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Estimating Conditional Betas and the Price of Risk for a Thin Stock Market

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Abstract

This paper examines the Sharpe-Lintner Capital Asset Pricing Model (CAPM) in which time-varying-parameter models are alternative to the static market model. Prior evidence does not support the CAPM and suggests that market risk is not priced or the price of the beta risk is significantly negative for a thin European stock market, e.g. the Finnish stock market. We show that this phenomenom is due to static ordinary least squares beta estimates that are spurious. We reduce the errors-in-variables problem by estimating the firm-specific betas using the Kalman filter technique and employ the forecasted beta values in cross-sectional analysis. It turns out that in our analysis of pooled data the sign for coefficient of the price of risk becomes positive and we are no longer able to reject the mean-variance efficiency of the market index. The data covers all Finnish common stocks listed on the Helsinki Stock Exchange throughout the years 1972–1989.

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1 Introduction

The CAPM states that expected return on an asset is positively and linearly related to its systematic risk, which is measured by the asset's beta. The Sharpe (1964)–Lintner (1965) version of the model states that

$$E(R_i) = R_f + \beta_i E(R_M - R_f),$$

where $E(R_i) = Expected return on security i$ $R_f = Risk-free rate of interest$ $\beta_i = Systematic risk coefficient (beta) for security i$ $E(R_M-R_f) = Expected excess return on the market over the risk-free rate.$

Actually, the CAPM is not testable as stated in Roll (1977), because the true market portfolio is not observable. Therefore, the CAPM is just a statement about the mean-variance efficiency of a given market portfolio. Thus, we test in empirical analysis whether the observed stock market portfolio is mean-variance efficient. The test is, of course, a joint test that a given portfolio is mean-variance efficient and that the CAPM is the correct model.

Unfortunately, we don't observe the true beta coefficient β_i implied by the CAPM. In the traditional two-pass approach, the beta is estimated by applying Sharpe's well known time-series regression (TSR) model, i.e. the market model, which is expressed below in terms of excess returns:

$$r_{it} = \alpha_i + \beta_i r_{mt} + \varepsilon_{it}$$

r_{it}

where

 α_i = The intercept term,

 β_i = Beta coefficient of asset i,

= the excess return on asset i at time t,

 r_{mt} = The excess return on the stock market portfolio at time t,

 $\varepsilon_{it} = A$ random error term.

In their seminal paper, Fama and McBeth (1973) introduce an iterative technique for estimating the second-pass cross-sectional regression (CSR). They revise the TSR each month in order to get a series of "rolling" beta estimates for each asset and compute the following CSR on the beta estimates for each month:

$$\mathbf{r}_{it} = \mathbf{a} + \lambda_t \hat{\beta}_{it-1} + \mathbf{e}_{it},\tag{3}$$

where

r_{it} = The expected excess return implied by the CAPM on asset i for period t (here monthly return over the entire period analysed),

a = The intercept term (H_0 : a = 0 according to the CAPM),

 λ_t = The risk premium,

 β_{it-1} = The beta coefficient estimated at the previous period,

e_{it} = A random error term.

(2)

(1)

In the literature, the betas are generally estimated from a five year period of time prior to each CSR. The final estimates for the intercept and risk premium are computed as the sample means of the time series of these coefficients. Computation of the standard errors is based on the assumption that the time series of estimates are independent and distributed identically to the means of final estimates. However, we know that the independence assumption is not strictly satisfied due to the measurement error in the beta estimates. We also introduce an errors-in-variables (EIV) problem in the second-pass regression by regressing returns on the betas that are measured with error. Due to the EIV problem, our CSR estimates are biased and inconsistent in small samples (for a review of EIV problems, see e.g. Shanken (1991)).

Most prior studies of Finnish stock market data follow the above approach. These studies do not support the existence of a robust positive risk-return relationship as implied by the CAPM. The most puzzling result is obtained in Malkamäki (1991) with monthly and quarterly stock market data on excess returns. He runs Fama-McBeth OLS regressions in a multifactor context, as in Ferson and Harvey (1991), and finds that the price of market risk is negative and statistically significant.

This paper examines the risk-return relationship implied in the Sharpe-Lintner CAPM using data from the thin Finnish stock market. We estimate the CAPM's systematic risk by employing the traditional OLS rolling beta procedure and, as alternatives, two different kinds of time-varying-parameter models. The time series for the beta coefficient of each stock are estimated by applying Sharpe's (1964) market model. We estimate the rolling OLS betas over five and three-year periods of time. We compute the dynamic beta estimates by applying OLS and maximum likelyhood (ML) Kalman filter techniques.

We proceed by testing whether the market risk, either static or time-varying, is priced by the market. We regress, as usual, expected monthly returns over the estimated beta series. However, we run this regression with pooled return and beta series. This is done by constructing only one composite return vector for all firms' return series and one corresponding beta vector for the entire period analysed here.¹ Therefore, we have in the monthly analysis 3875 observations in these two vectors for the time period 1977:2–1989:12. This implies that our tests for the risk premium have extremely high degrees of freedom, i.e. the tests are powerfull. Our pooled data estimation procedure avoids the above criticism regarding the standard deviations in the univariate tests. The pooled regression also has the nice feature that it gives higher weight to those observations that are highly correlated with each other, as compared to the standard univariate tests. As a final topic in our analysis, we examine whether our assumption of a stable risk premium should be relaxed.

This paper aims to do four things. First, the short term interest rate is computed from the Eurofutures market for the Finnish markka. This enables us to analyse excess returns of this kind for the first time with Finnish stock returns. Second, we compute static and dynamic monthly estimates for the beta time series. Third, we pool the data in order to test the pricing of risk and the potential variation in it. Fourth, the CAPM is tested in its restricted and unrestricted forms

¹ Regression over the pooled data implies an assumption that the cross-sectional and time-series variability (error variance) is the same.

to analyse the acuracy of our beta estimates obtained using different estimation methods.

The remainder of this paper is organised as follows. Section 2 discusses the methodological problems of estimating constant and time-varying betas and the risk premium. Section 3 describes the Kalman filtering technique. The next section describes the data and economic conditions in Finland during the period studied. Empirical results are presented in section 5 and, finally, we present the key findings and draw some conclusions in the section 6.

2 Methodological Aspects of Beta Estimation

2.1 Constant Beta Models

Let us assume that a firm's true beta is constant over time. Now, there are two ways to reduce the measurement error in the TSR. First, we could increase the time series period employed in the beta estimation. On the other hand, we know that betas are non-stationary which implies that five years is already a reasonably long period with respect to beta estimation. This is also a relevant criticism of contemporaneous multivariate tests of the CAPM (see e.g. Gibbons, Shanken and Ross 1989). These tests are statistically efficient but do not allow for time variation in the beta.

The second possibility is to minimize variance of the error term in the TSR. This is most commonly achieved by grouping securities into portfolios if the errors are not perfectly correlated cross-sectionally. The problem is that we should find a sorting variable that is highly correlated with the true betas and uncorrelated with the estimation error. However, Ball and Kothari (1989) and Shanken and Weinstein (1990) show that the grouping of securities may easily lead to spurious results as well. The security grouping approach is actually not available on thin stock markets because there are only a limited number of listed stocks available and different kinds of stock series are involved (e.g. common and preference shares and restricted and unrestricted stock series on the Helsinki Stock Exchange). The potential diversification effect in portfolio formation would be very limited. If we do not form portfolios, we have to face another statistical problem: non-normality of certain individual asset returns.

There are two additional problems when applying the two-pass regression approach in the analysis. These are the possible existence of autocorrelation in the TSR residuals and heteroscedasticity in the TSR and CSR residuals. The problem with autocorrelation in TSR residuals is usually reduced by measuring the returns over one month intervals, instead of using shorter intervals. If the residual variance turns out to be changing, one common solution is to use the weighted least squares regression method. Another solution is to apply conditional asset pricing models.

2.2 Time Varying Beta Models

Time variation of the market risk has been documented recently by a number of reserchers. We have, in fact, at least three relevant estimation procedures available when modeling the time variation in the betas. Bollerslev, Engle and Wooldridge (1988) and Ng (1991) employ different versions of the multivariate generalized autoregressive conditional heteroskedasticity (GARCH) method in modelling the conditional covariances as a function of past conditional covariances. However, Nelson (1991) states that there are at least three major drawbacks involved in the GARCH models and developes a univariate exponential ARCH model that does not suffer from these drawbacks. A multivariate version of his univariate model or some other satisfactory improvement on the ARCH models is still needed to avoid these problems when applying the models in asset pricing applications.

Harvey (1989) applies the generalized method of moments (GMM) method to allow conditional covariances to vary in a test of the CAPM. This procedure involves expected returns conditional on the true market information set. A problem here is that we do not observe the true market information set. Instead, we find a subset of observable variables that are called instrumental variables. Further, we assume in the GMM applications that a linear function relates conditional expectations to the information set.

The time-varying parameter (TVP) models are the third possibility to control for the time-variation in the betas. We can estimate TVP models by applying the Kalman filter technique. This technique gives us an insight into how a rational investor would revise his beta estimates in a Bayesian fashion when new information is available. A driving economic force behind the time-varying beta coefficient could be, for example, a change in leverage or riskiness of investment projects of a firm. Knif (1989) applies the Kalman filter technique to model time variation of the firm specific market risk in Finnish common stock data. He finds that the betas are clearly time varying. However, the most betas of Finnish common stocks follow a stationary autoregressive process.

3 The Kalman Filter

We apply four different estimation procedures to compute the betas. We run the OLS regressions by applying the market model of equation three in order to get the rolling beta estimates. We compute the betas from five and three year time periods prior to each cross-sectional regression. We estimate the market model also by applying the dynamic Kalman filter OLS and ML estimation procedures that account for time variation in the betas. Our first Kalman filter application is the OLS random walk (for the OLS version, see e.g. Doan, Litterman and Sims (1984), Cuthbertson (1988) and Knif (1989)). In this approach, only ex ante and current information are used in evaluating the initial values for the filtering and in updating the parameter vector and its covariance matrix in the Kalman equations. This is in accordance with the reality, where investors try to evaluate estimates for a beta conditional on the information available at the time. The market model is now conveniently written in state space form as

$$\mathbf{r}_{it} = \mathbf{X}_{t}^{*} \boldsymbol{\theta}_{t} + \boldsymbol{\varepsilon}_{t}, \tag{4}$$

where $X_{t}^{*} = [1, r_{mt}]$ $\theta_{t}^{*} = [\alpha_{it}, \beta_{it}]$ $\varepsilon_{t}^{*} = A$ random error with variance v_{t} .

The parameter vector θ_t is assumed to vary over time according to random walk transition equation

$$\theta_t = \theta_{t-1} + u_t, \tag{5}$$

where $u_t = A$ random error with covariance matrix M_t

Random errors ε_t and u_t are independent of each other. The corresponding variance v_t and covariance matrix M_t are assumed to be known, i.e. we estimate them. If we also have initial values for θ_{t-1} and its covariance matrix Σ_{t-1} , then the updated estimates for the Σ_t and θ_t , given r_{it} and X_t , are:

$$\Sigma p = \Sigma_{t-1} + M_t, \tag{6}$$

where Σp = One-step-ahead prediction based on the prior information for the covariance matrix of the new parameter vector.

$$F = X_t \Sigma p X_t + v_t, \tag{7}$$

where F = One-period prediction for the variance of the new parameter vector.

$$K_t = \sum p X_t F^{-1}$$
,

where $K_t = Kalman$ gain, i.e. the correction weight based on the one-step-ahead prediction for the covariance matrix Σp and variance F.

$$\tilde{\mathbf{r}}_{it} = \mathbf{r}_{it} - \mathbf{X}_t \boldsymbol{\theta}_{t-1}, \tag{9}$$

where \tilde{r}_{it} = One-step-ahead prediction error.

$$\Sigma_{t} = \Sigma_{p} - \Sigma_{p} X_{t} F^{-1} X_{t} \Sigma_{p}, \qquad (10)$$

where Σ_t = Updated estimate of the covariance matrix of the new parameter vector.

$$\theta_{t} = \theta_{t-1} + K_{t} \tilde{r}_{it}, \tag{11}$$

where θ_t = Updated estimate for the parameter vector.

The initial values for V_t , M_t , θ_{t-1} and Σ_{t-1} , as well as parameters for tightness in the Kalman filter estimation, were obtained by the method suggested in Doan, Litterman and Sims (1984). We estimated the initial values through an ordinary least squares regression for the market model over the period 1972:2-1975:1. The initial estimate for the variance V_t was weighted by 0.9 and the relative tightness on time variation for the parameter vector was assumed to be 0.1. The initial covariance matrix was assumed to be that of the OLS estimation, which implies that overall tightness was assumed to be one. The Kalman filter estimation covered the period of 1975:2–1989:12. As one observes, we use only ex ante and current information in this Kalman filter technique. This is in accordance with the real situation, where investors evaluate the time-variation in the betas.

Our maximum likelihood Kalman filter procedure is based on the study of Knif (1989); see also Goodrich (1989) and Berglund and Knif (1991). Knif found that Finnish common stock betas change according to a stationary first order autoregressive (AR1) process with a constant coefficient. The parameter vector is now assumed to vary according to the AR1 model, that is,

$$\theta_t - \overline{\theta} = F(\theta_{t-1} - \overline{\theta}) + u_t$$
 (12)

where $\overline{\theta}$ = The mean vector of the parameters F = The weights for the AR1 and mean parameters u_t = A random error with covariance matrix M_t.

The state space representation for the market model is now

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(8)

and for the parameter vector

$$\gamma_{t} = \begin{bmatrix} \overline{\theta} \\ \theta_{t} & -\overline{\theta}_{t} \end{bmatrix} = \begin{bmatrix} I & 0 \\ 0 & F \end{bmatrix} \begin{bmatrix} \overline{\theta}_{t-1} \\ \theta_{t-1} & -\overline{\theta}_{t-1} \end{bmatrix} + \begin{bmatrix} 0 \\ u_{t} \end{bmatrix}$$

$$= A\gamma_{t-1} + e_{t}$$
(14)

where
$$\underline{F} = \underline{D}iag [\omega_1, \omega_2]$$

 $\theta_1 = \theta_{t-1}$ for all t
 $e_t = A$ random error with covariance matrix N_t

We need to revise only the following updating Kalman equations

$$\Sigma_{p} = A_{t}\Sigma_{t-1}A_{t}' + N_{t}$$
⁽¹⁵⁾

where Σ_{t-1} = The covariance matrix of γ_{t-1} .

$$\tilde{\mathbf{r}}_{it} = \mathbf{r}_{it} - \mathbf{X}_t \mathbf{A}_t \gamma_{t-1} \tag{16}$$

$$\gamma_t = A_t \gamma_{t-1} + K_t \tilde{r}_{it} \tag{17}$$

Our AR1 model collapses into the random walk model if the A matrix is equal to one. However, the estimation technique is now quite different. In the first phase, we compute a maximum likelyhood solution for the parameter vector through the above forward recursive Kalman equations that use only past and current information. Next, we use information from the whole sample period and find another set of ML estimators by applying the backward recursions of the Kalman smoother, see Goodrich (1989) and for details. As a final stage, we employ the mean reverting AR(1) model to compute the forecasted beta series. We run the second-pass regression over the forecasted betas in order to reduce the EIV problem, at least to some extent. This will be the case if the changing residual variance of the market model is dependent on the time-variation in the betas.

4 The Data

The stock market data employed here consist of end-of-month excess returns for all the common stocks listed on the Helsinki Stock Exchange (HSE) for the whole period covered, 1972:2–1989:12 (Table 1). The availability of short term interest rate data prior to 1972:1 was the limiting factor. The HSE general index used here is value weighted and described in Berglund – Wahlroos – Grandell (1983). Prices are corrected for cash dividends, splits, stock dividends and new issues. The correction is based on the principle that all income from a stock is reinvested in the stock with no transaction costs. In this study, returns are measured as changes in logarithmic indices.

Table 1

Firms included in the analysis. This sample includes all restricted ordinary share series listed during the whole period of 1972:2–1989.

Firm	Designation
Don't of Åland I td V	
Balik Of Alaliu Llu K	AD
Enoa-Finland Steamsip Co Ltd K	EFFU
Enso-Guizeit Ltd A	ENSOA
Fiskars Corporation	FISKK
Huhtamäki Corporation K	HUHTK
Instrumentarium Corporation	INSTA
Kemi Corporation	KEMI
Kesko Corporation	KESK
KANSALLIS-OSAKE-PANKKI	KOP
Kymmene Corporation	KYMI
Lassila & Tikanoja Ltd	LASS
Lohja Corporation A	LOHJA
Nokia Corporation	NOKIK
Otava Publishing Company Ltd	OTAVK
Partek Corporation	PART
Rauma-Repola Corporation	RAUM
Finnish Sugar Co Ltd I	SOKEI
Stockman A	STOCA
Suomen Trikoo Corp. A	TRIK
Union Bank of Finland Ltd A	SYPA
Tamfelt Group K	TAMF
Tampella Ltd	TAMP
Talous-Osakekauppa Co	TAOK
Wärtsilä Co I	WARTI
United Paper Mills Ltd K	YHTYK

It is convenient to run asset pricing tests in the excess returns form. To do this, we constructed a short term interest rate which we were able to employ for the first time in studies of Finnish asset market returns (Figure 1). The Bank of Finland created the market for US dollar forwards in January 1972. Since then, the shortest maturity continously traded monthly is a three month forward

contract. To compute the end-of-month time series for a three month interest rate, we collected end-of-month data on three month currency forward prices, currency spot rates and US dollar interest rates. The three month interest rate for the Finnish markka was then computed by using the standard formulas. However, in the monthly analysis we still had to use the one-month return in the three-month Euromarket return for the Finnish markka, i.e. we assume that interest rate yield curve is flat between the one and three month maturities.

Figure 1.

Approximated three month interest rate on the Finnish markka, 1972–1989



As seen in figure 1, the short term interest rate was extremely volatile in the 1970s after the first oil crisis. There was a recession in Finland after the crisis, and on several occasions speculation occurred concerning a possible devaluation of the Finnish markka. The Bank of Finland devaluated the markka two times in 1977 and once again in February 1978, which reduced considerably the volatility of short term interest rates. The end of February 1978 is also the first point at which we apply Chow's (1983) test to examine whether the assumption of constant price of risk should be relaxed. Our hypothesis is that major changes in economic conditions are likely to change the pricing of market risk. However, we do not argue that the risk premium is constant over any period.

Table 2.

Summary statistics for the excess returns
(in percentages per month) for 1972:2-1989:12
(215 observations)

Asset	Mean	$\sigma_{\rm m}$	Skewness	Kurtosis
AB	0.746	10.683	1.332	16.702
EFFO	0.423	8.204	0.348	1.448
ENSOA	-0.234	7.922	0.645	3.114
FISKK	1.292	7.252	0.296	1.959
HUHTK	0.782	6.610	1.056	2.655
INSTA	1.156	7.118	0.607	3.206
KEMI	-0.360	10.646	-0.694	4.457
KESK	0.658	5.147	1.060	2.481
KOP	0.104	6.644	0.751	4.821
KYMI	-0.002	6.410	0.597	1.908
LASS	1.298	9.240	1.336	7.143
LOHJA	0.930	7.333	0.141	0.295
NOKIK	-0.009	6.910	0.159	0.684
OTAVK	1.234	9.496	1.773	10.212
PART	0.522	6.594	0.242	0.555
RAUM	0.034	6.741	1.042	2.112
SOKEI	0.694	8.094	0.762	2.001
STOCA	0.895	6.645	0.521	2.684
SYPA	0.433	6.083	1.230	4.425
TAMF	0.717	9.835	-0.486	6.468
TAMP	0.051	7.788	1.276	5.215
TAOK	1.866	9.520	-0.031	1.863
TRIK	0.136	11.697	0.255	6.330
WARTI	0.613	7.480	0.764	1.155
YHTYK	0.707	7.459	0.380	0.934
VWI ^a	0.254	4.230	0.265	0.976

^a The stock market index return.

Summary statistics of monthly excess returns for 25 firms and for the market index are shown in Table 2. Statistics are reported also for three subperiods according our structural analysis: 1972:2–1978:2, 1978:3–1984:3 and 1984:4–1989:12 (see Appendix 1). The statistics show us that the mean varied greatly as between periods. The monthly return distribution is, on the average, always somewhat skewed to the right and leptokurtic, as is usual. The first period ends with the third devaluation of the markka descriped above. The second period ends in 1984:3 for two reasons: First, unrestricted shares, i.e. shares that foreign investors are allowed to buy, have been listed separately on the Helsinki Stock Exchange since January; 1984. This may have changed the pricing of Finnish stocks. Another major change was made by the Bank of Finland, which first gave foreign banks access to central bank financing April; 1984. This meant in practice that competition was greatly enhanced in the Finnish money market.





We selected five additional economic changes that could affect the risk return relationship. The first of them occurred at the end of December 1981 when the stock market index started its rapid raise (Figure 2). Another break point occurs at the end of October 1982. The Finnish markka was devaluated twice in that month. The third change was associated with a partial abolition of the regulation of average rates on bank lending to the public. This change took place at the end of April 1983 and increased banks' activity in the money market. The next potential break point, after March 1984, is at the end of December 1986, when the market for certificates of deposit were introduced in Finland. The last stability test is computed because of the crash of October 1987.

5 Empirical Results

5.1 Market Risk Estimates

We carry out here the well known "rolling" beta estimation method introduced in Fama and McBeth (1973). We estimate the betas with the traditional market model described in the equation 2. Since the market risk is known to be non-stationary, we compute the OLS betas for three-year periods as well as for the traditional five year period. Furthermore, we also employ the OLS and ML Kalman filter techniques, which allow for conditional time variation in the betas.

Firm	5 year beta Mean	σ _m	3 year beta Mean	σ _m	KF RW Mean	σ _m	KF AR1 Mean	σ _m
AB	0.655	0.146	0.627	0.143	1.014	0.127	0.748	0.000
EFFO	0.614	0.175	0.553	0.250	1.254	0.248	0.888	0.005
ENSOA	0.758	0.258	0.767	0.406	1.377	0.186	1.010	0.005
FISKK	0.657	0.194	0.630	0.274	0.759	0.055	0.795	0.005
HUHTK	0.948	0.436	0.918	0.495	0.577	0.195	0.495	0.018
INSTA	0.872	0.106	0.910	0.164	0.416	0.205	0.868	0.002
KEMI	1.171	0.598	1.134	0.821	0.875	0.074	0.913	0.037
KESK	0.556	0.139	0.576	0.202	0.424	0.174	0.670	0.024
KOP	1.136	0.223	1.083	0.325	1.193	0.074	1.069	0.001
KYMI	1.008	0.137	1.088	0.241	0.284	0.344	0.935	0.009
LASS	0.754	0.194	0.751	0.279	0.351	0.132	0.711	0.021
LOHJA	1.231	0.131	1.210	0.241	0.979	0.052	1.202	0.010
NOKIK	1.112	0.224	1.157	0.293	0.851	0.128	1.074	0.006
OTAVK	0.543	0.392	0.479	0.297	1.421	0.010	0.684	0.102
PART	1.020	0.194	0.989	0.309	0.838	0.096	1.086	0.002
RAUM	1.103	0.208	1.071	0.304	1.377	0.201	0.993	0.011
SOKEI	0.932	0.145	0.888	0.225	1.173	0.152	0.928	0.010
STOCA	0.879	0.194	0.921	0.346	0.572	0.088	0.870	0.003
SYPA	0.940	0.091	0.912	0.135	1.398	0.216	1.010	0.018
TAMF	0.967	0.520	0.971	0.720	0.781	0.063	0.908	0.101
TAMP	0.935	0.462	0.935	0.553	0.710	0.040	0.935	0.063
TAOK	0.471	0.326	0.607	0.599	-0.124	0.397	0.474	0.002
TRIK	1.005	0.212	0.901	0.556	1.184	0.178	1.042	0.388
WARTI	1.307	0.329	1.300	0.460	0.572	0.131	1.001	0.000
YHTYK	1.278	0.186	1.247	0.304	0.963	0.108	1.153	0.011
MEAN	0.914	0.249	0.905	0.358	0.849	0.147	0.899	0.034
St.dev.	0.237	0.135	0.231	0.178	0.402	0.092	0.186	0.079

Table 3.Summary statistics for estimated beta series(155 observations per series)

We revise all the beta estimations monthly. The first five-year period for beta estimation is 1972:2–1977:1 and the corresponding three year period is 1974:2–1977:1. We then proceed by dropping and adding one observation and repeating the computation. Table 3 presents summary statistics for all the beta

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series. The time series for three-year betas are more volatile than those for fiveyear betas. Surprisingly, both the Kalman filtered beta series are a lot less volatile, specially the ML betas, than the static estimates for the betas. Correlation between the monthly beta series is highest for the static betas and lowest between the static betas and the OLS (RW) Kalman filter betas (Table 4).

Variable	B5Y	B3Y	BKFRW	BKFAR1
B5Y	1.000			
B3Y	0.756	1.000		
BKFRW	0.023	-0.050	1.000	
BKFAR1	0.430	0.311	0.417	1.000

Correlation matrix for estimated beta series (3875 observations)

Variables in the cross-moment matrix:

B5Y	=	Five-year beta estimation period.				
B3Y	=	Three-year beta estimation period.				
BKFRW	=	Kalman filter (RW) beta.				
BKFAR1	=	Kalman filter (AR1) beta. This series contains				
		forecasted betas $(\beta_{+} = \omega \beta_{+-1} + (1-\omega)\overline{\beta})$				

A closer look at the estimated beta series was found to be very interesting. For this purpose, we took three beta series for a firm in the same figure and reported the mean value for the AR1 beta estimates (see Appendix 2). By looking at these figures one sees immediately that the magnitude of variation in the statically estimated beta series is extremely high. These beta estimates typically vary between 0.3 and 2.0, five-year betas having a slightly lower range of variation. It is somewhat perplexing that an ongoing firm's beta could vary this much. Furthermore, shocks to the beta estimates seem to persist over time. This is evident in the beta estimates for the forest industry companies (Kemi, Kymi, Tamf, Tamp and Yhtyk). The Finnish markka was devaluated in April 1977. This shock caused a dramatic drop in the betas after three or five years, depending on the length of the estimation period.

The series for both the RW (OLS) and AR1 (ML) Kalman filter betas are more stable by nature, as was, of course, expected for the AR1 beta series that are mean reverting. The AR1 maximum likelihood estimation results are available in Appendix 3. Our ML beta estimates are even more mean reverting than those of Knif (1989:154). The beta values for a firm typically vary within the range of 0.2. However, the Random Walk OLS beta series do display dramatic jumps in the beta values in the late 1980s and particularly in 1989.² This indicates that there has been a rapid change in investors' expectations regarding the future earnings of certain companies. There are several reasonable explanations for this

Table 4.

 $^{^2}$ Note that the scale in the figures is extremely large for the Kalman filter betas. This creates the impression that the Kalman filter series hardly varies at all before the mid 1980s.

phenomenom: First, the collapse of trade with the Soviet Union, which had a drastic impact on only certain companies. Second, the suggestion of the EEC to start negotiations with the EFTA countries in order to create a large European Economic Area. Third, the revaluation of the Finnish markka in March 1989. Fourth, the Bank of Finland raised the cash reserve requirement several times, which reduced banks' earnings.

5.2 Pricing of Risk

The Sharpe-Lintner version of the CAPM is usually tested by iterating the CSR described in equation 4. We computed this regression over all periods t in one regression on pooled data instead of iterating monthly. We estimated the model with and without the constant. Strictly speaking, we assume that the CAPM holds in the restricted version of the model and obtain an estimate of the risk premium implied by the CAPM. Consequently, the unrestricted regression is, strictly speaking, a test of the mean-variance efficiency of the market index or a test of the risk premium implied by one-factor capital asset pricing model, where the prespecified factor is the market index.

Table 5 gives the outcome of these regressions. We find that the estimated risk premium of the restricted regressions is positive and highly significant. The regressions on the Kalman filter beta series have the highest t-values. However, the ML beta forecasts capture clearly better the variation of the excess returns. Note also that the annual market index excess return for the whole period is about 25 %.

The three first unrestricted regressions imply that the CAPM is not valid or the index is not mean-variance efficient because the constant has significant tvalues. Surprisingly, the risk premium is negative and highly significant for the regression on five year beta estimates. This supports the results of Malkamäki (1991). These betas have been commonly employed in the CSR's for about fifteen years to test the validity of the CAPM for thin markets. However, the three-year and OLS Kalman filter beta regressions do not give significant estimates for the negative risk premium.

The fourth regression on the forecasted ML betas gave quite different results. The constant is not significant i.e. we do not reject the mean-variance efficiency of the market index. Furthermore, the coefficient of the price of risk is now positive, as in the CAPM, but not statistically significant.

We assumed in the above tests that the risk-return relationship does not change over time. However, it is well known that this is not the case. Our pooled data enables us to test whether some prespecified structural break points in Finnish economy have affected the pricing of risk. We described the potential breaks to be tested in Chapter 4. We carried out the well-known Chow tests for structural stability (Chow 1983). The model here is always estimated with a constant. A test for a break always covers two years of data before and after the break. This implies that we have 1196 degrees of freedom in the F-value analysis. The outcome of these tests is presented in Table 6. The evidence is very straight forward. The risk premium is not stable over time. We have at least five clear breaks in the risk-return relationship for our entire period. The outcome was almost exactly the same regardless of the beta series employed. Monthly average risk premiums associated with the stock market general index (in percent per month) for 1977:2–1989:12 (3875 observations for 25 ordinary shares)

Model	a ^c	λ ^c	o ^{cd}
Restricted ^a			
5 year beta	-	0.696 (5.35)	7.975
3 year beta	-	0.684 (5.41)	7.975
Kalman filter RW Ex ante	-	0.768 (5.71)	7.971
Kalman filter AR1 ML	-	0.949 (6.84)	7.957
Unrestricted ^b			
5 year beta	1.791 (5.20)	-0.994 (-2.84)	7.949
3 year beta	1.295 (4.57)	-0.456 (-1.63)	7.954
Kalman filter RW Ex Ante	1.128 (3.99)	-0.290 (-0.98)	7.956
Kalman filter AR1 ML	0.615 (1.05)	0.297 (0.468)	7.957

a. Model estimated: $r_{it} = \lambda \beta_{it-1} + e_{it}$ i = 1, ..., 25t = 1, ..., 155

b. Model estimated: $r_{it} = a + \lambda \beta_{it-1} + e_{it}$ i = 1, ..., 25t = 1, ..., 155

c. All the coefficients are multiplied by 100.

d. Standard error of estimate

Suggested b	reak at the end	F-value	P-value
February	, 1978	33.05	0.00
December	, 1981	15.96	0.00
October	, 1982	0.02	0.98
April	, 1983	13.40	0.00
March	, 1984	11.10	0.00
December	, 1986	0.36	0.70
September	, 1987	. 32.50	0.00

Chow tests for structural breaks in the risk return relationship

Model estimated: $r_{it} = a + \lambda \beta_{it-1} + e_{it}$.

Table 6.

The model is estimated for a two year period before and after a tested break point and for the combined four year period. The F-tests have 1196 degrees of freedom.

Next, we did the same regression analyses as above but for subperiods (see Table 7). The periods are based on the empirical finding in Malkamäki (1991) that the risk premium varied around zero between 1978:3 and 1984:3 and were clearly negative after 1984:3. The first period is quite short. It was included because the break at the end, 1978:2, is extremely significant. All regressions gave the same result for the middle period: the risk premium is not significant. However, the regression on ML betas has a positive sign for the price of risk. The period after 1984:3 is interesting. The price of risk was negative and clearly significant in the regressions computed over the static estimates for betas. The risk premium has a negative sign in the Kalman filter beta regressions but the statistics show no significance. Our last time period studied excludes the periods before 1978:3 and after 1988:12. The latter period is excluded according to drastic slowdown of the Finnish economy that started in the early 1989. The risk-return relationship implied by the CAPM is strongest for this period. The regression on ML beta series has a t-value of 1.60 for the risk premium coefficient and does not reject the mean-variance efficency of the market index.

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Monthly average risk premiums associated with the stock market general index (in percent per month) for a set of subperiods

Period	a ^a	λ ^a	o ^{ab}					
77:2-78:2	77:2-78:2							
5 year beta	-2.416 (-2.03)	0.614 (0.51)	5.904					
3 year beta	-2.244 (-3.11)	0.401 (0.64)	5.912					
Kalman filter RW	-1.765 (-1.70)	-0.074 (-0.07)	5.916					
Kalman filter AR1	0.475 (0.304)	-2.550 (-1.51)	5.895					
78:3-84:3								
5 year beta	1.861 (4.43)	-0.54 (-1.35)	7.093					
3 year beta	1.357 (4.02)	-0.020 (-0.65)	7.097					
Kalman filter RW	1.910 (3.90)	-0.663 (-1.24)	7.094					
Kalman filter AR1	0.258 (0.34)	1.205 (1.45)	7.092					
84:4-89:12								
5 year beta	2.772 (4.37)	-2.185 (-3.12)	8.967					
3 year beta.	2.232 (3.81)	-1.559 (-2.42)	8.977					
Kalman filter RW	1.034 (2.62)	-0.149 (-0.37)	8.992					
Kalman filter AR1	0.962 (0.98)	-0.056 (-0.05)	8.993					
78:3-88:12								
5 year beta	2.428 (6.72)	-1.053 (-2.89)	7.986					
3 year beta	1.829 (5.96)	-0.399 (-1.31)	7.998					
Kalman filter RW	1.446 (4.33)	0.024 (0.07)	7.997					
Kalman filter AR1	0.472 (0.74)	1.11 (1.60)	7.993					

Model estimated: $r_{ii} = a + \lambda \beta_{ii-1} + c_{ii}$

a. All the coefficients are multiplied by 100.

b. Standard error of estimate.

6 Conclusions

We did an empirical analysis of the Sharpe-Lintner version of the CAPM for the thin Finnish stock market. Two unconditional and conditional sets of the market risk parameters of firms were computed. The unconditional beta of a firm was computed by the traditional OLS rolling beta technique, assuming that the beta is constant over a period of five/three years. As an alternative approach we applied dynamic OLS and ML Kalman filter techniques that account for time variation in the market risk. We found that the mean of returns, the systematic risk and pricing of the systematic risk vary through time. We also found again the puzzling prior result that the regression on the static OLS betas give us a negative and statistically significant coefficient for the risk premium. We show that this phenomenom is strongest after April 1984. Our ML Kalman filter betas also have extreme difficulties in explaining anything for that period. More research is needed to explain this phenomenom. However, our ML Kalman filter beta estimates are clearly able to capture best the excess returns on Finnish shares. In the restricted regressions, the regression ran over these betas had the largest risk premium, as well as the highest t-value. In the unrestricted regressions, the regression on the ML betas was the only one with a positive coefficient for the risk premium and contained also relatively high significance when we excluded extraordinary periods of the Finnish economy from the analysis. Furthermore, this regression does not reject the mean-variance efficiency of the market index, as the others do. In further research, it would be useful to examine whether our results are robust for other samples of firms. It is also quite evident that the constant risk premium assumption should be relaxed.

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Appendix 1.1

Asset	Mean	σ _m	Skewness	Kurtosis
AB	-0.234	11.341	-0.891	5.441
EFFO	-0.758	6.695	-0.243	1.797
ENSOA	-1.732	8.098	-0.027	3.707
FISKK	0.199	6.573	-0.103	0.044
HUHTK	-0.157	5.375	2.353	8.174
INSTA	0.623	7.574	0.343	0.517
KEMI	-1.191	8.916	0.162	1.704
KESK	-0.434	5.058	1.772	4.584
KOP	-0.857	6.867	0.063	0.404
KYMI	-0.926	6.521	0.231	2.054
LASS	-0.069	8.549	2.660	13.570
LOHJA	-0.215	7.519	0.648	0.988
NOKIK	-0.738	6.290	0.180	0.742
OTAVK	0.967	11.330	2.331	13.188
PART	-0.829	6.709	-0.007	0.096
RAUM	-0.881	7.280	1.131	1.873
SOKEI	-0.375	7.859	0.849	1.956
STOCA	-1.082	5.825	0.650	1.750
SYPA	-0.077	6.822	1.143	2.630
TAMF	-0.913	12.530	-0.756	4.601
TAMP	-2.466	6.961	0.071	0.501
TAOK	2.786	8.880	0.760	2.176
TRIK	-0.739	8.292	1.057	3.638
WARTI	-1.414	7.328	0.700	1.242
YHTYK	-0.483	7.854	0.421	0.466
VWI ^a	-0.721	4.406	0.942	2.167

Summary statistics for the excess returns, (in percentages per month) for 1972:2–1978:2 (73 observations)

^a The stock market index return.

Appendix 1.2

Asset	Mean	Std.	Skewness	Kurtosis
AB	1.263	7.092	0.067	2.436
EFFOA	0.655	6.433	-0.338	2.210
ENSOA	0.307	5.710	0.983	2.273
FISKK	0.931	5.492	0.108	1.176
HUHTK	2.584	7.120	0.992	3.180
INSTA	2.318	5.577	1.938	5.857
KEMI	-1.538	12.402	-1.469	5.919
KESK	0.748	3.368	-0.118	0.329
KOP	1.538	6.459	2.683	13.159
KYMI	0.178	5.365	0.512	2.742
LASS	1.993	6.848	0.029	1.367
LOHJA	2.052	6.423	-0.183	0.790
NOKIK	0.645	6.016	0.112	2.406
OTAVK	1.459	5.017	-0.090	1.482
PART	1.311	4.980	1.299	3.060
RAUM	0.680	6.502	1.264	2.163
SOKEI	2.189	7.682	0.820	1.867
STOCA	2.333	6.608	0.502	6.768
SYPA	1.005	5.551	2.423	13.827
TAMF	1.853	6.335	1.338	3.601
TAMP	0.659	6.517	0.695	3.246
TAOK	2.388	9.657	-0.332	3.069
TRIK	1.421	12.346	-1.345	10.440
WARTI	2.813	7.230	0.681	0.538
YHTYK	1.672	7.087	0.512	1.865
VWI ^a	1.172	3.278	0.000	2.024

Summary statistics for the excess returns (in percentages per month) for 1978:3–1984:3 (73 observations)

^a The stock market index return.

Appendix 1.3

Asset	Mean	Std.	Skewness	Kurtosis
AB	1.236	12.885	3.124	21.096
EFFO	1.427	10.860	0.442	0.010
ENSOA	0.776	9.476	0.982	4.491
FISKK	2.830	9.166	0.212	1.523
HUHTK	-0.131	6.926	0.400	-0.257
INSTA	0.490	7.974	0.590	4.397
KEMI	1.766	10.143	0.274	0.629
KESK	1.718	6.468	0.654	0.815
KOP	-0.397	6.431	-0.251	0.953
KYMI	0.784	7.228	0.896	1.039
LASS	2.008	11.774	0.937	4.501
LOHJA	0.954	7.859	-0.021	-0.151
NOKIK	-0.211	8.309	0.198	-0.181
OTAVK	1.280	11.003	1.028	1.963
PART	1.118	7.740	0.176	-0.319
RAUM	0.321	6.380	0.876	3.277
SOKEI	0.245	8.629	0.770	2.655
STOCA	1.466	7.073	0.373	0.642
SYPA	0.367	5.822	0.457	-0.182
TAMF	1.241	9.549	0.316	4.861
TAMP	2.073	9.125	1.986	5.879
TAOK	0.340	9.973	-0.261	0.593
TRIK	-0.298	13.915	1.176	3.198
WARTI	0.429	7.363	1.175	2.586
YHTYK	0.944	7.350	0.342	1.260
VWI ^a	0.314	4.737	0.042	0.241

Summary statistics for the excess returns (in percentages per month) for 1984:4–1989:12 (69 observations)

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^a The stock market index return.

Appendix 2

Monthly Beta Series for 25 Firms



























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Appendix 3

STOCK	ω	β	q	σ ²	α	R ²	P(F)
AB	0902	.7483*	.0016	.0104	.0049	.0954	.9995
EFFO	0227	.8885*	.4523	.0046	.0035	.1844	1.0
ENSOA	.0172	1.0106*	.6726	.0035	0052	.2575	1.0
FISKK	.0322	.7953*	.2926	.0035	.0126*	.2258	1.0
HUHTK	.4469*	.9676*	.4967	.0019	.0020	.2981	1.0
INSTA	0346	.8680*	.0989	.0036	.0097*	.2580	1.0
KEMI	0797	· .9139*	1.1405	.0079	0057	.1317	1.0
KESK	2138	.6707*	.1303	.0016	.0055*	.2955	1.0
KOP	.0027	1.0664*	.3458	.0016	0031	.3859	1.0
KYMI	.0694	.9342*	.2063	.0022	0013	.3590	1.0
LASS	.2163	.7103*	.1765	.0074	.0120*	.0938	.9994
LOHJA	0785	1.2017*	.0221	.0026	.0073*	.4318	1.0
NOKIK	0526	1.0748*	.1426	.0025	0036	.4354	1.0
OTAVK	.1064	.6889	2.8235	.0035	.0116*	.1357	1.0
PART	0104	1.0863*	.2200	.0021	.0031	.4179	1.0
RAUM	0472	.9927*	.3495	.0022	0038	.3930	1.0
SOKEI	.0329	.9927*	.5949	.0039	.0050	.2550	1.0
STOCA	0626	.8699	.0788	.0030	.0072	.2844	1.0
SYPA	.0431	1.0106*	.5339	.0011	.0011	.5006	1.0
TAMF	.3272	.9094*	.9270	.0062	.0079	.1870	1.0
TAMP	.7896*	.9484	.0262	.0045	.0006	.2410	1.0
TAOK	.0383	.4740	.1097	.0085	.0176*	.0419	.8982
TRIK	2379	1.0390*	4.5252	.0050	.00005	.1222	1.0
WARTI	.2530	1.001*	.0009	.0038	.0044	.3001	1.0
YHTYK	.0587	1.1527*	.3089	.0026	.0052	.4426	1.0

Maximum likelihood estimation results for the Kalman filter AR1 specification (estimation period 1972:2–1989:12)

Estimated model: $r_{it} = \alpha_t + \beta_t r_{mt} + \epsilon_t$

1	V	
where	$\alpha_{t} = \text{constant}$	$var(\varepsilon_{1}) = O^{2}$
	$\beta_{t} = \omega \beta_{t-1} + (1-\omega)\overline{\beta} + v_{t}$	$var(v_i) = q$

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