyclical earnings risk.

Over the business cycle, Guvenen et al. (2014), Busch et al. (2021), Harmenberg (2018) and Kramer (2022) among others, show that earnings risk is mainly characterised by its procyclical skewness.<sup>3</sup> Building on these results, our main empirical contribution is to show that the procyclical skewness characterising the earnings growth distribution arises primarily from those who changed employers and occupations at the same time. To the best of our knowledge this feature of the data is novel. As in Di Nardi et al. (2019) and Halvorsen et al. (2020) we find that changes in hours are important for cyclical earnings risk. However, our data show that the importance of simultaneous occupation and employer mobility in shaping cyclical earnings risk is strongly visible when considering hourly wages.

Our model focuses on ex-post worker heterogeneity through firm and occupation match-specific productivities, occupation-wide productivities and human capital accumulation. This complements the work of Gregory, Menzio and Wiczer (2021), Karahan, Ozkan, and Song (2019) and Kudlyak and Hall (2019) who emphasise ex-ante worker heterogeneity, particularly in terms of the job loss and job finding probabilities. An abiding difficulty in the literature highlighting the role of ex-ante heterogeneity is distinguishing between fixed types and long-lasting shocks. In occupations, and the careers they represent, our paper captures one such long-lasting shock and shows how it can create higher-order effects in cyclical earnings risk. The reality is certainly neither polar assumption but our evidence suggests occupational disruptions are an important feature.

We also contribute to the growing literature that uses job search models to explain earnings risk. In particular, the canonical job ladder models can naturally generate some of the left-skewness and excess kurtosis observed in the cross-sectional earning growth distribution. This is because in this model the majority of workers experience small wage changes, while some workers experience large losses due to job loss. Postel-Vinay and Turon (2010), for example, shows that a version of such a model in which firms match workers' outside offers is able to replicate many salient properties of earnings dynamics as well as the annual earnings growth distribution in the cross-section. Lise (2012)

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<sup>3</sup>This is in contrast to Storesletten, Telmer and Yaron (2004) who find that earnings risk is instead characterised by its countercyclical variance.



shows that a version of the job ladder model where risk averse workers chose their search intensities and accumulate wealth is consistent with the greater dispersion of the wealth distribution relative to the earnings distribution. More recently, Hubmer (2018) further consider human capital accumulation in the latter environment and shows that his model is consistent with the main properties of the cross-sectional earnings growth distribution (see also Karahan et al., 2020). Our model not only is able to reproduce the properties of the cross-sectional earnings growth distribution at the aggregate and by type of employment and occupation transition, but it also replicates their cyclical properties. We show that a version of our model without occupational mobility akin to the canonical job ladder model reveals an important trade-off. Either it is able to replicate the cyclical behaviour of the earnings growth distribution or the cyclicalities of worker transition flows, but not both at the same time.<sup>4</sup>

Kamborouv and Manovskii (2009a,b) and Busch (2020) have already highlighted the role of occupational mobility in explaining earnings dynamics through the importance of returns to occupational tenure and long run changes in earnings inequality. Carrillo-Tudela and Visschers (2021) show the importance of occupational mobility in determining the joint behaviour of cyclical unemployment and its duration distribution. Huckfeldt (2022) emphasises the role of occupational mobility during recessions in shaping the long term costs of job loss. The novelty here is to show that occupational mobility is the main driver behind cyclical earnings risk and to highlight the importance of the returns to occupational mobility relative to the probabilities of job loss and job finding. In addition to these papers, our analysis evaluates the sullyng effects of recessions on lifetime earnings focusing on the different outcomes between high- and low-paid workers.

The rest of this paper is organized as follows. In Section 2 we present empirical work highlighting the role of occupational mobility in the dispersion of earnings changes and on the procyclical skewness of the earnings growth distribution. Sections 3 and 4 present our job ladder model and provide a careful discussion of its estimation and fit to the data. In Section 5 we use our estimated model to decompose the change in the earnings growth distribution over the cycle. Section 6 evaluates a version of our model without occupational mobility and explores its implications. Section 7 considers the sullyng effect of recessions. Section 8 concludes. Details of our data construction, model derivations, its estimation procedure, identification and robustness exercises are relegated to an Online Appendix.

## 2 The Earnings Growth Distribution

### 2.1 Data

We use data from the SIPP from the 1990 to 2008 panels, covering the 1990-2013 period. The advantage of using this dataset is that each of its panels follows a large number of workers for up to four years. Within each panel individuals are divided into four rotation groups, where each group

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<sup>4</sup>Hamenberg (2021) investigate whether an on-the-job search model can reproduce the time series relationship between the skewness and mean of the earnings growth distribution. Like his, our model generates a high skewness-mean correlation over time. Kramer (2022) also investigates the cyclical properties of the earnings growth distribution, but in an environment without on-the-job search.

is interviewed in waves of four months. At the end of each wave individuals report information on their current and previous employment status, occupations, industries and earnings (hourly wages and hours worked), covering the last four months. Using this information, we define employer, occupation and earnings changes based on a worker’s main job for each period.<sup>5</sup>

**Labor market flows** Within a panel we identify for each individual whether he/she experienced an employer and/or an occupational transition. Employer changes that occurred without an intervening full month of unemployment are labeled *EE* transitions and those that occurred through unemployment are labeled *EUE* transitions. In the latter case, we include all transitions in which the worker returned to employment within the sample, even if the worker did not report actively searching. Since we only consider unemployment spells completed within the survey period, to minimize the potential under-representation of *EUE* relative to *EE* transitions we consider only transitions with at least 4 waves remaining in the panel. *EUE* transitions, however, would remain affected by our choice to exclude “temporary recalls”, as these workers do not seem to face the same reallocation and search frictions as those workers who do not expect to return to their previous employers (see Fujita and Moscarini, 2017). We further detail our procedure in Online Appendix A.

To measure occupation changes we homogenise the occupation classification across SIPP panels using the crosswalk translation scheme created by IPUMS based on the 1990 Standard Occupational Classification (1990 SOC). We then aggregate the resulting three-digit occupational codes. For our benchmark analysis we use the aggregation based on four task-based occupational categories: Non-routine Cognitive, Routine Cognitive, Non-routine Manual and Routine Manual. We chose this coarse aggregation to focus on those changes in an individual’s line of work that also involve a change in the main tasks performed. We then compare the task-based occupation for a given individual across waves. In Online Appendix A we discuss measurement error in occupational mobility, while in Online Appendix B we present robustness using two-digit occupational codes.

For an individual to be labeled an “employer/occupational stayer” in a given wave he/she should not have changed either of these dimensions in the previous or in the posterior year relative to this wave.<sup>6</sup> Under this categorisation we find that over 75% of the transitions are made up of employer/occupation stayers. The remainder observations contain at least one form of transition. From the latter we label an individual to be an “employer/occupation mover” in a given wave when he/she reported a simultaneous employer and occupational change. As mentioned above we distinguish on whether the employer change takes the form of a *EE* or *EUE* transition. An individual is labeled as an “employer stayer / occupation mover” (“employer mover / occupation stayer”) when we only observe a change in the occupation (employer) dimension of a job.

**Earnings** To study earnings we deflate nominal monthly earnings in the SIPP by the Personal Consumption Expenditure price index. Consistent with the recent literature on earnings risk, we use as our measure of earnings the residuals obtained from regressing log real earnings on a quadratic on

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<sup>5</sup>Since the SIPP records up to two jobs at a time for any individual, we define the main job as the one in which the worker spent the most hours, and break ties using earnings.

<sup>6</sup>See Card et al. (2013), Halvorsen et al. (2020) and Guvenen et al. (2021), for a similar definition of employer stayers.

potential experience, education and month dummies. After this step we clean reporting errors in the residual earnings data by dropping the bottom and top 2% of the wave-frequency earnings sample and drop imputed earnings (see Online Appendix A for further discussion about measurement error in earnings changes). Following the literature we focus on year-to-year earnings growth. We construct annual earnings as the sum of all (residual) monthly earnings observed during the past 12 months. This measure therefore includes any zero earnings associated with the months in which an individual was unemployed.

For employed workers who do not change employers or occupation and are continually at work, earnings growth are computed by comparing the one year earnings to the next. In the case of employer and/or occupation movers, we compare earnings differences in the year prior to a transition to earnings in the year following the wave in which the transition occurred<sup>7</sup>. As mentioned above, some of these transitions include either an *EU* or *UE* observation. Because some *EU* transitions entail re-employment after an unemployment spell that lasted for more than a year and hence these workers are associated with very low or zero earnings, we use the inverse hyperbolic sine differences  $\Delta_{i,t+1} = \log(w_{i,t+1} + (w_{i,t+1}^2 + 1)^{1/2}) - \log(w_{i,t} + (w_{i,t}^2 + 1)^{1/2})$  rather than log differences to compute annual earnings changes, where  $w_{i,t}$  denotes the earnings of individual  $i$  at time  $t$ . The inverse hyperbolic sine differences are approximately the same as log differences except in the case of very low and zero earnings.

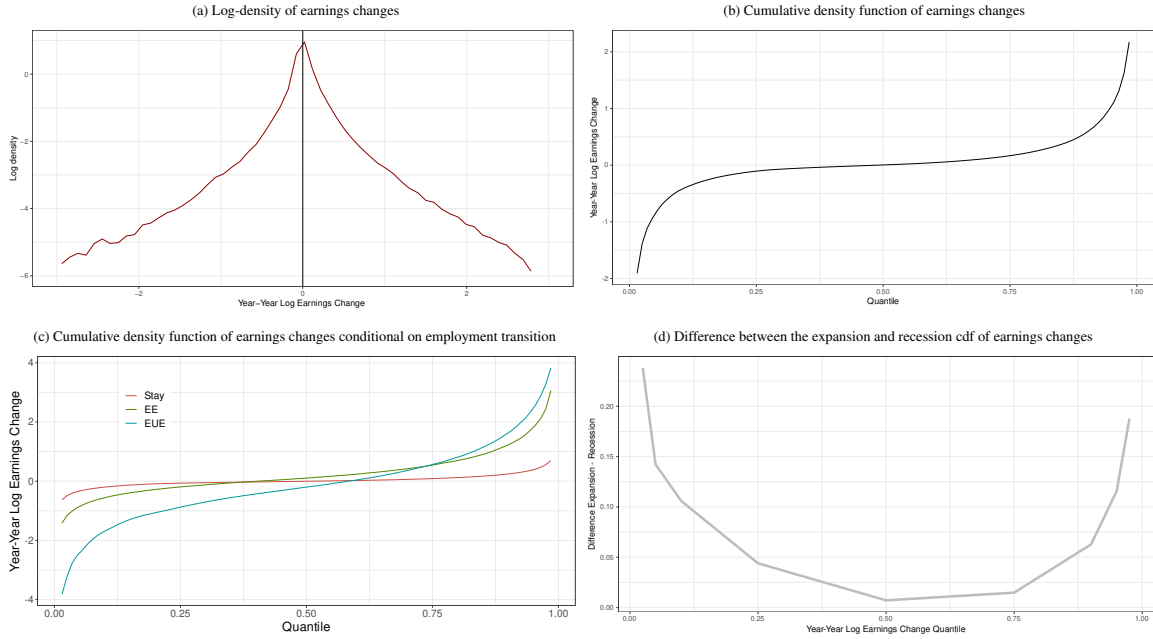
## 2.2 The earnings distribution in the cross-section and over the cycle

Figure 1a depicts the distribution of annual earnings growth pooling all years in our sample. Guvenen et al. (2021) shows that key features of this distribution is that it is left skewed and very leptokurtic, with approximately Pareto-distributed tails, hence we plot its log density to better visualize this latter property and show that both properties also are present in our sample. In Online Appendix B we present the density in levels to highlight its leptokurtosis. Figure 1b instead presents the earnings growth cdf, where we graph the earnings changes in the y-axis and the quantiles of the distribution in the x-axis. This figure further emphasises that large earnings changes lie at the bottom and top tails of the distribution. Figure 1c conditions this cdf by whether the earnings change was associated with the worker staying with the same employer or it was obtained through an *EE* or *EUE* transition. We observe that employer stayers (who represent the vast majority of workers in our sample) exhibit positive and negative earnings changes that are concentrated around zero. In contrast, employer movers have much more dispersed earnings changes and are primarily the ones behind the distribution's fat tails, as shown in Figure 1a. The large negative earnings changes are mainly due to workers who experienced *EUE* transitions, while the large positive earnings changes are due to workers who experienced *EE* transitions or came back into employment to complete an *EUE* transition.<sup>8</sup>

<sup>7</sup>In this case earnings in the reference period are measured without the aforementioned stability restriction that the respondent was at work every week of the reference period.

<sup>8</sup>In Online Appendix B we show that we arrive to a similar conclusion by analysing earnings growth conditional on previous earnings. The negative earnings/wage changes among workers who made an *EE* transitions have been

Figure 1: Earnings growth distribution in the cross-section and over the cycle



Note: The annual earnings growth distribution is constructed for the sample period 1990-2013. It is based on residual earnings after controlling for potential experience, education and month dummies. Section 2.1 presents the details of the definition of earnings and worker transitions. Recessions are defined as periods in which the HP-filtered unemployment rate is in the top 20% of realizations.

Figure 1d depicts the cyclical changes of the cdf of the earnings growth distribution.<sup>9</sup> This graph is the main data pattern of our analysis. It shows how the earnings growth distribution depicted in Figure 1b changes over the cycle by subtracting for a given quantile (x-axis) the earnings changes in periods of recessions from those in expansions (y-axis). As the median of the expansion and recession CDFs are essentially zero (0.006 and -0.003, respectively), the bottom half of these distributions represent earnings losses and the top half represent earnings gains. The pronounce U-shape depicted in Figure 1d implies that earnings losses (the left of the distribution) are larger in recession and earnings gains (the right of the distribution) are larger in expansions. For example, at the 25<sup>th</sup> percentile of the earnings growth distribution recessions have an earnings loss that is about four percentage points higher than in expansions, while at the 75<sup>th</sup> percentile expansions have an earnings gain that is about two percentage points higher than in recessions. This property has already been documented by Guvenen et al. (2014) and shows that the annual earnings growth distribution is mainly characterised by its procyclical skewness. If recessions were to bring a level-change in the observed earnings growth distribution then we would observe a horizontal line at the average loss in earnings. If recessions instead were to bring countercyclical variance, we would observe a downward sloping curve crossing zero, such that losses in recessions would be worse meaning positive values and gains in recessions

documented previously in Jolivet et al. (2006), among many others. Using the SIPP information on the reasons for leaving a job, we find that these changes are associated with both voluntary and involuntary transitions. Below we discuss this feature in the context of our model.

<sup>9</sup>Here recessions are defined as periods in which the HP-filtered unemployment rate is in the top 20% of realizations. We also analyse the cyclicity of the earnings change distribution by defining recessions as periods defined by the NBER, without a meaningful change to our conclusions.

would be higher meaning negative values. In Online Appendix B we show that the same U-shape that characterises procyclical skewness in earnings growth also arises when considering changes in hourly wages. We show that although changes in hours work do matter in determining cyclical earnings changes, particularly for the larger earnings losses during recessions, changes in hourly wages can explain a large part of the U-shape.

The key message from Figure 1 is therefore that the earnings risk as measured by the earnings growth distribution is characterized by long, thick tails that exhibit very large fluctuations over the business cycle and that this arise from changes in both hourly wages and hours worked. Hence, to understand cyclical changes in the earnings growth distribution, we need to understand its tails and the transitions that comprise it. We now present novel evidence showing the importance of occupational mobility in accounting for the behaviour of these tails.

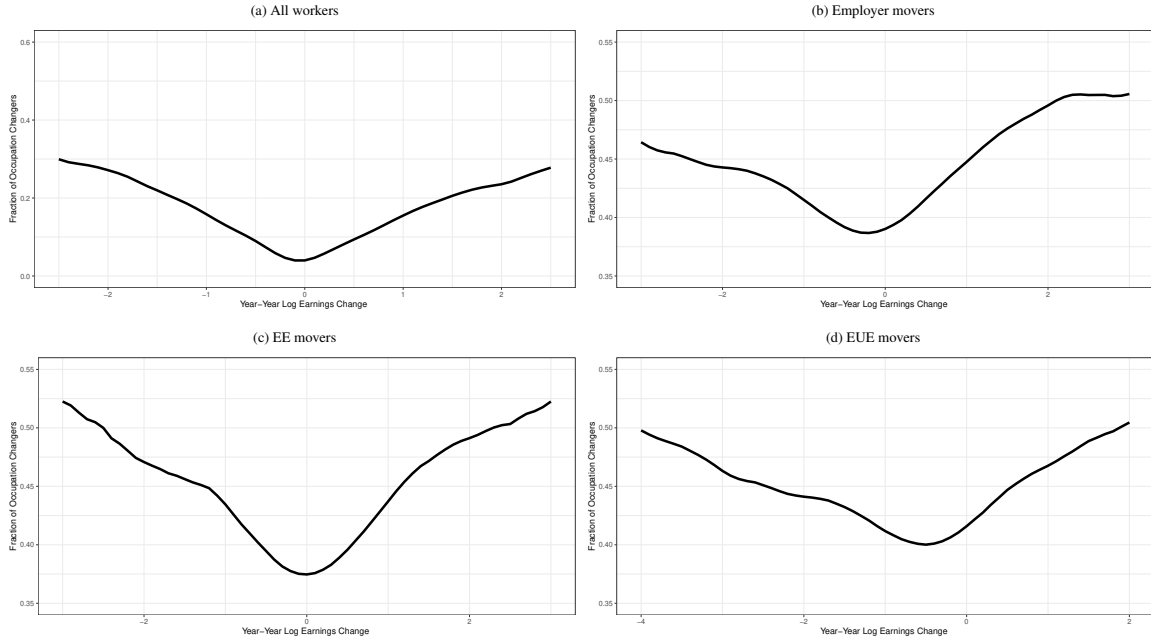
### 2.3 The importance of occupational mobility

**Occupation switching and cross-sectional earnings growth** Figure 2 depicts the probability of an occupational change associated with a given value of earnings growth. Figure 2a shows that when pooling together employer movers and stayers the fat tails of the annual earnings growth distribution depicted in Figure 1a are associated with a high probability of an occupational change (see also Guvenen et al., 2021). Small earnings changes centred around zero, however, are associated with a much smaller probability of an occupational change. Although the large difference in the probability of an occupational move can be accounted for by the larger propensity to change occupations among employer movers, we observe that the same pattern remains when only considering employer movers, as shown in Figure 2b. Figures 2c and 2d further show that this pattern holds even when analysing separately those individuals who changed employers through an *EE* or *EUE* transition. Among *EE* transitions we observe a near symmetric rise in the probability of occupational mobility and the size of the earnings losses and earnings gains. Among *EUE* transitions, however, we observe a faster rise in the probability of an occupational change among those workers who had positive earnings growth relative to those with negative earnings growth.<sup>10</sup> This evidence thus shows that large negative or positive earnings changes are associated with a higher propensity to change occupations than smaller earnings changes, even after an employer change has been taken into account.

To investigate further the role of occupational change on the the tails of the earnings growth distribution, we calculate the variance of this distribution as the proportion of the sum of squared deviations  $\sum_K \sum_{o \in K} (\Delta w_o - E_{pop}[\Delta w])^2$  that originates from a group  $K$  of workers who share an occupation and employer transition (for example, the set of workers with an *EE* transition and an occupation switch), and divide it by the overall sum of squared deviations  $\sum_{pop} (\Delta w_o - E_{pop}[\Delta w])^2$ . We find that occupation movers contribute about 50% of the overall variance of earnings growth,

<sup>10</sup>Note that for the *EUE* transitions plot we have top censored the earnings gains at +2 as the probability of occupational mobility for workers with larger earnings gains is estimated from a small number of observation in this region. The resulting pattern presents an essentially constant relationship between very large earnings gains (above +2) and the probability of an occupational change. This can be somewhat visualised in Figure 2b.

Figure 2: Earnings growth distribution and occupation mobility



Note: The probability of occupational change is computed as the proportion of workers with a given earnings change who took a job in a different task-based occupation: Non-routine cognitive, Routine cognitive, Non-routine manual and Routine manual. Earnings changes are based on residual earnings after controlling for potential experience, education and month dummies.

even though the share of occupation movers in our sample is about 17%, where the biggest share of this contribution arises from *EUE* transitions. As we move away from the tails and consider progressively the variance among those between the 0.95-0.05, 0.9-0.1 and 0.75-0.25 percentiles, the contribution of occupation movers and employer movers diminishes, reaching 15% when considering the interquartile range.<sup>11</sup>

**Occupation ladder** Earnings changes associated with occupational mobility can arise from workers moving from occupations with higher average earnings to occupations with lower average earnings, and vice versa, and from workers changing occupations due to idiosyncratic factors. To investigate the extent of these two sources of earnings growth, we derive conditional occupational earnings averages by estimating an earnings regression, which includes a quadratic for potential experience, dummies for education, gender and race and a set of dummies for occupational categories. We treat the coefficient on the occupational dummies as the occupation-wide earnings effect. For each occupation switcher we then calculate the difference between these coefficients at their source and destination occupation. A positive (negative) difference can be considered as climbing up (falling down) the occupational ladder. We perform this exercise using the 4 task-based categories and the 22 occupation categories of the two-digit 1990 SOC. Here we present the results based on the task-based categorisation to keep the benchmark analysis based on the same level of aggregation. Online Appendix

<sup>11</sup>Note that workers on average do seem to gain by switching occupations. In particular, employer stayers and *EE* movers who switched occupations gain on average about 4% and 26%, while employer stayers and *EE* movers gain on average about 1% and 16% when not switching occupations. For those workers who experienced *EUE* transitions, we find that occupation movers and stayers lose a very similar amount (around -34%).



B shows the results are very similar when using two-digit occupations, implying that the relative importance of an occupational ladder is not due to aggregation.

Figure 3: Occupational ladder



Note: Occupational switchers are ranked by their earnings growth in the horizontal axis. For each rank the vertical axis depicts the mean, median, 90<sup>th</sup> and 10<sup>th</sup> percentiles of the distribution of the differences in occupational earnings effects. A similar pattern also holds at two-digit level.

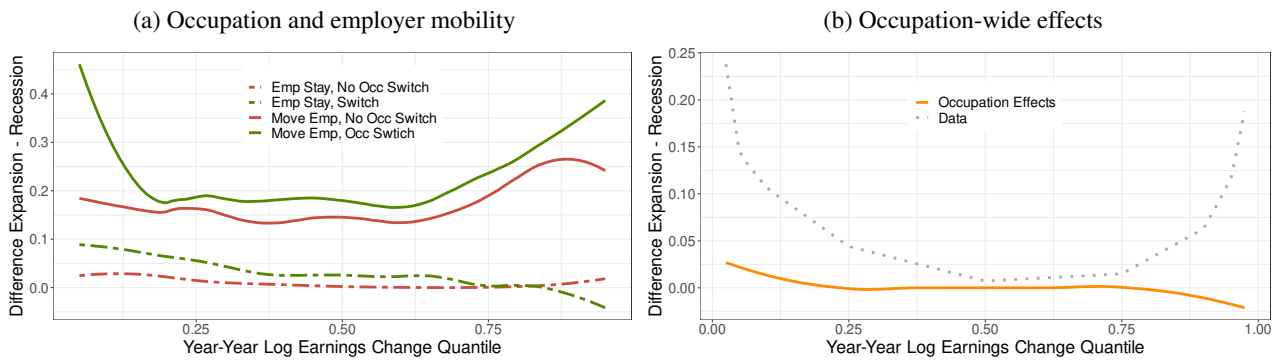
Figure 3 ranks occupational switchers by their earnings growth (x-axis) and relates each of these workers' rank to the associated distribution of the differences in occupational earnings effects (y-axis). For each rank we show the mean, median, 90<sup>th</sup> and 10<sup>th</sup> percentiles of the latter distribution. The bottom and top curves show the sequence of 10<sup>th</sup> and 90<sup>th</sup> percentiles obtained from each of these distributions. The middle two curves show the sequence of median and means. This exercise is done for each type of labour market transition. Figure 3b shows an occupation ladder for *EUE* movers, where the sequence of mean, median, 90<sup>th</sup> and 10<sup>th</sup> percentiles are all upward sloping. This implies that workers with higher earnings growth are more likely to move to higher paying occupations. Figure 3c also shows a similar ladder for employer stayers. For *EE* movers, however, the estimates depicted in Figure 3a only show a noticeable occupational ladder at the mean and the 10<sup>th</sup> percentile. Although occupational ladders are visible, the key feature of these figures is that these ladders have a very subdued effect on the distribution of changes in the occupational earnings effect. That is, large earnings changes are associated with movements both up or down the occupational ladder across all types of labour market transitions. Further, Figure 3d shows that the magnitude of the difference in the occupation effects is small compared to the magnitude of earnings growth. It does so by depicting comparing the distribution of changes in occupational earnings effects among all occupation movers to the CDF of the cross-sectional earnings growth distribution. These findings suggest that the more important factor for occupational change is the idiosyncratic motive rather than average occupation-

wide earnings differences when explaining the earnings growth distribution.<sup>12</sup>

**Occupation switching and cyclical earnings growth** To highlight the role of occupation mobility in the cyclical change of earnings growth, Figure 4a decomposes the difference in the earnings growth distribution between expansions and recessions by whether workers were occupational movers or stayers conditioning on employer change. As in Figure 1d we subtract the expansion from the recession earnings growth distribution.

Among employer stayers we observe that occupation movers have larger earnings losses during recessions than occupation stayers. However, these losses are modest, increasing only slightly towards the bottom end of the distribution. These workers also exhibit larger and modest earnings gains in expansions relative to occupational stayers. At the very top of the distribution (above the third quartile) we observe the opposite pattern. In recessions those who changed occupations within the same employer receive larger earnings gains relative to occupation stayers. Overall this leads to the earnings growth distribution of employer stayers/occupation movers to exhibit countercyclical variance. For occupational/employer stayers we instead observe a slight level-change between recession and expansions, whereby earnings losses in recessions are of similar magnitude as earnings gains in expansions.

Figure 4: Cyclical earnings growth distribution by occupation mobility



Note: In the left panel the cyclical change in the annual earnings growth distribution is constructed separately for those workers who (i) simultaneously change employers and occupations, (ii) change employers but did not change occupations, (iii) did not change employers and change occupations, (iv) or did not change either of these dimensions. In the right panel the cyclical changes in earnings are computed based on changes in the estimated occupation fixed effects. This is done separately for expansion and recessions. In either case we fix the quantile of the distribution along the horizontal axis and we subtract the associated expansion from the recession earnings growth along the vertical axis.

In contrast, employer movers who also changed their occupation exhibit larger losses in recessions relative to occupation stayers and these losses become much larger at the bottom end of the distribution. Further, they also exhibit larger gains in expansions, which also become even larger at the top end of the distribution. These cyclical features create a U-shape pattern that mimics quite closely that

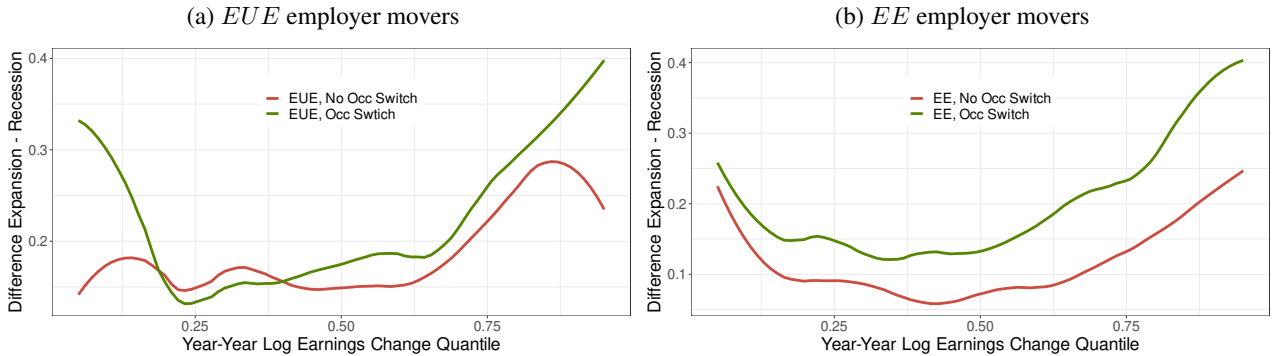
<sup>12</sup>Note that this finding does not contradict that of Groes et al. (2014). They show that (i) the probability of an occupational move is higher among those workers whose wages are at bottom or top end of their current occupation's wage distribution relative to those whose wages are around the median; and (ii) that among those workers who switched occupations, those whose wages are at the bottom (top) end of their pre-separation occupation's wage distribution have a higher probability of moving down (up) the occupation ladder. Although not shown here we also find evidence supporting these patterns in the SIPP when using 2-digit occupations from the 1990 SOC.



of the overall earnings growth distribution (Figure 1d) and implies that the earnings growth distribution of employer/occupation movers is characterised by procyclical skewness. Among those who changed employers but did not change occupations we observe a nearly constant increase in earnings losses during recessions, while an increasing pattern of larger earnings gains during expansions. That is, these workers do not seem to experience an increase in the downside earnings risk of changing employers during recessions.

Figure 4b investigates whether the joint effect of occupation/employer mobility in determining the procyclical skewness of the earnings growth distribution is due to workers moving more often to better or worse occupations at different points of the business cycle. We use the same procedure as described above to generate occupation-wide fixed effects and compute the difference in the fixed effects associated with workers switching occupations. We do this separately for expansions and recessions and then subtract the difference at each quantile. The figure shows that occupation-wide earnings differences do not seem to explain the observed cyclical changes in the earnings growth distribution. Instead, the figure points to earnings change due to idiosyncratic occupational mobility in explaining procyclical skewness. In Online Appendix B, we show that this result is not driven by using the aggregate task-based categories but also holds when using two-digit occupations.

Figure 5: The cyclicity of earnings growth - employer movers and occupation movers/stayers



Note: Among those who change employers and conditional on the type of employer transition (*EUE* or *EE*), the cyclical change in the annual earnings growth distribution is constructed separately for those workers who simultaneously change occupations and for those who did not change occupations. For each case we fix the quantile of the distribution along the horizontal axis and we subtract the associated expansion from the recession earnings growth along the vertical axis. Earnings changes are based on residual earnings after controlling for potential experience, education and month dummies.

Figure 5 decomposes the cyclicity of the earnings growth distribution among employer movers depicted in Figure 4a by the type of transition: *EUE* or *EE*. It is clear from this figure that those who simultaneously changed their occupation and employer either through an *EUE* or *EE* transition exhibit earnings growth distributions characterised by their procyclical skewness. Perhaps unsurprisingly, during recessions the earnings losses among those occupation/*EUE* movers are more pronounced than among occupation/*EE* movers. During expansions, however, both type of transitions lead to similar increases in earnings gains. Among employer movers/occupation stayers only those who experienced an *EE* transition are the ones that exhibit an earnings growth distribution characterised by procyclical skewness. Those who changed employers through an *EUE* transitions exhibit a level change in their earnings losses during recessions, but an increase in earnings gains dur-

ing expansions. Since we observe more *EUE* transitions during recessions, these pattern dominates the cyclical change of the downside earnings risk of the earnings growth distribution among employer movers/occupation stayers as depicted in Figure 4a.

In Online Appendix B we show that this exact same patterns also hold when considering changes hourly wages instead of earnings. This is important as occupation mobility is typically associated with changes in hours worked and the U-shape relationship we find among occupation/employer movers could be mostly driven by changes in hours worked. Our results shows this is not the case. We find that although changes in hours are relative more important among *EUE* occupational movers, changes in hourly wages can still explain a large part of the U-shape relationship characterising the procyclical skewness of the earnings growth distributions among *EUE* and *EE* occupation movers.

To provide a quantitative picture of the importance of occupation and employer movers in shaping the cyclicity of earnings growth, we apply the method developed by Halvorsen et al. (2020) in order to linearly decompose the skewness of the earnings growth distribution over the cycle. We present the results in Online Appendix B. This method shows that employer and occupation movers explain about 60% of the increase in the left-skewness of the earnings growth distribution over the business cycle, even though this group of workers represent no more than 5% of all observations (20,937 person/year observations). *EUE* occupation movers explain 48%, while *EE* occupation movers explain 12%. This is in contrast to *EUE* and *EE* occupation stayers who represent 28% and 8%, respectively, and make up 8% of all observations (36,396 person/year observations).

Taken together the above evidence strongly suggests that the procyclical skewness observed in the overall earnings growth distribution depicted in Figure 1d can be traced back to a combination of larger recessionary earnings losses among those occupation movers who changed employers through *EUE* (and to a lesser extent *EE*) transitions, and the larger earnings gains during expansions among those occupational movers who changed employers through either *EUE* or *EE* transitions. Further, these cyclical changes in earnings are a result of changes in both hourly wages and hours worked among employer/occupation movers. Underlying these transitions we find a prominent role for idiosyncratic occupation/employer mobility and not occupation-wide differences.

### 3 Theoretical Framework

The patterns documented above highlight the need to investigate occupation in addition to employer mobility to better explain the cyclicity of earnings risk. These patterns also pose two key questions. Do cyclical changes in the earnings risk arise from the occupation dimension or from the employer dimension? Does the importance of each dimension arise from cyclical changes in the returns to mobility or from cyclical changes in worker flows? We now develop a structural model of job search to answer these questions.

### 3.1 Environment

Time is discrete  $t = 0, 1, 2, \dots$ . A mass of infinitely-lived, risk-neutral workers with common discount rate  $\beta$  is distributed over a finite number of occupations  $o = 1, \dots, O$ . At any time  $t$ , workers within a given occupation can be either employed or unemployed and can differ in the following dimensions: an idiosyncratic firm-match productivity,  $\epsilon_t$ , an idiosyncratic occupation-match productivity,  $z_t$ , and occupation-specific human capital,  $x_h$ .

The idiosyncratic  $\epsilon$ -productivity determines how well the worker is doing with the employer he is currently working (see Mortensen and Pissarides, 1994). This productivity follows a common and exogenous first-order stationary Markov process, with transition law  $\Gamma(\epsilon_{t+1}|\epsilon_t)$ . The  $\epsilon$ -productivity realizations affect a worker only in employment and will allow us to generate employer-to-employer mobility. The idiosyncratic  $z$ -productivity represents a worker's "career match" and determines how well he is doing in the current occupation (see Neal, 1999). In the spirit of Braxton and Taska (2022), the  $z$ -productivities can be thought of measuring (in reduced form) the evolving distance between the skill requirements of an occupation and a worker's own innate skills. These productivities also follow a common and exogenous first-order stationary Markov process, with transition law  $F(z_{t+1}|z_t)$ . The  $z$ -productivity realizations affect workers both in employment and unemployment and will drive idiosyncratic occupational mobility and any earning growth associated with this type of occupational mobility.

In addition, workers accumulate occupational-specific human capital through a learning-by-doing process. In period  $t$  an employed worker with human capital level  $x_h$  increases his human capital to  $x_{h+1}$  with probability  $\chi_e(x_{h+1}|x_h)$ , where  $h = 1, \dots, H$ . A worker's occupational-specific human capital may also depreciate with unemployment. An unemployed worker with human capital level  $x_h$  decreases his human capital to  $x_{h-1}$  with probability  $\chi_u(x_{h-1}|x_h)$   $h = 1, \dots, H$ .<sup>13</sup> Workers can in principle also accumulate firm-specific human capital during employment spells. However, the empirical results of Kambourov and Manovskii (2009b) suggest that the returns to this type of human capital will be zero in the context of our model and will not play a meaningful role in our analysis. Therefore to simplify notation we do not consider this dimension.<sup>14</sup>

Business cycles are modelled through fluctuations in the economy-wide productivity, where  $A_t$  denotes this aggregate productivity, which follows a first-order stationary auto-regressive process. We also allow some occupations to be more attractive than others in terms of their occupation-wide

<sup>13</sup>The accumulation of occupation-specific human capital, which is shared across all workers with a given occupation, aims at capturing productivity increases that arise from performing the occupation-specific tasks. For simplicity we assume that occupation human capital  $x_h$  is orthogonal to the career match  $z$ -productivities.

<sup>14</sup>Kambourov and Manovskii (2009b) show that returns to seniority within a firm (wage-tenure effects) become negligible once they also include returns to occupational experience in their "Mincerian" style wage regressions after correcting for the well known endogeneity problems arising when estimating wage-tenure profiles (see Altonji and Shakotko, 1987). As we use their estimates to calibrate the occupational-specific human capital process (see Section 4), consistency will require also using their estimates to calibrate any firm-specific human capital process. This will result in the latter only having one level and not playing any meaningful role in our result. The same argument will apply if we were to use alternative estimates such as those in Sullivan (2010) who further consider within-employer occupation mobility as done in here.

productivities. Let  $p_{o,t}$  denote the occupation-wide productivity of occupation  $o$  at time  $t$  and assume it follows an auto-regressive process. Let  $\mathcal{P}_{O,t} = \{p_{o,t}\}_{o=1}^O$  denote the vector containing all the occupation-wide productivities at time  $t$ .

**Production and earnings** Firms are passive agents in our model. They only use labour in the production process under a constant return to scale technology and face no capacity constraints when meeting workers. The output of a worker characterised by  $(z_t, x_h, \epsilon_t)$  in occupation  $o$  is given by  $y(A_t, p_{o,t}, \epsilon_t, z_t, x_h)$ . This production function is increasing and continuous in all of its arguments. To keep the analysis as parsimonious as possible we assume that workers' earnings are also represented by an exogenous function of their current productivities,  $\hat{w}(A_t, p_{o,t}, \epsilon_t, z_t, x_h)$ , which is strictly increasing and continuous in all of its arguments. This assumption implies that any changes in hours worked and hourly wages are captured (in reduced form) through  $EE$  and  $EUE$  transitions and changes in workers' productivities.<sup>[15]</sup> Note, however, that the evolution of worker's output and earnings in the model remain endogenous as workers make employer and occupational transitions decisions that affect their productivities. When unemployed workers receive  $b$  each period.

**Job destruction** Jobs can break-up endogenously as workers may decide to quit to another employer in the same or in a different occupation. This can also occur if workers' productivities fall sufficiently such that they prefer to become unemployed within their occupation. Once unemployed, a worker can decide whether to change occupation or not. In addition, jobs can be destroyed due to exogenous reasons. We consider two sources of exogenous job destruction: one due to worker-firm idiosyncratic reasons and the other due to worker-occupation idiosyncratic reasons. Let  $\delta_\epsilon(A_t)$  denote the probability that an employed worker loses his firm-match productivity and is forced to transit into unemployment within his occupation. Similarly, let  $\delta_z(A_t)$  denote the probability that a worker loses his occupation-match productivity and is forced to change occupation through unemployment. In the spirit of Huckfeldt (2022) we interpret the latter as "obsolescence shocks".<sup>[16]</sup>

**Searching within and across occupations** Unemployed and employed workers face a probability  $\lambda_u(A_t)$  and  $\lambda_e(A_t)$  of meeting a firm when searching for jobs, respectively. Once a meeting takes

<sup>15</sup>As discussed in Section 2 and shown in Online Appendix B the cyclical dynamics of the earnings growth distribution and the importance of simultaneous occupation/employer mobility in driving these dynamics arise from changes in both hourly wages and hours worked. Although workers' productivities are typically closely linked with hourly wages, they can also determine workers' choice of hours. Instead of modelling these two dimensions separately we simplify and assume a flexible functional form to match the earnings process observed in the data without assuming a particular wage/hours determination process.

<sup>16</sup>This type of job destruction shock allows the model to capture the large, negative earnings changes observed across individuals who were previously employed in high paying jobs, experienced an  $EUE$  transition with an occupational switch and ended up re-employed in a lower paying job. Huckfeldt (2022) uses "obsolescence shocks" to match a similar feature in his data. The key difference is that in our setting the obsolescence shock occurs during employment, rendering the worker unemployed and forcing him to change occupations; while in Huckfeldt (2022) this shock hits the worker during unemployment. Further, we allow the obsolescence shock to vary with the business cycle to capture that in recessions we observe more frequent and larger earnings losses accompanied by occupational switching. Guvenen et al. (2021) also document large negative earnings shocks among those with high earnings and labels them "disaster" shocks. Anecdotal evidence suggests that this type of shock has been somewhat common during the Covid-19 pandemic recession, where some individuals, for example, musicians were forced into unemployment and take jobs as postal workers or delivery drivers (see <https://mbspmag.com/arts-and-culture/har-mar-superstar-becomes-mailman/>).

place, a worker draws an initial firm-match productivity  $\tilde{\epsilon}$  from  $\Gamma(\epsilon, A)$ . We allow  $\Gamma(\cdot)$  to shift according to the state of the business cycle to capture the possible cyclical changes in the quality of the worker-firm relationships and hence the returns to employer mobility.<sup>17</sup> If the worker finds the firm-match productivity sufficiently attractive, production takes place until the match is destroyed. Otherwise, the worker remains in his current employment state and waits until another meeting takes place. A worker who is searching in an occupation different from his current occupation faces job arrival rates  $\lambda_u^c(A_t), \lambda_e^c(A_t)$ . These are potentially different from  $\lambda_u(A_t), \lambda_e(A_t)$  to capture that job finding in a different occupation can be relatively more difficult (compared to those who are already in the occupation) at particular phases of the business cycle.

Search across occupations is modelled following an imperfect directed search technology in the spirit of Fallick (1993). Occupation mobility entails the benefit of re-starting a worker's  $z$ -productivity process, but it comes at the loss of the accumulated occupational-specific human capital upon reallocation. Workers draw their initial career match in any occupation from  $F(z, A)$ , which we also allow to shift according to the state of the business cycle in order to capture possible cyclical changes in the quality of the worker-occupation relationships. Given differences in occupation-wide labour market conditions  $p_{o,t}$ , workers are not indifferent about which occupation to draw the new  $z$ -productivity. We assume that within each period a worker can receive at most one  $z$ -productivity. The worker is endowed with a unit measure of search intensity which he must divide across occupations in order to maximise his chances of receiving such a  $z$ . In particular, a worker leaving occupation  $o$  has to decide which proportion  $s_{\tilde{o}}^i$  of his time to devote to obtain a  $z$ -productivity from occupation  $\tilde{o} \neq o$ , where  $i = U, E$  denotes the worker's employment status. Let  $S^i$  denote a vector of  $s_{\tilde{o}}^i$  for all  $\tilde{o} \in O^-$ , where  $O^-$  denotes the set of remaining occupations such that  $\sum_{\tilde{o} \in O^-} s_{\tilde{o}}^i = 1$ . The probability that a worker, currently in occupation  $o$ , receives a new  $z$  from an occupation  $\tilde{o}$  is given by  $\alpha(s_{\tilde{o}}^i, o)$ , where  $\alpha(\cdot, o)$  is a continuous, weakly increasing and weakly concave function with  $\sum_{\tilde{o} \in O^-} \alpha(s_{\tilde{o}}^i, o) \leq 1$ , for all  $o \in O$ . The latter implies that the probability of not receiving a new  $z$  is given by  $1 - \sum_{\tilde{o} \in O^-} \alpha(s_{\tilde{o}}^i, o)$ .

In the case of receiving the new  $z$ -productivity the workers changes occupation. If this worker is unemployed he starts with human capital  $x_1$  and searches for jobs the same period in which reallocation takes place. If no meeting takes place, the worker remains unemployed in the new occupation. If the worker is employed he also starts with human capital  $x_1$  and is able to search for jobs straight away. Follow Jolivet et al. (2006) and Bagger and Lentz (2017) once this employed worker meets a firm, with probability  $\gamma$  he is able to decide whether to accept the new job or not; and with probability  $1 - \gamma$  he is forced to accept the new job, as long as it offers a payoff above the value of unemployment. If no meeting takes place this worker stays with his current employer but in the new occupation. The worker's idiosyncratic productivities and occupational human capital then evolve as described above. Workers can decide to reallocate once again, but they must sit out one period in their new employ-

<sup>17</sup>The notion that there are cyclical changes in the quality of worker-firm or worker-occupation matches is not new. Moscarini (2001), for example, motivates his analysis on excess reallocation by arguing that "Depressed labour markets perform less well and produce noisier allocations: ceteris paribus, worker-firm matches formed at times of high unemployment are of relatively low quality". He then presents evidence in favour of this hypothesis.

ment state before doing so. In case the worker does not receive a  $z$ -productivity he retains his current occupation and employment status for the rest of the period and then starts the occupation mobility process once again.

**Timing and state space** The timing of the events is summarised as follows. At the beginning of the period the new values of  $A$ ,  $\mathcal{P}_O$ ,  $z$ ,  $x$  and  $\epsilon$  are realised. After these realisations, the period is subdivided into four stages: separation, reallocation, search and matching, and production. At this point it is useful to define the vector  $\Omega_t = \{A_t, \mathcal{P}_{O,t}\}$ . To simplify notation further we leave implicit the time subscripts, denoting the following period with a prime. We also leave implicit the dependence of output, wages and the exogenous match break-up and job finding probabilities on productivities as described above.

We now turn to formalise unemployed and employed workers' decision problems and derive the corresponding value functions. To save space the associate flow equations and earnings distribution are relegated to Online Appendix C.

### 3.2 Worker's problem

**Unemployed workers** Consider an unemployed worker currently characterised by  $(z, x_h, o)$ . The value function of this worker at the beginning of the production stage is given by

$$\begin{aligned} W^U(x, z, o, \Omega) = & b + \beta \mathbb{E}_{x', z', \Omega'} \left[ (1 - \delta_z(A')) \max \left\{ R^U(x', z', o, \Omega'), \left[ (1 - \lambda_U(A')) W^U(x', z', o, \Omega') \right. \right. \right. \\ & + \lambda_U(A') \int_{\underline{\epsilon}}^{\bar{\epsilon}} \max \left\{ W^E(\tilde{\epsilon}, x', z', o, \Omega'), W^U(x', z', o, \Omega') \right\} d\Gamma(\tilde{\epsilon}, A') \Big] \Big\} \\ & \left. + \delta_z(A') R^U(x', \underline{z}, o, \Omega') \right]. \end{aligned} \quad (1)$$

The value of unemployment consists of the flow benefit of unemployment  $b$ , plus the discounted expected value of being unemployed at the beginning of next period's reallocation stage. With probability  $(1 - \delta_z(A))$  the unemployed worker decides to search across occupations or not. This decision is captured by the choice between the expected net gains from drawing a new  $\tilde{z}$  in another occupation and the expected payoff of remaining in the current occupation. The latter entails meeting a firm with probability  $\lambda_U(A)$ , drawing a firm-match productivity  $\tilde{\epsilon}$  and deciding whether to accept it or not. However, with probability  $\delta_z(A)$  the worker draws the lowest  $z$ -productivity,  $\underline{z}$ , and searches across occupations with probability one.

The expected net value for an unemployed worker of searching across occupations,  $R^U(\cdot)$ , is given by

$$\begin{aligned} R^U(x, z, o, \Omega) = & \max_{s_o^U} \sum_{\tilde{o} \in O^-} \alpha^U(s_o^U) \int_{\underline{z}}^{\bar{z}} \left[ \lambda_U^c(A) \int_{\underline{\epsilon}}^{\bar{\epsilon}} \max \left\{ W^E(\tilde{\epsilon}, x_1, \tilde{z}, \tilde{o}, \Omega), W^U(x_1, \tilde{z}, \tilde{o}, \Omega) \right\} d\Gamma(\tilde{\epsilon}, A) \right. \\ & \left. + (1 - \lambda_U^c(A)) W^U(x_1, \tilde{z}, \tilde{o}, \Omega) \right] dF(\tilde{z}, A) + \left( 1 - \sum_{\tilde{o} \in O^-} \alpha^U(s_o^U) \right) W^U(x, z, o, \Omega), \end{aligned} \quad (2)$$

where the maximization is subject to  $s_o^U \in [0, 1]$  and  $\sum_{\tilde{o} \in O^-} s_o^U = 1$ . Note that this expression incorporates the value of immediately searching for an employer in the new occupation under the assumption that once a worker receives a new  $z$  in a new occupation, he will move to that occupation and enter the search and matching stage during the current period. It is only when the worker does not receive a new  $z$  that he remains unemployed in the old occupation and goes directly to the production stage.

**Employed workers** Now consider an employed worker currently characterised by  $(z, x, \epsilon, o)$ . The expected value of employment at the beginning of the production stage is described by

$$W^E(\epsilon, x, z, o, \Omega) = w + \beta \mathbb{E} \left[ \delta_z(A') R^U(x', \underline{z}, o, \Omega') + \delta_\epsilon(A') W^U(x', z', o, \Omega') + (1 - \delta_z(A') - \delta_\epsilon(A')) \right. \\ \left. \times \max \left\{ W^U(x', z', o, \Omega'), \max \left\{ R^E(\epsilon', x', z', o, \Omega'), \hat{W}^E(\epsilon', x', z', o, \Omega') \right\} \right\} \right]. \quad (3)$$

The value of employment consists of the earnings, plus the discounted value of being employed at the beginning of next period's separation stage, where the worker faces exogenous job loss with probability  $\delta_\epsilon + \delta_z$ . Otherwise, the worker must decide to separate into unemployment or stayed employed. If the worker remains employed, he enters the reallocation stage and must decide whether to search for jobs in a different occupation or not.

In the case of no reallocation, the expected value of employment at the beginning of the search and matching stage in the current occupation is

$$\hat{W}^E(\epsilon, x, z, o, \Omega) = \int_{\underline{\epsilon}}^{\bar{\epsilon}} \gamma \lambda_E(A) \max \left\{ W^E(\tilde{\epsilon}, x, z, o, \Omega), W^E(\epsilon, x, z, o, \Omega) \right\} d\Gamma(\tilde{\epsilon}, A) \\ + \int_{\underline{\epsilon}}^{\bar{\epsilon}} (1 - \gamma) \lambda_E(A) \max \left\{ W^E(\tilde{\epsilon}, x, z, o, \Omega), W^U(x, z, o, \Omega) \right\} d\Gamma(\tilde{\epsilon}, A) \\ + (1 - \lambda_E(A)) W^E(\epsilon, x, z, o, \Omega), \quad (4)$$

where, with probability  $\gamma \lambda_E$  the worker can decide to accept or reject the new job offer. The job acceptance decision truncates the distribution of  $\epsilon$  such that  $W^E(\tilde{\epsilon}, \Omega) > W^E(\epsilon, \Omega)$ . Note that in this case the worker's fall back position is keeping his job with the current employer and value of  $\epsilon$ . With probability  $(1 - \gamma) \lambda_E$ , however, the worker is forced to take the new  $\epsilon'$  in a different employer, as long as this gives a value higher than unemployment. This allows us to capture within-occupation employer transitions that are associated with earnings cuts and rises. With probability  $1 - \lambda_E$  the worker does not meet a new employer and remains in his current state.

If instead the worker decides to reallocate, the expected net value of searching across occupations is given by

$$R^E(\epsilon, x, z, o, \Omega) = \max_{S^E} \sum_{\tilde{o} \in O^-} \alpha^E(s_o^E) \left( \int_{\underline{z}}^{\bar{z}} \left[ \int_{\underline{\epsilon}}^{\bar{\epsilon}} \left( \gamma \lambda_E^c(A) \max \left\{ W^E(\tilde{\epsilon}, x_1, \tilde{z}, \tilde{o}, \Omega), W^E(\epsilon, x_1, \tilde{z}, \tilde{o}, \Omega) \right\} \right. \right. \right. \\ \left. \left. \left. + (1 - \gamma) \lambda_E^c(A) \max \left\{ W^E(\tilde{\epsilon}, x_1, \tilde{z}, \tilde{o}, \Omega), W^U(x_1, \tilde{z}, \tilde{o}, \Omega) \right\} \right) d\Gamma(\tilde{\epsilon}, A) \right. \right. \\ \left. \left. + (1 - \lambda_E^c(A)) W^E(\epsilon, x_1, \tilde{z}, \tilde{o}, \Omega) \right] dF(\tilde{z}, A) \right) + \left( 1 - \sum_{\tilde{o} \in O^-} \alpha^E(s_o^E) \right) W^E(\epsilon, x, z, o, \Omega), \quad (5)$$



where the maximization is subject to  $s_o^E \in [0, 1]$  and  $\sum_{\tilde{o} \in O-} s_o^E = 1$ . Conditional on drawing a  $z$ -productivity from another occupation  $\tilde{o}$ , the worker meets a new employer with probability  $\gamma \lambda_E^c(A)$ , draws a new value of  $\epsilon$  and decides whether to accept it or not. If the offer is rejected, the worker remains with his current employer but switches to occupation  $\tilde{o}$ . With probability  $(1 - \gamma) \lambda_E^c(A)$ , however, the worker is forced to take the new value of  $\epsilon'$  with a new employer in occupation  $\tilde{o}$ , as long as the value of this employment remains above the value of unemployment in the new occupation. Otherwise, the worker transits into unemployment in occupation  $\tilde{o}$ . With probability  $1 - \lambda_E^c(A)$ , the worker remains with his current employer, retains his current value of  $\epsilon$ , but changes to occupation  $\tilde{o}$ .

The formulation in (5) allows us to capture within and across employer occupational mobility in a simple way, with two key properties. First, we do not decouple in which occupation the worker is earning and in which occupation he is searching. This property allows us to ease computational burden by simplifying the state space, perhaps coming at a cost of realism. Second, through  $EE$  transitions workers can end up with positive or negative earnings growth when switching occupations as documented in Section 2. In the model this captures the increased risk inherent to occupation mobility: with probabilities  $(1 - \gamma) \lambda_E^c$  or  $(1 - \lambda_E^c)$  the worker gives up on his fallback option  $W^E(\epsilon, x, z, o, \Omega)$ . Yet, absent a  $\delta_z$  shock, this risk is not forced upon the worker. At the earlier (reallocation) stage, workers can opt to not expose themselves to this risk by deciding not to search across occupations, as described in the last maximand of equation (3).

## 4 Quantitative Analysis

We estimate our model using simulated method of moments. Assume a period to be equal to a month and set the discount rate  $\beta = 0.997$ . Set  $O = 4$ , consistent with the task-based categories (Non-Routine Cognitive, Routine Cognitive, Non-Routine Manual and Routine Manual) used to aggregate occupations in Section 2, such that  $o \in \{NRC, RC, NRM, RM\}$ . The following functional form assumptions yield a set of parameters that we jointly estimate on data from the SIPP based on the annual earnings growth patterns documented in Section 2 as well as on worker labour market flows across employers and occupations computed from the SIPP for our observation period, 1990-2013. We relegate the details of the estimation procedure to Online Appendix D.

### 4.1 Parametrization

We parametrise the aggregate productivity shock,  $A$ , by a two-state Markov process that can be represented by  $A_I$ , a cyclical indicator function which takes the value of one when the economy is in an expansion and zero otherwise.<sup>18</sup> The occupation-wide productivity shock,  $p_o$ , is such that  $p_{o,t+1} = \tilde{p}_o + \rho_p p_{o,t} + v_{o,t+1}$  for all  $o \in O$  where  $\tilde{p}_o$  is a time-invariant occupation specific productivity and  $v_o$  is assumed to be white noise with variance  $\sigma_p$ . Occupation-specific human capital accumulation follows a two state process. Inexperienced workers start in an occupation with productivity  $x_1$

<sup>18</sup>This approximation of an AR(1) process simplifies computation and is also consistent with our data work that considered two discrete phases of the business cycle. Expansions, when the aggregate productivity takes its high value, occurs 80% of the time.



and become experienced with probability  $\chi(x_2)$  to reach  $x_2$ . To simplify we assume no occupational human capital depreciation while unemployed.

The meeting probabilities are parametrised as  $\lambda_i(A_I) = \lambda_{1,i}A_I + (1 - A_I)\lambda_{0,i}$ , where  $i = U, E$  is the employment status indicator. For those who have just switched occupations, the (potentially) different meeting probabilities are given by  $\lambda_i^c(A_I) = \lambda_{1,i}^cA_I + (1 - A_I)\lambda_{0,i}^c$ . Recall that, conditional on meeting with a new employer and receiving a job offer,  $1 - \eta$  denotes the probability with which the employed worker would not be able to refuse such a job offer (as long as its optimal to remain employed). The exogenous occupation obsolescence shock,  $\delta_z$ , and firm separation shock,  $\delta_\epsilon$ , are given by  $\delta_z(A_I) = \delta_{1,z}A_I + (1 - A_I)\delta_{0,z}$  and  $\delta_\epsilon(A_I) = \delta_{1,\epsilon}A_I + (1 - A_I)\delta_{0,\epsilon}$ .

The worker-occupation match specific productivity shock is such that  $E[z_{t+1}|z_t] = \rho_z z_t + (1 - \rho_z)v_{z,t+1}$ , where  $v_z$  is distributed following  $\tilde{F}(\cdot)$ , which we parametrize as a Weibull distribution with shape and scale parameters  $\nu_z$  and  $\sigma_z$ . Upon a decision to switch occupations new values of  $z$  are then drawn from  $F(z, A) = A_I\tilde{F}(z) + (1 - A_I)[\omega_z\tilde{F}(z) + (1 - \omega_z)T(z, z_A)]$ , where during recessions the reallocating worker draws  $z$  from a convolution between  $\tilde{F}(\cdot)$  and a tilted uniform distribution  $T(z, z_A) = \frac{zz_A+1}{\tilde{z}(\tilde{z}z_A+1) - \tilde{z}(zz_A+1)}$ . The worker-firm match specific productivity  $\epsilon$  remains constant during the duration of the match and only changes upon a voluntary or involuntary employer-to-employer transition. This is motivated by the small variation in annual earning changes observed among employer stayers. Workers draw a new  $\epsilon$  from  $\Gamma(\cdot)$ , which is also allowed to shift during recessions in a similar way as  $F(\cdot)$ . In this case,  $\Gamma(\epsilon, A) = A_I\tilde{\Gamma}(\epsilon) + (1 - A_I)[\omega_\epsilon\tilde{\Gamma}(\epsilon) + (1 - \omega_\epsilon)T(\epsilon, \epsilon_A)]$ , where  $\tilde{\Gamma}(\cdot)$  is parametrized as a Double Exponentially-Modified Gaussian distribution (a normal distribution with exponential tails on both sides) with mean normalised to zero, central variance  $\sigma_\epsilon$  and shape parameters  $lt_\epsilon, rt_\epsilon$  governing the exponential distributions describing the left and right tails, respectively. The distributional choice for  $\Gamma(\cdot)$  allows for arbitrary skewness and kurtosis, which are both features of the earnings growth distribution in the data. Further, the mixtures  $F(\cdot)$  and  $\Gamma(\cdot)$  allows us to change the skewness during recessions through  $z_A$  and  $\epsilon_A$ , and to change the variance through  $\omega_z$  and  $\omega_\epsilon$ . These distributional assumptions are important because they determine the model's earnings growth distributions conditional on previous labour market transition. As we only observe accepted matches in the data, they are crucial for identification.<sup>[19]</sup>

Particularly important is how we design the functions  $\alpha^i(\cdot)$ , because they determine how workers switch and search across occupations. Our aim is to respect the observed gross and net mobility flows across occupations. We let  $\alpha^i(s_{\tilde{o}}) = \alpha_0 e^{\alpha_{\tilde{o}}\alpha_1^i s_{\tilde{o}}^{1-\alpha_1^i}}$ , where occupation  $\tilde{o} \in O^-$  denotes the search direction,  $i$  the worker's employment status and  $s_{\tilde{o}}$  denotes search intensity. To show why this functional form is useful consider  $i = U$  such that the first order condition of (2) is given by  $\alpha'(s_{\tilde{o}}^*) (\Psi^U(\tilde{z}, x_1, \tilde{o}, \Omega) - W^U(z, x_h, o, \Omega)) = \mu$ , where  $\mu$  denotes the multiplier on  $\sum_{\tilde{o} \in O^-} s_{\tilde{o}} = 1$ .

<sup>19</sup>In the estimation we verify that the support of the discretised  $F(\cdot)$  and  $\Gamma(\cdot)$  distributions are observed in employment for at least some workers. The reason is that we want to investigate whether shifts in the returns to mobility directly affect earnings changes of at least some employed workers. Without this restriction it would be difficult for the model to distinguish, in extreme cases, a higher mass of very bad returns realizations ( $\epsilon$  or  $z$ ) that are always rejected from lower job offer arrival rates. This should be kept in mind when considering the flow/return decomposition of earnings changes over the cycle in Section 5.

Together with the latter feasibility constraint, it implies that the search intensity takes a form similar to the Gumbel-distributed random utility model. If the directional terms  $\alpha_{\tilde{o}}$  are all equal we obtain that the optimal value of  $s_{\tilde{o}}$  is given by

$$s_{\tilde{o}}^* = \frac{e^{\frac{1}{\alpha_1^U} \log(\Psi^U(\tilde{z}, x_1, \tilde{o}, \Omega) - W^U(z, x_h, o, \Omega))}}{\sum_{\tilde{o} \in O^-} e^{\frac{1}{\alpha_1^U} \log(\Psi^U(\tilde{z}, x_1, \tilde{o}, \Omega) - W^U(z, x_h, o, \Omega))}}, \quad (6)$$

and

$$\begin{aligned} \Psi^U(\tilde{z}, x_1, \tilde{o}, \Omega) &= \int_{\tilde{z}}^{\tilde{z}} \left[ \lambda_U^c \int_{\underline{\epsilon}}^{\tilde{\epsilon}} \max\left\{ W^E(\tilde{\epsilon}, \tilde{z}, x_1, \tilde{o}, \Omega), W^U(\tilde{z}, x_1, \tilde{o}, \Omega) \right\} d\Gamma(\tilde{\epsilon}) \right. \\ &\quad \left. + (1 - \lambda_U^c) W^U(\tilde{z}, x_1, \tilde{o}, \Omega) \right] dF(\tilde{z}). \end{aligned}$$

In Online Appendix D we derive a similar expression for  $s_{\tilde{o}}^*$  when considering search across occupations among employed workers. In either case, with  $\alpha_{\tilde{o}}$  differing across occupational directions we end up with a multiplier that scales the search direction. Combined with the additive noise which we use to smooth our approximate solution (see Online Appendix D), this means the search direction problem takes a similar form to a nested, multinomial logit discrete choice model. This formulation is useful not only because is simple to estimate but it also allow us to capture net flows across occupations through two distinct channels. The parameter  $\alpha_1^i$  determines the extent to which workers adjust their search due to  $p_{o,t}$  differences. It inform us whether search is more or less directed. A value closer to zero implies search becomes more directed as differences in the returns across occupations get amplified; while as  $\alpha_1^i$  goes to infinity search becomes increasingly random, as workers weight all occupations more equally. The parameter  $\alpha_{\tilde{o}}$  scales the probability of moving from occupation  $o$  to occupation  $\tilde{o} \neq o \in \{NRC, RC, NRM, RM\}$  to capture any skill constraints that restrict worker mobility between occupation pairs.<sup>20</sup> The parameter  $\alpha_0$  is a scaling factor to guarantee the proper arrival rates, but does not play a role in the marginal choice of search direction. In Online Appendix D we provide a more detailed derivation of (6) and its relationship with the more used Gumbel-distributed random utility model.

Finally, we assume that per period earnings follow a standard Mincer formulation,

$$\log w_{o,t} = \gamma_w \log w_{o,t-1} + (1 - \gamma_w)(A_t + \tilde{p}_o + p_{o,t} + x_h + z_t + \epsilon_t), \quad (7)$$

where  $\gamma_w \in [0, 1]$  captures the extent of stickiness such that with probability  $\gamma_w$  the current earnings remains the same as last period's earnings. Annual earnings are then obtained by summing up monthly earnings, taking into account that during periods of unemployment the worker receives earnings of zero. Note, however, that the job acceptance and occupational mobility decisions of the unemployed depend on the per period payoff when unemployed  $b$ .<sup>21</sup>

<sup>20</sup>For example, it seems unlikely that many workers in *RM* jobs will end up in *NRC* jobs even if the latter occupations offer a much higher average pay.

<sup>21</sup>Given that the formulation of earnings described in (7) implies that past earnings affect workers' job acceptance and reallocation decisions, in the estimation we include earnings in the state space when solving the value functions described in Section 3. As it will be shown, however, we estimate a small value for  $\gamma_w$ , such that past earnings have little effect in practise on workers' mobility decisions.

## 4.2 Estimation

The above functional forms yield several parameters to estimate comprised of: the set that governs the arrival of job opportunities  $\{\lambda_{0,i}, \lambda_{1,i}, \lambda_{0,i}^c, \lambda_{1,i}^c\}_{i=U,E}$ , the set  $\{\delta_{0,z}, \delta_{1,z}, \rho_z, \nu_z, \sigma_z, \omega_z, z_A, \bar{z}, \underline{z}\}$  that governs the idiosyncratic worker-occupation productivities, the set  $\{\delta_{0,\epsilon}, \delta_{1,\epsilon}, \eta, \sigma_\epsilon, lt_\epsilon, rt_\epsilon, \omega_\epsilon, \epsilon_A, \bar{\epsilon}, \underline{\epsilon}\}$  that governs the idiosyncratic worker-employer productivities, the set  $\{\rho_p, \sigma_p, \tilde{p}_{NRC}, \tilde{p}_{RC}, \tilde{p}_{NRM}, \tilde{p}_{RM}\}$  that governs the occupation-wide productivities, the set of occupational human capital accumulation  $\{x_1, x_2, \chi(x_2)\}$  and the set of directional parameters across occupations  $\{\alpha_0, \alpha_1^U, \alpha_1^E, \alpha_{NRC}, \alpha_{NRM}, \alpha_{RM}, \alpha_{NRM}\}$ , and finally, the set that governs the aggregate productivity process and payments  $\{\gamma_w, b\}$ .

To ease computational burden we first normalise  $x_1$  to one, set  $\chi(x_2)$  such that human capital accumulation occurs on average after 5 years of occupational tenure and choose  $x_2$  to match the 12% 5-year returns to occupational tenure reported by Kambourov and Manovskii (2009b).<sup>[22]</sup> We also set  $b = 0.4$  to match a 40% replacement ratio (see Shimer, 2005). The aggregate productivity process parameters are set to the values of the autocorrelation and unconditional variance of output per worker as observed in the US during the period of study, similar to Shimer (2005), such that its persistence is 0.9580 and variance is 0.0090.<sup>[23]</sup> We also set  $\bar{z} = \bar{\epsilon} = 3$  and  $\underline{z} = \underline{\epsilon} = -3$  to generate the idiosyncratic productivity grid.

After fixing the above parameters we recover the remainder ones following a two-step procedure in which we split the parameter set between an inner and outer loop. Given values for the outer loop parameters, we can directly calibrate those in the inner loop such that their values match *exactly* the targeted moments. The inner loop contains the productivity levels  $\bar{p}_o$  which we set to match the task-based occupation fixed effects, where the regression to obtain these fixed effects in the simulated data is exactly the same as the one used to residualize earnings in Section 2. This loop also contains the directional parameters of the  $\alpha(\cdot)$  function,  $\alpha_{NRC}$ ,  $\alpha_{RC}$ ,  $\alpha_{NRM}$  and  $\alpha_{RM}$ . These are set to match the relative contribution of each occupation  $o$  on total net flows.<sup>[24]</sup> We then iterate on the values of the remaining (outer loop) parameters using simulated method of moments, adjusting the inner loop parameters at each iteration. The outer loop parameters are obtained as the solution to

$$\text{Min}(\mathbf{M}^D - \mathbf{M}^S(\cdot))' \mathcal{W}(\mathbf{M}^D - \mathbf{M}^S(\cdot)),$$

where  $\mathbf{M}^D$  is a vector of data moments,  $\mathbf{M}^S(\cdot)$  is a vector of the same moments obtained from model simulations, which are a function of the parameters to estimate as described above, and  $\mathcal{W}$  is a

<sup>22</sup>The returns to occupational tenure correspond to the IV estimates of Kambourov and Manovskii (2009). Since we parametrise the returns to occupational human capital outside the simulation minimum distance procedure, we chose to target the IV estimates as they already control for the endogeneity bias present in the OLS returns.

<sup>23</sup>Shimer (2005) uses the full post-war time period, which has the advantage of a longer time-series. While the process is different when considering the 80's onwards, using either one does not affect our conclusions. These data is available at a quarterly frequency from FRED, so we convert it to a monthly process, consistent with our simulation procedure.

<sup>24</sup>Total net flows are calculated as the absolute value of the difference between inflows and outflows per occupation, summed up over all occupations, and divided by two as one person net inflow in some occupation is also counted as a net outflow some other occupation. Hence, the relative contribution of occupation  $o$  on total net flows is given by  $\frac{|Inflow_o - Outflow_o|}{\sum_{o \in O} |Inflow_o - Outflow_o|}$ .

weighting matrix.<sup>25</sup>

**Targeted moments** Table 1 and Figure 6 present the set of data moments  $M^D$  to estimate the outer loop parameters, which consist of transition flows and productivity moments and percentiles describing 6 (cross-sectional) earnings growth distributions, conditioning on employer and occupation transitions. We now present some heuristic identification arguments that justify our choice of moments, keeping in mind that all parameters need to be estimated jointly. In Online Appendix D we present a graphical representation of the identification of these parameters by evaluating the loss function at the optimal and showing its change in value as we perturbate each parameter in turn.

The parameters governing the arrival probabilities of employment opportunities are informed by the observed transitions probabilities across employers and occupations. In particular, the arrival probability of job offers among occupational stayers,  $\lambda_{0,U}$ ,  $\lambda_{0,E}$  and  $\delta_{0,\epsilon}$  are informed by the average  $UE$ ,  $EE$  and  $EU$  transition rates. The cyclical ratio of the  $UE$ ,  $EE$  and  $EU$  rates inform the cyclical components of these offer arrival probabilities,  $\lambda_{1,U}$ ,  $\lambda_{1,E}$  and  $\delta_{1,\epsilon}$ . Similarly, the arrival probabilities of offers among occupational movers,  $\lambda_{0,U}^c$ ,  $\lambda_{0,E}^c$ , are informed by the average probabilities of an occupational change conditional on the worker's labour market transition,  $EE$ ,  $EUE$  or employer stayer. The parameters  $\lambda_{1,U}^c$ ,  $\lambda_{1,E}^c$  are then informed by the cyclical ratios of the occupational change probability through a  $EE$  and  $EUE$  transition. The ratio of the average unemployment duration among occupational movers and stayers further helps inform unemployed workers offer arrival probabilities.

To inform the curvature parameters  $\alpha_1^U$ ,  $\alpha_1^E$ , we use the variance of the distribution of net flows conditioning on whether the occupation switch occurred through a  $EUE$  or  $EE$  transition. Since the functional form of  $\alpha(\cdot)$  implies that a higher (lower) value of  $\alpha_1^i$  leads to workers searching more (less) randomly, one obtains a negative relationship between  $\alpha_1^i$  and the differences in each occupation's net flows. We measure dispersion in the latter through the variance of the distribution of these net flows. The shift parameter  $\alpha_0$  helps determine the level of occupational mobility and hence it is informed by the average occupational change probabilities conditional on workers' employment transition.

To inform the idiosyncratic worker-occupation match productivity process we use the earnings growth distributions of occupational movers. These are separated by whether workers made the occupational change through a  $EE$ ,  $EUE$  or within employer transition as depicted in Figure 6. For each of these distributions we target the 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup> and 90<sup>th</sup> percentile. In particular, the earnings losses observed upon an occupational transition through unemployment help inform  $\delta_0^z$  and  $\delta_1^z$ , the obsolescence shock parameters governing job loss with a forced occupational move: very large earnings losses among occupational movers imply forced moves because they are driven by high  $z$  match individuals who otherwise are unlikely to search outside of their current occupation. The earnings losses of those who changed occupations within their employers or through a  $EE$  transition also help to inform  $\omega_z$  and  $z_A$ , the parameters that shift  $F(\cdot)$ , as it is in recessions where we observe more of these losses. To further inform these parameters we also target the cyclical change

<sup>25</sup>Our weighting matrix aims to accomplish two key features: (i) normalise to the same scale the transition probabilities and their ratios over the business cycle; (ii) emphasis the role of the earnings change distributions in the minimisation procedure.

Table 1: Targeted moments in the estimation

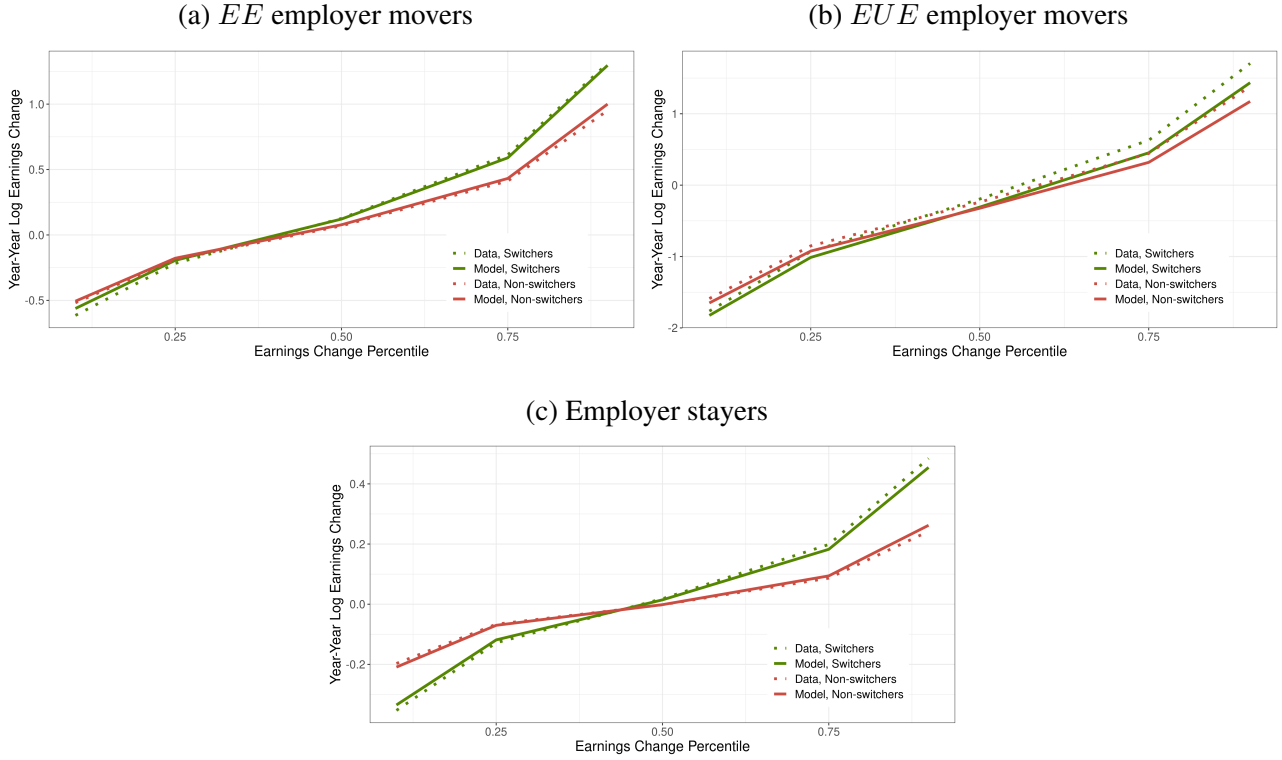
Moment	Model	Data	Moment	Model	Data
<b>Employer Switching</b>					
EE transition prob	0.0296	0.0340 (0.0003)	EE rate - expansion/recession ratio	1.1600	1.1846 (0.0469)
UE transition prob	0.3492	0.3947 (0.0025)	UE rate - expansion/recession ratio	1.0874	1.0876 (0.0244)
EU transition prob	0.0236	0.0223 (0.0002)	EU rate - expansion/recession ratio	0.7437	0.7460 (0.0333)
<b>Occupation Switching</b>					
Prob (Occ. change   EE)	0.3107	0.2685 (0.0037)	Prob (Occ. change   EE) - exp/rec ratio	1.1068	1.1068 (0.0196)
Prob (Occ. change   EUE)	0.2867	0.2892 (0.0034)	Prob (Occ. change   EUE) - exp/rec ratio	1.0670	1.0709 (0.0132)
U duration - Occ. movers/stayers ratio	1.2280	1.2709 (0.0215)	Prob (Occ. change   Stayer)	0.0101	0.0107 (0.0002)
Variance (Net flows   EE)	0.0293	0.0223 (0.0008)	Variance (Net flows   EUE)	0.0235	0.0218 (0.0012)
Net flow to NRC	0.1849	0.1851	Net flow to RC	0.3395	0.3432
Net flow to NRM	0.2209	0.2201	Net flow to RM	0.2547	0.2516
<b>Productivities</b>					
NRC wage fixed effect	1.000	1.000	RC wage fixed effect	0.767	0.767
NRM wage fixed effect	0.608	0.608	RM wage fixed effect	0.803	0.803

Note: Bootstrapped standard errors in parenthesis for the moments used in the outer loop.

of the earnings growth distribution as depicted in Figure 1d. In this case we target the  $2.5^{th}$ ,  $5^{th}$ ,  $10^{th}$ ,  $25^{th}$ ,  $50^{th}$ ,  $75^{th}$ ,  $90^{th}$ ,  $95^{th}$ ,  $97.5^{th}$  percentiles. The shape and scale of the  $F(\cdot)$  distribution,  $\nu_z$  and  $\sigma_z$ , and the persistence of the  $z$ -productivity process,  $\rho_z$  are informed by the remaining percentiles of the conditional earnings growth distributions of occupational movers. We also use these earnings growth distributions to recover the parameters of the occupation-wide productivity processes,  $\rho_p$  and  $\sigma_p$ . In particular we use the earnings growth distribution of those workers who changed occupations within their employers.

For the parameters governing the idiosyncratic worker-firm match productivities we use the earnings growth distributions of occupational stayers. The earnings losses of  $EE$  employer movers inform  $lt_\epsilon$ , the left tail parameter of  $\Gamma(\cdot)$ , and the rate at which employed workers are forced to move employers within their occupations,  $\eta$ . The earnings losses among  $EUE$  employer movers inform  $\omega_\epsilon$  and  $\epsilon_A$ , which shift  $\Gamma(\cdot)$ . As above we also use the cyclical change of the earnings growth distribution to inform these parameters. The earnings gains of  $EE$  and  $EUE$  employer movers then inform  $\sigma_\epsilon$  and  $rt_\epsilon$ , the variance and the shape of the upper tail of  $\Gamma(\cdot)$ . To inform the wage stickiness parameter,  $\gamma_w$ , we rely on the earnings growth distribution of those workers who did not change occupations or employers, especially the centre of this distribution.

Figure 6: Model fit for the conditional cross-sectional earnings growth distributions (cdf)



Note: The earnings growth distribution is computed separately for *EE* and *EUE* employer movers and employer stayers conditional on whether the worker switched occupation or not. Each graph present these distribution by showing the annual earnings growth value and the corresponding percentile. Our estimation targets the 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup> and 90<sup>th</sup> percentiles of each of these distributions. In Online Appendix D we present the bootstrapped standard errors for these moments.

**Parameter estimates** Table 2 reports the estimated parameter values. As implied by their simulated standard errors, these parameters are precisely estimated (see also Online Appendix D). The estimated job offer arrival probabilities among workers searching for jobs in their current occupation,  $\lambda_{0,U}$ ,  $\lambda_{1,U}$ ,  $\lambda_{0,E}$  and  $\lambda_{1,E}$ , together with their job acceptance decisions, capture the behaviour of the *UE* and *EE* transitions probabilities among occupational stayers. If a worker decides to search across occupations, he faces a job arrival probability with parameters  $\lambda_{0,U}^c$ ,  $\lambda_{1,U}^c$  or  $\lambda_{0,E}^c$ ,  $\lambda_{1,E}^c$  until a job is found. These values together with workers' search direction and job acceptance choices determine the *UE* and *EE* transitions probabilities among occupational movers. Indeed, the reason why we find a stronger procyclicality of occupational movers' arrival probabilities is because they have to be scaled by the parameters of the  $\alpha$  function, which are less than one, to match the observed transition probabilities. Overall, the model is consistent with the observed procyclical behaviour of the aggregate *UE* and *EE* transition probabilities and the occupational mobility probabilities observed along the four task-based occupational categories we consider.<sup>26</sup>

<sup>26</sup>The estimated value of  $\lambda_1^U$  implies that the offer arrival probability of unemployed workers decreases in expansions among occupational stayers. This occurs as the estimation procedure uses this parameter to help match not only the cyclicity of the aggregate *UE* rate, but also to reproduce the cyclical change in the 2.5 percentile of the aggregate earnings growth distributions, which is largely affected by the cyclicity of the earnings distribution for *EUE* transitions. By setting this parameter to zero (i.e. no cyclical change in the job finding probability of occupational stayers), for example, we worsen the fit of the model in this dimension by a factor of five, generating much larger earnings losses than



Table 2: Estimated parameter values

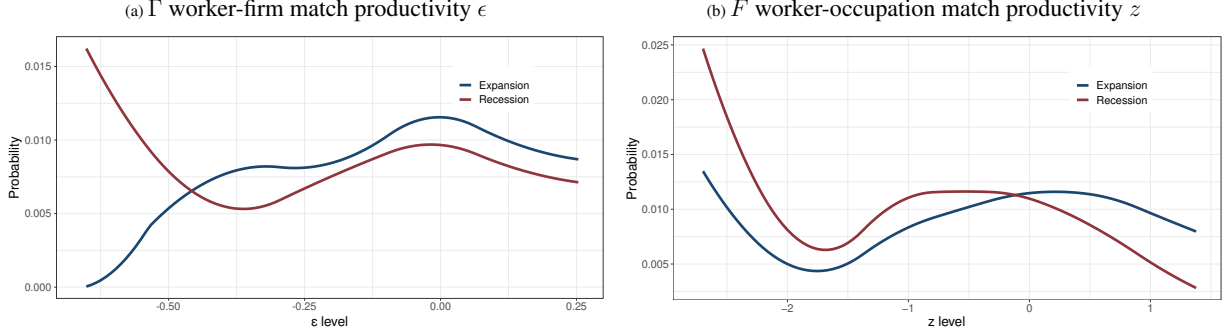
Job offer arrival				Employer-match productivities				Occupation-match productivities			
$\lambda_{0,U}$	0.8701 (0.0002)	$\lambda_{0,E}$	0.0935 (5.33E-05)	$\delta_{0,\epsilon}$	0.0025 (4.25E-06)	$lt_\epsilon$	3.4350 (0.0010)	$\delta_{0,z}$	0.0084 (4.25E-06)	$\nu_z$	7.7603 (0.0019)
$\lambda_{1,U}$	0.7051 (0.0002)	$\lambda_{1,E}$	0.1854 (7.44E-05)	$\delta_{1,\epsilon}$	0.0002 (2.38E-06)	$rt_\epsilon$	1.4356 (0.0007)	$\delta_{1,z}$	0.0030 (4.23E-06)	$\sigma_z$	6.593 (0.0013)
$\lambda_{0,U}^c$	0.1669 (0.0002)	$\lambda_{0,E}^c$	0.0171 (5.33E-05)	$\eta$	0.2763 (0.0002)	$\omega_\epsilon$	0.9952 (0.0001)	$\rho_z$	0.0070 (1.95E-05)	$\omega_z$	0.7573 (0.0002)
$\lambda_{1,U}^c$	0.5746 (0.0002)	$\lambda_{1,E}^c$	0.1716 (7.44E-05)	$\sigma_\epsilon$	0.0347 (2.11E-05)	$\epsilon_A$	-0.3076 (0.0004)			$z_A$	-0.7180 (0.0004)
Search direction across occupations				Occupation-wide productivities				Payments			
$\alpha_0$	0.0403 (4.20E-05)	$\alpha_{NRC}$	-0.4696	$\rho_p$	0.6168 (0.0001)	$\tilde{p}_{NRC}$	0 (normalize)	$\gamma_w$	0.0949 (2.11E-05)		
$\alpha_1^U$	0.1398 (0.0002)	$\alpha_{RC}$	0.5541	$\sigma_p$	0.0016 (5.22E-06)	$\tilde{p}_{RC}$	-0.2658				
$\alpha_1^E$	0.2990 (0.0002)	$\alpha_{NRM}$	-0.1796			$\tilde{p}_{NRM}$	-0.4976				
		$\alpha_{RM}$	-0.0844			$\tilde{p}_{RM}$	-0.2189				

Note: Standard errors in parenthesis only correspond to the outer loop parameters. See Appendix D for details.

Figure 7 depicts the density of the  $\Gamma(\cdot)$  and  $F(\cdot)$  distributions implied by the estimated parameters governing the worker-firm match productivity  $\epsilon$  and worker-occupation match productivity  $z$  in expansions and recessions. During recessions workers are more likely to draw from worse match productivities when starting in new employers and occupations. During expansion workers are more likely to draw better match productivities. This result is consistent with evidence that shows that during recession new worker-job matches worsen relative to expansions (see Moscarini, 2001). As we will demonstrate later, these cyclical changes in the productivities of new jobs contribute to the cyclical changes in the earnings growth distributions of employer/occupational movers as documented in Section 2. Another important characteristic of these distributions is that worker-occupation match productivities are estimated to be more dispersed than worker-firm match productivities, with variance of 1.041 and 0.585 expansions and of 1.085 and 0.540 in recessions, respectively, and an equal mean normalised to zero. This feature captures the increased earnings risk among occupational movers documented in Section 2. The parameters  $\gamma$  and  $\rho_z$  control how often workers move along the  $\Gamma(\cdot)$  and  $F(\cdot)$  distributions, such that with probability  $1 - \gamma$  the worker is forced to change employer and draw a new  $\epsilon$  and with probability  $\rho_z$  the worker draws a new  $z$ . Table 2 shows that re-draws of  $\epsilon$  are about four times more likely than re-draws of  $z$ , suggesting that involuntary  $EE$  transitions are far more likely than changes in occupation match productivities.

The probability of falling from the  $\Gamma(\cdot)$  and  $F(\cdot)$  distributions are controlled by  $\delta_{0,\epsilon}$ ,  $\delta_{1,\epsilon}$  and  $\delta_{0,z}$ ,  $\delta_{1,z}$ . As in the data, the probability of an  $EU$  transition increases in recessions because workers lose either their firm match or occupation match productivities more often than in expansions. The estimated values imply that workers fall about four times more frequently from  $F(\cdot)$  than from  $\Gamma(\cdot)$  during recessions. As demonstrated later, these shocks generate large earnings losses, particularly in the data during recessions.

Figure 7: The estimated  $\Gamma$  and  $F$  densities



among forced occupational movers, as workers at the top of the earnings distribution lose their positions and must start searching for jobs from unemployment.

The  $\alpha(\cdot)$  function parameters imply that workers' search across occupations is not fully directed in response to differences in occupation-wide productivities. As discussed in the previous sections, the value of  $\alpha_1$  controls the degree of directness such that a higher value implies that search is less directed. Table 2 shows that employed workers direct their search more than unemployed workers as  $\alpha_1^U > \alpha_1^E$ . An alternative way to evaluate the degree of directness is by using the effort exerted in searching for jobs in a given occupations, as this choice takes into account the frequency at which unemployed and employed workers encounter job opportunities. In this case, fully random search would arise when a worker targets all remaining occupations with an equal effort of  $1/3$ ; while fully directed search occurs when the worker exert all his effort in targeting one occupation. A simple measure of directness based on search effort is therefore  $(\max s_{\tilde{o}} - 1/3)/(1 - 1/3)$ , where  $\tilde{o} \in O^-$ .<sup>27</sup> Using the latter we find that unemployed workers have a directness measure of 20.6%, once again lower than the one for employed workers of 21.9%. We also find that during recessions employed workers decrease their degree of search directness, while unemployed workers increase their search directness.<sup>28</sup>

These measures suggest a mild degree of directness of search across occupations. This occurs due to the importance of the idiosyncratic worker-occupation and worker-firm match components in the overall payoff of new jobs. Since these productivities are randomly drawn from  $F(\cdot)$  and  $\Gamma(\cdot)$ , workers do not differentiate as much between occupations. However, the extent to which individual occupations are targeted heavily depends on the occupation a worker is moving away from. In the estimated model both employed and unemployed workers that leave *RM* occupations have a directness measure of about 31.3% and 29.7%, while those that leave *NRM* occupations a measure of 28.8% and 25.8%. This occurs because *RM* and *NRM* workers mainly target *RC* occupations, which offer the highest chance of drawing a  $z$ -productivity due to the high estimated value of  $\alpha_{RC}$  and offer a sufficiently high  $\tilde{p}$ . On the other hand, workers leaving *RC* and *NRC* do face a stronger trade-off

<sup>27</sup>For unemployed workers we measure  $\max s_{\tilde{o}}$  through the entire unemployment episode, while for employed workers we measure it just before the *EE* transition. In both cases we aggregate all data across the business cycle.

<sup>28</sup>However, the cyclicity on this measure is very mild. Employed workers increase their search directness from 21.8% to 22.0% from recessions to expansions, while unemployed worker decrease their search directness from 20.5% to 20.7%.

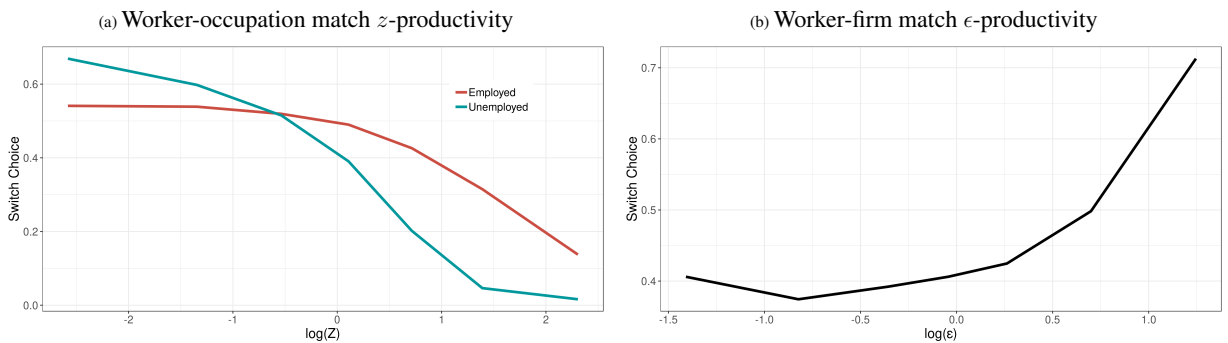


between the  $\alpha_o$  and  $\tilde{p}_o$  and hence they tend to spread more the search, particularly those (employed and unemployed) workers leaving *RC* occupations who show a degree of directness of about 8%.

Finally, we find that occupation-wide productivity shocks are less persistent but more volatile than aggregate productivity shocks. We estimate (real) earnings also to be rather flexible with the stickiness parameter suggesting that earnings remain at their previous level with only a 5% probability every month.

**Occupation and employer switching probabilities** Workers in our model make three key decisions: (i) when to change occupations, (ii) when to change employers, and (iii) when to quit into unemployment. The estimated parameters shape the probability of these events and hence how likely are workers to move along the occupation and employer dimensions of the job ladder. Figure 8a shows that the probability of an occupational change monotonically decrease with workers'  $z$ -productivities. Employed workers in the lower half of the occupation match productivity range face around a 50% probability of an occupational switch every month. For higher values of  $z$  this probability decreases faster reaching around 15% at the highest value of  $z$ . Among the unemployed the probability of an occupational change starts even higher at around 60%, but decreases faster than for employed workers essentially disappearing at the highest productivity level. The reason for the latter is that the worker-firm match productivity also plays an important role in occupational switching among employed workers. Figure 8b shows the relationship between  $\epsilon$  and the probability of occupational switching for employed workers. The positive relationship suggests that  $z$  and  $\epsilon$  can substitute each other as workers move along these two dimensions of the job ladder. That is, workers with higher  $\epsilon$ -productivities exhibit a higher probability of occupational switching when they also face a lower value of  $z$  and vice versa. This highlights that occupational mobility does not necessarily occur more often among those workers lower in the  $\epsilon$  rank.<sup>29</sup> By aggregating across  $z$  and  $\epsilon$  we recover the average occupation and employer switching probabilities shown in Table 1. Endogenous separations into unemployment account for 50.6% of all *EU* transitions and occur at lower levels of  $z$  and  $\epsilon$ , where matches have a lower probability of survival when a negative productivity shock hits the job.

Figure 8: Probabilities of changing occupations

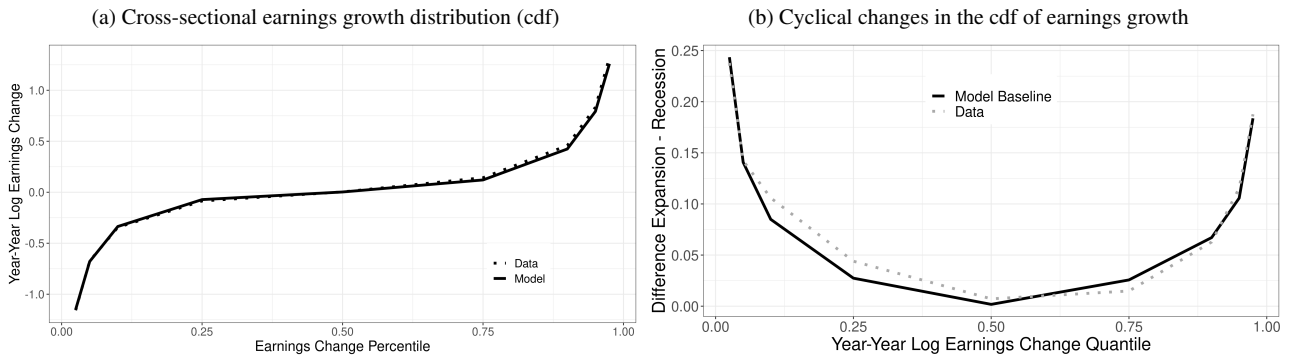


<sup>29</sup> Although not shown here, a similar pattern occurs when relating the probability of an employer change to  $\epsilon$  and  $z$ . We obtain that this probability falls monotonically with  $\epsilon$ , but increases with  $z$ .

### 4.3 Model fit

The model fits the data very well, given the amount of over-identification. Table 1 shows that it replicates the worker flow patterns in the cross-section and over the cycle among occupational movers and stayers as well as their search direction across occupations. Figure 6 shows quantile-by-quantile how well our minimum distance estimator does at bringing together the model and data on the cross-sectional cdf of the earnings growth distributions. Figures 6a and 6c show the model matches nearly perfectly the earnings growth distributions of occupational movers and stayers among *EE* employer movers and employer stayers. Figure 6b shows the fit of the earnings growth distribution among *EUE* employer movers is also very good, having slightly more trouble replicating these workers' earnings gains than their earnings losses. Note that aggregating within type of employer transitions recovers the earnings growth distributions depicted in Figure 1c in Section 2. Figure 9a then shows that when aggregating these conditional earnings growth distributions the model matches nearly perfectly the cdf of the observed cross-sectional earnings growth distribution, as depicted in Figure 1b in Section 2, even below the 10<sup>th</sup> and above the 90<sup>th</sup> percentiles which were not targeted.

Figure 9: Earnings growth distribution in the cross-section and over the cycle - model and data

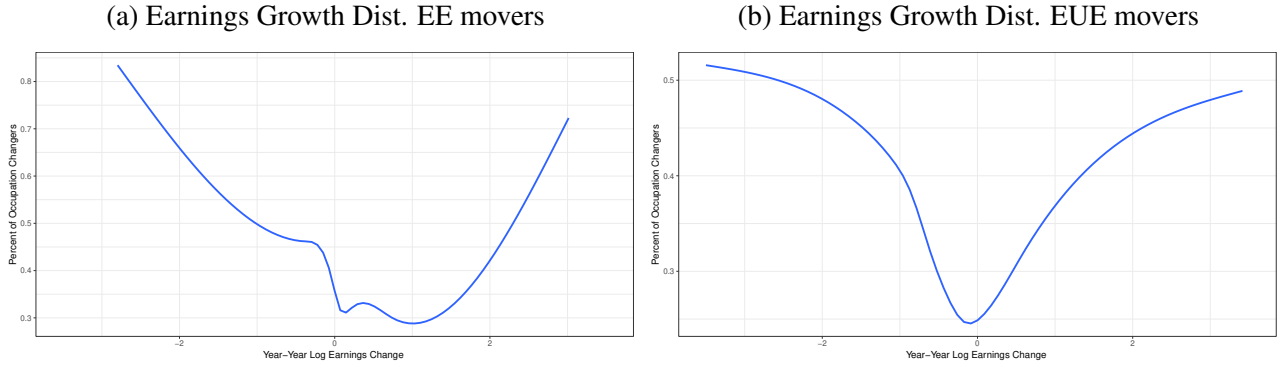


Note: The observed annual earnings growth distribution is constructed for the sample period 1990-2013. The left panel shows the cross-sectional earnings growth distribution (cdf) by plotting the associated earnings change to each selected percentile of the distribution. The percentiles used are 2.5<sup>th</sup>, 5<sup>th</sup>, 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup>, 90<sup>th</sup>, 95<sup>th</sup>, 97.5<sup>th</sup>. The simulated distribution are constructed in the same way as in the data. The right panel shows the difference between the expansion and recessions earnings growth distributions as documented in Section 2, where we targeted the 2.5<sup>th</sup>, 5<sup>th</sup>, 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup>, 90<sup>th</sup>, 95<sup>th</sup>, 97.5<sup>th</sup> percentiles.

The importance of occupation mobility in the tails of the cross-sectional earnings growth distribution can be observed when considering the model counterpart to the untargeted relationship between earnings growth and occupation mobility as depicted in Figure 2, Section 2. This figure documents that occupational movers contribute disproportionately to the largest changes in earnings, both positive and negative. In the model the relationship between earnings growth and occupation mobility among all workers is partially a result of the relatively fixed wages of the majority of employer/occupation stayers. It is less clear, however, that the model will be able to obtain the higher probability of occupational switching among those with the largest earnings changes when conditioning on *EE* or *EUE* transitions. There, the effect of drawing a new  $z$ -productivity has to dominate the other shock processes that drive extreme earnings changes, such as job loss from high on the  $\epsilon$  dimension of the job ladder. Figure 10 shows that this is indeed what happens. Conditional on *EUE*

transitions the relationship between earnings growth and occupational mobility reaches its bottom near the mean of earnings growth, just below zero, as in the data. The same holds for the relationship between earnings growth and occupational mobility conditional on  $EE$  transitions, where the average worker makes an earnings gain. As the earnings growth associated with a particular transition moves away from the middle of the distribution, the chance it involves an occupation switch increases.

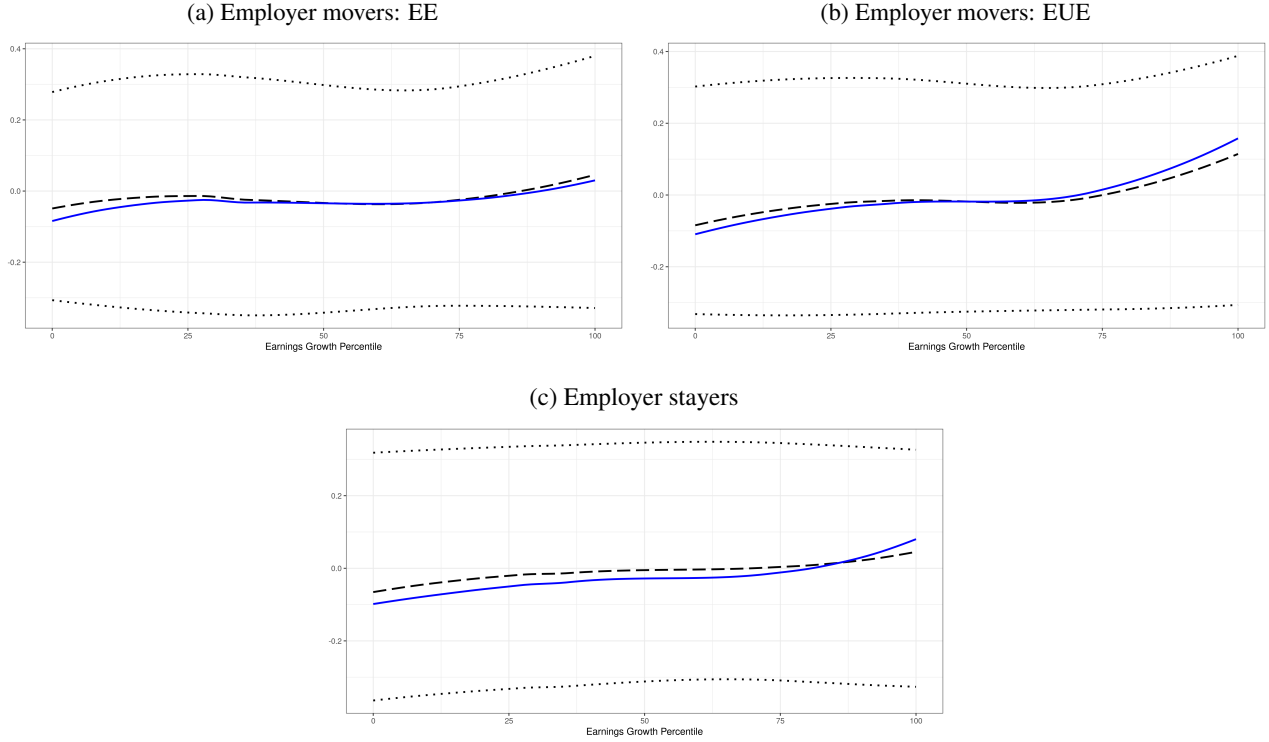
Figure 10: Model counter-part of earnings growth distributions



We can observe the importance of the idiosyncratic  $z$ -productivity relative to occupation-wide productivities in the model by computing the untargeted relationship between occupation fixed effects (occupational ladder) and earnings changes. Figure 11 shows that the model is able to reproduce the large earnings changes associated with larger movements both up or down the occupational ladder, as documented in Figure 3, Section 2. As in our empirical analysis, we compute conditional occupation earnings averages by estimating an earnings regression on a set of dummies for the task-based occupational categories. We treat the coefficients on these dummies as the occupation-specific earnings effect and compute the distribution of the difference between these coefficients at their source and destination occupation at each percentile earnings growth. Occupation-wide productivity differences imply that the mean, median, 90th and 10th percentiles are upward sloping and that workers with higher earnings growth are more likely to move to higher paying occupations. However, as in the data, these slopes are very weak and imply that workers main motive to switch occupation arises from the idiosyncratic worker-occupation match productivity. Moreover, this pattern is present when we focus on employer movers,  $EE$  or  $EUE$ , or employer stayers.

Over the business cycle, Figure 9b compares the targeted difference between the expansion and recession earnings growth distributions in the model and data. As in Figure 1d in Section 2, we condition on a quantile of the earnings growth distribution and then subtract expansion from recession values. Once again the model produces a nearly perfect fit across the distribution. Thus, our model is fully consistent with both the skewness and leptokurtosis of the cross-sectional earnings growth distribution and its prominent procyclical skewness, as well as with the observed worker mobility flows. Further, in Online Appendix D we present the equivalent of Figure 4a in Section 2 but using simulated data from the estimated model. As in the data, it shows that the procyclical skewness of the earnings growth distribution arises from individuals who change occupation and employer at

Figure 11: Model implied occupational ladder



Note: Model-based earnings changes of occupational switchers. Switchers are ranked by their earnings growth in the horizontal axis. For each rank the vertical axis depicts the mean (blue line), median (black line), 90<sup>th</sup> and 10<sup>th</sup> percentiles (dotted lines) of the distribution of the differences in occupational earnings effects.

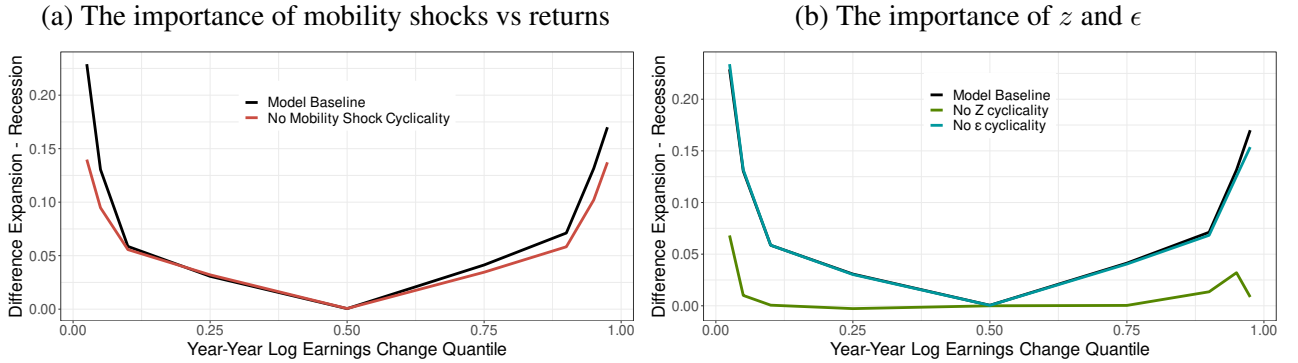
the same time. Also consistent with the data the cyclical change in the earnings growth distribution among employer movers/occupation stayers lies below that of employer/occupation movers and does not exhibit procyclical skewness. The cyclical change in the earnings growth distribution among employer stayers lies further below that of employer movers and also does not exhibit procyclical skewness either for occupation movers or stayers, as in the data.

## 5 Decomposition of Earnings Growth Dispersion Over The Cycle

What are the forces behind earnings growth and what makes it fluctuate over the cycle? To answer these questions we use our estimated model and decompose the cyclical changes in the earnings growth distribution, depicted in Figure 9b. The aim of this decomposition is to understand whether the importance of the occupation and employer components of a job arise from cyclical changes in the returns to mobility as captured by  $F(\cdot)$  and  $\Gamma(\cdot)$ , or from cyclical changes in the mobility shocks captured by the two unemployment (or job loss) probabilities  $\delta_z(A_I)$  and  $\delta_\epsilon(A_I)$  and the four employment (or job finding) probabilities  $\lambda_i(A_I)$  and  $\lambda_i^e(A_I)$ . This decomposition will in turn allows us to evaluate the relative importance of the occupation and employer components of a job in explaining the cyclicity of the earnings growth distribution, taking into account workers' employer and occupation reallocation decisions.

To evaluate the importance of these mobility shocks in relation to the returns to mobility, we perform a counterfactual exercise in which all mobility shocks are set to their expansion levels while returns to mobility are allowed to change between expansions and recessions periods. Figure 12a shows the result of this exercise, where the horizontal axis shows a set of quantiles of the earnings growth distribution and the vertical axis shows the difference in earnings growth at each quantile between expansion and recession as described in Section 2. The red line shows the contribution of (worse) recession returns to the cyclical change in the earnings growth distribution. The residual, the gap between black and red, is then attributed to cyclical changes of the unemployment/employment mobility shock processes. Consider first earnings growth that lie between the 10<sup>th</sup> and 90<sup>th</sup> percentiles of the distribution. Here we observe that nearly all of the changes in these percentiles arise from cyclical changes in returns to mobility. Further out into the bottom and top tails, however, the decomposition shows that mobility shocks have a more prominent role. Below the 10<sup>th</sup> percentile about 50% of the increase in earnings losses during recessions is due to cyclical changes in the mobility shock process. Above the 90<sup>th</sup> percentile up to 25% of the decline in earnings gains during recessions can be also attributed to cyclical changes in the mobility shocks.

Figure 12: Cyclical change in the earnings growth distribution



Note: Each panel shows the difference between the expansion and recessions earnings growth distributions using the 2.5<sup>th</sup>, 5<sup>th</sup>, 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup>, 90<sup>th</sup>, 95<sup>th</sup>, 97.5<sup>th</sup> percentiles. In the left panel we show the impact of holding all the mobility shocks  $\delta_z(A_I)$ ,  $\delta_\epsilon(A_I)$ ,  $\lambda_i(A_I)$  and  $\lambda_i^c(A_I)$  constant at their expansion levels. In the right panel we show the impact of holding the  $F(\cdot)$  or  $\Gamma$  constant at their expansion levels.

## 5.1 Idiosyncratic productivity shocks

Given the importance of changes in the returns to mobility in explaining the the earnings growth distribution over the cycle, we evaluate whether changes in  $F(\cdot)$  or  $\Gamma(\cdot)$  drive this result. Figure 12b shows the model's baseline fit and two counterfactuals, where either  $F(\cdot)$  or  $\Gamma(\cdot)$  are held at their expansions levels. For each counterfactual we let the remainder distribution and mobility shocks vary over the cycle as in the baseline estimation.

This counterfactual exercises demonstrate that worker-occupation match productivities are much more important in accounting for the cyclical change of the earnings growth distribution than worker-firm match productivities. Restricting the  $z$ -productivity distribution to be constant over the cycle,

significantly decreases the difference between the expansion and recessions earnings changes. Figure 12b shows that returns to idiosyncratic occupational mobility explains all the difference between expansions and recessions in the interquartile range. These returns also explain nearly all of what can be attributed to overall returns in both tails. In contrast, when restricting the  $\epsilon$ -productivity distribution to be constant over the cycle, the model hardly suffers in its ability to generate the difference between the expansion and recessions earnings changes.

## 5.2 Job loss and job finding

The above analysis demonstrates that the ability of mobility shocks to generate cyclical changes in earnings growth arises from its impact on the left and right tails of the earnings growth distribution, particularly the left tail. We now consider this feature further by investigating what type of mobility shocks are the major contributors in each of these tails. If workers' choices played no role in determining the measure of workers across employers and occupations, we could simply turn off the cyclical elasticity parameters of the mobility shocks one at a time and compare the earnings growth distributions with and without them. Instead, however, since different workers in our model respond to the different unemployment/employment shocks differently, the outcomes of the model are not linear in the cyclicalities of these shocks, but instead there are non-trivial interactions between each of them and the associated returns. The solution to this problem is to use a Shapley-Owen decomposition, in which we take every combination of turning on and off the cyclical elasticities and then attribute to each shock its average effect. In this decomposition we still allow for cyclical changes in  $F(\cdot)$  and  $\Gamma(\cdot)$  along with the aggregate and occupation-wide shocks.

With the six cyclical elasticities of the mobility shocks, there are a total of 61 combinations of counterfactuals we need to evaluate in which all but one element of the mobility shocks are set constant at their expansion levels and the remainder is allowed to change between expansion and recessions periods as in the baseline estimation. To make these experiments explicit, define  $\Lambda(\mathbb{I})$  as a function that takes a vector of indicators and gives a vector of mobility shocks. If all the indicators of the vector's elements are set to zero, the function  $\Lambda(\mathbb{I})$  gives the values of the mobility shocks at their expansion values, thus not allowing the mobility shocks to change over the cycle. However, if the  $i^{th}$  element of the vector of indicators is set to one, then  $\Lambda(\mathbb{I})$  implies that the mobility shock associated with  $i$  is allowed to vary with the cycle. Let  $\tilde{G}_R(\Delta w|\Lambda(\mathbb{I}))$  denote the distribution of earnings growth in all recession periods given  $\Lambda(\mathbb{I})$  and  $\tilde{G}_E(\Delta w|\Lambda(\mathbb{I}))$  denote the distribution of earnings growth in all expansion periods given  $\Lambda(\mathbb{I})$ . We then can evaluate counterfactuals with  $\Lambda(\mathbb{I})$  for every combination of indicators, and each time storing  $\tilde{G}_R(\Delta w|\Lambda)$ ,  $\tilde{G}_E(\Delta w|\Lambda)$  and computing their difference. Notice that these counterfactuals not only affect the mobility shocks, but also the value functions and hence the workers' mobility choices.

The top row of Table 3 presents the baseline model's difference between the expansion and recession earnings growth distributions. The final row, labeled "Total" is the portion of this that is attributed to the cyclicalities of all mobility shocks. That is, it is the wedge between the black and the red lines

Table 3: Contribution of cyclical mobility shocks in the tails

Quantile	0.025	0.05	0.10	0.90	0.95	0.975
Expansion - Recession (model)	0.229	0.131	0.059	0.071	0.132	0.170
<i>Contribution of cyclical mobility shocks</i>						
Occupation loss, $\delta_z$	0.122	0.061	0.020	-0.003	-0.007	-0.029
Employer loss, $\delta_\epsilon$	0.012	0.010	0.001	0.000	-0.001	-0.002
Unemp. occ. movers job finding, $\lambda_U^c$	-0.007	-0.005	-0.002	-0.001	-0.002	-0.008
Unemp. occ. stayers job finding, $\lambda_U$	0.001	0.001	0.001	-0.001	-0.003	-0.006
Emp. occ. movers job finding, $\lambda_E^c$	-0.009	-0.007	-0.003	0.011	0.023	0.044
Emp. occ. stayers job finding, $\lambda_E$	-0.029	-0.024	-0.013	0.008	0.019	0.034
Total	0.089	0.036	0.003	0.013	0.029	0.033

on Figure 12a, focusing on the left and right tails. The remainder rows decompose this difference at various quantiles by the impact each individual mobility shock has in creating the wedge such that all rows add to the final row's total.

The decomposition shows that cyclical changes in the probability of job loss makes the mobility shocks account for about half of the cyclical change of the left tail. The job finding probabilities among employed workers, in contrast, contribute in a negative way to earnings losses in this tail, and to some extent offsets the small effect of the unemployed job finding probabilities. This occurs as lower job finding probabilities among the employed during recessions lead to lower  $EE$  transitions. The smaller contribution of unemployed workers' job finding probabilities can be explained by two factors. First, since recessions are relatively short, the timing of re-employment matters. While the increase in separations into unemployment unambiguously increases downside earnings risk, as most of these separators will have been working prior to the recession, the decline in job finding probabilities during recessions might affect these workers (as well as those already unemployed) by increasing their jobless spell.<sup>30</sup> Second, since we are targeting the cyclical change in the average  $UE$  transition rate, we are not fully matching the long tail of the unemployment duration as this is not properly captured by the Poisson process assumed here. This implies that the model is attributing some of the effects of long-term unemployment to cyclical changes in  $F(\cdot)$  and  $\Gamma(\cdot)$ .

Table 3 shows that among the unemployment shocks, the obsolescence  $\delta_z$  shock, which forces employed workers to undergo an occupation switch through unemployment, is by far the most important one. It can explain the entire contribution of the mobility shocks on the left tail of the distribution. In comparison, cyclical changes in job loss due to the destruction of worker-firm match productivity,  $\delta_\epsilon$ , explains a very small portion of the increase in large earnings losses during recessions. Thus, these losses arise mainly from occupations "shutting down" on some workers (particularly those with high earnings), forcing them into unemployment and to switch occupation. The decomposition depicted in Figure 12b shows that upon changing occupations these workers face a worse  $F(\cdot)$  from which to draw  $z$ , contributing the remainder 50% in explaining the large earnings losses among  $EUE$

<sup>30</sup>Note also that  $\lambda_U, \lambda_U^c$  go in opposite directions because  $\lambda_U$  actually increases in recessions, a feature described in Section 4.2



transitions observed in the data during recessions.

At the right tail, Table 3 shows a different picture. In this case the importance of mobility shocks arises from cyclical changes in the job finding probability among employed workers who decided to change occupations. With lower job finding probabilities during recessions, workers have less opportunities to switch employers and occupations at the same time, contributing to the collapse of the right tail of the earnings growth distribution.

## 6 No Occupational Mobility

The analysis presented until now shows the importance of occupational mobility in explaining the cyclical changes in the earnings growth distribution. An important question is whether we need a model that encompasses employer and occupational mobility to simultaneously explain the cross-sectional and cyclical properties of earnings growth distribution *and* worker transition rates. Previous work has shown that a suitable extended version of the canonical on-the-job search model is consistent with the main properties of the cross-sectional earnings growth distribution as depicted in Figure 1 and workers transition rates (see Hubmer, 2018 and Karahan et al., 2020). However, this work does not tackle the cyclical properties of earnings changes or worker transition rates. We now show that without occupational mobility, our job ladder model is not able to reproduce well the *cyclical* properties of the earnings growth distribution as depicted in Figure 1d. By also investigating whether this result is driven by cyclical changes in the returns to employer mobility or in the job loss and job finding probabilities, we show that this job ladder model has very different policy implications relative to our baseline model.

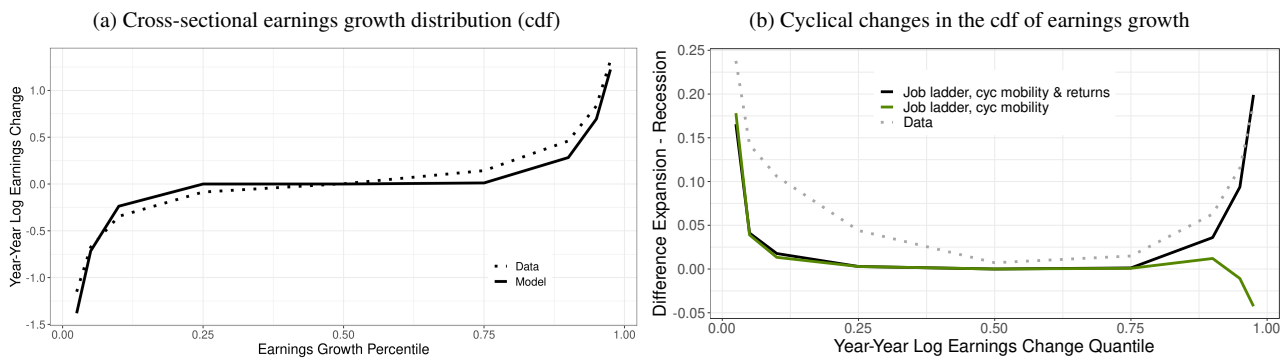
To formalize this exercise we shutdown occupational mobility in the baseline model by eliminating any differences in the  $z$ -productivities across workers and occupation-wide productivities. In this version workers lose their jobs and become unemployed with probability  $\delta(A_I)$ . They encounter job offers from unemployment with probability  $\lambda_U(A_I)$  and draw a match-specific productivity  $\epsilon$  from  $\Gamma(\epsilon, A)$ , which also can change over the cycle. The  $\epsilon$ -productivity maps one-to-one to the earnings associated with such a job offer. When employed, they draw a new  $\epsilon$  with probability  $\lambda_E(A_I)$ . With probability  $\gamma$  the worker decides whether to accept the new job or not; and with probability  $1 - \gamma$  he is forced to accept the new job, as long as it offers a payoff above the value of unemployment.

We structurally estimate such a model using the same moments presented in Section 4, except for those pertaining to occupational mobility. In Online Appendix D we show that this version of our model is able to replicate very well the targeted average  $EE$ ,  $EU$  and  $UE$  transition probabilities as well as their expansion/recessions ratios. Figure 13a show that the model is able also to replicate the cross-sectional earnings growth distribution (as depicted in Figure 1b in Section 2), capturing well its skewness and leptokurtosis, consistent with the results in Hubmer (2018) and Karahan et al. (2020). Underlying this fit, however, our estimation reveals that although the model is able to capture well the targeted earnings growth distribution conditional on  $EE$  employer movers, it fails to capture the targeted earnings growth distributions conditional on  $EUE$  employer movers and



employer stayers (see Online Appendix D). In particular, among *EUE* employer movers the model generates not only larger earnings losses relative to the data, but it hardly generates any earnings gains. This is a consequence of the shape of the estimated  $\Gamma(\cdot)$ , which implies employed workers can climb the job ladder and achieve high values of  $\epsilon$  relatively fast. This feature makes the model consistent with the earnings growth distribution of *EE* movers. However, when these workers fall into unemployment, the estimated  $\Gamma(\cdot)$  implies that at re-employment workers are more likely to draw low values of  $\epsilon$ . Even though these workers might not accept the lowest  $\epsilon$  draws (particularly during recessions), they will still face a higher probability of becoming re-employed in jobs associated with a low  $\epsilon$ . The initial large drop in earnings due to job loss coupled with low re-employment earnings then leads to larger earnings losses and smaller earnings gains among *EUE* workers relative to the data.

Figure 13: Earnings growth distribution implied by the model without occupations



Note: The observed annual earnings growth distribution is constructed for the sample period 1990-2013. The left panel shows the cross-sectional earnings growth cumulative distribution by plotting the associated earnings change to each selected percentile of the distribution. The percentile used are: 2.5, 5, 10, 25, 50, 75, 90, 95, 97.5. We construct the simulated distribution in the same way as done in the data. The right panel shows the difference between the expansion and recessions earnings growth distributions as documented in Section 2. In this case we use the same percentiles as in the cross-sectional distribution.

Figure 13b presents the implications of this model for the targeted cyclical change of the earnings growth distribution. The black curve shows the cyclical changes in the earnings growth distribution when allowing  $\Gamma(\cdot)$  to vary between expansions and recessions as estimated above. The green curve shows the implications when  $\Gamma(\cdot)$  is kept constant at its expansion level; i.e. no cyclical returns to mobility. The first key result of this exercise is that allowing the returns to mobility to change over the cycle is crucial to obtain procyclical skewness in the earnings growth distribution. Otherwise, this model exhibits countercyclical variance, which is counterfactual. The role of a cyclical  $\Gamma(\cdot)$  is important as it resolves two opposing effects. On the one hand, longer unemployment spells in recessions imply annual earnings fall. As workers become re-employed their earnings then increase from a lower base and generate larger earnings growth. On the other hand, more opportunities to make *EE* transitions imply larger earnings growth in expansions. With a constant  $\Gamma(\cdot)$  the effect of workers moving out of unemployment dominates and the model predicts both larger gains and losses in recessions. Allowing  $\Gamma(\cdot)$  to change over the cycle implies the second effect dominates.

The second key result is that even allowing  $\Gamma(\cdot)$  to change over the cycle the model remains far

from the data. Figure 13b shows that it consistently under-predicts the difference in the earnings losses/gains between expansions and recessions, except at the extremes. The lack of fit on this dimension arises as the model is unable to fully resolve a second related trade-off: reproducing the observed worker transitions flows and the earnings growth distribution over the cycle. The main tension arises from the relationship between unemployment and earnings changes. By reproducing the observed  $UE$  transition probability in expansions and recessions, the model already implies a degree of cyclical change in the earnings losses through unemployment. However, the very large gap between the simulated and the data distributions below the median, implies that these recessionary earnings losses are too similar to the ones in expansions. In order to generate larger earnings losses during recessions the model either has to have (i) a steeper  $\epsilon$  ladder, so that when workers fall they do so from higher up in the ladder. However, a steeper  $\epsilon$  ladder comes into tension with the observed earnings changes associated with  $EE$  transitions, which the model is able to reproduce quite well. Alternatively the model has to have (ii) counterfactually long unemployment durations, which comes into tension with the cyclicity of  $UE$  transitions that it also reproduces quite well. As the analysis of Sections 4 and 5 show, the aforementioned trade-off can be fully resolved when we account for occupational mobility in addition to employer mobility. This is because occupational mobility creates an additional source of downside earnings risk which drastically increases in recessions.

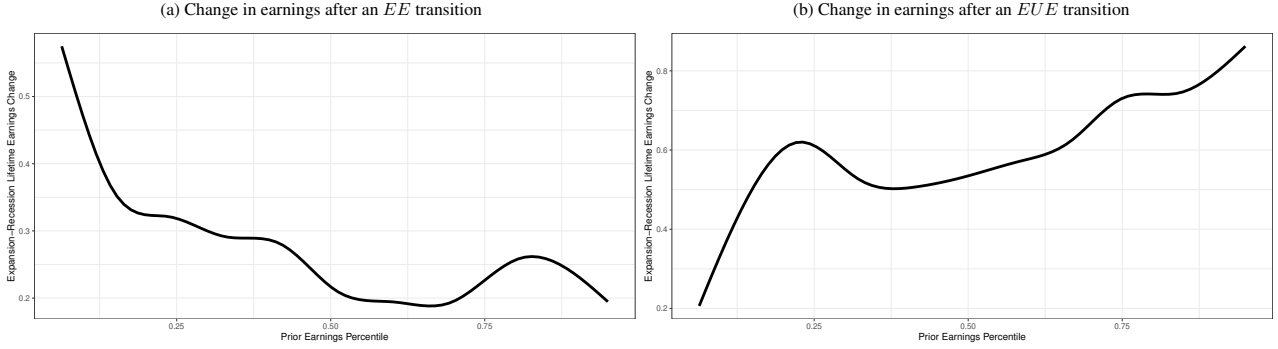
The third key result is that from the viewpoint of the no occupation model the larger earnings losses it generates in recessions arise purely from cyclical changes in the mobility shocks. A similar conclusion can be drawn when considering the (moderately) larger earnings gains it generates in expansions. Figure 13b shows that the cyclical difference in the earnings growth distribution remains nearly unaffected below the 75<sup>th</sup> percentile when not allowing the returns to mobility to change over the cycle. This implication is in contrast with the occupation mobility model where cyclical changes in the returns to mobility explain a large part of the cyclical pattern of the earnings growth distribution. Each model therefore suggest emphasising two very different policy tools for reducing the larger earnings losses during recessions. The no occupation model would favour policies that aim at getting unemployed workers back to work quickly through, for example, reductions in the generosity or length of unemployment insurance payments, like the ones implemented in the UK during the Covid-19 pandemic and in Germany through the Hartz reforms. The occupation mobility model instead would favour policies that aim at improving the job quality individuals can expect at re-employment, through, for example, re-training schemes.

## 7 Sullyng Effects of Recessions

Our model implies that cyclical changes in the returns to mobility and the mobility shocks affect workers differently. For example, by affecting their ability to climb the job ladder during expansions and recessions, workers might suffer differently from the sullyng effects of recessions. The nature of the job ladder in our model implies that those workers with lower earnings are the more likely to make an  $EE$  transition (with or without an occupational move). During recessions this probability

decreases (as  $\lambda_E$  and  $\lambda_E^c$  fall), not allowing them to climb the job ladder as fast as in expansions. In addition, worse returns to mobility also imply that if they manage to change jobs they will expect to draw lower  $\epsilon$  and  $z$  productivities, leading to lower earnings gains relative to expansions.

Figure 14: Changes in lifetime earnings after an  $EE$  and  $EUE$  transition

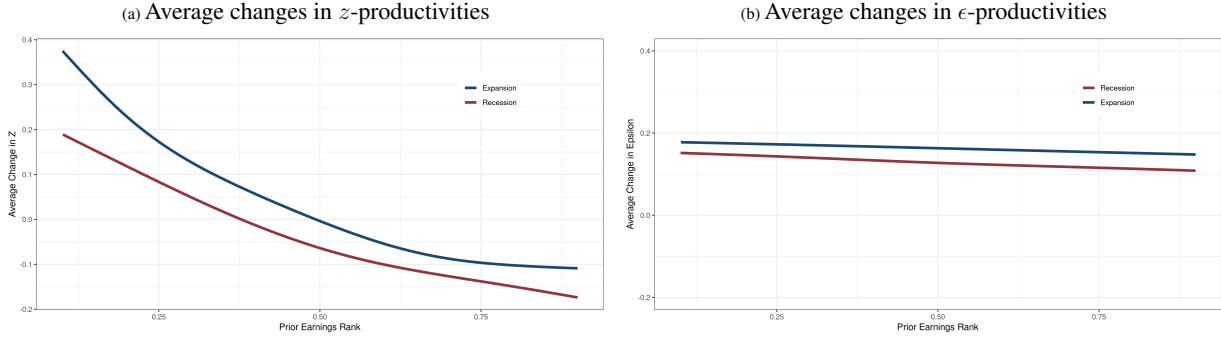


Note: The left panel depicts the expansions and recessions difference of workers' average lifetime earnings prior to an  $EE$  transition and their average lifetime earnings after this transition conditional on a worker's earnings immediately prior the transition. A positive value implies that during expansions workers typically have larger increases in average lifetime earnings after an  $EE$  transition. The right panel present the same exercise but using  $EUE$  transitions instead. A positive value implies that during recessions workers typically have larger losses in average earnings after an  $EUE$  transition.

Our model further implies that this sullyng effect persists over time. To show this implication we compare a worker's average lifetime earnings prior an  $EE$  transition to his average lifetime earnings after the  $EE$  transition. We do this separately for expansions and recessions periods and subtract the two values. Figure 14a shows the result of this exercise conditional on the worker's rank in the earnings distribution immediately prior the  $EE$  transition. The fact that the difference between expansion and recessions is positive across prior earnings percentiles shows that workers who made an  $EE$  transition increased their lifetime earnings more in expansions than in recessions. The fact that this difference decreases with earnings percentiles implies that low-paid workers suffer disproportionately more in terms of lifetime earnings from the sullyng effects of recessions than do high-paid workers.

Figure 15 shows that this occurs mainly through the occupational dimension of the job ladder. Figure 15a presents the average change in  $z$ -productivities due to an  $EE$  transition conditioning on a worker's rank in the earnings distribution immediately prior the  $EE$  transition. Figure 15b shows instead the average change in  $\epsilon$ -productivities. As low-paid (typically low  $z$ ) workers are more willing to switch occupations than higher paid (typically higher  $z$ ) workers (see Figure 8), they are also more sensitive to cyclical changes in the returns to mobility and the mobility shocks, particularly changes in  $F(\cdot)$  and  $\lambda_E^c$ . This implies that during recessions low-paid workers who make an  $EE$  transition will face an average increase in their  $z$ -productivity that is about 15 to 10 percentage points lower than in expansions, while workers with earnings at the top of the distribution face a reduction of about 5 percentage points. This strong differential effect is not present when considering  $\epsilon$ -productivities. Figure 15b shows that although during a recession all workers face a lower average changes in their  $\epsilon$ -productivities after an  $EE$  transition (due to a worsening in  $\Gamma(\cdot)$  and  $\lambda_E$ ), this decrease is small in comparison and there is no meaningful differential effect across the percentiles of the earnings distribution.

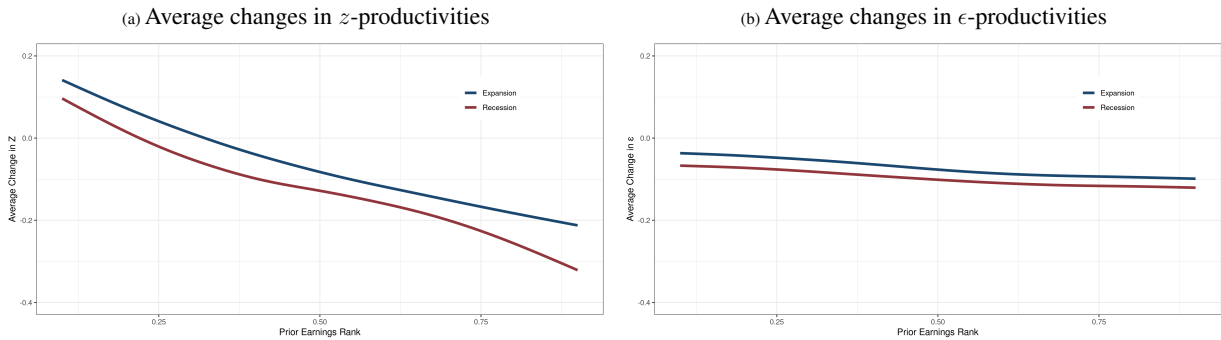
Figure 15: Climbing the job ladder



Note: The left panel depicts the average change in  $z$ -productivities worker obtain after an  $EE$  transition conditional on a worker's earnings immediately prior the transition in recessions and expansions periods. The right panel instead depicts the average change in  $e$ -productivities worker obtain after an  $EE$  transition conditional on a worker's earnings immediately prior the transition in recessions and expansions periods.

Cyclical changes in the returns to mobility and the mobility shocks also affect workers' re-employment outcomes after falling from the job ladder. Figure 14b shows that now it is high-paid workers who suffer disproportionately more in recessions from an  $EUE$  transition than low-paid workers. In this case we plot the difference between expansion and recessions average lifetime earnings losses after changing employers through an unemployment spell. The fact that the difference is positive show that lifetime earnings losses are larger in recessions relative to expansions in line with the results of Davis and Von Wachter (2011) and Huckfeld (2021). The fact that this difference increases with workers' prior earnings percentiles indicates that losses are even stronger during recessions among the high-paid workers.

Figure 16: Falling from the job ladder



Note: The left panel depicts the average change in  $z$ -productivities worker obtain after an  $EUE$  transition conditional on a worker's earnings immediately prior the transition in recessions and expansions periods. The right panel depicts the average change in  $e$ -productivities worker obtain after an  $EUE$  transition conditional on a worker's earnings immediately prior the transition in recessions and expansions periods.

Figure 16 shows these effects once again occur along the occupational dimension of the job ladder. This figure shows the average change in  $z$  and  $e$  productivities after and  $EUE$  transition by a worker's rank in the earnings distribution. The disproportionately worse outcomes of high-paid workers come as a result of forced occupational mobility due to a higher value of  $\delta_z$  and a worsening of  $F(\cdot)$  during recessions. The same argument as above applies: as high-paid (typically high  $z$ ) workers are less likely to change occupations voluntarily, they are more sensitive to a higher prevalence of the ob-

solescence shock and a higher likelihood of drawing a lower value of  $z$  during recessions. Figure 16b shows that this differential effect is not present along the employer dimension, where the worsening in  $\epsilon$  productivities is much smaller and very similar across the percentiles of the earnings distribution.

## 8 Conclusion

In this paper we have studied the structural causes of cyclical earnings risk through the lens of a job ladder model with endogenous occupation and employer mobility. A series of important research has highlighted that higher-order moments of the earnings growth distribution are the most cyclical, that is, the tails of the distribution move the most over the cycle. Thus, crucial to understanding a recession is to understand why largest earnings losses become even worse and top earnings gains become smaller. We document the importance of career changes, seen through occupational mobility, in explaining the tails of the earnings growth distribution. Workers who switch occupations and employers simultaneously have considerably more disparate outcomes in terms of earnings growth, both to the upside and downside and whether through unemployment or directly through an  $EE$  transition.

Recessions bring with them a reduction in the opportunity to find a new employer or to switch careers while simultaneously changing the returns to such transitions. Particularly salient, they bring a larger chance of job loss and a larger chance of job loss that displaces one from his career. These transitions also have different outcomes, for example, making the cost of job loss different in expansions or recessions. Our estimated model shows that changes in the returns to occupation mobility are the main source cyclical earnings risk. Beyond this force, job loss that also comes with career displacement plays an important role in explaining the increase in the larger earnings losses during recessions. During expansion, the increased chances of improving the occupational dimension of a job through direct job-to-job transitions contributes to increasing the largest earnings gains.

Our framework has focused on ex-post worker heterogeneity mostly through differences in idiosyncratic occupation and firm match-specific productivities. Recent work has emphasised instead the role of ex-ante heterogeneity in the probabilities of job loss and job finding among workers. Occupational components, whose importance is the message of this paper, can meaningfully interact with these ex-ante differences. For instance, the interaction can elucidate for which types of workers the cyclical collapse of the career and employer ladder are especially relevant and likewise can clarify the role of career paths to type-level differences. These extensions could be particularly useful to understand the great amount of heterogeneity in workers' experiences of the business cycle, seen both as cyclical changes in worker transition rates and earnings growth.

## Online Appendix

<https://github.com/CTVproject/CTVW/raw/main/CVWOnlineAppendix.pdf>

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# ONLINE APPENDIX

## Appendix A - Data

The Survey of Income and Programme Participation (SIPP) is a longitudinal data set based on a representative sample of the US civilian non-institutionalized population. It is divided into multi-year panels. Each panel comprise a new sample of individuals and is subdivided into four rotation groups. Individuals in a given rotation group are interviewed every four months such that information for each rotation group is collected for each month. At each interview individuals are asked, among other things, about their employment status as well as their occupations, industrial sectors and monthly earnings during employment in the last four months.<sup>31</sup>

The SIPP offers a high frequency interview schedule and aims explicitly at collecting information on worker turnover. Further, its panel dimension allows us to follow workers over time and construct uninterrupted spells of unemployment (or non-employment) that started with an employment to unemployment transitions and ended in a transition to employment. Its panel dimension also allows us to analyse these workers' occupational mobility patterns conditional on unemployment (or non-employment) duration and their post occupational mobility outcomes as outlined in Section 2 in the main text.

### Survey design and use of data

We consider the period 1990 - 2013. To cover this period we use the 1990-1993, 1996, 2001, 2004 and 2008 panels. For the 1990-1993 panels we have used the Full Panel files as the basic data sets, but appended the monthly weights obtained from the individual waves (sometimes referred to as core wave data). Until the 1993 panel we use the occupational information from the core waves. We do this for two reasons: (i) the full panel files do not always have an imputation flag for occupations; and (ii) between the 1990 and 1993 panels firm identities were retrospectively recoded, based on core wave firm identifiers. For the 1996, 2001, 2004 and 2008 panels there is no longer a Full Panel file nor a need for one. One can simply append the individual wave information using the individual identifier "lgtkey" and merge in the person weights of those workers for whom we have information from the entire panel (or an entire year). In this case, the job identifier information is also clearly specified.

The SIPP's sample design implies that in *all* panels the first and last three months have less than four rotation groups and hence a smaller sample size. For this reason we only consider months that have information for all four rotation groups. For individual-level histories, to match occupations after a separation we need to observe re-employment. In unemployment spells, if the separation occurs too close to the end of the panel, we will non-randomly select short unemployment spells. For this reason, we also exclude periods with less than 2 waves remaining until the end of the panel. This restriction is

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<sup>31</sup>See <http://www.census.gov/sipp/> for a detailed description of the data set.

also necessary for us to compute annual earnings growth. Of the remaining observations, we weight them according to the SIPP's person weights, "wpfinwgt".

The data also shows the presence of seams effects between waves, where transitions are more likely to occur at a seam (i.e. between waves, and therefore at 4,8, 12... months) than based on other characteristics, e.g. duration. When we consider time series and given the above restrictions, there is always one rotation at the seam in every month we consider which effectively smooths out the clustering at the seam. In the case of the duration statistics for which the seam effect matters, we consider observations in 4 months bins (e.g. survival at 4, 8, 12, 16 months of unemployment).

## **Sample selection, labour market status and transitions**

For the 1990-2008 panels, we consider all workers between 18 and 65 years of age who are not in self-employment or in the armed forces. We measure an individual's employment transitions in the SIPP using two sources of information. The first one relies on the monthly employment status recode. Using the SIPP 2001 wording as an example, we consider a worker to be employed during a month if the individual reported in the monthly employment status recode variable that he/she was "with a job entire month, worked all weeks", but also when "with a job all month, absent from work without pay 1+ weeks, absences not due to layoff", or "with a job all month, absent from work without pay 1+ weeks, absences due to layoff". If workers have spent part of the month in employment and part of the month in unemployment, workers are nonemployed only if they are nonemployed in week 2 *and* have been nonemployed for at least four weeks in total. That is, those who have less than a month of nonemployment in week 2 are still counted as employed. If the worker is "no job/business - looking for work or on layoff" during one of the weeks in nonemployment (i.e. in the "no job/business") state, we consider the worker to be unemployed. We have chosen this classification, because we want entry into unemployment to capture the serious weakening of the link with the previous firm of employment, rather than to be a definite period of nonproduction after which the worker would return to the previous employer. The restriction of nonemployment for at least four weeks is meant to further limit the role of short-term absences from the same firm and temporary layoffs. This is motivated by the analysis of Fujita and Moscarini (2017), who document that many workers with very short unemployment spells return to their previous employer. We want to focus on those unemployed who at least *consider* employment in other firms and possibly other occupations.

To measure job-to-job transitions we use the second source of information, start and end dates and job numbers. While each employer presumably gets a unique number, the month the job number changes does not necessarily correspond to the timing of the job-to-job change. Further, there are spurious job number changes. So, we corroborate these job number changes with employment end dates. So we require that the individual is fully employed in both adjoining months, but that one of the employment relationships ended and the job number switched in that wave.

## Assigning “source”/“destination” - occupations to unemployed workers

The SIPP collects information on a maximum of two jobs an individual might hold simultaneously. For each of these jobs we have information on, among other things, hours worked, total earnings, 3-digit occupation and 3-digit industry codes. We drop all observations with imputed occupations (and industries). If the individual held two jobs simultaneously, we consider the main job as the one in which the worker spent more hours. We break a possible tie in hours by using total earnings. The job with the highest total earnings will then be considered the main job, though this type of tie is exceedingly rare. Once the main job is identified, the worker is assigned the corresponding two, three or four digit occupation.

Each unemployment spell that is started and finished inside the panel can be assigned a “source”-occupation (main occupation right before the start of the unemployment spell), and a “destination”-occupation (main occupation right after becoming employed again). If the occupation code is missing just before the unemployment spell (e.g. due to imputation) and an occupation code is reported in a previous wave, while employment is continuous from the time that the occupation was reported until the start of the unemployment spell under consideration, we carry the latter occupation forward as source occupation. A worker is an occupation mover if source and destination occupations do not coincide. We thus conservatively count the following situation also as an occupational stay: the worker is simultaneously employed in two firms at the moment the worker becomes unemployed, and finds a job afterwards in an occupation that matches the occupation in one of the two previous jobs, even when it matches the job with less hours. The effect on the occupational mobility statistics of counting as occupational stays the unemployment spells with two simultaneous jobs at either side is small.

We construct the occupational mobility statistics from transitions of the form: at least a month in employment (with a non-imputed occupational code), followed by an unemployment spell which has a duration of at least a month, followed by at least a month in employment (with a non-imputed occupational code). We label these transitions as EUE transitions. We also consider transitions of the form: at least a month in employment (with a non-imputed occupational code), followed by a non-employment spell which has a duration of at least a month and involved at least one month of unemployment. We call these E-NUN-E transitions, or NUN-spells of nonemployment. Further convexifying the space between EUE and E-NUN-E, we also consider spells that started with a EU transition, i.e. employment directly followed by unemployment (though later the worker can report to stop looking for work), and those that ended with UE transition. We label these transitions as E-UN-E, E-NU-E, and if both restrictions apply, E-UNU-E transitions. We also tried other versions of the latter in which the full jobless spell was non-employed (ENE).

**Occupational Classifications** The SIPP uses the Census of Population Occupational System, which relates closely to the Standard Occupational Code (SOC). The 1984-1991 panels use the 1980 Census Occupational classification, while the 1992-1996 and 2001 panels use the 1990 Census Occupational classifications. These two classifications differ only slightly between them. The 2004 and 2008 panels

use the 2000 Census occupational classification, which differs more substantially from the previous classifications. We use the IPUMS recoding of the 1980 and 2000 Census Occupational Classification (very similar to David Dorn’s from Dorn, 2009, and Autor and Dorn, 2013) into the 1990 Census Occupational Classification to have a uniform, 3-digit coding system<sup>32</sup>

From these 3-digit, consistent occupational codes, we aggregate further into two usable groupings, a 2-digit and a 1-digit version. The 2-digit occupational codes correspond to the 22 Standard Occupation Codes, the system that is the federal statistical standard. For our 1-digit codes, we further combine the codes into 4 task-based categories defined by combinations of routine/non-routine and cognitive/non-cognitive. It is well-known that measurement error in occupational codes might give rise to spurious transitions, as discussed for example in Kambourov and Manovskii (2008) and Moscarini and Thomsson (2007). Since 1986 the SIPP interviewing procedure has implied that if the worker declared he/she did not change type of job and employer in a given interview, the occupational code recorded in the previous interview was carried forward. This form of “dependent interviewing” reduces spurious occupational transitions among employer stayers, but coding errors still remain among employer movers. Because we need a particular occupational code to determine an individual observation of an earnings change, we do not use the probabilistic correction methods as in Kambourov and Manovskii (2008). Rather, we use a high degree of aggregation to minimize this coding error. Carrillo-Tudela and Visschers (2021) show that among the employer movers correcting for coding errors when using the four task-based categories will decrease the observed gross occupational mobility rate by about 5 percentage points. Hence the high levels of occupational mobility we observe in the data will remain after correction. Further, to the extent that misclassification bias does not change much over the cycle (as shown in Carrillo-Tudela and Visschers, 2021), coding error will introduce a downward bias to the effect of occupational mobility in explaining the procyclical skewness of the earnings growth distribution. This is because the earnings changes of observed occupational stayers (which are individuals who are very likely to be true stayer) exhibit weak procyclical skewness relative to observed occupational movers. As it is likely that among the latter group there are true occupational stayers due to misclassification, the extent of procyclical skewness among true occupational movers should be higher than the one observed among observe occupational movers.

## Earnings and wages construction

Using the above panels of the SIPP we construct the earnings growth distribution for our sample period. As described in the main text we deflate nominal monthly earnings in the SIPP by the Personal Consumption Expenditure price index. Our measure of earnings is based on the residuals obtained from regressing log real earnings on a quadratic on potential experience, education, and month dummies. In terms of measurement error, note that with occasionally misreported earnings the variance of

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<sup>32</sup>In any of these classifications we have not included the Armed Forces. The 1980 and 1990 classifications can be found at <https://www.census.gov/people/io/files/techpaper2000.pdf>. The 2000 classification can be found in <http://www.bls.gov/soc/socguide.htm>. Additional information about these classifications can be found at <http://www.census.gov/hhes/www/ioindex/faqs.html>.

earnings changes will be biased upwards. This is especially a problem for employer/occupation stayers because true earnings changes are smaller and so the measurement error may be relatively larger. A common method for cleaning earnings dynamics applies time-series break-detection methods, as in Gottschalk (2005) to reject small transitory changes in earnings. The trouble with that method is that it will itself make our earnings process leptokurtic and evidence from administrative data (Kurmman and McEntarfer, 2018) suggest that these small changes are not just erroneous measurement error. Among those workers with interrupted careers, Hudomiet (2015) finds even bigger annual earnings changes in administrative data relative to survey data. This result suggests that the annual earnings changes of *EUE* occupation/employer movers we derive from the SIPP *underestimate* the true scale of earnings changes among this group of individuals.

Given this evidence and following Busch et al. (2021), to clean reporting errors in the residual earnings data we drop the bottom and top 2% of the wave-frequency earnings sample as well as imputed earnings. In less than 1% of the sample, earnings seem to be unrealistically reported in one period because they increase or decrease rapidly and then revert without any other transitions, suggesting a shifted decimal or entry error. We drop these periods, which we define as a change exceeding 200% but which reverts such that the two-period change is less than 10%. When checking for these spurious earnings changes, we allow them if there is an employment status change at either monthly or wave frequency. For both earnings and wages, we aggregate earnings within a wave. This is because seam effects are quite large and so changes are often mistimed within waves. If a worker is non-employed for one of these months, we count that as zero earnings. To construct annual earnings growth, we take the sum of all (residual) monthly earnings observed during the past 3 waves and next two waves from the reference wave. We drop observations in which either the full year prior or the next has earnings below \$1040.

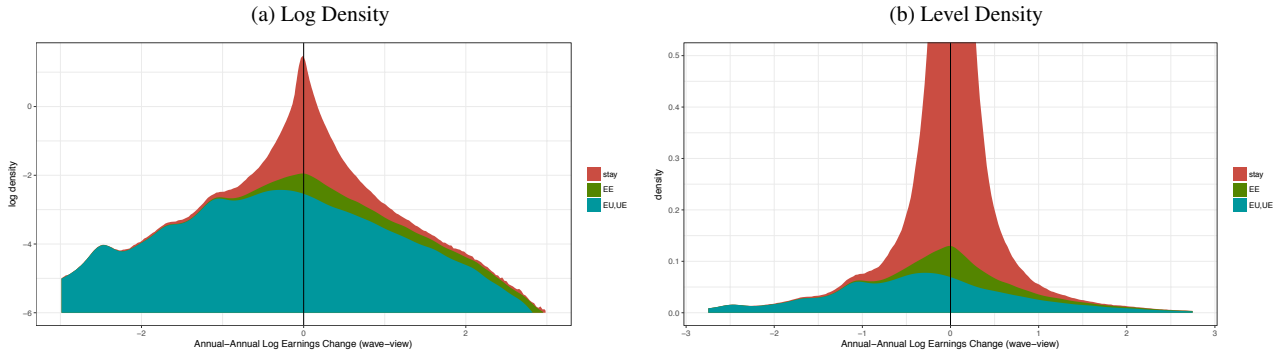
## Appendix B - Additional graphs

### Earnings growth distribution

Figure 1a, Section 2.2 of the main text depicts the derived cross-sectional earnings growth distribution. It shows that this distribution has the well documented properties: left-skewed and leptokurtic. There we present the log density of the earnings growth distribution to highlight its Pareto tails. Figure [1a](#) below depicts the same distribution but instead it stacks the distributions associated with *EUE*, *EE* transitions and employer stayers on top of each other to show the role of each of these transitions in shaping the earnings growth density. Figure [1b](#) shows the same stacked graph but instead using the density level to highlight its leptokurtosis. To show the role of *EE* and *EUE* transitions on the tails of the distribution, we only depict part of the density around zero earnings changes.

Figure [2a](#) shows that the SIPP data is also consistent with the relationship between earnings growth and previous earnings documented by Guvenen et al. (2014), who use the previous five-year earnings percentile based on SSA data for all US. Although here we only use the previous year earnings,

Figure 1: Earnings growth distribution

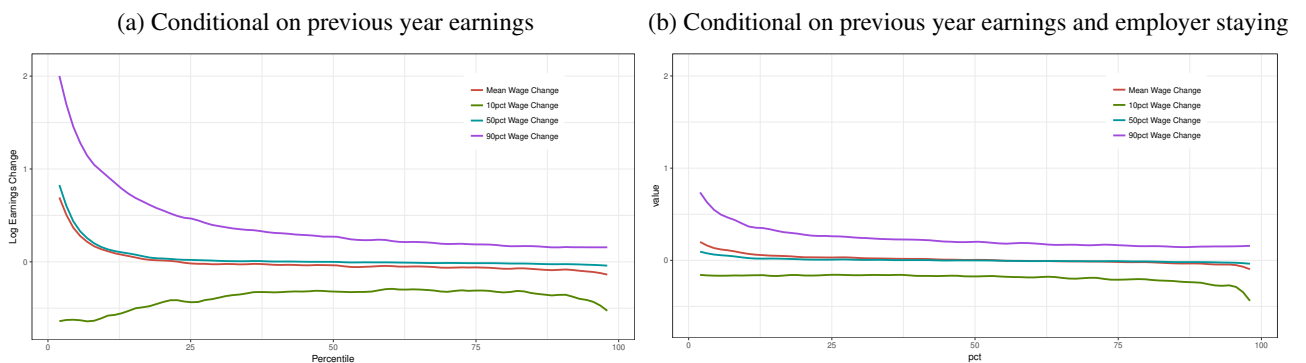


Note: The annual earnings growth distribution is constructed for the sample period 1990-2013. It is based on residual earnings after controlling for potential experience, education, gender, race and month dummies.

the figure shows that workers with the larger earnings changes are also those who had the lowest earnings, while those with progressively higher previous year earnings are associated with smaller changes. One of the advantage of the SIPP relative to the SSA data is that the former provides better information about individuals' labour market histories and demographic characteristics. These characteristics are the ones we exploit in this paper and it is reassuring that, despite the much smaller number of observations, the SIPP and the SSA data present consistent pictures of the earnings change distribution.

The role of the underlying labour market flows can be gauged from Figure 2b, which presents the same relation but for a sample restricted to only employer stayers. The earnings growth of employer stayers are not only much less dispersed, but the probability of an earnings changes (positive or negative) is much less sensitive to these workers' previous year earnings. In fact, the earnings growth distribution does not change much across the previous year's earnings distribution, apart from the probability of relatively larger improvements among the very low-earners, and the probability of earnings losses among very high earners.

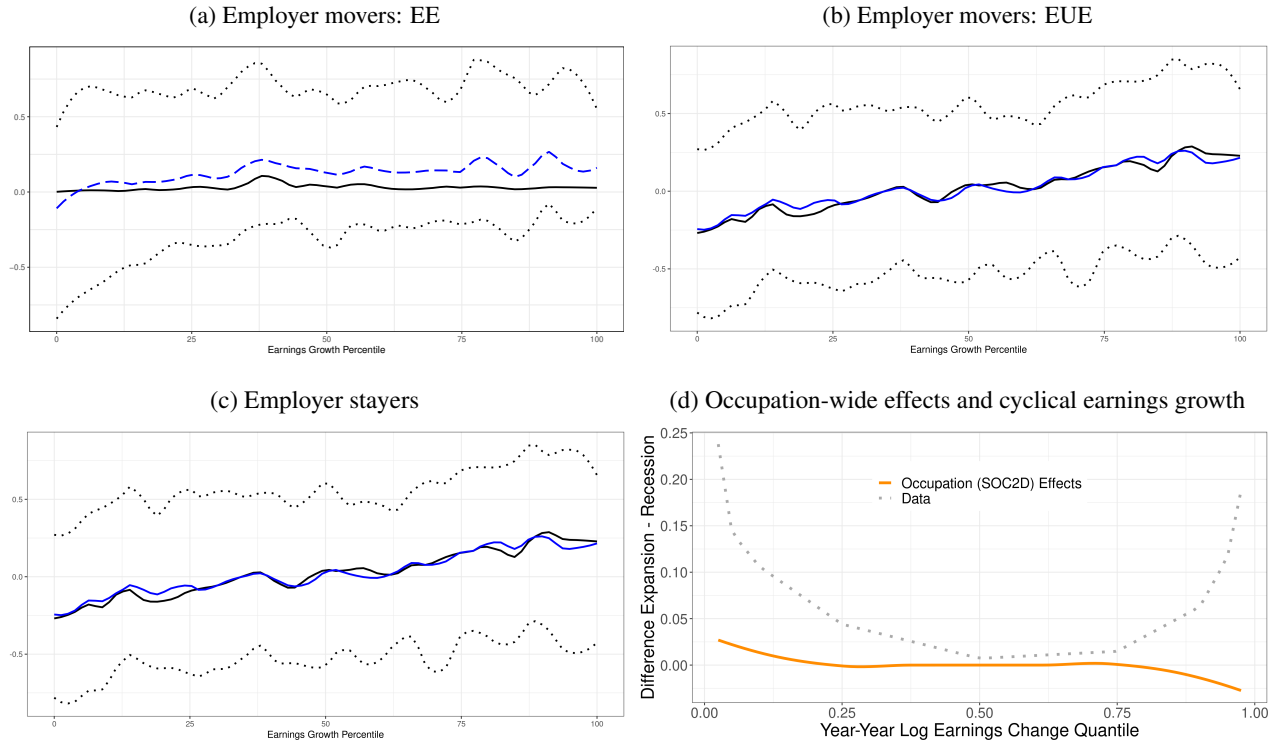
Figure 2: Earnings growth distribution conditional on previous earnings



This evidence then shows that those workers who experienced large earnings changes are also those who had low previous year earnings *and* changed employers. Further, the 90th percentile curve



Figure 3: Occupational Ladder with 22 2-digit SOC Codes



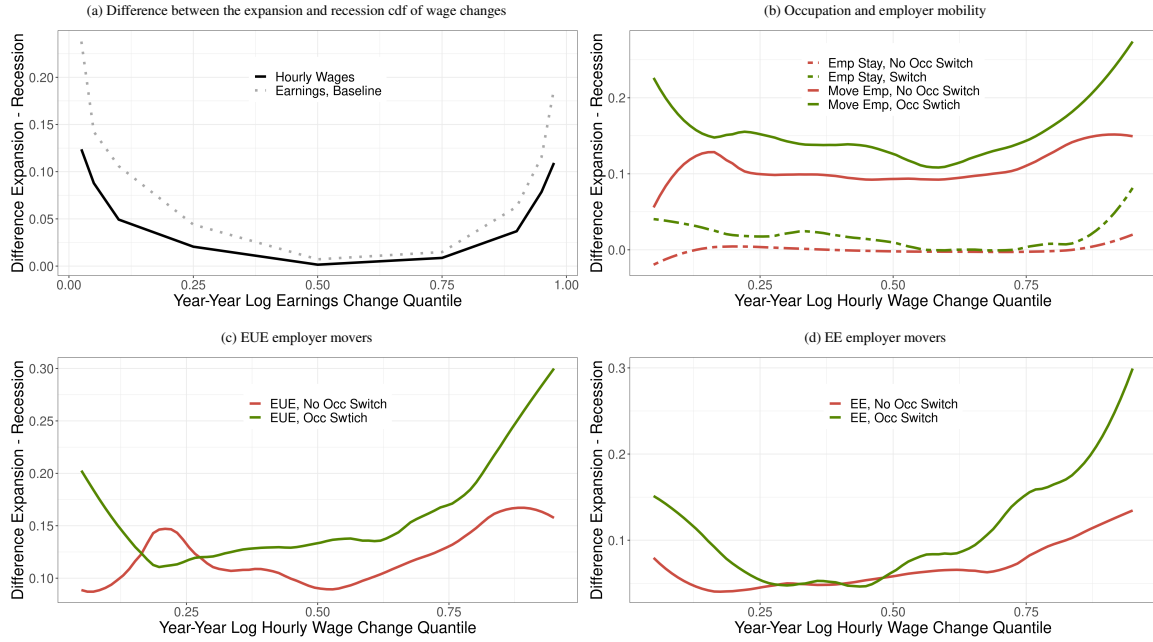
Note: Occupational switchers are ranked by their earnings growth in the horizontal axis. For each rank the vertical axis depicts the mean, median, 90<sup>th</sup> and 10<sup>th</sup> percentiles of the distribution of the differences in occupational earnings effects. Occupations defined at the 2-digit level of aggregation

in Figure 2a shows that workers who were at the bottom of the earnings distribution climb the most, while the slow decline of the curve reflects that the larger is a worker's earnings the lower is his/her gain from changing employer. These patterns are broadly inline with the implications of standard job ladder models.

## Earnings growth and the occupational job ladder

In Figure 3, Section 2.3 of the main text we highlighted the role of occupational mobility due to workers' *idiosyncratic* career concerns as the main underlying force behind the cross-sectional earnings growth distribution. To emphasize the idiosyncratic nature of these effects, we depicted the relationship between the distribution of the change between the source and destination occupation fixed effects (obtained from an earnings regression) and the percentile of these workers' earnings change in the cross-sectional earnings growth distribution. We presented the results using our baseline 4 task-based occupational categories. Here, Figure 3 now shows that the same patterns holds in our 22 occupation categories of the 2-digit 1990 SOC to highlight that our conclusions were not driven by aggregation into the 4 task-based categories.

Figure 4: Wage growth distribution over the cycle and the importance of occupational movers



Note: The annual wage growth distribution is constructed for the sample period 1990-2013. It is based on residual wages after controlling for potential experience, education and month dummies. Recessions are defined as periods in which the HP-filtered unemployment rate is in the top 20% of realizations.

## Cyclical changes in wage growth

In this section, we replicate our principle figures using wages instead of earnings. As described, we accumulate average hourly wages over the prior and posterior year following a transition, just as we did for earnings. When the worker is nonemployed, we assign a wage rate of zero. Hence, we isolate out changes along the intensive margin of hours. Particularly because we are focusing on workers who have large earnings changes one might be concern that these reflect occupation transitions that are accompanied by movements in and out of part-time work and/or changes in work habits. Including periods of unemployment here is fully consistent with our theoretical framework as our proposed job ladder model also include these periods. We observe that wage changes have remarkably similar patterns as earnings changes. We first replicate Figure 1d with wages rather than earnings: establishing the basic cyclical skewness in not only a feature on changes in hours worked. Then we show that occupation changes are the primary drivers of this skewness by replicating Figures 4a, 5a, and 5b again using wages rather than earnings. These hourly wage versions are in Figure 4.

## Skewness decomposition of cyclical earnings changes

As discussed in Section 2 of the main text, Table 4 presents a linear decomposition of the change in the skewness of the earnings growth distribution along the business cycle. This decomposition follows the method proposed by Halvorsen et al. (2020). The main implication of the exercise is that those workers who change occupations and employers at the same time contribute 59.2% to the observed

Table 4: Linear decomposition of third central moment of skewness

	No Occ Switch			Occ Switch		
	Emp Stay	EE	EUE	Emp Stay	EE	EUE
Skewness Contrib	0.031	0.087	0.281	0.008	0.123	0.469
Fraction of Observations	0.865	0.027	0.051	0.012	0.014	0.031
N (thous)	402.281	12.423	23.946	5.412	6.495	14.442

Note: Decomposition of cyclical change in third central moment following Halvorsen et al. (2020). Weights across groups held constant over the cycle. Annual earnings change based on residual wages after controlling for potential experience, education and month dummies. Recessions are defined as periods in which the HP-filtered unemployment rate is in the top 20% of realizations.

increase in the left-skewness of the earnings growth distribution during recessions. This happens even though occupation/employer movers represent 4.5% of all observations in our sample. This table also shows that the large contribution of this group mainly arises from *EUE* occupation movers.

## Appendix C - Model derivations

### Worker flows and the earnings distribution

The evolution of the earnings distribution  $G$  of workers across occupations and employment status is a result of the dynamics of the exogenous job separation and job finding probabilities  $\delta_\epsilon$ ,  $\delta_z$ ,  $\lambda_U$ ,  $\lambda_U^c$ ,  $\lambda_E$  and  $\lambda_E^c$  coupled with workers' job separation, job acceptance and occupational mobility decisions as described in the main text. Therefore to derive such a distribution we need to first derive the laws of motions of unemployed and employed workers. For this purpose it is useful to derive the measure of unemployed and employed workers at each stage  $j$  within a period, where  $j = s, r, m, p$  represent separations, reallocations, search and matching and production. Let  $u_t^j(z, x_h, o)$  denote the measure of unemployed workers with idiosyncratic productivity  $z$  and human capital  $x_h$  in occupation  $o$  at the beginning of stage  $j$  in period  $t$ . Similarly, let  $e_t^j(\epsilon, z, x_h, o)$  denote the measure of employed workers in labor market with idiosyncratic productivities  $\epsilon$  and  $z$  and human capital  $x_h$  in occupations  $o$  at the beginning of stage  $j$  in period  $t$ . Finally let  $\mathcal{G}$  denote the joint productivity distribution of unemployed and employed workers over all occupations, and  $\mathcal{G}^j$  denote this distribution at the beginning of stage  $j$ .

**Unemployed workers** Given the initial conditions  $(A_0, \mathcal{P}_{O,0}, \mathcal{G}_0^p)$ , the measure of unemployed workers characterised by  $z$  and  $x_h$  in occupation  $o$  at the beginning of next period's separation stage is given by

$$u_{t+1}^s(z, x_h, o)dz = \chi^u(x_h|x_h) \int_{\underline{z}}^{\bar{z}} u_t^p(\tilde{z}, x_h, o) dF(z|\tilde{z}) d\tilde{z} + \chi^u(x_h|x_{h+1}) \int_{\underline{z}}^{\bar{z}} u_t^p(\tilde{z}, x_{h+1}, o) dF(z|\tilde{z}) d\tilde{z},$$

where the two terms capture the measure of unemployed workers characterised by  $(\tilde{z}, x_h, o)$  and  $(\tilde{z}, x_{h+1}, o)$  in the previous period's production stage who will be characterised by  $(z, x_h, o)$  immediately after the  $z$  and  $x_h$  shocks occur. During the separation stage some employed workers will become unemployed within their own occupation with probability  $\delta_\epsilon$ . Since by assumption these newly

unemployed workers do not participate in the current period's reallocation or search and matching stages, we count them at the production stage. This implies that  $u_{t+1}^r(z, x_h, o)dz = u_{t+1}^s(z, x_h, o)dz$ . Since with probability  $\delta_z$  some of the unemployed at the beginning of the reallocation will be forced to change occupation, the previous arguments imply that the measure of unemployed workers characterised by  $(z, x_h)$  in occupation  $o$  at the beginning of the search and matching stage is given by

$$u_{t+1}^m(z, x_h, o)dz = (1 - \delta_z)(1 - \rho^U(\cdot))u_{t+1}^r(z, x_h, o)dz + (\mathbf{1}_{h=1})\tilde{u}_{t+1}^r(z, x_1, o)dz,$$

where the first term denotes those unemployed workers at the beginning of the reallocation period who did not leave to another occupation and  $\rho^U(z, x_h, o, A, \mathcal{P}_O)$  is an indicator function taking the value of one if the unemployed worker reallocates and zero otherwise. The second term corresponds to all those unemployed workers in other occupations who voluntarily or involuntarily reallocated and ended up in occupation  $o$  with productivity  $z$ , plus all those employed workers at the beginning of the separation stage in other occupations who involuntarily reallocated and also ended up in occupation  $o$  with productivity  $z$ . Namely,

$$\begin{aligned} \tilde{u}_{t+1}^r(z, x_1, o)dz &= \left[ \sum_{\tilde{o} \neq o} \sum_{\tilde{h}=1}^H \left[ \int_{\tilde{z}}^{\bar{z}} [(1 - \delta_z)\rho^U(\cdot) + \delta_z]\alpha_o^U(\cdot, \tilde{o})u_{t+1}^r(\tilde{z}, x_{\tilde{h}}, \tilde{o})d\tilde{z} \right] \right] dF(z) \\ &+ \left[ \sum_{\tilde{o} \neq o} \sum_{\tilde{h}=1}^H \left[ \int_{\tilde{z}}^{\bar{z}} \int_{\tilde{\epsilon}}^{\bar{\epsilon}} \delta_z \alpha_o^E(\cdot, \tilde{o})e_{t+1}^s(\tilde{\epsilon}, \tilde{z}, x_{\tilde{h}}, \tilde{o})d\tilde{\epsilon}d\tilde{z} \right] \right] dF(z), \end{aligned}$$

where  $\alpha_o^U(\tilde{z}, x_{\tilde{h}}, A, \mathcal{P}_O, \tilde{o})dF(z)$  denotes the probability that an unemployed worker characterised by  $(\tilde{z}, x_{\tilde{h}})$  in occupation  $\tilde{o}$ , received idiosyncratic productivity  $z$  from occupation  $o$  at the moment of reallocation; while  $\alpha_o^E(\tilde{\epsilon}, \tilde{z}, x_{\tilde{h}}, A, \mathcal{P}_O, \tilde{o})dF(z)$  denotes the probability that an employed worker characterised by  $(\tilde{\epsilon}, \tilde{z}, x_{\tilde{h}})$  in occupation  $\tilde{o}$ , received productivity  $z$  from occupation  $o$  when reallocating. Given that reallocation involves resetting any accumulated human capital, the indicator function  $\mathbf{1}_{h=1}$  in the expression for  $u_{t+1}^m(z, x_h, o)$  takes the value of one when we are considering the measure  $u_{t+1}^m(z, x_1, o)$  and zero otherwise.

The measure of unemployed workers characterised by  $(z, x_h)$  in occupation  $o$  during the production stage is then given by

$$\begin{aligned} u_{t+1}^p(z, x_h, o)dz &= [(1 - \lambda_U) + \lambda_U(1 - \phi^U(\cdot))]u_{t+1}^r(z, x_h, o)dz \\ &+ (\mathbf{1}_{h=1})[(1 - \lambda_U^c) + \lambda_U^c(1 - \phi^U(\cdot))]\tilde{u}_{t+1}^r(z, x_1, o)dz \\ &+ \int_{\tilde{\epsilon}}^{\bar{\epsilon}} [\delta_{\epsilon} + (1 - \delta_{\epsilon} - \delta_z)(1 - d(\tilde{\epsilon}, \cdot))]e_{t+1}^s(\tilde{\epsilon}, z, x_h, o)d\tilde{\epsilon}dz, \end{aligned} \tag{8}$$

where first two terms denote those  $u_{t+1}^m(z, x_h, o)dz$  workers who did not manage to get re-employed, while the third term denote the measure of all those employed workers with occupation-match productivity equal to  $z$ , who separated into unemployment and stayed in occupation  $o$ . In these terms,  $\phi^U(z, x_h, o, A, \mathcal{P}_O)$  is an indicator function that take the value of one if the unemployed worker accepts a firm's job offer and zero otherwise, while  $d(\tilde{\epsilon}, z, x_h, o, A, \mathcal{P}_O)$  is another indicator function that takes the value of one if the worker decides to quit into unemployment and zero otherwise.

**Employed workers** Given the initial conditions  $(A_0, \mathcal{P}_{O,0}, \mathcal{G}_0^p)$ , the measure of employed workers characterised by  $(\epsilon, z, x_h)$  in occupation  $o$  at the beginning of next period's separation stage,

$$\begin{aligned} e_{t+1}^s(\epsilon, z, x_h, o) d\epsilon dz &= \chi^e(x_h|x_h) \int_{\underline{z}}^{\bar{z}} \int_{\underline{\epsilon}}^{\bar{\epsilon}} e_t^p(\hat{\epsilon}, \hat{z}, x_h, o) d\Gamma(\epsilon|\hat{\epsilon}) d\hat{\epsilon} dF(z|\hat{z}) d\hat{z} \\ &+ (\mathbf{1}_{h>1}) \chi^e(x_h|x_{h-1}) \int_{\underline{z}}^{\bar{z}} \int_{\underline{\epsilon}}^{\bar{\epsilon}} e_t^p(\hat{\epsilon}, \hat{z}, x_{h+1}, o) d\Gamma(\epsilon|\hat{\epsilon}) d\hat{\epsilon} dF(z|\hat{z}) d\hat{z}, \end{aligned}$$

where the two terms show the probability that employed workers characterised by  $(\hat{\epsilon}, \hat{z}, x_h, o)$  and  $(\hat{\epsilon}, \hat{z}, x_{h-1}, o)$  in the previous period's production stage will be characterised by  $(\epsilon, z, x_h, o)$  immediately after the  $\epsilon, z$  and  $x_h$  shocks occur. The indicator function  $\mathbf{1}_{h>1}$  takes the value of one when the level of human capital is associated with a value of  $x_h > x_1$  and zero otherwise.

The same arguments used in the case of unemployed workers imply that the measure of employed workers at the beginning of the production stage is given by

$$\begin{aligned} e_{t+1}^p(\epsilon, z, x_h, o) d\epsilon dz &= [1 - \lambda_E \phi^E(\epsilon, \cdot)] e_{t+1}^m(\epsilon, z, x_h, o) d\epsilon dz + (\mathbf{1}_{h=1}) \lambda_E^c \tilde{e}_{t+1}^m(\epsilon, z, x_h, o) \\ &+ \int_{\underline{\epsilon}}^{\bar{\epsilon}} \lambda_E [\gamma \phi^E(\hat{\epsilon}, \cdot) + (1 - \gamma) d(\hat{\epsilon}, \cdot)] e_{t+1}^m(\hat{\epsilon}, z, x_h, o) d\hat{\epsilon} dz d\Gamma(\epsilon) \\ &+ \lambda_U \phi^U(\cdot) u_{t+1}^r(z, x_h, o) dz d\Gamma(\epsilon) + (\mathbf{1}_{h=1}) \lambda_U^c \phi^U(\cdot) \tilde{u}_{t+1}^r(z, x_1, o) dz d\Gamma(\epsilon), \end{aligned} \quad (9)$$

where  $\Gamma(\cdot)$  denotes the distribution of  $\epsilon$  across the cycle and  $e_{t+1}^m(\epsilon, z, x_h, o) d\epsilon dz = (1 - \delta_z - \delta_\epsilon)(1 - d(\epsilon, z, x_h, o, A, \mathcal{P}_O))(1 - \rho(\epsilon, z, x_h, o, A, \mathcal{P}_O)) e_{t+1}^s(\epsilon, z, x_h, o) d\epsilon dz$  denotes the measure of employed workers characterised by  $(\epsilon, z, x_h)$  who remained in the occupation and entered the search and matching stage, such that with probability  $[1 - \lambda_E \phi^E(\epsilon, z, x_h, o, A, \mathcal{P}_O)]$  they did not change employers, and  $\phi^E(\epsilon, z, x_h, o, A, \mathcal{P}_O)$  is an indicator function that take the value of one when the employed worker accepts the firm's job offer and zero otherwise.

The second term in (9) denotes the measure of employed workers from other occupations who re-allocate to occupation  $o$  arriving with idiosyncratic productivity  $z$  and drew idiosyncratic productivity  $\epsilon$  when meeting an employer. In this case, we need to take into account only of employed workers who voluntarily decided to change occupations. Some of these workers will be able (with probability  $\gamma$ ) to decide whether to change occupations within or across employers; while others (with probability  $1 - \gamma$ ) will have to take the position in a new employer, as long as it is above their expected value of unemployment. These arguments then imply that  $\tilde{e}_{t+1}^m(\epsilon, z, x_h, o)$  is given by

$$\begin{aligned} \tilde{e}_{t+1}^m(\epsilon, z, x_h, o) &= (1 - \delta_\epsilon - \delta_z) \left( \gamma \left[ \sum_{\tilde{o} \neq o} \sum_{\tilde{h}=1}^H \left[ \int_{\underline{z}}^{\bar{z}} \int_{\underline{\epsilon}}^{\bar{\epsilon}} \rho^E(\cdot) \alpha_o^E(\cdot, \tilde{o}) \phi^E(\cdot) e_{t+1}^s(\tilde{\epsilon}, \tilde{z}, x_{\tilde{h}}, \tilde{o}) d\tilde{\epsilon} d\tilde{z} \right] \right] \right. \\ &\quad \left. + (1 - \gamma) \left[ \sum_{\tilde{o} \neq o} \sum_{\tilde{h}=1}^H \left[ \int_{\underline{z}}^{\bar{z}} \int_{\underline{\epsilon}}^{\bar{\epsilon}} \rho^E(\cdot) \alpha_o^E(\tilde{\epsilon}, \tilde{\Omega}, \tilde{o}) d(\tilde{\epsilon}, \tilde{\Omega}) e_{t+1}^s(\tilde{\epsilon}, \tilde{z}, x_{\tilde{h}}, \tilde{o}) d\tilde{\epsilon} d\tilde{z} \right] \right] \right) dF(z) \Gamma(\epsilon), \end{aligned}$$

where  $\rho^E(\tilde{\epsilon}, \tilde{z}, x_{\tilde{h}}, A, \mathcal{P}_O, \tilde{o})$  is an indicator function taking the value of one if the employed worker reallocates and zero otherwise. The third term in (9) denotes the measure of employed workers within the same occupation  $o$  who found a new job with idiosyncratic productivity  $\epsilon$ . The last two terms denote the measure of unemployed workers who got re-employed in occupation  $o$  with idiosyncratic

productivities  $z$  and  $\epsilon$ , as implied by (8).

**Earnings distribution** Given the above measures we can now derive the earnings distribution. Given that  $\hat{w}(A, p_o, \epsilon, z, x_h)$  is increasing in all of its arguments and that  $e_t^p(\epsilon, z, x_h, o)$  can be equal to zero for some combinations of  $(\epsilon, z, x_h, o)$  as workers might prefer unemployment than remaining employed, the probability of observing earnings  $w' \leq w$  at time  $t$  is given by

$$G_t(w|A_t, \mathcal{P}_{O,t}) = \sum_{o \in O} \sum_{h \in H} \int_{\underline{z}}^{\bar{z}} \int_{\underline{\epsilon}}^{\max\{\underline{\epsilon}, \hat{w}^{-1}(w, A, p_o, z, x_h)\}} \hat{w}(A, p_o, \epsilon, z, x_h) e_t^p(\epsilon, z, x_h, o) d\epsilon dz, \quad (10)$$

where  $\hat{w}^{-1}(w, A, p_o, z, x_h)$  denotes the inverse of  $\hat{w}$ , such that the value of  $\epsilon$  solves  $\hat{w}$  for earnings equal to  $w$ . Aggregating (10) across  $p_o, A$  and  $t$ , then yields the cross sectional earnings distribution,  $G$ . Note that both  $e_t^p(\epsilon, z, x_h, o)$  and current earnings  $w = \hat{w}(\cdot)$  are endogenous objects as they depend on worker's employer and occupational mobility decisions.

## Appendix D - Estimation

### Simulation procedure

The parametric assumptions made in Section 4.1 imply that we need to recover 48 parameters which can be divided into several sets. The set that governs the arrival of job opportunities  $\{\lambda_0^i, \lambda_1^i, \lambda_0^{c,i}, \lambda_1^{c,i}\}_{i=U,E}$ . The set  $\{\delta_0^z, \delta_1^z, \rho_z, \nu_z, \sigma_z, \omega_z, z_A, \bar{z}, \underline{z}\}$  that governs the idiosyncratic worker-occupation productivities. The set  $\{\delta_0^\epsilon, \delta_1^\epsilon, \eta, \sigma_\epsilon, lt_\epsilon, rt_\epsilon, \omega_\epsilon, \epsilon_A, \bar{\epsilon}, \underline{\epsilon}\}$  that governs the idiosyncratic worker-employer productivities, the set  $\{\rho_p, \sigma_p, \tilde{p}_{NRC}, \tilde{p}_{RC}, \tilde{p}_{NRM}, \tilde{p}_{RM}\}$  that governs the occupation-wide productivities, the set of occupational human capital accumulation  $\{x_1, x_2, \chi(x_2)\}$  and the set of directional parameters across occupations  $\{\alpha_0, \alpha_1^U, \alpha_1^E, \alpha_{NRC}, \alpha_{NRM}, \alpha_{RM}, \alpha_{NRM}\}$ . The set that governs the aggregate productivity process  $\{\rho_A, \sigma_A\}$ , payments  $\{\gamma_w, b\}$  and the discount rate  $\beta = 0.997$ .

As mentioned in the main text we fix  $\beta = 0.997$ , normalise  $x_1$  to one, set  $\chi(x_2)$  such that human capital accumulation occurs on average after 5 years of occupational tenure and choose  $x_2$  to match the 12% 5-year returns to occupational tenure reported by Kambourov and Manovskii (2009). We also set  $b = 0.4$  to match a 40% replacement ratio (see Shimer, 2005). The aggregate productivity process parameters are set to the values of the autocorrelation and unconditional variance of output per worker as observed in the US during the period of study, similar to Shimer (2005), such that  $\rho_A = 0.9580$  and  $\sigma_A = 0.0090$ . To generate the idiosyncratic productivity grid, we apply an evenly spaced grid based on the deciles of the distributions  $F$  and  $\Gamma$ . These procedure then leads to  $\bar{z} = \bar{\epsilon} = 3$  and  $\underline{z} = \underline{\epsilon} = -3$ .

Given these pre-set parameters, we estimate the model following a two-step procedure in which we split all remaining parameters between an inner and outer loop. Given values for the outer loop parameters, we can directly calibrate those in the inner loop such that their values match *exactly* the targeted moments. The inner loop contains the productivity levels  $\bar{p}_o$  and the directional parameters of the  $\alpha(\cdot)$  function,  $\alpha_{NRC}, \alpha_{RC}, \alpha_{NRM}$  and  $\alpha_{RM}$ . We then iterate on the values of the outer loop

parameters using simulated method moments, adjusting the inner loop parameters at each iteration.

To simulate the model, we first solve it by value function iteration using global methods. Local methods would be unsuitable for our purpose as they truncate some of the variation in earnings changes in response to the shock (see Petrosky-Nadeau and Zhang, 2021). This is particularly important for our estimation as we want to investigate cyclical changes in the tails of the earnings growth distribution. Using global methods allows for unstructured changes in earnings as response to shocks. To solve the model around a set of outer loop parameters we re-set all of the grids for shocks and the distributions thereon. Because we are solving this using global methods, we use value function iteration until the convergence. Because of the discrete choices that imply value functions intersect, this can cause non-concave portions of the state space and long (or infinite) converge lengths. Hence, we smooth over the discrete choice to move occupations using a logit-type function with a very steep slope parameter.

We then draw 64 13-year histories of 10,000 agents each. We parallelize it on 64 labour market histories to match a multiple of the number of cores using in our cluster. Each history has its own draw of aggregate shocks, though on average 20% of periods are in recession and we preserve that auto-correlation structure of the cycle as well. The simulations are on the shocks grids, rather than interpolating between. To begin the history, workers in the first period have the ergodic distribution of  $x_h$  and occupations. Once the histories are simulated we convert them into a four monthly frequency as in the SIPP and average over histories to compute the moments in  $M^S(\cdot)$ , discussed in the text. This procedure is followed until convergences.

## Search across occupations and its relationship with the Gumbel-type shocks

In Section 4.1 we parameterized the probability of obtaining a  $z$  from a given occupation as  $\alpha^i(s_{\tilde{o}}) = \alpha_0 e^{\alpha_{\tilde{o}} \alpha_1^i s_{\tilde{o}}^{1-\alpha_1^i}}$ , where occupation  $\tilde{o} \in O^-$  denotes the search direction,  $i$  the worker's labour force status,  $i = U, E$ , and  $s_{\tilde{o}}$  denotes search intensity. Workers have to chose a  $s_{\tilde{o}}$  for each  $\tilde{o} \in O^-$  to maximise the probability of receiving a  $z$  given that  $\sum_{\tilde{o} \in O^-} s_{\tilde{o}} = 1$ . The first order condition for such maximisation is given by  $\alpha'(s_{\tilde{o}}^*) \Phi^i(\tilde{\Omega}_1) = \mu$ , where  $\mu$  denotes the multiplier on the constraint  $\sum_{\tilde{o} \in O^-} s_{\tilde{o}} = 1$ ,  $\tilde{\Omega}_1 = \{\tilde{z}, x_1, \tilde{o}, A, \mathcal{P}_O\}$  and  $\Phi^i(\tilde{\Omega}_1)$  denotes the net conditional return to searching in direction  $\tilde{o}$  such that  $\Phi^U(\tilde{\Omega}_1) \equiv \Psi^U(\tilde{z}, x_1, \tilde{o}, \Omega) - W^U(z, x_h, o, \Omega)$  with

$$\begin{aligned} \Psi^U(\tilde{z}, x_1, \tilde{o}, \Omega) &= \int_{\underline{z}}^{\tilde{z}} \left[ \lambda_U^c(A) \int_{\underline{\epsilon}}^{\tilde{\epsilon}} \max \left\{ W^E(\tilde{\epsilon}, \tilde{z}, x_1, \tilde{o}, \Omega), W^U(\tilde{z}, x_1, \tilde{o}, \Omega) \right\} d\Gamma(\tilde{\epsilon}) \right. \\ &\quad \left. + (1 - \lambda_U^c(A)) W^U(\tilde{z}, x_1, \tilde{o}, \Omega) \right] dF(\tilde{z}); \end{aligned}$$



and  $\Phi^E(\tilde{\Omega}_1) \equiv \Psi^E(\epsilon, \tilde{z}, x_1, \tilde{o}, \Omega) - W^E(\epsilon, z, x_h, o, \Omega)$  with

$$\begin{aligned} \Psi^E(\epsilon, \tilde{z}, x_1, \tilde{o}, \Omega) &= \left( \int_{\underline{z}}^{\tilde{z}} \left[ \int_{\underline{\epsilon}}^{\tilde{\epsilon}} \left( \gamma \lambda_E^c(A) \max \left\{ W^E(\tilde{\epsilon}, x_1, \tilde{z}, \tilde{o}, \Omega), W^E(\epsilon, x_1, \tilde{z}, \tilde{o}, \Omega) \right\} \right. \right. \right. \\ &\quad + (1 - \gamma) \lambda_E^c(A) \max \left\{ W^E(\tilde{\epsilon}, x_1, \tilde{z}, \tilde{o}, \Omega), W^U(x_1, \tilde{z}, \tilde{o}, \Omega) \right\} \Big) d\Gamma(\tilde{\epsilon}, A) \\ &\quad \left. \left. + (1 - \lambda_E^c(A)) W^E(\epsilon, x_1, \tilde{z}, \tilde{o}, \Omega) \right] dF(\tilde{z}, A) \right), \end{aligned}$$

and  $\Omega = \{A, \mathcal{P}_O\}$ . Substituting the assumed functional form for  $\alpha(\cdot)$  in the first-order condition yields,

$$s_{\tilde{o}}^* = \left( \frac{(1 - \alpha_1^i) \alpha_0 e^{\alpha_{\tilde{o}} \alpha_1^i}}{\mu} \right)^{1/\alpha_1^i} \left( \Phi^i(\tilde{\Omega}_1) \right)^{1/\alpha_1^U}.$$

Since this holds for all directions  $\tilde{o} \in O^-$ , we can use the equality constraint  $\sum_{\tilde{o} \in O^-} s_{\tilde{o}} = 1$  to obtain:

$$s_{\tilde{o}}^* = \frac{\left( \frac{(1 - \alpha_1^i) \alpha_0 e^{\alpha_{\tilde{o}} \alpha_1^i}}{\mu} \right)^{1/\alpha_1^i} \left( \Phi^i(\tilde{\Omega}_1) \right)^{1/\alpha_1^i}}{\sum_{\tilde{o} \in O^-} \left( \frac{(1 - \alpha_1^i) \alpha_0 e^{\alpha_{\tilde{o}} \alpha_1^i}}{\mu} \right)^{1/\alpha_1^i} \left( \Phi^i(\tilde{\Omega}_1) \right)^{1/\alpha_1^i}}.$$

Noting that  $\left( \frac{(1 - \alpha_1^i) \alpha_0}{\mu} \right)^{1/\alpha_1^i}$  cancels from the numerator and denominator, and using the transformation  $X^{\frac{1}{\alpha_1^i}} = e^{\frac{1}{\alpha_1^i} \log(X)}$  one obtains

$$s_{\tilde{o}}^* = \frac{e^{\alpha_{\tilde{o}} + \frac{1}{\alpha_1^i} \log(\Phi^i(\tilde{\Omega}_1))}}{\sum_{\tilde{o} \in O^-} e^{\alpha_{\tilde{o}} + \frac{1}{\alpha_1^i} \log(\Phi^i(\tilde{\Omega}_1))}}.$$

If the directional terms  $\alpha_{\tilde{o}}$  are all equal, this takes a very convenient form, such that the optimal value of  $s_{\tilde{o}}$  is given by

$$s_{\tilde{o}}^* = \frac{e^{\frac{1}{\alpha_1^i} \log(\Phi^i(\tilde{\Omega}_1))}}{\sum_{\tilde{o} \in O^-} e^{\frac{1}{\alpha_1^i} \log(\Phi^i(\tilde{\Omega}_1))}}, \quad (11)$$

Equation (11) is convenient because it allows more flexibility in matching net mobility across occupations. It does so by breaking the symmetry that the random utility model, which is the one typically used to model occupational mobility, imposes. Nevertheless, our approach has a direct counterpart in the random utility model where the utility shocks follow a Gumbel distribution. To show this suppose the worker obtains a vector of shocks  $\varpi$  whose elements are the shocks associated with each of the occupations in  $O^-$ . Each element of  $\varpi$  is Gumbel-distributed with dispersion parameter  $\alpha_1$  and are realised when the worker chooses to search across occupations. The slight difference from the usual random utility model is that here we require  $\varpi$  to enter in a multiplicative way (rather than additively) such that searching in direction  $\tilde{o}$  yields expected payoff  $\Phi(\tilde{\Omega}_1) e^{\tilde{\varpi}}$ . To identify one occupation from another, we will introduce the notation  $o^j$  and  $\Phi(\Omega_1^j)$  and to save notation we leave implicit the index  $i = U, E$ .

The probability that a worker chooses occupation  $o^j$  over  $o^k$ , is then given by  $v_{oj} = \Pr[\Phi(\Omega_1^j) e^{\varpi^j} >$

$\Phi(\Omega_1^k)e^{\varpi^k}]$ , which is equivalent to the monotonic transformation  $v_{oj} = \Pr[\log \Phi(\Omega_1^j) + \varpi^j > \log \Phi(\Omega_1^k) + \varpi^k]$ , and hence  $v_{oj} = \Pr[\log \Phi(\Omega_1^j) - \log \Phi(\Omega_1^k) + \varpi^j > \varpi^k]$  for any occupations  $j$  and  $k$ . Integrating over  $\varpi^j$  means that we are now considering the expected choice for the population, rather than the probability that an individual goes in given occupational direction. The population-level probability is written as:

$$v_{oj} = \int \prod_{k \neq j} F(\log \Phi(\Omega_1^j) - \log \Phi(\Omega_1^k) + \varpi^j) f(\varpi^j) d\varpi^j,$$

where  $F(\cdot)$  and  $f(\cdot)$  are the CDF and PDF of the Gumbel distribution with location parameter 0 and dispersion  $\alpha_1$ . Using the Gumbel functional form gives us

$$v_{oj} = \int \prod_k \exp(-\exp(-\alpha_1 \{\log \Phi(\Omega_1^j) - \log \Phi(\Omega_1^k) + \varpi^j\})) \exp(-\varpi^j) \exp(-\exp(-\varpi^j)) d\varpi^j.$$

After some tedious algebra this yields the well-known form for the choice probability:

$$v_{oj} = \frac{e^{\frac{1}{\alpha_1} \log \Phi(\Omega_1^j)}}{\sum_{k \in O^-} e^{\frac{1}{\alpha_1} \log \Phi(\Omega_1^k)}}.$$

To normalize this probability by any outside option  $\log \Phi^0$ , we simply multiply both top and bottom of this equation by  $\log(W^U(\cdot))$  or  $\log(W^E(\cdot))$ . Note that  $\tilde{v}$  is exactly  $s_{\tilde{o}}$  as derived in (11). To incorporate the parameters  $\alpha_k$ , one just needs to multiply the  $e^{\alpha_k}$  by the return to occupation  $k$ ,  $\Phi(\Omega_1^k)$  in the previous expression.

Finally, a comparison with the canonical on-the-job search model with endogenous search intensity developed from Burdett (1978) is also useful to further clarify our search across occupation technology. In such a model, for example, an unemployed worker receives with per-period probability  $\lambda \leq 1$  a wage draw (from a known stationary distribution) and with probability  $1 - \lambda$  he does not and remains unemployed. A similar process occurs when the worker becomes employed. With endogenous search intensity,  $\lambda$  is typically a continuous, weakly increasing and weakly concave function of search effort,  $s$ . Unemployed workers need to choose  $s$  in order to maximise the probability of receiving a wage offer subject to a convex search cost. Our set up builds on this structure. We assume that a worker (leaving  $o$ ) has one unit of search intensity,  $s$ , per period. With probability  $\sum_{\tilde{o} \in O^-} \alpha(s_{\tilde{o}}; o) \leq 1$  the worker receives a  $z$  and with complementary probability  $1 - \sum_{\tilde{o} \in O^-} \alpha(s_{\tilde{o}}; o)$  he does not and remains unemployed. The key difference with our technology is that the draw of  $z$  ( $w$  in the one-sided search model) can come from one of several occupations (all occupations sharing the same known stationary distribution,  $F$ ) and the worker has to choose how to allocate  $s$  across the remaining occupations in order to maximise the probability of receiving a  $z$ , knowing that  $\alpha$  is a continuous, weakly increasing and weakly concave function of  $s$  and  $\sum_{\tilde{o} \in O^-} s_{\tilde{o}} = 1$ .

## Standard errors of the conditional earnings growth distributions

To complement the standard errors of the targeted moments described in Table 1 in the main text, Table 5 now presents the bootstrapped standard errors of the quantiles of the earnings growth distribution depicted in Figure 6 in the main text.

Table 5: Bootstrapped standard errors of earnings growth distributions

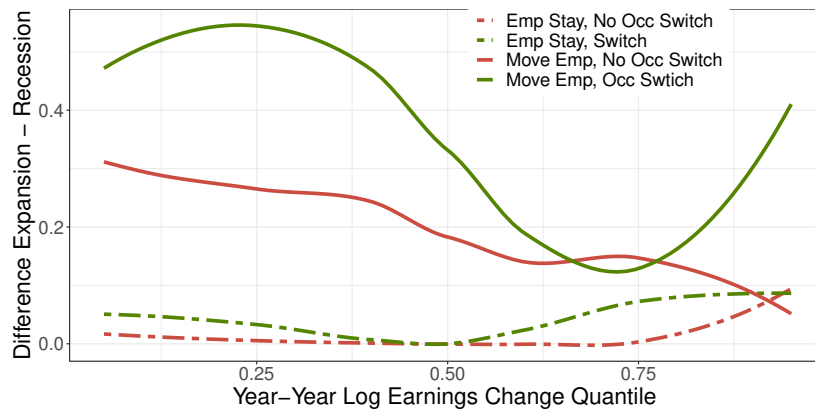
Percentile	Employer stayers		<i>EUE</i> movers		<i>EE</i> movers	
	Occ. movers	Occ. stayers	Occ. movers	Occ. stayers	Occ. movers	Occ. stayers
10 <sup>th</sup>	0.0007	0.0109	0.0108	0.0193	0.0207	0.0235
25 <sup>th</sup>	0.0002	0.0046	0.0059	0.0090	0.0079	0.0147
50 <sup>th</sup>			0.0046	0.0094	0.0076	0.0124
75 <sup>th</sup>	0.0005	0.0068	0.0072	0.0138	0.0121	0.0174
90 <sup>th</sup>	0.0007	0.0076	0.0153	0.0236	0.0280	0.0253

In addition, we target the 2.5<sup>th</sup>, 5<sup>th</sup>, 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup>, 90<sup>th</sup>, 95<sup>th</sup>, 97.5<sup>th</sup> cyclical change in the earnings growth distribution depicted in Figure 9b. The bootstrapped standard errors for these percentiles are 0.0265, 0.0128, 0.0076, 0.0026, 0.0024, 0.0079, 0.0138, 0.0260, respectively.

## Cyclical changes in the earnings growth distribution

In Section 4.3 of the main text we presented the fit of the model in relation to the cyclical change of the earnings growth distribution (see Figure 9a). Figure 5 presents the model counterpart of Figure 4a in Section 2, which conditions the cyclical shift of the earnings growth distribution by whether workers changed employers and/or occupations. The model does not match fully the exact shape of each of the curves relative to the data, but it does match its key features. In particular, it shows that both in the data and model the procyclical skewness of the earnings growth distribution is due to those workers who change occupations and employers simultaneously. The model is also consistent with the fact that among employer mover/ occupation stayers the cyclical change in the earnings growth distribution is below that of employer and occupation movers. Further, the model shows that among employer stayers /occupation movers or stayers the cyclical change in the earnings growth distribution is even lower.

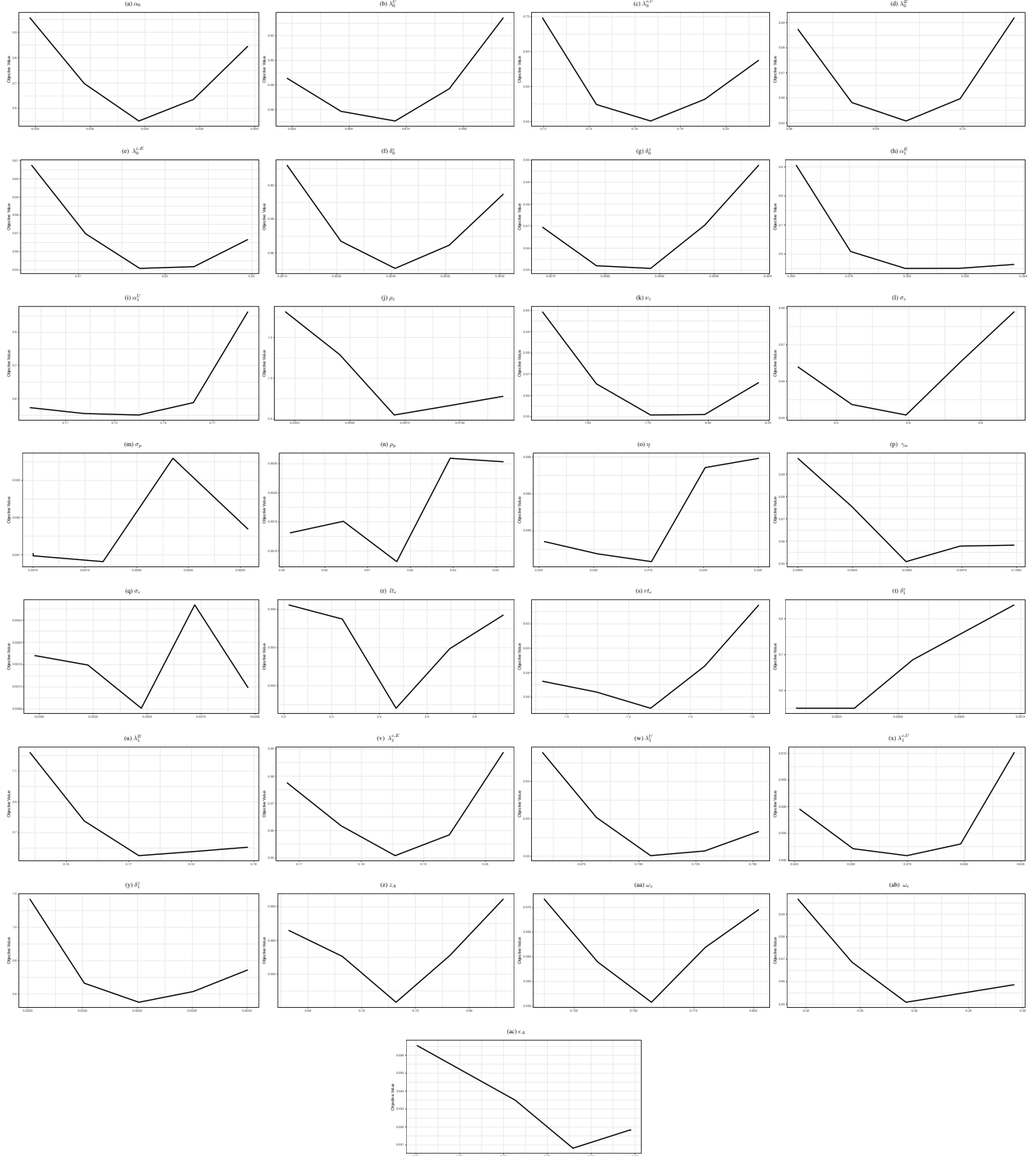
Figure 5: Cyclicalty of the earnings growth distribution by occupation/employer change - Model



Note: This figure present the difference between earnings growth distribution in expansion and recessions periods generated by the model. It conditions these distributions by whether workers changed occupations and employers at the same time, did not experience any of these changes or only experienced one of them. To construct these distributions we follow the same procedure as we did using the SIPP and depicted in Figure 4 in the main text.

# Identification graphs

Figure 6: Global Identification



Note: Each graph shows the re-optimized value of the loss function  $(\mathbf{M}^D - \mathbf{M}^S(.))' \mathcal{W} (\mathbf{M}^D - \mathbf{M}^S(.))$ , after perturbing each parameter in turn from its estimated value by  $\pm 2.5\%$  and the  $\pm 5\%$ .

Following Bilal et al. (2021) to show identification of the outer loop parameters we perturbate each parameter from its estimated value by  $\pm 2.5\%$  and the  $\pm 5\%$ . We then re-optimize all the other

parameters to minimize the loss function  $(\mathbf{M}^D - \mathbf{M}^S(.))' \mathcal{W}(\mathbf{M}^D - \mathbf{M}^S(.))$ , where  $\mathbf{M}^D$  denote the vector of data moments and  $\mathbf{M}^S$  the vector of simulated moments. Identification is achieved if the value of the loss function plotted against the perturbed values of each parameter traces a steep U shape relationship with a minimum at the estimated parameter values, described in Table 2 in the main text. Figure 6 depicts these U shape relationships and shows that the parameters are indeed identified.

## No occupation mobility model

In Section 6 of the main text we discuss the implications of a version of our model in which workers are not allowed to change occupations. We structurally estimate such a model using the same moments presented in Section 4 of the main text, except for those pertaining to occupational mobility. The estimated parameter values in this case are  $\lambda_{0,U} = 0.950$ ,  $\lambda_{1,U} = 0.001$ ,  $\lambda_{0,E} = 0.137$ ,  $\lambda_{1,E} = 0.503$ ,  $\eta = 0.237$ ,  $\delta_{0,\epsilon} = 0.003$ ,  $\delta_{1,\epsilon} = -0.564$ ,  $\sigma_\epsilon = 0.001$ ,  $rt_\epsilon = 0.600$ ,  $lt_\epsilon = 3.998$ ,  $\omega_\epsilon = 0.490$ ,  $\epsilon_A = 0.094$ , and  $\gamma_w = 0.080$ . Table 6 shows that this version is able to replicate very well the targeted average  $EE$ ,  $EU$  and  $UE$  transition probabilities as well as their expansion/recessions ratios.

Table 6: Targeted moments in the estimation, without occupations

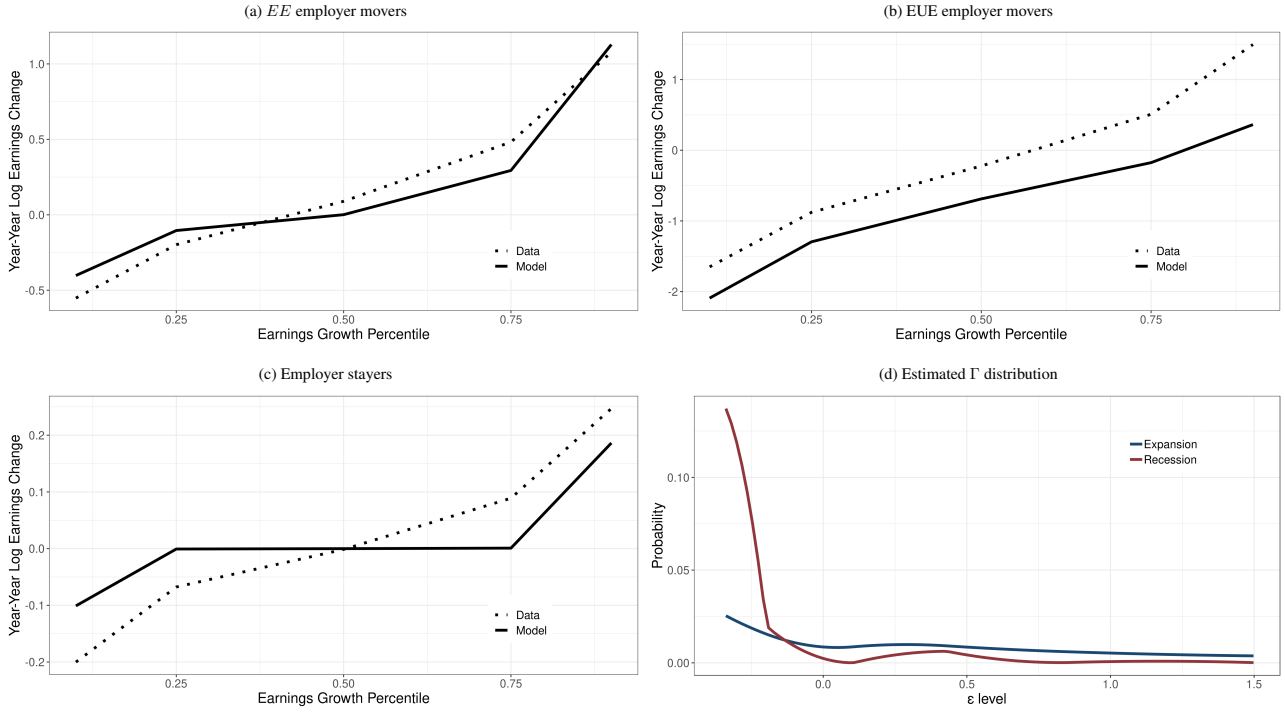
Moment	Model	Data	Moment	Model	Data
$EE$ transition prob	0.034	0.034 (0.0003)	$EE$ rate - expansion/recession ratio	1.173	1.185 (0.0469)
$UE$ transition prob	0.371	0.395 (0.0025)	$UE$ rate - expansion/recession ratio	1.078	1.088 (0.0244)
$EU$ transition prob	0.023	0.022 (0.0002)	$EU$ rate - expansion/recession ratio	0.710	0.746 (0.0333)

Note: Bootstrapped standard errors in parenthesis.

Figure 13a in the main text shows that the model is also able to replicate the cross-sectional earnings growth distribution, capturing well its skewness and leptokurtosis, consistent with the results in Hubmer (2018) and Karahan et al. (2020). Underlying this fit, however, Figures 7a, 7b and 7c reveal that the model fails to capture the targeted earnings growth distributions conditional on employer transitions, particularly the ones for  $EUE$  employer movers. Among the latter, the model generates not only larger earnings losses relative to the data, but it hardly generates any earnings gains. It is only close to the 90<sup>th</sup> percentile that we observe these earnings gains, while in the data earnings gains from  $EUE$  transition starts occurring much closer to median. This is a consequence of the shape of the estimated  $\Gamma_A(\cdot)$ , depicted in Figure 7d. Its long right tail implies that employed workers can climb the job ladder and achieve high values of  $\epsilon$  relatively fast. Figure 7a and the estimated transition probabilities show that this makes the model consistent with the earnings growth distribution of  $EE$  movers. However, when these workers fall into unemployment, the estimated  $\Gamma_A(\cdot)$  implies that at

re-employment workers are more likely to draw low values of  $\epsilon$ . Even though these workers might not accept the lowest  $\epsilon$  draws (particularly during recessions), they will still face a higher probability of becoming re-employed in jobs associated with a low  $\epsilon$ . The initial large drop in earnings due to job loss coupled with low re-employment earnings then leads to larger earnings losses and smaller earnings gains among *EUE* workers relative to the data.

Figure 7: Job ladder model - earnings growth distribution (cdf)



Note: The first three panels show that targeted earnings growth distribution, computed separately for *EE* and *EUE* employer movers and employer stayers. Each of these graphs presents the corresponding distribution by showing the annual earnings growth value and the corresponding percentile. The estimation targets the 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup> and 90<sup>th</sup> percentiles of each of these distributions. The last panel shows the estimated  $\Gamma$  distribution in expansions and recessions.

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