

A Service of



Leibniz-Informationszentrum Wirtschaft Leibniz Information Centre

Colas, Mark; Sachs, Dominik

Working Paper

The indirect fiscal benefits of low-skilled immigration

Discussion Paper, No. 281

Provided in Cooperation with:

University of Munich (LMU) and Humboldt University Berlin, Collaborative Research Center Transregio 190: Rationality and Competition

Suggested Citation: Colas, Mark; Sachs, Dominik (2021): The indirect fiscal benefits of low-skilled immigration, Discussion Paper, No. 281, Ludwig-Maximilians-Universität München und Humboldt-Universität zu Berlin, Collaborative Research Center Transregio 190 - Rationality and Competition, München und Berlin

This Version is available at: https://hdl.handle.net/10419/233504

Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.





The Indirect Fiscal Benefits of Low-Skilled Immigration

Mark Colas (University of Oregon)
Dominik Sachs (LMU Munich)

Discussion Paper No. 281

February 26, 2021

The Indirect Fiscal Benefits of Low-Skilled Immigration*

Mark Colas

Dominik Sachs

University of Oregon

University of Munich

February 2, 2021

Abstract

Low-skilled immigrants indirectly affect public finances through their effect on native wages & labor supply. We operationalize this indirect fiscal effect in various models of immigration and the labor market. We derive closed-form expressions for this effect in terms of estimable statistics. Empirical quantifications for the U.S. reveal that the indirect fiscal benefit of one low-skilled immigrant lies between \$770 and \$2,100 annually. The indirect fiscal benefit may outweigh the negative direct fiscal effect that has previously been documented. This challenges the perception of low-skilled immigration as a fiscal burden.

JEL codes: H20, J31, J62, J68

Keywords: Immigration, Fiscal Impact, General Equilibrium

^{*}mcolas@uoregon.edu and dominik.sachs@econ.lmu.de. We would like to thank Daniele Coen-Pirani, Jonathan M.V. Davis, Juan Dolado, Ben Elsner, Axelle Ferriere, Sebastian Findeisen, Lisandra Flach, Mette Foged, Tommaso Frattini, Ulrich Glogowsky, Emanuel Hansen, Bas Jacobs, Gaurav Khanna, Wojciech Kopczuk, Claus Kreiner, Keith Kuester, Fabian Lange, Ben Lockwood, Jonas Loebbing, Abdou Ndiaye, Andreas Peichl, Panu Poutvaara, Florian Scheuer, Monika Schnitzer, Stefanie Stantcheva, Holger Stichnoth, Kjetil Storesletten, Jan Stuhler, Juan Carlos Suárez-Serrato, Uwe Thuemmel, Aleh Tsyvinski, Alessandra Voena, Fabian Waldinger, Nicolas Werquin, Simon Wiederhold, Andreas Winkler and Woan Foong Wong as well as seminar participants at the CEPR Public Economics Symposium "Public Finance: Macro Insights", CESifo Public Sector Economics Area Conference, CRC "Rationality and Competition" Retreat as well as seminar participants at Ben Gurion University, University of Bonn, KU Ingolstadt, University of Pennsylvania, University of Pittsburgh, and University of Regensburg for helpful comments and suggestions. Financial support by Deutsche Forschungsgemeinschaft through CRC TRR 190 (project number 280092119) is gratefully acknowledged. We also thank Mehmet Ayaz, Lea Fricke, Oleksandr Morozov and Taylor Watson for great research assistance.

1 Introduction

Low-skilled immigrants are widely considered a fiscal burden in the United States.¹ In his widely-read blog, Paul Krugman (2006) concludes the following on this issue: "the fiscal burden of low-wage immigrants is also pretty clear... I think that you'd be hard pressed to find any set of assumptions under which Mexican immigrants are a net fiscal plus." The existing empirical evidence supports this perception: a recent National Academy of Sciences (NAS) report on the economic and fiscal consequences of immigration in the U.S. (National Academy of Sciences, 2017) uses state of the art methods to estimate the fiscal impact of immigration to the U.S.² For most of the scenarios that the report considers, low-skilled immigrants have negative effects on public finances. The report was politically influential and cited by Donald Trump in his address to congress in 2017, where he stated: "(a)ccording to the National Academy of Sciences, our current immigration system costs America's taxpayers many billions of dollars a year."³

The NAS report focuses on direct fiscal effects: taxes paid by the immigrants minus costs for benefits and services they receive. It abstracts from indirect fiscal effects: changes in natives' tax payments that result from general-equilibrium effects. The authors write:

"However, a comprehensive accounting of fiscal impacts is more complicated. Beyond the taxes they pay and the programs they use themselves, the flow of foreign-born also affects the fiscal equation for many natives... Because new additions to the workforce may increase or decrease the wages or employment probabilities of the resident population, the impact on income tax revenues from immigrant contributions may be only part of the picture. (National Academy of Sciences, 2017, p.248)

In this paper we analyze these so far neglected indirect fiscal effects. We find that one low-skilled immigrant that enters the U.S. adds between \$770 and \$2,100 annually to public finances through this indirect effect. This outweighs the direct fiscal costs for the more optimistic scenarios of the NAS report and significantly reduces the fiscal burden in the other scenarios. Our results therefore challenge the conventional wisdom of low-skilled immigrants as a fiscal burden.

To make the economic mechanism behind this result transparent, we first consider a simple textbook setup (Borjas, 2014) with two imperfectly substitutable skill levels and exogenous labor supply.⁴ In this setup, low-skilled immigration raises high-skilled wages and lowers

¹Alesina, Miano, and Stantcheva (2018) found that 15% of survey respondents believed that an average immigrant received more than twice as much transfers as the average U.S. citizen. According to a 2019 Gallup poll, the share of Americans that believed immigration made the tax situation worse, was larger than the share who believed immigration made the US worse off in terms of the economy in general, job opportunities, and social & moral values (news.gallup.com/poll/1660/immigration.aspx).

²E.g. they rely on methods used in Auerbach and Oreopoulos (1999), Storesletten (2003), Dustmann and Frattini (2014) and Preston (2014).

³https://www.whitehouse.gov/briefings-statements/remarks-president-trump-joint-address-congress/

⁴We generally use the term "natives" to refer to all individuals already in the country at the time of an immigrant inflow, including foreign-born workers who immigrated earlier. In Sections A.2 and A.4, we distinguish between native-born and foreign-born workers. This distinction has been highlighted as having important wage implications in the more recent literature (Peri and Sparber, 2009; Card, 2009; Ottaviano and Peri, 2012; Manacorda, Manning, and Wadsworth, 2012; Dustmann, Schönberg, and Stuhler, 2016).

low-skilled wages. Consequently, tax payments of high-skilled natives increase whereas tax payments of low-skilled natives decrease. If immigrants are paid their marginal product, what they contribute to aggregate income is equal to what they receive. Therefore, they affect the distribution of native income, but not the overall size of national income accruing to natives. Hence, what the low-skilled natives lose is what high-skilled natives gain. As a consequence, tax revenue from natives increases if high-skilled individuals face higher marginal tax rates than low-skilled individuals. We show that this effect boils down to the size of the wage effects as measured by the own-wage elasticity of low-skilled labor and the progressivity of the tax system as measured by the difference in the marginal tax rates of the two skill types.⁵

We then turn to our main model specification that includes two major extensions. First, workers can respond to immigrant inflows via both intensive and extensive labor supply adjustments. The labor supply responses of natives also induce wage effects, which mitigate the initial wage shocks. Further, they have fiscal consequences themselves; if immigration decreases native labor force participation, e.g., this would decrease tax revenue. Second, we enrich the heterogeneity and assume that individual productivity levels are continuously distributed conditional on skill, as in the "canonical model" (Acemoglu and Autor, 2011). We also allow for labor supply elasticities to differ with income, gender and family status.⁶

The endogenous labor supply decision of natives creates a nontrivial fixed point problem. We follow Sachs, Tsyvinski, and Werquin (2020) and formalize this fixed point problem in terms of integral equations. We show that the indirect fiscal effect can be expressed as a closed-form expression of estimable statistics: own-wage elasticities, income-weighted averages of (i) labor supply elasticities, (ii) marginal effective tax rates, as well as (iii) products of participation (marginal) tax rates and extensive (intensive) marginal labor supply elasticities – all conditional on skill level. Component (i) captures mitigation of wage effects by native labor supply responses. Component (ii) captures fiscal effects from the changes in relative wages holding labor supply fixed as described above. Component (iii) captures fiscal effects that arise from changes in native labor supply.

We evaluate this formula for the indirect fiscal benefit by combining data from the American Community Survey (ACS), the 1979 National Longitudinal Survey of Youth (NLSY79), and the Survey of Income and Program Participation (SIPP). We use the tax calculator TAXSIM to assign effective tax rates to each individual in our main dataset, the ACS. Immigration can also affect social security and welfare transfers received by natives, but TAXSIM does not

⁵High-skilled immigration also leads to indirect fiscal effects. Since low-skilled immigration is much more politically controversial, we focus on low-skilled immigrants. As we discuss in the conclusion, high-skilled immigrants could lead to indirect fiscal effects through their effect on productivity and innovation, in addition to their effect on relative wages and labor supply.

⁶E.g. Dustmann, Schönberg, and Stuhler (2016, p. 44) emphasize that "wage and employment responses need to be studied jointly to obtain an accurate picture of the labor market impacts of immigration". These authors also highlight that it is important to allow for labor supply responses that vary between different groups of natives. Dustmann, Schönberg, and Stuhler (2017) demonstrate the importance of this heterogeneity in labor supply responses empirically in the German context.

account for welfare-transfer programs nor does it account for future social security receipts. We therefore use the SIPP to estimate Supplementary Nutrition Assistance Program (SNAP) and Temporary Assistance for Needy Families (TANF) receipts as a function of income and household characteristics. We use the NLSY79 and the ACS to understand how changes in current income, combined with the distribution of the individual's earnings over the life cycle, affect their receipt of social security payments in the future. Another main component of the empirical quantification regards the labor supply elasticities along both the intensive and the extensive margin. We consider different values from the empirical literature and allow these elasticities to vary with family structure, gender and income.

Combining our empirical quantification of the model with our closed-form solutions for the indirect fiscal effect, we find that the indirect fiscal effect of one low-skilled immigrant is \$770-\$1,470 per year if we consider a plausible range for the elasticity of substitution between high and low-skilled labor (Card, 2009). We set these numbers into relation to the direct fiscal effects as reported by the National Academy of Sciences (2017). The report considers a number of scenarios which vary the marginal cost of public goods and the education of the immigrant. In almost all cases, the direct fiscal effect is negative and of a similar magnitude to the indirect fiscal effects we calculated. In some of the scenarios, accounting for the indirect fiscal costs of immigrant turns the *total* fiscal effect from a fiscal burden to a fiscal surplus.

Robustness There is some controversy in the literature over the appropriate model to analyze and estimate the wage effects of immigration. A natural concern is that the indirect fiscal effects are also sensitive to these modeling choices. Therefore, we extend our model to allow for a variety of different production functions and labor supply responses. These extensions and the associated indirect fiscal effects are summarized in Table 1. First, we consider three alternative production specifications that have been utilized in the immigration literature: 1) production with four imperfectly substitutable education groups and imperfect substitutability between experience levels, as utilized by Borjas (2003), 2) production with imperfectly substitutable foreign-born and domestic-born workers, as in Ottaviano and Peri (2012), and 3) production where skills are defined by an individual's position in the wage distribution, rather than their education, as in Dustmann, Frattini, and Preston (2013). We show that our formula extends naturally to these more elaborate production technologies. For all three specifications, we find annual indirect fiscal effects of the average low-skilled immigrant in the range of \$1,000 to \$1,870. When we use the same elasticity of substitution between skill levels in all three specifications, the indirect fiscal effects all lie within \$250 of each other.

Next, we consider a model with endogenous task supply as in Peri and Sparber (2009).⁷ In the model, low-skilled workers may react to additional low-skilled immigration by 'upgrading'

⁷See also Foged and Peri (2016) and Patt, Ruhose, Wiederhold, and Flores (2020) for evidence of native task supply responses to immigrant inflows. Llull (2018) highlights the importance of occupation adjustments in mitigating the wage effects of immigration on natives.

Specification	Indirect Effect	Section	Main Reference/Source of Estimates
Simple Textbook Model	\$1,104	Section 2	Borjas (2014)
Canonical Model		Sections 3 - 5	Acemoglu and Autor (2011), Card (2009)
Exogenous Native Labor Supply	\$975		
Intensive Margin Adjustments	\$1,113		Chetty (2012), Bargain, Orsini, and Peichl (2014)
Extensive Margin Adjustments	\$1,074		u
Both Intensive and Extensive	\$1,186		u
Education and Experience Groups	\$1,873	Section A.1	Borjas (2003)
Domestic- and Foreign-Born Complementarity	\$1,065	Section A.2	Ottaviano and Peri (2012)
Skills by Position in Wage Distribution	\$1,017	Section A.3	Dustmann, Frattini, and Preston (2013)
Endogenous Task Supply	\$2,131	Section A.4	Peri and Sparber (2009)
Decreasing Returns to Scale	\$1,057	Section A.5	Burnside (1996)

Table 1: Estimates of annual indirect fiscal effect of one low-skilled immigrant under different model specifications. For the "Simple Textbook Model" and the "Canonical Model" we use our results associated with an elasticity of substitution between high-skilled and low-skilled workers of 2, the central value we use in our quantification. For the "Canonical Model" with labor supply adjustments, we display our results with common labor supply elasticities. For all specifications, we show the indirect effect for the average low-skilled immigrant. See text for details on each specification.

their occupation. We find an indirect fiscal benefit of over \$2,130 in this framework, roughly half of which is due to occupation upgrading of domestic-born workers.

Finally, we calculate the indirect fiscal effect when production exhibits decreasing returns to scale. When production exhibits decreasing returns to scale, immigrant inflows not only change the relative wages between imperfectly substitutable worker groups, but also increase firm profits at the cost of total worker compensation. We show that this additional effect can be accommodated with an additional term in our indirect fiscal benefits formula which accounts for this shift in distribution of national income from workers to firms. Using an estimate of marginal profit tax rates, we show that the indirect fiscal effect with decreasing returns is unlikely to be significantly different from the case with constant returns to scale.

Welfare Effects We also show how the indirect fiscal effects change the overall picture of welfare. We show that the welfare effects of low-skilled immigration can be decomposed into four components: 1) direct fiscal effects, 2) increases in wage inequality, 3) tax mitigation effects – which capture how the increase in inequality is dampened by the progressive tax-transfer system and 4) fiscal externalities – the indirect fiscal effects arising from labor supply responses of natives to immigrant inflows.

Effects 1) and 2) are well understood. Effect 1) has been studied extensively in the literature and effect 2) has been alluded to in many studies and the political debate.⁸ Our contribution

⁸For example, Borjas (2016, p. 191) writes: "Although the mythical average person may be unaffected, immigration creates many winners and losers. [...] immigration turns out to be just another government redistribution program." Card (2009b, p. 1) writes: "These immigrants presumably compete for the same jobs held by the least-skilled native workers, contributing to a trifecta of economic factors – technology, trade and immigration – that are thought to have led to a rise in skill differentials in the US economy since the late 1970s." Krugman (2006a) notes the following in a New York times Op-Ed: "Because Mexican immigrants have much less education than the average U.S. worker, they increase the supply of less-skilled labor, driving down the wages of the worst-paid Americans".

here is to apply recent methods in public economics (Saez and Stantcheva, 2016; Hendren, 2020) to quantify the welfare loss associated with the increase in inequality. We show that the size of these welfare losses is very sensitive to how (i) domestic-born versus previous immigrants are weighted in the welfare function⁹ and (ii) whether immigrants and natives are substitutes or complements conditional on skill. E.g. for the framework and estimates of Ottaviano and Peri (2012), which incorporate complementarity between domestic- and foreign-born workers, we find that effect 2) is actually positive for domestic-born individuals – while inequality increases among domestic-born, the average wage among domestic-born natives increases sufficiently to outweigh the increase in inequality.

Effects 3) and 4) are the novel elements that our paper adds to the literature. They capture the welfare effects resulting from the interplay of low-skilled immigration and native tax payments and are directly tied with the indirect fiscal effect. For our main model, we find that they imply an additional, so far neglected, welfare gain between \$789 and \$1,166.¹⁰

To sum up, quantifying the overall welfare effect of low-skilled immigration is difficult because the decision of how to weigh domestic-born versus previous immigrants is a thorny normative issue whose discussion goes beyond the goals of this paper. Perhaps even more difficult is how to weigh the utility of *potential* immigrants. The welfare gains of immigrating to the United States for low-skilled individuals are likely to be very large, given that low-skilled immigrants experience massive income gains after moving to the United States (Hendricks and Schoellman, 2018). Therefore, the welfare effects of immigration are sensitive to how previous and potential immigrants are weighted in comparison to natives. The sensitivity of the conclusion regarding welfare effects contrasts with our findings on the indirect fiscal effects which are very robust across the different models. We therefore put a much stronger emphasis on the fiscal effects than on the welfare effects in this paper.

Related Literature The literature that studies the fiscal effects of immigration has primarily focused on the direct fiscal effect. Preston (2014) provides a comprehensive overview on the topic. Economists have employed a variety of methods to measure this direct fiscal impact of immigration. Borjas and Hilton (1996) quantify how much more likely immigrants are to participate in welfare programs. Dustmann and Frattini (2014) provide a detailed accounting approach for the UK and find that EEA (non EEA) immigrants on average contributed more (less) to public finances than public costs they cause. They emphasize the importance of accounting for the use of public goods and potential congestion externalities.¹¹

⁹The choice of welfare weights is generally a normative question. Alesina, Miano, and Stantcheva (2018, Figure 13) find that less than 40% of Americans agree to the following statement "The government should care equally about everyone living in the country whether born there or not".

¹⁰These numbers correspond to the case where labor supply is elastic along both the extensive and intensive margin and elasticities are set according to Chetty (2012).

¹¹Ruist (2015) estimates the fiscal burden of refugee immigration to be 1% of GDP in Sweden. Monras, Vázquez-Grenno, and Elias (2018) find that a policy which legalized 600,000 undocumented immigrants in Spain led to increases in payroll tax revenues, which includes both direct and indirect fiscal effects.

Storesletten (2000) takes a model-based perspective and quantifies the net present value of fiscal contributions of an immigrant as a function of age and education for the U.S. Storesletten (2003) provides a similar calculation for Sweden. Relatedly, several papers use quantitative equilibrium models to study the welfare effects of immigration in the presence of progressive taxation (Chojnicki, Docquier, and Ragot, 2011; Battisti, Felbermayr, Peri, and Poutvaara, 2018; Busch, Krueger, Ludwig, Popova, and Iftikhar, 2020). Indirect fiscal effects are present in these models. Our contribution is to explicitly work out the size of the indirect fiscal effects and the mechanism behind it. While such indirect fiscal effects have been mentioned previously, the conjecture was that the effects are of second order compared to the direct fiscal effects.¹²

This paper is also related to a large literature on the effects of immigration on natives wages. A number of papers find that low-skilled immigration leads to increases in wages inequality, but there is less consensus on which workers bear the largest incidence of low-skilled immigration (see e.g. Card (1999), Borjas (2003), Ottaviano and Peri (2012), Dustmann et al. (2013)). Among other things, the different results come from different assumptions on skill stratification (2 vs. 4 education levels or the wage percentile as skill measure)¹³ and the assumptions of whether natives and immigrants, conditional on skill, are (im)perfect substitutes.

Further, a smaller literature emphasizes the importance of labor supply and employment responses in understanding the effects of immigration (Borjas, Freeman, and Katz, 1997; Peri and Sparber, 2009; Dustmann, Schönberg, and Stuhler, 2016; Llull, 2018; Piyapromdee, 2020; Monras, 2020). We show analytically how endogenous labor supply choices mitigate the wage changes but also have fiscal effects in itself. Further, we rely on this large empirical literature to guide our modeling decisions while also doing justice to the fact that there is some disagreement in the empirical literature over the appropriate model to analyze the effects of immigration. We show that our main results are robust to different modeling choices and parameter estimates from the empirical immigration literature.

Roadmap In Section 2 we use a simple benchmark model to illustrate the mechanism behind the indirect fiscal effect transparently. Section 3 presents our main quantitative model and Section 4 presents our empirical quantification. Section 5 presents our main quantitative results. In Section 6, which evaluate the indirect fiscal effects under various alternative environments. Section 7 discusses further issues and Section 8 concludes.

¹² Preston (2014, p. 580) writes "(w)hile interesting, the implied tax effects are not plausibly large relative to the effects that will be found by a simple accounting approach."

¹³Card (1999) finds that the overall impact of immigration to the United States on wage inequality has been small. This is largely due to the fact that the skill composition of immigrants is similar to that of natives. Therefore, immigration overall has not lead to large changes in factor ratios in the United States. This does not imply that low-skilled immigration in isolation does not affect inequality. In fact, the value of the elasticity of substitution that we use in our main model are those that are favored by Card (1999).

2 The Simple Benchmark Model

To highlight our result transparently, we start with the simple textbook model for the impact of immigration on native wages (Borjas, 2014; Bodvarsson and Van den Berg, 2009). Consider an economy that is populated by individuals that are either high-skilled or low-skilled. The mass of low-skilled individuals is N_s . Denote individual labor supply by h_u and h_s . Production of the single consumption good, whose price is normalized to one, is described by a constant returns to scale production function $Y = F(\mathcal{L}_u, \mathcal{L}_s)$ where $\mathcal{L}_u = N_u h_u$ and $\mathcal{L}_s = N_s h_s$ denote the aggregate labor of each respective skill level. We assume that low- and high-skilled labor are imperfect substitutes in production of the single final good, the price of which is normalized to one. In equilibrium, profits are zero and wages are equal to marginal products, i.e. $w_e = \frac{\partial F}{\partial \mathcal{L}_e}$ for e = u, s. Finally, denote income of the two types of workers by $y_s = h_s w_s$ and $y_u = h_u w_u$ and denote aggregate income of the skill levels by $Y_s = y_s N_s$ and $Y_u = y_u N_u$.

For simplicity, we consider a very stylized tax system. τ_u is the tax rate on low-skilled income and τ_s is the tax rate on high-skilled income, where $\tau_u < \tau_s$ is a stylized way of capturing tax progressivity. Further, let C_u and C_s represent per-person costs which do not depend on income, representing, for example, public goods or schooling costs associated with each low- and high-skilled individual, respectively. Tax revenue in this economy is given by

$$\mathscr{R} = N_u \left(\tau_u y_u - C_u \right) + N_s \left(\tau_s y_s - C_s \right).$$

In the following, we formally study how tax revenue \mathscr{R} changes due to a small influx of low-skilled immigrants dN_u . This influx has a direct fiscal effect

$$d\mathcal{R}_{dir} = (\tau_u y_u - C_u) \times dN_u. \tag{1}$$

One low-skilled immigrant contributes $(\tau_u y_u - C_u)$ to the public budget. As stated above, this direct fiscal effect has already received much attention in the literature and is not the subject of this paper.¹⁴

The immigration influx also has an indirect fiscal effect. Given that labor of different skill levels are imperfect substitutes in production, the increase of the low-skilled (high-skilled) workforce by dN_u decreases (increases) the wage of low-skilled (high-skilled) workers and therefore their tax payment. We are interested in the sum of these two effects, which reads as

$$d\mathscr{R}_{ind} = N_u h_u \tau_u \frac{\partial w_u}{\partial N_u} dN_u + N_s h_s \tau_s \frac{\partial w_s}{\partial N_u} dN_u. \tag{2}$$

¹⁴The report of the National Academy of Sciences (2017) includes federal, state and local taxes, incarceration costs, scholarship and student loan costs, education costs, government healthcare costs, veteran's benefits, refugee support costs, public good costs, and a variety of federal and state level transfer programs in their calculation of direct fiscal effects.

The following lemma helps to relate the size of the wage increase of the low-skilled and the wage increase of the high-skilled.

Lemma 1. If the production function is characterized by constant returns to scale, then aggregate native labor income is unchanged:

$$N_{u}h_{u}\frac{\partial w_{u}}{\partial N_{u}}dN_{u} + N_{s}h_{s}\frac{\partial w_{s}}{\partial N_{u}}dN_{u} = 0$$

$$\Rightarrow \gamma_{s,cross} = |\gamma_{u,own}| \times \frac{w_{u}\mathcal{L}_{u}}{w_{s}\mathcal{L}_{s}},$$
(3)

where $\gamma_{u,own}$ is the own-wage elasticity of low-skilled labor and defined by $\gamma_{u,own} = \frac{\partial w_u}{\partial \mathcal{L}_u} \frac{\mathcal{L}_u}{w_u}$ and $\gamma_{s,cross}$ is the cross-wage elasticity of high-skilled labor and defined by $\gamma_{s,cross} = \frac{\partial w_s}{\partial \mathcal{L}_u} \frac{\mathcal{L}_u}{w_s}$.

Proof. Note that with constant returns to scale one has $F(N_u h_u, N_s h_s) = w_u N_u h_u + w_s N_s h_s$. Differentiating both sides w.r.t. to N_u and using $\frac{\partial F}{\partial \mathscr{L}_u} = w_u$ yields the result.

Intuitively, immigrants obtain their marginal product and do not affect the size of the overall pie accruing to natives. Immigrants only affect the distribution of the pie between high- and low-skilled natives. The income loss of one group equals the income gain of the other group.¹⁵ This relation is formally given by (3) and it provides a direct relation between the cross-wage elasticity of high-skilled labor $\gamma_{s,cross}$ and the own-wage elasticity of low-skilled labor $\gamma_{u,own}$. Based on Lemma 1, we can easily simplify the indirect fiscal effect and rewrite it as stated in the following proposition.¹⁶

Proposition 1. If native labor supply is exogenous, the indirect fiscal effect of low-skilled immigration dN_u is given by

$$d\mathcal{R}_{ind} = (\tau_s - \tau_u) \times |\gamma_{u,own}| \times y_u \times dN_u. \tag{4}$$

Proof. First, note that (3) implies $N_s h_s \frac{\partial w_s}{\partial N_u} = -N_u h_u \frac{\partial w_u}{\partial N_u}$. Inserting this into the indirect fiscal effect as defined in (2) yields:

$$d\mathcal{R}_{ind} = N_u h_u \tau_u \frac{\partial w_u}{\partial N_u} dN_u - \tau_s N_u h_u \frac{\partial w_u}{\partial N_u} dN_u = (\tau_u - \tau_s) \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} h_u dN_u,$$

which then yields (4).

The formula for the indirect fiscal effect (4) is very simple and allows for a straightforward interpretation.¹⁷ Since the change in overall income of natives is unaffected as shown in

¹⁵If the immigration influx is not infinitesimal, then there would indeed be an immigration surplus, i.e. aggregate native labor income would increase. However, the immigration surplus would be second order compared to the distributional implications, see e.g. (Borjas, 2014, Chapter 7).

¹⁶As discussed in Footnote 5, we focus on low-skilled immigration since it is more politically controversial. However, it is straightforward to do the analysis for high-skilled immigrants, where the formula would read as $(\tau_u - \tau_s) \times |\gamma_{s,own}| \times y_s \times dN_s$.

¹⁷A result that may be surprising, is that it is independent of the size of the native population. To understand this intuitively, consider two countries where skills are distributed in the same way, but the first

Lemma 1, the change in tax payment of natives would be zero if $\tau_s = \tau_u$. However, if taxes are progressive ($\tau_s > \tau_u$), aggregate tax payment of natives increases. High-skilled individuals, whose income increases, are taxed at a higher rate than low-skilled individuals, whose income decreases. The size of the effect is proportional to low-skilled income and the own-wage elasticity of low-skilled wages.¹⁸

Formula (4) allows for a straightforward quantification. As a normalization, we set $dN_u = 1$, i.e. we normalize it to one marginal immigrant. For a CRS production function, the own-wage elasticity is given by $\gamma_{u,own} = \frac{N_S y_s}{N_u y_u + N_S y_s}$, where σ is the elasticity of substitution, which we assume to be in [1.5, 2.5] (Card, 2009). Importantly, as we show in Appendix B.1, this relation does not require the elasticity of substitution to be constant – we are not imposing a CES production function. To quantify this, we use data from the 2017 American Community Survey (ACS). Average earnings of high school and college-education were $y_u = \$36,079$ and $y_s = \$67,432$, respectively. Further, we know that the share of workers with and without college education was .65 and .35.¹⁹ As a final step, we need to quantify $\tau_s - \tau_u$. We take the approximation of the U.S. tax code by Heathcote, Storesletten, and Violante (2017) which implies $\tau_s = 0.254$ and $\tau_u = 0.180$. This implies that the indirect fiscal effect is given by

$$d\mathcal{R}_{ind} \in [828, 1380].$$

This is a sizeable number even if we consider the lower range of wage effects (i.e. $\sigma = 2.5$).²⁰ This indicates that the indirect fiscal effect should not be ignored in policy discussions. We will now be more serious about its calculation and address various shortcomings of this simple model. First, wage effects are likely to be smaller since native labor supply (or native behavior more generally – they may move or change their occupation) is endogenous. Second, the production structure is simplistic in the sense that all workers of the same skill level have exactly the same productivity. Other production structures may be equally likely: e.g. even conditional on skill, natives and immigrants may be imperfect substitutes. Further, one can change the assumptions about the elasticity of capital supply (which was implicitly assumed

country is twice as large as the second. In the first country, the wage changes of natives due to one immigrant are smaller by a factor of two – one immigrant is 'smaller' in relative terms in country 1 as compared to country 2. However, at the same time, there are twice as many natives whose tax payment is affected in country 1. Thus, the fiscal effect is the same in both economies.

¹⁸Note that the increase in tax revenue comes at the cost of native net incomes. However, in modern welfare analysis income gains of different individuals and tax revenue are not weighted equally and therefore this redistribution between individuals and the government has first-order welfare effects (Hendren, 2020), see also our discussion in Section 3.2. Additionally, when we account for endogenous labor supply of natives in the next sections, low-skilled immigration causes fiscal externalities which also have immediate welfare implications (Hendren, 2015).

¹⁹Throughout the paper, we follow Borjas (2003), Peri and Sparber (2009), and Ottaviano and Peri (2012), and define low-skilled workers as those without any college experience and define high-skilled workers as workers with at least some college experience. In Appendix D.3, we consider an alternative skill classification, in which we divide workers with some college between the two skill groups as in Katz and Murphy (1992) or Card (2009). In Section A.3, we define worker skills by their position in the wage distribution, rather than their education.

²⁰We find $d\mathcal{R}_{ind}$ =\$1,104 given our intermediate value for the elasticity of substitution of $\sigma = 2$.

to be infinite so far), returns to scale and perfect competition. Finally, the tax function considered here is too simplistic.

We address these issues one by one. First, in the next section, we move to what we consider our main or benchmark model. We extend the simple model by (i) allowing for a continuum of productivities (and therefore income levels) conditional on skill and (ii) accounting for endogenous labor supply of natives along the extensive and intensive margin. In Section 4, we introduce our quantification of the tax-transfer system, which accounts for social security payments and welfare receipts in addition to income and payroll taxes. In Section 6, we then consider the robustness of the results for the other mentioned issues like skill-stratification, occupational choice of natives, imperfect substitutability of natives and immigrants etc.

3 The Main Model: Heterogeneity and Endogenous Labor Supply of Natives

We generalize the findings from the previous section in two important ways. First, we consider the so-called canonical model (Acemoglu and Autor, 2011) with two skill levels (corresponding to individuals with and without college education), and a continuous distribution of productivity for each skill level. We also allow individuals to differ in other variables that may affect their tax payment. Second, we account for endogenous labor supply of natives along both the extensive and the intensive margin. We introduce the additional heterogeneity and show how the formula for the indirect fiscal effect in Proposition 1 extends to this setting in Section 3.1. We then extend the setting to endogenous labor supply of natives in Section 3.2.

3.1 Incorporating Heterogeneity

An individual is indexed by its type $i \in \mathcal{I}$. A type contains many characteristics. First, individuals differ in their skill level $e_i \in \{u, s\}$. Second, they differ in their productivity ω_i . Third, they differ in terms of their tax payments: even if they have the same income, they may face a different tax schedule because of family status, living in a different state etc. Finally, different types differ in their participation rates ν_i and their labor supply elasticities: ε_i is the hours elasticity, η_i is the participation elasticity and $\xi_i = \varepsilon_i + \eta_i$ is the total hours elasticity. Denote by $L_i = h_i \nu_i m_i$ aggregate labor of type i, where h_i is hours worked of type i and m_i is the measure of type i. We first focus on the case of exogenous labor supply of natives and therefore set $\varepsilon_i = \eta_i = 0$ and $\nu_i = 1$ for all i. In Section 3.2, we remove this assumption.

Aggregate effective labor of each skill level is given by:

$$\mathscr{L}_e = \int_{\mathcal{I}_e} L_i \omega_i di$$

for $e \in \{u, s\}$, where \mathcal{I}_u (\mathcal{I}_s) is a subset of \mathcal{I} made up of low-skilled (high-skilled) types.

The production function reads as $\mathscr{F}(\mathscr{L}_u,\mathscr{L}_s)$ and we assume constant returns to scale. Wages are equal to marginal products $(w_e = \frac{\partial \mathscr{F}}{\partial \mathscr{L}_e})$ and aggregate income is given by $Y_e = w_e\mathscr{L}_e$. Hence, an individual of type i has gross income $y_i = h_i\omega_i w_{e_i}$, where the latter element, the skill price w_e is endogenous w.r.t. the skill ratio, $\frac{\mathscr{L}_s}{\mathscr{L}_u}$. We again define the own-wage elasticities $\gamma_{e,own} = \frac{dw_e}{d\mathscr{L}_e} \frac{\mathscr{L}_e}{w_e}$ and the cross-wage elasticities $\gamma_{e,cross} = \frac{dw_e}{d\mathscr{L}_{e'}} \frac{\mathscr{L}_{e'}}{w_e}$ with $e \neq e'$. The following lemma generalizes the relationship between the own- and cross-wage elasticities given by Lemma 1 to this setting.

Lemma 2. The cross- and own-wage elasticities are related through:

$$\gamma_{s,cross} = |\gamma_{u,own}| \times \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s}.$$

Before we show how Proposition 1 extends to this setting, we need to specify the tax and transfer system. We incorporate a flexible nonlinear tax and transfer system T(y, i) that maps a tax payment (which could be negative, i.e. transfer receipt) to each level of gross income y and type i. Proposition 1 generalizes as follows:

Proposition 2. Assume that labor supply of natives is exogenous. The fiscal effect of one immigrant of type i with low education (i.e. $e_i = u$) is given by:

$$d\mathcal{R}_{ind}^{ex}(i) = |\gamma_{u,own}| \times y_i \times (\bar{T}_s' - \bar{T}_u'), \qquad (5)$$

where \bar{T}'_e is the income-weighted average marginal tax rate of education group e.

Proof. See Appendix B.2.1.
$$\Box$$

The formula is very similar to the formula in Proposition 1 but there are two differences. First, we have to specify not only the education level of the immigrant but also the type i and therefore the income y_i . A type with higher income y_i supplies a greater amount of effective labor and therefore has a larger effect on native wages. Second, since there are more than two marginal tax rates in this economy, the objects of interest are the income-weighted average marginal tax rates of the two skill groups. Intuitively, wages of all college (high-school) workers increase (decrease) by the same factor. An individual with a higher income level will therefore experience a larger absolute change in earnings. To calculate the fiscal effect, the marginal tax rate of an individual with a higher income therefore receives a higher weight.

3.2 Incorporating Endogenous Native Labor Supply

With endogenous labor supply, the changes in the wages for low- and high-skilled labor affect labor supply decisions along the intensive and extensive margin of workers with non-zero elasticities. The implied changes in labor supply, in turn, affect the equilibrium wages again, which then triggers a change in labor supply and so on and so forth. All these adjustment effects will imply additional fiscal effects.

To formalize this, as a first step, note that tax revenue is formally given by:

$$\mathscr{R} = \int_{\mathcal{I}_u} \left(T(y_i, i) \nu_i + T(0, i) (1 - \nu_i) \right) m_i di + \int_{\mathcal{I}_s} \left(T(y_i, i) \nu_i + T(0, i) (1 - \nu_i) \right) m_i di,$$

where T(0, i) is the effective tax paid by type i if they earn zero income. The following lemma states how tax payments of natives change due to low-skilled immigration.

Lemma 3. Consider a low-skilled immigrant with effective labor supply L^{Im} that implies equilibrium changes in wages of $\frac{dw_u}{w_u}$ and $\frac{dw_s}{w_s}$. The implied change in tax payment of natives is given by:

$$d\mathcal{R}_{ind} = \int_{\mathcal{I}_u} T'(y_i, i) y_i \frac{dw_u}{w_u} (1 + \varepsilon_i) \nu_i m_i di + \int_{\mathcal{I}_s} T'(y_i, i) y_i \frac{dw_s}{w_s} (1 + \varepsilon_i) \nu_i m_i di + \int_{\mathcal{I}_u} T_{part}(y_i, i) y_i \frac{dw_u}{w_u} \eta_i \nu_i m_i di + \int_{\mathcal{I}_s} T_{part}(y_i, i) y_i \frac{dw_s}{w_s} \eta_i \nu_i m_i di,$$

$$(6)$$

where $T_{part}(y_i) = \frac{T(y_i,i)-T(0,i)}{y_i}$ is the participation tax rate of a type i individual that earns y_i .

Proof. See Appendix B.2.2.
$$\Box$$

In the first line, the indirect fiscal effects as described in Proposition 1 are scaled up by the intensive margin elasticities. The second line of (6) captures the change in tax revenue due to changes in labor force participation of natives. Note that the relevant tax rate here is not the marginal tax rate, but the participation tax rate. The participation tax rate captures the increase in public finances that occurs if the individual starts to work.

An important issue, however, is that the wage changes $\frac{dw_u}{w_u}$ and $\frac{dw_s}{w_s}$ are endogenous w.r.t. to the labor supply responses. To obtain an expression for these wage changes and hence obtain a closed form solution, we follow Sachs, Tsyvinski, and Werquin (2020) and formalize the associated fixed point in terms of integral equations.²¹ First, note that these equilibrium wage changes can be divided into the effects arising from immigrant inflows, low-skilled native labor supply responses, and high-skilled native labor supply responses as

$$\frac{dw_u}{w_u} = \gamma_{u,own} \frac{L^{Im}}{\mathcal{L}_u} + \gamma_{u,own} \int_{\mathcal{I}_u} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_u} dj + \gamma_{u,cross} \int_{\mathcal{I}_s} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_s} dj.$$
 (7)

The first term captures the wage change induced by immigration directly since $\frac{L^{Im}}{\mathcal{L}_u}$ captures the relative increase in effective low-skilled labor supply due to one immigrant with effective labor L^{Im} . The second term captures the own-wage effects implied by the change in low-skilled aggregate labor of natives and the third term captures the cross-wage effects implied by the

²¹Sachs, Tsyvinski, and Werquin (2020) study nonlinear tax reforms in a general equilibrium setting with endogenous labor supply and also highlight that a decrease in the skill ratio can trigger tax revenue effects in the case of progressive taxation.

change in high-skilled aggregate labor. Similarly, the equilibrium wage change for high-skilled workers is given by

$$\frac{dw_s}{w_s} = \gamma_{s,cross} \frac{L^{Im}}{\mathcal{L}_u} + \gamma_{s,cross} \int_{\mathcal{I}_u} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_u} dj + \gamma_{s,own} \int_{\mathcal{I}_s} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_s} dj.$$
 (8)

How the equilibrium changes in relative wages translate into labor supply changes directly follows from the definition of labor supply elasticities. The integral equations that describes the relative change in total hours worked for low-skilled workers can therefore be written as:

$$\forall i \in \mathcal{I}_u : \frac{dL_i}{L_i} = \xi_i \left(\gamma_{u,own} \frac{L^{Im}}{\mathcal{L}_u} + \gamma_{u,own} \int_{\mathcal{I}_u} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_u} dj + \gamma_{u,cross} \int_{\mathcal{I}_s} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_s} dj \right). \quad (9)$$

The bracket on the right hand side captures the equilibrium change in the relative wage $\frac{dw_u}{w_u}$. The relative change in labor supply of type i individuals is then simply given by the total hours elasticity ξ_i multiplied with the relative wage change. Equivalently, for high-skilled labor, the integral equation reads as

$$\forall i \in \mathcal{I}_s: \frac{dL_i}{L_i} = \xi_i \left(\gamma_{s,cross} \frac{L^{Im}}{\mathscr{L}_u} + \gamma_{s,cross} \int_{\mathcal{I}_u} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathscr{L}_u} dj + \gamma_{s,own} \int_{\mathcal{I}_s} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathscr{L}_s} dj \right). \tag{10}$$

The expressions given by (9) and (10) constitute a system of integral equations. In Appendix B.2.3 we derive the following result on the wage changes in general equilibrium.

Lemma 4. Consider a small influx of a low-skilled immigrant with effective labor L^{Im} . The equilibrium changes in wages are described by

$$\frac{dw_u}{w_u} = \frac{\gamma_{u,own}}{1 + \bar{\xi}^u | \gamma_{u,own}| + \bar{\xi}^s | \gamma_{s,own}|} \frac{L^{Im}}{\mathcal{L}_u}$$

$$\frac{dw_s}{w_s} = \frac{\gamma_{s,cross}}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \frac{L^{Im}}{\mathcal{L}_u},$$

where $\bar{\xi}^u$ and $\bar{\xi}^s$ are the income-weighted total hours elasticities of the two skill groups.²²

Proof. See Appendix B.2.3.
$$\Box$$

Note that absent native labor supply responses, an immigrant inflow leads to percentage low-skilled wage change of $\frac{d\hat{w}_u}{w_u} = \gamma_{u,own} \frac{L^{Im}}{\mathcal{L}_u}$ and a percentage high-skilled wage change of $\frac{d\hat{w}_s}{w_s} = \gamma_{s,cross} \frac{L^{Im}}{\mathcal{L}_u}$. We'll refer to these wage effects without labor supply responses as "first-round effects". This lemma shows that, with labor supply responses, the changes in equilibrium wages are given by these first-round effects scaled by $\frac{1}{1+\xi^u|\gamma_{u,own}|+\xi^s|\gamma_{s,own}|} < 1$, capturing how much these first-round effects are mitigated by labor supply responses. Greater labor supply responsiveness, as measured by the income-weighted total hours elasticities of the different

²²Formally, these are given by $\bar{\xi}^e = \frac{\int_{\mathcal{I}_e} y_i (\eta_i + \varepsilon_i) \nu_i m_i di}{Y_{\cdot}}$ for $e \in \{u, s\}$.

groups, implies a larger mitigation of the first round effects. This effect plays an important role because it mitigates the indirect fiscal effects that follow from the wage changes.

However, in addition to mitigating wage effects, the labor supply changes of natives also have fiscal implications themselves. The changes in equilibrium hours, participation, and aggregate labor supply directly follow from Lemma 4 and the definition of the elasticities

$$\forall i \in \mathcal{I}_e : \frac{dh_i}{h_i} = \varepsilon_i \frac{dw_e}{w_e}, \quad \frac{d\nu_i}{\nu_i} = \eta_i \frac{dw_e}{w_e}, \quad \frac{dL_i}{\nu_i} = \xi_i \frac{dw_e}{w_e}$$

for $e \in \{u, s\}$ and where $\frac{dw_e}{w_e}$ is defined as in Lemma 4.

We now combine Lemma 2, Lemma 4, and these equilibrium labor supply changes to rewrite the expression in Lemma 3 and obtain our main result.

Proposition 3. The indirect fiscal effect of a low-skilled immigrant of type i is given by:

$$d\mathscr{R}_{ind}(i) = \frac{y_i \times |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \Biggl(\bar{T}_s' - \bar{T}_u' + \overline{\varepsilon_s T'_s} - \overline{\varepsilon_u T'_u} + \overline{\eta_s T_{part,s}} - \overline{\eta_u T_{part,u}} \Biggr),$$

where

$$\frac{\overline{\eta_e T_{part,e}}}{\overline{\gamma_e T_{part,e}}} = \frac{\int_{\mathcal{I}_e} T_{part}(y_i, i) y_i \eta_i \nu_i m_i di}{Y_e}$$

is the income-weighted average of the product of the participation tax rate and the participation elasticity of education group e and

$$\overline{\varepsilon_e T_e'} = \frac{\int_{\mathcal{I}_e} T'(y_i, i) y_i \varepsilon_i \nu_i m_i di}{Y_e}$$

is the income-weighted average of the product of of the marginal tax rate and the hours elasticity of education group e.

Proof. See Appendix B.2.4.
$$\Box$$

How does this formula differ from that in Proposition 2? First of all the indirect fiscal effect is scaled down by $\frac{1}{1+\bar{\xi}^u|\gamma_{u,own}|+\bar{\xi}^s|\gamma_{s,own}|}$ since the wage effects are mitigated. Second, in addition to the difference of the income-weighted marginal tax rates $\bar{T}'_s - \bar{T}'_u$, the formula accounts for the fiscal effects caused by native labor supply responses, which can be thought of as fiscal externalities. The term $\overline{\varepsilon_s T'_s}$ captures that high-skilled natives increase their hours worked and pay more taxes while $\overline{\varepsilon_u T'_u}$ captures that low-skilled natives decrease their hours worked and pay less taxes. The term $\overline{\eta_s T_{part,s}}$ ($\overline{\eta_u T_{part,u}}$) captures the increase (decrease) in labor force participation of high-skilled (low-skilled).

We can decompose the indirect fiscal effect into the effect arising from differences in relative wages and the fiscal externalities as

$$d\mathcal{R}_{ind}(i) = \text{RelWages}(i) + \text{FiscExternalities}(i)$$

where

$$\text{RelWages}(i) = \frac{y_i \times |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \left(\overline{T'_s} - \overline{T'_u}\right),$$

and

$$FiscExternalities(i) = \frac{y_i \times |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \left(\overline{\varepsilon_s T'_s} - \overline{\varepsilon_u T'_u} + \overline{\eta_s T_{part,s}} - \overline{\eta_u T_{part,u}} \right). \tag{11}$$

These fiscal externalities have different welfare implications than the indirect fiscal effects that come from changes in relative wages holding labor supply fixed in that they capture efficiency gains for the natives. We now describe this in greater detail.

3.3 Welfare Effects

We now briefly describe how the indirect fiscal effect affects the overall picture of welfare. Characterizing the welfare effects is difficult, as low-skilled immigration leads to winners and losers. The welfare effects therefore depend crucially on how the social planner weighs the utility of different income groups, foreign-born versus domestic-born workers, and, perhaps more difficultly, on potential immigrants versus individuals in the United States. The welfare gains of low-skilled immigrants are likely to be very large, given that low-skilled immigrants experience massive income gains after moving to the United States (Hendricks and Schoellman, 2018). In what follows, the welfare calculation do not account for the welfare gains of the immigrants themselves. We get back to the issue of welfare gains of immigrants themselves in Section 5.3.

Concretely, let g(i) denote the welfare weight of individual i, such that g(i) gives the increase in social welfare – measured in units of public funds – associated with a one unit increase in income for individual i. These weights are normalized such that on average they are equal to one and one is the weight on government revenue (Saez and Stantcheva, 2016). The welfare surplus associated with one low-skilled immigrant is given by Proposition 4.

Proposition 4. The weighted surplus accruing to natives for one low-skilled immigrant is given by:

$$Surplus_{weighted}(i) =$$

$$d\mathcal{R}_{dir}(i) + \text{FiscExternalities}(i) + \text{Distributional}(i) + \text{TaxMitigation}(i),$$

where

Distributional(i) =
$$\frac{y_i \times |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \times \left(\overline{g_s} - \overline{g_u}\right)$$
,

$$\text{TaxMitigation}(i) = \frac{y_i \times |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \times \left(\left(\bar{T}'_s - \overline{g_s (T'_s)} \right) - \left(\bar{T}'_u - \overline{g_u (T'_u)} \right) \right),$$

and where $d\mathcal{R}_{dir}(i)$ is the direct fiscal effect, FiscExternalities(i) is the fiscal externality as defined by (11), $\overline{g_e}$ is the income-weighted average of the welfare weights conditional on skill e and $\overline{g_e(T'_e)}$ is the income-weighted average of the product of the welfare weights and marginal tax rates conditional on skill e.

Proof. See Appendix B.2.5.
$$\Box$$

Recall that the fiscal externality is the additional tax revenue generated by native labor supply responses. Note that the fiscal externality term would be zero if (i) labor supply of natives were exogenous or (ii) the tax system were proportional and labor supply elasticities were common between low- and high-skilled workers. The endogeneity of labor supply combined with the progressivity of the tax system jointly imply a welfare surplus: while the labor supply responses do not directly affect native welfare due to the envelope theorem, they affect native welfare through their implied indirect fiscal effects.

The term Distributional(i) captures the mechanical distributional effects between high-skilled and low-skilled natives resulting from the change in relative wages. These distributional effects are partially mitigated by the tax system, as captured by the term TaxMitigation(i). In particular, the term $\left(\bar{T}'_e - \overline{g_e}(T'_e)\right)$ captures that an increase (decrease) in wages for high-skilled (low-skilled) is partially offset by the tax code. We now consider two special cases for the welfare weights.

Kaldor-Hicks Immigration Surplus. The "immigration surplus", an application of the Kaldor-Hicks compensation test (Kaldor, 1939; Hicks, 1939, 1940), is a leading approach to study welfare in the immigration literature (see e.g. Borjas (2014)). The immigration surplus measures whether the natives hurt by immigration could hypothetically be compensated by those who benefit and is given by the sum of government revenue and the monetized gains and losses of all the natives. Note that the immigration surplus is simply a special case of the welfare effect in Proposition 4 with g(i) = 1 for all i. In this case, the welfare effect is simply given by the direct fiscal effects plus the fiscal externality. Both the distributional effects and tax mitigation effects are equal to zero because each dollar would be valued equally regardless of whether it accrues to high-skilled natives or low-skilled natives or to the government. The fact that this surplus is non-zero beyond the direct fiscal effect is novel.

Inverse-Optimum Weights. In our quantification, we calculate the welfare effects of immigration using the so-called inverse optimum weights as in Hendren (2020). These are the welfare weights for which the current U.S. tax-transfers system is optimal according to optimality conditions from the optimal income tax literature. Hendren (2020) shows that by using these weights, one can extend the Kaldor-Hicks surplus to account for distortionary costs of

compensation.²³ If the welfare effect is positive with such weights, then a Pareto improvement can be achieved because the losers can be compensated.²⁴

For the U.S., Hendren (2020) calibrates a weight function which is generally decreasing in income and thus gives higher weight to low-skilled than high-skilled individuals. For such weights, low-skilled immigration will lead to negative distributional effects because the income losses of low-skilled receive a higher weight than the income gains of high-skilled.

Additionally, we consider the effects of immigration on domestic-born welfare, in which the utility of previous immigrants are not weighted in welfare calculations. We use the weights from Hendren (2020) to weight domestic-born utility and normalize the weights such that they are equal to one on average.

4 Empirical Quantification

To quantify the formula of Proposition 3, we need earnings distributions conditional on education. Further, we need to know marginal and participation tax rates as well as labor supply elasticities along the earnings distributions. Note that even conditional on education and income, there is a distribution of tax rates and elasticities since family status, age, location, etc. are also determinants of an individual's tax burden and labor supply elasticity. Finally, we need a value for the own-wage elasticity of low-skilled wages.²⁵

In Section 4.1, we make assumptions on parameters such as labor supply elasticities for different groups and wage elasticities. The calibrated values are based on existing empirical evidence.

Regarding the values of marginal and participation tax rates, we conduct our own empirical analysis.²⁶ To obtain our sample of natives, we use data from the American Community Survey (ACS). To assign effective marginal and participation tax rates to all individuals in the sample, we make use of NBER's TAXSIM. However, TAXSIM does not account for the effective tax rates that are implied by welfare-transfer programs. Programs like the Supplementary Nutrition Assistance Program (SNAP) or Temporary Assistance for Needy Families (TANF) imply an increase in effective marginal tax rates since transfers are phased out as

²³Going one step further, Tsyvinski and Werquin (2019) generalize the compensation principle to a setting where distortive taxes also imply general equilibrium effects on wages, which creates a complicated fixed-point problem. The authors analytically describe the tax reform that achieves compensation in such a setting.

²⁴One underlying assumption that this can be achieved with a standard tax schedule, is that for a given income level, all individuals are affected in the same way. This assumption is apparently violated in our model where at a certain income level, both low and high-skilled individuals are present and hence compensating policies would need to condition on skill.

²⁵The raw data and code necessary to calculate effective marginal tax rates for all individuals in the ACS, calculate the income-weight effective tax rates, and calculate the main results in Table 3 are available for download at https://sites.google.com/site/markyaucolas/research.

²⁶The Congressional Budget Office estimates effective marginal tax rates for low- and medium- income workers in the U.S. (Congressional Budget Office, 2015). We cannot use their estimates directly as they only provide the median, 10th and 90th percentile of marginal tax rates for different income groups. Further their calculations do not include workers with income over 450% of the Federal Poverty Line and do not account for TANF of SSI payments.

income increases. To account for this, we use data from the Survey of Income and Program Participation (SIPP). With the SIPP, we estimate effective transfer phase-out rates conditional on household size and income. Another important detail that is not captured in TAXSIM is that the payroll tax is not a pure tax because higher earnings imply not only higher taxes but also higher benefits when retired (see e.g. Feldstein and Samwick (1992)). Accounting for this requires estimates of individuals' life-cycle earnings, which determine how current income affects future social security benefits. To predict the life-cycle earnings paths of the individuals in our sample, we make use of panel data from the NLSY79. We describe all the sample selection in Section 4.2 and the effective tax rate calibration in Section 4.3.²⁷

4.1 Calibrated Parameters

Wage Elasticities The own-wage elasticity of low-skilled labor can also be written as

$$\gamma_{u,own} = -\frac{1}{\sigma} \kappa_s,$$

where σ is the elasticity of substitution between high-skilled and low-skilled individuals and κ_s is the income share of high-skilled labor, which we estimate as $\kappa_s = .79$, using our ACS sample (see description in the next section). For σ , Card (2009) concludes that values are likely to be between 1.5 and 2.5, which implies own-wage elasticities ranging from -.51 ($\sigma = 1.5$) to -.31 ($\sigma = 2.5$) for these two polar cases.²⁸ The own-wage elasticity of high-skilled labor is given by

$$\gamma_{s,own} = -\frac{1}{\sigma} \kappa_u,$$

where κ_u is the income share of low-skilled labor. For our range of values for σ , this implies own-wage elasticity for high-skilled workers ranging from -.14 ($\sigma = 1.5$) to -.08 ($\sigma = 2.5$).

Labor Supply Elasticities A number of papers emphasize that labor supply elasticities differ across genders, marital statuses, and income levels but few papers have actually estimated these elasticities across the income distribution for both genders. We therefore employ three different approaches to calibrate our labor supply elasticities. As a first pass, we assume all individuals have common intensive and extensive labor supply elasticities. Specifically, we set the intensive margin elasticity of $\varepsilon_i = .33$ and an extensive margin elasticity of $\eta_i = .25$, for all individuals i, based on the pooled estimates in Chetty (2012).²⁹ Next, we allow labor

²⁷Our quantification could be extended to account for the taxation of interest and pension income, estate taxes and government sponsored healthcare for natives. Accounting for income and pension income and estate taxes would likely lead to larger indirect fiscal effects, given higher savings rates of high-skilled individuals and the progressivity of estate taxes. Accounting for government sponsored heathcare for natives would lead to smaller indirect fiscal effects as Medicaid and the Affordable Care Act subsidies are means tested.

²⁸Katz and Murphy (1992), for example, find an elasticity of substitution of 1.4. Card and Lemieux (2001) estimate an elasticity of substitution between 1.15 and 1.6 in their pooled sample of men and women.

²⁹In fact, these numbers of Chetty (2012) refer to compensated, Hicksian elasticities while the elasticities in our formulas are uncompensated elasticities. As argued e.g. by Chetty et al. (2013), uncompensated elasticities

supply elasticities to vary by gender and marital status. We use estimates of gender and marital status specific intensive and extensive labor supply elasticities from Bargain, Orsini, and Peichl (2014), who estimate a discrete choice model to estimate elasticities. Finally, we consider the scenario in which labor supply elasticities can vary by gender, age, and income. For this we use estimates of intensive and extensive labor supply elasticities by gender, marital status and quintile of the income distribution from Bargain, Orsini, and Peichl (2014).³⁰

Other parameters. We assume that agents start receiving social security at age 66. We assume the real discount rate for the government to be 1%.³¹ Finally, the formula in Proposition 3 shows that the income of the immigrants also plays a role beyond the education status. Since the exact income of an immigrant is not foreseeable before an immigrant has entered the country, we consider the case of taking expected immigrant income as reasonable. Using again data from the ACS, we find that the average annual gross income of a low-skilled immigrant worker in our sample is \$30,317. We also consider the indirect fiscal effects of high school dropout immigrants and high school graduate immigrants, who have average incomes of \$25,861 and \$33,442, respectively.

4.2 Data and Sample

ACS Our main data source is the 2017 ACS, which includes information on income and demographics for a nationally representative sample of 1% of the U.S. population. As is standard, we focus on individuals between 18 and 65 years old and eliminate individuals living in group quarters. In order to ensure that we can accurately determine an individual's tax-filing status, we limit our sample to heads of households and their spouses. This leaves us with a sample of over 1.2 million individuals.³² We utilize data on each individual's earnings, income from other sources, marital status, age, location, number and ages of children, and age and income of the individual's spouse, all of which determine an individual's tax liability and eligibility for various tax credits and deductions.³³ We also utilize data on each individual's

are likely to be only slightly smaller than compensated elastiticies as microeconometric evidence shows income effects are small. Accounting for this would push our results below in Table 3 with endogenous labor supply closer to the values with exogenous labor supply in the same table.

³⁰The intensive and extensive labor supply elasticities from Bargain, Orsini, and Peichl (2014) are reported in Appendix C.4. We choose to utilize the labor supply estimates from Bargain, Orsini, and Peichl (2014) because they estimate gender and income specific intensive and extensive margin elasticities using a common estimation procedure. Our results are very similar if we use estimates on extensive labor supply elasticities by wage percentile from Juhn, Murphy, and Topel (2002), who estimate extensive margin elasticities using a sample of U.S. men.

³¹The real interest rate on 30 year bonds was on average 0.99 (0.81) in the last ten (five) years. See https://home.treasury.gov/policy-issues/financing-the-government/interest-rate-statistics. We show our main results under the assumption of a 2% interest rate in Appendix D.2

³²Additional details on sample selection in the ACS are included in Appendix C.1.

 $^{^{33}}$ Top wage incomes are underrepresented in most survey data sets. We therefore append Pareto tails to the wage income distribution, starting at the highest wage income value that is not top-coded in each state, as is relatively common practice in the optimal tax literature (Piketty and Saez, 2013). We assume a shape parameter of $\alpha = 1.5$.

education, which we use to determine an individual's skill group. An important choice is how to define these skill groups. For this, we follow Borjas (2003), Peri and Sparber (2009), and Ottaviano and Peri (2012), and define low-skilled workers as those without any college experience and define high-skilled workers as workers with at least some college experience.³⁴

Figure 1 shows the density of individual earnings for high-skilled and low-skilled workers given our baseline definition of skills. Overall, low-skilled individuals have average earnings of \$35,600 while high-skilled individuals have average earnings of \$65,800.

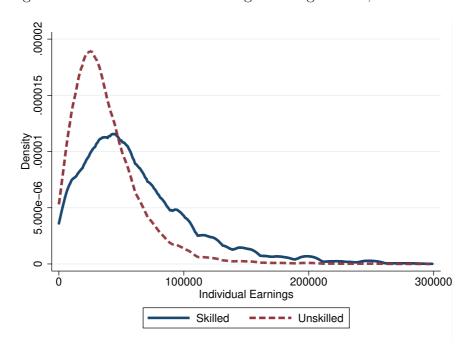


Figure 1: Kernel density plot of individual earnings for low-skilled and high-skilled individuals in our sample conditional on having positive earnings. We truncate the graph at income of \$300,000. We define low-skilled individuals as those without any college experience and define high-skilled individuals as workers with at least some college experience.

SIPP We also incorporate data from the SIPP, a nationally representative sample with detailed data on respondents' participation in income transfer programs, thereby allowing us to understand how benefits receipt varies across the earnings distribution. In particular, we utilize data from waves 1-4 of the 2014 SIPP, which includes monthly data on approximately 53,000 households from 2013 to 2016. From this dataset, we utilize data on household size, household earnings, and receipt of TANF and SNAP benefits over the year. We convert all monetary values to 2017 dollars.

One issue is that benefit receipts are generally underreported in household surveys, including the SIPP (Meyer, Mok, and Sullivan, 2015). To deal with this, we utilize data from the U.S. Bureau of Economic Analysis' National Income and Product Accounts (NIPA) tables, which

 $^{^{34}}$ An alternative approach to defining skills, employed by Katz and Murphy (1992) and Card (2009), is to divide workers with some college between the two skill groups. We consider this skill classification in Appendix D.3.

report annual government spending on various U.S. programs. We multiply benefit receipt amounts in the SIPP by a multiplicative constant such that the total population-weighted benefit receipts in the SIPP are consistent with the aggregates from the NIPA tables.³⁵

NLSY79 Our final data source is the NLSY79, a nationally representative panel dataset with data on over 12,000 individuals. Respondents were first interviewed in the year 1979, when respondents were between ages 14 and 22. The panel structure of the NLSY79 allows us to observe an individual's earnings over their life cycle, which determines an individual's social security benefit after retirement. Since we need data on as much of an individual's work history as possible, we drop individuals from our sample who drop out of the survey before age 50.³⁶ In addition to data on earnings, we utilize data on education, gender, marital status, age, and number of children over the life cycle. We use these variables to map estimates of earnings over the life cycle to individuals in the ACS.

4.3 Tax-Transfer System

Income Taxes and the EITC. To calculate marginal income and payroll tax rates, we use NBER's TAXSIM, a tax calculator that replicates the federal and state tax codes in a given year, accounting for differential tax schedules and tax deductions and credits afforded by various demographic groups, e.g. by marital status or number of dependents. Specifically, we begin by calculating the total income for each household head and their spouse for all households in the ACS. We then use TAXSIM to calculate the marginal income and payroll taxes for each individual, taking into account the individual's marital status (which determines filing status), number of children (a determinant in personal exemptions), age of children (a determinant in eligibility of the Dependent Care Credit, the Child Credit, and the Earned Income Tax Credit), location (which determines state income tax schedules), and age of the household head and spouse (which determine eligibility for various deductions and exemptions).

The solid blue line in Panel (a) of Figure 2 shows the average marginal tax rate arising from federal and state income taxes as a function of individual labor income. Panel (b) shows the same relationship for participation tax rates. As can be seen both are increasing in income, reflecting the progressivity of federal income tax schedule.³⁷

³⁵Specifically, we utilize data from NIPA Table 3.12. We multiply SNAP benefits in the SIPP by a constant such they are consistent with SNAP benefits from this table and multiple TANF benefits in the SIPP by a constant such they are consistent with "Family assistance" benefits from this table multiplied by the fraction of TANF benefits which are spend on basic assistance.

³⁶There are two complications in the NLSY that we need to deal with. First, we must deal with the fact that individuals are only interviewed on even numbered years after 1994. We therefore assume that data in odd numbered years post 1994 is the same as in the previous year. Further, in 2016, the last year from which data are available, respondents are between age 53 and 60. We therefore do not have income information for the last few years of individual's working lives. We therefore assume that income for the remainder of the working life is equal to a respondent's last observed income.

 $^{^{37}}$ Appendix D.1 shows the total marginal and participation tax rates by individual earnings as the sum of the effective tax rates arising from income taxes, social security, and transfer payments.

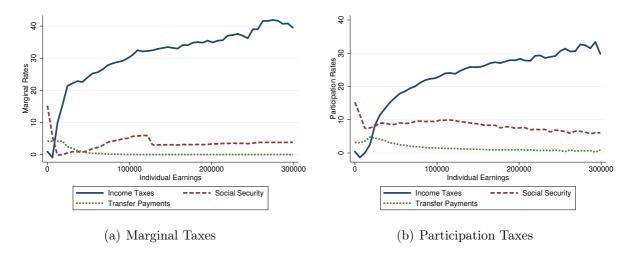


Figure 2: Marginal and participation tax rates by individual earnings. Panel (a) gives the marginal effective tax rates implied by income taxes, the social security system, and transfer programs. Panel (b) reports the participation tax rates implied by income taxes, the social security system, and transfer programs. Income taxes here are the sum of state and federal income taxes, social security is defined as payroll taxes minus the discounted sum of future social security benefits, and transfer payments are the sum of TANF and SNAP phase outs.

Object	Skilled	Unskilled
Taxes		
Federal Income Tax	27.3	20.4
State Income Tax	4.9	4.1
Transfers		
Food stamps (SNAP)	0.3	1.1
Welfare (TANF)	0.0	0.1
Social Security		
Payroll Tax	10.4	13.9
SSI Payments	-7.0	-11.9
Total	35.9	27.7

Table 2: Estimates of income weighted effective marginal tax rates. Each entry shows the income weighted average marginal tax rates arising from each source of effective tax rates in our sample of ACS data. See text for details.

Rows 1-2 of Table 2 give the income-weighted average marginal federal and state income taxes for high-skilled and low-skilled workers. Consistent with the progressivity of these taxes, we find marginal federal income tax rates of 27.3% for high-skilled workers and 20.4% for low-skilled workers. State income tax systems are less progressive. We find marginal state income tax rates of 4.9% and 4.1% for high- and low-skilled workers, respectively.

Welfare Programs. SNAP benefits are declining in income; in the phase-out region of the SNAP benefit schedule, a dollar increase in monthly income is associated with a 24 cent reduction in monthly SNAP benefits. Similarly, TANF benefits are determined as a function of income, though the formula differs by state. However, take-up of these programs is far from 100% (Currie, 2006), and therefore the implied changes in the effective tax rates are less than

these statutory values suggest. Therefore, in order to estimate SNAP and TANF benefits as a function income, while taking into account differences in eligibility and take-up across households, we estimate realized benefits as a function of income and household characteristics using data from the SIPP. Details on the procedure can be found in Appendix C.2.

The dashed green line in the left of Figure 2 gives the marginal phase-out rate of social transfers, where social transfers are given by the sum of TANF and SNAP benefits. We can see that the marginal phase-out rate of transfer payments is positive but small for low levels of income before approaching 0 for higher income levels.³⁸ The dashed green line in the right panel of Figure 2 gives the social transfer phase-out associated with labor force participation, which is also small and mostly decreasing as a function of income.

The income-weighted average marginal SNAP and TANF phase-out rates are shown in rows 3 and 4 in Table 2. The estimates of the average marginal phase-out rates of SNAP are small, at 0.3% for high-skilled workers and 1.1% for low-skilled workers. This might seem surprising, given that the phase out rate of SNAP for those who receive SNAP as a function of income is quite large. However, the relevant statistic for the marginal effect of immigration is the average income-weighted marginal benefit. To better see this, consider the average income weighted phase-out rate of SNAP for households with four members. As with other demographic groups, the phase-out rate for those on SNAP is 24%. However, given that take-up is less than 100%, we estimate an average phase-out rate of only 15% for households whose income places them in the phase-out region of the SNAP formula. Among four-member households, only households with gross monthly income below \$2,633 were eligible for SNAP. These households therefore receive little weight when calculating the income weighted marginal phase-out rates.³⁹

The estimates for TANF are even smaller— the average income weighted TANF benefits 0.1% for low-skilled workers and less than that for high-skilled workers. As with SNAP, TANF recipients have low incomes and therefore receive little weight in the calculation of the incomeweighted average marginal phase-out rate. Furthermore, only 2.5 million individuals received TANF in the average month in 2017. Therefore, while the marginal phase-out rates of TANF and SNAP for a given individual can potentially be large, the income-weighted averages are quite small.

³⁸The fact that the phase-out rate is so low reflects the facts that 1) take-up of TANF and SNAP is less than 100% and 2) the plot shows the phase-out as a function of individual's earnings, holding spouses earnings constant. Regarding 1), one reason could be that individuals "bank" their eligibility for the future since there are are time limits in most states (Low, Meghir, Pistaferri, and Voena, 2018). Regarding 2): as TANF and SNAP eligibility are generally determined by household income, many individuals would not be eligible for these benefits even if their individual income dropped to 0.

 $^{^{39}\}text{To}$ get a better sense of the magnitude, note that 21.5% of individuals belonging to four-member households have an average monthly income less than \$2,633. Further, the average household income conditional on being above this threshold is over 7 times higher than the average household income conditional on being below this threshold. This implies that the average income weighted phase-out rate of households with four members is well under 1%. A back of the envelope calculation yields an income weighted average of $15\% \times 0.215 \times \frac{1}{8} + 0\% \times 0.785 \times \frac{7}{8} \approx .40\%$

⁴⁰Source: https://www.acf.hhs.gov/sites/default/files/ofa/2017_recipient_tan.pdf

Social Security. Finally, our calculation of effective marginal tax rates includes social security benefits and payroll taxes. Payroll taxes are mostly decreasing with income; payroll taxes have a constant marginal tax rate of 15.3% until the maximum taxable earnings threshold after which the marginal rate drops to 2.9%.⁴¹

However, payroll taxes are not a pure tax because higher earnings are also associated with higher social security benefits after retirement. More specifically, an individual's social security benefits are calculated as an increasing function of the individual's average indexed monthly earnings (AIME), the average monthly earnings over the individual's 35 highest earnings years of their career, adjusted for overall growth in the economy over time. Therefore, if current year earnings are one of the individuals 35 highest earning years, an increase in current earnings can increase an individual's AIME and lead to a larger benefits payment after the individual retires. As these social security payments will be received in the future, the relevant calculation for our purposes is the discounted sum of the benefits.

In order to calculate how current income affects an individual's social security benefits, we need to know their AIME and their 35th highest year of earnings, which determines whether current income enters the AIME calculation. These cannot be observed directly in the ACS, which only contains data on an individual's current income. We therefore first compute these objects for each individual in our NLSY79 sample. We then impute an AIME and 35th highest earning year for individuals in the ACS using similar individuals in the NLSY79.⁴² The AIME is then used to determine the marginal rate of benefits associated with earnings and the 35th highest year of earnings is used to determine if current earnings will affect the individual's AIME. Details on this procedure can be found in Appendix C.3. Finally, a crucial element of this calculation is an individual's life expectancy, which determines how many years the individual receives benefits. To calculate life expectancy, we use estimates of life expectancy conditional on income from Chetty et al. (2016), who estimate life expectancy for household income percentiles using data from 1.4 billion tax and social security death records.⁴³

The dotted green line in the two panels of Figure 2 display the marginal tax rates and participation tax rates associated with the social security system, which we define as payroll taxes minus the marginal replacement rates.⁴⁴ At very low incomes, both marginal and participation tax rates are very high. This occurs because very low income levels are unlikely to be one of an individual's 35 highest earning years, and therefore do not increase their future social security benefits. Eventually, the social security tax begins to increase with income, as higher earnings imply higher social security benefits post-retirement. At the maximum taxable

⁴¹The maximum taxable earnings threshold was \$127,200 in the year 2017. At higher income levels, individuals must pay an Additional Medicare Tax, which increases the marginal tax rate by an additional 0.9%.

⁴²More specifically, we calculate the mean AIME and 35th highest year of the earnings by gender, marital status, education, age, and position in the income distribution for individuals in the NLSY79. We assign individuals in the ACS their corresponding group mean of AIME and 35th highest earning year.

⁴³We calculate each individuals household's income percentile within their age. We then use the gender specific life expectancy associated with this income percentile.

⁴⁴Note that payroll taxes also fund other programs, such as Medicare, in addition to Social Security.

earnings threshold of \$127,200, the payroll tax drops precipitously, leading to a drop in the marginal effective tax associated with social security.⁴⁵ The social security participation tax rate exhibits a kink, rather than a drop, at the maximum taxable earnings threshold, because individuals still pay payroll taxes on earnings up to this threshold.

The 5th and 6th rows of Table 2 give the income weighted average payroll tax rates and marginal discounted replacement rates. We find a higher marginal rate for low-skilled workers than high-skilled workers, at 13.9% for low-skilled workers and 10.4% for high-skilled workers, reflecting that payroll taxes drop dramatically at the maximum taxable earnings threshold. We estimate an income weighted marginal social security replacement rate of 11.9% for low-skilled workers and 7.0% for high-skilled workers, reflecting that marginal benefits rates are decreasing in AIME. Taken together, this implies an income weighted average effective social security tax of 2.0% for low-skilled and 3.4% for high-skilled workers.

The final row of Table 2 displays \bar{T}'_s and \bar{T}'_u , the income-weighted effective marginal tax rates, as the sum of these elements. We obtain $\bar{T}'_u = 27.7\%$ for low-skilled workers and $\bar{T}'_s = 35.9\%$ for high-skilled workers, implying a difference in marginal tax rates of 8.2%.

5 Results

We now present the quantification of our formula in Proposition 3. We then compare these numbers to direct fiscal effects in Section 5.2 and also turn to welfare analysis in Section 5.3.

5.1 Indirect Fiscal Effects

Table 3 displays estimates for the indirect fiscal effect under different assumptions on the elasticity of substitution between workers and labor supply elasticities. The three columns show the indirect fiscal effect under different assumptions of the elasticity of substitution, ranging from $\sigma = 1.5$ to $\sigma = 2.5$. Each row displays the results for different assumptions about the labor supply elasticity.

In Panel I, we display the indirect fiscal effect with exogenous labor supply, based on Proposition 2. We find indirect fiscal benefits of \$1,299 ($\sigma = 1.5$), \$975 ($\sigma = 2$), and \$780 ($\sigma = 2.5$).⁴⁶

Next, in Panel II, we calculate the indirect fiscal effects when we allow for intensive, but not extensive, margin adjustments. In all three scenarios, allowing for intensive margin adjustments increases the indirect fiscal effect of low-skilled immigration. Panel III calculates the indirect fiscal effects with extensive, but without intensive margin labor supply adjustments. When elasticities are common or only vary by gender and marital status, the indirect fiscal

⁴⁵ After this threshold, the marginal tax rate is mostly flat, reflecting that further income increases do not count for social security purposes.

⁴⁶These results are slightly smaller than those in Section 2 because the model in that section multiplies tax differences by the income of the average low-skilled worker, not the average low-skilled immigrant.

	Elasticity of Substitution		
	1.5	2.0	2.5
I. No Labor Supply Responses	1,299	975	780
II. Intensive Only			
Common Elasticity	$1,\!417$	1,113	916
By Gender and Marital Status	1,303	979	784
By Income, Gender and Marital Status	1,347	1,015	815
III. Extensive Only			
Common Elasticity	1,380	1,074	878
By Gender and Marital Status	1,335	1,020	826
By Income, Gender and Marital Status	1,268	965	779
IV. Intensive and Extensive			
Common Elasticity	1,471	1,186	993
By Gender and Marital Status	1,339	1,025	830
By Income, Gender and Marital Status	1,313	1,004	813

Table 3: Indirect Fiscal Effects of low-skilled immigrants with intensive and extensive margin labor supply responses. The three columns show the indirect fiscal effect under different assumptions of the elasticity of substitution, ranging from $\sigma = 1.5$ to $\sigma = 2.5$. Each row displays the indirect fiscal effect for different assumptions about the labor supply elasticity.

effect is larger than the case with no labor supply responses. However, when extensive margin elasticities can vary by income, gender and marital status, the indirect effect decreases slightly because extensive margin elasticities are generally decreasing in income.

Finally, Panel IV displays the results with both intensive and extensive labor supply adjustments. When labor supply elasticities are common across gender, marital status and income, we find indirect fiscal benefits of \$1,471 ($\sigma = 1.5$), \$1,186 ($\sigma = 2$), and \$993 ($\sigma = 2.5$).

Tables 14 and 15 in Appendix D.4 repeat the analysis for the average high school dropout immigrant and the average high school graduate immigrant. From (3) we can see that the income of the immigrant only enters as a multiplicative constant, therefore, the indirect fiscal effects associated with high school dropouts (graduates) can easily be calculated by multiplying the effects in Table 3 by the ratio of income of the immigrant high school dropouts (graduates) over the income of all low-skilled immigrants. As such, the indirect fiscal effects for high school dropouts are roughly 15% smaller than those for all low-skilled immigrants and range from \$660 to \$1,220 while the indirect fiscal effects for high school graduates are roughly 10% larger than those for all low-skilled immigrants and range from \$860 to \$1,620.

5.2 Relation to Direct Fiscal Effects

We now relate our results about the indirect fiscal effects to the direct fiscal effects of the report by the National Academy of Sciences (2017).

Our approach is as follows: we first consider the lifetime direct fiscal effect of a low-skilled immigrant who arrives at age 23 and lives until the age of 79. We choose 23 since this is the median age of arrival for low-skilled immigrants in the ACS and we chose 79 years because

the life expectancy at age 23 in the U.S. is roughly 79.⁴⁷ We make use of Figure 8-21 of the NAS report, which provides us with the net direct fiscal impact by age for both high school graduates and high school dropouts. These calculations account for the immigrant's federal, state and local taxes, incarceration costs, veteran's benefits, refugee support costs, government healthcare costs, and a variety of federal and state level transfer programs over an individual's life-cycle.⁴⁸ Further, we need to make an assumption about how immigrants affect government spending on public goods.⁴⁹ We consider four different scenarios, similar to the NAS report: (i) there are zero marginal costs of public goods and hence no costs are assigned to immigrants, (ii) marginal costs are equal to 25% the average costs of public goods, (iii) marginal costs are equal to 50% of average costs, and (iv) marginal costs equal average costs.⁵⁰ For all of these four scenarios, we can calculate the net present value (NPV) direct fiscal effect of low-skilled immigrants. To make this number comparable to our annual indirect fiscal effect, we calculate the annuity value for the period of 23 until 65 (labor market period) that corresponds to the NPV of the lifetime direct fiscal effect.

Table 4 contains these annuitized values for the four different scenarios. The first column gives the results for a high school dropout immigrant, the next column gives the results for high school graduates, and the last column gives the results for the average low-skilled immigrant. We can clearly see that low-skilled immigrants imply a direct fiscal burden in nearly every scenario – only high school graduates are a small fiscal surplus for the first scenario. Recall that we calculate indirect fiscal effects of \$660 to \$1220 for high school dropouts and \$860 to \$1620 for high school graduates. Accounting for these indirect effects in scenarios (ii) and (iii) can turn high school graduates from a fiscal burden into a small fiscal surplus. More generally, comparing the numbers in Table 4 with the numbers in Table 3, one can see that indirect fiscal effects are economically meaningful in comparison to the direct fiscal effects and should therefore be taken into account.

5.3 Welfare Effects

Table 5 summarizes the welfare effects associated with the distributional effects and the indirect fiscal effects of immigration as formalized in Proposition 4. In the first three columns, we calculate the welfare effects using the welfare weights of Hendren (2020), where the utility of all natives, both domestic-born and foreign-born, are considered. Given the intermediate

⁴⁷In 2017, the life expectancy at age 23 was 77.06 for men and 81.72 for women. This yields a simple average of 79.39. Source: https://www.ssa.gov/oact/STATS/table4c6.html

⁴⁸National Academy of Sciences (2017) also accounts for schooling costs, but these are less relevant here given that we consider low-skilled immigrants from age 23 onwards.

⁴⁹Dustmann and Frattini (2014) give a detailed discussion about this for the UK and point out that the exact specification matters significantly. Referring to assumptions on the marginal cost of public goods, the NAS report states "In fact, such assumptions are likely to swamp the impact of most of the other assumptions and data issues that arise in fiscal impact analyses." (National Academy of Sciences, 2017, p. 266).

⁵⁰Case (i) relates to scenario 6 and case (iv) relates to scenario 2 of Box 8-1 of National Academy of Sciences (2017). Cases (ii) and (iii) are intermediate cases of those two.

Public Goods	High School	High School	
Scenario	Dropout	Graduate	Average
Zero Marginal Costs	-4,151	695	-1,388
$\mathrm{MC} = 0.25 imes \mathrm{AC}$	-4,922	-86	-2,165
$\mathrm{MC} = 0.5 imes \mathrm{AC}$	-5,693	-867	-2,942
$\mathrm{MC}=\mathrm{AC}$	-7,235	-2,429	-4,496

Table 4: Annuitized direct fiscal effect of an immigrant that arrives at age 23 and dies at age 79. We use a discount rate of 1%. Only direct fiscal contributions are accounted for and rely on Figure 8-21 of National Academy of Sciences (2017). We calculate the annuity value for the period of 23 until 65 (age of retirement).

value of $\sigma = 2$, quantification of the formula in Proposition 4 reveals a distributional effect of -\$1,318. This formalizes the idea that the increase in inequality associated with low-skilled immigration can entail significant welfare costs. The magnitude of this distributional effect is sensitive to how the social welfare weights differ with income: here we use the welfare weights of Hendren (2020), which are the welfare weights implicitly used by the U.S. government.⁵¹

However, this distributional effect is partially offset by the two welfare effects related to indirect fiscal effects: the fiscal externalities associated with changes in native labor supply and the tax mitigation effect. Evaluating (11) with common labor supply elasticities and $\sigma=2$, we find a fiscal externality of \$430, roughly one third of the entire indirect fiscal effect. The distributional effect is further mitigated by the fact that the tax burden for low-skilled natives decreases while the tax burden for high-skilled natives increases. This tax mitigation effect creates an additional surplus of \$511. Therefore, the two novel welfare effects associated with the indirect fiscal effect — the fiscal externality and the tax mitigation effect — imply an additional, so far neglected, surplus of \$941. All together, this implies a welfare effect beyond the direct fiscal effect of -\$377 compared to a pure distributional effect of -\$1,318. An implication is that low-skilled immigration would be welfare improving only if immigrants had a positive direct fiscal effect above \$377. This could for example be achieved by accordingly set visa fees.

In the last three columns, we calculate the effects on domestic-born welfare by only assigning non-zero welfare weights to domestic-born individuals.⁵³ The distributional effects are slightly muted as domestic-born are more likely to be skilled than previous immigrants. For $\sigma = 2$, we find a distributional effect for domestic-born of -\$932. This implies a welfare effect beyond the direct fiscal effect of -\$77.

⁵¹Note that generally, the weights that Hendren (2020) obtained, depend on his calibration of the income distribution, the tax-transfer system calibration and the elasticities, which is not the same calibration for these objects as in our paper. We consider it as a reasonably good approximation to work with his weights, in particular because the welfare results are not the main results of this paper. The weights of Lockwood and Weinzierl (2016) are very similar, who study how welfare weights implicitly used by the U.S. government have changed over time.

 $^{^{52}}$ Note that holding labor supply elasticities constant, the fiscal externality is the same fraction of the indirect fiscal effect for any value of the elasticity of substitution, σ . Therefore, the result that the fiscal externality is over one third of the fiscal surplus is true for any value of the elasticity of substitution.

⁵³We again utilize the use the welfare weights of Hendren (2020) and set the weights for foreign-born individuals to zero. We then we normalize the welfare weights such that are equal to one on average.

	All Natives			Domestic-Born Only		
	1.5	2.0	2.5	1.5	2.0	2.5
I. Distributional Effect	-1634	-1318	-1104	-1157	-932	-781
II. Fiscal Externality	533	430	360	533	430	360
III. Tax Mitigation	633	511	428	527	425	356
Total Effect (Absent Direct Fiscal Effect)	-468	-377	-316	-96	-77	-65

Table 5: Welfare effects of low-skilled immigrants absent direct fiscal effects. The right panel displays the welfare effects when only domestic-born natives receive positive social welfare weights. Within each panel, the three columns show the indirect fiscal effect under different assumptions of the elasticity of substitution, ranging from $\sigma = 1.5$ to $\sigma = 2.5$ with common labor supply elasticities.

Overall, these welfare effects of natives are rather small in magnitude compared to estimates of wage gains that low-skilled immigrants experience as a result of coming to the United States. Clemens, Montenegro, and Pritchett (2008) find that U.S. immigrants from the countries in their sample have 200% to 1500% higher wages than observably identical individuals who remain in their home country. For a low-skilled Mexican male immigrant, this implies an income gain of nearly \$20,000 annually.⁵⁴ Hendricks and Schoellman (2018) find that immigrants from low- and middle-income countries increase their wages by 200% to 300% upon arriving in the United States. This suggests that the overall welfare effects are likely to be positive if the welfare of the immigrants themselves are accounted for.

6 Extensions and Robustness

We now discuss the sensitivity of our results to several alternative model specifications. The formulas for indirect fiscal effects and additional details and results for each specification are included in Appendix A. We summarize the results from these extensions in Table 1. Apart from Section 6.3, we consider exogenous labor supply of natives in these extensions. Generalizing the integral equation approach used in the benchmark model to also account for endogenous labor supply in these settings would be relatively straightforward.

6.1 Alternative Skill Stratifications

So far we assumed that all workers within a given skill group are perfectly substitutable. We now consider three different skill stratifications and production functions that have been utilized in the immigration literature. First, we evaluate the indirect fiscal effects using the model and estimates from Borjas (2003), who considers a nested-CES production function in which narrower education groups and experience levels are imperfect substitutes. We find that the average low-skilled immigrant leads to an indirect fiscal effect of \$1,873 in this context. The

 $^{^{54}}$ The average low-skilled male Mexican immigrant in our dataset has an average wage income of \$32,841. Clemens, Montenegro, and Pritchett (2008) estimate that Mexican immigrants have wages 2.53 times higher than observably identical Mexicans who do not immigrate. We calculate the average income gain as $32,841 - \frac{32,841}{2.53} = 19,860$.

main reason why the effect is higher than in our main model is that Borjas (2003) estimates a lower value for the elasticity of substitution between different education groups.⁵⁵

Dustmann, Frattini, and Preston (2013) argue than an immigrant's education level might give an inaccurate approximation of a worker's skills, given that skills are often not transferable. They propose a skill classification in which a worker's skill is given by her position in the wage distribution. Therefore, immigrants at a given position in the wage distribution compete with natives at the same position of the wage distribution, regardless of their education levels.⁵⁶ We calculate an indirect fiscal effect of low-skilled immigrants of \$1,017 in this setting.⁵⁷

6.2 Domestic- and Foreign-Born Complementarity

Next, we consider the model considered in Ottaviano and Peri (2012), which allows for domestic- and foreign-born workers to be imperfectly substitutable within education and experience groups. The production function takes a similar structure to that in Borjas (2003) but has two important differences. First, instead of assuming all four education groups aggregate within a single CES aggregator, we now follow Ottaviano and Peri (2012) and instead use a two level nested structure to model complementarity between education groups. High school dropouts and high school graduates aggregate to low-skilled labor and individuals with some college and college graduates aggregate to high-skilled labor. This specification allows for one elasticity of substitution between high-skilled and low-skilled workers and a second elasticity of substitution between narrow education groups. Second, within each skill-education-experience group, we allow for the possibility that domestic- and foreign-born workers may be imperfectly substitutable in production.⁵⁸ Using the estimates from Ottaviano and Peri (2012), we find an indirect fiscal effect of \$1,065.⁵⁹

While the indirect fiscal effects are similar to those above, the results on welfare can be quite different in this model. We find a distributional effect arising from an increase in inequality of -\$1,989, about one third of which is mitigated by progressive taxes. However, if we only focus on the welfare of domestic-born natives, we find a positive distributional effect of \$742. Therefore, as emphasized by Dustmann, Schönberg, and Stuhler (2016) and Ottaviano and Peri (2012), the inclusion of domestic-foreign complementarity in the production function has strong implications for which workers bear the incidence of low-skilled immigrant inflows.⁶⁰

⁵⁵We give the detail of the model and quantification in Appendix A.1. We also decompose the indirect effects into those arising from relative wages across experience groups and across education groups.

⁵⁶This is similar to the production function utilized in Heathcote, Storesletten, and Violante (2017), which combines labor from a continuum of skill types.

⁵⁷Details on this specification are included in Appendix A.3.

⁵⁸We focus on "Model B" from Ottaviano and Peri (2012), which the authors show is the most consistent with the data. We use their estimates from column 7 of Table 6.

⁵⁹Appendix A.2 presents the full specification and quantification.

⁶⁰Allowing for domestic-foreign complementarity implies that low-skilled foreign born workers who immigrated in the past experience the largest wages decreases as a result of new low-skilled immigrant inflows, while low-skilled domestic-born workers only experience small wage decreases or even wage increases.

However, domestic-foreign born complementary does not play a first-order role in determining the indirect fiscal effect of immigration. In fact, the indirect fiscal benefits calculated using the production function in Ottaviano and Peri (2012) and the production function in Borjas (2003) are quite similar if we use comparable estimates of the elasticity of substitution between education groups, see the last paragraphs of Appendices A.1, A.2 and A.3, respectively. Therefore, while the welfare implications differ across the two models, the implied indirect fiscal effects are similar.

6.3 Endogenous Occupation Choice

Next, we consider the model of immigration and the labor market developed by Peri and Sparber (2009).⁶¹ In this framework, low-skilled domestic-born workers differ from low-skilled foreign-born workers in that they choose different occupations due to different comparative advantages. Low-skilled foreign-born workers tend to choose occupations with a high manual task and lower communication task intensity than low-skilled natives. Since manual tasks and communication tasks are complementary in production, low-skilled domestic-born workers and low-skilled foreign-born workers are now imperfect substitutes.⁶² Additionally, occupation choices are endogenous and therefore low-skilled workers may respond to low-skilled immigration by changing to more communication-intensive occupations.

We take the estimates of production parameters and occupation choice elasticities from Peri and Sparber (2009) to calculate the indirect fiscal effect. First, we calculate the indirect fiscal effects under the assumption that natives do not adjust their occupation in response to immigration. In this case, we find a indirect fiscal effect of \$1,115, which is in a similar ballpark as the numbers we found in Section 5. However, with endogenous occupation choice, low-skilled domestic-born workers respond by switching into higher-paying occupations, thereby increasing their incomes and thus tax payments.⁶³ Therefore, when we allow for endogenous occupation choice, we find an indirect fiscal effect of \$2,131.

6.4 Decreasing Returns to Scale

With decreasing returns to scale, an immigrant inflow can lead to changes in firm profits in addition to changes in wages. Therefore, the indirect fiscal effects arise not only because of a change in relative incomes of high-skilled and low-skilled workers but also from an increase in firm profits relative to worker income. In Appendix A.5, we show that this additional effect can be accommodated into our indirect fiscal effect formulas with a term that captures the increase in profit taxes at the cost of a decrease in labor income taxes.

⁶¹The details of this specification are given in Appendix A.4.

⁶²In essence, the differences in task concentration between domestic- and foreign-born workers provide a microfoundation for the domestic- and foreign-born complementarity in Ottaviano and Peri (2012).

⁶³Note that this effect constitutes a fiscal externality. This fiscal externality is much larger than the fiscal externality resulting from hours worked and participation responses in the canonical model.

To evaluate indirect fiscal effects with decreasing returns to scale, we utilize estimates of returns to scale from Burnside (1996) and estimate the tax rate on profits arising from both corporations and pass-through businesses. We find an indirect fiscal effect of \$1,057.

6.5 Further Potential Extensions

Endogenous Education Low-skilled natives may respond to low-skilled immigrant inflows by further investing in their education (Llull, 2018). This would likely increase the indirect fiscal effects of immigration as increased education leads to increased lifetime income and therefore increased tax payments. As shown in Colas, Findeisen, and Sachs (2021), this fiscal externality associated with attending college is quantitatively important.⁶⁴

Monopsonistic Labor Markets Amior and Manning (2020) emphasize that most of the immigration literature rests on the assumption of perfectly competitive labor markets. They argue that this assumption is problematic because markdowns on wages in a setting with monopsony power are likely to be endogenous to immigration since labor supply of immigrants tends to be relatively inelastic.⁶⁵ In this case, low-skilled immigration would not only imply redistribution from low- to high-skilled workers but also from workers to firms, similar to the decreasing-returns to scale extension in Section 6.4. An important difference to Section 6.4 is that immigrants are not paid their marginal product in such a setting. This implies that the economic pie accruing to natives would increase and thereby reinforce the indirect fiscal benefit.

Search Frictions We have abstracted from search frictions in the labor market. As as been pointed out by Battisti, Felbermayr, Peri, and Poutvaara (2018) immigration can attenuate search frictions on the labor market, which also implies indirect fiscal benefits.

Native Migration Responses Low-skilled immigrant inflows into a given city can induce migration responses by natives (Borjas, Freeman, and Katz, 1997; Piyapromdee, 2020; Monras, 2020). These native migration responses, either in the form of outflows of low-skilled or inflows of high-skilled natives, would mitigate the effect of immigration on local wage inequality and therefore reduce the indirect fiscal effect generated locally, but would increase wage inequality and therefore generate indirect fiscal effects in other cities. Concretely, if the economy consists of J cities with different population sizes but that are otherwise identical, the total indirect fiscal effect generated across all cities would be independent of the distribution of the low-skilled immigrants across cities and of any native migration responses.⁶⁶ However, if cities

 $^{^{64}}$ Colas, Findeisen, and Sachs (2021) estimate average lifetime fiscal externalities of attending college ranging roughly \$60,000 to \$90,000, conditional on parental income.

⁶⁵For the US, the authors show that the assumption that markdowns are exogenous is rejected by the data. ⁶⁶This is because the indirect fiscal effect is independent of the size of the native population. See also the discussion in Foonote 17.

differ in their wage levels, a native's income and tax payments will depend on their location and therefore native migration will imply a fiscal externality. These effects could be jointly analyzed using a spatial equilibrium model with taxes, such as in Colas and Hutchinson (2021).

7 Discussion

In this section we discuss additional issues and address limitations of our analysis. First, in Section 7.1 we discuss the role of physical capital. In Section 7.2, we discuss some critical issues about the assumptions we made when estimating the indirect fiscal effect.

7.1 The Role of Physical Capital

We have abstracted away from the role of capital in production. Here we show how physical capital can be accommodated into our formulas. This does not significantly change our results.

Elastically Supplied Physical Capital Consider a constant returns production function $Y = F(\mathcal{L}_u, \mathcal{L}_s, K)$ that uses physical capital, K, as an input in addition to low- and high-skilled labor. Since the supply of capital is perfectly elastic and since $F(\cdot)$ exhibits constant returns to scale, the firm's optimal choice of capital level can be written as a function of the levels of high- and low-skilled labor, $K^*(\mathcal{L}_s, \mathcal{L}_u)$. Therefore, one can redefine production in terms of labor quantities given the endogenous capital level as

$$\tilde{F}(\mathcal{L}_u, \mathcal{L}_s) = F(\mathcal{L}_u, \mathcal{L}_s, K^{\star}(\mathcal{L}_s, \mathcal{L}_u)).$$

Note that \tilde{F} is a function of only labor quantities and exhibits constant returns to scale. Therefore, Proposition 3 can still be applied if we interpret the own-wage elasticity γ_{own} as the wage elasticity given optimal capital adjustments.⁶⁷ As a simple example, consider the case with the Cobb-Douglas production function $F(\mathcal{L}_u, \mathcal{L}_s, K) = K^{\alpha} (G(\mathcal{L}_u, \mathcal{L}_s))^{1-\alpha}$, where $G(\cdot)$ is a CRS labor aggregate. With elastic capital supply, the ratio of capital to the labor aggregate is constant. Therefore, we can rewrite the production function as $\tilde{F}(\mathcal{L}_u, \mathcal{L}_s) = \bar{A}G(\mathcal{L}_u, \mathcal{L}_s)$ where \bar{A} is a positive multiplicative constant, see Appendix B.7.

In addition, low-skilled immigration will lead to an increase in physical capital which may lead to increased tax revenue.

Inelastically Supplied Physical Capital Lewis (2011) argues that capital stocks adjust quickly to immigrant inflows, and therefore the case with elastic capital supply is appropriate for most settings. Yet, it is interesting to get a sense of how our results would change if capital

⁶⁷Note that the above does not rely on a particular production function (such as Cobb-Douglas) or separability of capital in the production function more generally. The above arguments also apply to cases with non-separable capital and capital-skill complementarity, as in the models in Lewis (2011) and Lewis (2013).

supply is inelastic. Consider again the Cobb-Douglas production function that combines physical capital, K, with a labor aggregate G

$$Y = K^{\alpha} G \left(\mathcal{L}_u, \mathcal{L}_s \right)^{1-\alpha},$$

where $\alpha \in (0,1)$ is a parameter and G is a constant returns to scale function. We assume capital is supplied inelastically and capital payments are taxed at rate τ_k .

As we show in Appendix B.7, the indirect fiscal benefit with inelastic labor supply for an immigrant of type i is given by

$$d\mathcal{R}_{ind}^{inelast}(i) = y_i \left[\underbrace{(\bar{T}_s' - \bar{T}_u') | \gamma_{u,own}^{elast}|}_{\text{Skill Ratio Effect}} + \underbrace{\alpha \left(\tau_k - \bar{T}_I'\right)}_{\text{Capital Labor Ratio Effect}} \right], \tag{12}$$

where $\gamma_{u,own}^{elast} = \frac{\partial \log \frac{\partial G}{\partial \omega_u}}{\partial \log \mathcal{L}_u}$ is the own-wage elasticity of low-skilled labor when capital supply is perfectly elastic.⁶⁸ Therefore, the indirect fiscal effect generated by the "skill ratio effect" is simply equal to the indirect fiscal effect with elastic capital supply. One reasonable assumption is that when physical capital supply is inelastic, returns to physical capital have a similar tax rate as firm profits. Therefore using the marginal tax rate for profit we calculated of 36.8% in the previous section, and capital share parameter of $\alpha = .33$, we find that the indirect fiscal effect of an average low-skilled immigrant with inelastic capital supply will increase by $y_i \alpha \left(\tau_k - \bar{T}_I' \right) = \273 compared to the case with elastic capital supply.

7.2 Further Issues

Steady State versus Dynamics In all our specifications, we have focused on a steady state interpretation and have abstracted from the fact that it may take some time until the economy reaches the new steady state after the arrival of the immigrants.⁶⁹ It would certainly be possible to extend our approach numerically to such more dynamic settings and discuss how the indirect fiscal effects differ in the short run. One can, however, interpret our results with exogenous labor supply as fiscal effects that apply in the short run and the results with endogenous labor supply as the fiscal effects that apply in the long run. As can be see in Table 3, short and long-run effects are rather similar.

More structural approaches have been taken in the literature more recently, e.g. by Llull (2018) who considers endogenous responses of workers along the occupation and education margin, by Bound, Braga, Golden, and Khanna (2015) who consider major and occupation choice responses of skilled natives, by Monras (2020) who considers a dynamic spatial equilibrium model, and by Colas (2019) who also considers sectoral choices of natives.

⁶⁸This is also equal to the own-wage elasticity when $\alpha = 0$.

⁶⁹See, for example, Card (1990), Cohen-Goldner and Paserman (2011), Llull (2017), Monras (2020), Borjas (2015) and Edo (2017) for reduced-form evidence comparing the short- and long-run wage impacts.

Documented versus Undocumented Immigration In our analysis we have not explicitly made the distinction between authorized and undocumented immigrants. This distinction would matter for the calculation of the indirect fiscal effect because undocumented immigrants differ in their eligibility status for welfare programs and their likelihood to pay income or payroll taxes. However, we focus on the indirect fiscal effect, which operates through a low-skilled immigrant's effect on native wages, independent of the taxes paid and benefits received by the immigrant themselves. As such, an immigrant's documentation status is unlikely to have a first-order effect on their indirect fiscal effect conditional on their income level y_i .

Other Indirect Effects Immigrants may have indirect fiscal effects on top of those described in this paper. We have focused on a single consumption good and therefore abstracted from how immigrants may affect tax revenue by changing relative consumption prices. For example, it has been shown that low-skilled immigration lowers prices for low-skilled services such as gardening or housekeeping (Cortes, 2008). Such effects would only matter if the goods or services whose relative prices increase is taxed at a different rate then the goods for which the relative prices decrease. An effect that probably matters more is the interaction between the prices for these services and native labor supply. Cortes and Tessada (2011) show that high-skilled female native labor supply increased due low-skilled immigration and, consistently with that, these women have reduced their time spent on household work. Additionally, immigration may increase local housing prices and rents (Saiz, 2003, 2007) and therefore lead to additional fiscal effects arising from property taxes and taxes on rental income.

Local Taxes versus Federal Taxes We have accounted in detail for how taxes paid and transfers received vary with income to obtain reliable estimates for income-weighted averages of marginal tax rates for the different income groups. We have not accounted for the fact that some taxes are raised at the state level and some at the federal level. Similarly, some transfers are paid by the states and some by the federal government. We have therefore taken a national perspective on public finances. We leave the issue of how the fiscal effect is distributed between different levels of government for future research.

Larger Immigrant Inflows We have focused on small inflows of immigrants and therefore considered first-order approximations throughout, thus allowing for a transparent analytical approach. For larger inflows of immigrants, these first-order approximations would become less

⁷⁰The National Academy of Sciences (2017) summarize the literature on the fiscal effects of undocumented immigrants as finding that undocumented immigrants tend to have a more positive impact than documented immigrants, largely due to the fact that undocumented immigrants tend to be younger. Undocumented immigrants are also ineligible for medical coverage under the Affordable Care Act and are ineligible for the Earned Income Tax Credit, among other programs.

⁷¹As undocumented immigrants on average have lower income than authorized immigrants, they will have on average a lower indirect fiscal effect because the indirect fiscal effect is increasing in the immigrant's income.

appropriate. It would be straightforward to consider larger immigration inflows numerically and thereby go beyond first-order approximations.

8 Conclusion

In this paper, we explore the indirect fiscal effect of immigration that works through the impact on the native wages and labor supply. Applying these formulas to the U.S., we find that the indirect fiscal effects of low-skilled immigration are sizable and positive. For some plausible scenario they turn low-skilled immigration from a fiscal burden to a fiscal surplus.

Future work could extend our analysis to other countries, where the tax system, labor supply responses and wage effects of immigration may differ from the U.S. case. Our approach could also be extended to calculate the indirect fiscal effects of high-skilled immigrants. In thinking about the indirect effects of high-skilled immigration, it would seem natural to allow for high-skilled immigrants to affect factor productivity, in addition to factor ratios (Kerr and Lincoln, 2010; Peri, Shih, and Sparber, 2015; Bound, Khanna, and Morales, 2017; Khanna and Lee, 2018). We leave these extensions for future research.

References

- ACEMOGLU, D. AND D. AUTOR (2011): "Skills, Tasks and Technologies: Implications for Employment and Earnings," Handbook of Labor Economics, 4, 1043–1171.
- ALESINA, A., A. MIANO, AND S. STANTCHEVA (2018): "Immigration and redistribution," Tech. rep., National Bureau of Economic Research.
- AMIOR, M. AND A. MANNING (2020): "Monopsony and the Wage Effects of Migration," <u>CEP</u> LSE Discussion Paper. Centre for Economic Performance, London School of Economics.
- AUERBACH, A. J. AND P. OREOPOULOS (1999): "Analyzing the fiscal impact of US immigration," <u>American Economic Review</u>, 176–180.
- BARGAIN, O., K. ORSINI, AND A. PEICHL (2014): "Comparing labor supply elasticities in europe and the united states new results," <u>Journal of Human Resources</u>, 49, 723–838.
- BATTISTI, M., G. FELBERMAYR, G. PERI, AND P. POUTVAARA (2018): "Immigration, search and redistribution: A quantitative assessment of native welfare," <u>Journal of the European Economic Association</u>, 16, 1137–1188.
- BODVARSSON, Ö. AND H. VAN DEN BERG (2009): "The economics of immigration," Theory and.
- BORJAS, G. J. (2003): "The Labor Demand Curve Is Downward Sloping: Reexamining the Impact of Immigration on the Labor Market," <u>The Quarterly Journal of Economics</u>, 118, 1335–1374.
- ——— (2014): Immigration economics, Harvard University Press.

- ——— (2015): "The wage impact of the Marielitos: A reappraisal," ILR Review.
- ——— (2016): We wanted workers: Unraveling the immigration narrative, WW Norton & Company.
- BORJAS, G. J., R. B. FREEMAN, AND L. F. KATZ (1997): "How much do immigration and trade affect labor market outcomes?" Brookings papers on economic activity, 1997, 1–90.
- BORJAS, G. J. AND L. HILTON (1996): "Immigration and the Welfare State: Immigrant Participation in Means-Tested Entitlement Programs*," The Quarterly journal of economics, 111, 575–604.
- BOUND, J., B. BRAGA, J. M. GOLDEN, AND G. KHANNA (2015): "Recruitment of foreigners in the market for computer scientists in the United States," <u>Journal of labor economics</u>, 33, S187–S223.
- BOUND, J., G. KHANNA, AND N. MORALES (2017): "Understanding the Economic Impact of the H-1B Program on the US," Tech. rep., National Bureau of Economic Research.
- Burnside, C. (1996): "Production function regressions, returns to scale, and externalities," Journal of monetary Economics, 37, 177–201.
- Busch, C., D. Krueger, A. Ludwig, I. Popova, and Z. Iftikhar (2020): "Should Germany Have Built a New Wall? Macroeconomic Lessons from the 2015-18 Refugee Wave," Journal of Monetary Economics.
- CARD, D. (1990): "The impact of the Mariel boatlift on the Miami labor market," <u>ILR Review</u>, 43, 245–257.
- ———— (2009): "Immigration and Inequality," American Economic Review, 99, 1–21.
- CARD, D. AND T. LEMIEUX (2001): "Can falling supply explain the rising return to college for younger men? A cohort-based analysis," The Quarterly Journal of Economics, 116, 705–746.
- CHETTY, R. (2012): "Bounds on Elasticities with Optimization Frictions: A Synthesis of Micro and Macro Evidence on Labor Supply," <u>Econometrica</u>, 80, 969–1018.
- CHETTY, R., A. GUREN, D. MANOLI, AND A. WEBER (2013): "Does indivisible labor explain the difference between micro and macro elasticities? A meta-analysis of extensive margin elasticities," NBER macroeconomics Annual, 27, 1–56.
- CHETTY, R., M. STEPNER, S. ABRAHAM, S. LIN, B. SCUDERI, N. TURNER, A. BERG-ERON, AND D. CUTLER (2016): "The association between income and life expectancy in the United States, 2001-2014," Jama, 315, 1750–1766.
- Chojnicki, X., F. Docquier, and L. Ragot (2011): "Should the US have locked the heaven's door? Reassessing the benefits of the postwar immigration," <u>Journal of Population</u> Economics, 24, 317–359.
- CLEMENS, M. A., C. E. MONTENEGRO, AND L. PRITCHETT (2008): <u>The place premium:</u> wage differences for identical workers across the US border, The World Bank.

- COHEN-GOLDNER, S. AND M. D. PASERMAN (2011): "The dynamic impact of immigration on natives' labor market outcomes: Evidence from Israel," <u>European Economic Review</u>, 55, 1027–1045.
- Colas, M. (2019): "Dynamic responses to immigration," Working Paper, Opportunity and Inclusive Growth Institute.
- Colas, M., S. Findeisen, and D. Sachs (2021): "Optimal Need-Based Financial Aid," Journal of Political Economy, Forthcoming.
- Colas, M. and K. Hutchinson (2021): "Heterogeneous workers and federal income taxes in a spatial equilibrium," American Economic Journal: Economic Policy, Forthcoming.
- CONGRESSIONAL BUDGET OFFICE, U. S. (2015): "Effective Marginal Tax Rates for Lowand Moderate-Income Workers in 2016." Tech. rep., Washington: U.S. Congress.
- CORTES, P. (2008): "The effect of low-skilled immigration on US prices: evidence from CPI data," Journal of political Economy, 116, 381–422.
- CORTES, P. AND J. TESSADA (2011): "Low-skilled immigration and the labor supply of highly skilled women," American Economic Journal: Applied Economics, 3, 88–123.
- Currie, J. (2006): "The Take-Up of Social Benefits," <u>Public Policy and the Income</u> Distribution, 80.
- DUSTMANN, C. AND T. FRATTINI (2014): "The fiscal effects of immigration to the UK," <u>The</u> economic journal, 124, 593–F643.
- DUSTMANN, C., T. FRATTINI, AND I. P. PRESTON (2013): "The effect of immigration along the distribution of wages," The Review of Economic Studies, 80, 145–173.
- Dustmann, C., U. Schönberg, and J. Stuhler (2016): "The impact of immigration: Why do studies reach such different results?" Journal of Economic Perspectives, 30, 31–56.
- EDO, A. (2017): "The Impact of immigration on wage dynamics: Evidence from the Algerian independence war," Journal of the European Economic Association.
- FELDSTEIN, M. AND A. SAMWICK (1992): "Social security rules and marginal tax rates," NBER Working Paper No. 3962.
- FOGED, M. AND G. PERI (2016): "Immigrants' effect on native workers: New analysis on longitudinal data," American Economic Journal: Applied Economics, 8, 1–34.
- HEATHCOTE, J., K. STORESLETTEN, AND G. L. VIOLANTE (2017): "Optimal tax progressivity: An analytical framework," The Quarterly Journal of Economics, 132, 1693–1754.
- HENDREN, N. (2015): "The Policy Elasticity," in <u>Tax Policy and the Economy, Volume 30</u>, University of Chicago Press.

- HENDRICKS, L. AND T. SCHOELLMAN (2018): "Human capital and development accounting: New evidence from wage gains at migration," The Quarterly Journal of Economics, 133, 665–700.
- HICKS, J. R. (1939): "The foundations of welfare economics," The Economic Journal, 49, 696–712.
- ——— (1940): "The valuation of the social income," Economica, 7, 105–124.
- JUHN, C., K. M. MURPHY, AND R. H. TOPEL (2002): "Current unemployment, historically contemplated," Brookings Papers on Economic Activity, 2002, 79–116.
- KALDOR, N. (1939): "Welfare propositions of economics and interpersonal comparisons of utility," The Economic Journal, 549–552.
- KATZ, L. F. AND K. M. MURPHY (1992): "Changes in Relative Wages, 1963-1987: Supply and Demand Factors," The Quarterly Journal of Economics, 107, 35–78.
- KERR, W. R. AND W. F. LINCOLN (2010): "The supply side of innovation: H-1B visa reforms and US ethnic invention," Journal of Labor Economics, 28, 473–508.
- KHANNA, G. AND M. LEE (2018): "High-skill immigration, innovation, and creative destruction," Tech. rep., National Bureau of Economic Research.
- KRUGMAN, P. (2006a): "North of the Boarder," New York Times, op-ed: https://www.nytimes.com/2006/03/27/opinion/north-of-the-border.html/.
- LEWIS, E. (2011): "Immigration, skill mix, and capital skill complementarity," The Quarterly Journal of Economics, 126, 1029–1069.
- ———— (2013): "Immigration and production technology," Annu. Rev. Econ., 5, 165–191.
- LLULL, J. (2017): "The effect of immigration on wages: exploiting exogenous variation at the national level," Journal of Human Resources, 0315–7032R2.
- LOCKWOOD, B. B. AND M. WEINZIERL (2016): "Positive and normative judgments implicit in US tax policy, and the costs of unequal growth and recessions," <u>Journal of Monetary Economics</u>, 77, 30–47.
- Low, H., C. Meghir, L. Pistaferri, and A. Voena (2018): "Marriage, labor supply and the dynamics of the social safety net," <u>NBER Working Paper No. 24356</u>.
- MANACORDA, M., A. MANNING, AND J. WADSWORTH (2012): "The impact of immigration on the structure of wages: Theory and evidence from Britain," <u>Journal of the European</u> Economic Association, 10, 120–151.
- MEYER, B. D., W. K. MOK, AND J. X. SULLIVAN (2015): "Household surveys in crisis," Journal of Economic Perspectives, 29, 199–226.
- Monras, J. (2020): "Immigration and wage dynamics: Evidence from the mexican peso crisis," Journal of Political Economy, 128.

- Monras, J., J. Vázquez-Grenno, and F. Elias (2018): "Understanding the Effects of Legalizing Undocumented Immigrants," CEPR Discussion Paper No. DP12726.
- NATIONAL ACADEMY OF SCIENCES, U. S. (2017): The economic and fiscal consequences of immigration, National Academies Press.
- Ottaviano, G. I. and G. Peri (2012): "Rethinking the effect of immigration on wages," Journal of the European economic association, 10, 152–197.
- PATT, A., J. RUHOSE, S. WIEDERHOLD, AND M. FLORES (2020): "International emigrant selection on occupational skills," Journal of the European Economic Association.
- PERI, G., K. SHIH, AND C. SPARBER (2015): "STEM workers, H-1B visas, and productivity in US cities," Journal of Labor Economics, 33, S225–S255.
- PERI, G. AND C. SPARBER (2009): "Task Specialization, Immigration, and Wages," <u>American</u> Economic Journal: Applied Economics, 1, 135–69.
- PIKETTY, T. AND E. SAEZ (2013): "Optimal labor income taxation," <u>Handbook of Public</u> Economics, Vol 5.
- PIYAPROMDEE, S. (2020): "The impact of immigration on wages, internal migration and welfare," Tech. rep., Working paper.
- PRESTON, I. (2014): "The effect of immigration on public finances," <u>The Economic Journal</u>, 124, 569–F592.
- Ruggles, S., J. T. Alexander, K. Genadek, R. Goeken, M. B. Schroeder, and M. Sobek (2010): "Integrated Public Use Microdata Series: Version 5.0 [Machine-readable database]," Minneapolis: University of Minnesota.
- Ruist, J. (2015): "The fiscal cost of refugee immigration: the example of Sweden," <u>Population</u> and <u>Development Review</u>, 41, 567–581.
- SACHS, D., A. TSYVINSKI, AND N. WERQUIN (2020): "Nonlinear tax incidence and optimal taxation in general equilibrium," Econometrica, 88, 469–493.
- SAEZ, E. AND S. STANTCHEVA (2016): "Generalized Social Marginal Welfare Weights for Optimal Tax Theory," American Economic Review, 106, 24–45.
- SAIZ, A. (2003): "Room in the kitchen for the melting pot: Immigration and rental prices," Review of Economics and Statistics, 85, 502–521.
- STORESLETTEN, K. (2000): "Sustaining fiscal policy through immigration," <u>Journal of political Economy</u>, 108, 300–323.
- Tsyvinski, A. and N. Werquin (2019): "Generalized Compensation Principle," Working Paper.

Appendix for Online Publication

A Extensions Appendix

In this Appendix, we evaluate the indirect fiscal effects using several alternative model specifications. Appendices A.1 through A.3 consider alternative production functions utilized in the immigration literature. As we focus on differences in production functions, we consider the case with exogenous native labor supply. Appendix A.4 considers the case when workers can endogenously choose their supply of communication- and manual-intensive tasks. Appendix A.5 considers the case with decreasing returns to scale. For the sake of readability, we have relegated most proofs to Appendix B.

A.1 Imperfectly Substitutable Education and Experience

In this Appendix, we evaluate the indirect fiscal effects using the model from Borjas (2003). Production takes the form of a two-level nested CES function.⁷² The top level of the production function combines labor supplies of four education groups: high school dropouts, high school graduates, some college, and college graduates. Letting e index education groups, output Y is given by

$$Y = \left(\sum_{e} \theta_{e} \mathcal{L}_{e}^{\frac{\sigma_{E} - 1}{\sigma_{E}}}\right)^{\frac{\sigma_{E}}{\sigma_{E} - 1}},$$

where \mathcal{L}_e is the labor aggregate of labor of education group e, σ_E is the elasticity of substitution between education groups, and θ_e is a factor-intensity parameter. Due to this finer stratification of skill groups, an increase in the number of high school dropouts, for example, affects the relative wages of dropouts to high school graduates, in addition to the relative wages of high-skilled versus low-skilled workers.

In turn, each education-specific labor aggregate is itself an aggregator of experience levels within a given education group. As in Borjas (2003), we divide workers into 8 experience levels consisting of 5-year experience intervals, starting with 1-5 years experience until 36-40 years of experience. Letting a index these experience levels, we can write

$$\mathscr{L}_e = \left(\sum_a \theta_{ae} \mathscr{L}_{ae}^{\frac{\sigma_X - 1}{\sigma_X}}\right)^{\frac{\sigma_X}{\sigma_X - 1}}$$

where \mathcal{L}_{ae} gives the labor supply of a given experience-education group and is given by $\mathcal{L}_{ae} = \int_{\mathcal{I}_{ae}} L_i \omega_i di$, and where \mathcal{I}_{ae} is the set of types within a given experience-education group. The parameter σ_X is equal to the elasticity of substitution of experience levels within the same education group and θ_{ae} is a factor-intensity parameter. Therefore, within the

 $^{^{72}}$ We abstract away from physical capital (or alternatively assume that capital supply is perfectly elastic) in Sections A.1 through A.5. We discuss the role of capital in Section 7.1.

Experience Group	HS Dropout	HS Graduate
1-5	1,595	1,368
6-10	1,803	$1,\!597$
11-15	1,720	1,650
16-20	1,844	1,732
21-25	1,825	1,786
26-30	1,948	1,926
31-35	2,043	2,016
36-40	2,172	2,056
Education Average	1,932	1,834
Overall Average	1,	873

Table 6: Indirect Fiscal Effects using model from Borjas (2003). Each entry gives the indirect fiscal effect associated with a worker in each narrow education and experience group. The "Education Average" gives the weighted average indirect fiscal effect within each education group and the "Overall Average" is the weighted average across all groups.

same education level, workers of different experience levels are imperfectly substitutable in production. Immigrant inflows therefore change the relative wages of different experience groups within the same education level.

As we show in Appendix B.3, if labor supply is inelastic, the indirect fiscal benefit of an immigrant of type i in experience group a and education group e is given by

$$d\mathcal{R}_{ind}^{\text{Borjas}}(a, e, i) = y_i \left[\underbrace{\left(\bar{T}'_{a' \neq a, e} - \bar{T}'_{ae}\right) |\tilde{\gamma}_{ae, own}|}_{\text{Experience Effect}} + \underbrace{\left(\bar{T}'_{e' \neq e} - \bar{T}'_{e}\right) |\gamma_{e, own}|}_{\text{Education Effect}} \right], \tag{13}$$

where $\tilde{\gamma}_{ae,own}$ is the own-wage elasticity of experience group a and education group e, holding the overall ratio of education groups constant, $\bar{T}'_{a'\neq a,e}$ is the income weighted average tax rate of all other experience groups in education group e, $\bar{T}'_{e'\neq e}$ is the income weighted tax rate of all other education groups, $\gamma_{e,own}$ is the own-wage elasticity of education group e, where the wage of an education group is defined as $\frac{\partial Y}{\partial \mathscr{L}_e}$. Therefore, we can decompose the indirect fiscal effect into two separate effects. The first effect, which we label the "experience effect" comes from the fact that an immigrant inflow of experience group a increases the supply of experience group a relative to all other experience groups within education group e. The "education effect" captures that the immigrant inflow also increases the ratio of labor from education group e relative to all other education groups.

Results Following Borjas (2003), we set $\sigma_X = 3.5$ and set $\sigma_E = 1.3$. The indirect fiscal effect associated with a worker in each of the experience groups for both high school dropouts and high school graduates are given in Table 6. The first column gives the indirect fiscal effect associated with high school dropouts and the second column gives the effect associated with high school graduates. The fiscal effect of both education levels is increasing in experience

level, reflecting that incomes are increasing in experience. Across all experience groups, the average high school dropout is associated with a \$1,932 indirect fiscal benefit and the high school graduate with a \$1,834 indirect fiscal benefit. The average low-skilled immigrant across education groups leads to a fiscal benefit of \$1,873.

To better understand why the indirect fiscal effect here is larger than in the previous sections, we now perform several alternative calculations. First, to understand the role of the "experience effect", we calculate the indirect fiscal benefit when experience groups are perfect substitutes within education, by setting $\frac{1}{\sigma_X} = 0$. This has only a slight effect on the indirect fiscal effect: the average indirect fiscal effect increases from \$1,873 in the baseline case to \$1,892 in the case when experience groups are perfect substitutes within education group. Next, to understand the role of the elasticity of substitution parameter, we calculate the indirect fiscal benefit under the assumption that the elasticity of substitution is equal to 2 by setting $\sigma_E = 2$. This reduces the average fiscal benefit to \$1,230, similar in magnitude to the effect we found in Section 3. Therefore, despite the key differences between the production function here and that presented in Section 3, both production functions lead to similar estimates of the indirect fiscal effect of low-skilled immigration, once we use comparable parameter estimates.

A.2 Domestic-Born and Foreign-Born Complementarity

Ottaviano and Peri (2012) consider a model in which domestic- and foreign-born workers are imperfect substitutes within education and experience groups. Ultimately the production function takes the form of a four-level nested CES labor aggregate function, with a top nest corresponding to skill groups (high skill and low skill), a second nest corresponding with education groups within these two skill groups (high school graduate and dropout within low-skilled workers, some college and college graduate within high-skilled), a third nest corresponding with 8 experience groups within each education group, and a final nest aggregating domesticand foreign-born workers.⁷³

Specifically, the top nest of the production functions combines a high-skilled labor aggregate \mathcal{L}_s and a low-skilled labor aggregate \mathcal{L}_u using the following production function

$$Y = \left(\theta_s \mathscr{L}_s^{\frac{\sigma-1}{\sigma}} + \theta_u \mathscr{L}_u^{\frac{\sigma-1}{\sigma}}\right)^{\frac{\sigma}{\sigma-1}}.$$

 \mathcal{L}_s aggregates some college and college graduate labor while \mathcal{L}_u aggregates high school dropout and high school graduate labor. Let e_1, e_2, e_3 , and e_4 denote high school dropout, high school graduate, some college and college graduate labor, respectively. Then we can write

$$\mathcal{L}_{s} = \left(\theta_{e_{3}}\mathcal{L}_{e_{3}}^{\frac{\sigma_{S}-1}{\sigma_{S}}} + \theta_{e_{4}}\mathcal{L}_{e_{4}}^{\frac{\sigma_{S}-1}{\sigma_{S}}}\right)^{\frac{\sigma_{S}}{\sigma_{S}-1}}$$

⁷³We focus on "Model B" from Ottaviano and Peri (2012), which the authors show is the most consistent with the data. We use their estimates from column 7 of Table 6.

and

$$\mathcal{L}_{u} = \left(\theta_{e_{1}} \mathcal{L}_{e_{1}}^{\frac{\sigma_{U}-1}{\sigma_{U}}} + \theta_{e_{2}} \mathcal{L}_{e_{2}}^{\frac{\sigma_{U}-1}{\sigma_{U}}}\right)^{\frac{\sigma_{U}}{\sigma_{U}-1}}.$$

Each of these education aggregates combine labor from 8 experience groups, indexed by a, as

$$\mathcal{L}_e = \left(\sum_{a} \theta_{ae} \mathcal{L}_{ae}^{\frac{\sigma_{EXP} - 1}{\sigma_{EXP}}}\right)^{\frac{\sigma_{EXP}}{\sigma_{EXP} - 1}}.$$

for $e \in \{e_1, e_2, e_3, e_4\}$. Finally, each of the education, experience labor aggregates, \mathcal{L}_{ae} combines nativity groups (domestic-born and foreign-born) labor using

$$\mathscr{L}_{ae} = \left(heta_{aef} \mathscr{L}_{aef}^{rac{\sigma_{N,U}-1}{\sigma_{N,U}}} + heta_{aed} \mathscr{L}_{aed}^{rac{\sigma_{N,U}-1}{\sigma_{N,U}}}
ight)^{rac{\sigma_{N,U}}{\sigma_{N,U}-1}}$$

and low-skilled labor $(e \in \{e_1, e_2\})$ and

$$\mathcal{L}_{ae} = \left(\theta_{aef} \mathcal{L}_{aef}^{\frac{\sigma_{N,S}-1}{\sigma_{N,S}}} + \theta_{aed} \mathcal{L}_{aed}^{\frac{\sigma_{N,S}-1}{\sigma_{N,S}}}\right)^{\frac{\sigma_{N,S}}{\sigma_{N,S}-1}}$$

for high-skilled labor ($e \in \{e_3, e_4\}$). \mathcal{L}_{aen} gives the labor supply of a given education-experience-nativity group ($n \in \{d, f\}$) and is given by $\mathcal{L}_{aen} = \int_{\mathcal{I}_{aen}} L_i \omega_i di$, and where \mathcal{I}_{aen} is the set of types i within a given education-experience-nativity group.

The indirect fiscal benefit of an immigrant of type i in experience group a' and education group e' is given by

$$d\mathcal{R}_{ind}\left(a',e',i\right) = \frac{y_i}{\bar{y}_{a'e'f}} \sum_{a} \sum_{e} \sum_{n} \bar{T}'_{aen} \frac{N_{aen}}{N_{a'e'f}} \bar{y}_{aen} \gamma_{aen,a'e'f}$$

where \bar{y}_{aen} is the average income of workers of experience group a, education group e, and nativity n, \bar{T}'_{aen} is the income-weighted average marginal tax of workers in this group, and $\gamma_{aen,a'e'f} = \frac{\partial w_{aen}}{\partial L_{a'e'f}} \frac{L_{a'e'f}}{w_{aen}}$ is the elasticity of wages of workers of experience group a and education e and nativity n with respect to labor supply of foreign-born workers of experience group a' and education e'. We refrain from further simplifying the formula in this case.

Results We quantify the model using parameters estimates from Ottaviano and Peri (2012). Table 7 gives the indirect fiscal effect associated with an immigrant with average income in each experience group for both high school dropouts and high school graduates. The average high school dropout immigrant leads to an indirect fiscal benefit of \$920 while the average high school graduate immigrant leads to an indirect fiscal benefit of \$1,161. Taken together, this implies the average low-skilled immigrant leads to an average indirect fiscal effect of \$1,065.

Experience Group	HS Dropout	HS Graduate
1-5	796	888
6-10	945	1,014
11-15	876	1,026
16-20	868	1,112
21-25	838	1,111
26-30	915	1,206
31-35	996	1,289
36-40	1,014	1,321
Education Average	920	1,161
Overall Average	1,0	065

Table 7: Indirect Fiscal Effects using model from Ottaviano and Peri (2012). Each entry gives the indirect fiscal effect associated with a worker in each narrow education and experience group. The "Education Average" gives the weighted average indirect fiscal effect within each education group and the "Overall Average" is the weighted average across all groups. We focus on "Model B" from Ottaviano and Peri (2012), which the authors show is the most consistent with the data. We use estimates from column 7 of Table 6, which gives an elasticity of substitution between skill levels of 1.85.

To better understand the implications of the nesting structure on the indirect fiscal effects, we sequentially recalculate the indirect fiscal effects under the assumptions that labor supplies in each of the CES nests are perfectly substitutable. First, we assume domestic- and foreignborn workers within experience-education-skill groups are perfect substitutes. This leads to a fiscal benefit of \$1,057. Next, we additionally assume workers of difference experience groups within the same education level are perfect substitutes. This implies a fiscal benefit of \$1,065. Finally, we remove imperfect substitutability between narrow education groups. This model now shares the same structure as the model presented in Section 3, as all workers within the two skill groups are perfectly substitutable. In this case the indirect fiscal benefit is \$1,059.

A.3 Skills Defined by Position in Wage Distribution

In this Appendix, we calculate the indirect fiscal effects using the model presented in Dustmann et al. (2013), which a worker's skill is given by her position in the wage distribution. Let total output be given by the CES aggregator

$$Y = \left(\sum_{j} \theta_{j} \mathcal{L}_{j}^{\frac{\sigma-1}{\sigma}}\right)^{\frac{\sigma}{\sigma-1}},$$

where \mathcal{L}_j gives the labor supply of a given skill group, and skill groups are defined by position in the wage distribution (for example percentiles or deciles). Formally, \mathcal{L}_j is given by $\mathcal{L}_j = \int_{\mathcal{I}_j} L_i \omega_i di$, where \mathcal{I}_j is the set of workers types within skill group j. The parameter σ gives the elasticity of substitution between skill groups and each θ_j parameter measures the factor

Decile of	Indirect	% of LS
Wage Distribution	Fiscal Effect	Immigrants
1	970	20
2	1,182	22
3	1,366	17
4	1,625	10
5	1,825	9
6	1,768	7
7	1,460	5
8	643	4
9	-588	3
10	-10,924	2
Overall Average	1,0	17

Table 8: Indirect Fiscal Effects using model from Dustmann, Frattini, and Preston (2013). The second columns gives the indirect fiscal effect for an immigrant in each decile of the wage distribution. The right column gives the percent of total low-skilled immigrants in each wage decile. The bottom row gives the weighted average of the indirect fiscal effects across the wage distribution.

intensity of skill type j. As we show in Appendix B.4, the indirect fiscal benefit associated with an immigrant of type i in skill group j is given by

$$d\mathcal{R}_{ind}^{\text{DFP}}(j,i) = y_i \times |\gamma_{j,own}| \times (\bar{T}'_{k\neq j} - \bar{T}_j),$$

where y_i is the income level of workers of type i, $\bar{T}'_{k\neq j}$ is the income weighted average marginal tax rate of all other groups $k\neq j$, and \bar{T}'_j is the income weighted average marginal tax rate income group j. Given the CES production function, the own-wage elasticity has the simple expression $\frac{1-\kappa_j}{\sigma}$, where κ_j is the income share of workers in skill group j.

Results We define skill groups using deciles of the wage distribution.⁷⁴ The results are not sensitive to the grouping of j. We use our central value for the elasticity of substitution between skill groups and set $\sigma = 2$.⁷⁵ Table 8 gives the indirect fiscal effect associated with the average immigrant of each decile of the wage distribution. The indirect fiscal effect is increasing in wage decile up until the 5th decile, reflecting the fact that income is increasing in the wage decile. Starting with the 6th decile, the indirect fiscal benefit decreases as the average marginal tax rates increase relative to the average marginal tax rates of other groups. The weighted average indirect fiscal effect is \$1,017, similar to the fiscal effect found in Section 3 when we set $\sigma = 2$.

⁷⁴We calculate wages as total wage and self-employment income divided by weeks worked and average hours worked. In the 2017 ACS, weeks worked are intervalled, we use the midpoint of the interval.

 $^{^{75}}$ Using data from the UK, Dustmann, Frattini, and Preston (2013) find that an elasticity of substitution between skill group of 0.6 fits their reduced form evidence best. Using this value as the elasticity of substitution yields and an average indirect fiscal benefit of low-skilled immigrants of \$2,766. We believe the value of $\sigma = 2$ to be more appropriate for the US context.

A.4 Endogenous Occupational Choice of Natives

In this Appendix, we evaluate the indirect fiscal effects in a model with endogenous occupation choice, as in Peri and Sparber (2009). Perfectly competitive firms produce a numeraire output good using cognitive, communication and manual tasks. Cognitive tasks are supplied by high-skilled individuals. Communication and manual tasks are performed by low-skilled individuals. Denote by M total manual task supply and by C total communication task supply. In the bottom nest of the production function, these tasks combine to form the aggregate of low-skilled labor, \mathcal{L}_u , as

$$\mathcal{L}_{u} = \left(\theta_{u} M^{\frac{\sigma_{u} - 1}{\theta_{u}}} + (1 - \theta_{u}) C^{\frac{\sigma_{u} - 1}{\sigma_{u}}}\right)^{\frac{\sigma_{u}}{\sigma_{u} - 1}}.$$
(14)

The parameter σ_u measures the elasticity of substitution between communication and manual tasks and θ_u measures the factor intensity of manual tasks. The task supplies M and C are given by the sum of each task supplied by both low-skilled domestic-born and foreign-born workers. Letting d index low-skilled domestic-born workers, and f index low-skilled foreign-born workers, we can write the total manual task supply as $M = N_f m_f + N_d m_d$ where N_f and N_d are the total number of low-skilled foreign-born and domestic-born workers in the economy and m_f and m_d are the amounts of manual tasks supplied by each low-skilled foreign- and domestic-born worker, respectively. Similarly, we can write the supply of communication tasks as $C = N_f c_f + N_d c_d$ where c_f and c_d are the endogenous amounts of communication tasks supplied by each low-skilled foreign- and domestic-born worker, respectively.

Each high-skilled worker inelastically supplies one unit of the cognitive task; aggregate high-skilled labor \mathcal{L}_s is simply the total cognitive task supplied in the economy. High-skilled labor \mathcal{L}_s and the aggregate of low-skilled labor, \mathcal{L}_u , are aggregated according to:

$$Y = A \left(\theta \mathcal{L}_{u}^{\frac{\sigma-1}{\sigma}} + (1-\theta) \mathcal{L}_{s}^{\frac{\sigma-1}{\sigma}}\right)^{\frac{\sigma}{\sigma-1}}, \tag{15}$$

where Y is the produced amount of the numeraire output good. The parameter σ corresponds with the elasticity of substitution between high-skilled labor and the low-skilled aggregate. Total factor productivity is given by A and θ gives the factor intensity of low-skilled labor.

Let w_c , w_m and w_s denote the compensation for one unit of communication, manual and cognitive tasks. As firms are perfectly competitive, these task prices are given by the marginal products of each task. Since high-skilled workers supply exactly one unit of the cognitive task, their income equals the task wage, hence we have $y_s = w_s$. For low-skilled workers, income is given by the sum of the worker's task supplies multiplied by the appropriate task prices. Letting $j \in \{f, d\}$ index low-skilled worker types (foreign-born or domestic-born), we can write the agent's income as $y_j = c_j w_c + m_j w_m$.

The indirect fiscal benefit resulting from an inflow of dN_f workers is given by

$$d\mathscr{R}_{ind}^{PS} = T_s' N_s \frac{dy_s}{dN_f} dN_f + T_f' N_f \frac{dy_f}{dN_f} dN_f + T_d' N_d \frac{dy_d}{dN_f} dN_f.$$
 (16)

That is, the total indirect fiscal effect is given by the change in income of each type of worker multiplied by the number of workers of that type and the marginal tax rate. It's important to note that changes in income for low-skilled workers, $\frac{dy_f}{dN_f}$ and $\frac{dy_d}{dN_f}$, arise for two reasons. First, low-skilled immigrant inflows change task prices w_c and w_m , and therefore the incomes of foreign- and domestic-born workers. Second, income will change as a result of changes in task supplies in response to these inflows. For example, if low-skilled domestic-born workers respond to immigrant inflows by increasing the amount of communication task they supply (perhaps by moving into managerial occupations), this will lead to an additional change in native income in response to immigrant inflows. We show in Appendix B.5 how this formula can be written as a function of structural parameters and task supply elasticities.

Quantification We quantify the indirect fiscal effects by utilizing estimates of task intensities from ONET and selected parameter estimates from Peri and Sparber (2009). The procedure we use for estimating income and marginal tax rates are similar to those in other sections. Details can be found in Appendix C.5. Here we focus on the parameter estimates we take from Peri and Sparber (2009).

Peri and Sparber (2009) estimate the elasticity of substitution between manual and communication tasks, σ_u , using state level variation in immigrant inflows. We set $\sigma_u = 1$ and set the elasticity of substitution between low- and high-skilled workers as $\sigma = 1.75$, based on their estimates. Peri and Sparber (2009) also use this variation to estimate the elasticities of task supplies with respect to the immigrant share of low-skilled workers. We directly use these estimates of task supply elasticities. Most notably, they find that domestic-born workers respond to low-skilled immigrant inflows by increasing their communication task supply and that foreign-born workers do not change their task supplies in response to immigrant inflows.

Results First of all, we calculate the indirect fiscal effect which would result if workers did not adjust their occupation. We find this number to be \$1,115, which is in a similar ballpark as the numbers we found in Section 5.However, once we allow for endogenous occupation choice, low-skilled domestic-born workers respond by switching into higher-paying communication-intensive occupations. This increases their incomes and thus their tax payments. Holding task prices constant, this occupation upgrading leads to an additional fiscal effect of \$899.⁷⁶ Finally, these occupation changes lead to additional changes in the equilibrium task prices

⁷⁶Note that this effect constitutes a fiscal externality. This fiscal externality is much larger than the externality resulting from hours worked and participation responses in the canonical model.

leading to an additional fiscal effect of \$117.77 Ultimately, the indirect fiscal effect is equal to $d\mathcal{R}_{ind}^{PS} = \$2,\!131$ with endogenous occupation choice.

A.5 Decreasing Returns to Scale

Consider a homogeneous production function with two inputs,

$$Y = F\left(\mathcal{L}_u, \mathcal{L}_s\right),\,$$

where, as before, $\mathcal{L}_u = \int_{\mathcal{I}_u} L_i \omega_i di$ and $\mathcal{L}_s = \int_{\mathcal{I}_s} L_i \omega_i di$. Let λ be the degree of homogeneity: $F\left(t\mathcal{L}_u, t\mathcal{L}_s\right) = t^{\lambda} F\left(\mathcal{L}_u, \mathcal{L}_s\right)$. With decreasing returns to scale $(\lambda < 1)$, an immigrant inflow can also lead to changes in firm profits in addition to changes in wages. Therefore, holding labor supply constant, the indirect fiscal effects of immigration with decreasing returns are given by:

$$d\mathscr{R}_{ind}^{\mathrm{DRS}}\left(i\right) = h_{i}\omega_{i}\left[\tau_{p}\frac{\partial\pi}{\partial\mathscr{L}_{u}} + \int_{\mathcal{I}_{s}}T'\left(y_{i},i\right)\frac{\partial w_{s}}{\partial\mathscr{L}_{u}}h_{i}\omega_{i}m_{i}di + \int_{\mathcal{I}_{u}}T'\left(y_{i},i\right)\frac{\partial w_{u}}{\partial\mathscr{L}_{u}}h_{i}\omega_{i}m_{i}di\right],$$

where π represents total firm profits and τ_p is the tax rate on firm profits.

In the case of constant returns to scale, the indirect fiscal effects arose because of a change in relative incomes of high-skilled and low-skilled workers. With decreasing returns to scale, there is a second effect arising from an increase in firm profits relative to worker income. As we show in Appendix B.6 the indirect fiscal effect of an immigrant of type i with decreasing returns to scale is given by

$$d\mathcal{R}_{ind}^{DRS}(i) = y_i \left[\underbrace{\left(\bar{T}_s' - \bar{T}_u'\right) |\tilde{\gamma}_{u,own}|}_{\text{Factor Ratio Effect}} + \underbrace{\left(1 - \lambda\right) \left(\tau_p - \bar{T}_I'\right)}_{\text{Scale Effect}} \right]. \tag{17}$$

Consider the first term of (17), which we refer to as the "factor ratio effect". The term $\tilde{\gamma}_{u,own}$ gives the own-wage elasticity for low-skilled workers, holding total labor income constant. Specifically, this term is given by $\tilde{\gamma}_{u,own} = \gamma_{u,own} + \kappa_u (1 - \lambda)$, where $\kappa_u = \frac{\mathcal{L}_u w_u}{\mathcal{L}_s w_s + \mathcal{L}_u w_u}$ is the labor income share of low-skilled labor.⁷⁸ This factor ratio effect gives the indirect fiscal effect as a result of changing the relative wages of high-skilled relative to low-skilled workers.

In addition to changing the factor ratio, an influx of low-skilled labor also increases the scale of production and therefore increases profits at the cost of worker income. We refer to the resulting fiscal effect as the "scale effect", which is the second term in (17). The term \bar{T}'_I

⁷⁷This term is positive because the increase in supply of communication tasks by low-skilled workers implies an increase in cognitive wages, an increase in manual wages but a decrease in communication wages.

⁷⁸Note that $-\kappa_u (1 - \lambda)$ is the effect of immigration on low-skilled income that occurs through the scale effect – if total income changes but the share going to low-skilled workers stays constant. Therefore, we can think of $\tilde{\gamma}_{u,own}$ as as the change in low-skilled income from immigration minus the scale effect. Note that if the production function exhibits constant returns to scale, then this elasticity is independent of scale and we have $\tilde{\gamma}_{u,own} = \gamma_{u,own}$.

gives the income-weighted average marginal tax of all workers. A smaller value of λ implies lower returns to scale and therefore a greater redistribution of surplus from workers to firms. The fiscal effects of the redistribution are scaled by the differences in the average tax rates between firms and workers, $(\tau_p - \bar{T}'_I)$.

Results To calculate the fiscal effects with decreasing returns to scale, we need estimates of the profit tax τ_p , income weighted marginal tax rates, the returns to scale, λ , and $\tilde{\gamma}_{u,own}$, the own-wage elasticity of low-skilled labor, holding labor income constant. For the profit tax, we use the weighted average of the state and federal corporate tax rates and the business income weighted average income tax rate, which is the tax rate that applies for pass-through businesses. This gives us an estimate of $\tau_p = 36.8\%$. We estimate a marginal tax rate for all workers as $\bar{T}'_I = 34.2\%$. Finally, we take our value of $\lambda = .9$ from Burnside (1996), who estimates returns to scale for US industries. Finally, $\tilde{\gamma}_{u,own} = -\frac{1}{\sigma}\kappa_s$, where again σ is the elasticity of substitution between low- and high-skilled labor. Therefore, $\tilde{\gamma}_{u,own}$ is the same as the own-wage elasticity with constant returns to scale, given the same value for σ .

Putting this together, we estimate that if production exhibits decreasing returns to scale, the indirect fiscal effect associated with the average low-skilled immigrant is equal to \$1,057 given an elasticity of substitution of $\sigma = 2$. Recall that with constant returns to scale and $\sigma = 2$, we calculated an indirect fiscal effect with exogenous labor supply of \$975. The small increase in the fiscal effect with decreasing returns is due to the scale effect: profits increase relative to labor income and profits face a higher marginal tax rate than labor income.⁸²

B Theoretical Appendix

B.1 Relation between Own-Wage Elasticity and Elasticity of Substitution

To understand the relationship $\gamma_{u,own} = \frac{\frac{N_s y_s}{N_u y_u + N_s y_s}}{\sigma}$, first recall the definition of the elasticity of substitution

 $^{^{79}\}mathrm{Corporations}$ account for 60% of total net income from business. We calculate τ_p as .6 times federal and average state corporate tax rate plus .4 times the business income weighted average effective tax rate arising from income taxes and transfers using our ACS data. In 2017, the federal corporate tax rate plus the average of the state income tax rates was 38.9%. Source: https://taxfoundation.org/us-corporate-income-tax-more-competitive/. We find a business income weighted effective tax rate of 33.9%.

⁸⁰Burnside (1996) estimates a weighted average of industry specific returns to scale of .9.

⁸¹As we show in Appendix B.6, the own-wage elasticity with decreasing returns to scale is given by $\gamma_{u,own} = (\lambda - 1) \kappa_u - \frac{1}{\sigma} \kappa_s$. Therefore, the own-wage elasticity holding labor income constant is simply given by $\tilde{\gamma}_{u,own} = -\frac{1}{\sigma} \kappa_s$.

 $^{-\}frac{\pi}{6}\kappa_s$.

82It's worth noting that corporate tax rates dropped substantially in 2018 to a weighted average of 25.7%. Performing this calculating with 2018 corporate tax rates implies an indirect fiscal effect of \$817.

$$\sigma = -\frac{\frac{\partial \mathcal{L}_u}{\partial \mathcal{L}_s} / \frac{\mathcal{L}_u}{\mathcal{L}_s}}{\frac{\partial w_u}{\partial w_s} / \frac{w_u}{w_s}}.$$

Now consider an increase of low skilled labor by 1%. This increases the ratio of low-skilled over high-skilled labor by 1% (since the high skilled labor stays constant). This directly implies that the relative wage ratio $\frac{\partial w_u}{\partial w_s}/\frac{w_u}{w_s}$ decreases by $\frac{1}{\sigma}$.

Next, derive the percentage change of $\frac{w_u}{w_s}$ by using the cross- and own-wage elasticity. The numerator changes by $\gamma_{u,own}\%$. The denominator changes by $\gamma_{s,cross}\%$. Hence, $\frac{\partial w_u}{\partial w_s}/\frac{w_u}{w_s} = \gamma_{u,own} - \gamma_{s,cross}$. Using Lemma 1, this can be written as: $\gamma_{u,own} + \gamma_{u,own} \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s}$.

As a consequence, we have to have

$$-\frac{1}{\sigma} = \gamma_{u,own} + \gamma_{u,own} \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s}$$

which yields the result: $\gamma_{u,own} = -\frac{\frac{N_s y_s}{N_u y_u + N_s y_s}}{\sigma}$.

B.2 Canonical Model with Labor Supply

B.2.1 Proof of Proposition 2

Note that tax revenue in this economy provided by natives is given by:

$$\mathscr{R} = \int_{\mathcal{T}_{r}} T(y_i, i) m_i di + \int_{\mathcal{T}_{r}} T(y_i, i) m_i di.$$

The indirect fiscal effect associated with an immigrant with productivity ω_j and hours h_j is given by the effect of an immigrant on tax revenue derived from natives

$$d\mathcal{R}_{ind}^{ex}(j) = \frac{d\mathcal{R}}{d\mathcal{L}_{u}} \omega_{j} h_{j}.$$

Taking derivatives yields

$$d\mathscr{R}_{ind}^{ex}(j) = \frac{\partial w_u}{\partial \mathscr{L}_u} \omega_j h_j \int_{\mathscr{I}_u} \frac{\partial T(y_i, i)}{\partial y_i} h_i \omega_i m_i di + \frac{\partial w_s}{\partial \mathscr{L}_u} \omega_j h_j \int_{\mathscr{I}_s} \frac{\partial T(y_i, i)}{\partial y_i} h_i \omega_i m_i di.$$

Next, we can use the definitions of own- and cross-wage elasticities to write

$$d\mathscr{R}_{ind}^{ex}(j) = \gamma_{u,own} \frac{\omega_j h_j}{\mathscr{L}_u} \int_{\mathcal{I}_u} \frac{\partial T(y_i, i)}{\partial y_i} h_i \omega_i w_u m_i di + \gamma_{s,cross} \frac{\omega_j h_j}{\mathscr{L}_u} \int_{\mathcal{I}_s} \frac{\partial T(y_i, i)}{\partial y_i} h_i \omega_i w_s m_i di.$$

Applying the relationship between cross- and own-wage elasticities in Lemma 2 yields

$$d\mathscr{R}_{ind}^{ex}(j) = |\gamma_{u,own}| \left(-\frac{\omega_j h_j w_u}{\mathscr{L}_u w_u} \int_{\mathcal{I}_u} \frac{\partial T(y_i, i)}{\partial y_i} h_i \omega_i w_u m_i di + \frac{w_u \mathscr{L}_u}{w_s \mathscr{L}_s} \frac{\omega_j h_j}{\mathscr{L}_u} \int_{\mathcal{I}_s} \frac{\partial T(y_i, i)}{\partial y_i} h_i \omega_i w_s m_i di \right).$$

Finally, defining income-weighted marginal tax rates as $\bar{T'}_e = \frac{\int_{i \in \mathcal{I}_e} \frac{\partial T(y_i, i)}{\partial y_i} y_i m_i di}{Y_e}$, we can rewrite the above equation as

$$d\mathcal{R}_{ind}^{ex}(j) = |\gamma_{u,own}| \times y_j \times (\bar{T'}_s - \bar{T'}_u).$$

B.2.2 Proof of Lemma 3

Tax revenue is given by

$$\mathscr{R} = \int_{\mathcal{I}_n} \left(T(y_i, i) \nu_i + T(0, i) (1 - \nu_i) \right) m_i di + \int_{\mathcal{I}_s} \left(T(y_i, i) \nu_i + T(0, i) (1 - \nu_i) \right) m_i di.$$

Denote by $\frac{dw_u}{w_u}$ and $\frac{dw_s}{w_s}$ the equilibrium changes in wages that occur due to the immigrant and the implied endogenous responses of the natives along both the intensive and the extensive margins. Then, it follows from the definitions of the labor supply elasticities that tax revenue changes according to:

$$d\mathcal{R}_{ind} = \int_{\mathcal{I}_u} T'(y_i, i) y_i \frac{dw_u}{w_u} (1 + \varepsilon_i) \nu_i m_i di + \int_{\mathcal{I}_s} T'(y_i, i) y_i \frac{dw_s}{w_s} (1 + \varepsilon_i) \nu_i m_i di + \int_{\mathcal{I}_u} T_{part}(y_i, i) y_i \frac{dw_u}{w_u} \eta_i \nu_i m_i di + \int_{\mathcal{I}_s} T_{part}(y_i, i) y_i \frac{dw_s}{w_s} \eta_i \nu_i m_i di.$$
(18)

B.2.3 Proof of Lemma 4

The set of integral equations is given by

$$\forall i \in \mathcal{I}_u : \frac{dL_i}{L_i} = \xi_i \left(\gamma_{u,own} \frac{L^{Im}}{\mathcal{L}_u} + \gamma_{u,own} \int_{\mathcal{I}_u} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_u} dj + \gamma_{u,cross} \int_{\mathcal{I}_s} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_s} dj \right)$$

and

$$\forall i \in \mathcal{I}_s : \frac{dL_i}{L_i} = \xi_i \left(\gamma_{s,cross} \frac{L^{Im}}{\mathcal{L}_u} + \gamma_{s,cross} \int_{\mathcal{I}_u} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_u} dj + \gamma_{s,own} \int_{\mathcal{I}_s} \frac{dL_j}{L_j} \frac{L_j \omega_j}{\mathcal{L}_s} dj \right).$$

This is a system of integral equations with a simple solution because the kernels of the integral equations are separable. Let's first consider the integral equation for low-skilled workers. Multiplying both sides by $\frac{\omega_i L_i}{\mathscr{L}_u}$ and integrating over \mathcal{I}_u gives

$$\int_{\mathcal{I}_{u}} \frac{dL_{i}}{L_{i}} \frac{\omega_{i} L_{i}}{\mathcal{L}_{u}} di = \int_{\mathcal{I}_{u}} \xi_{i} \left(\gamma_{u,own} \frac{L^{Im}}{\mathcal{L}_{u}} + \gamma_{u,own} \int_{\mathcal{I}_{u}} \frac{dL_{j}}{L_{j}} \frac{L_{j} \omega_{j}}{\mathcal{L}_{u}} dj + \gamma_{u,cross} \int_{\mathcal{I}_{s}} \frac{dL_{j}}{L_{j}} \frac{L_{j} \omega_{j}}{\mathcal{L}_{s}} dj \right) \frac{\omega_{i} L_{i}}{\mathcal{L}_{u}} m_{i} di$$

which can be written as

$$\frac{d\mathcal{L}_u}{\mathcal{L}_u} = \bar{\xi}^u \gamma_{u,own} \frac{L^{Im}}{\mathcal{L}_u} + \bar{\xi}^u \gamma_{u,own} \frac{d\mathcal{L}_u}{\mathcal{L}_u} + \bar{\xi}^u \gamma_{u,cross} \frac{d\mathcal{L}_s}{\mathcal{L}_s},$$

where $d\mathcal{L}_u = \int_{\mathcal{I}_u} dL_i \omega_i di$ and $\bar{\xi}^u = \frac{\int_{\mathcal{I}_i} \xi_i \omega_i L_i di}{\mathcal{L}_u} = \frac{\int_{\mathcal{I}_u} \xi_i y_i m_i \nu_i di}{Y_u}$ is the income-weighted average of the total hours elasticity of low-skilled labor.

Equivalently, we obtain

$$\frac{d\mathcal{L}_s}{\mathcal{L}_s} = \bar{\xi}^s \gamma_{s,cross} \frac{L^{Im}}{\mathcal{L}_u} + \bar{\xi}^s \gamma_{s,cross} \frac{d\mathcal{L}_u}{\mathcal{L}_u} + \bar{\xi}^s \gamma_{s,own} \frac{d\mathcal{L}_s}{\mathcal{L}_s}.$$

This is just a simple system of two linear equations and it is easy to show that it has the following solution:

$$\frac{d\mathcal{L}_u}{\mathcal{L}_u} = \frac{\bar{\xi}^u \gamma_{u,own}}{1 - \bar{\xi}^u \gamma_{u,own} - \bar{\xi}^s \gamma_{s,own}} \frac{L^{Im}}{\mathcal{L}_u}$$

and

$$\frac{d\mathcal{L}_s}{\mathcal{L}_s} = \frac{\bar{\xi}^s \gamma_{s,cross}}{1 - \bar{\xi}^u \gamma_{u,own} - \bar{\xi}^s \gamma_{s,own}} \frac{L^{Im}}{\mathcal{L}_u}.$$

Next, we obtain the wage changes for e=s,u. We can rewrite the definition of the total hours elasticity as

$$\frac{dL_i}{L_i} = \xi_i \frac{dw_e}{w_e}.$$

Again multiplying both sides by $\frac{\omega_i L_i}{\mathscr{L}_e}$ and integrating over \mathcal{I}_e yields

$$\int_{\mathcal{I}_e} \frac{dL_i}{L_i} \frac{\omega_i L_i}{\mathscr{L}_e} di = \frac{dw_e}{w_e} \int_{\mathcal{I}_e} \xi_i \frac{\omega_i L_i}{\mathscr{L}_e} di.$$

Using $d\mathcal{L}_e = \int_{\mathcal{I}_e} dL_i \omega_i di$ and $\bar{\xi}^e = \frac{\int_{\mathcal{I}_i} \xi_i \omega_i L_i di}{\mathcal{L}_e}$ gives us

$$\frac{dw_e}{w_e} = \frac{d\mathcal{L}_e}{\mathcal{L}_e} \frac{1}{\bar{\xi}^e}.$$

Therefore, we have

$$\frac{dw_u}{w_u} = \frac{\gamma_{u,own}}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \frac{L^{Im}}{\mathscr{L}_u}$$

$$\frac{dw_s}{w_s} = \frac{\gamma_{s,cross}}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \frac{L^{Im}}{\mathscr{L}_u}.$$

B.2.4 Proof of Proposition 3

Now we have described the equilibrium changes of labor supply. We can now turn to the indirect fiscal effect, which is given by:

$$\begin{split} d\mathcal{R}_{ind} &= \int_{\mathcal{I}_u} T'(y_i, i) y_i \frac{dw_u}{w_u} \left(1 + \varepsilon_i \right) \nu_i m_i di + \int_{\mathcal{I}_s} T'(y_i, i) y_i \frac{dw_s}{w_s} \left(1 + \varepsilon_i \right) \nu_i m_i di \\ &+ \int_{\mathcal{I}_u} T_{part}(y_i, i) y_i \frac{dw_u}{w_u} \eta_i \nu_i m_i di + \int_{\mathcal{I}_s} T_{part}(y_i, i) y_i \frac{dw_s}{w_s} \eta_i \nu_i m_i di. \end{split}$$

Now using the equilibrium wage changes:

$$\frac{dw_u}{w_u} = \frac{\gamma_{u,own}}{1 - \bar{\xi}^u \gamma_{u,own} - \bar{\xi}^s \gamma_{s,own}} \frac{L^{Im}}{\mathcal{L}_u}$$

and

$$\frac{dw_s}{w_s} = \frac{\gamma_{s,cross}}{1 - \bar{\xi}^u \gamma_{u,own} - \bar{\xi}^s \gamma_{s,own}} \frac{L^{Im}}{\mathcal{L}_u}$$

as well as

$$\gamma_{s,cross} = |\gamma_{u,own}| \times \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s}$$

implies the following:

$$d\mathcal{R}_{ind} = \frac{\frac{\mathcal{L}^{Im}}{\mathcal{L}_{u}} | \gamma_{u,own} | Y_{u}}{1 - \bar{\xi}^{u} \gamma_{u,own} - \bar{\xi}^{s} \gamma_{s,own}} \left(-\frac{\int_{\mathcal{I}_{u}} T'(y_{i}, i) y_{i} (1 + \varepsilon_{i}) \nu_{i} m_{i} di}{Y_{u}} + \frac{\int_{\mathcal{I}_{s}} T'(y_{i}, i) y_{i} (1 + \varepsilon_{i}) \nu_{i} m_{i} di}{Y_{s}} - \frac{\int_{\mathcal{I}_{u}} T_{part}(y_{i}, i) y_{i} \eta_{i} \nu_{i} m_{i} di}{Y_{u}} + \frac{\int_{\mathcal{I}_{s}} T_{part}(y_{i}, i) y_{i} \eta_{i} \nu_{i} m_{i} di}{Y_{s}} \right)$$

$$(19)$$

and hence

$$d\mathcal{R}_{ind}(i) = \frac{y_i |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \left(\bar{T}_s' - \bar{T}_u' + \overline{\varepsilon_s T'_s} - \overline{\varepsilon_u T'_u} + \overline{\eta_s T_{part,s}} - \overline{\eta_u T_{part,u}} \right). \tag{20}$$

B.2.5 Kaldor-Hicks Surplus

To obtain the Kaldor-Hicks surplus, one has to add up the monetized gains and losses of all citizens and the fiscal effects. Denote the direct fiscal effect by $d\mathcal{R}_{dir}$. The indirect fiscal effect is given by (see Proposition 3):

$$d\mathcal{R}_{ind}(i) = \frac{y_i |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \left(\bar{T}_s' - \bar{T}_u' + \overline{\varepsilon_s T'_s} - \overline{\varepsilon_u T'_u} + \overline{\eta_s T_{part,s}} - \overline{\eta_u T_{part,u}} \right).$$

The monetized utility effect of native individuals is simply given by the change in income that arises due to the change in wages. The changes in income due to changes in labor supply

do not matter for utility due to the envelope theorem. Hence, an individual of type i with $e_i = e$ has a utility change of

 $(1 - T'(y_i, i))y_i \frac{dw_e}{w_e},$

where $\frac{dw_e}{w_e}$ is given in Lemma 4. Integrating over all natives and adding the monetized gains and losses to the tax revenue effects gives the immigration surplus:

$$Surplus_{Kaldor-Hicks}(i) = d\mathcal{R}_{dir} + \frac{y_i |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \left(\overline{\varepsilon_s T'_s} - \overline{\varepsilon_u T'_u} + \overline{\eta_s T_{part,s}} - \overline{\eta_u T_{part,u}} \right).$$

The indirect fiscal effects that were not caused by fiscal externalities and the monetized gains and losses from natives add up to zero. What the government gains is what native taxpayers in aggregate lose.

Note that this only holds because all gains and losses are given equal weight. If we follow Hendren (2020) and weight the monetized utility gains and losses by the inverse optimum weights g(y), then we obtain:

$$Surplus_{weighted}(i) = d\mathcal{R}_{dir} + \frac{y_i |\gamma_{u,own}|}{1 + \bar{\xi}^u |\gamma_{u,own}| + \bar{\xi}^s |\gamma_{s,own}|} \times \left(\frac{\overline{g_s (1 - T'_s)} - \overline{g_u (1 - T'_u)} + \overline{T}'_s - \overline{T}'_u + \overline{\varepsilon_s T'_s} - \overline{\varepsilon_u T'_u} + \overline{\eta_s T_{part,s}} - \overline{\eta_u T_{part,u}} \right).$$

B.3 Indirect Fiscal Effect with Four Education Groups and Imperfectly Substitutable Experience Groups

We consider an immigrant i with experience a and education e. The indirect fiscal effect is given by:

$$d\mathcal{R}_{ind}\left(a,e,i\right) = h_{i}\omega_{i} \left[\sum_{e'\neq e} \sum_{a'} \left(\bar{T}'_{a'e'} \mathcal{L}_{a'e'} \frac{\partial w_{a'e'}}{\partial \mathcal{L}_{ae}} \right) + \sum_{a'\neq a} \left(\bar{T}'_{a'e} \mathcal{L}_{a'e} \frac{\partial w_{a'e}}{\partial \mathcal{L}_{ae}} \right) + \left(\bar{T}'_{ae} \mathcal{L}_{ae} \frac{\partial w_{ae}}{\partial \mathcal{L}_{ae}} \right) \right],$$

The first term captures the wage changes of individuals with different education levels, whose wage unambiguously increases. The second term captures the wage change of those with the same education but different experience, whose wage may increase or decrease. The third term captures the wage change of those with the same education and experience, whose wage unambiguously decreases.

Now we rewrite it in terms of elasticities

$$d\mathcal{R}_{ind}\left(a,e,i\right) = h_{i}\omega_{i} \left[\sum_{e' \neq e} \sum_{a'} \left(\bar{T}'_{a'e'} \frac{\mathcal{L}_{a'e'} w_{a'e'}}{\mathcal{L}_{ae}} \gamma_{a'e',ae} \right) + \sum_{a' \neq a} \left(\bar{T}'_{a'e} \frac{\mathcal{L}_{a'e} w_{a'e}}{\mathcal{L}_{ae}} \gamma_{a'e,ae} \right) + \left(\bar{T}'_{ae} w_{ae} \gamma_{ae,ae} \right) \right].$$

Let $Y_{ae} = w_{ae} \mathcal{L}_{ae}$ give aggregate income for a given education-experience group and let $Y_e = \sum_a Y_{ae}$ give aggregate income of a given education group. Further, let $\kappa_e = \frac{Y_e}{Y}$ give the income share of education group e and let $\kappa_{a,e} = \frac{Y_{ae}}{Y_e}$ give the income share of experience group e within education group e. Some standard algebra shows, that the wage elasticities read as follows for this nested CES production function:

$$\gamma_{e,e} = -\frac{1 - \kappa_e}{\sigma_E}$$

and

$$\gamma_{e',e} = \frac{\kappa_e}{\sigma_E}.$$

Further, for $e' \neq e$, we have:

$$\gamma_{a'e',ae} = \frac{\kappa_e}{\sigma_E} \kappa_{a,e} = \gamma_{e',e} \kappa_{a,e}.$$

For e' = e, this becomes:

$$\gamma_{a'e,ae} = -\frac{1 - \kappa_e}{\sigma_E} \kappa_{a,e} + \underbrace{\frac{\kappa_{a,e}}{\sigma_X}}_{:=\tilde{\gamma}_{a'e,ae}} = \gamma_{e,e} \kappa_{a,e} + \tilde{\gamma}_{a'e,ae}.$$

Finally, for e' = e and a' = a, this becomes

$$\gamma_{ae,ae} = -\frac{1 - \kappa_e}{\sigma_E} \kappa_{a,e} \underbrace{-\frac{1 - \kappa_{a,e}}{\sigma_X}}_{:=\tilde{\gamma}_{ae,ae}} = \gamma_{e,e} \kappa_{a,e} + \tilde{\gamma}_{ae,ae}.$$

Plugging this into the indirect fiscal effect formulas gives:

$$d\mathcal{R}_{ind}^{\text{Borjas}}(a, e, i) = h_{i}\omega_{i} \left[\frac{\kappa_{a,e}}{\mathcal{L}_{ae}\sigma_{E}} \left(\kappa_{e} \sum_{e' \neq e} \sum_{a'} \left(\bar{T}'_{a'e'} \mathcal{L}_{a'e'} w_{a'e'} \right) - (1 - \kappa_{e}) \left(\sum_{a'} \bar{T}'_{a'e} \mathcal{L}_{a'e} w_{a'e} \right) \right) + \frac{1}{\mathcal{L}_{ae}\sigma_{X}} \left(\kappa_{a,e} \sum_{a' \neq a} \left(\bar{T}'_{a'e} \mathcal{L}_{a'e} w_{a'e} \right) - (1 - \kappa_{a,e}) \left(\bar{T}'_{ae} \mathcal{L}_{ae} w_{ae} \right) \right) \right].$$

This can be rewritten as

$$d\mathcal{R}_{ind}^{\text{Borjas}}(a, e, i) = \underbrace{h_i \omega_i w_{ae}}_{y_i} \left[\frac{\kappa_{a,e}}{Y_{ae} \sigma_E} \left(\kappa_e \sum_{e' \neq e} (Y'_e) \times \bar{T}'_{e' \neq e} - (1 - \kappa_e) Y_e \bar{T}'_e \right) + \frac{1}{Y_{ae} \sigma_X} \left(\kappa_{a,e} \sum_{a' \neq a} (Y_{a'e}) \times \bar{T}'_{a' \neq a,e} - (1 - \kappa_{a,e}) Y_{ae} \bar{T}'_{ae} \right) \right].$$

Now use the definition of the income shares to write this as:

$$d\mathcal{R}_{ind}^{\text{Borjas}}\left(a,e,i\right) = y_{i} \left[\frac{\kappa_{a,e}\left(1-\kappa_{e}\right)Y_{e}}{Y_{ae}\sigma_{E}} \left(\bar{T}_{e'\neq e}' - \bar{T}_{e}'\right) + \frac{\left(1-\kappa_{a,e}\right)Y_{ae}}{Y_{ae}\sigma_{X}} \left(\bar{T}_{a'\neq a,e}' - \bar{T}_{ae}'\right) \right].$$

and hence

$$d\mathscr{R}_{ind}^{\mathrm{Borjas}}\left(a,e,i\right) = y_{i} \left[\left(\bar{T}_{a'\neq a,e}^{\prime} - \bar{T}_{ae}^{\prime} \right) | \tilde{\gamma}_{ae,own}| + \left(\bar{T}_{e'\neq e}^{\prime} - \bar{T}_{e}^{\prime} \right) | \gamma_{e,own}| \right].$$

B.4 Indirect Fiscal Effects in Dustmann, Frattini, and Preston (2013)

The indirect fiscal effect for an immigrant of skill group j is given by

$$d\mathcal{R}_{ind}\left(j,i\right) = h_{i}\omega_{i} \sum_{k} \int_{\mathcal{I}_{k}} T'\left(y_{i}\left(\omega'\right)\right) L_{i} \frac{\partial w_{j}}{\partial \mathcal{L}_{i}} di = h_{i}\omega_{i} \sum_{k} \bar{T}_{k}' \mathcal{L}_{j} \frac{\partial w_{k}}{\partial \mathcal{L}_{j}}.$$

Since the production function is CRS, we know by Euler's equation that

$$\mathcal{L}_j \frac{\partial w_j}{\partial L_j} = -\sum_{k \neq j} \mathcal{L}_k \frac{\partial w_k}{\partial \mathcal{L}_j}.$$

Plugging this into the indirect fiscal effect and rearranging yields:

$$d\mathcal{R}_{ind}(j,i) = h_i \omega_i \sum_{k \neq j} (\bar{T}'_k - \bar{T}'_j) \mathcal{L}_k \frac{\partial w_k}{\partial \mathcal{L}_j}$$

which can be rewritten in terms of elasticities as

$$d\mathcal{R}_{ind}(j,i) = h_i \omega_i \sum_{k \neq j} \left(\bar{T}'_k - \bar{T}'_j \right) \frac{w_k \mathcal{L}_k}{\mathcal{L}_j} \gamma_{k,j}$$

where $\gamma_{k,j} = \frac{\partial w_k}{\partial \mathcal{L}_j} \frac{\mathcal{L}_j}{w_k}$ gives the cross-wage elasticity of k's wages with respect to \mathcal{L}_j .

Given the CES production function, these cross-wage elasticities are all given by $\gamma_{k,j} = \frac{1}{\sigma} \kappa_j$, where $\kappa_j = \frac{w_j L_j}{Y}$. Plugging in and rearranging yields

$$d\mathcal{R}_{ind}(j,i) = \frac{y_i}{\sigma} \left[\left(\sum_{k \neq j} \left(\bar{T}'_k \kappa_k \right) \right) - \bar{T}'_j \sum_{k \neq j} \kappa_k \right].$$

Dividing and multiplying by $\sum_{k\neq j} \kappa_k = 1 - \kappa_j$ yields

$$d\mathscr{R}_{ind}\left(j,i\right) = \frac{y_i}{\sigma} \left[\bar{T}'_{k \neq j} - \bar{T}'_j \right] \left(1 - \kappa_j\right)$$

where $\bar{T}'_{k\neq j} = \frac{\sum_{k\neq j} T'(y_k)\omega_k}{\sum_{k\neq j} \omega_k}$ is the income weighted tax of all other group $k\neq j$.

$$d\mathcal{R}_{ind}^{DFP}(j,i) = y_i \times \left(\bar{T}'_{k\neq j} - \bar{T}_j\right) \times |\gamma_{j,own}| = y_i \times \left(\bar{T}'_{k\neq j} - \bar{T}_j\right) \frac{1 - \kappa_j}{\sigma},$$

where we used $\frac{1-\kappa_j}{\sigma} = |\gamma_{j,own}|$.

B.5 Indirect Fiscal Effect in Peri and Sparber (2009)

The starting point is equation (16)

$$d\mathscr{R}_{ind}^{PS} = T_s' N_s \frac{dy_s}{dN_f} dN_f + T_f' N_f \frac{dy_f}{dN_f} dN_f + T_d' N_d \frac{dy_d}{dN_f} dN_f.$$

We now show how this can be decomposed into three terms:

$$d\mathcal{R}_{ind} = \underbrace{d\mathcal{R}_{ind}^{SR}}_{short \text{ run effect}} + \underbrace{d\mathcal{R}_{ind}^{SORT}}_{sorting \text{ effect}} + \underbrace{d\mathcal{R}_{ind}^{PR}}_{secondary \text{ price effect}}.$$
(21)

The first term captures the indirect fiscal effect that would arise if task choices were exogenous. The second term gives the change in tax revenue that is due to the change in task supplies – holding task wages constant. The third term is similar to the first term again in that it captures changes in wages for given task supplies. It captures the changes in tax payment due to wage changes that are due to the changes in task supply of low-skilled natives and low-skilled (previous) immigrants.

To arrive at this decomposition, first note that the effect of immigration N_f on task supplies can be written (note that cognitive task supply is by assumption exogenous):

$$\frac{dM}{dN_f} = m_f + N_d \frac{dm_d}{dN_f} + N_f \frac{dm_f}{dN_f} = m_f + \left(\frac{dM}{dN_f}\right)_{ind}$$

and

$$\frac{dC}{dN_f} = c_f + N_d \frac{dc_d}{dN_f} + N_f \frac{dc_f}{dN_f} = c_f + \left(\frac{dC}{dN_f}\right)_{ind},$$

where $(\cdot)_{ind}$ captures the indirect effect through changes in task supply. These indirect effect are given by

$$\left(\frac{dC}{dN_f}\right)_{ind} = c_d \eta_d^c (1-f)^2 + c_f \eta_c^f f^2$$

and

$$\left(\frac{dM}{dN_f}\right)_{ind} = m_d \eta_d^m (1-f)^2 + m_f \eta_f^m f^2$$

where

$$\eta_j^c = \frac{dc^j}{df} \frac{1}{c^j} \text{ and } \eta_j^m = \frac{dm^j}{df} \frac{1}{m^j} \ \forall \ j = f, d \text{ and } f = \frac{N_f}{N_f + N_d}.$$

Note that η_j and η_j^m are general equilibrium elasticities that captures all adjustments and higher order wage effects. The reason why we express – in contrast to our analysis in the main model – the formula in terms of such general equilibrium elasticities is that Peri and Sparber (2009) provide estimates for these general equilibrium elasticities.

As a next step, note that the wage changes of high-skilled, foreign and domestic low-skilled workers can be written as (recall that for high skilled we have $y_s = w_s$ – wage equals income since the high-skilled exogenously supply one unit of cognitive taks):

$$\begin{split} \frac{dy_s}{dN_f} &= \frac{\partial y_s}{\partial M} \frac{dM}{dN_f} + \frac{\partial y_s}{\partial C} \frac{dC}{dN_f} \\ &= \underbrace{\frac{\partial y_s}{\partial M} m_f + \frac{\partial y_s}{\partial C} c_f}_{\text{direct effect}} + \underbrace{\frac{\partial y_s}{\partial M} \left(\frac{dM}{dN_f}\right)_{ind}}_{\text{indirect price effect}} + \underbrace{\frac{\partial y_s}{\partial C} \left(\frac{dC}{dN_f}\right)_{ind}}_{\text{indirect price effect}}, \end{split}$$

for high skilled natives,

$$\frac{dy_f}{dN_f} = \frac{dw_m}{dN_f} m_f + \frac{dw_c}{dN_f} c_f + \underbrace{w_m \frac{dm_f}{dN_f} + w_c \frac{dc_f}{dN_f}}_{\text{sorting effect}},$$

for low-skilled foreigners and

$$\frac{dy_d}{dN_f} = \frac{dw_m}{dN_f} m_d + \frac{dw_c}{dN_f} c_d + \underbrace{w_m \frac{dm_d}{dN_f} + w_c \frac{dc_d}{dN_f}}_{\text{sorting effect}},$$

for low-skilled natives. For the latter two, the changes in wages of the manual and communication tasks can be written as:

$$\frac{dw_m}{dN_f} = \underbrace{\frac{\partial w_m}{\partial M} m_f + \frac{\partial w_m}{\partial C} c_f}_{\text{direct effect}} + \underbrace{\frac{\partial w_m}{\partial M} \left(\frac{dM}{dN_f}\right)_{ind}}_{\text{indirect price effect}} + \underbrace{\frac{\partial w_m}{\partial C} \left(\frac{dC}{dN_f}\right)_{ind}}_{\text{indirect price effect}},$$

and

$$\frac{dw_c}{dN_f} = \underbrace{\frac{\partial w_c}{\partial M} m_f + \frac{\partial w_c}{\partial C} c_f}_{\text{direct effect}} + \underbrace{\frac{\partial w_c}{\partial M} \left(\frac{dM}{dN_f}\right)_{ind}}_{\text{indirect price effect}} + \underbrace{\frac{\partial w_c}{\partial C} \left(\frac{dC}{dN_f}\right)_{ind}}_{\text{indirect price effect}}.$$

Rearranging terms, we can now obtain (21). We describe the three terms one after another. All the terms are expressed in terms of empirical objects. For the quantification, see Appendix C.5.

Short Run Effect: Collecting the terms that do not involve endogenous task responses yields:

$$d\mathcal{R}_{ind}^{SR} = T_s' N_s \frac{dy_s}{dN_f} |_{dc_j = dm_j = 0} dN_f + T_f' N_f \frac{dy_f}{dN_f} |_{dc_j = dm_j = 0} dN_f + T_d' N_d \frac{dy_d}{dN_f} |_{dc_j = dm_j = 0} dN_f,$$

where

$$\frac{dy_s}{dN_f}|_{dc_j = dm_j = 0} = \frac{\partial y_s}{\partial M} m_f + \frac{\partial y_s}{\partial C} c_f$$

$$\frac{dy_f}{dN_f}|_{dc_j = dm_j = 0} = m_f \left(\frac{\partial w_m}{\partial M} m_f + \frac{\partial w_m}{\partial C} c_f \right) + c_f \left(\frac{\partial w_c}{\partial M} m_f + \frac{\partial w_c}{\partial C} c_f \right),$$

and

$$\frac{dy_d}{dN_f}|_{dc_j = dm_j = 0} = m_d \left(\frac{\partial w_m}{\partial M} m_f + \frac{\partial w_m}{\partial C} c_f \right) + c_d \left(\frac{\partial w_c}{\partial M} m_f + \frac{\partial w_c}{\partial C} c_f \right)$$

give the income elasticities of the three worker groups, holding all task supplies of a given worker constant.

Holding task supplies constant, the production function exhibits constant returns to scale in labor from the three worker types. Therefore, using Euler's theorem, we know that

$$\frac{dy_d}{dN_f}|_{dc_j = dm_j = 0} + \frac{dy_s}{dN_f}|_{dc_j = dm_j = 0} = -\frac{dy_f}{dN_f}|_{dc_j = dm_j = 0}.$$

Plugging this in and writing in terms of elasticities yields:

$$\begin{split} \mathscr{R}_{ind}^{SR} = & \frac{N_d}{N_f} \left(T_d' - T_f' \right) y_d \times \gamma_{y_d,M} \Big|_{dc_j = dm_j = 0} m_f dN_f \\ & + \frac{N_d}{N_f} \left(T_d' - T_f' \right) y_d \times \gamma_{y_d,C} \Big|_{dc_j = dm_j = 0} c_f dN_f \\ & + \frac{N_s}{N_f} \left(T_s' - T_f' \right) y_s \times \gamma_{y_s,M} \Big|_{dc_j = dm_j = 0} m_f dN_f \\ & + \frac{N_s}{N_f} \left(T_s' - T_f' \right) y_s \times \gamma_{y_s,C} \Big|_{dc_j = dm_j = 0} c_f dN_f. \end{split}$$

where $\gamma_{y_d,M}\Big|_{dc_j=dm_j=0}$, $\gamma_{y_d,C}\Big|_{dc_j=dm_j=0}$, $\gamma_{y_s,M}\Big|_{dc_j=dm_j=0}$, and $\gamma_{y_s,C}\Big|_{dc_j=dm_j=0}$ are 'short run' elasticities that capture how the incomes of low- and high-skilled natives change in response to changes in task supplies under the assumption that past immigrants and low-skilled natives do not react. $\gamma_{y_d,M}\Big|_{dc_j=dm_j=0}$ and $\gamma_{y_d,C}\Big|_{dc_j=dm_j=0}$ can be written in terms of native task elasticities as

$$\gamma_{y_d,C}\Big|_{dc_j=dm_j=0} = \gamma_{w_c,C} \frac{w_c c_d}{y_d} + \gamma_{w_m,C} \frac{w_m m_d}{y_d}$$

and

$$\gamma_{y_d,M}\Big|_{dc_j=dm_j=0} = \gamma_{w_c,M} \frac{w_c c_d}{y_d} + \gamma_{w_m,M} \frac{w_m m_d}{y_d}.$$

Finally, the task price elasticities can be solved for via CES algebra as

$$\gamma_{y_s,M}\Big|_{dc_j=dm_j=0} = \gamma_{w_s,M} = \frac{\kappa_m}{\sigma},$$

$$\gamma_{y_s,C}\Big|_{dc_j=dm_j=0} = \gamma_{w_s,C} = \frac{\kappa_c}{\sigma},$$

$$\gamma_{w_c,C} = \left(\frac{1}{\sigma}\right)\kappa_c + \left(\frac{1}{\sigma_u} - \frac{1}{\sigma}\right)\kappa_c^u - \frac{1}{\sigma_u},$$

$$\gamma_{w_m,M} = \left(\frac{1}{\sigma}\right)\kappa_m + \left(\frac{1}{\sigma_u} - \frac{1}{\sigma}\right)\kappa_m^u - \frac{1}{\sigma_u},$$

$$\gamma_{w_c,M} = \left(\frac{1}{\sigma}\right)\kappa_m + \left(\frac{1}{\sigma_u} - \frac{1}{\sigma}\right)\kappa_m^u,$$

$$\gamma_{w_m,C} = \left(\frac{1}{\sigma}\right)\kappa_c + \left(\frac{1}{\sigma_u} - \frac{1}{\sigma}\right)\kappa_c^u,$$

and

where κ_j for $j \in \{c, m\}$ is the fraction of total income paid to factor j, ar

where κ_j for $j \in \{c, m\}$ is the fraction of total income paid to factor j, and κ_j^u is the fraction of total low-skilled income paid to factor j.

Sorting Effect: The fiscal effect of sorting is given by

$$\underbrace{T_f' N_f \left(w_m \frac{dm_f}{dN_f} + w_c \frac{dc_f}{dN_f} \right) dN_f}_{\text{Immigrant Sorting Effect}} + \underbrace{T_d' N_d \left(w_m \frac{dm_d}{dN_f} + w_c \frac{dc_d}{dN_f} \right) dN_f}_{\text{Native Sorting Effect}}.$$

The terms in brackets multiplied by dN_f give the change in income per past immigrant and native. Multiplying this with their amount and the marginal tax rate gives the implied tax effects.

We can rewrite this formula in terms of task supply elasticities η_j^c and η_j^m , for j = f, d as

$$\underbrace{T_f' N_f \left(w_m m_f \eta_f^m \frac{df}{dN_f} + w_c c_f \eta_f^c \frac{df}{dN_f} \right) dN_f}_{\text{Immigrant Sorting Effect}} + \underbrace{T_d' N_d \left(w_m m_d \eta_d^m \frac{df}{dN_f} + w_c c_d \eta_d^c \frac{df}{dN_f} \right) dN_f}_{\text{Native Sorting Effect}}.$$

Using $\frac{df}{dN_f} = \frac{N_d}{\left(N_d + N_f\right)^2}$, we can rewrite this term again solely in terms of shares and independent of population size:

$$d\mathscr{R}_{ind}^{SORT} = \underbrace{T_f' f(1-f) \left(w_m m_f \eta_f^m + w_c c_f \eta_f^c\right) dN_f}_{\text{Immigrant Sorting Effect}} + \underbrace{T_d' (1-f)^2 \left(w_m m_d \eta_d^m + w_c c_d \eta_d^c\right) dN_f}_{\text{Native Sorting Effect}}.$$

Secondary Price Effect: Collecting the remaining terms yields the indirect price effect:

$$d\mathcal{R}_{ind}^{PR} = T_s' N_s \left[\frac{\partial y_s}{\partial M} \left(\frac{dM}{dN_f} \right)_{ind} + \frac{\partial y_s}{\partial C} \left(\frac{dC}{dN_f} \right)_{ind} \right] + T_f' N_f \left[m_f \left(\frac{\partial w_m}{\partial M} \left(\frac{dM}{dN_f} \right)_{ind} + \frac{\partial w_m}{\partial C} \left(\frac{dC}{dN_f} \right)_{ind} \right) + c_f \left(\frac{\partial w_c}{\partial M} \left(\frac{dM}{dN_f} \right)_{ind} + \frac{\partial w_c}{\partial C} \left(\frac{dC}{dN_f} \right)_{ind} \right) \right] + T_d' N_d \left[m_d \left(\frac{\partial w_m}{\partial M} \left(\frac{dM}{dN_f} \right)_{ind} + \frac{\partial w_m}{\partial C} \left(\frac{dC}{dN_f} \right)_{ind} \right) + c_d \left(\frac{\partial w_c}{\partial M} \left(\frac{dM}{dN_f} \right)_{ind} + \frac{\partial w_c}{\partial C} \left(\frac{dC}{dN_f} \right)_{ind} \right) \right].$$

$$(22)$$

We can rearrange this to yield

$$d\mathcal{R}_{ind}^{PR} = \left(\frac{dM}{dN_f}\right)_{ind} \left[T_s' N_s \frac{\partial y_s}{\partial M} + T_f' N_f \frac{\partial y_f}{\partial M} + T_d' N_d \frac{\partial y_d}{\partial M}\right] + \left(\frac{dC}{dN_f}\right)_{ind} \left[\bar{T}_s' N_s \frac{\partial y_s}{\partial C} + T_f' N_f \frac{\partial y_f}{\partial C} + T_d' N_d \frac{\partial y_d}{\partial C}\right].$$
(23)

Using again Euler's theorem again, this yields:

$$\begin{split} \mathscr{R}_{ind}^{PR} = & \frac{N_d}{N_f} \left(T_d' - T_f' \right) y_d \times \gamma_{y_d, M} \Big|_{dc_j = dm_j = 0} \left(\frac{dM}{dN_f} \right)_{ind} dN_f \\ + & \frac{N_d}{N_f} \left(T_d' - T_f' \right) y_d \times \gamma_{y_d, C} \Big|_{dc_j = dm_j = 0} \left(\frac{dC}{dN_f} \right)_{ind} dN_f \\ + & \frac{N_s}{N_f} \left(T_s' - T_f' \right) y_s \times \gamma_{y_s, M} \Big|_{dc_j = dm_j = 0} \left(\frac{dM}{dN_f} \right)_{ind} dN_f \\ + & \frac{N_s}{N_f} \left(T_s' - T_f' \right) y_s \times \gamma_{y_s, C} \Big|_{dc_i = dm_j = 0} \left(\frac{dC}{dN_f} \right)_{ind} dN_f. \end{split}$$

B.6 Indirect Fiscal Effect with Decreasing Returns to Scale

The indirect fiscal effect associated with an immigrant of type i is

$$d\mathscr{R}_{ind}^{\mathrm{DRS}}\left(i\right) = h_{i}\omega_{i}\left[\tau_{p}\frac{\partial\pi}{\partial\mathscr{L}_{u}} + \int_{\mathscr{I}_{s}}T'\left(y_{i},i\right)\frac{\partial w_{s}}{\partial\mathscr{L}_{u}}h_{i}\omega_{i}m_{i}di + \int_{\mathscr{I}_{u}}T'\left(y_{i},i\right)\frac{\partial w_{u}}{\partial\mathscr{L}_{u}}h_{i}\omega_{i}m_{i}di\right].$$

We can rewrite this as

$$d\mathcal{R}_{ind}^{DRS}(i) = h_i \omega_i \left[\tau_p \frac{\partial \pi}{\partial \mathcal{L}_u} + \bar{T}_s' \mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} + \bar{T}_u' \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} \right].$$

where \bar{T}'_u and \bar{T}'_s are the income-weighted marginal tax rates of low and high skilled labor and τ_p is the tax on profits. First, we derive a relation between a change in profits and the change in labor income. Consider the effect of the inflow on profits:

$$\frac{\partial \pi}{\partial \mathcal{L}_u} = \left(\frac{\partial \pi}{\partial w_s} \frac{\partial w_s}{\partial \mathcal{L}_u} + \frac{\partial \pi}{\partial w_u} \frac{\partial w_u}{\partial \mathcal{L}_u}\right).$$

By Hotelling's lemma $\frac{\partial \pi}{\partial w_s} = -\mathcal{L}_s$ and same for low-skilled labor. Therefore we can write:

$$\frac{\partial \pi}{\partial \mathcal{L}_u} = -\left(\mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} + \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u}\right).$$

Denote by I aggregate labor income. Then we of course have

$$\frac{\partial I}{\partial \mathcal{L}_u} = \mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} + \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u}$$

and we can write

$$\frac{\partial \pi}{\partial \mathcal{L}_{u}} = -\frac{\partial I}{\partial \mathcal{L}_{u}}.$$

With constant returns to scale, we of course have that both sides are equal to zero. With decreasing returns, profits increase and labor income decreases. Aggregate native income (sum of profits and labor income) it not affected, however. We can therefore write the indirect fiscal effect as:

$$d\mathcal{R}_{ind}^{DRS}(i) = h_i \omega_i \left[-\tau_p \frac{\partial I}{\partial \mathcal{L}_u} + \bar{T}_s' \mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} + \bar{T}_u' \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} \right],$$

Let $\kappa_s = \frac{\mathscr{L}_s w_s}{\mathscr{L}_s w_s + \mathscr{L}_u w_u}$ be the high-skilled fraction of labor income. Adding and subtracting $(\bar{T}_s' \kappa_s + \bar{T}_u' \kappa_u) \frac{\partial I}{\partial \mathscr{L}_u}$:

$$d\mathcal{R}_{ind}^{DRS}(i) = h_i \omega_i \left[-\tau_p \frac{\partial I}{\partial \mathcal{L}_u} + \bar{T}_s' \left(\mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} - \kappa_s \frac{\partial I}{\partial \mathcal{L}_u} \right) + \bar{T}_u' \left(\mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} - \kappa_u \frac{\partial I}{\partial \mathcal{L}_u} \right) + \left(\bar{T}_s' \kappa_s + \bar{T}_u' \kappa_u \right) \frac{\partial I}{\partial \mathcal{L}_u} \right].$$

Rearranging the above equation yields

$$d\mathcal{R}_{ind}^{DRS}(i) = h_i \omega_i \left[\left(\bar{T}_I' - \tau_p \right) \frac{\partial I}{\partial \mathcal{L}_u} + \bar{T}_s' \left(\mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} - \kappa_s \frac{\partial I}{\partial \mathcal{L}_u} \right) + \bar{T}_u' \left(\mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} - \kappa_u \frac{\partial I}{\partial \mathcal{L}_u} \right) \right],$$

where $\bar{T}'_I = \bar{T}'_s \kappa_s + \bar{T}'_u \kappa_u$ is income weighted average income tax. Note that

$$\mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} + \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} = \kappa_u \frac{\partial I}{\partial \mathcal{L}_u} + \kappa_s \frac{\partial I}{\partial \mathcal{L}_u}$$

So we can plug in $\mathscr{L}_s \frac{\partial w_s}{\partial \mathscr{L}_u} - \kappa_s \frac{\partial I}{\partial \mathscr{L}_u} = -\left(\mathscr{L}_u \frac{\partial w_u}{\partial \mathscr{L}_u} - \kappa_u \frac{\partial I}{\partial \mathscr{L}_u}\right)$ which yields

$$d\mathcal{R}_{ind}^{\mathrm{DRS}}\left(i\right) = h_{i}\omega_{i} \left[\left(\bar{T}_{I}^{\prime} - \tau_{p} \right) \frac{\partial I}{\partial \mathcal{L}_{u}} + \left(\bar{T}_{u}^{\prime} - \bar{T}_{s}^{\prime} \right) \left(\mathcal{L}_{u} \frac{\partial w_{u}}{\partial \mathcal{L}_{u}} - \kappa_{u} \frac{\partial I}{\partial \mathcal{L}_{u}} \right) \right].$$

The term $\kappa_u \frac{\partial I}{\partial \mathcal{L}_u}$ is the effect of immigration on low-skilled income that occurs through the scale effect that arises from changing the total income but keeping share going to low-skilled workers constant. Therefore, we can think of the whole term $N_u h_u \frac{\partial w_u}{\partial \mathcal{L}_u} - \kappa_u \frac{\partial I}{\partial \mathcal{L}_u}$ as the total change in low-skilled income from immigration minus the scale effect. Therefore, this whole term captures the effect of immigration on wages, holding total labor income constant. Define $\frac{\partial \tilde{w}_u}{\partial \mathcal{L}_u} = N_u h_u \frac{\partial w_u}{\partial \mathcal{L}_u} - \kappa_u \frac{\partial I}{\partial \mathcal{L}_u}$ as the effect of immigration on wages, holding total labor income constant. Let's further assume that the production function is homogenous of degree λ , where $\lambda < 1$ if we have decreasing returns to scale. Hence, $F(t\mathcal{L}_u, t\mathcal{L}_s) = t^{\lambda} F(\mathcal{L}_u, \mathcal{L}_s)$. Taking derivatives w.r.t. to t and normalizing t = 1 yields:

$$\mathcal{L}_u w_u + \mathcal{L}_s w_s = \lambda F,$$

Now taking derivatives of both sides w.r.t. \mathcal{L}_u yields:

$$w_u + \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} + \mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u} = \lambda w_u.$$

Therefore (recall $\frac{\partial I}{\partial \mathcal{L}_u} = \mathcal{L}_u \frac{\partial w_u}{\partial \mathcal{L}_u} + \mathcal{L}_s \frac{\partial w_s}{\partial \mathcal{L}_u}$)

$$\frac{\partial I}{\partial \mathcal{L}_u} = (\lambda - 1) \, w_u.$$

Inserting this into the indirect fiscal effect yields

$$d\mathcal{R}_{ind}^{\mathrm{DRS}}\left(i\right) = h_{i}\omega_{i}w_{u}\left[\left(\tau_{p} - \bar{T}_{I}^{\prime}\right)\left(1 - \lambda\right) + \left(\bar{T}_{s}^{\prime} - \bar{T}_{u}^{\prime}\right)\left(\left|\gamma_{u,own} + \kappa_{u}\left(1 - \lambda\right)\right|\right)\right],$$

which yields

$$d\mathcal{R}_{ind}^{DRS}(i) = y_i \left[\left(\tau_p - \bar{T}_I' \right) (1 - \lambda) + \left(\bar{T}_s' - \bar{T}_u' \right) (|\tilde{\gamma}_{u.own}|) \right],$$

where $\tilde{\gamma}_{u,own} = \gamma_{u,own} + \kappa_u (1 - \lambda)$ is own-wage elasticity, holding total labor income constant. To solve for $\tilde{\gamma}_{u,own}$ as a function of the elasticity of substitution, note that as shown in

Appendix B.1, we can use the definition of the elasticity of substitution to write:

$$-\frac{1}{\sigma} = \gamma_{u,own} - \gamma_{s,cross}.$$
 (24)

From Euler's homogenous function theorem we know that

$$w_{u}\mathcal{L}_{u} + w_{s}\mathcal{L}_{s} = \lambda Y.$$

Taking derivatives with respect to \mathcal{L}_u and rearranging yields

$$\gamma_{s,cross} = -\gamma_{u,own} \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s} + (\lambda - 1) \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s}.$$

Plugging this into (24) yields

$$-\frac{1}{\sigma} = \gamma_{u,own} \underbrace{\left(1 + \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s}\right)}_{=\frac{\lambda Y}{w_s \mathcal{L}_s}} - \frac{w_u \mathcal{L}_u}{w_s \mathcal{L}_s} (\lambda - 1).$$

Solving for $\gamma_{u,own}$ yields

$$\gamma_{u,own} = (\lambda - 1) \frac{w_u \mathcal{L}_u}{\lambda Y} - \frac{1}{\sigma} \frac{w_s \mathcal{L}_s}{\lambda Y}.$$

Using $\frac{w_u \mathcal{L}_u}{\lambda Y} = \kappa_u$ and $\frac{w_s \mathcal{L}_s}{\lambda Y} = \kappa_s$ by Euler's homogeneous function theorem yields

$$\gamma_{u,own} = (\lambda - 1) \kappa_u - \frac{1}{\sigma} \kappa_s.$$

Therefore, we can write

$$\tilde{\gamma}_{u,own} = -\frac{1}{\sigma} \kappa_s.$$

B.7 Indirect Fiscal Effect with Inelastically Supplied Capital

We show the proof for the more general CES production function. Let production Y be given by

$$Y = (\theta_k K^{\rho} + \theta_l G (\mathcal{L}_u, \mathcal{L}_s)^{\rho})^{1/\rho}.$$

We begin by solving for the relationship of factor price elasticities when capital supply is elastic and capital supply is inelastic. For this, first consider the case when capital supply is perfectly elastic. In this case, the capital labor ratio is constant. In this case, we can write $K = CG(\mathcal{L}_u, \mathcal{L}_s)$ where C is the constant capital labor ratio. The production function can be written as

$$Y = \bar{A}G\left(\mathcal{L}_u, \mathcal{L}_s\right),\,$$

where \bar{A} is a constant.⁸³ The elasticities of wages with respect to low-skilled labor with perfectly elastic capital supply are given by

$$\gamma_{s,u}^{elast} = \frac{\partial \log \frac{\partial G}{\partial \mathcal{L}_s}}{\partial \log \mathcal{L}_u}$$

and

$$\gamma_{u,u}^{elast} = \frac{\partial \log \frac{\partial G}{\partial \mathcal{L}_u}}{\partial \log \mathcal{L}_u}.$$

⁸³Concretely, note that $Y = (\theta_k (CG)^{\rho} + \theta_l G^{\rho})^{1/\rho}$ and hence $Y = (\theta_k C^{\rho} + \theta_l)^{\frac{1}{\rho}} G$. Hence, the constant is given by $\bar{A} = (\theta_k C^{\rho} + \theta_l)^{\frac{1}{\rho}}$.

Next, consider the case in which capital supply is perfectly inelastic. Let $\kappa_L = \frac{w_u \mathcal{L}_u + w_s \mathcal{L}_s}{Y}$ be the share of factor payments that go to labor, let $\kappa_K = 1 - \kappa_L$, and let $\kappa_u = \frac{w_u \mathcal{L}_u}{w_u \mathcal{L}_u + w_s \mathcal{L}_s}$ be the share of wage payments that go to low-skilled labor.

Let r give the price of capital. Standard CES algebra yields the capital price elasticity

$$\gamma_{r,u} = \frac{\kappa_L}{\sigma} \kappa_u.$$

Further, note that log wages for each skill group are given by

$$\log w_u = \log \frac{\partial Y}{\partial G} + \log \frac{\partial G}{\partial \mathcal{L}_u}$$

and

$$\log w_s = \log \frac{\partial Y}{\partial G} + \log \frac{\partial G}{\partial \mathcal{L}_s}.$$

Taking derivatives of these log wage functions with respect to $\log \mathcal{L}_u$ yields

$$\gamma_{s,u} = \underbrace{\frac{\partial \log \frac{\partial Y}{\partial G}}{\partial \log \mathcal{L}_u}}_{= -\frac{\kappa_L}{\kappa_u}} + \underbrace{\frac{\partial \log \frac{\partial G}{\partial \mathcal{L}_s}}{\partial \log \mathcal{L}_u}}_{\gamma_{s,u}^{elast}}$$

and

$$\gamma_{u,u} = \underbrace{\frac{\partial \log \frac{\partial Y}{\partial G}}{\partial \log \mathcal{L}_u}}_{=-\frac{\kappa_K}{\kappa_u}} + \underbrace{\frac{\partial \log \frac{\partial G}{\partial \mathcal{L}_u}}{\partial \log \mathcal{L}_u}}_{\gamma_u^{elast}},$$

which give the relationship between own wage elasticity with elastically supplied and inelastically supplied capital.

Now, consider the indirect fiscal effect with inelastically supply supplied capital:

$$d\mathcal{R}_{ind}\left(i\right) = h_{i}\omega_{i} \left[\tau_{k}K\frac{\partial r}{\partial\mathcal{L}_{u}} + \bar{T}_{s}'\mathcal{L}_{s}\frac{\partial w_{s}}{\partial\mathcal{L}_{u}} + \bar{T}_{u}'\mathcal{L}_{u}\frac{\partial w_{u}}{\partial\mathcal{L}_{u}}\right].$$

We can rewrite this as

$$d\mathcal{R}_{ind}(i) = h_i \omega_i \left[\tau_k \frac{rK}{\mathcal{L}_u} \gamma_{r,u} + \bar{T}_s' \frac{\mathcal{L}_s w_s}{\mathcal{L}_u} \gamma_{s,u} + \bar{T}_u' w_u \gamma_{u,u} \right].$$

Plugging in the factor price elasticities from above yields

$$d\mathcal{R}_{ind}(i) = h_i \omega_i \left[\frac{\kappa_u}{\mathcal{L}_u \sigma} \left(\tau_k r K \frac{w_u \mathcal{L}_u + w_s \mathcal{L}_s}{Y} - \bar{T}_s' \mathcal{L}_s w_s \frac{rK}{Y} - \bar{T}_u' \mathcal{L}_u w_u \frac{rK}{Y} \right) + \bar{T}_s' \frac{\mathcal{L}_s w_s}{\mathcal{L}_u} \gamma_{s,u}^{elast} + \bar{T}_u' w_u \gamma_{u,u}^{elast} \right].$$

Factorizing $\kappa_K = \frac{rK}{Y}$ in the first line yields

$$d\mathcal{R}_{ind}(i) = h_i \omega_i \left[\kappa_K \frac{\kappa_u}{\mathcal{L}_u \sigma} \left(\tau_k (w_u \mathcal{L}_u + w_s \mathcal{L}_s) - \bar{T}_s' \mathcal{L}_s w_s - \bar{T}_u' \mathcal{L}_u w_u \right) + \bar{T}_s' \frac{\mathcal{L}_s w_s}{\mathcal{L}_u} \gamma_{s,u}^{elast} + \bar{T}_u' w_u \gamma_{u,u}^{elast} \right].$$

Letting $\bar{T}'_I = \frac{\bar{T}'_s \mathcal{L}_s w_s + \bar{T}'_u \mathcal{L}_u w_u}{w_u \mathcal{L}_u + w_s \mathcal{L}_s}$, we can rewrite this as:

$$d\mathcal{R}_{ind}(i) = h_i \omega_i \left[(w_u \mathcal{L}_u + w_s \mathcal{L}_s) \kappa_K \frac{\kappa_u}{\mathcal{L}_u \sigma} \left(\tau_k - \bar{T}_I' \right) + \bar{T}_s' \frac{\mathcal{L}_s w_s}{\mathcal{L}_u} \gamma_{s,u}^{elast} + \bar{T}_u' w_u \gamma_{u,u}^{elast}, \right]$$

which can be simplified to

$$d\mathcal{R}_{ind}\left(i\right) = h_{i}\omega_{i} \left[w_{u} \frac{\kappa_{K}}{\sigma} \left(\tau_{k} - \bar{T}_{I}' \right) + \bar{T}_{s}' \frac{\mathcal{L}_{s} w_{s}}{\mathcal{L}_{u}} \gamma_{s,u}^{elast} + \bar{T}_{u}' w_{u} \gamma_{u,u}^{elast}. \right]$$

Further, we know that F is constant returns to scale, which implies that $w_u \gamma_{u,u}^{elast} = -\frac{\mathscr{L}_s w_s}{\mathscr{L}_u} \gamma_{s,u}^{elast}$ (recall Lemma 2). We can therefore write

$$d\mathcal{R}_{ind}\left(i\right) = h_{i}\omega_{i} \left[w_{u} \frac{\kappa_{K}}{\sigma} \left(\tau_{k} - \bar{T}_{I}' \right) + \left(\bar{T}_{s}' - \bar{T}_{u}' \right) w_{u} | \gamma_{u,u}^{elast} | \right].$$

Rearranging this equation yields

$$d\mathcal{R}_{ind}\left(i\right) = y_i \left[\left(\bar{T}_s' - \bar{T}_u'\right) \left| \gamma_{u,own}^{elast} \right| + \frac{\kappa_K}{\sigma} \left(\tau_k - \bar{T}_I'\right) \right]. \tag{25}$$

If the production function is Cobb-Douglas in capital and the labor aggregate, then $\frac{\kappa_K}{\sigma} = \alpha$.

C Empirical Appendix

C.1 Data Cleaning and Sample Selection in the ACS

We use data from the 2017 ACS. We limit the sample to individuals between ages 18 and 65 who do not live in group quarters. We limit our sample to household heads and their spouses, as tax filling status is less clear for other individuals. This leaves us with a sample of over 1.2 million individuals.

When calculating taxes, we account for an individual's wage income and business income as sources of taxable income. All income weighted averages are weighted by wage incomes and sample weights. When calculating the income-weighted pass-through tax rate in Section A.5, we weight by business income.

C.2 Calculation of Marginal Phase-Out Rates and TANF and SNAP

We begin by calculating total monthly SNAP benefits and TANF benefits for each household in the SIPP. To deal with underreporting, we estimate these estimated monthly benefits such that the total benefits received match national aggregates reported from the Bureau of Economic Analysis. Next, we divide households by household size and estimate monthly TANF and SNAP benefits as a linear spline in household income. We estimate a separate spline for each household size. Next, using these function of benefits as a function of income, we can calculate the marginal average monthly benefits as a function of monthly income and household size. We aggregate these monthly estimates to yearly estimates by taking the income-weighted average across months for each household in the SIPP.

C.3 Calculation of Marginal Replacement Rates of Social Security Benefits

An individual's social security benefits are calculated as a function of their average indexed monthly earnings (AIME). If the current year's income is one of the 35 highest earning years, a \$1 increase in current year income will increase an individual's AIME by \$1/35. If the current year's income is not one of the 35 highest earning years, a marginal increase in current year income will have no effect on social security benefits. Further, if current year's income is above the maximum taxable earnings threshold, an increase in current income has no effect on social security benefits.

We assume an individual receives social security from age 66 until their death.

Let $MRR(AIME_i)$ denote the marginal increase in yearly social security benefits as a function of an individual's AIME and let T_i represent an individual's life expectancy. The discounted marginal replacement rate associate with current earnings of an individual of age age_i is given by:

$$DRR_{i} = MRR(AIME_{i}) \frac{1}{35} \left(\frac{1+g}{1+r}\right)^{65-age_{i}} \sum_{t=66}^{T_{i}} \left(\frac{1}{1+r}\right)^{t-65}$$
(26)

if current year income is one of the individual's 35 highest earning years and income is below the maximum taxable earnings threshold, and 0 otherwise, where g is the aggregate growth rate and r is the interest rate. This gives the increase in yearly social security benefits associated with a \$1 increase in AIME. An increase in the current year's income increase the average career income by 1/35, which in turn increases yearly future social security benefits from the agents retirement until death.

We estimate an individual's AIME and 35th highest year of earning as a function of current income and household characteristics using data from the NLSY79. The NLSY79 is a nationally representative panel dataset which provides data on respondents from 1979 until 2016. There are a few issues with missing data that we need to resolve. First, starting in 1994,

Income	Females		Males		
Quintile	Married	Single		Married	Single
1	0.12	0.19		0.07	0.20
2	0.12	0.31		0.05	0.25
3	0.12	0.23		0.05	0.20
4	0.12	0.16		0.04	0.16
5	0.11	0.09		0.02	0.10

Table 9: Estimates of extensive margin labor supply elasticities from Bargain, Orsini, and Peichl (2014) by income quintile, gender, and marital status.

individuals are only interviewed in even numbered years. We therefore assume that data in odd numbered years post 1994 is the same as in the previous year. Further, in 2016, the last year from which data are available, respondents are between age 53 and 60. We therefore do not have income information for the last few years of individual's working lives. We therefore assume that income for the remainder of the working life is equal to a respondent's last observed income.

After dealing with these data issues, we can calculate an individual's AIME as the average of their 35 highest income years, adjusted for inflation, and an individual's 35th highest income year. We calculate the average of these two statistics conditional the following characteristics:

- 1. An individual's education high school dropout, high school graduate, some college, or college graduate
- 2. Whether or not an agent is married
- 3. 5-year age bins
- 4. Whether or not the agent has children living in their household
- 5. Quintiles of the income distribution, conditional on working and conditional on the above characteristics.

For individuals in the ACS, we impute AIME and 35th highest earning year as the average of these two statistics conditional on the characteristics above.

C.4 Intensive and Extensive Labor Supply Elasticities from Bargain, Orsini, and Peichl (2014)

Tables 9 and 10 display the extensive and intensive labor supply elasticities estimated in Bargain, Orsini, and Peichl (2014). The first column displays the income quintile. The next four columns display the labor supply elasticities for married females, single females, married males, and single males, respectively.

Income	Females		Males		
Quintile	Married	Single		Married	Single
1	0.02	0.03		0.02	0.01
2	0.02	0.03		0.03	0.02
3	0.02	0.04		0.03	0.02
4	0.02	0.05		0.03	0.02
5	0.04	0.06		0.05	0.04

Table 10: Estimates of intensive margin labor supply elasticities from Bargain, Orsini, and Peichl (2014) by income quintile, gender, and marital status.

C.5 Quantifying the Fiscal Effect in Peri and Sparber (2009)

We now calculate the indirect fiscal benefits and its decomposition as expressed in equation 21. In order to evaluate this equation, we need estimates of the following:

- 1. (w_m, w_c, w_s) the task prices of manual, communication, and cognitive tasks.
- 2. (σ, σ_u) the elasticities of substitution between high-skilled and low-skilled workers, and between manual tasks and cognitive tasks.
- 3. $(\eta_c^f, \eta_f^m, \eta_d^c, \eta_d^m)$ the elasticities of task intensities with respect to immigrant inflows.
- 4. (N_f, N_d, N_s) the number of low-skilled immigrants, low-skilled natives and high-skilled workers.
- 5. (c_f, c_d, m_f, m_d) the task intensities of low-skilled natives and immigrants
- 6. $(\bar{T}'_f, \bar{T}'_d, \bar{T}'_s)$ marginal tax rates faced by low-skilled immigrants, low-skilled natives, and high-skilled workers.

We take estimates of items (1) - (3) directly from Peri and Sparber (2009). Specifically, Peri and Sparber (2009) estimate the state level task prices of manual and cognitive tasks, w_m and w_c , using variation in task supplies and wages across occupations. We take the national average of these task prices for our measures of w_m and w_c . Peri and Sparber (2009) estimate the elasticity of substitution between manual and communication tasks, σ_u , using state level variation in immigrant inflows. We set $\sigma_u = 1$ as the preferred estimates from Peri and Sparber (2009) and set the elasticity of substitution between low- and high-skilled workers as $\sigma = 1.75$, based on the calibration in Peri and Sparber (2009). Peri and Sparber (2009) also use across-state immigrant variation to estimate the elasticities of task supplies with respect to the immigrant share of low-skilled workers. They find that natives respond to low-skilled immigrant inflows by increasing their communication task supply but do not change their manual task supply, and that immigrants do not change their task supplies in response to immigrant inflows. We therefore set $\eta_f^c = \eta_f^m = \eta_d^m = 0$ and take $\eta_d^c = 0.33$ from their estimates.

Object	Value	Description	Source
Task Prices			
w_m	773	Manual task wage	PS inflated to 2017
w_c	820	Communication task wage	PS inflated to 2017
w_s	69,311	Skilled income	ACS
Production Parameters			
σ	1.75	Elasticity of substitution, skilled and unskilled workers	PS
σ_u	1	Elasticity of substitution, manual and communication tasks	PS
Task Supply Elasticities			
η_c^d	.33	Elasticity of native communication task supply with respect to immigrants	PS
$\eta_m^d, \eta_m^f, \eta_c^f$	0	Other task supply elasticities	PS
Population Shares			
$\frac{N_f}{N}$	0.069	Low-skilled immigrants as fraction of population	ACS
$\frac{\dot{N}_d}{N}$	0.318	Low-skilled natives as fraction of population	ACS
$rac{N_f}{N_d} \ rac{N_s}{N}$	0.613	Hig- skilled workers as fraction of population	ACS
Task Supplies			
c_f	12.47	Communication task supply of low-skilled immigrants	ONET and ACS
c_d	19.15	Communication task supply of low-skilled natives	ONET and ACS
m_f	27.71	Manual task supply of low-skilled immigrants	ONET and ACS
m_d	29.18	Manual task supply of low-skilled natives	ONET and ACS
Marginal Tax Rates			
$ar{T}'_f \ ar{T}'_d \ ar{T}'_s \$	0.299	Marginal tax rate of low-skilled immigrants	Tax quantification
$ec{T}_d'$	0.293	Marginal tax rate of low-skilled natives	Tax quantification
$ar{T}_s'$	0.369	Marginal tax rate of high-skilled workers	Tax quantification

Table 11: Summary of data sources and calibrated values. "PS" refers to estimates taken from Peri and Sparber (2009).

To measure (4)-(6) we follow Peri and Sparber (2009) closely using data from the 2017 ACS downloaded from IPUMS (Ruggles, Alexander, Genadek, Goeken, Schroeder, and Sobek, 2010) and data on task composition of occupations from ONET. We define low-skilled workers as workers with a high school degree or less. We can therefore calculate N_f , N_d and N_s directly from the 2017 ACS as the number of low-skilled immigrants, low-skilled natives and high-skilled workers. To estimate the task supplies, we proceed in two steps. The ONET dataset measures the task requirement for each census occupation code. We use the procedure described in Peri and Sparber (2009) to assign a manual and communication intensity to each occupation. Then, for each worker in the ACS, we calculate the manual and communication task requirements associated with the worker's occupation. Let \tilde{c}_j and \tilde{m}_j represent the average communication and manual task intensity of workers of type j.

Recall that the task supplies are defined as the task intensities multiplied by labor supply: $c_j = h_j \tilde{c_j}$ and $m_j = h_j \tilde{m_j}$. Note that the worker's budget constraint can be rewritten as

$$y_j = h_j \left(\tilde{c}_j w_c + \tilde{m}_j w_m \right),\,$$

where task prices, w_c and w_m , are known values from Peri and Sparber (2009), and the average income of workers of type j, y_j , can be estimated directly from the ACS. We can therefore use this equation to solve for h_j for low-skilled immigrants and natives and therefore for all four task supplies, c_f , c_d , m_f , and m_d .

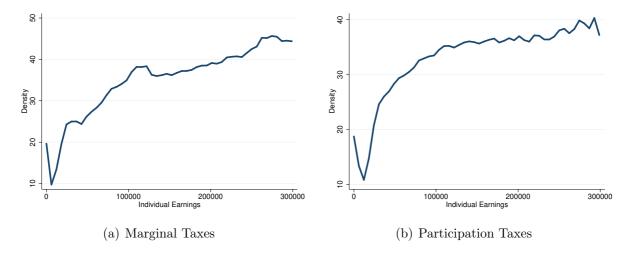


Figure 3: Total marginal and participation tax rates by individual earnings. Panel (a) gives the marginal effective tax rates as the sum of marginal races from income taxes, the social security system, and transfer programs. Panel (b) reports the total participation tax rates implied by income taxes, the social security system, and transfer programs.

D Further Quantitative Results

D.1 Total Marginal and Participation Tax Rates

Figure 3 shows the total marginal and participation tax rates by individual earnings as the sum of the effective tax rates arising from income taxes, social security, and transfer payments. Panel (a) gives the marginal effective tax rates as the sum of marignal races from income taxes, the social security system, and transfer programs. Panel (b) reports the total participation tax rates implied by income taxes, the social security system, and transfer programs.

D.2 Indirect Fiscal Effects in Canonical Model with Real Interest Rate=2

In Section 3 we chose a real interest rate of 1%. In Table 12 we replicated our baseline results under the assumption of a real interest rate of 2%. The table shows the indirect fiscal effects of the average low-skilled immigrant. The effects range from \$682 to \$1,309.

D.3 Indirect Fiscal Effects in Canonical Model with Alternative Skill Definitions

In Section 3, we followed Borjas (2003), Peri and Sparber (2009) and Ottaviano and Peri (2012) and defined low-skilled workers as those with no college experience and defined high-skilled workers as individuals with some college and college graduates. An alternative way to delineate skills is to divide individuals with some college between low-skilled and high-skilled workers, as in Card (2009) or Katz and Murphy (1992).

	Elasticity of Substitution		
	1.5	2.0	2.5
I. No Labor Supply Responses	1,141	856	685
II. Intensive Only			
Common Elasticity	1,244	977	804
By Gender and Marital Status	1,145	860	689
By Income, Gender and Marital Status	1,188	896	719
III. Extensive Only			
Common Elasticity	1,233	959	784
By Gender and Marital Status	1,181	903	730
By Income, Gender and Marital Status	1,110	845	682
IV. Intensive and Extensive			
Common Elasticity	1,309	1,055	884
By Gender and Marital Status	1,185	907	734
By Income, Gender and Marital Status	1,155	883	715

Table 12: Indirect Fiscal Effects with intensive and extensive margin labor supply responses with real interest rate of 2%.

In this section we replicate our baseline results from Section 5, except we define skill groups as in Card (2009), by dividing individuals with some college evenly between the groups. Overall the indirect fiscal effects here are slightly smaller than our baseline result. This makes sense, the skill definitions we use in this section imply a smaller high-skilled share of income and therefore a smaller own-wage elasticity for low-skilled workers, holding the parameter σ constant. However, the results are still in the same ballpark as those presented in Section 5.

D.4 Indirect Fiscal Effects in Canonical Model with for High School Dropouts and High School Graduates

Tables 14 and 15 show the indirect fiscal effects for the average high school dropout immigrant and the average high school graduate immigrant.

	Elasticity of Substitution		
	1.5	2.0	2.5
No Labor Supply Responses	1,221	916	733
II. Intensive Only			
Common Elasticity	1,332	1,046	861
By Gender and Marital Status	1,222	919	736
By Income, Gender and Marial Status	1,266	955	766
Extensive Only			
Common Elasticity	1,295	1,008	824
By Gender and Marital Status	1,245	952	770
By Income, Gender and Marital Status	1,181	898	725
Intensive and Extensive			
Common Elasticity	1,381	1,113	932
By Gender and Marital Status	1,246	954	773
By Income, Gender and Marital Status	1,223	935	757

Table 13: Indirect Fiscal Effects with intensive and extensive margin labor supply responses with alternative skill definition.

	Elasticity of Substitution		
	1.5	2.0	2.5
I. No Labor Supply Responses	1,108	831	665
II. Intensive Only			
Common Elasticity	1,208	949	781
By Gender and Marital Status	1,112	835	669
By Income, Gender and Marital Status	1,149	866	695
III. Extensive Only			
Common Elasticity	1,177	916	749
By Gender and Marital Status	1,139	870	704
By Income, Gender and Marital Status	1,082	823	665
IV. Intensive and Extensive			
Common Elasticity	1,254	1,011	847
By Gender and Marital Status	1,142	874	708
By Income, Gender and Marital Status	1,120	857	694

Table 14: Indirect Fiscal Effects for high school dropouts with intensive and extensive margin labor supply responses. See description from Table 3.

	Elasticity of Substitution		
	1.5	2.0	2.5
I. No Labor Supply Responses	1,433	1,075	860
II. Intensive Only			
Common Elasticity	1,563	$1,\!227$	1,010
By Gender and Marital Status	1,438	1,080	865
By Income, Gender and Marital Status	1,485	1,120	899
III. Extensive Only			
Common Elasticity	1,523	1,184	969
By Gender and Marital Status	1,473	$1,\!125$	911
By Income, Gender and Marital Status	1,399	1,065	859
IV. Intensive and Extensive			
Common Elasticity	1,622	1,308	1,095
By Gender and Marital Status	1,477	1,130	915
By Income, Gender and Marital Status	1,449	1,108	897

Table 15: Indirect Fiscal Effects for high school graduates with intensive and extensive margin labor supply responses. See description from Table 3.