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## Finance, Trade, Man and Machines: A New-Ricardian Heckscher-Ohlin-Samuelson Model

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# Finance, Trade, Man and Machines: A New-Ricardian Heckscher-Ohlin-Samuelson Model

## Abstract

This paper attempts to build up a Heckscher-Ohlin-Samuelson model of production and trade where capital is introduced outside the production process as a financial capital or credit as per the classical Ricardian wage fund framework. Stock of credit or financial capital as past savings, finances employment and machines or capital goods used in the process of production with Ricardian fixed coefficient technology. We derive the relationship between factor prices and rate of interest on one hand and relative price and endowments on the other. Availability of finance does not impact production or pattern of trade only nominal factor prices. International financial flows will not alter pattern of trade, but movement of labour and machines will. Such results change drastically when we consider a model with unemployment and finance dictates real outcomes much more than before. Introducing finance affects trade patterns with unemployment and especially with imperfect credit markets. The results could explain a vast array of stylized facts such as, financial crisis or shock, credit rationing and their impact on production, trade and unemployment. The paper has policy implications for role of financial development, quality of institutions in economic development.

JEL-Codes: B120, B130, B170, F110, F630, F650, F160, O120.

Keywords: wage-fund, Heckscher-Ohlin-Samuelson, Ricardo, inequality, credit, general equilibrium, financial development, unemployment, trade.

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## 1. Introduction

Importance of finance or credit for carrying out production for trade has received much less attention. This is different from common parlance of typical ‘trade-finance’ literature where the focus hinges essentially on financing of trade and commercial transactions so as to ‘mitigate, or reduce, the risks involved in international trade transaction’, involving two parties, exporter and importer.<sup>1</sup> In this paper we deal with the issue where credit finances purchase of factor input services like labor costs, capital goods, and other material inputs, and what are consequences of changes in availability of such ‘financial capital’ to alter production structure, trade patterns, and factor returns.

The core reason for engaging in this exercise is that the literature in trade and finance till date has not made use of the wage fund approach in modern trade theory, although wage fund is possibly the earliest framework of introducing financial capital in analysing issues related to trade and growth (Ricardo 1817). Moreover, the usual way of bringing in the impact of financial problems in trade models has been to consider the role of trade finance. For example, in an empirical paper Chor and Manova (2012) has discussed the adverse impacts of tightened credit conditions and especially the access to trade credit on exports volume. In another paper, Manova (2013) has extended the analysis with similar implications, but in a firm-heterogeneity model with imperfect competition (product differentiation), and highlights the role of financial market imperfections and institutional frictions in shaping trade volume.

All these highlight the significance of introducing financial capital into conventional workhorse of Neo-classical trade models such as, Ricardo, Specific Factor and Heckscher-Ohlin-Samuelson. Lack of financial capital or barriers to access credit could impair firms’ performance, trade, and could tell upon economic growth and employment. Our papers fill this gap. Incorporating wage-fund theory, entrepreneurial finance and borrowing constraints in the traditional GE model is a novel mechanism. Wage fund theory was developed in the Classical models of Ricardo (1817) and J. S. Mill (1848), but unlike the classical notion, its Neo-Classical treatment considered the features of diminishing returns (DMR)-see Hicks and Hollander (1977), Steedman (1979), Mansechi et al. (1983), Findlay (1984). This paper builds upon precursors, viz., Marjit and Das (2021) and Marjit and Nakanishi (2021) by incorporating finance in a conventional general equilibrium model of HOS structure using the classical or Ricardian perspective on Wage Fund hypothesis.

The fundamental question we try to address in this paper is –How significant is the role of availability of finance in a standard HOS trade model when financial capital is necessary to purchase the services of labour and machines or capital goods to produce final goods? The answer to this question is critical to assess the mechanism of how finance is likely to affect the key variables of the system. Only then, we can evaluate what financial crisis should do the international trading system in terms of its impact on output, pattern of trade, factor prices, factor mobility etc. In this context, we prove two sets of interesting results in our fully specified general equilibrium HOS model.

Without any distortions in the system, shortage of finance does not affect production or pattern of trade in a HOS model. But, it does affect factor prices as it affects interest rates and hence can induce factor

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<sup>1</sup> See Global Trade Review for overview <https://www.gtreview.com/what-is-trade-finance/>. The issue of financing of trade, such as, exports and imports are not touched upon in this paper, as our focus is different. However, this could be extended.

movements thus affecting the pattern of trade. However, international mobility of finance does not change production or trade but alters income distribution.

These results change drastically in a model with unemployment. Finance plays a much more significant role and hence shortage of finance, hallmark of nations under siege of financial crisis, would affect each real variable starting with employment. In a way without such a distortion, our framework partly emanates the classical macroeconomic flavour where money does not matter and with wage distortion, it has Keynesian outcome.

Relatively modern treatments of classical models with neo-classical flavour such as, Hicks and Hollander(1977), Findlay (1984,1995), Steedman (1979) etc. were usually interested with modelling agriculture with diminishing returns and industry with unlimited supplies of labour at a given level of subsistence real wage. Marjit (2020), Marjit and Das (2021), and Marjit and Nakanishi (2021) have tried to explore the implication of wage fund or stock of credit in a full employment Ricardian trade model, introducing finance or credit in an otherwise well-known text book version of the model. Such an inclusion yields many results of a typical Neo-Classical production theory. It completely replicates Solow (1956) and its antecedents such as optimal growth theory (Ramsey 1928, Cass 1965, Koopmans 1965).

However, here we reconstruct the Jones (1965) framework which is still hailed as a major contribution ( See Markusen 2021, Jones 2018), the building block of the trade models, to include 'Capital (K)' construed as financial capital used to finance homogeneous labor costs, and machines or capital goods (which embodies the role of physical capital simultaneously working with the labor (L))<sup>2</sup>. In this paper, capital is not used 'directly' as a factor of production within the production process, it is represented as finance that makes production possible. Thus, unlike the canonical Neo-classical models capital operates *outside* the production process to replicate the 2X2 model with two-sectors, two inputs. We have a given supply of labour (L) and stock of machines (M) that are needed to be used in the production of two goods X and Y. But the wage bill and the expenses to acquire 'M' require finance at the beginning of the period. Total value of payments for wage bills and capital equipment or machines must equal 'K', the stock of credit or finance. At the end of the period, outputs (X and Y) are sold, revenues are generated and financiers, owners of 'K' are paid back in terms of the principal and interest (r). Thus, the system starts with stock of K, L, and M and the general equilibrium generates the wage (w), price of machines ( $p_m$ ) and interest rate 'r', along with outputs of X and Y and relative price  $P_x/P_y$  given a (relative) demand function. The major purpose of this paper is to highlight what role finance, i.e., K plays in such a model, in terms of production, factor prices and trade pattern. This is novel with financial capital. Finance or credit in Neo-Classical trade theory is not very common. In fact, role of imperfect credit market in a proper trade theoretic framework has been discussed by Jones and Marjit (2001), Matsuyama(2005), Antras and Caballero(2009), Manova (2008), Manova(2013), Manova et al. (2009), Amiti and Weinstein (2011), Egger and Keuschnigg (2015), Marjit and Misra(2020), etc. This is about how finance alters fundamental trade theorems and related theoretical outcomes.

Our purpose and framework are entirely different from these papers. *Firstly*, we want to explore what happens when finance is introduced in a standard competitive general equilibrium model. As such it belongs to the class of more recent works on the usefulness of competitive trade models, such as

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<sup>2</sup> We can conceive this as putty-clay type where flexibility or malleability of capital goods is maintained. 'M' is produced means of production, which is used as intermediate input for final good production.

Jones and Marjit(1985, 2003, 2009), Marjit and Kar(2018), Jones(2018), Marjit Mandal and Nakanishi(2020), Das (2013), etc. *Second*, because we do not use standard and neo-classical production model but a framework, which is Ricardian in nature, we bring in classical wage fund hypothesis to introduce financial capital and debits after withdrawing capital from within the product process. Another purpose is to compare the theoretical insights derived from this new Ricardian structure with the well-known trade theorems. *Third*, we will explore how this innovation could provide some fresh perspectives on some contemporary issues of relevance. For example, how financial crisis or unanticipated financial shocks affect the entire system or, how international financial flows, trade flows and factor flows are interrelated, and last but not the least, whether men and machines are helped or hurt by trade etc. This is very pertinent in the context of emergence of fourth industrial revolution or use of artificial intelligence (AI) or ICT causing disruptions in sectoral adjustments.

The results that we derive here are as follows: (i) with full-employment, level of finance does not affect the pattern of trade, only influences factor prices and interest rate; (ii) even without trade in goods, factors of production and financial capital could be traded without any change in the relative returns to labour and machines and relative prices; (iii) direction of financial flow is *reverse* of the direction of factor flows. Goods trade can lead to financial flows in any direction depending on financing intensity of man and machines.

Interestingly, we retain the Stolper–Samuelson and Rybczynski type result or magnification outcomes as formalized in Jones(1965, 2018) as in this framework existence of finance does not disturb these. However, *absolute values* of factor prices are uniquely affected by the availability of finance.

The paper is laid out as follows. In the second section, we develop the model and describe the determination of equilibrium, pattern of trade, role of credit and factor flows, and compare with standard HOS results. The third section considers endowment and price effects, while we introduce two critical extensions of the model in terms of factor flows, and fixed wage and unemployment, imperfect credit market in the fourth section. The last section concludes.

## 2. Model and Equilibrium

The economy produces two goods X and Y with labour (L) and machines (M) with *fixed coefficient* production functions. We deliberately abstract from possibilities of substitution to retain the Ricardian flavour, thus, features of DMR and/or, DMP are set aside. Thus, factor-substitution is ruled out. At the beginning of the period the economy inherits K as the stock of credit of finance to be invested in production, a given supply of labour L and a stock of machines.<sup>3</sup> Demand for credit (K) is induced via demand for ‘L’ and ‘M’ and resultant cost. Thus, credit market equilibrium must enforce that ‘K’ is sufficient to finance (WL + P<sub>M</sub>.M) where ‘W’ is the wage rate and p<sub>m</sub> is the price of machines, to be determined via

$$K=WL + p_m.M \quad (1)$$

Production involves time. At the beginning of the period labour is hired and machines are purchased, financed by loans from the bank or financiers. After production and sale are over, the

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<sup>3</sup> In a dynamic model, ‘K’ can change as in say, via typically perpetual inventory accumulation over time.

borrowed amount is returned with interest 'r'.<sup>4</sup> With perfectly competitive markets, price of goods will be just sufficient to cover average wage cost, machine cost and interest payments. The notations are as follows:

$a_{ij}$  : fixed unit input requirement of 'i' per unit of  $j^{\text{th}}$  product,  $i \in \{L, M\}$  and  $j \in \{X, Y\}$ .

$a_{Lj}$  : fixed unit labor requirement per unit of  $j^{\text{th}}$  product,  $j \in \{X, Y\}$ .

$a_{Mj}$  : fixed per unit requirement of capital equipment for the  $j^{\text{th}}$  product.  $j \in \{X, Y\}$ .

$\lambda_{ij}$  : endowment shares of  $i^{\text{th}}$  resource in the production of X, Y

$\theta_{ij}$  : Cost-shares of  $i^{\text{th}}$  resource in the production of X, Y

$P_j$  : final good prices for  $j \in \{X, Y\}$ .

$p_M$  : unit price of the machines.

$P$  : relative price of X i.e.  $P = \frac{P_X}{P_Y}$ . 'Y' is the numeraire good (i.e.,  $P_Y = 1$ ).

$\hat{V}$  : proportional changes of any generic variable, V, such that  $\hat{V} = \frac{dV}{V}$

The following system of Competitive price equations [i.e., (2) and (3)], and the full-employment conditions [viz., (4) and (5)] for primary factor 'L and material inputs 'M' determine the supply side of the model as below:

$$[Wa_{Lx} + p_M a_{Mx}] (1+r) = P \quad (2)$$

$$[Wa_{Ly} + p_M a_{My}] (1+r) = 1 \quad (3)$$

$$a_{Lx}X + a_{Ly}Y = L \quad (4)$$

$$a_{Mx}X + a_{My}Y = M \quad (5)$$

where (2)-(3) are competitive price conditions,  $P = AC$  (average cost), and (4)-(5) are full employment constraints. With a given credit size 'K', specific size of the labor force, and fixed stock of machines at a point in time, with full-employment of resources certain level of 'W' and ' $p_M$ ' are paid to the workers and the industrialists owning the machines of certain vintage. Given fixed coefficients  $a_{ij}$ ,  $\bar{L}$ , and  $\bar{M}$ , X and Y are determined by (4) and (5) and depend only on (L, M) and technology, independent of P and K. From (2) and (3), W and  $p_M$  are determined as functions of P and (1+r). Given (exogenous) P, we plug that into (1) to solve for (1+r). Given P, L, M, r and  $a_{ij}$ 's where  $i \in \{L, M\}$ , we determine W,  $p_M$ , X, and Y from Equations (2)–(5). L and M are given as stocks of labor and machine from the last period. Hence,

<sup>4</sup> However, we do not build intertemporal framework but as in different static equilibrium, production and sales occur at a single point of time. Without sale proceeds to pay interest rate, at a particular time period 'credit-capital' can't be borrowed. Extending the model to 3-Sector with skill-unskilled split would transform the equation (1) as  $K = WL + P_m.M + W_s.S$ , where S is skilled and  $W_s$  is their wage. That does not change the pivotal elements of the paper.



$$K^d = W(r).L + p_M(r).M \quad (6)$$

where  $K^d$  is demand for capital. 'P' is given and hence suppressed in  $W(r)$  and  $p_M(r)$ .

$$\text{As } W' < 0 \text{ and } p'_M < 0, K'_d(r) = W'(r).L + p'_M(r).M < 0 \quad (7)$$

$$\text{Financial market equilibrium condition is given by: } \bar{K} = K_d(r) \quad (8)$$

Implication of (8) is that  $K_d$  is an inverse function of 'r', and as 'P' determines 'W' and 'p<sub>M</sub>', and hence 'r'.

Right hand side (RHS) of (8) is demand for credit ( $K_d$ ) to equilibrate with supply ( $\bar{K} = K_s$ ). Eq. (8) determines 'r' in equilibrium. Since (P, L, M, K) are parameters,

$$r = r(P, \bar{L}, \bar{M}, \bar{K}) \quad (9)$$

One can easily show using Caves, Frankel and Jones (2011) and Feenstra (2003) that, with '^' denoting proportional change:

$$\hat{X} - \hat{Y} = \alpha(\hat{M} - \hat{L})$$

where  $\alpha = \frac{1}{\lambda_{MX} - \lambda_{MY}} > 0$ , and due to intensity assumption  $\lambda_{MY} < \lambda_{MX}$ . Or, via integration

$$\left[ \frac{X}{Y} \right]^s = f \left[ \frac{M}{L} \right], f' > 0 \quad (10a)$$

This is relative supply (RS) of X vis-à-vis Y with  $f' > 0$ .

We assume negatively sloped homothetic demand to express Relative Demand (RD) as below:

$$\left[ \frac{X}{Y} \right]^d = D(P), D' < 0 \quad (10b)$$

Using (10a) and (10b) RS-RD conjointly determine market-clearing for X and Y so that equilibrium  $P = P_e$  can be expressed as .

$$P_e = F \left( \frac{M}{L} \right), F' < 0 \quad (10c)$$

This completes the determination of the general equilibrium. Thus, we determine X, Y; W, (1+r), p<sub>M</sub>, P and RD. Equation (1) representing credit-constraint plays crucial role to internalize the demand and supply of 'L' and 'M' as it represents matching demand and supply via two full-employment conditions.

### 3. Comparative Static Changes.<sup>5</sup>

We consider the following parametric changes—changes in P (exogenous) and changes in K—to compare and contrast with the conventional HOS setup.

<sup>5</sup> For parsimony, most of the detailed derivations are relegated to the Appendices 1, 2 and 3.

### 3.1 Price Effects

Following CFJ (2011)—using (2) and (3) and assuming  $\widehat{P} = 0$  --we derive that:

$$\widehat{W}\theta_{LX} + \widehat{p}_M\theta_{MX} = -\widehat{(1+r)} \quad (11a)$$

$$\widehat{W}\theta_{LY} + \widehat{p}_M\theta_{MY} = -\widehat{(1+r)} \quad (11b)$$

$$\text{where } \theta_{LX} + \theta_{MX} = \theta_{LY} + \theta_{MY} = 1$$

Assume X is relatively M-intensive and Y is relatively L-intensive. Also,  $\theta_{MX} > \theta_{MY}$  and equivalently,  $\theta_{LY} > \theta_{LX}$ . Hence,  $|\theta| = \theta_{LX}\theta_{MY} - \theta_{MX}\theta_{LY} = \theta_{MY} - \theta_{MX} = \theta_{LX} - \theta_{LY} \Rightarrow |\theta| < 0$ . For our results, intensity ranking can be reversed without anticipating any significant changes.

Using (11a) and (11b), by Cramer's rule,  $\widehat{W} = \widehat{p}_M = -\widehat{(1+r)}$ . It is obvious that given P, from (2) and (3),  $(\widehat{W}, \widehat{p}_M) < 0$  if  $\widehat{(1+r)} > 0$ . As mentioned above (see Appendix 2), following Caves, Frankel and Jones (CFJ 2011) it is straightforward to show that

$$\widehat{W} = \widehat{P} \frac{\theta_{MY}}{|\theta|} \quad (12a)$$

$$\widehat{p}_M = -\widehat{P} \frac{\theta_{LY}}{|\theta|} \quad (12b)$$

which on simplification gives:

$$\widehat{p}_M - \widehat{W} = \frac{-\widehat{P}}{|\theta|} > 0, \text{ as } |\theta| < 0, \widehat{P} > 0$$

Equations (12a) and (12b) occur at a given 'r'. From (12a) and (12b), it can be inferred that:

$$\widehat{p}_M > \widehat{P} > 0 > \widehat{W} \quad (12c)$$

It is well-known magnification effect (Jones 1965, and CFJ 2011).

From (6), demand for credit and its allocation is given by derived demand for credit ( $K_d$ ) to finance costs of 'L' and 'M' such that  $\widehat{K}_d = \lambda_{LK}\widehat{W} + \lambda_{MK}\widehat{p}_M$  (13)

Here,  $\lambda_{LK}$  is share of credit-finance  $K_d$  devoted to wage bill (for labor services) and purchasing capital goods so that  $\lambda_{LK} + \lambda_{MK} = 1$ . This indirectly affects production via financing equipment purchase.

$$\text{Furthermore, using (12a\&b), } \widehat{K}_d = \frac{\widehat{P}}{|\theta|} [\lambda_{LK}\theta_{MY} - \lambda_{MK}\theta_{LY}] \quad (14)$$

$$\text{Eq. (14) suggests that when } |\theta| < 0, \text{ if } \widehat{P} > 0, \widehat{K}_d < 0 \text{ iff } \lambda_{LK}\theta_{MY} > \lambda_{MK}\theta_{LY} \quad (15)$$

Using (13), we write  $\widehat{K}_d = -\widehat{(1+r)} = \frac{r\widehat{r}}{(1+r)} = \widehat{K}_d[\widehat{(1+r)}, \widehat{W}, \widehat{p}_M]$ , (15a)

Demand for credit or finance drops with a rise in 'P' as 'W' drops and share of investment in 'L' is relatively large, i.e., high  $\lambda_{LK}$  and/or, drop in W is large, i.e., high  $\theta_{MY}$ . Thus,  $K_d$  can rise or fall and given  $K_s = \bar{K}$ , 'r' can also rise or fall simultaneously as  $K'_d < 0$  to clear the financial market. Given (1+r), with rise in P (=  $P_X$ ),  $\widehat{X} > 0$ , demand for 'M' rises (as X is relatively more M-intensive), resulting in rise in ' $p_M$ ' with  $K_s = \bar{K}$ , and eventually (1+r) will rise as  $K_d$  rises, given  $\lambda_{LK}$ , via Eq. (15). Intuitively speaking, when ' $p_M$ ' rises and 'W' falls higher value of  $\lambda_{MK}$  compared to  $\lambda_{LK}$  will imply ' $K_d$ ' will increase pushing (1+r) upward to rise. Higher value of  $\lambda_{LK}$  will mean ' $K_d$ ' will shrink and correspondingly, (1+r) falls.

Note that  $(\widehat{W} - \widehat{p}_M)$  is independent of 'r'. That is,  $\frac{W}{P_M}$  remains the same whichever way 'r' moves. For

better understanding, we assume that  $\lambda_{LK}$  is low, so that  $\widehat{P} > 0$  will imply  $\widehat{K}_d > 0$  and  $\widehat{r} > 0$ . Hence, as 'P' goes up  $\frac{W}{P_M}$  will fall and 'r' will go up. One can think of the impact in two stages: first, given 'r',

'W' goes down and  $p_M$  goes up; second, as 'r' goes up both will drop. But,  $\frac{W}{P_M}$  remains the same. Given

L and M,  $\bar{K}$  determines the nominal value of these stocks determining 'r' and hence, from given 'P', determining 'W' and ' $p_M$ '. This leads us to write the following propositions.

**Proposition 1:**  $\widehat{r} \geq 0$  iff  $\widehat{P} > 0$  and  $\widehat{K}_d \geq 0$  iff  $\lambda_{MK}\theta_{LY} - \lambda_{LK}\theta_{MY} \geq 0 \Rightarrow \lambda_{MK}\theta_{LY} \geq \lambda_{LK}\theta_{MY}$

**Proof:** See the discussion above. From equation (14) and (15), effects on 'r' depends on relative-intensity of finance in sectors (i.e., whether M-intensive or L-intensive). See appendix 2 for derivation.

**Proposition 2:** Availability of finance does not affect  $\frac{W}{P_M}$ , but it affects absolute values of 'W' and ' $p_M$ '

via changes in 'r'.

**Proof:** Higher  $\bar{K}$  will reduce 'r' to equilibrate financial market, increasing (W,  $p_M$ ). But at a given P,  $\frac{W}{P_M}$

remains the same. (as discussed above). QED.

### 3.2 Endowment effects

**Proposition 3:** Given  $P = \bar{P}$ ,  $\widehat{L} = 0$ ,  $\widehat{M} = 0$ ,  $\widehat{K}_s > 0$  does not affect trade patterns.

**Proof:**  $\widehat{K}_d = 0$ ,  $\widehat{K}_s > 0$  means supply of credit increases resulting in lower (1+r) ( $\widehat{r} < 0$ ).

As  $\widehat{P} = 0$ , from Eq. (11a&b),  $\widehat{(1+r)} < 0$ . ' $p_M$ ' rises along with 'W'. Given  $\widehat{L} = 0$ ,  $\widehat{M} = 0$ , via Eq (10c), M/L is unaltered meaning RD-RS remains the same, with no change in relative prices  $P_e$ . Thus,  $\widehat{X} = 0$ ,  $\widehat{Y} = 0$ . Demand for L and M rises due to credit availability with fixed supply of resources causing  $p_M$  and W to

rise. Real wage is unaffected. This result is analogous to the canonical macroeconomic systems where credit is similar to money supply and it has neutrality (i.e., classical dichotomy is valid) in the same sense that it affects absolute factor prices  $p_M$  and  $W$ , but not the relative ones and the output itself as  $X$  and  $Y$  do not change.<sup>6</sup> This is similar to Marjit and Das (2021) in a Ricardian Specific Factor framework. With perfect financial market, competitive firms can get as much as they want at given 'r' and hence, it does not play an important role *unless imperfection is built in*. Differences in credit availability (i.e., finance) and its allocation across home and the foreign (or, the rest-of-the-world-ROW) will cause changes in factor prices (viz.,  $W$  and  $p_M$ ) via factor movements discussed in entirely different model in the literature (Mussa 1991, Lucas 1990, etc.).

#### 4. Further extensions:

##### 4.1 Factor Flows.

Denote foreign variables by '\*' Consider two economies-- home and foreign-- with endowments being  $M, M^*, L, L^*$ , and  $K, K^*$ . These endowments could be the same or different. With differences such that  $L \neq L^*$ , and  $M \neq M^*$ , no doubt trade will occur irrespective of  $K \geq K^*$ .

**Proposition 4:** Given  $M=M^*$  and  $L=L^*$ ,  $\widehat{K} > 0$  implies that with  $K > K^*$ , without trade in  $X$  and  $Y$  and with *no control* on capital outflows and immigration, home will import labour and machines while financial capital will outflow. International mobility of financial capital does not affect pattern of trade.

**Proof:** In the full employment model, with such identical endowments in both the Home and the foreign country, RS of  $X$  and  $Y$  will be the same ( $RS=RS^*$ ), and  $P=P^*$  being the same, no goods trade will take place. As  $K > K^*$ ,  $\widehat{K} = 0 \Rightarrow \widehat{W} = \widehat{p_M} = -(\widehat{1+r})$  and  $\widehat{K}^* = 0 \Rightarrow \widehat{W}^* = \widehat{p_M}^* = 0$ . As explained earlier, this will mean at a *given*  $P$ ,  $(1+r) < (1+r^*)$ ,  $W > W^*$  and  $p_M > p_M^*$ . With higher real wage at Home, immigration opens up. Similarly, imports of machinery will occur. 'K' finances intermediate goods and immigrations. *Without restrictions* on outflows of financial capital ( $K$ ), capital flight will occur from Home, as it is dearer abroad.<sup>7</sup> Gradually, outflow might make 'K' (relatively) scarcer at Home with upward pressure on 'r' to raise 'r' at home in the long-run (HOS is a long run model), 'W' and 'p\_M' will start falling to arrest imports of machines and workers from abroad. *With restrictions* on financial flows, however, although 'r' will be low initially, but *no restriction* on labor movements or machine imports will cause (due to arbitrage) 'W' and  $p_M$  to fall at home, and '(1+r)' to rise as more  $L+L^*$  and  $M+M^*$  raises demand for  $K$ . Here factor trade complementing commodity trade unlike HOS model (QED).

**Proposition 5:** Given  $M=M^*$ ,  $L=L^*$ , and  $\widehat{K} > 0$ , without capital control, FPE will hold.

**Proof:** With identical endowments, since  $P$  remains the same and so are  $RS(X/Y) = RS^*(X^*/Y^*)$ , from Proposition 3, no trade occurs. As  $\widehat{W} = \widehat{p_M} = -(\widehat{1+r})$ ,  $\widehat{W/p_M} = 0$  i.e., such trade does not disturb  $\frac{W}{p_M}$ .

Thus, if only cross-country financial flows are allowed *absolute factor prices will be equalized*.

<sup>6</sup> See Patinkin (1958), Lucas (1990). Derivations are in Appendix 2 and 3.

<sup>7</sup> Lucas (1990) and others on hindrances of capital flow from rich to poor countries despite higher rate of return. In the economic growth literature, several barriers to capital flows including institutional have been mentioned. For a small open economy as price taker,  $K$  moves to ROW or foreign and with less than perfect capital mobility FPE does not occur while with free financial flows with perfect mobility, FPE occurs.

Even if with  $K > K^*$ ,  $(1+r) < (1+r^*)$ , absolute factor prices will be different. i.e.  $W > W^*$  and  $p_m > p_m^*$  (a la Proposition 3) and with free financial flows across borders (i.e., without Capital control), perfect arbitrage ensures, i.e.  $(1+r)=(1+r^*)$  and hence,  $r=r^*$ ,  $W=W^*$ ,  $p_m=p_m^*$ . However, relative factor prices will always be the same, since it does not depend on  $(1+r)$ . Therefore, without trade in goods, factor flows or movement in credit across borders does not generate overall gains from trade. Even if with  $K > K^*$ ,  $(1+r) < (1+r^*)$ , absolute factor prices will be different. i.e.  $W > W^*$  and  $p_m > p_m^*$  (a la Proposition 3) and with free financial flows across borders (i.e., without Capital control), arbitrage ensures, i.e.  $(1+r)=(1+r^*)$  and hence,  $r=r^*$ ,  $W=W^*$ ,  $p_m=p_m^*$ . Given  $P=P^*$  in home and foreign country, with free trans-border capital flows,  $\frac{W}{p_m} = \frac{W^*}{p_m^*}$  (QED).

## 4.2 Trade, Unemployment and Role of Credit Market

In the context of our benchmark model, we considered full-employment without any minimum wage. Unemployment problem is quite common when labor supply exceeds demand. However, in the presence of wage fund or working capital imperfection in the credit market or borrowing constraints could have severe jolt in the labor market and hence, could affect production and trade pattern. Excess demand for funds to be borrowed creates this situation. Thus, depending upon the credit crunch and default risk unemployment problem could be severe (Calvo et al, 2012, Popov et al. 2018). In fact, that issue is quite pertinent for the consideration of financial development and interesting perspectives on the role of financial institutions for inclusive development (Rajan and Zingales 1998, Noack and Costello 2022). For example, Alexandre et al. (2021) has considered the case of financially distressed firms in case of minimum wage increases as it reduce employment growth and profitability, especially after the pandemic eroding the financial condition of firms. Aizenman et al.(2022) explored the role of bank lending in times of pandemic-led shock when government also comes forward with fiscal stimulus for expansionary effects.

### 4.2.1 Unemployment in the benchmark model

First, we consider the case Unemployment in this 2x2-model with no credit constraints. Just to reiterate, we start from a stock of finance or working capital or bank credit generated out of savings in the last period. For this section, we coin the financiers as bankers. There is a fixed minimum wage  $\bar{W}$  for hiring workers. Let  $W = \bar{W}$  and  $L_e$  be the level of employment of labor (L) such that  $(\bar{L} - L_e)$  is unemployment at Home. Following three equations determine  $p_m$ ,  $r$  and  $L_e$ .

$$\frac{P}{(1+r)} = \bar{W}a_{LX} + p_M a_{MX} \quad (16)$$

$$\frac{1}{(1+r)} = \bar{W}a_{LY} + p_M a_{MY} \quad (17)$$

$$K = \bar{W}L_e + p_M .M \quad (18)$$

'M' is still given from last-period production of machines. Once 'Le' is known,  $(L_e, M)$  determine X and Y. The interesting question is how the system responds to a hike in wage from  $W$  to  $\bar{W} > W$ , given  $(P, M)$ . From (1) and (2) at a given  $P = \bar{P}$ , assuming a small economy facing  $P$  of the rest of the world (i.e., price-taker), average cost of production of X ( $C_x$ ) and Y ( $C_y$ ), we can write:

$$\frac{C_X}{C_Y} = \frac{p_M a_{Mx} + \bar{W} a_{Lx}}{p_M a_{My} + \bar{W} a_{Ly}} = P \quad (19)$$

Therefore,  $\widehat{C}_X - \widehat{C}_Y = 0$   
 $\Rightarrow (\theta_{MX} - \theta_{MY}) \widehat{p}_M + (1 - \theta_{MX} - 1 + \theta_{MY}) \bar{W} = 0$

Or,  $\widehat{p}_M = \widehat{\bar{W}} > 0 \quad (20)$

Hence,  $\widehat{r} < 0 \quad (21)$

From (18), following CFJ (2011) we can write:

$$\lambda_{LK} (\widehat{\bar{W}} + \widehat{L}_e) + \lambda_{MK} \widehat{p}_M = 0 \quad (18a)$$

Therefore,  $\widehat{L}_e < 0 \quad (22)$

As  $\bar{W}$  and  $P_M$  both rise, given  $\bar{K}$ ,  $L_e$  must fall.

Since  $P$  and  $\bar{W}$  are given,  $C_x$  and  $C_y$  both should change in the same proportion. A rise in  $\bar{W}$ , at a given 'r' increased  $C_x$  and  $C_y$ . But  $C_x$  rises less than  $C_y$  as  $X$  is assumed to be  $M$ -intensive. So the rates will fall and to prevent this  $P_M$  will rise equiproportionately with  $\bar{W}$ . As both  $(P_M, \bar{W})$  rise, 'r' must fall to satisfy (16) and (17). Given  $\bar{K}$ ,  $L_e$  must fall. Thus, higher wage or a minimum wage leads to unemployment. The mechanism is completely different from the diminishing marginal productivity argument (here  $\alpha_{ij,s}$  are fixed coefficients).

As  $L_e$  drops,  $\frac{L_e}{M}$  will fall and  $\frac{X}{Y}$  will rise. So a labour abundant economy will produce less of labor-intensive good. This will lower  $P$  in the large country case, reduce  $P_M$  and raise 'r'. Given  $\bar{K}$  initial fall in  $L_e$  would recover to some extent. *The major result with unemployment is that now higher  $\bar{K}$  will affect the pattern of trade, relative prices, etc.* Given  $\bar{W}$ , hence  $(P_M, r)$  at a given  $P$ , a higher stock of  $K$  must increase  $L_e$  and  $\frac{L_e}{M}$  leading to greater export by the labor-abundant country increasing global production of  $Y$  and  $Y/X$ . Consequent rise in  $P$  and  $P_M$  will increase demand for 'K' and reduce  $L_e$ . But initial excess supply of 'K' will prevail and 'r' will drop in ultimate equilibrium.

The main takeaway from this section is that in a world ridden with unemployment, finance plays a pivotal role. Greater credit-finance ( $K$ ) will increase global income and employment. But it will also adversely affect the terms of trade of the labor-abundant economy. Machine producers will be better off. This leads to the following proposition.

**Proposition 6:** Financial boom ( $\hat{K} > 0$ ) or crisis ( $\hat{K} < 0$ ) affects patterns of trade, relative price 'P',  $\frac{\bar{W}}{P_M}$ , in a minimum wage driven unemployment equilibrium.

**Proof:** See the discussion above. (QED).

If  $\hat{K} > 0$  and given P, in this unemployment model, extra cash-in-advance will increase employment and will determine  $L_e$ , X and Y (i.e., real changes or non-neutrality unlike the full employment scenarios in the previous section). This will increase Y from the full employment conditions. This country will export Y and import X. After trade, P will be lower.  $P_M$  will be lower and  $L_e$  will rise furthest. So higher unemployment economy will export the labour-intensive good. But price changes or changes in levels of K will not affect wages (alike Keynesian case). This is an added theoretical feature.

#### 4.2.2 Trade and Unemployment in the presence of Imperfect Credit Market:

Stiglitz and Weiss (1981) seminal paper as well as Williamson (1987) has discussed Credit rationing with imperfect information when borrower's riskiness of default and lenders loan interest as well as the monitoring cost matters. Let us assume that  $K = \bar{K}$  is the total supply of fund in a country, where there are two sources of finance, viz., own entrepreneurial finance as source of internal fund ( $K_e$ ) as well as external funds from banks or other financial sources ( $K_b$ ) so that we write collaterals as:

$$\bar{K} = K_b + K_e \quad (23)$$

This is important for trade-finance and expansion of credit.

Also, 
$$K_b = (K_b - B) + B \quad (24)$$

Apparently, this identity tells us that 'B' is the fixed amount such that with credit rationing ( $K_b - B$ ) is not lent out (leakage) due to imperfect credit market, and  $K_b$  is constrained by  $B^{\max}$ .

Suppose there are 'n' entrepreneurs each with identical endowment of internal finance ( $k_e$ ) such that

$$K_e = k_e \times n \quad (23a)$$

Let the lending by the banks be denoted by 'B' with 'R' being the *borrowing rate* (cost of borrowing). For internal finance, *opportunity cost is exogenous 'r'* ('r' = 0 with no other opportunities for investment). This is the deposit rate and  $R > r$ , implying that the entrepreneurs can borrow to augment their financial capital stock by paying  $R > r$  (the deposit or lending rate). For 'n' identical entrepreneurs each with "b" amount of disbursed credit, with total disbursement of 'B' fixed by Credit-rationing, we write:

$$B = K_b = b \times n \quad (23b)$$

'B' is allocated endogenously to X-Y sectors via credit rationing depending on risk of default and corresponding appropriation of funds. Let ' $0 < q < 1$ ' be probability of default and ' $0 < S < 1$ ' be the proportion collateralized from the defaulters by the financiers. 'B' will be more as ' $K_e$ ' rises because the later could be used as collateral in case of default. Bankers—when 'q' is high (risky)—will hedge against risk by charging higher 'R' and hence will have higher 'S'. 'qS' determines the degree of defaulter punishment. It is a parameter (exogenous) in this model. A relation between maximum loanable  $B^{\max}$

and “R” will endogenise ‘B’. As ‘qS’ becomes higher, ‘R’ is charged low, and ‘B’ rises. Using no-default constraint, it can be derived that (see Marjit and Das 2021):

$$B = \frac{qS}{(1+R) - qS} K_e \quad (25)$$

with  $\lambda_b = \frac{K_e}{K_e + K_b}$  same across X-Y assuming same economy-wide ‘qS’.

Now credit market equilibrium ensures that supply matches the funds required to purchase factor inputs, rewriting (18) as:

$$B + K_e = \bar{W}L_e + p_M M \quad (26)$$

As mentioned before, instead of ‘r’ now we have two rates –borrowing (R) and deposit (r) –with weighted average of both. Using (26), with dual sources of finance, we now rewrite (16) and (17) as:

$$(\bar{W}a_{LX} + p_M a_{MX}) \left[ \frac{k_b}{k_b + k_e} (1+R) + \frac{k_e}{k_b + k_e} (1+r) \right] = P_X \quad (27)$$

$$(\bar{W}a_{LY} + p_M a_{MY}) \left[ \frac{k_b}{k_b + k_e} (1+R) + \frac{k_e}{k_b + k_e} (1+r) \right] = P_Y \quad (28)$$

where  $\lambda_e = \frac{k_e}{k_e + k_b}$ ,  $\lambda_b = 1 - \lambda_e = \frac{k_b}{k_e + k_b}$

From the benchmark model, full-employment condition (4) is rewritten as:

$$a_{LX}X + a_{LY}Y = L_e \quad (4a)$$

$$a_{MX}X + a_{MY}Y = M \quad (5)$$

From (26), using (25) derive:

$$K_e \left[ \frac{(1+R)}{(1+R) - qS} \right] = \bar{W}L_e + p_M M \quad (29)$$

With these specifications, we have 5 variables:  $P_M$ ,  $R$ ,  $L_e$ ,  $X$  and  $Y$ . Given  $P_X$  and  $P_Y$ , Eqs. (27) and (28) determine  $P_M$  and  $R$ ; then, (29) determines  $L_e$ , and (4a), (5) determine  $X$ ,  $Y$ . Note that with credit-rationing (fixed “B”), increasing  $K_b$  has no role as “B” remains unaltered.

Let us consider two nations with identical endowments of collaterals where in autarkic equilibrium,  $K_b = K_b^*$ ,  $K_e = K_e^*$ , and  $\bar{W} = \bar{W}^*$ . Suppose ceteris paribus,  $(qS) > (qS^*)$  (same ‘q’ but degree of appropriation due to default differs contingent on rule of law or governance) which implies that probability of penalty of defaulter is higher in the home than in the foreign country thanks to better quality institutions, judiciary, or financial development.

Now from Eqns. (27) and (28), a la Jones (1965), we get:



$$\widehat{p}_M \theta_{MX} + \lambda_b \widehat{(1+R)} = \widehat{P}_X \quad (30)$$

$$\widehat{p}_M \theta_{MY} + \lambda_b \widehat{(1+R)} = \widehat{P}_Y \quad (31)$$

Solving, we get:

$$(\theta_{MX} - \theta_{MY}) \widehat{p}_M = \widehat{P}_X - \widehat{P}_Y = \left[ \frac{\widehat{P}_X}{\widehat{P}_Y} \right] \quad (32)$$

Now, rise in  $L_e$  would affect (X, Y) production and pattern of trade thanks to financial institution development couched in terms of rise in 'qs'. However, given (Px, Py) and r, (R, p<sub>M</sub>) are not different.

But if Y is  $L_e$  intensive, rise in credit would cause Y, and hence,  $\frac{Y}{X}$  to increase in autarky, resulting in

$$\left[ \frac{\widehat{P}_X}{\widehat{P}_Y} \right] > 0, \text{ and hence } (R, p_M) \text{ would now be different. If } \left[ \frac{\widehat{P}_X}{\widehat{P}_Y} \right] > 0, \widehat{p}_M > 0 \text{ for } \theta_{MX} > \theta_{MY}.$$

From (30) and (31), we can derive:  $\widehat{(1+R)} = -\frac{\theta_{MX} \widehat{p}_M + \widehat{P}_X}{\lambda_b} = -\frac{\theta_{MY} \widehat{p}_M + \widehat{P}_Y}{\lambda_b}$  (33).

For relative supply changes, following Jones (1965):  $\widehat{X} - \widehat{Y} = -\frac{\widehat{L}_e}{|\lambda|}$  where  $|\lambda| = \lambda_{MX} - \lambda_{LY}$  (34)

Similarly, closing the model from demand relationship, changes in the ratio of X/Y consumption is:

$$\widehat{X}_D - \widehat{Y}_D = -\sigma_D (\widehat{P}_X - \widehat{P}_Y) \quad (35)$$

where  $\sigma_D$  is the elasticity of substitution between X and Y on the demand side. As prices adjust to clear

the markets for X and Y in general equilibrium adjustments, we can write:  $-\sigma_D (\widehat{P}_X - \widehat{P}_Y) = -\frac{\widehat{L}_e}{|\lambda|}$  so that:

$$(\widehat{P}_X - \widehat{P}_Y) = \frac{\widehat{L}_e}{|\lambda| \sigma_D} \quad (36)$$

Choosing 'Y' as numeraire good so that  $P_Y = 1$  and relative price  $P = P_X$ , we further rewrite (36) as:

$$\widehat{P} = \frac{\widehat{L}_e}{|\lambda| \sigma_D} \quad (36a)$$

From (32), we can then find where  $(\theta_{MX} - \theta_{MY}) = |\theta|$ ,  $\widehat{p}_M = \frac{\widehat{P}}{(\theta_{MX} - \theta_{MY})} = \frac{\widehat{L}_e}{|\theta| |\lambda| \sigma_D}$  (37)

Hence, using (33),  $\widehat{(1+R)} = -\frac{\theta_{MY} \widehat{p}_M}{\lambda_b} = -\frac{\theta_{MY}}{\lambda_b} \frac{\widehat{L}_e}{|\theta| |\lambda| \sigma_D} \Rightarrow \widehat{(1+R)} < 0$  (38)

As we have seen before, competitive price equation determines 'R' and given 'qS',  $B^{\max}$  is determined.  $p_M$  is already determined. Intuitively speaking, for a given  $\bar{P}$  in an economy with higher "qS" (due to better financial development and good quality institutions), credit-rationed is relaxed to supply more credit in keeping with "K<sub>b</sub>", causing "L<sub>e</sub>" to rise. Thus, demand for credit adjusts with rise in employment as supply of credit expands. As "X/Y" falls (Y is L-intensive relatively), with trade the general equilibrium adjustments trigger rise in "P", translating concomitant rise in  $p_M$ . Consequently, as more financing will be necessary for  $p_M M$  further rise in credit demand is envisaged. But fall in (1+R)—as explained before—will reduce default possibility or incentive. "B<sup>max</sup>" will increase further. If  $\gamma_M$  is very high,  $K_b > B^{\max}$  (i.e., demand exceeds supply of credit), causing shrinkage of employment to some extent (i.e.,  $\hat{L}_e < 0$ ). However, general equilibrium adjustments where  $\hat{L}_e > 0$  is the trigger of chain of events described so far will stabilize the economy's adjustment to new equilibrium, and secondary effect can't outweigh the primary effect. This leads to:

**Proposition 7:** Given  $\bar{P}$ , as  $(qS) > (qS^*)$ ,  $L_e > L_e^*$

**Proof:** See above discussion.  $L_e > L_e^*$  and right hand side of (26) must rise as increase in  $L_e$  at given  $P_x$ ,  $P_y$  causes changes in  $p_M$ . If trade opens up (due to changes in relative price—P), Y will be exported. Even when P is changing, if  $(qS) > (qS^*)$ ,  $L_e > L_e^*$  (QED).

$$\text{Now, from Eqn. (29), rewriting as: } K_e \left[ \frac{1}{1 - qS / (1 + R)} \right] = \bar{W} L_e + P_M M \quad (29a)$$

Taking total differentials on both sides, we get:

$$-\frac{d[1 - qS / (1 + R)]}{1 - qS / (1 + R)} = \gamma_L \hat{L}_e + \gamma_M \hat{P}_M \quad (39)$$

where  $\gamma_L, \gamma_M$  are cost-shares respectively.

On simplification: we get:

$$[\hat{qS} - \hat{(1 + R)}] \cdot \left[ \frac{qS}{(1 + R) - qS} \right] = \gamma_L \hat{L}_e + \gamma_M \left[ \frac{\hat{L}_e}{|\theta| |\lambda| \sigma_D} \right] = \hat{L}_e \left[ \gamma_L + \gamma_M \frac{1}{|\theta| |\lambda| \sigma_D} \right] \quad (40)$$

Plugging in (38) into (40) and using (25), it simplifies to:

$$\left[ \hat{qS} + \frac{\theta_{MY}}{\lambda_b} \frac{\hat{L}_e}{|\theta| |\lambda| \sigma_D} \right] \cdot \left[ \frac{B}{K_e} \right] = \hat{L}_e \left[ \gamma_L + \gamma_M \frac{1}{|\theta| |\lambda| \sigma_D} \right] \quad (41)$$

$$\text{We can write (41) succinctly as: } \left[ \hat{qS} + \hat{L}_e \cdot A2 \right] \cdot \left[ \frac{B}{K_e} \right] = \hat{L}_e \cdot A1 \quad (42)$$

where  $A1 = \left[ \gamma_L + \gamma_M \frac{1}{|\theta| |\lambda| \sigma_D} \right]$  and  $A2 = \frac{\theta_{MY}}{\lambda_b |\theta| |\lambda| \sigma_D}$

Further with algebraic manipulation (42) simplifies to: 
$$\widehat{L}_e = \frac{\widehat{qS}(B/K_e)}{A1 - A2 \cdot \frac{B}{K_e}} \quad (43)$$

As  $(qS) > (qS^*)$ ,  $L_e > L_e^*$  and via Proposition 7,  $\widehat{p}_M > 0$ ,  $(1+R) < (1+R^*)$ ,  $P > P^*$ , affecting production and trade. With  $(qS) > (qS^*)$ ,  $(B/K_e) > 0$ ,  $\widehat{L}_e > 0$  iff  $A1 > A2 \cdot \frac{B}{K_e}$  or  $\frac{A1}{A2} > \frac{B}{K_e}$ . This is the

Stability Condition. This boils down to 
$$\frac{\gamma_L[|\theta||\lambda|\sigma_D] + \gamma_M}{\theta_{MY}} > \frac{B/K_e}{\lambda_b} = \frac{qS}{\lambda_b[(1+R) - qS]}$$

In other words, despite rise in  $p_M$  might have a ‘choking-off’ impact on  $L_e$ , it cannot overturn as  $(B/K_e)$  or  $\gamma_M$  cannot be very high. Pivotal role is played by share of credit going to machine-sector as

well as ratio of external finance to stock of capital ( $\lambda_b = \frac{k_b}{k_e + k_b}$ ). This leads to the following

proposition:

**Proposition 8:** From (42) and (43), it follows that given  $\theta_{MX} > \theta_{MY}$ ,  $\theta_{MY}$  is fairly low enough and  $\gamma_M \rightarrow 0$ , so that  $\gamma_L \rightarrow 1$ , and  $\sigma_D$  is high enough then stability condition will always hold and  $B/K_e$  will not be high enough. In other words, the condition  $A1 > A2 \cdot \frac{B}{K_e}$  ensures that given quite low values of  $\theta_{MY}$  and  $\gamma_M$  even if  $B/K_e$  is bit high, positive impact on  $\widehat{L}_e$  could be insignificantly low, but not negative (i.e., reduced).

**Proof:** See the discussion above. (QED). This is the ‘Stability condition’.

#### 4. Concluding Remarks and implications:

In this paper, we have extended the traditional two-sector Neo-Classical trade model—workhorse of Heckscher-Ohlin-Samuelson model couched in the framework of Jones (1965)—by incorporating Ricardian wage fund theory *a la* Marjit and Das (2021). Incorporating finance in general equilibrium trade model is quite novel as it offers important valuable insights such as role of finance in affecting production and trade patterns. With perfect credit market and full employment, finance does not affect trade pattern; however, it does affect absolute values of wage and price of machines via changes in the market interest rate. In the full employment model, with identical endowments in both the home and foreign country, no trade will occur with same price as in the world market price. With differences in endowments, alike HOS model trade will take place. With differences in availability of capital, and mobility of financial capital factor trade complements commodity trade unlike the HOS model. Trade pattern is not affected. Without capital control, factor prices will be equalized. Higher minimum wage will lead to unemployment without diminishing marginal productivity, and a labor-abundant economy might produce less of labour-intensive goods. With unemployment, however, higher wage fund will affect trade pattern as well as relative prices. Financial crash or boom—as exogenous shocks—affect pattern of trade, relative prices, in a minimum wage-driven unemployment equilibrium.

For example, given prices of goods and machines and interest rate, higher working capital will increase labor employment translating into greater export by a labor-abundant economy initially lacking enough credit to finance trade. The main takeaway is that in a world ridden with unemployment, finance plays a pivotal role with impact on global income and employment. However, it will also adversely affect the terms of trade of the labor-abundant economy. Machine producers will be better off. With imperfect credit market and credit-rationing, the story becomes more interesting and of course, realistic because when demand for loanable funds exceed supply to finance production and trade, then risks of default and quality of financial institutions engineering penalty for bringing someone to book will matter to a great extent. The model shows that for two otherwise identical countries with same initial conditions, the country with higher degree of financial development (e.g., judiciary, rule of law, accountability, etc.) will have higher stocks of finance and hence, will lend more at lower rate of interest so that employment growth will occur. The country where entrepreneurs have better access to external finance on top of their own financial resources will be better off in curing unemployment problem and will participate in trade in the world market. From the model, we could also elicit a mechanism where incentive to invest in R&D to induce technical progress in the machine sector could account for the secular decline in the labor-share of income. Additionally, the model develops some empirically testable hypothesis such as, role of financial institutions, and financial development for inclusive growth via job and employment. In fact, Emara and Said (2021) has shown empirically in the context of African economies and emerging markets that improvement in governance, supervisory and regulatory regimes, judicial independence, and contract enforcement coupled with financial access is conducive for economic growth. Empirical validation of our results with numerical simulation of the cost-shares of machines vis-à-vis labor along with changes in prices of goods and factors can be mounted in further extension of this research. However, our conjecture and mechanism differs from the Stiglitz and Weiss (1981) and Williamson (1987) conjectures. Ours value-addition lies in showing a novel mechanism by blending traditional Neo-Classical 2x2 sector workhorse of trade models with finance, credit rationing along the lines of classical wage-fund theory.

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## Appendices

### Appendix 1.

Following CFJ (2011) and Feenstra (2003), using (4) and (5)

$$\lambda_{LX} \hat{X} + \lambda_{LY} \hat{Y} = \hat{L}$$

$$\lambda_{MX} \hat{X} + \lambda_{MY} \hat{Y} = \hat{M}$$

$$\text{Using Cramer's Rule: } \hat{X} = \frac{\lambda_{MY} \hat{L} - \lambda_{LY} \hat{M}}{\lambda_{LX} \lambda_{MY} - \lambda_{MX} \lambda_{LY}}, \hat{Y} = \frac{\lambda_{LX} \hat{M} - \lambda_{MX} \hat{L}}{\lambda_{LX} \lambda_{MY} - \lambda_{MX} \lambda_{LY}} \Rightarrow \hat{X} - \hat{Y} = \frac{\hat{L} - \hat{M}}{|D|},$$

where  $|D| = \lambda_{LX} \lambda_{MY} - \lambda_{MX} \lambda_{LY} = \lambda_{LX} - \lambda_{LY} = \lambda_{MY} - \lambda_{MX} < 0$  as X uses more M (by assumption)

Thus,  $\widehat{X} - \widehat{Y} = \frac{\widehat{L} - \widehat{M}}{|D|} = \alpha [\widehat{M} - \widehat{L}] > 0$  as  $\lambda_{MX} > \lambda_{MY}$ , and  $\alpha = \frac{1}{\lambda_{MX} - \lambda_{MY}} > 0$  (QED).

### **Appendix 2.**

From (2) and (3), via Jones (1965), when  $\widehat{P} \neq 0$

$$\begin{pmatrix} \theta_{LX} & \theta_{MX} \\ \theta_{LY} & \theta_{MY} \end{pmatrix} \begin{pmatrix} \widehat{W} \\ \widehat{p}_M \end{pmatrix} = \begin{pmatrix} \widehat{P} - \widehat{(1+r)} \\ -\widehat{(1+r)} \end{pmatrix} \text{ and } |\theta| = \theta_{LX}\theta_{MY} - \theta_{MX}\theta_{LY} = \theta_{MY} - \theta_{MX} = \theta_{LX} - \theta_{LY} < 0 \text{ (by}$$

intensity assumption). Applying Cramer's rule yields:

$$\widehat{W} = \frac{1}{|\theta|} \begin{pmatrix} \widehat{P} - \widehat{(1+r)} & \theta_{MX} \\ -\widehat{(1+r)} & \theta_{MY} \end{pmatrix} = \widehat{P} \frac{\theta_{MY}}{|\theta|} - \widehat{(1+r)}$$

$$\widehat{p}_M = \frac{1}{|\theta|} \begin{pmatrix} \theta_{LX} & \widehat{P} - \widehat{(1+r)} \\ \theta_{LY} & -\widehat{(1+r)} \end{pmatrix} = -\widehat{P} \frac{\theta_{LY}}{|\theta|} - \widehat{(1+r)}$$

Using these and (11),

$$\widehat{K}_d = -\frac{\widehat{P}}{|\theta|} [-\lambda_{MK}\theta_{LY} + \lambda_{LK}\theta_{MY}] = \lambda_{LK} \left[ \frac{\widehat{P}\theta_{MY}}{|\theta|} - \widehat{(1+r)} \right] + \lambda_{MK} \left[ -\widehat{(1+r)} - \frac{\widehat{P}\theta_{LY}}{|\theta|} \right]$$

$$\Rightarrow \widehat{K}_d = -\widehat{(1+r)}[\lambda_{LK} + \lambda_{MK}] + \frac{\widehat{P}}{|\theta|} [\lambda_{LK}\theta_{MY} - \lambda_{MK}\theta_{LY}] = -\widehat{(1+r)} + \frac{\widehat{P}}{|\theta|} [\lambda_{LK}\theta_{MY} - \lambda_{MK}\theta_{LY}] \text{ (QED).}$$

Given P, higher 'K' will imply lower (1+r) or 'r'. With  $\widehat{P} > 0$  from (2) and (3), derive:

$$\widehat{W}\theta_{LX} + \widehat{p}_M\theta_{MX} = -\widehat{(1+r)} + \widehat{P} = \widehat{W}\theta_{LY} + \widehat{p}_M\theta_{MY} + \widehat{P} \Rightarrow \widehat{W}(\theta_{LX} - \theta_{LY}) + \widehat{p}_M(\theta_{MX} - \theta_{MY}) = \widehat{P}$$

$$\text{Thus, } \widehat{p}_M - \widehat{W} = \frac{-\widehat{P}}{|\theta|} = \frac{\widehat{P}}{\beta}, \text{ where } |\theta| = \theta_{LX} - \theta_{LY} = \theta_{MY} - \theta_{MX} < 0, \beta = -|\theta|$$

### **Appendix 3.**

$$\text{From above, } \widehat{K}_d = 0 \Rightarrow -\widehat{(1+r)} = \frac{\widehat{P}}{|\theta|} [\lambda_{LK}\theta_{MY} - \lambda_{MK}\theta_{LY}]$$

$$\text{Thus, } \widehat{P} - \widehat{(1+r)} = \widehat{P} - \frac{\widehat{P}}{|\theta|} [\lambda_{LK}\theta_{MY} - \lambda_{MK}\theta_{LY}] \Rightarrow \widehat{P} - \widehat{(1+r)} = \widehat{P} \left[ 1 - \frac{\lambda_{LK}\theta_{MY} - \lambda_{MK}\theta_{LY}}{|\theta|} \right]$$

$$\text{And } \widehat{P} - \widehat{(1+r)} = \frac{\widehat{P}}{|\theta|} [\theta_{MY}(1 - \lambda_{LK}) + \lambda_{MK}\theta_{LY} - \theta_{MX}] = \frac{\widehat{P}}{|\theta|} [(\theta_{MY} + \theta_{LY})\lambda_{MK} - \theta_{MX}] = \frac{\widehat{P}}{|\theta|} [\lambda_{MK} - \theta_{MX}] \text{ (QED.)}$$