

Jungherr, Joachim; Schott, Immo

**Article — Published Version**

## Slow Debt, Deep Recessions

American Economic Journal: Macroeconomics

*Suggested Citation:* Jungherr, Joachim; Schott, Immo (2022) : Slow Debt, Deep Recessions, American Economic Journal: Macroeconomics, ISSN 1945-7715, American Economic Association, Nashville, TN, Vol. 14, Iss. 1, pp. 224-259,  
<https://doi.org/10.1257/mac.20190306>

This Version is available at:

<https://hdl.handle.net/10419/249352>

### Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

### Terms of use:

*Documents in EconStor may be saved and copied for your personal and scholarly purposes.*

*You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.*

*If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.*

**Copyright American Economic Association;  
reproduced with permission.**

## Slow Debt, Deep Recessions<sup>†</sup>

By JOACHIM JUNGHERR AND IMMO SCHOTT\*

*Business credit lags GDP growth by about one year. This contributes to high leverage during recessions and slow deleveraging. We show that a model in which firms use risky long-term debt replicates this slow adjustment of firm debt. In the model, slow-moving debt has important effects for real activity. High levels of firm debt issued during expansions are only gradually reduced during recessions. This generates an adverse feedback loop between high default rates and low investment and thereby amplifies the downturn. Sluggish deleveraging slows down the recovery. (JEL E23, E32, E44, G31, G32)*

Firm debt follows GDP with a lag. Peaks and troughs in firm credit growth tend to occur about one year later than in GDP. While GDP growth turned negative in 2008, US firm debt continued to grow at a robust annual rate of more than 5 percent. This slow adjustment of debt is potentially important because it contributes to high levels of debt during recessions and a prolonged deleveraging process. In this paper, we show that slow-moving firm debt can generate deep recessions and slow recoveries.

Using firm-level data, we find that the slow adjustment of debt is related to the extent to which firms use long-term debt. We then build a business cycle model of production, firm financing, and costly default in which firms can borrow long term. The model replicates the empirical co-movement between firm debt and output. Risky long-term debt is crucial for this result. When firms borrow long term, high debt levels during a boom carry over into the subsequent recession. During the downturn, firms are reluctant to reduce the high debt levels inherited from the past because the benefits of this reduction would mostly fall to creditors. As a result, firm leverage, default rates, and credit spreads all peak during recessions, in line with the empirical evidence.

\* Jungherr: Department of Economics, University of Bonn (email: joachim.jungherr@uni-bonn.de); Schott: Department of Economics, Université de Montréal, and CIREQ (email: immoschott@gmail.com). Simon Gilchrist was coeditor for this article. We thank two anonymous referees, Árpád Ábrahám, Alice Albonico, Christian Bayer, Carlos Garriga, Tryphon Kollintzas, Anton Korinek, Andrea Lanteri, Albert Marcet, Ramon Marimon, Juan Pablo Nicolini, Veronika Selezneva, Guillaume Sublet, Pedro Teles, and Jaume Ventura for helpful comments and insightful discussions. We also thank participants at various seminars and conferences for valuable feedback. This research was funded in part by the European Union's Horizon 2020 Program through ERC-CoG project Liquid-House-Cycle under grant agreement No. 724204 and by the Spanish Ministry of Economy and Competitiveness through a Seed Grant of the Barcelona Graduate School of Economics Severo Ochoa Programme for Centres of Excellence in R&D (SEV-2015-0563).

<sup>†</sup>Go to <https://doi.org/10.1257/mac.20190306> to visit the article page for additional materials and author disclosure statement(s) or to comment in the online discussion forum.

The rise in credit spreads during downturns drives up firms' cost of capital and induces them to cut back on investment. Firm assets fall at a faster rate than debt because firms adjust debt slowly. The resulting rise in leverage causes an additional increase in default risk and credit spreads, which depresses investment even further. In this way, slow-moving debt gives rise to an adverse feedback loop between high default rates and low investment, which amplifies and prolongs the downturn.

Importantly, the additional volatility in output generated by slow-moving debt is inefficient. Firms adjust debt slowly because they do not internalize all associated costs. They exert an externality on the holders of previously issued debt, who bear a large part of the costs of elevated credit risk. In the constrained efficient allocation, debt is adjusted immediately in response to aggregate shocks. This avoids the strong increase in default rates and credit spreads during downturns and thereby substantially reduces macroeconomic volatility.

We begin our analysis in a simple two-period version of our model. This allows us to characterize the key mechanisms analytically. We then proceed to a quantitative analysis of a dynamic business cycle model in which firms choose capital, labor, leverage, and debt maturity. We show that the model successfully replicates the empirical lag structure between firm debt and output. The model is also successful in generating countercyclical leverage, default risk, and credit spreads, as well as a procyclical term structure in credit spreads. We compare the decentralized equilibrium to the constrained efficient allocation and find that slow debt substantially increases output volatility. This implies room for welfare-improving stabilization policies.

Our paper contributes to a large literature that studies the role of firm debt for cyclical fluctuations. The standard approach in this literature is to model all firm debt as short term; i.e., all debt issued in period  $t$  fully matures in period  $t + 1$ . From an empirical point of view, the disregard of long-term debt is problematic. About 75 percent of US corporate debt does not mature within the next year. At issuance, the average term to maturity is three to four years for bank loans and more than eight years for corporate bonds (Adrian, Colla, and Shin 2013). Our results suggest that models that take firms' use of long-term debt into account can contribute to our understanding of cyclical fluctuations and effective stabilization policies.

Computational difficulties are the main reason why risky long-term debt is usually absent from dynamic macroeconomic models. Optimal firm behavior depends on the price of long-term debt, which itself depends on firm behavior both today and in the future. A firm that cannot commit to future actions must take into account how today's choices will affect future firm behavior. In this paper, we compute the global solution to this fixed point problem. This allows us to study how firms optimally adjust their debt structure over time and how these choices shape the business cycle.

The paper most closely related to ours is Gomes, Jermann, and Schmid (2016), who use first-order perturbation methods to study a New Keynesian business cycle model with risky long-term debt in which firms' borrowing and investment decisions exert an externality on existing creditors. Their main result is that shocks to inflation change the real burden of outstanding nominal long-term debt and thereby generate persistent cyclical variations in leverage and investment. We show that a model with risky long-term debt is successful in replicating the empirical lag structure between

firm debt and output and that slow debt gives rise to amplified and prolonged macroeconomic fluctuations that are constrained-inefficient. We derive these results by studying a fully nonlinear global solution of a flexible-price model with productivity shocks. A new feature is that firms simultaneously issue short- and long-term debt. Endogenous debt maturity allows firms to respond to the distortions introduced by risky long-term debt.<sup>1</sup>

Our paper also relates to Cooley, Marimon, and Quadrini (2004), who study a model of long-term financing with limited commitment. One key difference is that in their model the commitment problem becomes more severe during booms, while default does not occur in equilibrium. In our model, the commitment problem endogenously becomes more severe during downturns, which renders the default rate and credit spreads countercyclical and gives rise to amplification.<sup>2</sup>

More generally, our paper relates to the broader literature on the role of firm debt for cyclical fluctuations. In this literature, all firm debt is short term (e.g., Kiyotaki and Moore 1997; Bernanke, Gertler, and Gilchrist 1999; Jermann and Quadrini 2012; Khan and Thomas 2013; Christiano, Motto, and Rostagno 2014; Gilchrist, Sim, and Zakrajšek 2014; Arellano, Bai, and Kehoe 2019). In these short-term debt models, high debt levels during a boom do not carry over into the subsequent recession, and there is no link between slow debt and deep recessions.

Another feature of standard financial accelerator models is that financing matters because firm net worth is scarce and equity issuance is costly (or ruled out completely). In contrast, there are no social costs of equity issuance in our model. Net worth falls sharply during downturns because firms are unwilling to raise equity from shareholders if the associated benefits would mainly go to creditors. This mechanism causes leverage, default rates, and credit spreads to rise during downturns and thereby amplifies the recession.<sup>3</sup>

The commitment problem generated by risky long-term debt is the focus of several contributions in the literature on sovereign default (e.g., Arellano and Ramanarayanan 2012; Chatterjee and Eyigungor 2012; Hatchondo, Martinez, and Sosa-Padilla 2016) and corporate finance (e.g., Admati et al. 2018). Aguiar et al. (2019) and DeMarzo and He (2020) show that risky long-term debt induces sovereigns and firms to adjust debt slowly over time. The key distinctive feature of our analysis relative to this work is endogenous output and investment. Because slow debt drives up firms' cost of capital during downturns, it generates deep recessions and slow recoveries.<sup>4</sup>

<sup>1</sup>Also related is Miao and Wang (2010), who study a model of long-term debt in which firms do not anticipate that current debt issuance affects future firm behavior. Poeschl (2020) focuses on firms' optimal maturity choice. Crouzet (2017), Karabarbounis and Macnamara (2021), and Jungherr and Schott (2021) study long-term debt in models without aggregate shocks.

<sup>2</sup>Occhino and Pescatori (2015) analyze the effect of an exogenous stock of existing short-term debt on firm behavior. Caggese and Pérez Orive (2015) and Paul (2020) study amplification in environments where long-term debt levels are fixed.

<sup>3</sup>In financial accelerator models with short-term debt, first moment shocks often generate a procyclical default rate that is at odds with the data (see, e.g., Carlstrom and Fuerst 1997; Gomes, Yaron, and Zhang 2003; Covas and Den Haan 2012).

<sup>4</sup>In practice, market participants try to mitigate the commitment problem generated by risky long-term debt through various contracting features, such as seniority structures (as in Chatterjee and Eyigungor 2015) or debt

In Section I, we establish empirical facts about the dynamic co-movement between firm debt and output. Section II provides analytical results on slow debt and deep recessions in a two-period setup. Section III presents the main results of the paper. We study a quantitative business cycle model of production, firm financing, and costly default, and we compare the decentralized allocation to its constrained efficient counterpart. Concluding remarks follow.

## I. Empirical Facts

In this section, we document several empirical facts about the relationship between US firm credit and the business cycle. In particular, we show that firm credit lags output by about one year and that this lag is related to the extent to which firms use long-term debt.

The left panel of Figure 1 shows aggregate leverage of US nonfinancial firms together with the growth rate of real GDP. Leverage peaks during recessions, and deleveraging takes a considerable amount of time. After the 2008–2009 recession, GDP growth had returned to its 2007 level by 2010, while leverage had not yet returned to its 2007 level by 2015. One reason why leverage peaks during recessions is displayed in the right panel of Figure 1: firm debt follows GDP with a lag. Peaks and troughs in firm credit growth tend to occur about one year later than in output. When GDP growth turned negative in 2008, firm credit continued to grow at an annual rate of more than 5 percent.

This dynamic co-movement between output and firm credit is examined more formally in Figure 2. The left side shows pairwise correlations between total firm credit growth in year  $t$  and GDP growth in year  $t + x$ . Because we use data from the corporate sector to inform our quantitative model, we also show correlations between corporate credit and corporate value added in the right half of Figure 2. In both cases, the correlations highlight the slow-moving behavior of debt. While the contemporaneous correlation between growth in firm credit and output is positive, firm credit is most strongly correlated with output growth one year ago.<sup>5,6</sup>

The slow adjustment of debt is potentially important because it contributes to high levels of debt during recessions and a prolonged deleveraging process, which could slow down the recovery. Using firm-level data, we show that this lag in credit is related to firms' use of long-term debt. From Compustat, we extract balance sheet information on a large panel of publicly traded nonfinancial firms. We repeat the exercise above for firms with different shares of long-term debt, i.e., the share of debt with remaining term to maturity of more than one year. In every year, we sort firms into quartiles based on their share of long-term debt. For each group, we calculate total firm debt and show the correlations with output growth in year  $t + x$ .

---

covenants (e.g., Xiang 2019). In the online Appendix, we provide a brief discussion of the empirical literature on seniority and debt covenants.

<sup>5</sup>Using quarterly data, we find that the correlation between firm credit and GDP growth peaks at a lag of five to six quarters (seven quarters for the correlation between corporate credit and corporate value added). See online Appendix for details.

<sup>6</sup>The behavior of firm leverage is determined by changes in the numerator (debt) and the denominator (assets). We also calculate the dynamic co-movement between output and firm assets. In contrast to debt, no lag is present for firm assets. See online Appendix for details.

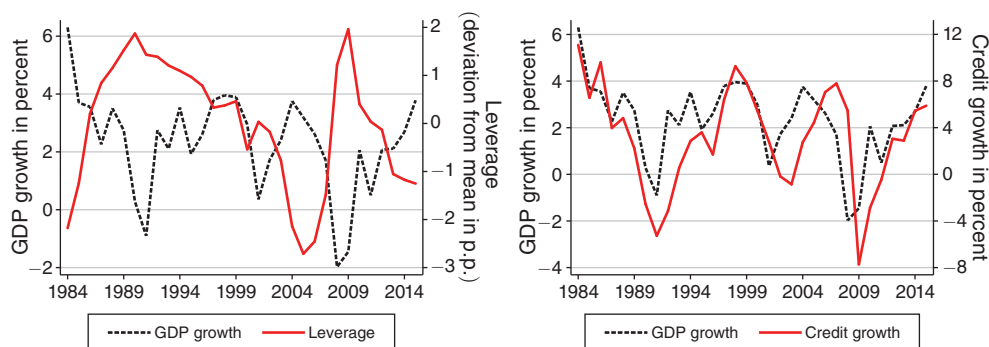
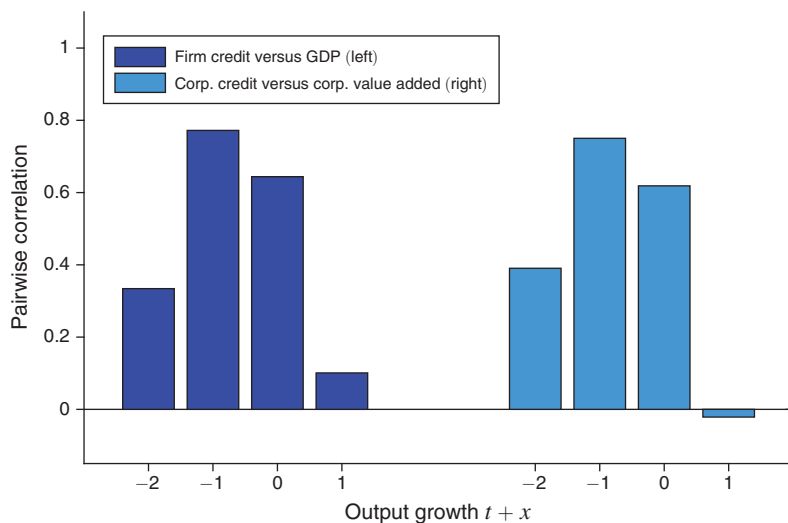


FIGURE 1. LEVERAGE AND CREDIT GROWTH

*Notes:* *Leverage* (left panel, solid red line, right axis) is total debt of nonfinancial firms divided by total assets (book value, marked-to-market). *GDP growth* (dashed black line, left axis) is annual growth of real GDP. *Credit growth* (right panel, solid red line, right axis) is annual growth of real total debt of nonfinancial firms. Stock variables are end-of-year. Time period: 1984–2015.

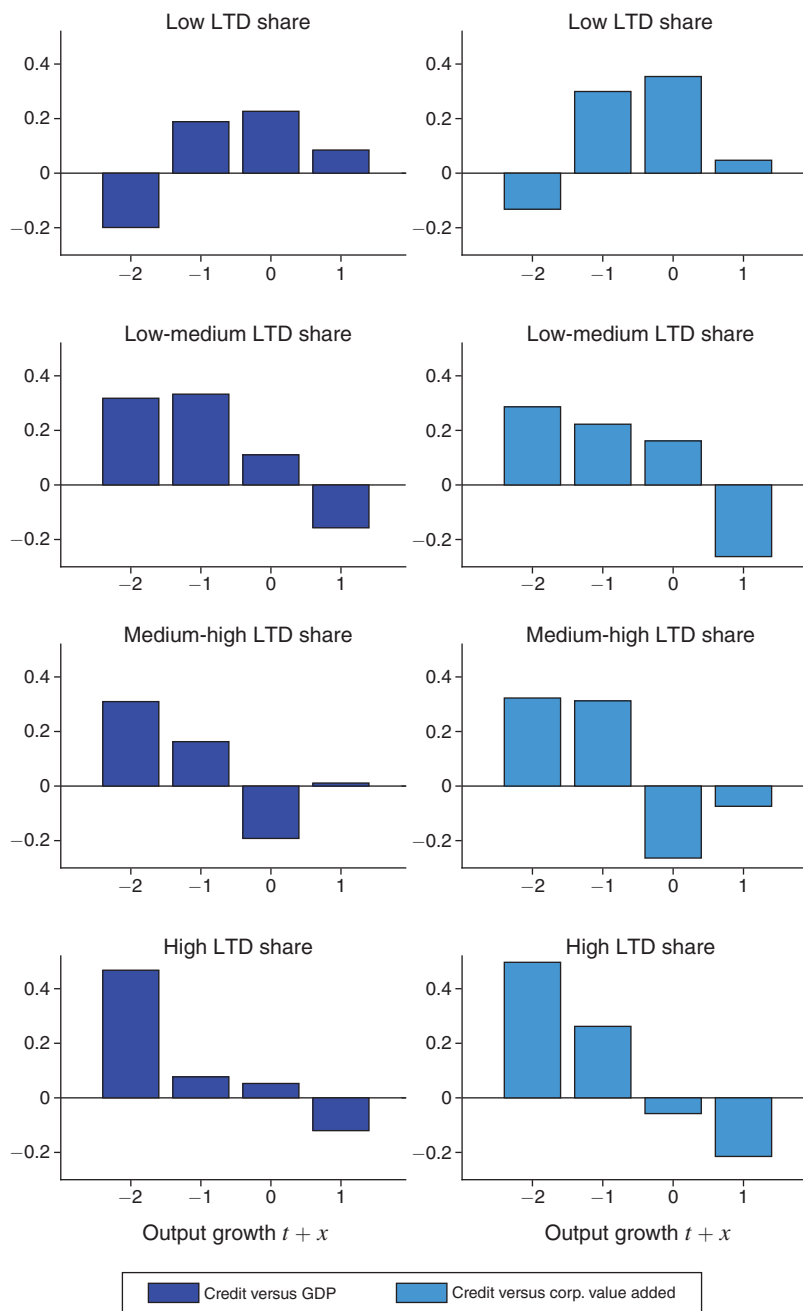
*Source:* US Flow of Funds. See online Appendix for details.

FIGURE 2. CORRELATIONS FIRM CREDIT GROWTH  $t$  WITH OUTPUT GROWTH  $t + x$  (FLOW OF FUNDS)

*Notes:* Bars show pairwise correlations. The left bars show correlations between annual growth of real total debt of nonfinancial firms at the end of year  $t$  and real GDP growth in year  $t + x$ . The right bars show correlations between annual growth of real total debt of nonfinancial corporate firms at the end of year  $t$  and real growth of nonfinancial corporate value added in year  $t + x$ . Time period: 1984–2015.

*Source:* US Flow of Funds. See online Appendix for details.

The results are shown in Figure 3. Output is measured as GDP (left panels) and corporate value added (right panels). The panels in the top row of Figure 3 show correlations for the quartile of firms with the lowest long-term debt shares. The rows below show the corresponding correlations for firms with higher shares of long-term debt.

FIGURE 3. CORRELATIONS FIRM CREDIT GROWTH  $t$  WITH OUTPUT GROWTH  $t + x$  (COMPUSTAT)

Notes: Bars show pairwise correlations between annual growth of real total credit of nonfinancial Compustat firms at the end of year  $t$  and real GDP growth in year  $t + x$  (left), and real growth of corporate value added in year  $t + x$  (right). Credit is total debt of all firms in the respective quartile of the long-term debt (LTD) share distribution. The LTD share is debt due in more than one year divided by total debt. Time period: 1984–2015.

Sources: Compustat (firm debt, LTD share) and US Flow of Funds. See online Appendix for details.



The figure shows that the lag of firm credit with respect to output is more pronounced for firms with a higher long-term debt share. For firms in the lowest quartile, credit co-moves most strongly with contemporaneous output growth. For firms with longer debt maturities, firm credit co-moves more and more strongly with lagged output. For firms in the second quartile of the long-term debt share distribution, the correlation peaks at the first lag of GDP growth. For firms in the third and fourth quartiles, the co-movement is strongest with output growth two years ago.<sup>7</sup>

This firm-level evidence suggests that the slow response of firm credit to changes in output is related to firm's use of long-term debt. In order to study the role of slow debt for the business cycle, a model of long-term debt is needed.

## II. Two-Period Model

We begin our analysis in a simple two-period environment. This allows us to describe analytically how an existing stock of long-term debt can give rise to slow debt and deep recessions.

A risk-neutral firm produces output using capital and labor. Investment is financed with equity and debt. The optimal capital structure solves a trade-off between the tax advantage of debt and the expected cost of default. The firm decides on its scale of production and the preferred capital structure in the presence of previously issued long-term debt. This variable is exogenous in the two-period setup. It will be endogenized in the dynamic business cycle model of Section III.

### A. Setup

There are two periods:  $t = 1, 2$ . Consider a firm owned by risk-neutral shareholders. In period 2, the firm uses capital  $k$  and labor  $l$  to produce output  $y$  according to

$$(1) \quad y = z(k^\psi l^{1-\psi})^\zeta, \quad \text{with } \zeta, \psi \in (0, 1).$$

The firm chooses capital and labor in period 1. Productivity  $z$  is known at this point. Firm earnings are uncertain because of a capital quality shock  $\varepsilon$ . This is the only source of uncertainty. Earnings before interest and taxes in  $t = 2$  are given by

$$(2) \quad y + \varepsilon k - wl - \delta k,$$

where  $w$  is the wage rate and  $\delta$  is depreciation. At  $t = 1$ ,  $\varepsilon$  is a random variable with probability density  $\varphi(\varepsilon)$ . An example for a negative capital quality shock is an unforeseen change in technology or consumer demand, which reduces the value of existing firm-specific capital.

There are two ways of financing capital: equity and debt.

<sup>7</sup> Alternative firm-level criteria used to group firms into different subsamples (e.g., total assets, total debt, leverage, profitability, or asset liquidity) do not generate systematic patterns with respect to the lag in firm debt relative to output.



**DEFINITION (Debt):** A debt security is a promise to pay one unit of the numeraire good together with a fixed coupon payment  $c$  at the end of period 2.

Let  $p$  be the market price of a one-period bond sold by the firm in period 1. If the firm sells a number  $\Delta$  of new bonds, it raises an amount  $p\Delta$  on the bond market. This newly issued debt matures in period 2. In addition, an exogenous number  $b$  of bonds is due in period 2. One may think of  $b$  as long-term debt that has been issued before period 1. The stock of total debt in period 2 becomes  $\tilde{b} = b + \Delta$ .

An alternative to debt financing is equity issuance, denoted as  $e$ . This is the net cash flow from shareholders to the firm. With a stock of capital  $q$  in place at the beginning of period 1, the capital stock  $k$  in period 2 becomes

$$(3) \quad k = q + e + p\Delta = q + e + p(\tilde{b} - b).$$

Firm earnings are taxed at rate  $\tau$ . Debt coupon payments are tax deductible. The firm's stock of assets after production and repayment of debt in period 2 is

$$(4) \quad \tilde{q} = k - \tilde{b} + (1 - \tau)(y + \varepsilon k - wl - \delta k - c\tilde{b}).$$

The fact that coupon payments are tax deductible lowers the total tax payment by the amount  $\tau c\tilde{b}$ . This is the benefit of debt. The downside is that the firm cannot commit to repaying its debt after firm earnings are realized in period 2.

**DEFINITION (Limited Liability):** Shareholders are protected by limited liability. They are free to default and hand over the firm's assets to creditors for liquidation. Default is costly. A fixed fraction  $\xi$  of firm assets is lost in this case.

The timing is summarized in Figure 4. In period 1, the firm starts with given levels of debt  $b$ , capital  $q$ , and productivity  $z$ . The firm chooses capital  $k$  and labor  $l$ . Capital is financed through equity issuance  $e$  and the revenue from selling additional bonds  $p(\tilde{b} - b)$ . In period 2, production takes place. After the realization of the capital quality shock  $\varepsilon$ , the firm decides whether to default.

### B. Firm Problem

The firm maximizes shareholder value. Because shareholders are risk neutral, the firm's objective is the expected present value of net cash flows to shareholders.

We solve the firm's problem using backward induction, beginning with the default decision after the realization of firm earnings in period 2. Limited liability protects shareholders from large negative realizations of  $\varepsilon$ . There is a unique threshold realization  $\bar{\varepsilon}$ , which sets the firm's stock of assets after repayment of debt (i.e., end-of-period-2 equity) equal to zero:

$$(5) \quad \bar{\varepsilon}: \quad \tilde{q} = 0 \Leftrightarrow k - \tilde{b} + (1 - \tau)(y + \bar{\varepsilon}k - wl - \delta k - c\tilde{b}) = 0.$$

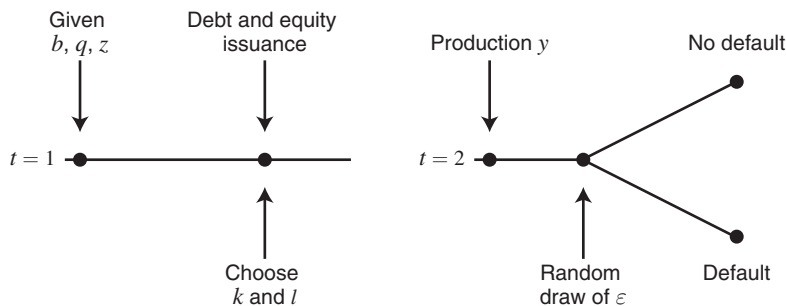


FIGURE 4. TWO-PERIOD MODEL—TIMING

If  $\varepsilon$  is smaller than  $\bar{\varepsilon}$ , full repayment would result in negative equity, whereas default provides an outside option of zero. In this case, the firm optimally defaults on its liabilities. The threshold value  $\bar{\varepsilon}$  is increasing in total debt  $\tilde{b}$  and falling in capital  $k$ . By choosing the ratio of debt  $\tilde{b}$  to capital  $k$  in period 1, the firm controls the default threshold  $\bar{\varepsilon}$  and thereby the probability of default.

In period 1, the firm decides on its scale of production and its preferred financing mix between equity and debt. The firm anticipates that shareholders receive  $\tilde{q}$  whenever  $\varepsilon \geq \bar{\varepsilon}$  and zero otherwise:

$$(6) \quad \max_{k, l, e, \tilde{b}, \bar{\varepsilon}} -e + \frac{1}{1+r} \int_{\bar{\varepsilon}}^{\infty} [k - \tilde{b} + (1-\tau)(y + \varepsilon k - wl - \delta k - c\tilde{b})] \varphi(\varepsilon) d\varepsilon$$

subject to

$$y = z(k^{\psi} l^{1-\psi})^{\zeta},$$

$$\bar{\varepsilon}: \quad 0 = k - \tilde{b} + (1-\tau)(y + \bar{\varepsilon} k - wl - \delta k - c\tilde{b}),$$

$$k = q + e + p(\tilde{b} - b),$$

where  $r$  is the risk-free interest rate. The optimal firm policy crucially depends on the bond price  $p$ . A high bond price implies a low credit spread, which reduces the firm's cost of capital. We derive the firm-specific bond price from the creditors' optimization problem.

### C. Creditors' Problem

Creditors are risk neutral and discount the future at the same rate  $1/(1+r)$  as shareholders. They buy firm bonds in period 1. If the firm does not default in period 2, creditors receive full repayment. In case of default, they receive the firm's liquidation value  $(1-\xi)q$ , where

$$(7) \quad q \equiv k + (1-\tau)(y + \varepsilon k - wl - \delta k).$$

Creditors are perfectly competitive and break even on expectation. The break-even price of firm debt depends on the probability  $\Phi(\bar{\varepsilon})$  that the firm defaults in period 2:

$$(8) \quad p = \frac{1}{1+r} \left[ [1 - \Phi(\bar{\varepsilon})] (1+c) + \frac{(1-\xi)}{\tilde{b}} \int_{-\infty}^{\bar{\varepsilon}} q\varphi(\varepsilon) d\varepsilon \right].$$

The credit spread is defined as the excess return on firm debt (conditional on full repayment) over the riskless rate:  $(1+c)/p - (1+r)$ . If creditors expect a positive probability of default, they will charge a positive spread.

#### D. Equilibrium

We solve for the partial equilibrium allocation for a given wage  $w$  and a given risk-free rate  $r$ . The firm maximizes shareholder value (6) subject to creditors' break-even condition (8). As we show in the Appendix, this problem can be simplified by rewriting it in terms of only two endogenous variables: the scale of production determined by firm capital  $k$  and the default threshold  $\bar{\varepsilon}$ . Accordingly, an interior solution is characterized by two first-order conditions.

*First-Order Conditions.*—For analytical tractability, in this part we consider the special case of  $\xi = 1$ . This means that the liquidation value of the firm is zero in case of default and the bond price in (8) only depends on  $\bar{\varepsilon}$ :

$$(9) \quad p = \frac{1+c}{1+r} [1 - \Phi(\bar{\varepsilon})].$$

The firm's first-order condition with respect to capital  $k$  is

$$(10) \quad \underbrace{-1}_{\text{Marginal cost of capital}} + \underbrace{\frac{1+c}{1+r} [1 - \Phi(\bar{\varepsilon})] \frac{1 + (1-\tau)(\text{MPK} - \delta + \bar{\varepsilon})}{1 + (1-\tau)c}}_{\text{Marginal increase in market value of newly issued debt } p(\tilde{b}-b)} + \underbrace{\frac{1-\tau}{1+r} \int_{\bar{\varepsilon}}^{\infty} (\varepsilon - \bar{\varepsilon}) \varphi(\varepsilon) d\varepsilon}_{\text{Marginal increase in expected stock of equity } \tilde{q}} = 0.$$

A marginal increase in  $k$  has an opportunity cost of one. The marginal benefit consists of an increase in the market value of newly issued debt  $p(\tilde{b} - b)$  and in the expected stock of firm equity after production  $\tilde{q}$ . Shareholders benefit from a high market value of newly issued debt because less equity issuance  $e$  is required to finance a given level of capital  $k$ . The marginal product of capital MPK is increasing in  $z$  and falling in  $k$ .

The first-order condition for an optimal choice of the default probability  $\bar{\varepsilon}$  is

$$(11) \quad \underbrace{[1 - \Phi(\bar{\varepsilon})] \frac{\partial \tilde{b}}{\partial \bar{\varepsilon}} \tau c}_{\text{Marginal tax benefit of } \bar{\varepsilon}} - \underbrace{\varphi(\bar{\varepsilon}) (1+c) (\tilde{b} - b)}_{\text{Marginal increase in expected cost of default internalized by the firm}} = 0.$$

The first term is the marginal benefit of an increase in  $\bar{\varepsilon}$ . A higher value of  $\bar{\varepsilon}$  implies a higher debt level  $\tilde{b}$ . If default is avoided, this is beneficial, as it costs shareholders only  $(1 - \tau)c$  to increase the promised payment to creditors by  $c$ . Because competitive creditors break even, the entire tax benefit of debt is captured by shareholders.

The second term in (11) plays a key role in this model. It shows the firm's marginal cost of an increase in  $\bar{\varepsilon}$ . A higher value of  $\bar{\varepsilon}$  increases the default probability by  $\varphi(\bar{\varepsilon})$ , which lowers the bond price and therefore the market value of newly issued debt. In case of default, creditors lose the entire amount  $(1 + c)\tilde{b}$  (because  $\xi = 1$ ). Through the bond market, the firm internalizes that the buyers of newly issued debt lose  $(1 + c)(\tilde{b} - b)$  in case of default. However, the firm disregards all potential losses, which accrue to the holders of previously issued debt. There is a gap between the firm's marginal cost of  $\bar{\varepsilon}$  and the social cost. As we show below, this has important implications for firm behavior and the business cycle.

*Slow Debt and Deep Recessions.*—We characterize the equilibrium of this economy using comparative statics. All proofs are deferred to the Appendix. The first proposition describes the effect of existing long-term debt on the firm's choice of debt  $\tilde{b}$ , holding the level of capital fixed.

**PROPOSITION 1 (Slow Debt):** *For a given level of capital  $k$ , the firm's choice of debt  $\tilde{b}$  is increasing in the stock of existing debt  $b$ .*

Consider the firm's decision to issue one additional bond in period 1. This would increase the probability of default in period 2 and lower the expected payoff for all creditors. However, through the bond market the firm only internalizes the expected losses, which accrue to the buyers of newly issued debt. With a higher stock of existing debt  $b$ , a larger part of the increase in expected default costs is shared with existing creditors. This allows the firm to enjoy a given amount of the tax benefits of debt at a lower private cost. As a result, the firm optimally decides to utilize the tax benefit of debt more intensively by choosing higher values of  $\bar{\varepsilon}$  and  $\tilde{b}$ .

Proposition 1 implies that the firm's choice of debt  $\tilde{b}$  is history dependent. For any given amount of capital, the firm chooses a higher debt level  $\tilde{b}$  if the stock of existing debt is larger. Note that the firm's first-order condition (11) can never hold if  $\tilde{b} < b$  (as the left-hand side of (11) is strictly positive in this case). This means that debt repurchases (i.e., choosing  $\tilde{b} < b$ ) are never optimal for the firm. The benefits from active deleveraging would entirely fall to the holders of existing debt in the form of lower default risk and a higher bond price. At the same time, the firm would drive up the price of the outstanding debt that it repurchases, and shareholders would lose part of the tax benefit of debt (Admati et al. 2018).

For the following propositions, we allow capital to adjust optimally according to the first-order condition in (10).

**PROPOSITION 2 (Cyclicality of Leverage, Default Risk, and Credit Spread):** *If  $b = 0$ , leverage, default risk, and the credit spread are constant in productivity  $z$ . If  $b > 0$  and capital increases in  $z$ , default risk and the credit spread are decreasing in  $z$ . Leverage is decreasing in  $z$  if  $\zeta$  is sufficiently close to one.*

A higher level of productivity  $z$  increases output. Proposition 2 states that without existing long-term debt, leverage, default risk, and credit spreads are acyclical. The reason is that changes in capital  $k$  are proportional to changes in debt  $b$  if  $b = 0$ . Productivity  $z$  affects the firm's optimal scale of production but not leverage or the risk of default.<sup>8</sup>

This result changes for  $b > 0$ . Dividing the firm's first-order condition (11) by  $k$  shows that, compared to the case when  $b = 0$ , the marginal cost of an increase in  $\bar{\varepsilon}$  is reduced by the term

$$\varphi(\bar{\varepsilon})(1 + c)\frac{b}{k}.$$

It denotes the part of the marginal increase in the expected cost of default that is disregarded by the firm. This term is scaled by the ratio  $b/k$ . A large stock of existing debt  $b$  relative to capital  $k$  provides a strong incentive to increase the risk of default.

Changes in productivity  $z$  affect the choice of  $k$ , whereas existing debt  $b$  is fixed. As a result, the ratio  $b/k$  increases when  $k$  falls. This implies that a given stock of existing debt increases the default risk by more during downturns than during expansions. The firm's default risk and credit spread become countercyclical. If the curvature parameter  $\zeta$  is sufficiently close to one, leverage is countercyclical as well.<sup>9</sup>

Proposition 2 demonstrates that a model with risky long-term debt can generate the countercyclical behavior of default risk, credit spreads, and leverage observed in the data. A countercyclical default rate implies that the firm's cost of capital increases during downturns. Proposition 3 states that this mechanism can amplify output fluctuations.

**PROPOSITION 3 (Deep Recessions):** *If  $b > 0$  and  $\zeta$  is sufficiently close to one, then a fall in capital  $k$  and output  $y$  that is caused by a drop in productivity  $z$  is amplified by the resulting increase in default risk.*

If  $b > 0$ , default risk increases when capital falls, which drives up expected default costs and the credit spread. This increases the firm's cost of capital and can thereby amplify the fall in investment and production.<sup>10</sup>

Taken together, Propositions 2 and 3 describe an adverse feedback loop between high default rates and low investment. If a firm chooses a low amount of capital, a

<sup>8</sup>The optimal scale of production depends on the *marginal* product of capital, while optimal leverage depends on expected default costs, which increase with the *average* product of capital. Given the assumed production technology, the marginal product is always proportional to the average product. As shown in the Appendix, this implies that optimal leverage does not vary with  $z$  or  $k$  in the benchmark case of  $b = 0$ .

<sup>9</sup>Ceteris paribus, higher default risk implies higher leverage, but this effect is counteracted if the fall in  $z$  reduces the firm's average product of capital. As we show in the Appendix, increased default risk discourages investment and thereby imposes a lower bound on the firm's marginal product of capital. Because the marginal product is approximately equal to the average product for  $\zeta \rightarrow 1$ , this implies that leverage increases together with default risk during a downturn.

<sup>10</sup>If  $b = 0$ , leverage and default risk are chosen to maximize the *average* return on capital net of taxes and default costs. Because of decreasing returns to scale, the *marginal* return net of taxes and default costs is maximized at a higher value of leverage and default risk. This implies that for low values of  $\zeta$ , a small increase in leverage and default risk can locally encourage investment (as shown in the Appendix). For  $\zeta \rightarrow 1$ , the gap between the firm's average and its marginal return disappears, and the increase in default risk unambiguously amplifies the fall in  $k$  and  $y$ .

positive stock of previously issued debt implies that the default rate and the credit spread increase (Proposition 2). The higher cost of capital can further depress investment (Proposition 3), which in turn drives up the default rate even more, and so on.

The described mechanism is very general. While we consider changes in (revenue) productivity, any initial change in  $k$  induced by various kinds of demand and supply shocks can be amplified in the way described above.

### E. Constrained Efficiency

The output response to changes in  $z$  is amplified because of the firm's disregard for the effects of its actions on the value of existing debt. A social planner who values the payoffs to all agents (shareholders *and* creditors) would maximize firm value (i.e., the value of all equity and debt claims) instead of shareholder value as in (6). Accordingly, the planner's objective reads as

$$(12) \quad pb - e + \frac{1}{1+r} \int_{\varepsilon}^{\infty} \left[ k - \tilde{b} + (1 - \tau)(y + \varepsilon k - wl - \delta k - c\tilde{b}) \right] \varphi(\varepsilon) d\varepsilon.$$

The constrained efficient allocation maximizes (12) subject to the same constraints as in the firm problem (6) and creditors' break-even condition (8). Proposition 4 states that both the history dependence of debt and the amplified output response due to countercyclical default are absent in this case.

**PROPOSITION 4 (Constrained Efficiency):** *If the firm internalizes the value of existing debt as in (12), the choice of debt  $\tilde{b}$  is independent of  $b$ . Leverage, default risk, and the credit spread are constant in productivity  $z$  for any value of  $b$ .*

The allocation described by Proposition 4 is markedly different from the equilibrium described above. Neither slow debt nor deep recessions arise. The difference between the equilibrium described above and the constrained efficient allocation is entirely due to the stock of existing debt  $b$ . It is therefore important to endogenize firms' choice of long-term debt in a dynamic model. This is the model we study in Section III.

## III. Business Cycle Model

After having established analytical results on slow debt and deep recessions, we now proceed to a dynamic open economy business cycle model of production, leverage, and debt maturity. The main additional feature is that firms can now sell short- and long-term bonds. The stock of existing debt  $b$  becomes endogenous: the amount of long-term debt issued today determines the stock of existing debt next period.

We introduce a linear issuance cost for new bonds. Short-term debt needs to be constantly rolled over, which implies high issuance costs. Long-term debt allows maintaining a given stock of debt at a lower level of bond issuance. The downside of long-term debt is that it increases the future amount of outstanding debt, which raises future default risk.

### A. Firm Setup

A firm  $i$  uses capital  $k_{it}$  and labor  $l_{it}$  to produce output according to

$$(13) \quad y_{it} = z_t (k_{it}^\psi l_{it}^{1-\psi})^\zeta, \quad \text{with: } \zeta, \psi \in (0, 1).$$

The natural logarithm of aggregate (revenue) productivity  $z_t$  follows an AR(1) process and is realized at the end of period  $t - 1$ . Earnings before interest and taxes are given as

$$(14) \quad y_{it} + \varepsilon_{it} k_{it} - w_t l_{it} - \delta k_{it} - f,$$

where  $f$  is a fixed cost of operation. The firm-specific idiosyncratic capital quality shock  $\varepsilon_{it}$  is i.i.d. and follows a continuous probability distribution  $\varphi(\varepsilon)$ .

The firm can finance capital with equity, short-term debt, and long-term debt.

**DEFINITION (Short-Term Debt):** A short-term bond issued at the end of period  $t - 1$  is a promise to pay one unit of the numeraire good in period  $t$  together with a fixed coupon payment  $c$ . The number of short-term bonds sold by firm  $i$  and due in period  $t$  is  $\tilde{b}_{it}^S$ .

**DEFINITION (Long-Term Debt):** A long-term bond issued at the end of period  $t - 1$  is a promise to pay a fixed coupon payment  $c$  in period  $t$ . In addition, the firm repays a fraction  $\gamma \in (0, 1)$  of the principal in period  $t$ . In period  $t + 1$ , a fraction  $1 - \gamma$  of the bond remains outstanding. The firm pays a coupon payment  $(1 - \gamma)c$  and repays the fraction  $\gamma$  of the remaining principal. In this manner, payments decay geometrically over time. The maturity parameter  $\gamma$  controls the speed of decay. The number of long-term bonds chosen by the firm at the end of period  $t - 1$  is  $\tilde{b}_{it}^L$ .

This computationally tractable specification of long-term debt goes back to Leland (1994). Short-term debt and long-term debt are of equal seniority.

**DEFINITION (Issuance Cost):** The firm pays an amount  $\eta$  for each new short-term or long-term bond sold. Repurchasing outstanding long-term debt (by choosing  $\tilde{b}_{it}^L < b_{it-1}$ ) is costless. The total issuance cost  $H(\tilde{b}_{it}^S, \tilde{b}_{it}^L, b_{it-1})$  is therefore

$$(15) \quad H(\tilde{b}_{it}^S, \tilde{b}_{it}^L, b_{it-1}) = \eta(\tilde{b}_{it}^S + \max\{\tilde{b}_{it}^L - b_{it-1}, 0\}),$$

where  $b_{it-1}$  is the stock of previously issued long-term bonds outstanding before the firm decides on its investment and financing policy at the end of period  $t - 1$ .

This issuance cost makes short-term debt unattractive because it needs to be constantly rolled over, which implies high issuance costs.



The firm finances its capital stock by injecting equity and by selling new short- and long-term bonds. Let  $q_{it-1}$  be the stock of assets in place before the firm decides on equity and debt issuance, and let  $e_{it-1}$  denote net equity issuance at the end of period  $t - 1$ . A negative value of  $e_{it-1}$  indicates a net dividend payment from the firm to shareholders. Capital in period  $t$  is given by

$$(16) \quad k_{it} = q_{it-1} + e_{it-1} + p_{it-1}^S \tilde{b}_{it}^S + p_{it-1}^L (\tilde{b}_{it}^L - b_{it-1}) - H(\tilde{b}_{it}^S, \tilde{b}_{it}^L, b_{it-1}).$$

The stock of firm assets in period  $t$  after production and repayment of debt is

$$(17) \quad q_{it} = k_{it} - \tilde{b}_{it}^S - \gamma \tilde{b}_{it}^L + (1 - \tau) [y_{it} + \varepsilon_{it} k_{it} - w_t l_{it} - \delta k_{it} - f - c(\tilde{b}_{it}^S + \tilde{b}_{it}^L)].$$

**DEFINITION (Limited Liability):** *Shareholders are free to default and hand over the firm's assets to creditors for liquidation. A fixed fraction  $\xi$  of firm assets is lost in this case.*

The timing is as follows. At the end of period  $t - 1$ , a firm has an amount  $b_{it-1}$  of long-term debt outstanding and assets  $q_{it-1}$ . The firm knows the aggregate state of the economy  $S_{t-1}$ , which includes aggregate productivity  $z_t$  and will be specified below. It chooses capital  $k_{it}$  by issuing equity  $e_{it-1}$  and by selling short-term bonds  $\tilde{b}_{it}^S$  and additional long-term bonds  $\tilde{b}_{it}^L - b_{it-1}$ . In period  $t$ , the firm hires labor  $l_{it}$  and produces output  $y_{it}$ . The idiosyncratic capital quality shock  $\varepsilon_{it}$  is realized, and the firm decides whether to default. If it decides not to default, the firm continues with assets  $q_{it}$  and outstanding long-term debt  $b_{it} = (1 - \gamma) \tilde{b}_{it}^L$ .

### B. Firm Problem

Firms maximize shareholder value and discount cash flows at the international risk-free rate  $r$ . Conditional on not defaulting, shareholder value at the end of period  $t - 1$  can be written as the sum of assets in place and a term that depends on future firm behavior:  $q_{it-1} + V_{t-1}(b_{it-1}, S_{t-1})$ . Because there are no equity adjustment costs, the amount of assets in place,  $q_{it-1}$ , has no influence on the optimal firm policy and the value  $V_{t-1}(b_{it-1}, S_{t-1})$ .

The amount of assets after production  $q_{it}$  in (17) is an increasing function of  $\varepsilon_{it}$ . There is a unique threshold realization  $\bar{\varepsilon}_{it}$ , which sets shareholder value to zero:

$$(18) \quad \bar{\varepsilon}_{it} : \quad q_{it} + E_{S_t|S_{t-1}} V_t((1 - \gamma) \tilde{b}_{it}^L, S_t) = 0.$$

If  $\varepsilon_{it}$  is smaller than  $\bar{\varepsilon}_{it}$ , the firm optimally decides to default.

We assume that the firm has no ability to commit to future actions. This lack of commitment not only affects the firm's default choice but also its decision of how much to produce and how to finance capital. The firm must therefore take its own future behavior as given. It can influence the value  $E_{S_t|S_{t-1}} V_t((1 - \gamma) \tilde{b}_{it}^L, S_t)$  through today's choice of long-term debt  $\tilde{b}_{it}^L$ .

Prior to the draw of  $\varepsilon_{it}$ , the firm chooses labor demand  $l_{it}$ :

$$(19) \quad l_{it} = \frac{\zeta(1-\psi)y_{it}}{w_t} \Leftrightarrow l_{it} = \left( \frac{\zeta(1-\psi)z_t k_{it}^{\psi\zeta}}{w_t} \right)^{\frac{1}{1-\zeta(1-\psi)}}.$$

Finally, we consider the firm's capital choice. At the end of period  $t-1$ , the firm chooses capital  $k_{it}$  and its financing mix:  $e_{it-1}$ ,  $\tilde{b}_{it}^S$ , and  $\tilde{b}_{it}^L$ . Given a stock of assets in place  $q_{it-1}$ , existing debt  $b_{it-1}$ , and the aggregate state of the economy  $S_{t-1}$ , a firm solves

$$(20) \quad \max_{\substack{k_{it}, e_{it} \geq \underline{e}, \\ \tilde{b}_{it}^S, \tilde{b}_{it}^L, \bar{\varepsilon}_{it}}} -e_{it-1} + \frac{1}{1+r} \int_{\bar{\varepsilon}_{it}}^{\infty} [q_{it} + E_{S_t|S_{t-1}} V_t((1-\gamma)\tilde{b}_{it}^L, S_t)] \varphi(\varepsilon) d\varepsilon$$

subject to

$$q_{it} = k_{it} - \tilde{b}_{it}^S - \gamma \tilde{b}_{it}^L + (1-\tau)[y_{it} + \varepsilon_{it}k_{it} - w_t l_{it} - \delta k_{it} - f - c(\tilde{b}_{it}^S + \tilde{b}_{it}^L)],$$

$$y_{it} = z_t (k_{it}^{\psi} l_{it}^{1-\psi})^{\zeta},$$

$$l_{it} = \left( \frac{\zeta(1-\psi)z_t k_{it}^{\psi\zeta}}{w_t} \right)^{\frac{1}{1-\zeta(1-\psi)}},$$

$$\bar{\varepsilon}_{it} : \quad q_{it} + E_{S_t|S_{t-1}} V_t((1-\gamma)\tilde{b}_{it}^L, S_t) = 0,$$

$$k_{it} = q_{it-1} + e_{it-1} + p_{it-1}^S \tilde{b}_{it}^S + p_{it-1}^L (\tilde{b}_{it}^L - b_{it-1}) - H(\tilde{b}_{it}^S, \tilde{b}_{it}^L, b_{it-1}).$$

The firm's choice of  $e_{it-1}$  is bounded from below:  $e_{it-1} \geq \underline{e}$ , with  $\underline{e} < 0$ . This constitutes an upper limit for dividend payments.<sup>11</sup>

### C. Creditors' Problem

The optimal firm policy crucially depends on the two bond prices  $p_{it-1}^S$  and  $p_{it-1}^L$ . Competitive creditors break even on expectation. Like shareholders, they discount cash flows at the international risk-free rate  $r$ . In case of default, the value of the firm's assets is

$$(21) \quad \underline{q}_{it} \equiv k_{it} + (1-\tau)(y_{it} + \varepsilon_{it}k_{it} - w_t l_{it} - \delta k_{it} - f).$$

<sup>11</sup> If the stock of existing debt  $b_{it-1}$  is sufficiently large, the firm may find it optimal to choose a corner solution and pay out the entire asset value of the firm as dividend:  $e_{it-1} = -q_{it-1}$ . In practice, it is illegal to pay dividends that substantially exceed firm earnings and deplete a firm's stock of capital. We choose the value of the constraint  $\underline{e}$  such that it rules out this corner solution but is not binding in equilibrium. The exact value of  $\underline{e}$  does not affect equilibrium variables.

At this point, creditors liquidate the firm's assets and receive  $(1 - \xi) q_{it}$ . Because short-term debt and long-term debt have equal seniority, the price of short-term debt is

$$(22) \quad p_{it-1}^S = \frac{1}{1+r} \left[ [1 - \Phi(\bar{\varepsilon}_{it})] (1+c) + \frac{(1-\xi)}{\tilde{b}_{it}^S + \tilde{b}_{it}^L} \int_{-\infty}^{\bar{\varepsilon}} q_{it} \varphi(\varepsilon) d\varepsilon \right].$$

The break-even price of short-term debt  $p_{it-1}^S$  only depends on firm behavior at time  $t$ , in particular on the risk of default  $\Phi(\bar{\varepsilon}_{it})$ . In contrast, the price of long-term debt  $p_{it-1}^L$  also depends on the future market value of long-term debt  $p_{it}^L = g_t((1-\gamma)\tilde{b}_{it}^L, S_t)$ :

$$(23) \quad p_{it-1}^L = \frac{1}{1+r} \left[ [1 - \Phi(\bar{\varepsilon}_{it})] [\gamma + c + (1-\gamma) g_t((1-\gamma)\tilde{b}_{it}^L, S_t)] + \frac{(1-\xi)}{\tilde{b}_{it}^S + \tilde{b}_{it}^L} \int_{-\infty}^{\bar{\varepsilon}} q_{it} \varphi(\varepsilon) d\varepsilon \right].$$

Because the future price of long-term debt  $p_{it}^L = g_t((1-\gamma)\tilde{b}_{it}^L, S_t)$  depends on future firm behavior, it is a function of the future state of the firm. Because the firm cannot directly control future firm behavior, the only way in which it can influence the future bond price is through today's choice of long-term debt  $\tilde{b}_{it}^L$ .

#### D. Equilibrium Firm Policy

In equilibrium, a firm maximizes shareholder value (20) subject to creditors' two break-even conditions (22) and (23). When selling long-term debt, a firm would like to commit to maintaining low levels of default risk in the future. This would raise today's price of long-term debt and lower the cost of capital. But such a promise is not credible. Once the debt has been sold, the firm has no incentive to take the effects of its actions on the value of existing debt into account. Because creditors have rational expectations, they correctly anticipate and price in the firm's future behavior.

Because we assume that the firm has no ability to commit to future actions, it must take its own future behavior as given and chooses today's policy as a best response. In other words, the firm plays a game against its future selves. As in Klein, Krusell, and Ríos-Rull (2008), we restrict attention to the Markov Perfect equilibrium; i.e., we consider policy rules that are functions of the payoff-relevant state variables. The time-consistent policy is a fixed point in which the future firm policy coincides with today's firm policy.

The value  $V_{t-1}(b_{it-1}, S_{t-1})$  can be computed recursively. We define the sum of assets in place  $q_{it-1}$  and equity issuance  $e_{it-1}$  as a choice variable:  $\tilde{e}_{it-1} \equiv q_{it-1} + e_{it-1}$ . Each period, the firm chooses a policy vector  $\phi(b, S) = \{k, \tilde{e}, \tilde{b}^S, \tilde{b}^L, \bar{\varepsilon}\}$ , which solves

$$(24) \quad V(b, S) = \max_{\phi(b, S) = \{k, \tilde{e} \geq \bar{\varepsilon}, \tilde{b}^S, \tilde{b}^L, \bar{\varepsilon}\}} -\tilde{e} + \frac{1}{1+r} \int_{\bar{\varepsilon}}^{\infty} \left[ q' + E_{S'} V((1-\gamma)\tilde{b}^L, S') \right] \varphi(\varepsilon) d\varepsilon$$

subject to

$$q' = k - \tilde{b}^S - \gamma \tilde{b}^L + (1 - \tau) [y + \varepsilon k - w(S)l - \delta k - f - c(\tilde{b}^S + \tilde{b}^L)],$$

$$y = z' (k^\psi l^{1-\psi})^\zeta,$$

$$l = \left( \frac{\zeta(1-\psi)z'k^{\psi\zeta}}{w(S)} \right)^{\frac{1}{1-\zeta(1-\psi)}},$$

$$\bar{\varepsilon} : q' + E_{S'|S} V((1-\gamma)\tilde{b}^L, S') = 0,$$

$$k = \bar{e} + p^S \tilde{b}^S + p^L (\tilde{b}^L - b) - H(\tilde{b}^S, \tilde{b}^L, b),$$

$$p^S = \frac{1}{1+r} \left[ [1 - \Phi(\bar{\varepsilon})] (1+c) + \frac{(1-\xi)}{\tilde{b}^S + \tilde{b}^L} \int_{-\infty}^{\bar{\varepsilon}} q\varphi(\varepsilon) d\varepsilon \right],$$

$$p^L = g(b, S)$$

$$= \frac{1}{1+r} \left[ [1 - \Phi(\bar{\varepsilon})] [\gamma + c + (1-\gamma)g((1-\gamma)\tilde{b}^L, S')] + \frac{(1-\xi)}{\tilde{b}^S + \tilde{b}^L} \int_{-\infty}^{\bar{\varepsilon}} q\varphi(\varepsilon) d\varepsilon \right].$$

Firm outcomes differ ex post because of the i.i.d. shock  $\varepsilon$ . However, because there are no equity adjustment costs, past earnings do not affect the current optimal firm policy  $\phi(b, S)$ .

To construct aggregate variables, we assume a constant unit mass of firms. Defaulting firms exit the economy and are replaced by new entrants. To enter, firms pay a cost, which is financed with long-term debt. This entry cost is set such that entrants always operate with the same amount of outstanding long-term debt  $b$  as incumbent firms. This assumption ensures that at any point in time the mass of firms remains constant and that all firms in the economy are ex ante identical.<sup>12</sup>

### E. Households

We close the model by introducing a representative domestic household. The household works, consumes, and invests its savings at the international risk-free rate  $r$ . Government revenue from taxation is paid out to the household as a lump-sum

<sup>12</sup>Crouzet (2017), Karabarounis and Macnamara (2021), and Jungherr and Schott (2021) study heterogeneous firm models with risky long-term debt without aggregate shocks.

transfer. We assume GHH preferences over consumption  $C$  and labor  $L$ . Period utility is therefore

$$(25) \quad u\left(C - \frac{L^{1+\theta}}{1+\theta}\right),$$

with  $u(\cdot)$  being strictly increasing and concave and  $\theta > 0$ . These preferences yield the labor supply curve

$$(26) \quad w_t = L_t^\theta.$$

### F. Equilibrium

We study the equilibrium of a dynamic open economy business cycle model with a given international risk-free rate  $r$  and an endogenous wage  $w$ . The sufficient aggregate state of the economy consists of aggregate productivity  $z'$  and the aggregate stock of existing debt  $B$ :  $S = (z', B)$ .

**DEFINITION** (Recursive Competitive Equilibrium): *A recursive competitive equilibrium consists of (i) a policy vector  $\phi(b, S) = \{k, \tilde{e}, \tilde{b}^S, \tilde{b}^L, \tilde{\varepsilon}\}$ , bond prices  $p^S$  and  $p^L$ , and a value function  $V(b, S)$ ; (ii) a wage function  $w(S)$ ; and (iii) a stochastic aggregate law of motion  $S' = F(S)$  such that*

(i)  $\phi(b, S)$ ,  $p^S$ ,  $p^L$ , and  $V(b, S)$  solve the firm problem (24) for  $b = B$ .

(ii) The labor market clears:

$$L(S) = w(S)^{\frac{1}{\theta}} = l(b, S) \quad \text{for } b = B.$$

(iii) The stochastic aggregate law of motion  $S' = F(S)$  is consistent with individual behavior:

$$B' = (1 - \gamma)\tilde{b}^L(b, S) \quad \text{for } b = B.$$

GDP in this economy is

$$(27) \quad Y = y - f - \xi \int_{-\infty}^{\tilde{\varepsilon}} q\varphi(\varepsilon) d\varepsilon - H(\tilde{b}^{S'}, \tilde{b}^{L'}, b').$$

### G. Solution Method

We find the global solution to the dynamic firm problem in (24) and the equilibrium defined above using value function iteration and interpolation. The key difficulty consists in finding the equilibrium price of long-term debt  $p^L$ . Optimal firm behavior depends on  $p^L$ , which itself depends on the expected future price of long-term debt, which in turn depends on future firm behavior. We solve this fixed point problem by computing the equilibrium of a finite-horizon economy. Starting from a final date, we iterate backward until all prices and quantities have converged. We then

use the first-period equilibrium allocation as the equilibrium of the infinite-horizon economy. This means that we iterate simultaneously on the value  $V(b, S)$  and the long-term bond price  $p^L$  (as in Hatchondo and Martinez 2009). The presence of the idiosyncratic i.i.d. capital quality shock  $\varepsilon$  with continuous probability distribution  $\varphi(\varepsilon)$  facilitates the computation of  $p^L$  (cf. Chatterjee and Eyigungor 2012).

In solving (24), firms take the wage rate  $w(S)$  and the aggregate law of motion  $S' = F(S)$  as given. To compute these equilibrium objects, we start with a guess for  $w(S)$  and a candidate law of motion  $S' = F(S)$ . We then solve the firm problem (24) and use its solution to update the aggregate law of motion  $S' = F(S)$ . Once individual firm behavior is consistent with the aggregate law of motion, we use labor demand  $l(b, S)$  with  $b = B$  and labor supply  $L(S)$  to update our initial guess for the wage function  $w(S)$ . We provide a detailed description of the computational algorithm in the online Appendix.

### H. Calibration

We follow Arellano, Bai, and Kehoe (2019) in calibrating an open economy business cycle model to US data. Mendoza and Quadrini (2010) document that about one-half of the rise in net borrowing by the US nonfinancial sector since the mid-1980s has been financed by net foreign capital inflows, and by 2008 about one-half of the stock of Treasury bills held outside the US financial sector was owned by foreign agents.<sup>13</sup>

For some of the model parameters, we use standard values, while others are calibrated to match moments from the US nonfinancial corporate sector. All parameters are summarized in Table 1.

The model period is one year. The international riskless rate is set to  $r = 1/0.97 - 1 = 3.09$  percent. The debt coupon is  $c = r$ , which implies that the equilibrium price of a riskless short-term bond and a riskless long-term bond are both equal to one.

The production technology parameters  $\zeta$  and  $\psi$  are taken from Bloom et al. (2018). The annual depreciation rate  $\delta$  is 10 percent. The fixed cost  $f$  is set to generate zero firm profits on average, which implies that  $EV(0, z) = 0$ . The value for  $\theta$  is chosen to generate a Frisch elasticity of labor supply of four as in King and Rebelo (1999).

The probability distribution of the idiosyncratic capital quality shock  $\varepsilon$  is assumed to be Normal with zero mean and standard deviation  $\sigma_\varepsilon$ . The natural logarithm of aggregate productivity follows an AR(1) process:

$$(28) \quad \ln z_t = \rho_z \ln z_{t-1} + \epsilon_t,$$

where  $\epsilon_t$  is white noise with standard deviation  $\sigma_z$ . The autocorrelation  $\rho_z$  is 0.909, as in Khan and Thomas (2013). The standard deviation  $\sigma_z$  generates the same volatility of GDP as in the US data.

<sup>13</sup> The main advantage of working with an open economy is that this setup avoids the strongly procyclical riskless real interest rate characteristic of the standard closed economy RBC model but at odds with the US postwar data. Alternative approaches include habits (Beaudry and Guay 1996, Winberry 2021) or nominal rigidities in combination with an appropriately specified monetary policy rule (e.g., Bernanke, Gertler, and Gilchrist 1999).

TABLE 1—PARAMETERIZATION

Parameter	Description	Value
$r$	riskless rate	0.0309
$c$	debt coupon	$r$
$\zeta$	technology parameter	0.75
$\psi$	technology parameter	0.33
$\delta$	depreciation rate	0.1
$f$	fixed cost	0.1641
$\theta$	inverse Frisch elasticity	0.25
$\rho_z$	persistence aggregate shock	0.909
$\sigma_z$	SD aggregate shock	0.0028
$\tau$	corporate income tax rate	0.4
$\gamma$	repayment rate long-term debt	0.1284
$\sigma_\varepsilon$	SD idiosyncratic shock	0.6519
$\xi$	default cost	0.669
$\eta$	debt issuance cost	0.0077

TABLE 2—MODEL FIT

Moment	Data	Model
Leverage: Firm debt/firm assets	29.3%	29.3%
Long-term debt share	75.4%	75.4%
Average credit spread	2.3%	2.3%

*Sources:* Data on leverage and the long-term debt share are from Compustat. The average credit spread is from Adrian, Colla, and Shin (2013). See online Appendix for details.

We follow Gomes, Jermann, and Schmid (2016) in setting the tax rate  $\tau = 0.4$ .<sup>14</sup> The repayment rate of long-term debt  $\gamma$  is a key parameter. We set it to match the Macaulay duration of US corporate bonds with remaining term to maturity above one year. Gilchrist and Zakrajsek (2012) calculate an average duration of 6.47 years. This implies  $\gamma = 0.1284$ .

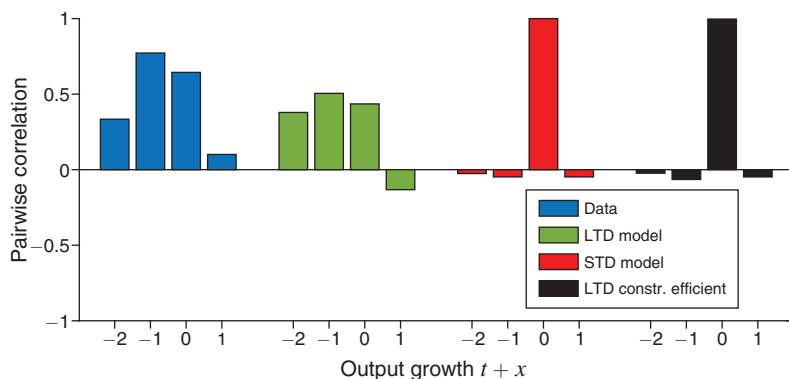
The remaining three parameters  $\sigma_\varepsilon$ ,  $\xi$ , and  $\eta$  are chosen to match moments from the US nonfinancial corporate sector: firm leverage, the average credit spread, and the share of long-term debt. The leverage ratio is informative about the standard deviation of the firm-specific capital quality shock  $\sigma_\varepsilon$ , as a higher volatility of earnings induces firms to reduce leverage in order to contain the risk of default. The average credit spread pins down the default cost  $\xi$ . The share of long-term debt is informative about the debt issuance cost  $\eta$ , as a higher issuance cost increases firms' long-term debt share in the model.<sup>15</sup>

Table 2 compares the empirical moments to simulated data from the business cycle model. The model matches the data very well. Our calibration is also broadly consistent with a number of untargeted moments. Altinkılıç and Hansen (2000) provide micro-evidence for the debt issuance cost  $\eta$ . They calculate an average underwriter spread of 1.1 percent of bond proceeds. Our model generates a value of 0.8 percent.

<sup>14</sup> Hennessy and Whited (2005) suggest a value of 0.3. Gomes, Jermann, and Schmid (2016) argue that  $\tau$  should be thought of as capturing additional relative benefits of using debt rather than equity (e.g., equity issuance costs).

<sup>15</sup> We provide results on the sensitivity of key model moments with respect to parameter values in the online Appendix.



FIGURE 5. CORRELATIONS FIRM CREDIT GROWTH  $t$  AND OUTPUT GROWTH  $t + x$ 

Notes: Bars show pairwise correlations between annual growth of total firm debt at the end of year  $t$  and GDP growth in year  $t + x$ . The four blue bars to the left (*Data*) are calculated using Flow of Funds data on real total debt of nonfinancial firms and real GDP (cf. Figure 2). All other correlations are calculated from simulated model data.

The annual default rate in our model is 2.6 percent, which is slightly lower than the estimate for the business failure rate used in Bernanke, Gertler, and Gilchrist (1999) or the average of Moody's expected default frequency across rated and unrated Compustat firms reported in Hovakimian, Kayhan, and Titman (2011).

### I. Quantitative Results

We use the numerical solution of our dynamic business cycle model to study the economy's response to cyclical shocks. We show that the model replicates the dynamic co-movement between firm debt and output growth. Slow debt gives rise to deep recessions and slow recoveries.

*Slow Debt.*—Figure 5 shows the co-movement between firm credit and output. The first four blue bars on the left show the US data. They represent pairwise correlations between growth in firm debt in year  $t$  and GDP growth in year  $t + x$ . They are identical to the bars on the left-hand side of Figure 2. The second group of green bars, labeled *LTD model*, shows the corresponding moments generated from simulated time series of the dynamic business cycle model with short-term and long-term debt described above.

An important result is that the model generates the slow adjustment of debt. The model correlations tend to be slightly lower than in the data, but the overall pattern of the empirical correlations is well captured. In particular, the model correlations display the characteristic peak at the first lag of output observed in the data. These moments were not targeted during the calibration of the model.

*Deep Recessions.*—We now explore the economic mechanism that allows the model to replicate the slow-moving behavior of firm debt. Figure 6 shows impulse response functions following a negative shock to aggregate productivity  $z_t$  of the size of 2.4 standard deviations at  $t = 1$ . The solid green line depicts the economy's

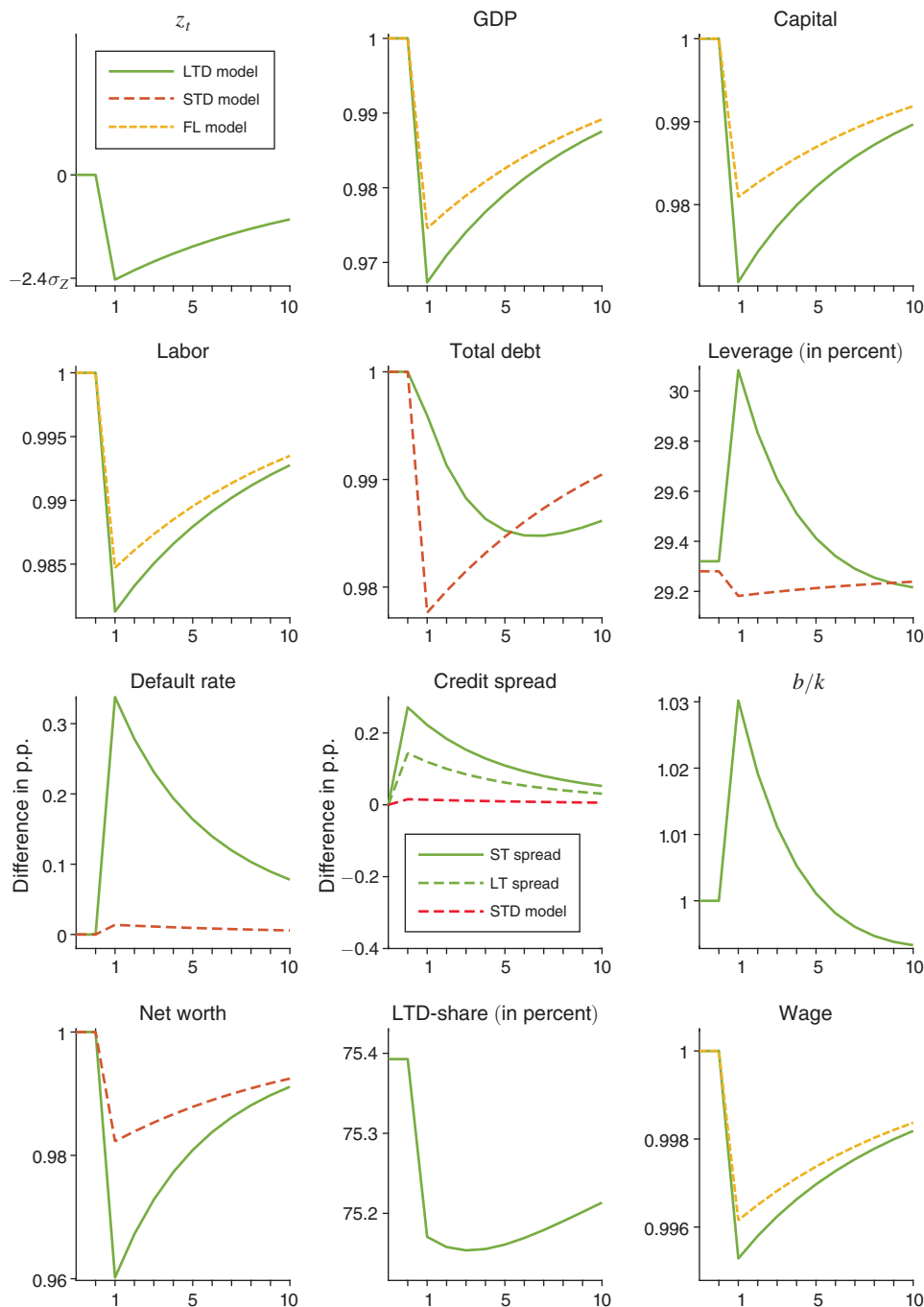


FIGURE 6. IMPULSE RESPONSE FUNCTIONS

*Notes:* **LTD model:** Green lines show impulse response functions in the benchmark model with long-term and short-term debt (Section III F). In the *Credit spread* panel, the spread on short-term debt in the benchmark model is shown by the solid green line (*ST spread*); the spread on long-term debt is the dashed green line (*LT spread*). **STD model:** Red dashed lines show impulse response functions in a short-term debt model (see online Appendix for details). **FL model:** Yellow dash-dotted lines show impulse response functions of GDP, capital, labor, and the wage rate in a frictionless model (see online Appendix for details).

response in the model described above (*LTD model*). The dash-dotted yellow line shows the response of output, capital, labor, and wages in a frictionless model without default costs, taxes, or debt issuance costs (*FL model*). The Modigliani-Miller irrelevance result holds in the frictionless model.<sup>16</sup>

In both models, firms react to a negative shock to  $z_t$  by reducing investment and labor demand. In the long-term debt model, firms enter the downturn with an existing stock of long-term debt which has been issued prior to the shock, when investment and debt issuance were high. The fall in investment increases the ratio of existing debt  $b$  over capital  $k$ . As shown above, firms do not internalize potential default costs, which accrue to the holders of existing debt. When the ratio of existing debt over capital rises, firms choose higher levels of leverage and default risk. Leverage is increased by reducing total debt at a slower rate than capital. This mechanism generates the slow response of total debt relative to capital and output shown in Figure 6.<sup>17</sup>

The increase in leverage also maps into a rise in credit spreads during the downturn. Firms issue short- and long-term debt. The credit spread on short-term debt (*ST spread*, green solid line) rises by more during the downturn than the spread on long-term debt (*LT spread*, green dashed line). This is because the price of short-term debt  $p^S$  only depends on the risk of default next period, while the price of long-term debt  $p^L$  depends on expected default rates in all future periods.

Within a period, the initial fall in capital and the corresponding rise in default risk amplify each other. Higher default risk increases firms' cost of capital through higher credit spreads and thereby further discourages investment. Capital falls by more, which in turn raises the ratio  $b/k$ . Firms respond by choosing even higher levels of leverage and default risk, which again drives up the default risk and credit spreads and so forth. This adverse feedback loop between high default risk and low investment explains the difference between the initial output response of the long-term debt model and the frictionless model. Instead of a drop in output of 2.5 percentage points as in the frictionless model, GDP falls on impact by 3.25 percentage points in the long-term debt model. The unconditional volatility of output is increased by 20 percent relative to the frictionless model.<sup>18</sup>

*Slow Recoveries.*—We showed how slow debt gives rise to an amplified output response following a shock. Figure 6 shows that the long-term debt model also generates a slow recovery.<sup>19</sup> Several periods after the shock, the distance of output from its unconditional mean is still larger relative to its frictionless counterpart. With the aggregate stock of existing debt being the only endogenous state variable of the economy, these dynamics are shaped by firms' endogenous adjustment of the stock of existing debt  $b$ .

<sup>16</sup> See online Appendix for a detailed description of the frictionless model.

<sup>17</sup> A linear debt issuance cost such as (15) can generate an inaction region for debt issuance. This does not play a role in our model. Given our parameterization, firms issue positive amounts of short-term debt and long-term debt in each period.

<sup>18</sup> The parameter sensitivity analysis in the online Appendix provides additional results on the tight link between the slow adjustment of firm debt and GDP volatility in this model.

<sup>19</sup> We use the term "slow recovery" in the sense of Taylor (2014) and Fernald et al. (2017). In their terminology, a recovery is "slow" if output remains below trend for a long time, as was the case for the United States after the 2008–2009 recession.

After the initial shock, the ratio  $b/k$ , leverage, the default rate, and credit spreads remain elevated for several periods. Firms understand that by actively reducing long-term debt, they can decrease the future stock of existing debt and thereby also future levels of  $b/k$ , leverage, and default risk. Long-term debt can be decreased in two ways: (i) firms can reduce total debt for a given long-term debt share, or (ii) firms can reduce the long-term debt share for a given level of total debt. In the first case, firms forgo the tax benefit of debt. In the second case, firms incur higher future costs of debt issuance. While firms fully internalize these costs, they do not internalize all benefits of lower future default risk. Most of these benefits accrue to the holders of existing long-term debt. For this reason, firms choose to adjust the stock of long-term debt slowly. This implies that  $b/k$ , leverage, the default rate, and credit spreads remain elevated after the initial shock. Through this persistent increase in the cost of capital, slow debt generates slow recoveries.

These results highlight the crucial role of history dependence in firms' debt management. The issuance of long-term debt during a boom creates a liability, which extends well into the subsequent downturn. Firms are reluctant to reduce the high debt levels inherited from the past because the benefits of this reduction would mostly fall to the holders of existing debt. The resulting persistent increase in default risk and credit spreads amplifies and prolongs the downturn.

*Business Cycle Statistics.*—Table 3 compares the cyclical behavior of key model variables to the data. The table reports each variable's contemporaneous correlation with GDP growth as well as its standard deviation and autocorrelation.

The model replicates the countercyclical behavior of leverage, the default rate, and credit spreads. This is a success of the model. Financial accelerator models often generate procyclical leverage and default risk in response to standard first moment shocks (e.g., Carlstrom and Fuerst 1997). Adding second moment shocks results in countercyclical default risk and credit spreads, but leverage remains procyclical (e.g., Gilchrist, Sim, and Zakrajšek 2014). Our long-term debt model generates countercyclical default rates, credit spreads, and leverage.

The model is also successful in generating a procyclical term structure of credit spreads. The term structure of credit spreads is the difference between the credit spread on long-term debt and short-term debt. It decreases during a recession because the short-term spread increases by more than the long-term spread (both in the model and in the data). Whereas the short-term spread only depends on next period's risk of default, the long-term spread is a weighted average of default risk in all future periods and is therefore less sensitive to short-term fluctuations.<sup>20</sup>

In the model, variations in the ratio of existing debt over capital  $b/k$  are an important part of the mechanism that generates deep recessions and slow recoveries. Table 3 shows that the model captures the countercyclical behavior of this variable together with a similar degree of persistence as in the data. Importantly, the quantitative model does not overstate the empirical volatility of  $b/k$ .

<sup>20</sup>This result is consistent with the estimated impulse responses of corporate bond spreads of different maturities to credit shocks in Gilchrist, Yankov, and Zakrajšek (2009).

TABLE 3—BUSINESS CYCLE STATISTICS

Variable $x$ (in percent)	Data	LTD model	STD model
<i><math>\Delta</math>Total Debt</i>			
$\text{corr}(x, \Delta\text{GDP})$	0.59	0.44	1.00
$\sigma_x$	4.22	0.34	0.96
$\rho_x$	0.59	0.81	−0.05
<i>Leverage: Debt/Assets</i>			
$\text{corr}(x, \Delta\text{GDP})$	−0.24	−0.61	0.21
$\sigma_x$	2.32	0.45	0.10
$\rho_x$	0.68	0.73	0.91
<i>Default rate</i>			
$\text{corr}(x, \Delta\text{GDP})$	−0.48	−0.33	−0.21
$\sigma_x$	0.72	0.25	0.01
$\rho_x$	0.37	0.85	0.91
<i>Average credit spread</i>			
$\text{corr}(x, \Delta\text{GDP})$	−0.89	−0.33	−0.21
$\sigma_x$	0.83	0.15	0.02
$\rho_x$	0.52	0.85	0.91
<i>Spread term structure</i>			
$\text{corr}(x, \Delta\text{GDP})$	0.57	0.35	—
$\sigma_x$	0.41	0.09	—
$\rho_x$	0.51	0.83	—
<i><math>b/k</math></i>			
$\text{corr}(x, \Delta\text{GDP})$	−0.30	−0.60	—
$\sigma_x$	1.92	0.45	—
$\rho_x$	0.63	0.76	—
<i>LTD share</i>			
$\text{corr}(x, \Delta\text{GDP})$	−0.08	0.01	—
$\sigma_x$	5.31	0.36	—
$\rho_x$	0.85	0.97	—

Notes:  $\Delta$  is the real growth rate. Other variables are in levels.  $\text{corr}(x, \Delta\text{GDP})$  is the contemporaneous correlation between  $x$  and real GDP growth.  $\sigma_x$  and  $\rho_x$  denote the standard deviation and autocorrelation.

Sources: US Flow of Funds, Compustat, St. Louis Fed (FRED), and Giesecke et al. (2014). All data is annual. See online Appendix for details.

Whereas the cyclicity of financial variables in the long-term debt model is broadly in line with the data, the size of these fluctuations is generally too small. This suggests an important role of additional forces (e.g., credit supply shocks, monetary policy shocks) in shaping the empirical behavior of financial variables in the corporate sector.

*The Role of Long-Term Debt.*—To illustrate the crucial role of long-term debt in generating slow debt and deep recessions, we compare the results described above to an alternative model in which firms use only short-term debt (*STD model*).<sup>21</sup>

Consider the third group of red bars in Figure 5, which shows correlations between growth in firm debt at time  $t$  and output at time  $t + x$  in the short-term debt model. The difference between the dynamic patterns generated by the *STD model* and the

<sup>21</sup> For the short-term debt model, we set  $\gamma = 1$  and calibrate it to the same moments as the benchmark model with long-term debt. See online Appendix for details.

*LT*D model is striking. In the short-term debt model, firm debt strongly co-moves with contemporaneous output. In contrast to the long-term debt model and the data, there is no positive correlation with lagged output in the short-term debt model.

The dashed red lines in Figure 6 show impulse response functions from the short-term debt model. The dynamics of GDP, capital, labor, and wages are virtually identical to the frictionless model and therefore almost indistinguishable in Figure 6. Leverage, the default rate, and credit spreads hardly move over the business cycle. The model lacks the feedback loop between default risk and investment, which gives rise to amplification in the long-term debt model.

Finally, in the third column of Table 3, we present business cycle statistics from the short-term debt model. The co-movement between output and firm debt is too strong, and firm debt is not persistent enough. The lack of volatility in financial variables is even more pronounced than in the long-term debt model.

While the short-term debt model cannot replicate the empirical lag structure between output and credit growth, the absence of a lag in the correlations of Figure 5 is in line with the firm-level evidence from Section I, where we showed that credit of firms with low long-term debt shares does not lag output growth.

### J. Constrained Efficiency

In the long-term debt model, firms adjust debt slowly because they do not internalize all associated costs. They exert an externality on the holders of previously issued debt, who bear a large part of the costs of increased default risk. Ultimately though, the costs of slow debt fall back on shareholders. Creditors break even on expectation. They correctly anticipate and price in all effects of existing debt on current and future firm behavior.

When a firm sells long-term debt, it would like to promise to maintain low future levels of default risk in order to raise today's price of long-term debt. But because a low bond price today becomes a sunk cost tomorrow, this promise is not credible. Slow debt is a symptom of firms' lack of commitment to future actions.

A social planner who is subject to the same lack of commitment and faces the same set of constraints as the firm can do better in the sense that the payoff of creditors *and* shareholders can be increased. To see this, we revisit the problem of constrained efficiency studied in the two-period model above. Just as in Section IIE, we study an individual firm that is controlled by a planner who maximizes the entire firm value, that is, the sum of all equity and debt claims, existing and newly issued bonds alike. The planner solves<sup>22</sup>

$$(29) \quad W(b, S) = \max_{\{k, \bar{e} \geq \underline{e}, \bar{b}^S, \bar{b}^L, \bar{\varepsilon}\}} p^L b - T(b, S) - \bar{e} \\ + \frac{1}{1+r} E_{S|S} \left\{ \int_{\bar{\varepsilon}}^{\infty} [q' + W((1-\gamma)\bar{b}^L, S')] \varphi(\varepsilon) d\varepsilon \right\}$$

<sup>22</sup>In order to highlight the commitment problem at the firm level and to stay as close as possible to the equilibrium allocation studied above, the planner chooses the policy of an individual firm without taking into account general equilibrium effects, e.g., on the wage rate.

subject to the same set of constraints as in (24). The state-contingent tax  $T(b, S)$  in (29) is specified such that in equilibrium  $T(b, S) = p^L b$ . In this way, the planner takes into account how firm behavior affects the market value of existing debt,  $p^L b$ , without mechanically affecting the value  $W(b, S)$ . The value  $W(b, S)$  will differ from  $V(b, S)$  in (24) only because of different firm behavior. See online Appendix for details.

Figure 7 compares the solution of the constrained efficient problem in (29) (black dashed lines) to the decentralized long-term debt model (green solid lines). The main result is that neither slow debt nor deep recessions are part of the constrained efficient allocation. The planner strongly reduces total debt in response to a negative productivity shock and thereby avoids the rise in leverage and credit spreads observed in the long-term debt model. This reduces the initial output drop of 3.25 percentage points in the long-term debt model to 2.5 percentage points in the constrained efficient allocation.

The reason for the difference between the constrained efficient allocation and the decentralized long-term debt model is that the planner does not face the same commitment problem as firms. The planner always internalizes the effect of current debt issuance on the payoff of existing creditors. The reason is not that the planner has more commitment power than firms but simply that the planner's objective includes the payoff of creditors *and* shareholders. After a negative shock, slow adjustment of debt would increase the default risk and hurt the holders of existing debt. Because the planner internalizes these costs, debt is adjusted immediately.<sup>23</sup>

The four black bars on the right of Figure 5 show the dynamic correlation between debt and output growth in the constrained efficient solution. Slow debt is absent because the constrained efficient debt issuance policy does not feature history dependence.

#### IV. Conclusion

Firm-level data suggest that the slow adjustment of firm debt to changes in economic activity is related to firms' use of long-term debt. We have shown that introducing long-term debt into a standard business cycle model of production, firm financing, and costly default successfully replicates the empirical lag structure between firm debt and output. The model is also successful in generating countercyclical firm leverage, default rates, and credit spreads as well as the procyclical term structure of credit spreads.

Rising credit spreads during downturns increase firms' cost of capital and thereby amplify the fall in investment and output. Because firms choose to reduce debt only gradually, deep recessions are followed by slow recoveries.

In the model, firms exert an externality on the holders of existing debt. A social planner who internalizes the payoff to existing creditors would implement a different

<sup>23</sup> Absent the commitment problem described above, the downside of long-term debt relative to short-term debt disappears. As a result, only long-term debt is issued in the planner's allocation, and the optimal maturity choice is always at a corner solution. Therefore, the long-term debt share is acyclical in the constrained efficient allocation. Because only long-term debt is issued, only the long-term spread is displayed for the constrained efficient allocation in Figure 7.



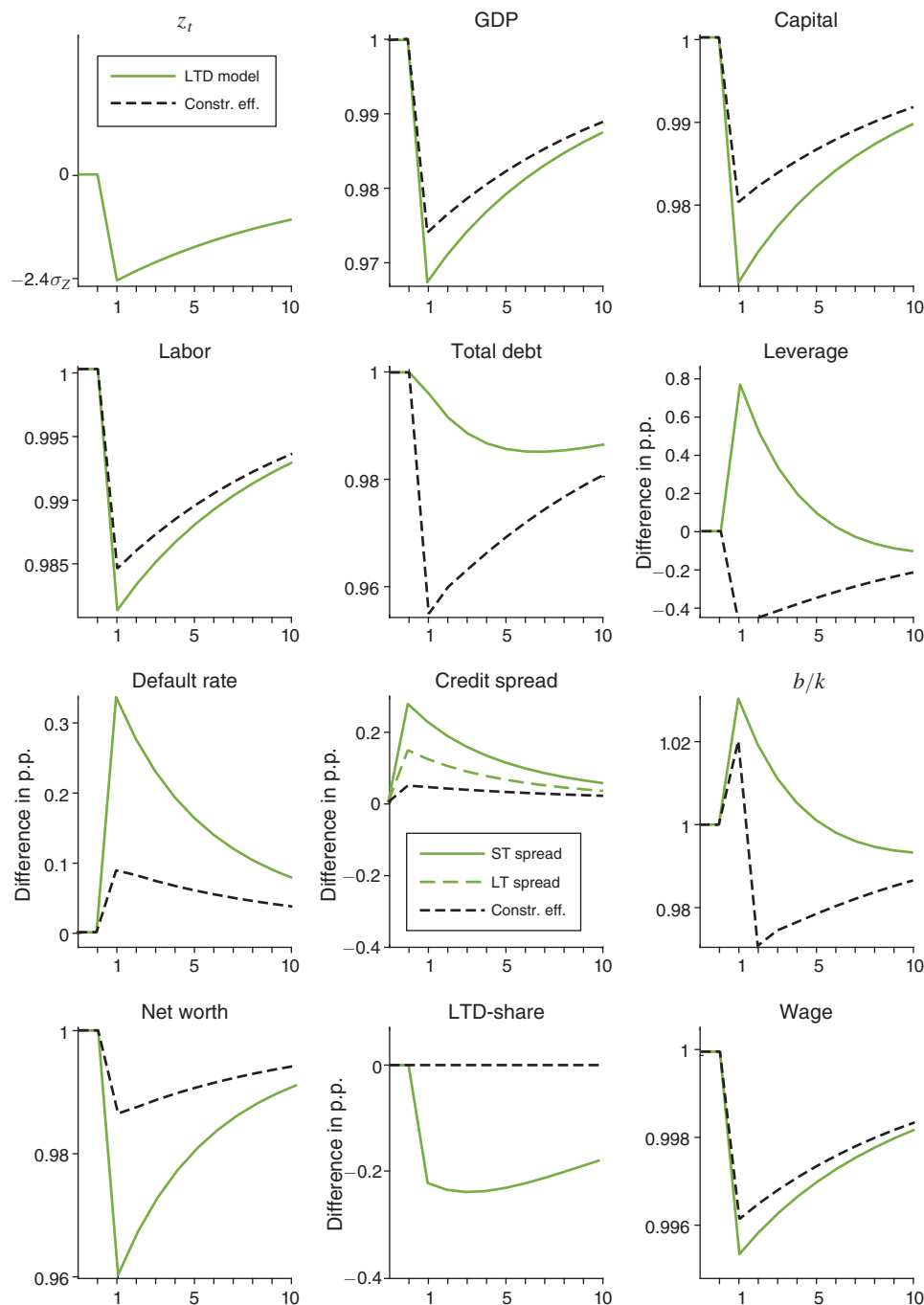


FIGURE 7. IMPULSE RESPONSE FUNCTIONS—CONSTRAINED EFFICIENCY

*Notes:* **LTD model:** Green lines show impulse response functions in the benchmark model with long-term and short-term debt (Section IIIF). In the *Credit spread* panel, the spread on short-term debt in the benchmark model is shown by the solid green line (*ST spread*); the spread on long-term debt is the dashed green line (*LT spread*). **Constr. eff.:** Black dashed lines show impulse response functions of the constrained efficient allocation (see online Appendix for details). Because only long-term debt is issued in the constrained efficient allocation, the *Credit spread* panel shows only the spread on long-term debt (*Constr. eff.*).

allocation. Neither slow debt nor deep recessions are constrained efficient. The results presented above suggest substantial room for welfare-improving stabilization policies. Studying specific policies that target this inefficiency is an important topic for future work.

Throughout our analysis, aggregate fluctuations were caused by productivity shocks. However, the adverse feedback loop between high credit spreads and low investment triggered by slow debt is a very general mechanism. Any initial change in firm investment induced by various kinds of shocks can be amplified in the same way. It would be interesting to explore the role of different types of shocks (e.g., financial shocks) within the framework described above.

Another potential direction for future work is to add working-capital constraints. When firms need to pay part of the wage bill up front, credit spreads directly affect firms' labor demand. This generates a time-varying labor wedge, which has been found to be important in explaining aggregate fluctuations (e.g., Chari, Kehoe, and McGrattan 2007; Jermann and Quadrini 2012; Arellano, Bai, and Kehoe 2019).

#### APPENDIX: TWO-PERIOD MODEL—PROOFS AND DERIVATIONS

In the two-period model, the firm solves (6) subject to creditors' break-even constraint (8). As shown below, this problem can be rewritten in terms of only two choice variables:  $k$  and  $\bar{\varepsilon}$ .

The first step is to express output net of wage payments  $y - wl$  as a function of capital only. Given the wage rate  $w$ , a necessary and sufficient condition for optimal labor demand is

$$(A1) \quad l^* = \frac{\zeta(1-\psi)y}{w} \Leftrightarrow l^* = \left( \frac{\zeta(1-\psi)zk^{\psi\zeta}}{w} \right)^{\frac{1}{1-\zeta(1-\psi)}}.$$

This implies for output net of wage payments

$$(A2) \quad y^* - wl^* = Ak^\alpha,$$

where  $A$  and  $\alpha$  are functions of productivity  $z$ , the wage  $w$ , and the technology parameters  $\zeta$  and  $\psi$ :

$$(A3) \quad A \equiv z^{\frac{1}{1-\zeta(1-\psi)}} [1 - \zeta(1-\psi)] \left( \frac{\zeta(1-\psi)}{w} \right)^{\frac{\zeta(1-\psi)}{1-\zeta(1-\psi)}} \quad \text{and} \quad \alpha \equiv \frac{\zeta\psi}{1 - \zeta(1-\psi)},$$

with  $\alpha \in (0, 1)$ . Applying (A2) to the definition of  $\bar{\varepsilon}$  in (5) yields

$$(A4) \quad \tilde{b}[1 + (1-\tau)c] = k + (1-\tau)(Ak^\alpha + \bar{\varepsilon}k - \delta k) \\ \Leftrightarrow \tilde{b} = \frac{k + (1-\tau)(Ak^\alpha + \bar{\varepsilon}k - \delta k)}{1 + (1-\tau)c}.$$

Substituting (A2), (A4), and (3) into the firm problem in (6), we obtain

$$(A5) \quad \max_{k, \tilde{b}, \bar{\varepsilon}, p} q - k + p(\tilde{b} - b) + \frac{1 - \tau}{1 + r} k \int_{\bar{\varepsilon}}^{\infty} (\varepsilon - \bar{\varepsilon}) \varphi(\varepsilon) d\varepsilon$$

subject to

$$p = \frac{1}{1 + r} \left[ [1 - \Phi(\bar{\varepsilon})] (1 + c) + \frac{(1 - \xi)}{\tilde{b}} \int_{-\infty}^{\bar{\varepsilon}} q \varphi(\varepsilon) d\varepsilon \right],$$

$$\tilde{b} = \frac{k + (1 - \tau)(A k^{\alpha} + \bar{\varepsilon} k - \delta k)}{1 + (1 - \tau)c}.$$

The firm problem (A5) characterizes the equilibrium allocation in terms of the two choice variables  $k$  and  $\bar{\varepsilon}$ . The first-order conditions for capital (10) and  $\bar{\varepsilon}$  (11) are derived under the assumption made in the main text that  $\xi = 1$ . The marginal product of capital is  $MPK \equiv A \alpha k^{\alpha-1}$ , which is increasing in  $z$  (through  $A$ ) and decreasing in  $k$ . The partial derivative used in (11) is  $\partial \tilde{b} / \partial \bar{\varepsilon} = (1 - \tau)k / [1 + (1 - \tau)c]$ .

#### *Proof of Proposition 1*

PROOF:

The first-order condition for  $\bar{\varepsilon}$  is given by (11). At an interior solution, the second derivative of the objective function (A5) with respect to  $\bar{\varepsilon}$  is negative. The left-hand side of (11) is increasing in  $b$ , with  $d/db = \varphi(\bar{\varepsilon})(1 + c)$ . It follows that with a higher  $b$ , (11) can only hold at a higher level of  $\bar{\varepsilon}$ . For a given  $k$ , this implies a higher level of  $\tilde{b}$  because from (A4) we have that  $\partial \tilde{b} / \partial \bar{\varepsilon} > 0$ . It follows that  $\partial \tilde{b} / \partial b > 0$ . ■

#### *Proof of Proposition 2*

PROOF:

By writing (A4) as

$$(A6) \quad \tilde{b} = k \frac{1 + (1 - \tau)(A k^{\alpha-1} + \bar{\varepsilon} - \delta)}{1 + (1 - \tau)c},$$

and dividing the first-order condition for  $\bar{\varepsilon}$  in (11) by  $k$ , we obtain

$$(A7) \quad [1 - \Phi(\bar{\varepsilon})] \frac{(1 - \tau)}{1 + (1 - \tau)c} \tau c - \varphi(\bar{\varepsilon})(1 + c) \left( \frac{1 + (1 - \tau)(A k^{\alpha-1} - \delta + \bar{\varepsilon})}{1 + (1 - \tau)c} - \frac{b}{k} \right) = 0.$$

Productivity  $z$  enters the firm problem through the term  $A$ , which is increasing in  $z$ . Furthermore,  $\alpha$  converges to one when  $\zeta$  tends toward one. There are two cases to consider: (i)  $b = 0$  and (ii)  $b > 0$ .

(i) If  $b = 0$ , (A7) reads as

$$(A8) \quad [1 - \Phi(\bar{\varepsilon})] \frac{(1 - \tau)}{1 + (1 - \tau)c} \tau c - \varphi(\bar{\varepsilon})(1 + c) \left( \frac{1 + (1 - \tau)(Ak^{\alpha-1} - \delta + \bar{\varepsilon})}{1 + (1 - \tau)c} \right) = 0.$$

By isolating the *marginal* product of capital  $MPK = A\alpha k^{\alpha-1}$  in (10) and combining it with (A8) to substitute out the *average* product of capital  $Ak^{\alpha-1}$ , one is left with a single equation with  $\bar{\varepsilon}$  as the only endogenous variable. Neither profitability  $A$  nor capital  $k$  appear in this equation. It follows that the optimal choice of  $\bar{\varepsilon}$  and the default rate  $\Phi(\bar{\varepsilon})$  do not depend on  $A$  if  $b = 0$ . This result extends to the bond price and the credit spread. From (A6), leverage is

$$(A9) \quad \frac{\tilde{b}}{k} = \frac{1 + (1 - \tau)(Ak^{\alpha-1} - \delta + \bar{\varepsilon})}{1 + (1 - \tau)c}.$$

We know from (A8) that the average product of capital  $Ak^{\alpha-1}$  must be constant if  $\bar{\varepsilon}$  does not change. It follows that also leverage is constant in  $A$  if  $b = 0$ .

(ii) If  $b > 0$ , the first-order condition for  $\bar{\varepsilon}$  is given by (A7). The left-hand side is obtained by adding the term  $\varphi(\bar{\varepsilon})(1 + c)b/k$  to the left-hand side of (A8). This term is positive and decreasing in  $k$ :

$$(A10) \quad \frac{\partial}{\partial k} \left[ \varphi(\bar{\varepsilon})(1 + c) \frac{b}{k} \right] = -\frac{b}{k^2} \varphi(\bar{\varepsilon})(1 + c).$$

If the optimal choice of  $k$  is increasing in  $A$ , it follows that higher values of  $A$  imply lower optimal values of  $\bar{\varepsilon}$  if  $b > 0$ . In this case, the default rate  $\Phi(\bar{\varepsilon})$  is falling in  $A$ . This implies that the bond price  $p$  rises and the credit spread falls in  $A$ .

It remains to be shown that also leverage decreases in  $A$  if  $\alpha$  is sufficiently close to one. From (A9), leverage is increasing in the term  $Ak^{\alpha-1} + \bar{\varepsilon}$ . Consider the third term on the left-hand side of (10): the *Marginal increase in expected stock of equity*  $\tilde{q}$ . This term increases if  $\bar{\varepsilon}$  falls. Because  $\bar{\varepsilon}$  falls if  $A$  rises, this term increases in  $A$ . In order for the first-order condition (10) to hold, the second term, the *Marginal increase in market value of newly issued debt*  $p(\tilde{b} - b)$ , must fall if  $A$  increases. But the probability  $[1 - \Phi(\bar{\varepsilon})]$  increases in  $A$ . It follows that the term  $MPK + \bar{\varepsilon} = A\alpha k^{\alpha-1} + \bar{\varepsilon}$  must fall in  $A$ . If  $\alpha$  is sufficiently close to one, this term is approximately equal to the term  $Ak^{\alpha-1} + \bar{\varepsilon}$ . But if  $Ak^{\alpha-1} + \bar{\varepsilon}$  falls in  $A$ , also leverage falls in  $A$ . ■

*Proof of Proposition 3*

PROOF:

Consider the marginal effect ( $ME_k$ ) of capital on the firm's objective (A5) as given by the left-hand side of first-order condition (10):

$$(A11) \quad ME_k \equiv -1 + \frac{1+c}{1+r} [1 - \Phi(\bar{\varepsilon})] \frac{1 + (1-\tau)(A\alpha k^{\alpha-1} - \delta + \bar{\varepsilon})}{1 + (1-\tau)c} \\ + \frac{1-\tau}{1+r} \int_{\bar{\varepsilon}}^{\infty} (\varepsilon - \bar{\varepsilon}) \varphi(\varepsilon) d\varepsilon = 0.$$

Consider an increase in  $z$ . This increases  $A$  and therefore the marginal product of capital  $A\alpha k^{\alpha-1}$ . This is the direct effect of an increase in  $z$  on the firm's choice  $k$ . In addition, there is also an indirect effect of  $A$  through  $\bar{\varepsilon}$ :

$$(A12) \quad \frac{\partial ME_k}{\partial A} = \frac{1+c}{1+r} [1 - \Phi(\bar{\varepsilon})] \frac{1-\tau}{1 + (1-\tau)c} \alpha k^{\alpha-1} + \frac{\partial \bar{\varepsilon}}{\partial A} \frac{\partial ME_k}{\partial \bar{\varepsilon}}.$$

The first term on the right-hand side of (A12) is the direct effect of an increase in  $A$ . It is always positive. The second term is the indirect effect, which runs through  $\bar{\varepsilon}$ . From Proposition 2, we know that  $\bar{\varepsilon}$  decreases in  $A$  if  $k$  increases and  $b > 0$ :  $\partial \bar{\varepsilon} / \partial A < 0$ . It follows that a fall in  $\bar{\varepsilon}$  amplifies the positive response of  $k$  to an increase in  $A$  if and only if  $\partial ME_k / \partial \bar{\varepsilon} < 0$ .

A marginal increase of  $\bar{\varepsilon}$  affects  $ME_k$  according to

$$(A13) \quad \frac{\partial ME_k}{\partial \bar{\varepsilon}} = -\frac{1+c}{1+r} \varphi(\bar{\varepsilon}) \frac{1 + (1-\tau)(A\alpha k^{\alpha-1} + \bar{\varepsilon} - \delta)}{1 + (1-\tau)c} \\ + [1 - \Phi(\bar{\varepsilon})] \frac{1-\tau}{1+r} \frac{\tau c}{1 + (1-\tau)c}.$$

An increase in  $\bar{\varepsilon}$  increases default risk by  $\varphi(\bar{\varepsilon})$ . This discourages investment because it increases the probability that the *marginal* product of capital  $A\alpha k^{\alpha-1}$  is lost. Because  $\bar{\varepsilon}$  is chosen optimally, the first-order condition (11) holds. Dividing (11) by  $k$  yields

$$(A14) \quad [1 - \Phi(\bar{\varepsilon})] (1-\tau) \frac{\tau c}{1 + (1-\tau)c} - \varphi(\bar{\varepsilon}) (1+c) \frac{\tilde{b} - b}{k} = 0,$$

where  $(\tilde{b} - b)/k$  is

$$(A15) \quad \frac{\tilde{b} - b}{k} = \frac{1 + (1-\tau)(A\alpha k^{\alpha-1} - \delta + \bar{\varepsilon})}{1 + (1-\tau)c} - \frac{b}{k}.$$

The firm chooses  $\bar{\varepsilon}$ , taking into account part of the total expected costs of default, which increase with leverage  $\tilde{b}/k$  and therefore with the *average* product of capital  $Ak^{\alpha-1}$ . By combining (A14) with (A13), we derive

$$(A16) \quad \frac{\partial ME_k}{\partial \bar{\varepsilon}} = -\frac{1+c}{1+r} \varphi(\bar{\varepsilon}) \frac{1 + (1-\tau)(A\alpha k^{\alpha-1} - \delta + \bar{\varepsilon})}{1 + (1-\tau)c} + \varphi(\bar{\varepsilon}) \frac{1+c}{1+r} \frac{\tilde{b} - b}{k}.$$

This expression is negative if and only if

$$(A17) \quad \frac{(1 - \tau)A k^{\alpha-1}(1 - \alpha)}{1 + (1 - \tau)c} < \frac{b}{k}.$$

The left-hand side of (A17) is positive if  $\alpha < 1$ . If  $b$  is sufficiently small, this may imply that the inequality (A17) does not hold and  $\partial ME_k / \partial \bar{\varepsilon} > 0$ . For small positive values of  $\alpha$  and  $b$ , a small decrease in  $\bar{\varepsilon}$  may therefore discourage investment and mitigate rather than amplify changes in  $z$ . The reason is that the firm chooses  $\bar{\varepsilon}$  by taking into account the expected loss of the *average* product of capital. At the same time, the firm chooses  $k$  by taking into account the expected loss of the *marginal* product of capital, which is always lower than the *average* product. The marginal return net of taxes and default costs is maximized at a higher value of leverage and default risk than the average return.

This gap between the average and the marginal product disappears as  $\alpha \rightarrow 1$ . The left-hand side of (A17) is approximately zero in this case, and the inequality (A17) is always satisfied. In this case, the fact that  $\bar{\varepsilon}$  falls in  $A$  (and  $z$ ) amplifies the positive response of  $k$  with respect to  $A$  (and  $z$ ). Through the same mechanism, the negative response of  $k$  to a fall in  $A$  is amplified by the resulting increase in  $\bar{\varepsilon}$ . The last step is to recall that optimal labor demand  $l$  is an increasing function of  $k$  and output  $y$  is an increasing function of  $k$  and  $l$ . ■

#### *Proof of Proposition 4*

PROOF:

The planner's objective is given by (12). With  $\xi = 1$ , the derivative of (12) with respect to  $k$  yields the same first-order condition for capital as in (10). The stock of existing debt  $b$  does not appear in that expression. The planner's first-order condition for  $\bar{\varepsilon}$  is

$$(A18) \quad [1 - \Phi(\bar{\varepsilon})] \frac{\partial \tilde{b}}{\partial \bar{\varepsilon}} \pi c - \varphi(\bar{\varepsilon})(1 + c)\tilde{b} = 0.$$

The planner's choice of  $\bar{\varepsilon}$  differs from the firm's choice characterized by (11). In particular, it is independent of the stock of existing debt  $b$ . Because neither  $k$  depends on  $b$ , it follows that the planner's choice of  $\tilde{b}$  (A4) is independent of  $b$ .

Equation (A18) is identical to the firm's first-order condition (11) for the case without existing debt:  $b = 0$ . By applying the same reasoning as in the Proof of Proposition 2, it is straightforward to show that leverage, default risk, and the credit spread are independent of  $z$  (for any value of  $b$ ). ■

#### REFERENCES

Admati, Anat R., Peter M. DeMarzo, Martin F. Hellwig, and Paul Pfleiderer. 2018. "The Leverage Ratchet Effect." *Journal of Finance* 73 (1): 145–98.

- Adrian, Tobias, Paolo Colla, and Hyun Song Shin.** 2013. "Which Financial Frictions? Parsing the Evidence from the Financial Crisis of 2007 to 2009." In *NBER Macroeconomics Annual 2012*, Vol. 27, edited by Daron Acemoglu, Jonathan Parker, and Michael Woodford, 159–214. Cambridge, MA: National Bureau of Economic Research.
- Aguiar, Mark, Manuel Amador, Hugo Hopenhayn, and Iván Werning.** 2019. "Take the Short Route: Equilibrium Default and Debt Maturity." *Econometrica* 87 (2): 423–62.
- Altunkılıç, Oya, and Robert S. Hansen.** 2000. "Are There Economies of Scale in Underwriting Fees? Evidence of Rising External Financing Costs." *Review of Financial Studies* 13 (1): 191–218.
- Arellano, Cristina, Yan Bai, and Patrick J. Kehoe.** 2019. "Financial Frictions and Fluctuations in Volatility." *Journal of Political Economy* 127 (5): 2049–2103.
- Arellano, Cristina, and Ananth Ramanarayanan.** 2012. "Default and the Maturity Structure in Sovereign Bonds." *Journal of Political Economy* 120 (2): 187–232.
- Beaudry, Paul, and Alain Guay.** 1996. "What Do Interest Rates Reveal about the Functioning of Real Business Cycle Models?" *Journal of Economic Dynamics and Control* 20 (9–10): 1661–82.
- Bernanke, Ben S., Mark Gertler, and Simon Gilchrist.** 1999. "The Financial Accelerator in a Quantitative Business Cycle Framework." In *Handbook of Macroeconomics*, Vol. 1, edited by John B. Taylor and Michael Woodford, 1341–1393. Amsterdam: Elsevier.
- Bloom, Nicholas, Max Floetotto, Nir Jaimovich, Itay Saporta-Eksten, and Stephen J. Terry.** 2018. "Really Uncertain Business Cycles." *Econometrica* 86 (3): 1031–65.
- Caggese, Andrea, and Ander Pérez Orive.** 2015. "The Interaction between Household and Firm Dynamics and the Amplification of Financial Shocks." Barcelona GSE Working Paper 866.
- Carlstrom, Charles T., and Timothy S. Fuerst.** 1997. "Agency Costs, Net Worth, and Business Fluctuations: A Computable General Equilibrium Analysis." *American Economic Review* 87 (5): 893–910.
- Chari, Varadarajan V., Patrick J. Kehoe, and Ellen R. McGrattan.** 2007. "Business Cycle Accounting." *Econometrica* 75 (3): 781–836.
- Chatterjee, Satyajit, and Burcu Eyigungor.** 2012. "Maturity, Indebtedness, and Default Risk." *American Economic Review* 102 (6): 2674–99.
- Chatterjee, Satyajit, and Burcu Eyigungor.** 2015. "A Seniority Arrangement for Sovereign Debt." *American Economic Review* 105 (12): 3740–65.
- Christiano, Lawrence J., Roberto Motto, and Massimo Rostagno.** 2014. "Risk Shocks." *American Economic Review* 104 (1): 27–65.
- Cooley, Thomas, Ramon Marimon, and Vincenzo Quadrini.** 2004. "Aggregate Consequences of Limited Contract Enforceability." *Journal of Political Economy* 112 (4): 817–47.
- Covas, Francisco, and Wouter J. Den Haan.** 2012. "The Role of Debt and Equity Finance over the Business Cycle." *Economic Journal* 122 (565): 1262–86.
- Crouzet, Nicolas.** 2017. "Default, Debt Maturity, and Investment Dynamics." [https://www.kellogg.northwestern.edu/faculty/crouzet/html/papers/Default\\_DebtMaturity\\_Investment\\_latest.pdf](https://www.kellogg.northwestern.edu/faculty/crouzet/html/papers/Default_DebtMaturity_Investment_latest.pdf) (accessed June 1, 2019).
- DeMarzo, Peter, and Zhiguo He.** 2020. "Leverage Dynamics without Commitment." *Journal of Finance* 76 (3): 1195–1250.
- Fernald, John G., Robert E. Hall, James H. Stock, and Mark W. Watson.** 2017. "The Disappointing Recovery of Output after 2009." NBER Working Paper 23543.
- Giesecke, Kay, Francis A. Longstaff, Stephen Schaefer, and Ilya A. Strebulaev.** 2014. "Macroeconomic Effects of Corporate Default Crisis: A Long-Term Perspective." *Journal of Financial Economics* 111 (2): 297–310.
- Gilchrist, Simon, Jae W. Sim, and Egon Zakrajšek.** 2014. "Uncertainty, Financial Frictions, and Investment Dynamics." NBER Working Paper 20038.
- Gilchrist, Simon, Vladimir Yankov, and Egon Zakrajšek.** 2009. "Credit Market Shocks and Economic Fluctuations: Evidence from Corporate Bond and Stock Markets." *Journal of Monetary Economics* 56 (4): 471–93.
- Gilchrist, Simon, and Egon Zakrajšek.** 2012. "Credit Spreads and Business Cycle Fluctuations." *American Economic Review* 102 (4): 1692–1720.
- Gomes, João, Urban Jermann, and Lukas Schmid.** 2016. "Sticky Leverage." *American Economic Review* 106 (12): 3800–28.
- Gomes, João, Amir Yaron, and Lu Zhang.** 2003. "Asset Prices and Business Cycles with Costly External Finance." *Review of Economic Dynamics* 6 (4): 767–88.
- Hatchondo, Juan Carlos, and Leonardo Martinez.** 2009. "Long-Duration Bonds and Sovereign Defaults." *Journal of International Economics* 79 (1): 117–125.



- Hatchondo, Juan Carlos, Leonardo Martinez, and César Sosa-Padilla.** 2016. "Debt Dilution and Sovereign Default Risk." *Journal of Political Economy* 124 (5): 1383–1422.
- Hennessy, Christopher A., and Toni M. Whited.** 2005. "Debt Dynamics." *Journal of Finance* 60 (3): 1129–65.
- Hovakimian, Armen, Ayla Kayhan, and Sheridan Titman.** 2011. "Are Corporate Default Probabilities Consistent with the Static Trade-Off Theory?" *Review of Financial Studies* 25 (2): 315–40.
- Jermann, Urban, and Vincenzo Quadrini.** 2012. "Macroeconomic Effects of Financial Shocks." *American Economic Review* 102 (1): 238–71.
- Jungherr, Joachim, and Immo Schott.** 2021. "Optimal debt maturity and firm investment." *Review of Economic Dynamics* 42: 110–32.
- Jungherr, Joachim, and Immo Schott.** 2022. "Replication data for: Slow Debt, Deep Recessions." American Economic Association [publisher], Inter-university Consortium for Political and Social Research [distributor]. <https://doi.org/10.3886/E120385V1>.
- Karabarbounis, Marios, and Patrick Macnamara.** 2021. "Misallocation and financial frictions: The role of long-term financing." *Review of Economic Dynamics* 40: 44–63.
- Khan, Aubhik, and Julia K. Thomas.** 2013. "Credit Shocks and Aggregate Fluctuations in an Economy with Production Heterogeneity." *Journal of Political Economy* 121 (6): 1055–1107.
- King, Robert G., and Sergio T. Rebelo.** 1999. "Resuscitating Real Business Cycles." In *Handbook of Macroeconomics*, Vol. 1, edited by John B. Taylor and Michael Woodford, 927–1007. Amsterdam: Elsevier.
- Kiyotaki, Nobuhiro, and John Moore.** 1997. "Credit Cycles." *Journal of Political Economy* 105 (2): 211–48.
- Klein, Paul, Per Krusell, and José-Víctor Ríos-Rull.** 2008. "Time-Consistent Public Policy." *Review of Economic Studies* 75 (3): 789–808.
- Leland, Hayne.** 1994. "Bond Prices, Yield Spreads, and Optimal Capital Structure with Default Risk." University of California at Berkeley Research Program in Finance Working Paper 240.
- Mendoza, Enrique G., and Vincenzo Quadrini.** 2010. "Financial Globalization, Financial Crises and Contagion." *Journal of Monetary Economics* 57 (1): 24–39.
- Miao, Jianjun, and Pengfei Wang.** 2010. "Credit Risk and Business Cycles." <http://people.bu.edu/miao/credit22.pdf>.
- Occhino, Filippo, and Andrea Pescatori.** 2015. "Debt Overhang in a Business Cycle Model." *European Economic Review* 73: 58–84.
- Paul, Pascal.** 2020. "A Macroeconomic Model with Occasional Financial Crises." *Journal of Economic Dynamics and Control* 112: 103830.
- Poeschl, Johannes.** 2020. "Corporate Debt Maturity and Investment over the Business Cycle." [https://www.nationalbanken.dk/en/research/economists/Documents/debt\\_maturity\\_paper.pdf](https://www.nationalbanken.dk/en/research/economists/Documents/debt_maturity_paper.pdf).
- Taylor, John B.** 2014. "The Role of Policy in the Great Recession and the Weak Recovery." *American Economic Review* 104 (5): 61–66.
- Winberry, Thomas.** 2021. "Lumpy Investment, Business Cycles, and Stimulus Policy." *American Economic Review* 111 (1): 364–96.
- Xiang, Haotian.** 2019. "Time Inconsistency and Financial Covenants." SSRN Working Paper 3274047.