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# Article

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# Article A Note on the Empirical Relation between Oil Prices and the Value of the Dollar

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**Abstract:** This paper offers an empirical characterization of the relation between the international price of oil and exchange rates that is both useful and reliable. Our characterization is useful because it rests on information of asset prices that are determined in functioning asset markets. Our characterization is reliable because its maintained assumptions are not rejected by the data. Four features differentiate our work from previous analyses. First, our reliance on bilateral rates opens previously ignored financial arbitrage opportunities between oil prices and exchange rates. Second, our emphasis on statistical testing makes our characterization empirically reliable. Specifically, we use a vector-error correction modeling strategy in which both oil prices and exchange rates are endogenous. This framework allows testing for the existence of an arbitrage relation, for the direction of causality, for parameter constancy, for white noise residuals, and for forecast accuracy. Third our reliance on data through 2020 makes our analysis timely. Fourth, to emphasize the advantages of our approach, we compare our results to those derived for formulations relying on effective exchange-rate indexes.

Keywords: oil prices; real effective exchange rate; cointegration; China; renminbi; forecasts

# 1. Introduction

This paper offers an empirical characterization of the relation between movements in the price of oil and movements in bilateral exchange rates. Four features differentiate our work from previous analyses. First, our reliance on bilateral rates opens up previously ignored financial arbitrage opportunities between oil prices and exchange rates.<sup>1</sup> Second, our emphasis on statistical testing makes our characterization empirically reliable. To this end, we use a vector-error correction modeling strategy in which both oil prices and exchange rates are endogenous. This framework allows testing for the existence of an arbitrage relation, for the direction of causality, for parameter constancy, for white noise residuals, and for forecast accuracy. Third our reliance on data through 2020 makes our analysis timely. Specifically, we compare models' forecasts from January 2019 to April 2020, when the price of oil was negative for the first time.<sup>2</sup> Fourth, to emphasize the advantages of our approach, we compare our results to those derived for formulations relying on effective exchange-rate indexes.

Section 2 shows the relevant empirical studies of the relation between the price of oil and exchange rates.<sup>3</sup> Half of the studies rely on samples that exclude developments since 2008 and two thirds of all

<sup>&</sup>lt;sup>1</sup> For an early treatment of oil as a financial asset, see Fratzscher et al. (2014).

<sup>&</sup>lt;sup>2</sup> As noted in the June 2020 Monetary Policy Report of the Federal Reserve, "On April 20, the price of front-month oil futures contracts for West Texas Intermediate (WTI) closed at negative \$38 per barrel. These WTI futures contracts are settled by physical delivery; as worries about the lack of available storage space intensified, prices spiraled downward. Few contracts were actually traded at these negative prices, and prices recovered in the following days." See https://www.federalreserve.gov/monetarypolicy/files/20200612\_mprfullreport.pdf.

<sup>&</sup>lt;sup>3</sup> For a recent and thorough review of this literature see Beckmann et al. (2017).

studies rely on effective exchange-rate indexes. Section 3 describes the pitfalls of using real effective exchange-rate indexes. For this paper, the main pitfall is that for the effective exchange-rate index to be helpful, all the bilateral rates need to change in the same direction and proportion, which is not observed in foreign exchange markets. Section 4 develops our empirical application using the currencies included in the IMF's Special Drawing Right (SDR): The U.S. dollar, the euro, the yen, the pound sterling, and the renminbi.<sup>4</sup> For estimation, we use monthly observations from January 1999 (the introduction of the Euro) to April 2020 (the collapse of oil prices).<sup>5</sup> The results show a statistically reliable arbitrage relation between oil prices and bilateral exchange rates.

# 2. Previous Work

The theoretical work in this area began with Krugman (1980) and Golub (1983). They focused on how bilateral exchange rates responded to exogenous changes in the price of oil. The subsequent empirical literature (Table 1A) has retained the two-country framework by using effective exchange-rate indexes.<sup>6</sup> Finally, even though China is the largest economy in the world<sup>7</sup> and the renminbi is now included in the SDR, the role of China has been largely neglected in this literature.<sup>8</sup>

(A)										
Study	Measure	of Dollar	Samp	ole Span	China Included?					
Huang et al. (2020)	Bilateral Rates		1997-202	15-Monthly	yes					
Reboredo et al. (2014)	Bilatera	al Rates	2000–2012-Monthly		no					
Fratzscher et al. (2014)	NE	ER	2001–2012-Daily		no					
Grisse (2010)	NE	ER	2003-20	10-Weekly	no					
Breitenfellner and Cuaresma (2008)	ŧ		1983-200	06-Monthly	no					
Cheng (2008)	NEER &	& REER	2000-200	07-Monthly	no					
Yousefi and Wirjanto (2005)	RE	ER	1989–199	99-Monthly	no					
Benassy-Quere et al. (2005)	REEF	₹& <u>€</u>	1974-200	04-Monthly	yes					
Amano and van Norden (1998)	RE	ER	1972–199	93-Monthly	no					
This study	Bilatera	al Rates	1999–202	20-Monthly	yes					
Memo. REER: real eff	Memo. REER: real effective exchange rate; NEER: nominal effective exchange rate									
		(B)								
Study	Study Parameter Residuals' Constancy Properties Forecasts Stationari									
Huang et al. (2020)	no	no	no	yes	no					
Reboredo et al. (2014)	no	no	no	no	yes					
Fratzscher et al. (2014)	no	no	no	no	yes					
Grisse (2010)	no	no	no	no	yes					
Breitenfellner and Cuaresma (2008)	no	no	yes	no	no					
Cheng (2008)	no	no	no	no	no					
Yousefi and Wirjanto (2005)	no	no	no	no	no					
Benassy-Quere et al. (2005)	no	indep.	no	yes	yes					
Amano and van Norden (1998)	no	no	yes	yes	yes					
This study	yes	yes	yes	yes	yes					

**Table 1.** (**A**) Design Characteristics of Selected Studies (by publication date). (**B**) Reported Statistical Tests of Selected Studies (by publication date).

<sup>&</sup>lt;sup>4</sup> More than 90 percent of international foreign exchange reserves are held in assets denominated in these currencies. See the IMF's Currency Composition of Official Foreign Exchange Reserves. In terms of the global oil market, these five countries account for 55 percent of world oil consumption in 2019.

<sup>&</sup>lt;sup>5</sup> A switch to daily data would preclude measuring the variables in real terms because there are no official data for daily CPIs.

<sup>&</sup>lt;sup>6</sup> Breitenfellner and Cuaresma (2008) trace the origins of this relation.

<sup>&</sup>lt;sup>7</sup> Using PPP exchange rates. See the IMF's World Economic Outlook.

<sup>&</sup>lt;sup>8</sup> Important exceptions are Benassy-Quere et al. (2005), Cheng (2008), and Huang et al. (2020).

For estimation, the literature reports little or no evidence on the reliability of their findings (Table 1B).<sup>9</sup> Key questions regarding parameter constancy, residuals' properties, forecast accuracy, and stationarity are generally not reported. Why, then, should we rely on their conclusions if we cannot assess their statistical reliability?

# 3. Real Effective Exchange Rates

Figure 1 shows the relation between the real price of oil and the Fed's real effective exchange-rate index. That there is a strong relation is clear: Since 1999, real appreciations of the dollar are associated with declines in the real price of oil, even during the unprecedented changes of the first quarter of 2020. What is not clear is how this information helps the management of financial risks, given that there is no financial market in which the Fed's measure of the dollar is internationally traded. To see how aggregation can create such a correlation we now focus on the measurement of the Fed's index.

#### 3.1. Measurement

The Federal Reserve Board's measure of the real effective exchange rate uses chained aggregation of 26 bilateral exchange rates. These exchange rates are adjusted for differentials in CPI movements relative to U.S. CPI; the selected currencies are associated with the bulk of U.S. trade. The formula is

$$\frac{D_t}{D_{t-1}} = \prod_{i=1}^{26} \left( \frac{R_{\frac{i}{\$},t}}{R_{\frac{i}{\$},t-1}} \right)^{w_{it}}$$
$$R_{\frac{i}{\$},t} = \left( \frac{D_{\frac{i}{\$},t}}{D_{\frac{i}{\$},t-1}} \right) \cdot \left( \frac{CPI_{us,t}}{CPI_{i,t}} \right)$$
$$w_{it} = 0.5 \cdot \mu_{it} + 0.25 \cdot \chi_{it} + 0.25 \cdot \sum_{i \neq j} \omega_{ikt} \cdot \phi_{ijt}$$
$$\sum w_{it} = 1$$

where  $D_{\frac{i}{5},t}$  is the nominal price of the U.S. dollar in terms of the *i*th currency,  $CPI_j$  is the consumer price index for the *j*th country, and  $w_{it}$  is the "total" trade share (Leahy 1998).<sup>10</sup>  $\mu_{it}$  is the share of U.S. *non-oil* imports from the *i*th country,  $\chi_{it}$  is the share of U.S. of *non-oil* exports to the *i*th country,  $\omega_{ikt}$  is the share of imports of the *i*th country coming from the *k*th country, and  $\phi_{ijt}$  is the share of imports of the *i*th country coming from the *j*th country (Leahy 1998).<sup>11</sup> To measure the level of *D*, one selects a base period in which  $D_{t=base} = 100$  with the level of the index for all other periods defined recursively. Note, however, that for the purposes of this paper, aggregation of bilateral exchange rates implies the existence of an active market for *D*.

#### 3.2. Limitations

By construction, movements in  $D_t$  owe to changes in both exchange rates and weights:

$$dlnD_t = \sum_i [w_{it} \cdot dln(R_{it}) + dw_{it} \cdot ln(R_{it})].$$

<sup>&</sup>lt;sup>9</sup> Important exceptions are Amano and van Norden (1998), and Yousefi and Wirjanto (2005).

<sup>&</sup>lt;sup>10</sup> We are using the U.S. official measure of the external value of the dollar which uses weights that are updated every year. The measures of the IMF and the BIS update their weights with less frequency. See Truman (2019, pp. 126–31) for the history of this index.

<sup>&</sup>lt;sup>11</sup> Appendix A.1 contains all the data sources and transformations used in this paper.

Thus, the first limitation is that movements in the effective exchange rates cannot be uniquely mapped into movements in bilateral rates. This consideration undermines the usefulness of Figure 1 for hedging strategies and managing financial risks.

Second, movements in the effective value of the dollar owe to changes in both exchange rates and weights, and thus one cannot identify whether the relation in Figure 1 is between oil prices and trade weights or between oil prices and exchange rates. Specifically, if all the bilateral real exchange rates were unchanged, then

$$dlnD_t = \sum_i dw_{it} \cdot ln(R_i) \neq 0.$$

Thus, one cannot identify whether the relation of Figure 1 is between oil prices and trade weights or between oil prices and exchange rates.<sup>12</sup> In brief, for practitioners interested in the question of "how do we know?" the identification problems associated with effective exchange-rate indexes cannot be avoided: How do we know that the relation is between the price of oil and exchange rates and not between the price of oil and weights of the aggregate? How do we know that a particular currency is responsible for a movement in *D* and not a combination of other currencies?



**Figure 1.** The dashed line is the West Texas Intermediate (WTI) price of oil delineated by the U.S. CPI; the solid line is the Federal Reserve's broad measure for real effective exchange rate (FX/\$). Variables are expressed in logarithms. The mean and range of the series are matched.

Third, and just as an illustration, suppose that  $lnP_t = \alpha + \beta \cdot lnD_t$  where *P* is the real price of oil. Then the ceteris paribus effect of a change in the *i*th currency on lnP is  $\beta w_{it}$  which depends on how much the country (or countries) with the *i*th currency trade with the United States. If that trade is zero, then that currency is irrelevant for oil prices regardless of the importance of that country for the international oil market.<sup>13</sup> Avoiding this limitation involves assuming that all currencies change by the same proportion, which contradicts the data on exchange rates (Figure 2).

<sup>&</sup>lt;sup>12</sup> In this sense, *D* is unlike the CPI in which the weights do not change from year to year. The obvious solution to this limitation is to use an effective exchange rate in which the weights do not vary from year to year as the indexes from the IMF and the BIS. Nevertheless, even if the weights were literally fixed, the reliance on the resulting aggregates still requires us to assume the existence of a market for *D* and would not remove the identification issues raised above.

<sup>&</sup>lt;sup>13</sup> Specifically, the 2020 weights for Russia and Saudi Arabia, two large oil producers are 0.53 percent and 0.49 percent, respectively. See https://www.federalreserve.gov/releases/hl0/weights/default.htm.

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Fourth, the weights  $\omega_{it}$  are not independent of oil prices, especially the weights for the third country effects  $\sum_{i \neq j} \omega_{ikt} \phi_{ijt}$  <sup>14</sup> Data for these shares come from the IMF's Direction of Trade and include the value of trade in oil. To the extent that movements in the value of oil trade are dominated in the short run by movements in oil prices, then reliance on effective exchange rates uses the price of oil to explain the price of oil. Finally, the weights for non-oil bilateral trade are not measured on a value added basis. To the extent that non-oil imports include goods that were produced with oil, then the weights are contaminated by oil prices.<sup>15</sup>



**Figure 2.** Bilateral Real Exchange Rates for the Currencies in the Special Drawing Right (SDR). Series are set 1999 = 100.

# 4. Analysis

## 4.1. Unconditional Correlations

Figure 3 shows the scatter plot between the broad real effective exchange-rate index and the real price of oil. There is no question about the strength of this correlation. To examine whether this correlation is sensitive to the currency mix, Figure 4 shows the scatter plot using the Federal Reserve's effective exchange-rate indexes for Major Currencies and for Other Important Trading Partners. Again, the evidence shows a strong and inverse association between the real price of oil and these two real effective exchange-rate indexes.

<sup>&</sup>lt;sup>14</sup> Note that using fixed weights would address that issue but it would not provide a financial market for the "fixed-weight external value of the dollar." Further, movements in a fixed-weight index cannot, by construction, identify which currencies are responsible for those movements.

<sup>&</sup>lt;sup>15</sup> One of the referees noted that one could use the volatility spillover measure. This suggestion reinforces the point of the paper about using bilateral exchange rates. The volatility of the effective exchange rates is not meaningful, given that offsetting changes in exchange rates would induce a seemingly stable average.



**Figure 3.** The horizontal axis represents the WTI price of oil deflated by the U.S. CPI; the vertical axis represents the Federal Reserve's broad measure for the real effective exchange rate. Variables are expressed in logarithms.

But if we consider the relation between the real price of oil and each of the bilateral currencies (Figure 5), then we find that the unconditional correlations are sensitive to the currency. Indeed, the relation for the yen is absent and the one for the renminibility of the volution. This result emphasizes that reliance on the effective exchange-rate index embodies a fallacy of composition: that what holds for *D* holds exactly for each of its components.



**Figure 4.** The horizontal axis represents the WTI price of oil deflated by the U.S. CPI; the vertical axis for the top panel represents the Federal Reserve's measure for the real effective exchange rate for the major currencies. The vertical axis for the bottom panel represents the Federal Reserve's measure for real effective exchange rate for the Other Important Trading Partners' currencies. Variables are expressed in logarithms.



**Figure 5.** The horizontal axis represents the WTI price of oil deflated by the U.S. CPI; the vertical axis for each panel represents the bilateral exchange rate adjusted by movements in that currency's CPI relative to the U.S. CPI. Variables are in logarithms.

#### 4.2. Vector Error Correction Framework

We use a vector error correction model treating both oil prices and exchange rates as endogenous. Specifically,

$$\Delta \boldsymbol{y}_t = \boldsymbol{c} + \boldsymbol{\Gamma}(\boldsymbol{L}) \cdot \Delta \boldsymbol{y}_{t-1} + \boldsymbol{\Pi} \cdot \boldsymbol{y}_{t-1} + \boldsymbol{u}_t, \ \boldsymbol{u}_t \sim N(0, \Omega)$$
(1)

where  $\Gamma(L) = ||\lambda_{il}(L)||$  and  $\lambda_{il}(L)$  is a polynomial of order 6 in the lag operator *L* and  $\Pi$  is a matrix of unknown coefficients; the specification includes seasonal dummies. This approach has two advantages: it addresses the spurious regression critique and differentiates between short- and long-run responses to shocks. In addition, Equation (1) allows us to conduct out-of-sample forecasts, to evaluate the properties of the residuals, and to test the assumed constancy of the parameters.

Empirically, the existence of an arbitrage relation depends on the rank of  $\Pi$ . If the rank equals one, then

$$\Pi = \alpha \cdot \beta'$$

and  $\beta' \cdot y = 0$  represents the arbitrage condition, with  $\beta'$  being the associated coefficients;  $\alpha$  characterizes responsiveness of y to deviations from the arbitrage condition. We assess the sensitivity of the results using three alternative measures of the dollar:

Model 1: Effective Broad  $\mathbf{y}_t = (p_t d_t)'$ Model 2: Effective, Major and Other Trading Partners  $\mathbf{y}_t = (p_t d_{mt} d_{ot})'$ Model 3: Bilateral rates  $\mathbf{y}_t = \left(p_t r_{\frac{yen}{\$},t} r_{\frac{yen}{\$},t} r_{\frac{pound}{\$},t} r_{\frac{rmb}{\$},t}\right)'$ 

where variables in lower case denote logarithms and

*p* is the real price of oil

*d* is the broad measure of the dollar

 $d_t$  is the measure of the dollar for the major currencies

 $d_o$  is the measure for other important trading partners

 $r_{\frac{yen}{a}}$  is the price-adjusted price of the dollar in terms of the yen

- $r_{\underline{pound}}$  is the price-adjusted price of the dollar in terms of the pound
- $r_{\underline{rmb}}$  is the price-adjusted price of the dollar in terms of the renminbi.

For model 3, the no-arbitrage condition  $\beta' \cdot y = 0$  can be re-written as

$$p = -\beta_{r_{\frac{yen}{4}}} \cdot r_{\frac{yen}{5}} - \beta_{r_{\frac{euro}{5}}} \cdot r_{\frac{euro}{5}} - \beta_{r_{\frac{pound}{5}}} \cdot r_{\frac{pound}{5}} - \beta_{r_{\frac{rmb}{5}}} \cdot r_{\frac{rmb}{5}}.$$

Importantly, this equation is not determining *p* in terms of  $r_{\frac{i}{\$}}$ , *s* or the other way around. Rather, this equation is the long-run, no-arbitrage equilibrium relation between *p* and the  $r_{\frac{i}{\$}}$ . Thus, shocks that create arbitrage opportunities which then trigger changes in all of the endogenous variables as indicated in Equation (1). We now proceed to examine whether the rank of  $\Pi$  is one.

# 4.2.1. Time-Series Properties

Stationarity: A necessary condition for cointegration is  $\Pi \cdot y = 0$  which implies that y is non-stationary. To test stationarity, we use monthly observations from January 1999 to April 2020 and rely on Augmented Dickey Fuller tests. Appendix A.2 shows that one cannot reject the hypothesis that log-levels of the variables are integrated of order one.

Granger Causality: A property of interest is whether exchange rates Granger-cause the price of oil or the other way around. For example, model 3 has five equations and each variable has six lags. The null hypothesis that exchange rates do not Granger cause the price of oil involves excluding all the exchange rates from the equation for the price of oil; this exclusion involves zeroing 24 coefficients. Similarly, the null hypothesis that the price of oil does not Granger-cause exchange rates involves setting the six coefficients for oil prices to zero in each of the four exchange rate equations for a total of 24 zero restrictions. These two hypotheses are tested with a  $\chi^2(n)$  test where *n* is the number of restrictions; Table 2 displays the results.

	H <sub>0</sub>	n	<i>p</i> -Value for $\chi^2(n)$
Model 1	p→d	6	0.75
	d≁p	6	0.004
Model 2	р≁е	12	0.71
	e→p	12	0.002
Model 3	p≁r	24	0.03
	r≁p	24	0.03
p: real price of oil d: of model 1			

Table 2. Granger Causality Tests: 1999:1-2020:4.

e:  $2 \times 1$  vector ( $d_m$ ,  $d_o$ ) of model 2

r:  $4 \times 1$  vector of bilateral real exchange rates of model 3

According to the results, exchange rates Granger-cause the real price of oil for the three models. In other words, excluding exchange rates from the equation for the price of oil carries a statistically significant loss of information. The results also indicate that the price of oil Granger-causes the real bilateral exchange rates but not the real effective exchange rates. In other words, models using bilateral exchange rates embody global interdependencies in which real oil prices and real bilateral rates are jointly determined.

#### 4.2.2. Cointegration

Having established that the series are integrated of order one, we now estimate the rank of  $\Pi$  using Johansen's Trace and Max tests, corrected for degrees of freedom (Johansen 1988). This method begins by testing whether the rank of  $\Pi$  is zero. If this hypothesis is not rejected, then the arbitrage relation between oil prices and exchange rates is absent. If this hypothesis is rejected, then Johansen tests whether the rank of  $\Pi$  is one. If this hypothesis cannot be rejected, then the rank of  $\Pi$  is one and there is just one linear combination of the levels of the real price of oil and real exchange rates that is stationary-that is, the no-arbitrage condition.<sup>16</sup>

For estimation, we use monthly data from January 1999 to December 2018; observations from January 2019 to April 2020 are reserved for out-of-sample forecasting. The estimation results are shown in Table 3.

Number of Eigenvalues	Model 1		Mo	del 2	Model 3	
Rank of <i>I</i>	Trace	Max	Trace	Max	Trace	Max
0	0.009	0.003	0.007	0.005	0.001	0.005
1	0.680	0.679	0.301	0.415	0.441	0.461
2			0.337	0.336	0.655	0.623
3					0.761	0.791
4					0.628	0.626

Table 3. *p*-Values for Johansen's Rank Tests 1999:1–2018:12.

The evidence rejects the null hypothesis that the rank of  $\Pi$  is zero for all three models. Further, the evidence cannot reject the null hypothesis that the rank of  $\Pi$  is one for all three models. Taken together, these results suggest the existence of one cointegration relation between the real price of oil and real exchange rates, however measured. The associated cointegration coefficient estimates are shown in Table 4.

Model	Cointegration Coefficients				Adjustment Coefficients					
Model 1	β				с	α <sub>p</sub>	α <sub>d</sub>			
	3.92				1.79	-0.12	0			
se	0.47				0.14	0.03	0.04			
Model 2	βm	β <sub>0</sub>			с	α <sub>p</sub>	α <sub>m</sub>	αο		
	2.59	1.1			1.76	-0.14	0	0		
se	0.44	0.53			0.12	0.03	0.01	0.003		
Model 3	β <sub>yen/\$</sub> 0.46	β <sub>euro/\$</sub> 1.93	β <sub>pound/\$</sub> 0.65	β <sub>rmb/\$</sub> 1.05	с -5.12	$\alpha_p$ -0.1	α <sub>yen/\$</sub> 0.01	$\alpha_{euro/\$}$ -0.02	$\alpha_{\text{pound/}\$}$	$\alpha_{rmb/\$}$
se	0.27	0.4	0.57	0.34	2.04	0.03	0.01	0.01	0.01	0.003

Table 4. Cointegration Results—1999:1-2018:12-Johansen Method.

The adjustment coefficients (the  $\alpha$ s) for the oil price is significant and negative in all cases and they vary from -0.12 to -0.14, meaning that the adjustment to the long run is less than one year if all else is constant. The adjustment coefficients associated with exchange rates are negligible and insignificant. This result owes to volatility of exchange rates exceeding the volatility of oil prices.

The cointegration coefficients (the  $\beta$ s) for the effective exchange rates are significant (models 1 and 2): a one percent real appreciation in the dollar is associated with a decline in the real price of oil ranging from a nearly four percent for model 1 to a 2.6 percent decline for model 2 when using  $d_m$ ; note that the coefficient for the measure of Other Trading Partners is barely significant. If taken at face

<sup>&</sup>lt;sup>16</sup> Following the suggestion of one of the referees, the intercept *c* is included in the cointegration vector  $\beta'$ .

value, this result suggests that the renminbi is not a relevant asset price for arbitrage, even though China has the third largest share of world oil consumption.<sup>17</sup>

The coefficient estimates for model 3 reveal several features of interest. First, the no-arbitrage equation is

$$p = -0.46 \cdot r_{\frac{yen}{a}} - 1.93 \cdot r_{\frac{euro}{\$}} - 0.65 \cdot r_{\frac{pound}{a}} - 1.05 \cdot r_{\frac{rmb}{a}}$$

which indicates that real appreciations of these currencies are associated with a decline in the price of oil.<sup>18</sup> Second, only the coefficients for the euro and the renminbi are significant; this result is not surprising given the importance of these two economies for both the oil and the foreign-exchange markets. Indeed, the Euro area and China are the largest oil consumers (after the United States) and account for a 29% of world oil consumption in 2019. Third, the significance of the estimate for the renminbi contrasts with the results of model 2, which implies that the renminbi is not relevant for arbitrage. Fourth, there is a significant asymmetry in the coefficients for the euro and the renminbi: the coefficient for  $r_{euro}$  is nearly twice the coefficient for  $r_{rmb}$ . This asymmetry implies that identical percent changes in these two exchange rates have a differential effect on the price of oil because of the greater extent to which the euro is used in financial transactions globally.<sup>19</sup> In other words, the differential in the coefficient estimates reflects the greater economic importance of the euro relative to the renminbi.<sup>20</sup>

Finally, and at the risk of stating the obvious, differences in coefficient estimates across models are not due to differences in sample periods or estimation methods or econometric specifications: these design features are identical for the three models. Instead, the differences in estimates are due to the pitfalls of aggregation.

Residuals Properties: Table 5 reports the test results associated with the maintained assumptions used in estimation: serial independence, normality, and homoskedasticity. The results show that the residuals generally satisfy these assumptions but, to be sure, there are exceptions; this consideration needs to be considered when assessing the usefulness of the results.

Parameter Constancy. To assess the assumed parameter constancy, we estimate the  $\beta$ s recursively. We begin with an initial sample size and then increase that sample size one observation at a time. Figures 6–8 show the recursive 95 percent confidence intervals for the estimated  $\beta$ s: All of the parameter estimates are consistent with their assumed constancy.<sup>21</sup>

 <sup>&</sup>lt;sup>17</sup> Indeed, the Euro area and China are the largest oil consumers (after the United States) and account for 29 percent of world oil consumption in 2019; if we include both Japan and the United Kingdom, that share increases to 34 percent. Source: International Energy Agency as reported in https://en.wikipedia.org/wiki/List\_of\_countries\_by\_oil\_consumption.
 <sup>18</sup> Again, note that this equation is not determining *p* in terms of r<sub>i</sub>/s or the other way around. Instead, it is showing the relation

<sup>&</sup>lt;sup>10</sup> Again, note that this equation is not determining *p* in terms of *r*<sub>1</sub> 's or the other way around. Instead, it is showing the relation among five endogenous variables that is consistent with no-arbitrage relation in these markets. In response to a shock, all the variables in the model respond according to Equation (1). These responses stop as soon as arbitrage opportunities are fully exploited.

<sup>&</sup>lt;sup>19</sup> For example, based on the IMF's COFER data, the euro accounts for 20 percent of the world's official foreign exchange reserves, whereas the remninbi accounts for 2 percent. Using an alternative indicator, the turnover of OTC foreign exchange instruments in 2019 for the euro is \$2.1 trillion and \$285 billion dollars for the remninbi. See https://stats.bis.org/statx/srs/table/dll.3.

<sup>&</sup>lt;sup>20</sup> These observations benefited greatly from the comments by a referee.

<sup>&</sup>lt;sup>21</sup> We could not reject dynamic stability based on impulse responses. These results are available on request.

	Variable	H <sub>0</sub> :Indep.	H <sub>0</sub> :Homosk.	H <sub>0</sub> :Normality
NA 111	р	0.78	0.61	0.06
Model 1	d	0.06	0.72	0
	р	0.39	0.58	0.09
Model 2	$d_m$	0.07	0.39	0.77
	$d_o$	0.33	0.09	0
	р	0.93	0.15	0
	r <sub>ven/\$</sub>	0.36	0.17	0.49
Model 3	r <sub>euro/\$</sub>	0.14	0	0.83
	r <sub>pound/\$</sub>	0.21	0.51	0.2
	r <sub>rmb/\$</sub>	0.04	0	0

**Table 5.** *p*-Values for statistical properties of residuals 1999:1–2018:12.

*Indep.*: test of autocorrelation of residuals; F-test to an AR(7) of estimated residuals. *Homosk.*: test of homoskesdasticity of residuals; F-test to an AR(7) of estimated squared residuals. *Normality*: test of normality;  $X^2$ (2). For implementation details and degrees of freedom, see Doornik, J. and D. Hendry (Doornik and Hendry 2013).



**Figure 6.** Recursive Estimate of Coefficient for the Broad Real Effective Exchange Rate. Bands represent twice the standard deviation of the estimate.



**Figure 7.** Recursive Estimate of Coefficient for the Major (top panel) and Other Important Trading Partners (bottom panel) Real Effective Exchange Rates. Bands represent twice the standard deviation of the estimate.



**Figure 8.** Recursive Estimate of Coefficient for Bilateral Exchange Rates. Bands represent twice the standard deviation of the estimate.

Predictive Accuracy. Projections for oil prices and bilateral exchange rates play a role in the formulation of U.S. monetary policy.<sup>22</sup> However, for some practitioners, the pitfalls of real effective exchange rates might be acceptable if using them increases predictive accuracy. Figures 9 and 10 show the 95 percent confidence bands of the models' forecasts from January 2019 to April 2020.<sup>23</sup>

Inspection of the results reveals several features of interest. First, the predictive accuracy for exchange rates of models using real effective exchange-rate indexes is worse than the predictive accuracy of the model based on bilateral rates. Indeed, the forecasts for model 3 show that the bilateral exchange rates are well within the 95 percent confidence bands, whereas the forecasts for models 1 and 2 are outside their bands starting in 2020. Second, the forecast for the real oil price is comparable across models: predictions are close to the actual price through February 2020. Third, the models show a significant decline in the predicted price of oil but not as large as the one observed in the market. As a result, there is a significant overprediction for March and April of 2020.

This overprediction is not likely to be the result of forecast errors in the exchange rates spilling over to the forecast for the price of oil. The prediction errors of the exchange-rate indexes cannot account for the nearly 50 percent overprediction of the price of oil in those models. Likely then, the overprediction for the price of oil is due to developments in the oil market as such. The models used here, however, cannot identify whether the decline in the price of oil owes to a contraction in oil demand, due to the contraction in economic activity, and/or to an expansion in oil supply, owing to the political tensions between Saudi Arabia and Russia during April 2020. Identifying the separate contributions involves using a structural Vector Autoregressive model such as the one developed by Kilian (2009)<sup>24</sup>.

<sup>&</sup>lt;sup>22</sup> See the Minutes of the Federal Open Market Committee from May 2020 at https://www.federalreserve.gov/monetarypolicy/ files/fomcminutes20200429.pdf. Further, the Federal Reserve Bank of New York's Oil Price Dynamics Report does not rely on effective exchange rates but instead on bilateral rates (Federal Reserve Bank of New York 2020).

<sup>&</sup>lt;sup>23</sup> The estimation sample ends in December 2018, meaning that forecasts are based on those estimates without further update. The "one-step-ahead" refers to the practice of financial forecasters of starting their forecasts from the most recent data. As for the length of the horizon, one year is arbitrary but it is the horizon over which analysts focus, such as the Federal Reserve Bank of New York's Oil-price Dynamics Report.

<sup>&</sup>lt;sup>24</sup> We appreciate the comments from a referee on the lack of identification associated with our model.



Figure 9. Out-of-sample 1-step ahead forecasts for the real price of oil. Sensitivity to Model Specification.



Figure 10. Out-of-sample l-step ahead forecasts for exchange rates. Sensitivity to Model Specification.

# 5. Conclusions

This paper offers an empirical characterization of the relation between the international price of oil and exchange rates that is both useful and reliable. Our characterization is useful because it rests on information about asset prices that are determined in functioning asset markets.<sup>25</sup> Our characterization is reliable because its maintained assumptions are not rejected by the data. To be sure, our work has several limitations. First, the number of observations is not large, which means that both statistical estimates and forecast evaluation will benefit from expanding the sample. Second, using monthly observations limits the applicability of the findings to address high-frequency financial decisions.

<sup>&</sup>lt;sup>25</sup> For example, one could combine futures and options contracts. The futures contract would be for a given price of oil; the option contract would have strike prices determined by a long-run relation between the price of oil and the dollar. Moreover, the Federal Reserve Bank of New York releases its weekly analysis of the price of oil and they use bilateral exchange rates.

Until these, and other, limitations are addressed, the findings have an undeniably tentative character and need to be treated as preliminary ones.

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# Appendix A.

Appendix A.1. Data Sources and Transformations

All the data come from the St. Louis Federal Reserve database Fred: https://fred.stlouisfed.org/ Variables in upper case represent the mnemonics used in the Fred data base. Numerical entries represent the values of these variables in January 2000.

```
d = \log(\text{TWEXBPA}/99.84)
d_m = \log(\text{TWEXMPA}/98.189)
d_o = \log(\text{TWEXOPA}/\text{l10.784})
p = po - pus
po = \log(MCOILWTICO)
pus = \log(CPIAUCNS)
r_{\underline{yen}} = \log(\text{EXJPUS*CPIAUCNS/JPNCPIALLMINMEI})
r_{pound} = \log((1/EXUSUK)*CPIAUCNS/CP0000GBM086NEST)
r_{\underline{mb}} = \log(\text{EXCHUS*CPIAUCNS/CHNCPIALLMINMEI})
r_{\underline{euro}} = \log((1/EXUSEU)*CPIAUCNS/CP0000EZ19M086NEST)
Nominal Yen/dollar DEXJPUS
Nominal China: DEXCHUS
Nominal Euro: DEXUSEU
Nominal UK: DEXUSUK
US CPI: CPIAUCNS
Japanese CPI: JPNCPIALLMINMEI
Chinese CPI: CHNCPIALLMINMEI
euro CPI: CP0000EZ19M086NEST
UK CPI CP0000GBM086NEST
```

Beginning in January of 2020, the Federal Reserve initiated a new weighting scheme which uses total trade, including oil. The revised series are indistinguishable from the series used in this paper. See von Beschwitz et al. (2019). For the new weights see https://www.federalreserve.gov/releases/h10/weights/default.htm

# Appendix A.2. Augmented Dickey-Fuller Test Results

The equation for the augmented ADF test includes a constant and six lags of the change of the variable being examined.

					Levels of I	ogarithms			
	ADF $(T = 249, Constant; 5\% = -2.87, 1\% = -3.46)$								
	Lag	£/\$	rmb/\$	€/\$	¥/\$	D	$D_m$	Do	р
	6	-1.48	-0.71	-1.71	-1.31	-1.35	-1.38	-1.16	-1.42
	5	-1.58	-0.81	-1.60	-1.38	-1.31	-1.33	-1.15	-1.50
	4	-1.72	-0.88	-1.59	-1.58	-1.27	-1.40	-1.09	-1.44
	3	-1.67	-0.91	-1.50	-1.71	-1.15	-1.15	-1.11	-1.51
	2	-1.50	-0.93	-1.50	-1.85	-1.07	-1.17	-1.02	-1.67
	1	-1.39	-0.97	-1.63	-1.66	-1.30	-1.31	-1.25	-1.59
	0	-0.91	-0.71	-1.23	-1.23	-0.70	-0.76	-0.72	-0.77
					Difference o	f Logarithms			
	(T = 248, Constant; 5% = -2.87, 1% = -3.46)								
	Lag	$\Delta \mathcal{E}/\$$	$\Delta rmb/\$$	Δ€/\$	$\Delta$ ¥/\$	ΔD	$\Delta D_m$	$\Delta D_o$	Δp
	6	-6.414 **	-6.307 **	-5.771 **	-6.602 **	-5.996 **	-6.050 **	-5.630 **	-4.956 **
	5	-6.228 **	-7.664 **	-5.616 **	-7.400 **	-5.221 **	-5.539 **	-5.417 **	-5.282 **
	4	-6.472 **	-7.144 **	-6.450 **	-7.944 **	-5.754 **	-6.118 **	-5.886 **	-5.164 **
	3	-6.589 **	-7.288 **	-7.156 **	-7.940 **	-6.430 **	-6.437 **	-6.849 **	-6.159 **
	2	-7.479 **	-7.816 **	-8.663 **	-8.282 **	-7.920 **	-8.474 **	-7.658 **	-6.614 **
	1	-9.327 **	-8.879 **	-10.36 **	-8.875 **	-10.08 **	-9.899 **	-10.29 **	-6.805 **
	0	-12.65 **	-10.24 **	-12.19 **	-12.25 **	-10.47 **	-11.28 **	-10.66 **	-9.471 **
				Sample Stat	istics				
		$\Delta E/\$$	∆rmb/\$	Δ€/\$	Δ¥/\$	ΔD	$\Delta D_{m}$	ΔDo	Δp
				Monthly (	Growth Rates	1990:2-2020:4	4 255 Obs.		
Mean		0.001	-0.001	0.001	0.001	0.000	0.001	0.000	-0.001
Std.Devn.		0.021	0.010	0.023	0.023	0.012	0.016	0.011	0.098
Skewness		0.400	0.086	-0.080	-0.030	0.438	-0.113	1.329	-1.799
Excess Kurtosis		1.143	0.690	0.429	0.596	1.653	0.590	4.923	7.329
Minimum		-0.057	-0.033	-0.068	-0.073	-0.034	-0.048	-0.032	-0.561
Maximum		0.077	0.035	0.070	0.072	0.056	0.058	0.062	0.210
Median		0.000	-0.001	0.001	0.000	0.000	0.002	-0.001	0.013
Normality	test (p-val)	0.0018 **	0.0432 *	0.211	0.082	0.0000 **	0.082	0.0000 **	0.0000 **

 Table A1. Augmented Dickey Fuller Tests—1999:1–2020:4.

Note: \* significant at the 5% significance level, \*\* significant at the 1% significance level.

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