

A Service of



Leibniz-Informationszentrum Wirtschaft Leibniz Information Centre

Kind, Hans Jarle; Koethenbuerger, Marko; Schjelderup, Guttorm

Working Paper

Efficiency enhancing taxation in two-sided markets

CESifo Working Paper, No. 2262

Provided in Cooperation with:

Ifo Institute – Leibniz Institute for Economic Research at the University of Munich

Suggested Citation: Kind, Hans Jarle; Koethenbuerger, Marko; Schjelderup, Guttorm (2008): Efficiency enhancing taxation in two-sided markets, CESifo Working Paper, No. 2262, Center for Economic Studies and ifo Institute (CESifo), Munich

This Version is available at: https://hdl.handle.net/10419/26307

Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.



Efficiency Enhancing Taxation in Two-sided Markets

HANS JARLE KIND MARKO KOETHENBUERGER GUTTORM SCHJELDERUP

CESIFO WORKING PAPER NO. 2262 CATEGORY 1: PUBLIC FINANCE MARCH 2008

Efficiency Enhancing Taxation in Two-sided Markets

Abstract

This paper examines the efficient provision of goods in two-sided markets and characterizes optimal specific and ad-valorem taxes. We show that (i) a monopoly may have too high output compared to the social optimum; (ii) output may be reduced by imposing negative value-added taxes (subsidy) or positive specific taxes.

JEL Code: D4, D43, H21, H22, L13.

Hans Jarle Kind
Norwegian School of Economics and
Business Administration
Helleveien 30
5045 Bergen
Norway
hans.kind@nhh.no

Marko Koethenbuerger
Ifo Institute and CESifo at
the University of Munich
Poschingerstrasse 5
81679 Munich
Germany
koethenbuerger@ifo.de

Guttorm Schjelderup
Norwegian School of Economics and Business Administration
Helleveien 30
5045 Bergen
Norway
guttorm.schjelderup@nhh.no

March 11, 2008

1 Introduction

Two-sided platform firms cater to two distinct groups of customers that are connected through quantity spillovers, and the firms maximize profit by facilitating value-creating interactions between these groups. Two-sided platforms operate in many economically significant industries, such as the media sector, the financial sector (payment card systems), real-estate brokerage, and the computing industry (computer operating systems, software, game consoles etc.). The pricing strategies of a platform firm must account for interactions between the demands of different customer groups and the externalities that arise in these relationships. For instance, in the credit card industry there are positive quantity spillovers between merchants and card-holders. Merchants who accept a credit card value an increase in the number of households joining the credit card system, and vice versa.

We analyze the efficient provision and taxation of goods in two-sided markets. We find that under both perfect competition and monopoly goods may be over- or underprovided depending on the size and sign of the customer group spillover effects. In particular, if there are positive intergroup spillovers, both goods will be underprovided in the competitive equilibrium. In contrast, a monopoly platform may actually overprovide both goods. Our analysis shows that if both sides of the market can be taxed, ad valorem and unit taxes can be used to achieve the social optimum. However, there is an inherent asymmetry between ad valorem and unit taxes under monopoly. In particular, a firm always reduces output of a good which is subject to an increased unit tax. This is the only way the firm can reduce its tax burden. In contrast, the monopoly can raise output of a good subject to a higher advalorem tax and still reduce its tax burden by lowering the end-user price. Depending on the interrelationship between the two markets, we show that this may be a profitable strategy for the firm. If so, it could be optimal for the government to increase the ad-valorem tax rate if the firm produces above the socially optimal quantity. This result differs markedly from findings in one-sided markets (e.g. Guesnerie and Laffont, 1978).

Our analysis is related to recent papers in Industrial Organization which study two-sidedness (e.g. Anderson and Coate, 2005, and Rochet and Tirole, 2003, 2007). This literature, however, does not study taxation. The public finance literature has a long tradition for investigating efficiency enhancing

¹Evans (2003) provides examples and classifications of two-sided markets.

taxation (see e.g. Anderson et al., 2001, and Auerbach and Hines, 2002), but to our knowledge the issue of two-sidedness has not received any attention. Our study seeks to remedy this oversight.

2 Model

We consider a two-sided market with two different groups of customers, where group i = 1, 2 buys x^i units of good i at price p^i . Each customer group has a quasi-linear utility function of the form

$$u^i = m^i + \phi^i\left(x^i, x^j\right)$$
 $i \neq j$ and $i = 1, 2,$

where $m^i \gtrsim 0$ is consumption of the outside good (the numeraire good).² For ease of exposition, we suppress the fact that $i \neq j$ and i, j = 1, 2 in the remainder of the text. The utility function $\phi^i(x^i, x^j)$ satisfies all the usual conditions for utility maximization, in particular that $\partial \phi^i/\partial x^i \equiv \phi^i_{x^i} > 0$ and $\phi^i_{x^ix^i} < 0$ (in what follows subscripts denote partial derivatives). If higher output of good j increases (decreases) the utility from good i we have $\phi^i_{x^j} > 0$ ($\phi^i_{x^j} < 0$).

We assume that both groups are price takers with budget constraints $\omega^i = m^i + p^i x^i$. Maximization of the utility function subject to the budget constraint for each group yields the inverse demand function for good i

$$p^{i}\left(x^{i}, x^{j}\right) = \phi_{x^{i}}^{i}\left(x^{i}, x^{j}\right). \tag{1}$$

The profit of a monopoly platform (or of a representative platform in a perfectly competitive market) equals

$$\pi = \sum_{i=1}^{2} \frac{(p^{i} - \tau^{i}) x^{i}}{(1 + t^{i})} - C(x^{i}, x^{j}), \qquad (2)$$

where $\tau^i \gtrsim 0$ and $t^i > -1$ are the per unit and ad valorem tax, respectively, on good i. The cost function $C(x^i, x^j) \geq 0$ satisfies $C_{x^i} > 0$ and $C_{x^i x^i} \geq 0$.

²We allow for $m^i < 0$ so that we do not have to consider corner solutions (see Mas-Colell, Whinston and Green, 1995).

2.1 The social optimum

A social planner chooses output to maximize the sum of consumer surplus minus the costs of providing the two goods. This amounts to solving

$$\{x^{1}, x^{2}\} = \arg\max\left\{\sum_{i=1}^{2} \phi^{i}(x^{i}, x^{j}) - C(x^{1}, x^{2})\right\}.$$

Given that the second-order conditions for interior solutions are satisfied, the socially optimal quantities (marked by an asterix) are implicitly given by

$$p^{i*} = C_{x^i} \left(x^{i*}, x^{j*} \right) - \phi_{x^i}^j \left(x^{i*}, x^{j*} \right). \tag{3}$$

By noting that

$$\phi_{x^{i}}^{j}\left(x^{i}, x^{j}\right) = \int_{0}^{x^{j}} \phi_{x^{i}x^{j}}^{j}\left(x^{i}, \tilde{x}^{j}\right) d\tilde{x}^{j} = \int_{0}^{x^{j}} p_{x^{i}}^{j}\left(x^{i}, \tilde{x}^{j}\right) d\tilde{x}^{j},\tag{4}$$

we can rewrite equation (3) as

$$p^{i*} = C_{x^i} \left(x^{i*}, x^{j*} \right) - \int_0^{x^{j*}} p_{x^i}^j \left(x^{i*}, \tilde{x}^j \right) d\tilde{x}^j.$$
 (5)

The term $\int_0^{x^{j*}} p_{x^i}^j(x^{i*}, \tilde{x}^j) d\tilde{x}^j$ in (5) measures the externality that the marginal unit of good i imposes on the total utility of customer group j. If this term is positive, the price of good i should be set below its marginal cost (and vice versa for the opposite constellation).

In what follows we discuss efficiency enhancing taxation in the competitive equilibrium as well as under monopoly. In either case it is worth pointing out that efficiency can be preserved for any distribution of the tax revenue among consumers. This is due to the quasi-linearity of the preferences.

2.2 Competitive equilibrium

A competitive firm maximizes (2) with respect to x^1 and x^2 , taking the end-user prices as given. In absence of taxes ($t^i = \tau^i = 0$) this yields the first-order condition for good i

$$p^{i}\left(x^{i}, x^{j}\right) = C_{x^{i}}\left(x^{i}, x^{j}\right). \tag{6}$$

Equation (6) shows that under perfect competition, each platform firm fails to account for the spillover in demand between the two goods. Depending on the sign of these spillovers, there will consequently be underprovision or overprovision of x^1 and x^2 relative to the first-best allocation. Market failure in provision can be corrected for by levying appropriate pigovian taxes, and it suffices to use either ad valorem or unit taxes. By comparing the two conditions in (5) to (6), we see that the competitive equilibrium yields first-best output if the per-unit pigovian tax scheme is characterized by

$$\tau^{i*} = -\int_0^{x^{j*}} p_{x^i}^j \left(x^{i*}, \tilde{x}^j \right) d\tilde{x}^j, \qquad t^1 = t^2 = 0.$$
 (7)

Alternatively, the government can use solely pigovian ad valorem taxes to achieve first-best outputs:

$$t^{i*} = -\frac{\int_0^{x^{j*}} p_{x^i}^j (x^{i*}, \tilde{x}^j) d\tilde{x}^j}{C_{x^i}}, \qquad \tau^1 = \tau^2 = 0.$$
 (8)

In both cases the sign of the optimal pigovian tax of good i is equal to the sign of the externality it imposes on the buyers of good j. If there are positive spillovers between the groups $(p_{x^j}^i > 0, i = 1, 2)$, both goods will be underprovided in the competitive equilibrium. A first-best solution can then be obtained by appropriately subsidizing the production of both goods.

3 Monopoly

Under imperfect competition the firms' price setting behavior on the two sides of the market may at least partially internalize demand spillovers. In order to abstract from strategic interactions, we only consider a monopoly platform. Let us again start out by considering the equilibrium if none of the goods are taxed. Differentiating (2) w.r.t. x^1 and x^2 and using (1), the platform's first-order conditions are now:

$$p^{i}(x^{i}, x^{j}) + x^{i} p_{x^{i}}^{i}(x^{i}, x^{j}) = C_{x^{i}}(x^{i}, x^{j}) - x^{j} p_{x^{i}}^{j}(x^{i}, x^{j}).$$
(9)

Compared to the first-order conditions in the competitive equilibrium there are two additional terms under monopoly. The first of these appears on the left-hand side of equation (9) and is well known; by selling one extra unit of good i, the platform will have to reduce the price of good i by $|p_{x^i}^i(x^i, x^j)|$ units. This generates a revenue loss equal to $|x^i p_{x^i}^i(x^i, x^j)|$. Taken in isolation, this term implies underprovision of commodity i due to monopoly pricing.

The last term on the right-hand side of equation (9) is also new compared to the competitive equilibrium. It captures the fact that a marginally higher output of good i increases the willingness to pay for good j by $p_{x^i}^j(x^i, x^j)$ units, generating extra income equal to $x^j p_{x^i}^j(x^i, x^j)$. This reduces the alternative cost of producing good i if $p_{x^i}^j > 0$, and acts like a reduction in the marginal costs of producing the good. Thereby the monopolist internalizes the intergroup externalities, but not perfectly so from a social point of view. To clarify this, we use equations (5) and (9) to define the difference in the spillovers internalized by the monopolist and the social planner as

$$\Omega^j \equiv x^j p_{x^i}^j - \int_0^{x^j} p_{x^i}^j d\tilde{x}^j. \tag{10}$$

The sign of Ω^j is in general ambiguous, showing that the monopolist may put higher weight on intergroup externalities than what a social planner would do.³ The reason is that the monopolist accounts for how a larger output of good i affects the willingness to pay for the marginal unit of good j, while a social planner also cares for the change in the valuation for inframarginal units. Suppose, for instance, that the externalities are positive $(p_{x^i}^j > 0)$ and that $p_{x^i}^j$ is increasing in x^j . In this case the value of the external-

ity is smaller on average than it is for the marginal unit, $\int_0^{x^j} p_{x^i}^j d\tilde{x}^j/x^j < p_{x^i}^j$, implying that $\Omega^j > 0$.⁴

The fact that Ω^j might be positive opens up the interesting possibility that the monopolist has too high output compared to the social optimum even if there are positive intergroup externalities. To see this, suppose that

³It is straightforward to give examples where Ω^i may be positive or negative.

⁴Note that this outcome resembles the result that a monopolist may oversupply quality compared to what a social planner would do for any given output. To see the analogy we may interpret a higher output of good i as having the effect of increasing the perceived quality of good j if $p_{x^i}^j > 0$. Thus, we may perceive the monopolist as choosing a too high quality level of good j (i.e., producing too much of good i) if the marginal willingness to pay for the "quality improvement" is higher than the increased average valuation (e.g. Tirole, 1988, pp. 100-104, Spence, 1975).

 x^i is exogenously given. Then there is a one-to-one relationship between p^j and x^j . Assuming that $x^i = x^{i*}$, it follows from equations (5) and (9) that $x^j > x^{j*}$ if $p^j < p^{j*}$, or

$$\Omega^i + x^j p_{x^j}^j > 0. (11)$$

We shall say that the monopoly has an overprovision incentive of good j if inequality (11) holds, while it has an underprovision incentive if the inequality is reversed. In what follows we examine how the government can use tax policy to correct for such over- and underprovision incentives. We start out by examining a case where the government only taxes one side of the market.

3.1 Only one good taxed

In a two-sided market a government will in general need two tax instruments to ensure that the monopolist provides the socially optimal outputs. However, the government can still use tax policy to improve resource allocation even if it taxes only one side of the market with either ad valorem or unit taxes.

3.1.1 Ad valorem taxes

Suppose that only good 1 is taxed. With an ad-valorem tax (and no unit taxes) we have

$$\pi = \frac{x^1 p^1}{1 + t^1} + x^2 p^2 - C(x^1, x^2).$$

Maximization of profit yields the following first-order conditions

$$\pi_{x^1} = \frac{p^1 + x^1 p_{x^1}^1}{1 + t^1} + x^2 p_{x^1}^2 - C_{x^1} = 0$$
 (12)

$$\pi_{x^2} = \frac{x^1 p_{x^2}^1}{1 + t^1} + p^2 + x^2 p_{x^2}^2 - C_{x^2} = 0.$$
 (13)

and the second-order conditions require

$$H = \pi_{x^1x^1}\pi_{x^2x^2} - \pi_{x^1x^2}^2 > 0, \quad \pi_{x^1x^1} < 0 \text{ and } \pi_{x^2x^2} < 0.$$

Taking the total differential of the first-order conditions yields:

$$\frac{dx^{1}}{dt^{1}} = \frac{-\pi_{x^{2}x^{2}} \left(x^{2} p_{x^{1}}^{2} - C_{x^{1}}\right)}{H\left(1 + t^{1}\right)} + \frac{1}{\left(1 + t^{1}\right)^{2}} \frac{-\pi_{x^{1}x^{2}} x^{1} p_{x^{2}}^{1}}{H}$$
(14)

$$\frac{dx^2}{dt^1} = \frac{\pi_{x^1x^2} \left(x^2 p_{x^1}^2 - C_{x^1} \right)}{H \left(1 + t^1 \right)} + \frac{1}{\left(1 + t^1 \right)^2} \frac{\pi_{x^1x^1} x^1 p_{x^2}^1}{H} \tag{15}$$

In order to have a two sided market, there must be positive externalities from at least one side of the market to the other.⁵ The implication of this is that $p_{x^j}^i > 0$ for at least one good. The interesting feature of equations (14) and (15) is that a higher value-added tax on good 1 may increase output of both goods. To illustrate this possibility, assume that the following holds:

Example: Suppose that; (a) $p_{x^1}^2 > 0$ and $p_{x^2}^1 = 0$; (b) $(x^2 p_{x_1}^2 - C_{x^1}) > 0$, and; (c) $\pi_{x^1 x^2} > 0$.

With assumption (a) in the Example the willingness to pay for good 2 is increasing in the sales of good 1 $(p_{x^1}^2 > 0)$, while consumers of good 1 are indifferent about the output level of good 2 $(p_{x^2}^1 = 0)$. The latter implies that the last term on the right-hand side of (14) and (15) vanishes. We then have $dx^1/dt^1 > 0$ and $dx^2/dt^1 > 0$ if assumptions (b) and (c) hold.⁶

We thus see that a higher value-added tax might lead to higher sales, contrary to what is the standard result in one-sided markets. The reason is that a higher tax on good 1 makes it profitable for the firm to shift revenue from the more heavily taxed to the untaxed side of the market (good 2). To see why this induces the platform to increase production in the Example, note that a marginally higher output of good 1 increases the willingness to pay for good 2 by $p_{x_1}^2$ units. This gives rise to an extra income equal to $x^2p_{x_1}^2$. With our assumption that $(x^2p_{x_1}^2 - C_{x_1}) > 0$, the income gain is higher than the marginal cost of producing good 1. This explains why $dx^1/dt^1 > 0$. Since we further have presupposed that the marginal profitability of selling good 2

⁵See Evans (2003a,b) for an informal definition of two-sidedness and Rochet and Tirole (2003) for a formal definition.

⁶The condition (b) $(x^2p_{x^1}^2 - C_{x^1}) > 0$ is unambiguously satisfied for $C_{x^1} = 0$. This is particularly likely for electronic communications services. Consider for instance an internet newspaper which sells its product to x^1 readers and has an advertising volume equal to x^2 . A larger number of readers increases the advertisers willingness to pay for inserting an ad (generating an extra platform income equal to $x^2p_{x^1}^2$). Since the marginal cost of increasing the number of readers is approximately equal to zero, we have $(x^2p_{x^1}^2 - C_{x^1}) \approx x^2p_{x^1}^2 > 0$.

is increasing in output of good 1 $(\partial \pi_{x^2}/\partial x^1 = \pi_{x^1x^2} > 0)$, it follows directly that $dx^2/dt^1 > 0$.

Note that the results which follow from the example are strengthened if we relax the assumption $p_{x^2}^1 = 0$ to $p_{x^2}^1 \leq 0$, and that they survive at least in the neighborhood of $p_{x^2}^1 = 0$ if there are positive intergroup externalities across both customer groups. Hence, assumption (a) is not crucial. Neither is assumption (c), in that we still have $dx^1/dt^1 > 0$ even if $\pi_{x^1x^2} < 0$. However, since $\pi_{x^1x^2} < 0$ implies that the marginal profitability of good 2 is decreasing in x^1 , it follows that $dx^2/dt^1 < 0$. In this case we therefore get the interesting result that output of the good which is subject to a higher tax increases while output of the untaxed good falls.⁷

We shall now see what implications equations (14) and (15) have for the optimal tax policy. To this end, define welfare as the sum of consumer surplus (S^i) , producer surplus (π) , and tax revenue (T);

$$W = \underbrace{\phi^{1}(x^{1}, x^{2}) - x^{1}p^{1}}_{S^{1}} + \underbrace{\phi^{2}(x^{1}, x^{2}) - x^{2}p^{2}}_{S^{2}} + \pi + T, \tag{16}$$

where T is defined as

$$T = \frac{t^1}{1 + t^1} x^1 p^1.$$

Differentiating consumer surplus, profit and tax revenue with respect to t^1 and using the envelope theorem we obtain⁸

$$\frac{dS^{i}}{dt^{1}} = -\Omega^{i} \frac{dx^{j}}{dt^{1}} - x^{i} p_{x^{i}}^{i} \frac{dx^{i}}{dt^{1}}; \quad \frac{d\pi}{dt^{1}} = -\frac{x^{1} p^{1}}{(1+t^{1})^{2}} \text{ and} \qquad (17)$$

$$\frac{dT}{dt^{1}} = \frac{x^{1} p^{1}}{(1+t^{1})^{2}} + \frac{t^{1}}{1+t^{1}} \left[\left(p^{1} + x^{1} p_{x^{1}}^{1} \right) \frac{dx^{1}}{dt^{1}} + x^{1} p_{x^{2}}^{1} \frac{dx^{2}}{dt^{1}} \right].$$

With only one tax instrument it is generally not possible to achieve socially optimal outputs. However, by solving $dW/dt^1 = 0$ and assuming that the second-order conditions hold, we find that a second-best equilibrium can

⁷The price of good 2 will then rise, both because own quantity falls and because output of good 1 increases. See Kind, Koethenbuerger and Schjelderup (2006) for a detailed discussion of the sign of $\pi_{x^1x^2}$ and of how the strength and size of the externalities affect output responses to a tax increase.

⁸If the platform's first-order conditions yield an interior solution we have $\pi = \pi(x^1(t^1), x^2(t^1), t^1)$, so that $d\pi/dt^1 = \partial \pi/\partial t^1$.

be obtained by setting the tax rate equal to

$$\frac{\hat{t}^1}{1+\hat{t}^1} = \frac{\left(\hat{\Omega}^1 + \hat{x}^2 \hat{p}_{x^2}^2\right) \frac{d\hat{x}^2}{dt^1} + \left(\hat{\Omega}^2 + \hat{x}^1 \hat{p}_{x^1}^1\right) \frac{d\hat{x}^1}{dt^1}}{\left(\hat{p}^1 + \hat{x}^1 \hat{p}_{x^1}^1\right) \frac{d\hat{x}^1}{dt^1} + \hat{x}^1 \hat{p}_{x^2}^1 \frac{d\hat{x}^2}{dt^1}},\tag{18}$$

where the hat indicates that we consider equilibrium values (and derivatives evaluated at the equilibrium values).

Using the assumptions in the Example we can now sign the optimal tax rate in (18) as follows:⁹

$$\frac{\hat{t}^{1}}{1+\hat{t}^{1}} = \frac{\hat{x}^{2}\hat{p}_{x^{2}}^{2}}{\hat{d}t^{1}} + (\hat{\Omega}^{2} + \hat{x}^{1}\hat{p}_{x^{1}}^{1}) \underbrace{\hat{d}\hat{x}^{1}}_{dt^{1}}}_{(\hat{p}^{1} + \hat{x}^{1}\hat{p}_{x^{1}}^{1})} \underbrace{\hat{d}t^{1}}_{dt^{1}}.$$
(19)

Suppose that $(\hat{\Omega}^2 + \hat{x}^1 \hat{p}_{x^1}^1) < 0$. Other things equal the monopoly then has incentives to underprovide good 1. In order to correct for this, we see from equation (19) that the government must set a positive tax ($\hat{t}^1 > 0$). Thereby it induces the monopoly to increase production. A positive tax is warranted also if $(\hat{\Omega}^2 + \hat{x}^1 \hat{p}_{x^1}^1) > 0$ but not high enough to make the numerator in (19) positive. The reason why $\hat{t}^1 > 0$ in this case is that the monopoly always underprovides good 2 in absence of taxes (since a higher output of this good does not generate higher income on the other side of the market when $p_{x^2}^1 = 0$). Thus, the fact that $dx^2/dt^1 > 0$ makes it optimal to set a positive tax rate unless the overprovision incentive for good 1 is sufficiently high.

3.1.2 Unit taxes

In this section we assume that there are no ad valorem taxes and that the unit tax only falls on good 1. Profits can then be written as

$$\pi = x^1 (p^1 - \tau^1) + x^2 p^2 - C(x^1, x^2)$$

⁹From equation (12) we see that assumption (b) in the example implies that $(p^1 + x^1 p_{x^1}^1) < 0$.

Maximizing profit yields the first order conditions

$$\pi_{x^1} = p^1 - \tau^1 + x^1 p_{x^1}^1 + x^2 p_{x^1}^2 - C_{x^1} = 0$$
 (20)

$$\pi_{x^2} = x^1 p_{x^2}^1 + p^2 + x^2 p_{x^2}^2 - C_{x^2} = 0. (21)$$

The second order conditions are the same as under ad valorem taxation, and totally differentiating (20) and (21) we find

$$\frac{dx^1}{d\tau^1} = \frac{\pi_{x^2x^2}}{H} < 0 \qquad \frac{dx^2}{d\tau^1} = -\frac{\pi_{x^1x^2}}{H}.$$
 (22)

As in a one-sided market, we see that a higher specific tax on a good leads to lower output of that good. This simply reflects the fact that an increase in τ^1 is like an increase in the marginal costs of producing good 1. If the marginal profit of selling good 2 is increasing in output of good 1 $(\pi_{x^1x^2} > 0)$, the reduced output of good 1 further makes it optimal to reduce output of good 2 $(dx^2/d\tau^1 < 0)$. Otherwise the firm's tax burden will increase. We thus have an asymmetry between unit taxes and ad-valorem taxes; as shown above it might be optimal for the firm to increase output of a good which is subject to higher ad-valorem taxes.

Welfare is still given by (16), but tax revenue is now equal to $T = \tau x^1$. We also have a similar expression for the changes in consumer surplus as under ad valorem taxation, that is:

$$\frac{dS^1}{d\tau^1} = -\Omega^1 \frac{dx^2}{d\tau^1} - x^1 p_{x_1}^1 \frac{dx^1}{d\tau^1} \text{ and } \frac{dS^2}{d\tau^1} = -\Omega^2 \frac{dx^1}{d\tau^1} - x^2 p_{x_2}^2 \frac{dx^2}{d\tau^1}.$$
 (23)

For the changes in profits and tax revenue we have:

$$\frac{d\pi}{d\tau^1} = -x^1, \qquad \frac{dT}{d\tau^1} = x^1 + \tau^1 \frac{dx^1}{d\tau^1}.$$

Using this information in the expressions for change in welfare we find that $dW/d\tau^1 = 0$ implies

$$\hat{\tau}^1 = \left[\left(\hat{\Omega}^1 + \hat{x}^2 \hat{p}_{x^2}^2 \right) \frac{d\hat{x}^2}{d\tau^1} + \left(\hat{\Omega}^2 + \hat{x}^1 \hat{p}_{x^1}^1 \right) \frac{d\hat{x}^1}{d\tau^1} \right] \left[\frac{d\hat{x}^1}{d\tau^1} \right]^{-1}. \tag{24}$$

With the assumptions in the Example we have $dx^1/d\tau^1 < 0$ and $dx^2/d\tau^1 < 0$. If the monopoly has underprovision incentives for both goods $(\hat{\Omega}^i + \hat{x}^j \hat{p}_{x^j}^j < 0)$, we thus see that the government should subsidize production in order to

increase output, while it is optimal to tax production if $\hat{\Omega}^i + \hat{x}^j \hat{p}_{x^j}^j > 0$. These results are in accordance with insight from traditional tax analysis. Only if there exists an overprovision incentive for one good and an underprovision incentive for the other is the sign of the specific tax ambiguous.

3.2 Taxation of both goods

The government can achieve first-best outputs under monopoly by appropriately choosing unit or ad valorem taxes. Setting $t^1 = t^2 = 0$, it follows from equation (2) that the platform's first-order conditions in the presence of only unit taxes are equal to

$$p^{i}(x^{i}, x^{j}) = \tau^{i} - x^{i} p_{x^{i}}^{i}(x^{i}, x^{j}) - x^{j} p_{x^{i}}^{j}(x^{i}, x^{j}) + C_{x^{i}}(x^{i}, x^{j}).$$
 (25)

Equating the monopolist's equilibrium prices with those of a social planner (c.f. equation (5)), it follows that the optimal unit taxes are given by 10

$$\tau^{i*} = \Omega^{j*} + x^{i*} p_{x^i}^{i*}. \tag{26}$$

The intuition behind equation (26) is straightforward; the specific tax on good i should be positive (negative) if the monopoly otherwise oversupplies (undersupplies) the good.

The government can also reproduce the first best solution by use of ad valorem taxes. Setting $\tau^1 = \tau^2 = 0$, we find that the firm's first-order conditions equal

$$\pi_{x^1} = 0 = > \frac{p^1 + x^1 p_{x^1}^1}{1 + t^1} + \frac{x^2 p_{x^1}^2}{1 + t^2} - C_{x^1} = 0$$
 (27)

$$\pi_{x^2} = 0 = > \frac{x^1 p_{x^2}^1}{1 + t^1} + \frac{p^2 + x^2 p_{x^2}^2}{1 + t^2} - C_{x^2} = 0.$$
 (28)

Using the same procedure as under unit taxes, it can be shown that the optimal ad valorem taxes that reproduce the first-best output levels are

$$t^{i*} = \frac{\left(p^{j*} + x^{j*}p_{x^{j}}^{j*}\right)\left(\Omega^{j*} + x^{i*}p_{x^{i}}^{i*}\right) - x^{j*}p_{x^{i}}^{j*}\left(\Omega^{i*} + x^{j*}p_{x^{j}}^{j*}\right)}{\left(p^{j*} + x^{j*}p_{x^{j}}^{j*}\right)C_{x^{i}}^{*} - x^{j*}p_{x^{i}}^{j*}C_{x^{j}}^{*}}.$$
 (29)

¹⁰Recall, variables marked by an asterix denote first-best allocations.

In order to see that it may be optimal to set a positive tax on good 1 if it is otherwise overproduced and vice versa, we continue to use the assumptions specified in the Example. From (29) we then find

$$t^{1*} = \underbrace{\frac{\left(p^{2*} + x^{2*}p_{x^2}^{2*}\right)\left(\Omega^{2*} + x^{1*}p_{x^1}^{1*}\right) + \left(x^{2*}\right)^{2}p_{x^1}^{2*}\left(-p_{x^2}^{2*}\right)}_{+}^{+} \underbrace{\left(p^{2*} + x^{2*}p_{x^2}^{2*}\right)C_{x^1}^{*} + \left(-x^{2*}p_{x^1}^{2*}C_{x^2}^{*}\right)}_{-}^{+}}_{(30)}$$

$$t^{2*} = \frac{x^{2*}p_{x^2}^{2*}}{C_{x^2}^{*}} < 0.$$

Given the assumption $p_{x^2}^1 = 0$ the monopoly does not have any externalities to internalize when it decides the output level of good 2. Totally differentiating first-order conditions (27) and (28) we therefore find that $\frac{dx^2}{dt^2} = -\frac{p^2 + x^2 p_{x^2}^2}{(1+t^2)^2} \left(\frac{-\pi_{x^2 x^2}}{H}\right) < 0$, similar to what we would have in a onesided market. Since the good in absence of taxes is undersupplied compared to social optimum, we consequently get the standard result that $t^{2*} < 0$.

Whether also t^{1*} is negative depends on the sizes of $(\Omega^{2*} + x^{1*}p_{x^1}^{1*})$ and C_{x1}^{*} . To see why, suppose in accordance with the assumptions in the Example that the marginal costs of producing good I are "low". We then know that $dx^{1}/dt^{1} > 0.12$ If the firm otherwise overproduces good 1 $(\Omega^{2*} + x^{1*}p_{x^{1}}^{1*} > 0)$, the government would like the firm to produce less of it. This can be achieved by setting a negative tax rate $(t^{1*} < 0)$. If the underprovision incentive for good 1 is sufficiently strong $(\Omega^{2*} + x^{1*}p_{x^1}^{1*} << 0)$, on the other hand, it is optimal for the government to set $t^1 > 0$. This positive tax induces the monopoly to produce more of good 1. Note that these results are qualitatively equivalent to those we arrived at when only Good 1 was taxed.

Finally, it should be noted that the crucial assumption in our working example is that $(x^2p_{x^1}^2 - C_{x^1}) > 0$; the assumptions that $\pi_{x^1x^2} > 0$ and

¹¹ Note that with $t^2 < 0$ and $x^2 p_{x^1}^2 - C_{x^1} > 0$ we have $(p^1 + x^1 p_{x^1}^1) < 0$. This follows from the first-order condition (27).

¹²With two ad valorem taxes the quantity response is equivalent to equation (14) except that $p_{x^1}^2$ has to be replaced by $\frac{1}{1+t^2}p_{x^1}^2$. In this case assumption (b) reads $\frac{1}{1+t^2}x^2p_{x^1}^2 - C_{x^1}$.

¹³When $(\Omega^2 + x^1p_{x_1}^1) > 0$ and C_{x^1} is "small" the numerator in (30) is positive and the

denominator negative.

 $p_{x^2}^1=0$ are made only to verify as simply as possible that output responses to a higher tax and the sign of the optimal taxes may be the opposite of those we typically find in one-sided markets. If in contrast $(x^2p_{x^1}^2-C_{x^1})<0$, tax responses are more likely to be qualitatively similar in one-sided and two-sided markets. This makes intuitive sense, since the two-sidedness is then not very pronounced.

4 Conclusion

In this paper we have shown that in absense of taxes, a monopoly platform in a two-sided market may have too high outputs compared to the social optimum. We have also identified situations where higher value-added taxes increase output, such that a negative VAT rate (subsidy) may be warranted if the monopoly otherwise produces too much. These results are in sharp contrast to those we typically find in one-sided markets, and they are more probable the smaller the marginal production costs and the larger the marginal value of the externalility of a taxed good. Through a formal analysis we have further demonstrated that the signs of the optimal VAT rates may be the opposite to those of the optimal specific taxes. In particular, while a higher VAT rate in some cases increases output, the monopoly will always produce less of a good that faces a higher specific tax. The reason is that there is a one-to-one relationship between tax payments and quantity under specific taxes, while there is no direct link between output and the burden of taxation under ad valorem taxation. In fact, subsequent to a higher ad valorem tax the firm can in principle both reduce tax payments and increase the quantity by lowering the price.

References

- [1] Anderson, P.S. and Coate, S., 2005. Market Provision of Broadcasting: A Welfare Analysis. Review of Economic Studies 72, 947-972.
- [2] Auerbach, A. and Hines, J., 2002. Taxation and Economic Efficiency. In: A. Auerbach and M. Feldstein, eds., Handbook of Public Economics, vol. 3, Chapter 21. North-Holland.

- [3] R. Guesnerie and Laffont, J., 1978. Taxing price makers. Journal of Economic Theory 19, 423–455.
- [4] Evans, D. S., 2003a. Some Empirical Aspects of Multi-Sided Platform Industries. Review of Network Economics 2, 191 209.
- [5] Evans, D.S., 2003b. The Antitrust Economics of Two-Sided Markets. Yale Journal of Regulation 20, 325-381.
- [6] Keen M. and Delipalla, S., 1992. The comparison between ad valorem taxes and specific taxation under imperfect competition. Journal of Public Economics 49, 351-367.
- [7] Kind, H.J., Koethenbuerger, M., and Schjelderup, G., 2006. Taxation in Two-Sided Markets, CESifo WP No. 1871, Munich.
- [8] Mas-Colell, A., Whinston, M.D, and Green, J.R., 1995. Microeconomics Theory. New York: Oxford University Press.
- [9] Rochet, J.C., and Tirole, J., 2003. Platform Competition in Two-Sided Markets. Journal of the European Economic Association 1, 990-1029.
- [10] Rochet, J.C. and Tirole, J., 2006. Two-Sided Markets: A Progress Report. Rand Journal of Economics (forthcoming).
- [11] Spence, M., 1975. Monopoly, Quality and Regulation. The Bell Journal of Economics 6, 417-429.
- [12] Tirole, J., 1988. Industrial Organization, Massachusetts, MIT Press.

CESifo Working Paper Series

for full list see www.cesifo-group.org/wp (address: Poschingerstr. 5, 81679 Munich, Germany, office@cesifo.de)

- 2196 Antonis Adam, Margarita Katsimi and Thomas Moutos, Inequality and the Import Demand Function, January 2008
- 2197 Helmut Seitz, Democratic Participation and the Size of Regions: An Empirical Study Using Data on German Counties, January 2008
- 2198 Theresa Fahrenberger and Hans Gersbach, Minority Voting and Long-term Decisions, January 2008
- 2199 Chiara Dalle Nogare and Roberto Ricciuti, Term Limits: Do they really Affect Fiscal Policy Choices?, January 2008
- 2200 Andreas Bühn and Friedrich Schneider, MIMIC Models, Cointegration and Error Correction: An Application to the French Shadow Economy, January 2008
- 2201 Seppo Kari, Hanna Karikallio and Jukka Pirttilä, Anticipating Tax Change: Evidence from the Finnish Corporate Income Tax Reform of 2005, January 2008
- 2202 Walter Krämer and André Güttler, On Comparing the Accuracy of Default Predictions in the Rating Industry, January 2008
- 2203 Syed M. Ahsan and Panagiotis Tsigaris, The Efficiency Loss of Capital Income Taxation under Imperfect Loss Offset Provisions, January 2008
- 2204 P. Mohnen, F. C. Palm, S. Schim van der Loeff and A. Tiwari, Financial Constraints and other Obstacles: Are they a Threat to Innovation Activity?, January 2008
- 2205 Sascha O. Becker and Mathias Hoffmann, Equity Fund Ownership and the Cross-Regional Diversification of Household Risk, January 2008
- 2206 Pedro R. D. Bom and Jenny E. Ligthart, How Productive is Public Capital? A Meta-Analysis, January 2008
- 2207 Martin Werding, Ageing and Productivity Growth: Are there Macro-level Cohort Effects of Human Capital?, January 2008
- 2208 Frederick van der Ploeg and Steven Poelhekke, Globalization and the Rise of Mega-Cities in the Developing World, February 2008
- 2209 Sara Biancini, Regulating National Firms in a Common Market, February 2008
- 2210 Jin Cao and Gerhard Illing, Liquidity Shortages and Monetary Policy, February 2008
- 2211 Mathias Kifmann, The Design of Pension Pay Out Options when the Health Status during Retirement is Uncertain, February 2008

- 2212 Laszlo Goerke, Tax Overpayments, Tax Evasion, and Book-Tax Differences, February 2008
- 2213 Jun-ichi Itaya and Heinrich W. Ursprung, Price and Death, February 2008
- 2214 Valentina Bosetti, Carlo Carraro and Emanuele Massetti, Banking Permits: Economic Efficiency and Distributional Effects, February 2008
- 2215 Assar Lindbeck, Mårten Palme and Mats Persson, Social Interaction and Sickness Absence, February 2008
- 2216 Gary E. Bolton and Axel Ockenfels, The Limits of Trust in Economic Transactions Investigations of Perfect Reputation Systems, February 2008
- 2217 Hartmut Egger and Peter Egger, The Trade and Welfare Effects of Mergers in Space, February 2008
- 2218 Dorothee Crayen and Joerg Baten, Global Trends in Numeracy 1820-1949 and its Implications for Long-Run Growth, February 2008
- 2219 Stephane Dees, M. Hashem Pesaran, L. Vanessa Smith and Ron P. Smith, Identification of New Keynesian Phillips Curves from a Global Perspective, February 2008
- 2220 Jerome L. Stein, A Tale of Two Debt Crises: A Stochastic Optimal Control Analysis, February 2008
- 2221 Michael Melvin, Lukas Menkhoff and Maik Schmeling, Automating Exchange Rate Target Zones: Intervention via an Electronic Limit Order Book, February 2008
- 2222 Raymond Riezman and Ping Wang, Preference Bias and Outsourcing to Market: A Steady-State Analysis, February 2008
- 2223 Lars-Erik Borge and Jørn Rattsø, Young and Old Competing for Public Welfare Services, February 2008
- 2224 Jose Apesteguia, Steffen Huck, Jörg Oechssler and Simon Weidenholzer, Imitation and the Evolution of Walrasian Behavior: Theoretically Fragile but Behaviorally Robust, February 2008
- 2225 Walter Krämer, Long Memory with Markov-Switching GARCH, February 2008
- 2226 António Afonso and Christophe Rault, What do we really Know about Fiscal Sustainability in the EU? A Panel Data Diagnostic, February 2008
- 2227 Sergey M. Kadochnikov and Igor M. Drapkin, Market Structure, Technological Gap and Vertical Linkage Effects from Foreign Direct Investment, February 2008
- 2228 Guglielmo Maria Caporale, Davide Ciferri and Alessandro Girardi, Fiscal Shocks and Real Exchange Rate Dynamics: Some Evidence for Latin America, February 2008

- 2229 Scott Alan Carson, Geography and Insolation in 19th Century US African-American and White Statures, February 2008
- 2230 Wolfgang Buchholz and Jan Schumacher, Discounting and Welfare Analysis Over Time: Choosing the η , February 2008
- 2231 M. Hashem Pesaran, Christoph Schleicher and Paolo Zaffaroni, Model Averaging in Risk Management with an Application to Futures Markets, February 2008
- 2232 Wilhelm Kohler, Offshoring: Why Do Stories Differ?, February 2008
- 2233 Stefan Bach, Giacomo Corneo and Viktor Steiner, Effective Taxation of Top Incomes in Germany, 1992-2002, February 2008
- 2234 Robert S. Chirinko, σ: The Long And Short Of It, February 2008
- 2235 Volker Grossmann and Holger Strulik, Should Continued Family Firms Face Lower Taxes than other Estates?, February 2008
- 2236 Guido Tabellini, The Scope of Cooperation: Values and Incentives, February 2008
- 2237 Heinrich W. Ursprung and Christian Wiermann, Reputation, Price, and Death: An Empirical Analysis of Art Price Formation, March 2008
- 2238 Hans Fehr and Christian Habermann, Private Retirement Savings in Germany: The Structure of Tax Incentives and Annuitization, March 2008
- 2239 Joseph Francois and Ian Wooton, Market Structure and Market Access, March 2008
- 2240 Hiroyuki Kasahara and Beverly Lapham, Productivity and the Decision to Import and Export: Theory and Evidence, March 2008
- 2241 Gary E. Bolton and Axel Ockenfels, Does Laboratory Trading Mirror Behavior in Real World Markets? Fair Bargaining and Competitive Bidding on EBay, March 2008
- 2242 Atsushi Oshima, B. Ravikumar and Raymond Riezman, Entrepreneurship, Organization Capital and the Evolution of the Firm, March 2008
- 2243 Walter Krämer and Sebastian Schich, Large-Scale Disasters and the Insurance Industry, March 2008
- 2244 Leif Danziger, Adjustment Costs, Inventories and Output, March 2008
- 2245 Anne van Aaken, Lars P. Feld and Stefan Voigt, Power over Prosecutors Corrupts Politicians: Cross Country Evidence Using a New Indicator, March 2008
- 2246 Hans-Christian Heinemeyer, Max-Stephan Schulze and Nikolaus Wolf, Endogenous Borders? The Effects of New Borders on Trade in Central Europe 1885-1933, March 2008

- 2247 Johannes Becker and Clemens Fuest, Tax Competition Greenfield Investment versus Mergers and Acquisitions, March 2008
- 2248 Giorgio Bellettini and Hubert Kempf, Why not in your Backyard? On the Location and Size of a Public Facility, March 2008
- 2249 Jose Luis Evia, Roberto Laserna and Stergios Skaperdas, Socio-Political Conflict and Economic Performance in Bolivia, March 2008
- 2250 Bas Jacobs and A. Lans Bovenberg, Optimal Taxation of Human Capital and the Earnings Function, March 2008
- 2251 Jan-Egbert Sturm and Timo Wollmershäuser, The Stress of Having a Single Monetary Policy in Europe, March 2008
- 2252 Guido Schwerdt, Labor Turnover before Plant Closure: 'Leaving the Sinking Ship' vs. 'Captain Throwing Ballast Overboard', March 2008
- 2253 Keith E. Maskus and Shuichiro Nishioka, Development-Related Biases in Factor Productivities and the HOV Model of Trade, March 2008
- 2254 Jeremy Edwards and Sheilagh Ogilvie, Contract Enforcement, Institutions and Social Capital: the Maghribi Traders Reappraised, March 2008
- 2255 Imed Drine and Christophe Rault, Purchasing Power Parity for Developing and Developed Countries. What can we Learn from Non-Stationary Panel Data Models?, March 2008
- 2256 Scott Alan Carson, Health, Wealth and Inequality: a Contribution to the Debate about the Relationship between Inequality and Health, March 2008
- 2257 C.A.E. Goodhart, The Regulatory Response to the Financial Crisis, March 2008
- 2258 Stefan Bauernschuster, Oliver Falck and Stephan Heblich, The Impact of Continuous Training on a Firm's Innovations, March 2008
- 2259 Michael Grimm and Stephan Klasen, Geography vs. Institutions at the Village Level, March 2008
- 2260 Fwu-Ranq Chang, Property Insurance, Portfolio Selection and their Interdependence, March 2008
- 2261 J. Atsu Amegashie and Marco Runkel, The Paradoxes of Revenge in Conflicts, March 2008
- 2262 Hans Jarle Kind, Marko Koethenbuerger and Guttorm Schjelderup, Efficiency Enhancing Taxation in Two-sided Markets, March 2008