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Environmental efficiency measurement when producers control pollutants under heterogeneous conditions: A generalization of the materials balance approach

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Environmental efficiency measurement when producers control pollutants under heterogeneous conditions: a generalization of the materials balance approach

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Abstract

This article provides a generalization of the materials balance-based production model introduced by Coelli et al. (2007). Based on this, some new environmental efficiency (EE) measures are presented. The Coelli et al. (2007) EE measure and its extension by Rødseth (2016) produce biased efficiency estimates if the material flow coefficients (MFCs) are heterogeneous across decision-making units and non-discretionary. Furthermore, the Coelli et al. (2007) measure fails to reward emission reductions by emission control. To overcome these shortcomings, this paper proposes production models which allow for heterogeneous MFCs reflecting differences of external environmental factors or non-controllable heterogeneities in inputs and outputs, and which properly take into account emission abatement activities. Based on this, we provide new EE measures and decompose them into i) a part reflecting emission control efficiency (ECE), ii) a part measuring material input efficiency (MIE), and iii) a part reflecting the efficient allocation between material and non-material inputs (environmental allocative efficiency, EAE). The approach is illustrated by an empirical application to arable farming in Austria utilizing data from 90 farms for the year 2011. Soil erosion is considered an undesirable output and land a material input. The average EE, ECE, MIE, and EAE are 0.53, 0.96, 0.69, and 0.79, respectively. The results indicate that actual output can be potentially achieved with 47% less soil loss. Most of the potential to improve EE is due to differences in MIE and EAE. Removing inefficiencies in the implementation of existing, subsidized erosion controls allows soil loss to be reduced by 4%.

Keywords: Emission-generating technologies, Materials balance condition, Weak-G disposability, Data envelopment analysis, Non-discretionary factors, Soil erosion, Crop farms

JEL Classification C61, D24, Q12, Q15

1 Introduction

Multiple approaches to incorporate environmental perspectives into productivity and efficiency analysis exist (see Dakpo et al. 2016 for a survey of the literature): i) Färe et al. (1986, 1989) were the first to introduce undesirable outputs (bad outputs) into an empirical production model, allowing for inefficiencies. They treat bad outputs as weakly disposable outputs; ii) Hailu and Veeman (2001) model bad outputs as strongly disposable inputs; iii) Lovell et al. (1995) and Seiford and Zhu (2002) transform bad outputs and model the transformed values as strongly disposable outputs; iv) the eco-efficiency approach by Kuosmanen and Kortelainen (2005) ignores inputs and only considers good and bad outputs; v) recently, the by-production approach that models polluting technology as the intersection of multiple sub-technologies has been introduced (Murty et al. 2012) and extended (Serra et al. 2014; Dakpo 2016; Ray et al.

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2018; Lei 2020), and its application has gained popularity (see e.g., Dakpo et al. 2017; Ait Sidhoum et al. 2020).²

All these approaches have been criticized for various reasons (see, e.g., Färe and Grosskopf 2004; Førsund 2009; Dakpo et al. 2016; Førsund 2018; Hampf, 2018). The most widely applied approaches, for example, i) and ii), are criticized for not complying with physical laws (i.e., the materials balance principle, law of mass conservation, or first law of thermodynamics) and for allowing for physically impossible production possibilities (Färe and Grosskopf 2003; Coelli et al. 2007; Førsund 2009; Hoang and Coelli 2011; Podinovski and Kuosmanen 2011; Rødseth 2017). To overcome this problem, Coelli et al. (2007) and Rødseth (2017) introduced production models that insure consistency with the materials balance principle. These models rely on the materials balance equation (MBE), an accounting identity that describes the relationship between potentially polluting by-products (residuals) of a production process, the amount of inputs used, and the amount of good outputs produced. Residuals (i.e., pollutants or bad outputs), inputs and good outputs are linked by material flow coefficients (MFCs) such that the amount of materials tied up in the inputs must equal the amount of the flow of materials embedded in intended outputs plus residuals.

Due to non-homogeneity in inputs and outputs and the role of some external factors, the MFCs may differ from one decision-making unit (DMU) to another (Dakpo et al. 2016). Although the MBE-based models have been applied in numerous efficiency analyses, especially in agriculture (see e.g., Hoang and Rao 2010; Hoang and Coelli 2011; Hoang and Alauddin 2012; Nguyen et al. 2012; Hoang and Nguyen 2013) and energy generation (see e.g., Welch and Barnum 2009; Hampf and Rødseth 2015, 2017, 2019), heterogeneous MFCs have received little attention in the literature. An exception is Hampf and Rødseth (2019). Their model accommodates heterogeneous MFCs that reflect differences in input qualities across DMUs. They assume that the input quality can be freely chosen by DMUs and, as such, the MFCs are considered controllable.

This article extends the Coelli et al. (2007) model and the weak G-disposability technology introduced by Rødseth (2017), allowing for heterogeneous MFCs which reflect differences of some non-discretionary, environmental/external factors. These models can also be applied to situations where input and output quality is heterogeneous across DMUs but non-controllable (i.e., input or output quality switching, such as fuel switching from coal to gas is not possible). Contrary to that of Rødseth (2019), the approach presented in this article accounts for emission abatement activities that require the use of additional inputs. While network technologies (see e.g., Färe et al. 2013; Hampf 2014; Lozano 2015; Bostian et al. 2016, 2019; Bi et al. 2018;) separately model the production and the abatement stages, our approach models the amount of abated emission as strongly disposable output together with all other inputs and outputs in a single stage. Inputs are jointly consumed by desirable output production and emission control. Hence, the procedure does not require information on the amount of inputs devoted to each of these processes.

Based on these extended production models, environmental efficiency (EE) measures are proposed that reward emission reductions from emission control. The presented procedure is a generalization of the MBE-based approach introduced by Coelli et al. (2007). It is shown that the Coelli et al. (2007) measure is a special case of the EE measures proposed here. The EE

² Multi-equation modelling of good and bad outputs was also established by Førsund (2009, 2018) building on the ideas of Frisch (1965).

³ The materials balance principle was introduced by Ayres and Kneese (1969) and Kneese et al. (1970) in the economic literature but, according to Pethig (2003), has been stepmotherly treated therein.

measures are decomposed into three components that reveal the sources of inefficiencies with regard to emission generation. Taking the production of desirable outputs as given, the components reflect inefficiencies associated with i) too low of an amount of abated emission for the given amount of inputs used, ii) too much usage and misallocation of polluting inputs, and iii) an unfavorable allocation between polluting and non-pollution inputs.

The approach is illustrated by an empirical application to arable farming using data from 90 Austrian crop farms for the year 2011, and considering soil erosion as an unintended, potentially polluting by-product that should be minimized. Soil erosion results from energy transmitted from wind or rainfall and leads to the loss of topsoil and soil organic matter, which are essential for plant growth. Soil erosion is the most important cause of soil degradation, which is recognized as one of the most pressing problems facing humanity (Young et al. 2015) and a serious threat to sustainable development as envisaged in the European Union (EU) Sustainable Development Strategy (EC 2001) and the Sustainable Development Goals of the United Nations (Griggs et al. 2013; Keesstra et al. 2018). The private and social costs of soil erosion are considerable, including reduced soil productivity and off-site effects, such as sedimentation, flooding, landslides, and water eutrophication (Pimentel et al. 1995; Adhikari and Nadella 2011; Graves 2015; Panagos et al. 2018). Clearly, agriculture plays a key role, as agricultural land accounts for 68.3% of total soil loss in Europe (Panagos et al. 2015c).

Besides farmers' land use and management decisions, including crop choice and applied erosion control measures, the degree of soil loss mainly depends on exogenous environmental (non-discretionary) factors, such as rainfall quantity and intensity, soil texture and structure, and slope gradient and length. To the best of my knowledge, attempts to consider soil erosion as undesirable output in empirical production models are restricted to frontier eco-efficiency studies (see Picazo-Tadeo et al. 2012a, 2012b, 2014; Eder et al. 2021) in the mode of Kuosmanen and Kortelainen (2005), an approach that completely ignores inputs and fails to capture all the input substitution possibilities that could help to optimize environmental performance (Dakpo et al., 2016). Hence, this is the first study modeling soil erosion as an undesirable output within a production theoretical framework that simultaneously accounts for inputs, desirable outputs, and undesirable outputs.

2 Background

The MBE introduced in the economic literature by Ayers and Kneese (1969) is a simplified form of the first law of thermodynamics and states that during a production process material cannot disappear. A general discussion and justification for incorporating the MBE in production analysis can be found in Lauwers (2009). Using empirical data as well as results from Monte Carlo simulations, Hampf (2018) finds that ignoring the physical restrictions imposed by the MBE when estimating technology sets, leads to seriously biased efficiency results. Moreover, the same study also shows that, even in the case of misspecifications, models based on the MBE outperform models which ignore the physical restrictions.

production activity causes the emission of potentially polluting substances as a by-product. The amount of emissions is defined by the MBE:

$$b^{uc} = ux - vy. (1)$$

Eq. (1) represents uncontrolled emissions, where $u \in \mathbb{R}$ and $v \in \mathbb{R}$ are vectors of known non-negative constants representing the MFCs of inputs and desirable outputs. Material inputs (i.e., polluting inputs) have MFCs that are positive and non-material inputs (i.e., non-polluting inputs) are associated with MFCs that are zero. If desirable outputs are taken as given, emissions can be reduced by using fewer material inputs or by substituting polluting with non- or less-polluting inputs. Another strategy to reduce uncontrolled emissions is the use of emission abatement activities that require the use of additional inputs. This is formalized by Eq. (2) as follows:

$$b^c = ux - vy - a. (2)$$

Eq. (2) represents controlled emissions, that is, the amount of uncontrolled emissions reduced by emission control. The abatement output $a \in \mathbb{R}$ is the amount of emission avoided by emission control. Eq. (2) is linear in inputs and outputs, but one can also formulate a non-linear relationship (Pethig, 2006).

Coelli et al. (2007) consider the output vector y as fixed and minimize the uncontrolled emission in Eq. (1) by choosing the optimal input vector x subject to a traditional production technology. The model insures that the MBE is satisfied by considering Eq. (1) explicitly as the target function of the optimization problem. However, the model by Coelli et al. (2007) ignores emission abatement activities that usually require the use of additional inputs. Hence, the EE measure proposed by Coelli et al. (2007) provides biased efficiency rankings if emission control is a common compliance strategy (cf. Rødseth, 2016).

To overcome this problem, Rødseth (2016) proposes a new EE measure that rewards emission reductions by emission control and shows that the new efficiency measure coincides with Coelli et al.'s (2007) efficiency measure if none of the considered DMUs control emissions and the MFCs of the desirable outputs are zero. Contrary to the initial approach of Coelli et al. (2007), which considers the MBE as the objective function of a minimization problem, Rødseth (2016) imposes a set of axioms on the production technology to insure that the MBE shown in Eq. (2) holds for all production points within the production possibility set (PPS). This weak G-disposability technology is described and compared with other modeling approaches of production technologies in Rødseth (2017). The weak G-disposability technology allows the specification of a production model that includes controlled emissions as undesirable outputs.

If emission control is a common compliance strategy, an alternative to Rødseth's (2016) approach is to modify the traditional production technology by introducing an extra "abatement output" variable and to minimize Eq. (2) by choosing the optimal abatement output a and the optimal input vector x, subject to the modified technology. As emphasized by Coelli et al. (2007), the abatement output would be a good output variable, not a bad output variable.⁴ Although this procedure is proposed by Coelli et al. (2007), this article is the first that formalizes and applies this approach and derives a corresponding, new measure of EE. In addition, the new

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⁴ Note that this extension of the model by Coelli et al. (2007) requires exactly the same data as the model by Rødseth (2016). If the controlled emissions, inputs, outputs, and the MFCs are known, the abatement output can be calculated by using Eq. (2).

measure of EE is compared with the measure developed by Rødseth (2016), and it is shown that the two measures coincide under quite general conditions.

Table 1 Review of MBE-based models

Model	With emission control	MFCs heterogeneous across DMUs	MFCs controllable
Coelli et al. (2007)	no	no	no
Rødseth (2016)	yes	no	no
Hampf and Rødseth (2019)	no	yes	yes
The new models in this article	yes	yes	no

MBE: materials balance equation; MFCs: material flow coefficients.

Table 1 provides an overview of MBE-based production models and their features. Until recently, heterogeneous MFCs have received little attention in the literature. The approach of Coelli et al. (2007) and Rødseth (2016) were originally applied to situations where MFCs are homogeneous across all DMUs. Welch and Barnum (2009) apply the model of Coelli et al. (2007) to electricity generation and maintain the assumption of homogeneous MFCs. Nguyen et al. (2012) uses the approach of Coelli et al. (2007) to measure the nutrient use efficiency of South Korean rice farms and apply heterogeneous MFCs reflecting differences in the eutrofying power of fertilizers across DMUs. However, the consequences for EE measurement when comparing farms which use fertilizers with different nutrient content are not discussed.⁵

Hampf and Rødseth (2019) are the first to explore the consequences of heterogeneous MFCs for EE measurement. Differences in MFCs across DMUs are interpreted as differences in input qualities. They find that failing to control for this heterogeneity leads to performance measurement errors, that is, input quality differences are confused with technical inefficiency. Also, they develop a production model that accounts for heterogeneous MFCs. Based on this model, a measure of EE is proposed that is decomposed into a part reflecting input quality and a part reflecting technical efficiency. This approach is applied to evaluate the EE of coal-fired power plants in the United States using a panel dataset covering the years 1997 to 2015. Carbon dioxide (CO₂) and sulfur dioxide (SO₂) are considered undesirable outputs. The power plants use different qualities of coal with varying sulfur and carbon contents, which are captured by heterogeneous MFCs. It is assumed that DMUs can switch among inputs of different quality (coal types), and choosing a suboptimal input (coal) quality is reflected by a lower EE. However, fuel switching is not always possible. For instance, the decision on which type of coal is used depends on the location of the power plant, transportation costs, and the sulfur content of coal. These factors are likely to be uncontrollable by the power plant operators. When evaluating the EE of power plants that use even more heterogeneous types of fuel, for example, coal and gas (cf. Welch and Barnum 2009), the assumption that fuel switching is feasible is even more questionable. A coal boiler is usually designed to burn coal, not natural gas. Even if a coal plant were modified to accept natural gas, the resultant fuel efficiency would be low and production costs would remain elevated.

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⁵ If switching from urea fertilizers to complex fertilizers is constrained by manure management, the estimated potentials to reduce the eutrofying power of the farms are seriously overestimated. Furthermore, technical efficiency variations are mixed up with differences in fertilizer quality.

In addition, there are situations where heterogeneous MFCs do not result from differences in input quality, but rather reflect heterogeneous environmental factors, also known as non-discretionary variables or Z-variables (cf. Ruggiero 1998), which govern the transformation of inputs into good and bad outputs. For instance, consider the use of arable land to produce agricultural commodities. The usage of arable land in the production process inevitably causes soil erosion by water and wind. Soil erosion is an unintended by-product of agricultural production that causes private and social costs, including reduced soil productivity and off-site effects such as sedimentation, flooding, landslides, and water eutrophication (cf. Pimentel et al., 1995; Adhikari and Nadella, 2011; Graves, 2015; Panagos et al., 2018). However, the degree of soil loss depends on exogenous environmental factors, such as rainfall quantity and intensity, soil texture and structure, and slope gradient and length.⁶

The examples given above describe production processes where the MFCs are heterogeneous across DMUs but uncontrollable by the operators, at least to a certain extent. Assuming that MFCs are controllable in such situations leads to biased efficiency estimates, and inefficiencies are confused with non-discretionary factors. To account for this, the production models presented in this study extend the approach of Coelli et al. (2007) and Rødseth (2016) to account for heterogeneous and non-discretionary MFCs. In contrast to Hampf and Rødseth (2019), focusing on uncontrolled emissions, the new models allow for emission control and the substitution of polluting inputs with non-polluting inputs. Based on these models, conditional data envelopment analysis (DEA) estimators of EE are proposed that control for environmental factors influencing the production of the bad output. This is achieved by introducing conditional technology sets that depend on non-discretionary factors and restrict the reference set of the DMUs under evaluation to DMUs that face comparable environments (cf. Ruggiero 1996, 1998). The procedure guarantees that differences in EE are not confused with differences in non-discretionary factors.

To put it differently, the proposed EE measures evaluate a DMU's potential to reduce its controlled emission given its production of desirable outputs. The measures are decomposed into three parts, which assess the contribution of different emission abatement strategies to the overall emission reduction potential: i) emission reductions for given inputs and desirable outputs, which reflect the emission control performance of a DMU (emission control efficiency); ii) emission reductions by reducing and reallocating material inputs (material input efficiency); and iii) emission reductions by substituting material inputs with non-material inputs (environmental allocative efficiency).

3 Methodology

This section presents two approaches for theoretical modeling and estimating the production technology as well as measuring the EE of DMUs that control emissions and have homogeneous MFCs. The first approach extends the Coelli et al. (2007) production model by an abatement output, and the second approach was introduced by Hampf and Rodseth (2015) and Rødseth (2016, 2017). These two approaches deliver identical solutions under quite general conditions. We can exploit this useful property for EE measurement of DMUs with heterogeneous and non-

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⁶ In addition, the extent of soil loss is also determined by farmers' land use and management decisions. In particular, appropriate crop choice and erosion control measures can reduce soil erosion rates (Pimentel et al., 1995; Panagos et al., 2015a; Panagos et al., 2015b).

⁷ In the case of soil erosion, arable land can be considered as the single material input, and the MFC of arable land represents the farm-specific uncontrolled soil loss in t/ha per year. The material content and the MFCs of other inputs and outputs are zero (see section 3.2).

discretionary MFCs. In addition, I discuss the consequences of uncontrollable differences in MFCs across DMUs for the production possibilities and demonstrate how EE can be evaluated and decomposed in such situations.

Throughout this section, it is assumed that we observe i=1,2,...,N DMUs that produce a vector of m=1,2,...,M desirable outputs, $y_i \in \mathbb{R}$ using a vector of k=1,2,...,K inputs, $x_i \in \mathbb{R}$. The input vector is partitioned into a sub-vector of S material inputs, $x_i^P \in \mathbb{R}$, and a sub-vector of K-S non-material inputs, $x_i^{NP} \in \mathbb{R}$. The DMUs control emissions, where $a_i \in \mathbb{R}$ is the amount of prevented emission by emission control (i.e., a desirable output) and $b_i^c \in \mathbb{R}$ is the controlled emission (i.e., an undesirable output).

3.1 Production with homogeneous MFCs

3.1.1 Modeling and estimating the production technology

Consider a traditional production technology which is extended by an abatement output (desirable output) $a \in \mathbb{R}$, ignoring the controlled emission (undesirable output) $b^c \in \mathbb{R}$:

$$T_1 = \{\langle x, y, a \rangle \in \mathbb{R} \quad can \ produce(y, a) \}.$$
 (3)

For estimating T_1 from empirical data, it is assumed that the input vector x can be employed both to desirable output production and emission control activities. Furthermore, the standard axioms of a neo-classical production model are assumed to hold. In particular, outputs are assumed to be freely disposable, which means that an increase, for example, in the abatement output takes place at the expense of at least one other output when the production is efficient.

Next, consider a traditional production technology that is extended by a controlled emission (undesirable output) $b^c \in \mathbb{R}$, ignoring the abatement output (desirable output) $a \in \mathbb{R}$:

$$T_2(=\{\langle x, y, b^c \rangle \in \mathbb{R} \quad can \, produce(y, b^c)\}. \tag{4}$$

To estimate T_2 from empirical data, Rødseth (2017) introduces the weak-G disposability technology assuming that T_2 is a non-empty, closed, convex set that is bounded from above and that there is no free lunch. In addition to these standard axioms of neoclassical production technologies, three further axioms are assumed to hold: i) input essentiality, ii) output essentiality, and iii) weak-G disposability. The essentiality axioms state that polluting inputs cannot completely be transformed into good outputs, and thus, the use of polluting inputs inevitably results in the production of polluting by-products. In addition, these pollutants can only result from the production process if polluting inputs are used. The weak-G disposability axiom guarantees that the disposal of inputs and outputs takes place according to the MBE.

⁸ Note that the model presented in this article considers only one undesirable output. However, the approach can be generalized to multiple bad outputs following the procedure outlined in Coelli et al. (2007).

 $^{^9}$ T_1 is a non-empty, closed, and convex set that is bounded from above (output boundedness). There is no free lunch, and inputs and outputs are freely disposable. For details see, for example, Färe and Primont (1995).

To estimate T_1 and T_2 , the nonparametric DEA estimator by Banker et al. (1984) and Hampf and Rødseth (2015) is applied, respectively. In contrast to parametric methods, DEA does not impose a specific functional form on the technology set, but estimates a piecewise-linear approximation of the technology frontier based on the above defined axioms. The DEA estimator for T_1 is defined as:

$$\hat{T}_{1} = \begin{cases}
\langle x, y, a \rangle \in \mathbb{R} & {}^{k} = \sum_{i=1}^{N} \lambda_{i} x_{i}^{k} + \varepsilon_{x^{k}}, k = 1, ..., K; \\
y^{m} = \sum_{i=1}^{N} \lambda_{i} y_{i}^{m} - \varepsilon_{y^{m}}, m = 1, ..., M; a = \sum_{i=1}^{N} \lambda_{i} a_{i} - \varepsilon_{a}; \\
\sum_{i=1}^{N} \lambda_{i} = 1; \lambda_{i}, \varepsilon_{x^{k}}, \varepsilon_{y^{m}}, \varepsilon_{a} \geq 0, \forall i, k, m
\end{cases}$$
(5)

The DEA estimator for T_2 is given by:

$$\hat{T}_{2} = \begin{cases}
\langle x, y, b^{c} \rangle \in \mathbb{R} & \stackrel{i}{=} \sum_{i=1}^{N} \lambda_{i} x_{i}^{k} + \varepsilon_{x^{k}}, k = 1, ..., K; \\
y^{m} = \sum_{i=1}^{N} \lambda_{i} y_{i}^{m} - \varepsilon_{y^{m}}, m = 1, ..., M; b^{c} = \sum_{i=1}^{N} \lambda_{i} b_{i}^{c} + \varepsilon_{b^{c}}; \\
\sum_{k=1}^{K} u^{k} \varepsilon_{x^{k}} + \sum_{m=1}^{M} v^{m} \varepsilon_{y^{m}} - \varepsilon_{b^{c}} = 0; \\
\sum_{i=1}^{N} \lambda_{i} = 1; \lambda_{i}, \varepsilon_{x^{k}}, \varepsilon_{y^{m}}, \varepsilon_{b^{c}} \geq 0, \forall i, k, m
\end{cases}$$
(6)

In Eqs. (5) and (6), λ_i (i=1,...,N) denotes the weight factors which are used to construct convex combinations of observations. Restricting them to sum up to unity implies that the technology satisfies variable returns to scale (VRS) (cf. Banker et al. 1984). A constant returns to scale (CRS) technology can be imposed by removing this restriction. All epsilons are slack variables. The slack variables $\varepsilon_{x^k}, \varepsilon_{y^m}, \varepsilon_{b^c}$ in \hat{T}_2 are restricted according to the MBE. This summing up constraint on the slack variables guarantees that slacks in feasible input—output combinations are only part of \hat{T}_2 if they satisfy the MBE.

3.1.2 Measuring EE

In this section, we benchmark the DMUs in terms of their ability to produce desirable outputs with a minimum of environmental damage. We minimize controlled emissions subject to i) the production technology T_1 and ii) the production technology T_2 . Given the DEA estimator for T_1 in Eq. (5), the minimal emission for DMU o can be estimated by solving the following linear programming problem [extension of Coelli et al.'s (2007) model]:

Given the DEA estimator for T_2 in Eq. (6), the minimal emission for DMU o can be estimated by solving the following linear programming problem (Rødseth, 2016):

$$\min_{\lambda,\varepsilon,b^c,x} b_{II}^{c^{***}} = b^c$$

$$s.t. \quad x^k = \sum_{i=1}^N \lambda_i x_i^k + \varepsilon_{x^k} \qquad k = 1,...,K$$

$$y_o^m = \sum_{i=1}^N \lambda_i y_i^m - \varepsilon_{y^m}, \quad m = 1,...,M$$

$$b^c = \sum_{i=1}^N \lambda_i b_i^c + \varepsilon_{b^c} \qquad .$$

$$\sum_{k=1}^K u^k \varepsilon_{x^k} + \sum_{m=1}^M v^m \varepsilon_{y^m} - \varepsilon_{b^c} = 0$$

$$\sum_{i=1}^N \lambda_i = 1$$

$$\lambda_i, \varepsilon_{x^k}, \varepsilon_{y^m}, \varepsilon_{b^c} \ge 0, \quad \forall i, k, m$$

$$(8)$$

The linear programs are solved by choosing a feasible, emission minimizing combination of the polluting inputs, x^P , the non-polluting inputs, x^{NP} , and the abatement output, a, for producing the observed desirable outputs, y_o . Hence, the models allow for three emission reduction strategies: i) emission reduction by increasing the abatement output, ii) emission reduction by reducing and reallocating material inputs, and iii) emission reduction by substituting material with non-material inputs. The EE measure for DMU o based on Eqs. (7) and (8) is defined by the ratio of the minimal emission to the observed emission:

$$EE_I = \frac{b_I^{c^{***}}}{b_c^c} \tag{9}$$

$$EE_{II} = \frac{b_{II}^{c^{****}}}{b_o^c}$$
 (10)

The EE measures take values less than or equal to 1, where 1 indicates that the DMU under consideration is efficient. The measure evaluates the DMU's possibility to reduce its controlled emission given its production of desirable outputs, y_o . This leads to the following propositions:

Proposition 1: The minimal emissions obtained from Eq. (7), $b_I^{c^{***}}$, and from Eq. (8), $b_{II}^{c^{***}}$ are identical if the slack of the abatement output in Eq. (7), ε_a , is zero. Hence, if ε_a is zero, the environmental efficiency measure of Rødseth (2016), EE_{II} , and the new measure, EE_{II} , coincide. The formal proof is available in the Appendix.

Proposition 2: Rødseth (2016) shows that his efficiency measure, EE_{II} , is a generalization of the efficiency measure of Coelli et al. (2007) and coincides with the Coelli et al. (2007) measure, if none of the producers control emissions, and the MFCs of the desirable outputs are zero. It follows from this result and Proposition 1, that EE_{I} coincides with the Coelli et al. (2007) measure if none of the producers control emissions, which implies that a and ε_a are zero for all DMUs, and the MFCs of the desirable outputs are zero. 10

3.2 Production with heterogeneous MFCs

So far, we have assumed that the vector of MFCs for inputs, u, and outputs, v, consists of constants. Let us assume that the MFCs are non-discretionary and differ across DMUs. The vector of MFCs are represented by u_i and v_i . The problem with ignoring heterogeneous, non-discretionary MFCs in EE measurement is illustrated by the following numerical example on soil erosion in arable farming.

Consider a farm that produces maize using the inputs land and labor. The usage of arable land in the production process causes soil erosion (an unintended output) by water and wind. The degree of soil loss by water depends on exogenous environmental factors, such as slope, slope length, and soil type of the fields as well as rainfall quantity and intensity. These differences in operating environments are captured by the heterogeneous MFCs of the single polluting input land. The MFC of land is the uncontrolled soil erosion in tons per hectare. Since labor is a non-polluting input, and maize does not contain any soil, the MFCs of labor and maize are zero. Farms implement erosion control measures to reduce erosion. These abatement activities (e.g., planting winter cover crops and using mulch tillage) require additional inputs and often result in higher production costs.

All farms in Table 2 employ the same amount of inputs, 10 ha land and 1000 h labor, to produce the same amount of maize, 100 t. Farms A and B operate under more favorable conditions, for example, flatter fields than farms C and D resulting in lower MFCs, that is, 0.5 t/ha soil loss vs. 1 t/ha. The farms also differ with respect to their share of abated erosion. Erosion control measures allow farms A and C to reduce uncontrolled erosion by 40%, and farms B and D by 60%.

10

¹⁰ Note that Coelli et al. (2007) and Rødseth (2016) assume that the production technology exhibits constant returns to scale, while this article assumes a VRS technology. Proposition 1 and all further assertions that rely on comparisons of the production models of Coelli et al. (2007), Rødseth (2016), and the new models in this article are only valid if we assume that the returns to scale assumption is identical across these models.

Table 2 Data matrix of the soil erosion example with heterogeneous MFCs

Farm ID	Abatement erosion (t)	Controlled erosion (t)	Uncontrolled erosion (t)	Material flow coefficient (t/ha)	Share of abated erosion (%)
A	2	3	5	0.5	40
В	3	2	5	0.5	60
C	4	6	10	1	40
D	6	4	10	1	60

MFCs: material flow coefficients. All farms use 10 ha land, 1000 h labor, and produce 100 t of maize. The MFCs of maize are zero. The only erosion generating input with strictly positive MFCs is land.

The left-hand graph of Fig. 1 illustrates the measurement of EE following Eqs. (7) and (9), that is, assuming that MFCs are homogeneous across farms. Since farm D produces the highest abatement output, it is classified as environmentally efficient and spans the production frontier represented by the line 0D and its extension. All other farms are benchmarked against farm D, resulting in an optimal abatement output of 6 t. However, this is not feasible for farms A and B operating under a more favorable environment than farm D and having an uncontrolled erosion of 5 t, compared with 10 t for farm D. The optimal abatement output of 6 t would result in a negative value of the optimal controlled erosion and in negative EE scores. Hence, Eq. (7) overestimates the potential of farms A and B to increase the abatement output. 12

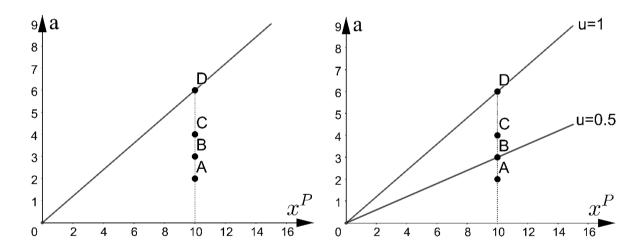


Fig. 1 EE measurement with heterogeneous MFCs. The left-hand (right-hand) graph shows the technology set(s) under constant returns to scale in line with Eq. (5) (Eq. [14]) ignoring (taking into account) the non-discretionary nature of the MFCs.

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¹¹ Note that Fig. 1 shows CRS technology sets, while Eqs. (7) and Eq. (9) assume a VRS technology. However, the reasoning associated with the numerical example and Fig. 1 is identical under a CRS and VRS technology.

¹² Note, that the abatement output is a fraction between zero and one of the uncontrolled emission, that is, $a = sb^{uc} = s(ux - vy)$, $s \in [0,1]$. Hence, everything else being equal, farms operating under less favorable conditions, those with a more unfavorable MFCs, can produce a higher abatement output in absolute terms.

The right-hand graph of Fig. 1 shows how to measure EE correctly. The idea is formalized by Eqs. (14), (18) and (25.1) in the next section. The heterogeneity and non-discretionary nature of the MFCs is taken into account by estimating production frontiers and technology sets conditional on the MFCs. The line passing the origin to D represents the production frontier for u = 1, and the line 0B and its extension represent the production frontier for u = 0.5. Farms D and B, abating 60% of their uncontrolled erosion, are classified as environmentally efficient. Only farms having the same MFCs are compared with each other. Farm C is benchmarked against farm D, and farm A is benchmarked against farm B, resulting in an optimal abatement output of 3 t for farm A and 6 t for farm C. In accordance with Eq. (25.1), the EE of farms A and farm C, abating 40% of their uncontrolled erosion, is 0.66. Since there are no inefficiencies in the level and allocation of inputs, the EE scores reflect the erosion control performance of the farms. The scores are equal to the share of abated erosion (40%) divided by the maximum observed value of this share (60%).

The left-hand graph of Fig. 2 illustrates the EE measurement based on the weak G-disposability technology according to Eqs. (8) and (10). Contrary to technology, set \hat{T}_1 , shown in the left-hand graph of Fig. 1, the DEA estimator of the weak G-disposability technology, \hat{T}_2 , depends on the MFCs, which are part of the summing-up restriction on the slacks in Eq. (8). Hence, the PPS of the evaluated DMUs depends on their MFCs. This is shown in the left-hand graph of Fig. 2, depicting the PPS for u=0.5 and u=1 when holding the abatement output constant. Both sets are bounded by the solid line connecting B and C. In the case of u=0.5, the PPS is additionally bounded by the dashed extensions with slope 0.5. The technology set pivots upward if u=1, leading to different production possibilities. However, since the PPSs for u=0.5 and u=1 overlap, it is possible that DMUs with different MFCs are benchmarked against each other.

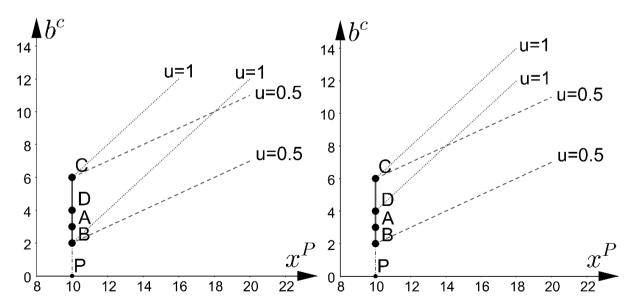


Fig. 2 EE measurement with heterogeneous MFCs. The left-hand (right-hand) graph shows the technology sets according to Eq. (6) (Eq. [15]) ignoring (taking into account) the non-discretionary nature of the MFCs.

The left-hand graph of Fig. 2 shows that Farm B has the least amount of controlled emission and is, therefore, classified as environmentally efficient by Eq. (10). All other farms are benchmarked against farm B, resulting in a target for controlled erosion of 2 t. The EE of farm C is evaluated by $EE_{II} = PB / PC = 2 / 6 = 0.33$. The same procedure applies to farms A and D, having EE scores of 0.66 and 0.5, respectively. The question is whether this is a fair ranking of environmental performance.

For instance, farm D reduces its uncontrolled erosion by the same share as farm B (i.e., by 60%) using the same amount of inputs and producing the same amount of desirable outputs. The only difference between B and D is that D operates under less favorable environmental conditions (e.g., steeper slope of fields) leading to an uncontrolled (and controlled) soil loss that is twice that of farm B. Hence, farm D is punished for operating under harsher environmental conditions, and Eq. (8) overestimates the potential of farm D to decrease the controlled erosion.

To overcome this problem, I suggest that farms are only allowed to be benchmarked against DMUs operating in the same or a less favorable environment (i.e., having a u higher or equal). This avoids that reduction potentials for controlled soil erosion are overestimated due to a comparison with DMUs operating in a more favorable environment (i.e., having a lower u).

Accordingly, the right-hand graph of Fig. 2 shows the PPS for u = 0.5 and u = 1. The PPS for u = 0.5 remains unchanged, but the PPS for u = 1 is now bounded by the solid line connecting D and C and the dotted extensions with slope 1. Farm A is again benchmarked against farm B because they have the same MFCs. The EE of farm A is 0.66. Contrary to farm A, the EE scores of farms C and D change compared with the situation depicted on the left-hand graph of Fig. 2. Farm D is classified as environmentally efficient, while farm C is benchmarked against farm D and has an EE of 0.66. Note that in this simple example, the EE scores obtained by the two new procedures presented in this section coincide (cf. right-hand graph of Figs. 1 and 2). The next two subsections clarify that, in general, the two approaches do not result in identical EE scores.

3.2.1 Modeling and estimating the conditional production technology

As shown in the last section, the non-discretionary MFCs affect the production of the abatement output and the uncontrolled emission. Everything else being equal, farms operating under less favorable conditions have a higher uncontrolled emission and can produce a higher abatement output, that is, the abatement output and the uncontrolled emission is increasing in u and decreasing in v.¹³ The following index of environmental harshness is proposed to measure the unfavorability of the MFCs:

$$z_{i} = \sum_{k=1}^{K} w_{i}^{k} u_{i}^{k} - \sum_{m=1}^{M} w_{i}^{m} v_{i}^{m}, \quad \text{where, } w_{i}^{k} = \frac{u_{i}^{k} x_{i}^{k}}{\sum_{k=1}^{K} u_{i}^{k} x_{i}^{k} + \sum_{m=1}^{M} v_{i}^{m} y_{i}^{m}} \quad \text{and } w_{i}^{m} = \frac{v_{i}^{m} y_{i}^{m}}{\sum_{k=1}^{K} u_{i}^{k} x_{i}^{k} + \sum_{m=1}^{M} v_{i}^{m} y_{i}^{m}}.$$
 (11)

The index z_i is a weighted sum of the MFCs. The proposed weights measure how much each input and output contributes to the material flow (i.e., inflow plus outflow). The sum of the weights is one. A lower value of z represents a more favorable environment, in the sense that less uncontrolled emissions are generated.

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¹³ This can easily be inferred from the fact that $a = sb^{uc} = s(ux - vy)$, $s \in [0,1]$.

Consider a traditional production technology extended by an abatement output. The production technology depends on z, and the conditional PPS can be written as:

$$T_1(z) = \{ \langle x, y, a \rangle \in \mathbb{R} \quad can \ produce(y, a) \ given \ z(u, v) \}.$$
 (12)

Next, consider a traditional production technology that is extended by a controlled emission. The production technology depends on z, and the conditional PPS is given by:

$$T_2(z) = \left\{ \left\langle x, y, b^c \right\rangle \in \mathbb{R} \qquad can \ produce(y, b^c) \ given \ z(u, v) \right\}. \tag{13}$$

The production axioms described in section 3.1.1 hold for $T_1(z)$ and $T_2(z)$. In addition, it holds that $T_1(z_1) \subseteq T_1(z_2)$ for all $z_1 \le z_2$. This implies that a DMU with a less favorable environment, z_2 , should be able to produce at least as much abatement output as any DMU with a more favorable environment, z_1 . For $T_2(z)$, it is clear that a DMU with a more favorable environment, z_1 , should be able to have a lower controlled emission for a given abatement output than a DMU with a less favorable environment, z_2 . 14

Having these modifications in mind, it becomes clear that, if the production possibilities are defined in terms of $T_1(z)$, a given DMU should be compared only with DMUs with the same or a more favorable environment (i.e., DMUs having the same or a lower z). If the production possibilities are defined in terms of $T_2(z)$, a given DMU should be compared only with DMUs with same or a less favorable/harsher environment (i.e., DMUs having the same or a higher z). While, in the case of $T_1(z)$, this procedure avoids an overestimation of the potential to increase the abatement output, in the case of $T_2(z)$, this avoids an overestimation of the potential to decrease the controlled emission.

For the empirical estimation of $T_1(z)$ and $T_2(z)$, we follow the procedure suggested by Ruggiero (1996, 1998) and restrict the set of possible reference units of a given DMU by introducing weight restrictions. The DEA estimator of $T_1(z)$ for DMU o is given by:

$$\hat{T}_{1}(z_{o}) = \begin{cases}
\langle x, y, a \rangle \in \mathbb{R} & k = \sum_{i=1}^{N} \lambda_{i} x_{i}^{k} + \varepsilon_{x^{k}}, k = 1, ..., K; \\
y^{m} = \sum_{i=1}^{N} \lambda_{i} y_{i}^{m} - \varepsilon_{y^{m}}, m = 1, ..., M; a = \sum_{i=1}^{N} \lambda_{i} a_{i} - \varepsilon_{a}; \\
\sum_{i=1}^{N} \lambda_{i} = 1; \lambda_{i}, \varepsilon_{x^{k}}, \varepsilon_{y^{m}}, \varepsilon_{a} \geq 0, \forall i, k, m \\
\lambda_{i} \geq 0 \quad \forall i : z_{i} \leq z_{o} \\
\lambda_{i} = 0 \quad \forall i : z_{i} > z_{o}
\end{cases}$$
(14)

 $^{^{14}}$ Note that, for both the PPS in Eq. (12) and Eq. (13), it is assumed that the production of y is independent of z

The DEA estimator of $T_2(z)$ for DMU o is given by:

$$\begin{cases}
\langle x, y, b^{c} \rangle \in \mathbb{R} & \stackrel{t}{=} \sum_{i=1}^{N} \lambda_{i} x_{i}^{k} + \varepsilon_{x^{k}}, k = 1, ..., K; \\
y^{m} = \sum_{i=1}^{N} \lambda_{i} y_{i}^{m} - \varepsilon_{y^{m}}, m = 1, ..., M; b^{c} = \sum_{i=1}^{N} \lambda_{i} b_{i}^{c} + \varepsilon_{b^{c}}; \\
\sum_{k=1}^{K} u_{o}^{k} \varepsilon_{x^{k}} + \sum_{m=1}^{M} v_{o}^{m} \varepsilon_{y^{m}} - \varepsilon_{b^{c}} = 0; \\
\sum_{i=1}^{N} \lambda_{i} = 1; \lambda_{i}, \varepsilon_{x^{k}}, \varepsilon_{y^{m}}, \varepsilon_{b^{c}} \geq 0, \forall i, k, m \\
\lambda_{i} \geq 0 \quad \forall i : z_{i} \geq z_{o} \\
\lambda_{i} = 0 \quad \forall i : z_{i} < z_{o}
\end{cases}$$
(15)

3.2.2 Measuring and decomposing environmental efficiency

The optimization problems in the left and right column of Table 3 minimize the controlled emission of DMU o subject to $\hat{T}_1(z_o)$ and $\hat{T}_2(z_o)$, respectively. The only abatement strategy allowed in Eqs. (16) and (19) is the increase of the abatement output for given desirable outputs and for fixed inputs. In addition, Eqs. (17) and (20) also allow reducing the emission by reducing and reallocating the material inputs, x^P , for given desirable outputs and fixed non-material inputs, x^{NP} . Finally, Eqs. (18) and (21) additionally allow for emission reduction by substituting material inputs with non-material.

Table 3 Linear programming problems 16–21

Models based on $\hat{T_1}(z_o)$		Models based on $\stackrel{}{T_2}(z_o)$		
$\min_{\lambda, \varepsilon, a} b_1^{c^*} = \sum_{k=1}^{K} u_o^k x_o^k - \sum_{m=1}^{M} v_o^m y_o^k - a$ s.t $(x_o, y_o, a) \in \hat{T}_1(z_o)$	(16)	$ \min_{\lambda,\varepsilon,b^c} b_2^{c^*} = b^c s.t (x_o, y_o, b^c) \in \hat{T}_2(z_o) $ (19)		
$\min_{\lambda, \varepsilon, a, x^{P}} b_{1}^{c^{**}} = \sum_{k=1}^{S} u_{o}^{k} x^{P,k} - \sum_{m=1}^{M} v_{o}^{m} y_{o}^{k} - a$ $S.t (x^{P}, x_{o}^{NP} y_{o}, a) \in \hat{T}_{1}(z_{o})$	(17)	$ \min_{\lambda,\varepsilon,b^c,x^P} b_2^{c^{**}} = b^c $ $ s.t (x^P, x_o^{NP} y_o, b^c) \in \hat{T}_2(z_o) $ (20)		
$\min_{\lambda, \varepsilon, a, x} b_1^{c^{***}} = \sum_{k=1}^{K} u_o^k x^k - \sum_{m=1}^{M} v_o^m y_o^k - a$ $s.t (x, y_o, a) \in \hat{T}_1(z_o)$	(18)	$\min_{\lambda,\varepsilon,b^c,x} b_2^{c^{***}} = b^c$ $s.t (x,y_o,b^c) \in \hat{T}_2(z_o)$ (21)		

Note that, while the reference set for DMU o in Eqs. (16)–(18) is restricted to include only DMUs i=1,...,N with $z_i \leq z_o$, Eqs. (19)–(21) restrict the comparison set of DMU o to include only DMUs i=1,...,N having $z_i \geq z_o$. Since the models in the left and right column of Table 3 deal with almost disjoint sets of possible reference units for DMU o, it should be clear that, in general, the solutions for each of the corresponding models do not coincide. Furthermore, there is no rule which of the corresponding models give the optimal solution with the lowest controlled emission. For some evaluated DMUs, Eq. (18) detects improvement potentials, which are not detected by Eq. (21), and for other DMUs under evaluation exactly the opposite can be the case. Therefore, we consider the minimal value of the controlled emission of both Eqs. (18) and (21) as the final solution: 15

$$b_3^{c^{***}} = \min(b_1^{c^{***}}, b_2^{c^{***}}) . \tag{22}$$

To get an exact decomposition of the EE measure shown below, the final solution for the other two pairs of the minimization problems in Table 3, that is, Eq. (16) and Eq. (19) as well Eq. (17) and Eq. (20), should be based on the same technology set as the final solution in Eq. (22):

$$b_3^{c^{**}} = \begin{cases} b_1^{c^{**}} & \text{if } b_1^{c^{***}} < b_2^{c^{***}} \\ b_2^{c^{**}} & \text{if } b_1^{c^{***}} > b_2^{c^{***}} \end{cases}$$
 (23)

$$b_3^{c^*} = \begin{cases} b_1^{c^*} & \text{if } b_1^{c^{***}} < b_2^{c^{***}} \\ b_2^{c^*} & \text{if } b_1^{c^{***}} > b_2^{c^{***}} \end{cases}$$
(24)

Contrary to using only models based on either $\hat{T_1}(z_o)$ or $\hat{T_2}(z_o)$, the proposed procedure does not throw away valuable information. The estimated improvement potentials are based on a richer set of information and are therefore more accurate. The presented approach allows comparing the DMU under evaluation with all other DMUs in the sample, that is, the set of possible reference units of DMU o is not restricted to a subset of DMUs as would be the case if only the models based on either $\hat{T_1}(z_o)$ or $\hat{T_2}(z_o)$ are applied. 16

Based on the linear programming problems presented in Table 3 and the minimum model shown in Eqs. (22)–(24), the following measures of EE and its decompositions are introduced:

$$EE_{j} = \frac{b_{j}^{c^{****}}}{b_{o}^{c}} = \frac{b_{j}^{c^{*}}}{b_{o}^{c}} \times \frac{b_{j}^{c^{***}}}{b_{j}^{c^{**}}} \times \frac{b_{j}^{c^{***}}}{b_{j}^{c^{***}}} , \quad j = 1, 2, 3.$$
(25.j)

Emission control Material input Environmental efficiency efficiency allocative efficiency

⁻

¹⁵ Clearly, the final solution also includes the optimal input mix and abatement output corresponding to either Eq. (18) or Eq. (21).

¹⁶ My approach allows the reference point of DMU o to be either a linear combination of DMUs with $z_i \le z_o$ or $z_i \ge z_o$. Linear combinations of DMUs having $z_i < z_o$ and $z_i > z_o$ are ruled out as reference points.

The index j = 1,2,3 indicates the EE measure and its decomposition based on $\hat{T}_1(z_o)$, $\hat{T}_2(z_o)$, and the minimum model according to Eqs. (22)–(24), respectively. The overall efficiency measures and their components take values smaller or equal to 1, where 1 indicates that the DMU under evaluation is efficient. The overall measures evaluate the DMU's potential to reduce its controlled emission, given its production of desirable outputs, while the components assess the contribution of different abatement strategies to the overall emission reduction potential. More specifically, the overall efficiency measures are decomposed into a part reflecting i) emission reductions for given inputs and desirable outputs, which corresponds to the efficiency of the emission control activities (emission control efficiency, ECE), ii) additional emission reductions by reducing and reallocating material inputs (material input efficiency, MIE), and iii) further emission reductions by substituting material inputs with non-material inputs (environmental allocative efficiency, EAE).

As shown by Eq. (26.j), the procedure also allows decomposing the actual emission, b_o^c , into the optimal emission, b_o^{c****} , and emissions by source of inefficiency, that is, L_j^* , L_j^{***} , and L_j^{****} . Where L_j^* represents emissions due to inefficient implementation of erosion control measures, L_j^{**} represents emissions resulting from inefficient use of material inputs, and L_j^{***} reflects emissions due to inefficient allocation between material and non-material inputs:

$$b_{o}^{c} = L_{j}^{*} + L_{j}^{***} + L_{o}^{****} + b_{o}^{c****}, \quad j = 1, 2, 3$$

$$where, \quad L_{j}^{*} = b_{o}^{c} - b_{j}^{c*}, \qquad j = 1, 2, 3$$

$$L_{j}^{**} = b_{j}^{c*} - b_{j}^{c***}, \qquad j = 1, 2, 3$$

$$L_{j}^{***} = b_{j}^{c**} - b_{j}^{c****}, \qquad j = 1, 2, 3$$

$$(26.j)$$

Last but not least, the relationship between the new EE measures in Eqs. (25.1)–(25.3) with the EE measures of Coelli et al. (2007) and Rødseth (2016) are explored in proposition 3 as follows:

Proposition 3: If the MFCs are homogeneous across all DMUs, Eq. (18) and Eq. (21) collapse into Eq. (7) and Eq. (8), respectively. It follows from this result and Proposition 1 and 2 that the new EE measures, EE_1 , EE_2 , and EE_3 are generalizations of the Coelli et al. (2007) measure and coincide with the Coelli et al. (2007) measure if the MFCs are homogeneous across all DMUs, none of the producers control emissions and the MFCs of the desirable outputs are zero.

Furthermore, the Rødseth (2016) EE measure is a special case of the new measures EE_1 , EE_2 , and EE_3 . The Rødseth (2016) measure coincides with the new measures if the MFCs are homogeneous across all DMUs and \mathcal{E}_a in Eq. (18) is zero.

4 Empirical Illustration

This section applies the proposed methodology to the EE measurement of crop farms considering soil erosion as an undesirable output that has to be minimized. The approach is illustrated using a sample of 90 Austrian crop farms observed in 2011.

4.1 Data

Soil erosion estimates are based on a revised universal soil loss equation (RUSLE; Renard et al. 1997) using plot-level data from the Austrian Integrated Accounting and Control System (IACS). The calculation of all other inputs and outputs is based on farm bookkeeping data from the Austrian section of the EU's Farm Accountancy Data Network (FADN).

The RUSLE is expressed as A = RKLSCP, where A is the annual average soil loss from water in t/ha per year for the area under investigation. As shown in the equation, A is determined by a multiplication of the rainfall erosivity factor (R-factor), soil erodibility factor (K-factor), slope length factor (L-factor), slope steepness factor (S-factor), cover-management factor (C-factor), and support practices factor (P-factor). While R-, K-, L-, and S-factors represent environmental conditions, such as precipitation, soil type, and topography, the C- and P-factors represent management practices of farmers. Since the desirable outputs are taken as given, we also consider the C-factor, that is, crop choice, as fixed. The P-factor is considered as the single factor adjustable by the farmer.

The P-factor is a ratio which describes how implemented erosion control measures cause soil loss to deviate from losses that occur without the implementation of these measures (Panagos et al. 2015b). The erosion control measures considered in this study include i) mulch-till and no-till associated with a P-factor of 0.5, meaning that soil erosion is reduced by 50% relative to conventional tillage, and ii) eight variants of winter cover crops differentiated by type of cover crop and duration of coverage associated with P-factors of 0.5–0.9. The coverage associated with P-factors of 0.5–0.9.

The farm-specific MFC for land, that is, the uncontrolled erosion in t/ha per year, is estimated by u = RKLSC. The controlled erosion in tons is given by $b^c = RKLSCPL$ where L and is the utilized agricultural area (UAA) in hectares. The abatement output in tons is estimated by subtracting the controlled erosion from the uncontrolled erosion: a = RKLSCL and (1-P).

Information on implemented erosion control measures is derived from the IACS. The IACS provides parcel-level information for almost all agricultural parcels in Austria in terms of the main crops planted and implemented agri-environmental schemes, including specific erosion control measures, such as tillage type (mulch-till and no-till) and different modes of soil coverage (type of cover crop and duration of coverage). This information allows us to assign a C- and a P-factor to each parcel (see Eder et al. 2021 for a complete list of C- and P-factors used in this study). For estimating R-, K-, L- and S-factors, we follow Wpa GmbH and BWA (2009). Due to data availability and for the ease of exposition, we use cross-sectional data for the year 2011.

All other information is taken from the Austrian section of the EU's FADN. The farms included in the FADN dataset are a stratified sample, representing the Austrian agricultural sector in terms of standard output, production orientation, and altitude.

The dataset for the year 2011 consists of 2,265 farms. However, this illustration focuses on specialized crop farms whose share of revenues from crops in total revenues is larger or equal to 65%. In addition, to increase the homogeneity of the sample, farms whose share of revenues

¹⁷ This study covers all erosion control measures subsidized by agri-environmental schemes in Austria (cf. BMLFUW, 2009). Additional non-subsidized measures applied by farmers cannot be taken into account due to data unavailability.

¹⁸ Values for P-factors are taken from Wpa GmbH and BWA (2009). Six wine- and fruit-specific erosion control measures are also considered. Since the sample only includes crop farms, those measures are of minor importance.

from potatoes and sugar beets in crop revenues is larger than 20% are excluded. When merging FADN with IACS data, some observations are removed due to missing information on erosion control measures or differences in farms' UAA being larger than 20% between the FADN and IACS. Finally, after applying the outlier detection method described in Bogetoft and Otto (2011), we are left with a sample of 90 farms for the year 2011.

Table 4 Descriptive statistics of data used for analysis (N = 90)

Variables	Mean	SD	Min	Max
Inputs				
Land, UAA (ha)	63.68	38.13	9.84	165.99
Labor (AWU)	0.94	0.60	0.11	4.00
Capital (Euro, real)	122,843.86	86,321.91	6,766.88	449,625.45
Intermediate Inputs (Euro, real)	22,954.78	16,853.78	2,188.81	81,749.53
Desirable Outputs Total Revenue (Euro, real)	54,960.45	37,384.50	937.55	159,368.36
Abatement Erosion (t)	18.72	33.41	0.00	180.37
Undesirable Output				
Controlled Erosion (t)	162.97	187.53	4.33	1,038.87
Material Flow Coefficient (Land)				
Uncontrolled Erosion (t/ha)	3.18	3.34	0.10	19.88

Authors' calculations from Austrian FADN and IACS data. Data obtained from the Federal Ministry of Sustainability and Tourism. Note: The sample is a cross-section of 90 farms observed in 2011. UAA: utilized agricultural area; AWU: agricultural working unit. One AWU is 2,160 working hours.

Table 4 provides descriptive statistics on input and output variables used in the DEA models as well as on the MFCs. The production factor land is measured by UAA in hectares and includes owned and rented land. UAA ranges from 10 to 166 ha, and 96% is arable land on average. Labor is measured in agricultural working units (AWUs), where one AWU is equal to 2,160 working hours. Capital includes farm buildings, machinery, equipment, standing timber, livestock, and assets from activities related to farming (e.g., agri-tourism, renting out machinery, and services for other farms). Intermediate inputs cover expenditures for land use (e.g., seeds, fertilizer, and pesticides), livestock (e.g., fodder and veterinary), energy, insurance, and expenditures for other activities related to farming. Total revenues (desirable output) include earnings net of subsidies from plant production, livestock, forestry, services, direct marketing, financial income (e.g., insurance), and other activities related to farming. Capital, intermediate inputs, and total revenue are implicit quantity values, that is, the nominal values of the components of each variable are divided by proper price indices.

On average, the abatement output of a farm is 19 t, that is, erosion control measures reduce the soil loss by 19 t on average which corresponds to a reduction of 10%. However, there is a substantial variation in the abatement output. About 11% of the farms do not implement erosion control measures having a zero abatement output (or a P-factor of one). On the other end of the spectrum are farms reducing the uncontrolled soil loss by 50% through erosion control. The

average MFC of land, that is, the average uncontrolled soil loss in t/ha per year, is 3.2 and ranges from 0.1 t/ha to almost 20 t/ha.

4.2 Results

Table 5 shows the descriptive statistics of the estimated EE scores and their components. Models 1, 2, and 3 refer to the estimates based on $\hat{T}_1(z_o)$ (i.e., Eqs. [16]–[18]), $\hat{T}_2(z_o)$ (i.e., Eqs. [19]–[21]), and the minimum model (i.e., Eqs. [22]–[24]), respectively.

Table 5 Descriptive statistics of efficiency scores for Models 1-3 (N = 90)

Table 3 Descriptive statistics of efficiency scores for Models 1	Model 1	Model 2	Model 3
Efficiency Index	Eq. (25.1)	Eq. (25.2)	Eq. (25.3)
Environmental Efficiency (EE)			
Geom. Mean	0.54	0.71	0.53
SD	0.27	0.26	0.26
Min	0.15	0.24	0.15
Max	1	1	1
Number of efficient farms	20	40	15
Erosion Control Efficiency (ECE)			
Geom. Mean	0.97	0.99	0.96
SD	0.05	0.04	0.06
Min	0.75	0.68	0.68
Max	1	1	1
Number of efficient farms	58	82	56
Material Input (Land Use) Efficiency (MIE)			
Geom. Mean	0.69	0.86	0.69
SD	0.27	0.20	0.27
Min	0.17	0.27	0.17
Max	1	1	1
Number of efficient farms	42	65	39
Environmental Allocative Efficiency (EAE)			
Geom. Mean	0.80	0.83	0.79
SD	0.21	0.21	0.21
Min	0.21	0.29	0.21
Max	1	1	1
Number of efficient farms	34	50	32

Descriptive statistics of efficiency indices according to Eqs. (25.1)–(25.3) are shown. Reported values are based on a sample of 90 Austrian crop farms observed in 2011.

The average EE is 0.54 in Model 1, and 0.71 in Model 2. While Model 1 classifies 22% of the farms as environmentally efficient, Model 2 classifies 44% as efficient. Hence, in this

specific empirical example, Model 1 detects larger average inefficiencies than Model 2. Remember, the sets of possible reference units that are used for performance comparisons of a particular DMU in Model 1 and Model 2 are almost disjoint, which explains most of the differences in EE scores between the two models. Since the final EE (Model 3) represents the minimum value of the efficiency scores of Models 1 and 2, it is on average very close to that of Model 1. The final average EE is 0.53, meaning that the same amount of output can be potentially achieved with 47% less soil loss. Finally, about 17% of the farms are classified as environmentally efficient.

Table 6 shows that optimal average soil loss according to Model 3 is 73 t per farm in 2011 compared with an actual average soil loss of 163 t per farm. The main source of this inefficiency is the inefficient use of land (contributes 55 t), followed by an inefficient allocation of inputs (contributes 28 t). The inefficient implementation of erosion controls contributes only little (7 t) to the overall inefficiency. This is also indicated by the efficiency indices in Table 5, where the average MIE, EAE, and ECE is 0.69, 0.79, and 0.96, respectively. Fig. 3 complements Table 6 by showing the decomposition of soil loss by source for all farms.

Table 6 Decomposition of soil erosion by source under Model 3 (N = 90)

	Mean	SD	Min	Max
Soil loss (t) due to				
Erosion control inefficiency	7.16	16.49	0.00	104.22
Land use inefficiency	54.89	107.53	0.00	752.17
Environmental allocative inefficiency	27.87	69.26	0.00	368.18
Optimal soil loss (t)	73.05	79.94	4.33	513.47
Actual soil loss (t)	162.97	187.53	4.33	1038.87

The decomposition of actual soil erosion according to Eq. (26.3) is shown. Reported values are based on a sample of 90 Austrian crop farms observed in 2011.

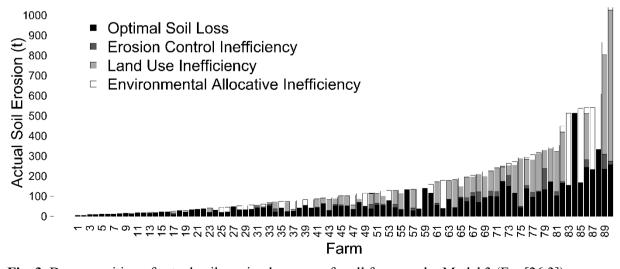


Fig. 3 Decomposition of actual soil erosion by source for all farms under Model 3 (Eq. [26.3]).

Table 7 compares the actual, average abatement output and input ratios with the optimal average values according to the solutions associated with Eqs. (22)–(24), that is, Model 3, whereas Optimal 1 considers erosion control, that is, increasing the abatement output, as the single abatement strategy. In addition, Optimal 2 allows for the reduction of land, and Optimal 3 further allows for the substitution of land with labor, intermediate inputs, and capital.

Table 7 Optimal vs. observed abatement output and input ratios (N = 90)

Variable	Actual	Optimal 1	Optimal 2	Optimal 3
Abatement Erosion (t)	18.72	25.88	8.46	3.41
Input ratios				
Labor-Land (hours/ha)	38.28	38.28	61.40	76.10
Intermediate inputs–Land (€/ha)	371.41	371.41	627.50	639.60
Capital–Land (€/ha)	2,369.61	2,369.61	3,843.92	3,584.77

Mean values for a sample of 90 Austrian crop farms observed in 2011 are reported. The optimal solution of Model 3 is shown. Optimal 1 considers erosion control as a single abatement strategy. In addition, Optimal 2 allows for the reduction of land, and Optimal 3 considers the substitution of land with labor, intermediate inputs, and capital as further abatement strategy. Mean optimal land use under Optimal 3 is 31.9 ha.

Table 7 indicates that, under Optimal 1, with the actually employed amount of inputs, the average abatement output can be increased from 19 t to 26 t per farm, while keeping real total revenues constant. Hence, if farmers consider erosion control as the single available abatement strategy, the efficient implementation of those measures allows reducing the average soil loss by 7 t per farm (cf. Table 6) or by 4% (cf. Table 5). In Optimal 2, the optimal average land use is 42 ha per farm compared with 64 ha actual land use. Since the usage of other inputs remains constant the optimal labor—land, intermediate inputs—land and capital—land ratios increase substantially. Allowing for the substitution of land with other inputs reduces the optimal land use under Optimal 3 to 32 ha per farm and leads to a further increase of the labor—land and intermediate inputs—land ratios.

The results indicate that the same amount of output can be potentially achieved by using substantially less arable land, that is, the optimal average land use is 32 ha per farm compared with 61 ha actual land use. Land use inefficiencies caused, on average, a soil loss of 55 t per farm in 2011, and the substitution of land with labor, capital, and intermediate inputs would have allowed an additional reduction of average soil loss by 28 t per farm. Overall, the results suggest that a considerable reduction of arable land and its conversion into wood- or grassland is potentially achievable without reducing real total revenues. The higher optimal input ratios under Optimal 2 and Optimal 3 suggest an intensification of agriculture on the reduced arable area.

5 Conclusion

The productive efficiency models and EE measures introduced by Coelli et al. (2007) and Rødseth (2016, 2017), which are based on the materials balance condition, have been applied in numerous efficiency analyses (see e.g., Hoang and Rao 2010; Hoang and Coelli 2011; Hoang and Alauddin 2012; Nguyen et al. 2012; Hoang and Nguyen 2013; Hampf and Rødseth 2015,

2017). However, these EE measures produce biased efficiency estimates if the MFCs are heterogeneous across DMUs and not under managerial control, that is, non-discretionary. In addition, the Coelli et al. (2007) measure fails to reward emission reductions by emission control.

To overcome these shortcomings, this article provides a generalization of Coelli et al.'s (2007) materials balance-based production model by allowing for heterogeneous MFCs and considering emission control as an additional abatement strategy. MFCs are considered to be uncontrollable by the DMUs and may reflect i) differences of some external environmental factors that govern the transformation of inputs into good and bad outputs or ii) non-controllable heterogeneities in inputs and outputs (e.g., input or output quality). Based on this generalized production model, a new EE measure and its decomposition are proposed. The new EE measure coincides with the Coelli et al. (2007) measure if the MFCs are homogeneous across all DMUs, none of the producers control emissions, and the MFCs of the desirable outputs are zero. In this context, it is shown that the proposed EE measure can be decomposed into three parts: a part reflecting the efficiency of the emission control activities, a part associated with the efficient use of material inputs and a part reflecting the efficient allocation between material and non-material inputs These separate effects provide useful insights on the potential sources of environmental inefficiency.

The methodology is illustrated by an empirical application to arable farming using data from 90 Austrian crop farms for the year 2011. The usage of arable land for crop production naturally and inevitably causes soil erosion by water, an undesirable by-product of agriculture production that we want to minimize. The extent of soil erosion by water depends on external factors, such as rainfall erosivity, soil texture and structure, slope length and gradient, but also on crop choice and farmer's decisions to implement erosion controls. Soil erosion causes considerable private and social costs, including reduced soil productivity and off-site effects, such as sedimentation, flooding, landslides, and water eutrophication Considering that actual soil erosion rates for tilled, arable land in Europe are, on average, 3 to 40 times greater than the upper limit of tolerable soil erosion (Verheijen et al. 2009), the application is of particular importance. The proposed method might also be applied to EE assessment of livestock farms with respect to nutrient pollution if fertilizer quality is not under managerial control, or the EE analysis of power plants regarding greenhouse gas emissions if switching between fuels is restricted by technical constraints.

We find evidence of a high potential to reduce soil loss from arable farming without sacrificing output, that is, relatively low levels of EE. On average, farms can potentially achieve the same real revenues with 47% less soil loss, which reflected a reduction of soil loss from 163 t to 73 t per farm in 2011. The results are driven by the inefficient usage of agricultural land and the inefficient allocation of inputs towards an overutilization of agricultural area vis-à-vis labor, capital, and other inputs (e.g., fertilizer, pesticide, energy, seeds, etc.). Inefficiencies in the implementation of subsidized erosion control measures, such as planting cover crops, mulch-tillage and direct seeding, are of minor importance. The findings indicate that soil loss can be reduced at reasonable costs, in terms of forgone output, by using less arable land more intensively and setting aside a considerable amount of arable land for conservation uses.

The results have important policy implications. Policies aiming to reduce soil erosion should go beyond subsidizing erosion control measures and incentives farmers to take erosion-prone areas with low yield potential out of production, that is, a land-use change from agricultural land to permanent grassland or woodland. Policies that increase the price of especially erosion-prone, agricultural land relative to other inputs could incentivize farmers to adjust their factor mix, decrease the overexploitation of land and reduce soil loss. This might be achieved, for

example, by a land tax that increases with increasing risk of erosion. Another policy option is to oblige or subsidize farmers to set aside a proportion of their arable land, especially arable land vulnerable to erosion, and devote it to erosion-friendly uses (e.g., green manure).

Finally, it is important that actions taken against one particular environmental problem do not increase other problems. Agricultural production not only affects soil erosion, but also nutrient and pesticide residue and run-offs, greenhouse gases emissions, water usage, and biodiversity. For instance, a reduction of soil loss through reduced agricultural land use might be achieved by increased fertilizer and pesticide usage. This would allow for a land-use change from agriculture to woodland which not only reduces soil loss, but also improves a farm's carbon balance and increases biodiversity. On the other hand, increased fertilizer and pesticide usage potentially increases environmental and health problems and reduces biodiversity. A limitation of this study is that only one undesirable output is considered. Future research should extend this analysis to multiple bad outputs and analyze the trade-offs among them.

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Appendix

Proof of proposition 1

Step 1: Rewrite Rødseth's (2016) emission minimizing problem in Eq. (8) by inserting the equality constraint for b^c in the objective function:

$$\begin{aligned} & \underset{\lambda,\varepsilon,x}{\min} \ b_{II}^{c^*} = \sum_{i=1}^{N} \lambda_i b_i^c + \varepsilon_{b^c} \\ & s.t. \quad x^k = \sum_{i=1}^{N} \lambda_i x_i^k + \varepsilon_{x^k} \quad k = 1, ..., K \\ & y_o^m = \sum_{i=1}^{N} \lambda_i y_i^m - \varepsilon_{y^m}, \ m = 1, ..., M \\ & \sum_{k=1}^{K} u^k \varepsilon_{x^k} + \sum_{m=1}^{M} v^m \varepsilon_{y^m} - \varepsilon_{b^c} = 0 \\ & \sum_{i=1}^{N} \lambda_i = 1 \\ & \lambda_i, \varepsilon_{x^k}, \varepsilon_{y^m}, \varepsilon_a \ge 0, \ \forall i, k, m \end{aligned}$$

$$(A1)$$

Step 2: Exploit the summing up restriction for the slack variables $\sum_{k=1}^{K} u^k \varepsilon_{x^k} + \sum_{m=1}^{M} v^m \varepsilon_{y^m} - \varepsilon_{b^c} = 0 \text{ and that the convexity constraints of the inputs and desirable outputs can be rewritten as } \varepsilon_{x^k} = x^k - \sum_{i=1}^{N} \lambda_i x_i^k, \ k = 1, \dots, K \text{ and } \varepsilon_{y^m} = \sum_{i=1}^{N} \lambda_i y_i^m - y_o^m, \ m = 1, \dots, M \text{ , to rewrite (A1) as:}$ $\min_{\lambda, \varepsilon, x} \sum_{i=1}^{N} \lambda_i b_i^c + \sum_{k=1}^{K} u^k (x^k - \sum_{i=1}^{N} \lambda_i x_i^k) + \sum_{m=1}^{M} v^m (\sum_{i=1}^{N} \lambda_i y_i^m - y_o^m)$ $s.t. \quad x^k = \sum_{i=1}^{N} \lambda_i x_i^k + \varepsilon_{x^k} \qquad k = 1, \dots, K$ $y_o^m = \sum_{i=1}^{N} \lambda_i y_i^m - \varepsilon_{y^m}, \ m = 1, \dots, M$ $\sum_{i=1}^{N} \lambda_i = 1$ $\lambda_i, \varepsilon_{x^k}, \varepsilon_{y^m}, \varepsilon_a \ge 0, \ \forall i, k, m$ (A2)

Step 3: Rewrite the objective function in (A2) by substituting b_i^c with the expression of controlled emission given by Eq. (2):

$$\sum_{i=1}^{N} \lambda_{i} \left(\sum_{k=1}^{K} u^{k} x_{i}^{k} - \sum_{m=1}^{M} v^{m} y_{i}^{m} - a_{i} \right) + \sum_{k=1}^{K} u^{k} \left(x^{k} - \sum_{i=1}^{N} \lambda_{i} x_{i}^{k} \right) + \sum_{m=1}^{M} v^{m} \left(\sum_{i=1}^{N} \lambda_{i} y_{i}^{m} - y_{o}^{m} \right)$$

$$= \sum_{k=1}^{K} u^{k} x^{k} - \sum_{m=1}^{M} v^{m} y_{o}^{m} - \sum_{i=1}^{N} \lambda_{i} a_{i}$$
(A3)

Step 4: Insert (A3) into (A2):

$$\min_{\lambda,\varepsilon,x} \sum_{k=1}^{K} u^{k} x^{k} - \sum_{m=1}^{M} v^{m} y_{o}^{m} - \sum_{i=1}^{N} \lambda_{i} a_{i}$$

$$s.t. \quad x^{k} = \sum_{i=1}^{N} \lambda_{i} x_{i}^{k} + \varepsilon_{x^{k}} \qquad k = 1, ..., K$$

$$y_{o}^{m} = \sum_{i=1}^{N} \lambda_{i} y_{i}^{m} - \varepsilon_{y^{m}}, \quad m = 1, ..., M \quad .$$

$$\sum_{i=1}^{N} \lambda_{i} = 1$$

$$\lambda_{i}, \varepsilon_{x^{k}}, \varepsilon_{y^{m}}, \varepsilon_{a} \geq 0, \quad \forall i, k, m$$
(A4)

The emission minimization problem accounting for abatement activities that is developed in this article, that is, Eq. (7), can be rewritten by inserting the equality constraint for a into the objective function:

Hence, (A4), the model developed by Rødseth (2016), and (A5), my model, deliver exactly the same solution if the slack of the abatement output in Eq. (7), ε_a , is zero.