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## Article

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## Research paper

## Experimental modeling of PEM fuel cells using a new improved seagull optimization algorithm

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## ABSTRACT

This study proposes an optimal model to design and simulate the proton exchange membrane fuel cell (PEMFC) systems. The purpose of this paper is to present an improved version of seagull optimization algorithm for optimal parameter identification of the PEMFC stacks. The new algorithm uses the Lévy flight mechanism to give faster convergence rates. The sum of the squared error between the empirical values and achieved optimal model is analyzed based on two empirical PEMFC models including BCS 500-W and NedStack PS6. This analysis is performed to show the potential of the presented method by considering different conditions. Simulation results are compared with several optimization algorithms and show the algorithm's superiority in terms of the solutions quality and the convergence speed.

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## 1. Introduction

Renewable energy refers to a variety of energy sources that, unlike non-renewable (fossil fuels), have the potential to be renewed by nature in a short period of time (Ahadi et al., 2015; Aghajani and Ghadimi, 2018; Mirzapour et al., 2019). Natural energy storage on Earth is coming to an end, and the resources that human beings have used to date will sooner or later be over. The only way to save on future generations and the survival of humanity is taking refuge in renewable energy resources.

Renewable energy is the energy that comes from recyclable or renewable resources and can be replaced by natural resources. This kind of energy has a much less environmental impact than fossil fuels which make them more popular toward fossil fuels. One of the potential renewable energy resources with high advantage like high performance energy conversion and greater environmental compatibility is fuel cell (Ghadimi, 2012; Abbaspour et al., 2016; Longo et al., 2019; Technology, 2019; Wang et al., 2019).

The increasing demand for energy and the limitation of natural energy sources have led researchers into study on fuel cells. Although there are still problems with fuel cell, they have advantages over non-polluting energy, high energy conversion efficiency, noise-free operation, and high reliability compared to other energy-generating products, and hopes to be one of the

most important sources of clean energy for household and transportation purposes in the future.

The market for fuel cell power generators is very large and includes government, military and industrial applications. It is also used as a backup force in emergencies in telecommunications, medical industries, offices, hospitals, large hotels and computer systems (Noori et al., 2016). The fuel cells are relatively quiet and silent, so they are suitable for local power generation. In addition to reducing the need to expand the distribution network, the heat generated from these plants can be used to heat and produce steam.

Unlike other energy converters, fuel cells are not limited to use a particular power source and are capable of using different fuels such as methanol, ethanol, hydrogen, natural gas, propane and gasoline (Dicks and Rand, 2018; Choudhary and Sahu, 2019). Fuel cells, because of the ability to be portable, are widely used in mobile and portable applications such as UAVs and electric vehicles (Karimi et al., 2012; Mekhilef et al., 2012; Ijaodola et al., 2019).

Among several kinds of fuel cells, proton exchange membrane fuel cells (PEMFCs) are considered as a satisfied model which is because of its fast start-up, low operating temperature, and high efficiency (Hames et al., 2018; Taner, 2018). Polymer fuel cells are high power generators that can achieve a 40%–50% electrical efficiency in different power scales. They have also an operating temperature between 30 °C and 100 °C.

The basis for energy conversion in polymer fuel cells is the thermal reaction between oxygen and hydrogen in the air. The result of this reaction is electricity, heat and distilled water.

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## Nomenclature

|            |                                                |
|------------|------------------------------------------------|
| $N_{nc}$   | Aumber for series connected cells of the PEMFC |
| $E_{op}$   | Activation over-potential of the cells         |
| $E_{ops}$  | Over-potential saturation in cells             |
| $T_{PEM}$  | Operating cell temperature                     |
| $P_H$      | Partial pressure of the $H_2$                  |
| $P_{O_2}$  | Partial pressure of the $O_2$                  |
| $P_{H_2O}$ | Partial pressure of the $H_2O$                 |
| $I_{PEM}$  | Operating current of the PEMFC                 |
| $C_{H_2}$  | Hydrogen saturation                            |
| $C_{O_2}$  | Oxygen saturation                              |
| $l$        | Thickness for the membrane                     |
| $\lambda$  | Tunable parameter                              |
| $\beta$    | Parametric coefficient                         |
| $J_{max}$  | Maximum value of $J$                           |
| $E_{oc}$   | Open circuit potential condition per cell      |
| $E_O$      | Ohmic voltage drop in each cell                |
| $S$        | Membrane surface                               |
| $R_{hc}$   | Vapor relative humidity at cathode             |
| $R_{ha}$   | Vapor relative humidity at anode               |
| $P_a$      | Inlet pressure for the anode                   |
| $P_c$      | Inlet pressure for the cathode                 |
| $R_m$      | Membrane resistance                            |
| $R_c$      | Connections resistance                         |
| $\beta_i$  | Experimental coefficients                      |
| $\rho_m$   | Membrane resistivity                           |
| $J$        | Real current density                           |

Advantages of polymer fuel cell, such as lower weight and the possibility of the system's renewability in a closed and independent battery cycle, have attracted research on replacing the polymer fuel cell system with the use of batteries in satellites.

For more realizing and design of PEMFCs, we need to perform a reliable model for them. PEMFC have different features such as dynamic models of the system, empirical data from the experiments that can be utilized for modeling and steady-state stability (Sun et al., 2015; Ge et al., 2018; El-Hay et al., 2019). There are several approaches for modeling PEMFC in the literatures.

In 1991, Springer et al. proposed a one-dimensional steady-state model of a PEMFC (Springer et al., 1991). The model was based on isothermal parameterization. In 2010, Caux et al. proposed a state-space model for identification of fuel cells in EVs (Caux et al., 2010). The method used energy management in HEVs. They finally work on temperature and gas flows control of the fuel cell.

In 2014, Panagiotis et al. proposed two dynamical models based on semi-empirical formulas and the electrical equivalent for PEMFC stack (Papadopoulos et al., 2014). Furthermore, the model was improved based on transfer function and semi-empirical equations. The main objective was to design a parametric analysis model for models capability.

In 2017, Solsona et al. presented an empirically validated model for a low-temperature PEMFC along with a humidifier (Solsona et al., 2017). They also utilized a control strategy model based on Nafion® membrane. Simulation results were compared with the Experimental results.

In 2017, a real-time model for PEMFC was presented by Kumar et al. They studied the modality of the method by different validation such as ARX and ARMAX (Kumar et al., 2018). They

used MATLAB platform for system identification. To control the desired load current, PI and PID controllers were employed. In addition, several research works have been established on the modeled PEMFC (Bao and Bessler, 2015; Solsona et al., 2017).

However using aforementioned methods for modeling are useful for designing and analyzing the fuel cells, there is some depletion to these methods. Classic methods are based on considering all physical concepts of the fuel cells such as power, thermodynamics, momentum's conservation to achieve a precise thermal model for anything that happens in them which makes the modeling progress complicated.

We also know that all the uncertain processes which happen in the system cannot be modeled by the analytical modeling. This subject hardens using this type of modeling, especially in the practical operations. Meanwhile, for enhancing the accuracy of the model to achieve a close performance model from the actual PEMFC, it is important to reach the best parameter values of the system model.

Recently, the applications of bio-inspired meta-heuristic algorithm for different fields have been extensively increasing (Holand, 1992; Razmjoooy and Ramezani, 2014; Razmjoooy et al., 2016; Bagheri et al., 2018).

There are great deals of research works about the applications of bio-inspired optimization methods for parameter identification in the PEMFCs.

For example, particle swarm optimization (Li et al., 2010), Multi-verse optimizer (Fathy and Rezk, 2018), Genetic algorithm (Ariza et al., 2018), dragonfly algorithm (Hamal et al., 2018), differential evolution algorithm (Sun et al., 2015), etc.

In 2018, Mamaghani (Mamaghani et al., 2018) proposed a multi-objective procedure for an HT-PEM fuel cell utilized in a micro combined heat and power system. Various optimization methods were performed to find the optimal value of a defined multi-objective function. The method determined the optimal operating parameters and their corresponding efficiency indices. For the multi-objective optimization, electrical and thermal efficiencies have been utilized. The results showed that during the optimization, the electrical performance of the net is up to 32.3% and its thermal efficiency is higher than 61.1%.

Literature review show that utilizing optimization algorithms gives better results for the PEMFC identification. The main objective is that they can escape from the local minimum which leads them to obtain global optimum (Razmjoooy and Ramezani, 2014; Namadchian et al., 2016; Razmjoooy et al., 2016).

Seagull Optimization Algorithm (SOA) is a newly meta-heuristic technique that is proposed by Dhiman and Kumar (Dhiman and Kumar, 2019). The simplicity of SOA by less parameters and also its easy to implement feature make it applicable for different works. However, sometimes SOA trapped into the local optima. In this study, a new developed version of the SOA algorithm has been used for solving the nonlinear modeling problem of the PEMFCs identification problem.

## 2. Mathematical model of PEMFC

There are different models for PEMFCs which have been given based on the thermodynamic and the chemical aspects (Luo et al., 2015; Razmjoooy et al., 2018). A fuel cell includes an electrolyte membrane, an anode (negative charge electrode), and a cathode (positive charge electrode). Hydrogen is ionized in the anode, producing electrons and protons. The electrons are sent to an external circuit and generate the current, and hydrogen protons pass through the membrane by transferring molecules to other molecules. In cathode, oxygen synthesizes with the electrons from the external circuit and the protons from the anode, generating heat and water. Both the cathode and anode include

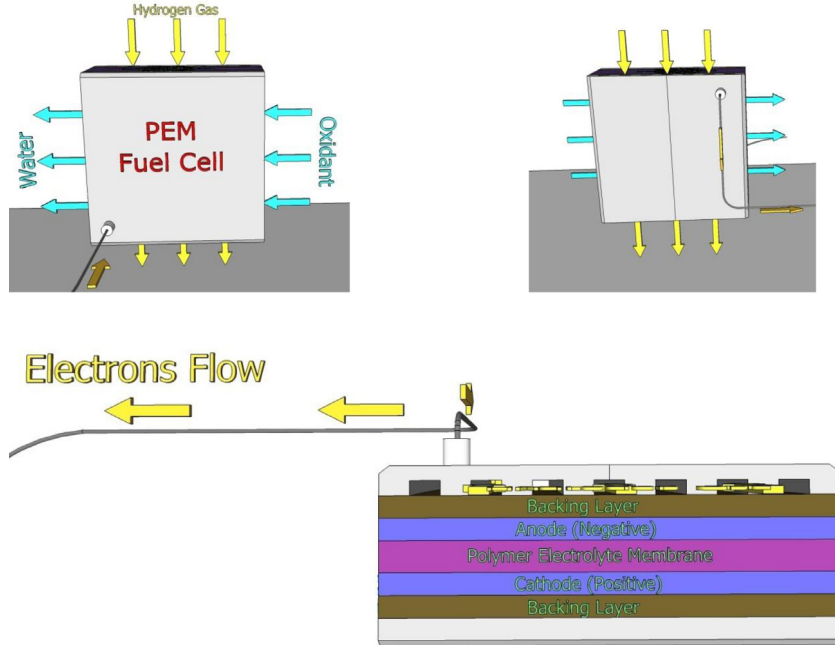


Fig. 1. The model of PEMFC stack.

catalysts to accelerate the electrochemical reaction. Fig. 1 shows the chemical reactions of the anode and cathode in the fuel cell.

The main purpose of the presented technique is to parameter identification of the PEMFCs using a new improved version of the Balanced Seagull Optimization Algorithm.

The cost function here is the error between achieved value of the designed model and the values obtained from the empirical values measured for the voltage data. Here, two empirical case studies are applied to show the efficiency of the presented modified BSOA through essential comparisons.

By considering entropy and irreversibility losses in a single PEMFC stack, the nominal output voltage is in the range 0.9 to 1.23 V. Therefore, to use the PEMFC stack in applications, a large number of them are combined with together in series.

Due to the activation voltage in PEMFC stacks, the current-voltage polarization curve falls down with a high slope, and then Ohmic resistive voltage drops make the curve to slowly falls down.

From (Corrêa et al., 2004; Aouali et al., 2017), the mathematical model of the total output voltage for PEMFC stack is formulated as follows:

$$V_o = N_{nc} (E_{oc} - E_{op} - E_O - E_{ops}) \quad (1)$$

where,  $N_{nc}$  represents the number for series connected cells of the PEMFC,  $E_{oc}$  is the open circuit potential condition per cell,  $E_{op}$  is the activation over-potential of the cells,  $E_O$  describes the Ohmic voltage drop in each cell, and  $E_{ops}$  is the over-potential saturation in cells.

To model the open circuit voltage of the PEMFC which is so-called reversible voltage, Nernst equation for this hydrogen/oxygen fuel cell has been utilized based on standard-state entropy change (Mann et al., 2000; Chen and Wang, 2019),

$$E_{oc} = 1.23 - 8.5 \times 10^{-4} (T_{PEM} - 298.15) + 4.31 \times 10^{-5} \times T_{PEM} \times \ln (P_{H_2} \sqrt{P_{O_2}}) \quad (2)$$

where,

$$P_{O_2} = R_{hc} \times P_{H_2O} \left[ \frac{1}{\frac{R_{hc} \times P_{H_2O}}{P_c} \times e^{\frac{1.635 I_{PEM} / A}{T^{1.334} I_{PEM}}} - 1} \right] \quad (3)$$

$$P_{H_2} = \frac{R_{ha} \times P_{H_2O}}{2} \left[ \frac{1}{\frac{R_{ha} \times P_{H_2O}}{P_a} \times e^{\frac{1.635 I_{PEM} / A}{T^{1.334} I_{PEM}}} - 1} \right] \quad (4)$$

$$\log_{10} (P_{H_2O}) = 2.95 \times 10^{-2} T_c - 9.18 \times 10^{-5} T_c^2 + 1.4 \times 10^{-7} T_c^3 - 2.18 \quad (5)$$

$$T_c = T_{PEM} - 273.15 \quad (6)$$

The reference temperature value during the operating variations is considered 25 °C (77 °F).

The mathematical model of the activation over-potential is formulated below:

$$E_{op} = - [\gamma_1 + \gamma_2 T_{PEM} + \gamma_3 T_{PEM} \ln (C_{O_2}) + \gamma_4 T_{PEM} \ln (I_{PEM})] \quad (7)$$

where,

$$\gamma_2 = 2.9 \times 10^{-3} + 2.1 \times 10^{-4} \ln (A) + 4.3 \times 10^{-5} \ln (C_{H_2}) \quad (8)$$

and  $C_{O_2}$  represents the oxygen saturation in the cathode's catalytic interface (mol/cm<sup>3</sup>) and is achieved as follows:

$$C_{O_2} = \frac{P_{O_2}}{5.1 \times 10^6} \times e^{\frac{498}{T_{PEM}}} \quad (9)$$

The hydrogen saturation in the cathode's catalytic interface (mol/cm<sup>3</sup>) is equal to:

$$C_{H_2} = \frac{P_{H_2}}{1.1 \times 10^6} \times e^{\frac{-77}{T_{PEM}}} \quad (10)$$

And the Ohmic voltage drop in the cells is formulated as follows:

$$E_O = I_{PEM} (R_m + R_c) \quad (11)$$

where,

$$R_m = \rho_m l S^{-1} \quad (12)$$

$$\rho_m = \frac{181.6 \left[ 0.062 \left( \frac{T_{PEM}}{303} \right)^2 \left( \frac{I_{PEM}}{S} \right)^{2.5} + 0.03 \left( \frac{I_{PEM}}{S} \right) + 1 \right]}{\left[ \lambda - 0.063 - 3 \left( \frac{I_{PEM}}{S} \right) \right] \times e^{\frac{T_{PEM} - 303}{I_{PEM}}}} \quad (13)$$

And, the over-potential saturation ( $E_{ops}$ ) in cells is as follows:

$$E_{ops} = -\beta \ln \left( 1 - \frac{J}{J_{max}} \right) \quad (14)$$

where,  $T_{PEM}$  represents the operating cell temperature (K),  $P_H$ ,  $P_{O_2}$ , and  $P_{H_2O}$  describe the partial pressure of the  $H_2$ ,  $O_2$  and  $H_2O$ , respectively.  $S$  describes the membrane surface ( $cm^2$ ),  $R_{hc}$  and  $R_{ha}$  are the vapor relative humidity at cathode and anode, respectively,  $P_a$  and  $P_c$  represent the inlet pressure for the anode and the cathode,  $I_{PEM}$  represents the operating current of the PEMFC,  $C_{H_2}$  and  $C_{O_2}$  are the hydrogen and oxygen ( $mol/cm^3$ ) saturation,  $R_m$  and  $R_c$  are the membrane resistance and the connections resistance,  $l$  is the thickness for the membrane,  $\beta_i$  describes the experimental coefficients,  $\lambda$  is tunable parameter,  $\rho_m$  is the membrane resistivity,  $\beta$  describes a parametric coefficient,  $J$  represents the real current density, and  $J_{max}$  is the maximum value of  $J$ .

By considering the aforementioned formulations, six parameters are need to be clarified which are not given by the manufacturer's datasheet.

In this condition, to achieve a satisfied model of PEMFCs, accurate values for the parameters are required. The six undetermined parameters here are  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$ ,  $\beta_4$ ,  $\beta$ ,  $R_{c,\lambda}$ .

In this study, we will try to achieve optimized values for the parameters by considering their constraints. A motivation of the algorithm is to use a new improved version of the recently introduced Balanced Seagull Optimization Algorithm to enhance the convergence speed on the algorithm.

### 3. Balanced seagull optimization algorithm (BSOA)

Seagulls (scientific name: *Larus minutus*) are among the birds of the coastal environments that have lived on Earth for about thirty million years and are present on almost all parts of the planet. Their wings are tall and their hind legs have evolved to move in water. However fish is the main food source of Seagulls, they also feed on insects, reptiles, amphibians, earthworms, and moles. In other words, seagulls are omnivorous. Seagulls are very smart birds that live for about 10 to 15 years (Trotter, 2019).

They live in large groups and have different voices to communicate with their band members. One of their strangest behaviors is that they are steal food from the grip of other birds, animals and even humans. They also use other techniques for hunting. For example, they attract fish with a bread crumbs or create a rain shower sound with their feet to drag. In general, seagulls live in swarm. Another capability is their specific behavior in migration.

Migration is the movement of seagulls to the south in the fall and northwards in the spring or moving from the ground to the heights or from coast to coast to survive from winter conditions and to achieve the most abundant food sources which provides enough easement (La Sorte et al., 2016). This mechanism is considered as a seasonal behavior of seagulls to move from one place to another to achieve a wide range of wealthy food sources to provide adequate energy (Avisé, 2017). This process is illustrated below:

- Migration starts by traveling a swarm of seagulls. To avoid from collisions, their initial positions are different from each other.
- They benefit from their swarm experience, i.e. they attempts to move in the direction of the best survival to achieve the lowest cost value.

Generally, seagulls attack to the migrating birds over the sea. This process is performed by the spiral natural shape behavior of them during attacking.

In the following, the model of seagulls for Seagull Optimization Algorithm (SOA) is discussed.

#### 3.1. Migration (exploration)

Migration behavior simulates the seagulls swarm moving toward the positions. To do so, three conditions should be satisfied:

(A) Collisions Avoidance: To avoid the collision among neighbor seagulls, a model is defined by additional variable  $A$  for updating the new position of the considered seagull (search agent):

$$\vec{P}_N = A \times \vec{P}_c(i), \quad (15)$$

$$i = 0, 1, 2, \dots, \text{Max}(i)$$

where,  $\vec{P}_N$  describes the position that prevent from colliding with the other search agent,  $\vec{P}_c(i)$  is the position of the candidate in the present iteration ( $i$ ), and  $A$  describe the motion behavior of the search agent in the search space and is modeled as follow:

$$A = f_c - \left( i \times \left( \frac{f_c}{\text{Max}(i)} \right) \right) \quad (16)$$

where,  $i$  describes the iteration,  $f_c$  represents the frequency control of variable  $A$  in the interval  $[0, f_c]$ .

(B) Using the other neighbor's experience: After collision avoidance form the neighbors, the candidates try to proceed into the direction of the best neighbor (best solution).

$$\vec{d}_e = B \times (\vec{P}_b(i) - \vec{P}_c(i)) \quad (17)$$

where,  $\vec{d}_e$  describe the candidate positions  $\vec{P}_c(i)$  toward the best fit candidate  $\vec{P}_b(i)$ . The coefficient  $B$  is a random value that makes trade-off between exploitation and exploration.  $B$  is achieved as follows:

$$B = 2 \times A^2 \times R \quad (18)$$

where,  $R$  describes a random value between 0 and 1.

(C) Move toward the best solution (search agent): finally, search agents update their position based on the best solution by the following formula:

$$\vec{D}_e = |\vec{P}_N + \vec{d}_e| \quad (19)$$

where,  $\vec{D}_e$  describes the difference between the seagulls and the best cost.

#### 3.2. Attacking (exploitation)

During migration, seagulls can continuously vary the attack's angle and speed. The position of them in can be kept in the air with the help of their weight and wings.

During the attack process, seagulls they move spiral in the air in  $x$ ,  $y$ , and  $z$  planes as follows:

$$\hat{x} = r \times \cos(t) \quad (20)$$

$$\hat{y} = r \times \sin(t) \quad (21)$$

$$\hat{z} = r \times t \quad (22)$$

where,  $t$  describes a random value in the interval 0 and  $2\pi$  and  $r$  declares the radius of the spiral turns and is formulated as follows:

$$r = \alpha \times e^{\beta t} \quad (23)$$

where,  $e$  describes the natural logarithm base, and  $\alpha$  and  $\beta$  represent the shape of the spiral. The new position of seagulls is updated by the following formula:

$$\vec{P}_c(i) = (\vec{D}_e \times \hat{x} \times \hat{y} \times \hat{z}) + \vec{P}_b(i) \quad (24)$$

where,  $\vec{P}_c(i)$  keeps the best results.

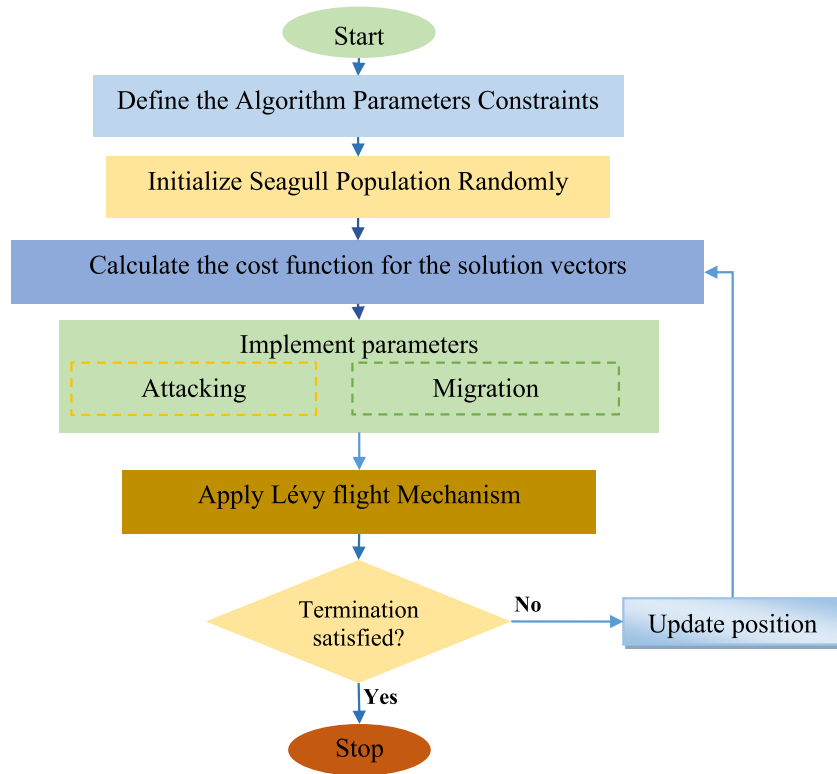


Fig. 2. The flowchart diagram of the proposed BSOA.

### 3.3. The balanced SOA

In this section, Lévy flight have been used for improving the proposed SOA. This mechanism is utilized to further relieve the premature convergence drawback, which are the core disadvantage of the SOA. Lévy flight (LF) provides a random walk mechanism to proper control of local search (Choi and Lee, 1998). This mechanism is represented as follows:

$$Le(w) \approx w^{-1-\tau} \quad (25)$$

$$w = \frac{A}{|B|^{1/\tau}} \quad (26)$$

$$\sigma^2 = \left\{ \frac{\Gamma(1+\tau)}{\tau \Gamma((1+\tau)/2)} \frac{\sin(\pi\tau/2)}{2^{(1+\tau)/2}} \right\}^{\frac{2}{\tau}} \quad (27)$$

where,  $0 < \tau \leq 2$ ,  $A \sim N(0, \sigma^2)$  and  $B \sim N(0, \sigma^2)$ ,  $\Gamma(\cdot)$  is Gamma function,  $w$  describes the step size,  $\tau$  represents Lévy index,  $A/B \sim N(0, \sigma^2)$  means that the samples generate from a Gaussian distribution in which mean is zero and variance is  $\sigma^2$ , respectively.

In this paper, based on (Li et al., 2018),  $\tau = 3/2$ .

Based on the aforementioned mechanism, the new improved part for update the solution of SOA is:

$$\bar{D}_{el} = \bar{D}_e + \left| \bar{P}_N + \bar{d}_e \right| \times Le(\delta) \quad (28)$$

where,  $\bar{D}_{el}$  represents the new position of search agent  $\bar{D}_e$ .

For guaranteeing the best solution candidates, fitter agents are kept:

$$\bar{D}_{el} = \begin{cases} \bar{D}_{el} & F(\bar{D}_{el}) > F(\bar{D}_e) \\ \bar{D}_e & \text{otherwise} \end{cases} \quad (29)$$

The flowchart of the presented BSOA is given in Fig. 2.

### 4. Validation of the proposed balanced SOA

For validation of the balanced SOA, four standard benchmarks have been studied. The results of the presented BSOA are compared with some different state of the art algorithms including particle swarm optimization algorithm (PSO) (Bansal, 2019), world cup optimization algorithm (WCO) (Razmjooy et al., 2016), genetic algorithm (GA) (Holland, 1992), fluid search optimization algorithm (FSO) (Dong and Wang, 2018), and the original seagull optimization algorithm (SOA) (Dhiman and Kumar, 2019). The simulations have been applied to a laptop with MATLAB R2017b platform with processor Intel® Core™ i7-4720 HQ CPU@2.60 GHz with 16 GB RAM. The equation and the constraints of the studied benchmark are illustrated in Table 1.

The results of the introduced benchmarks are given in Table 2. Here, the mean deviation (MD) and the standard deviation (SD) values of the compared methods are illustrated.

Simulation results from Table 2 show that the proposed BSOA gives promising results toward the other methods, especially the original SOA.

Fig. 3 shows the convergence curves for f1(A), f2(B), f3(C), and f4(D).

### 5. Objective function for PEMFC and its constraints

The PEMFC model parameters are optimized by the proposed BSOA to predict an optimal model which matches with the actual outputs of the system as much as possible.

By considering the aforementioned formulations and parameters, after determining the parameters ( $\beta_1, \beta_2, \beta_3, \beta_4, \beta, R_{c,\lambda}$ ), we can predict the output voltage for any definite input current. In this study, the sum of squared error (SSE) has been adopted to show the similarity of the output voltage for the model and the empirical result.

**Table 1**

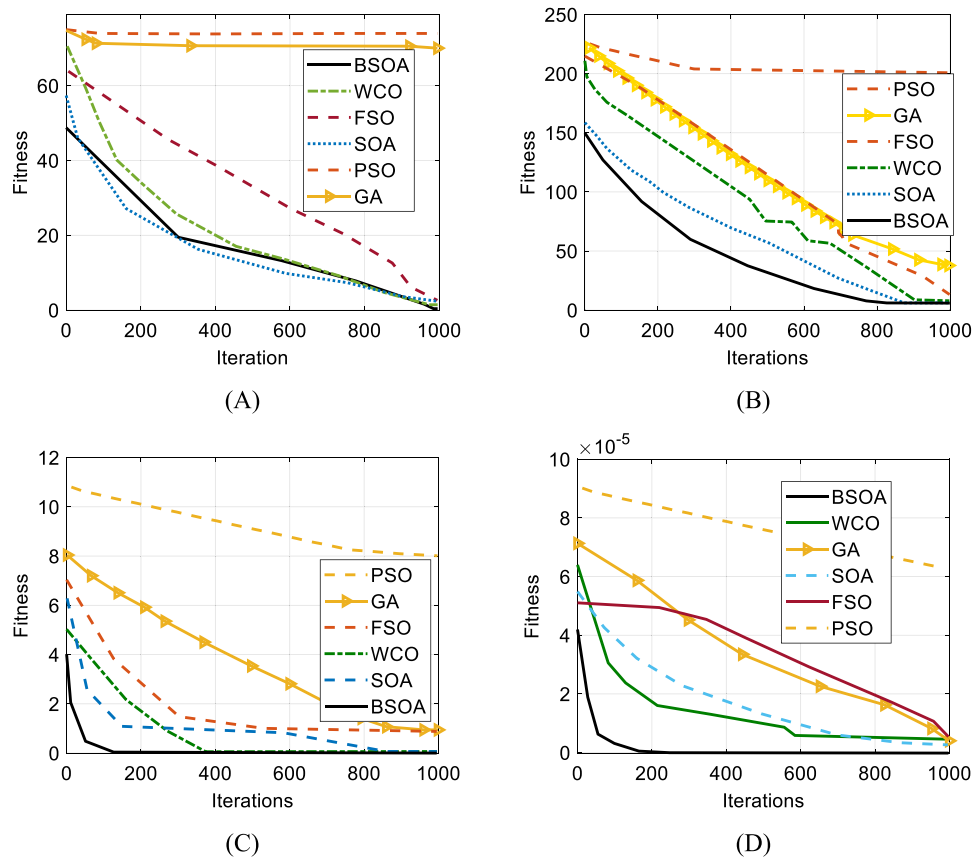
The utilized benchmarks for efficiency analysis.

| Benchmark  | Formula                                                                                                                                              | Constraints       | Dimension |
|------------|------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------|-----------|
| Rastrigin  | $f_1(x) = 10D + \sum_{i=1}^D (x_i^2 - 10 \cos(2\pi x_i))$                                                                                            | $[-512, 512]$     | 30–50     |
| Rosenbrock | $f_2(x) = \sum_{i=1}^{D-1} (100(x_i^2 - x_{i+1}) + (x_i - 1)^2)$                                                                                     | $[-2.045, 2.045]$ | 30–50     |
| Ackley     | $f_3(x) = -20 \exp \left( -0.2 \sqrt{\frac{1}{D} \sum_{i=1}^D x_i^2} \right) - \exp \left( \frac{1}{D} \sum_{i=1}^D \cos(2\pi x_i) \right) + 20 + e$ | $[-10, 10]$       | 30–50     |
| Sphere     | $f_4(x) = \sum_{i=1}^D x_i^2$                                                                                                                        | $[-512, 512]$     | 30–50     |

**Table 2**

The results of the efficiency analysis by considering 30-dimensions.

| Benchmark |    | BSOA | SOA (Dhiman and Kumar, 2019) | GA (Holland, 1992) | PSO (Bansal, 2019) | WCO (Razmjooy et al., 2016) | FSO (Dong and Wang, 2018) |
|-----------|----|------|------------------------------|--------------------|--------------------|-----------------------------|---------------------------|
| $f_1$     | MD | 0.00 | 2.11                         | 70.61              | 74.24              | 2.19                        | 3.42                      |
|           | SD | 0.00 | 3.26                         | 1.66               | 8.96               | 4.35                        | 3.27                      |
| $f_2$     | MD | 6.32 | 6.53                         | 35.41              | 200.1              | 13.16                       | 8.64                      |
|           | SD | 3.85 | 1.96                         | 27.15              | 59.00              | 4.62                        | 2.56                      |
| $f_3$     | MD | 0.00 | 1.63e−17                     | 3.19e−2            | 8.26               | 3.14e−3                     | 4.46e−16                  |
|           | SD | 0.00 | 0.00                         | 2.14e−2            | 1.19               | 1.12e−3                     | 0.00                      |
| $f_4$     | MD | 0.00 | 3.57e−13                     | 1.15e−4            | 8.27e−4            | 6.19e−9                     | 1.55e−12                  |
|           | SD | 0.00 | 8.97e−18                     | 3.14e−5            | 5.12e−4            | 3.28e−9                     | 5.37e−17                  |

**Fig. 3.** Convergence curves for  $f_1$ (A),  $f_2$ (B),  $f_3$ (C), and  $f_4$ (D).

Therefore, the cost function is assumed as follows:

$$F_{SSE} = \min (SSE) = \min \left\{ \sum_{i=1}^n (V_e(i) - V_o(i))^2 \right\} \quad (30)$$

where,  $n$  represents the number of measured points,  $i$  describes the number of iteration, and  $V_e$  and  $V_o$  are the empirical and the evaluated voltage stack of the PEMFC.

And the constraints for this function are declared in the following:

$$s.t. \begin{cases} \beta_{i,min} \leq \beta_i \leq \beta_{i,max} \\ \beta_{min} \leq \beta_i \leq \beta_{max} \\ R_{c,min} \leq R_c \leq R_{c,max} \\ \lambda_{min} \leq \lambda_i \leq \lambda_{max} \end{cases} \quad (31)$$

where,  $\beta_{i,min}$  and  $\beta_{i,max}$  represent the lower and the higher ranges for the empirical results,  $\beta_{min}$  and  $\beta_{max}$  describe the lower and the higher bounds for the parameters of the model,  $R_{c,min}$  and  $R_{c,max}$  are the lower and the higher ranges of the resistance for the cell connections, and  $\lambda_{min}$  and  $\lambda_{max}$  are lower and higher ranges of the water content.

## 6. Simulation results

To efficiency analysis of the proposed method, two practical case studies including BCS 500-W and NedStack PS6 have been adopted.

Some different optimized algorithms are also employed to fair efficiency analysis of the presented technique by assuming the same constraints from Priya et al. (2015), Ali et al. (2017) and El-Fergany (2017). The lower and the upper ranges for the studied six undetermined PEMFC parameters are given below:

$$\begin{cases} -1.2 \leq \beta_1 \leq -0.85 \\ 3.6e - 5 \leq \beta_3 \leq 9.8e - 5 \\ -2.6e - 4 \leq \beta_4 \leq -9.54e - 5 \\ 1.4e - 2 \leq \beta \leq 0.5 \\ 0.1 \leq R_c \leq 0.8 \\ 13 \leq \lambda_i \leq 23 \end{cases}$$

The relative humidity of vapors for both anode and cathode are assumed 1.00.

### 6.1. Case study 1: NedStack PS6

In this part, for evaluating efficiency of the algorithm, a NedStack PS6 of 6 kW rated power PEMFC system has been studied. For simulating this case study, its information is collected from El Monem et al. (2014) and Technology (2019). The required parameters of the NedStack PS6 is given in Table 3. By using the proposed BSOA for determining the best solution for the six undetermined parameters of NedStack PS6 system along with computed  $\beta_2$ , the final optimal values for the identified PEMFC model are given to shows the minimum value for the SSE overall 50 independent runs. The simulation results and elapsed time of the proposed BSOA compared with Seeker optimization (SO) algorithm (Dai et al., 2011), grasshopper optimiser (GHO) (El-Fergany, 2017), Salp Swarm Optimizer (SSO) (El-Fergany, 2018), and standard seagull optimization algorithm (SOA) and the results are given in Tables 4 and 5.

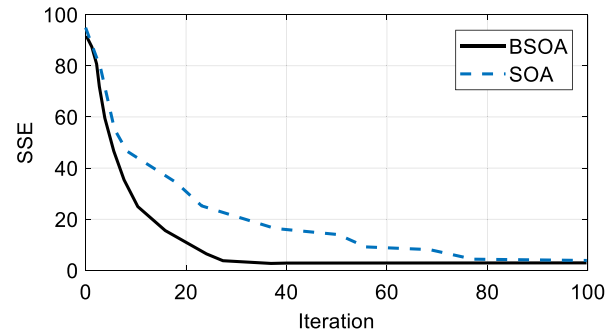
Fig. 4 shows the convergence diagram of the presented BSO algorithm on the NedS stack PS6 of 6 kW system.

Results show that the minimum SSE value after convergence is 2.18 which belong to the proposed method. It is clear that after 22 iterations, the SSE satisfied its minimum value that shows a high

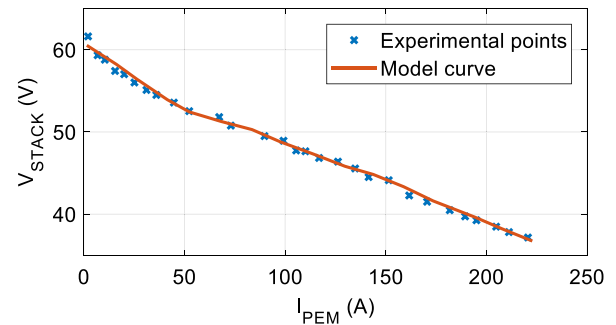
**Table 3**

Required parameters of the NedStack PS6.

| Parameter               | Value    | Unit            |
|-------------------------|----------|-----------------|
| N <sub>cells</sub>      | 65       | —               |
| A                       | 240      | cm <sup>2</sup> |
| L                       | 178      | μm              |
| T <sub>PEM</sub>        | 343      | K               |
| Output voltage changes  | [32, 60] | V               |
| Output current changes  | [0, 225] | A               |
| Supply pressure changes | [0.5, 5] | bar             |



**Fig. 4.** The simulation results of SSE convergence on the NedS stack based on BSOA and SOA.



**Fig. 5.** The current-voltage curve for the NedStack.

convergence characteristic than the standard SOA which needs 80 iterations.

Running time for the proposed method and the compared methods are illustrated in Table 5. Experimental results show that using the presented BSOA algorithm gives the best solution for the problem based on its improved convergence feature.

The current-voltage curve of the NedStack for the experimental curve and model curve based on BSOA is shown in Fig. 5.

Fig. 5 shows that the proposed BSOA gives satisfying precision to achieve the optimal fitting and by giving proper values for the undetermined parameters.

To better performance analysis of the algorithm, different conditions of partial pressures and the cell temperature are also studied. The current-voltage diagram for these variations is shown in Figs. 6 and 7.

Fig. 6 shows the partial pressure variations with 1/1 bar, 2/1.5 bar, and 3/2 bar. The results show that increasing the supply pressures of the P<sub>H2</sub>/P<sub>O2</sub> makes the stack output voltage increased.

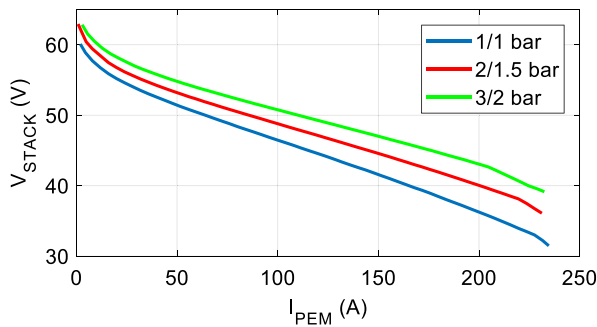
Fig. 7 shows the constant cell temperature variations with 323 K, 343 K, and 363 K. The results show that increasing temperature make the stack output voltage increased.

**Table 4**  
SSE validation for the NedStack PS6.

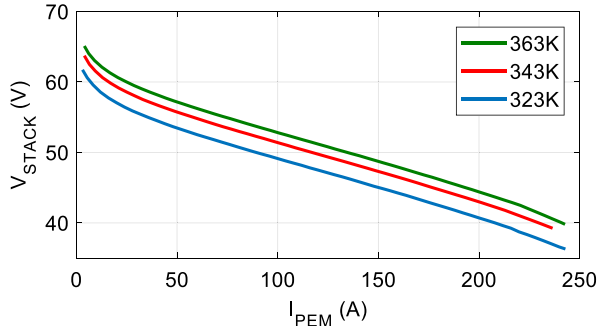
| Parameter  | Algorithm |          |                       |                        |                        |
|------------|-----------|----------|-----------------------|------------------------|------------------------|
|            | BSOA      | SOA      | SO (Dai et al., 2011) | SSO (El-Fergany, 2018) | GHO (El-Fergany, 2017) |
| $\beta_1$  | −0.89     | −0.89    | 1.21                  | 1.13                   | −0.96                  |
| $\beta_2$  | 3.42e−3   | 3.45e−3  | 3.38e−3               | 3.46e−3                | 3.41e−3                |
| $\beta_3$  | 7.76e−5   | 7.52e−5  | 3.58e−5               | 4.59e−5                | 8.13e−5                |
| $\beta_4$  | −9.55e−5  | −9.49e−5 | −9.49e−5              | −9.62e−5               | −9.37e−5               |
| $\lambda$  | 13.00     | 13.14    | 13.10                 | 12.91                  | 13.00                  |
| $R_c$      | 0.10      | 0.09     | 0.14                  | 0.10                   | 0.10                   |
| $\beta$    | 0.05      | 0.40     | 0.04                  | 0.06                   | 0.05                   |
| <b>SSE</b> | 2.18      | 2.21     | 2.41                  | 2.23                   | 2.19                   |

**Table 5**  
Running time for the BSOA algorithm and the compared methods on the NedS stack.

| Algorithm        | BSOA | SOA  | SO (Dai et al., 2011) | SSO (El-Fergany, 2018) | GHO (El-Fergany, 2017) |
|------------------|------|------|-----------------------|------------------------|------------------------|
| Elapsed time (s) | 3.95 | 4.19 | 6.20                  | 5.29                   | 7.82                   |



**Fig. 6.** The current-voltage curve characteristics of NedStack for pressure variations.



**Fig. 7.** The current-voltage curve characteristics of NedStack for varying temperatures.

## 6.2. Test case 2

This case study includes BCS PEMFC at a 500 W rated power with a 30 A maximum current. The model is made by American Company BCS Technologies (Co, 2001).

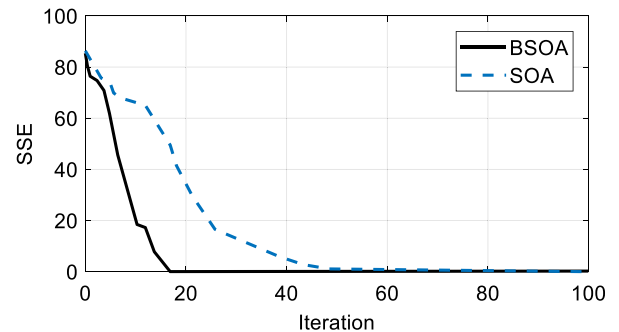
For simulating the BCS PEMFC stack, its information is collected from Corrêa et al. (2004). Table 3 illustrates the required parameters of the NedStack PS6 (see Table 6).

The simulation results and the running time of the proposed BSOA compared with Seeker optimization (SO) algorithm (Dai et al., 2011), grasshopper optimiser (GHO) (El-Fergany, 2017), Salp Swarm Optimizer (SSO) (El-Fergany, 2018), and standard seagull optimization algorithm (SOA) and the results are given in Tables 7 and 8.

Table 7 illustrates the simulation results of the optimal value selection for the voltage stack-based parameters based on the

**Table 6**  
Required parameters of the NedStack PS6.

| Parameter                           | Value    | Unit            |
|-------------------------------------|----------|-----------------|
| $N_{cells}$                         | 32       | —               |
| A                                   | 64       | cm <sup>2</sup> |
| L                                   | 178      | μm              |
| TPEM                                | 333      | K               |
| Partial pressures of H <sub>2</sub> | 1        | atm             |
| Partial pressures of O <sub>2</sub> | 0.21     | atm             |
| Output voltage changes              | [32, 60] | V               |
| Output current changes              | [0, 225] | A               |
| Supply pressure changes             | [0.5, 5] | bar             |



**Fig. 8.** The simulation results of SSE convergence on the BCS stack based on BSOA and SOA.

proposed BSOA compared with other methods on BCS PEMFC model for 100 independent runs.

From Table 7, it is obvious that show utilizing the presented BSOA gives better efficiency with minor SSE value toward the others in 100 independent runs.

Fig. 8 shows the SSE convergence diagram of the proposed BSOA on the BCS PEMFC. From figure, it is observed that, like the earlier case study, the proposed method gives the minimum SSE value.

Fig. 8 shows the high speed of the proposed algorithm into the minimum SSE after 18 iterations.

Simulations results declare that the proposed BSOA gives the best speed among the other methods. This is illustrated in Table 8.

The current-voltage diagram of the BCS PEMFC for the experimental curve and model curve based on the presented BSOA is shown in Fig. 9.

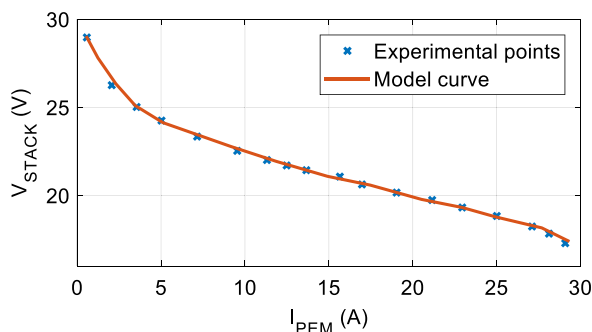
Like the previous case study, the results declare that a satisfied fitting between the empirical voltage model and the data obtained by the proposed BSOA and shows high precision to achieve the optimized values for the undetermined parameters.

**Table 7**  
SSE validation for the BCS PEMFC.

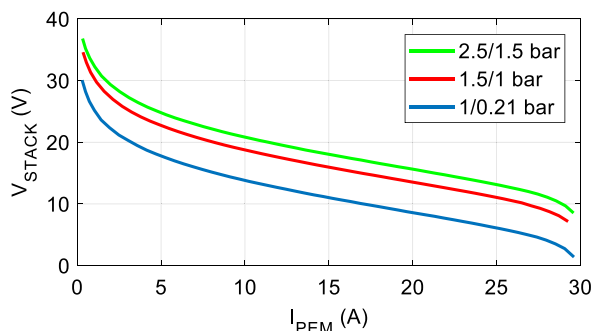
| Parameter  | Algorithm |          |                       |                        |                        |
|------------|-----------|----------|-----------------------|------------------------|------------------------|
|            | BSOA      | SOA      | SO (Dai et al., 2011) | SSO (El-Fergany, 2018) | GHO (El-Fergany, 2017) |
| $\beta_1$  | −0.81     | −0.75    | −1.02                 | −1.01                  | −0.79                  |
| $\beta_2$  | 5.17e−3   | 5.34e−3  | 5.14e−3               | 3.22e−3                | 4.12e−3                |
| $\beta_3$  | 8.79e−5   | 9.15e−5  | 7.96e−5               | 5.45e−5                | 8.37e−5                |
| $\beta_4$  | −2.39e−4  | −2.14e−4 | −2.17e−4              | −1.42e−4               | −2.12e−4               |
| $\lambda$  | 22.95     | 22.92    | 22.86                 | 20.17                  | 22.95                  |
| $R_c$      | 0.32      | 0.32     | 0.31                  | 0.75                   | 0.37                   |
| $\beta$    | 0.01      | 0.02     | 0.02                  | 0.01                   | 0.02                   |
| <b>SSE</b> | 0.01      | 0.02     | 0.02                  | 0.03                   | 0.02                   |

**Table 8**  
Running time for the BSOA algorithm and the compared methods on the BCS PEMFC.

| Algorithm        | BSSO | SSO  | SO (Dai et al., 2011) | SSO (El-Fergany, 2018) | GHO (El-Fergany, 2017) |
|------------------|------|------|-----------------------|------------------------|------------------------|
| Elapsed time (s) | 3.75 | 4.94 | 6.28                  | 5.13                   | 6.95                   |



**Fig. 9.** The current–voltage curve for the BCS stack.



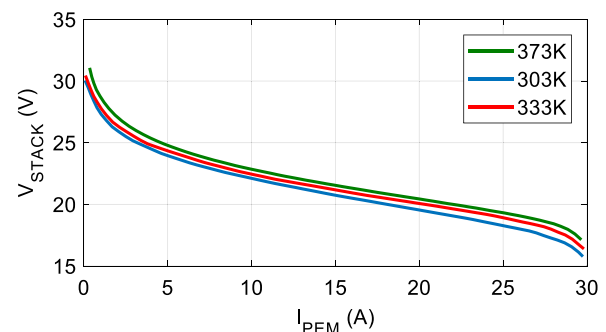
**Fig. 10.** The current–voltage diagram characteristics of BCS Stack for pressure variations.

In Figs. 10 and 11, the current–voltage diagram of the BCS PEMFC for different temperature and pressure values are plotted.

The variations of the partial pressure values for 2.5/1.5 bar, 1.5/1 bar, and 1/0.21 bar are shown in Fig. 10. It is obvious that increasing the supply pressures of the  $P_{H_2}/P_{O_2}$ , enhances the output voltage of the stack.

Fig. 10 shows the constant cell temperatures variations with for 373 K, 333 K, and 303 K in which increasing the temperature value, enhances the stack output voltage.

The results for both case studies give better performance for the proposed balanced SOA method compared with the other analyzed optimization algorithm in terms of both precision and convergence speed. Therefore, the results prove that using the proposed method is a promising method for parameter identification of the PEMFC with different conditions.



**Fig. 11.** The current–voltage diagram characteristics of BCS Stack for varying temperatures.

## 7. Conclusions

This study presents a new improved bio-inspired method for solving the nonlinear modeling problem of the PEMFCs identification problem. The method uses bio-inspired technique to guarantee the optimal values for modeling the complex nonlinear PEMFC systems. Here, a balanced version of the seagull optimization algorithm is presented. The BSOA algorithm uses Lévy flight mechanism that makes the standard seagull optimization algorithm to get better convergence. The BSOA was analyzed based on two empirical PEMFC types in comparison with some different optimization algorithms. Simulation results show that the proposed technique gives dynamic behavior of PEMFC output current/voltage properly and has effective performance.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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