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## Healthy Climate, Healthy Bodies: Optimal Fuel Taxation and Physical Activity

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## Healthy Climate, Healthy Bodies: Optimal Fuel Taxation and Physical Activity

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# Healthy Climate, Healthy Bodies: Optimal Fuel Taxation and Physical Activity

## Abstract

Transport has significant externalities including carbon emissions and air pollution. Public health research has identified additional social gains from active travel, due to health benefits of physical exercise. Per mile, these benefits greatly exceed the external costs from car use. We introduce active travel into an optimal fuel taxation model and analytically characterise the optimal second-best fuel tax. We find that accounting for active travel benefits increases the optimal fuel tax by 49% in the US and 36% in the UK. Fuel taxes should be implemented jointly with other policies aimed at increasing the uptake of active travel.

JEL-Codes: H230, I120, Q530, Q540, Q580, R410, R480, Z280.

Keywords: transport externalities, congestion, active travel, fuel, health behaviour, optimal taxation.

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# 1 Introduction

Transport policies need to balance the economic gains from vehicle use with a large number of significant externalities, including air pollution, accidents, congestion, and climate change. For example, in the US and UK, the transport sector is now the largest contributor of greenhouse-gas emissions (Hockstad and Hanel, 2018; Gabbatiss, 2018). Increased active travel such as cycling and walking – even to the nearest public transport stop – can reduce these externalities, especially in urban areas. In addition, the physical exercise involved in active travel is beneficial for health, especially given high rates of inactivity and obesity in many populations. Previous scenario-based modelling in public health has indicated that these health benefits exceed the benefits from abating emissions and air pollution of private vehicles (Woodcock et al., 2009; De Hartog et al., 2010). For example, Woodcock et al. (2009) find that an increased active travel scenario would avoid 530 premature deaths per million population in London annually, while a lower-carbon-emission motor vehicles scenario would only save 17 through lower air pollution exposure.

Surprisingly, economists have yet to examine the significance of the health benefits from active travel for optimal regulation of urban transport. Many citizens are not aware of the full health benefits exercise provides (Fredriksson et al., 2018). For instance, the effectiveness of simple interventions such as reminders to go to the gym (Calzolari and Nardotto, 2017), initial payments (Charness and Gneezy, 2009), and evidence of overspending on gym contracts (DellaVigna and Malmendier, 2006) point to self-control problems and an underappreciation of the health benefits of exercise, especially before they materialise. Therefore, the health benefits of active travel make passenger transport an unexamined case of a “behavioural-environmental second-best problem” (Shogren and Taylor, 2008). It is, however, yet to be determined whether instruments such as fuel taxes are appropriate to reap these health benefits in addition to mitigating the externalities of car use.

In this article, we examine a novel economic effect by adding an active travel mode to a model of transport externalities from car use. Households

respond to higher fuel taxes by buying more fuel-efficient cars and reducing car travel, and additionally shift to alternative models of travel that involve exercise, such as walking or cycling. However, they do not fully internalise that they get healthier by adopting such active modes of travel. We confirm that, on a per mile basis, the monetary value of the health benefits from active travel exceeds the social costs of unregulated externalities of carbon emissions, air pollution, congestion, and accidents by two orders of magnitude. Any first-best policy would thus involve a large subsidy to promote active travel. In the absence of such subsidies, we derive the optimal second-best fuel tax that corrects for the externalities and the unrealised health benefits. We examine the difference for the tax rule and quantify the appropriate tax rate both including, and excluding health benefits from active travel.

We find that the optimal tax increases by 49% in the US and 36% in the UK when health benefits from physical exercise are included. The second-best optimal fuel tax for the US is \$10.13/gal, and \$6.81/gal without physical inactivity costs, while the current rate in the US is \$0.55/gal (API, 2020). The optimal fuel tax for the UK is \$4.54/gal, which is somewhat higher than the current rate of \$4.06/gal (RAC, 2020). Without physical activity costs, the optimal second-best tax would be \$3.35/gal.

Previous work established that the external costs of transport are not fully reflected in fuel price; fuel taxes are inefficiently low in most European countries (Santos, 2017) and the US (Bento et al., 2009).<sup>1</sup> Accounting for the physical health benefits from active travel thus further increases the gap between actual and optimal fuel taxes. Our sensitivity analysis shows that the optimal second-best tax varies significantly within the range of realistic parameter values, from \$6/gal to \$13/gal for the US, and from \$3.75/gal to \$7/gal for the UK. Hence, neither the UK nor the US current fuel taxes likely exceed the optimal rate.

On a per mile basis, physical inactivity represents the largest social cost of motorised private transport. Nevertheless, the “active travel adjustment” of the optimal fuel tax is comparatively small. This is explained by the fact that

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<sup>1</sup>An exception is Parry and Small (2005), who claim that UK fuel taxes are too high.

a fuel tax is a fairly inefficient instrument to address these high costs because the uptake of active travel is not highly responsive to fuel price. A greater responsiveness of active travel to fuel taxation would increase the optimal tax adjustment. The broader insight from our article is therefore that, when it is acknowledged that individuals' health decisions are not always welfare-maximising, pricing car use should be complemented with infrastructure re-development. This mirrors results from urban planning and transportation research (Banister, 2008; Buehler et al., 2017).

This manuscript builds on three distinct strands of literature: First, a large body of literature studies optimal levels of fuel taxes, and which externalities should be addressed by them (van Essen et al., 2019). In addition to generating government revenue, fuel taxes are typically used for the purpose of reducing most forms of non-priced costs of transport, e.g. the externalities of carbon dioxide and particulate matter, or reducing congestion by raising the cost of driving. Parry and Small (2005) derive the optimal gasoline taxes for the US and Britain, accounting for congestion, accidents, carbon emissions and air pollution, and Antón-Sarabia and Hernández-Trillo (2014) apply this framework to Mexico. Sterner (2012) compares the optimality of fuel taxes in Europe and US, concluding that fuel taxes vary considerably between countries. In 2017, the fuel tax raised on a gallon of unleaded gasoline in the US was \$0.55, and \$3.75 in the UK (API, 2020; RAC, 2020).<sup>2</sup> Yet, the optimal fuel tax literature has so far not considered the health benefits from active travel.

Second, the field of public health, starting with Woodcock et al. (2009), has identified high social benefits from active travel over and above the benefits from abating emissions and air pollution of private vehicles (De Hartog et al., 2010; Wolking et al., 2018). To the majority of the population, increasing physical activity outweighs the negative impacts of increased exposure to air pollution (Tainio et al., 2016). This is due to the overwhelmingly sedentary lifestyles that people in both the UK and US lead, making physical inactivity

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<sup>2</sup>For the UK, this is the sum of the fuel and the excise taxes. For the US this is the average over the different federal and state taxes.

a leading risk factor for 6 of the 10 largest causes of death worldwide (WHO, 2018). Most UK adults do not exercise regularly (37% never, 16% less than once a week, 57% admit they never do activity strenuous enough to be out of breath, Commission (2018)). This leads to significant costs including higher rates of disease incidence, lower quality of life, loss of income, excess healthcare costs, and productivity losses in the workplace. We build on the valuation methods in public health to quantify the welfare cost of travel that is inactive.

Third, behavioural public economics research has elaborated on the important role of “internalities” in various domains of public policy (Allcott and Sunstein, 2015). An “internality” occurs when an individual imposes a significant cost on herself due to behavioural failures. As these private costs are imposed only or mainly on oneself – which is true for lack of physical activity –, they fall outside the definition of an externality. Nonetheless, governments regulate internalities, in cases where scientific evidence substantiates it. Internality taxes have been applied to the market for smoking (Gruber and Kőszegi, 2004), gym memberships and exercise (in the form of subsidies, DellaVigna and Malmendier, 2006), sugary drinks (Allcott et al., 2019a; Allcott et al., 2019b) and the energy and automobile market (Allcott and Wozny, 2014; Allcott and Sunstein, 2015), where they also interact with environmental externalities. In the latter case, the interaction leads to a behavioural-environmental second-best problem (Shogren and Taylor, 2008). Chetty (2015), Bhargava and Loewenstein (2015), Allcott and Sunstein (2015), and Allcott et al. (2019b) all provide more extensive discussions of why regulating internalities is desirable, arguing that the complexity of choices people face, and large internal costs in e.g. health and energy efficiency, warrant the greater use of behavioural economics in regulation. Sin taxes, surcharges on prices of goods of which people consume too much because of internalities, have been modelled as either simple extensions of a Pigouvian tax (O’Donoghue and Rabin, 2006), or as complex interactions between taxes and individuals’ heuristics and decisions, to achieve an optimal outcome in second-best settings (Allcott et al., 2014).

However, this body of literature has not considered the internality of



physical inactivity in urban transport. Walking, cycling, and switching to public transport are considered ways in which people can achieve “appropriate” levels of physical activity as prescribed by public health guidelines (Gibson-Moore, 2019; OSG, 2015). Physical activity has been referred to as a “miracle cure” (Davies et al., 2019) in the UK Chief Medical Officers’ 2019 Physical Activity Guidelines. Meeting the minimum recommendations of 150 minutes of moderate-intensity physical activity per week can reduce the risk of cognitive impairment and dementia, depression, hypertension, type 2 diabetes and cardiovascular disease, as well as increase bone mineral density (Davies et al., 2019). People generally under-value the contribution of physical exercise to their long-term health (Zamir and Teichman, 2014). There are two behavioural biases behind this under-valuation, which lead to insufficient levels of exercise and further health impacts: imperfect information and insufficient self-control (Allcott et al., 2019b). This reinforces the case for building active travel into commuting routines.

Our contribution to the literature is threefold: First, we introduce a physical activity-related health externality into an established framework of transport decisions (Parry and Small, 2005), and use this behavioural-environmental framework to provide an analytical solution for the optimal second-best fuel tax. Second, we provide an updated quantification of the external costs of travel provided by Parry and Small (2005), considering recent research and global climate policy goals, and complement this with a quantification of the health benefits of active travel. For example, updating the carbon price estimates increases the contribution of fuel pollution to the optimal fuel tax by an order of magnitude. Third, in terms of policy implications, we contribute to evaluating the potential use of a fuel tax as opposed to other policies. We confirm that raising the propensity of consumers to switch to active travel modes can greatly impact the appropriate fuel tax: the demand for vehicle miles travelled (VMT) is so inelastic that increasing appropriate elasticities to their upper bound found in the literature raises the fuel tax by up to 62% for the UK and 155% for the US.<sup>3</sup>

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<sup>3</sup>It may be argued that, especially in the US case, realising such an increase is politically

Fuel taxes have some distinct advantages over more specific transport policies such as congestion charges or emission zones. First, they can be implemented with relatively small administrative costs compared to other policies, since most countries already have fuel taxes in place and levels would only have to be adjusted accordingly. Second, fuel taxes have a proven track record of reducing carbon emissions (Bento et al., 2009; Bretschger and Grieg, 2020; OECD, 2019; Sterner, 2012). Third, they generate government revenue, which could be used either for green spending, for instance on low-carbon transport infrastructure, or for compensating households that are especially affected by the tax (Bento et al., 2009). Both measures could make the public more supportive of fuel taxation (Klenert et al., 2018).

The remainder of the paper is organised as follows. Section 2 describes the model, and our analytical result for the optimal fuel tax. Section 3 explains our choice of parametrisation. Section 4 presents the quantitative results and Section 5 discusses the policy implications. Section 6 concludes.

## 2 Analytical Framework

### 2.1 Model

To explore how the fuel tax might be optimally adjusted to account for health benefits of public transport, we extend Parry and Small (2005) to account for active travel decisions and associated health benefits. We take advantage of the fact that in certain settings, internalities can be treated as extensions of externalities (O’Donoghue and Rabin, 2006).

We consider a representative agent with the utility function

$$U = u(\psi(C, M, T^{in}, T^{ac}, G), N) - \varphi(P) - \delta(A) + \xi(Q), \quad (1)$$

where  $C$  is the quantity of numeraire consumption,  $M$  total distance travelled,

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unrealistic in the foreseeable future. Still, our result indicates that current fuel tax rates are further below their preferred levels than previously thought, which, as we discuss in Subsection 4.2, implies fuel tax increases have greater benefits.

$T^{in}$  and  $T^{ac}$  is total time travelled using active and inactive modes respectively,  $G$  exogenous government spending, and  $N$  leisure, with  $U_C, U_M, U_G, U_N > 0$ , and  $U_{T^{in}}$  and  $U_{T^{ac}} < 0$ , with the subscript denoting a partial derivative. The level of pollution is denoted by  $P$ ,  $A$  captures accidents, and health is denoted by  $Q$ . As Parry and Small (2005), we assume  $u(\cdot)$  and  $\psi(\cdot)$  are quasi-concave, and  $\varphi(\cdot)$  and  $\delta(\cdot)$  are convex. The functions  $\varphi(\cdot)$  and  $\delta(\cdot)$  capture the dis-utility from pollution and accidents, respectively. We add the concave function  $\xi(\cdot)$ , which captures the positive utility from health  $Q$ .<sup>4</sup>

Total travel  $M$  can be separated into two components, inactive travel  $M^{in}$  and active travel  $M^{ac}$ .

$$M = M^{in} + M^{ac}. \quad (2)$$

Inactive travel denotes travel using modes that require very little physical activity, most importantly using the car. Active travel instead captures walking and cycling. We also consider public transport as an active mode of travel, as it typically requires the individual to walk or bike to the bus stop, tram stop, or train station, in some cases providing up to 30% of daily exercise recommendations (Besser and Dannenberg, 2005). As such, active travel requires spending  $S$ , which will be further specified below. Inactive travel distance  $M^{in}$  requires fuel  $F$  and other travel inputs  $H$ :  $M^{in} = \chi(F, H)$ . In line with Parry and Small (2005), we assume that  $M^{in}$  is homogeneous of degree one with respect to its inputs. This specification allows for multiple channels of substitution. For instance, as fuel prices increase, the consumer can decide to i) reduce total distance travelled,  $M$ , ii) spend more on other inactive travel inputs,  $H$ , such as purchasing a vehicle with higher fuel economy, or iii) increase active travel distance,  $M^{ac}$ .

The agent spends time  $T^{in}$  in inactive travel. For a given distance  $M^{in}$ , this time is increasing in the amount of congestion on roads, which we take as an increasing function of the population average inactive miles travelled,  $\bar{M}^{in}$ :

$$T^{in} = \pi^{in}(\bar{M}^{in})M^{in}, \quad (3)$$

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<sup>4</sup>Equation (1) models the utility from health and leisure as separable. As a consequence, any improvement in health will leave the labour-leisure trade-off unaffected.

where  $\pi_{\bar{M}^{in}}^{in} > 0$ .  $\pi^{in}$  is equal to the inverse of speed of inactive travel, which we assume the agent takes as exogenous. In equilibrium,  $\bar{M}^{in} = M^{in}$ . For active travel we abstract from congestion,<sup>5</sup> and model time travelled as directly proportional to distance:

$$T^{ac} = \pi^{ac} M^{ac}, \quad (4)$$

with  $\pi^{ac}$  the inverse of speed from active mobility. Only inactive travel contributes to pollution, both in the form of carbon dioxide emissions, and local air pollution. CO<sub>2</sub> emissions are directly proportional to fuel use. To capture local air pollution effects, inactive miles travelled offer a better proxy (Hitchcock et al., 2014).<sup>6</sup> This allows us to write

$$P = P^f(\bar{F}) + P^m(\bar{M}^{in}), \quad (5)$$

with  $P_{\bar{F}}^f > 0$  and  $P_{\bar{M}^{in}}^m > 0$ . We also assume the agent will take pollution as given; she will not internalise the effect of travel decisions on the population averages  $\bar{F}$  and  $\bar{M}^{in}$ .

Both active and inactive travel are subject to accident risk. We separate accident costs associated to active and inactive travel. For inactive travel, accident costs are increasing with the amount of travel. As travel increases, the agent also imposes an “accident externality” upon other users: the higher average travel,  $\bar{M}^{in}$ , the more likely a road user will be involved in an accident. For active travel, we similarly assume that higher travel increases the number of, and thereby costs of, accidents. Yet, roads that are busier with cars tend to be more dangerous to both cyclists and pedestrians. Conversely, there exists a so-called “safety in numbers” effect: more cyclists on the road tend to make cycling safer overall (Elvik and Bjørnskau (2017), Kahlmeier et al. (2017)). Hence, we assume that the accident costs associated with active travel are increasing in the average amount of inactive travel,  $\bar{M}^{in}$ , and decreasing in

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<sup>5</sup>Even though public transport can get congested, this does not typically increase travel time. Bicycle paths do not generally get congested to the extent that travel time increases.

<sup>6</sup>Substantial emissions of particulate matter from transport are due to tyre, brake, and road abrasion, rather than fuel consumption. Fuel emissions contribute mostly to noxious gas emissions such as NO<sub>x</sub> and ozone.

average active travel,  $\bar{M}^{ac}$ . This gives

$$A = A^{in}(M^{in}, \bar{M}^{in}) + A^{ac}(M^{ac}, \bar{M}^{in}, \bar{M}^{ac}), \quad (6)$$

with  $A_{M^{in}}^{in} > 0$  and  $A_{\bar{M}^{in}}^{in} > 0$ . Likewise,  $A_{M^{ac}}^{ac} > 0$ , and  $A_{\bar{M}^{in}}^{ac} > 0$ , while  $A_{\bar{M}^{ac}}^{ac} < 0$ .

We assume active travel is conducive to health. To capture this we write health as a function of active travel:

$$Q = Q(M^{ac}, O), \quad (7)$$

where  $O$  are other forms of exercise,<sup>7</sup> with  $Q_{M^{ac}} > 0$  and  $Q_O > 0$ . We assume that the agent considers only a constant share  $\omega \in [0, 1]$  of  $Q$  as relevant in her optimisation problem. Instead of considering actual health  $Q$ , she considers “perceived health”,  $Q^{per}$ :

$$Q^{per} = \omega Q + \tilde{Q}, \quad (8)$$

where the agent considers  $\tilde{Q}$  as outside of her control, while in reality,  $\tilde{Q} = (1 - \omega)Q$ . Whenever  $\omega < 1$ , Equation (8) represents the notion that the individual underestimates the effect of exercise on health. This underestimation is consistent with substantive evidence that individuals do not fully appreciate the positive effects of activity-related health.<sup>8</sup>

With Equation (8) we adopt a specification of limited attention proposed by DellaVigna (2009), which assumes that the benefit of completing travel (in active mode) is “visible”, while the health benefit from active travel is “opaque”. This seems justified as many citizens are largely unaware of the high health benefits of even short walks (Fredriksson et al., 2018; Bennett et al., 2009). Alternatively, the unrealised health benefits from active travel could represent a case of time-inconsistent preferences (Laibson, 1997; O’Donoghue and Rabin, 1999), where citizens highly value their health, but repeatedly postpone undertaking exercise (DellaVigna and Malmendier, 2006). This can

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<sup>7</sup>Note that any adverse effect of pollution on health is already subsumed in  $\varphi(P)$ .

<sup>8</sup>Additionally, publicly financed healthcare systems and moral hazard in health insurance imply that individuals may not bear the full cost of unhealthy decisions.

be captured by an equivalent formulation of Equation (8) in our *static* model, as the assumption of time-inconsistent preferences implies an activity level less than desirable in the long term is pursued at any point in time. This holds in the absence of commitment devices, which arguably do not exist for active travel.

The agent's budget constraint is given by

$$C + (p^f + t^f)F + p^h H + p^o O + S = w(1 - t^l)L, \quad (9)$$

where  $p^f + t^f$  is the consumer price of fuel,  $p^h$  is the price of other inactive travel inputs, and  $p^o$  is the price of other forms of exercise. In addition, active travel requires the consumer to spend on items such as a bicycle or public transport. We denote by  $S$  any such spending on active travel (with normalised price), with  $S = S(M^{ac})$ ,  $S(0) = 0$  and  $S_{M^{ac}} > 0$ . Finally, we denote the gross wage rate by  $w$ , and the labour tax rate by  $t^l$ . The total amount of time available is given by  $\bar{L}$ , which is allocated to labour  $L$ , leisure,  $N$ , and time spent travelling  $T^{in}$  and  $T^{ac}$ , such that

$$L + N + T^{in} + T^{ac} = \bar{L}. \quad (10)$$

In the remainder of this paper, we assume that all prices are exogenous and constant. The fuel tax  $t^f$ , will be set by the policymaker. The proceeds of the fuel tax will be used to fund government spending  $G$ . The labour tax will in turn be set such that the government budget constraint is binding:

$$G = t^f F + t^l w L. \quad (11)$$

Throughout, we assume that there exists a unique and interior equilibrium, where the consumer chooses strictly positive levels of  $C$ ,  $F$ ,  $H$ ,  $M^{ac}$ ,  $O$  and  $L$ , and that  $G$  is such that  $t^l > 0$ .

## 2.2 Second-Best Fuel Tax

In the above setup, an increase in fuel use is associated with carbon emissions. Additionally, higher fuel use increases the number of miles travelled, which increases local pollution, as well as congestion, and accident risk. All these effects are not internalised by the representative consumer, who takes these factors as given. On their own, these externalities already justify the introduction of a positive “externality tax” on fuel. Such a tax will be welfare-improving, as it forces the agent to internalise (part of) the externality. In addition to the externalities, our framework also features an “internality”: whenever  $\omega < 1$ , the agent underestimates the extent to which higher levels of active travel deliver positive health benefits. Consequently, the choices of  $M^{ac}$  and  $O$ , and resulting  $Q$ , may be suboptimally low.

Our aim is to quantify how the consideration of these health benefits of active travel affects the welfare-maximising (optimal) fuel tax. For this purpose, we derive the solution for the optimal fuel tax,  $t^{f*}$ , and calibrate its value. We present the full derivation of  $t^{f*}$  in Appendix A, where we obtain the following result:

$$t^{f*} = Z^{P_{\bar{F}}} + [Z^{P_{\bar{M}^{in}}} + Z^C + Z^{A_{\bar{M}^{in}}}] \left( \frac{-dM^{in}}{dt^f} / \frac{-dF}{dt^f} \right) + Z^{A_{\bar{M}^{ac}}} \left( \frac{-dM^{ac}}{dt^f} / \frac{-dF}{dt^f} \right) - (1 - \omega) \tilde{Z}^Q \left( \frac{-dQ}{dt^f} / \frac{-dF}{dt^f} \right) - wt^l \left( \frac{-dL}{dt^f} / \frac{-dF}{dt^f} \right). \quad (12)$$

Here we define

$$Z^{P_{\bar{F}}} \equiv \frac{\varphi_P}{\mu_I} P_{\bar{F}}^f; \quad Z^{P_{\bar{M}^{in}}} \equiv \frac{\varphi_P}{\mu_I} P_{\bar{M}^{in}}^m; \quad Z^C \equiv \Gamma^{in} \pi_{\bar{M}^{in}}^{in} M^{in},$$

and

$$Z^{A_{\bar{M}^{in}}} \equiv \frac{\delta_A}{\mu_I} [A_{\bar{M}^{in}}^{in} + A_{\bar{M}^{in}}^{ac}]; \quad Z^{A_{\bar{M}^{ac}}} \equiv \frac{\delta_A}{\mu_I} A_{\bar{M}^{ac}}^{ac}; \quad \tilde{Z}^Q \equiv \frac{\xi_Q}{\mu_I},$$

with  $\Gamma^{in} \equiv w(1 - t^l) - \frac{\psi_{T^{in}}}{\psi_C}$ .

Equation (12) characterises the optimal fuel tax. This tax is equal to the sum of un-internalised costs associated with fuel use. The first term in

(12),  $Z^{P_{\bar{F}}}$ , is the direct pollution externality of fuel use. It is equal to the marginal cost of pollution,  $\varphi_P$ , multiplied by the effect of additional fuel use on pollution,  $P_{\bar{F}}^f$ , and converted to consumption units using the shadow value of income,  $\mu_I$ .

Next, higher fuel use is associated with more inactive miles travelled. The marginal externality cost of inactive miles travelled is captured by  $Z^{P_{\bar{M}^{in}}} + Z^C + Z^{A_{\bar{M}^{in}}}$ , the cost associated with increased air pollution, congestion, and accidents, respectively.<sup>9</sup> The contribution of these costs to the magnitude of the optimal fuel tax depends on the extent to which fuel taxes reduce miles travelled vis-à-vis fuel use. If the reduction in fuel use due to higher fuel taxes is associated with a small reduction in miles travelled (small  $\left(\frac{-dM^{in}}{dt^f} / \frac{-dF}{dt^f}\right)$ ), then only a small portion of the externality costs associated with miles travelled can (implicitly) be attributed to fuel use.

Likewise, fuel taxes may lead to changes in active travel distance, which is associated with accident externalities, with cost  $Z^{A_{\bar{M}^{ac}}}$ . The contribution of those costs to the optimal fuel tax then depends on the relative response of active travel to fuel taxes:  $\left(\frac{-d\bar{M}^{ac}}{dt^f} / \frac{-dF}{dt^f}\right)$ .

Our main effect of interest is  $(1 - \omega) \tilde{Z}^Q \left(\frac{dQ}{dt^f} / \frac{-dF}{dt^f}\right)$ : the adjustment of the optimal fuel tax to the health internality.  $\tilde{Z}^Q$  is the marginal value of additional health, with  $1 - \omega$  the un-internalised portion, see Sections 3.1.6 and 3.1.7. As can be seen from (12), a high value of  $\tilde{Z}^Q$  does not automatically imply that, once health internalities are accounted for, the optimal fuel tax is adjusted much; this is only the case if the fuel tax is an effective tool to increase health  $Q$ . Following (7), fuel taxes can affect health through two channels: by changing active travel  $M^{ac}$ , or through other forms of exercise  $O$ . In the remainder of this article, and consistent with the empirical literature (Martin et al., 2012), we will assume that the effect of fuel taxes on other forms of exercise  $O$  is negligible. This implies we set  $dO/dt_f = 0$ , and focus on changes in active travel as the primary channel through which fuel taxation affects health.

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<sup>9</sup>The term  $\Gamma^{in}$  in  $Z^C$  captures the notion that congestion is costly for two reasons: it creates a direct disutility (see (1)) and reduces time available to allocate to labour (see (10)).



The interpretation of the final remaining term is similar. Fuel taxes may also affect labour supply. Even though the agent takes into account that higher labour supply increases income, she does not internalise the positive effect of increased labour on the government budget. This effect is equal to the wage, multiplied by the labour tax rate,  $wt^l$ . The contribution of this effect to the optimal fuel tax is larger the larger the increase in labour supply in response to higher fuel taxes.

In the next section we quantify the optimal  $t^f$  and the effect of considering the health benefits of active travel thereon. To facilitate this quantification, we further manipulate Equation (12) to

$$t^{f*} = \frac{MEC}{1 + MEB} + \frac{t^l (p^f + t^f)}{1 - t^l} \frac{\varepsilon_{LL}^c (1 - \eta^{M^{in}I})}{-\eta^{FF}} + \frac{t^l}{1 - t^l} \left[ \varepsilon_{LL} - \varepsilon_{LL}^c (1 - \eta^{M^{in}I}) \right] Z^C \beta^{M^{in}} \frac{M^{in}}{F}, \quad (13)$$

with  $\varepsilon_{LL}^c$  and  $\varepsilon_{LL}$  the compensated and uncompensated labour supply elasticity. Akin to Parry and Small (2005), this optimal tax is separated in three components. The first component is the “adjusted Pigouvian tax,” equal to the marginal external cost associated to fuel use, corrected by the marginal excess burden of labour taxation. The marginal external cost of fuel use is given by

$$MEC \equiv Z^{P\bar{F}} + [Z^C + Z^{A\bar{M}^{in}} + Z^{P\bar{M}^{in}}] \beta^{M^{in}} \frac{M^{in}}{F} + [Z^{A\bar{M}^{ac}} - (1 - \omega) Z^Q] \beta^{M^{ac}} \frac{M^{ac}}{F}, \quad (14)$$

with  $Z^Q \equiv \frac{\xi_Q}{\mu_I} Q_{M^{ac}}$  the marginal value of active travel through induced changes in health. We use the following ratios of fuel and income price elasticities to capture the indirect benefits of fuel taxes through inactive and active distance

travelled and health<sup>10</sup>:

$$\beta^{M^{in}} \equiv \frac{\eta^{M^{in}F}}{\eta^{FF}}; \quad \beta^{M^{ac}} \equiv \frac{\eta^{M^{ac}F}}{\eta^{FF}}, \quad (15)$$

with  $\eta^{XF}$  the fuel price elasticity of  $X \in \{F, M^{in}, M^{ac}\}$ , and  $\eta^{M^{in}I}$  the income elasticity of inactive travel. The marginal excess burden  $MEB$  is commonly defined as

$$MEB \equiv \frac{\frac{t^l}{1-t^l} \varepsilon_{LL}}{1 - \frac{t^l}{1-t^l} \varepsilon_{LL}}. \quad (16)$$

The second component is the “Ramsey tax”: fuel taxes raise revenues, which are used to finance government spending. This component commands a positive tax on fuel even in the absence of external costs. The third component is the “congestion feedback”: a reduction in travel due to fuel taxation reducing congestion, freeing up time for labour. This creates a positive welfare effect as long as labour is taxed at a positive rate ( $t^l > 0$ ), and as such increases the optimal fuel tax.

### 3 Fuel tax components

In this section we explain how we choose the parameter values for the quantification of the optimal fuel tax. We specify a central value and a plausible range. Table 1 summarises the main parameter values, and Figure 1 provides a graphical representation of the costs  $Z$ . For comparability, where relevant, we adjust all values to year 2017 US dollar prices and US gallons. Finally, we state the implications for first-best policy.

In Figure 1, we converted CO<sub>2</sub> emissions pollution per gallon into per mile units using baseline fuel efficiency as presented in Table 1, such that all social costs are expressed in per mile units. It shows that the per mile benefits of using an active mode of travel are two orders of magnitude larger than most

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<sup>10</sup>The  $\beta$ ’s are equal to the response of miles travelled to fuel taxes relative to the response in fuel taxes. As such, they capture the relative effectiveness of fuel taxes in inducing changes in miles travelled, both active and inactive.

Table 1: Parameter values used for optimal fuel tax calculation and sensitivity analyses

Parameter	US		UK	
	Central value	Range	Central value	Range
Baseline fuel efficiency, $M^{in,0}/F^0$	24		28	
Fuel pollution (CO <sub>2</sub> ), per gallon, $Z^{PF}$	91	[41, 405]	86	[38, 380]
Distance pollution (air), per mile, $Z^{PM}$	4.5	[1, 9]	3.6	[1, 8]
Congestion, per mile, $Z^C$	10	[3, 14]	5	[0.1, 7.3]
Accidents, inactive, per mile, $Z^{A_{Min}}$	6.4	[2, 18]	1.6	[1, 2.3]
Accidents, active, per mile, $Z^{A_{Mac}}$	5.3	[1.5, 15]	1.6	[1.2, 2.6]
Inactivity, per mile, $Z^Q$	691	[403, 999]	244	[146, 683]
Rate of health internalisation, $\omega$	0.5	[0.3, 0.7]	0.5	[0.3, 0.7]
Fuel price elasticity, $\eta^{FF}$	-0.36	[-0.21, -0.75]	-0.48	[-0.3, -0.9]
VMT-fuel price elasticity, $\eta^{M^{in}F}$	-0.25	[-0.05, -0.3]	-0.35	[-0.2, -0.5]
Income elasticity of inactive travel, $\eta^{M^{in}I}$	0.4	[0.02, 0.6]	0.605	[0.3, 0.8]
Cross-elasticity of active travel, $\eta^{M^{ac}F}$	0.18	[0.17, 0.25]	0.18	[0.17, 0.25]
Current tax rate on gasoline*, $t_f^0$	55	n.a.	406	n.a.

\*Includes VAT for the UK but not US. All values are provided in USD cents using the end 2017 exchange rates 1 GBP = 1.351 USD. = 1.1251 EUR, and either per mile or per US gallon.  $M^{in,0}$  and  $F^0$  denote intensive miles travelled and fuel used at the initial gasoline tax rate. Justification for the social cost values is given in subsections 3.1.2 through 3.1.7.

other social costs. This difference is partly due to the difference in travel time between motorised transport and walking or cycling.

### 3.1 Parametrisation

#### 3.1.1 Baseline fuel efficiency and elasticities

**Baseline fuel efficiency** We set  $M^{in,0}/F^0$  according to average fuel efficiency of the UK and US vehicle fleets. The US average was 24 miles/gallon in 2016 (Administration, 2018), the UK average 28 miles/gallon (DfT, 2018b; DfT, 2018c). The difference in fuel efficiency is due to a smaller average size of the UK private vehicle fleet, and a higher proportion of diesel cars, which have a higher average fuel economy.

**Fuel price elasticities** Based on Dieler et al. (2015) and Litman (2013), we choose a fuel price elasticity,  $\eta^{FF}$ , of -0.38 for the US as a central estimate. This is slightly less elastic than the UK value of -0.45, where wider public

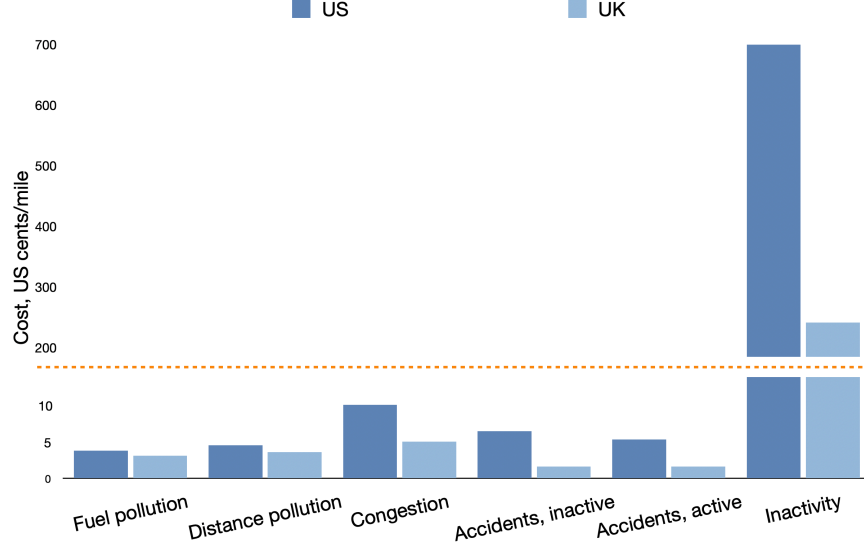


Figure 1: Social costs of personal car travel in US cents and on a per-mile basis.

transit offers alternatives to car use. The elasticities of inactive miles travelled (VMT) with respect to fuel price,  $\eta^{M^{in}F}$ , are calibrated at -0.25 in US, and -0.35 in the UK.<sup>11</sup>

To our knowledge, few direct estimates of the cross-elasticity of active travel (walking and cycling) with respect to the fuel price,  $\eta^{M^{ac}F}$ , exist. Instead, we primarily utilise estimates of the cross-elasticity of public transport with respect to fuel price (Litman, 2019). The use of public transit requires getting to and from stations, often done on foot or by an alternative active mode, and certain public transit investments have been found to be an effective way of increasing active travel (Reis et al., 2016). We adopt a range of 0.17 - 0.25 for  $\eta^{M^{ac}F}$ , with a central value of 0.18 for both the US and the UK.

**Income elasticity of inactive travel** The elasticity of inactive travel demand with respect to income,  $\eta^{M^{in}I}$ , is calibrated at 0.4 (0.02-0.6) for the

<sup>11</sup>The lower elasticity of miles travelled vis-à-vis fuel use is explained by the fact that the most significant response of an increase in fuel price is typically not reduction in the distance travelled by people, but rather upgrading to a higher fuel economy car (Coglianese et al., 2017).

US, and 0.605 (0.3-0.8) in the UK. We use long-term elasticities where possible to allow for mode shifts and other behaviour changes. Further details and a full list of references on fuel price and income elasticities can be found in Appendix B.2.

**Labour supply elasticities** For the compensated and uncompensated labour supply elasticities,  $\varepsilon_{LL}^c$  and  $\varepsilon_{LL}$ , we adopt the same values as Parry and Small (2005). These estimates fall in between the more recent estimates by e.g. Bargain et al. (2011) and Erosa et al. (2016).

### 3.1.2 External cost of CO<sub>2</sub> emissions (fuel pollution), $Z^{P_{\bar{F}}}$

The external costs of fuel use are the cost of carbon emissions and associated climate damages. We derive our central estimate and range of plausible values from a large body of literature (see Appendix B.3 for a full overview). We multiply the value of climate change costs per tonne of CO<sub>2</sub> emitted by the amount of CO<sub>2</sub> emitted per gallon of fuel burnt, weighted by fuel type consumption in both countries (diesel/gasoline) to derive an average value of fuel pollution costs per gallon of fuel.<sup>12</sup> With a social cost of carbon of \$90/tCO<sub>2</sub> and a range \$40 - 400/tCO<sub>2</sub>, the central estimate for the US is 91 cents/gallon, with a range of 41-405 cents/gallon. The central estimate for the UK is 86 cents/gallon, with a range of 38-380 cents/gallon. Throughout, we abstract from any effects of fuel taxation on the cost of carbon.

### 3.1.3 External cost of air pollution (distance pollution), $Z^{P_{Min}}$

Local air pollution is caused by car tyre and break wear emissions of PM<sub>2.5</sub> and PM<sub>10</sub>, which are approximately proportional to miles travelled, and by gases from incomplete fuel combustion processes.

For the US, estimates of the cost of air pollution per mile range from high values of \$0.089 (OECD, 2015) to extremely low values of \$0.007 (Muller et

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<sup>12</sup>As fuel mix is almost exclusively gasoline in the US but approximately half and half gasoline and diesel in the UK, the marginal cost of climate damages per gallon of fuel is not the same in both countries.

al., 2011), with several values in between: \$0.03 (Mashayekh et al., 2011), \$0.06/mile Parry et al. (2014). To reflect this uncertainty, we adopt values of \$0.01, \$0.045 and \$0.09 as the low, central, and high estimates for the US, respectively.

For the UK, national project evaluations use a value of \$0.036/mile (Hitchcock et al., 2014). OECD (2015) report a high value of \$0.08/mile travelled, while the average for a passenger car in the EU is estimated at \$0.009/mile for gasoline and \$0.033/mile for diesel cars. Reflecting the 55-45% split between gasoline and diesel cars in the UK and updated costs of air pollution (Birchby et al., 2019), we adopt values of \$0.01, \$0.036 and \$0.08 as the low, central, and high estimates.

#### 3.1.4 External cost of congestion, $Z^C$

Congestion is defined as the travel delay due to crowding of roads. For the US, we adopt the values by Inrix (2018), who provide a central value of \$0.1/mile, and a range of \$0.03- \$0.14/mile. In the UK, we follow Inrix (2019) and set the per-mile congestion costs at \$0.05/mile, with a lower and upper bound of \$0.001/mile and \$0.073/mile, respectively.<sup>13</sup>

#### 3.1.5 External cost of accidents, $Z^{A_{\bar{M}in}}$ and $Z^{A_{\bar{M}ac}}$

There are two components to accident costs: the internalised cost of knowing and accounting for the risk of getting into a crash; and the external cost of the increased risk of causing an accident imposed on others by travelling. Hence, using the full cost of accidents per mile driven would overestimate the size of the accident externality. Instead, we adopt the approach by Lemp and Kockelman (2008), who estimate the external costs of transport in the US and

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<sup>13</sup>Parry and Small (2005) already noted that the values available in empirical studies in transportation are VMT-weighted, but congestion costs enter the optimal fuel tax equation as being both VMT-weighted and fuel-price elasticity weighted. This is because demand for travel is more inelastic in more congested times and people internalise more of the waiting time cost. Adjusting for this reduces the marginal cost of congestion.

assume that 50% of accident costs are external.<sup>14</sup>

Using accident data and cost estimates from the report by Blincoe et al. (2015), we find that accident costs attributable to inactive modes of transport,  $Z^{A\bar{M}in}$ , amount to \$0.064/mile, with a range of \$0.02-\$0.18/mile for the US. Accident costs attributable to active modes of transport,  $Z^{A\bar{M}ac}$  amount to \$0.053/mile, with a range of \$0.015-\$0.15/mile. This is due to the proportionately higher death rate per accident and per mile travelled for active modes.

In the UK,  $Z^{A\bar{M}in}$  amounts to \$0.015/mile, with a range of \$0.01-\$0.023/mile. Accident costs attributable to active modes of transport,  $Z^{A\bar{M}ac}$ , amount to \$0.016/mile as well, with a range of \$0.012-\$0.026/mile (DfT, 2018a).

### 3.1.6 Cost of inactivity, $Z^Q$

The health benefits of exercise are well-known to be the most substantial health-related impact of active travel, dwarfing air pollution or accident effects. For example, De Hartog et al. (2010) estimate that people shifting from car to bicycle for short trips lose 7 days of life due to traffic accidents, 21 days of life due to air pollution, but gain 8 months of life due to physical activity. Our analysis requires translating such benefits into monetary values.

First, health benefits comprise all mortality- and morbidity-reducing effects. Second, there may be productivity benefits, due to a reduction in absenteeism (taking sick leave), and presenteeism (being at work but having lower productivity due to illness). Third, greater health reduces the (public) health system costs. Depending on the characteristics of the health system (and the extent to which the individual bears the cost of absenteeism), the costs can be labelled as private or external. In the remainder of the analysis, we focus on the value of unrealised private health benefits only, as they are

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<sup>14</sup>To determine the external cost of accidents associated to inactive travel, we consider all costs associated to car-on-car and car-on-pedestrian accidents, as well as 50% of the car-on-cyclist accident costs. Similarly for active travel, we include pedestrian only and cyclist-on-pedestrian accident costs and the remaining half of the car-on-cyclist accident costs.

much larger than the direct productivity gains to the economy.

In order to calculate the marginal value of the private health benefits from physical activity for the UK and US, we used the Health Economic Assessment Tool (HEAT) developed by the World Health Organisation (Kahlmeier et al., 2017). HEAT calculates the value of the changes in mortality arising from a specified change in walking and cycling for travel purposes.<sup>15</sup> Further details regarding the HEAT model, inputs and corresponding data sources can be found in Appendix B.4.

We convert the HEAT output to an estimate of the health benefit per mile of active travel. We obtained a central  $Z^Q$  value of \$6.91/mile for the US, with a range of \$4.03-9.99/mile. For the UK, this value is \$2.44/mile, with a range of \$1.46-6.83/mile. The UK-US discrepancy has two sources: higher VSL estimates for the US, and higher US baseline mortality rates for younger members of the population.

### 3.1.7 Rate of health internalisation, $\omega$

The extent to which individuals are aware of the health benefits of exercise and active travel are captured by the parameter  $\omega$ . High numbers of respondents (50-85%) in attitudinal transport surveys cite health reasons as one of their top three reasons for walking or cycling for travel (Börjesson and Eliasson, 2012; Useche et al., 2019). However, in general exercise knowledge surveys, only about half of respondents are knowledgeable of the amounts of physical activity required for health, and about 20-30% are capable of identifying the approximate odds of developing diseases without physical activity (Fredriksson et al., 2018; Bennett et al., 2009). We therefore chose a central value of 0.5 and a range of 0.3-0.7 for  $\omega$ .

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<sup>15</sup>HEAT is designed as a practitioner-oriented tool for health impact assessments. More complex assessments could quantify the effect of exercise on morbidity as well as mortality. Our results are therefore likely to be conservative estimates of the health benefits of physical activity.



### 3.2 Implications for first-best policy

Table 1 already permits a quantitative conclusion about first-best policy. In a first-best world, there exist appropriate policy instruments to address all market failures, as well as non-distortive (e.g. lump-sum) taxes to generate government revenues. One can verify that under these assumptions, the optimal carbon (fuel) tax is equal to the cost of fuel pollution,  $Z^{P\bar{F}}$ . Similarly, the socially optimal level of the price instruments for all other externalities (and internality, by analogy) are at their respective Pigouvian levels. For the internality, this Pigouvian level is equal to the social cost of inactivity, multiplied by the uninternalised share  $(1-\omega)$ . Importantly, this means that, on a per mile basis, a first-best subsidy paid to individuals for incentivising active travel modes would be at a much higher level than any of the tax levels for the externalities, or indeed, the sum of all other externality taxes.<sup>16</sup>

## 4 Quantitative Results

### 4.1 Optimal second-best fuel tax rates

We use Equations (13)-(15) and the parameter estimates provided in Table 1 to calculate the optimal fuel tax.<sup>17</sup> An increase in fuel taxation will reduce fuel use and inactive miles travelled, which will in turn affect the optimal tax through Equation (14). To account for this, we follow Parry and Small (2005), and endogenise  $F$ ,  $M^{in}$ , and  $M^{ac}$  in our numerical solution. Further details can be found in Appendix B.5.

We find an optimal fuel tax of \$4.54/gallon of fuel in the UK, which is slightly higher than the current fuel tax.<sup>18</sup> In the US, the optimal fuel tax amounts to \$10.13/gallon of fuel, which is more than ten times the current (population-weighted) average fuel tax across the fifty states. Table 2 lists the

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<sup>16</sup>For comparison to second-best see Section 4, and for the policy implications of that comparison see Section 5.

<sup>17</sup>We used R for all computations. Code available from authors on request.

<sup>18</sup>The total tax on UK fuel includes VAT (110 cents/gallon) and fuel duty (296 cents/gallon). In the United States, value added or indirect taxes are not levied on fuel.

Table 2: Central calculations of the optimal fuel tax rate

Cost, USD cents/gallon	United States	United Kingdom
Fuel efficiency, $M^{in}/F$	28.6	28.3
Adjusted Pigouvian tax:		
Pollution, fuel-related, $Z^{P\bar{F}}$	91	86
Pollution, distance-related, $Z^{P\bar{M}^{in}}\beta^{M^{in}}M^{in}/F$	90	74
Congestion, $Z^C\beta^{M^{in}}M^{in}/F$	199	103
Accidents inactive, $Z^{A\bar{M}^{in}}\beta^{M^{in}}M^{in}/F$	127	33
Accidents active, $Z^{A\bar{M}^{ac}}\beta^{M^{ac}}M^{ac}/F$	-4	-1
Physical inactivity, $(1 - \omega)\beta^{M^{ac}}M^{ac}/F$	256	109
Adjustment to $MEC$ for excess burden	-71	-36
Ramsey tax	326	83
Congestion feedback	-1	3
<b>Optimal fuel tax rate with physical activity, <math>t_1^{f*}</math></b>	<b>1013</b>	<b>454</b>
Optimal fuel tax rate without physical activity	681	335
Naïve fuel tax rate	593	372
Actual (2017) tax rate	55	406

Based on Equation (13) and (14), the optimal rate is the adjusted Pigouvian tax, adjustments for the excess burden, the Ramsey tax, and the congestion feedback, combined. The naïve rate is given by  $MEC_F$  (excluding the health externality) from Equation (14) with  $M^{in}/F = M^{in,0}/F^0$  and all  $\beta$ 's equal to 1.

optimal tax levels and their decomposition. This decomposition shows that costs associated to congestion and physical inactivity are the main contributors to the fuel tax, albeit this is somewhat reduced due to the compensation for the marginal excess burden of labour taxation. Ramsey taxes are substantial, especially in the US; the congestion feedback does not significantly influence the optimal fuel tax rate.

Including physical activity increases the UK fuel tax by 36%, and the US fuel tax by 49%. Although this increase is significantly smaller than the pure per-mile social cost of physical inactivity, the inactivity component is still the largest contributor to the MEC part of the tax.

Consistent with both Parry and Small (2005) and Santos (2017), we find that the second largest externality component of the second-best optimal fuel tax for both countries is congestion. In London, congestion impacts are 28 times higher than the EU average (Cookson, 2016), which greatly influences

the congestion costs for the UK, even though the value of travel time estimates for the US are higher than for the UK.

This is followed by inactive accidents in the United States. In the US, traffic accidents are associated with a far higher per-mile cost, even though the rates of traffic injuries are very similar in both countries. This is explained by a higher nominal value that is attached to human life in the US. Contrary to Parry and Small (2005), air pollution costs for both countries contribute less to the fuel tax than carbon emissions. This is the result of both increasingly stringent fuel air pollutant emissions standards,<sup>19</sup> and growing consensus that the social cost of carbon is higher (see Subsection 3.1.2).

In addition to the second-best optimal tax, we compute the “naïve” tax rate, which is based on three assumptions: first, all  $\beta$ s are equal to 1; i.e. both active and inactive miles travelled are equally responsive to fuel taxation as fuel use. Second, the feedback of tax-induced changes in fuel use and miles travelled to the tax rate is ignored. Third, interactions of the fuel tax with the labour tax, as well as the Ramsey component are abstracted from. Instead, the only relevant components to the tax are the external effects of car use. The naïve rate as such mimics common practice in transport and cost-benefit analysis evaluations.<sup>20</sup> In our central calculations  $\beta^{M^{in}} = 0.69$  (US) or 0.73 (UK), and  $\beta^{M^{ac}} = -0.50$  (US) and -0.38 (UK). The low  $\eta^{M^{in}F}$  reflects the very inelastic demand for vehicle-miles travelled (VMT), meaning that most reduction in fuel use comes from increases in fuel economy of driving and the vehicle fleet, not reductions in distances covered in cars. Thus, mileage-related externalities (air pollution, congestion, and accidents) are all inflated in the naïve fuel tax calculation.

Treating fuel efficiency, fuel consumption and distance travelled as endogenous, rather than exogenous, in the second-best optimal fuel tax

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<sup>19</sup>Such as Corporate Average Fuel Economy (CAFE) standards.

<sup>20</sup>In applied transportation research, the difference between the responsiveness of fuel consumption to fuel prices and miles travelled to fuel prices are often disregarded, and assumed to be unitary. Multiplying externalities only by fuel efficiency, and not by the responsiveness of VMT to fuel price, is considered the naïve approach in literature, and can sometimes lead to a doubling of the optimal fuel tax estimation (Newbery et al., 1995).

calculation causes fuel consumption to fall by 43.9% and 3.7% in the US and UK, respectively. Inactive travel  $M^{in}$  falls slightly less, by 33.1% in the US, and this is more than compensated for by an increase of 33.5% in active travel. In the UK, inactive travel also falls by less than fuel consumption, by 1.7%. However, as active travel increases only by 1.4%, total travel in the UK falls. The overall tax increases by 81.1% in the US and 3% in the UK. The change is more dramatic in the US because of the low fuel efficiency of motor vehicles, and higher contingent valuation of people's time and lives, resulting in a bigger Pigouvian tax. In the UK, the current tax level is very close to the optimal level. The fuel efficiency of motor vehicles in the UK therefore does not change much in response to moving to the optimal level, and the endogenous solution does not change the optimum level significantly.

## 4.2 Welfare Effects

The welfare gain of implementing the second-best optimal fuel tax is presented in Table 3. We use the current tax rate as a benchmark, and consider a fuel tax that does, and does not, take into account active travel benefits. All gains are expressed as a share of current fuel expenditure. The analytical derivation of the welfare benefit is discussed in Appendix B.6. The welfare gain of implementing the second-best optimal tax that accounts for the health externality is 129% for the US, but only 0.16% for the UK. Contrary to the UK, in the US, any increase in the fuel tax yields significant welfare improvements. This difference is primarily due to the very low current US fuel tax, while the UK fuel tax is already close to the optimal rate.

We additionally present the changes in active and inactive miles travelled following the change in the fuel tax. In the UK, the small change in fuel taxes results in relatively small changes in distance travelled. In the US, however, the fuel price changes are large, and induce a substantial shift from inactive to active miles.<sup>21</sup>

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<sup>21</sup>However, as we used constant fuel price elasticities to calculate these changes, these results should be interpreted with caution. It is unlikely that a 20-fold increase in the fuel tax in the US would induce the same rate of response as a 20% increase in the tax.

Table 3: Welfare effects of fuel taxation

US					
Fuel tax	Rate (c/gal)	Welfare change	$M^{in}$ change	$M^{ac}$ change	Annual lives
$t^{J*}$	1013	129%	-33.04%	33.47%	6266 saved
$t^f$ , excluding health benefits	681	124%	-27.39%	25.92%	4701 saved

UK					
Fuel tax type	Rate (c/gal)	Welfare change	$M^{in}$ change	$M^{ac}$ change	Annual lives
$t^{J*}$	454	0.16%	-2.67%	1.40%	39 saved
$t^f$ , excluding health benefits	335	-0.99%	4.58%	-2.28%	120 lost

Calculated relative to the current rate, expressed as a percentage of current fuel expenditure (approximately \$1800 in the US and \$1500 per person per year in the UK, according to household expenditure surveys (BLS, 2019; ONS, 2019)). The current US fuel tax rate is \$0.55/gal, and the current UK fuel tax rate is \$4.06/gal.

Finally, we compute the effect of the tax increase on mortality through increased active travel using the HEAT tool, described in Section 3.1.6 and Appendix B.4. Increases in active travel primarily save lives by improving health from increasing exercise. HEAT then corrects this value for the lives lost due to greater air pollution exposure, and increase in accident fatalities of pedestrians and cyclists (see also Appendix B.7).<sup>22</sup> Due to a larger tax increase and larger population size, lives saved are greatest in the US: setting the fuel tax at its optimal level saves 6266 lives each year.

### 4.3 Sensitivity Analysis

In Figure 2, we illustrate the sensitivity of the optimal second-best fuel tax with respect to the elasticities and rate of health internalization, keeping all other parameters at their central values (denoted X in the graphs). Figure B.2 presents additional results where we vary the cost parameters  $Z$ . Further details and figures can be found in Appendix B.8.

For both the UK and US, the fuel tax is most sensitive to  $\eta^{FF}$ , the fuel price elasticity. This elasticity directly affects the optimal fuel tax through

<sup>22</sup>HEAT only computes the lives saved due to an increase in active travel. Higher fuel taxation also reduces inactive miles travelled, which reduces air pollution and vehicle traffic fatalities. As we do not capture these effects, the values reported in Table 3 can be considered a lower bound for the lives saved due to the tax increase.

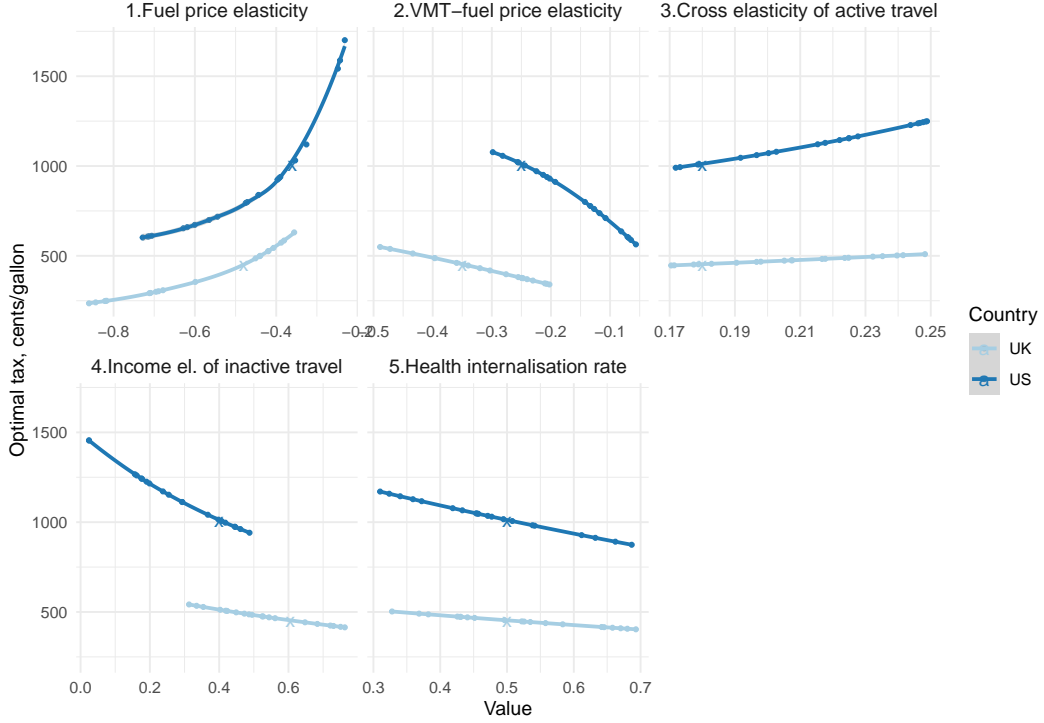


Figure 2: Sensitivity of the fuel tax to relevant elasticities and the rate of health internalisation

$\beta^{M^{in}}$  and  $\beta^{M^{ac}}$  in the MEC component (see Equation (14)), and indirectly by governing the response of fuel use  $F$  to the introduction of the fuel tax. Jointly, as shown in the figure, this results in a positive relationship between the fuel price elasticity and the optimal fuel tax. Using the upper or lower bound of the fuel price elasticity, as opposed to the central value, can either increase or decrease the fuel tax by as much as 50 percent. Conversely, the net effect of the elasticity of inactive travel (VMT) with respect to the fuel prices,  $\eta^{M^{in}F}$ , on the fuel tax is negative. Using the upper bound instead of the central value for  $\eta^{M^{in}F}$ , reduces the fuel tax by up to 50 percent; using the lower bound instead has a noticeably smaller effect. The fuel tax is relatively insensitive to the cross elasticity of active travel,  $\eta^{M^{ac}F}$  and the rate of health internalisation. The income elasticity of inactive travel affects the fuel tax especially for the US. This effect materialises via the Ramsey tax component,

which is comparatively large for the US to begin with (see Table 2).

The fuel tax in both the US and the UK increases approximately linearly with all social cost parameters and the cost of inactivity (that is  $Z^{P\bar{F}}$ ,  $Z^{A\bar{M}in}$ ,  $Z^{A\bar{M}ac}$ ,  $Z^{P\bar{M}in}$ ,  $Z^C$ , and  $Z^Q$ ), reacting most strongly to  $Z^{P\bar{F}}$ , fuel pollution, i.e. the social cost of carbon. For more details see Appendix B.8.

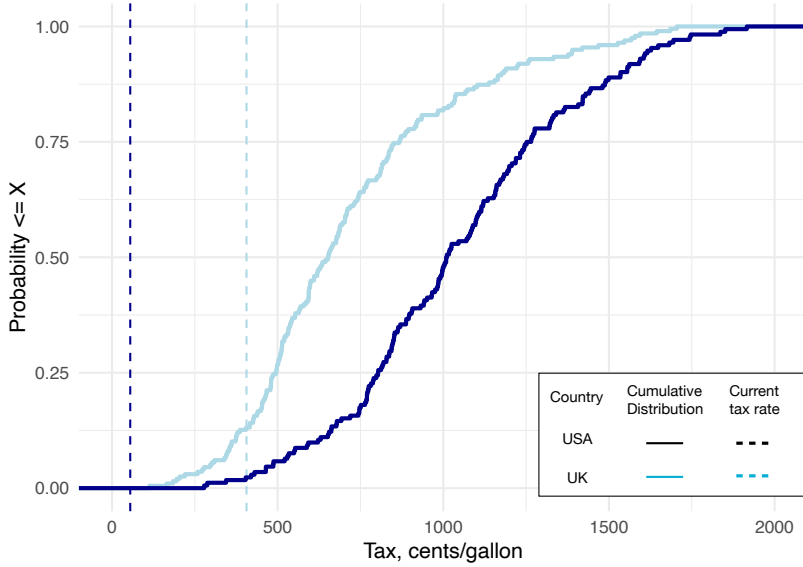


Figure 3: Cumulative distribution function of optimal fuel tax values for both US and UK.

Figure 3 presents the results of a Latin Hypercube parameter sensitivity analysis using the *pse* package in R (Chalom and de Prado, 2015). We varied parameters for external costs and the elasticities using 20 values drawn at random from a uniform distribution, and allowed fuel use and mileage to be generated endogenously. The function was run 200 times, with 50 bootstrap replicates. For the United States, the optimal fuel tax is less than 0.01% likely to be below the current 55 cents/gallon. For the UK, the optimal fuel tax is below current fuel tax of 406 cents/gallon with a 15% probability.

## 5 Discussion

This article shows that it may be very costly to societies not to reap the health benefits from choosing travel modes that lead to more physical activity. Including these benefits in an analysis of optimal fuel taxation shows that the optimal fuel tax increases significantly, although to a lesser extent than one might expect based on assessments of the benefits of active travel measured in public health. Here we discuss how our findings align with current thought on optimal transport policy, and subsequently discuss limitations of our approach.

Experts on urban transport policy have long argued for a mix of “push” and “pull” factors to efficiently reduce societal costs from car use (Pucher and Buehler, 2007; Creutzig and He, 2009). “Push measures” discourage car use and include fuel or road pricing and parking fees; “pull measures” encourage uptake of other forms of transport by making them more attractive. Our study only explicitly considers a fuel tax, but a number of conclusions about other policy instruments may be drawn. First, both active and inactive miles travelled are relatively inelastic to the fuel tax. This not only affects the second-best optimal level, but also implies that a fuel tax on its own is not an ideal instrument for reducing mileage-related externalities. Parry and Small (2005) suggest that using a VMT tax for all externalities other than carbon emissions would be preferable. Indeed, there is renewed academic interest in alternative road pricing mechanisms, such as congestion or GPS-based charging, cordon pricing, optimal toll pricing, or real time road pricing (see Guo et al., 2017; Cramton et al., 2018; Bjertnæs, 2019). However, ideal externality-correcting mechanisms have not been widely implemented and most plans to introduce congestion charging are advancing slowly. Still, the benefit of the fuel tax over a congestion charge is that a fuel tax can, at least indirectly, address all large externalities caused by driving concurrently, and be used to generate a broader revenue base for the government (Rietveld and van Woudenberg, 2005). It also encourages improvements in the fuel economy of the fleet by encouraging the purchase of more efficient new cars, and in some cases, more fuel efficient driving patterns (Dhondt et al., 2013;



Bjertnæs, 2019).

Second, our study has further implications for policies encouraging active transport. Akin to congestion charges, a straightforward public finance approach could involve a direct subsidy for active modes of travel (Wardman et al., 2007; EBS, 2020) or indirect subsidies in the form of suitable cycling and washing facilities for employees that would improve comfort of cycling relative to driving (Useche et al., 2019).

Appropriate active travel infrastructure may however be a more important “pull” measure to make walking and cycling attractive.<sup>23</sup> Car-free city centres, bicycle lane networks and improvements in public transport provision will increase the mode share of active travel (Pucher and Buehler, 2007; Buehler and Pucher, 2012; Gössling, 2013). For example, in a study of 167 European cities, Mueller et al. (2018) find that increasing bicycle lane infrastructure in urban areas up to 315km/100,000 inhabitants increases the mode share of cycling up to 24.7%. Further, the lack of appropriate street lighting, and badly maintained roads and cycle lanes have all been identified as factors impeding active commuting (Yang et al., 2017; NHTS, 2019). Active travel infrastructure policies also create opportunities to adopt active travel modes to begin with, by making the demand for both active miles travelled, and miles by car more responsive to fuel prices. Investing in cycling infrastructure has not been considered a significant investment strategy until recently, and neither have infrastructure cost assessments been including it in their analyses (Van Essen et al., 2011).

Our optimal tax result signals that the extent to which an increase in fuel taxes is welfare enhancing is constrained by the presence of viable low-carbon alternatives (high  $\beta$ 's). This result was also demonstrated by Martens (2016), and (in part) justifies the grievances of the Gilets Jaunes movement in France. Conversely, this implies that improvements in infrastructure designed for active travel and public transport as discussed above could further support

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<sup>23</sup>Standalone marginal increases in fuel taxes are unlikely to spur significant behaviour change in drivers, because the response to a fuel tax is to alter fuel consumption, but not to reduce the amount or distances travelled by car – the demand for VMT is more inelastic than the demand for fuel (Gillingham and Munk-Nielsen, 2019).

increased fuel taxation.<sup>24</sup> While greater willingness of citizens to switch to active travel in particular would manifest itself in a higher responsiveness of active travel to fuel taxation,  $\eta^{M^{ac}F}$ , it would likely also result in higher active miles travelled  $M^{ac}$ , lower fuel use  $F$ , and higher (absolute) elasticities  $\eta^{M^{in}F}$ . From (13)-(15), all of these effects would justify higher fuel taxes.

A full characterisation of the “pull effect,” would include the public good characteristics of infrastructure – everyone benefits from safer and more comfortable cycling infrastructure – which will lead individuals to derive more utility from active travel and therefore “pull” them into these modes. This channel is not considered in our model and yet could lead to either higher *or lower* second-best optimal fuel taxes (Siegmeier, 2016), once infrastructure changes are seen as an additional policy instrument rather than an exogenous change in elasticities (similar to Bovenberg and van der Ploeg, 1994). In other words, as improved public transport infrastructure moves active travel decisions closer to optimal decisions, it may reduce the need for and value of higher fuel taxes as captured through  $Z^Q$ . We believe this is a crucial area for further work.

We note a number of limitations to our study: health manifests itself only as an externality within the utility function, though there is evidence that health-labour feedback loops might exist, specifically between physical activity and productivity (Proper et al., 2006), and presenteeism (Pereira et al., 2015). We abstract from these effects in our analysis; if anything, including such effects would strengthen the case for including health benefits from active travel in transport policy assessments. Further, we do not consider distributional concerns of the policy instruments, especially related to income, location or race (see Bento et al., 2009 and Tessum et al., 2019, Creutzig et al., 2020). We further do not explicitly model pre-existing regulation such as fuel efficiency standards, which are an important element in current transport regulation (Greene, 2011). Finally, we combine public transport with walking

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<sup>24</sup>Future research could investigate how cost-benefit analysis of public transport infrastructure project changes once health benefits are taken into account. Such an analysis should note that the health benefits are unevenly distributed across the population.

and cycling as an active mode of transport, and so omit recent trends in urban travel such as ride-hailing and sharing apps such as Uber, or the increasing popularity of e-scooters.

## 6 Conclusion

This article shows that optimal fuel tax rates increase significantly if the health benefits from increased active travel, such as reduced rates of diabetes, cardiovascular diseases, dementia, and depression are not fully internalised by citizens. Building on the established framework developed by Parry and Small (2005), we present an assessment of optimal fuel taxation when an externality through physical inactivity is also considered in the tax design.

We confirm the main conclusion of a large body of research in public health that, per mile travelled, the social costs of inactivity dominate the social costs from transport externalities by two orders of magnitude. We examine how this fact changes the appropriate second-best optimal fuel tax, which targets active travel health benefits only indirectly. We conclude that the second-best optimal fuel tax increases from \$3.35 to \$4.54/gallon in the UK and \$6.81 to \$10.13/gallon in the US. Due to the inelastic demand for vehicle miles travelled and cross-elasticity of active travel, the tax rate increases by less than the value of the per-mile externality.

In contrast to Parry and Small (2005), we find that the fuel tax rate in the United Kingdom is close to optimal when the health benefits from active travel are accounted for. We confirm that, even without these benefits, in the United States fuel is significantly undertaxed: it exceeds the current average fuel tax rate across the 50 states, as well as the previous estimate by Parry and Small (2005). Over the past two decades, the economic cost of damages to human health (air pollution and accident externalities) have risen significantly; more time is being spent in congestion on US roads, and the value of time has also risen faster than inflation. Further, the social cost of carbon estimates we derived from the literature (\$40-400/tCO<sub>2</sub>) are now several times higher than the values Parry and Small used in 2005 (\$6.8/tCO<sub>2</sub>, \$0.2-27/tCO<sub>2</sub>). Whereas

pollution linked to CO<sub>2</sub> emissions contributed the least to their Pigouvian tax component, it is the third largest component according to our estimates. It has the most significant influence on the fuel tax as the cost of carbon damages increases.

Including the significant health benefits from active travel means that fuel taxes should be increased, as they are an established instrument for addressing all social costs of transport. The modest relevance of a fuel tax on an individual's decision to walk or cycle indicates, however, that the fuel tax may not be the most appropriate policy instrument to encourage active travel. This is further reinforced as the optimal US fuel tax can be deemed politically unrealistic. Instead, more targeted measures to increase the relative price of car travel such as congestion charges, and measures aimed at reducing barriers to other modes of transport such as building better active travel infrastructure, will permit societies to reap the high health benefits. Congestion charging would be effective in both the UK and the US for this purpose (Cramton et al., 2018). The US specifically would benefit from more public transit infrastructure that would result in more active trips as people reach the transit stops by foot or bicycle. The UK, characterised by denser cities, would especially benefit from improved urban infrastructure for walking and cycling. Nonetheless, without an associated change in the price signal in the form of a fuel tax rise or congestion charge, infrastructure investment is unlikely to lead to sufficient changes in travel decisions on its own (Buehler et al., 2017; Pucher et al., 2010). Different policies at multiple levels are needed to realise meaningful change in transport.

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Healthy climate, healthy bodies: Optimal fuel taxation and physical activity

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## A Mathematical Appendix.

### A.1 Derivation of the optimal fuel tax $t^f$

We derive the optimal fuel tax in two steps. First, we consider the consumer's optimisation problem. We define  $V$  as the consumer's maximised value function, and determine the first-order conditions corresponding to the solution of this value function. Next, we determine the optimal fuel tax by computing the total derivative of  $V$  with respect to the tax on fuel,  $dV/dt^f$ . Setting this term equal to zero then allows us to obtain Equation (13) as detailed below.

#### A.1.1 Consumer optimisation problem

The consumer maximises (1) with respect to (2)-(10). As described in the text, it takes pollution  $P$ , measures for congestion  $\pi$  and a large part of the accident risk as given. Instead of considering actual health (7), it considers perceived health (8). This allows us to define the following maximised value function:

$$\begin{aligned}
 V \equiv \text{Max}_{C,F,H,M^{ac},O,L} \{ & u(\psi(C, M, T^{in}, T^{ac}, G), N) - \varphi(P) - \delta(A) + \xi(Q^{per}) \\
 & + \mu_M [M^{in} + M^{ac} - M] + \mu_{M^{in}} [\chi(F, H) - M^{in}] + \mu_{T^{in}} [\pi^{in}(\bar{M}^{in})M^{in} - T^{in}] \\
 & + \mu_{T^{ac}} [\pi^{ac}M^{ac} - T^{ac}] + \mu_A [A^{in}(\bar{M}^{in}, M^{in}) + A^{ac}(M^{ac}, \bar{M}^{in}, \bar{M}^{ac}) - A] \\
 & + \mu_{Q^{per}} [\omega Q(M^{ac}, O) + \bar{Q} - Q^{per}] \\
 & + \mu_I [w(1 - t^l)L - C - (p^f + t^f)F - p^hH - p^oO - S^{ac}] \\
 & + \mu_S [S(M^{ac}) - S^{ac}] + \mu_L [\bar{L} - L - N - T^{in} - T^{ac}] \}, \quad (\text{A.1})
 \end{aligned}$$

with corresponding first-order conditions

$$u_\psi \psi_C - \mu_I = 0, \quad (\text{A.2})$$

$$u_\psi \psi_M - \mu_M = 0, \quad (\text{A.3})$$

$$-\delta_A - \mu_A = 0, \quad (\text{A.4})$$

$$\mu_M - \mu_{M^{in}} + \mu_{T^{in}} \pi^{in} + \mu_A A_{M^{in}}^{in} = 0, \quad (\text{A.5})$$

$$\mu_M + \mu_{T^{ac}} \pi^{ac} + \mu_A A_{M^{ac}}^{ac} + \mu_Q \omega Q_{M^{ac}} + \mu_S S_{M^{ac}} = 0, \quad (\text{A.6})$$

$$u_\psi \psi_{T^{in}} - \mu_{T^{in}} - \mu_L = 0, \quad (\text{A.7})$$

$$u_\psi \psi_{T^{ac}} - \mu_{T^{ac}} - \mu_L = 0, \quad (\text{A.8})$$

$$\mu_{M^{in}} \chi_F - \mu_I (p^f + t^f) = 0, \quad (\text{A.9})$$

$$\mu_{M^{in}} \chi_H - \mu_I p^h = 0, \quad (\text{A.10})$$

$$\xi_Q - \mu_Q = 0, \quad (\text{A.11})$$

$$\mu_Q \omega Q_O - \mu_I p^o = 0, \quad (\text{A.12})$$

$$-\mu_I - \mu_S = 0, \quad (\text{A.13})$$

$$u_N - \mu_L = 0, \quad (\text{A.14})$$

$$-\mu_L + \mu_I w (1 - t^l) = 0. \quad (\text{A.15})$$

### A.1.2 Optimal taxation

The optimal fuel tax is implicitly determined by  $dV/dt^f = 0$ , taking into account that  $t^l$  is determined through (11), and that in equilibrium  $\bar{M}^{in} = M^{in}$ ,  $\bar{M}^{ac} = M^{ac}$ ,  $\bar{F} = F$ , and  $\tilde{Q} = (1 - \omega)Q$ . From (A.1) and (A.2)-(A.15) we then obtain

$$\begin{aligned} \frac{dV}{dt^f} = & \left[ \mu_{T^{in}} \pi_{M^{in}}^{in} \chi_F M^{in} - \delta_A [A_{M^{in}}^{in} + A_{M^{in}}^{ac}] \chi_F - \right. \\ & \left. \varphi_P [P_{\bar{F}}^f + P_{M^{in}}^m \chi_F] + \mu_I t^f \frac{dF}{dt^f} \right. \\ & \left. + [\mu_{T^{in}} \pi_{M^{in}}^{in} M^{in} \chi_H - \delta_A [A_{M^{in}}^{in} + A_{M^{in}}^{ac}] \chi_H - \varphi_P P_{M^{in}}^m \chi_H] \frac{dH}{dt^f} \right. \\ & \left. + [-\delta_A A_{M^{ac}}^{ac} + \xi_Q (1 - \omega) Q_{M^{ac}}] \frac{dM^{ac}}{dt^f} + \xi_Q (1 - \omega) Q_O \frac{dO}{dt^f} + \mu_I w t^l \frac{dL}{dt^f} \right]. \end{aligned}$$

Further rearranging this term and using  $\frac{dM^{in}}{dt^f} = \chi_F \frac{dF}{dt^f} + \chi_H \frac{dH}{dt^f}$  and  $\frac{dQ}{dt^f} = Q_{Mac} \frac{dM^{ac}}{dt^f} + Q_O \frac{dO}{dt^f}$ , we obtain

$$\begin{aligned} \frac{1}{\mu_I} \frac{dV}{dt^f} = & \left[ t^f - \frac{\varphi_P}{\mu_I} P_{\bar{F}}^f \right] \frac{dF}{dt^f} \\ & + \left[ \frac{\mu_{T^{in}}}{\mu_I} \pi_{M^{in}}^{in} M^{in} - \frac{\delta_A}{\mu_I} [A_{M^{in}}^{in} + A_{M^{in}}^{ac}] - \frac{\varphi_P}{\mu_I} P_{M^{in}}^m \right] \frac{dM^{in}}{dt^f} \\ & + \left[ -\frac{\delta_A}{\mu_I} A_{Mac}^{ac} \right] \frac{dM^{ac}}{dt^f} + (1 - \omega) \frac{\xi_Q}{\mu_I} \frac{dQ}{dt^f} + wt^l \frac{dL}{dt^f}. \quad (\text{A.16}) \end{aligned}$$

Equation (A.16) is a generalisation of Equation (2.9) in Parry and Small (2004), taking into account active travel decisions. To find the optimal fuel tax we then set (A.16) equal to zero, and isolate  $t^f$ . We obtain

$$\begin{aligned} t^{f*} = & Z^{P_{\bar{F}}} + [Z^C + Z^{A_{\bar{M}^{in}}} + Z^{P_{\bar{M}^{in}}}] \left( \frac{-dM^{in}}{dt^f} / \frac{-dF}{dt^f} \right) + Z^{A_{Mac}} \left( \frac{-dM^{ac}}{dt^f} / \frac{-dF}{dt^f} \right) \\ & - (1 - \omega) \tilde{Z}^Q \left( \frac{-dQ}{dt^f} / \frac{-dF}{dt^f} \right) - wt^l \left( \frac{-dL}{dt^f} / \frac{-dF}{dt^f} \right), \quad (\text{A.17}) \end{aligned}$$

where we define

$$\begin{aligned} Z^{P_{\bar{F}}} &\equiv \frac{\varphi_P}{\mu_I} P_{\bar{F}}^f; \quad Z^{P_{\bar{M}^{in}}} \equiv \frac{\varphi_P}{\mu_I} P_{M^{in}}^m; \quad Z^{A_{\bar{M}^{in}}} \equiv \frac{\delta_A}{\mu_I} [A_{M^{in}}^{in} + A_{M^{in}}^{ac}]; \\ Z^{A_{Mac}} &\equiv \frac{\delta_A}{\mu_I} A_{Mac}^{ac}; \quad \tilde{Z}^Q \equiv \frac{\xi_Q}{\mu_I}, \text{ and } Z^C \equiv \Gamma^{in} \pi_{M^{in}}^{in} M^{in}. \end{aligned}$$

To obtain  $Z^C$ , we use (A.7) and (A.15), and define  $\Gamma^{in} \equiv w(1 - t^l) - \psi_{T^{in}} / \psi_C$ . Equation (A.17) can in turn be expressed as

$$t^{f*} = MEC - wt^l \left( \frac{-dL}{dt^f} / \frac{-dF}{dt^f} \right), \quad (\text{A.18})$$

with

$$MEC \equiv Z^{P_{\bar{F}}} + [Z^C + Z^{A_{\bar{M}^{in}}} + Z^{P_{\bar{M}^{in}}}] \beta^{M^{in}} \frac{M^{in}}{F}$$

$$+ [Z^{A_{Mac}} - (1 - \omega) Z^Q] \beta^{Mac} \frac{M^{ac}}{F},$$

$$\beta^{Min} \equiv \frac{\eta^{Min F}}{\eta^{FF}}; \beta^{Mac} \equiv \frac{\eta^{Mac F}}{\eta^{FF}}; Z^Q \equiv \frac{\xi_Q}{\mu_I} Q_{Mac},$$

where  $\eta^{XF}$  is the fuel price elasticity of  $X \in \{M^{in}, M^{ac}\}$ , and we impose  $dO/dt^f = 0$ .

By linear homogeneity,  $M^{in} = \chi_F F + \chi_H H$ . Then, using (A.3)-(A.5), (A.7), (A.9), (A.10) and (A.15) we obtain

$$\frac{u_M}{\mu_I} = p^{Min}, \quad (A.19)$$

with  $u_M \equiv u_\psi \psi_M$ ,  $p^{Min} \equiv [(p^f + t^f)\alpha^F + p^h\alpha^H] + \Gamma^{in}\pi^{in} + \Lambda^{in}$ ,  $\alpha^F \equiv F/M^{in}$ ,  $\alpha^H \equiv H/M^{in}$ , and  $\Lambda^{in} \equiv \frac{\delta A_{M^{in}}^{in}}{u_\psi \psi_C}$ . Similarly, from (A.2), (A.3), (A.4), (A.6), (A.8), (A.11), (A.13) and (A.15) we can write

$$\frac{u_M}{\mu_I} = p^{Mac}, \quad (A.20)$$

with  $p^{Mac} \equiv S_{Mac} + \Gamma^{ac}\pi^{ac} + \Lambda^{ac} - \Omega^Q$ ,  $\Gamma^{ac} \equiv w(1 - t^l) - \frac{\psi_T^{ac}}{\psi_C}$ ,  $\Lambda^{ac} \equiv \frac{\delta A_{Mac}^{ac}}{u_\psi \psi_C}$ , and  $\Omega^Q \equiv \frac{\xi_Q}{u_\psi \psi_C} \omega Q_{Mac}$ . From the perspective of the consumer,  $p^{Min}$  and  $p^{Mac}$  denote the (minimised) effective price of inactive and active travel, respectively. As in Parry and Small (2004), the homogeneity assumption will ensure that we can write  $\alpha^F(t^f)$  and  $\alpha^H(t^f)$ . Repeated substitutions using (3), (9), (10), the first order conditions and (A.19) and (A.20) then allow us to write the following demand functions

$$\begin{aligned} C &= C(p^{Min}, t^l); & L &= L(p^{Min}, t^l); \\ M^{in} &= M^{in}(p^{Min}, t^l); & M^{ac} &= M^{ac}(p^{Min}, t^l); \\ F &= F(p^{Min}, t^l, t^f) = \alpha^F(t^f) M^{in}(p^{Min}, t^l); \\ H &= H(p^{Min}, t^l, t^f) = \alpha^H(t^f) M^{in}(p^{Min}, t^l). \end{aligned} \quad (A.21)$$

where the last two follow from the definition of  $\alpha^F$  and  $\alpha^H$ . For prices we can



similarly write

$$p^{M^{in}} = p^{M^{in}}(t^f, \pi^{in}, t^l); \quad p^{M^{ac}} = p^{M^{ac}}(t^f, \pi^{in}, t^l). \quad (\text{A.22})$$

The demand and price functions (A.21) and (A.22) are equivalent to expressions (B3a) and (B3b) in Parry and Small (2004). The remainder of the derivations then similarly follows Parry and Small (2004). First, from (A.21) and (A.22), we can write  $L(t^f, \pi^{in}, t^l)$ . Then

$$\frac{dL}{dt^f} = \frac{\partial L}{\partial t^f} + \frac{\partial L}{\partial \pi^{in}} \frac{d\pi^{in}}{dt^f} + \frac{\partial L}{\partial t^l} \frac{dt^l}{dt^f}. \quad (\text{A.23})$$

Now from (11), we have  $wLdt^l + wt^l dL + Fdt^f + t^f dF = 0$ , which gives

$$\frac{dt^l}{dt^f} = -\frac{F + t^f \frac{dF}{dt^f} + wt^l \frac{dL}{dt^f}}{wL}. \quad (\text{A.24})$$

Combining (A.24) and (A.23) then allows us to write

$$\frac{dt^l}{dt^f} = -\frac{F + t^f \frac{dF}{dt^f} + wt^l \left[ \frac{\partial L}{\partial t^f} + \frac{\partial L}{\partial \pi^{in}} \frac{d\pi^{in}}{dt^f} \right]}{w \left[ L + t^l \frac{\partial L}{\partial t^l} \right]}. \quad (\text{A.25})$$

Substituting (A.25) into (A.23) and multiplying by  $t^l$  then yields

$$t^l \frac{dL}{dt^f} = \frac{-t^l \frac{\partial L}{\partial t^l}}{w \left[ L + t^l \frac{\partial L}{\partial t^l} \right]} \left[ t^f \frac{dF}{dt^f} \right] + \frac{t^l}{w \left[ L + t^l \frac{\partial L}{\partial t^l} \right]} \left[ w \frac{\partial L}{\partial t^f} L - \frac{\partial L}{\partial t^l} F + wL \frac{\partial L}{\partial \pi^{in}} \frac{d\pi^{in}}{dt^f} \right]. \quad (\text{A.26})$$

Now define  $MEB \equiv \frac{-\frac{\partial L}{\partial t^l} \frac{t^l}{L}}{1 + \frac{\partial L}{\partial t^l} \frac{t^l}{L}}$ , and let  $\varepsilon_{LL}$  denote the uncompensated labour supply elasticity:  $\varepsilon_{LL} \equiv \frac{\partial L}{\partial [(1-t^l)w]} \frac{(1-t^l)w}{L} = \frac{\partial L}{\partial t^l} \frac{\partial t^l}{\partial (1-t^l)w} \frac{(1-t^l)w}{L}$ . Then  $MEB_L = \frac{\frac{t^l}{1-t^l} \varepsilon_{LL}}{1 - \frac{t^l}{1-t^l} \varepsilon_{LL}}$ , which we use in (A.26) to obtain

$$wt^l \frac{dL}{dt^f} = MEB \left[ t^f \frac{dF}{dt^f} \right] - \frac{MEB}{\partial L / \partial t^l} \left[ w \frac{\partial L}{\partial t^f} L - \frac{\partial L}{\partial t^l} F + wL \frac{\partial L}{\partial \pi^{in}} \frac{d\pi^{in}}{dt^f} \right]. \quad (\text{A.27})$$

Next consider the second term in brackets in (A.27). Then  $t^f$  and  $\pi$  only affect  $L$  through  $p^{M^{in}}$  (consider (A.21) and (A.22)). So

$$\frac{\partial L}{\partial t^f} = \frac{\partial L}{\partial p^{M^{in}}} \frac{\partial p^{M^{in}}}{\partial t^f} = \frac{\partial L}{\partial p^{M^{in}}} \alpha^F, \quad (\text{A.28})$$

and

$$\frac{\partial L}{\partial \pi^{in}} = \frac{\partial L}{\partial p^{M^{in}}} \frac{\partial p^{M^{in}}}{\partial \pi^{in}} = \frac{\partial L}{\partial p^{M^{in}}} \Gamma^{in}. \quad (\text{A.29})$$

Next, from (3),

$$\frac{d\pi^{in}}{dt^f} = \frac{\partial \pi^{in}}{\partial M^{in}} \frac{dM^{in}}{dt^f}. \quad (\text{A.30})$$

In turn,  $\frac{\partial L^c}{\partial p^{M^{in}}} = \frac{\partial L}{\partial p^{M^{in}}} + \frac{\partial L}{\partial I} \frac{\partial I}{\partial p^{M^{in}}}$ , where  $I = w(1-t^l)L$  denotes income and the superscript  $c$  denotes a compensated coefficient. Then we obtain from (A.21):

$$\frac{\partial L}{\partial p^{M^{in}}} = \frac{\partial L^c}{\partial p^{M^{in}}} - \frac{\partial L}{\partial I} M^{in}, \quad \frac{\partial L}{\partial t^l} = \frac{\partial L^c}{\partial t^l} - \frac{\partial L}{\partial I} wL. \quad (\text{A.31})$$

The Slutsky symmetry property gives  $\frac{\partial L^c}{\partial p^{M^{in}}} = -\frac{\partial M^{in,c}}{\partial (1-t^l)w}$ . Note again that  $\frac{\partial M^{in,c}}{\partial (1-t^l)w} = \frac{\partial M^{in,c}}{\partial t^l} \frac{\partial t^l}{\partial (1-t^l)w} = -\frac{\partial M^{in,c}}{\partial t^l} w^{-1}$ , so

$$\frac{\partial L^c}{\partial p^{M^{in}}} = \frac{\partial M^{in,c}}{\partial t^l} w^{-1}. \quad (\text{A.32})$$

Next, leisure is weakly separable in utility. So when  $t^l$  changes, it affects consumption and demand only through disposable income. This gives

$$\frac{\partial M^{in,c}}{\partial t^l} = \frac{\partial M^{in,c}}{\partial I} w (1-t^l) \frac{\partial L^c}{\partial t^l}, \quad (\text{A.33})$$

where  $w(1-t^l) \partial L^c / \partial t^l$  is the change in disposable income following a compensated increase in the labour tax. Then we can use (A.28)-(A.33) to find

$$w \frac{\partial L}{\partial t^f} L - \frac{\partial L}{\partial t^l} F = (\eta^{MI} - 1) \frac{\partial L^c}{\partial t^l} F, \quad (\text{A.34})$$

and

$$wL \frac{\partial L}{\partial \pi^{in}} \frac{d\pi^{in}}{dt^f} = \left[ \eta^{M^{in}I} \frac{\partial L^c}{\partial t^l} - wL \frac{\partial L}{\partial I} \right] Z^C \frac{dM^{in}}{dt^f}, \quad (\text{A.35})$$

with  $\eta^{MI} \equiv \frac{\partial M^{in,c}}{\partial I} \frac{I}{M^{in}}$ . Substituting (A.34) and (A.35) back in (A.27) then gives

$$\begin{aligned} wt^l \frac{dL}{dt^f} = MEB \left[ t^f \frac{dF}{dt^f} \right] - \frac{MEB}{\varepsilon_{LL}} \left[ \varepsilon_{LL}^c \left( \eta^{M^{in}I} - 1 \right) F \right. \\ \left. + \left[ \varepsilon_{LL} - \varepsilon_{LL}^c \left( 1 - \eta^{M^{in}I} \right) \right] Z^C \frac{dM^{in}}{dt^f} \right], \end{aligned}$$

where we use the compensated labour elasticity  $\varepsilon_{LL}^c = -\frac{\partial L^c}{\partial t^l} \frac{1-t^l}{L} = -\frac{\partial L^c}{\partial t^l} \frac{t^l}{L} \frac{1-t^l}{t^l}$ , and, from the Slutsky equation,  $\varepsilon_{LL} = \varepsilon_{LL}^c + \eta_{LI}$ . We then substitute (A.36) into (A.18) to obtain (13).

## B Parametrisation, further details

### B.1 Additional parameters

Table B.1 lists additional values used in our calculations of Equation (13), but not previously specified in Table 1.

Table B.1: Remaining parameter values

Parameter	US Central value	UK Central value
Number of active miles travelled per person per year, $M^{ac}$	267	740
Number of vehicle miles travelled per person per year, $M^{in}$	10,307	9124
Uncompensated labour supply, $\varepsilon_{LL}$	0.2	0.2
Compensated labour supply, $\varepsilon_{LL}^c$	0.35	0.35
Producer price of gasoline, $p^f$	186	186
Tax on labour, $t_L$	0.318	0.31

## B.2 Elasticities

Tables B.2, B.3 and B.4 provide an overview of the elasticity of fuel, inactive, and active miles travelled with respect to the fuel price established in the literature. These elasticities capture the extent to which fuel consumption, inactive miles travelled (VMT), and active miles travelled change in response to fuel prices. We use these values to parametrise our model as explained in Section 3.1.1. Similarly, Table B.5 lists the literature estimates for the income elasticity of inactive travel, which captures the response of inactive miles travelled to income changes.

The only direct estimate of a cross-elasticity of active modes of travel (walking and cycling) with respect to fuel price,  $\eta^{M^{ac}F}$ , we identified is a 1999 report summarising the research of several European studies (Hague Publishing et al., 1999). To our knowledge, no cross-elasticity estimates for the US exist in the literature. This poses two problems: first, the data on cross-elasticities is old, and cultural differences may mean that people’s behaviour is more (less) elastic towards other modes of travel, including bike sharing, ride-hailing services such as Uber, or electric non-active modes such as e-scooters (see e.g. Hollingsworth et al. (2019)). Second, the data is context-specific to higher density European cities.

To adjust for this gap in the literature, we additionally consider the cross-elasticity of public transport with respect to the fuel price. Although we recognise that the relationship between active travel, public transport, and car use is likely to be different in the UK and US, we use the same values of  $\eta^{M^{ac}F}$  for both countries. This is because of the limited number of studies estimating this value.

For the income elasticity of inactive travel,  $\eta^{M^{in}I}$ , we consider the following. Direct estimates of  $\eta^{M^{in}I}$  can be found in Small and Van Dender (2007), Santos and Catchesides (2005) and Fouquet (2012). Additionally, and akin to Parry and Small (2005), we consider estimates for the income elasticity of *fuel use* (Mattioli et al., 2018; West and Williams III, 2007). This approach is justified by Johansson and Schipper (1997), who found that the income elasticity of fuel use and miles travelled were approximately equal.

Table B.2: Fuel price elasticity,  $\eta^{FF}$ 

Country	Value	Range	Notes	Source
OECD	-0.3	-0.6 to -0.8	short run and long run, resp.	Graham and Glaister (2002)
UK and US	-0.55	-0.3 to -0.9		Parry and Small (2005)
US	-0.21	-0.21 to -0.75	short run	Hughes et al. (2006)
US	-0.43			Small and Van Dender (2007)
US	-0.46	-0.1		Davis and Kilian (2011)
US	-0.3			Dahl (2012)
UK	-0.33			Dahl (2012)
UK	-0.6			Fouquet (2012)
US	-0.31			Havranek et al. (2012)
Europe	-0.82		response to change in tax size	Dieler et al. (2015)
US	-0.37			Coglianesi et al. (2017)
US	-0.27	-0.27 to -0.35		Levin et al. (2017)
Denmark	-0.3	up to -0.87		Gillingham and Munk-Nielsen (2019)

Table B.3: Fuel price elasticity of inactive miles travelled (VMT),  $\eta^{M^{in}F}$ 

Country	Value	Range	Notes	Source
OECD	-0.3	-0.15 to -0.3	short run and long run, resp.	Graham and Glaister (2002)
UK and US	-0.4	0.2-0.6		Parry and Small (2005)
US	-0.1			Small and Van Dender (2007)
Germany	-0.45			Frondel and Vance (2013)
California	-0.147	0.041 to -0.288		Knittel and Sandler (2018)
Denmark	-0.32	-0.32 to -0.45		De Borger et al. (2016)
UK	-0.301	-0.1803 to -0.417		Cerruti et al. ("Charging Drivers by the Pound: How Does the UK Vehicle Tax System Affect CO <sub>2</sub> Emissions?")
US	-0.3	-0.05 to -0.3		Gillingham and Munk-Nielsen (2019)

Table B.4: Cross-elasticity of active travel and public transport (PT) use,  $\eta^{M^{ac}F}$ 

Type	Country	Value	Notes	Source
PT	Australia	0.104 to 0.291		Hensher and King (1998)
Walking and cycling	Europe	0.13		Hague Publishing et al. (1999)
PT	Europe	0.14		Hague Publishing et al. (1999)
PT - transit general	US	0.12		Currie and Phung (2007)
PT - light rail	US	0.27 to 0.38		Currie and Phung (2007)
PT - buses	US	0.04		Currie and Phung (2007)
PT	US	0.24		Haire and Machemehl (2007)
PT	US	0.4	short term	Holmgren (2007)
PT	Australia	0.22		Currie and Phung (2008)
PT	US	0.366	Upward trend in elasticities	Lane (2008)
PT	US	0.08 to 0.16	(medium-)small cities only	Mattson (2008)
PT	South Korea	0.32		Lee et al. (2009)
PT - rail, regional	US	0.27 to 0.38		Maley and Weinberger (2009)
PT - local, bus	US	0.15 to 0.23		Maley and Weinberger (2009)
PT - commuter rail	218 US cities	-0.012 to 0.213	Upward trend in elasticities 2002-2008	Blanchard (2009)
PT - light rail	218 US cities	-0.103 to 0.507	elasticities increased 2002-2008	Blanchard (2009)
PT		0.116		Iseki, Ali, et al. (2014)

Table B.5: Income elasticity of inactive travel,  $\eta^{M^{in}I}$ 

Country	Value	Range	Source
UK	0.8	0.4-1.2	Parry and Small (2005)
US	0.6	0.3-0.9	Parry and Small (2005)
UK	0.4	0.0681 to 0.6335	Santos and Catchesides (2005)
US	0.02		West and Williams III (2007)
US	0.53		Small and Van Dender (2007)
UK	0.8		Fouquet (2012)
UK high income	0.62	0.54 to 0.7	Mattioli et al. (2018)
UK low income	0.56	0.36 to 0.75	Mattioli et al. (2018)

### B.3 External cost of fuel (CO<sub>2</sub>) pollution, $Z^{P_{\bar{F}}}$

Table B.6 provides an overview of literature estimates for the social cost of carbon. We assign the greatest weight to the recent studies by Pindyck (2019) and Hänsel et al. (2020), which both rely on interviews conducted with experts in the field and their view regarding the appropriate value of the SCC.

Table B.6: Social cost of carbon estimates literature overview

USD 2017, per tonne CO <sub>2</sub>	Plausible SCC range	Source
91.8	2.6 - 367	Parry and Small (2005)
78.8	0 - 297.6	Tol (2011)
900	up to 1500	Ackerman and Stanton (2012)
49.7	14.2 - 73.3	Environmental Protection Agency (2016)
40	17 - 84	van den Bijgaart et al. (2016) and DICE as calculated by OECD (2018)
517	5274.4	Adler et al. (2017)
92.4	46.2 - 140	BEIS (2018)
41.3	25.4-157.5	Nordhaus (2018)
417	177 - 805	Ricke et al. (2018)
319.3	253.2 - 385.4	Cai and Lontzek (2019)
90	80 - 100	Pindyck (2019)
96	16.2 - 494.4	Hänsel et al. (2020)

A selection of the social cost of carbon estimates found in the literature. BEIS (2018) is a UK specific value.

To obtain the externality cost per gallon of fuel used, we need to account for the different fuel CO<sub>2</sub> emission intensities, as well as the country-specific average fuel composition. The average emissions intensity of diesel is 8.7 kgCO<sub>2</sub>/gallon, and 10.1 kgCO<sub>2</sub>/gallon for gasoline. The US fuel mix is 98.5%

gasoline, while the UK fuel mix is 55% gasoline and 45% diesel. Using a central value for the social cost of carbon of 90 \$/tCO<sub>2</sub>, and a low (high) value of 40 (400) \$/tCO<sub>2</sub>, we obtain the estimates for  $Z^{P\bar{F}}$  as specified in Table 1.

#### B.4 Marginal value of health through active travel $Z^Q$ (HEAT)

To determine the marginal value of health through active travel increases,  $Z^Q$ , we use estimates from the WHO Health Economic Assessment Tool (HEAT). HEAT is an open-access online tool for conducting economic assessments of active transport (changes) and their impact on health benefits from physical activity, air pollution, accidents, and effects on carbon emissions.<sup>25</sup> Importantly, the tool relies on international expert consensus and the methodology is regularly updated to reflect new research evidence and data. The tool can be used for cost-benefit analysis, and requires inputs on baseline levels of active travel, the assessed change in active travel, the time needed to achieve those changes, as well as assumptions regarding substitution away from other forms of exercise. Other (optional) inputs are the discount rate, the value of statistical life (VSL), and the source the information supplied to the model comes from (count data, population survey, modelled data, hypothetical scenario). In its computations, HEAT assumes a linear relationship between active travel increases and health benefits. More details can be found in Section 3.4 of Kahlmeier et al. (2017).<sup>26</sup>

While the tool is not designed for use outside of Europe,<sup>27</sup> it has been applied to US settings. Examples are Colorado (BBC Consulting, 2017), Arkansas (BBC Consulting, 2018) and Boston (James et al., 2014). We

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<sup>25</sup>The tool is available on [www.heatwalkingcycling.org](http://www.heatwalkingcycling.org).

<sup>26</sup>Discussions of the strengths and limitations of HEAT, and the best methods for economic evaluations of active travel, can be found in Fishman et al. (2015) and Deenihan and Caulfield (2014).

<sup>27</sup>US cities are less dense and have too small shares of walking and cycling (about 0.2% of total travel) to make a country-wide assessment about the impact of active travel on health. Conversely, Asian cities, though often high-density, have such elevated levels of air pollution exposure that the physical activity relative risk reduction coefficients HEAT uses are not appropriate.

therefore used HEAT for both the UK and the US, and used country-specific values to calibrate the model.

Further details regarding the data inputs we used are given below. Baseline average levels of walking and cycling of 4.8 and 1.2 minutes per day in the UK, and 5.6 and 0.4 for the US. We consider an increase of 5 minutes of activity per person per day for the population aged 20-74, split between the walking and cycling according to current proportions of the two modes. We assume changes materialize over a three year adjustment period, and denote an average of lives saved per year over a 10 year period as our outcome variable of interest. We use 2017 population data from Murphy et al. (2018) for the US, and Patel (2017) for the UK. HEAT requires the user to specify the degree to which increases in active travel crowd out other forms of activity. As evidence suggests that exercise through active travel is additive, rather than crowding out other forms of exercise (Foley et al., 2015; Laeremans et al., 2017; Dons et al., 2018; Castro et al., 2019), we assume that all increases in physical activity are additional. Finally, we maintain the HEAT default parameter values for “mortality relative risk reductions” associated with walking (0.89) and cycling (0.90), which affect the number of lives saved due to a given increase in active travel.

HEAT focuses on mortality reductions due to active travel. A more accurate representation of the health effects of active travel would also account for quality of life effects. Adopting a healthy lifestyle can, for instance, increase the disease-free lifetime of an adult by up to 10 years (“Healthy lifestyle and life expectancy free of cancer, cardiovascular disease, and type 2 diabetes: prospective cohort study”). As HEAT does not include such benefits, we consider it a conservative estimate of the overall health benefits of active travel per mile travelled.

The main output from HEAT is the number of deaths saved through the specified increase in active travel. We use the VSL, which reflects the value society places on a life and is commonly used in cost-benefit analyses, to convert these lives saved to \$ amounts. The central value of VSL used for the US is \$9.26 million, with a range of \$5.4m-13.4 million (Moran and Monje,



2016). The central value of VSL for the UK is more conservative, \$4.36 million (WHO 2015), with a range of \$2.2m-12.6 million (Thomas, 2020). HEAT assumes a linear relationship between exercise and health benefits for sedentary societies (Kahlmeier et al., 2017). This approach gives the value of the total number of lives saved due to an increase in active travel by 5 minutes. We finally convert this value to the value of health gained per additional mile of active travel, by dividing by the total increase in active travel, assuming a speed of 15 minutes per mile. This gives a central value of  $Z^Q$  of \$6.91 for the US, and \$2.44 for the UK.

## B.5 Obtaining the numerical results

Our quantification of the optimal fuel tax takes into account that the fuel consumption  $F$  and miles travelled  $M^{in}$  and  $M^{ac}$  depend on the fuel tax level. In other words, we approximate  $Z/F$  in (14) by

$$\frac{Y}{F} = \frac{Z^0}{F^0} \left( \frac{p^f + t_1^{f*}}{p^f + t^{f0}} \right)^{\eta^{ZF} - \eta^{FF}},$$

with  $Y \in \{M^{in}, M^{ac}\}$ , and where  $t^{f0}$  and  $Y^0$  denote the baseline level of  $t^f$  and  $Y$ .<sup>28</sup> We take labour supply  $L$  and labour taxes  $t^l$  as constant throughout the quantification. While through Equations (10) and (11), changes in time spent travelling and fuel tax revenues may affect labour supply and taxes, this effect is likely minor, and abstracting from this interaction substantially simplifies computations.

## B.6 Quantifying welfare effects

We follow Parry and Small (2005) and Parry and Small (2004) to obtain a formula for the welfare gain of a marginal tax increase. First, we use the

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<sup>28</sup>See also Parry and Small (2005).

definitions for  $Z$  to rewrite (A.16) as

$$\begin{aligned} \frac{1}{\mu_I} \frac{dV}{dt^f} = & [Z^{P_{\bar{F}}} - t^f] \frac{-dF}{dt^f} + [Z^C + Z^{A_{\bar{M}^{in}}} + Z^{P_{\bar{M}^{in}}}] \frac{-dM^{in}}{dt^f} + \\ & [Z^{A_{\bar{M}^{ac}}} - (1 - \omega) \tilde{Z}^Q] \frac{-dM^{ac}}{dt^f} - (1 - \omega) \tilde{Z}^Q \frac{-dQ}{dt^f} - wt^l \frac{-dL}{dt^f}. \end{aligned}$$

Next, assuming that the effect of  $t^f$  on  $Q$  runs through  $M^{ac}$  alone, we can write

$$\begin{aligned} \frac{1}{\mu_I} \frac{dV}{dt^f} = & [Z^{P_{\bar{M}^{in}}} - t^f] \frac{-dF}{dt^f} + [Z^C + Z^{A_{\bar{M}^{in}}} + Z^{P_{\bar{M}^{in}}}] \frac{-dM^{in}}{dt^f} + \\ & [Z^{A_{\bar{M}^{ac}}} - (1 - \omega) Z^Q] \frac{-dM^{ac}}{dt^f} - wt^l \frac{-dL}{dt^f}. \end{aligned}$$

Now use the definitions of  $\eta^{FF} \equiv \frac{dF}{dp_F} \frac{p_F}{F}$ ,  $\eta^{M^{in}F} \equiv \frac{dM^{in}}{dp_F} \frac{p_F}{M^{in}}$ ,  $\eta^{M^{ac}F} \equiv \frac{dM^{ac}}{dp_F} \frac{p_F}{M^{ac}}$ ,  $\beta^{M^{in}} = \eta^{M^{in}F}/\eta^{FF}$  and  $\beta^{M^{ac}} = \eta^{M^{ac}F}/\eta^{FF}$ . Then  $\frac{-dF}{dt^f} = -\frac{dF}{dp_F} \frac{p_F}{F} \frac{F}{p_F} = -\eta_{FF} \frac{F}{p_F}$  and, using a similar approach for  $\frac{-dM^{in}}{dt^f}$ , we can write

$$\begin{aligned} \frac{1}{\mu_I} \frac{dV}{dt^f} = & [Z^{P_{\bar{M}^{in}}} - t^f] \left( -\eta^{FF} \frac{F}{p^f + t^f} \right) \\ & + [Z^C + Z^{A_{\bar{M}^{in}}} + Z^{P_{\bar{M}^{in}}}] \left( -\eta^{M^{in}F} \frac{M^{in}}{p^f + t^f} \right) \\ & + [Z^{A_{\bar{M}^{ac}}} - (1 - \omega) Z^Q] \left( -\eta^{M^{ac}F} \frac{M^{ac}}{p^f + t^f} \right) - wt^l \frac{-dL}{dt^f}. \end{aligned}$$

Next use (14) to find

$$\frac{1}{\mu_I} \frac{dV}{dt^f} = [MEC - t^f] \left( -\frac{F\eta^{FF}}{p^f + t^f} \right) + wt^l \frac{dL}{dt^f}. \quad (\text{B.1})$$

Note that in Parry and Small (2005), wages  $w$  are normalised to 1. In addition, the (negative) value of  $\eta^{FF}$  is expressed in absolute terms. Finally, they define  $p^F$  as the tax-inclusive fuel price, which in our setting is given by  $p^f + t^f$ . In sum, this means that Equation (D1) in Parry and Small (2004) and (B.1) and all subsequent expressions in the derivations are equivalent solutions.

Finally, further substitutions along the lines suggested in Appendix D in

Parry and Small (2004) allow us to further rewrite (B.1), as

$$\frac{1}{\mu_I} \frac{dV}{dt^f} = \left( -\frac{F\eta^{ff}}{p^f + t^f} \right) (1 + MEB_L) [t^{f*} - t^f] .$$

## B.7 Quantifying changes in mortality

To quantify the number of lives lost or gained as discussed in Section 4, we used HEAT and followed instructions by Kahlmeier et al. (2017). We parameterise HEAT as described in Section B.4. Further conditions that were specifically calibrated to the US and UK contexts are listed in Table B.7 below.

Table B.7: Country-specific HEAT inputs into welfare change analysis

Input	US		UK	
	Value	Source	Value	Source
Traffic conditions	35km/h	HEAT def., some congestion	32km/h	HEAT def., EU av.
Air quality, PM <sub>2.5</sub> $\mu\text{g}/\text{m}^3$	7.5	EPA (2017)	10.5	HEAT def., UK av.
Fatalities/100m km, walking	4.7	Buehler and Pucher (2017)	2.2945	HEAT def., UK av.
Fatalities/100m km, cycling	9.7	Buehler and Pucher (2017)	2.1377	HEAT def., UK av.

Additional inputs that calibrate the calculations HEAT does to the context of the US and UK. Values labelled “HEAT def.” are default values provided by the HEAT tool and are average values that apply specifically to the UK or European context.

HEAT provides risk-specific mortality changes, which we aggregated in to a single value in the main text. Table B.8 shows the disaggregation of this value for the change from the current tax levels to the second-best optimal fuel tax levels for both countries.

Table B.8: Country and cause-specific mortality changes, as provided by HEAT

Cause of death	US	UK
	Value	Value
Physical activity	-6457	-40
Air pollution exposure	83	0.9
Crash risk	108	0.3

Number of lives gained (negative value) or lost (positive value) per country per year, following a change from current to second-best optimal fuel tax levels,  $t^f$ .

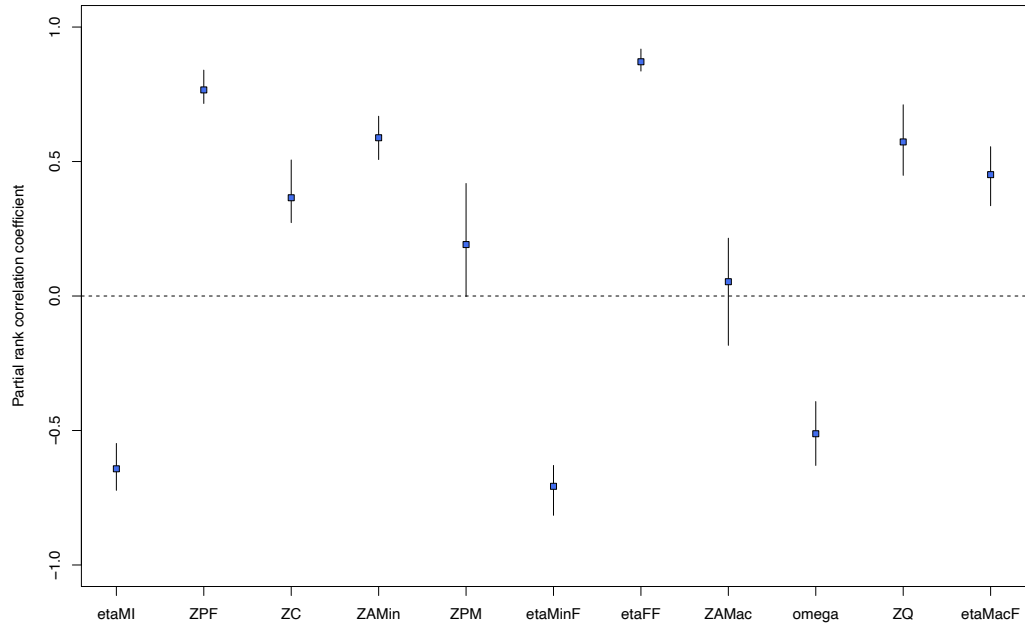
## B.8 Sensitivity analysis

The sensitivity analysis was done by applying Latin Hypercube algorithms, implemented by the *pse* package in R (Chalom and de Prado, 2015). Latin Hypercube sampling is a method of parameter space exploration and optimisation, and is described in more detail (and compared against other methods, such as individual parameter disturbance and Monte Carlo) in Chalom and de Prado (2015). The results are depicted in Figure 3, which specifies the probabilities that the second-best optimal fuel taxes lie below a pre-specified value.

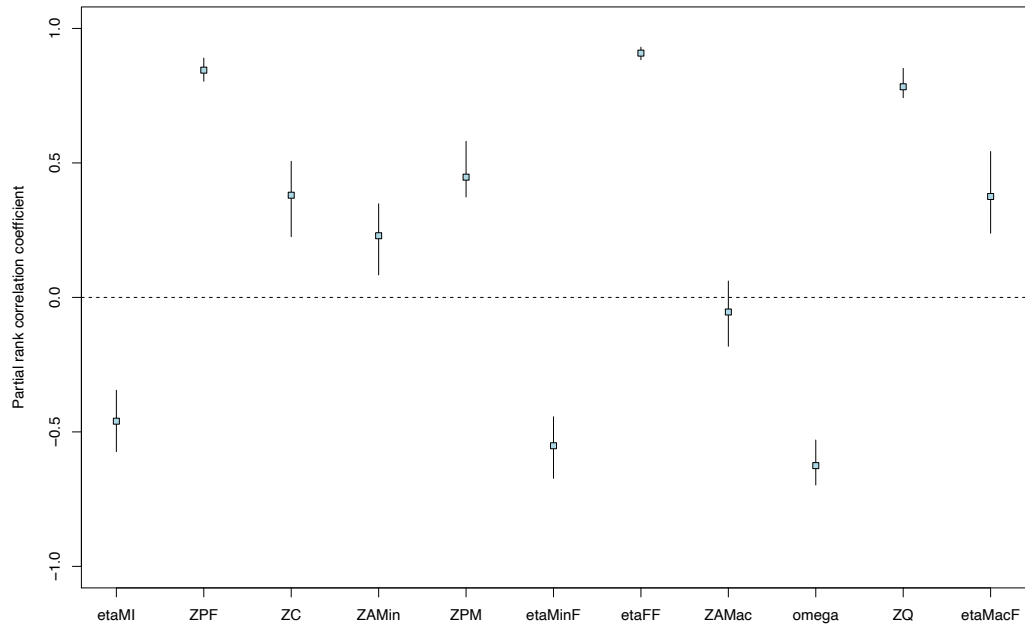
Figures B.1a and B.1b additionally show the relative influence of each parameter on the optimal fuel tax. More specifically, each Figure shows the partial rank correlation coefficient, defined as the effect of changing one parameter, *ceteris paribus*, relative to changing any other parameter, *ceteris paribus*, on the fuel tax. A negative value means that a larger parameter value reduces the size of the optimal fuel tax, and vice versa. From the figure, the external cost of CO<sub>2</sub>,  $Z^{P\bar{F}}$  and the fuel price elasticity,  $\eta^{FF}$  have the greatest effect on the optimal tax, both for the US and the UK. The effect of the external cost of accidents is comparatively small.

Regarding social costs, the fuel tax is most sensitive to  $Z^{P\bar{F}}$ , fuel pollution, i.e. the social cost of carbon. This is attributed to the fact that  $Z^{P\bar{F}}$  has a very high right-hand tail, which follows from high estimates for the social cost of carbon under a business-as-usual scenario for global carbon emissions in the relevant literature (see also Table B.6 in Appendix B.3). Increasing  $Z^{P\bar{F}}$  to this upper bound increases the optimal fuel taxes by more than \$4/gal for both the UK and US. We find a similar sensitivity of the fuel tax to the calibration of  $Z^{A\bar{M}in}$  for the US, while the UK fuel tax increases by only a little when moving from the central value to the upper bound for  $Z^{A\bar{M}in}$ .

Finally, the fuel tax shows similarly strong sensitivity to the remaining social cost parameters, with the exception of active accident costs,  $Z^{A\bar{M}ac}$ . Higher social costs  $Z^Q$ ,  $Z^{P\bar{M}in}$  and  $Z^C$  result in higher levels of optimal fuel taxation, with the upper (lower) bound increasing the optimal fuel tax by around \$1.50-2.50/gal.



(a) PRCC plot for the US.



(b) PRCC plot for the UK.

Figure B.1: Partial rank correlation coefficient (PRCC) plots showing the relative influence of each parameter on the optimal fuel tax, obtained using Latin Hypercube sensitivity analysis.

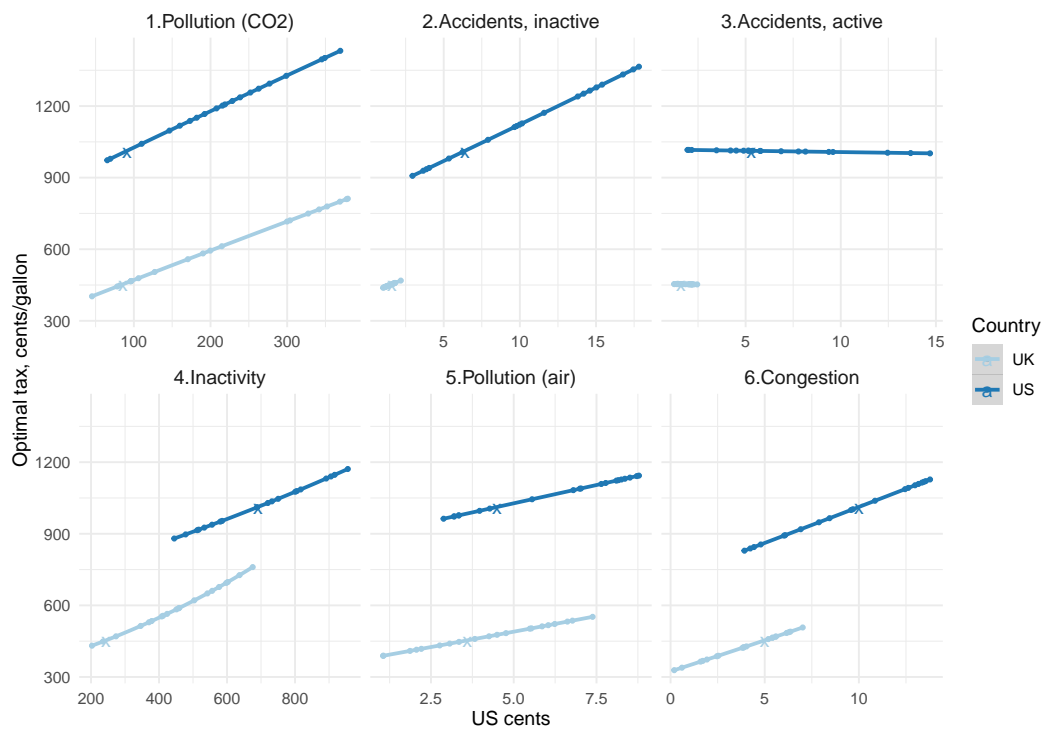


Figure B.2: The sensitivity of the fuel tax to the social cost parameters.

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