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## Dynamic Competition in Negotiated Price Markets

by Jason Allen ${ }^{1}$ and Shaoteng Li ${ }^{2}$

${ }^{1}$ Economic and Financial Research Department Bank of Canada, Ottawa, Ontario, Canada K1A 0G9 jallen@bankofcanada.ca

²Queen's University, Kingston, Ontario, Canada K7L 3N6
lis@econ.queensu.ca


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## Abstract

This paper develops a framework for investigating dynamic competition in markets where price is negotiated between an individual customer and multiple firms repeatedly. Using contractlevel data for the Canadian mortgage market, we provide evidence of an "invest-then-harvest" pricing pattern: lenders offer relatively low interest rates to attract new borrowers and poach rivals' existing customers, and then at renewal charge interest rates which can be higher than what may be available through other lenders in the marketplace. We build a dynamic model of price negotiation with search and switching frictions to capture key market features. We estimate the model and use it to investigate (i) the effects of dynamic competition on borrowers' and banks' payoffs, (ii) the implications of dynamic versus static settings for mergerstudies, and (iii) the impacts from recent Canadian macroprudential policies.

Topics: Financial institutions; Financial services; Market structure and pricing
JEL codes: L2, D4, G21

## 1 Introduction

This paper develops a framework for investigating dynamic competition in markets where prices are negotiated between an individual customer and multiple firms repeatedly. Examples include mortgage markets (Woodward and Hall (2012) and Allen et al. (2019)), auto insurance markets (Honka (2014)), health insurance markets (Dafny (2010)), and many business-to-business transactions (Salz (2017) and Marshall (2019)). Customers in these markets normally face non-trivial costs of searching for price quotes and switching providers.

Search frictions are especially relevant in negotiated-price markets. Unlike in postedprice markets, where product comparison websites might be available, each price quote entails costly search and negotiation. In addition, repeated interactions over time induce switching costs. ${ }^{1}$ Both search and switching costs lead to a form of lock-in that places the incumbent firm in a stronger bargaining position than rival firms and thereby increases its market power. The additional rents that accrue to an incumbent firm, however, mean that all firms compete more aggressively ex ante to build their customer base. In the presence of switching costs, we expect to observe dynamic pricing patterns: firms using relatively low prices to attract new customers and poach those of their rivals, and then charging higher prices once these customers are locked in. In spite of the fact that firms in negotiated-price markets essentially solve dynamic optimization problems to trade off between current profits and future incumbency advantages, we are unaware of any quantitative study taking this salient feature into account.

In this paper, we focus on one negotiated-price market: the Canadian mortgage market. In Canada, a typical newly originated mortgage amortizes in 25 years. Lenders, however, do not offer long-term contracts. The majority of home buyers take out 5 -year fixed-rate mortgages (FRM). Hence, every five years borrowers are forced to renew their mortgage with either the current provider or a rival lender; a new interest rate must be negotiated for the outstanding balance. We take advantage of this deterministic timing for renegotiation to gain insight into the dynamic pricing game played by lenders.

Given our emphasis on dynamic pricing, we require information on mortgage contracts both at origination and at renewal. Importantly, we need to observe the identity of borrowers' current lenders and previous providers and hence borrowers' switching activities. We therefore use anonymized credit bureau data. TransUnion, a national credit bureau,

[^2]provides the Bank of Canada monthly updates on the credit portfolios of the population of Canadian households, including contract-level information on mortgages. Starting in 2012, we observe a borrower's mortgage payment history and use it, along with balance changes, to back out the contract rate. Additionally, we observe borrower characteristics (age, credit score, location), contract information (original loan size, outstanding balance, funding date), and, crucially, the lender's identity and the borrower's switching behavior. Finally, for a subset of borrowers, we are able to match the credit bureau data to administrative data, providing us with additional borrower and contract information.

Our descriptive analysis provides preliminary evidence of "invest-then-harvest" pricing behavior: borrowers who renew their mortgage with their incumbent bank on average pay interest rates 6.1 basis points (bps) higher than new borrowers, and borrowers who switch banks at renewal on average pay 10.2 bps lower than those who stay. Consider an average newly originated mortgage of $\$ 264,000$ that amortizes in 25 years. The differences in rates imply differences in total interest costs over 5 years of $\$ 746$ to $\$ 1,243$. In spite of these potential savings, only $12.1 \%$ of renewers switch mortgage providers.

In order to rationalize the observed pricing pattern, we build a dynamic model of price negotiation with search and switching costs. We follow Allen et al. (2019) but extend their model in an important way. Specifically, we incorporate and emphasize the intertemporal trade-off lenders face when pricing mortgage contracts. This trade-off influences the interpretation of equilibrium outcomes and has meaningful policy implications. For example, in a dynamic framework, switching frictions need not necessarily hurt consumers. Forward-looking lenders compete more aggressively for borrowers, and this competition might result in lower prices. Our focus on pricing dynamics also highlights the importance of treating new and repeated customers separately in policy evaluations, because lenders price these two types of borrowers asymmetrically.

We model the mortgage financing process over the entire amortization period as a finite period game. The first period is mortgage origination, and the subsequent periods are renewals. The game ends when the mortgage is fully paid. Each period, the borrower (new or renewer) is attached to a home bank. ${ }^{2}$ The home bank moves first to offer the borrower a free initial quote. Depending on the realization of a per-bank search cost, and the expected gain from search, the borrower either accepts the home-bank offer or chooses how many quotes to gather. If the borrower decides to search, she obtains quotes from an endogenously chosen set of lenders and uses the best offer in hand to negotiate for even

[^3]better quotes. Lenders face heterogeneous realizations of lending costs. They are willing to bid lower than the lending cost as long as the quotes generate positive expected profits over the life of the mortgage. Importantly, lenders are forward-looking and understand the future value of being a home bank, which includes (1) the first-mover advantage of making an initial offer that might retain borrowers drawing high search costs, (2) the opportunity of making additional offers given that borrowers always include their home bank in their choice set, and (3) the switching costs that could prevent borrowers from switching even if they receive slightly better quotes from rival lenders.

Our model describes the data-generating process in a tractable way. The model primitives are (1) the borrowers' search cost distribution and switching cost, and (2) the banks' lending cost distribution and discount factor. We present an identification argument based on a dataset consisting of borrowers' interest-cost distribution and switching activity. The crucial assumption required is that there exists some observable(s) influencing borrowers' switching costs, but not the other model primitives. ${ }^{3}$ In our empirical analysis, we estimate a parametric model using a cross-sectional sample of new borrowers and renewers to make use of observed heterogeneity across borrowers.

Overall, we find that banks' lending costs for the same borrower are not very dispersed. Borrowers, on the other hand, have non-trivial search and switching costs. On average they face a per-bank search cost of $\$ 486$ (that is, $1.8 \%$ of the average interest cost) and obtain only 2.5 quotes, one of which is free from the home bank. For an average new borrower, the cost of switching away from a pre-mortgage relationship is $\$ 115$ (per $\$ 100 \mathrm{k}$ loan). The number is tripled for renewers; it is much more costly to switch away from a mortgage relationship than a relationship, for example, based on a credit card.

We use the model to conduct counterfactual analyses to investigate (1) the effects of search and switching frictions on borrowers' and banks' payoffs, (2) the implications of dynamic versus static settings for merger analysis, and (3) the impacts of recently adopted mortgage stress testing in Canada. The first two experiments highlight the importance of understanding lenders' dynamic pricing strategies. The static model overestimates the benefit of eliminating search and switching costs because it ignores changes in lenders' investment incentives and pricing dynamics. For the same reasons, static merger simulations overestimate merger impacts. ${ }^{4}$ The last experiment, which exogenously increases

[^4]switching costs, suggests that about $12 \%$ of new borrowers in our sample would fail the stress test if they were subject to it at renewal. For these unqualified borrowers, the stress test would substantially increase the home bank's market power and lead to a $10 \%$ increase in interest costs.

There is a large empirical literature investigating search frictions in markets where firms post prices. See, for example, Sorensen (2001) for prescription drugs, Hortaçsu and Syverson (2004) for mutual funds, and Hong and Shum (2006) for textbooks. A typical assumption is that firms have common costs in servicing every consumer. In a negotiatedprice market, however, the final price that a customer pays is individualized to reflect the heterogeneity in firm-specific servicing costs, which might be unobserved to researchers. The main challenge is therefore to disentangle the distribution of both servicing costs and search costs from the observed negotiated-price distribution.

There is also a large theoretical and empirical literature that focuses on switching costs in posted-price markets. See Klemperer (1995) and Farrell and Klemperer (2007) for an overview. ${ }^{5}$ Recent empirical studies include Shum (2004) for the breakfast-cereal market, Kim (2006) for cellular service, Dubé et al. (2009) for packaged foods, Shcherbakov (2016) for cable television, Handel (2013) for health insurance, Fleitasl (2016) for drug insurance, and Illanes (2017) for pension plans. In banking markets there is also extensive interest in switching costs. See, for example, Ausubel (1991) for credit cards, Ho (2015) for deposits, Kim et al. (2003) for bank loans, and Thiel (2018) for the Dutch mortgage market.

From the above list, Dubé et al. (2009) and Shcherbakov (2016) investigate switching costs in dynamic frameworks. The authors find that switching costs can lead to lower equilibrium prices. Consistent with their findings, in a counterfactual experiment, we show that new borrowers' interest costs are lower with than without switching costs. Therefore, policies aimed at promoting competition through reducing switching costs may not be effective. These papers, however, ignore search frictions and assume that consumers have perfect information about the prices available in the market. This assumption is reasonable in posted-price markets but does not fit into a negotiated-price market setting.

In our negotiated-price setting, we only observe the final contract price rather than all the quotes obtained by borrowers. Therefore, we need to explicitly model how the observed price distributions are generated and how they are affected by search and switching frictions. Our approach is to approximate the price negotiation process as an English pro-

[^5]curement auction, where lenders gradually lower their quotes to bid for a borrower. This setting captures, in a tractable way, the important feature that borrowers use the best offer in hand to extract better quotes, and lenders are willing to accept profitable counteroffers. The auction setting provides a clear interpretation of the final price, which is associated with the second order statistic of lenders' reservation values. Other studies applying auction-like models to approximate price negotiation include Woodward and Hall (2012), Rosenbaum (2013), Salz (2017), Beckert et al. (2018), Allen et al. (2019), Slattery (2019), and Cuesta and Sepulveda (2019).

In our model, firms' pricing strategies are not as complicated as in posted-price markets. When a firm posts a non-negotiable price, it applies to all potential consumers. Therefore, firms' pricing strategies depend crucially on their market shares: high-marketshare firms have more incentive to raise prices and harvest consumers, while low-marketshare firms tend to compete aggressively to invest in their customer base. Forward-looking firms take into account the effect of current prices on consumers' choices, future market shares, and future profits. They solve dynamic optimization problems under rational beliefs about the market share transition. In negotiated-price markets, prices are individualized. Firms' pricing strategies for different borrowers are independent, and hence are not constrained by their market shares.

There is now a growing literature that investigates both search and switching frictions in a unified framework. Wilson (2012), for example, points out that models taking into account only one type of market friction can generate biased estimates when both frictions exist. Honka (2014) quantifies search and switching costs in the US auto insurance markets using information on consumers' consideration sets, purchase prices, and switching behavior. Both Wilson (2012) and Honka (2014) assume a static framework, where firms' pricing does not take into account the future value of locked-in customers. Braido and Ledo (2018) build a parsimonious model of dynamic pricing competition in the Brazilian auto insurance brokerage market to rationalize the co-existence of zero and positive fees. Insurance brokers do not observe if consumers search for quotes, therefore, even though prices are individualized, the brokers play a mixed strategy in equilibrium to balance the trade-off between a low fee to strike a deal and a high fee to exploit the potentially locked-in customer. This does not fit into the setting of negotiated-price markets, where the key feature is that customers use current best quotes to negotiate for better offers.

The paper is organized as follows. Section 2 introduces institutional details and the data. Section 3 describes the model primitives and characterizes the equilibrium. Section 4 discusses non-parametric identification of the model. Section 5 specifies our empirical
framework. Section 6 presents the estimation results. Section 7 presents our counterfactual experiments. Section 8 concludes.

## 2 Institutional Details and Data

### 2.1 Institutional Details

The Canadian mortgage market is dominated by a small number of large players, including six national banks (Bank of Montreal, Bank of Nova Scotia, Canadian Imperial Bank of Commerce, National Bank of Canada, Royal Bank of Canada, and Toronto-Dominion Bank), one regional cooperative network (Desjardins in Quebec), one provincially owned financial institution (ATB Financial in Alberta), two other banks operating primarily in specific provinces (Laurentian Bank of Canada and HSBC Bank Canada), and two mortgage finance companies operating nationally (MCAP and First National). Together these lenders originate more than $85 \%$ of the residential mortgages in Canada. For brevity, we denote these major lenders as the "big 12". Other lenders in the Canadian mortgage market include local credit unions and private lenders. In addition, independent mortgage brokers can serve as intermediaries between borrowers and lenders. ${ }^{6}$

Posted mortgage rates are set weekly and nationally. Lenders post their mortgage rates across different maturities, and these are common across all local markets. Website aggregators then advertise these rates along with a host of other lender rates and might even provide advice. The Bank of Canada uses these rates to construct a benchmark rate which is used as part of the government's macroprudential policy toolkit. Nonbroker mortgage applications are done at the branch level and not electronically. Broker transactions often happen over the phone. Less than $1 \%$ of borrowers pay the standard posted rate. ${ }^{7}$ Normally, borrowers visit a few banks in a local market and negotiate with branch managers to receive discounts off the posted rate. Banks compete with rival banks in prices, but branches of the same bank do not compete against each other. Finally, the majority of insured mortgages (i.e. those mortgages with loan-to-value ratios greater than $80 \%$ at origination) are securitized and the collection of securitized mortgages (MBS) is held on the balance sheet as high-quality liquid assets for regulatory purposes.

[^6]In Canada, a typical newly originated mortgage amortizes in 25 years. The loan term, however, is much shorter, between 1 and 10 years, during which time the interest rate is either fixed or variable. The majority of home buyers take out 5 -year FRMs. Hence, every 5 years they are forced to renew their mortgage and obtain a new interest rate for the outstanding balance. ${ }^{8}$ Mortgage markets in many other countries (e.g. Netherlands, Switzerland, UK) are similar: borrowers periodically renew short-term FRM over a much longer amortization period. This feature makes studying banks' pricing strategies substantially easier than the US market, where borrowers sign long-term contracts and have an option to refinance where it is advantageous to do so. ${ }^{9}$ Chen et al. (2018), for example, document strong counter-cyclical mortgage refinancing activity associated with equity extraction. The refinancing decision is therefore endogenous. This substantially complicates the search and switch decision for borrowers as well as the pricing strategies for lenders. Mortgage renewal in Canada, however, is almost entirely exogenous and depends on the date of origination. We take advantage of the deterministic timing for repeated interactions to gain insight into the dynamic pricing strategies of lenders. ${ }^{10}$

How do renewals work in Canada? A household will typically sign a 5-year FRM. Near the end (typically 6 months prior) of the 5 -year contract, the incumbent lender sends the borrower a notice by mail about the upcoming renewal and offers a rate. ${ }^{11}$ If the borrower does not engage at this time, the lender sends a new letter at the 3-month mark, potentially with a new rate. It is often at this 3 -month mark that the lender and borrower start to negotiate, and the borrower may search for better offers from rival

[^7]banks. A clear advantage for the incumbent is that borrowers face non-trivial switching costs. ${ }^{12}$ In addition, unlike in posted-price markets, it is costly for borrowers to obtain quotes from rival banks. The home bank enjoys a first-mover advantage by offering an initial quote that might prevent the borrower from searching.

### 2.2 Data

Our main data set comes from TransUnion, one of two credit bureau companies operating in Canada, which collects information on credit products for the Canadian population. We focus on mortgages, but are also able to control for other debt, such as auto loans, lines of credit, demand loans, credit cards, student loans, and utilities. ${ }^{13}$ All major lenders report their borrowers' monthly payment records from January 2012 to July 2019. The dataset contains anonymized information on borrowers' characteristics: age, credit score, non-mortgage debt obligations, monthly payments, and physical address up to the forward sortation area (FSA). ${ }^{14}$ We also observe mortgage contract information, including the lender's identity, loan amount, term, amortization, funding date, monthly payment, outstanding balance, and an indicator for mortgage insurance. ${ }^{15}$ We use the monthly payment and changes in outstanding balance to calculate the interest rate and effective amortization. We use the interest rate pattern to identify the loan term whenever it is missing. We also calculate the interest costs over the loan term as our price measure. In addition, we use the lender's identity to identify switching behavior. We define the new borrowers' home banks by the pre-mortgage relationships built on other credit products. ${ }^{16}$

In addition to monthly credit bureau data, we access a second anonymized contractlevel administrative dataset, which offers information on mortgages provided by federally

[^8]regulated lenders. We match individuals at the loan-account level. This dataset is similar to that used in Allen et al. (2019). ${ }^{17}$ Although it lacks information on a borrower's previous lender, it allows us to complement the credit bureau data by including information on the borrower's income, broker usage, house value, loan-to-value ratio, and total debt-servicing ratio. We also supplement our data set with 2016 FSA-level demographic information such as population and median income level. Finally, we include the quarterly FSA-level house price index and housing transaction number generated by Teranet.

We obtain a cross-sectional sample of new borrowers and first-time renewers, who negotiated their interest rates within the period from January 2014 to December 2017. We then further restrict our sample to keep only insured mortgages that were negotiated individually (without a broker) and with 5 -year fixed-rate terms. ${ }^{18}$ We drop borrowers who have moved, taken out equity, or opened multiple mortgages. Finally, we only keep mortgages provided by four specific big banks that record the most accurate information.

We define a local market at the FSA level. More formally, we follow Allen et al. (2019) and assume borrowers can search for quotes from any of the big 12 lenders that has a branch located within 10 km of the centroid of their FSAs. We treat the two mortgage finance companies as a single option and assume it is available across all markets. Indeed, they have originated mortgages in more than $90 \%$ of FSAs.

### 2.3 Market Features

In this subsection, we present some descriptive evidence that motivates the development of our structural model. In Section 3, we build a model that captures and explains these salient market features. Table 1 presents the summary statistics of borrowers' characteristics and contract information. Table 2 reports the regression results that describe the correlations between negotiated contract rates and borrower characteristics. We present five key features that characterize the pricing pattern and shopping behavior in the Canadian mortgage market. Similar features are shared by most negotiated-price markets.

[^9]Table 1: Summary Statistics

|  | mean | sd |  | p25 |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
|  | Panel A: New Borrowers |  |  |  |  |
| Interest rate | 2.75 | 0.29 | 2.59 | 2.69 | 2.90 |
| Outstanding amount | 253.72 | 123.36 | 164.95 | 234.27 | 322.15 |
| Origination amount | 253.72 | 123.36 | 164.95 | 234.27 | 322.15 |
| Credit score | 754.01 | 50.48 | 721.00 | 757.00 | 792.00 |
| Age | 36.15 | 10.66 | 28.00 | 33.00 | 42.00 |
| Bond rate | 1.04 | 0.37 | 0.73 | 0.92 | 1.44 |
| Amortization | 24.08 | 1.86 | 22.36 | 24.95 | 25.00 |
| No. of lenders | 6.58 | 1.85 | 6.00 | 7.00 | 8.00 |
| FSA income | 77.34 | 22.24 | 61.76 | 73.10 | 89.73 |
| FSA house price | 380.33 | 162.62 | 262.11 | 336.36 | 479.55 |
| FSA transaction no. | 7557.42 | 15168.21 | 476.00 | 1200.00 | 3196.00 |


|  | Panel B: Renewers |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Interest rate | 2.81 | 0.36 | 2.60 | 2.70 | 2.99 |
| $\quad$ Loyal renewal | 2.82 | 0.36 | 2.60 | 2.74 | 2.99 |
| $\quad$ Switch renewal | 2.71 | 0.29 | 2.50 | 2.64 | 2.89 |
| Outstanding amount | 191.40 | 92.33 | 124.98 | 176.06 | 242.77 |
| Origination amount | 220.94 | 104.79 | 145.92 | 204.35 | 280.00 |
| Credit score | 781.20 | 76.59 | 734.00 | 794.00 | 842.00 |
| Age | 45.78 | 11.94 | 36.00 | 44.00 | 54.00 |
| Bond rate | 1.07 | 0.38 | 0.75 | 0.94 | 1.51 |
| Amortization | 21.19 | 5.24 | 17.39 | 20.29 | 24.96 |
| No. of lenders | 6.78 | 1.85 | 6.00 | 7.00 | 8.00 |
| FSA income | 77.74 | 22.59 | 61.63 | 73.52 | 90.68 |
| FSA house price | 396.73 | 189.39 | 263.90 | 342.91 | 489.43 |
| FSA transaction no. | 5895.41 | 13325.42 | 429.50 | 1029.00 | 2617.00 |

Note: The sample includes 16,711 mortgage contracts negotiated between 2014 and 2017: 8,131 are new borrowers and 8,580 are renewers (including 1,037 switchers). Units for outstanding amount, origination amount, FSA income, and house prices are $\$ 1,000$; units for interest rate and bond rate are percentage points, and units for amortization and age are years. Outstanding amount refers to the current outstanding balance of the mortgage contract, while origination amount is the initial loan amount for a newly issued mortgage. Number of lenders is within 10 km of the borrower's FSA centroid. FSA income is the median income level of the borrower's FSA recorded in the 2016 Census. FSA house price and FSA transaction number are, respectively, the average house price and the total number of housing transactions within the borrower's FSA in the quarter of origination/renewal and are taken from Teranet.

Feature 1: Mortgage rates are determined via negotiation. Most lenders post a common interest rate for all potential borrowers and then offer individual-level discounts. Less than $1 \%$ of borrowers pay the posted price.

## Feature 2: Borrowers shop around for lower interest rates, taking into account

 the cost of obtaining quotes and switching. Mortgage products offered by different lenders are fairly homogeneous. According to the Canada Mortgage and Housing Corporation (CMHC)'s Mortgage Consumer Survey in 2018, the top reason for a borrower to choose a specific lender is a better interest rate. Other than rates, borrowers most value convenience and trust in existing relationships.Feature 3: Most borrowers only search for quotes from a subset of lenders available in their local markets. Survey evidence from the Canadian Association of Accredited Mortgage Professionals in 2009 shows that about $95 \%$ of borrowers obtain no more than 4 quotes. The 2018 Mortgage Consumer Survey conducted by CMHC finds that borrowers on average contact 2.8 lenders. The average number of quotes reported in Allen et al. (2014b) was under 3. Table 1, however, suggests that the average number of available lenders in local markets is close to $7 .{ }^{19}$

Table 2: Regression Results

|  | Interest Rate (bps) |  |
| :--- | :---: | :---: |
| Credit score | $-0.0431^{* * *}$ | $(0.00385)$ |
| Outstanding amount | $-0.0276^{* * *}$ | $(0.00218)$ |
| Bond rate | $0.421^{* * *}$ | $(0.0117)$ |
| Amortization | $0.247^{* * *}$ | $(0.0627)$ |
| FSA income | -0.0121 | $(0.0114)$ |
| Age | $0.0733^{* * *}$ | $(0.0189)$ |
| House price (log) | $-2.684^{* * *}$ | $(0.768)$ |
| Transaction no. $(\mathrm{log})$ | $-0.948^{* * *}$ | $(0.215)$ |
| No. of lenders | $-0.777^{* * *}$ | $(0.154)$ |
| Loyal renewal | $6.139^{* * *}$ | $(0.585)$ |
| Switch renewal | $-4.026^{* * *}$ | $(0.830)$ |

> Note: This table presents results from an OLS regression of mortgage rates (in basis points) on observable transaction characteristics. We include year, region, and lender fixed effects. There are 16,711 observations. The $R^{2}$ is 0.395 . Units for outstanding amount and FSA income are $\$ 1,000$, and units for interest rate and bond rate are basis points. Number of lenders is within 10 km of the borrower's home. Region is defined as the first digit of the postal code. Robust standard errors are reported in parentheses. ${ }^{*} p<0.05,{ }^{* *} p<0.01,{ }^{* * *} p<0.001$.

[^10]Feature 4: Renewers rarely switch even though switchers tend to have better interest rates. Table 1 shows that only $12.1 \%$ of renewers switch banks. This is despite the fact that switchers, on average, receive a discount relative to non-switchers of 11 bps .

## Feature 5: An "Invest-and-harvest" pricing pattern. Borrowers renewing with

 their home bank tend to pay higher interest rates than new borrowers. This can be seen from the summary statistics in Table 1 as well as the regression estimates in Table 2.
## 3 Model

Consider a borrower $i$ searching for a mortgage contract with interest rate fixed for $m$ years, and amortizing in $T \times m$ years. We model this as a $T$-period game. Each period can be further broken down into two stages: an initial quote stage where the borrower receives a quote from her home bank and decides to accept or search for more quotes, and a negotiation stage, where the borrower negotiates price with multiple lenders in her choice set if she rejects the home-bank offer. Since prices are individualized, we treat each borrower as an independent market. For brevity, we omit the borrower's index $i$ and add it back in the next section to emphasize borrower heterogeneity.

### 3.1 Preferences and Costs

Borrower Preferences. In each period $t=1,2, \cdots, T$, the borrower is attached to a home bank $h^{t}$. In $t=1$, the home bank is the lender that had provided the borrower with some other product prior to the mortgage. In $t>1$, the home bank is just the lender providing the mortgage in the previous period.

At the beginning of every period, the home bank moves first by offering the borrower a free initial quote $p_{0}^{t}$. The borrower can either accept $p_{0}^{t}$ or reject the offer and search for more quotes by paying a per-bank search cost $\kappa^{t}$ drawn from a distribution $H(\cdot)$. There are $N^{t}$ lenders available in the borrower's local market. If the borrower rejects the home-bank offer, this initial offer cannot be recalled. ${ }^{20}$ She will choose a subset of

[^11]available lenders as her choice set $n^{t} \subseteq N^{t},{ }^{21}$ maximizing her expected net benefit from searching, in which the home bank is always included. The borrower then negotiates with all $n^{t}$ lenders and commits to take the best offer. Given the quotes, the borrower solves a discrete-choice problem and chooses a lender that maximizes her expected present value from financing a mortgage:
\[

$$
\begin{equation*}
\max _{j \in n^{t}} v_{j}^{t}-p_{j}^{t}+\rho U_{j}^{t+1} \tag{1}
\end{equation*}
$$

\]

where $v_{j}^{t}$ is the borrower's valuation for a mortgage provided by lender $j, p_{j}^{t}$ is the interest payment required by lender $j, \rho$ denotes the borrower's discount factor, and $U_{j}^{t+1}$ denotes the continuation value of being attached to lender $j$.

Since products are homogeneous, the borrower has no special preference for any lender other than a utility loss from switching:

$$
v_{j}^{t}= \begin{cases}\bar{v}^{t}, & j=h^{t} \\ \bar{v}^{t}-\lambda^{t}, & \mathrm{o} / \mathrm{w} .\end{cases}
$$

We assume $\bar{v}^{t}$ is finite but high enough that the borrower always demands a mortgage. There is no outside option.
Lending Costs. The lending cost measures the direct and indirect cost of providing a mortgage (funding costs, default and prepayment risks, overhead expenses, etc.), net of the expected future profits that might be derived from a borrower. In the negotiation stage, the lending cost for bank $j$ is

$$
c_{j}^{t}=c^{t}+\omega_{j}^{t} .
$$

We assume all lenders face a common funding cost, $c^{t}$, drawn from a distribution $F(\cdot)$. This common component captures lenders' consensus estimates regarding the borrower's profitability. For example, a part of it can be the cost of retail deposits or the borrower's prepayment risk. Randomness in the common cost absorbs heterogeneity across borrowers that is observable to lenders but not to the econometrician. We also allow each lender to have a different match value with the borrower, denoted as the idiosyncratic cost component $\omega_{j}^{t}$, which is drawn i.i.d. from a mean-zero distribution $G(\cdot)$.

In the initial-quote stage, we assume that the lending cost from the home bank is just the common cost component, $c^{t}$. The motivation for this assumption is that borrowers

[^12]only draw an idiosyncratic match value when they enter negotiations with a loan officer. ${ }^{22}$

### 3.2 Timing and Information

In each period $t$, we divide the price-generating process into two stages. In the initial quote stage, the home bank offers a free quote. The borrower can accept the offer (end of the game in period $t$ ) or search for more quotes. Given the number of available banks in the local market, $N^{t}$, the borrower decides the number of banks to be included in the choice set, $n^{t}$, and commits to take the best offer. At this point, the borrower has met with all lenders within the choice set and is ready to step into the negotiation stage. In this stage, the negotiation process is approximated as an English auction: the borrower obtains quotes from all lenders in the choice set and uses the best offer in hand to negotiate for even better quotes. This process goes on until the borrower obtains an offer that no other lender is willing to beat. The winning lender provides the highest expected utility and becomes the borrower's home bank in the next period. The auction setting provides a clear interpretation of the final price, which is associated with the second order statistic of lenders' reservation values.

The borrower and lenders learn about borrower preferences and lending costs in sequence. In stage 1, the home bank, $h^{t}$, notices that the borrower is looking for a new mortgage $(t=1)$ or renewing her remaining balance $(t>1)$. The state variables commonly observed by both parties are the home-bank identity $h^{t}$, the number of locally available lenders $N^{t}$, the common cost realization $c^{t} \sim F(\cdot)$, and the switching cost $\lambda^{t}$. The search cost distribution $H(\cdot)$ and the idiosyncratic cost distribution $G(\cdot)$ are also common knowledge, but the search cost realization $\kappa^{t}$ is the borrower's private information. For simplicity, assume $N^{t}$ and $\lambda^{t}$ do not vary over time. The commonly observed state vector in period $t$ is just $\left(h^{t}, N, c^{t}, \lambda\right)$. Given the state $\left(h^{t}, N, c^{t}, \lambda, \kappa^{t}\right)$ in the initial quote stage, the home bank chooses a price $p_{0}^{t}$, and the borrower decides $n^{t}$.

In the negotiation stage, each lender in the choice set draws an idiosyncratic cost shock $\omega_{j}^{t}$ i.i.d. from $G(\cdot)$. The distribution is commonly known, but the cost realization is private information. Denote the full state vector in period $t$ as $s^{t}=\left(h^{t}, N, c^{t}, \lambda, \kappa^{t}, \boldsymbol{\omega}^{t}\right)$, where $\boldsymbol{\omega}^{t}$ is the vector of idiosyncratic cost draws. At this point, lender $j$ chooses the quote to offer $p_{j}^{t}$, and the borrower determines the winner in the English auction $\left(w^{t}\right)$.

[^13]Note that the only state variable determined by past actions is the home-bank identity:

$$
h^{t+1}= \begin{cases}h^{t}, & n^{t}=1 \\ w^{t}, & \mathrm{o} / \mathrm{w}\end{cases}
$$

The remaining state variables in the next period either stay the same $(N, \lambda)$ or are determined by a new draw from a certain distribution $\left(c^{t+1}, \kappa^{t+1}, \boldsymbol{\omega}^{t+1}\right) .{ }^{23}$

In what follows, we first characterize the equilibrium bidding strategies and equilibrium pricing functions in the negotiation stage conditional on the borrower's chosen choice set. We then solve the borrower's problem of choice-set formation and the home bank's problem of optimal initial-quote offering.

### 3.3 Negotiation Stage: English Auction

In each period $t$, conditional on $n^{t}$, we solve for the equilibrium pricing functions. If $n^{t}=1$, the borrower is satisfied with her home bank's initial offer and does not enter into the negotiation stage. The equilibrium price is $p^{t *}=p_{0}^{t}$.

If $n^{t} \geq 2$, lenders compete in expected utility via an English auction. An English auction approximates negotiation by capturing two important features in the process: (1) borrowers use the best offer in hand to extract better quotes, and (2) lenders are willing to lower their offers to win as long as they expect positive profits.

The weakly dominant bidding strategy is to bid one's reservation value (cost). Lenders drop out at the point where they are indifferent between winning and losing. Let the current best offer be $\tilde{b}^{t}$. Lender $j$ stays in the auction and keeps bidding so long as the present value of winning at $\tilde{b}^{t}$ is greater than the present value of losing:

$$
\begin{equation*}
\tilde{b}^{t}-\left(c^{t}+\omega_{j}^{t}\right)+\delta W_{j}^{t+1} \geq \delta L_{j}^{t+1} \tag{2}
\end{equation*}
$$

where $\delta$ is the lenders' discount factor, $W_{j}^{t+1}$ is lender $j$ 's continuation value of winning the auction, and $L_{j}^{t+1}$ is its continuation value of losing. Since all lenders have a symmetric cost structure, the continuation values are the same across lenders. ${ }^{24}$ We therefore drop

[^14]the lender index $j$. Note that current actions do not affect the continuation values. While formulating bids, the lenders can simply treat them as constant.

The equilibrium bidding strategy for lender $j$ specifies the price level at which it will drop out of the competition:

$$
\begin{equation*}
b_{j}^{t}\left(c^{t}, \omega_{j}^{t}\right)=c^{t}+\omega_{j}^{t}-\delta\left(W^{t+1}-L^{t+1}\right) \tag{3}
\end{equation*}
$$

Lenders might bid lower than their costs because they take into account the future value of winning the contract. The net continuation value of winning $V^{t+1} \equiv W^{t+1}-L^{t+1}$ describes the future benefits of being a home bank in period $t+1$ and also represents the value of an attached borrower. $V^{t+1}$ highlights the lenders' investment incentives: banks compete ex ante for a future incumbency advantage. Given that it depends on the home bank's profit and hence the borrower's search decision, we show exactly how it can be calculated after solving the home bank's and the borrower's problems in the initial quote stage (see subsection 3.5).

Due to switching costs, the winner is determined by the ranking in expected utility rather than in bids. In particular, given the equilibrium bidding strategies and the switching cost $\lambda$, if bank $j$ wins the auction, the equilibrium price $p_{j}^{t *}$ should satisfy:

$$
\begin{equation*}
\bar{v}^{t}-\lambda \mathcal{I}_{j \neq h^{t}}-p_{j}^{t *}+\rho U_{j}^{t+1}=\max _{k \neq j}\left\{\bar{v}^{t}-\lambda \mathcal{I}_{k \neq h^{t}}-b_{k}^{t}+\rho U_{k}^{t+1}\right\}, \tag{4}
\end{equation*}
$$

where $\mathcal{I}_{j \neq h^{t}}$ is an indicator function that equals 1 if $j$ is not the home bank. The righthand side of equation (4) represents the highest expected utility/surplus that the rival banks can offer. Because lenders have symmetric cost structures, the continuation value of
$j$ 's continuation value of winning is the same as the other lenders'. Whichever lender wins the current auction, it enters the next period as the home bank and plays the same game delineated in subsection 3.2. More importantly, conditional on the market structure $N$, the switching cost $\lambda$, and whether or not it is the home bank, a lender's expected profit only depends on the future realization of $\boldsymbol{\omega}$ and $\kappa$, which are drawn independently and repeatedly every period. Therefore, a lender's current bid would not affect the continuation values $W^{t+1}$ and $L^{t+1}$. This greatly simplifies the equilibrium bidding strategies and the calculation of continuation values. To understand how asymmetric idiosyncratic cost distributions complicate the model, consider a case with two types of lenders, one of which is more likely to draw relatively low idiosyncratic costs. The continuation values now depend on both the bidder's type and the winning bank's type (and hence the bidding strategies): $L_{j}^{t+1}$ is higher if the winning bank is of high cost since it is more likely to poach the borrower in the next period. Therefore, while formulating the bidding strategies, lenders need to form beliefs about the winning probabilities of the other competitors, which need to be updated every time a lender drops out. We can no longer ensure that there exists a unique equilibrium. Nonetheless, if we have access to more information (e.g. choice set chosen, drop-out order, and drop-out prices), the model could be modified and estimated using the two-step estimation method proposed by Bajari et al. (2007), assuming lenders play the same type of equilibrium for each borrower.
being attached to any bank $U_{j}^{t+1}$ is the same. At the end, the highest surplus lender wins at a price just beating the second-best option. Specifically, we can write the equilibrium price as a function of the state vector:

$$
p^{t *}\left(s^{t}\right)= \begin{cases}c^{t}-\delta V^{t+1}+\omega_{(2)}^{t}+\lambda, & \omega_{h^{t}}-\lambda=\omega_{(1)}^{t}  \tag{5}\\ c^{t}-\delta V^{t+1}+\omega_{(2)}^{t}, & \omega_{h^{t}}-\lambda \leq \omega_{(2)}^{t}\end{cases}
$$

where $\omega_{h^{t}}$ is the home bank's idiosyncratic match value and $\omega_{(k)}^{t}$ denotes the $k^{t h}$ order statistic among $\left(\omega_{h^{t}}-\lambda, \omega_{1}, \omega_{2}, \cdots, \omega_{n^{t}-1}\right) .{ }^{25}$ Equation (5) describes the equilibrium price in cases where the home bank ranks $1^{\text {st }}$ and the $2^{\text {nd }}$ or lower place in terms of expected utility. This equation shows that lenders compete aggressively ex ante for the ex post rent, $V^{t+1}$. The home bank clearly enjoys an incumbency advantage originating from the switching cost, $\lambda$.

### 3.4 Initial Quote Stage

Given the home bank's offer $p_{0}^{t}$ and the search cost realization $\kappa^{t}$, the borrower's tradeoff is between accepting $p_{0}^{t}$ or paying $\left(n^{t}-1\right) \kappa^{t}$ to obtain the expected winning price $E\left[p^{t *}\left(s^{t}\right) \mid n^{t}\right]$, where the expectation is taken with respect to the idiosyncratic cost shocks drawn by the $n^{t}$ lenders in the choice set. ${ }^{26}$

Given $p_{0}^{t}$ and the equilibrium pricing function (5), we can calculate the expected equilibrium price conditional on $n^{t}=l$ :

$$
\begin{aligned}
E\left[p^{t *} \mid n^{t}=l\right]= & \operatorname{Pr}\left(\omega_{h^{t}}-\lambda \leq \omega_{-h^{t}} \mid n^{t}=l\right) E\left[c^{t}-\delta V^{t+1}+\omega_{(2)}^{t}+\lambda \mid n^{t}=l\right] \\
& +\operatorname{Pr}\left(\omega_{h^{t}}-\lambda>\omega_{-h^{t}} \mid n^{t}=l\right) E\left[c^{t}-\delta V^{t+1}+\omega_{(2)}^{t} \mid n^{t}=l\right] \\
= & c^{t}-\delta V^{t+1}+E\left[\omega_{(2)}^{t} \mid n^{t}=l\right]+\operatorname{Pr}_{h^{t}} \lambda,
\end{aligned}
$$

where $\operatorname{Pr} h_{h^{t}}=\operatorname{Pr}\left(\omega_{h^{t}}-\lambda \leq \omega_{-h^{t}} \mid n^{t}=l\right)$ is the probability that the home bank wins the auction and $\omega_{-h^{t}}=\min _{j \in n^{t} \backslash h^{t}}\left\{\omega_{j}^{t}\right\}$ is the minimum among the $n^{t}-1$ idiosyncratic cost shocks drawn by the rival banks in the choice set.

[^15]We can then write $\bar{\kappa}_{l}^{t}$ as the total expected gain from searching $l$ lenders versus accepting the initial offer, taking into account the expected utility loss from switching.

$$
\bar{\kappa}_{l}^{t}= \begin{cases}0, & l=1  \tag{6}\\ p_{t}^{0}-\lambda-\left(c^{t}-\delta V^{t+1}+E\left[\omega_{(2)}^{t} \mid n^{t}=l\right]\right), & l=2,3, \cdots, N\end{cases}
$$

The expected marginal benefit from searching $l$ instead of $l-1$ lenders is $\bar{\kappa}_{l}^{t}-\bar{\kappa}_{l-1}^{t}$; specifically,

$$
\kappa_{l}^{t}= \begin{cases}p_{t}^{0}-\lambda-\left(c^{t}-\delta V^{t+1}+E\left[\omega_{(2)}^{t} \mid n^{t}=2\right]\right), & l=2,  \tag{7}\\ \left.\left.E\left[\omega_{(2)}^{t} \mid n^{t}=l-1\right]\right)-E\left[\omega_{(2)}^{t} \mid n^{t}=l\right]\right), & l=3,4, \cdots, N .\end{cases}
$$

A borrower with search cost $\kappa_{l}^{t}$ is indifferent between searching for $l$ versus $l-1$ quotes.
The cost of searching $l$ lenders is $(l-1) \kappa^{t}$ because the home bank is always in the choice set. The borrower chooses $n^{t}$ to maximize the net benefit from searching:

$$
\begin{equation*}
n^{t}=\operatorname{argmax}_{l} \bar{\kappa}_{l}^{t}-(l-1) \kappa^{t}, \quad l=1,2, \cdots, N . \tag{8}
\end{equation*}
$$

The initial home bank quote $p_{0}^{t}$ influences the search intensity $n^{t}$ through the expected gain from searching. When $p_{0}^{t}$ is low enough, the borrower might never choose a choice set of size $l$ because she expects a loss from searching $\bar{\kappa}_{l}^{t}<0$. The borrower would search $l \geq 2$ lenders for some realization of $\kappa^{t}$ if and only if the following condition is satisfied:

$$
\begin{equation*}
\bar{\kappa}_{l}^{t} /(l-1)>\kappa_{l+1}^{t} . \tag{9}
\end{equation*}
$$

This condition implicitly requires $\bar{\kappa}_{l}^{t}>0$. If condition (9) fails, then $\forall \kappa^{t}<\bar{\kappa}_{l}^{t} /(l-1)$, $\kappa^{t}<\kappa_{l+1}^{t}$; the borrower prefers searching $l+1$ rather than $l$ lenders as the expected marginal gain outweighs the search cost.

Let $\bar{l}^{t}$ be the smallest number that satisfies condition (9). Given the search cost distribution, $H(\cdot)$, the home bank expects the borrower searching $l$ lenders with the following probabilities:

$$
\operatorname{Pr}\left(n^{t}=l\right)= \begin{cases}1-H\left(\bar{\kappa}_{\bar{l}^{t}}^{t} /\left(\bar{l}^{t}-1\right)\right), & l=1  \tag{10}\\ 0, & l<\bar{l}^{t} \& l \neq 1 \\ H\left(\bar{\kappa}_{\bar{l}^{t}}^{t} /\left(\bar{l}^{t}-1\right)\right)-H\left(\kappa_{\bar{l}^{t}+1}^{t}\right), & l=\bar{l}^{t} \\ H\left(\kappa_{l}^{t}\right)-H\left(\kappa_{l+1}^{t}\right), & l>\bar{l}^{t} \& l<N \\ H\left(\kappa_{N}^{t}\right), & l=N .\end{cases}
$$

The home bank can therefore choose $p_{0}^{t}$ to influence $\bar{l}^{t}$ and hence the borrower's search probabilities.

For simplicity of exposition, from now on assume in equilibrium that the optimal initial offer $p_{0}^{t *}$ is high enough such that $\bar{l}^{t}=2$. In this case, the home bank's belief is that every size $l$ of the choice set will be reached with positive probability as set out in equation (10). In what follows we derive conditions under which the belief system is well defined and consistent with the home bank's optimal initial quote choice in equilibrium. It is straightforward to adapt to cases where in equilibrium $\bar{l}^{t}>2$.

Anticipating the borrower's search probabilities and the corresponding auction outcomes, the home bank chooses initial quote $p_{0}^{t *}$ to maximize its expected profit:

$$
\begin{align*}
\max _{p_{0}^{t}} & {\left[1-H\left(\bar{\kappa}_{2}^{t}\left(p_{0}^{t}\right)\right)\right]\left(p_{0}^{t}-c^{t}+\delta W^{t+1}\right)+\left[H\left(\bar{\kappa}_{2}^{t}\left(p_{0}^{t}\right)\right)-H\left(\kappa_{3}^{t}\right)\right] E\left[\pi_{h}^{t *} \mid n^{t}=2\right] } \\
& +\sum_{l=3}^{N-1}\left[H\left(\kappa_{l}^{t}\right)-H\left(\kappa_{l+1}^{t}\right)\right] E\left[\pi_{h}^{t *} \mid n^{t}=l\right]+H\left(\kappa_{N}^{t}\right) E\left[\pi_{h}^{t *} \mid n^{t}=N\right] \tag{11}
\end{align*}
$$

where $E\left[\pi_{h}^{t *} \mid n^{t}=l\right]$ is the profit that the home bank expects to obtain in the negotiation stage conditional on the choice set size $n^{t}=l$. It can be calculated as

$$
\begin{aligned}
E\left[\pi_{h}^{t *} \mid n^{t}=l\right] & =P r_{h^{t}}\left\{E\left[p^{t *}-\left(c^{t}+\omega_{h^{t}}\right) \mid n^{t}=l, \omega_{h^{t}}-\lambda \leq \omega_{-h^{t}}\right]+\delta W^{t+1}\right\}+\left(1-P r_{h^{t}}\right) \delta L^{t+1} \\
& =E\left[\max \left\{\omega_{-h^{t}}-\left(\omega_{h^{t}}-\lambda\right), 0\right\} \mid n^{t}=l\right]+\delta L^{t+1} .
\end{aligned}
$$

We can then write the first order condition for the optimal initial quote:

$$
p_{0}^{t}=\frac{1-H\left(\bar{\kappa}_{2}^{t}\left(p_{0}^{t}\right)\right)}{H^{\prime}\left(\bar{\kappa}_{2}^{t}\left(p_{0}^{t}\right)\right)}+c^{t}-\delta V^{t+1}+E\left[\max \left\{\omega_{-h^{t}}-\left(\omega_{h^{t}}-\lambda\right), 0\right\} \mid n^{t}=2\right] .
$$

Replacing $p_{0}^{t}$ on the left-hand side using equation (6) and rearranging, the first order
condition is equivalent to

$$
\begin{equation*}
\bar{\kappa}_{2}^{t}\left(p_{0}^{t}\right)=\frac{1-H\left(\bar{\kappa}_{2}^{t}\left(p_{0}^{t}\right)\right)}{H^{\prime}\left(\bar{\kappa}_{2}^{t}\left(p_{0}^{t}\right)\right)} . \tag{12}
\end{equation*}
$$

Assuming the Mills ratio on the right-hand side is monotonically decreasing, we can obtain a unique solution $\bar{\kappa}_{2}^{t *}$, and hence the optimal initial quote: ${ }^{27}$

$$
\begin{equation*}
p_{0}^{t *}=\bar{\kappa}_{2}^{t *}+\lambda+c^{t}-\delta V^{t+1}+E\left[\omega_{(2)}^{t} \mid n^{t}=2\right] . \tag{13}
\end{equation*}
$$

### 3.5 Continuation Values

We can now summarize the results obtained from the initial-quote stage and the negotiation stage. Given the choice set $n^{t}$ and the state vector $s^{t}$, the equilibrium price from the auction $p^{t *}$ is described in equation (5). Knowing the payoff from accepting $p_{0}^{t}$ and the expected payoff from searching $n^{t}$ lenders, the borrower chooses $n^{t}$ optimally to solve the search problem (8). Anticipating the search intensity (equation (10)) and the corresponding auction outcome, the home bank chooses the optimal initial quote $p_{0}^{t *}$ to maximize its expected profit.

Stepping back to the previous period, $t-1$, anticipating the borrower's and the banks' equilibrium strategies in the following period, the lenders can calculate the continuation value of winning and losing. Specifically, the continuation value of winning is just the sum of the home bank's expected profit from retaining the borrower in the initial quote stage and the expected profit from the negotiation stage if the borrower decides to search:

$$
\begin{align*}
W^{t}= & {\left.\left[1-H\left(\bar{\kappa}_{2}^{t *}\right)\right]\left(p_{0}^{t *}-c^{t}+\delta W^{t+1}\right)+\left[H\left(\bar{\kappa}_{2}^{t *}\right)\right)-H\left(\kappa_{3}^{t}\right)\right] E\left[\pi_{h}^{t *} \mid n^{t}=2\right] } \\
& +\sum_{l=3}^{N-1}\left[H\left(\kappa_{l}^{t}\right)-H\left(\kappa_{l+1}^{t}\right)\right] E\left[\pi_{h}^{t *} \mid n^{t}=l\right]+H\left(\kappa_{N}^{t}\right) E\left[\pi_{h}^{t *} \mid n^{t}=N\right] \\
= & \delta L^{t+1}+\left[1-H\left(\bar{\kappa}_{2}^{t *}\right)\right]\left(\bar{\kappa}_{2}^{t *}+E\left[\max \left\{\omega_{-h^{t}}-\left(\omega_{h^{t}}-\lambda\right), 0\right\} \mid n^{t}=2\right]\right)  \tag{14}\\
& +\sum_{l=2}^{N} \operatorname{Pr}\left(n^{t}=l\right) E\left[\max \left\{\omega_{-h^{t}}-\left(\omega_{h^{t}}-\lambda\right), 0\right\} \mid n^{t}=l\right] .
\end{align*}
$$

In order to calculate the continuation value of losing, consider a representative non-home bank $j$ with idiosyncratic match value $\omega_{j}^{t}$. $\omega_{-j}^{t}$ denotes the first order statistic among the

[^16]$n^{t}-1$ variables $\left(\left\{\omega_{k}^{t}\right\}_{k \neq j, k \neq h^{t}}, \omega_{h^{t}}-\lambda\right)$. The continuation value of losing can be written as
\[

$$
\begin{equation*}
\left.\left.L^{t}=\delta L^{t+1}+\sum_{l=2}^{N} \operatorname{Pr}\left(n^{t}=l\right) \frac{l-1}{N-1} E\left[\max \left\{\omega_{-j}^{t}-\omega_{j}^{t}\right), 0\right\} \right\rvert\, n^{t}=l\right], \tag{15}
\end{equation*}
$$

\]

where the fraction $\frac{l-1}{N-1}$ is the probability that bank $j$ gets selected into the choice set conditional on $n^{t}=l$. Therefore, the net continuation value of winning is

$$
\begin{align*}
V^{t}= & W^{t}-L^{t} \\
= & {\left[1-H\left(\bar{\kappa}_{2}^{t *}\right)\right]\left(\bar{\kappa}_{2}^{t *}+E\left[\max \left\{\omega_{-h^{t}}-\left(\omega_{h^{t}}-\lambda\right), 0\right\} \mid n^{t}=2\right]\right) } \\
& +\sum_{l=2}^{N} \operatorname{Pr}\left(n^{t}=l\right) E\left[\max \left\{\omega_{-h^{t}}-\left(\omega_{h^{t}}-\lambda\right), 0\right\} \mid n^{t}=l\right]  \tag{16}\\
& \left.\left.-\sum_{l=2}^{N} \operatorname{Pr}\left(n^{t}=l\right) \frac{l-1}{N-1} E\left[\max \left\{\omega_{-j}^{t}-\omega_{j}^{t}\right), 0\right\} \right\rvert\, n^{t}=l\right] .
\end{align*}
$$

The investment incentive $V^{t}$ is purely determined by the search cost distribution $H(\cdot)$, the idiosyncratic cost distribution $G(\cdot)$, the switching cost $\lambda$, and the number of available lenders $N$, which are all assumed to be invariant over time. ${ }^{28}$ As a result of the symmetric cost structure, $V^{t}$ does not depend on future continuation values.

Intuitively, the investment incentive is always increasing in the switching cost $\lambda$. It tends to be smaller, however, if the lenders expect search costs to be small, because retaining the borrower becomes less likely in the next period. Other things being equal, as $G(\cdot)$ gets more dispersed, the expected marginal saving from searching an extra bank increases, the borrower obtains more quotes, and the home bank finds it harder to retain the borrower; $V^{t}$ tends to be smaller. Its relationship with $N$ is more subtle. If search costs are expected to be low on average, higher $N$ implies more quotes and more competition in the next period, hence $V^{t}$ would be lower. However, if search costs are very high on average, the borrower would not obtain more quotes even though $N$ increases. $L^{t}$ decreases because the chance of being selected in the next period gets smaller, therefore $V^{t}$ could even increase in $N$.

[^17]
## 4 Identification

This section provides an argument for non-parametric identification of our model. In section 5 , we specify a parametric version in order to make use of observed heterogeneity across borrowers in estimation. The model consists of five primitives: (i) the common cost distribution $F\left(\cdot \mid x_{i}\right)$, the realization of which is the same for all lenders providing a mortgage to borrower $i$, but may vary across borrowers due to both observed and unobserved heterogeneity; (ii) the idiosyncratic cost distribution $G\left(\cdot \mid x_{i}\right)$; (iii) the search cost distribution $H\left(\cdot \mid x_{i}\right)$; (iv) the switching cost, $\lambda_{i}=\Lambda\left(x_{i}\right)$; and (v) the lenders' discount factor $\delta$.

In the data, we observe a cross-section of borrowers (new borrowers and first-time renewers) with (i) observed borrower characteristics $\left(x_{i}\right)$, (ii) the number of lenders available in a borrower's local market $\left(N_{i}\right)$, (iii) the home-bank identity, the chosen lender's identity, and (iv) the contract price offered by the final winner $\left(p_{i}^{*}\right)$. From these observables we wish to recover the model primitives.

There are two main identification challenges. The first is to disentangle the randomness originating from the funding cost distributions $F\left(\cdot \mid x_{i}\right)$ and $G\left(\cdot \mid x_{i}\right)$ and the search cost distribution $H\left(\cdot \mid x_{i}\right)$ from the observed contract price distribution. The price distribution for borrowers staying with their home banks is a mixture of accepted initial quotes and auction prices, while the price distribution for switchers is determined by the search intensity and the corresponding auction outcome. Neither is ideal for separating out the search-cost distribution from the lending-cost distributions.

The second challenge is to disentangle the common cost and idiosyncratic cost distributions. In the auction, due to the random common cost component, lenders' cost for providing a mortgage are not independent. This prevents us from using standard identification strategies under the independent private values framework. Indeed, Athey and Haile (2002) suggest that identification fails in such case without observing all the bids.

In order to get around the negative identification result, we need to put more restrictions on the model primitives. We rely crucially on an exclusion restriction assumption:

Assumption 1. (Exclusion Restriction)
There exists some observable $z_{i}$ that influences the switching cost $\lambda_{i}=\Lambda\left(x_{i}, z_{i}\right)$ but not the other model primitives $F\left(\cdot \mid x_{i}\right), G\left(\cdot \mid x_{i}\right)$, and $H\left(\cdot \mid x_{i}\right) .{ }^{29}$

[^18]For the sake of a more transparent identification argument, we also make the following assumption to abstract away from some observable differences across borrowers:

Assumption 2. $x_{i}$ are the same across contracts.
Further, we make some assumptions on the support of the distributions. These are not imposed in the estimation.

Assumption 3. (Support Assumptions)
(i) The common cost distribution $F(\cdot)$ has bounded support $[\underline{c}, \bar{c}]$.
(ii) The idiosyncratic cost distribution $G(\cdot)$ is mean 0 , and has bounded support $[\underline{\omega}, \bar{\omega}]$.
(iii) The number of available lenders $N_{i}$ has full support ranging from 2 to $\bar{N}$.
(iv) There is enough variation in $z$, such that $\lambda=\Lambda(z)$ ranges from 0 to $+\infty$.

The following assumptions imposed on model primitives are needed to ensure that (1) we are dealing with a unique equilibrium, and (2) in equilibrium the home bank's belief is correct that every size $l$ of the choice set will be reached with positive probability, as set out in equation (10).

## Assumption 4.

(i) The Mills ratio $\frac{1-H(\kappa)}{H^{\prime}(\kappa)}$ is monotonically decreasing.
(ii) In equilibrium, $\kappa_{2}^{*}>\kappa_{3}$.

In what follows, we first focus on markets where only two banks are available to identify all model primitives except for the search cost distribution, and then use price variation across markets with different $N$ to pin down the search cost distribution.

### 4.1 Identification of Switching Costs

We focus on the sub-sample of borrowers located in markets with only two available lenders $(N=2)$. In such markets, if we observe that a borrower switches lenders, she must have rejected the home bank's initial quote and searched. Denote the home bank and rival bank in the choice set as $h$ and $r$, respectively. In the data, we observe the empirical distribution of prices for borrowers financing with their home bank, $P_{h}$, and prices for borrowers switching to the rival bank, $P_{r}$. $P_{h}$ is a mixture of accepted initial quotes, $P_{h 1}$, and prices paid by borrowers who search but don't switch, $P_{h 2}$.

Using the support Assumptions 3(i) and 3(ii), for borrowers with observable $z, P_{h}(z)$ and $P_{r}(z)$ are bounded from below by the following prices:

$$
\begin{align*}
& \underline{P}_{h}(z)=\underline{c}+\underline{\omega}+\Lambda(z)-\delta V(z),  \tag{17}\\
& \underline{P}_{r}(z)=\underline{c}+\underline{\omega}-\delta V(z) .
\end{align*}
$$

$\Lambda(z)$ is therefore identified from $\underline{P}_{h}(z)-\underline{P}_{r}(z)$.

### 4.2 Identification of the Search Probability and Discount Factor

Given Assumption 4(i) and Equation (12), all borrowers face the same unique search cost threshold $\kappa_{2}^{*}=\bar{\kappa}_{2}^{*}$. Therefore, all borrowers accept the home bank initial offer with probability $1-H\left(\kappa_{2}^{*}\right)$.

Now consider the sub-sample of borrowers in 2-bank markets with $\Lambda(z)=0$, who are equally likely to stay or switch in the negotiation stage. In the data, we observe the empirical probability that borrowers search and switch:

$$
\operatorname{Pr}(\text { search, } \operatorname{switch} \mid \Lambda(z)=0)=\operatorname{Pr}\left(\kappa<\kappa_{2}^{*}\right) \operatorname{Pr}\left(\omega_{h}>\omega_{r}\right)=H\left(\kappa_{2}^{*}\right) / 2 .
$$

Therefore, the probability of searching $H\left(\kappa_{2}^{*}\right)$ is identified.
Similarly, we can write the empirical probability of search and switch for the subsample of borrowers with $\lambda=\Lambda(z)$ :

$$
\operatorname{Pr}(\text { search, switch } \mid \lambda=\Lambda(z))=H\left(\kappa_{2}^{*}\right) \operatorname{Pr}\left(\omega_{h}-\Lambda(z)>\omega_{r}\right) .
$$

Therefore $\operatorname{Pr}\left(\omega_{h}-\omega_{r}<-\Lambda(z)\right)$ is identified. By varying $\Lambda(z)$, the distribution of the idiosyncratic cost difference $\left(\omega_{h}-\omega_{r}\right)$ is identified.

Now go back to the sub-sample of borrowers with $\Lambda(z)=0$ in 2-bank markets. We can write the expected values of the switchers' prices, the home-bank initial offers, and the loyal borrowers' prices:

$$
\begin{aligned}
& E\left[P_{r} \mid \Lambda(z)=0\right]=E[c]+E\left[\max \left\{\omega_{h}, \omega_{r}\right\}\right]-\delta V(z), \\
& E\left[P_{h 1} \mid \Lambda(z)=0\right]=E[c]+E\left[\max \left\{\omega_{h}, \omega_{r}\right\}\right]-\delta V(z)+\kappa_{2}^{*}, \\
& E\left[P_{h} \mid \Lambda(z)=0\right]=\left[1-H\left(\kappa_{2}^{*}\right)\right] E\left[P_{h 1} \mid \Lambda(z)=0\right]+\frac{H\left(\kappa_{2}^{*}\right)}{2} E\left[P_{r} \mid \Lambda(z)=0\right] .
\end{aligned}
$$

The last equality holds because the expected values of $P_{r}$ and $P_{h 2}$ are the same when
switching costs are zero. In the data, the average prices of $P_{r}$ and $P_{h}$ are observed. We can therefore use the above equations to derive $\kappa_{2}^{*}$.

Given the search cost threshold $\kappa_{2}^{*}$, the search probability $H\left(\kappa_{2}^{*}\right)$, the switching cost $\Lambda(z)$, and the distribution of $\left(\omega_{h}-\omega_{r}\right)$, the investment incentive conditional on observable $z$ can be calculated:

$$
V(z)=\left[1-H\left(\kappa_{2}^{*}\right)\right]\left(\kappa_{2}^{*}+E\left[\max \left\{\omega_{r}-\left(\omega_{h}-\lambda\right), 0\right\}\right]\right)+H\left(\kappa_{2}^{*}\right) \Lambda(z)
$$

The discount factor $\delta$ is identified from the lower bounds of prices in Equation (17) by varying $z$. The lower bound on funding costs $\underline{c}+\underline{\omega}$ is also identified.

### 4.3 Identification of Cost Distributions

We have now identified the probability of searching $H\left(\kappa_{2}^{*}\right)$. It will help to separate out the distribution of initial home bank offers $P_{h 1}$ from the observed loyal borrowers' price distribution $P_{h}$.

We again focus on the sub-sample of borrowers with $\Lambda(z)=0$ in 2-bank markets. The distribution of $P_{h}$ is given by

$$
\operatorname{Pr}\left(P_{h} \leq p \mid \Lambda(z)=0\right)=\left[1-H\left(\kappa_{2}^{*}\right)\right] \operatorname{Pr}\left(P_{h 1} \leq p \mid \Lambda(z)=0\right)+\frac{H\left(\kappa_{2}^{*}\right)}{2} \operatorname{Pr}\left(P_{r} \leq p \mid \Lambda(z)=0\right)
$$

because the distributions of $P_{h 2}$ and $P_{r}$ are the same when switching costs are zero. The distribution of $P_{h 1}$ is identified because the empirical distributions of $P_{h}$ and $P_{r}$ are known. Therefore the distribution of the common cost distribution $F(\cdot)$ is identified from the following equation:

$$
\begin{aligned}
\operatorname{Pr}\left(P_{h 1} \leq p \mid \Lambda(z)=0\right) & =\operatorname{Pr}\left(c+E\left[\max \left\{\omega_{h}, \omega_{r}\right\}\right]-\delta V(z)+\kappa_{2}^{*} \leq p \mid \Lambda(z)=0\right) \\
& =\operatorname{Pr}\left(c \leq p-\left(E\left[\max \left\{\omega_{h}-\omega_{r}, 0\right\}\right]-\delta V(z)+\kappa_{2}^{*}\right) \mid \Lambda(z)=0\right) .
\end{aligned}
$$

In addition, using the empirical distribution of switcher's prices, we can identify the distribution of $c+\max \left\{\omega_{h}, \omega_{r}\right\}$ :

$$
\begin{aligned}
\operatorname{Pr}\left(P_{r} \leq p \mid \Lambda(z)=0\right) & =\operatorname{Pr}\left(c+\max \left\{\omega_{h}, \omega_{r}\right\}-\delta V(z) \leq p \mid \Lambda(z)=0\right) \\
& =\operatorname{Pr}\left(c+\max \left\{\omega_{h}, \omega_{r}\right\} \leq p+\delta V(z) \mid \Lambda(z)=0\right)
\end{aligned}
$$

The distribution of $\max \left\{\omega_{h}, \omega_{r}\right\}$ is identified using a standard deconvolution approach. ${ }^{30}$ The parent distribution $G(\cdot)$ is therefore also identified.

### 4.4 Identification of the Search Cost Distribution

From above, we have already obtained some information about the search cost distribution: the search cost threshold $\kappa_{2}^{*}$ and the search probability $H\left(\kappa_{2}^{*}\right)$ in 2-bank markets. Recall that $\kappa_{2}^{*}$ is solely determined by the search cost distribution as shown in Equation (12). Therefore, in all markets $(N \geq 2)$, borrowers will accept the initial quotes with probability $\left(1-H\left(\kappa_{2}^{*}\right)\right)$ and search multiple quotes with probability $H\left(\kappa_{2}^{*}\right)$. The search cost distribution is identified at the cut-off value $\kappa_{2}^{*}$. By varying $N$, we can identify the search cost distribution at more cut-off values $\left(\kappa_{l>2}(z)\right)$. And by varying the observable $z$, the set of cut-off values will also change, tracing out most of the search cost distribution. However, $H(\cdot)$ cannot be identified for search costs above $\kappa_{2}^{*}$, because borrowers who draw such high search costs would all simply accept the home banks' initial offers, making them observationally equivalent.

Consider a sub-sample of borrowers with observable $z$ in 3-bank markets. The cut-off value $\kappa_{3}(z)$ can be calculated using Equation (7) because we know the idiosyncratic cost distribution $G(\cdot)$ and the switching cost $\Lambda(z)$. The overall switching probability is

$$
\begin{aligned}
\operatorname{Pr}(\text { switch })= & \operatorname{Pr}(n=2) \operatorname{Pr}\left(\omega_{-h} \leq \omega_{h}-\Lambda(z) \mid n=2\right) \\
& +\operatorname{Pr}(n=3) \operatorname{Pr}\left(\omega_{-h} \leq \omega_{h}-\Lambda(z) \mid n=3\right)
\end{aligned}
$$

where all probabilities are also conditional on $\lambda=\Lambda(z)$ and $N=3$. Given that the search probabilities $\operatorname{Pr}(n=2 \mid \lambda=\Lambda(z), N=3)$ and $\operatorname{Pr}(n=3 \mid \lambda=\Lambda(z), N=3)$ add up to $H\left(\kappa_{2}^{*}\right)$, they are identified. Note that the probability of searching only 2 banks in the 3-bank market can also be written as

$$
\begin{aligned}
\operatorname{Pr}(n=2 \mid \lambda=\Lambda(z), N=3) & =\operatorname{Pr}(n=2 \mid \lambda=\Lambda(z), N=\bar{N}) \\
& =H\left(\kappa_{2}^{*}\right)-H\left(\kappa_{3}(z)\right) .
\end{aligned}
$$

Therefore, $H(\cdot)$ is also identified at the point $\kappa_{3}(z)$. Inductively, $H\left(\kappa_{4}(z)\right)$ is identified using the sub-sample of borrowers with switching cost $\Lambda(z)$ in the 4 -bank markets, and so forth. By varying $z$ and hence $\Lambda(z)$, we can obtain different sets of cut-off values $\kappa_{l}(z)$,

[^19]tracing out the search cost distribution $H(\cdot)$ evaluated at these points.

## 5 Empirical Specification

Consider a borrower $i$ in a market with $N_{i}$ available lenders looking to originate or renew a mortgage with loan size $\$ M_{i}$. We model the common cost of all lenders for providing the mortgage over the 5 -year term as $M_{i} c_{i}$, which naturally depends on the loan size. The per-unit common cost $c_{i}$ is assumed to be drawn from a normal distribution $N\left(\boldsymbol{x}_{\boldsymbol{i}} \boldsymbol{\beta}, \sigma_{c}^{2}\right)$. The vector $\boldsymbol{x}_{\boldsymbol{i}}$ includes borrower-specific observable characteristics such as outstanding amount, credit score, and amortization, as well as market characteristics such as the 5 year bond rate, FSA median income in 2016, quarterly number of housing transactions per FSA, quarterly average sale price per FSA, year fixed effects, and location fixed effects. ${ }^{31}$ The loan size $M_{i}$ is normalized so that the per-unit common cost measures the cost of a $\$ 100,000$ mortgage.

Denote borrower $i$ 's mortgage loan size at origination (origination amount) as $M_{i}^{1}$. $M_{i}^{1}$ is the same as $M_{i}$ for new borrowers, but greater than $M_{i}$ for renewers, because renewers have paid down some of their outstanding balance over the first 5 -year term. We model the idiosyncratic cost for lender $j$ in the negotiation stage as $M_{i}^{1} \omega_{i, j}$, where $\omega_{i, j}$ is drawn i.i.d. from a type-1 extreme value distribution $\operatorname{T1EV}\left(\gamma \sigma_{\omega}, \sigma_{\omega}\right) .{ }^{32} M_{i}^{1}$ captures the effect of loan-size on costs. Fixing the loan size to the amount at origination has two benefits. First, the origination amount can be seen as more informative about a borrower's profitability beyond the mortgage product. The second benefit is technical: it prevents the outstanding amount from entering into the lenders' pricing problem. ${ }^{33}$

The switching cost is assumed to be a linear function of borrower's age, credit score, and median income at FSA level in 2016. For new borrowers, we allow the switching cost from a pre-mortgage relationship to be different from the regular switching costs for renewers:

$$
\lambda_{i}=M_{i}^{1} \times\left(\lambda_{0}+\lambda_{\text {credit }} \text { Credit }_{i}+\lambda_{\text {inc }} \text { Income }_{i}+\lambda_{\text {age }} \text { Age }_{i}+\lambda_{\text {new }}\right) .
$$

[^20]The search cost is assumed to follow an exponential distribution with its mean determined by the borrower's age, credit score, and the FSA-level median income:

$$
H_{i}(\kappa)=1-\exp \left(-\frac{\kappa}{\alpha_{i}}\right), \quad \alpha_{i}=\exp \left(\alpha_{0}+\alpha_{\text {credit }} \mathrm{Credit}_{i}+\alpha_{i n c} \mathrm{Income}_{i}+\alpha_{\text {age }} \mathrm{Age}_{i}\right) .
$$

Given the parametric assumptions, we can analytically solve the search probabilities, the net continuation value of winning, the home bank's optimal initial offer, the auction price in the negotiation stage conditional on stay/switch and the choice set size. We can then derive the likelihood contribution of each borrower (loyal or switch). Since we do not observe the number of quotes, we first construct the likelihood function conditional on the choice set, $n_{i}$, and then integrate out $n_{i}$ using the search probabilities. We estimate the model by maximum likelihood. The likelihood function is derived in Section B.

## 6 Estimation Results

### 6.1 Model Estimates

Table 3 displays the maximum likelihood estimates from both our benchmark dynamic model and a static model that restricts the lenders' discount factor $\delta=0$. In the dynamic model, we estimate a lender discount factor of 0.73 over a 5 -year span, which translates into an annual discount factor of 0.94 . The likelihood ratio test rejects the static model at the $0.1 \%$ significance level.

The mortgage loan size is normalized to be measured in $\$ 100,000$. The estimated parameters, measured in $\$ 1,000$, describe how the interest cost of a $\$ 100,000$ mortgage is determined by the observable characteristics and the random shocks. For example, in the first row $\sigma_{c}=0.8534$ implies that the standard deviation of the common cost for lending $\$ 100,000$ over a 5 -year term is $\$ 853.4$. In what follows, we discuss the economic magnitude of the model estimates.

Lending Costs. The standard deviation of the idiosyncratic cost distribution is $\$ 187.6$, which is only about one fifth of the standard deviation of the common cost shock. ${ }^{34}$ This means that most of the unexplained price variation should be attributed to unobserved borrower heterogeneity rather than idiosyncratic differences across banks. This is consistent with Allen et al. (2019).

The dispersion of the idiosyncratic cost distribution is key for understanding the bor-

[^21]Table 3: Maximum Likelihood Estimation Results

|  | Dynamic Model |  | Static Model |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Estimate | (S.E.) | Estimate | (S.E.) |
| Cost shocks |  |  |  |  |
| $\sigma_{c}$ | 0.8534 | $(0.003)$ | 0.8563 | $(0.0031)$ |
| $\sigma_{\omega}$ | 0.1463 | $(0.0022)$ | 0.1503 | $(0.0021)$ |
| Search cost |  |  |  |  |
| $\alpha_{0}$ | -1.0557 | $(1.2617)$ | -0.0527 | $(0.0185)$ |
| $\alpha_{\text {credit }}$ | -0.0478 | $(0.1597)$ | -0.1203 | $(0.0026)$ |
| $\alpha_{\text {income }}$ | 0.1199 | $(0.0166)$ | 0.1120 | $(0.0083)$ |
| $\alpha_{\text {age }}$ | -0.0667 | $(0.0353)$ | -0.1533 | $(0.0111)$ |
| Switching cost |  |  |  |  |
| $\lambda_{0}$ | -0.1422 | $(0.0952)$ | -0.1705 | $(0.0283)$ |
| $\lambda_{\text {credit }}$ | 0.0471 | $(0.0123)$ | 0.0528 | $(0.0029)$ |
| $\lambda_{\text {income }}$ | -0.0062 | $(0.0018)$ | -0.0071 | $(0.0017)$ |
| $\lambda_{\text {age }}$ | 0.0269 | $(0.0043)$ | 0.0282 | $(0.0033)$ |
| $\lambda_{\text {new }}$ | -0.1452 | $(0.008)$ | -0.1488 | $(0.0079)$ |
| Mean common cost |  |  |  |  |
| Constant | 11.8419 | $(0.3811)$ | 11.4375 | $(0.2735)$ |
| Credit score | -0.1122 | $(0.0103)$ | -0.1392 | $(0.0095)$ |
| Outstanding amount | -0.0891 | $(0.0108)$ | -0.0383 | $(0.0067)$ |
| Bond rate | 1.7871 | $(0.0315)$ | 1.7728 | $(0.0303)$ |
| Amortization | 0.4965 | $(0.0097)$ | 0.5074 | $(0.0073)$ |
| Income | -0.0126 | $(0.004)$ | -0.0191 | $(0.0031)$ |
| House price $(\log )$ | -0.1072 | $(0.0313)$ | -0.0879 | $(0.0239)$ |
| Transaction no. $(\log )$ | -0.0425 | $(0.0056)$ | -0.0495 | $(0.005)$ |
| Discount factor $\delta$ | 0.7278 | $(0.1118)$ |  |  |
| Log likelihood | $45,625.00$ |  | $45,277.99$ |  |
| LR test $\left(H_{0}: \delta=0\right)$ |  |  | 25.98 |  |

Note: outstanding amount is measured in $\$ 100,000$, credit score is measured in 100 , median income at FSA level is measured in $\$ 10,000$, amortization is measured in 5 years, and bond rate is measured in percentage points. We include year fixed effects and region fixed effects. We trim the bottom and top $1 \%$ of observations in terms of interest rate. Each specification has 16,377 observations. The likelihood ratio test rejects the null hypothesis $\delta=0$ at significance level $0.1 \%$. The critical value of $\chi^{2}(1)$ distribution associated with the $0.1 \%$ significance level is 10.83 .
rowers' search decisions. When banks' idiosyncratic costs vary a lot, borrowers are more likely to find banks with a low enough price to switch to, and hence they are more likely to search. Figure 1 shows a median borrower's expected marginal benefit of adding an extra bank to the choice set. The expected marginal benefit decreases as the choice set
gets bigger, declining from over $\$ 450$ for $n=1$ to around $\$ 30$ for $n=9$.
Turning to the mean of the common cost component, the coefficient estimates all have intuitive interpretations. The mean common cost is decreasing in credit score and increasing in bond rate. On average, mortgages with a higher outstanding balance or shorter amortization cost less per unit. The lending costs are on average lower in markets with higher income level, higher house price, and greater volume of housing transactions. Search Costs. Since we do not observe the search cost realizations and search decisions, we use a simulated sample to help understand the estimated search cost distribution. We simulate 100,000 contracts by sampling borrowers' observable characteristics from the empirical distribution and drawing search cost and lending cost shocks from the estimated distributions. We then solve the equilibrium outcomes and summarize the variables of interest in Table 4. See subsection 6.2 for more details about the simulation process.

Searchers, on average, have much lower per-bank search costs than do non-searchers: $\$ 204$ versus $\$ 972$. On average they obtain 3.4 quotes, one of which is from the home bank. Figure 2 shows how average search costs vary by credit score, income, and age. The income level at the borrower's FSA plays a major role in shaping the search costs. This is intuitive because the search and negotiation process is time consuming and time costs can be approximated by borrowers' income. In addition, search costs are on average decreasing in credit score and age, possibly due to more leverage and experience in negotiations.

Switching Costs. Renewers on average face much higher switching costs than new borrowers, $\$ 656$ versus $\$ 293$, as shown in Table 4. This is reasonable given the extra fees and inconvenience incurred from transferring mortgages across lenders relative to, say, a credit card. Figure 2 shows, for a $\$ 100,000$ mortgage, the variation of renewers' switching costs by credit score, income, and age. Switching costs are increasing in credit score and age, while the FSA-level income does not seem to have significant impact. This is also intuitive since the switching process itself is not very time consuming. ${ }^{35}$

[^22]Figure 1: Expected Marginal Benefit of Adding an Extra Bank


Note: For each choice set size $n=1,2,3, \cdots, 10$, we simulate 10,000 purchase (renewal) mortgage contracts for a borrower with median observable characteristics and calculate the average cost of financing (equilibrium price plus switching cost incurred). The expected marginal benefit of adding an extra bank to a choice set of size $n$ is calculated as the change in cost of financing.

Table 4: Summary Statistics of Variables of Interest

|  | mean | sd | p25 | p50 | p75 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Search cost | 485.7 | 545.8 | 130 | 317 | 652 |
| Searcher | 203.6 | 164.7 | 78 | 173 | 294 |
| Non-searcher | 971.8 | 625.5 | 578 | 796 | 1,166 |
| Number of quotes | 2.5 | 1.9 | 1 | 2 | 3 |
| Searcher | 3.4 | 1.9 | 2 | 3 | 4 |
| Switching cost | 478.2 | 315.6 | 244 | 402 | 642 |
| New purchase | 293.2 | 171.4 | 175 | 260 | 370 |
| Renewal | 655.9 | 320.3 | 426 | 604 | 824 |
| Investment incentive | 774.4 | 278.9 | 572 | 738 | 937 |

Note: We simulate 100,000 mortgage contracts by sampling borrowers' observable characteristics from the empirical distribution and drawing lenders' cost shocks and borrowers' search cost shocks from the estimated distributions. We then solve the lenders' equilibrium pricing and borrowers' search decisions.

Figure 2: Search and Switching Costs by Credit Score, Income, Age


Note: Each subplot shows the variation of search (switching) cost by credit score, income, and age, respectively, while fixing the other two factors at median level. For example, the upper middle plot displays the average search cost level for borrowers with median credit score and median age but at different income percentiles. The lower middle plot shows the switching cost per $\$ 100,000$ mortgage for renewers with median credit score and median age but at different income percentiles.

### 6.2 Goodness of Fit

In order to understand the goodness of fit for the structural model, we simulate mortgage contracts by feeding observable transaction characteristics into the estimated model. If the model approximates well the underlying data-generating process, the simulated sample should be similar to the data. We obtain the observed and simulated samples as follows:

1. With replacement, randomly draw 100,000 mortgage contracts (including the observable transaction characteristics and the equilibrium outcomes) from the data to form the observed sample.
2. Use the observed sample, keep the transaction characteristics $\left(x_{i}, h_{i}, N_{i}\right)$, and draw individual shocks $\left(c_{i}, \boldsymbol{\omega}_{i}, \kappa_{i}\right)$ from the estimated lending cost and search cost distributions.
3. Solve the model and compute the equilibrium outcomes for the simulated sample: the home bank's initial offer $p_{i, 0}^{*}$, the borrower's search decision $n_{i}^{*}$, the borrower's switch decision, and the winning price $p_{i}^{*}$.

Table 5 summarizes the equilibrium outcomes from both the observed and simulated
samples. Panel A shows the comparison for new borrowers' contracts, while Panel B is for renewal contracts. Overall, the unconditional distributions of interest rate, interest cost, and switch indicator from the simulated sample closely match those from the observed sample. The model seems to overpredict the median interest rate ( $2.69 \% \mathrm{vs} .2 .73 \%$ for purchase, and $2.70 \%$ vs. $2.77 \%$ for renewal) and the share of switching borrowers, but matches very well the interest cost distribution.

Table 5: Summary Statistics for Observed and Simulated Samples

|  | Observed Sample |  |  | Simulated Sample |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Panel A: New Purchase |  |  |  |  |  |
|  | Rate(\%) | Interest Cost | 1(Switch) | Rate(\%) | Interest Cost | 1(Switch) |
| mean | 2.75 | 31.88 | 0.259 | 2.75 | 31.85 | 0.283 |
| sd | 0.25 | 15.30 | 0.438 | 0.26 | 15.21 | 0.450 |
| p25 | 2.59 | 21.03 |  | 2.57 | 20.91 |  |
| p50 | 2.69 | 29.51 |  | 2.73 | 29.62 |  |
| p75 | 2.90 | 40.21 |  | 2.91 | 40.24 |  |


|  | Panel B: Renewal |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| mean | Rate(\%) | Interest Cost | 1(Switch) | Rate(\%) | Interest Cost | 1(Switch) |  |
|  | 2.79 | 23.94 | 0.120 |  | 2.80 | 23.95 | 0.136 |
| sd | 0.27 | 11.83 | 0.325 |  | 0.28 | 11.79 | 0.343 |
| p25 | 2.60 | 15.48 |  | 2.60 | 15.43 |  |  |
| p50 | 2.70 | 21.98 |  | 2.77 | 21.96 |  |  |
| p75 | 2.99 | 30.36 |  | 2.98 | 30.42 |  |  |

Note: The observed sample is obtained by drawing 100,000 mortgage contracts from the data with replacement. The simulated sample is obtained by keeping the transaction characteristics the same as the observed sample while drawing shocks from the estimated distributions. Unit for interest cost is $\$ 1,000$.

In Table 6, we assess the model's ability to generate the same correlations between equilibrium outcomes (e.g. interest rate and switching decision) and transaction characteristics as those observed in the data. Regression estimates in columns (1)-(2) are based on the observed sample, while those in columns (3)-(4) are from the simulated data. The first exercise ((1) and (3)) regresses interest rates on the observable characteristics and the contract purpose (new purchase, loyal renewal, or switch renewal). We also report estimates from linear probability models for the switch decisions in columns (2) and (4).

Table 6: Reduced-form Regressions Using Observed and Simulated Samples

|  | Observed Sample |  | Simulated Sample |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (1) <br> Rate | (2) <br> 1(Switch) | (3) <br> Rate | (4) <br> 1(Switch) |
| Credit score | $\begin{gathered} -2.20^{* * *} \\ (0.099) \end{gathered}$ | $\begin{gathered} -0.034^{* * *} \\ (0.0017) \end{gathered}$ | $\begin{gathered} -2.52^{* * *} \\ (0.099) \end{gathered}$ | $\begin{gathered} -0.040^{* * *} \\ (0.0020) \end{gathered}$ |
| Outstanding amount | $\begin{gathered} -2.28^{* * *} \\ (0.067) \end{gathered}$ | $\begin{aligned} & 0.025^{* * *} \\ & (0.0014) \end{aligned}$ | $\begin{gathered} -2.51^{* * *} \\ (0.072) \end{gathered}$ | $\begin{aligned} & 0.042^{* * *} \\ & (0.0015) \end{aligned}$ |
| Income | $\begin{gathered} -0.18^{* * *} \\ (0.036) \end{gathered}$ | $\begin{aligned} & -0.00043 \\ & (0.00076) \end{aligned}$ | $\begin{gathered} -0.14^{* * *} \\ (0.038) \end{gathered}$ | $\begin{gathered} -0.0064^{* * *} \\ (0.00078) \end{gathered}$ |
| No. of lenders | $\begin{gathered} -0.62^{* * *} \\ (0.044) \end{gathered}$ | $\begin{aligned} & 0.0035^{* * *} \\ & (0.00084) \end{aligned}$ | $\begin{aligned} & -0.085^{*} \\ & (0.042) \end{aligned}$ | $\begin{aligned} & 0.0054^{* * *} \\ & (0.00084) \end{aligned}$ |
| Loyal renewal | $\begin{gathered} 3.71^{* * *} \\ (0.15) \end{gathered}$ |  | $\begin{gathered} 5.10^{* * *} \\ (0.15) \end{gathered}$ |  |
| Switch renewal | $\begin{gathered} -5.30^{* * *} \\ (0.24) \\ \hline \end{gathered}$ |  | $\begin{gathered} -9.70^{* * *} \\ (0.26) \\ \hline \end{gathered}$ |  |
| $R^{2}$ | 0.492 | 0.038 | 0.496 | 0.033 |

Note: Sample size: 100,000. Additional controls include bond rate, amortization, age, FSA house price, and FSA transaction number, the estimated coefficients of which are well matched. We include year and region fixed effects. Robust standard errors in parentheses. ${ }^{*} p<0.05,{ }^{* *} p<0.01,{ }^{* * *} p<0.001$.

The estimated model almost perfectly reproduces the correlation between interest rates and observable transaction characteristics, except that it underestimates the coefficient on the number of lenders. We obtain similar $R^{2} \mathrm{~s}$ from the observed and simulated samples, indicating that a similar amount of rate dispersion cannot be explained by the observable characteristics. The structural model attributes this unexplained portion to the random draws of the structural shocks.

However, the average loyalty premium predicted by the model is somewhat higher than that estimated from the observed sample. This is partly explained by the fact that we have trimmed mortgage contracts with extreme values for interest rates in the observed sample but not in the simulated one.

The estimated model also performs well in terms of matching the correlation between borrowers' switching decisions and the observable transaction characteristics. The linear probability regression estimates from the simulated sample display the same signs as those obtained from the observed sample, and many of the coefficient estimates are close in magnitude.

## 7 Counterfactual Experiments

In this section we conduct three counterfactual experiments to investigate (i) the effects of search and switching frictions on borrowers' and banks' payoffs, (ii) the implications of dynamic versus static settings for merger-studies, and (iii) the impacts from the recently adopted mortgage stress tests in Canada.

The first two experiments highlight the importance of understanding lenders' dynamic pricing strategies. A static model overestimates the benefit of removing search and switching costs because it ignores the changes in lenders' investment incentives and pricing dynamics. For the same reasons, a static merger simulation overestimates the impact of a merger, and a retrospective merger evaluation using only purchase contracts underestimates the impact of a merger on renewals.

Finally, we examine the potential impact of a recent government-mandated mortgage affordability test, which requires borrowers to satisfy tighter debt-to-income constraints. Importantly, uninsured renewers are required to pass the test if they choose to switch lenders but not if they renew with their current lender. As a result, the test increases their switching costs and potentially increases their interest rates. In the counterfactual experiment, we find that about $12 \%$ of new borrowers in our sample would fail the test if they were subject to it at renewal. For these borrowers, the stress test would substantially increase the home bank's market power and lead to a $10 \%$ increase in interest costs.

### 7.1 Frictionless Markets

To better understand the effect of search and switching frictions on the prices that the borrowers pay and the profits that lenders obtain, we compare the equilibrium outcomes in the current environment to environments in which at least one of the market frictions is eliminated. We simulate 100,000 borrowers' new purchase contracts and their subsequent renewal contracts as follows:

1. Using only the sub-sample of new borrowers, draw observable characteristics $\left(x_{i}, h_{i}, N_{i}\right)$ from the empirical distribution.
2. Draw individual shocks $\left(c_{i}, \boldsymbol{\omega}_{i}, \kappa_{i}\right)$ from the estimated distributions.
3. Solve the model and compute the equilibrium outcomes: the lenders' investment incentive $V_{i}$, the home bank's initial offer $p_{i, 0}^{*}$, the borrower's search decision $n_{i}^{*}$, the winning price in the negotiation stage $p_{i}^{*}$, the winning bank's identity, the total cost of financing the mortgage including the search and switching costs, the implied
interest rate, the remaining balance at renewal, the present discounted value of profits expected by the home bank and rival banks.
4. Assume the borrower's characteristics remain the same at renewal. Given the remaining balance and amortization period, repeat steps 2 and 3 to obtain the equilibrium outcomes for the subsequent renewal contract.

Benchmark. Table 7 summarizes the equilibrium outcomes from different counterfactuals. Column (1) shows the results simulated from our benchmark model with both search and switching frictions. An immediate observation is that with all observables (except for outstanding amount and amortization) unchanged, borrowers are less likely to switch due to the higher switching costs. The profits expected by the home bank and the rival banks are higher in the dynamic setting than in the static one, because forward-looking banks take into account future profits.
Removal of Switching Costs. Column (2) describes a counterfactual, where switching costs are eliminated and the only friction is the search costs. Relative to the benchmark dynamic setting, new borrowers at origination are worse off in terms of the interest costs and total cost for financing a mortgage (interest cost plus the search and switching costs incurred). Lenders compete less aggressively because the net continuation value of winning $V$ decreases. Renewers are better off in terms of the total cost, saving an average of $\$ 146$. Assuming borrowers are patient enough, with an annual discount factor of at least 0.87 , the savings in the renewal periods would make up for the increase in total cost at origination $(\$ 134) .{ }^{36}$ On the lenders' side, home banks suffer from the removal of switching costs, while rival banks are better off. In sum, banks' total expected profit from a new borrower is higher without switching costs, but no bank is willing to lower the costs of switching for its own customers because it only benefits rival banks. Therefore, if the banks were to endogenously determine the level of switching costs, they face the prisoner's dilemma. ${ }^{37}$

The static model predicts unambiguous gains for the borrowers, both at origination and at renewal. On average, new borrowers and renewers receive a $0.4 \%$ and $1.6 \%$ reduction in interest costs, respectively, when we remove switching costs. The savings in total costs due

[^23]Table 7: The Effects of Removing Market Frictions: Dynamic Versus Static Predictions

|  | $(1)$ |  | $(2)$ |  | $(3)$ |  | $(4)$ |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: |
|  | Benchmark |  | Search Cost |  | Switching Cost |  | No Frictions |  |  |  |  |  |
|  | Dynamic | Static | Dynamic |  | Static | Dynamic | Static | Dynamic |  |  |  |  |
| Static |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | Panel A: New Purchase Contracts |  |  |  |  |  |  |  |  |  |  |
| Loan size | 253.985 | 253.985 | 253.985 | 253.985 | 253.985 | 253.985 | 253.985 | 253.985 |  |  |  |  |
| Interest cost | 31.842 | 31.790 | 32.049 | 31.662 | 31.553 | 31.089 | 31.717 | 31.052 |  |  |  |  |
| Total cost | 32.120 | 32.084 | 32.253 | 31.878 | 31.755 | 31.303 | 31.717 | 31.052 |  |  |  |  |
| Interest rate | 2.748 | 2.740 | 2.766 | 2.729 | 2.723 | 2.677 | 2.737 | 2.674 |  |  |  |  |
| Profit $_{\text {home }}$ | 0.556 | 0.570 | 0.453 | 0.406 | 0.192 | 0.143 | 0.193 | 0.070 |  |  |  |  |
| Profit $_{\text {rival }}$ | 0.243 | 0.127 | 0.542 | 0.192 | 0.592 | 0.284 | 0.967 | 0.348 |  |  |  |  |
| Profit $_{\text {total }}$ | 0.798 | 0.697 | 0.995 | 0.599 | 0.785 | 0.427 | 1.159 | 0.417 |  |  |  |  |
| $V$ | 0.784 | - | 0.337 | - | 0.270 | - | 0.000 | - |  |  |  |  |
| \# quotes | 2.494 | 2.459 | 2.583 | 2.547 | 6.583 | 6.583 | 6.583 | 6.583 |  |  |  |  |
| Pr(switch) | 0.286 | 0.278 | 0.405 | 0.402 | 0.692 | 0.684 | 0.831 | 0.831 |  |  |  |  |


|  | Panel B: Renewal Contracts |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Loan size | 214.037 | 214.019 | 214.111 | 213.973 | 213.934 | 213.768 | 213.993 | 213.755 |  |
| Interest cost | 26.090 | 26.072 | 26.050 | 25.653 | 25.708 | 25.279 | 25.706 | 25.039 |  |
| Total cost | 26.398 | 26.390 | 26.251 | 25.863 | 26.022 | 25.600 | 25.706 | 25.039 |  |
| Interest rate | 2.756 | 2.753 | 2.751 | 2.709 | 2.716 | 2.668 | 2.715 | 2.643 |  |
| Profit $_{\text {home }}$ | 0.815 | 0.832 | 0.435 | 0.389 | 0.348 | 0.318 | 0.172 | 0.069 |  |
| Profit $_{\text {rival }}$ | 0.158 | 0.065 | 0.485 | 0.194 | 0.429 | 0.178 | 0.863 | 0.348 |  |
| Profit $_{\text {total }}$ | 0.973 | 0.896 | 0.920 | 0.583 | 0.777 | 0.497 | 1.034 | 0.417 |  |
| $V$ | 0.801 | - | 0.329 | - | 0.290 | - | 0.000 | - |  |
| \# quotes | 2.528 | 2.531 | 2.604 | 2.602 | 6.583 | 6.583 | 6.583 | 6.583 |  |
| $\operatorname{Pr}$ (switch) | 0.153 | 0.149 | 0.406 | 0.406 | 0.446 | 0.437 | 0.830 | 0.830 |  |

Note: We simulate 100,000 purchase contracts using the estimated dynamic model by randomly drawing observable characteristics from the sub-sample of new borrowers. From these new purchase contracts, we obtain the average loan size (outstanding amount), interest cost, total cost (interest cost plus search and switching costs incurred), present discounted value of profits expected by the home bank, rival banks, and their sum, investment incentive $(V)$, number of quotes, and switching probability. Assume all these purchase contracts are renewed after 5 years with all observable characteristics remaining the same but smaller outstanding balance and shorter amortization. We then simulate the equilibrium outcomes for these subsequent renewal contracts. Repeat the simulation experiment using the estimated static model. Column (2) shows the simulated outcomes from models where search cost is the only friction. Column (3) is obtained by simulating contracts from models where switching cost is the only friction. Column (4) assumes neither search cost nor switching cost is present. All monetary values are measured in $\$ 1,000$.
to the elimination of switching frictions are even bigger. The static model overestimates the benefit of eliminating switching frictions on borrowers, because it ignores the fact that lenders compete less aggressively for a borrower who might easily switch to a rival
bank in future periods. Predictions from the static model would support policies aimed at promoting competition through reducing switching costs. However, the dynamic model suggests that such policies may not achieve the intended goal.

Removal of Search Costs. Column (3) describes the counterfactual world, where search costs are eliminated and only switching costs are present. In the simulation, borrowers no longer receive an initial home-bank quote. Rather, they search all the available lenders and on average obtain four more quotes than the benchmark sample. The benefit of the extra free quotes are significant. In a dynamic world, borrowers enjoy $1.1 \%$ and $1.4 \%$ decreases in total costs at origination and at renewal, respectively. The static model predicts even higher savings in total costs: $2.4 \%$ at origination and $3.0 \%$ at renewal. ${ }^{38}$ The static model again overestimates the benefit of removing search costs because it ignores the reduction in lenders' investment incentives.

Removal of Both Frictions. Column (4) describes the counterfactual world, where both switching costs and search costs are eliminated. In this case, the lenders' net continuation value of winning becomes zero. In a dynamic world, new borrowers' total costs on average decrease by $1.3 \%$. Renewers benefit even more, paying $2.6 \%$ lower total costs than the benchmark sample. The static model predicts $3.2 \%$ and $5.1 \%$ reductions in total costs at origination and at renewal, respectively.

In summary, the static model overestimates the benefit of removing search and switching costs because it ignores the changes in lenders' investment incentives. In the dynamic world, removing the switching costs alone - depending on how patient borrowers are could potentially disadvantage the new borrowers in terms of the discounted total costs over the entire mortgage life. Removing the search costs, however, is much more helpful because it directly promotes competition among more lenders and results in lower prices.

### 7.2 Merger Analysis: Taking Dynamics into Account

This section highlights the importance of modeling lenders' dynamic pricing strategies when conducting policy analysis. We focus on mergers. Due to search costs, an average borrower only obtains 2.5 quotes in a market where there are on average 6.6 lenders. This means that for most borrowers their search decisions and choice sets are unaffected by a merger. The impact of the merger on prices is indirectly reflected in changes in the

[^24]lenders' investment incentives and may not be noticeable. In order to best compare the merger analysis in a static versus dynamic setting, we therefore focus on the sub-sample of borrowers who would be most affected by a merger. We investigate the effect of a two-bank merger on borrowers who obtain multiple quotes in three-bank markets.

### 7.2.1 Ex Ante Merger Simulation

We simulate 100,000 contracts from the sub-sample of borrowers in three-bank markets using the estimated models under both status quo and counterfactual market structures, holding fixed the realizations of all random shocks. We abstract from the cost-efficiency effects that might come from the merger and assume that the merged entity's idiosyncratic cost realizations are just random draws from the two merging parties' idiosyncratic cost shocks. In the simulated samples, we drop all borrowers who do not search for multiple quotes under the status quo market structures. Table 8 summarizes the equilibrium outcomes pre- and post-merger in both dynamic and static models.

Pre-merger, borrowers on average obtain 2.4 quotes. Post-merger, most of the borrowers would still search and obtain 2 quotes. The dynamic model predicts that new borrowers and renewers see a $0.3 \%$ and $0.4 \%$ increase in interest costs post-merger, respectively. The static model predicts a $0.4 \%$ and $0.6 \%$ increase, respectively. The static merger simulation overestimates the merger impact because it ignores the fact that lenders' investment incentive increases by $8 \%$ for new purchase contracts, and by $7 \%$ for renewal contracts. Lenders expect less competition in future renewal periods and hence compete more aggressively ex ante to attract customers. The higher investment incentive dampens the size of the merger impact predicted by the static model.

### 7.2.2 Retrospective Merger Evaluation

Now consider a different case in which a merger has already happened. A researcher wants to perform a retrospective evaluation to investigate the price impact. Suppose the researcher ignores the pricing dynamics and mistakenly believes that lenders price renewal contracts in the same way as they do for new borrowers. The researcher may conduct the retrospective merger evaluation using only the new borrowers' contracts, which can often be accessed more easily. See, for example, Allen et al. (2014a).

A retrospective merger evaluation based on new borrowers (panel A of Table 8) would estimate a $0.3 \%$ increase in interest costs post-merger. It underestimates the true merger impact, because it ignores the fact that renewers suffer more from having one less available
lender (renewers' interest costs on average increase by $0.4 \%$ ). After the merger, finding a lender with a low enough cost to switch to becomes much harder. Due to higher switching costs, renewers are more likely to be retained by their home bank and therefore pay relatively high prices.

Table 8: The Impact of a Merger

|  | Dynamic |  | Static |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Before | After | Before | After |
| Outstanding amount | 216.721 | 216.721 | 216.693 | 216.693 |
| Interest cost | 27.173 | 27.248 | 27.109 | 27.227 |
| Investment incentive | 0.720 | 0.779 | - | - |
| \# quotes | 2.446 | 1.989 | 2.425 | 1.989 |
| Pr(switch) | 0.386 | 0.312 | 0.374 | 0.304 |


|  | Panel B: Renewal Contracts |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Outstanding amount | 159.884 | 159.884 | 159.884 | 159.884 |
| Interest cost | 19.746 | 19.826 | 19.733 | 19.859 |
| Investment incentive | 0.697 | 0.745 | - | - |
| \# quotes | 2.452 | 1.990 | 2.476 | 1.981 |
| Pr(switch) | 0.163 | 0.120 | 0.158 | 0.115 |

Note: From the sub-sample of borrowers living in markets where only 3 banks are available, we simulate 100,000 contracts under both the current market structure and the counterfactual market structure after a merger. We keep only borrowers obtaining multiple quotes before the hypothetical merger (about $63 \%$ of the sample). All monetary values are measured in $\$ 1,000$.

### 7.3 The Impact of Mortgage Stress Testing

Since 2008, mortgage rates in Canada have been declining and reached record lows in 2016. Low interest rates stimulated housing market activities, with home buyers taking out larger mortgage loans than they otherwise could afford. Worried about large-scale mortgage default, the Department of Finance and the Office of the Superintendent of Financial Institutions (OSFI) introduced a series of four stress tests between 2010 and 2018 to improve underwriting standards and ensure that borrowers could meet their mortgagepayment obligations in case of rising rates. ${ }^{39}$

[^25]One of the debt-to-income constraints imposed by the stress test is that borrowers' gross debt-servicing ratio (GDS) cannot exceed $39 \%$. GDS is defined as follows:

$$
\text { GDS } \equiv \frac{\text { Mortgage Payment }+ \text { Property Tax }+ \text { Heating Cost }+50 \% \text { of Condo Fee }}{\text { Gross Income }} .
$$

The mortgage payment in the formula, however, is not the actual payment that the borrower would make according to the negotiated contract rate. Rather, it is a hypothetical mortgage payment calculated using a 'qualifying' rate, which is approximately 200 bps more than the median contract rate. ${ }^{40}$

All four stress tests are applied to borrowers at origination. For the latest stress tests, introduced in 2018, uninsured borrowers are even subject to it at renewal should they switch to a different bank. ${ }^{41}$ In a speech on the stress test, OSFI emphasized that it does "not want borrowers who do not meet the increased underwriting standards to become the focus of price competition among lenders." ${ }^{42}$ As we will show in the simulation experiment, this leads to some unintended consequences: (1) home banks enjoy a much greater incumbency advantage, and (2) unqualified renewers suffer from higher switching costs and therefore higher interest rates.

In the counterfactual experiment, we use only a sub-sample of new borrowers and show the impact of the stress test on these borrowers if they suddenly became subject to the stress test at renewal. At renewal, we work out the borrowers' remaining balances and remaining amortization periods and assume that all of the other observable borrower characteristics stay the same. Using the borrowers' reported income and the qualifying rate $(5.19 \%)$, we calculate the the maximum loan amount for which they could qualify. ${ }^{43}$

If a borrower's remaining balance at renewal is smaller than the qualified amount, she can pass the stress test, and the equilibrium outcomes of this borrower are unaffected. However, if the remaining balance at renewal exceeds the qualified amount, the borrower fails the stress test and will need to pay down the excess balance in order to switch lenders. We interpret this as an exogenous one-time increase in switching costs faced by unqualified

[^26]renewers. We approximate the switching cost increment by the cost required to pass the stress test. More specifically, we assume that unqualified borrowers can borrow from private lenders at an annual interest rate of $10 \% .{ }^{44}$ The switching cost increase can then be approximated by the cost of borrowing the excess amount from the private lenders. ${ }^{45}$

Table 9: The Impact of Mortgage Stress Testing

|  | All Renewers |  | Unqualified Renewers |  |
| :--- | :---: | :---: | :---: | :---: |
| Outstanding amount | No Test | Test | No Test | Test |
| Qualified amount | 213.409 | 213.409 | 307.337 | 307.337 |
| Income | 321.109 | 321.109 | 270.819 | 270.819 |
| Interest cost | 24.469 | 74.469 | 65.915 | 65.915 |
| Total cost | 26.015 | 26.448 | 36.814 | 40.527 |
| Interest rate | 2.756 | 26.737 | 37.250 | 40.810 |
| Profit | 2.785 | 2.695 | 2.947 |  |
| Profit | 0.814 | 1.227 | 1.068 | 4.610 |
| \# quotes | 0.157 | 0.146 | 0.250 | 0.158 |
| Pr(switch) | 2.526 | 2.526 | 2.873 | 2.873 |
| Switching cost | 0.153 | 0.135 | 0.177 | 0.021 |
| Obs | 0.693 | 1.119 | 1.018 | 4.670 |

Note: We draw 100,000 mortgage contracts with replacement from the sub-sample of new borrowers and assume their contracts are renewed after 5 years with all observable characteristics remaining the same but smaller outstanding balance and shorter amortization. We then simulate the equilibrium outcomes for the subsequent renewal contracts both in the regular case and in the case when borrowers are subject to stress test. The last two columns focus on the subset of borrowers who would fail the stress test. All monetary values are measured in $\$ 1,000$.

Table 9 summarizes the impact of the stress test on the renewal contracts. In the simulated sample of all borrowers at renewal, they are largely unaffected by the stress test. Most of the renewers have their remaining mortgage balance well below the qualified amount. On average, renewers are slightly less likely to switch and experience a 3 bps increase in interest rates due to the stress test.

[^27]However, the impact on unqualified renewers is much more significant. About $12 \%$ of borrowers would fail the stress test at renewal. Their remaining balance exceeds the maximum qualified amount by $\$ 36,518$. These affected renewers need to incur more than four times their original switching costs to pass the stress test and switch to rival banks. As a result, home banks are able to retain about $98 \%$ of the affected renewers and charge higher prices. The unqualified renewers on average experience a 25 bps increase in interest rates and a $10 \%$ increase in interest costs. ${ }^{46}$

Note that the current stress test only applies to uninsured renewers, while the borrowers in our sample are all insured. However, we expect the impact on uninsured renewers would be even more significant. As pointed out by Clark and Li (2019), the share of high loan-to-income mortgages in the uninsured sector is higher than the share in the insured sector. Therefore uninsured renewers are more likely to be constrained by the stress tests.

## 8 Conclusion

We develop a framework for investigating dynamic competition in negotiated-price markets. Using contract level data for the Canadian mortgage market, we provide evidence of an "invest-then-harvest" pricing pattern: lenders offer relatively low interest rates to attract new borrowers and poach rivals' existing customers, and then at renewal in some instances, charge interest rates which can be higher than what may be available through other lenders in the marketplace. We build a dynamic model of price negotiation with search and switching frictions to capture the key market features.

Our counterfactual experiments highlight the importance of understanding lenders' dynamic pricing strategies in policy evaluations. A static model overestimates the benefit of eliminating search and switching costs because it ignores the changes in lenders' investment incentives and pricing dynamics. For the same reasons, static merger analyses also yield biased results: (i) static merger simulation overestimates the merger impact, and (ii) retrospective merger evaluation using only purchase contracts underestimates the merger impact on renewals. In our experiment that simulates the impact of mortgage stress tests, we find $12 \%$ of new borrowers in our sample would fail if they were subject to it at renewal. For these unqualified borrowers, the stress test would substantially increase the home bank's market power and lead to a $10 \%$ increase in interest costs.

[^28]
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## A Sample Mortgage Renewal Letter

## Your mortgage is up for renewal on November 10, 2019

Date: October 4, 2019
Your mortgage number:
Property address:

Questions about your Mortga
Renewal Agreement?
Call us at
Visit our website at

Thank you for choosing for your mortgage. Your current mortgage term is coming to an end soon and it's time for you to select a renewal term. This Mortgage Renewal Agreement contains our current posted interest rates for the terms we offer but we have special offers available if you contact us.

Call your branch today to set up an appointment to renew your mortgage and receive expert advice and competitive rates. If you prefer, you can renew by calling

We are pleased to help you find the mortgage solution that best meets your specific needs.
P.S. Be sure to call us to renew your mortgage before the renewal date to avoid your mortgage being automatically renewed into a 6 month fixed rate closed term.

## Your current mortgage details

| Maturity Date / New Term Start Date | Nov 10, 2019 |
| :---: | :---: |
| Your mortgage term and prepayment type | 5 Year Closed |
| Interest Rate | 2.8900\% |
| Rate Type | Fixed |
| Payment Frequency | Bi-Weekly |
| Principal and Interest Payment |  |
| Property Tax |  |
| Your Total Payment ${ }^{4}$ |  |
| Estimated Principal Balance at Maturity Date ${ }^{1}$ |  |
| Mortgage Protection Premium | Uninsured |
| Time remaining to payoff your mortgage (Amortization period) | 21 years, 7 months |

${ }^{1}$ Accrued interest from the last regular payment date to the maturity date would be due if you paid your mortgage in full on the maturity date.
The renewal options outlined in this Mortgage Renewal Agreement are based on your existing payment frequency and assuming all payments that are due up to and including the maturity date are paid as scheduled.

1 - Please indicate which term and mortgage solution option you are accepting by signing your initial in the appropriate area indicated and return your signed Mortgage Renewal Agreement to your branch.

Your New Term Start Date will begin on the current maturity date. Based on your preference selected below, interest will be calculated and charged from this date on and your new term will end on the New Maturity Date.

Fixed Interest Rate Renewal Options

| New Term | New Maturity Date | Annual <br> Interest <br> Rate $^{2} /$ APR $^{3}$ | New Principal and Interest Payment | Property Tax | New Total Bi-Weekly Payment ${ }^{4}$ | Total P \& I <br> Payments over the Term | Total cost of borrowing over the Term | Initial your choice here |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6 Month Flexible ${ }^{11}$ | May 10, 2020 | 4.7500\% |  |  |  |  |  |  |
| 1 Year Closed | Nov 10, 2020 | 3.6400\% |  |  |  |  |  |  |
| 2 Year Closed | Nov 10, 2021 | 3.7400\% |  |  |  |  |  |  |
| 3 Year Closed | Nov 10, 2022 | 4.3900\% |  |  |  |  |  |  |
| 4 Year Closed | Nov 10, 2023 | 4.5900\% |  |  |  |  |  |  |
| 5 Year Closed | Nov 10, 2024 | 5.1900\% |  |  |  |  |  |  |
| 7 Year Closed | Nov 10, 2026 | 5.6900\% |  |  |  |  |  |  |
| 10 Year Closed | Nov 10, 2029 | 6.1900\% |  |  |  |  |  |  |
| 6 Month Open ${ }^{11}$ | May 10, 2020 | 7.2500\% |  |  |  |  |  |  |
| 1 Year Open ${ }^{11}$ | Nov 10, 2020 | 7.2500\% |  |  |  |  |  |  |

## B Likelihood Function

Consider three different types of borrowers and the respective likelihood functions: (1) switching borrowers, (2) loyal borrowers obtaining multiple quotes, and (3) loyal borrowers accepting the home banks' free initial quote. The likelihood function depends on borrowers' search probabilities, $\operatorname{Pr}\left(n_{i}=l\right)$, as set out in equation (10). For simplicity of exposition, assume in equilibrium that the optimal initial offer is high enough, such that the borrower searches $l$ banks with positive probability, $\forall l=2,3, \cdots, N$.

## Case 1: Switching Borrowers

Let $B_{i}$ denote the winning bank and $P_{i}$ denote the winning price. The probability of observing a borrower switching to a rival provider $j$ and paying a price lower than $p$ is

$$
\begin{aligned}
& \operatorname{Pr}\left(P_{i} \leq p, B_{i}=j, B_{i} \neq h\right) \\
& =\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \operatorname{Pr}\left(P_{i} \leq p, B_{i}=j, B_{i} \neq h \mid n_{i}=l\right) \\
& =\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \operatorname{Pr}\left(B_{i}=j, B_{i} \neq h \mid n_{i}=l\right) \operatorname{Pr}\left(P_{i} \leq p \mid n_{i}=l, B_{i}=j, B_{i} \neq h\right) \\
& =\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \frac{1-\operatorname{Pr}\left(\omega_{h}-\lambda \leq \omega_{-h} \mid n_{i}=l\right)}{l-1} \frac{l-1}{N-1} \operatorname{Pr}\left(P_{i} \leq p \mid n_{i}=l, B_{i}=j, B_{i} \neq h\right)
\end{aligned}
$$

where the probability of a borrower paying a price lower than $p$ conditional on her searching $l$ lenders and switching to lender j is given by

$$
\begin{aligned}
& \operatorname{Pr}\left(P_{i} \leq p \mid n_{i}=l, B_{i}=j, B_{i} \neq h\right) \\
& =\operatorname{Pr}\left(C-\delta V+\omega_{(2)} \leq p \mid n_{i}=l, \omega_{(1)}=\omega_{j}, j \neq h\right) \\
& =\int_{-\infty}^{\infty} \operatorname{Pr}\left(\omega_{(2)} \leq p-(c-\delta V) \mid n_{i}=l, \omega_{(1)}=\omega_{j}, j \neq h\right) d F(c) \\
& =\int_{-\infty}^{\infty}\left\{\left(1-\frac{1}{\operatorname{Pr}}\right) G_{(1) \mid n_{i}=l}(p-c+\delta V)+\left(\frac{1}{P r_{j \mid n_{i}=l}}\right) G_{-j \mid n_{i}=l}(p-c+\delta V)\right\} d F(c) .
\end{aligned}
$$

$\operatorname{Pr} r_{j \mid n_{i}=l} \equiv \operatorname{Pr}\left(\omega_{j} \leq \omega_{-j} \mid n_{i}=l\right)$ is the probability that bank $j$ wins the auction conditional on $j$ being in the $l$-bank choice set, where $\omega_{-j} \equiv \min \left\{\min _{k \in n_{i} \backslash\{j, h\}}\left\{\omega_{k}\right\}, \omega_{h}-\lambda\right\}$. Recall that $\omega_{(k)}^{t}$ denotes the $k^{t h}$ order statistic among $\left(\omega_{h^{t}}-\lambda, \omega_{1}, \omega_{2}, \cdots, \omega_{n_{i}-1}\right) . G_{(1) \mid n_{i}=l}$ and $G_{-j \mid n_{i}=l}$ are the CDFs of $\omega_{(1)}$ and $\omega_{-j}$, respectively. The last equation follows from the
property of the T1EV distributed idiosyncratic cost shocks. See Brannman and Froeb (2000) for a more detailed discussion.

The first order derivative of $\operatorname{Pr}\left(P_{i} \leq p, B_{i}=j, B_{i} \neq h\right)$ with respect to $p$ yields the likelihood contribution of a switching borrower $i$ :

$$
\begin{aligned}
& l_{i}\left(p, B_{i}=j, B_{i} \neq h\right) \\
& =\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \frac{1-P r_{h \mid n_{i}=l}}{N-1} \\
& \quad \times \int_{-\infty}^{\infty}\left\{\left(1-\frac{1}{P r_{j \mid n_{i}=l}}\right) g_{(1) \mid n_{i}=l}(p-c+\delta V)+\left(\frac{1}{P r_{j \mid n_{i}=l}}\right) g_{-j \mid n_{i}=l}(p-c+\delta V)\right\} d F(c) .
\end{aligned}
$$

## Case 2: Loyal Borrowers Holding Auctions

The probability of observing a borrower who obtains multiple quotes but chooses to stay with her home bank and pays a price lower than $p$ is

$$
\begin{aligned}
& \operatorname{Pr}\left(P_{i} \leq p, B_{i}=h, n_{i}>1\right) \\
& =\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \operatorname{Pr}\left(P_{i} \leq p, B_{i}=h \mid n_{i}=l\right) \\
& =\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \operatorname{Pr}\left(B_{i}=h \mid n_{i}=l\right) \operatorname{Pr}\left(P_{i} \leq p \mid n_{i}=l, B_{i}=h\right),
\end{aligned}
$$

and the corresponding likelihood contribution is

$$
\begin{aligned}
& l_{i}\left(p, B_{i}=h, n_{i}>1\right) \\
& =\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) P r_{h \mid n_{i}=l} \\
& \quad \times \int_{-\infty}^{\infty}\left\{\left(1-\frac{1}{\operatorname{Pr}}\right) g_{(1) \mid n_{i}=l}(p-c+\delta V)+\left(\frac{1}{P r_{h \mid n_{i}=l}}\right) g_{-h \mid n_{i}=l}(p-c+\delta V)\right\} d F(c)
\end{aligned}
$$

## Case 3: Loyal Borrowers Accepting Initial Quotes

The probability of observing a borrower who accepts her home bank's free initial quote and pays a price lower than $p$ is

$$
\begin{aligned}
& \operatorname{Pr}\left(P_{i} \leq p, B_{i}=h, n_{i}=1\right) \\
& =\operatorname{Pr}\left(n_{i}=1\right) \operatorname{Pr}\left(P_{i} \leq p \mid n_{i}=1\right) \\
& =\left(1-H\left(\bar{\kappa}_{2}^{*}\right)\right) \operatorname{Pr}\left(\bar{\kappa}_{2}^{*}+\lambda+C-\delta V+E\left[\omega_{(2)}^{t} \mid n^{t}=2\right] \leq p\right) \\
& =\left(1-H\left(\bar{\kappa}_{2}^{*}\right)\right) F\left(p-\left(\bar{\kappa}_{2}^{*}+\lambda-\delta V+E\left[\omega_{(2)}^{t} \mid n^{t}=2\right]\right)\right),
\end{aligned}
$$

and the corresponding likelihood contribution is

$$
\begin{aligned}
& l_{i}\left(p, B_{i}=h, n_{i}=1\right) \\
& =\left(1-H\left(\bar{\kappa}_{2}^{*}\right)\right) f\left(p-\left(\bar{\kappa}_{2}^{*}+\lambda-\delta V+E\left[\omega_{(2)}^{t} \mid n^{t}=2\right]\right)\right) .
\end{aligned}
$$

## Likelihood function

Conditional on the home-bank identity $h$ and the winning bank identity $b$, the borrower's likelihood contribution is given by

$$
\begin{aligned}
& l_{i}(p, h, h)=\left\{\begin{array}{ll}
\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \frac{1-P r_{h \mid n_{i}=l}}{N-1} & \\
\times \int_{-\infty}^{\infty}\left\{\left(1-\frac{1}{P r_{b \mid n_{i}=l}}\right) g_{(1) \mid n_{i}=l}(p-c+\delta V)\right. & b \neq h, \\
& \left.+\left(\frac{1}{P r_{b \mid n_{i}=l}}\right) g_{-b \mid n_{i}=l}(p-c+\delta V)\right\} d F(c) \\
& \\
\sum_{l=2}^{N} \operatorname{Pr}\left(n_{i}=l\right) \operatorname{Pr}_{h \mid n_{i}=l} \\
& \times \int_{-\infty}^{\infty}\left\{\left(1-\frac{1}{P r_{h \mid n_{i}=l}}\right) g_{(1) \mid n_{i}=l}(p-c+\delta V)\right.
\end{array} \quad b=h .\right. \\
& \begin{array}{c}
\left.+\left(\frac{1}{P r_{h \mid n_{i}=l}}\right) g_{-h \mid n_{i}=l}(p-c+\delta V)\right\} d F(c) \\
\left.H\left(\bar{\kappa}_{2}^{*}\right)\right) f\left(p-\left(\bar{\kappa}_{2}^{*}+\lambda-\delta V+E\left[\omega_{(2)}^{t} \mid n^{t}=2\right]\right)\right)
\end{array}
\end{aligned}
$$


[^0]:    Suggested Citation: Allen, Jason; Li, Shaoteng (2020) : Dynamic competition in negotiated price markets, Bank of Canada Staff Working Paper, No. 2020-22, Bank of Canada, Ottawa, https://doi.org/10.34989/swp-2020-22

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[^2]:    ${ }^{1} \mathrm{~A}$ switching cost is incurred every time a customer switches providers. Switching costs may come from transaction costs related to switching providers, brand loyalty, psychological cost of ending a current relationship, etc. See Klemperer (1995) for a detailed discussion.

[^3]:    ${ }^{2}$ The home bank for a new borrower is one with a pre-existing relationship, e.g. credit card. For a renewer, the home bank is the previous period mortgage provider.

[^4]:    ${ }^{3}$ For instance, the qualifying rate used in mortgage stress testing exogenously shifts borrowers' switching costs at renewal and satisfies the exclusion restriction assumption. We discuss stress testing in detail in section 7.3. See also Clark and Li (2019).
    ${ }^{4}$ This is consistent with MacKay and Remer (2019), who consider a hypothetical merger in a postedprice (gasoline) market. They find that a static model overestimates the post-merger price compared to a dynamic model that takes into account consumer inertia and firms' investment incentive.

[^5]:    ${ }^{5}$ Theory mainly focuses on the effects of switching costs where forward-looking firms compete repeatedly and provides conditions under which switching costs are pro- or anti-competitive (c.f. Von Weizsäcker (1984), Klemperer (1987), Farrell and Shapiro (1988), Beggs and Klemperer (1992), Padilla (1995), Chen (1997), Somaini and Einav (2013), Pearcy (2016), and Cabral (2016).

[^6]:    ${ }^{6}$ Brokers intermediate about one third of mortgages over our sample period. See Allen et al. (2014b) for a detailed analysis of brokers in the Canadian market and Robles-Garcia (2019) for the UK market.
    ${ }^{7}$ This is much lower than in Allen et al. (2019). The reason is that lenders now advertise two posted prices - their standard posted prices used to calculate prepayment fees and discourage early refinancing, and 'specials'. The 'standard' posted rate represents a price ceiling, since it is illegal to charge interest rates higher than one's posted rates. Specials tend to be targeted at first-time home buyers and switchers.

[^7]:    ${ }^{8}$ Banks impose significant penalties for refinancing before the end of the term. Refinancing is uncommon in Canada, unlike in the US. This is mostly because of the relatively short term of the mortgage contract (5 years versus 30), which makes the benefits from refinancing, that might come from lower interest rates relative to the large penalties imposed, less attractive compared to simply waiting for renewal.
    ${ }^{9}$ This feature also introduces a number of potential risks for borrowers. First is renewal risk. A borrower's life situation might have drastically changed in five years, and banks might simply not lend to a renewer. See, for example, DeFusco and Mondragon (2019). Second is interest-rate risk. With respect to renewal risk, this is largely mitigated by mortgage insurance. Borrowers with an LTV ratio above $80 \%$ at origination are mandated to buy mortgage insurance backed by the government. Banks must renew even in the case where insured mortgages go underwater. Mortgages with an LTV below $80 \%$ at origination have substantial equity, and renew risk is minimal, especially since Canada has experienced positive house price growth since the early 2000s. With respect to interest-rate risk, households are exposed and aware that they might face a very different rate environment at renewal.
    ${ }^{10} \mathrm{~A}$ further benefit of fixed renegotiation is that we can better interpret consumer inertia as either coming from search costs or switching costs and not from inattention (c.f. Andersen et al. (2017) and Agarwal et al. (2015).)
    ${ }^{11}$ Loan originator and loan servicer are the same in Canada. By law, federally regulated lenders must provide borrowers with renewal statements 21 days before the mortgage maturity dates. See Appendix A for an example of a renewal letter.

[^8]:    ${ }^{12}$ The monetary costs of switching lenders include the appraisal fee to verify a property's value, an assignment fee to transfer the mortgage from the home bank to the new provider, and sometimes a discharge fee, as well as legal fees if the mortgage is a collateral-charge product. Psychological costs also seem to be relevant. According to the 2018 Mortgage Consumer Survey conducted by the Canada Mortgage and Housing Corporation, other than rates, the top reason for not switching is the value placed on a pre-existing relationship.
    ${ }^{13}$ TransUnion has monthly reports for over 35 million individuals. This is approximately 13 TB of data. To construct our dataset, we search the entirety of the population using PySpark for anyone with a mortgage. We capture their monthly mortgage payments and aggregates for other debt as well as information about age, home location, and credit score. The raw sample is approximately 50 GB .
    ${ }^{14}$ The FSA is the first three digits of a postal code. The median population of an FSA is 18,000 .
    ${ }^{15}$ We observe both the monthly required payment and the actual payment made. Borrowers are allowed to prepay a certain amount every month. Therefore, the actual payment might exceed what is required. Also, mortgage insurance is mandatory for mortgages with LTV ratios greater than $80 \%$.
    ${ }^{16}$ Some borrowers have multiple banking relationships prior to obtaining a mortgage. If the borrower chooses such a bank, we assume that the chosen bank is the borrower's home bank.

[^9]:    ${ }^{17}$ Allen et al. (2019) focus on newly originated contracts only. Our study requires observing renewers' contract information and, crucially, their previous lender and switching behaviors.
    ${ }^{18}$ The share of uninsured mortgages during our sample period is around two thirds. We do not model the choice of broker usage because we do not have the necessary information to interpret the interest rate obtained through the broker channel. For example, for each contract we need to observe (i) the broker's identity, (ii) the set of lenders searched by the broker, and (iii) the baseline interest rate and compensation scheme specified by each lender. The third point is important because brokers might not work for the best interest of the borrower and might choose high-commission products over low-interest ones. In addition to the data requirement, we need to model the way in which lenders compete in the broker channel. We leave this for future work.

[^10]:    ${ }^{19}$ Honka (2014) finds that consumers in US auto insurance markets on average obtain only three quotes, while the number of insurance companies is more than ten.

[^11]:    ${ }^{20}$ This assumption simplifies home banks' problem of solving the optimal initial quote and is also reasonable in our setting. One might think that the borrower must be able to recall the offer specified in her renewal letter. However, in reality, banks often offer the highest that they can charge (the standard posted rates) in the renewal letters. See Appendix A for an example. These quotes are not worth recalling. In such case, borrowers can simply call their home banks asking for quotes better than the posted rates and the banks would propose new offers. Therefore, one should think of the home banks" "initial" quotes as these new offers rather than the posted rates in renewal letters. It is reasonable to assume that these offers cannot be recalled if the borrowers do not accept them and go through the paperwork.

[^12]:    ${ }^{21}$ We assume symmetric lenders; $n^{t}$ refers to both the choice set and number of lenders in this set.

[^13]:    ${ }^{22}$ Individual loan officers have substantial discretion to offer discounts off the posted price. Larger discounts typically reduce the commission earned by loan officers; see KPMG (2008).

[^14]:    ${ }^{23}$ The assumption of $i . i . d$. idiosyncratic cost draws greatly simplifies the model. It allows us to focus on the pricing dynamics induced by search and switching costs rather than the potentially minor asymmetry in cost structure. We discuss this in detail in subsection 3.3. Given the similarity in funding sources across the large Canadian banks, this assumption seems reasonable. In general, the symmetric cost assumption is applicable in markets where consumers obtain quotes from fairly comparable firms.
    ${ }^{24}$ In the terminal period, the continuation values are 0 . In each of the prior periods, a specific bank

[^15]:    ${ }^{25}$ The equilibrium price depends on the search intensity through the number of idiosyncratic cost draws.
    ${ }^{26} \mathrm{We}$ assume that the borrower qualifies for a mortgage at every lender. Therefore, the borrower searches only for a lower price rather than to qualify. In the empirical analysis, we restrict our attention to only mortgages insured by the government. It is reasonable to assume that borrowers never get rejected, since the government bears all the default risk. See Agarwal et al. (2017) for a model that takes into account the interaction between searching and screening in the presence of asymmetric information. Borrowers' mortgage applications might get rejected, and they are forced to search more for approval.

[^16]:    ${ }^{27}$ Condition (9) must be satisfied for $l=2$, so that given the optimal initial quote the borrower's search probabilities are well defined and the same as those being used in the home bank's optimization problem (11). Specifically, the condition $\bar{\kappa}_{2}^{t *}>\kappa_{3}^{t}$ must hold.

[^17]:    ${ }^{28}$ It is straightforward to allow for exogenous trends in these model primitives.

[^18]:    ${ }^{29} \mathrm{An}$ example of $z_{i}$ would be the qualifying rate for renewers under the mortgage stress tests, which exogenously influences the switching cost without changing the other model primitives. We discuss the stress tests in more detail in the counterfactual experiments.

[^19]:    ${ }^{30}$ See Diggle and Hall (1993) for a more detailed discussion. Krasnokutskaya (2011) applies the deconvolution methods in identifying auction models with unobserved heterogeneity.

[^20]:    ${ }^{31}$ A location is defined by the first digit of a borrower's postal code. Quebec and Ontario are split into 3 and 5 regions, respectively. Other provinces have a single region.
    ${ }^{32} \gamma$ is the Euler constant, and the idiosyncratic cost distribution in this specification has mean 0.
    ${ }^{33}$ Otherwise, the outstanding amount becomes a payoff-relevant state variable. Lenders' net continuation value of winning will depend on their expectation on the outstanding balance at renewal and hence depend on their belief regarding the winning bank's identity and winning bid. This would result in multiple equilibria in the negotiation stage. This problem will often be negligible because the difference in expected outstanding balance after 5 years due to different interest rates is small.

[^21]:    ${ }^{34}$ The standard deviation of a T1EV distributed random variable is $\sigma_{\omega} \pi / \sqrt{6}$.

[^22]:    ${ }^{35}$ The new provider would handle the mortgage-transfer process on behalf of the borrower.

[^23]:    ${ }^{36}$ The consumer discount factors estimated from other empirical studies are often much lower. For example, Dubé et al. (2014) use survey data on Blu-ray player adoption and estimate an average annual discount factor of 0.7 . See Frederick et al. (2002) and Yao et al. (2012) for a more detailed review on consumer discount rates.
    ${ }^{37} \mathrm{~A}$ word on collateral charge mortgages, which have recently increased in popularity. This type of mortgage is readvanceable, meaning that banks can lend more after closing without the need to refinance. This increases switching costs, however, since they are non-transferable and hence borrowers need to incur legal fees (around $\$ 1,500$ ) to switch lenders. Our model suggests that this is ultimately unprofitable, since future rents are competed away at origination.

[^24]:    ${ }^{38}$ Allen et al. (2019) estimate that search frictions lead to a loss in consumer surplus equivalent to $2 \%$ of the interest costs. The effect is smaller because they assume borrowers obtain quotes from all available lenders once they decide to search. Eliminating search frictions does not help searchers obtain more quotes.

[^25]:    ${ }^{39}$ See Clark and Li (2019) for a more detailed discussion of the mortgage stress tests and Allen et al. (2017) for a discussion of the effectiveness of macroprudential policies in Canada.

[^26]:    ${ }^{40}$ The qualifying rate is determined by the mode of the big 6 banks' posted rates on 5 -year fixed-rate mortgages. For insured mortgages the qualifying rate is just the modal 5 -year posted rate. For uninsured mortgages, the qualifying rate is the greater of the modal rate and the contract rate plus 200 bps . As of January 2020, the 5 -year modal rate is $5.19 \%$, about 220 bps higher than the average contract rate.
    ${ }^{41}$ Insured borrowers do not face a stress test at renewal because the loans are free of default risk from the point of view of the lender.
    ${ }^{42}$ See https://www.osfi-bsif.gc.ca/Eng/osfi-bsif/med/sp-ds/Pages/CR20190205.aspx.
    ${ }^{43}$ Assume the GDS constraint holds with equality and the other maintenance costs in the formula amount to $1 \%$ of the initial loan size: the maximum hypothetical mortgage payment is obtained. Along with the qualifying rate and amortization, the maximum qualified loan amount can be calculated.

[^27]:    ${ }^{44}$ According to the financial comparison platform Ratehub.ca, interest rates offered by private lenders range from $10 \%$ to $18 \%$.
    ${ }^{45}$ An alternative for some borrowers is to switch from a federally regulated lender to a credit union, which are provincially regulated. Credit unions are not subject to the uninsured stress test to the same extent as federally regulated lenders. Banks in our model are symmetric, therefore allowing for this substitution would require extending the model. In the US there has been mounting documentation that following increased capital regulation on banks post-financial crisis, borrowers have switched from traditional lenders to non-traditional ones. See for example Buchak et al. (2018).

[^28]:    ${ }^{46}$ This unintended consequence is similar to the one studied by Amromin and Kearns (2014) in the US mortgage market, where they find that the Home Affordability Refinancing Program strengthened the incumbency advantage in mortgage refinancing by reducing home lenders' underwriting risk more than the rival lenders' and hence increased home lenders' market power.

