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## Production and employment in the BOF4 quarterly model of the Finnish economy

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PRODUCTION AND EMPLOYMENT IN THE BOF4  
QUARTERLY MODEL OF THE FINNISH ECONOMY

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## ABSTRACT

This paper contains a description of the production and labour demand sections of the BOF4 model. CES value added production functions are developed and estimated for the five sectors of the economy. From these the marginal product of labour and capital functions are derived which are important factors in determining investments and the prices of gross outputs in each of the sectors. The demand for labour hours is defined as a gradual adjustment process towards the level determined by the inverted production functions. An input-output model is used to determine output and value-added deflators by sectors as well as the prices of the different demand components.



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## 1 INTRODUCTION

The BOF4 model of the Finnish economy is a quarterly econometric model developed at the Bank of Finland for forecasting and policy analysis.<sup>1</sup> The present paper appears in a series intended to cover all sectors of the present version of BOF4. This report describes a part of the supply side of the model, namely the production functions and technology, the determination of sectoral outputs and labour demand. Exports and imports have been described in Tarkka and Willman (1988). Consumption and investment, the rest of the supply side i.e. labour supply, wages and prices, the government sector and the financial markets will be described in forthcoming reports.

First, the technological assumptions of the model and the estimation of the sectoral CES-production functions are described. Production functions are used to calculate the marginal costs of production and the marginal products of fixed capital, which drive the price and investment equations of the model. Second, we describe the use of an input-output model to determine the relation between production prices and value-added deflators on the other hand and output by sectors on the other. Inverted production functions are used to solve for required labour inputs. The modelling of the demand for work hours and the determination of employment consists the third part of the paper.

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<sup>1</sup>The earlier version of the model, BOF3, is documented in Tarkka and Willman (1985).



## 2 PRODUCTION FUNCTIONS AND TECHNOLOGY

### 2.1 The General Modelling Strategy

In BOF4, production is disaggregated into the following five sectors:

Table 1

Sector	Code in BOF4	1985 share in GDP
- Agriculture	1	4.4 %
- Forestry	3	3.7 %
- Manufacturing	4	25.4 %
- Private services etc.	2	49.8 %
- Government services	G	16.8 %

Manufacturing includes mining, and the private services sector includes construction, electricity, gas and water sectors. Fishing is included in agriculture.

For each sector we have estimated a production function. These production functions are not directly parts of the model, but they are used in the derivation of the factor demand equations (i.e. investment and work hours equations) and in estimating marginal costs of production; the marginal costs in turn enter the pricing equations. This two-stage strategy of modelling the supply side helps to ensure the consistency of the the equations in the model with each other and with the chosen technology assumptions.

## 2.2 The CES Value Added Production Functions

The production functions are assumed to be "nested" in the sense that labour and capital are separable from the other inputs. This allows us to model the production of real value added in the different sectors as functions of labour and capital inputs only. The value added production functions are of the "CES" type with Hicks-neutral technical progress and constant returns to scale:

$$(1) \quad Q = A \cdot \exp(\gamma \cdot \text{TREND}) \cdot (a \cdot K^{-\rho} + (1-a) \cdot L^{-\rho})^{-1/\rho}$$

Here  $Q$  is the real value added originating from the sector in question,  $K$  is the stock of fixed capital and  $L$  is the labour input (measured in hours worked). The impact of technical progress is captured by the inclusion of the linear time trend  $\text{TREND}$ .  $A$ ,  $\gamma$ ,  $a$  and  $\rho$  are parameters; of these,  $\gamma$  measures the rate at which technical progress increases the efficiency of production and  $\rho$  governs the elasticity of substitution between labour and capital,  $a$  indicates the weighting of capital and labour and  $A$  is a factor reflecting the scale of operation.

Although the functional form is assumed to be the same for each of the five sectors of the model, separate parameter values are estimated for each of them. For the agricultural sector the CES function was estimated directly by nonlinear least squares (in a form solved for the labour/capital ratio). For the other sectors, we have used a two-step procedure broadly similar to that described in Klein and Bodkin (1967). This method circumvents the problem of multicollinearity by assuming that the observed labour share in the value added is consistent with the cost-minimizing optimum. This allows us to write the following loglinear regression equation for each sector:

$$(2) \quad \log((PQ-WL)/WL) = \log(a/(1-a)) - \rho \cdot \log(K/L)$$

Here  $WL$  denotes labour costs (wage bill plus employers' social security payments) and  $PQ-WL$  is the gross operating surplus of the

sector in question (total value added at factor cost minus labour costs).

From the regression coefficients of the above equation we can solve for parameters  $a$ ,  $\rho$  and, further, the elasticity of substitution  $s = 1/(1+\rho)$ . If  $\rho$ , the coefficient of the capital-labour ratio in equation (2) were zero, the factor shares explained by the equation would be independent of the capital-labour ratio and the technology would be of the Cobb-Douglas type (with unit elasticity of substitution). The regression (2) is hence a kind of test of the CES specification against the more restrictive Cobb-Douglas specification.

After solving for the estimates of  $a$  and  $\rho$ , these are substituted into the original production function (1) and the scale parameter  $A$  and the rate of technical progress  $\gamma$  are estimated by loglinear least squares. After this second step, we have obtained all of the required parameter estimates.

The estimation was carried out using annual data for the period 1960 - 1985. The factor share data was adjusted for the labour input of the self-employed persons so that the wage bill was multiplied by the ratio of total hours worked to the hours worked by employees. In estimating the CES production function for the private services sector, the housing sector (letting and operating of dwellings and use of owner-occupied dwellings) was deducted from both the value added and the capital stock concept.

A comprehensive account of the estimation results is given in appendix 1. The most important characteristics of the estimated production functions are the elasticities of substitution and the rates of technical progress. These are given in the following table:

Table 2

Sector	elasticity of substitution	rate of technical progress (% p.a.)
	$s = \frac{1}{1+\rho}$	$\gamma$
- Agriculture	0.97	0
- Forestry	1.48	0.3
- Manufacturing	0.88	3.0
- Private services etc.	0.62	3.2
- Government services	0.51	0.7

The production functions which are actually used in BOF4 are quarterly versions of the estimated annual production functions. The conversion of annual CES functions into quarterly ones is done by multiplying the capital stock by four in the estimation of the annual functions. The finally obtained quarterly functions are:

Agriculture:

$$(3) \quad \text{GDP1} = 0.424 \cdot (0.6663 \cdot \text{KF1}^{-.028} + 0.3337 \cdot \text{LH}^{-.028})^{-1/.028}$$

Forestry:

$$(4) \quad \text{GDP3} = 9.042 \cdot e^{.003 \cdot \text{TREND}} (0.1611 \cdot \text{KF3}^{.326} + 0.8389 \cdot \text{LH3}^{.326})^{1/.326}$$

Manufacturing:

$$(5) \quad \text{GDP4} = 2.268 \cdot e^{.031 \cdot \text{TREND}} (0.5535 \cdot \text{KF4}^{-.143} + 0.4465 \cdot \text{LH4}^{-.143})^{-1/.143}$$

Private services etc. (excl. housing):

$$(6) \quad \text{GDP2} = 1.073 \cdot e^{.032 \cdot \text{TREND}} (0.8882 \cdot \text{KF2}^{-.605} + 0.1118 \cdot \text{LH2}^{-.605})^{-1/.605}$$

Government services:

$$(7) \quad \text{GDPG} = 0.807 \cdot e^{.007 \cdot \text{TREND}} (0.9864 \cdot (\text{KFCG} + \text{KFLG})^{-.978} + 0.0136 \cdot \text{LHG}^{-.978})^{(-1/.978)}$$

See appendix 3 for a list of symbols.

From these functions it is straightforward to derive the inverted production functions (the labour requirement ( $\text{LH}_i$ ) functions), the marginal product of labour ( $\text{MPL}_i$ ), the marginal product of capital ( $\text{MPK}_i$ ), and the marginal cost of production ( $\text{SMC}_i$ ) functions used in BOF4.

The marginal product of labour implied by the equation (1), can be written as

$$(8) \quad \partial Q / \partial L = (1-a) \cdot A \cdot \exp(\gamma \cdot \text{TREND}) \cdot [a \cdot (K/L)^{-\rho} + (1-a)]^{-(\rho+1)/\rho}$$

This formula is used in developing the sectoral short-run marginal cost of production functions. These are of the form

$$(9) \quad \text{SMC} = (1-a_Q) \cdot P^m + (a_Q) \cdot W / (\partial Q / \partial L),$$

where  $P^m$  is the weighted sum of input prices from other sectors and raw materials and the parameter  $a_Q$  describes the division of costs between material inputs and value added. The marginal product of labour (8) could also be expressed in terms of  $Q/L$  on the right hand side. This form was actually used in the earlier versions of the SMC functions. (See BOF4: Equations, TU 6/87). Having production in the denominator of the SMC function reduces costs (and prices) in the short run when GDP rises because labour hours react slowly to changes in production. This feature was regarded as undesirable in simulations and so the  $\text{MPL}_i$  functions were written in the form (8).

The marginal product of capital derived from equation (1) is

$$(10) \quad (\partial Q/\partial K) = a \cdot A^{-\rho} \cdot \exp(-\rho \cdot \gamma \cdot \text{TREND}) \cdot \left(\frac{\text{GDP}}{K^F - 1}\right)^{\rho+1}.$$

Using the parameters estimated from the production functions we can calculate time series for (10) to be used in the investment equations.

### 2.3 The Leontief Outer Production Functions

In the technology assumption used in the BOF4 model, the CES value added production functions are nested in a Leontief outer or "gross" production function in each sector of production. This means that the proportions of real value added in real output are assumed to be fixed, as are the proportions of non-primary inputs - meaning imports and purchases from other sectors used in production. These assumptions make it possible to use an input-output table to evaluate the cost structure of the different sectors in the model.

Since gross outputs and intersectoral flows of goods are not explicitly included in the model as variables, the outer production functions are not needed as such. Rather, the Leontief functions assigned for each sector are used in the actual model structure in two ways.

First, the cost functions implied by the outer production functions are used to determine the relationships between producer prices and value added deflators. This is possible because the knowledge of input coefficients enables us to compute the share of the producer price needed to cover costs of non-primary inputs and so the value added deflator is "residually" determined. This is explained more closely in the report describing the modelling of prices and wages in BOF4 (forthcoming; see also Tarkka & Willman (1985)).

Second, the information on input coefficients is used in the determination of the value added by sectors. This is explained in more detail in the next section. The idea is familiar from

input-output models: assume that the structure of aggregate demand is known, and also that each component of aggregate demand uses gross output of the different sectors in fixed proportions. This makes it possible to calculate the gross outputs of different sectors used to satisfy final demand. However, since gross outputs are also used as intermediate inputs in production, information on the input coefficients is needed before the gross output and the real value added produced in each sector can be solved for.

In estimating the input coefficients the Finnish input-output table of 1982 is used. The results are shown in the following table, where

$a_1$  is the coefficient of inputs from agriculture,  
 $a_3$  inputs from forestry,  
 $a_4$  inputs from manufacturing,  
 $a_2$  inputs from the private service sector,  
 $a_G$  inputs from the govt. services sector,  
 $a_{MR}$  imported raw materials (excl. fuels),  
 $a_{MF}$  imported fuels,  
 $a_Q$  capital and labour (i.e. value added).

Table 3

## The Input Coefficients in 1982.

	Sector:				
	Agric. (1)	Forestry (3)	Manufact. (4)	Priv.serv. (2)	Govt. (G)
$a_1$	0.0648	0.0096	0.0652	0.0014	0.0000
$a_3$	0.0079	0.0307	0.0393	0.0013	0.0000
$a_4$	0.2684	0.0223	0.3004	0.1413	0.0000
$a_2$	0.1132	0.0307	0.1082	0.2582	0.0000
$a_G$	0.0000	0.0000	0.0000	0.0000	0.0000
$a_{MR}$	0.0359	0.0074	0.1115	0.0495	0.0000
$a_{MF}$	0.0095	0.0148	0.0700	0.0148	0.0000
$a_Q$	0.5003	0.9200	0.3054	0.5335	1.0000
Sum	1.0000	1.0000	1.0000	1.0000	1.0000

The cost functions in the different sectors have the following form:

$$(11) \quad C = X \cdot (a_1 \cdot P_1 + a_3 \cdot P_3 + a_4 \cdot P_4 + a_2 \cdot P_2 + a_G \cdot P_G + a_{MR} \cdot P_{MR} + a_{MF} \cdot P_{MF} + a_Q \cdot P_{GDP}),$$

where  $C$  is the total cost of production,  $X$  is gross output,  $a_i$ 's are input-output coefficients,  $P_1, P_3, P_4, P_2, P_G, P_{MR}$  and  $P_{MF}$  are the prices of respective inputs and  $P_{GDP}$  is the value added deflator. This is the form of the total cost functions. It is useful mainly because it can be inverted to a formula for the value added deflator.

When evaluating the relevant marginal cost of production, a short-run variable cost concept is needed instead of the total cost given by (11). If the stock of fixed capital is treated as predetermined at each instant, the short-run marginal costs do not include gross operating surplus. Hence the short-run marginal costs can be expressed by eq. (9). These matters are discussed in more detail in a later report of the modelling of prices.



### 3 THE SUPPLY SIDE: PRODUCTION AND EMPLOYMENT

The supply side in BOF4 consists of two types of equations. On the one hand, the production and employment equations determine how a given aggregate demand is satisfied by production taking place in the different sectors of the economy. On the other hand, the labour supply, wage and price equations describe the behavioural aspects of supply, namely the decisions of workers, unions and firms. The first, technological aspect of the supply side in BOF4 is discussed in the present chapter.

#### 3.1 The Determination of Output by Sectors

The determination of the sectoral composition of real value added starts from the composition of aggregate demand given by the equations on the demand side of the model. The structure of demand is converted to the corresponding structure of output and indirect taxes (less subsidies) by means of an input-output model.<sup>1</sup> Estimates of this conversion matrix (except for inventories) are based on the input-output coefficient matrix presented in table 4.

Note that general government is a peculiar production sector in that its output is used only for public consumption. This implies that no other demand component but public consumption affect, directly or indirectly, general government production. Equation Q.6 (in appendix 2), which defines the production of general government sector (equalling its value-added), states that 67 per cent of the the increase in public consumption is directed at the production of general government sector.

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<sup>1</sup>A more profound description of such a model can be found in Tarkka & Willman (1985), pp. 156 - 158.

Equations Q.1 - Q.5 convert the rest of the final demand and imports of inputs into value-added of four private sectors and into indirect taxes less subsidies. Denote the conversion matrix contained by these equations by B. Now, after cancelling the row of general government production and the column of public consumption originating from the government sector in table 4, the matrix B can be expressed in terms of coefficients presented in table 4 as follows:

$$B = \begin{bmatrix} F^d(I_4-A)^{-1}D(I_{10}+\gamma^d)^{-1} \\ [\pi(I_4-A)^{-1}D+\gamma](I_{10}+\gamma^d)^{-1} \end{bmatrix}$$

where

- F is the row vector of value added coefficients
- A is the matrix of inter industry input coefficients
- D is the matrix of the coefficients of imported inputs and final demand components
- $\gamma$  is the row vector of indirect tax coefficients levied on production
- $\pi$  is the row vector of indirect tax coefficients levied on imported inputs and final demand
- $I_4$  is the four by four identity matrix
- $I_{10}$  is the ten by ten identity matrix

and superscript d is used to denote diagonal matrixes formed by row vectors F and  $\gamma$ .

However, as to the conversion of the change in inventories into sectoral production and indirect taxes, the input-output estimates obtained by this way were not accepted. Estimates based on the input-output study are point estimates of a single year (in this case 1982), and can deviate, especially in the case of inventories, quite considerably from their longer-run averages. That is why the parameters of this row were estimated by using the OLS method.

Table 4.

The matrix of input-output coefficients in 1982

Selling Industries	Buying Industries						Final Demand									Change in inventories
	agric.	priv. services	forest.	manuf.	govt.	imported inputs	priv. consumption			public consumpt.		investment		exports		
	(1)	(2)	(3)	(4)	(6)		durabl.	non-dur.	services	priv. origin	govt. origin	prod. inv.	housing inv.	goods	services	
agriculture (1)	.0766	.0016	.0095	.0769	.0000	-.0478	.0000	.0626	.0002	.0038	.0000	.0000	.0000	.0192	.0000	2.5554
priv. services (2)	.1096	.2730	.0306	.1141	.0000	-.1191	.4427	.4178	.9938	.5956	.0000	.8738	1.0000	.0000	1.0000	2.0997
forestry (3)	.0076	.0013	.0056	.0439	.0000	-.0151	.0000	.0160	.0003	.0104	.0000	.0087	.0000	.0017	.0000	.6156
manufacturing (4)	.2901	.1740	.0340	.4710	.0000	-.8180	.5573	.5035	.0057	.3902	.0000	.1175	.0000	.9791	.0000	-4.2707
government (6)	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	1.0000	.0000	.0000	.0000	.0000	.0000
indirect taxes minus subsidies	.0316	.0357	.0039	-.0162	.0000	.0000	.1370	.2513	-.0036	.0486	.0000	.0423	.0197	-.0228	.0197	-.4715
value added	.4845	.5144	.9164	.3103	1.0000	-	-	-	-	-	-	-	-	-	-	-
sum	1.0000	1.0000	1.0000	1.0000	1.0000	-1.0000	1.1370	1.2513	.9964	1.0486	1.0000	1.0423	1.0197	.9772	1.0197	.5285

In calculating the conversion estimates for the imported final goods the following additional assumptions were needed:

- The tax content of imported and domestically produced services is the same.
- Indirect taxes are levied 23.22 per cent and 9.71 per cent of the imports of consumption goods and investment goods, respectively.
- Of the imports of consumption goods 34 per cent is included in the private consumption of durables, 49 per cent in the private consumption of non- and semi-durables and 17 per cent in public consumption.
- All imports of investment goods are included in the private nonresidential investment and public investment.

### 3.2 The Demand for Labour Hours

In BOF4, two measures of labour input are used: work hours ( $LH_i$ ) and paid labour inputs ( $LW_i$ ). The latter are defined as the wage bill at constant (base-year) wages.

$$(12) \quad LW_i = 100 \cdot \frac{YW_i}{WR_i},$$

where  $LW_i$  is paid labour inputs,  $YW_i$  is the wage bill and  $WR_i$  is the wage rate all referring to the sector in question. Since the wage rate indices do not reflect changes in paid holidays nor changes in overtime compensation, paid labour inputs overestimate the real hours worked. Furthermore, work hours include the effort of self-employed persons, whereas paid labour input depends only on "bought" labour. On the other hand, by using the concept of paid labour input the sectoral wage bill can be expressed as the product of the paid labour input and the wage rate, which is more consistent from the point of view of the whole model.

The demand for hours in each production sector is explained by the inverted CES production functions. Thus, the effects of capital

deepening and technical progress on the demand for labour are captured in a way consistent with the technological assumptions of the whole BOF4 model. However, the inverted production function approach is incapable of taking into account the dynamics of labour demand. In particular, the observed procyclical movement of productivity cannot be explained by the inverted production function approach alone. (For a survey of labour demand equations see Fair (1969), also Intriligator (1978) ch. 8.5.)

To overcome this notorious problem, we have allowed a slow adjustment in the demand for work hours towards the equilibrium dictated by the inverted production functions. The adjustment mechanisms are obtained as results of an iterative specification search method, starting from unconstrained dynamics and dropping one by one, those lags of the explanatory variables which were statistically insignificant. The conformity of the equations in the long run with the inverted production function is ensured by the so-called error correction terms.

The dynamic properties of the demand for hours equations are described in the following tables, in which the elasticities of work hours with respect to output and the capital stock are presented. In table 6 the elasticity of labour demand is expressed in terms of the elasticity of productivity holding output constant.

Table 5. The Dynamic Elasticities of Work Hours With Respect to Changes in Output in the BOF4 Model.

sector	immediate elasticity	one-year elasticity	fifth-year elasticity
agriculture	0.11	0.20	1.05
forestry	0.56	0.66	1.97
manufacturing	0.45	0.64	1.36
priv. services etc.	0.45	0.51	1.04
general government	0.00	0.70	1.08
total economy	0.33	0.54	1.13

Table 6. The Dynamic Elasticities of Productivity With Respect to Changes in the Stock of Fixed Capital in the BOF4 Model.

sector	immediate elasticity	one-year elasticity	fifth-year elasticity
agriculture	0.00	0.06	0.61
forestry	0.00	0.16	1.16
manufacturing	0.00	0.07	0.42
priv. services etc.	0.00	0.03	0.13
general government	0.00	0.05	0.07
total economy	0.00	0.05	0.26

Changes in the sectoral composition of the value added also have an effect on the average labour productivity, since the productivities differ across sectors, as indicated by the following table:

Table 7. The Productivity of Labour in Different Sectors of the BOF4 Model in 1985, (average for the economy = 100)

agriculture	34
forestry	169
manufacturing	116
priv. services etc.	108
general government	100

After the demand for labour hours is determined in the model, these are used to solve for paid labour inputs. This is done by simple linkage equations (L.6 to L.10 in the list of equations).

### 3.3 Employment

The equation for employment (see L.12 in appendix 2) determines the number of employed persons on the basis of the total demand for work hours. The elasticity of employment with respect to the demand for hours is given in the following table.

Table 8. The Dynamic Elasticity of Employment With Respect to Changes in the Demand for Work Hours.

	immediate elasticity	one-year elasticity	fifth-year elasticity
total economy	0.14	0.45	0.95

In the long run the elasticity is constrained to unity. In addition, the equation contains a trend variable which causes a decrease in hours per person at a rate of 0.86 per cent per annum.

A simple linear relationship (L.11) is used to convert the Labour Force Survey statistics to correspond to the SNA concept of employment.

## REFERENCES

- FAIR, R.C. (1969) The Short-Run Demand for Workers and Hours, Amsterdam: North-Holland Publishing Co.
- INTRILIGATOR, M. (1978) Economic Models, Techniques & Applications, Prentice-Hall, Inc., Englewood Cliffs, N.J.
- KLEIN, L.R. & BODKIN, R. (1967) Nonlinear Estimation of Aggregate Production Functions, Review of Economics and Statistics, 49, February 1967, 28 - 44.
- MAYES, D.G. (1981) Applications of Econometrics, Prentice-Hall, Inc., USA.
- THE BOF4 QUARTERLY MODEL OF THE FINNISH ECONOMY (1987) Equations, Bank of Finland, Research Department TU 6/87.
- TARKKA, J. & WILLMAN, A. (eds. 1985) The BOF3 Quarterly Model of the Finnish Economy, Bank of Finland, Series D:59, Helsinki.
- TARKKA, J. & WILLMAN, A. (1988) Exports and Imports in the BOF4 Quarterly Model of the Finnish Economy, Bank of Finland Discussion Papers 3/88.





## APPENDIX 1

## THE ESTIMATION OF THE CES VALUE ADDED PRODUCTION FUNCTIONS

For sectors 2, 3, 4 and G the following loglinear equation is estimated with annual data. The capital stock is multiplied by four to get parameter estimates equivalent to quarterly equations. (A list of variables is in appendix 3).

$$(A1) \quad \log((PQ - WL \cdot Z)/WL \cdot Z) = \log(a/(1-a)) - \rho \cdot \log((4 \cdot K/L))$$

Where Z is the correction term to account for the self-employed in sectors 2, 3 and 4.<sup>1</sup> From this the value for a (the distribution parameter) and  $\rho$  (the parameter which governs the elasticity of substitution between labour and capital:  $s = 1/(1+\rho)$ ) are solved for and substituted into:

$$(A2) \quad Q = A \cdot \exp(\gamma \cdot \text{TREND}) \cdot [a \cdot (4 \cdot K)^{-\rho} + (1-a) \cdot L^{-\rho}]^{-1/\rho}.$$

Dividing by  $[a \cdot (4 \cdot K)^{-\rho} + (1-a) \cdot L^{-\rho}]^{-1/\rho}$  and taking logs gives

$$(A3) \quad \log(Q/[a \cdot (4K)^{-\rho} + (1-a) \cdot L^{-\rho}]^{-1/\rho}) = \log A + \gamma \cdot \text{TREND}$$

From this second stage equation we get estimates for A and  $\gamma$ . Using the estimated parameters for a,  $\rho$ , A and  $\gamma$  the final production functions can be written as equations (3) - (7) in the main text. See tables A1 and A3 below.

For the agricultural sector where no technical progress could be identified ( $\gamma = 0$  in equation A2) the CES value added production

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<sup>1</sup>See the list of variables in appendix 3 for a more accurate explanation.

function (A2) was estimated directly by nonlinear least squares in a form solved for the labour/capital - ratio:

$$(A4) \quad L/K = \left[ \frac{A^\rho}{(1-a)} \cdot \left(\frac{Q}{K}\right)^{-\rho} + \frac{a}{1-a} \right]^{-\frac{1}{\rho}}$$

The estimation results are

$$\frac{LH1}{KF1} = \left[ \begin{array}{c} 2.9253 \\ (19.91) \end{array} \left(\frac{GDP1}{KF1}\right)^{\begin{array}{c} -.0281 \\ (-2.69) \end{array}} - \begin{array}{c} 1.9967 \\ (28.01) \end{array} \right] \begin{array}{c} (1/-.0281) \\ (2.69) \end{array}$$

$\bar{R}^2 = 0.444$                       DW = 0.430                      SE = 0.00129

Estimation period 1960 - 1985. The solved parameters are  $A = .4242$ ,  $\rho = 0.0281$  and  $a = 0.6663$ . Numbers in brackets are standard deviations.

Note that here the stock of capital is not multiplied by four since it appears on the both sides of the equation.

PRODUCTION FUNCTION ESTIMATION RESULTS FOR SECTORS 2, 3, 4 and G

TABLE A1 EQUATION A1 (First stage)

		$\bar{R}^2$	DW	SE	estimation period	Solved from the equation a	$\rho$	s
Private services etc. (excl. housing)	$\log\left(\frac{GDPV2 - QIV83}{(1+SOCCR2) \cdot YW2 \cdot ZL2} - 1\right) = 2.0726 - 0.6050 \log\left(4 \cdot \frac{KF2}{LH2}\right)$ (0.4034) (0.0682)	0.756	1.129	0.118	1960 - 1985	0.8882	-0.605	0.623
Forestry	$\log\left(\frac{GDPV3}{(1+SOCCR3) \cdot YW3 \cdot ZL3} - 1\right) = -1.6501 + 0.3261 \log\left(4 \cdot \frac{KF3}{LH3}\right)$ (0.1970) (0.0336)	0.789	1.170	0.138	1960 - 1985	0.1611	0.326	1.484
Manufacturing	$\log\left(\frac{GDPV4}{(1+SOCCR4) \cdot YW4 \cdot ZL4} - 1\right) = 0.2148 - 0.1429 \log\left(4 \cdot \frac{KF4}{LH4}\right)$ (0.5755) (0.0977)	0.044	1.042	0.148	1960 - 1985	0.5535	-0.143	0.875
Government services	$\log\left(\frac{GDPVG}{(1+SOCCRG) \cdot YWG} - 1\right) = 4.2834 - 0.9781 \log\left(4 \cdot \frac{(KFCG+KFLG)}{LHG}\right)$ (0.8955) (0.1281)	0.696	0.905	0.043	1960 - 1985	0.9864	-0.978	0.506

TABLE A3 EQUATION A3 (Second stage)

		$\bar{R}^2$	DW	SE	estimation period	Solved from the equation A	$\gamma$
Private services etc. (excl. housing)	$\log \left[ \frac{GDP2 - QIV83 / (.01 \cdot PGDP2)}{(.8882(4 \cdot KF2)^{-.605} + .1118LH^{-.605})} \right] = 0.0702 + 0.0316 \cdot \text{TREND}$ (0.0104) (0.0007)	0.988	0.390	0.026	1960 - 1985	1.073	0.032
Forestry	$\log \left[ \frac{GDP3}{(.1611(4 \cdot KF3)^{.3261} + .8389LH3^{.3261})} \right] = 2.2019 + 0.0029 \cdot \text{TREND}$ (0.0299) (.0020)	0.041	0.842	0.076	1960 - 1985	9.042	0.003
Manufacturing	$\log \left[ \frac{GDP4}{(.5535(4 \cdot KF4)^{-.143} + .4465LH4^{-.143})} \right] = 0.8191 + 0.0306 \cdot \text{TREND}$ (0.0145) (0.0010)	0.976	0.557	0.037	1960 - 1985	2.268	0.031
Government services	$\log \left[ \frac{GDPG}{(.9864(4 \cdot (KFCG+KFLG))^{-.978} + .0136LHG^{-.978})} \right] = -0.2147 + 0.0071 \cdot \text{TREND}$ (0.0056) (0.0004)	0.937	0.834	0.014	1960 - 1985	0.807	0.007

List of symbols, see appendix 3.  
Standard deviations are given in brackets under the parameters.

## APPENDIX 2

## LIST OF EQUATIONS

List of output and employment equations for the BOF4 quarterly model of the Finnish economy, May 1988 version.

Notation used:

Values of parameter estimates are ordinary least squares estimates.

Standard errors of parameter estimates are in parentheses below the coefficients.

When standard error is not shown, the parameter in question is fixed a priori e.g. on the basis of input-output studies.

Weights of Almon lags are denoted by  $a_i$ ,  $b_i$ , etc.

Variables with a subscript are lagged. Subscripts refer to number of lags in quarters.

$\Delta$  is the difference operator.  
 $\Delta^n$  denotes difference over  $n$  quarters.  
 $\log$  denotes natural logarithms.

Units:

Values are in millions of FIM.  
 Volumes are in millions of FIM at 1985 prices.  
 Price indices take the value 100 in 1985.  
 Interest rates are in per cent.  
 Energy is in 1000 toe.  
 Labour force figures are in 1000 persons.

$\bar{R}^2$  = corrected coefficient of determination  
 DW = Durbin - Watson statistic  
 SE = standard error of estimate  
 rho = coefficient of first-order autocorrelation correction

The estimation period is given after the summary statistics

Q. TUOTANTO  
PRODUCTION

Q.1 - Q.5 Tuotannon määrä sektoreittain  
Production at Factor Cost by Sectors

	ΔCD	ΔCND	ΔCS	ΔCG-ΔGDPG	ΔIF+ΔIG	ΔIH	ΔXG	ΔXS	ΔMC	ΔMS	ΔMI	ΔMR+ΔMFL	IIS
ΔGDP1	+0.0507	+0.0698	+0.0224	+0.0465	+0.0281	+0.0214	+0.0971	+0.0214	-0.0773	-0.0224	-0.0311	-0.0996	+0.1134
ΔGDP2	+0.3844	+0.3341	+0.7517	+0.4977	+0.6522	+0.7380	+0.1898	+0.7380	-0.4937	-0.7517	-0.7224	-0.2497	(0.02173) +0.3275
ΔGDP3	+0.0515	+0.0563	+0.0233	+0.0546	+0.0365	+0.02220	+0.0897	+0.02220	-0.0708	-0.0233	-0.0404	-0.0898	(0.03804) +0.1278
ΔGDP4	+0.3827	+0.3281	+0.1609	+0.3345	+0.2062	+0.1544	+0.6614	+0.1544	-0.4529	-0.1609	-0.2284	-0.5663	(0.01919) +0.3841
ΔTIN	+0.1307	+0.2117	+0.0417	+0.0667	+0.0770	+0.0640	-0.0380	+0.0640	+0.0947	-0.0417	+0.0223	+0.0054	(0.03774) +0.0439 (0.02215)

	R <sup>2</sup>	DW	SE	aikaväli
GDP1 Tuotannon määrä, maatalous Production at Factor Cost, Agriculture, Volume	0.2246	2.888	240.2729	62.1 - 85.4
GDP2 Tuotannon määrä, palvelukset ym. Production at Factor Cost, Services etc., Volume	0.4382	2.811	420.6088	62.1 - 85.4
GDP3 Tuotannon määrä, metsätalous Production at Factor Cost, Forestry, Volume	0.3219	2.489	212.1714	62.1 - 85.4
GDP4 Tuotannon määrä, teollisuus Production at Factor Cost, Manufacturing, Volume	0.5216	3.1411	417.2685	62.1 - 85.4
TIN Välilliset verot miinus tukipalkkiot, määrä Indirect Taxes Less Subsidies, Volume	0.0392	2.996	244.9243	62.1 - 85.4

CG Total public consumption, millions of 1985 FIM  
 GDP1 Production at factor cost, agriculture, millions of 1985 FIM  
 GDP2 Production at factor cost, services etc., millions of 1985 FIM  
 GDP3 Production at factor cost, forestry, millions of 1985 FIM  
 GDP4 Production at factor cost, manufacturing, millions of 1985 FIM  
 GDPF GDP at factor cost, millions of 1985 FIM  
 GDPG Production at factor cost, general government, millions of 1985 FIM  
 GDPV GDP in Purchasers' Values, FIM million  
 GDPV1 Production at factor cost, agriculture, FIM million  
 GDPV2 Production at factor cost, services and other, FIM million  
 GDPV3 Production at factor cost, forestry, FIM million  
 GDPV4 Production at factor cost, manufacturing, FIM million  
 PGDP1 Value added deflator in agriculture, 1985 = 100  
 PGDP2 Value added deflator in services etc., 1985 = 100  
 PGDP3 Value added deflator in forestry, 1985 = 100  
 PGDP4 Value added deflator in manufacturing, 1985 = 100

Q.6 Tuotannon määrä, julkinen toiminta  
 Production at Factor Cost, General Government, Volume

$$\Delta \text{GDPG} = 0.66225 \cdot \Delta \text{CG} \\ (0.02210)$$

Q.7 Bruttokansantuotteen määrä, tuottajahintaan  
 Gross Domestic Product at Factor Cost, Volume

$$\text{GDPF} = \text{GDP1} + \text{GDP2} + \text{GDP3} + \text{GDP4} + \text{GDPG}$$

Q.8 Tuotannon arvo, maatalous  
 Production at Factor Cost, Agriculture, Value

$$\text{GDPV1} = \text{GDP1} \cdot \text{PGDP1}/100$$

Q.9 Tuotannon arvo, palvelukset ym.  
 Production at Factor Cost, Services etc., Value

$$\text{GDPV2} = \text{GDP2} \cdot \text{PGDP2}/100$$

Q.10 Tuotannon arvo, metsätalous  
 Production at Factor Cost, Forestry, Value

$$\text{GDPV3} = \text{GDP3} \cdot \text{PGDP3}/100$$

Q.11 Tuotannon arvo, teollisuus  
 Production at Factor Cost, Manufacturing, Value

$$\text{GDPV4} = \text{GDP4} \cdot \text{PGDP4}/100$$

GDP GDP in Purchasers' Values, millions of 1985 FIM  
 GDPF GDP at factor cost, millions of 1985 FIM  
 GDPFV GDP at factor cost, FIM million  
 GDPG Production at factor cost, general government, millions of 1985 FIM  
 GDPV1 Production at factor cost, agriculture, FIM million  
 GDPV2 Production at factor cost, services and other, FIM million  
 GDPV3 Production at factor cost, forestry, FIM million  
 GDPV4 Production at factor cost, manufacturing, FIM million  
 GDPVG Production at factor cost, FIM million  
 PGDPG Value added deflator in general government, 1985 = 100  
 SUB Subsidies, millions of 1985 FIM  
 TIN Indirect taxes less subsidies, millions of 1985 FIM  
 TIV Central government revenue from commodity taxes, FIM million

Q.12 Tuotannon arvo, julkinen toiminta  
 Production at Factor Cost, General Government, Value

$$\text{GDPVG} = \text{GDPG} \cdot \text{PGDPG}/100$$

Q.13 Bruttokansantuotteen arvo, tuottajahintaan  
 Gross Domestic Product at Factor Cost, Value

$$\text{GDPFV} = \text{GDPV1} + \text{GDPV2} + \text{GDPV3} + \text{GDPV4} + \text{GDPVG}$$

Q.14 Bruttokansantuotteen määrä, markkinahintaan  
 Gross Domestic Product in Purchasers' Values, Volume

$$\text{GDP} = \text{GDPF} + \text{TIN}$$

Q.15 Bruttokansantuotteen arvo, markkinahintaan  
 Gross Domestic Product in Purchasers' Values, Value

$$\text{GDPV} = \text{GDPFV} + \text{TIV} - \text{SUB}$$



GDP1 Production at factor cost, agriculture, millions of 1985 FIM  
 GDP2 Production at factor cost, services etc., millions of 1985 FIM  
 KF1 Net stock of fixed capital, agriculture, millions of 1985 FIM  
 KF2 Net stock of fixed capital, service etc., millions of 1985 FIM  
 KH Net stock of private residential capital, net, millions of 1985 FIM  
 LH1 Performed working hours, agriculture, millions of hours  
 LH2 Performed working hours, services etc., millions of hours  
 TREND Linear trend: 60.1 = .25, 60.2 = .50 etc.  
 DQ1 Seasonal dummy, the first quarter  
 DQ2 Seasonal dummy, the second quarter

L. TYÖLLISYYS  
 EMPLOYMENT

L.1 Tehdyt työtunnit, maatalous  
 Performed Working Hours, Agriculture

$$\Delta \log LH1 = -0.00817$$

(0.0073)

$$+ 0.10695 \cdot \Delta \log GDP1$$

(0.0868)

$$- 0.06912 \cdot \log(GDP1T_{-1}/GDP1_{-1})$$

(0.0638)

$$\text{jossa } GDP1T = 0.4242 \cdot (0.6663 \cdot KF1_{-0.0281} + 0.3337 LH1_{-0.0281})^{35.6}$$

$$\bar{R}^2 = 0.000 \quad DW = 2.334 \quad SE = 0.07112 \quad 62.1 - 85.4$$

L.2 Tehdyt työtunnit, palvelukset ym.  
 Performed Working Hours, Services etc.

$$\Delta \log LH2 = 0.01131$$

(0.0057)

$$- 0.20657 \cdot \Delta \log LH2_{-1}$$

(0.0783)

$$+ 0.44686 \cdot \Delta \log(GDP2 - 0.04885 \cdot KH/4)$$

(0.1760)

$$- 0.15057 \cdot \log(GDP2T_{-1}(GDP2_{-1} - 0.04885 \cdot KH_{-1}/4))$$

(0.0677)

$$- 0.02853DQ1$$

(0.0071)

$$- 0.05755DQ2$$

(0.0070)

$$\text{jossa } GDP2T = 1.07269 \cdot e^{0.0316 \cdot \text{TREND}} \cdot (0.88821 \cdot KF2_{-0.605} + 0.1118 \cdot LH2_{-0.605})^{-1.65}$$

$$\bar{R}^2 = 0.506 \quad DW = 2.155 \quad SE = 0.02739 \quad 62.1 - 85.4$$

GDP3 Production at factor cost, forestry, millions of 1985 FIM  
 KF3 Net stock of fixed capital, forestry, millions of 1985 FIM  
 LH3 Performed working hours, forestry, millions of hours  
 TREND Linear trend: 60.1 = .25, 60.2 = .50 etc.

L.3 Tehdyt työtunnit, metsätalous  
 Performed Working Hours, Forestry

$$\Delta \log LH3 = - 0.01816$$

(0.0083)

$$- 0.30126 \cdot \Delta \log LH3_{-1}$$

(0.0838)

$$+ 0.56133 \cdot \Delta \log GDP3$$

(0.0930)

$$- 0.20716 \cdot \log(GDP3T_{-1}/GDP3_{-1})$$

(0.0901)

$$\text{jossa } GDP3T = 9.04218 \cdot e^{0.00285 \cdot \text{TREND}} \cdot (0.161 \cdot KF3^{0.326} + 0.839 \cdot LH3^{0.326})^{3.07}$$

$$\bar{R}^2 = 0.340 \quad DW = 2.310 \quad SE = 0.08015 \quad 62.1 - 85.4$$

D75 Dummy 60.1 - 74.4 = 1, 75.1 - 85.4 = 0  
 GDP4 Production at factor cost, manufacturing, millions of  
 1985 FIM  
 KF4 Net stock of fixed capital, manufacturing, millions of  
 1985 FIM  
 LH4 Performed working hours, manufacturing, millions of hours  
 \*TREND Linear trend: 60.1 = .25, 60.2 = .50 etc.

L.4 Tehdyt työtunnit, teollisuus  
 Performed Working Hours, Manufacturing

$$\begin{aligned} \Delta \log LH4 &= - 0.00572 \\ &\quad (0.0024) \\ &- 0.15119 \cdot \Delta \log LH4_{-1} \\ &\quad (0.0643) \\ &+ 0.44859 \cdot \Delta \log GDP4 \\ &\quad (0.0821) \\ &- 0.13498 \cdot \log(GDP4T_{-1}/GDP4_{-1}) \\ &\quad (0.0539) \\ &- 0.20787 \cdot \Delta D75 \\ &\quad (0.0210) \\ &+ 0.21837 \cdot \Delta D75_{-1} \\ &\quad (0.0262) \end{aligned}$$

$$\text{jossa } GDP4T = 2.2685 \cdot e^{0.0306 \cdot \text{TREND}} \cdot (0.553 \cdot KF4 - 0.143 + 0.447 \cdot LH4 - 0.143) - 6.997$$

$$\bar{R}^2 = 0.721 \quad DW = 2.347 \quad SE = 0.0207 \quad 62.1 - 85.4$$

GDPG Production at factor cost, general government; millions of 1985 FIM

KFCG Net stock of fixed capital, central government, millions of 1985 FIM

KFLG Net stock of fixed capital, local government, millions of 1985 FIM

LH1 Performed working hours, agriculture, millions of hours

LHG Performed working hours, general government, millions of hours

LW1 Paid labour input, agriculture, millions of 1985 FIM

TREND Linear trend: 60.1 = .25, 60.2 = .50 etc.

L.5 Tehdyt työtunnit, julkinen toiminta  
Performed Working Hours, Central and Local Government

$$\Delta \log \text{LHG} = - 0.00267$$

$$(0.0127)$$

$$- 0.76273 \cdot \log(\text{GDPGT}_{-1}/\text{GDPG}_{-1})$$

$$(0.1035)$$

$$\text{jossa GDPGT} = 0.80682 \cdot e^{0.0071 \cdot \text{TREND}} \cdot (0.986 \cdot (\text{KFCG} + \text{KFLG})^{-0.978} + 0.014 \cdot \text{LHG}^{-0.978})^{-1.022}$$

$$\bar{R}^2 = 0.359 \quad \text{DW} = 1.916 \quad \text{SE} = 0.12424 \quad 62.1 - 85.4$$

L.6 Ansiotyöpanos, maatalous  
Paid Labor Input, Agriculture

$$\Delta \log \text{LW1} = + 0.00093$$

$$(0.00182)$$

$$+ 0.73582 \cdot \Delta \log \text{LW1}_{-1}$$

$$(0.09196)$$

$$+ 0.80796 \cdot \Delta \log \text{LH1}$$

$$(0.03987)$$

$$- 0.72775 \cdot \Delta \log \text{LH1}_{-1}$$

$$(0.07661)$$

$$\bar{R}^2 = 0.930 \quad \text{DW} = 1.437 \quad \text{SE} = 0.0113 \quad 76.1 - 85.4$$

LH2 Performed working hours, services etc., millions of hours  
 LH3 Performed working hours, forestry, millions of hours  
 LW2 Paid labour input, services etc., millions of 1985 FIM  
 LW3 Paid labour input, forestry, millions of 1985 FIM

L.7 Ansiotyöpanos, palvelukset ym.  
 Paid Labor Input, Services etc.

$$\begin{aligned} \Delta \log LW2 &= + 0.00118 \\ &\quad (0.00102) \\ &+ 0.67917 \cdot \Delta \log LW2_{-1} \\ &\quad (0.11294) \\ &+ 0.95488 \cdot \Delta \log LH2 \\ &\quad (0.02964) \\ &- 0.70972 \cdot \Delta \log LH2_{-1} \\ &\quad (0.10979) \end{aligned}$$

$$\bar{R}^2 = 0.970 \quad DW = 0.527 \quad SE = 0.0061 \quad 76.1 - 85.4$$

L.8 Ansiotyöpanos, metsätalous  
 Paid Labor Input, Forestry

$$\begin{aligned} \Delta \log LW3 &= + 0.00166 \\ &\quad (0.00201) \\ &+ 0.79961 \cdot \Delta \log LW3_{-1} \\ &\quad (0.10022) \\ &+ 0.98501 \cdot \Delta \log LH3 \\ &\quad (0.02836) \\ &- 0.80135 \cdot \Delta \log LH3_{-1} \\ &\quad (0.10031) \end{aligned}$$

$$\bar{R}^2 = 0.976 \quad DW = 0.452 \quad SE = 0.0123 \quad 76.1 - 85.4$$

LH4 Performed working hours, manufacturing, millions of hours  
 LHG Performed working hours, general government, millions of hours  
 LW4 Paid labour input, manufacturing, millions of 1985 FIM  
 LWG

L.9 Ansiotyöpanos, teollisuus  
 Paid Labor Input, Manufacturing

$$\Delta \log LW4 = - 0.00084$$

$$(0.00195)$$

$$+ 0.39085 \cdot \Delta \log LW4_{-1}$$

$$(0.14376)$$

$$+ 0.74732 \cdot \Delta \log LH4$$

$$(0.07261)$$

$$- 0.47563 \cdot \Delta \log LH4_{-1}$$

$$(0.11698)$$

$$\bar{R}^2 = 0.742 \quad DW = 0.818 \quad SE = 0.0123 \quad 76.1 - 85.4$$

L.10 Ansiotyöpanos, julkinen toiminta  
 Paid Labor Input, Central and Local Government

$$\log LWG = + 3.67023$$

$$(0.28325)$$

$$+ 1.05517 \cdot \log LHG$$

$$(0.05632)$$

$$\bar{R}^2 = 0.900 \quad DW = 1.476 \quad SE = 0.0347 \quad 76.1 - 85.4$$

LE Employment, 1000 persons  
 LES Employment (Labour Force Survey), 1000 persons  
 LH Performed working hours total, millions of hours  
 TREND Linear trend: 60.1 = .25, 60.2 = .50 etc.

L.11 Työlliset  
 Employment (SNA)

LE = + 301.62638  
 (92.09294)

+ 0.82249 • LES

$\bar{R}^2 = 0.931$       RHO = 0.980      SE = 3.2134      76.1 - 85.4

L.12 Työlliset, työvoimatutkimus  
 Employment (Labour Force Survey)

$\Delta \log \text{LES} = 0.05141$   
 (0.02786)

+ 0.07800 •  $\log(\text{LH}_{-1}/\text{LES}_{-1})$   
 (0.04247)

+ 0.14397 •  $\Delta \log \text{LH}$   
 (0.03588)

+ 0.13635 •  $\Delta \log \text{LH}_{-1}$   
 (0.04364)

+ 0.15048 •  $\Delta \log \text{LH}_{-2}$   
 (0.03963)

+ 0.18175 •  $\Delta \log \text{LH}_{-3}$   
 (0.03558)

+ 0.07713 •  $\Delta \log \text{LH}_{-4}$   
 (0.03499)

+ 0.00067 • TREND  
 (0.00033)

$\bar{R}^2 = 0.3007$       DW = 1.7749      SE = 0.0048      62.1 - 85.4

C Total private consumption, millions of 1985 FIM  
 LES Employment (Labour Force Survey), 1000 persons  
 LFS  
 LH Performed working hours total, millions of hours  
 LH1 Performed working hours, agriculture, millions of hours  
 LH2 Performed working hours, services etc., millions of hours  
 LH3 Performed working hours, forestry, millions of hours  
 LH4 Performed working hours, manufacturing, millions of hours  
 LHG Performed working hours, general government, millions of hours  
 LU Unemployment, 1000 persons  
 LW Paid labour input, total, millions of 1985 FIM  
 LW1 Paid labour input, agriculture, millions of 1985 FIM  
 LW2 Paid labour input, services etc., millions of 1985 FIM  
 LW3 Paid labour input, forestry, millions of 1985 FIM  
 LW4 Paid labour input, manufacturing, millions of 1985 FIM  
 LWG  
 MTAX Personal marginal tax rate, estimate  
 N Population of working age (15-74 years), 1000 persons  
 PCP Private consumption prices, 1985 = 100  
 UR Unemployment rate, per cent  
 WR Wage rate, total, 1985 = 100

L.13 Työvoima, työvoimatutkimus  
 Labour Force (Labour Force Survey)

$$\Delta \log(LFS/N) = + 0.00026$$

$$(0.00030)$$

$$+ 0.64817 \cdot \Delta \log(LES/N)$$

$$(0.04672)$$

$$+ 0.00520 \cdot \Delta \log((1 - MTAX) \cdot WR/PCP)$$

$$(0.00336)$$

$$- 0.03026 \cdot \Delta \log(C/N)$$

$$(0.01609)$$

$$\bar{R}^2 = 0.6871 \quad DW = 2.0315 \quad SE = 0.0027 \quad 63.1 - 85.4$$

L.14 Tehdyt työtunnit, yhteensä  
 Performed Working Hours, Total

$$LH = LH1 + LH2 + LH3 + LH4 + LHG$$

L.15 Ansiotyöpanos, yhteensä  
 Paid Labour Input, Total

$$LW = LW1 + LW2 + LW3 + LW4 + LWG$$

L.16 Työttömät, työvoimatutkimus  
 Unemployment (Labour Force Survey)

$$LU = LFS - LES$$

L.17 Työttömyysaste, työvoimatutkimus  
 Unemployment Rate (Labour Force Survey)

$$UR = 100 \cdot LU/LFS$$



## APPENDIX 3

## LIST OF VARIABLES

PQ-WL	gross operating surplus
WL	labour costs
K	capital stock
L	labour input (hours)
Q	real value added
TREND	linear trend

---

GDPG	Production at factor cost, general government, millions of 1985 FIM
GDPVG	Production at factor cost, general government, FIM million
GDPV1	Production at factor cost, agriculture, FIM million
GDPV2	Production at factor cost, services and other, FIM million
GDPV3	Production at factor cost, forestry, FIM million
GDPV4	Production at factor cost, manufacturing, FIM million
GDP1	Production at factor cost, agriculture, millions of 1985 FIM
GDP2	Production at factor cost, services etc., millions of 1985 FIM
GDP3	Production at factor cost, forestry, millions of 1985 FIM
GDP4	Production at factor cost, manufacturing, millions of 1985 FIM
KFCG	Net stock of fixed capital, central government, millions of 1985 FIM
KFLG	Net stock of fixed capital, local government, millions of 1985 FIM
KF1	Net stock of fixed capital, agriculture, millions of 1985 FIM

KF2	Net stock of fixed capital, service etc., millions of 1985 FIM
KF3	Net stock of fixed capital, forestry, millions of 1985 FIM
KF4	Net stock of fixed capital, manufacturing, millions of 1985 FIM
LHG	Performed working hours, general government, millions of hours
LH1	Performed working hours, agriculture, millions of hours
LH2	Performed working hours, services etc., millions of hours
LH3	Performed working hours, forestry, millions of hours
LH4	Performed working hours, manufacturing, millions of hours
PGDP2	Value added deflator in services etc., 1985 = 100
Q1V83	Production at factor cost, housing, FIM million
SOCCRG	Employers' social security contribution rate, general government, FIM million
SOCCR1	Employers' social security contribution rate, agriculture
SOCCR2	Employers' social security contribution rate, services etc.
SOCCR3	Employers' social security contribution rate, forestry
SOCCR4	Employers' social security contribution rate, manufacturing
YW1	Wages and salaries, agriculture, FIM million
YW2	Wages and salaries, services etc., FIM million
YW3	Wages and salaries, forestry, FIM million
YW4	Wages and salaries, manufacturing, FIM million
Z	Total hours worked per hours worked by employees in the sector; adjustment term to deduct the compensation of the work of the self-employed from the value-added of the sector.
ZL <sub>i</sub>	See Z
(i=2,3,4)	



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