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## Generalized exponential estimators for the finite population mean

Tolga Zaman<sup>1</sup>

### ABSTRACT

This study proposes a new class of exponential-type estimators in simple random sampling for the estimation of the population mean of the study variable using information of the population proportion possessing certain attributes. Theoretically, mean squared error (MSE) equations of the suggested ratio exponential estimators are obtained and compared with the Naik and Gupta (1996) ratio and product estimators, the ratio and product exponential estimator presented in Singh et al. (2007) and the ratio exponential estimators presented in Zaman and Kadilar (2019a). As a result of these comparisons, it is observed that the proposed estimators always produce more efficient results than the others. In addition, these theoretical results are supported by the application of original datasets.

**Key words:** ratio-exponential estimators, auxiliary attribute, mean square error, efficiency.

Mathematical classification: 62D05

### 1. Introduction

When there is a positive correlation between the study variable and the auxiliary variable in the simple random sampling method, ratio-type estimators are used to estimate the population mean. But when the correlation coefficient between the study and auxiliary variables is negative, the product estimator is used. Many authors have proposed estimators based on auxiliary attribute. Bahl and Tuteja (1991) estimator and a family of estimators considered by Jhajj et al. (2006), Singh et al. (2008), Koyuncu (2012), Malik and Singh (2013), Shabbir and Gupta (2010), Solanki and Singh (2013), Zaman (2018), Zaman and Kadilar (2019b) suggested a class of estimators by using auxiliary attributes. In this paper, a new class of exponential type estimators is proposed to estimate the population mean for the study variable using information on auxiliary attributes.

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Let  $y_i$  be  $i$ -th characteristic of the population and  $\phi_i$  is the case of possessing certain attributes. If  $i$ th unit has the desired characteristic, it takes the value 1; if not then the value 0. That is:

$$\phi_i = \begin{cases} 1 & , \text{ if } i\text{th unit of the population possesses attribute} \\ 0 & , \text{ otherwise.} \end{cases}$$

Let  $A = \sum_{i=1}^N \phi_i$  and  $a = \sum_{i=1}^n \phi_i$  be the total count of the units that possess certain attribute in the population and the sample, respectively. And  $P = \frac{A}{N}$  and  $p = \frac{a}{n}$  are the ratio of these units, respectively.

The Naik and Gupta (1996) estimator for the population mean  $\bar{Y}$  of the variate of study, which makes use of information concerning the population proportion possessing certain attribute, is defined by

When the relationship between the study variable and the auxiliary attribute is positive, the ratio estimator of the population proportion of the study variable,

$$\bar{y}_{NG1} = \frac{\bar{y}}{p} P \quad (1.1)$$

When the relationship between the study variable and the auxiliary attribute is negative, the product estimator of the population proportion of the study variable,

$$\bar{y}_{NG2} = \frac{\bar{y}}{p} p \quad (1.2)$$

where it is assumed that the population proportion  $P$  of the form of attribute  $\phi$  is known.

The expressions of MSE of the Naik and Gupta estimators are

$$MSE(\bar{y}_{NG1}) \cong \frac{1-f}{n} \bar{Y}^2 (C_y^2 - 2\rho_{pb} C_y C_p + C_p^2) \quad (1.3)$$

$$MSE(\bar{y}_{NG2}) \cong \frac{1-f}{n} \bar{Y}^2 (C_y^2 + 2\rho_{pb} C_y C_p + C_p^2) \quad (1.4)$$

Considering Bahl and Tuteja (1991), Singh et al. (2007) suggested the following ratio estimator when the study variable and the auxiliary attribute are positively correlated.

$$t_1 = \bar{y} \exp\left(\frac{p-p}{p+p}\right) \quad (1.5)$$

Singh et al. (2007) suggested the following ratio estimator when the study variable and the auxiliary attribute are negatively correlated.

$$t_2 = \bar{y} \exp\left(\frac{p-P}{p+P}\right) \quad (1.6)$$

The MSEs of these estimators are

$$MSE(t_1) \cong \frac{1-f}{n} \bar{Y}^2 \left( C_y^2 - \rho_{pb} C_y C_p + \frac{C_p^2}{4} \right) \tag{1.7}$$

$$MSE(t_2) \cong \frac{1-f}{n} \bar{Y}^2 \left( C_y^2 + \rho_{pb} C_y C_p + \frac{C_p^2}{4} \right) \tag{1.8}$$

Zaman and Kadilar (2019a) suggested modified exponential ratio estimators using auxiliary attribute information for estimating  $\bar{Y}$  as

$$t_{ZKi} = \bar{y} \exp \left[ \frac{(kP+l)-(kp+l)}{(kP+l)+(kp+l)} \right] \quad i = 1, 2, \dots, 9 \tag{1.9}$$

where  $k(\neq 0)$  and  $l$  are either the real number or the functions of the known parameters of the attribute,  $C_p$ ,  $\beta_2(\phi)$  and the known parameter of the attribute with the study variable,  $\rho_{pb}$ . Note that the sum of  $k$  and  $l$  is not necessarily equal to one.

The MSE of these estimators

$$MSE(t_{ZKi}) \cong \frac{1-f}{n} \bar{Y}^2 [\theta_i^2 C_p^2 - 2\theta_i \rho_{pb} C_y C_p + C_y^2], i = 1, \dots, 9 \tag{1.10}$$

$$\theta_1 = \frac{P}{2(P+\beta_2(\phi))}; \theta_2 = \frac{P}{2(P+C_p)}; \theta_3 = \frac{P}{2(P+\rho_{pb})}; \theta_4 = \frac{\beta_2(\phi)P}{2(\beta_2(\phi)P+C_p)}; \theta_5 = \frac{C_p P}{2(C_p P+\beta_2(\phi))}$$

$$\theta_6 = \frac{C_p P}{2(C_p P+\rho_{pb})}; \theta_7 = \frac{\rho_{pb} P}{2(\rho_{pb} P+C_p)}; \theta_8 = \frac{\beta_2(\phi)P}{2(\beta_2(\phi)P+\rho_{pb})}; \theta_9 = \frac{\rho_{pb} P}{2(\rho_{pb} P+\beta_2(\phi))}.$$

where  $f = \frac{n}{N}$ ;  $N$  is the number of units in the population;  $C_p$  is the coefficient of population variation of the form of attribute and  $C_y$  is the coefficient of population variation of the study variable.  $\rho_{pb}$  is the point biserial correlation coefficient.  $\beta_2(\phi)$  is the coefficient of population kurtosis of the auxiliary attribute.

## 2. Suggested estimators

Following Ozel (2016), the improved class of estimator  $\bar{y}_{pri}$  for the population is proposed as follows

$$\bar{y}_{pri} = \bar{y} \left( \frac{p}{P} \right)^\alpha \exp \left[ \frac{(kP+l)-(kp+l)}{(kP+l)+(kp+l)} \right]; i = 1, 2, \dots, 10 \tag{2.1}$$

A class of new estimators generated from Equation (2.1) is listed in Table 1.

**Table 1.** Proposed Estimators

Estimators	Values of	
	$k$	$l$
$\bar{y}_{pr1} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{P-p}{P+p}\right]$	1	0
$\bar{y}_{pr2} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{P-p}{P+p+2\beta_2(\phi)}\right]$	1	$\beta_2(\phi)$
$\bar{y}_{pr3} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{P-p}{P+p+2C_p}\right]$	1	$C_p$
$\bar{y}_{pr4} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{P-p}{P+p+2\rho_{pb}}\right]$	1	$\rho_{pb}$
$\bar{y}_{pr5} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{\beta_2(\phi)(P-p)}{\beta_2(\phi)(P+p)+2C_p}\right]$	$\beta_2(\phi)$	$C_p$
$\bar{y}_{pr6} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{C_p(P-p)}{C_p(P+p)+2\beta_2(\phi)}\right]$	$C_p$	$\beta_2(\phi)$
$\bar{y}_{pr7} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{C_p(P-p)}{C_p(P+p)+2\rho_{pb}}\right]$	$C_p$	$\rho_{pb}$
$\bar{y}_{pr8} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{\rho_{pb}(P-p)}{\rho_{pb}(P+p)+2C_p}\right]$	$\rho_{pb}$	$C_p$
$\bar{y}_{pr9} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{\beta_2(\phi)(P-p)}{\beta_2(\phi)(P+p)+2\rho_{pb}}\right]$	$\beta_2(\phi)$	$\rho_{pb}$
$\bar{y}_{pr10} = \bar{y} \left(\frac{p}{P}\right)^\alpha \exp\left[\frac{\rho_{pb}(P-p)}{\rho_{pb}(P+p)+2\beta_2(\phi)}\right]$	$\rho_{pb}$	$\beta_2(\phi)$

In Table 1,  $C_p$ ,  $\beta_2(\phi)$  and  $\rho_{pb}$  are coefficient of variation, coefficient of population kurtosis of the form of the auxiliary attribute and the point biserial population correlation coefficient between the auxiliary attribute and the study variable, respectively.  $\bar{y}$  and  $p$  are the sample mean belonging to the study variable and the sample proportion possessing certain attributes, respectively.

To obtain the MSE expression of these estimators  $\bar{y}_{pri}$ , let  $\bar{y} = \bar{Y}(1 + e_0)$  and  $p = P(1 + e_1)$  such that  $E(e_0) = E(e_1) = 0$  and  $E(e_0^2) = \frac{1-f}{n} C_y^2$ ,  $E(e_1^2) = \frac{1-f}{n} C_p^2$  and  $E(e_0 e_1) = \frac{1-f}{n} C_{yp} = \frac{1-f}{n} \rho_{pb} C_y C_p$ .

Expressing the estimator  $\bar{y}_{pri}$  in terms of  $e_j$ , ( $j = 0, 1$ ) and shortened terms up to the first two and the first three components of  $e$ 's as follows

$$\bar{y}_{pri} = \bar{Y}(1 + e_0)(1 + e_1)^\alpha \exp\{-\theta e_1(1 + \theta e_1)^{-1}\}$$

$$\bar{y}_{pri} = \bar{Y}(1 + e_0) \left[ 1 + \alpha e_1 + \frac{\alpha(\alpha - 1)}{2} e_1^2 + \dots \right] [1 + (-\theta e_1)(1 + \theta e_1)^{-1}]$$

$$= \bar{Y}(1 + e_0) \left[ 1 + \alpha e_1 + \frac{\alpha(\alpha - 1)}{2} e_1^2 + \dots \right] [1 - \theta e_1 + \theta^2 e_1^2] \tag{2.2}$$

Expanding the right-hand side of (2.2) to the first order approximation and subtracting  $\bar{Y}$  from both sides, the following expression is obtained

$$\bar{y}_{pri} - \bar{Y} \cong \bar{Y} \left[ -\theta_i e_1 + \theta_i^2 e_1^2 + \alpha e_1 - \alpha \theta_i e_1^2 + \frac{\alpha(\alpha - 1)}{2} e_1^2 + e_0 - \theta_i e_0 e_1 + \alpha e_0 e_1 \right] \tag{2.3}$$

Squaring both sides of equation (2.3) and then taking the expectation of both sides, the following expression of MSE of the estimator  $\bar{y}_{pri}$  is obtained

$$MSE(\bar{y}_{pri}) \cong \frac{1-f}{n} \bar{Y}^2 [\alpha^2 C_p^2 + \theta_i^2 C_p^2 - 2\alpha\theta_i C_p^2 + C_y^2 + 2\alpha\rho_{pb} C_y C_p - 2\theta_i C_y C_p]; i = 1, 2, \dots, 10 \tag{2.4}$$

Using the following equations, the optimal value of  $\alpha$  can be obtained:

$$\begin{aligned} \frac{\partial MSE(\bar{y}_{pri})}{\partial \alpha} &= \frac{1-f}{n} \bar{Y}^2 (2\alpha C_p^2 - 2\theta_i C_p^2 + 2\rho_{pb} C_y C_p) = 0 \\ \alpha_{opti} &= \frac{\theta_i C_p - \rho_{pb} C_y}{C_p}; i = 1, 2, \dots, 10 \end{aligned} \tag{2.5}$$

The minimum MSE of the proposed estimator can be calculated using  $\alpha$  equations in (2.5). The suggested estimators have the same minimum MSE as follows:

$$MSE_{min}(\bar{y}_{pr}) \cong \frac{1-f}{n} \bar{Y}^2 C_y^2 (1 - \rho_{pb}^2) \tag{2.6}$$

### 3. Efficiency comparisons

The expressions of MSE of classical estimators  $\bar{y}$ ,  $\bar{y}_{NG1}$ ,  $\bar{y}_{NG2}$ ,  $t_1$ ,  $t_2$  and  $zt_i$  are compared with the MSE of the suggested estimator  $\bar{y}_{pri}$ .

Under simple random sampling without replacement (SRSWOR) the variance of the sample mean is

$$V(\bar{y}) = \frac{1-f}{n} \bar{Y}^2 C_y^2 \tag{3.1}$$

From (2.6) and (3.1), we have

$$\begin{aligned} MSE_{min}(\bar{y}_{pri}) &< V(\bar{y}) \\ \frac{1-f}{n} \bar{Y}^2 C_y^2 (1 - \rho_{pb}^2) &< \frac{1-f}{n} \bar{Y}^2 C_y^2 \\ \rho_{pb}^2 &> 0 \end{aligned} \quad (3.2)$$

From (2.6) and (1.3), we have

$$\begin{aligned} MSE_{min}(\bar{y}_{pri}) &< MSE(\bar{y}_{NG1}) \\ \frac{1-f}{n} \bar{Y}^2 C_y^2 (1 - \rho_{pb}^2) &< \frac{1-f}{n} \bar{Y}^2 (C_y^2 - 2\rho_{pb} C_y C_p + C_p^2) \\ (C_y \rho_{pb} - C_p)^2 &> 0 \end{aligned} \quad (3.3)$$

From (2.6) and (1.4), we have

$$\begin{aligned} MSE_{min}(\bar{y}_{pri}) &< MSE(\bar{y}_{NG2}) \\ \frac{1-f}{n} \bar{Y}^2 C_y^2 (1 - \rho_{pb}^2) &< \frac{1-f}{n} \bar{Y}^2 (C_y^2 + 2\rho_{pb} C_y C_p + C_p^2) \\ (C_y \rho_{pb} + C_p)^2 &> 0 \end{aligned} \quad (3.4)$$

From (2.6) and (1.7), we have

$$\begin{aligned} MSE_{min}(\bar{y}_{pri}) &< MSE(t_1) \\ \frac{1-f}{n} \bar{Y}^2 C_y^2 (1 - \rho_{pb}^2) &< \frac{1-f}{n} \bar{Y}^2 \left( C_y^2 - \rho_{pb} C_y C_p + \frac{C_p^2}{4} \right) \\ \left( C_y \rho_{pb} - \frac{C_p}{2} \right)^2 &> 0 \end{aligned} \quad (3.5)$$

From (2.6) and (1.8), we have

$$\begin{aligned} MSE_{min}(\bar{y}_{pri}) &< MSE(t_2) \\ \frac{1-f}{n} \bar{Y}^2 C_y^2 (1 - \rho_{pb}^2) &< \frac{1-f}{n} \bar{Y}^2 \left( C_y^2 + \rho_{pb} C_y C_p + \frac{C_p^2}{4} \right) \\ \left( C_y \rho_{pb} + \frac{C_p}{2} \right)^2 &> 0 \end{aligned} \quad (3.6)$$

From (2.6) and (1.10), we have

$$\begin{aligned}
 &MSE_{min}(\bar{y}_{pri}) < MSE(t_{zki}) \\
 &\frac{1-f}{n} \bar{Y}^2 C_y^2 (1 - \rho_{pb}^2) < \frac{1-f}{n} \bar{Y}^2 [\theta_i^2 C_p^2 - 2\theta_i \rho_{pb} C_y C_p + C_y^2] \\
 &(C_y \rho_{pb} - \theta_i C_p)^2 > 0
 \end{aligned}
 \tag{3.7}$$

We infer that the suggested exponential estimators  $\bar{y}_{pr}$  perform better than the competing estimators in all conditions because the condition given in (3.2)-(3.7) is always satisfied.

**4. Empirical study**

For empirical study, we use the data given in Sukhatme and Sukhatme (1970) and Zaman et al. (2014).

The values of the required parameters for these data sets are given in Tables 2 and 3.

Population 1: The data is defined as follows:

$$\phi_i = \begin{cases} y = \text{the number of villages in the circles} \\ 1, & \text{if a circle consists of more than five villages} \\ 0, & \text{otherwise.} \end{cases}$$

**Table 2.** Data Statistics of Population 1

$N=89$	$\bar{Y} = 3.3596$	$\theta_1 = 0.0171$	$\theta_5 = 0.0433$	$\theta_9 = 0.0132$
$n= 20$	$P = 0.1236$	$\theta_2 = 0.0221$	$\theta_6 = 0.1508$	
$\beta_2(\phi) = 3.492$	$C_y = 0.6008$	$\theta_3 = 0.0695$	$\theta_7 = 0.0171$	
$\rho_{pb} = 0.766$	$C_p = 2.6779$	$\theta_4 = 0.0694$	$\theta_8 = 0.1802$	

Population 2: The data is defined as follows:

$$\phi_i = \begin{cases} y = \text{the number of teachers} \\ 1, & \text{if the number of teachers is more than 60} \\ 0, & \text{otherwise.} \end{cases}$$

**Table 3.** Data Statistics of Population 2

$N=111$	$\bar{Y} = 29.279$	$\theta_1 = 0.0146$	$\theta_5 = 0.0382$	$\theta_9 = 0.0117$
$n= 30$	$P = 0.117$	$\theta_2 = 0.0203$	$\theta_6 = 0.1441$	
$\beta_2(\phi) = 3.898$	$C_y = 0.872$	$\theta_3 = 0.0640$	$\theta_7 = 0.0164$	
$\rho_{pb} = 0.797$	$C_p = 2.758$	$\theta_4 = 0.0709$	$\theta_8 = 0.1819$	



Table 4. MSE Values of the Classical and Suggested Estimators

Estimator	MSE	
	Population 1	Population 2
$\bar{y}$	0.1579	15.8557
$\bar{y}_{NG1}$	2.2168	94.532
$\bar{y}_{NG2}$	4.3742	254.4077
$t_1$	0.4030	15.5403
$t_2$	1.4817	95.4782
$t_{ZK1}$	0.1404	14.7247
$t_{ZK2}$	0.1357	14.2948
$t_{ZK3}$	0.0981	11.3891
$t_{ZK4}$	0.0982	10.9827
$t_{ZK5}$	0.1171	13.0318
$t_{ZK6}$	0.0667	7.6304
$t_{ZK7}$	0.1404	14.5909
$t_{ZK8}$	0.0654	6.5614
$t_{ZK9}$	0.1442	14.9436
$\bar{y}_{pr}$	<b>0.0652</b>	<b>5.7840</b>

From the Table 4, it is observed that the suggested exponential estimators  $\bar{y}_{pri}$ , ( $i = 1, 2, \dots, 10$ ) perform better than the usual unbiased estimator  $\bar{y}$ , ratio and product estimators of Naik and Gupta (1996), ratio and product estimators suggested by Singh et al. (2007) and the ratio exponential estimators presented in Zaman and Kadilar (2019a). Finally, it is inferred that the suggested estimators perform better than the considered ratio estimators in all conditions, because the conditions given in Section 3 are always satisfied.

## 5. Conclusion

This paper proposes exponential families of estimators and presents a theoretical argument. All of the suggested estimators have the same minimum MSE equation. Considering MSE equations, the suggested exponential estimators are always more efficient than those of the sample mean, the ratio and product estimators of Naik and Gupta (1996), the ratio and product estimators of Singh et al. (2007) and the ratio exponential estimators of Zaman and Kadilar (2019a), under all the conditions. The results presented here support these conclusions by theoretical development and numerical analysis. In forthcoming studies, we hope to extend the suggested class of estimators presented in this article to the stratified random sampling.

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