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Incentives in regulatory DEA models with discretionary outputs: The case of Danish water regulation

Emil Heesche¹ and Peter Bogetoft²

Abstract

Data Envelopment Analysis (DEA) based cost norms have attractive properties in the regulation of natural monopolies. However, they are also sensitive to the choice of cost drivers. When some of the cost drivers are discretionary, this may lead to suboptimal incentives. When a regulated firm compares the marginal change in its cost norm with its marginal cost of changing the discretionary output, the gains from adjusting the output will be very context specific. It is therefore unlikely that the regulation will induce socially optimal output levels.

In this paper, we analytically and numerically examine the impacts of including a discretionary quality indicator in the benchmarking model used to regulate Danish water firms. We show that the eight-year catch-up period allowed in this regulation gives strong incentives to reduce costs since the firms can keep possible cost reductions for several years before the cost norm fully internalizes the cost reduction potentials. On the other hand, this scheme also provides very weak quality incentives since it takes eight years before the extra cost of increasing quality is fully internalized in the cost norm.

Keywords: Data Envelopment Analysis; incentives; regulation; discretionary outputs; water sector

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1 Introduction

Natural monopolies are not subject to the disciplining forces of a competitive market and are, therefore, often assumed to provide services that are too limited at costs that are too high if left unregulated.

Network firms in the water, electricity and gas industries are examples of such natural monopolies due to the high fixed costs associated with the construction of the networks. Most countries, therefore, have regulations on the services provided and the tariffs that such firms are allowed to charge. In Europe, in particular, it is common to use benchmarking-based regulations: the allowed revenues of the individual firms are determined by benchmarking its costs for the services provided against the best practice costs that can be inferred for all network firms. If the best practice costs of a given firm's service level are lower than the firm's actual costs, it is forced to reduce costs. Therefore, instead of real market competition, the regulation relies on model-based pseudocompetition. A commonly used benchmarking approach is data envelopment analysis (DEA), sometimes combined with stochastic frontier analysis (SFA). For recent references, see, e.g., Agrell and Bogetoft (2017,18), Agrell, Bogetoft and Tind (2002,05), Bogetoft (2012) and Bogetoft and Otto (2011), Dai and Kuosmanen (2014) and Ramanathan, Ramanathan, and Bentley (2018). For more on the theory of when DEA-based regulation may be optimal, see Bogetoft (1994a, 94b, 95, 97, 2000, 12) and Bogetoft and Otto (2011).

A key characteristic of typical network regulation is that the demand for different services is largely insensitive to prices, at least for the range of prices naturally allowed by regulators. That is, demand can be considered exogenous, and the challenge is mainly to determine the minimal costs of providing these services.

The regulatory problem can formally be formulated as an agency problem, cf. the references above; the aim is to find reimbursements to firms that are individually rational and incentive compatible. Firms must have private incentives to reduce costs, and the allowed income must be sufficient to make production profitable, i.e., reimbursements must exceed the true underlying minimal costs. The advantage of DEA is precisely that it offers the smallest upper bound of the minimal cost when there is considerable initial uncertainty about the underlying cost function.

However, if demand is not exogenous, things become more complex, and DEA-based regulation may not be optimal. When a regulated firm can affect the services demanded, i.e., the cost drivers in the usual regulatory cost benchmarking model, there is a risk that the firm may use this strategically. By inducing either a very low or very high demand for certain services, or in other ways inducing consumers to demand a less common mix of services, it will be more difficult to find comparators in the benchmarking model, and the firm may gain increased information rents, i.e., the difference between the true underlying costs and cost norms determined by benchmarking. We will illustrate this in Section 2 below. The key insight is, however, simple. A regulated firm will try to maximize its profits, and this entails a search for levels of discretionary outputs where the benchmarking is more lenient. This also implies that the firm will not be guided by the potential value to consumers of the discretionary outputs and that the resulting outcomes, therefore, are no longer socially optimal.

A good example of a potentially discretionary output is quality. Consumers may be willing to forgo some quality, e.g., live with some services not always being delivered if the price reductions are sufficiently large. Regulation of quality is often handled by some ad-on regulation rewarding (penalizing) the firms if services are delivered more (less) steadily than some threshold. A good example of such a scheme is the Norwegian so-called KILE system used to incentivize steady service delivery in electricity distribution, cf. NVE (2019). The use of add-ons to traditional cost benchmarking can make it easier to control the quality incentives and

can be a natural approach, particularly if quality is a property of all the services being provided. In contrast to a more traditional add-on approach, in this paper, we investigate the direct integration of discretionary services such as quality into the cost benchmarking model. There are also examples of this approach in network regulation, e.g., in the model used by the Brazilian Electricity Regulatory Agency (ANEEL) to regulate electrical distribution firms.

While it is relatively straightforward to show the challenges of discretionary outputs in benchmarking-based regulations in the abstract, as we will do in Section 2, we need more specific settings, i.e., more specific regulations and regulatory cost norms, to gauge the size and significance of the problem. The bulk of this paper, therefore, examines a specific regulatory framework, namely, that used to regulate Danish water firms.

Danish drinking and wastewater firms are natural monopolies and subject to two different regulations: economic and environmental.

Economic regulation is intended to reduce firms' costs and thereby prices. The regulator, the Danish Competition and Consumer Authority (DCCA), sets a revenue cap for each firm. The DCCA's goal is to set a revenue cap that is equal to the cost of the most efficient firms. This will force inefficient firms to reduce their costs. However, the DCCA needs to take into account different underlying conditions and to allow a reasonable time for inefficient firms to catch up to best practices. Therefore, they need to use more advanced benchmarking models to compare the firms. DCCA uses both a DEA and SFA as part of this.

Environmental regulation is intended to secure a high quality of water and to reduce pollution. This is typically done by setting minimum requirements for the firms. If the firms do not fulfil the requirement, the environmental regulator starts a dialogue with the firm to get the firm back on track. For some environmental parameters, such as pollution, firms need to pay a fee. This fee does not, however, give high economic incentives because firms are allowed to charge the full amount of such fees to consumers in the economic regulation. Hence, the interaction between the two regulations is suboptimal, and this has recently led to some criticism.

In a perfect regulation, firms have incentives to reduce their costs and choose the level of quality that is socially optimal. This requires, however, good information about society's utility, viz., consumers' willingness to pay for quality. In Denmark, such information is still not available for most quality parameters. Moreover, even when it becomes available, it may not be simple to find the best balance between production costs and consumer preferences. Recall that this has to take place in a second-best world where the regulator has inferior information about the underlying cost function. Varying the services provided may come with extra information rents to the firms since they may become less comparable, making the benchmarking less effective, cf. Bogetoft and Eskesen (2021). In fact, extra information rents that can be extracted when service mixes change may preclude such adjustment and make it second best optimal to stick to past production mixes, cf., e.g., Antle and Bogetoft (2019).

In our analysis of Danish water regulation, we will therefore not look at the demand for different qualities but rather look at the supply side. The question we investigate is which are the incentives that firms would have to change quality levels when quality is part of the cost drivers in the benchmarking model used to set the income cap in the Danish water regulation.

We first investigate the cost reduction incentives in the present regulation. Firms have incentives to reduce costs. Assuming that quality is costly, it follows that firms have incentives to limit quality when it is not directly rewarded. We next examine the incentives if the regulator uses the same revenue cap formula but

includes quality measures in the benchmarking model. In this case, the quality incentives are more complicated. Inefficient firms may still have strong incentives to limit their quality, but for some firms, a high-quality strategy may also become attractive since it may protect the firm against reductions in the revenue cap. The details depend on the specific context of the firms and their placement in the production space.

The rest of this paper is structured as follows. Section 2 outlines the principal problems of using DEA-based revenue cap schemes when some of the cost drivers are discretionary. In Section 3, we first describe the current benchmarking model used to regulate Danish water firms and discuss the incentives. Next, we assume that quality is incorporated in the benchmarking model and show how this affects incentives. In Section 4, we show an application based on data from the Danish water sector, which confirms the discussion in the previous sections. In Section 5, we discuss the difference between static and dynamic incentives, taking into account the long-run ramifications of changes in costs or quality levels. In Section 6, we discuss the different limitations and extensions of our analyses. Concluding remarks are given in Section 7.

2 Regulation with discretionary outputs

To illustrate the complications of using a revenue cap scheme to incentivize the choice of an optimal quality level, let us assume that the underlying true benefits of quality to the consumers and costs of quality to the firm are as illustrated in Figure 2-1 below.

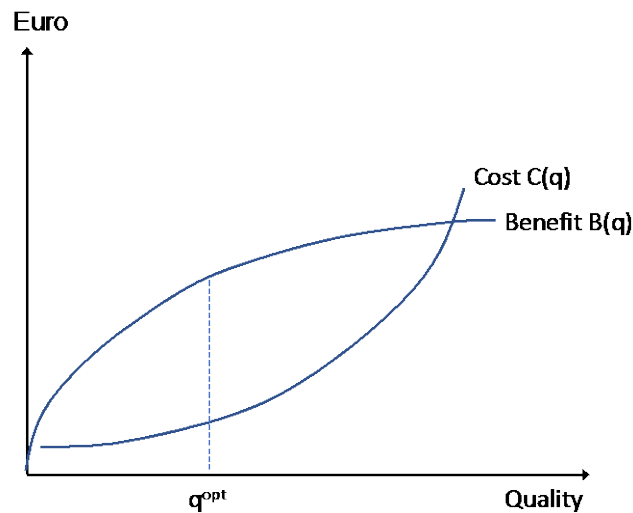


Figure 2-1 Underlying cost and benefits of quality

Now, if the regulator has perfect information about the underlying costs and benefits, he can determine the optimal quality level q^{opt} . In principle, he can simply demand that the firm implements this quality level, perhaps by revoking his concessions rights if the quality level is not realized. There are, of course, many other schemes that could be used, the most obvious of which are illustrated in Figure 2-2 below.

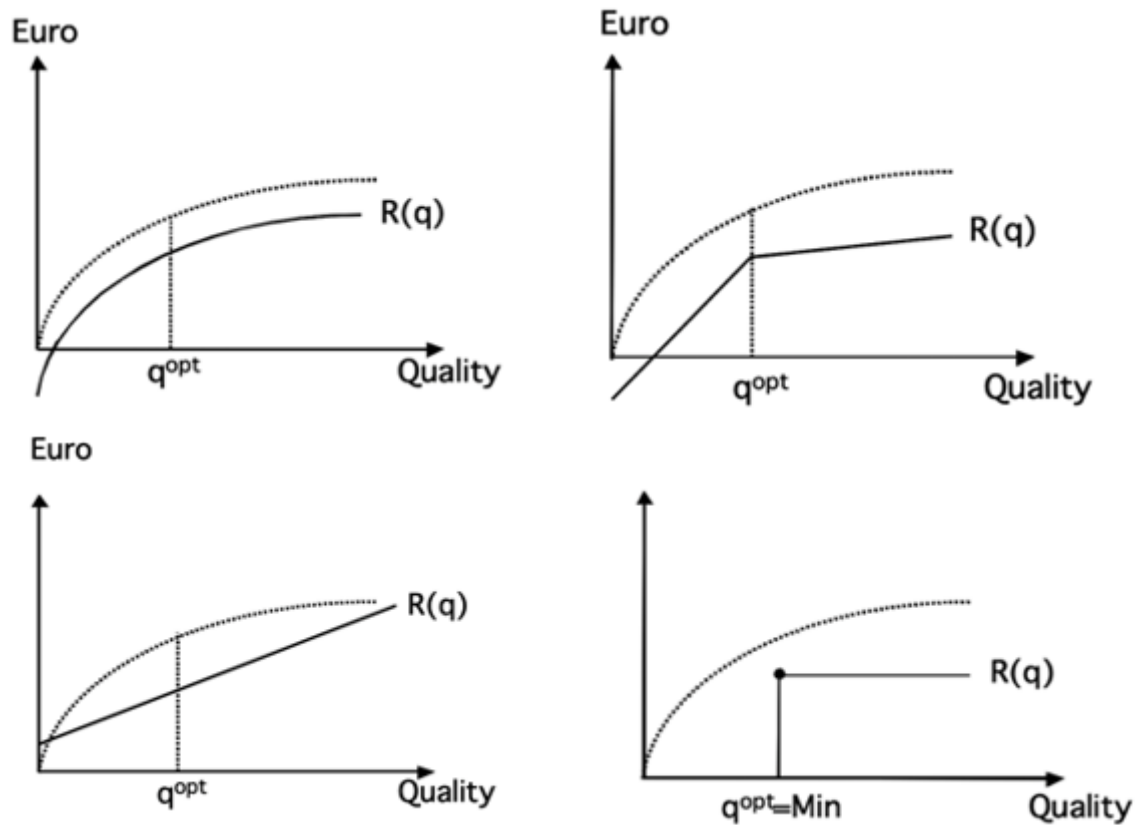


Figure 2-2 Alternative incentive schemes

One possibility is to pay the firm whichever benefits $B(q)$ it creates except for a lumpsum amount A (upper left panel). Another is to use a two-price schedule where the marginal revenue is relatively high, p_1 until the desired quality level and lower ($p_1 - p_2$) after (upper right panel). A third option is to simply work with a marginal reward scheme with a slope p equal to the slope of the benefits (and cost) curves at the optimal quality level (lower left panel). Finally, an option is to simply demand the required quality and to penalize if quality is below (lower right panel). Formally, we can express the revenue functions as:

- Generalized price plan $R(q) = A + B(q)$
- Two price plan $R(q) = A + p_1q - p_2\max\{q - q^{opt}, 0\}$
- Marginal price plan $R(q) = A + pq$
- Restriction or bonus based $R(q) = A \text{ if } q \geq q^{opt}, = 0 \text{ otherwise}$

It is worth noting that all of the above, except the generalized price plan or benefit-sharing rule (upper left), require some knowledge of the underlying cost function. Only in this way can the q^{opt} value be determined.

Now, consider using a typical revenue cap approach. As explained above, many countries use such approaches where the allowed revenue is determined. Abstracting from a series of details in actual regulations, for example, the time allowed to catch up to best practices, the core of benchmarking-based

revenue caps is that the cap is determined by estimating the underlying costs of providing different service levels. The C^{DEA} function in Figure 2-3 below may illustrate the resulting revenue cap if DEA is used to approximate best practice costs.

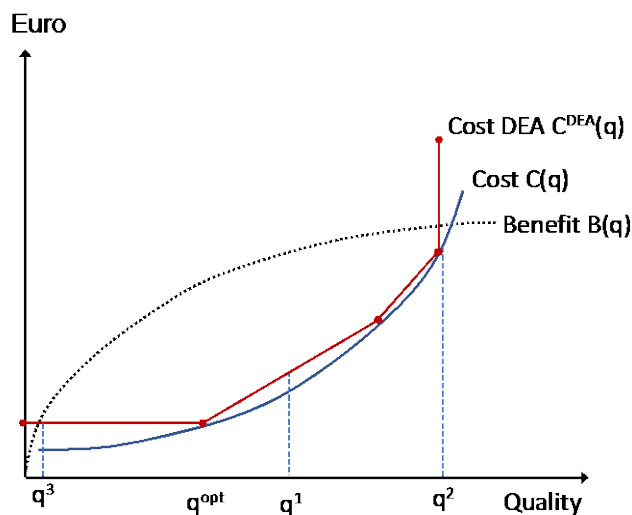


Figure 2-3 Using a DEA-based revenue cap

Three important observations can be made based on this.

First, we note that the resulting revenue function is now convex, while it was concave in all cases in Figure 2-2 above. The firm will, therefore, maximize the difference between a convex revenue $C^{DEA}(\cdot)$ and a convex cost function $C(\cdot)$.

Second, there may be many solutions to the firm's profit maximization problem, and it is unlikely that the optimal quality level will be implemented. In the illustration, the estimated cost function must provide a close approximation of the true cost function around the optimal production level to support near-optimal quality levels such as q^1 .

Third, by using the fact that the cost function will typically have horizontal and vertical parts - or more general non-full facets - it is clear that it may sometimes be optimal to simply choose the minimal possible quality level such as q^3 , while in other cases it may be optimal to choose a very high-quality level, such as q^2 .

In summary, it is intuitively clear that the use of a DEA-based revenue cap is likely to lead to suboptimal endogenous choices of discretionary outputs. DEA-based regulations work well when the outputs are exogenous but not when outputs are discretionary.

We will examine this intuitive insight further below, where we look at a regulation in more detail and examine the incentives to increase quality both analytically and empirically.

3 The Danish regulation of water firms

The specific regulation of Danish water firms has a series of institutional details. For a precise description, see (Konkurrence- og Forbrugerstyrelsen, 2020)³. The core of the regulation is simple, however, based on a traditional RPI-X regulatory framework. The allowed revenue to a firm in period t is determined as

$$R_t = R_{t-1} \cdot (1 - X_{t-1:t}^{ge} - X_{t-1}^{sp}) \quad (1)$$

$$X_{t-1}^{sp} = \frac{(R_{t-1} - \hat{C}_{t-1})}{8} \quad (2)$$

where R_t is the revenue cap, $X_{t-1:t}^{ge}$ is a general efficiency requirement to account for expected price developments and productivity growth from time $t - 1$ to t , and X_{t-1}^{sp} is an individual efficiency requirement that forces inefficient firms to catch up to best practice. The individual efficiency requirement is lagged one year because the regulator cannot obtain the relevant information for the calculations at time t . Finally, \hat{C}_{t-1} is the firm's best practice cost level as determined by the benchmarking model. We will often refer to this simply as the cost norm.

Note that the individual efficiency requirement is divided by 8 because DCCA assumes it takes eight years to meet the full efficiency requirement.

Note also that the specific requirement X_{t-1}^{sp} is not, as is often the case, calculated by comparing the actual costs last period, x_{t-1} and the cost norm \hat{C}_{t-1} and allowing for a certain period to catch up. Instead, the maximum allowed costs, the revenue cap R_{t-1} , are compared with the cost norm and are gradually reduced. In effect, this will force actual costs down as well.

Note that the cost norm is the only element in (1)-(2) that the firms can influence. All other elements are given. Therefore, it is interesting to examine the cost norm when we investigate firms' incentives. The cost norm is calculated in a so-called "best-of-two" benchmarking model, where DCCA uses both a DEA and SFA model, and the highest score from the two models for each firm is used. Our calculations in this paper apply in most cases for both types of models, but for simplicity, we only use DEA in the examples.

DCCA uses 1 input and 2 outputs in the models. The input is the firms' controllable costs (hereafter costs), and the outputs are so-called net volumes. The net volumes can be thought of as aggregations of all the tasks the firms need to undertake. The tasks are split into operational tasks and capital tasks, which give two separate net volumes. For a detailed description, see (Heesche & Asmild, 2020). In this paper, an important property of the net volumes is that DCCA assumes they are fixed. The firms can, therefore, not influence these but only try to reduce the costs. In reality, firms can influence the net volumes to some extent, e.g., by introducing spare capacity via extra assets that are not necessary, but we ignore such blunt approaches to playing the regulations. Instead, we will later focus on the introduction of another explicit discretionary output, quality. The model is input-oriented, and DCCA assumes constant returns to scale.

The firms are not allowed to withdraw profit, but they are allowed to use it inside the firms. Firms can, for example, save the profit to buffer themselves against future costs, or they can use it to allow themselves

³ We ignore some institutional details that are not consequential to the incentives. Only one caveat is important to mention here. The specific efficiency requirement may in theory be negative if industry costs increase or if a firm increases the services it delivers. This possibility is, however, excluded in the regulation. The regulator uses $\max(X_{t-1}^{sp}, 0)$ instead of X_{t-1}^{sp} . A negative efficiency requirement however is rare and will therefore be ignored for now. We return to the problem in Section 0.

some slack. The firms are in general municipalities or cooperatively owned, and some firms argue that they would rather pay back the profit to consumers because they think it is the socially responsible thing to do. In this paper, we assume that the firms are profit maximizing. We discuss an extension to this assumption in section 6.

For simplicity, we suppress the time notation in most of the paper. This does not significantly influence the conclusions. The only 'mistake' is a time lag. The revenue in a given period does not depend on this period's costs, but possibly the costs of the last period. We ignore the need for a one-period discounting to account for this.

Rewriting the revenue cap formula, we can therefore express the allowed revenue as

$$R = R^* \cdot (1 - X_{t-1:t}^{ge}) - \frac{1}{8}R^* + \frac{1}{8}\hat{C}$$

where R^* is the last period's revenue cap and, as such, a constant. The only way that the revenue cap is affected in a given period is therefore via the cost norm \hat{C} .

The cost norm depends on the outputs produced y as well as the costs and the outputs of all the firms, which we can collect in the cost and output matrices \mathbf{X} and \mathbf{Y} . With n firms in the industry, the input matrix is $n \times 1$ and the output matrix is $n \times m$ if we assume that there are m outputs, $y \in R_+^m$. In the present model without quality, we have that

$$\hat{C} = \hat{C}(y|\mathbf{X}, \mathbf{Y})$$

And if we introduce quality q in the model, we have

$$\hat{C} = \hat{C}(y, q|\mathbf{X}, \mathbf{Y}, \mathbf{Q})$$

where \mathbf{Q} is the quality matrix, which is $n \times 1$ when only one quality variable is considered.

If the firms are profit maximizing, they will charge the full revenue cap R in a given year, and since the cost is x , profit Π is simply

$$\Pi = R - x$$

3.1 Cost reduction incentives

If a firm with a fixed output changes its cost x , it will have a direct effect of reducing profit by the same amount. It will also have an indirect effect by affecting revenue. From the definition of the revenue cap, we see that

$$\frac{\partial R}{\partial x} = \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x}$$

Increasing the cost may lead to a higher cost norm and, thereby, less of a reduction in the revenue. Since the difference between the revenue cap and cost norm is only planned to be eliminated over eight periods, the possible revenue gain is only $\frac{1}{8}$ of the increase in the cost norm. Summing up, we have

$$\frac{\partial \Pi}{\partial x} = \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x} - 1$$

and we, therefore, know that firms have strict cost reduction incentives as long as

$$\frac{\partial \hat{C}}{\partial x} < 8$$

When the cost norm is determined by a DEA model, this is always the case. Inefficient firms do not affect the frontier, and for an inefficient firm, we thus have $\frac{\partial \hat{C}}{\partial x} = 0$. Efficient firms may directly set the cost norm in which case we have $\frac{\partial \hat{C}}{\partial x} = 1$. In the few cases where a firm is efficient but not strictly superefficient, i.e., it is located on a facet spanned by other efficient firms, we even have $\frac{\partial \hat{C}}{\partial x} = 0$. Either way, firms have a good incentive to reduce costs when a DEA cost norm is used⁴.

We also note that efficient firms have incentives to reduce their costs only because DCCA divides the efficiency requirement by eight. If DCCA did not do this, $\frac{\partial \hat{C}}{\partial x}$ would need to be less than one before the firms have strict cost-reducing incentives. In this case, the efficient firms would be neutral to a change in their costs as the marginal change in the profit would be zero⁵. If slack, therefore, has some value to the firms, the cost reduction incentives would vanish when the catch-up period is one. As we will show in section 6, however, even with strong preferences for slack, the present regulation would give strong cost reduction incentives when DCCA allows for an eight-year catch-up period.

It is interesting to note how the catch-up period strengthens the cost reduction incentives. The catch-up period is usually thought of as a reflection of the time needed to implement the technical, managerial and organizational changes necessary to implement best practices. The catch-up period, however, also plays another role. It allows the firm to reap the gains from cost reductions for a period of time before the norm catches up. In other words, it serves to reduce the so-called ratchet effect (Milgrom & Roberts, 1992) that may destroy incentives.

3.2 Quality expansion incentives

Let us now turn to the quality incentives. To make the quality decisions explicit⁶, let us assume that, in addition to the nondiscretionary outputs y , there is now a discretionary quality variable q . Additionally, let us assume that there is a cost associated with higher qualities. Let the underlying true costs of providing quality q when the nondiscretionary outputs are y be

$$c^q(q | y)$$

⁴ In the case of an SFA norm, it is theoretically feasible that the marginal impact on the cost norm may be larger than eight and hence deprive the firms of incentives to reduce costs. It is, however, not a likely outcome since it would require a very large change in the estimated SFA function. In the present Danish SFA model, it never happens.

⁵ Note that this is only true in DEA. In SFA, the functional form is not changed too much, the efficient companies typically have $\frac{\partial \hat{C}}{\partial x} < 1$ because part of the cost increase is interpreted as an increase in bad luck (noise term). In addition, the SFA frontier is calculated based on all the companies and not only the efficient ones. A cost increase for a single firm will, therefore, only influence the frontier to some extent.

⁶ In the abstract, we can think of quality as an output and, thereby, one of the y -dimensions.

We assume that larger qualities lead to larger costs⁷, i.e., $\frac{\partial c^q}{\partial q} > 0$.

Since quality is not part of the present cost norm, $\hat{C} = \hat{C}(y|\mathbf{X}, \mathbf{Y})$, it is obvious that firms will have no incentives to provide quality; it will only increase costs, and as we know from Section 3.1, increasing costs will decrease profit for both efficient and inefficient firms. More formally, we have that the derivative of profit with respect to quality is

$$\frac{\partial \Pi}{\partial q} = \frac{\partial R}{\partial q} - \frac{\partial x}{\partial q} = \frac{\partial R}{\partial x} \frac{\partial x}{\partial q} - \frac{\partial x}{\partial q} = \left(\frac{\partial R}{\partial x} - 1 \right) \frac{\partial x}{\partial q} = \left(\frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x} - 1 \right) \frac{\partial x}{\partial q} < 0$$

Hence, as long as quality q does not affect the cost norm, firms will try to reduce quality. We can therefore conclude that DCCA's present regulation gives the desired incentive to reduce costs but gives the wrong quality incentives, which is no surprise since quality is not part of the cost norm.

Let us now see what happens if quality is included in the cost norm, i.e., when $\hat{C} = \hat{C}(y, q|\mathbf{X}, \mathbf{Y}, \mathbf{Q})$. In this case, the revenue depends on both the costs and the quality, $R(x, q)$, and since x depends on q , we obtain

$$\frac{\partial \Pi}{\partial q} = \frac{\partial R}{\partial q} + \frac{\partial R}{\partial x} \frac{\partial x}{\partial q} - \frac{\partial x}{\partial q}$$

The first term is the direct effect of quality on the revenue cap. The second term is the effect on the revenue from the cost increase necessary to increase quality. The last is the direct effect on profit from the extra cost of producing higher quality. We can rewrite this as

$$\frac{\partial \Pi}{\partial q} = \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial q} + \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x} \frac{\partial x}{\partial q} - \frac{\partial x}{\partial q}$$

or similarly

$$\frac{\partial \Pi}{\partial q} = \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial q} + \left(\frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x} - 1 \right) \frac{\partial x}{\partial q} \quad (3)$$

The factor in parentheses is the marginal profit resulting from a marginal cost increase of 1, as we also saw in Section 3.1. We know that it is negative. In the quality formula, it is multiplied by the marginal cost of quality. Last, the first term is the direct impact of quality on the cost norm. It is positive, but it only enters the equation with a factor of $\frac{1}{8}$.

The factor $\frac{1}{8}$ on the $\frac{\partial \hat{C}}{\partial q}$ term points to another interesting impact of the assumed eight periods to catch up in the Danish water model. This leads to much weaker quality incentives since an increase in the estimated underlying costs $\hat{C} = \hat{C}(y, q|\mathbf{X}, \mathbf{Y}, \mathbf{Q})$ from an increase in quality is only expected to be fully accounted for

⁷ We normally think of quality as being positively correlated with costs, but it could also be negatively correlated if the costs to repair quality exceed the costs to achieve high quality. It could, for example, be more expensive to repair a broken pipeline than to properly maintain it. The correlation between quality and costs is discussed in (Heesche & Asmild, 2020).

in eight periods. If the cost norm model predicts that an increase in quality comes at an extra cost of four, the revenue will increase by $\frac{4}{8} = \frac{1}{2}$. The length of the catch-up period therefore negatively affects the incentives to increase quality. On the other hand, it strongly rewards reductions in quality. The regulator only requires the cost to be reduced by $\frac{1}{8}$ of what the cost norm suggests to be saved by reducing the quality level. In addition, there is an indirect benefit if the actual costs decrease. In this case, firms keep the cost reduction except that there will be a small reduction in the cost norm due to the $\frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x}$ factor.

Consider as a small example a case where a firm can increase its quality level by 1 if it spends 1 DKK extra. Likewise, it can save 1 DKK if it reduces the quality by 1. Additionally, let us assume that the cost norm model perfectly depicts these changes. We then have the following changes in profit:

$$\begin{aligned} \text{Increase quality:} & \quad \frac{1}{8} \cdot 1 + \left(\frac{1}{8} \cdot 1 - 1\right) 1 = -\frac{6}{8} \\ \text{Decrease quality:} & \quad \frac{1}{8} \cdot (-1) + \left(\frac{1}{8} \cdot (-1) - 1\right) (-1) = 1 \end{aligned}$$

This shows how the use of a long catch-up period increases the incentives to lower quality. The reduction in quality will be partially forgiven the first seven periods. Similarly, if the firm was to increase quality, it would take seven periods before this was fully accommodated in the revenue cap.

In the next sections, we discuss and illustrate these incentives to lower costs and improve quality using first an illustrative example and then in the context of the Danish DEA model used to define the cost norms of firms.

3.3 Graphical illustrations

To further illustrate the analytical insights above, let us illustrate the relationship between quality, cost and revenue cap, as in Figure 3-1 below. If the general productivity requirement $X_{t-1:t}^{ge}$ is 0, we have

$$R = R^* \cdot (1 - 0) - \frac{1}{8}R^* + \frac{1}{8}\hat{C} = \frac{7}{8}R^* + \frac{1}{8}\hat{C} \quad (4)$$

where R^* is the last period's revenue cap and, as such, a constant. In Figure 3-1, we keep the net volume constant and only consider the impact of changing the quality level and the assumption that the cost norm is a perfect approximation of the true cost function, $\hat{C} = C$. We see that the marginal change in revenue when the quality increase is $\frac{1}{8}$ of the change in the cost norm. If, therefore, the cost norm provides a reasonably good approximation of the true costs, all firms will provide the minimal possible quality level.

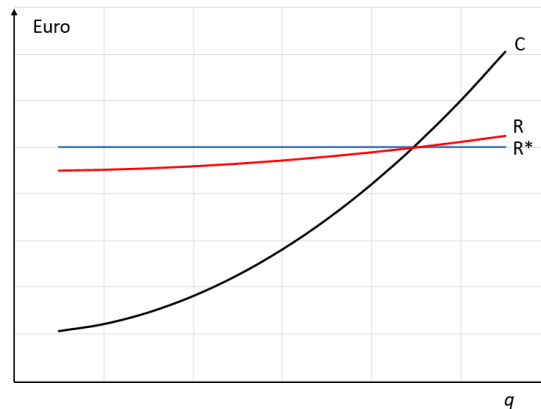


Figure 3-1 Illustrative example

In reality, the cost norm is not a perfect replication of the true, underlying cost function. Instead, it provides an upper bound on the true costs, as in Figure 3-2 below. In this case, and assuming a variable returns to scale (VRS) DEA model, we see that the allowed revenue will be slightly larger (the dotted red piecewise linear curve). It is not in general going to lower the incentives to reduce quality. A firm that increases quality is still only rewarded with $\frac{1}{8}$ of the estimated best practice changes in costs. An alternative strategy for a firm may, however, be to choose a quality level slightly above the highest quality level of the previous period. This corresponds to the movement from A to B in Figure 3-2 below. By doing so, a firm can obtain a much larger marginal increase in revenue.

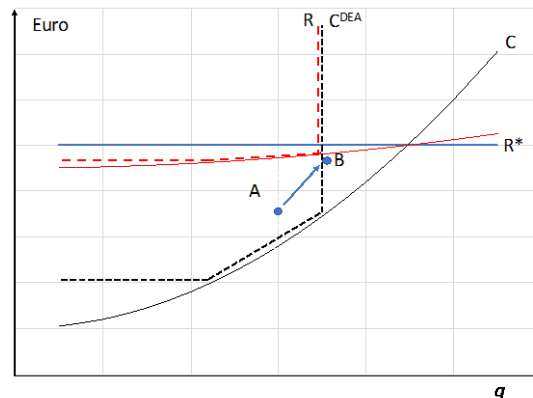


Figure 3-2 Illustrative example with DEA-based cost norms

In Figure 3-3 below, we illustrate the above cases using data from the Danish waterworks 2019, cf. the summary statistics in Table 3.1.

Table 3.1 - Summary statistics

Statistics	N	Mean	St. Dev.	Min	Pctl(25)	Pctl(75)	Max
Costs (in mio. DKK)	71	29.46	29.51	7.03	13.29	31.71	174.61
Quality	71	92.42	3.27	81.92	90.76	94.42	98.63
Net volume (in mio. DKK)	71	29.00	26.79	7.70	14.28	31.93	163.51

We have zoomed in on the lower part of the frontier where we find the most firms. The green facets are the fully dimensional efficient facets⁸, and the grey facets are those that are nonfully dimensional efficient. The blue dots show the efficient firms, and the red dots show the inefficient firms. As an example of quality, we use water wastage. Because water wastage is an undesirable output⁹, we use 100 minus water wastage as a percentage. A value of 92 means that 92% of the water fed into the network is metred with the end consumers.¹⁰

We see that the non-fully dimensional efficient facets will work as a benchmark in the cost direction for several firms. Nevertheless, most of the firms are projected on fully dimensional efficient facets.

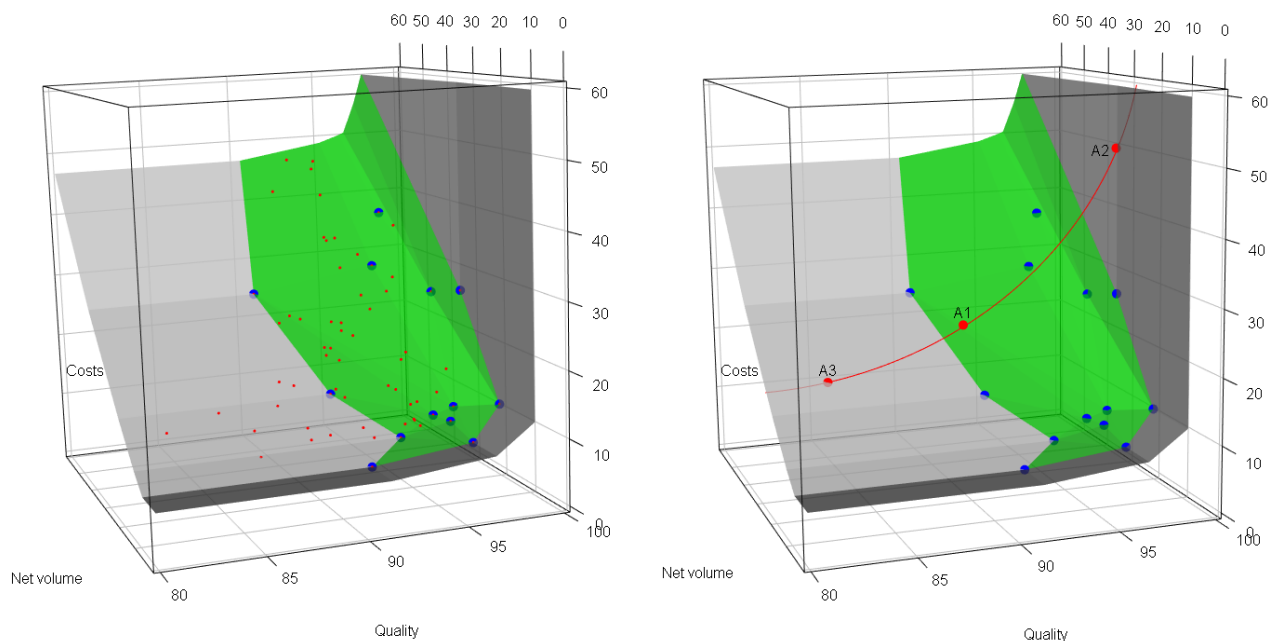


Figure 3-3 DEA-VRS frontier based on reel data and seen from the inside. The green facets are fully dimensional efficient facets, and the red line shows an inefficient firm gradually adjusting its quality.

Consider now an individual firm considering changing its quality level. We assume that net volume is fixed and that changing quality comes with a cost, as illustrated by the red curve.

We start by examining the area around A1. A1 is defined as the lowest level of quality where the firm is benchmarked against a fully dimensional efficient facet.

If the firm chooses to marginally reduce its quality from here, it will now be benchmarked against a nonfully dimensional efficient facet, where the cost norm is constant. The firm, therefore, profits from further reducing its quality - the revenue cap stays constant while the cost reduces. At A3, the firm's costs will be

⁸ A fully dimensional efficient facet is a facet that is estimated based on a convex combination of the observed data together with the assumption of returns to scale but not the assumption of free disposability (Olesen & Petersen, 1996).

⁹ An undesirable output is characterized as an output that is negatively correlated with the input. Hence, it is essentially an input that can be substituted with other inputs.

¹⁰ It can be problematic to use percentage in DEA (Dyson, et al., 2001), but we ignore this, as the specifics are not very important to examine the companies' incentives.

equal to the cost norm, and continuing to lower the quality level will lead to the firm establishing its own cost norm. This means that the revenue cap will also decline, but since the revenue cap is only affected by $\frac{1}{8}$ of the cost norm reduction, it still pays to reduce quality.

If the firm instead considered increasing the quality from A1, it is benchmarked against the fully dimensional efficient facets up to point A2. Between A1 and A2, the incentives are ambiguous. It is possible that the marginal increase in cost is low and that the cost norm increases enough to make the marginal revenue higher than the marginal change in cost. This seems unlikely, but not impossible, since we know that the DEA cost frontier is biased, and the more so, the fewer firms are located in the neighbourhood of A1 and A2, cf., e.g., (Wilson & Simar, 2000). Moreover, in reality, the firms' costs of providing quality are not a smooth function of the quality level. Quality provision may require both fixed and variable costs. A firm may therefore need some starting assets to increase its quality. It will hereafter become marginally less expensive to improve quality until the assets reach their maximum capacity. Hereafter, the firm may need new assets, and so on. In such cases, the possibility of having optimal quality levels somewhere between A1 and A2 becomes more likely since the marginal quality costs may be low and the fixed costs may already be sunk.

Now assume that the firm is considering quality levels around A2, where the firm again meets a nonfully dimensional efficient facet. In this case, the firm may have incentives to increase its quality. If the firm increases the quality up to A2 and thereby is identified as fully efficient, its cost norm will likely make a discrete jump. The firm, therefore, goes from having a low cost norm compared to its actual costs to suddenly having a cost norm that is equal to its costs. Even though the jump in the cost norm is only internalized by the fraction $\frac{1}{8}$, this may suffice to make the increase in quality worthwhile if the marginal quality cost is not too large. It is therefore possible that firms located close to the nonfully dimensional efficient facet will have incentives to increase quality. It is, however, also clear that it will not have incentives to increase quality any further, since after A2, the firm will determine its own cost norm, and only the fraction $\frac{1}{8}$ of the actual marginal cost will be internalized in the revenue cap.

In summary, we know that the firm benefits from lowering quality when it starts at A1. The best option, in this case, is to choose the lowest possible quality level. Between A1 and A2, the firm may have marginal incentives to increase quality if the DEA norm provides a bad approximation of the cost of changing quality. Close to A2, it is likely that the firm may have incentives to increase quality to the A2 level, but it will have no incentives to increase quality above A2.

In our discussions above, we have made a few simplifications compared to the model and the regulation used by DCCA. First, we have assumed that the revenue cap can increase above the old revenue cap. In reality, this is not the case, i.e., the revenue is always capped at R^* . This of course limits the incentives to increase quality further. Second, we have assumed that the DEA-based cost norm relies on variable returns to scale. In reality, however, the model used by DCCA assumes constant returns to scale. Hence, there are no parts of the cost function that go to infinity¹¹. However, due to the existence of nonfully dimensional efficient facets, it is still possible to have a large discrete jump in the cost norm.

¹¹ To see this, assume namely, that a firm has demonstrated the possibility of producing (y^0, q^0) at the cost of x^0 . Now consider a firm producing (y, q) . By the CRS assumption and free disposability, the costs of doing so can never exceed $x^0 \cdot \max\left(\frac{y}{y^0}, \frac{q}{q^0}\right)$.

4 Simulating marginal and discrete quality incentives in Danish water

In this section, we examine in more detail when Danish water firms have incentives to make marginal and discrete changes in the quality level. As in the previous section, we use the firms' costs as input, the sum of the net volumes as a fixed output and water wastage as the quality proxy, which is also an output. We use VRS for illustrative purpose. The summary statistics are given in Table 3.1.

4.1 Marginal quality incentives

Recall from Eq. (3) above that

$$\frac{\partial \Pi}{\partial q} = \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial q} + \left(\frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x} - 1 \right) \frac{\partial x}{\partial q}$$

If a firm is inefficient, it does not affect the best practice cost norm, i.e., $\frac{\partial \hat{C}}{\partial x} = 0$, and therefore, the firm has incentives to increase quality only if

$$\frac{\partial x}{\partial q} \leq \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial q}$$

i.e., only if the firm's marginal cost of increasing quality is at most one-eighth of the marginal cost according to the cost norm. If the firm is fully efficient, we have $\frac{\partial \hat{C}}{\partial x} = 1$, and therefore marginal quality improvements are attractive as long as $\frac{\partial x}{\partial q} \leq \frac{1}{7} \cdot \frac{\partial \hat{C}}{\partial q}$. This does, however, not hold for any efficient companies because their marginal costs with respect to quality are equal to the marginal estimated cost norm with respect to quality, $\frac{\partial x}{\partial q} = \frac{\partial \hat{C}}{\partial q}$.

In Figure 4-1, left panel, we show the cost norm for an efficient firm as its quality increases. The function is derived simply by an iterative process where quality changes in small steps while the net volume and costs are kept fixed. Additionally, in the right panel, we calculate $\frac{\partial \hat{C}}{\partial q}$. Note that the costs of the firm will likely change with the quality as well, but we do not know how much, and we can ignore this as long as the firm is inefficient since then the cost norm is not affected. We stop the iterative process when a firm becomes efficient. To calculate when the firm becomes efficient, we assume that its marginal costs are equal to the marginal costs of the frontier¹². This assumption will only have an influence when the firm becomes efficient and the cost norm reaches this point.

¹² That is, we assume that $\frac{\partial x}{\partial q} = \frac{\partial \hat{C}}{\partial q}$. We do this to get a better approximation of the quality level where efficiency is obtained. As soon as we find that the firm is efficient, we stop examining the incentives. In this way, we still only examine the incentives for an inefficient firm, but we find a more realistic level of quality before it is identified as being efficient.

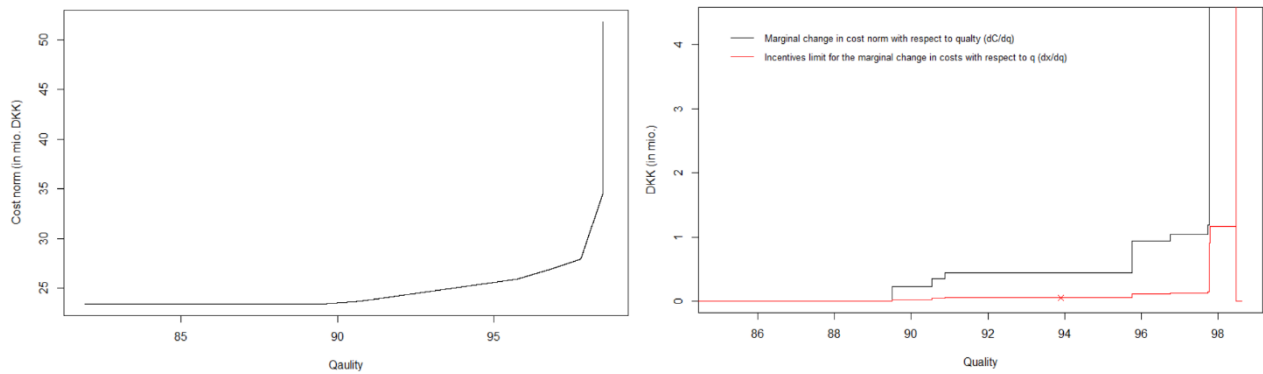


Figure 4-1 Relationship between quality, cost norm, marginal changes in cost norm, and marginal quality cost

Quality goes from the lowest observable level of quality to the highest among all firms. We observe that the difference between the highest and lowest cost norms is approximately 20 mio DKK. This means that if the firm chooses the highest level of quality (the exact level where they become fully efficient), it will have a cost norm that is 84 per cent higher than if it had chosen the lowest level of quality. The level of quality in this model, therefore, has a huge effect on this firm's cost norm and, thereby, potentially also on the profit.

In the right panel, we show the marginal cost norm $\frac{\partial \hat{c}}{\partial q}$ in black and the maximal marginal quality costs $\frac{\partial x}{\partial q}$ in red for which the firm has incentives to marginally increase quality. As shown above, the red curve is $\frac{1}{8}$ of the black curve since the firm has incentives to increase quality as long as $\frac{\partial x}{\partial q} \leq \frac{1}{8} \cdot \frac{\partial \hat{c}}{\partial q}$, c.f. above.

For the first many iterations, the cost norm is constant, $\frac{\partial \hat{c}}{\partial q} = 0$. This is due to the firm being benchmarked against a nonfully dimensional efficient facet. At approximately 89, the cost norm starts to increase. Hereafter, the firm is benchmarked against several different facets, which results in a steeper and steeper slope.

Finally, we observe a huge jump in the cost norm when quality reaches approximately 98. This is because the firm is now identified as being efficient. The size of the jump here depends on the marginal cost of quality and, for the sake of the illustrations, has been assumed to be equal to the marginal costs in the cost norm, $\frac{\partial x}{\partial q} = \frac{\partial \hat{c}}{\partial q}$.

In the right panel, we show not only the marginal change in the cost norm (black) but also $\frac{1}{8} \cdot \frac{\partial \hat{c}}{\partial q}$ (red), which is the highest marginal cost of quality that provides incentives to improved quality. If the firm has a $\frac{\partial x}{\partial q}$ that is lower than the red line, it will have incentives to marginally increase quality in the specific area¹³.

¹³ Note that we have zoomed in, leaving out the highest defined $\frac{\partial \hat{c}}{\partial q}$ and the last jump from Figure 4-1 where the firm goes from being inefficient to efficient.

The firms' present quality level is marked with the red cross. This specific firm has a quality level of 93.9, and it needs a marginal quality level of $\frac{\partial x}{\partial q} < 55,280$ to have incentives to marginally increase quality from its given level.

The greater the firm wants to increase quality, the higher the marginal cost of quality $\frac{\partial x}{\partial q}$ can be. Immediately before it becomes fully efficient (where quality is approximately 98.5), the firm has incentives to increase quality even if $\frac{\partial x}{\partial q}$ is extremely high.

The marginal change in the cost norm differs between the firms based on their net volumes and level of quality. Therefore, the incentives differ as well. The discussion above is an example of the marginal change in the cost norm and the corresponding incentives for one firm. In Figure 4-2, we show the incentives for four other firms. The firms differ in size based on their net volumes. They are selected to represent the 20th, 40th, 60th and 80th percentiles of the net volume values.

The first two firms are both benchmarked to a nonfully dimensional efficient facet. They, therefore, do not have incentives to marginally increase quality. The incentives to marginally increase quality in the last two firms depend on their marginal cost of quality $\frac{\partial x}{\partial q}$. As explained above, it must be below the red line to give strict quality improvement incentives.

Note that the first three firms first become efficient when they have the highest observed quality. Therefore, for these firms, we cannot see the red line going down to zero subsequently, which is, of course, the case if they could increase quality even more.

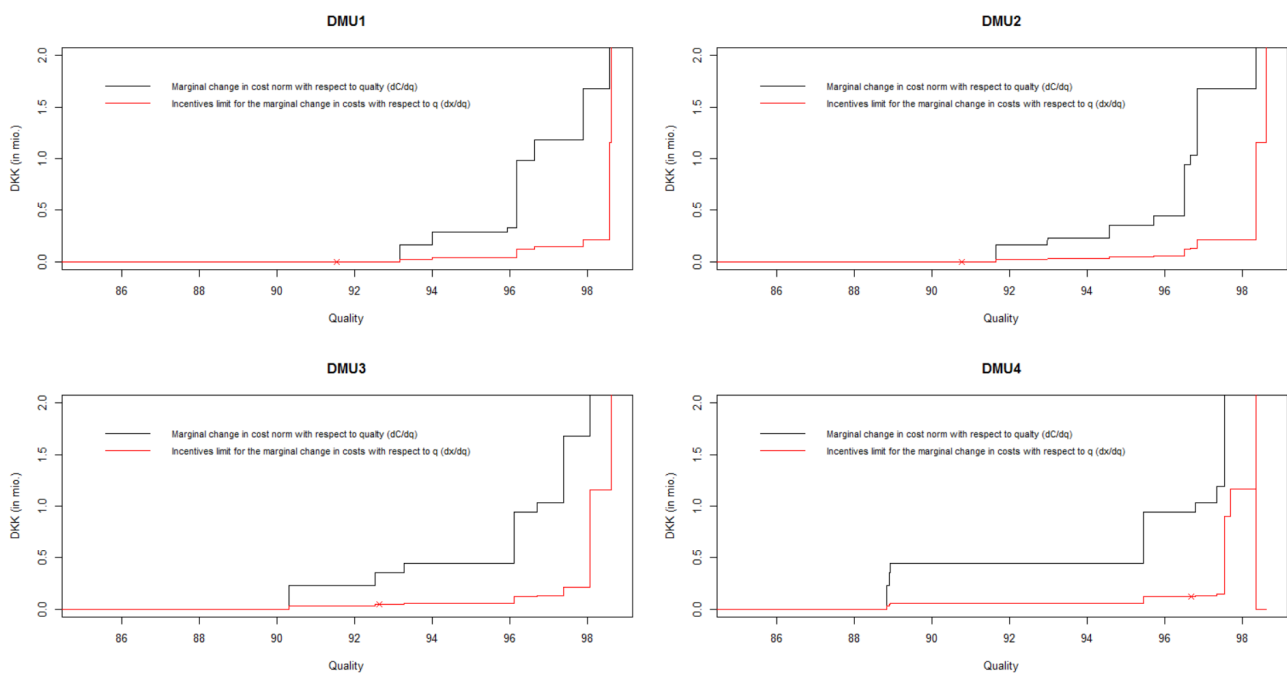


Figure 4-2 Marginal changes in cost norms and marginal quality thresholds for four inefficient firms

4.2 Discrete quality incentives

Above, we examined the incentives to marginally increase quality for five firms.

Unfortunately, the setting does not have the standard textbook regularity of concave revenue and a convex cost function. It, therefore, does not suffice to look at local incentives to determine global incentives. The marginal revenue from quality curves and the marginal cost of quality curves may cross at multiple quality levels.

Truly, we can assume that the cost of increasing quality for an individual firm is convex, but the revenue cap is essentially

$$R = R^* \cdot (1 - X_{t-1:t}^{ge}) - \frac{1}{8}R^* + \frac{1}{8}\hat{C}$$

and therefore, convex as well. This means that a firm considering varying its quality should ideally look at the possible gains from all reductions and expansions of quality to determine the optimal quality level. Put differently, let us assume that a firm initially produces q^* and now considers changing to another quality level q . If it can estimate the change in its cost of producing quality as Δc and the corresponding change in revenue cap as ΔR , where

$$\Delta c = c(q) - c(q^*) \leq \frac{1}{8}(\hat{C}(q) - \hat{C}(q^*)) = \Delta R,$$

and $c(\cdot)$ is the firm's cost of quality for the given net-volume level; then, it is attractive to move from q^* to q . Put differently, the optimal quality level for the firm is determined as the solutions to

$$\max_q \frac{1}{8}\hat{C}(q) - c(q) - \left(\frac{1}{8}\hat{C}(q^*) - c(q^*) \right)$$

If a firm is inefficient and if we believe it is no more efficient in producing quality than the best practice firms are, then there are only two potentially optimal solutions: one is to set quality as low as possible and the other is to make a discrete increase in quality such that the best practice cost of the other firms is infinite, as in Figure 3-2. The advantage of the latter approach is that the best practice cost will now be the costs of the firm in question. Hence, the firm may obtain a discrete jump in the cost norm large enough to justify its extra costs of quality.

To illustrate this idea, we have calculated the increase in quality, say Δq , necessary for each firm to become fully efficient, even though the cost of quality, like the best practice costs, increases up until the last non-Archimedean infinitesimal quality addition. Let us denote the cost level for the firm at this increased quality level q' as $c(q')$. The corresponding increase in the revenue cap is now

$$\Delta R = \frac{1}{8}(c(q') - \hat{C}(q^*))$$

and is generated by a change in the quality of $\Delta q = q' - q^*$. We can therefore say that if it is possible to increase quality from q^* to q' at an average marginal cost less than

$$MC_D = \frac{\Delta R}{\Delta q}$$

then it is attractive to make this discrete jump in quality. The idea is illustrated in Figure 4-3 below.

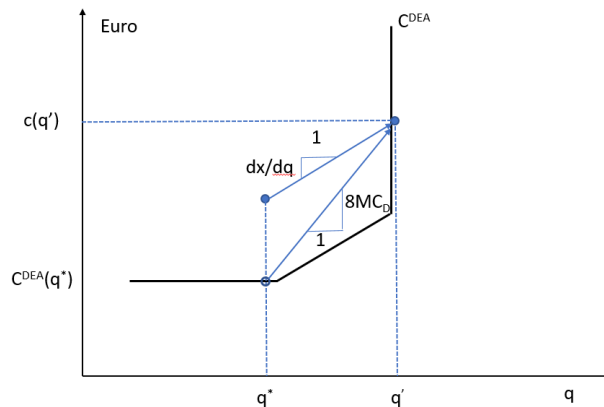


Figure 4-3 Gains from a discrete quality increase

We calculated these values for the different Danish waterworks and illustrated the results in Figure 4-4.

The red dot for a given firm shows the thresholds for the firm's marginal costs below which it is worthwhile to make marginal increases in quality. This value corresponds to the red line over the red crosses in Figure 4-1 and Figure 4-2. The black dots show the discrete marginal cost thresholds, MC_D . If a firm can maintain an average marginal cost below MC_D while increasing quality to make the firm efficient, the firm will have incentives to make this discrete increase in quality. The size of this discrete jump in quality is illustrated with the blue cross.

The figure shows that firms with low quality should not be willing to pay much to increase quality. This is no surprise because they are most likely benchmarked against a nonfully dimensional efficient facet, making marginal gains zero. In addition, their quality should increase considerably for their costs to become efficient, i.e., Δq in the MC_D formula is large.

For some firms, the distance between the black and red dots is high. This occurs when the firm is currently being benchmarked on a facet with low $\frac{\partial \hat{c}}{\partial q}$ but where a relatively small increase in quality Δq suffices to make it efficient. In other words, a small marginal change in quality will only increase the cost norm slightly, but a slightly higher discrete improvement in quality will change the cost norm considerably. Another reason could be that such a firm is highly inefficient with high costs. If such a firm can become efficient by increasing quality, it will likely have incentives to do this, as it will let the cost norm be equal to its high costs.

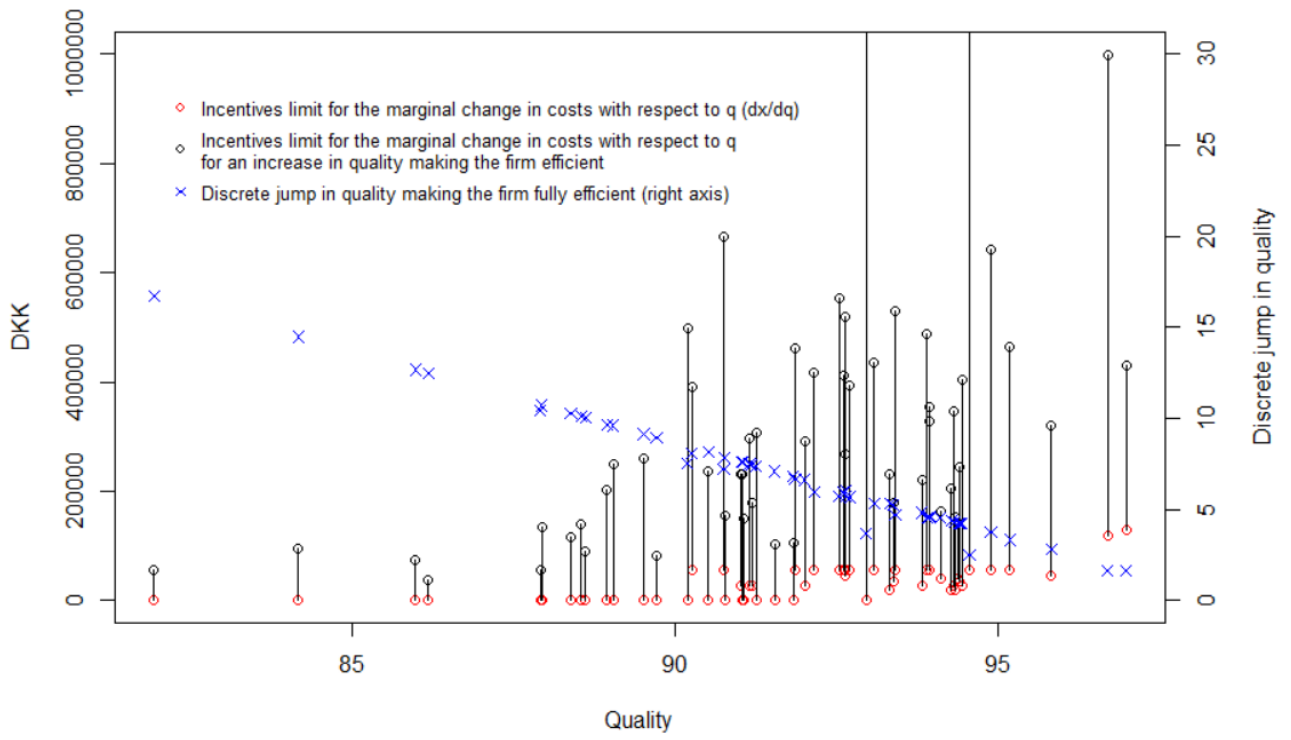


Figure 4-4 Thresholds on marginal quality costs making marginal and discrete quality changes attractive.

5 Dynamic incentives

Thus far, we have focused on firms' myopic, single-period incentives to reduce costs and expand quality. We will now consider the dynamic incentives. What are the incentives to reduce costs and expand quality in a given period when we take into account the effects on the revenue cap in later periods?

For an inefficient firm, the myopic and dynamic incentives are the same since the firm does not influence cost norms and therefore, nor the development of the revenue cap.

For an efficient firm, things are more complex. If an efficient firm improves its performance in one period, it will affect the future revenue caps downwards. The firm, therefore, faces a so-called Ratchet effect - by improving in one period, it makes its own future harsher, which in turn lowers the incentives to improve in the first place.

To analyse the dynamic effects, we can ignore the general productivity requirements since they affect the revenue cap irrespective of the firms' behaviour. We can therefore focus on the key updating rule

$$R_t = \alpha R_{t-1} + \beta \hat{C}_t$$

wherein the case of Danish water, we have $\alpha = \frac{7}{8}$ and $\beta = \frac{1}{8}$.

Assume, first, that an efficient firm lowers its cost with Δx in period 1 and hereafter returns to its original cost level. We will now investigate how this affects the revenue cap. In period 1, the revenue cap is reduced with $\beta \Delta x$. In the next period, the reduction is $\alpha \beta \Delta x$; in the third year, it is $\alpha^2 \beta \Delta x$; in the fourth year, it is $\alpha^3 \beta \Delta x$; etc. In summary, the reduction in the sum of future revenue caps is

$$\beta \Delta x + \alpha \beta \Delta x + \alpha^2 \beta \Delta x + \alpha^3 \beta \Delta x + \dots = \beta \Delta x \frac{1}{1 - \alpha}$$

as long as $\alpha < 1$. If we discount future gains and losses with $\rho \leq 1$, we obtain a loss in future revenue cap values of

$$\beta \Delta x \frac{1}{1 - \rho \alpha}$$

The gain to the firm was a cost reduction of Δx in period 1, and therefore, the total discounted profit effects of the one-period cost reduction are

$$\left(1 - \beta \frac{1}{1 - \rho \alpha}\right) \Delta x$$

Note that when $\beta = 1 - \alpha$, as in the Danish water model, and we assume $\rho = 1$, the accumulated loss over an infinite time horizon is precisely equal to the gain in accumulated costs, Δx . Hence, when there is no discounting, the firm does not have strict incentives to reduce costs. When the discount factor is less than one, $\rho < 1$, then the firm has strict incentives to reduce costs, although the incentives are much less than in the myopic model since it takes 'forever' to approach the old revenue cap¹⁴.

¹⁴ As mentioned earlier, in our analysis we have disregarded the 'no-revenue-cap-increase' restriction, which is also part of the Danish water regulation. In that case, the revenue cap reductions will not increase, i.e., the efficient firm will experience a reduction in revenue cap of $\beta \Delta x$ in each period. It follows that a one-shot cost reduction is not

If, instead of a one-period reduction in cost, the firm introduces a cost reduction from period 1 and onwards, we obtain the same conclusions. Hence, the incentives to reduce in period 2 (following a period 1 reduction) are the same as the incentives to reduce in period 1. The reason is that the period 2 cost reduction will trigger a similar reduction in the cost norm followed by a gradual increase in the cost norm toward the starting point.

In summary, we see that inefficient firms have the same incentives in a multiperiod model as in a single-period model - as long as they stay inefficient. Efficient firms, however, have much weaker incentives to reduce costs and may have no strict incentives to do so if the discount factor is 1.

Now, consider the quality incentives.

As in the case of pure cost reductions, for an inefficient firm, the myopic and dynamic quality incentives are the same since the firm influences neither the cost norm nor the revenue cap in later periods.

Consider now an efficient firm that increases its quality with Δq in the first period and hereafter returns to its original quality. The corresponding increase in costs along the efficient frontier, Δx , will only be recovered with the β factor the first year. Later, however, further gains will materialize since the revenue cap will gradually grow. More precisely, in the first year, the revenue cap increases with $\beta\Delta x$, and in subsequent periods, it increases with $\alpha\beta\Delta x$, $\alpha^2\beta\Delta x$, etc. corresponding to an aggregated gain in revenue cap of $\beta\Delta x \frac{1}{1-\rho\alpha}$ when the discount factor is ρ . Hence, the extra cost of increasing quality is barely recouped over the coming years assuming that the future gains are not discounted (ρ). In other words, even with long-run gains, the quality incentives are very weak.

Reducing quality, however, is more attractive. Truly, it comes not only with a cost reduction of Δx in the first period but also with an accumulated loss in revenue caps of $\beta\Delta x \frac{1}{1-\rho\alpha}$. Hence, in the very long run and when there is no discounting, the gains and losses cancel out.

In summary, the very negative (positive) incentives toward quality improvements (reductions) from our single-period analysis are softened when a dynamic perspective is introduced

attractive unless $\Delta x \geq \beta\Delta x + \rho\beta\Delta x + \rho^2\beta\Delta x \dots$, i.e., a one-shot reduction is only attractive if $\frac{\beta}{1-\rho} \leq 1$, which is equivalent to $\rho \leq 1 - \beta$. With $\beta = \frac{1}{8}$, this corresponds to an interest rate of at least $\frac{1}{7} \approx 14.3\%$.

6 Limitations and extensions

Our analyses above come with several limitations and relevant extensions. Before concluding the paper, let us point to a few limitations and other interesting extensions.

We have examined the incentives to increase quality in a model where quality is either entirely absent from the benchmarking model or is included directly in the benchmarking model. It is important to mention that several other approaches can be used. The most common approach is to have a strict minimum requirement on the quality or to incentivize quality via an add-on payment/penalty to the cost-focused revenue cap scheme. We discussed some alternatives in Section 2.

There are, however, further alternatives that are more akin to the inclusion of quality in the benchmarking model. One possibility is to adjust for quality in a second-stage analysis or to perform a quality adjustment of the traditional volume-based cost drivers such as the net-volume measures in the Danish water regulation. Again, it requires more specific assumptions to examine incentives in such cases, but it seems a worthwhile topic for future research.

Another limitation of our analysis is that we have assumed all firms to have full information. This is not the case in reality. The benchmarking results differ considerably from year to year; therefore, firms cannot determine the exact consequences of changing their level of quality. In our analysis, for example, it will be extremely difficult to find the exact level of quality that will make them efficient. If they try to exploit the possibility of obtaining a discrete "jump" in cost norms where they go from being inefficient to efficient, as discussed in Section 4.2, they risk losing if they do not become efficient.

A few other extensions are also worthwhile mentioning.

First, from the point of view of incentive theory, we have used a relatively naïve model in the sense that we did not have any cost of effort associated with cost reduction. One easy way to remedy this is to assume that firms like slack, i.e., excess spending of resources beyond what is strictly necessary to produce the services. Specifically, we might assume that a firm producing outputs y by spending costs x does so by adding slack s to the underlying true minimal cost $C(y)$,

$$x = C(y) + s$$

and to assume that they are not just interested in maximizing profits but also in benefitting from slack, i.e., by assuming that the firm's objective is to maximize firm utility

$$U = \Pi + \rho \cdot s$$

where the marginal value of slack compared to profit is $\rho < 1$. A similar approach has been used in several other papers on regulations, cf., e.g., Agrell, Bogetoft and Tind (2005) and Bogetoft (1994a, 97, 2000). It is intuitively clear that the gains from slack dampen the incentives to reduce costs and thereby also dampen the incentives to reduce quality since these incentives are derived mainly by cost reductions. To see the first effect, it is easy to see that the marginal gains from changing costs x are now

$$\frac{\partial U}{\partial x} = \frac{\partial \Pi}{\partial x} + \rho = \frac{1}{8} \cdot \frac{\partial \hat{C}}{\partial x} - 1 + \rho$$

The firm, therefore, has incentives to reduce costs as long as

$$\frac{\partial \hat{C}}{\partial x} < 8(1 - \rho)$$

i.e., less often than previously where the condition was $\frac{\partial \hat{C}}{\partial x} < 8$.

Another interesting extension would be to work with superefficiencies instead of efficiencies. In our analysis, we found that efficient firms had weaker incentives in general since a cost reduction leads to a decline in revenue cap. If a firm is only compared to best practices among the other firms, then there is no ratchet effect, i.e., a firm is not penalized in later periods from doing well in a given period. Again, the advantage of superefficiency from an incentive perspective has been emphasized in several of the papers cited above.

A final extension worth considering is the benchmarking of actual costs rather than the revenue cap. The Danish water regulation in each period finds the required savings by benchmarking the revenue cap of the last period again the cost norm,

$$x^{sp\ DW} = \frac{\left(\frac{R - \hat{C}}{R}\right)}{8}$$

In more traditional benchmarking-based revenue cap schemes, the required savings are determined by comparing the actual costs x with the cost norm

$$x^{sp\ TR} = \frac{\left(\frac{x - \hat{C}}{x}\right)}{8}$$

The impact of using the more traditional approach $x^{sp\ TR}$ depends on the revenue cap R . If the revenue cap is above the actual costs, x , the Danish water model requires a larger reduction $x^{sp\ DW}$ of the revenue cap than the traditional approach. If the revenue cap is below the actual costs, x , the Danish water model requires a smaller reduction herein than the traditional approach. It seems, therefore, that the special Danish water variant puts extra cost reduction incentives on very profitable firms while lowering the pressure on firms that are already struggling with a negative profit.

7 Conclusion

In this paper, we have examined how benchmarking-based revenue cap regulations fare when some of the cost drivers are discretionary. As an example, we considered the inclusion of a discretionary quality parameter in the benchmarking model and showed that the incentives to choose socially optimal quality levels are very limited.

At the abstract level, the challenge is that the benchmarking-based revenue cap is a convex function. Hence, a regulated firm faces a convex cost function and a convex revenue function, which in general does not lead to a unique optimal solution. Another general problem is that a regulated firm may choose quality strategically by searching for levels of discretionary outputs where the benchmarking is more lenient.

To obtain more insight, it is useful to analytically and numerically examine a more specific regulation. We, therefore, examined the incentives in the Danish regulatory framework for water firms. As with any other regulation, this regulation has particular features, and we showed how these features affect the incentives.

As in the case of most regulations, the Danish water regulation allows for a catch-up period. We showed that the catch-up period provides strong incentives to reduce costs since firms can keep possible cost reductions for several years before the cost norm fully internalizes the cost reduction potentials. On the other hand, it also gives very weak quality incentives since it takes eight years before the extra cost of increasing quality is fully internalized in the cost norm.

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